

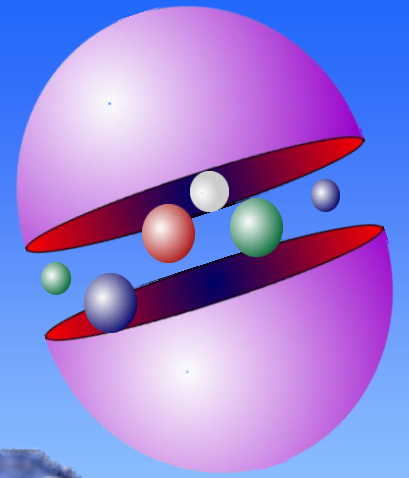


# Facets of the strong interaction



Hirschegg 2012

Michael Pennington  
Jefferson Lab



# Glimpsing colour in a world of black & white

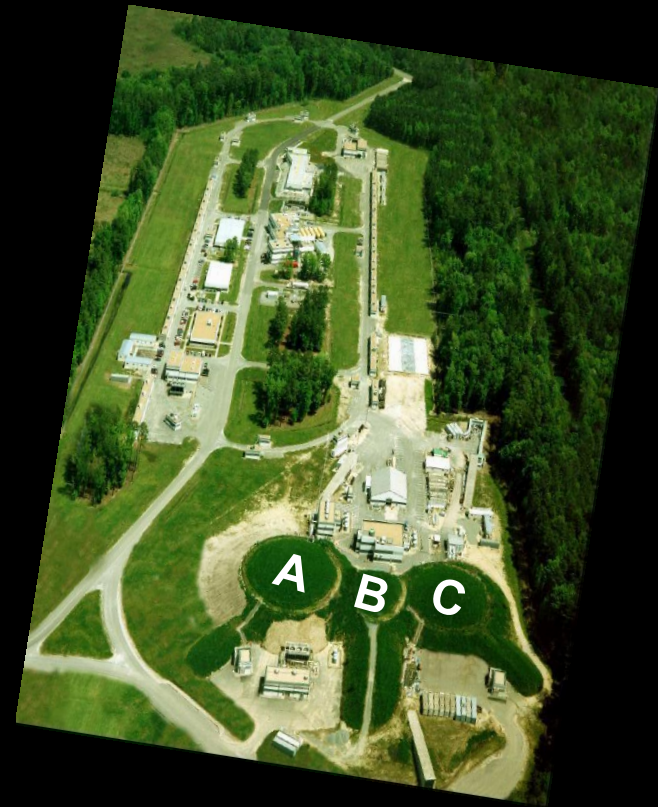
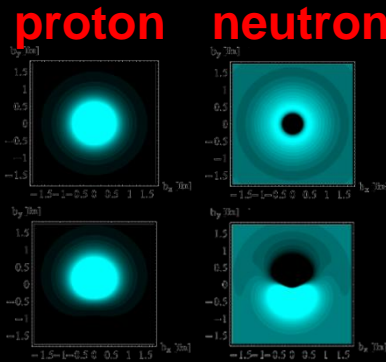
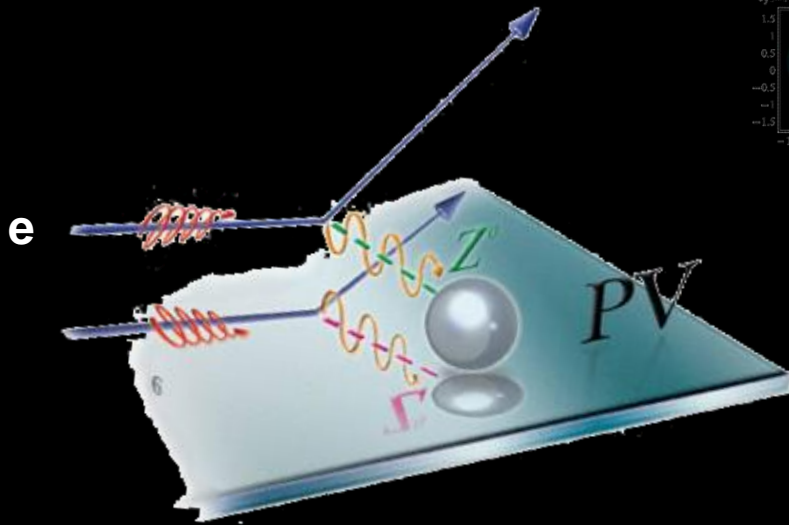
Hirschegg 2012



**Glimpsing colour  
in a world of black & white**



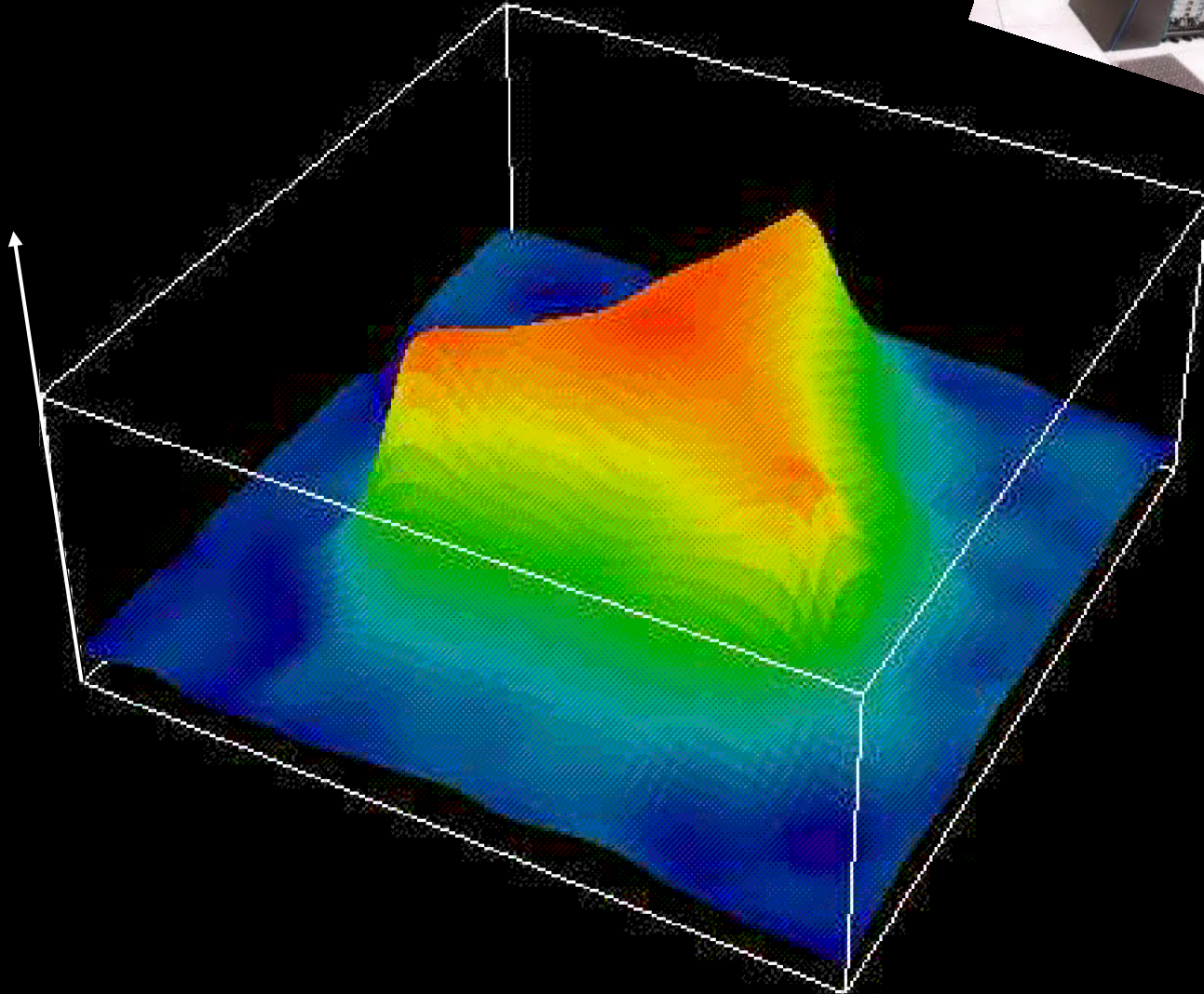
# Glimpsing colour in a world of black & white

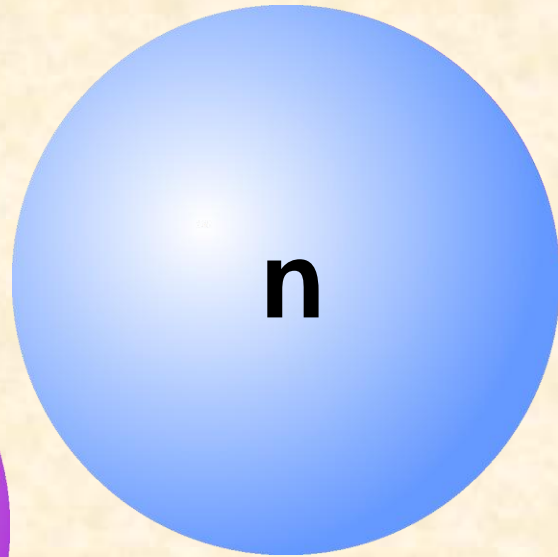
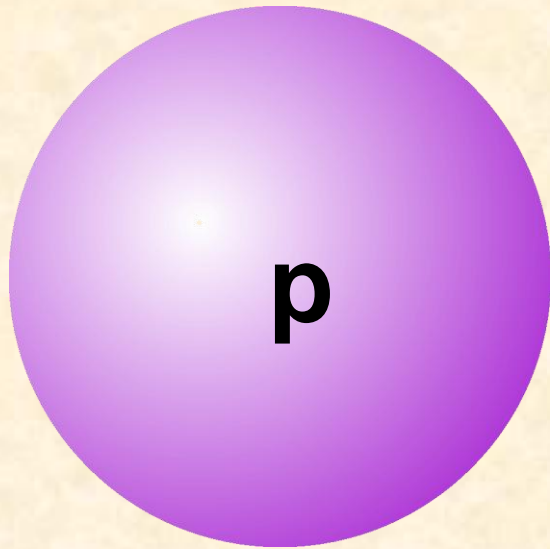


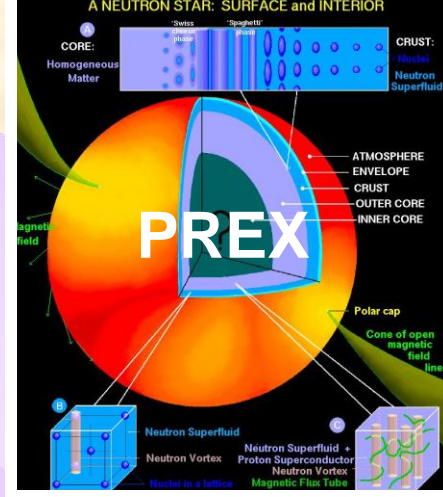
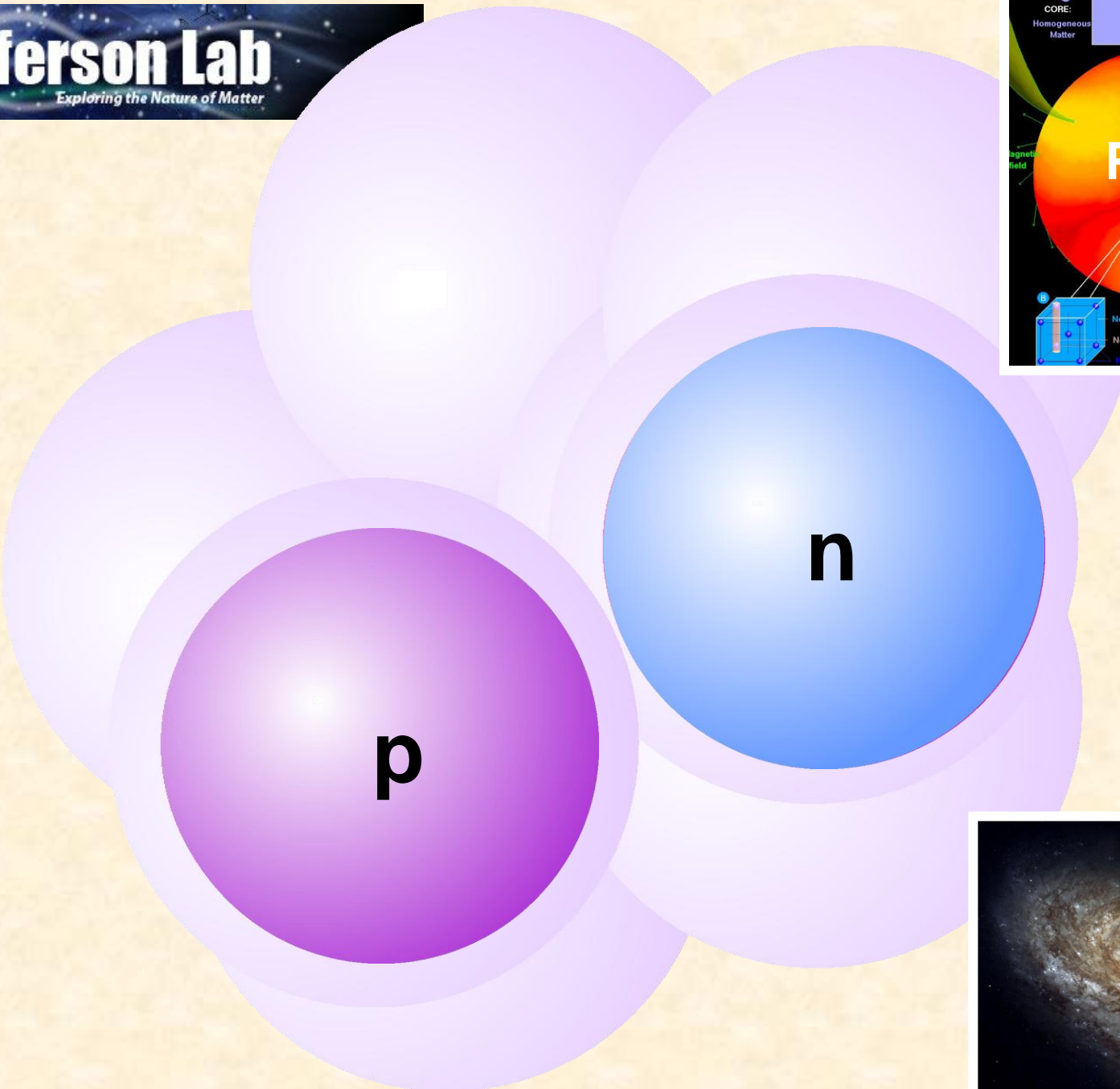
Jefferson Science Associates, LLC  
a SURA/CSC Company

# Colour Forces

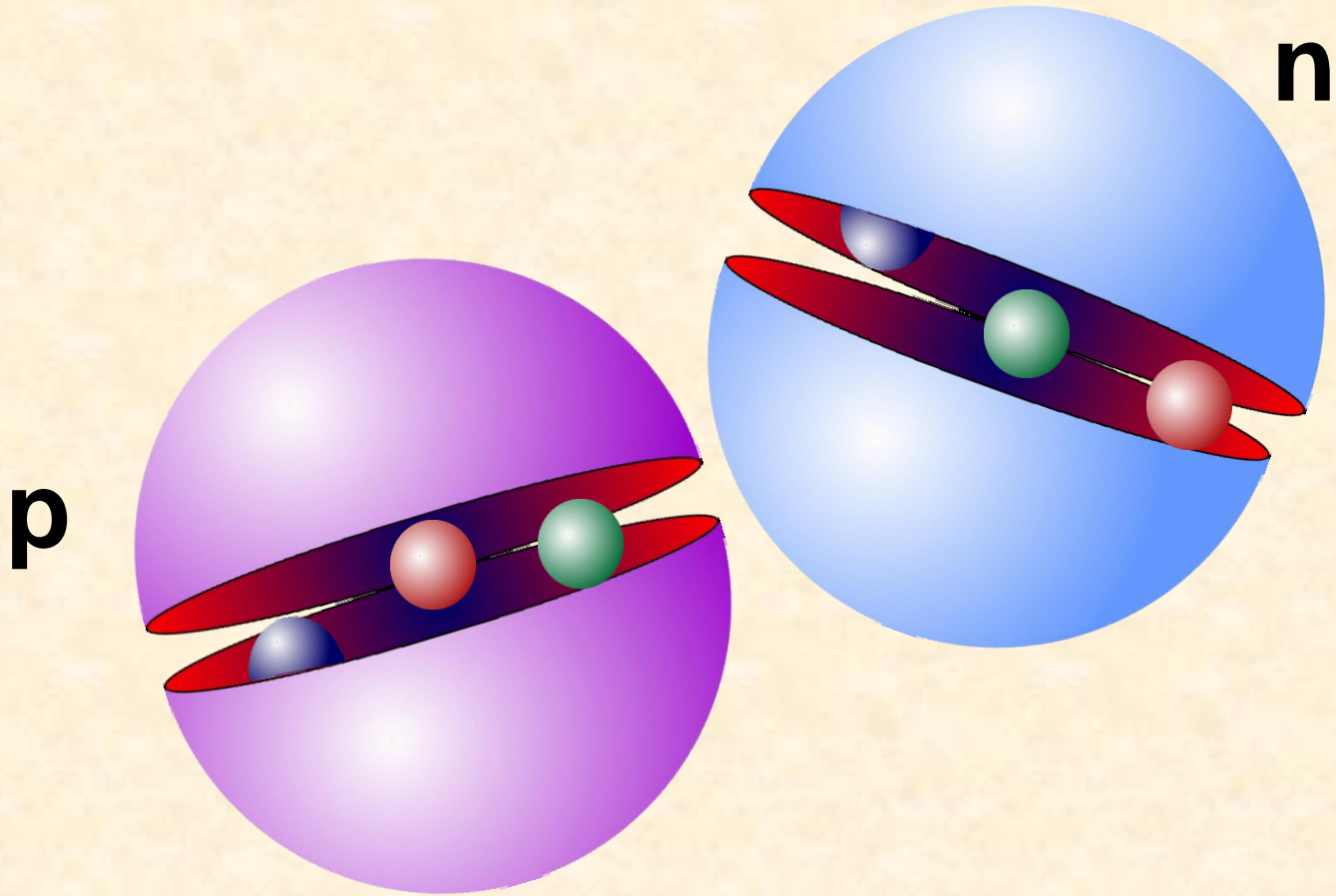
energy  
density







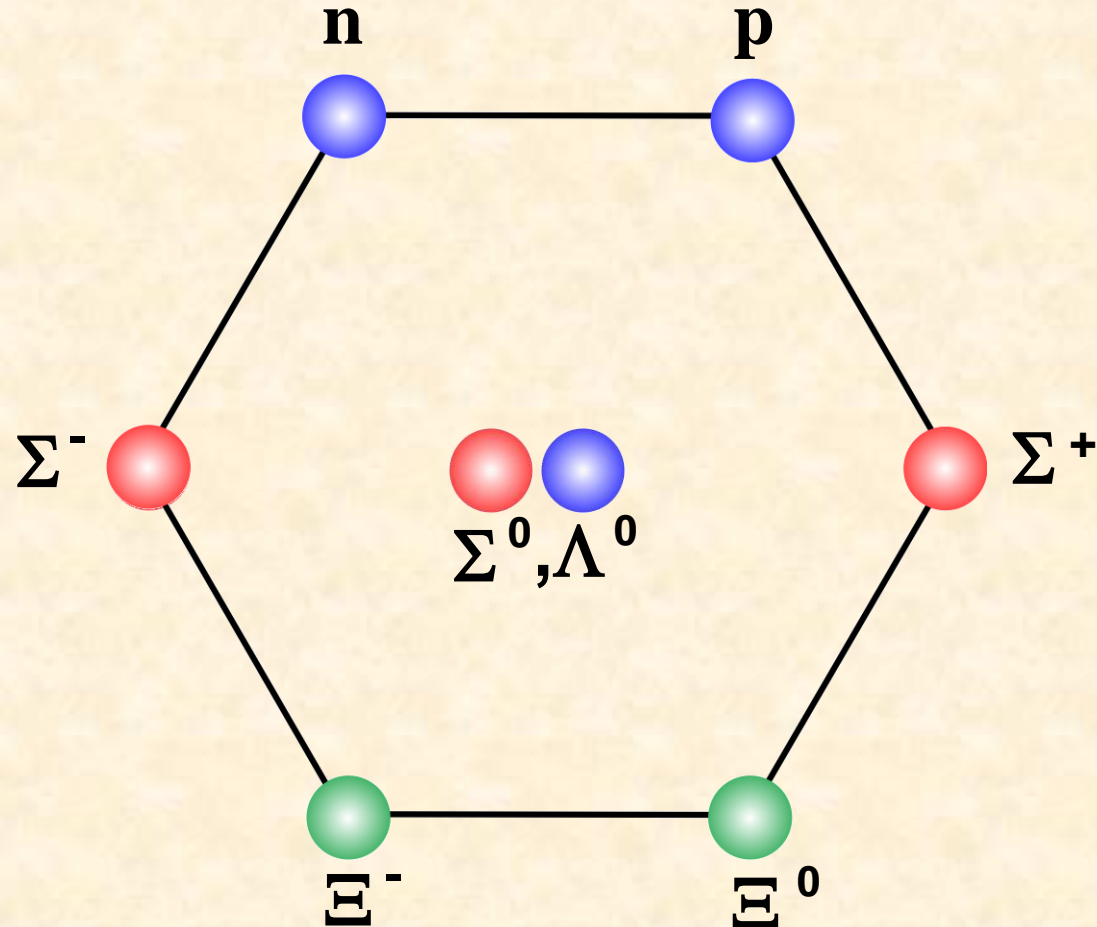




# Baryon octet

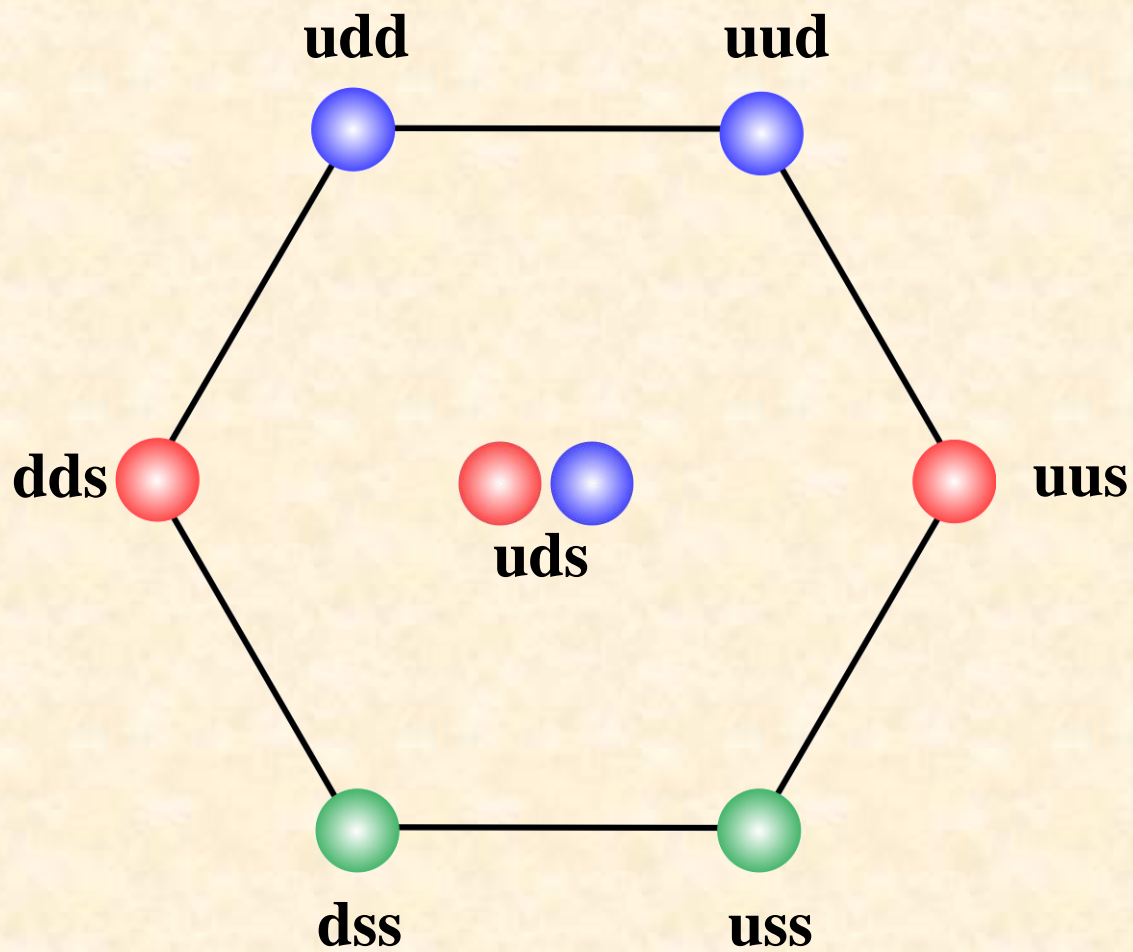
$\Xi$	—	1320
$\Sigma, \Lambda$	—	1130
$p, n$	—	940

energy  
↑  
0



**Ground States**

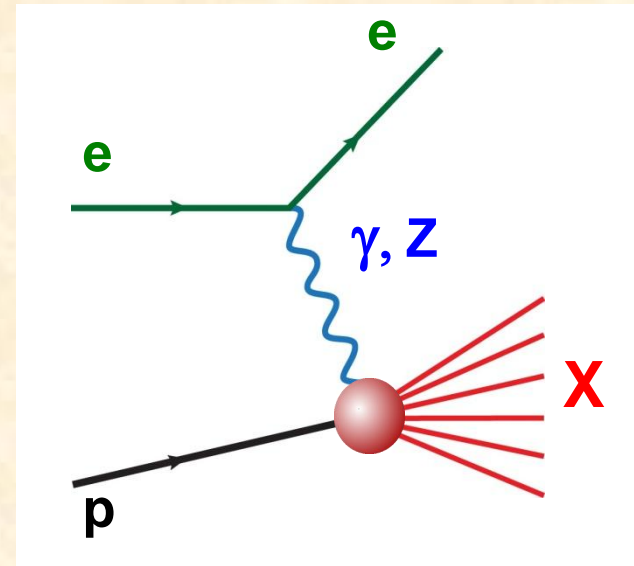
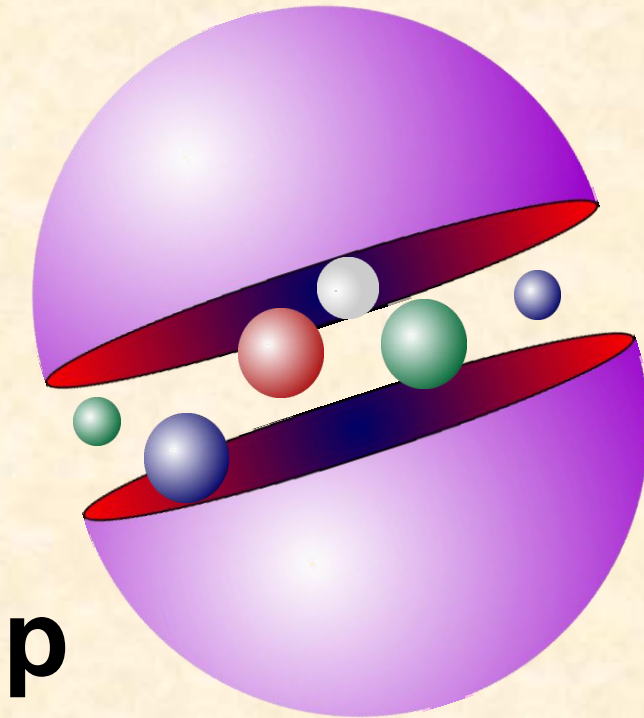
# Baryon octet



