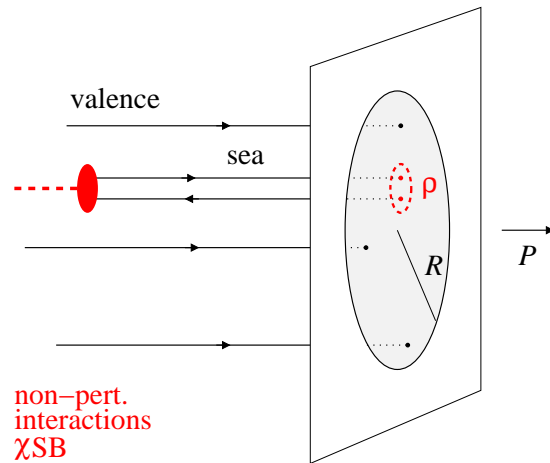


# Intrinsic transverse momentum and dynamical chiral symmetry breaking

C. Weiss (JLab), QCD Evolution Workshop, JLab, 14–May–12,  
based on P. Schweitzer, M. Strikman, CW 12, to appear



- Chiral symmetry breaking in QCD
  - Short-distance scale  $\rho \ll R$
  - Imprint on partonic structure
- Effective description of  $\chi$ SB
  - Constituent quarks and Goldstone bosons
  - Nucleon as chiral soliton  $N_c \rightarrow \infty$
- Transverse momentum distributions
  - Valence quarks  $p_T \sim R^{-1}$
  - Sea quarks “tail”  $p_T \lesssim \rho^{-1}$  Qualitative difference!
  - Coordinate space correlator New interpretation!
  - Short-range correlations in LCWF
- Implications for SIDIS
  - Initial condition for QCD evolution
  - Charge/ flavor separation techniques

## I) Intrinsic $p_T$ of sea quarks?

Sea vs. valence quarks  
Role of chiral symmetry breaking

## II) Parton correlations in LCWF?

Mean field  $\rightarrow$  correlations

# Chiral symmetry breaking in QCD

- $\chi$ SB in QCD vacuum

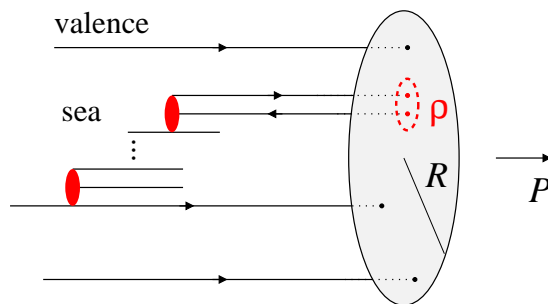
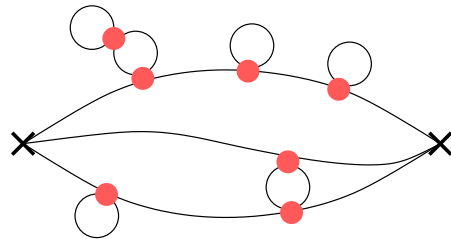
Strong gluon fields of size  $\rho \ll R \sim 1 \text{ fm}$   
 Shuryak; Diakonov, Petrov 80's

Condensate of  $q\bar{q}$  pairs,  $\pi$  as collective excitation

Gauge-invariant measure of  $q\bar{q}$  pair size  
 $\langle \bar{\psi} \nabla^2 \psi \rangle / \langle \bar{\psi} \psi \rangle \sim 1 \text{ GeV}^2$  "average virtuality"

Lattice: Teper 87, Doi 02, Chiu 03. Instantons: Polyakov, CW 96

Nucleon: Dynamical mass, short-range interactions  
 Euclidean correlation functions  $\rightarrow$  Lattice, analytic methods



- How does it affect partonic structure?

