

# Light Nuclei from keV to GeV Energies: a Review

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- Strong and electromagnetic interactions in nuclei
- Relativistic descriptions of few-nucleon dynamics
- Tensor forces and ground-state structure
- Inferring nucleon properties from nuclear experiments
- Summary(ies)
- Future prospects

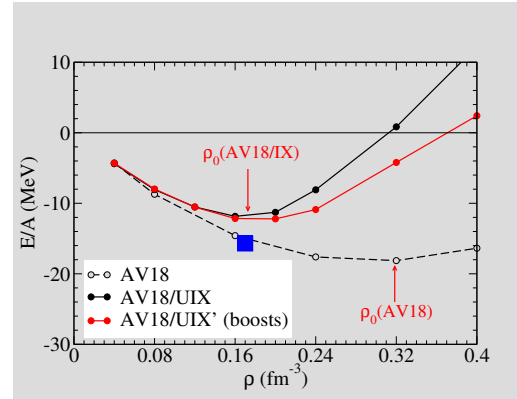
In collaboration with:

J. Carlson	A. Kievsky	L. Marcucci	K. Nollett
S. Pieper	M. Viviani	R. Wiringa	

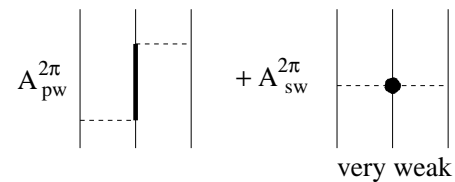
# Nuclear Interactions and Currents: an Update

## Nuclear Interactions

- $NN$  interactions alone fail to predict:
  1. spectra of light nuclei
  2.  $Nd$  scattering
  3. nuclear matter  $E_0(\rho)$



- $2\pi$ - $NNN$  interactions [EFT w/o explicit  $\Delta$ 's overestimates strength of  $V_{pw}^{2\pi}$ , Pandharipande *et al.*, PRC71, 064002 (2005)]:

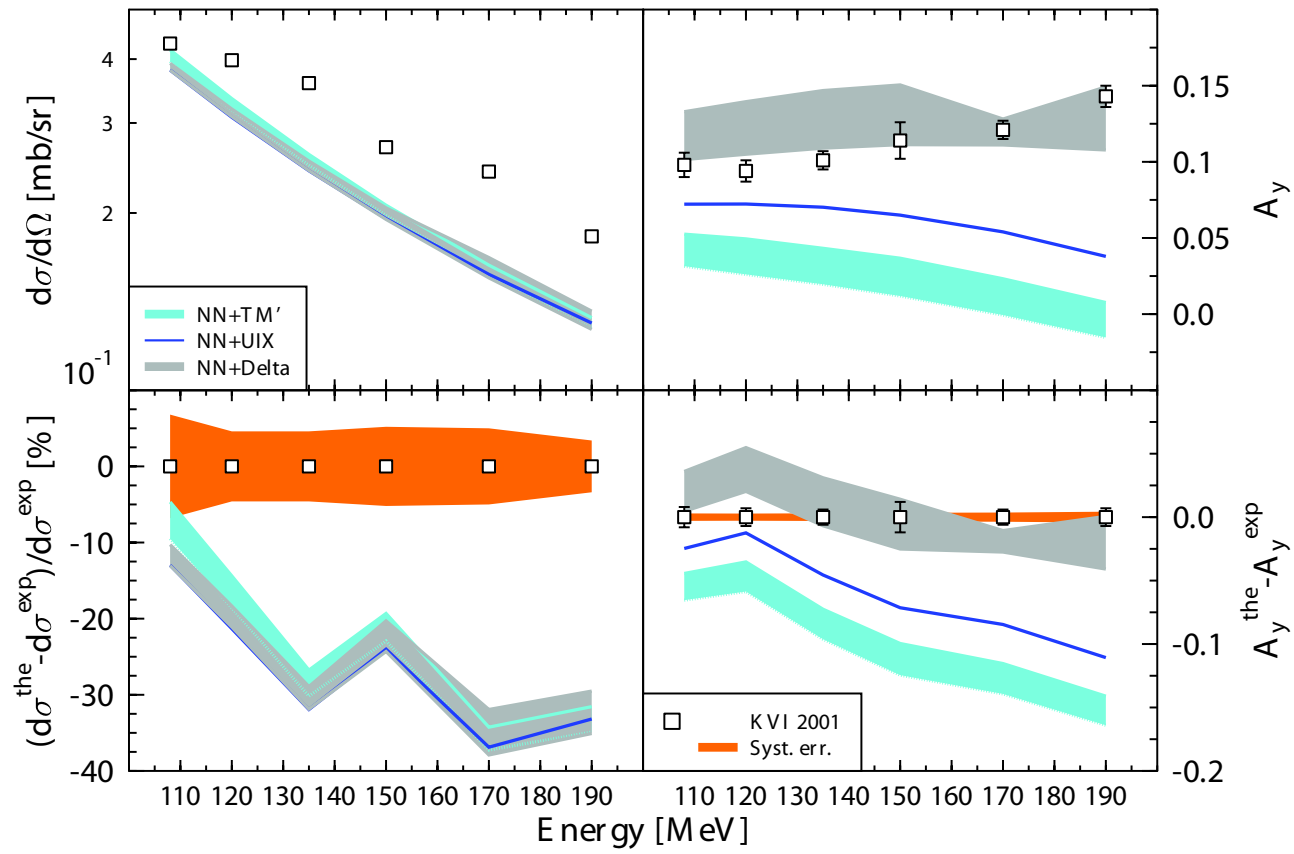


- $V^{2\pi}$  alone does not fix problems above

# Proton-Deuteron Elastic Scattering

Ermisch *et al.* (KVI collaboration), PRC71, 064004 (2005)

Kalantar-Nayestanaki, private communication



Beyond  $2\pi$ -exchange (IL2 model, with important  $T = 3/2$  terms)

$$V^{2\pi} + A^{3\pi} \left[ \text{diagram 1} + \text{diagram 2} \right] + A^R \sum_{\text{cyc}} T^2(r_{ij}) T^2(r_{jk})$$

parameters ( $\sim 3$ ) fixed by a best fit to the energies of low-lying states ( $\sim 17$ ) of nuclei with  $A \leq 8$  (IL2 presently under revision ...)

AV18/IL2 Hamiltonian reproduces well:

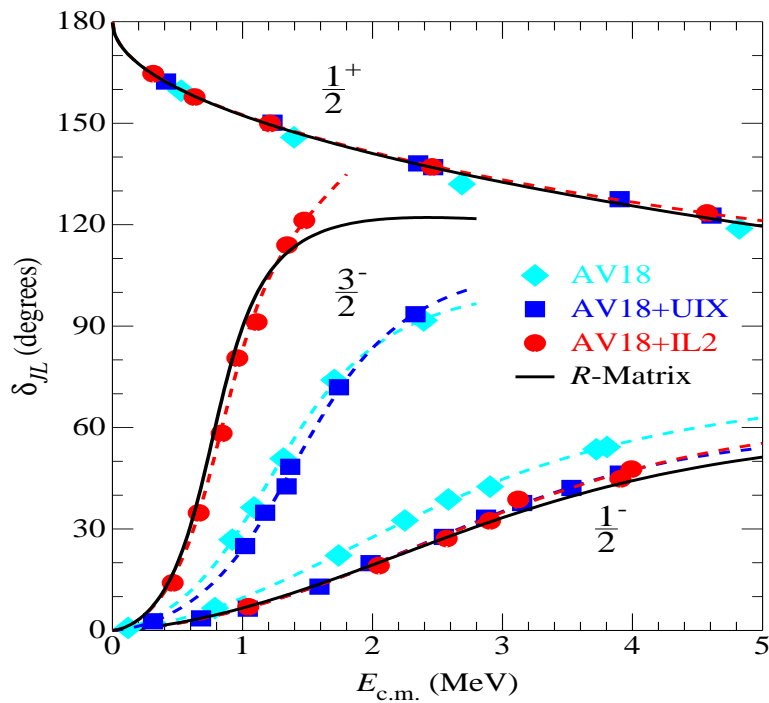
- spectra of  $A=9-12$  nuclei (attraction provided by IL2 in  $T = 3/2$  triplets crucial for  $p$ -shell nuclei)
- low-lying  $p$ -wave resonances with  $J^\pi = 3/2^-$  and  $1/2^-$  respectively, as well as low-energy  $s$ -wave ( $1/2^+$ ) scattering

but needs to be tested in three- and four-nucleon scattering (work by the Pisa group is in progress)