**s** ———  
**u,d** ———

energy  
↑  
0

# Deep inelastic scattering

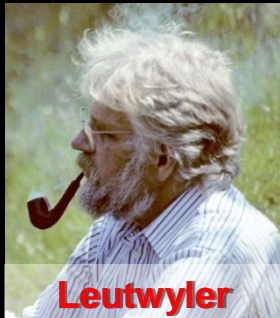


# QCD

1971



Fritzsch



Leutwyler

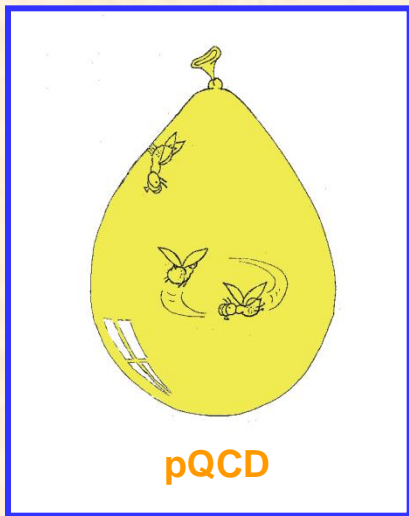


Gell-Mann

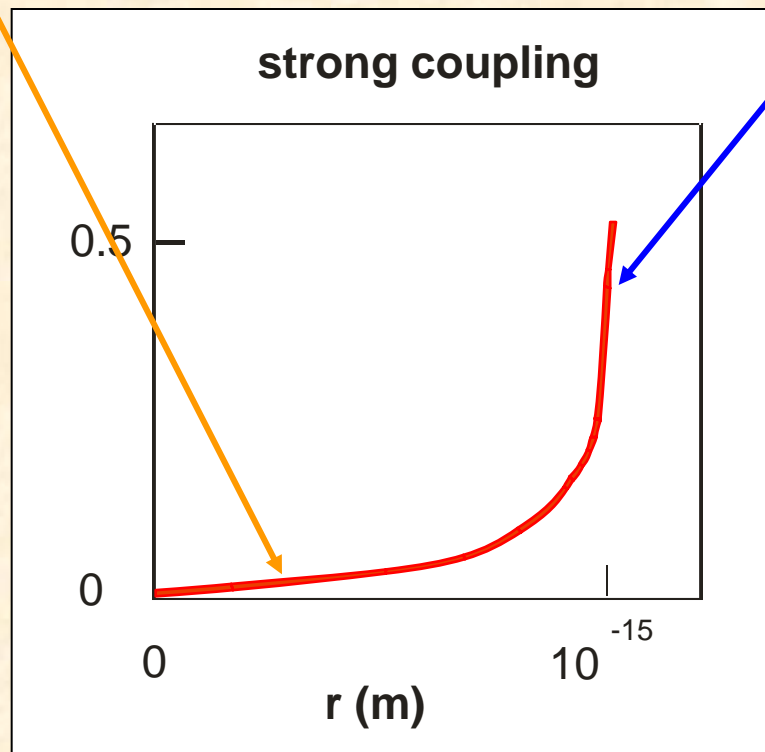
$$\mathcal{L}_{\text{QCD}} = \sum_{q=u,d,s,c,b} \bar{q} (i\gamma_{\mu} D^{\mu} - m_q) q - \frac{1}{4} G^{\mu\nu} G_{\mu\nu}$$

# QCD

asymptotic freedom



confinement



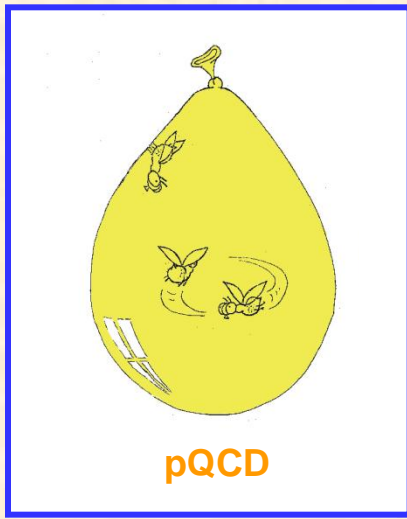


Politzer

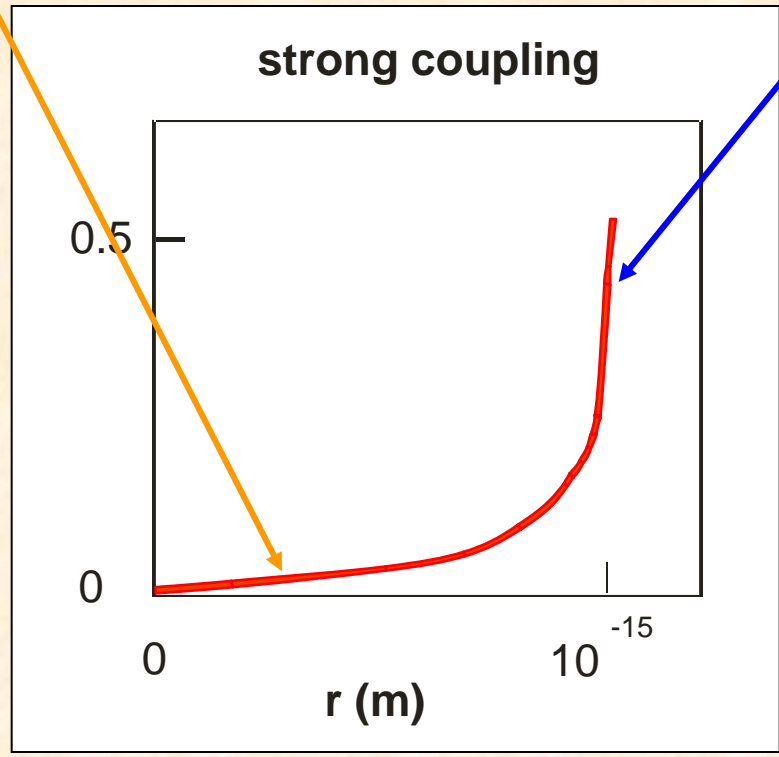
# QCD

asymptotic freedom

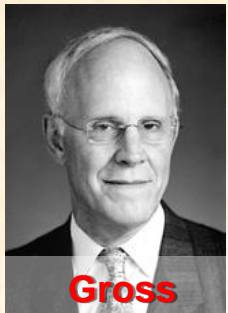
confinement



pQCD



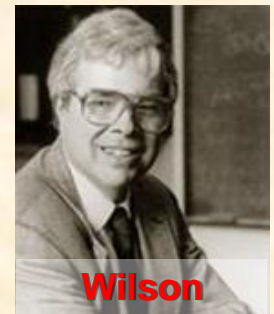
strong QCD



Gross



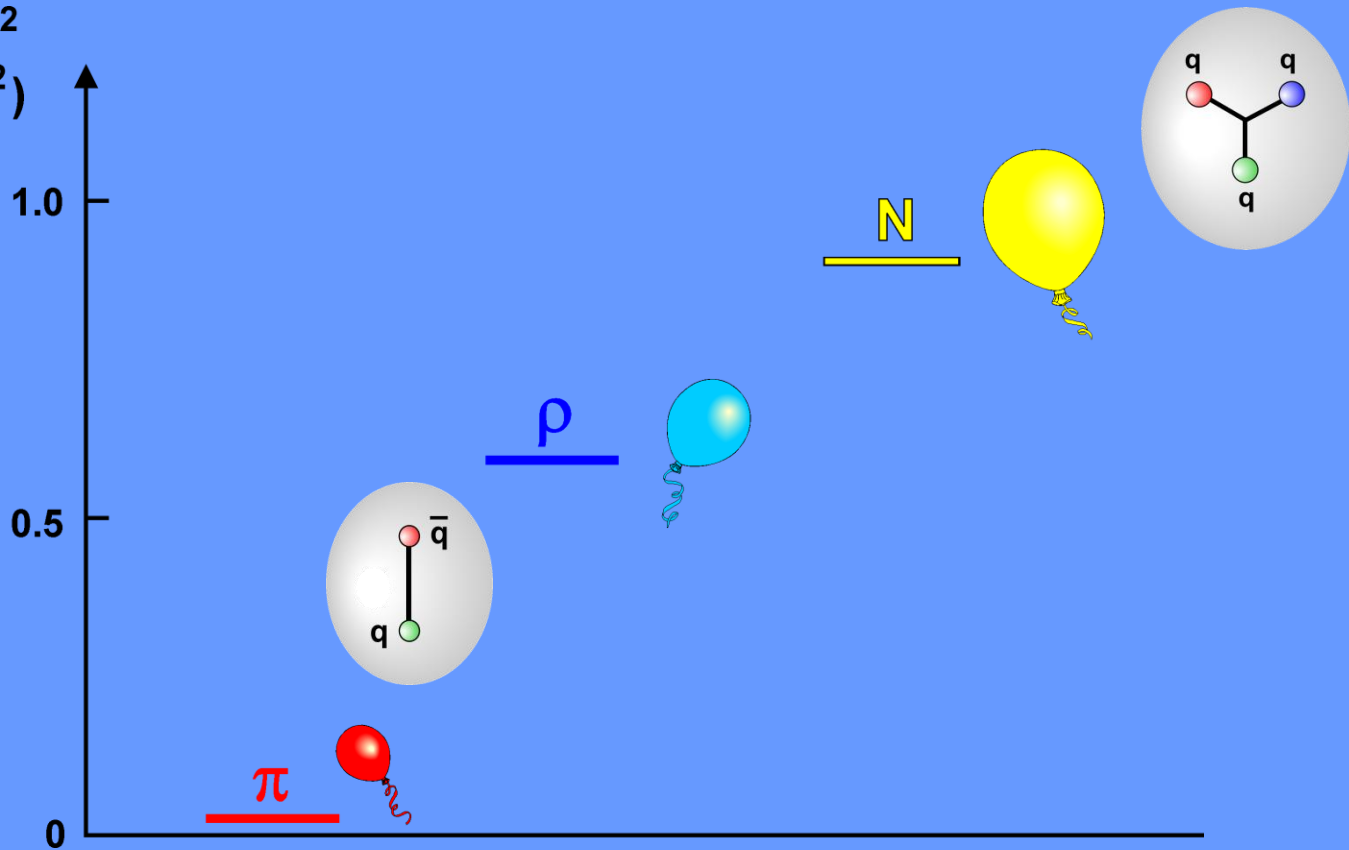
Wilczek



Wilson

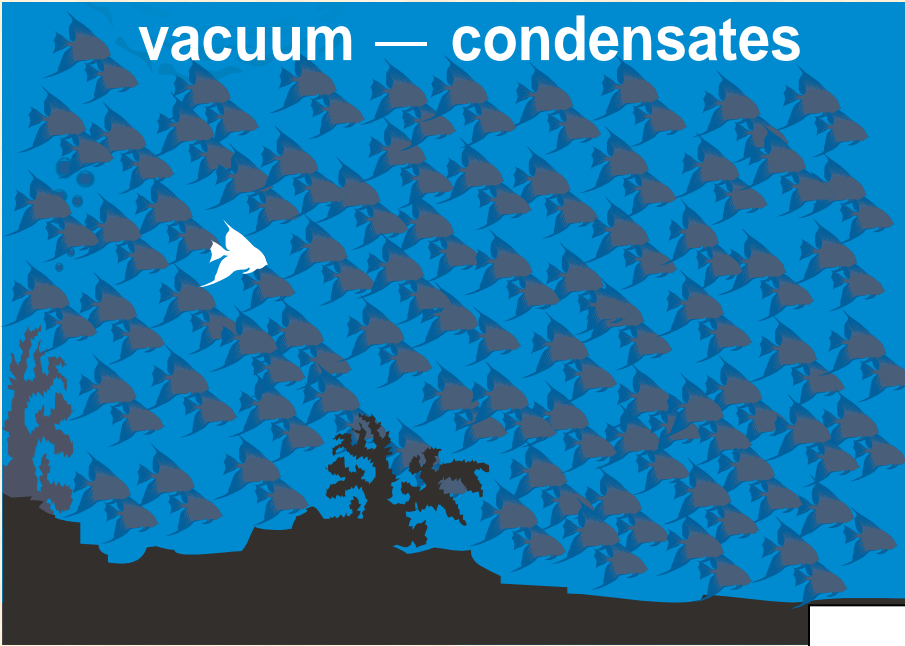
# Hadron masses <sup>2</sup>

Mass<sup>2</sup>  
(GeV<sup>2</sup>)

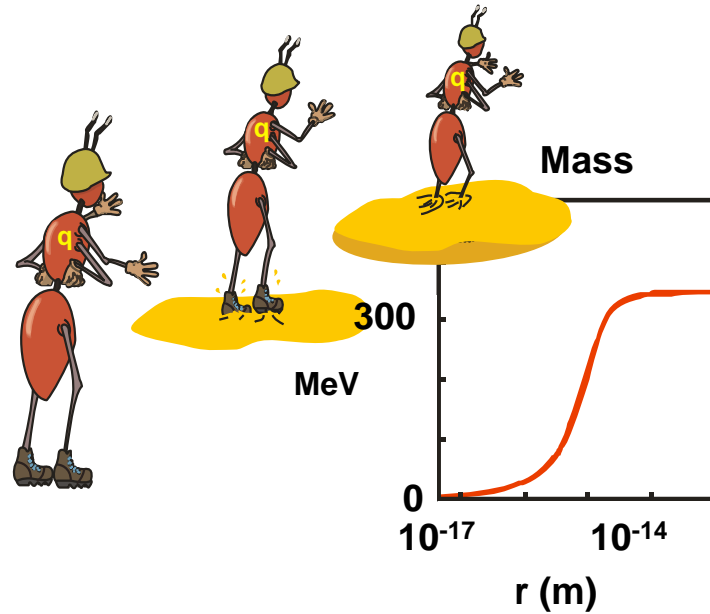




# vacuum — condensates



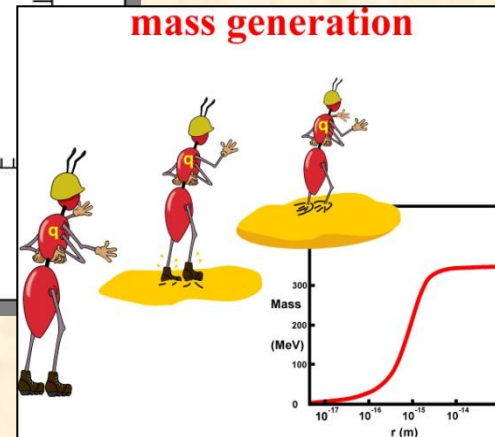
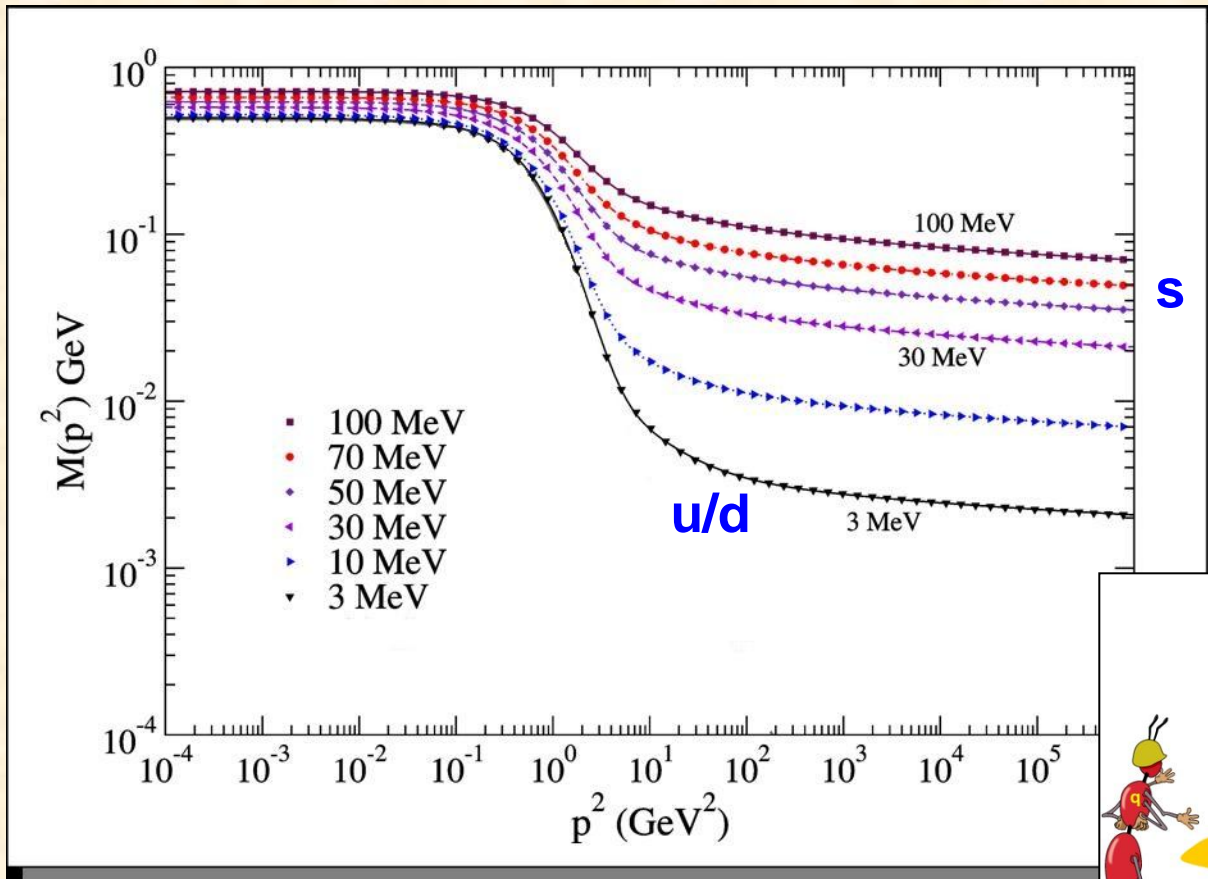
## u/d quarks propagating



# Quark mass function

$$\alpha_s > 1 \implies \chi\text{SB}$$

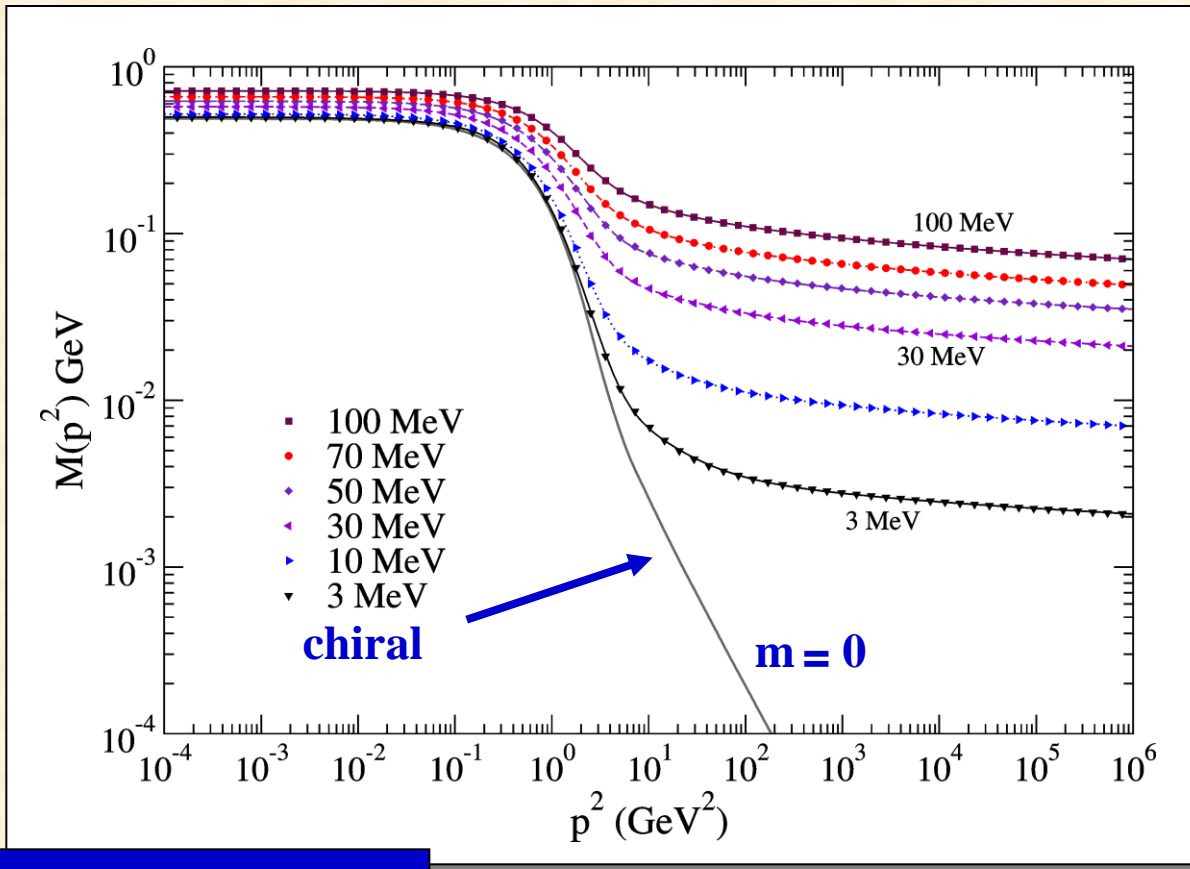
Williams,  
Fischer,  
P



# Quark mass function

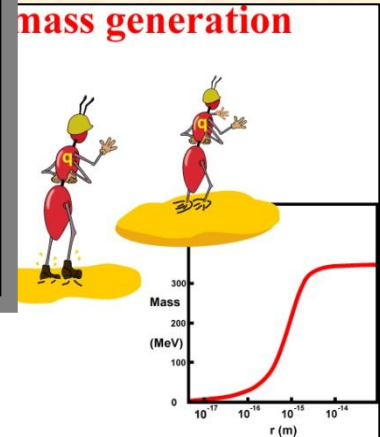
$$\alpha_s > 1 \implies \chi\text{SB}$$

Williams,  
Fischer,  
P



$$\langle \bar{q}q \rangle_0 \sim - (240 \text{ MeV})^3$$

Bhagwat & Tandy/ Roberts *et al.*



# Spectrum of hadrons



**Rutherford:**

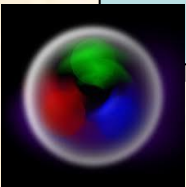
***“Science is either physics or stamp-collecting”***

# colour wave-functions

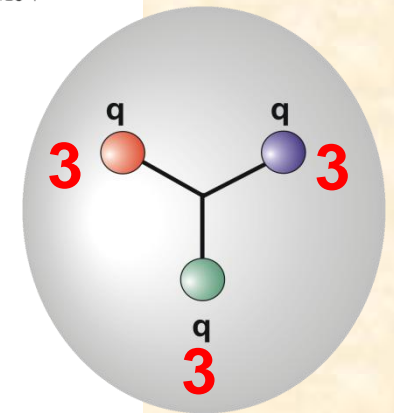
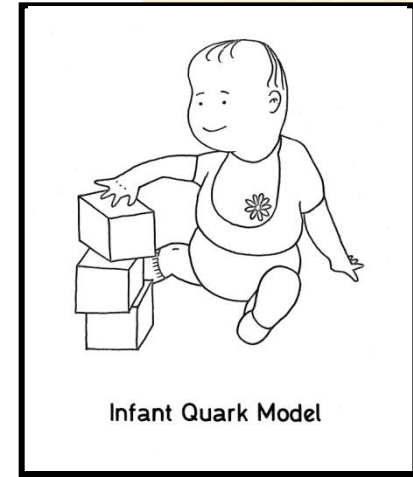
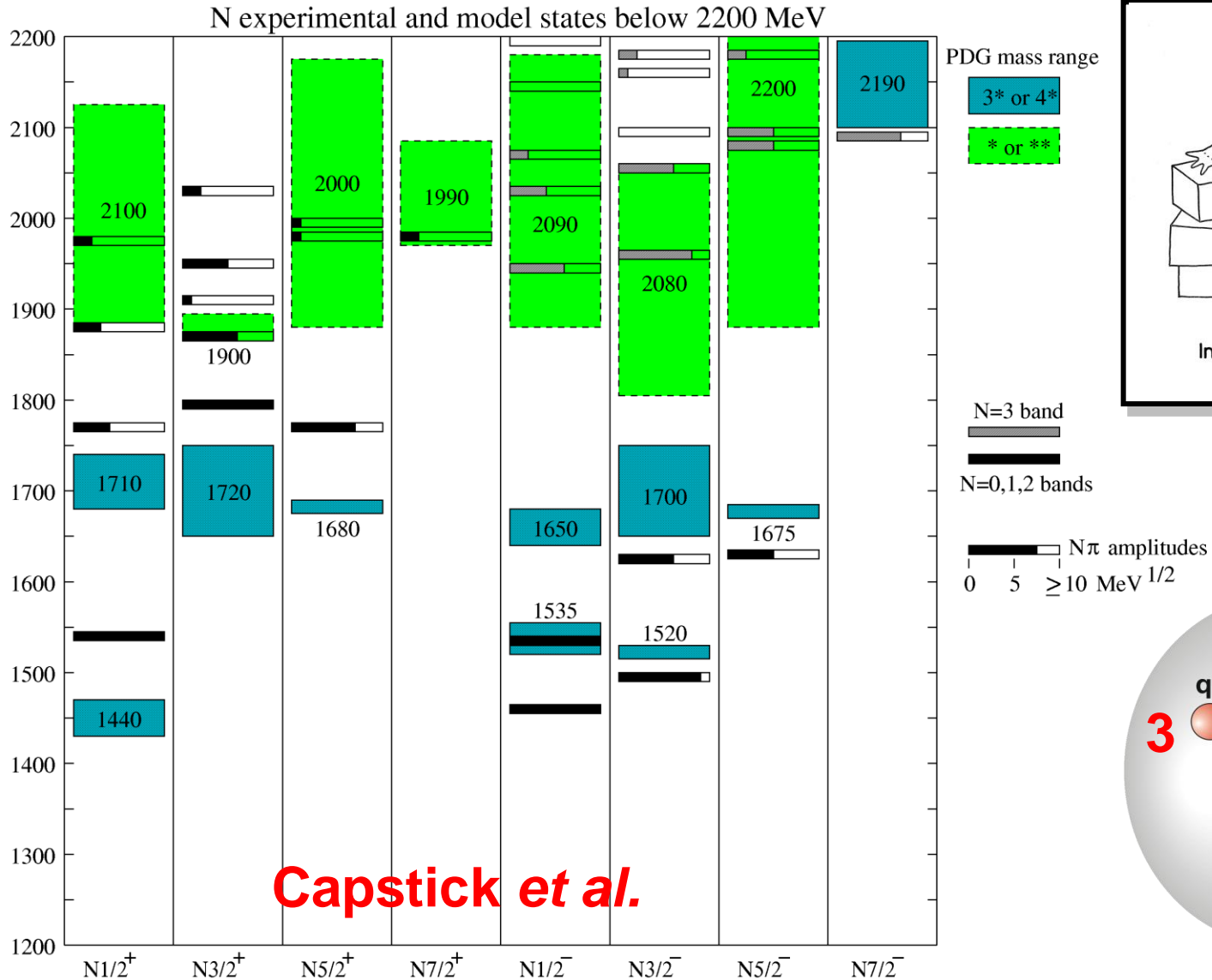
$$\pi^+ = \frac{1}{\sqrt{N_c}} [ u\bar{d} + u\bar{d} + u\bar{d} + u\bar{d} + \dots ]$$