Nucleon fast-moving  $P \rightarrow \infty$ :  
 Wave function description Gribov 70's

Valence quark configurations of size  $\sim R$

Sea quarks in correlated pairs of size  $\lesssim \rho$

Soft wave function at scale  $\rho^{-2}$

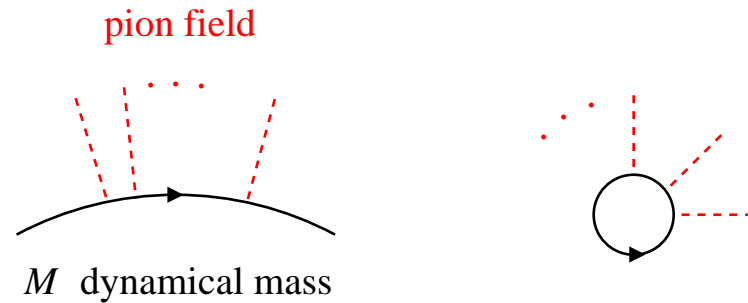
QCD radiation builds up  $p_T^2 \sim Q^2$  in hard processes

Can we quantify it? . . . Dynamical model!

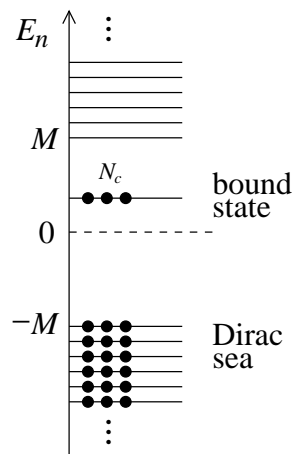
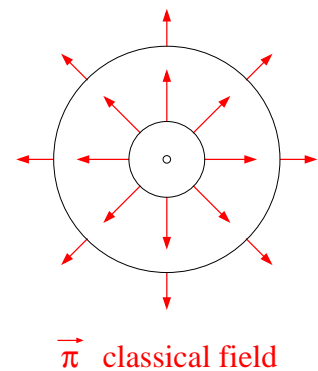
# Chiral quark–soliton model: Dynamics

- Effective description of  $\chi$ SB

Diakonov, Eides 83; Diakonov, Petrov 86



$$L_{\text{eff}} = \bar{\psi} (i\partial - M e^{i\gamma_5 \vec{\tau} \vec{\pi} / f_\pi}) \psi$$



Constituent quarks/antiquarks with dynamical mass  $M \sim 0.3\text{-}0.4$  GeV

Coupled to Goldstone pion field with eff. coupling  $M/f_\pi = 3\text{-}4$  strongly coupled!

Valid up to  $\chi$ SB scale  $\rho^{-2}$ :  
Matching with QCD quarks/gluons

Field theory, solved non-perturbatively in  $1/N_c$  expansion

- Nucleon as chiral soliton

Diakonov, Petrov, Pobylitsa 88; Kahana, Ripka 84

Classical pion field: “Hedgehog” rest frame

Quarks in single-particle orbits:  
Bound state, Dirac continuum

Relativistic mean-field approximation

Fully field-theoretical: Completeness, conservation laws, positivity  $\rho^{-2} \gg M^2$

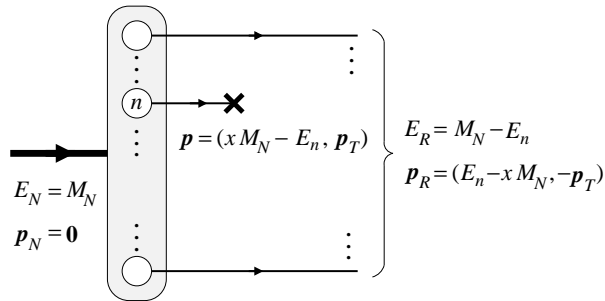
No Fock space truncation!

→ PDFs, sea quarks

# Chiral quark–soliton model: Parton distributions

$$f^q(x, \mathbf{p}_T) = \langle N_P | a^\dagger a(xP, \mathbf{p}_T) | N_P \rangle_{P \rightarrow \infty}$$

$$f^{\bar{q}}(x, \mathbf{p}_T) = b^\dagger b$$



- Parton densities in  $\chi$ QSM

Diakonov, Petrov, Pobylitsa, Polyakov, CW 96+.