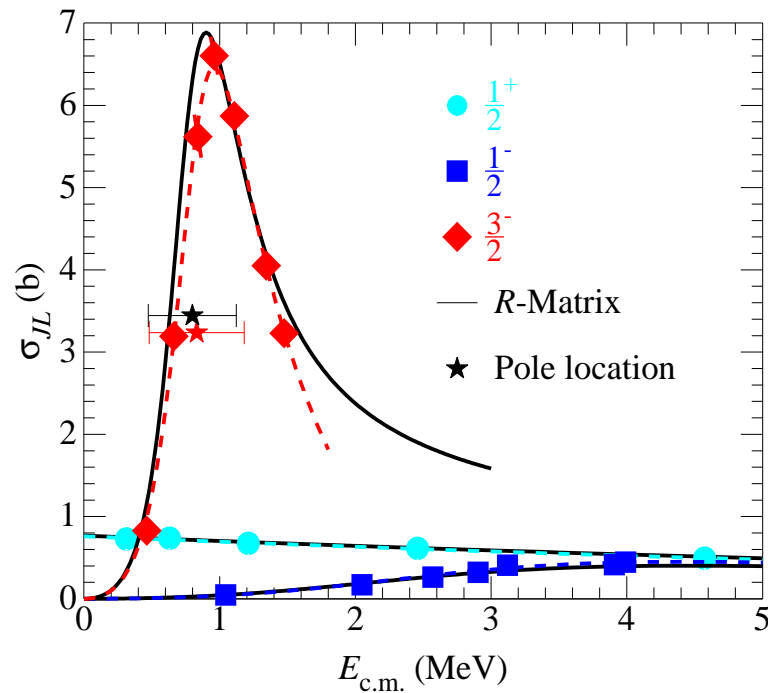
# QMC Calculations of Low Energy n- $\alpha$ Scattering

Nollett *et al.*, nucl-th/0612035, PRL in press

## Phase Shifts



## Cross Sections (AV18/IL2)



AV18, AV18/IX, and AV18/IL2 phase shifts compared to experimental determinations from *R*-matrix fits

## Nuclear Electromagnetic Currents

Marcucci *et al.*, PRC**72**, 014001 (2005)

$$\mathbf{j} = \mathbf{j}^{(1)} + \mathbf{j}^{(2)}(v) + \mathbf{j}^{(3)}(V^{2\pi})$$

transverse

- Gauge invariant:

$$\mathbf{q} \cdot \left[ \mathbf{j}^{(1)} + \mathbf{j}^{(2)}(v) + \mathbf{j}^{(3)}(V^{2\pi}) \right] = \left[ T + v + V^{2\pi}, \rho \right]$$

$\rho$  is the nuclear charge operator

- Terms from static part  $v_0$  of  $v$  (and  $V^{2\pi}$ ) assumed to arise from pion-like ( $PS$ ) and rho-like ( $V$ ) exchanges:

$$\mathbf{j}_{ij}(v_0; PS) = i (\boldsymbol{\tau}_i \times \boldsymbol{\tau}_j)_z \left[ v_{PS}(k_j) \boldsymbol{\sigma}_i (\boldsymbol{\sigma}_j \cdot \mathbf{k}_j) + \frac{\mathbf{k}_i - \mathbf{k}_j}{k_i^2 - k_j^2} v_{PS}(k_i) (\boldsymbol{\sigma}_i \cdot \mathbf{k}_i) (\boldsymbol{\sigma}_j \cdot \mathbf{k}_j) \right] + i \Leftrightarrow j$$

with  $v_{PS} = v^{\sigma\tau} - 2v^{t\tau}$

- Terms from velocity-dependent part  $v_1$  of  $v$  by minimal substitution:  $\mathbf{p}_i \rightarrow \mathbf{p}_i - e \mathbf{A}(\mathbf{r}_i)$
- $\mathbf{j}^{(2)}(v)$  satisfies:

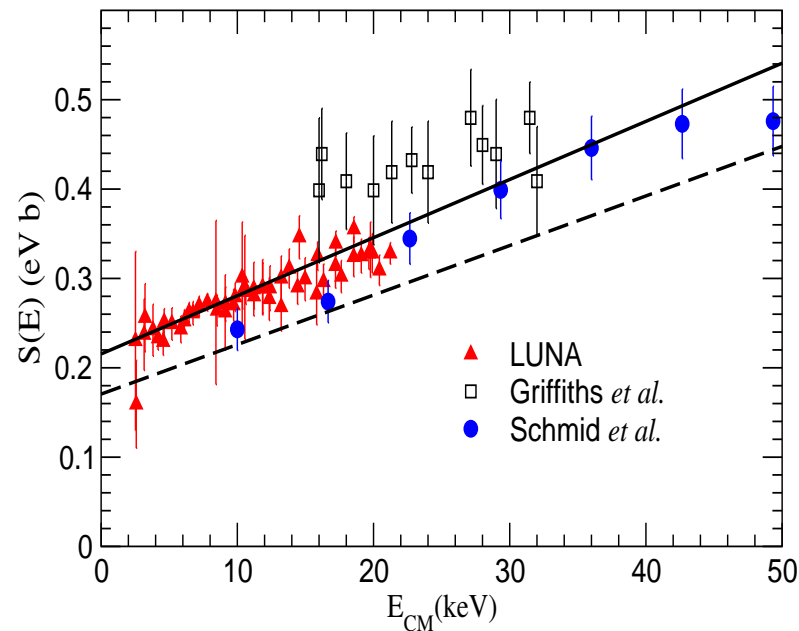
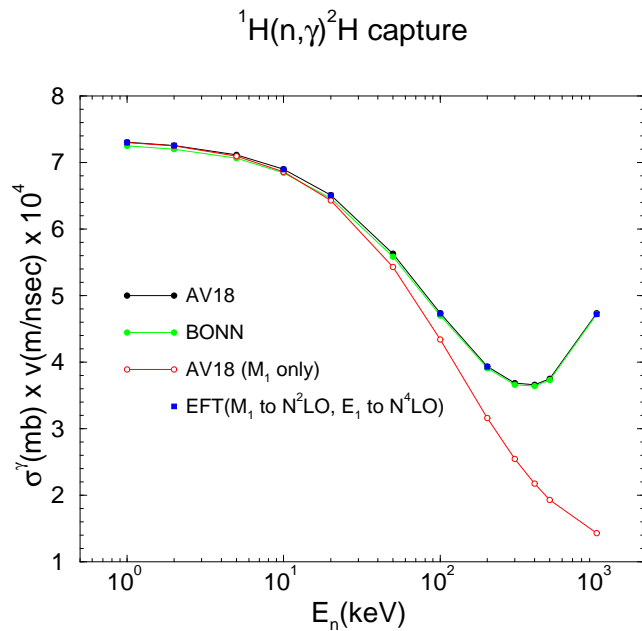
$$\mathbf{j}^{(2)}(v) \xrightarrow{\text{long range}} \begin{array}{c} | \quad \pi \quad | \\ \text{---} \text{---} \text{---} \\ | \quad \pi \quad | \\ \text{---} \text{---} \text{---} \\ | \quad \pi \quad \pi \quad | \\ \text{---} \text{---} \text{---} \end{array}$$