$$N_c = 3$$

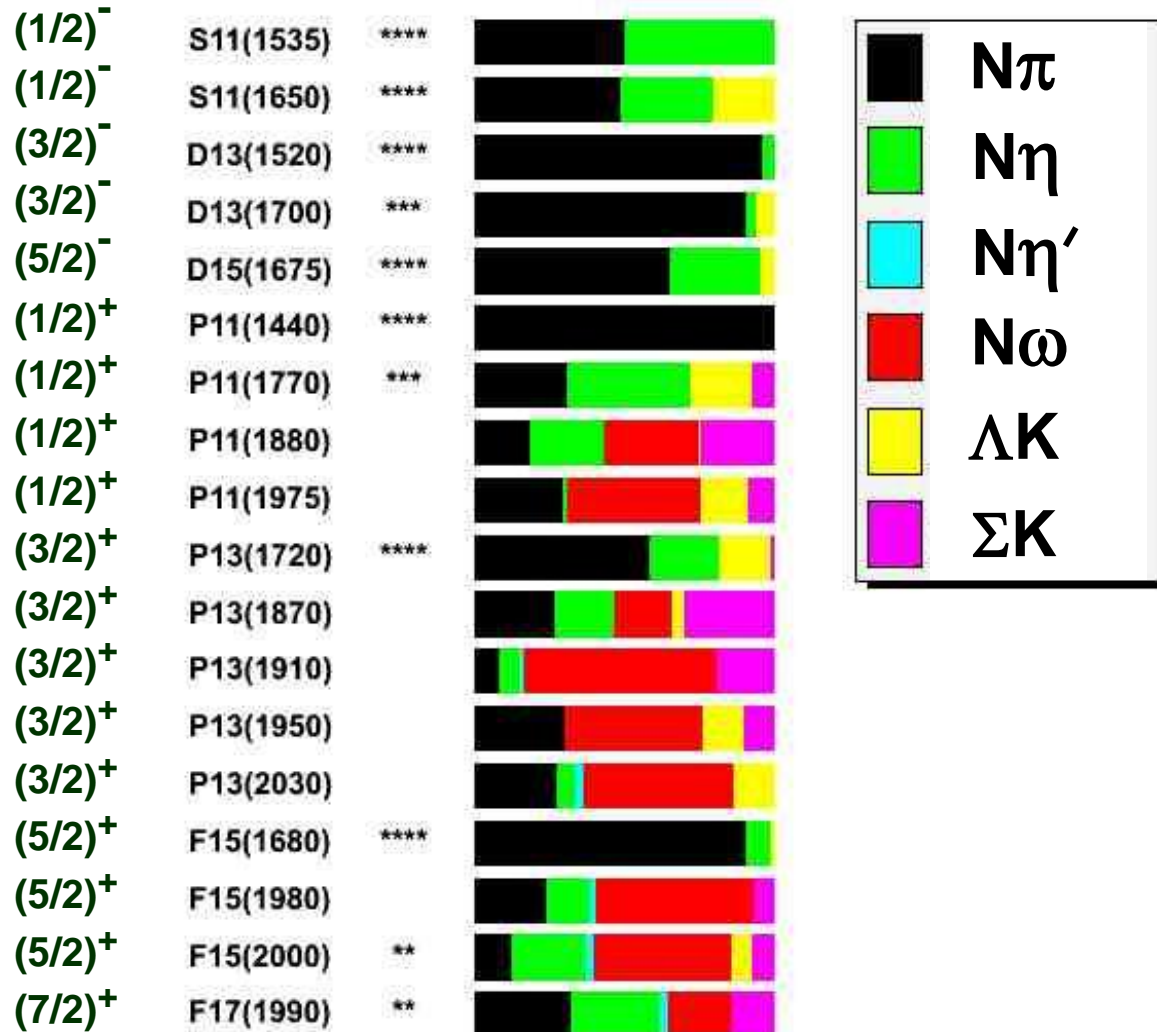
$$p = \frac{1}{\sqrt{6}} [ uud + uud + uud \\ - uud - uud - uud ]$$



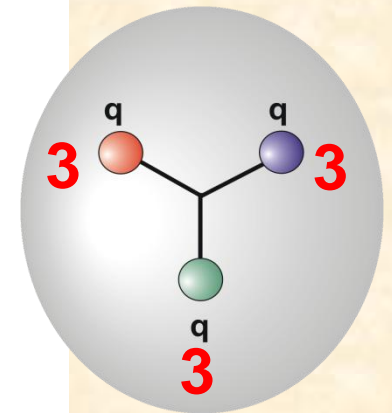
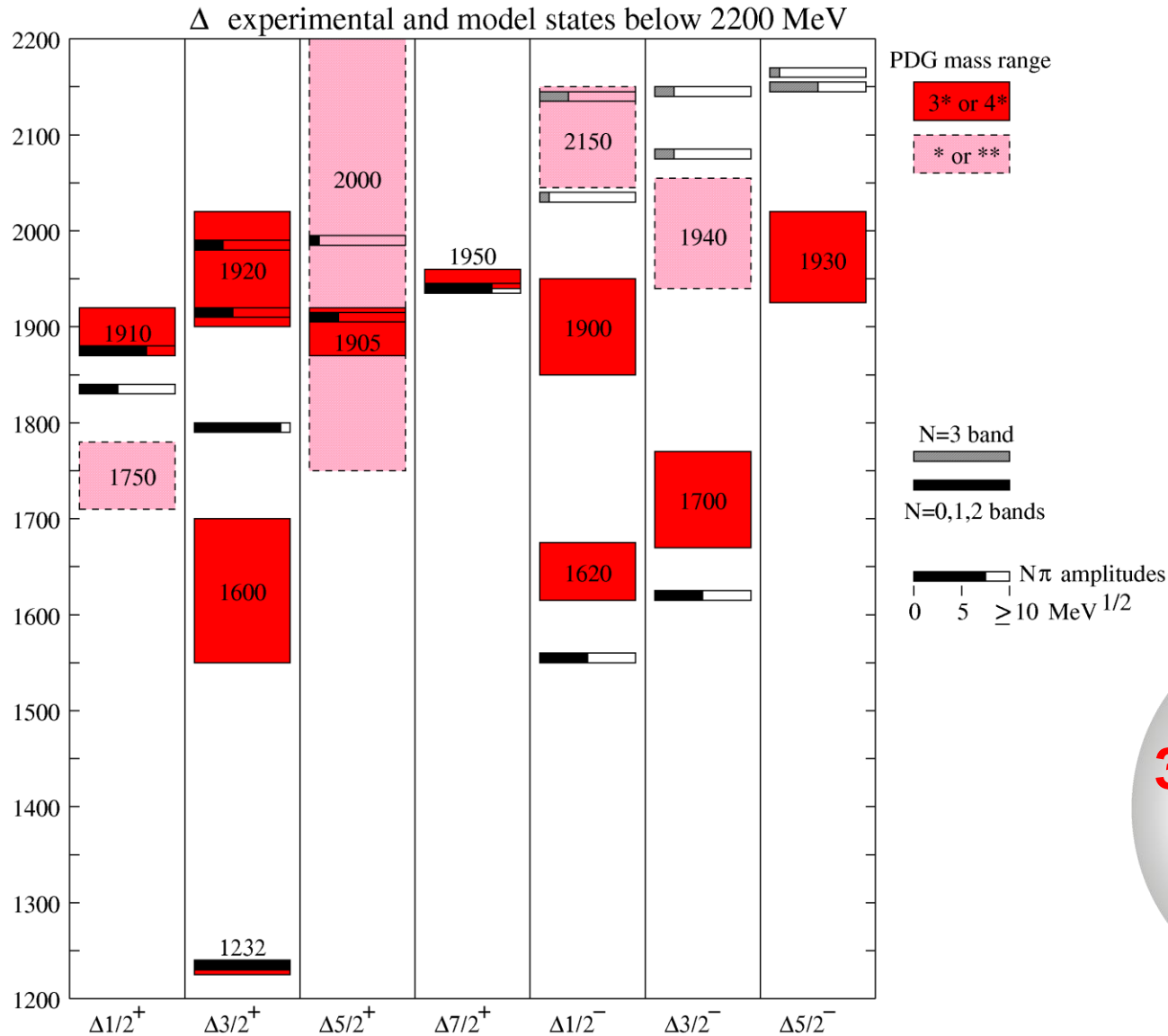
# Nucleon model states ( $\pi N$ couplings)



# search all channels: not just $\pi N$

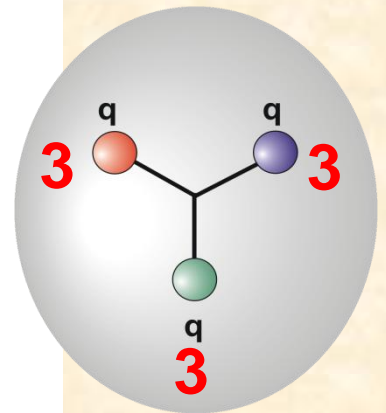
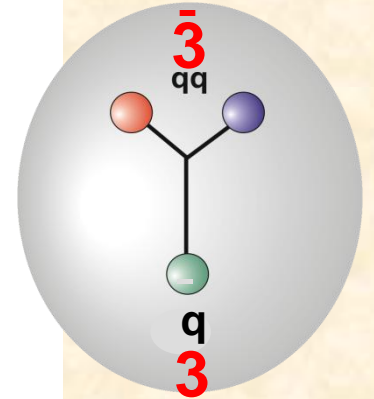
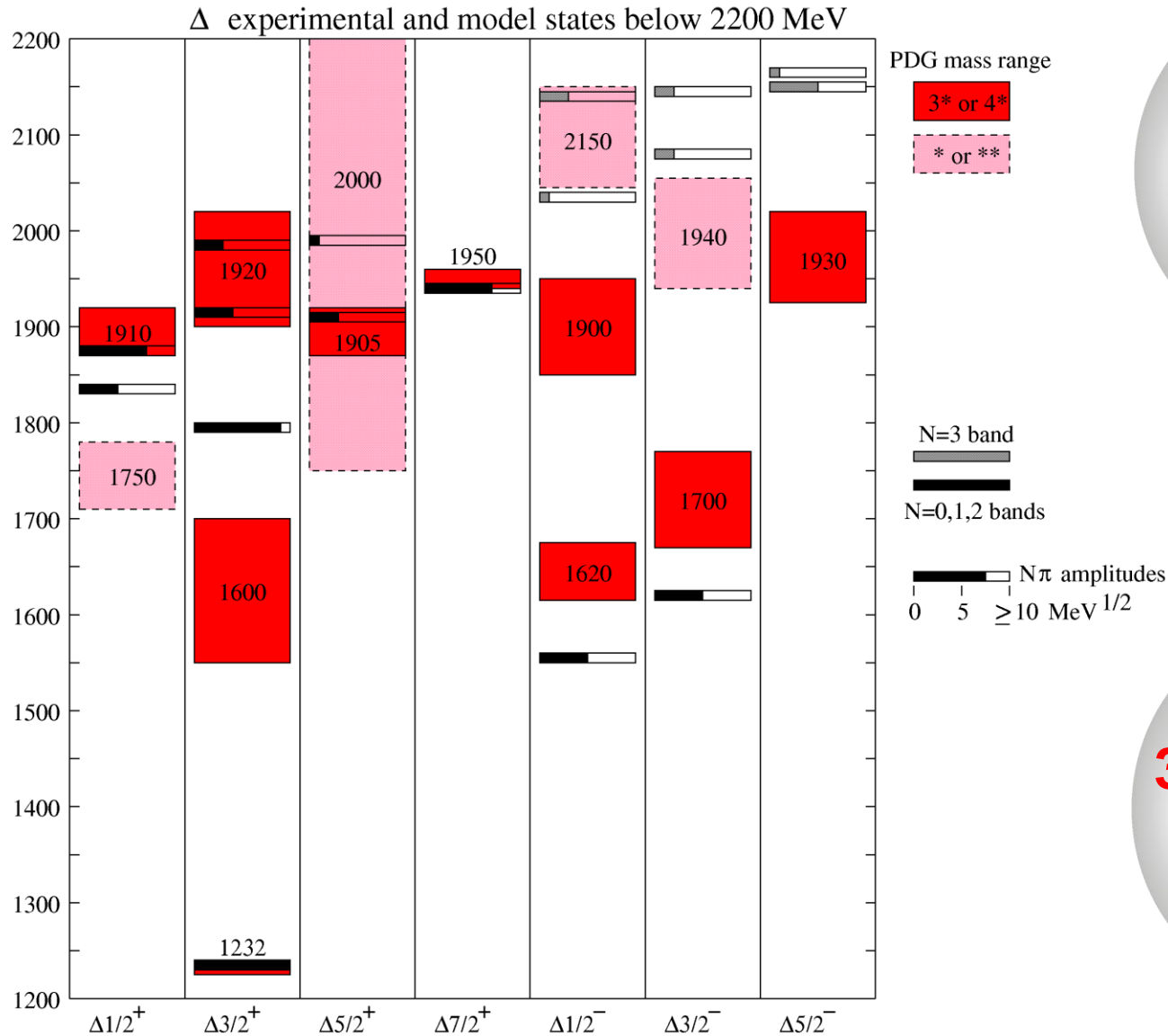


# $\Delta$ model states ( $\pi N$ couplings)

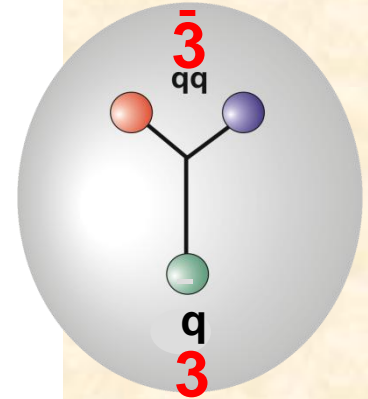
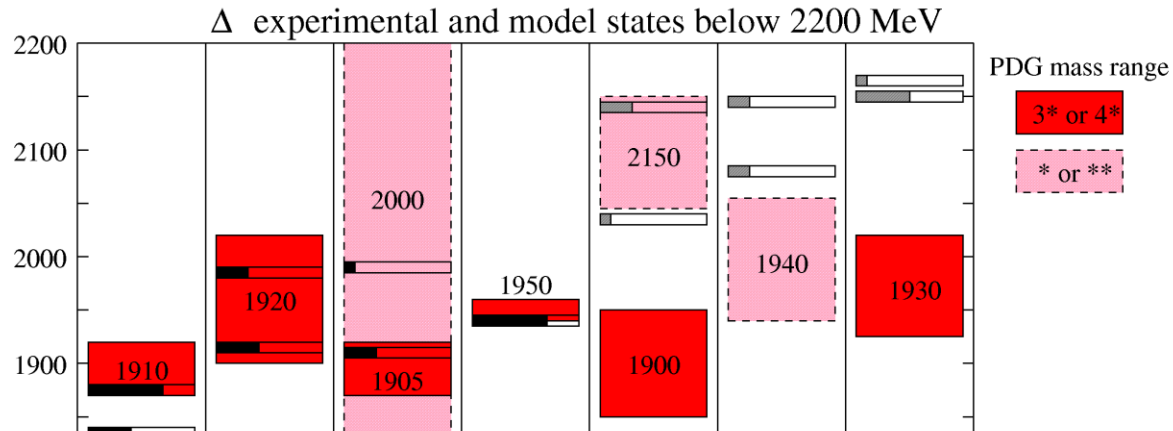




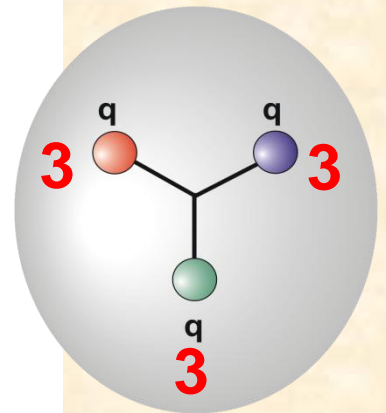
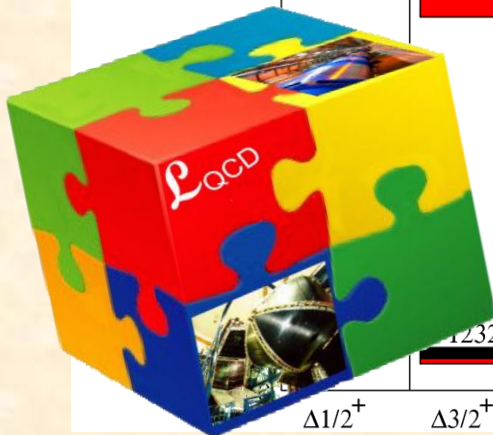
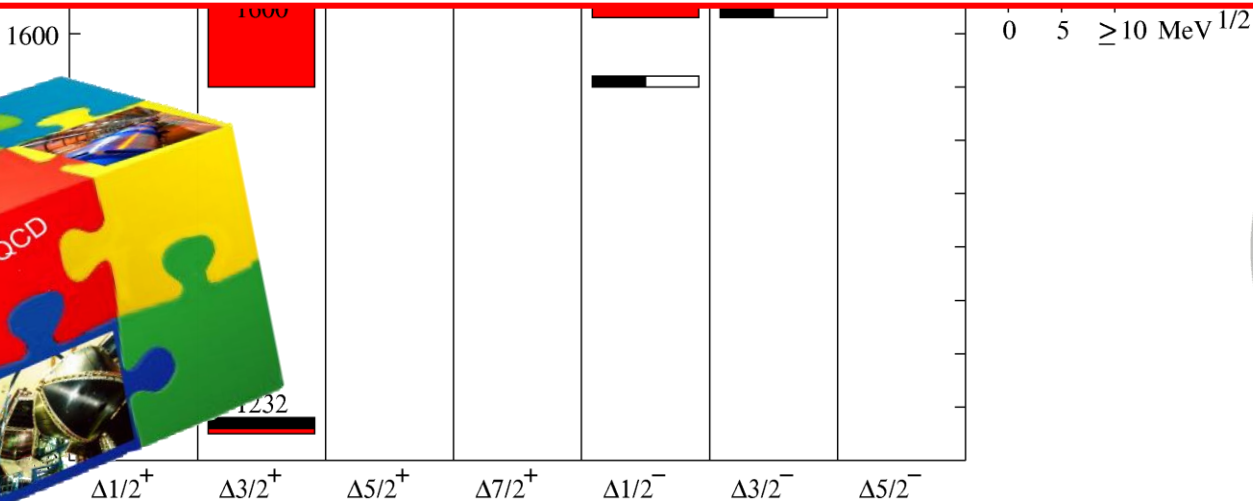
# $\Delta$ model states ( $\pi N$ couplings)



# $\Delta$ model states ( $\pi N$ couplings)

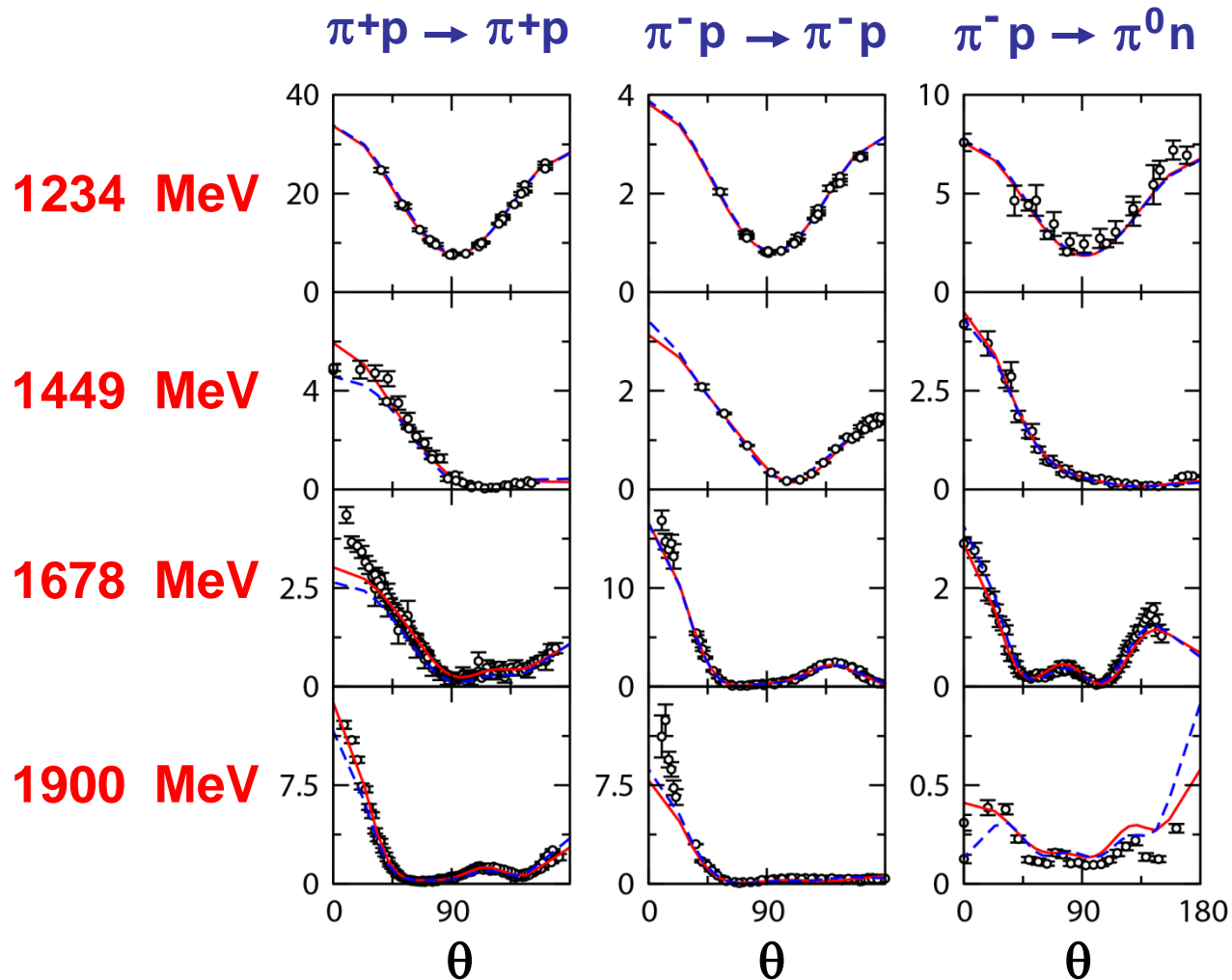


$$\mathcal{L}_{\text{QCD}} = \sum_{q=u,d,s,c,b} \bar{\psi}_q (i \gamma_\mu D^\mu - m_q) \psi_q - \frac{1}{4} \mathcal{F}_{\mu\nu} \mathcal{F}^{\mu\nu}$$