Also: Gamberg, Weigel, Reinhardt 96+; Wakamatsu et al. 97+

Quark number densities at  $P \rightarrow \infty$   
 Light-cone “plus” momentum density  
 Equivalent! Relativistic field-theoretical formulation

Sum over single-particle levels rest frame

$p_T$  integral convergent due to cutoff  $\rho^{-2}$

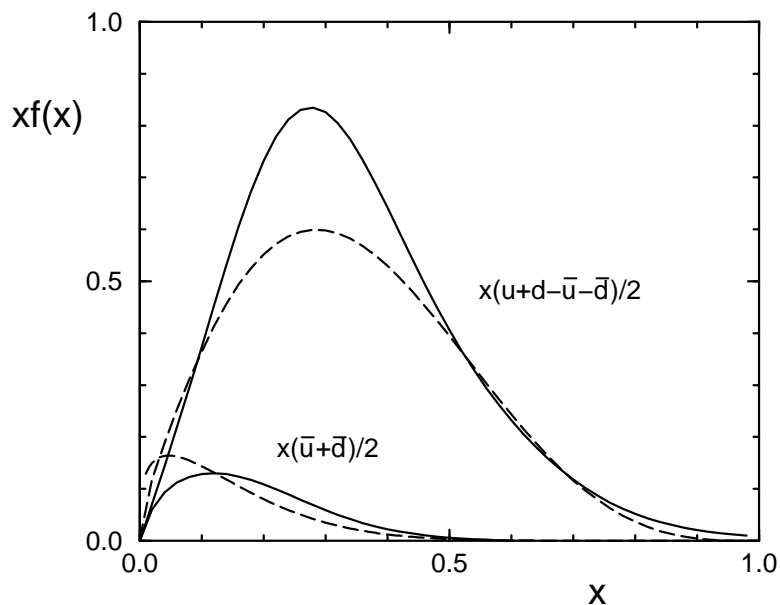
- Interpretation of distributions

$x$  and  $p_T$  distribution of constituent quarks and antiquarks

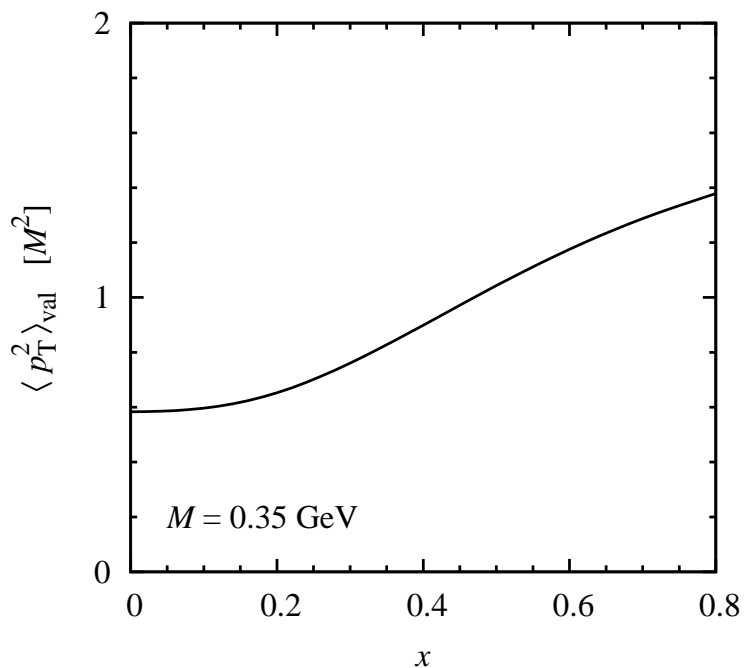
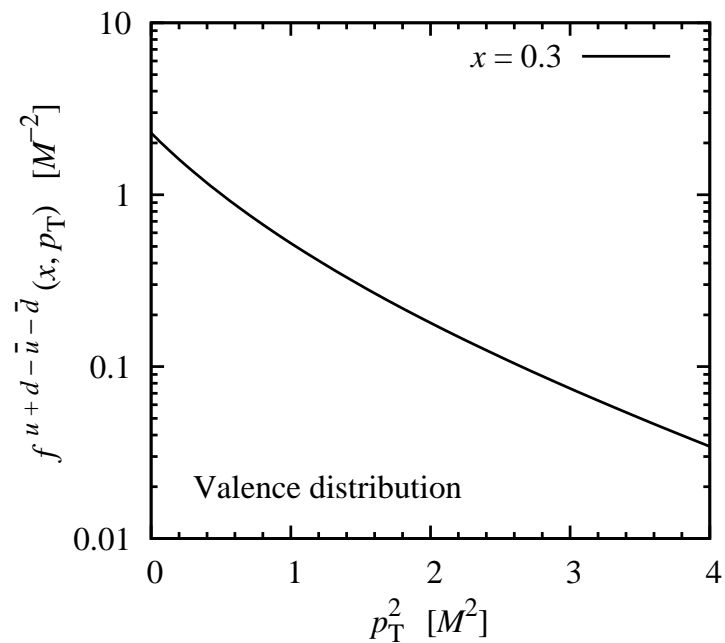
Matching with QCD quarks, antiquarks and gluons at scale  $\rho^{-2}$ ; requires info “beyond” effective dynamics

