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# NICS



## Numerical Simulation of a Coupled Electro-Mechanical Heart Model

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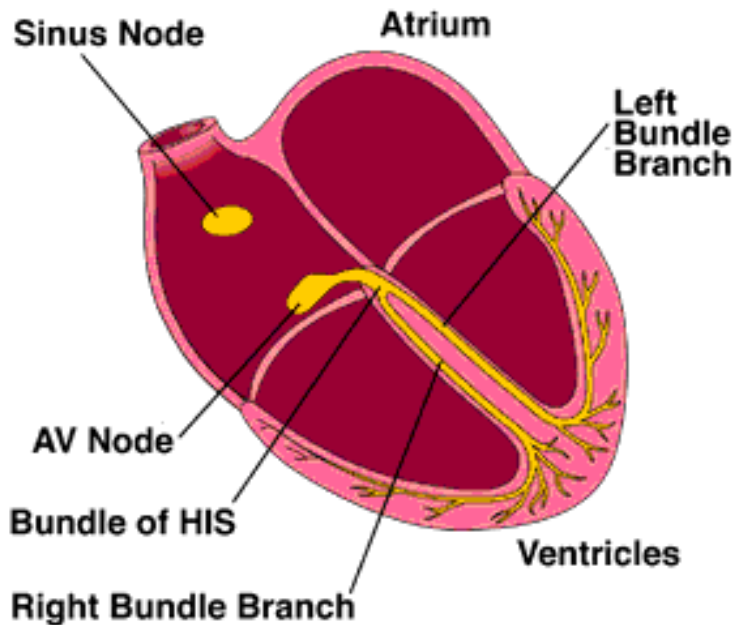


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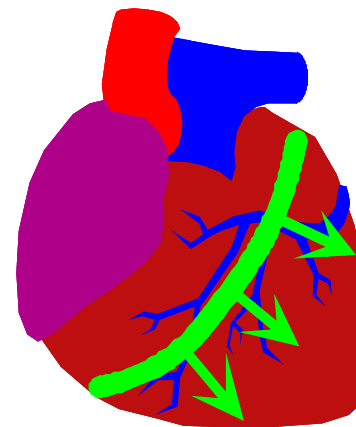


# Goal: Understand the dynamics of Sudden Cardiac Arrest

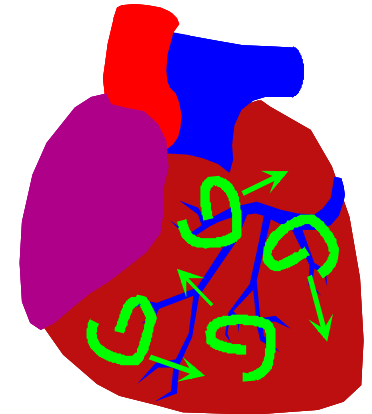
- Heart: An electro-mechanical pump
- Pumps 2,000 gallons of blood
- Beats 100,000 times/day
- 2.5 billion times in lifetime
- Sudden Cardiac Arrest: Not a heart attack
- Occur rapidly without warning
- A **dynamical disease**, that affects anyone, regardless of age, gender, and physical fitness



<http://heartpoint.com>



Normal Rhythm



Sudden Cardiac Arrest

# Model: Electrical + Physiological + Mechanical

$$\frac{dV}{dt} = -(I_{stim} + I_{Na} + I_{Kl} + I_{Kr} + I_{Ks} + I_{to} + I_{Kp} + I_{NaK} + I_{NaCa} + I_{Nab} + I_{Cab} + I_{pCa} + I_{Ca} + I_{CaK})$$

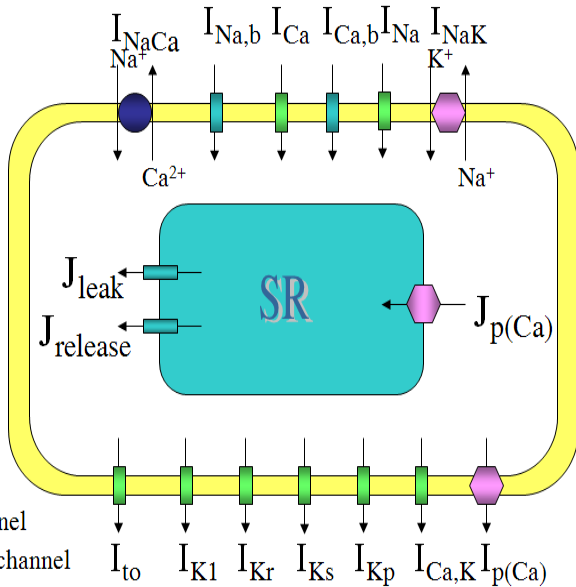
Model at cellular level: a set of ODEs describing the change of voltage and ionic currents.