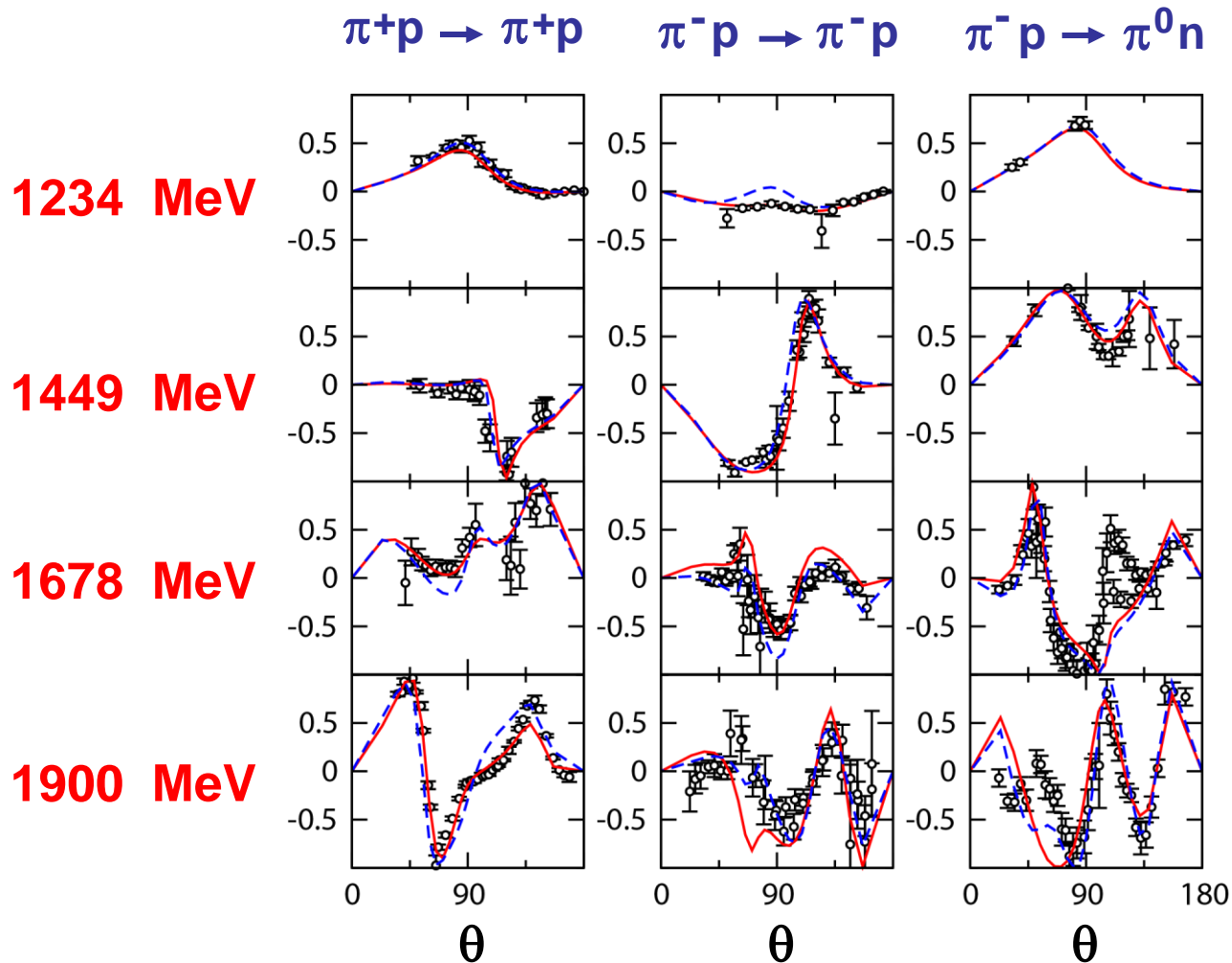
# $\pi N \rightarrow \pi N$ scattering

$d\sigma/d\Omega$

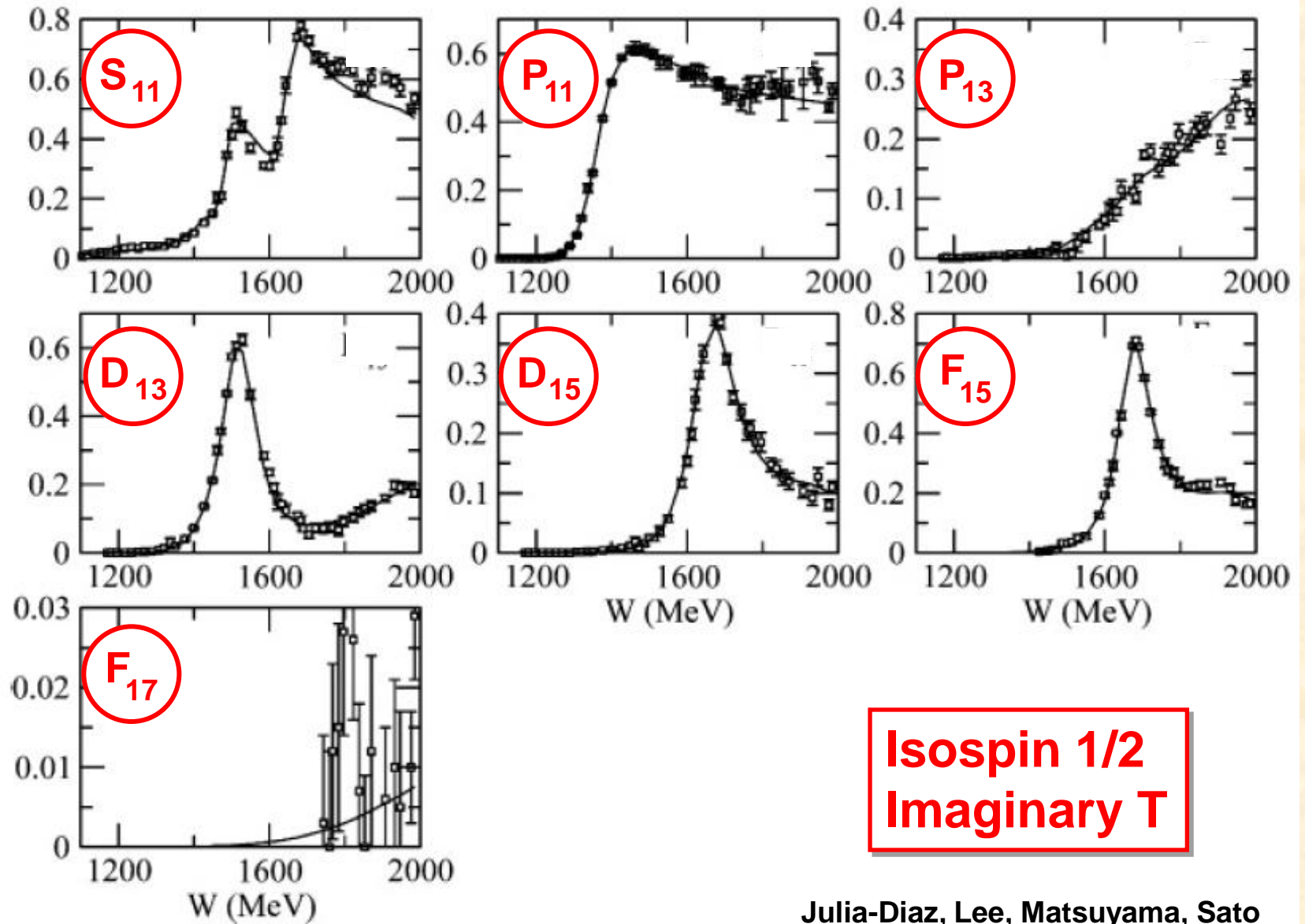


# $\pi N \rightarrow \pi N$ scattering

P

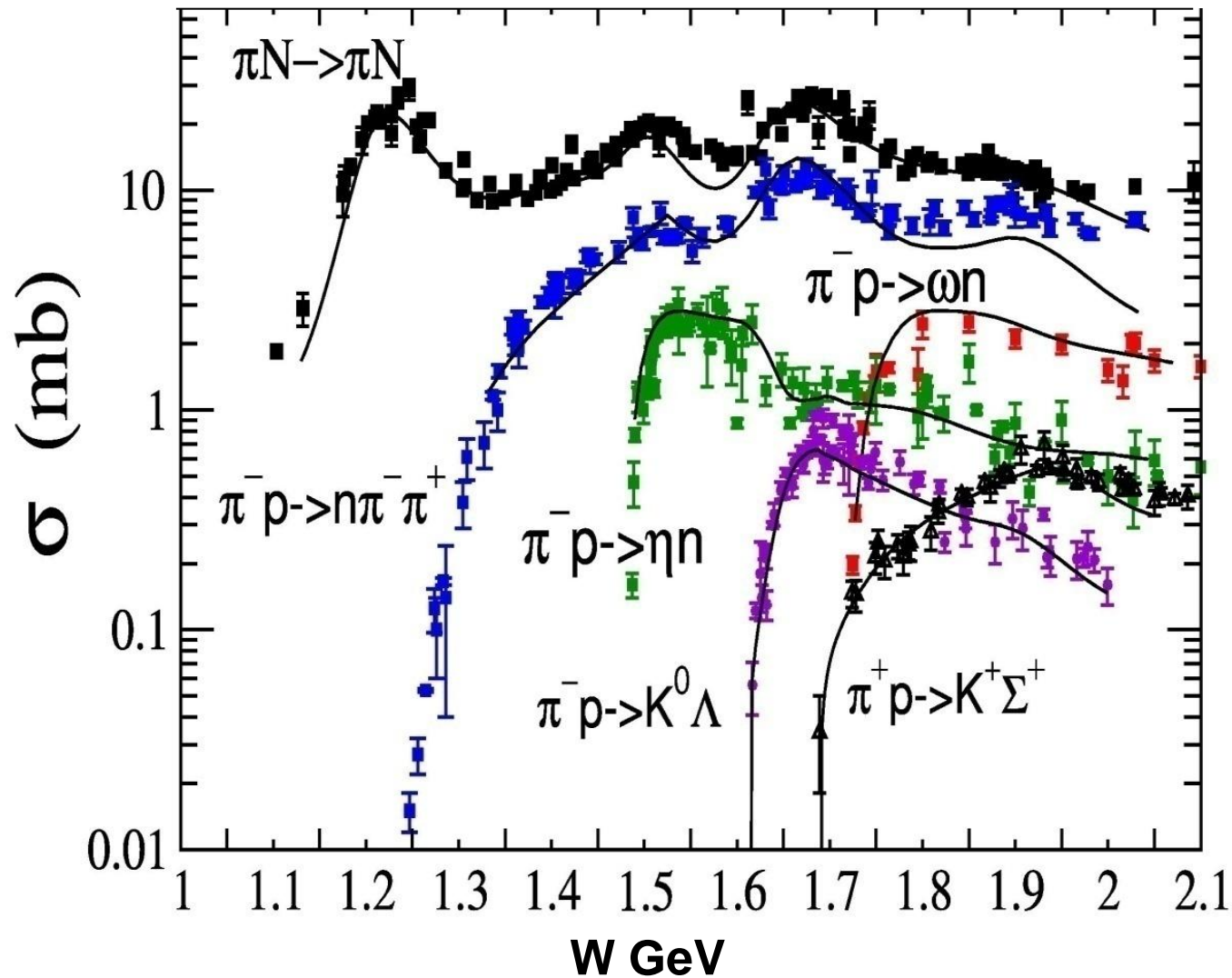


# $\pi N$ amplitudes



Isospin 1/2  
Imaginary T

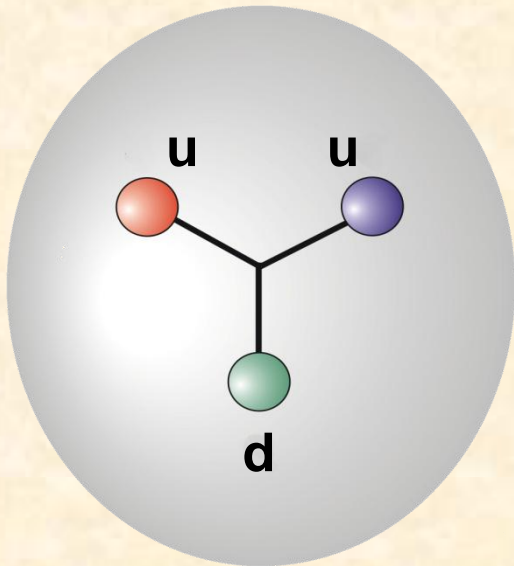
# $\pi N$ exclusive channels



# $\Delta(1232)$ colour wave-function

$$N_c = 3$$

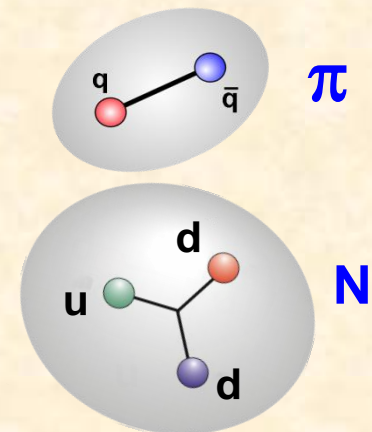
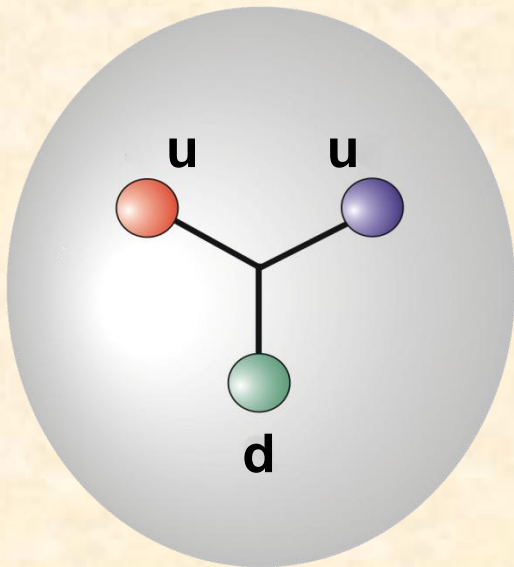
$$\Delta^+ = \frac{1}{\sqrt{6}} \left[ \begin{aligned} & \text{uud} + \text{uud} + \text{uud} \\ & - \text{uud} - \text{uud} - \text{uud} \end{aligned} \right]$$



# $\Delta(1232)$ colour wave-function

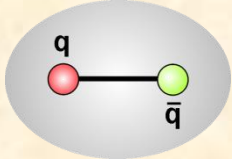
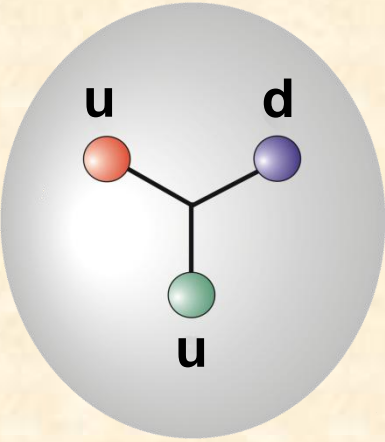
$$N_c = 3$$

$$\Delta^+ = \frac{1}{\sqrt{6}} \left[ \begin{aligned} &uud + uud + uud \\ &- uud - uud - uud \end{aligned} \right]$$

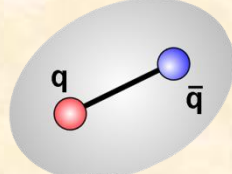




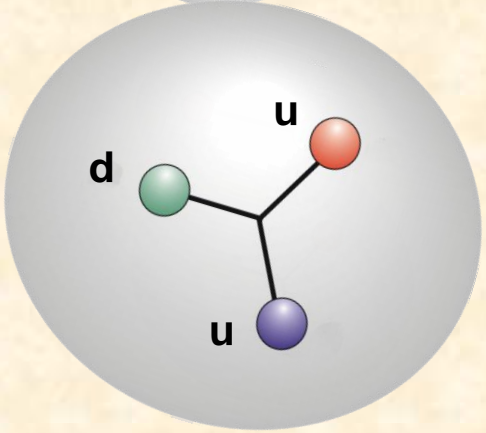
# $N^*(1xxx)$



$\pi$



$\pi$



$N$

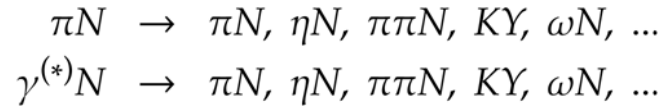
**Coupled channels**



**Coupled channels**

# Properties of Excited Baryons

## Reaction Data



Dynamical Coupled-Channels Analysis @ EBAC

## Excited Baryon Program

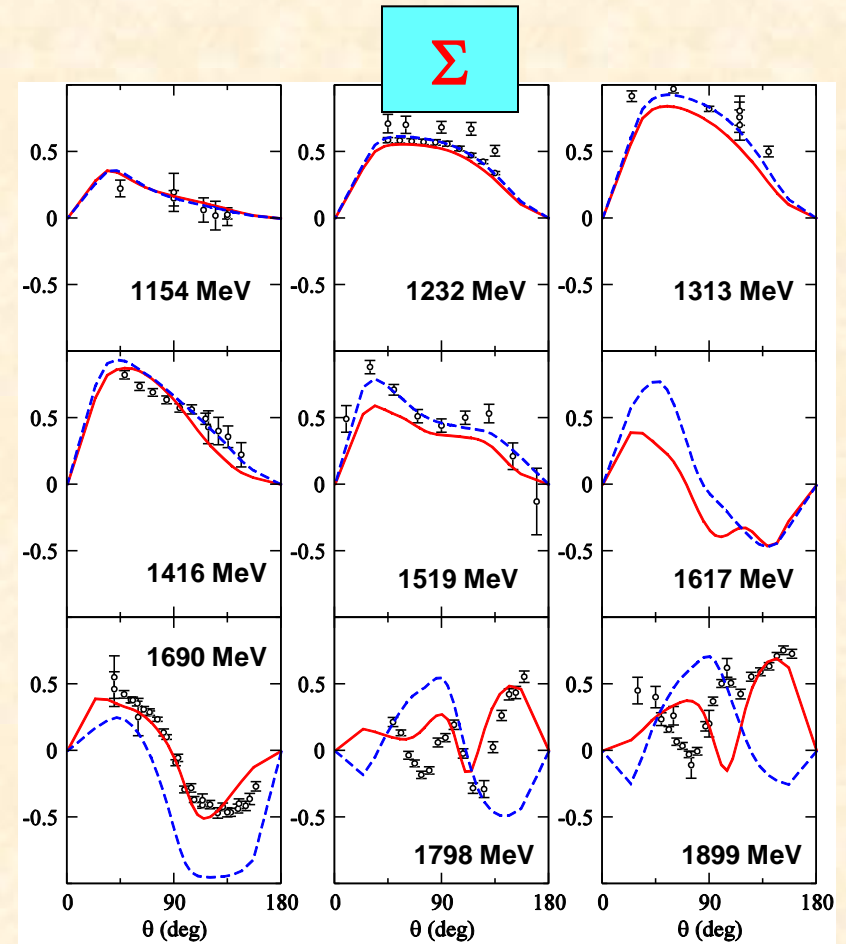
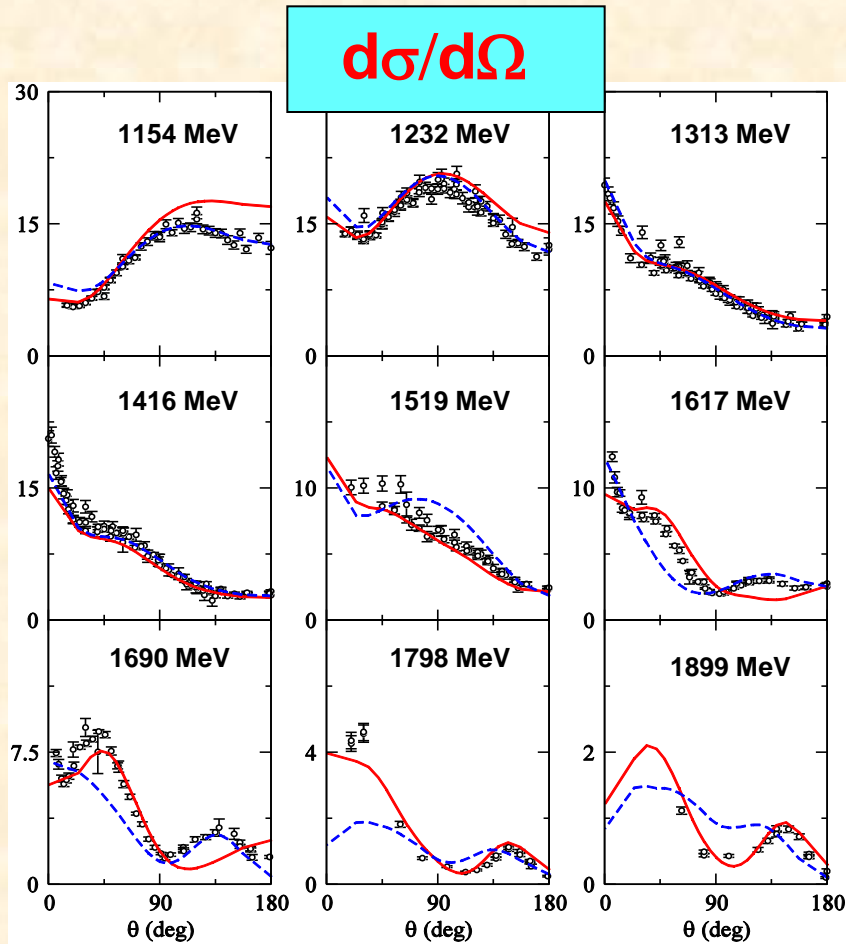
N\* parameters

Hadron models

Strong QCD

QCD

# pion photoproduction: $\gamma p \rightarrow \pi^+ n$



— Current model  
(full combined analysis)

- - - Previous model (fitted to  $\gamma N \rightarrow \pi N$  data **up to 1.6 GeV**)

# $\pi N \rightarrow K \Lambda$

$d\sigma/d\Omega$

P

$\pi^+ p \rightarrow K^+ \Sigma^+$

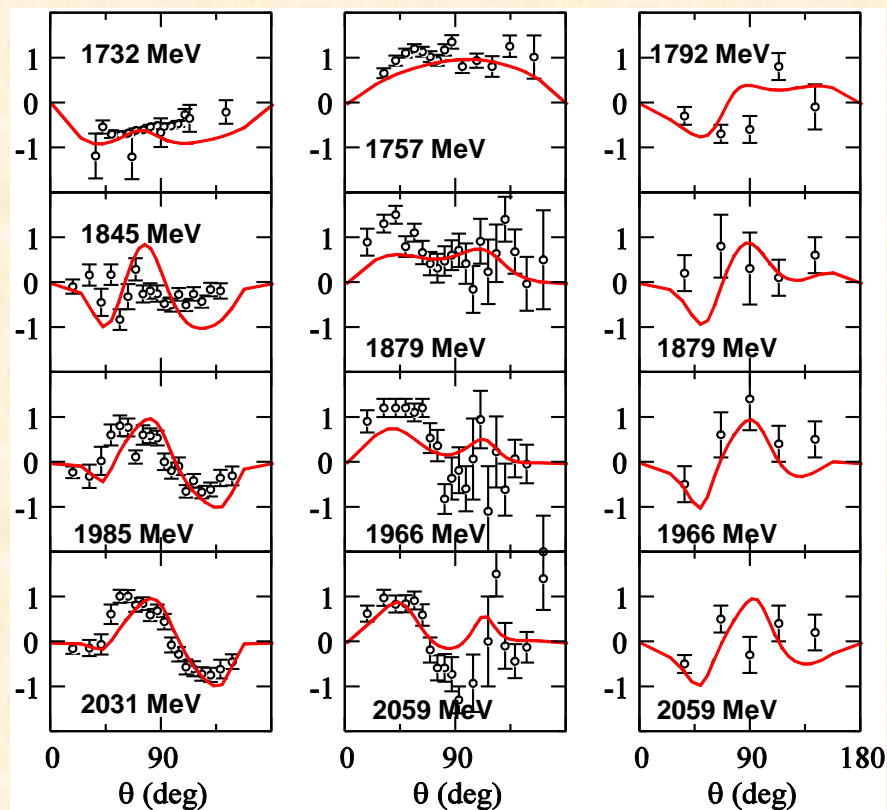
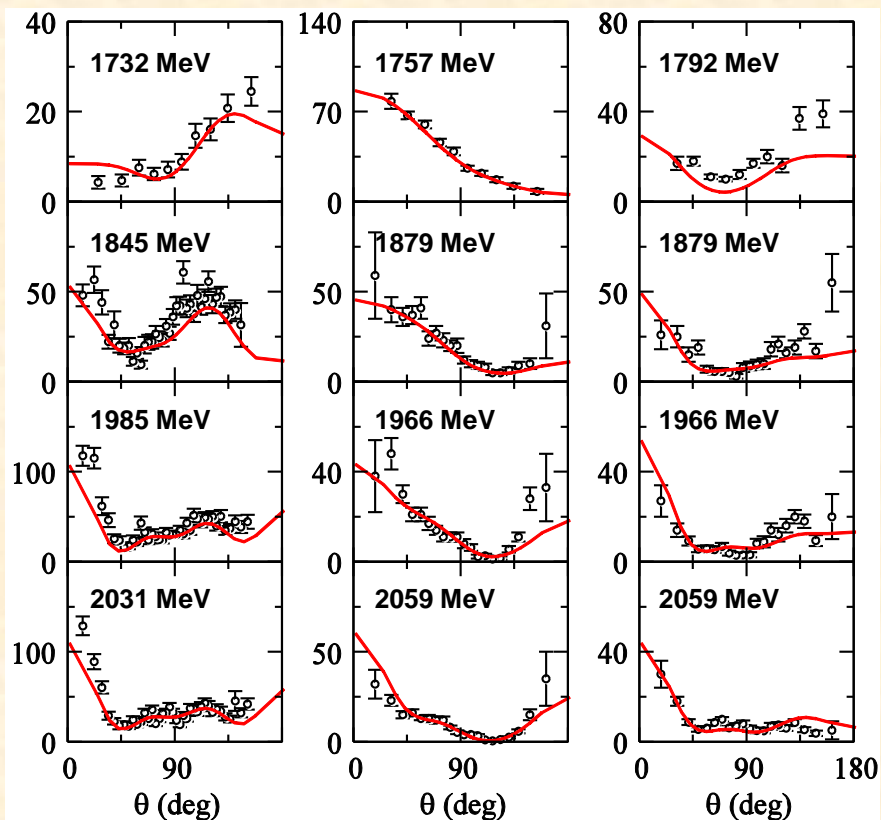
$\pi^- p \rightarrow K^0 \Lambda^0$

$\pi^- p \rightarrow K^0 \Sigma^0$

$\pi^+ p \rightarrow K^+ \Sigma^+$

$\pi^- p \rightarrow K^0 \Lambda^0$

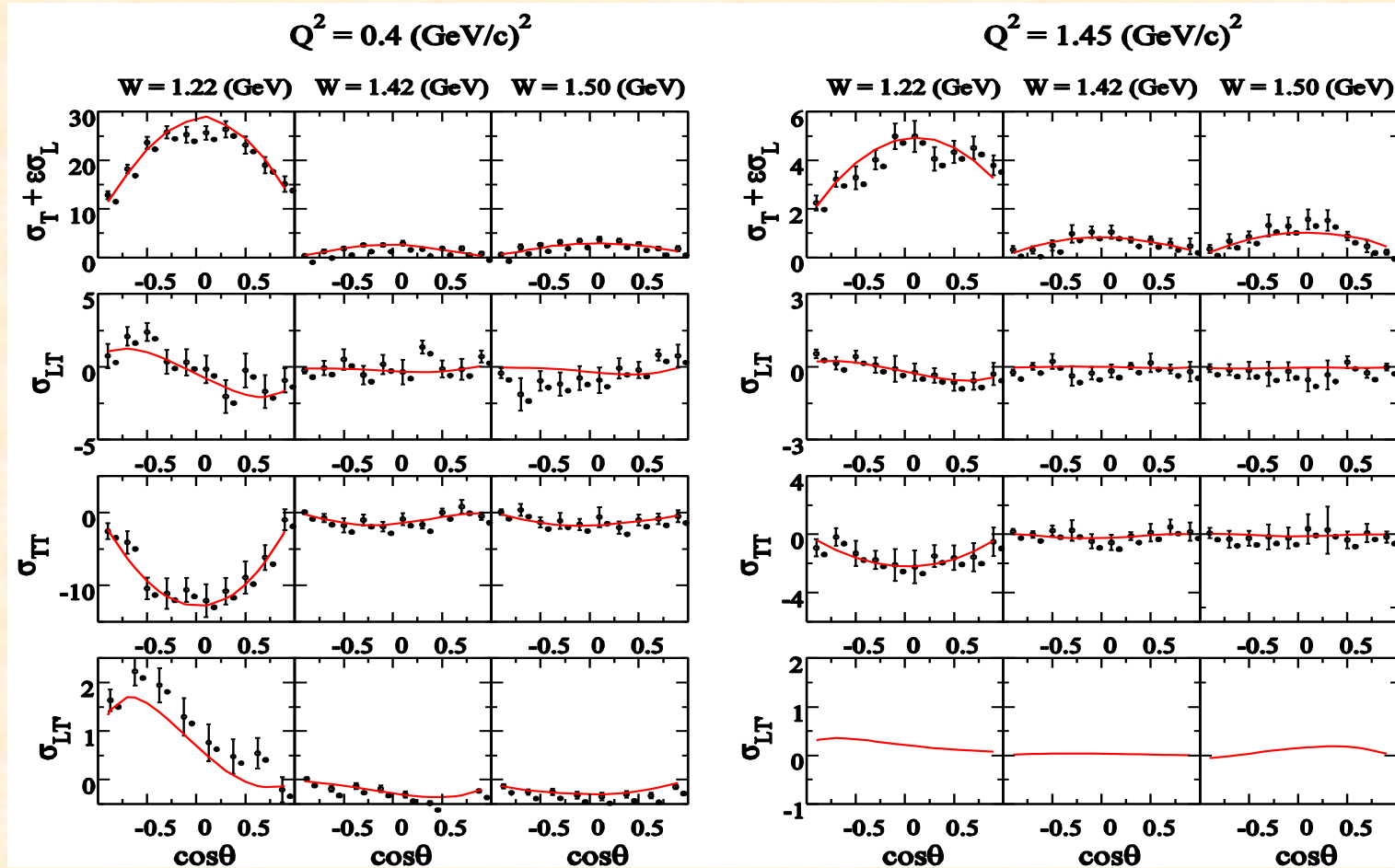
$\pi^- p \rightarrow K^0 \Sigma^0$



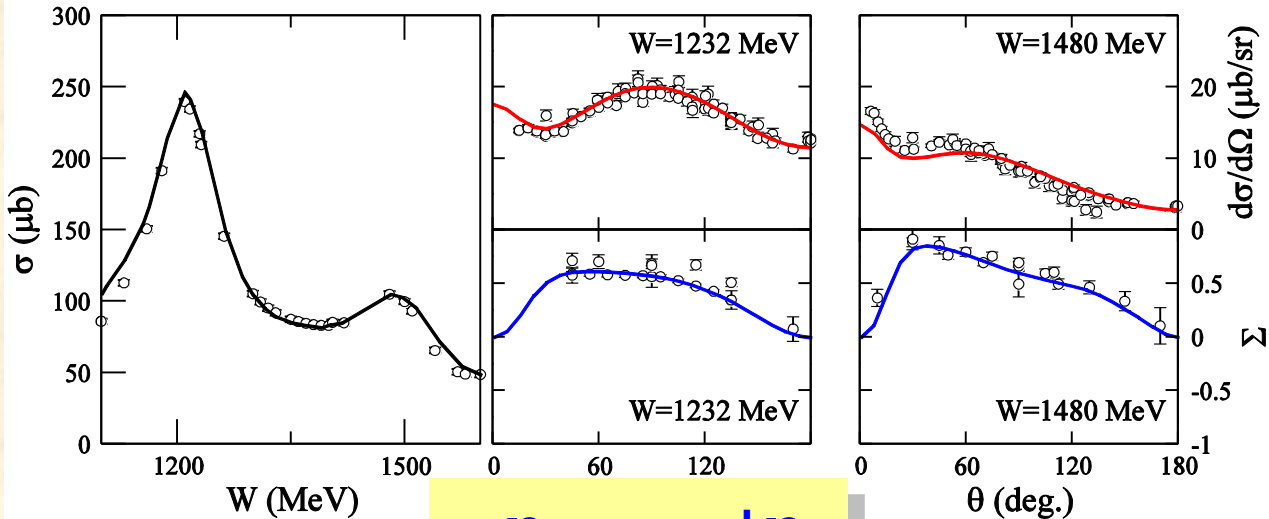
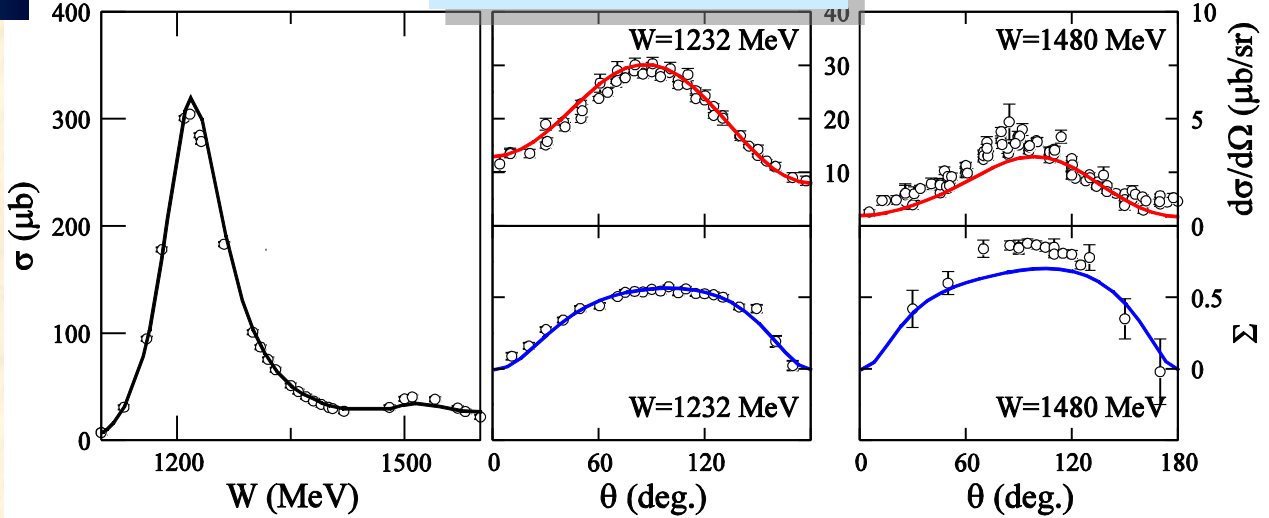
# pion electroproduction: $ep \rightarrow e'\pi^0 p$