Simplest approximation: Match constituent quarks with QCD quarks at  $\rho^{-2}$ , no gluons. Accuracy?

PDF fits show 30% of nucleon momentum carried by gluons at  $\mu^2 \sim 0.4 \text{ GeV}^2$  GRV98



# $p_T$ distribution: Valence quarks



- Valence distribution  $f^{q-\bar{q}}(x, p_T)$  dominated by bound-state level

Wakamatsu 09, Schweitzer, Strikman CW 12

Concentrated at  $p_T^2 \sim M^2 \sim R_{\text{nucl}}^{-2}$

Not sensitive to scale  $\rho^{-2}$

Roughly Gaussian shape

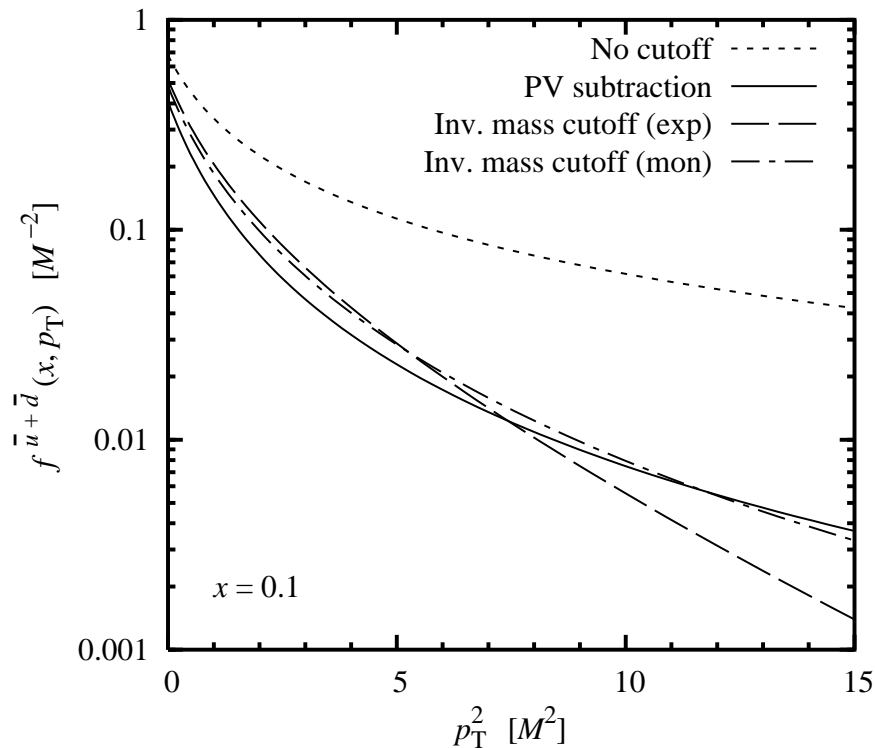
- Average  $\langle p_T^2 \rangle_{\text{val}}$  increases with  $x$