Model at global level: a system of PDEs describing the interactions of the electromechanical and physiological actions.

$$\frac{dV}{dt} = \sum I_i$$

$$I_i = g_i(V - E_i)$$

$$g_i = f(V, t)$$



-  Pump
-  Exchanger
-  Voltage-gated ion channel
-  Non-voltage-gated ion channel

$$\nabla \cdot (\mathbf{D}(\mathbf{C})\nabla V) = C_m(\mathbf{C})\frac{\partial V}{\partial t} + I_m(\mathbf{C})$$

$$T^{MN} = \frac{1}{2} \left( \frac{\partial W}{\partial E_{MN}} + \frac{\partial W}{\partial E_{NM}} \right) + T_a C^{MN}$$

$$C_m \frac{\partial V}{\partial t} = \frac{1}{\sqrt{C}} \frac{\partial}{\partial X^M} \left( \sqrt{C} D_N^M C^{NL} \frac{\partial V}{\partial X^L} \right) - kV(V - a)(V - 1) - rV + I_s,$$

$$\frac{\partial r}{\partial t} = \left( \epsilon + \frac{\mu_1 r}{\mu_2 + V} \right) (-r - kV(V - b - 1)),$$

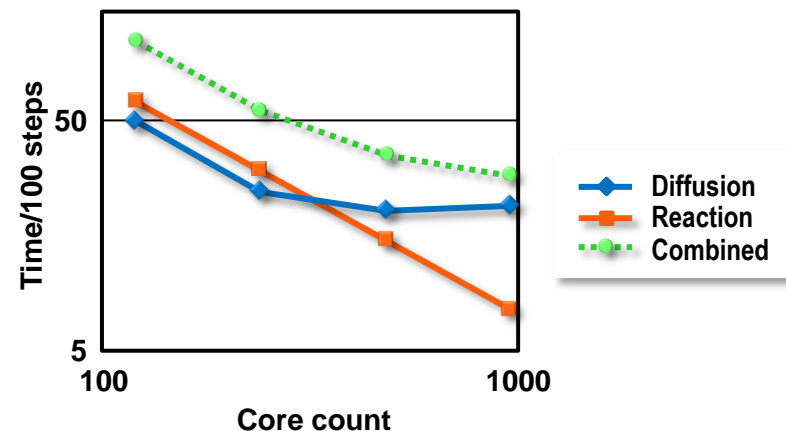
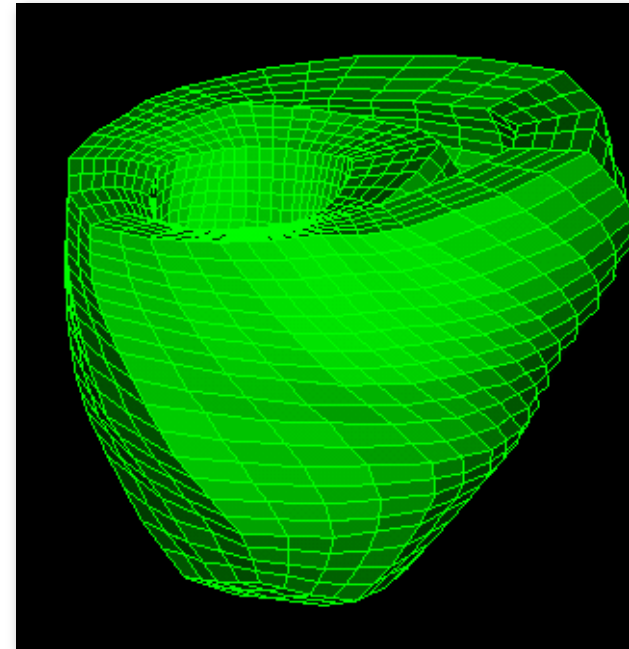
$$\frac{\partial T_a}{\partial t} = \epsilon(V)(k_{T_a} V - T_a),$$

Fox et al., Am J Physiol, 2002



# Collaborative Computational Effort: 1000+ Cores

- Collaborative research on kraken between NICS and University partners
- Transform a 2D serial research code to a multi-physics 3D parallel code (1000 + Core)
- Solve a set of diffusion reaction equations
- Mesh refinement: CUBIT
- Domain decomposition: Metis
- Efficient I/O distribution
- Finite Element scheme: 3D hexahedron
- Cell-wise reaction: Euler ischeme
- Linear solve package: Trilinos
- VTK output: VISIT used for visualization





## Contact

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