## Radiative Captures in $A=2$ and 3 Systems

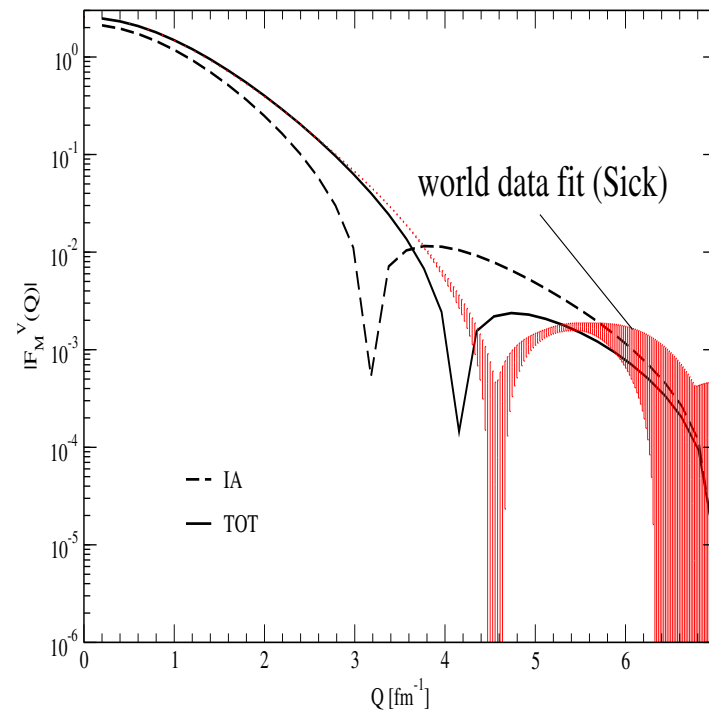
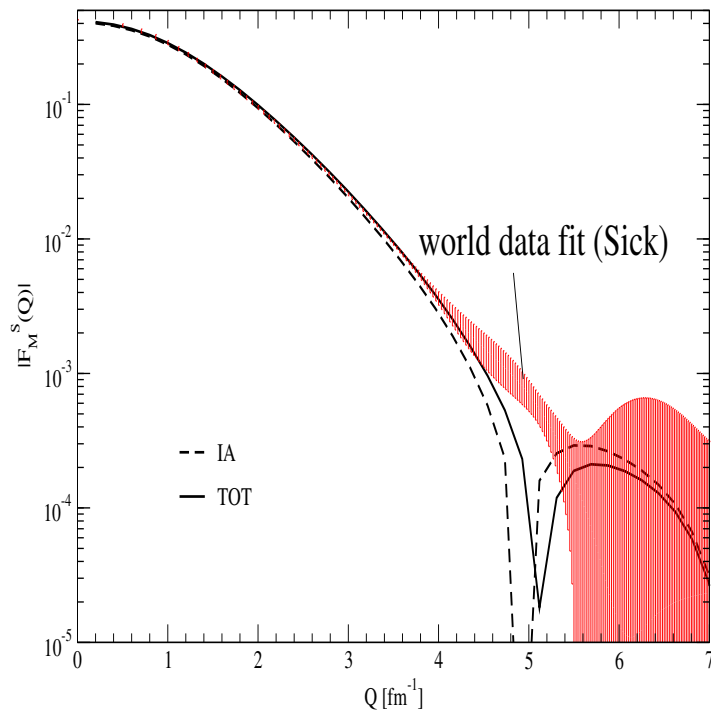
Marcucci *et al.*, PRC**72**, 014001 (2005)

### ${}^2\text{H}(p, \gamma){}^3\text{He}$ capture



- however, theory overpredicts  ${}^2\text{H}(n, \gamma){}^3\text{H}$  and  ${}^3\text{He}(n, \gamma){}^4\text{He}$  x-sections at thermal energies by 9% and  $\approx 30\%$  respectively

## Isoscalar and Isovector Magnetic Structure in $A=3$ Nuclei



- diffraction region in  $F_M^V$  “problematic” for theory: similar trend seen in deuteron threshold  $e$ -disintegration

(Arriaga and Schiavilla, arXiv:0704.2514, PRC in press)

## Summary (I)

- Energy spectra and  $n$ - $\alpha$  scattering well described by two- and three-nucleon interactions (AV18/IL2)
- $3N$  and  $4N$  scattering as a crucial testing ground for three-nucleon interactions (tests of IL2 are in progress)
- Constructed current (and charge) operators, which reproduce well a variety of light-nuclei EM observables (charge f.f.'s, inclusive  $(e, e')$  and exclusive  $(e, e'p)$  responses, ...)
- But a few discrepancies persist:  $nd$  (and  $n^3\text{He}$ ) radiative capture(s), diffraction region in  $F_M^V(q)$ , ...

# Approaches to Relativistic Dynamics

## Hamiltonian Dynamics

(Instant-form) Hamiltonian dynamics [Krajcik and Foldy, PRD10, 1777 (1974);

Carlson, Pandharipande, and Schiavilla, PRC47, 484 (1993)]:

$$H = \sum_i \sqrt{\mathbf{p}_i^2 + m^2} + \sum_{i < j} [v_{ij} + \delta v_{ij}(\mathbf{P}_{ij})] + \dots$$

- $v$  is the rest frame interaction (fitted to  $NN$  data)
- $\delta v(\mathbf{P})$  (“boost interaction”) depends on pair momentum  $\mathbf{P}$ , and is determined from  $v$  via (Poincaré group)  $[\hat{\mathbf{K}}, \hat{H}] = i \hat{\mathbf{P}}$ :

$$\delta v(\mathbf{P}) = -\frac{P^2}{8m^2} v + \frac{i}{8m^2} [\mathbf{P} \cdot \mathbf{r} \mathbf{P} \cdot \mathbf{p}, v] + \frac{i}{8m^2} [(\boldsymbol{\sigma}_i - \boldsymbol{\sigma}_j) \times \mathbf{P} \cdot \mathbf{p}, v]$$

- Boosting (two-body, for example) states from the rest frame to a frame moving with velocity  $\boldsymbol{\beta}$ :

$$\psi_{\boldsymbol{\beta}}(\mathbf{p}) = \frac{1}{\sqrt{\gamma}} \left[ 1 - \frac{i}{4m} \boldsymbol{\beta} \cdot (\boldsymbol{\sigma}_i - \boldsymbol{\sigma}_j) \times \mathbf{p} \right] \psi_0(\mathbf{p}_{\parallel}/\gamma, \mathbf{p}_{\perp})$$

## Spectator Formalism

Spectator formalism, aka Gross equation<sup>a</sup>: explicit  $N$  and  $\bar{N}$  d.o.f. (consequently, deuteron develops P-wave components)

- Bound state obtained from:

$$\begin{array}{c} * \\ \diagdown \\ \text{---} \end{array} \begin{array}{c} \diagup \\ * \end{array} = \begin{array}{c} * \\ \diagdown \\ \text{---} \end{array} \begin{array}{c} \text{---} \\ \text{---} \end{array} \begin{array}{c} \diagup \\ * \end{array} \quad \text{with} \quad \begin{array}{c} * \\ \diagdown \\ \text{---} \end{array} \begin{array}{c} \text{---} \\ \text{---} \end{array} = \begin{array}{c} * * \\ \text{---} \end{array} \pm \begin{array}{c} * \\ \diagdown \\ \text{---} \end{array} \begin{array}{c} \diagup \\ * \end{array}$$