Fit to the structure function data ( $\sim 20000$ ) from CLAS

$$Q^2 > 0$$



$\gamma p \rightarrow \pi^0 p$

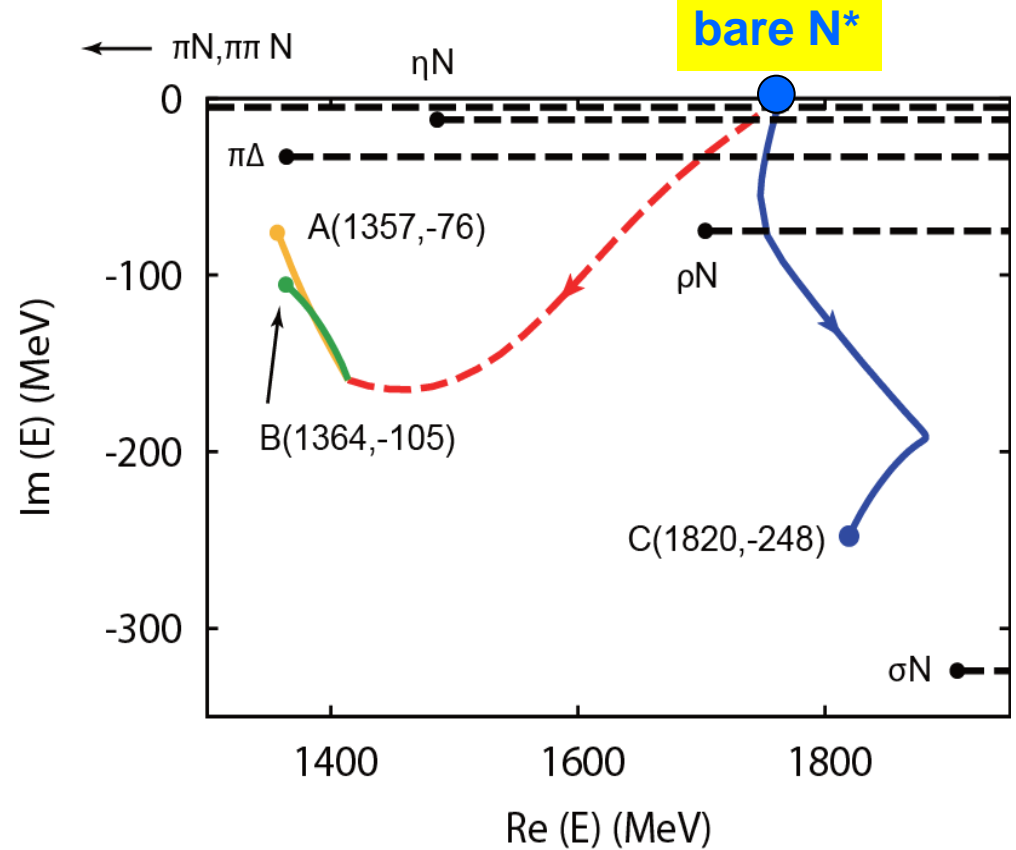
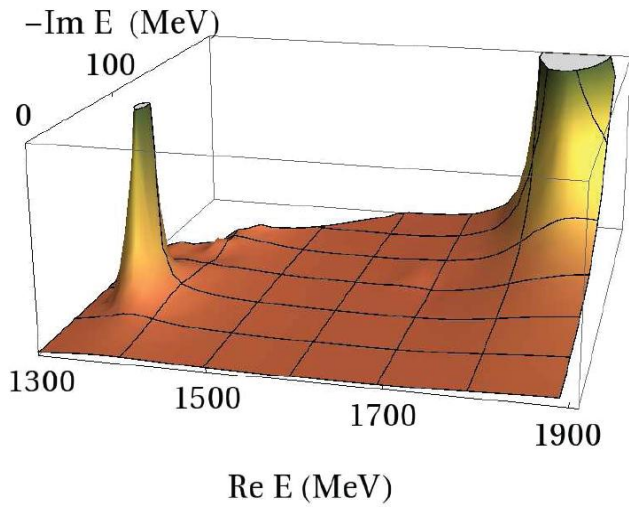


$\gamma p \rightarrow \pi^+ n$

# $P_{11}(1360)$ , $P_{11}(1820)$

EBAC

Suzuki et al.

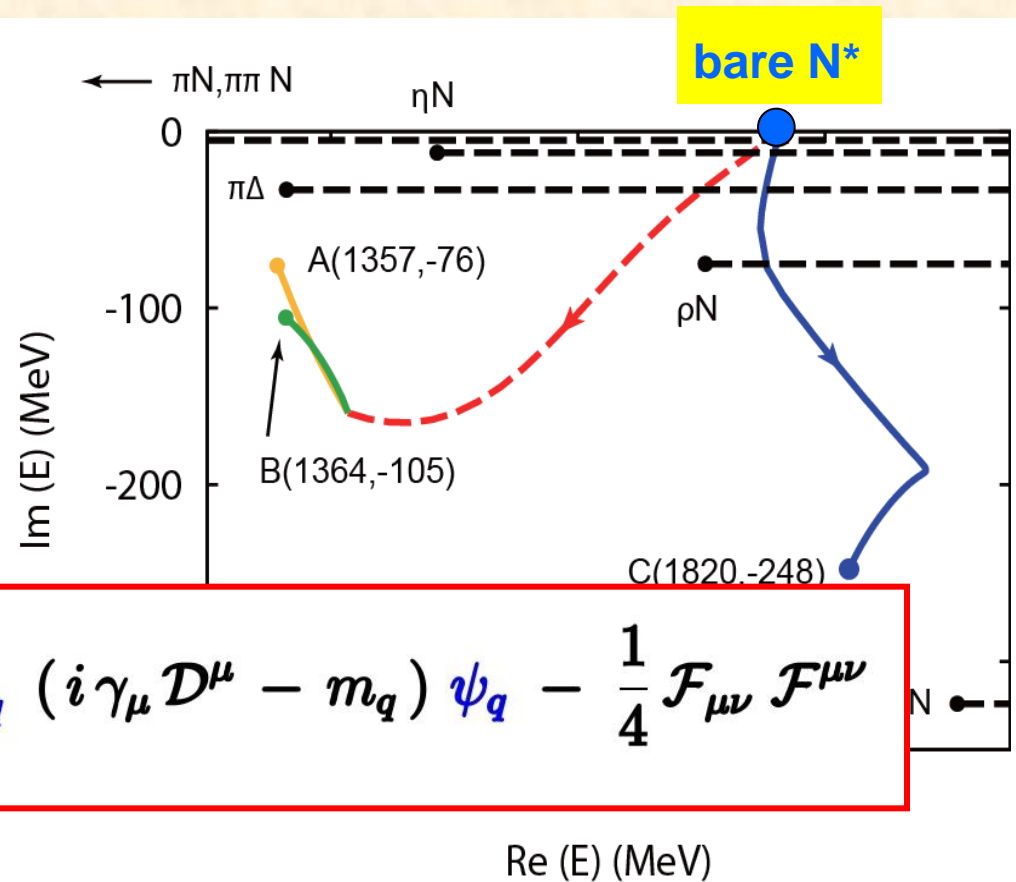
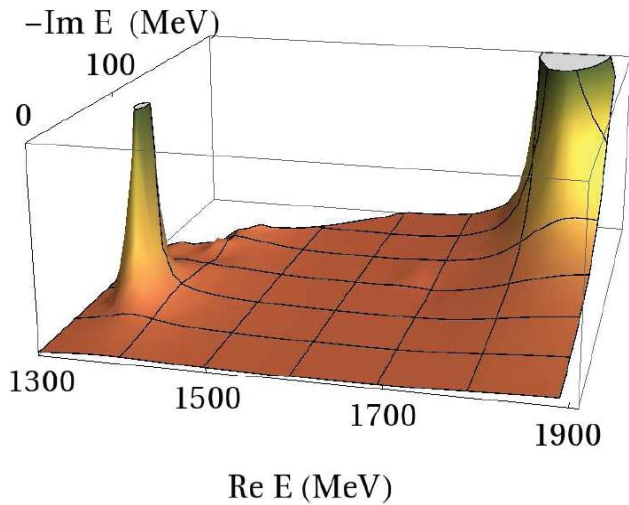




$P_{11}(1360)$ ,  $P_{11}(1820)$

EBAC

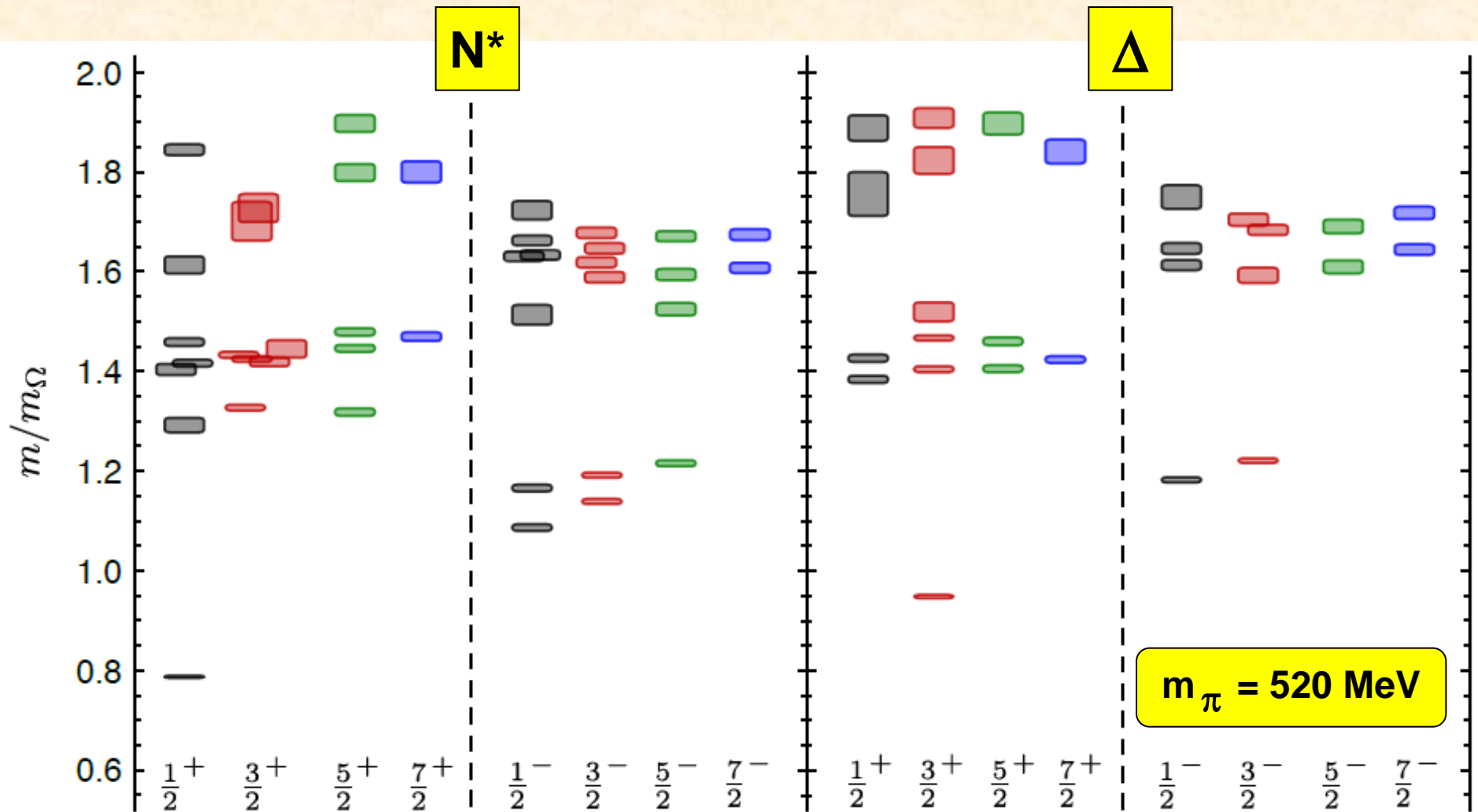
Suzuki et al.



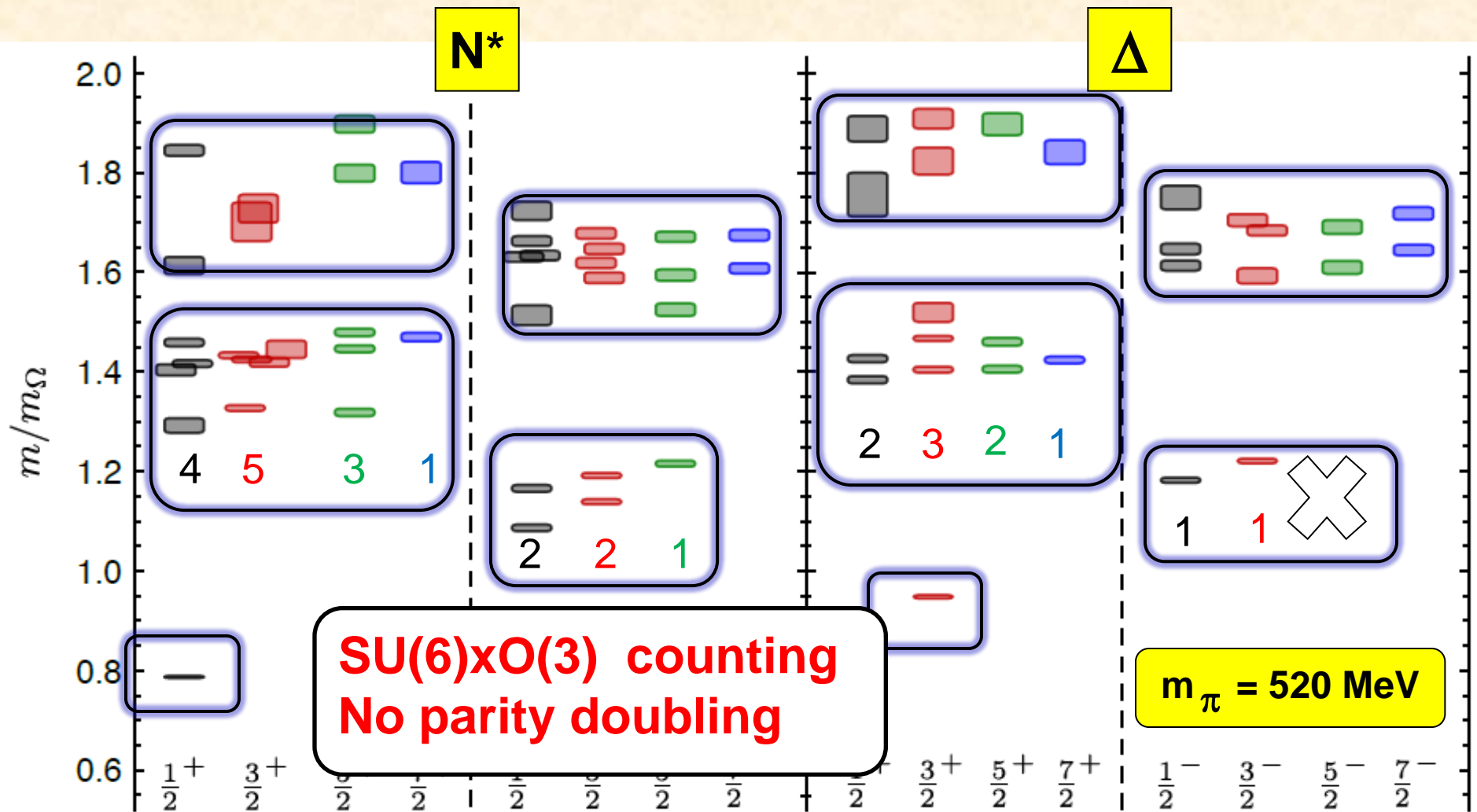
$$\mathcal{L}_{\text{QCD}} = \sum_{q=u,d,s,c,b} \bar{\psi}_q (i \gamma_\mu D^\mu - m_q) \psi_q - \frac{1}{4} \mathcal{F}_{\mu\nu} \mathcal{F}^{\mu\nu}$$

Re (E) (MeV)

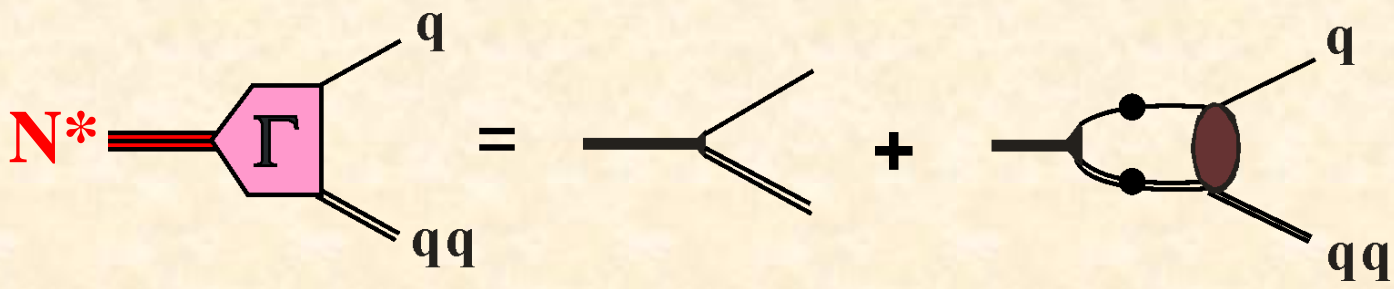
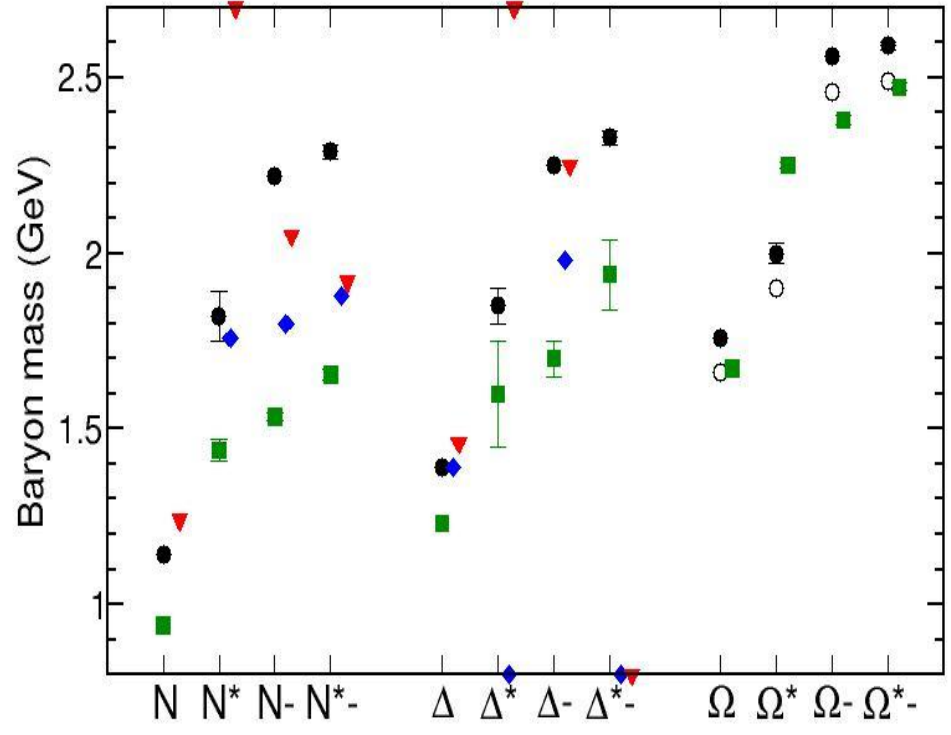
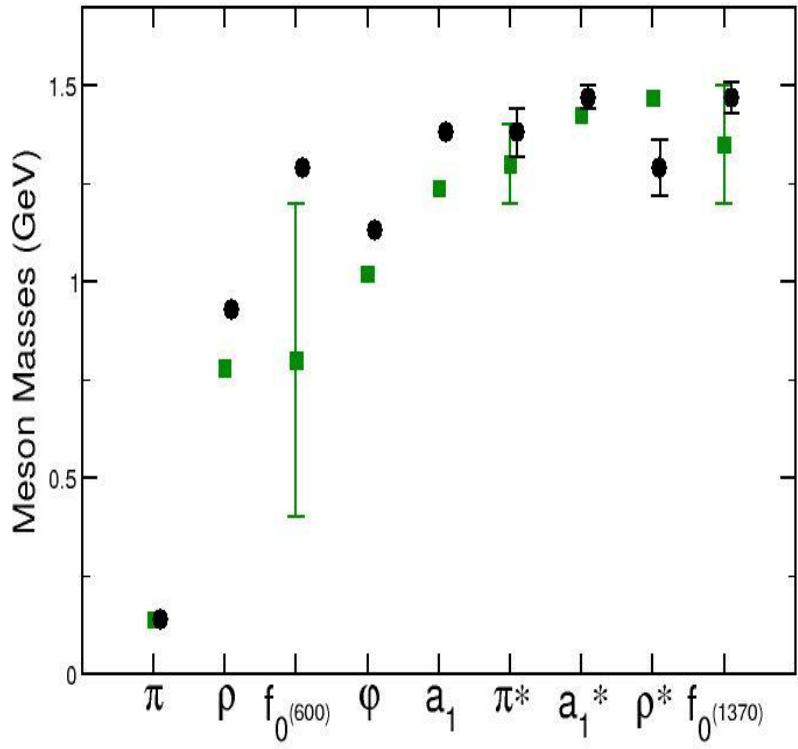
# Spin identified $N^*$ and $\Delta$ states