General property of relativistic bound state

Cf. bag model, light-front quark model

Valence quark  $p_T \sim 1/R_{\text{nucl}}$

# $p_T$ distribution: Sea quarks



Schweitzer, Strikman, CW 12

- Sea quark distribution  $f^{\bar{q}}(x, p_T)$  dominated by Dirac continuum

Analytic expression from expansion in  $\nabla\pi/M$  “Gradient expansion” DPPPW96

$$f^{\bar{q}}(x, p_T) \sim \frac{C(x)}{p_T^2 + M^2}$$

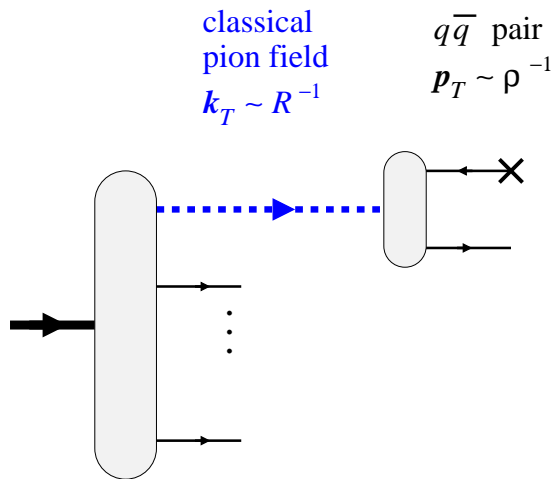
Power-like tail at  $p_T^2 \gg M^2$ , regularized by cutoff  $\rho^{-2}$

Numerical distributions at  $p_T^2 \sim \text{few } M^2$  not sensitive to regularization scheme  
Physical conditions: Schweitzer, Strikman, CW 12

- Average  $\langle p_T^2 \rangle_{\text{val}}$  not a sensible measure of “width” of sea quark distribution

Sea quark  $p_T$  distribution qualitatively different from valence quarks

# $p_T$ distribution: Short-range correlations



$$f^{\bar{q}}(x, \mathbf{p}_T) = \int_x \frac{dy}{y} \int d^2 k_T$$

$$\times f_\pi(y, \mathbf{k}_T) f_{\text{pair}}(x/y; \mathbf{p}_T, \mathbf{k}_T)$$

Gradient expansion as partonic convolution,  
cf. DGLAP evolution. SSW 12

- How do configurations with  $p_T \sim \rho^{-1}$  arise dynamically?
- Short-range correlations in partonic wave function

Classical pion field creates  $q\bar{q}$  pair

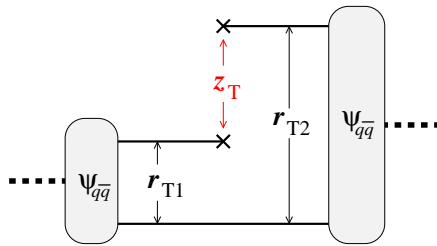
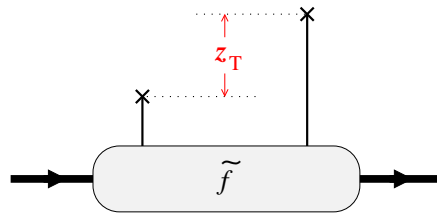
$q\bar{q}$  pair has intrinsic  $p_T \lesssim \rho^{-1}$

Pair quantum numbers  $\pi, \sigma$

Analogy with “pion cloud model,”  
but rigorous formulation based on  
 $1/N_c$  expansion: Strong coupling,  
all orders, classical field!