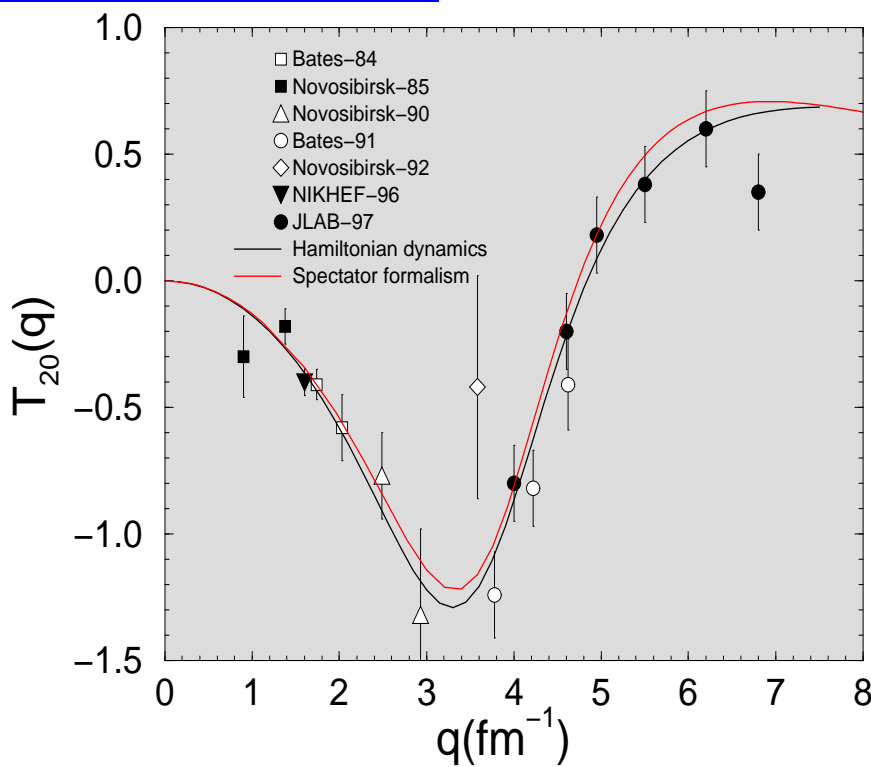
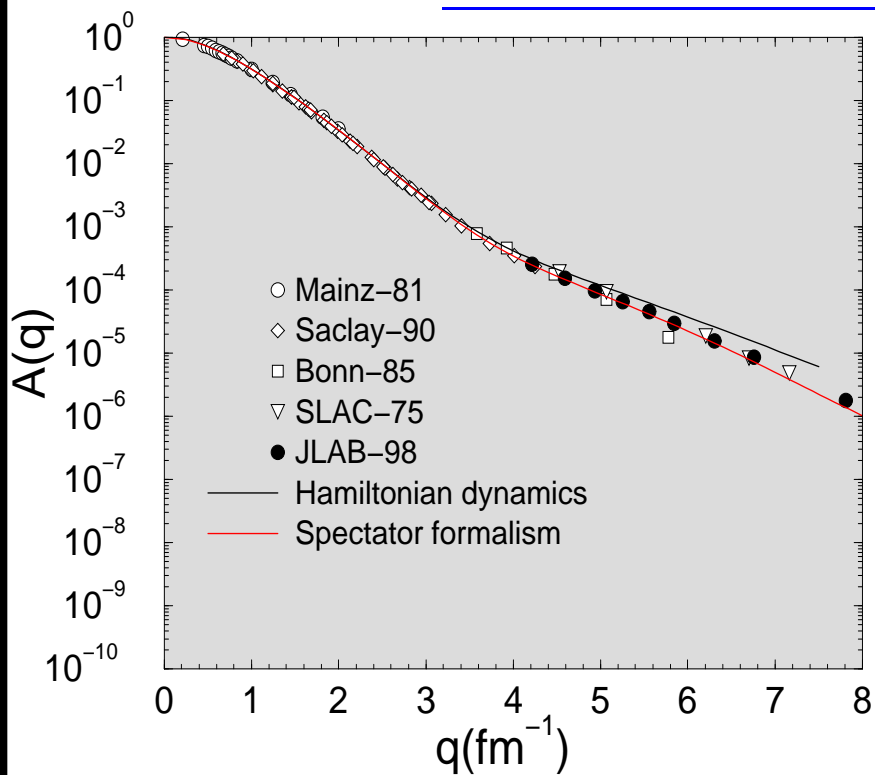
- $v$  is a high-quality ( $\chi^2=1$ ) OBE model with effective  $I=0$  and  $1$ ,  $J^\pi=0^+, 0^-, 1^-$  exchanges; it includes off-shell couplings<sup>b</sup>:

$$\text{scalar vertex} = g_S - \nu_S \left[ (m - \not{p}) / (2m) + (m - \not{k}) / (2m) \right]$$

- $v$  reproduces  $E_0(^3\text{H})$ : crucial off-shell couplings simulate  $NNN$  interaction effects<sup>b</sup>
- Boosts are kinematical and exactly accounted for

<sup>a</sup>Gross, PR186, 1448 (1969); <sup>b</sup>Gross and Stadler, arXiv:0704.1229 and PRL78, 26 (1997)

## Deuteron Electromagnetic Structure



Hamiltonian dynamics (HD): Schiavilla and Pandharipande, PRC**65**, 064009 (2002)

Spectator formalism (SF): Van Orden, Devine, and Gross, PRL**75**, 4369 (1995), older OBE model

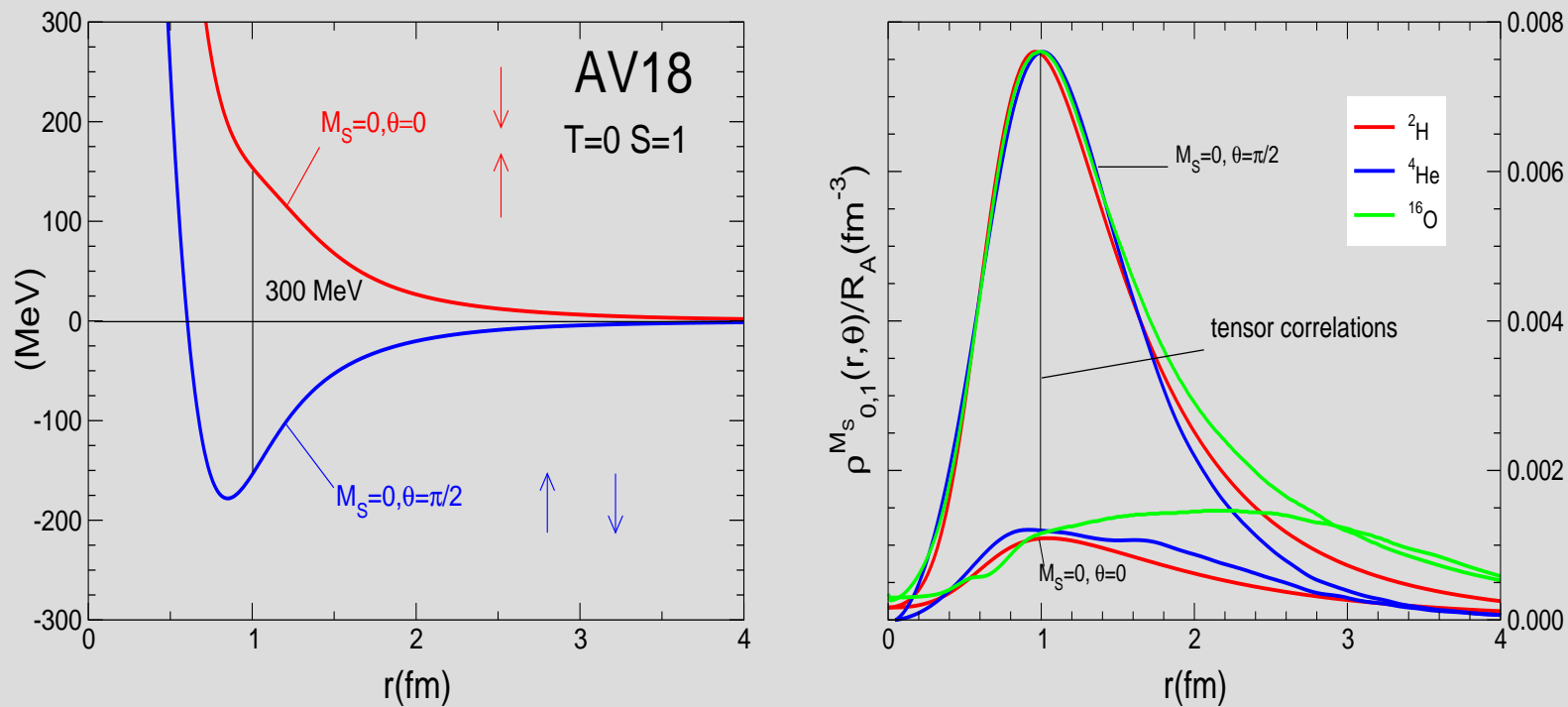
- HD and SF represent drastically different approaches, yet lead to equally satisfactory description of  $e-d$  elastic scattering