# Spin identified $N^*$ and $\Delta$ states

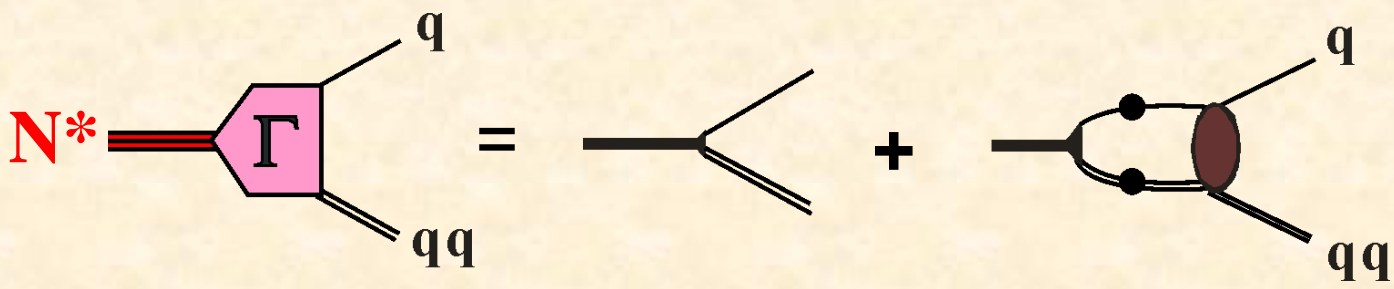
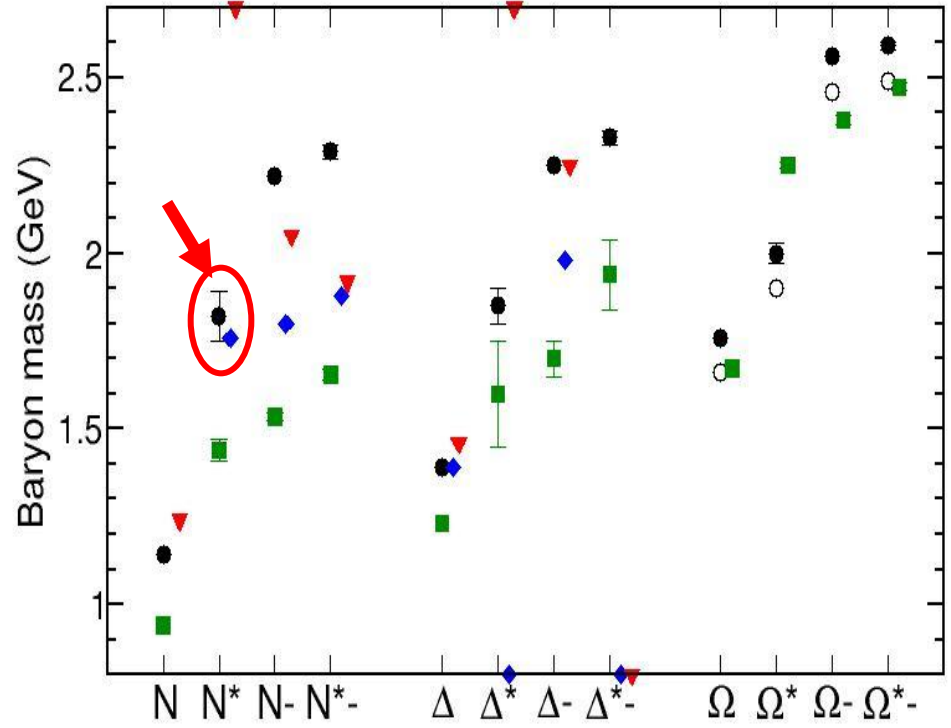
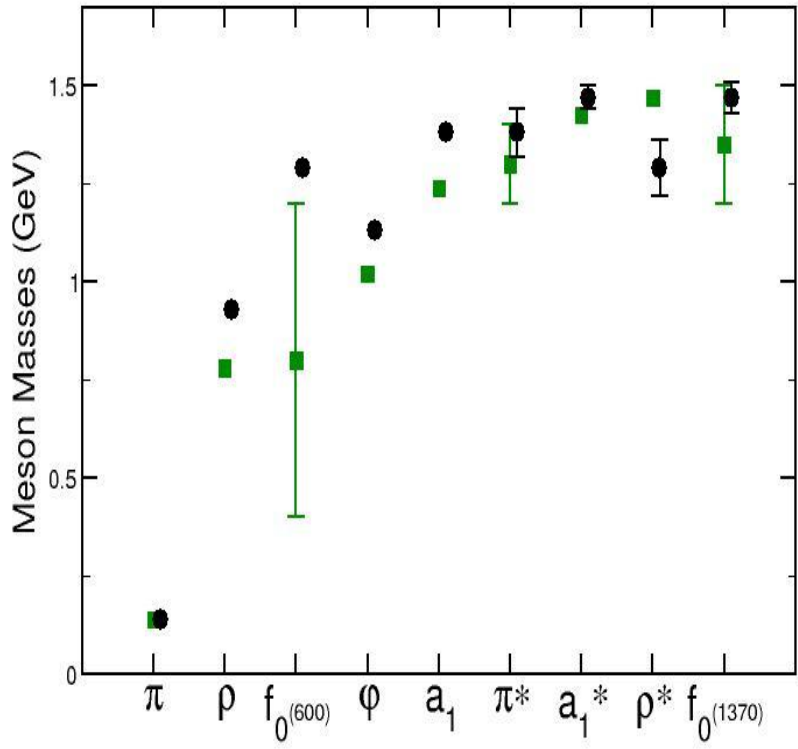


# Hadron Spectrum in ANL BS model

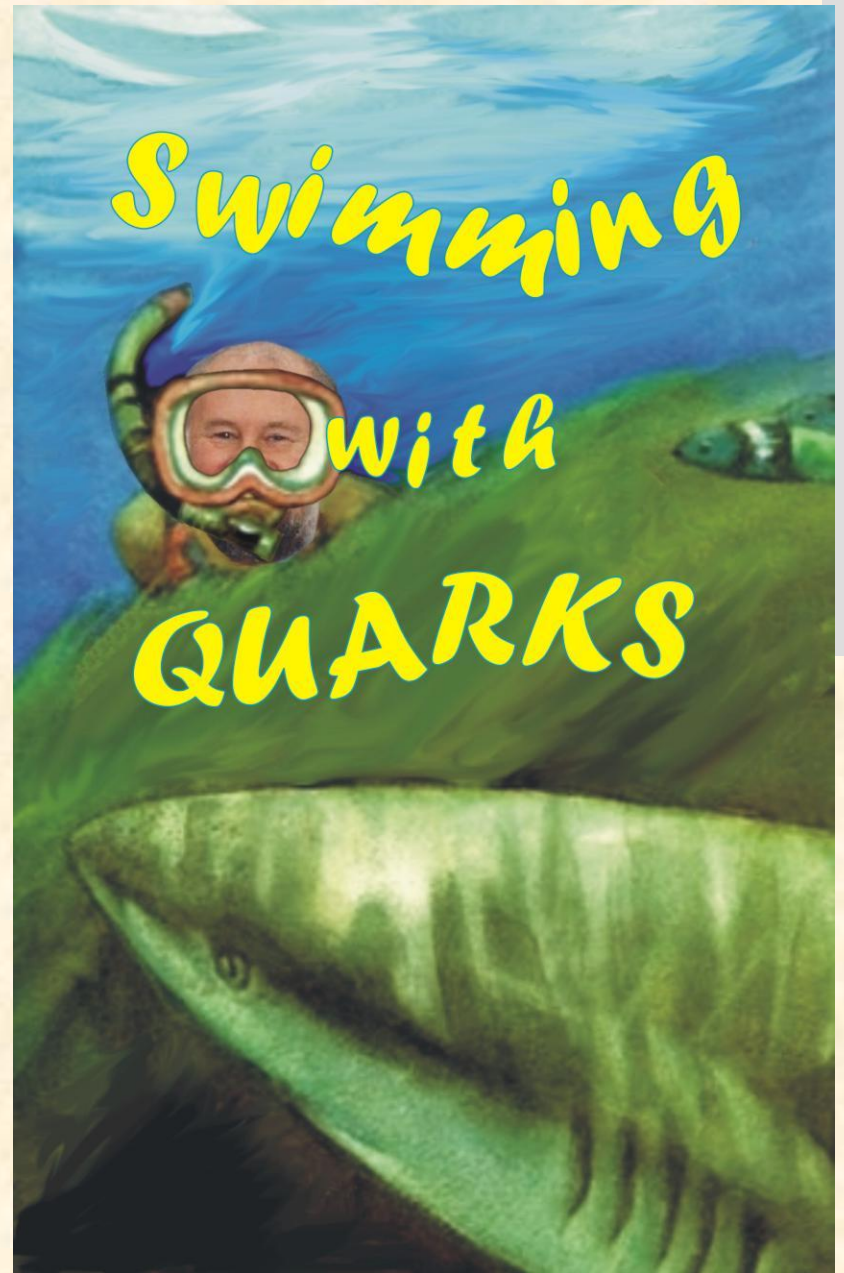
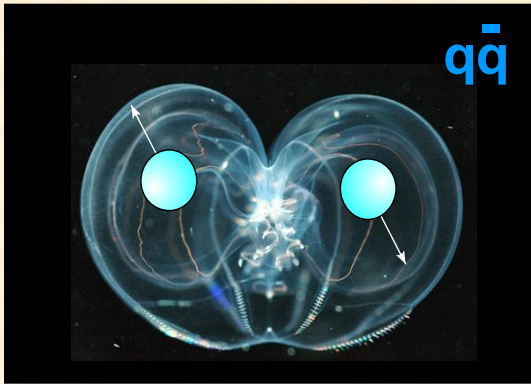


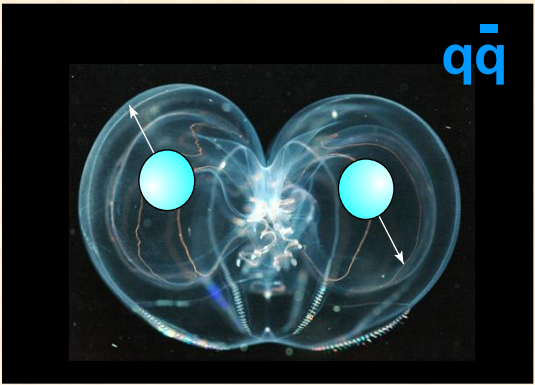
- Legend:**
- Particle Data Group
  - H.L.L. Roberts *et al.*
  - ◆ EBAC
  - ▼ Jülich

# Hadron Spectrum in ANL BS model



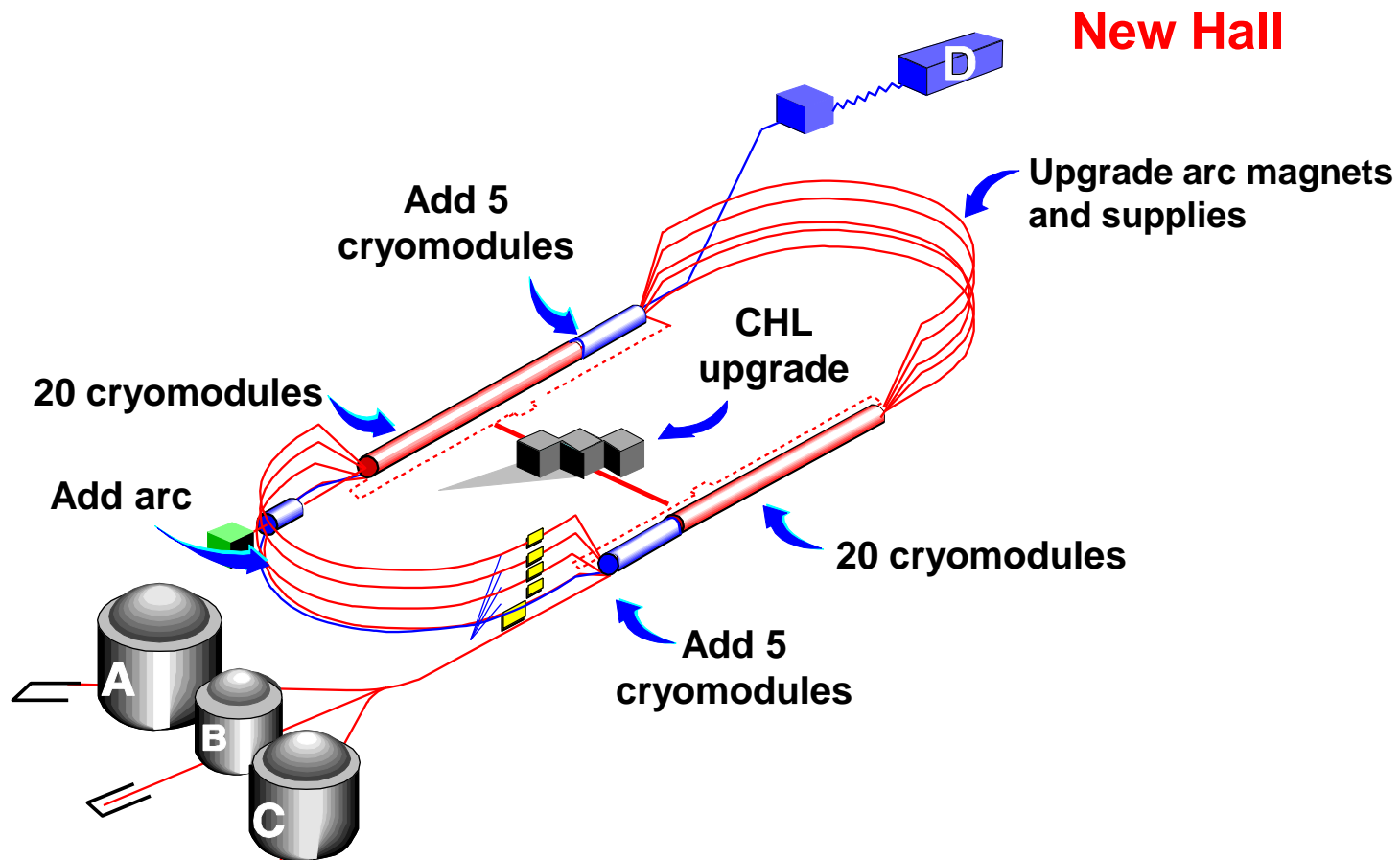
- Legend:**
- Particle Data Group
  - H.L.L. Roberts *et al.*
  - ◆ EBAC
  - ▼ Jülich





# Jefferson Lab 12 GeV upgrade

Exploring the Nature of Matter

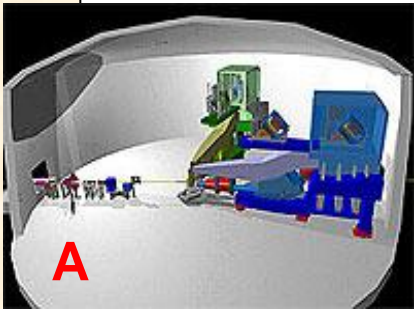


**Enhanced capabilities  
in existing Halls**

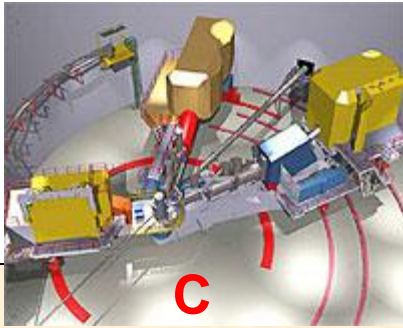
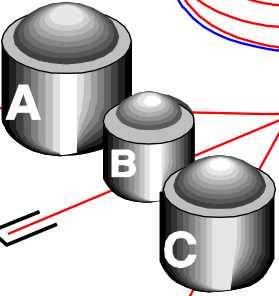
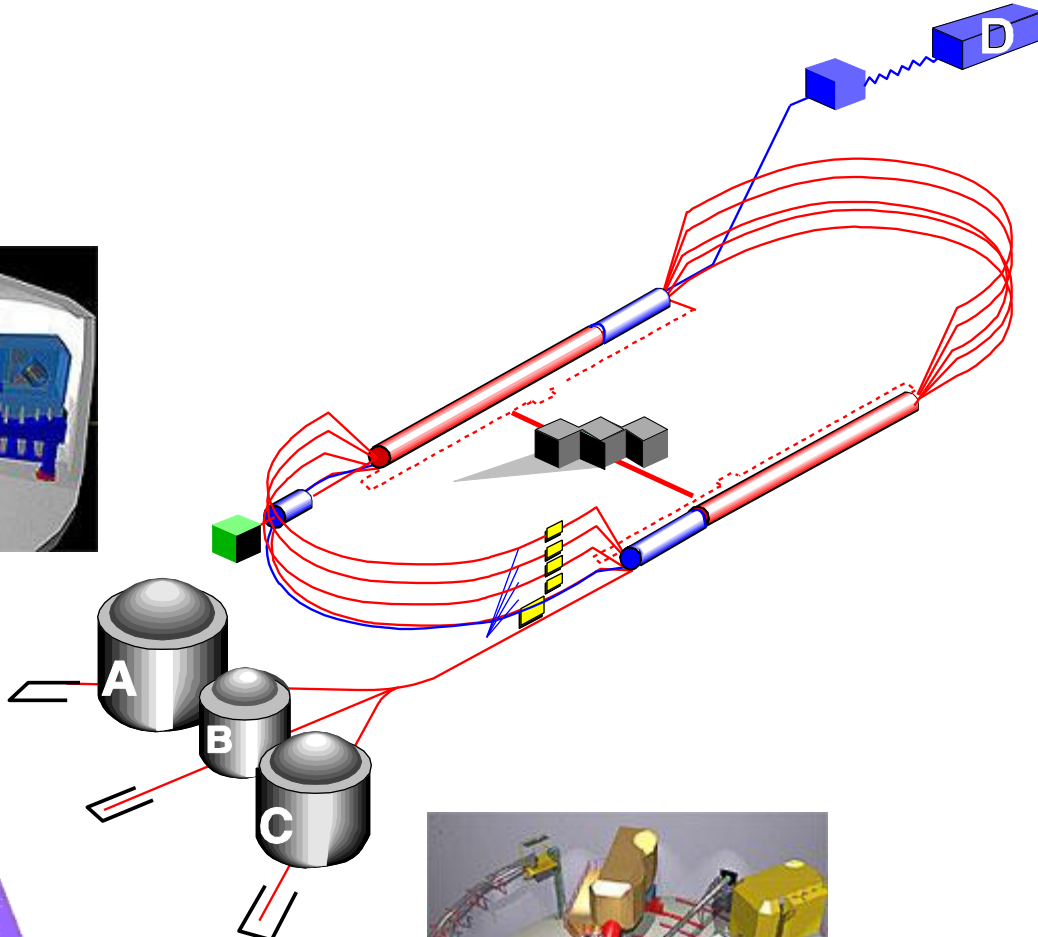


# Jefferson Lab 12 GeV upgrade

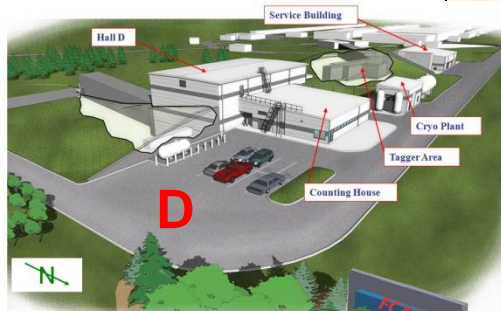
Exploring the Nature of Matter



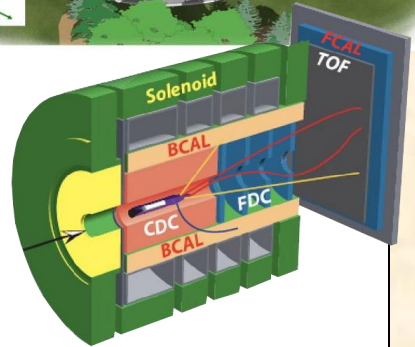
A



C



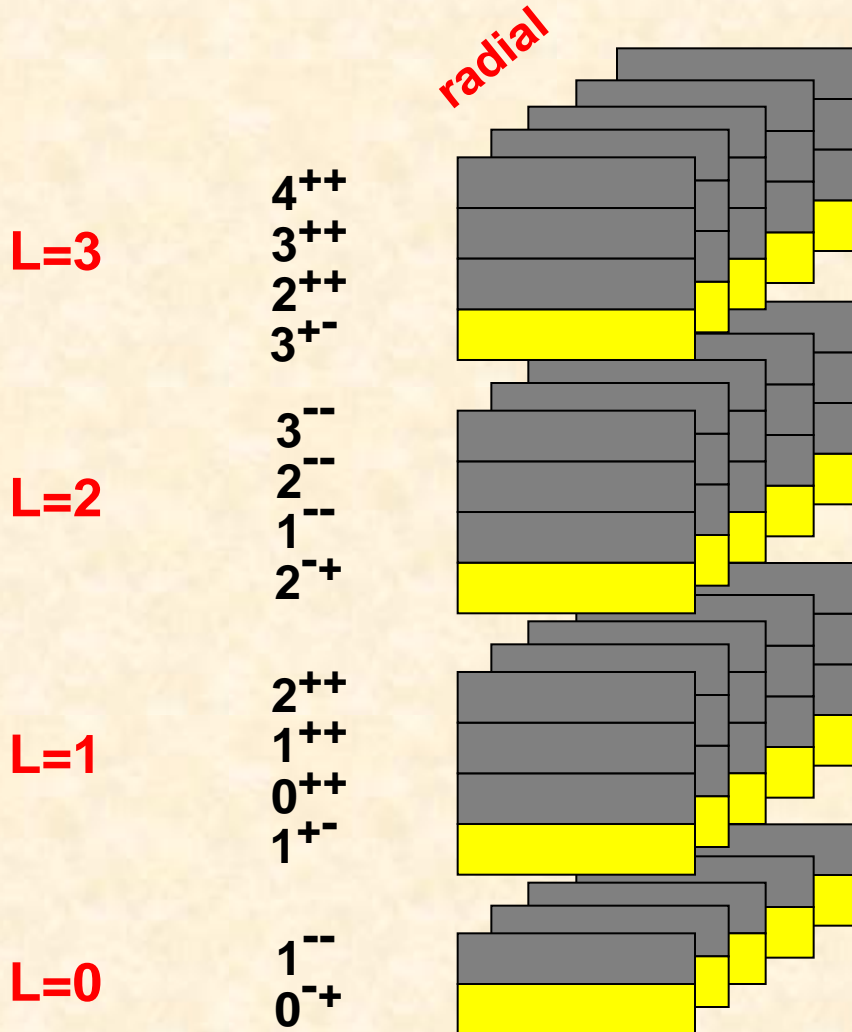
D



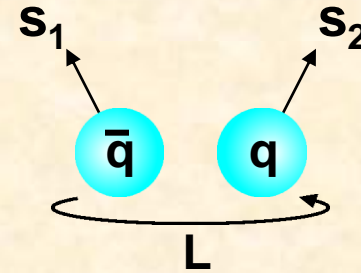
GlueX

B CLAS12

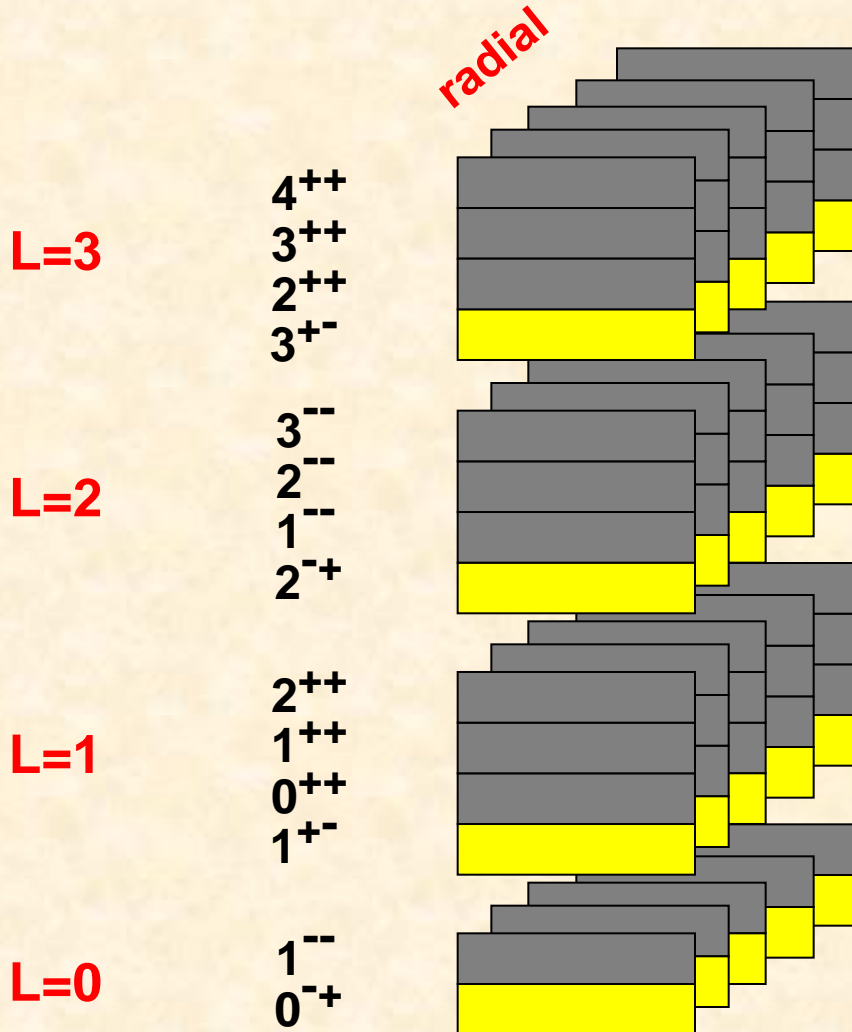
# Meson spectrum



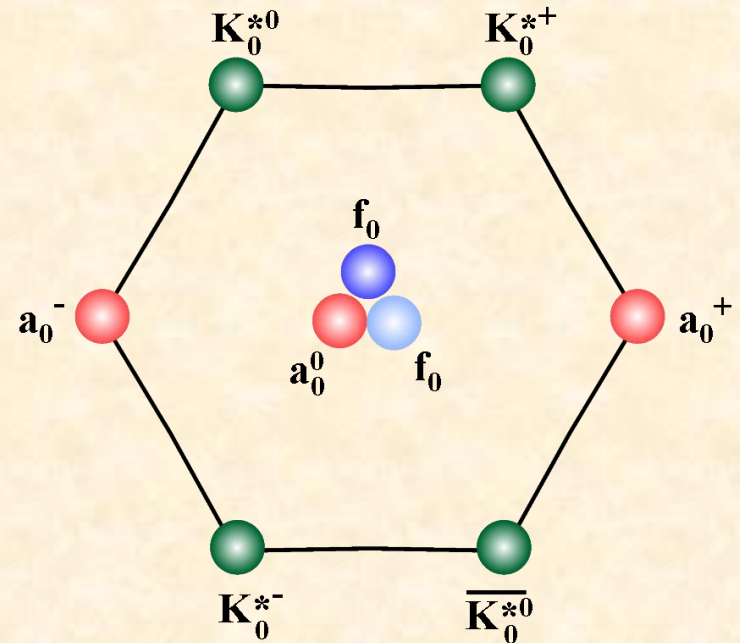
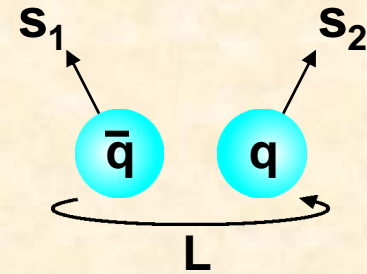
$$S = 0, 1$$



# Meson spectrum



$$S = 0, 1$$



# allowed $J^{PC}$

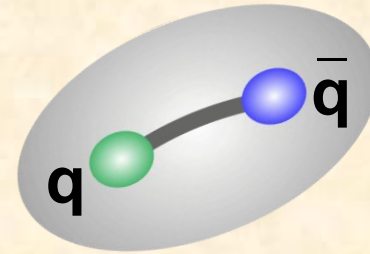
$0^{--}$   $0^{-+}$   $0^{+-}$   $0^{++}$

$1^{--}$   $1^{-+}$   $1^{+-}$   $1^{++}$

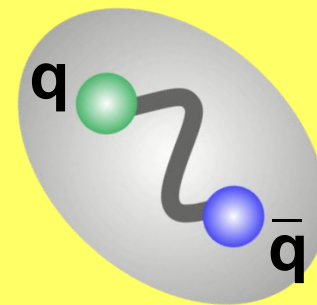
$2^{--}$   $2^{-+}$   $2^{+-}$   $2^{++}$

$3^{--}$   $3^{-+}$   $3^{+-}$   $3^{++}$

$4^{--}$   $4^{-+}$   $4^{+-}$   $4^{++}$



$J^{PC} \rightarrow$  not  $\bar{q}q$



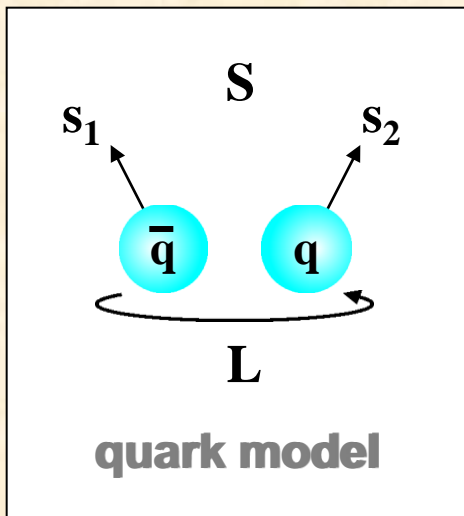
# Mesons: $J^{PC}$ quantum numbers

$0^{++}$   $0^{+-}$   $0^{-+}$   $0^{--}$

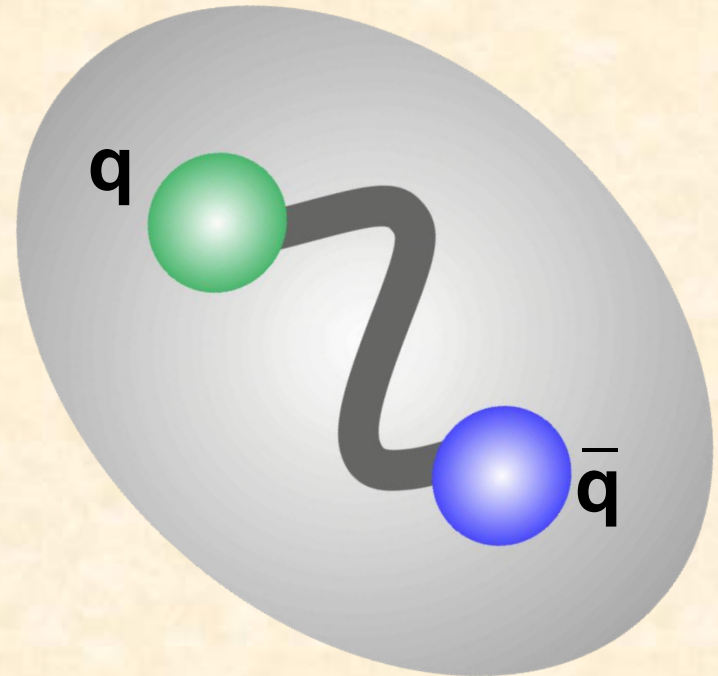
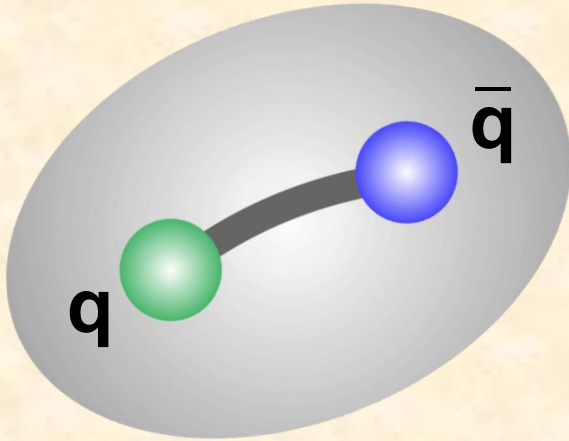
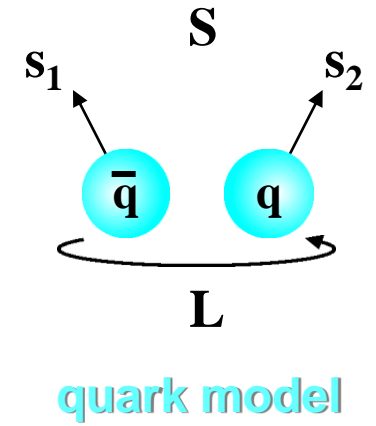
$1^{++}$   $1^{+-}$   $1^{-+}$   $1^{--}$

$2^{++}$   $2^{+-}$   $2^{-+}$   $2^{--}$

...