Short-range correlations: Imprint  
of  $\chi$ SB on partonic structure

# $p_T$ distribution: Coordinate-space correlator

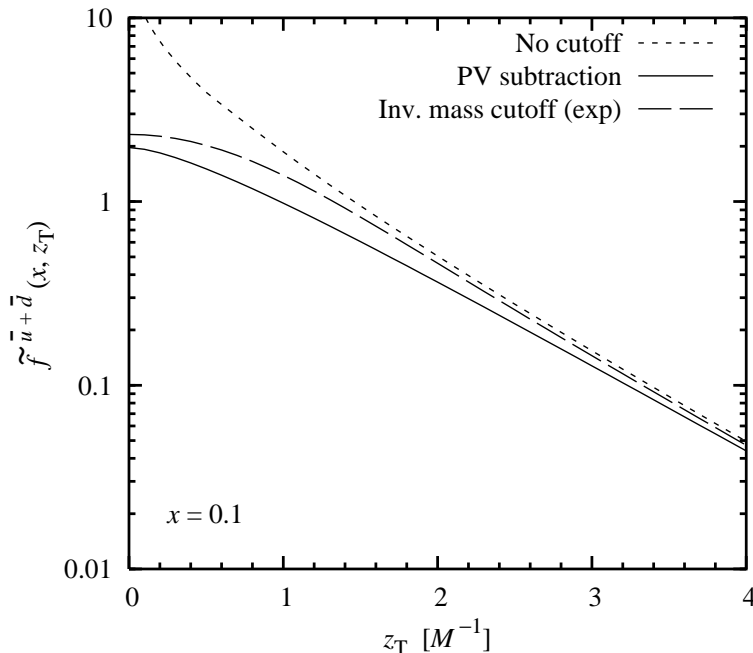


- Quark field correlator w. transverse separation

$$\tilde{f}(x, z_T) = \int dz^- e^{ixP^+z^-} \times \langle P | \bar{\psi}(0) \gamma^+ \psi(z) | P \rangle_{z^+=0}$$

Fourier transform of  $f(x, \mathbf{p}_T)$

Defined here within effective model;  
no relation to “TMD” in QCD  
Intrinsic  $p_T$ , no final-state interactions



- Interesting properties

$$z_T = 0 \quad \tilde{f}^{\bar{u}+\bar{d}}(x, 0) = f^{\bar{u}+\bar{d}}(x) \quad \text{PDF}$$

$$z_T \rightarrow \infty \quad \tilde{f}^{\bar{u}+\bar{d}}(x, z_T) \sim e^{-Mz_T} \quad \text{“mass gap”}$$

Intermediate  $z_T$  tightly constrained  
New general framework for modeling  $p_T$  distributions?

- Interpretation within model

Measures size distribution of correlated  $q\bar{q}$  pairs in nucleon



# Intrinsic $p_T$ : Hard processes

- Model describes “intrinsic”  $p_T$  due to non-perturbative dynamics.  
In hard processes  $p_T \lesssim Q$  are built up by QCD radiation
- QCD evolution should start at  $\chi$ SB scale  $\rho^{-2} \approx 0.4 \text{ GeV}^2$ , “GRV scale,” cf. PDF fits  
not  $R^{-2} \approx 0.04 \text{ GeV}^2$

Non-perturbative short-distance scale!

Data show that  $\langle P_T^2 \rangle_{\text{hadron}}$  in SIDIS practically independent of  $Q^2$ , varies only with  $W$ .  
Suggests limited role of QCD evolution.

EMC 91:  $\langle P_T^2 \rangle_{\text{hadron}}$  unchanged between  $Q^2 = 2 \text{ GeV}^2$  and  $60 \text{ GeV}^2$

- Charge/ flavor separation techniques in SIDIS may need to be modified  
if valence and sea quarks have different  $p_T$  distributions

Frankfurt et al 89; Christova, Leader 00

$$\int_{\text{finite range}} d^2 p_T [f^q(x, p_T) - f^{\bar{q}}(x, p_T)] \quad \text{not simply related to } f_{\text{val}}^q(x)$$

# Summary and outlook

- Dynamical  $\chi$ SB in QCD creates short-distance scale  $\rho \ll R \sim 1 \text{ fm}$

Natural scale for separating soft wave function  $\leftrightarrow$  pQCD radiation

- Qualitatively different  $p_T$  distributions of valence and sea quarks

Valence quarks  $p_T \sim R^{-1}$

Sea quarks “tail”  $p_T \lesssim \rho^{-1}$

- Short-range correlations in partonic wave function

Imprint of QCD vacuum on partonic structure

Coordinate-space  $z_T$  distribution measures size of correlated  $q\bar{q}$  pairs

- Outlook

Implications for single-particle inclusive DIS

Direct study of  $q\bar{q}$  correlations through simultaneous measurements of current and target fragmentation regions

Identify kinematic region dominated by non-perturbative correlations. Schweitzer, Strikman, CW, in progress

Multiparton interactions in high-energy  $pp$  collisions LHC. New field of study!