# Tensor Forces and Ground-State Structure



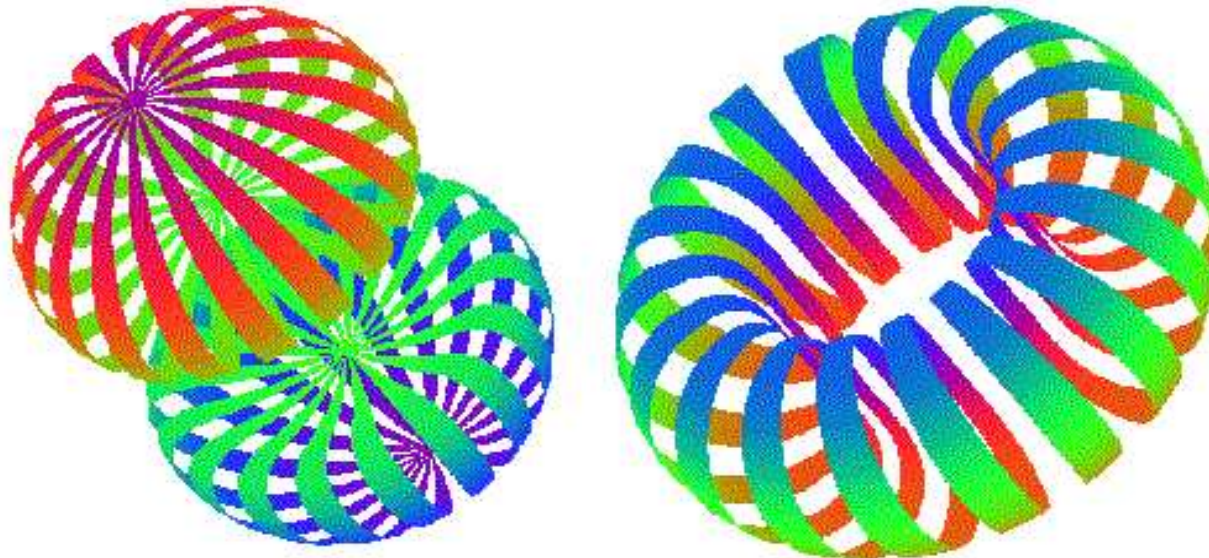
Preeminent features of  $v_{ij}$ :

- short-range repulsion (common to many systems)
- intermediate- to long-range tensor character (unique to nuclei)



Forest *et al.*, PRC54, 646 (1996)

## Two-Nucleon Density Profiles in $T, S=0,1$ States



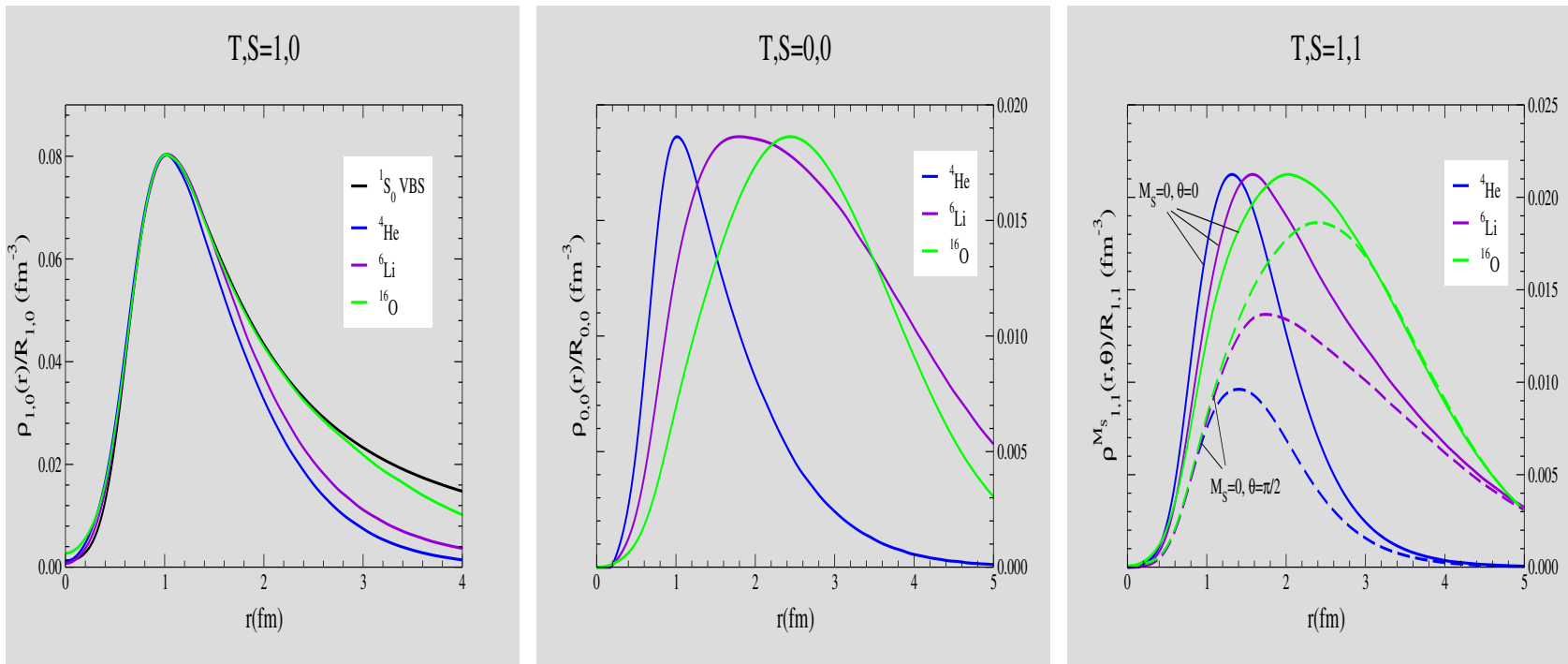
$$M_S = \pm 1$$

$$M_S = 0$$

- Hole due to short-range repulsion, angular confinement due to tensor force
- Size of torus:  $d \simeq 1.4$  fm,  $t \simeq 0.9$  fm (at  $\approx$  half-max density)
- Confirmed by  $e-d$  elastic scattering measurements

## Two-Nucleon Density Profiles in $T, S \neq 0, 1$ States

- Scaling persists in  $T, S=1, 0$  channel (quasibound  $^1S_0$  state) for  $r \leq 2$  fm
- But no scaling occurs in remaining channels (interaction either repulsive or weakly attractive)

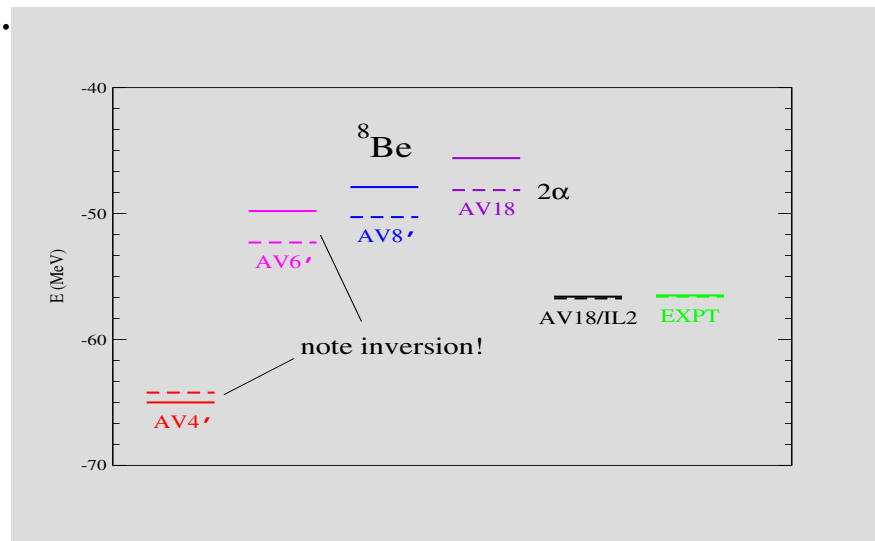


## Experimental Evidence for Tensor Correlations in $A > 2$ Nuclei

While many nuclear properties are affected by tensor correlations, their effects are generally subtle, and not easily isolated in data