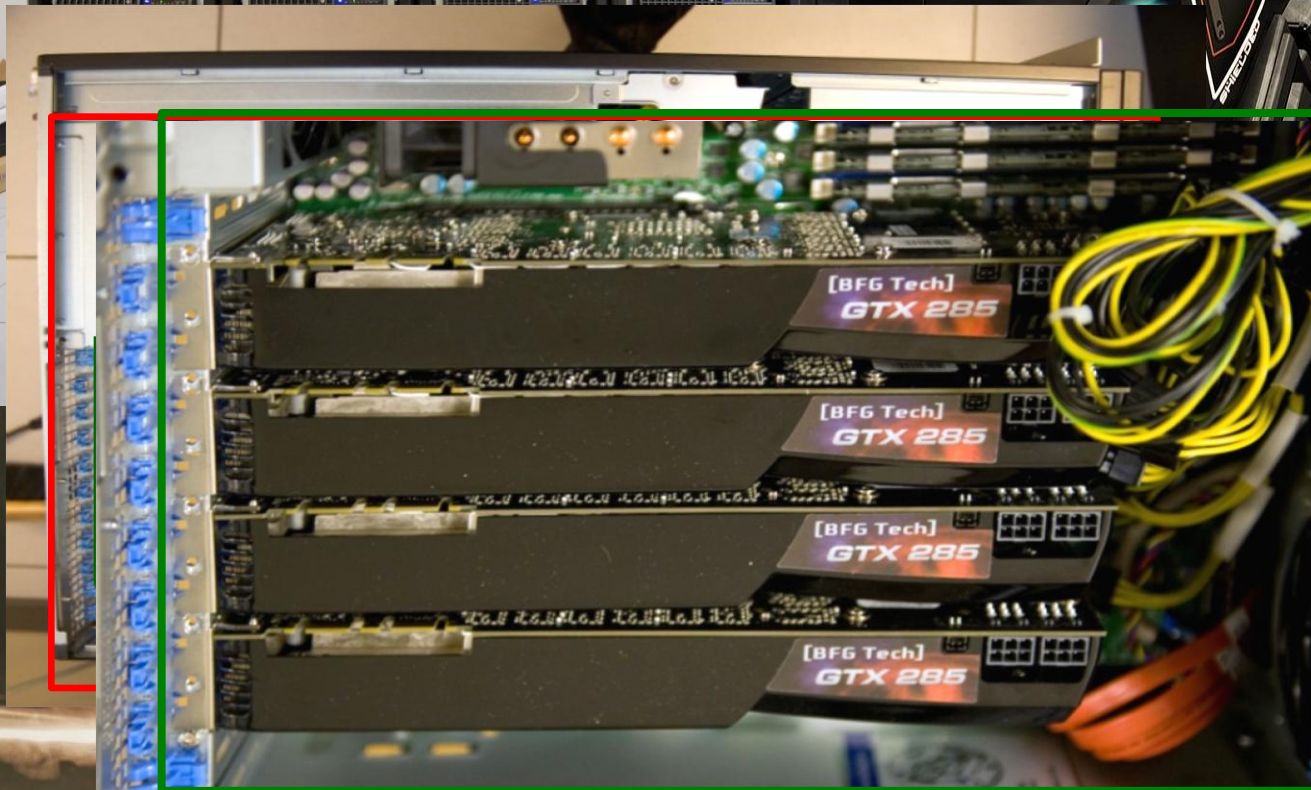
# Calculating Exotic Mesons



# Lattice Game Show



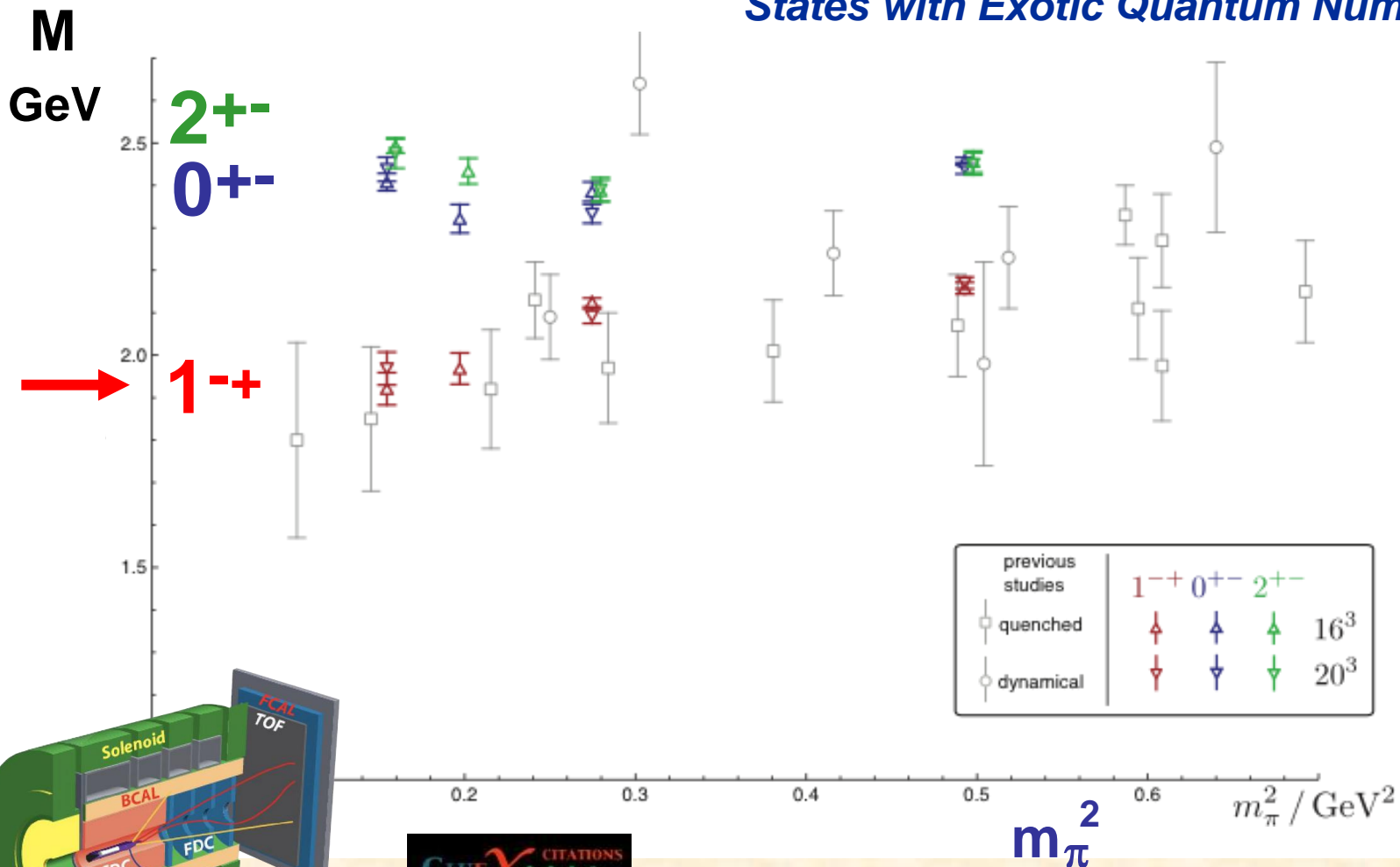
# Lattice Game Show



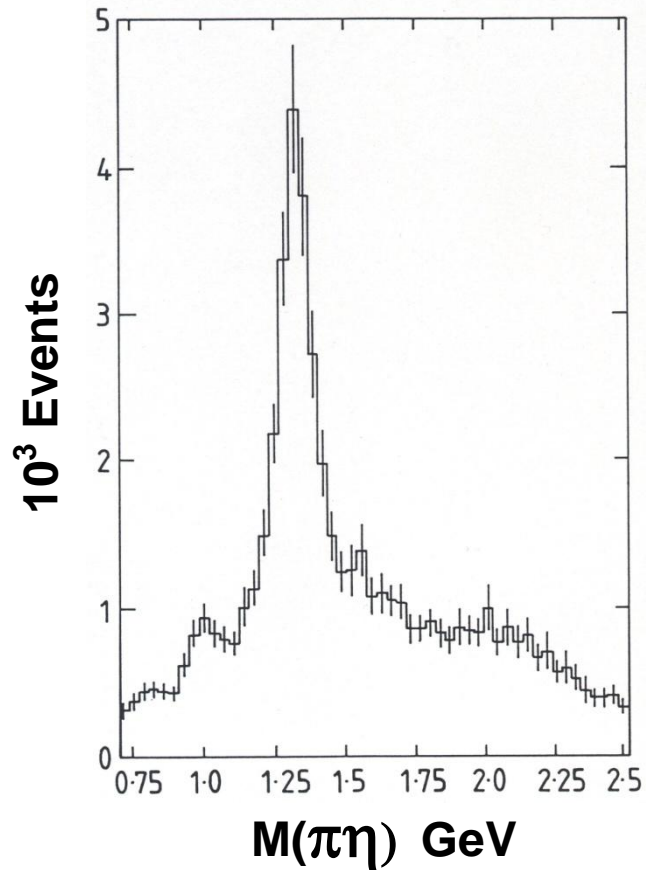
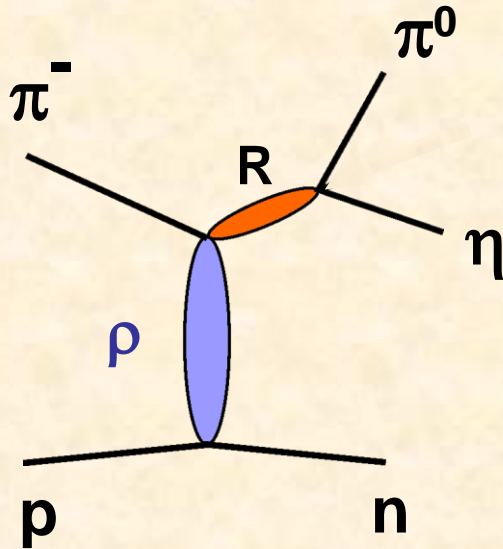
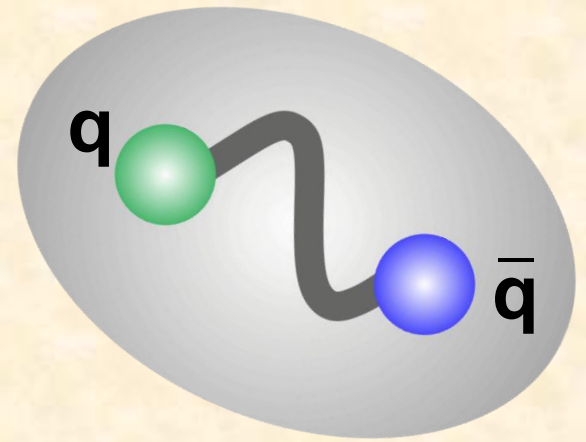


# Isvector Meson Spectrum

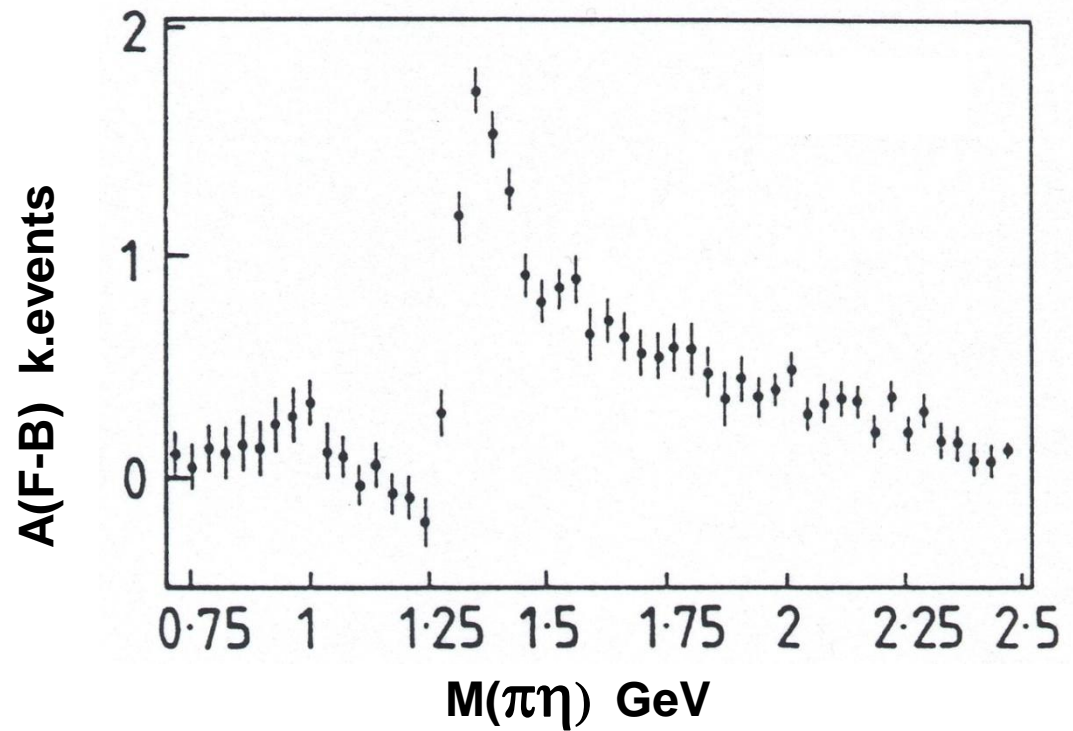
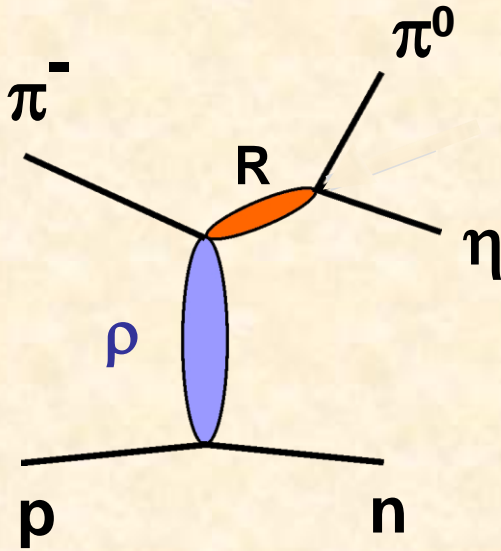
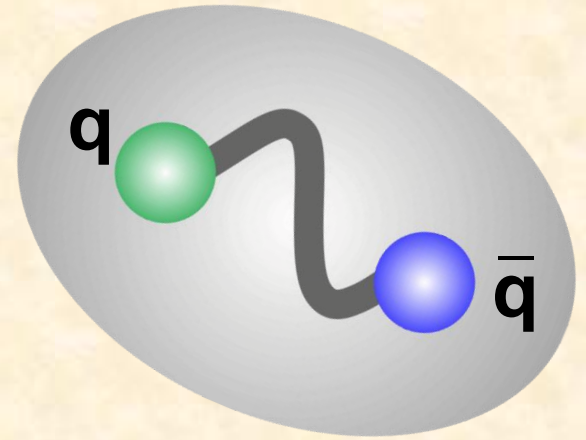
## States with Exotic Quantum Numbers



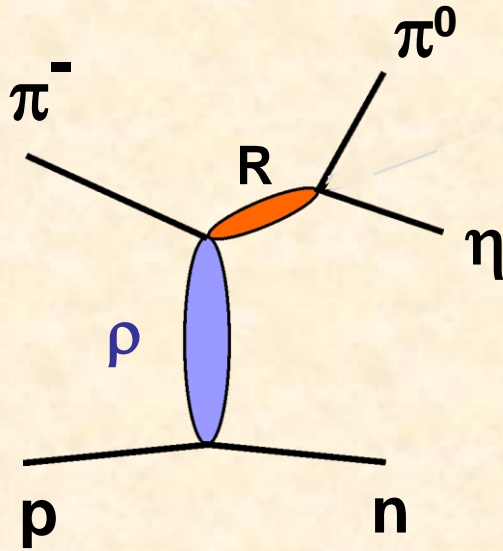
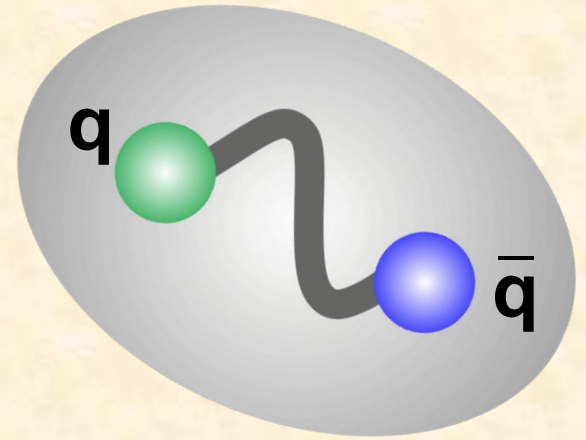
**GAMS:  $\pi^- p \rightarrow \pi^0 \eta n$**



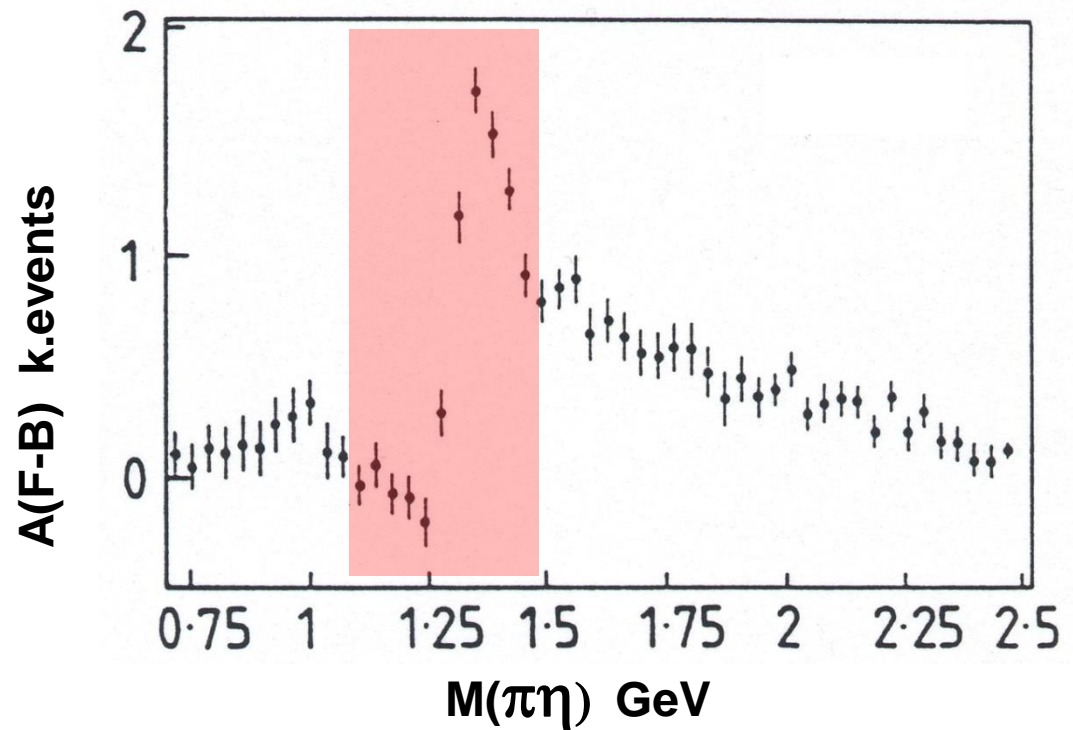
**GAMS:  $\pi^- p \rightarrow \pi^0 \eta n$**



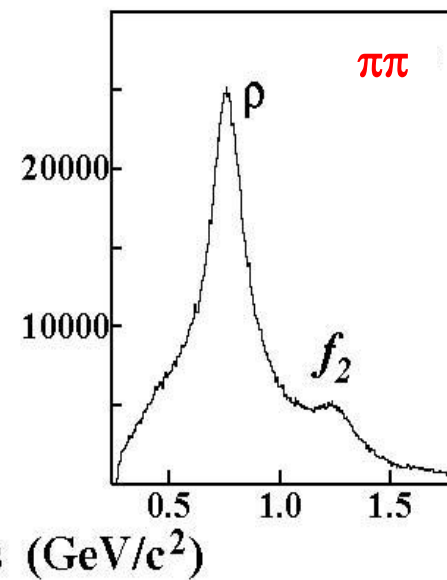
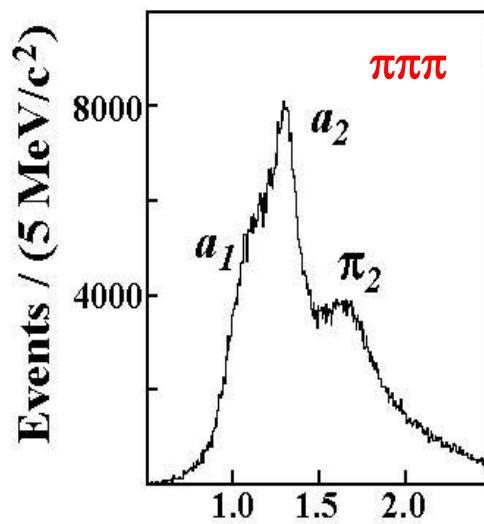
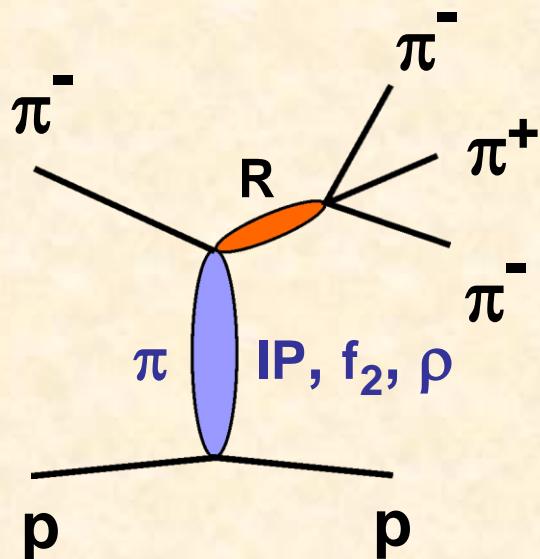
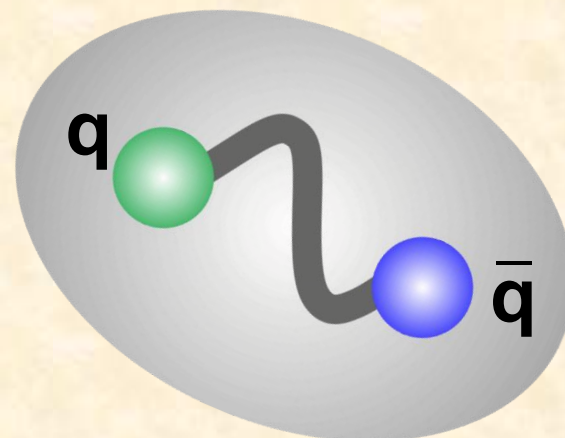
GAMS:  $\pi^- p \rightarrow \pi^0 \eta n$



$1^{-+}$



BNL-E852:  $\pi^- p \longrightarrow \pi^+ \pi^- \pi^- p$

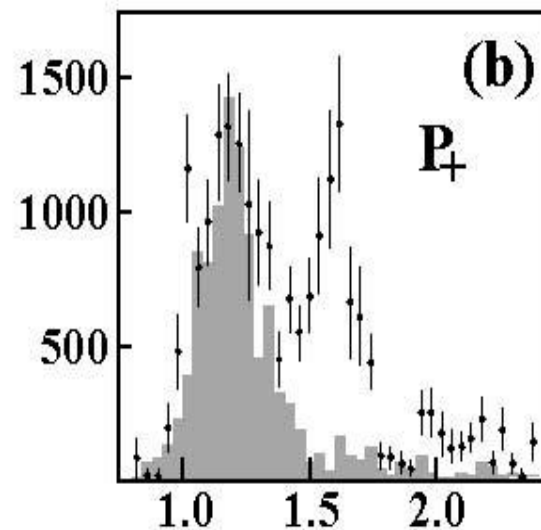
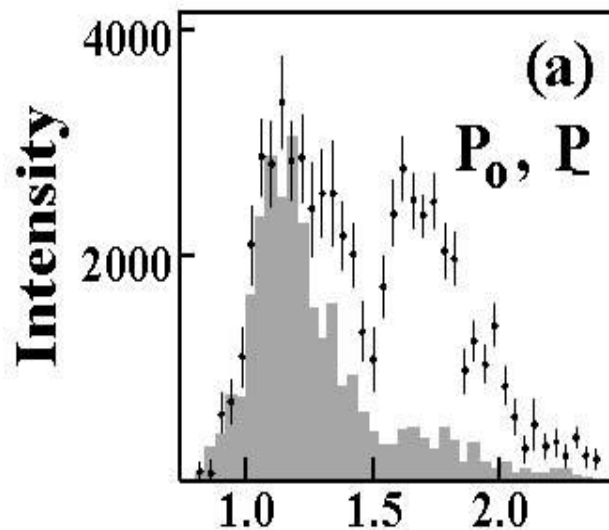