For example, absence of stable  $A=8$  nuclei:

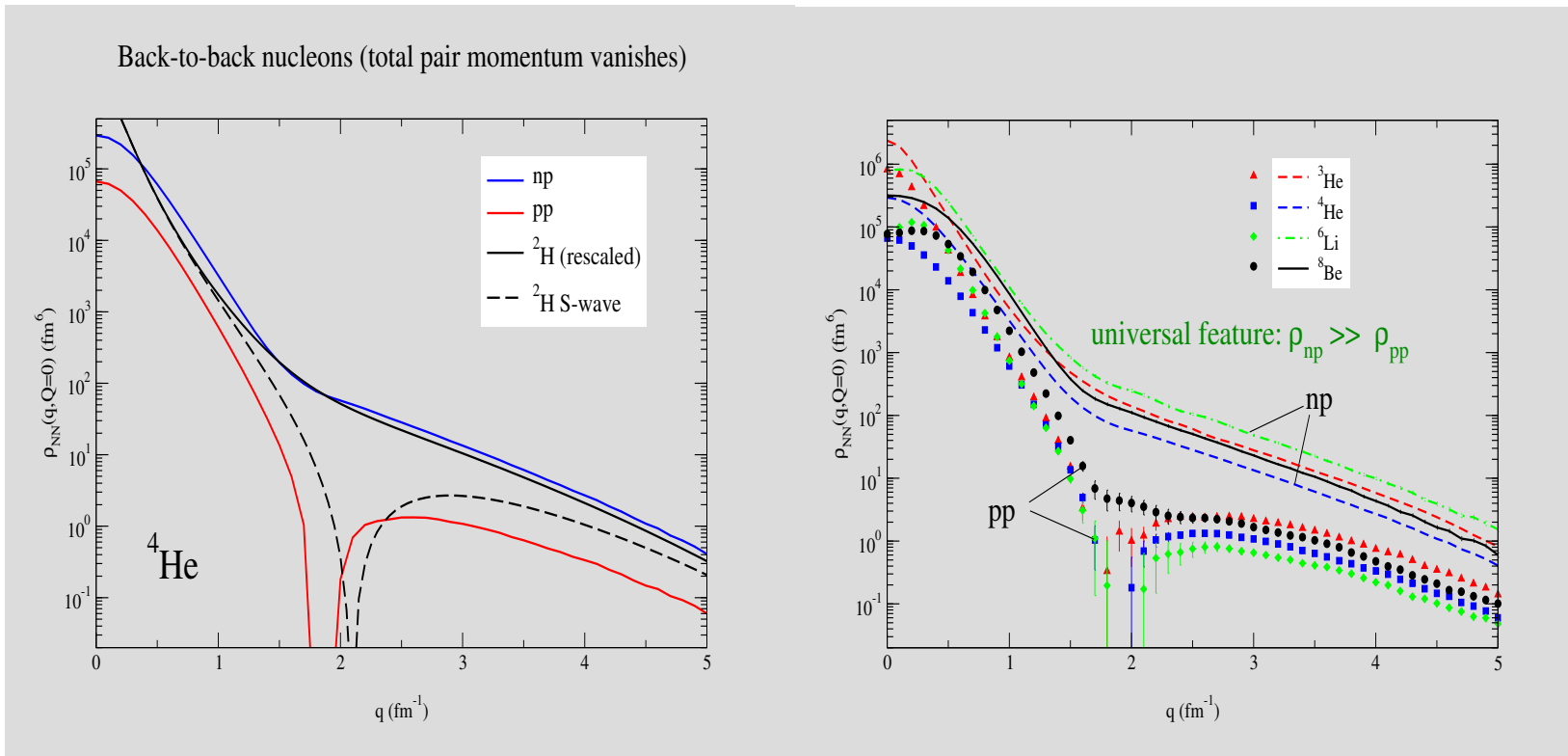
1.  $AV4'$  =  $[1, \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2] \otimes [1, \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2]$
2.  $AV6'$  =  $AV4'$  + tensor
3.  $AV8'$  =  $AV6'$  + spin-orbit, ...



Wiringa and Pieper, PRL $\mathbf{89}$ , 182501 (2002)

## New Opportunities for Observing Tensor Correlations

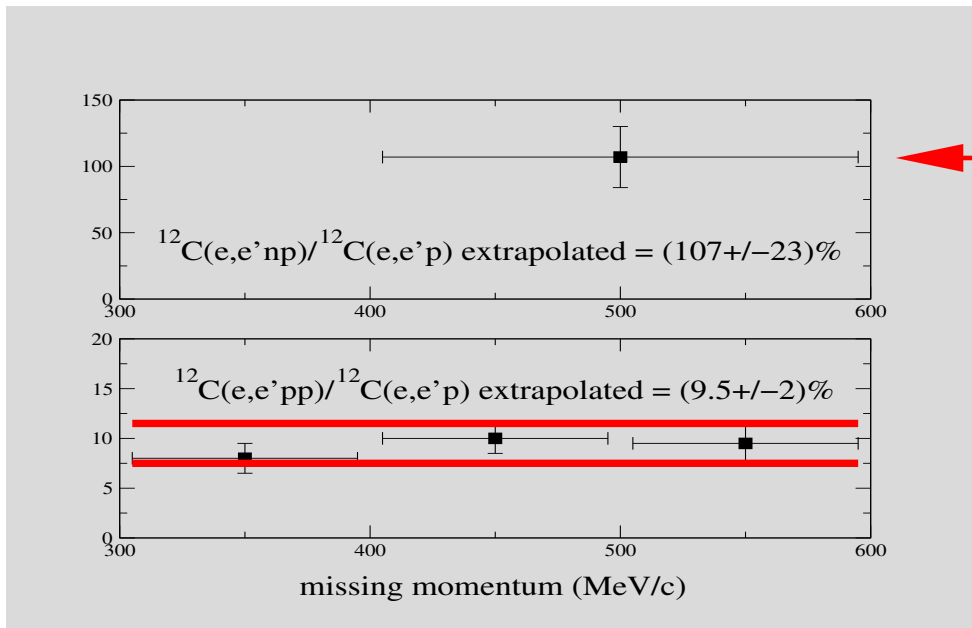
$np$  and  $pp$  pairs predominantly in deuteron-like and  $^1S_0$  states:  
large differences between  $np$ - and  $pp$ -pair momentum distributions



Schiavilla, Wiringa, Pieper, and Carlson, PRL98, 132501 (2007)

## Two-Nucleon Knockout Processes and Tensor Correlations

- JLab measurements on  $^{12}\text{C}(e, e'pp)^{\text{a}}$  and  $(e, e'np)^{\text{b}}$
- Analysis of  $^{12}\text{C}(p, pp)$  and  $(p, ppn)$  BNL data<sup>c</sup>
- Possibly also seen in  $\pi$ -absorption:  $\sigma(\pi^-, np)/\sigma(\pi^+, pp) \ll 1^{\text{d}}$



Analysis of BNL data:

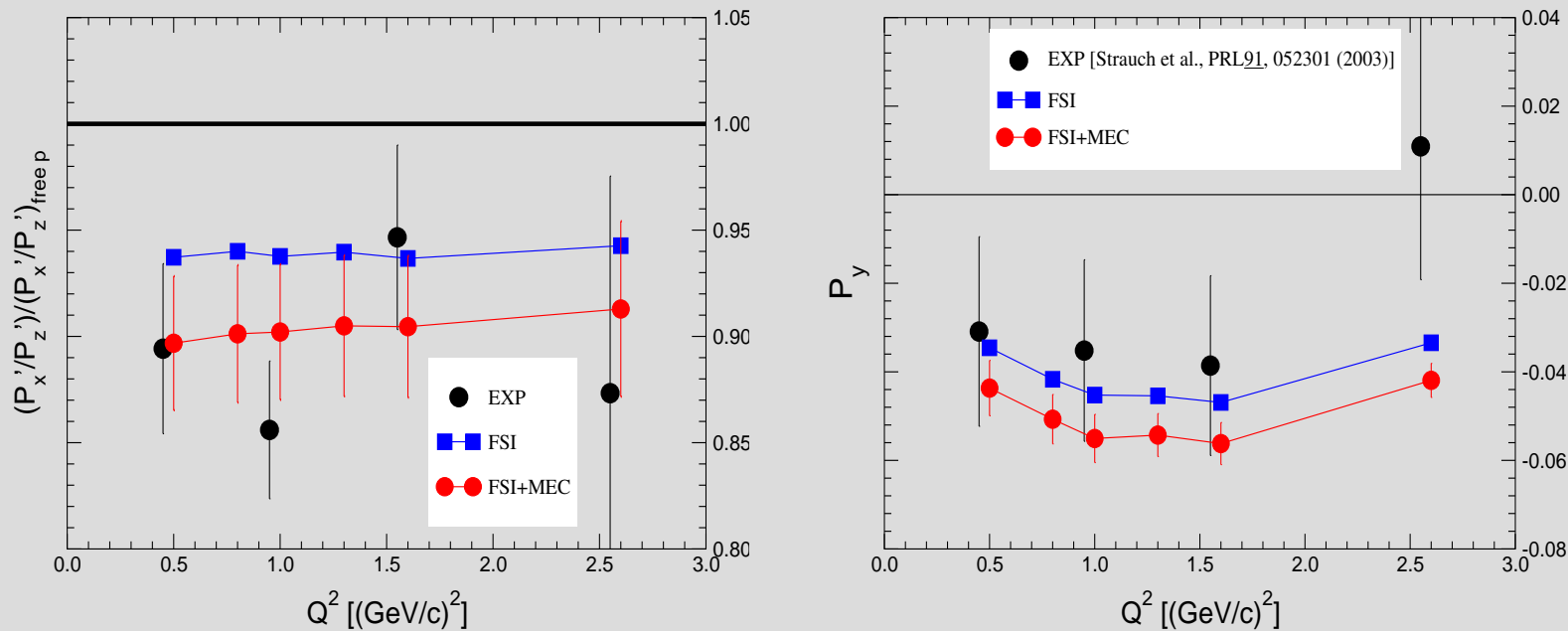
$$\frac{P_{pn}}{P_{pX}} = 92^{+8}_{-18}\%$$

<sup>a</sup> Shneor *et al.*, nucl-ex/0703023, submitted to PRL; <sup>b</sup> Subedi *et al.*, in preparation; <sup>c</sup> Piassetzky *et al.*, PRL**97**, 162504 (2006); <sup>d</sup> Ashery *et al.*, PRL**47**, 895 (1981)

# Nucleon Properties from Nuclear Experiments

## Medium-Modified $p$ f.f.: the ${}^4\text{He}(\vec{e}, e'\vec{p}){}^3\text{H}$ process

- In **PWIA**:  $P'_x/P'_z \propto (G_{Ep}/G_{Mp})$
- FSI effects and MEC contributions explain measured ratio:  
no in medium modification is required



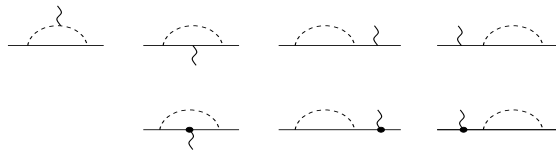
Schiavilla, Benhar, Kievsky, Marcucci, and Viviani, PRL94, 072303 (2005)



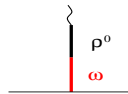
## Parity-Violating ${}^4\text{He}(\vec{e}, e'){}^4\text{He}$ Scattering and $G_E^s$

$$A_{\text{PV}} = \frac{G_\mu Q^2}{4\pi\alpha\sqrt{2}} \left[ 4\sin^2\theta_W - 2\frac{F^{(1)}(q)}{F^{(0)}(q)} - \frac{2G_E^{\lambda} - G_E^s}{(G_E^p + G_E^n)/2} + \text{RC/MEC} \right]$$

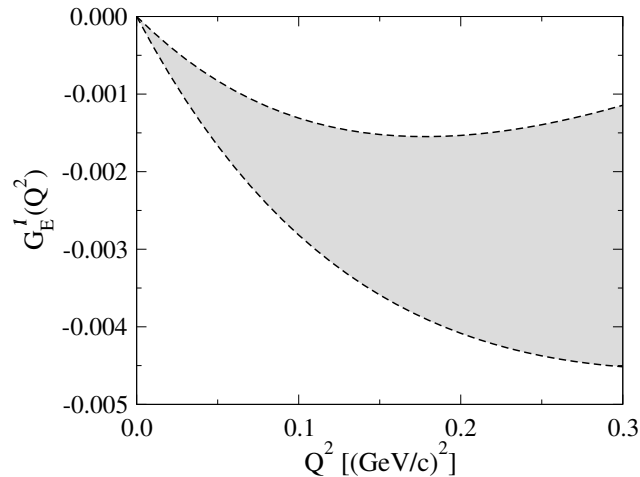
- $G_E^{\lambda}$  parameterizes nucleonic isospin symmetry breaking (ISB):  
 $(G_E^p + G_E^n)/2 = G_E^0 + G_E^{\lambda}$ ,  $G_E^{\lambda}$  obtained up to NLO in ChPT<sup>a</sup>
- $F^{(1)}$  nuclear ISB, would vanish if  $|{}^4\text{He}\rangle$  pure  $T=0$  state
- At low  $Q^2$ , RC/MEC contributions calculated to be tiny<sup>b</sup>



loop effects proportional to  $m_n - m_p$

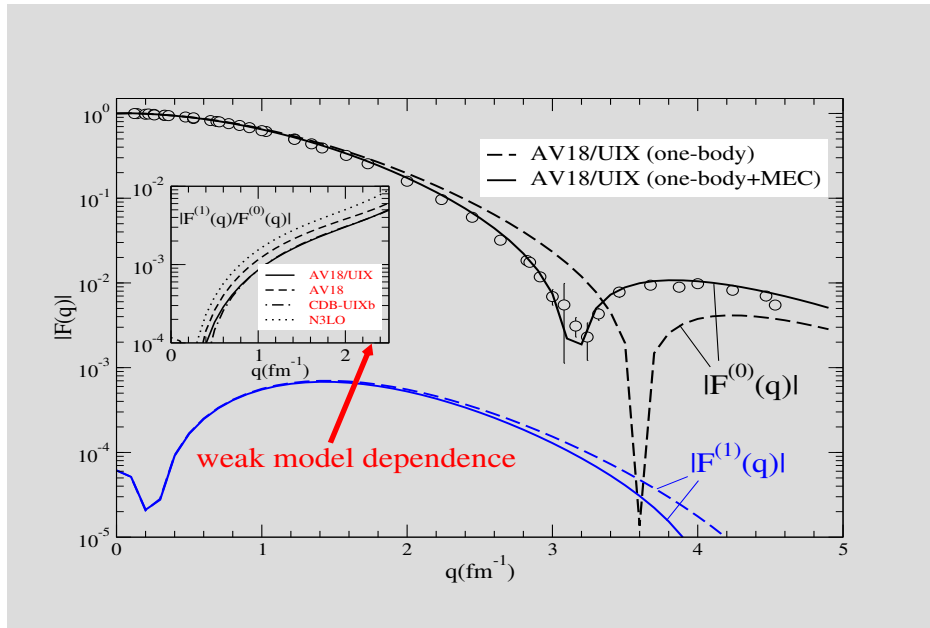


counterterm fixed by resonance saturation



<sup>a</sup>Kubis and Lewis, PRC $\mathbf{74}$ , 015204 (2006); <sup>b</sup>Musolf, Schiavilla, and Donnelly, PRC $\mathbf{50}$ , 2173 (1994)

- Nuclear ISB: i) EM interactions (Coulomb, ...), ii)  $n$ - $p$  mass difference in kinetic energy, and iii) CD/CA strong interactions
- Calculated  $A=3-8$  isomultiplet energies in good agreement with experiment [Pieper, Pandharipande, Wiringa, and Carlson, PRC**64**, 014001 (2001)]

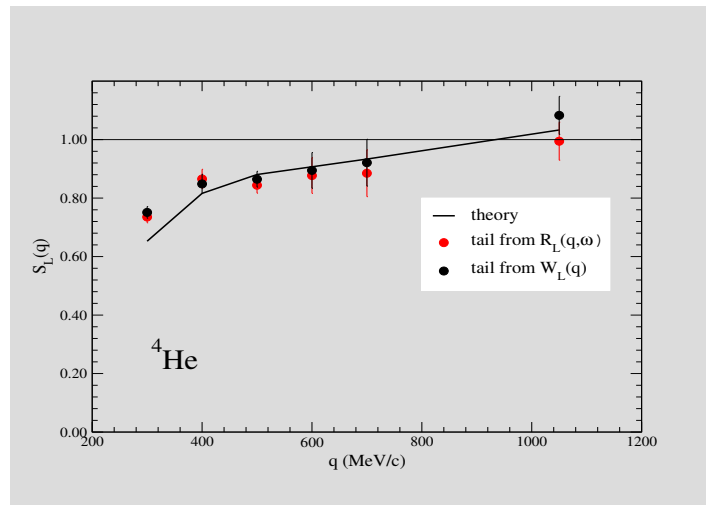


Viviani *et al.*, nucl-th 0703051

$-2 G_E^1 / [(G_E^p + G_E^n) / 2] \approx 0.008$  and  $-2 F^{(1)}(q) / F^{(0)}(q) \approx 0.00314$  in HAPPEX  $A_{\text{PV}}$  give  $G_E^s [Q^2 = 0.077 (\text{GeV}/c)^2] = -0.001 \pm 0.016$

## Summary (II)

- Conventional nuclear effects explain suppression of  $(P'_x/P'_z)_{4\text{He}}$
- Present and Coulomb sum rule analysis indicate no in-medium modification for  $G_{Ep}$  and  $G_{Mp}$



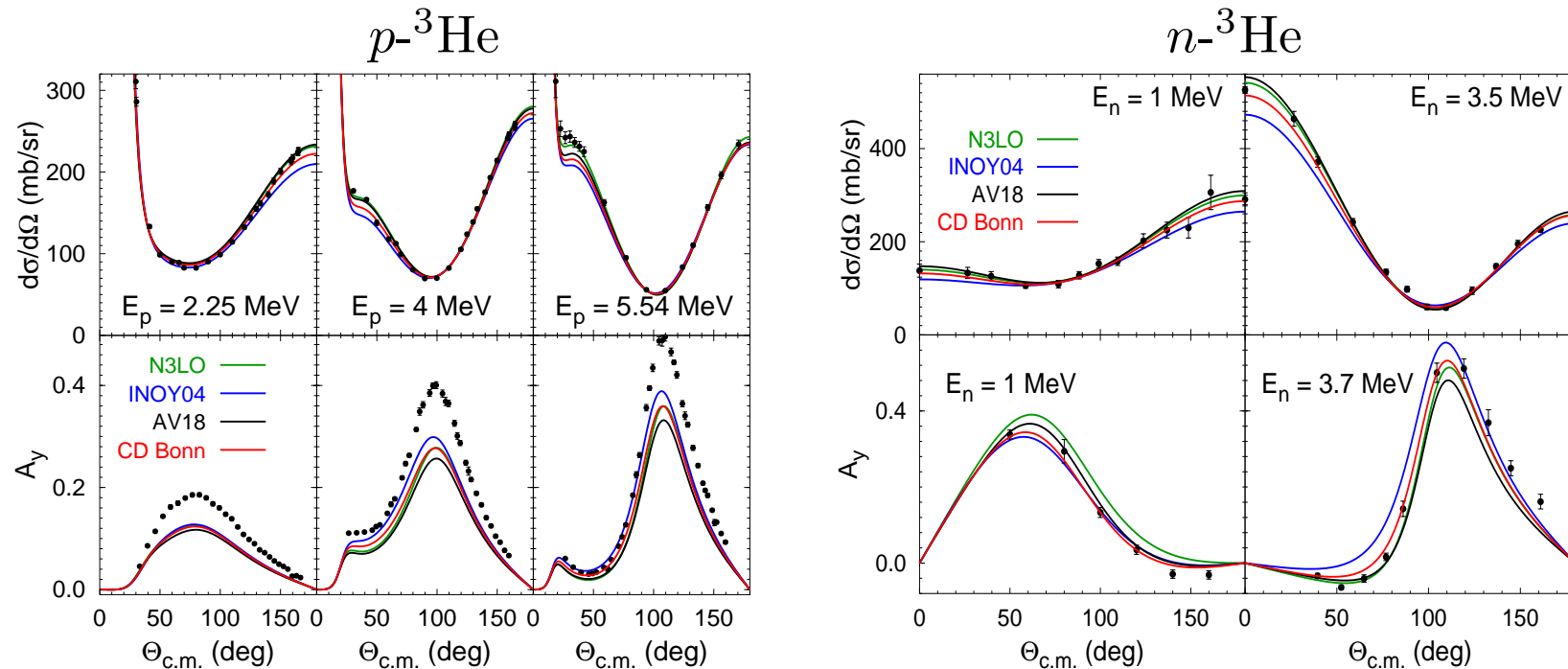
Carlson, Jourdan, Schiavilla, and Sick, PLB**553**, 191 (2003)

- $|G_E^s| \lesssim |\text{ISB}|$ : measuring ISB admixtures?
- Inferred  $G_E^s$  consistent (in magnitude!) with estimate obtained by using LQCD input [Leinweber *et al.*, PRL**97**, 022001 (2006)]

# New Frontiers

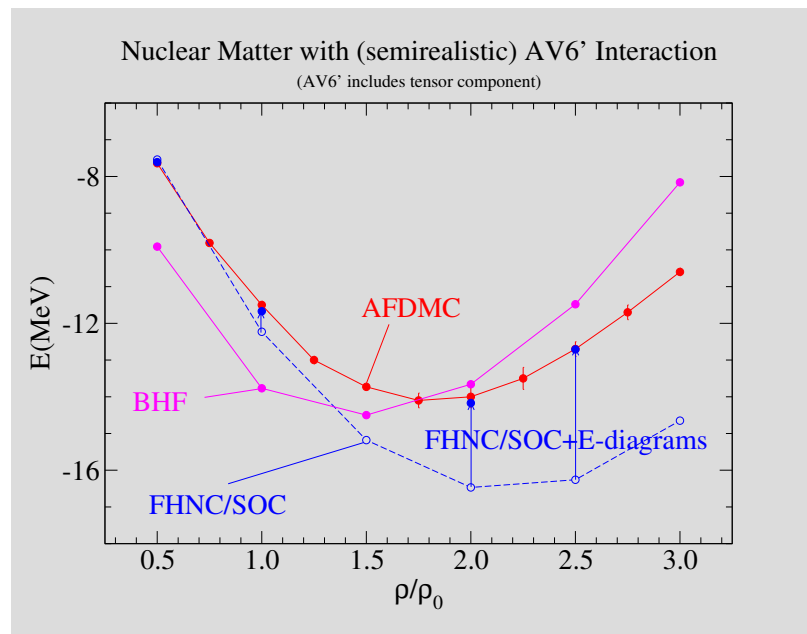
# AGS formulation of 4-body scattering including channel couplings

[Deltuva and Fonseca, PRL $\mathbf{98}$ , 162502 (2007) and nucl-th/0703066]



- $NN$  interactions only (for the time being)
- $A_y$  puzzle in 4-body scattering: strong isospin dependence, theory underestimate in  $^3\text{He}\text{-}p$  ( $T=1$ ) much reduced relative to  $^3\text{He}\text{-}n$  and  $^3\text{H}\text{-}p$  ( $T=0$  and  $T=1$  superpositions)

## Auxiliary-Field-Diffusion-Monte-Carlo (AFDMC) calculations of nuclear matter and of $A \leq 40$ nuclei



Gandolfi, Pederiva, Fantoni, and Schmidt, PRL98, 102503 (2007); arXiv:0704.1774

- In AFDMC spin-isospin variables are sampled rather than summed over explicitly as in GFMC
- Power-law rather than exponential growth with  $A$  ( $^{12}\text{C}$  GFMC calculations presently require  $\simeq 70,000$  processor hours)