250k events

BNL-E852:  $\pi^- p \rightarrow \pi^+ \pi^- \pi^- p$

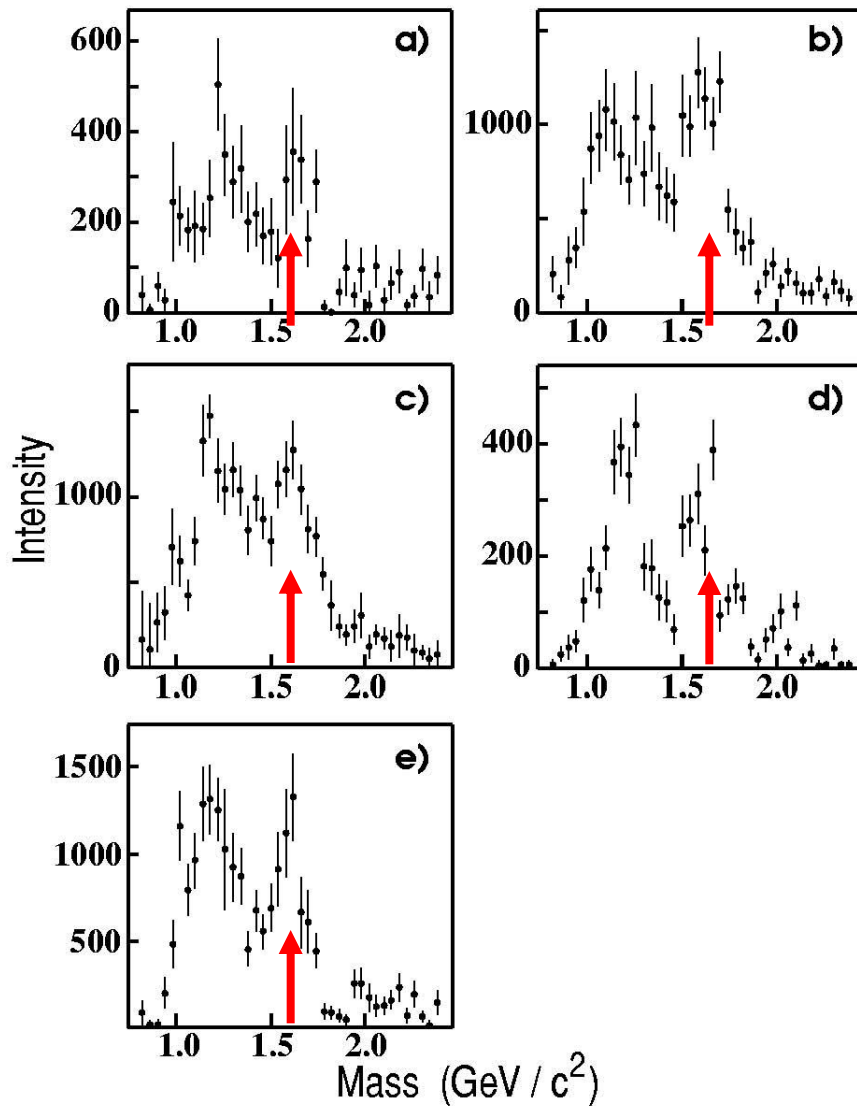


Monte Carlo  
with NO  $1^{++}$



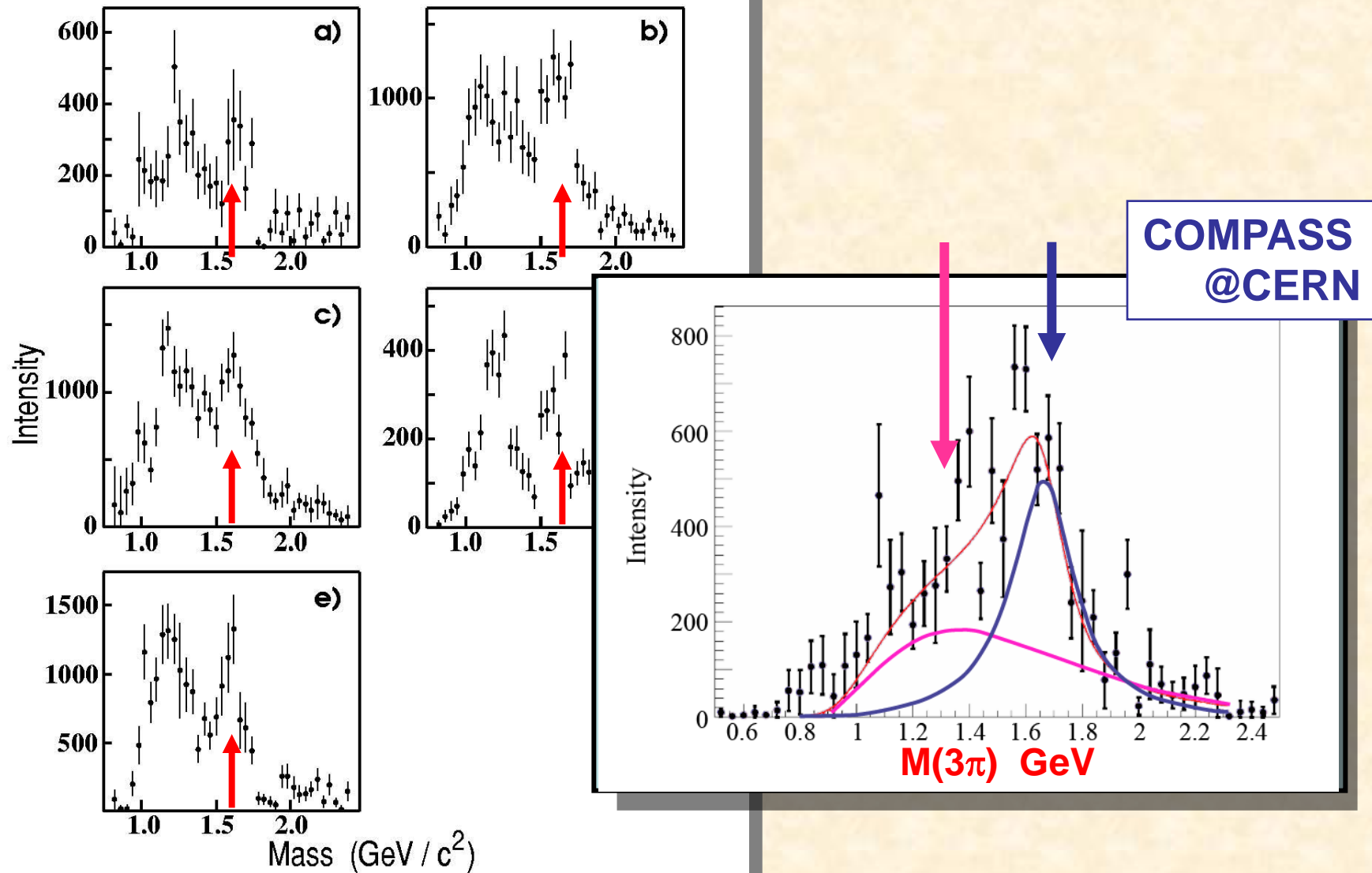
Mass ( $\text{GeV}/c^2$ )

# BNL-E852: $\pi^- p \rightarrow \pi^+ \pi^- \pi^- p$



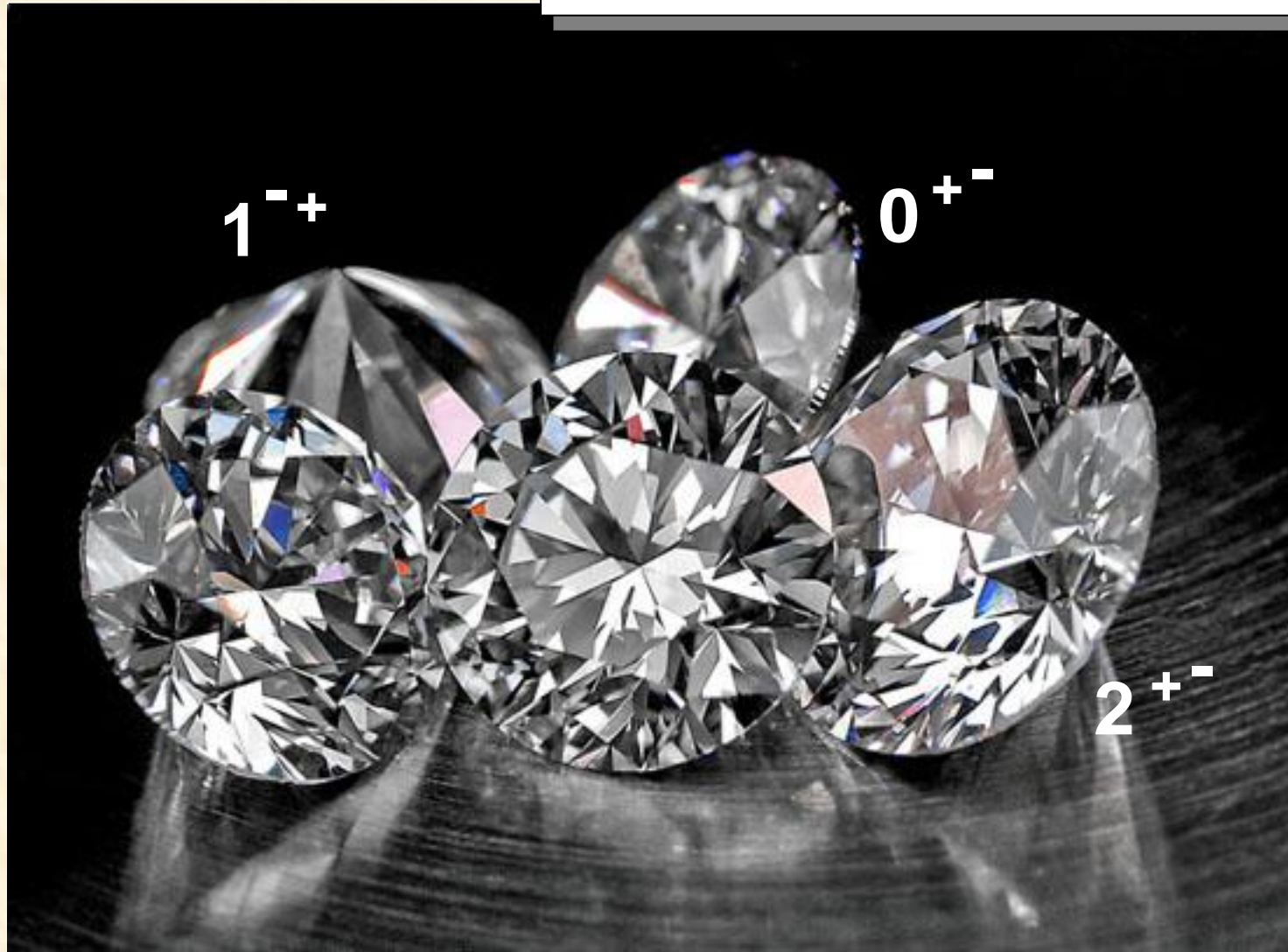
variation of  $1^{-+}$  with  $0^{++}$

# BNL-E852: $\pi^- p \rightarrow \pi^+ \pi^- \pi^- p$

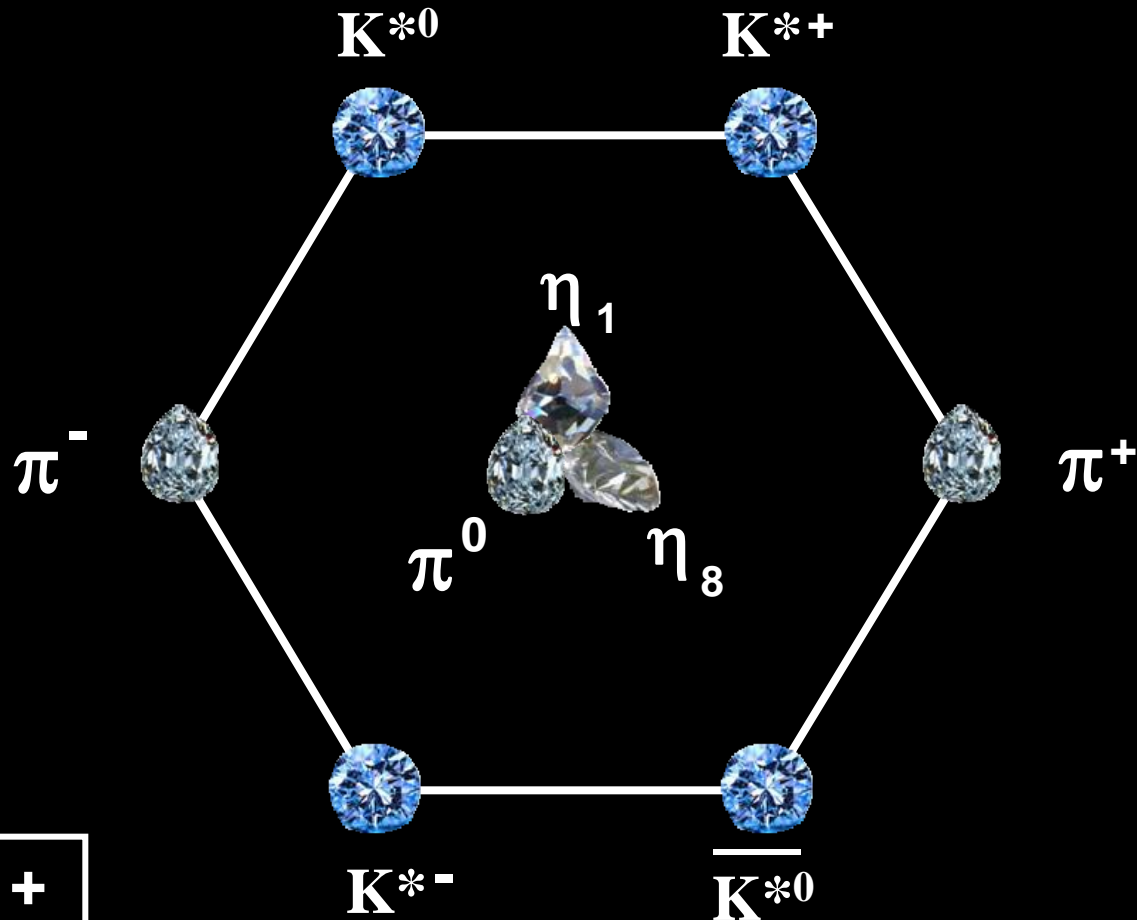




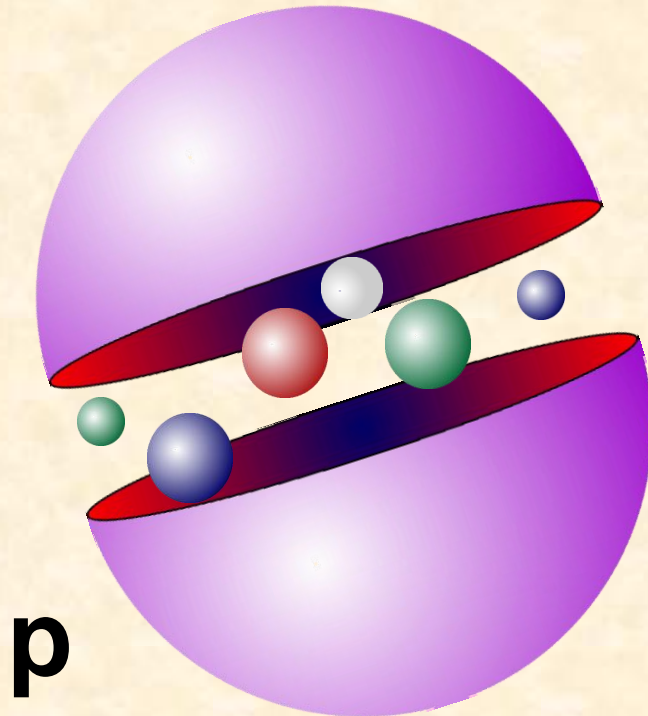
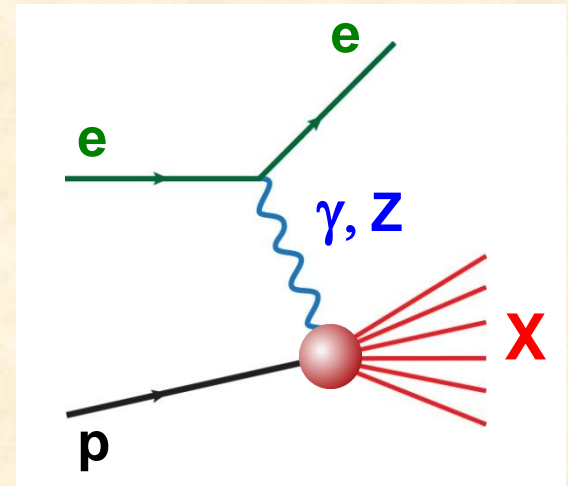
# Precision analysis tools

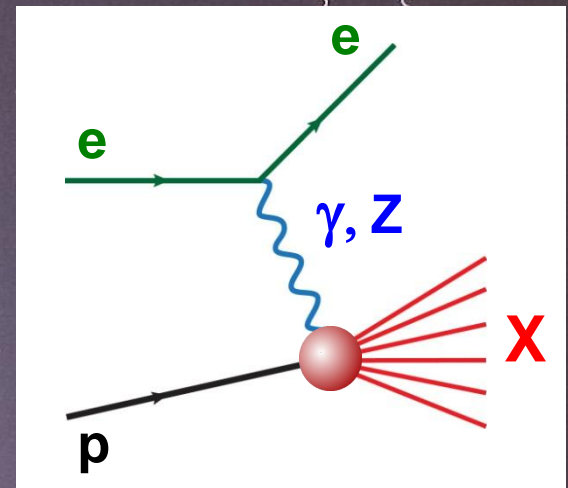
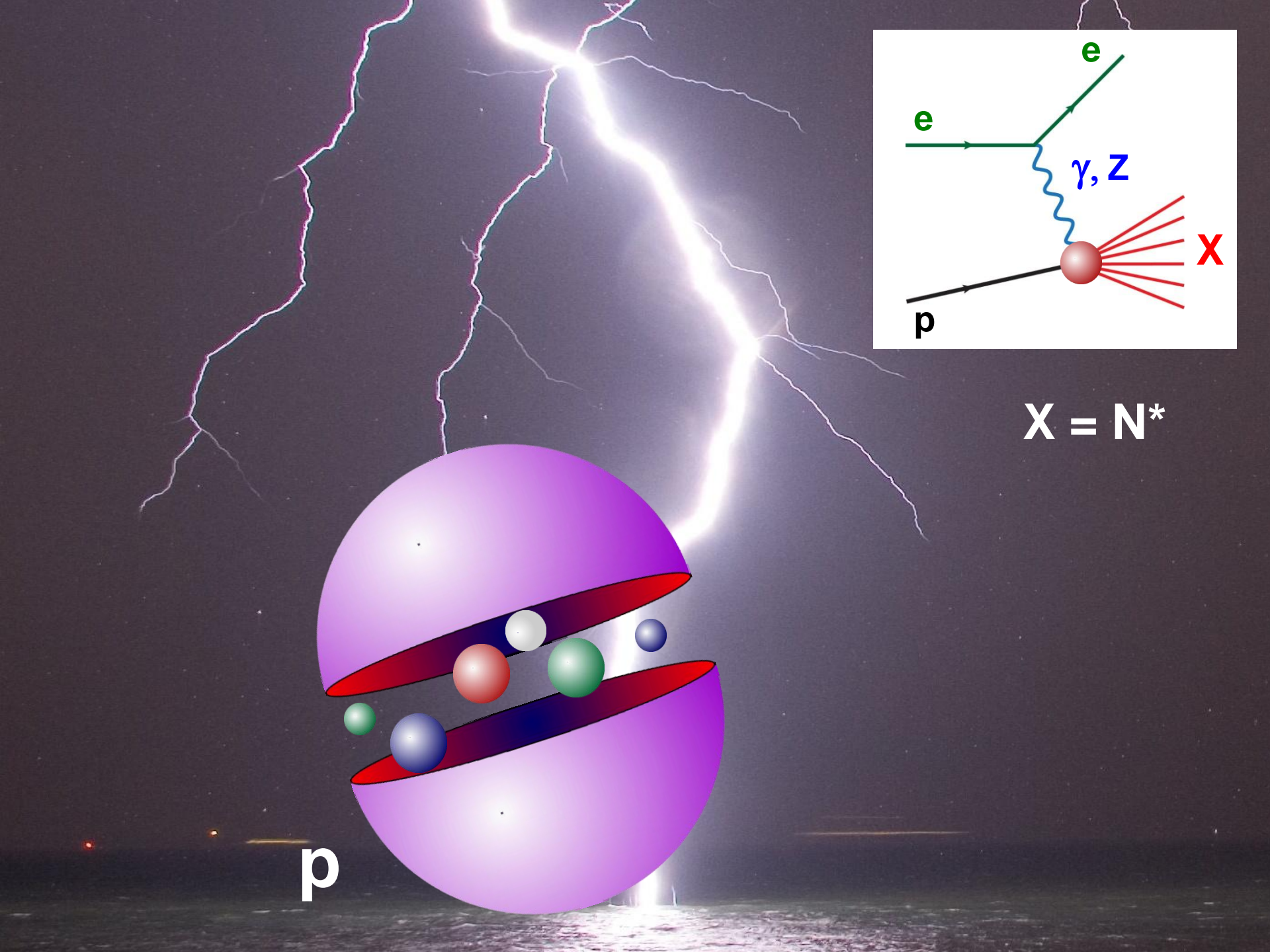


# Precision analysis tools

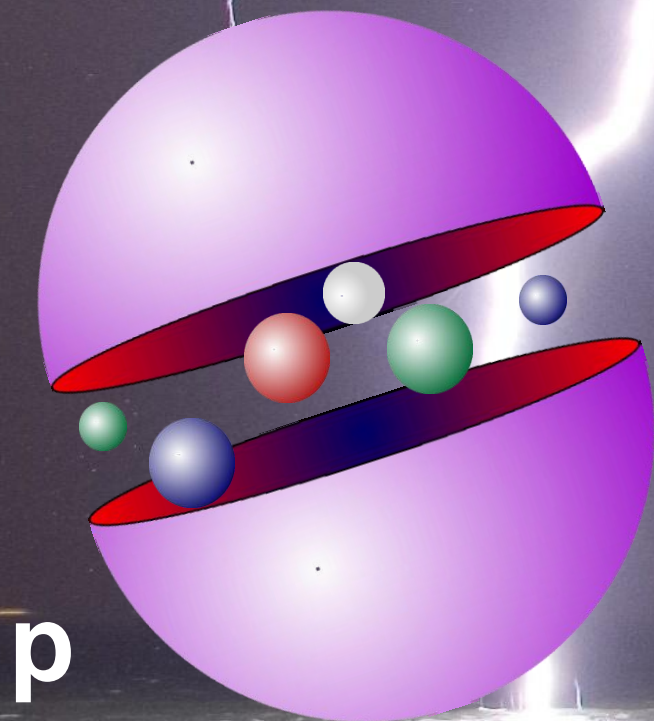


# probing excited baryons

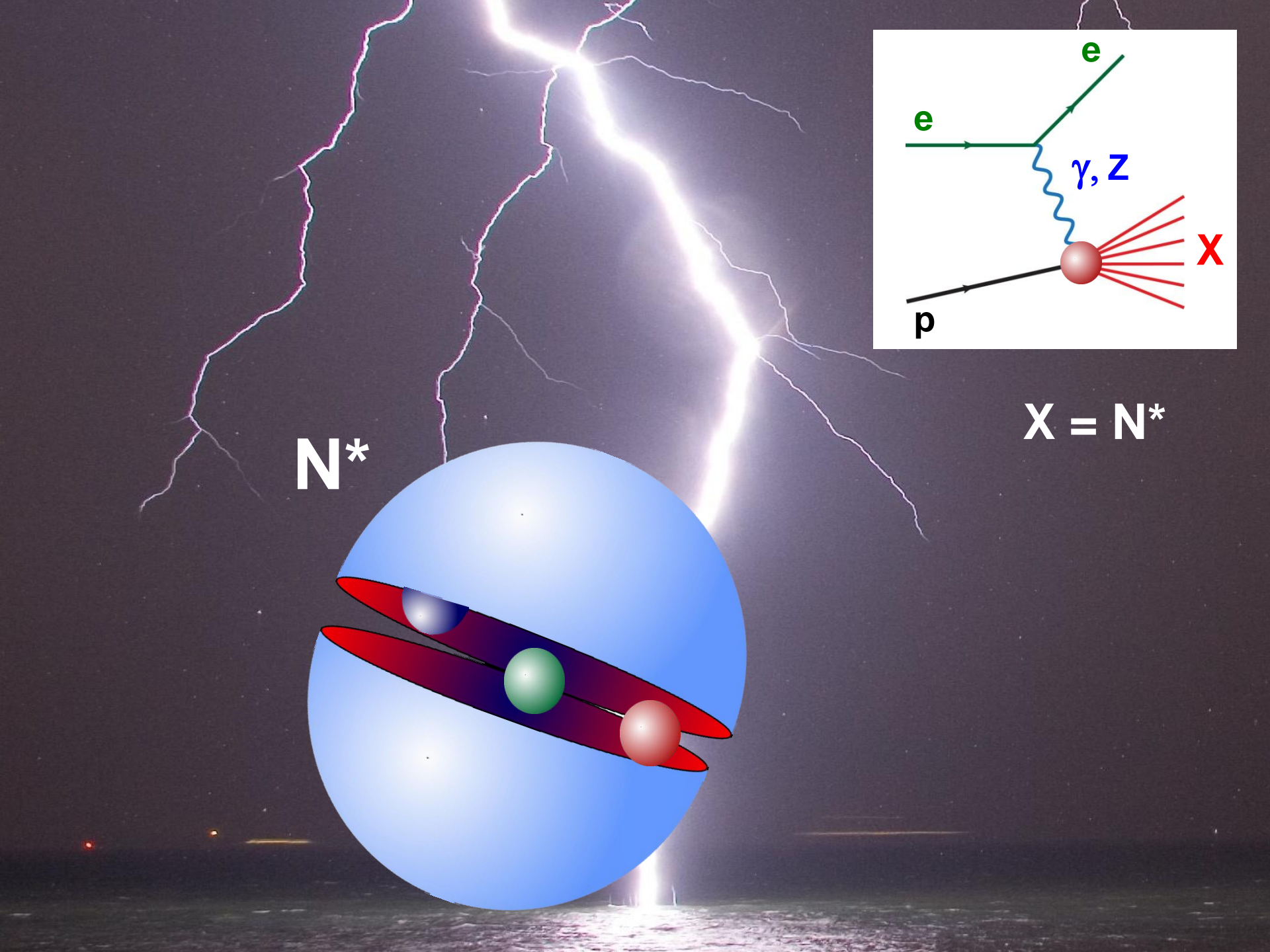




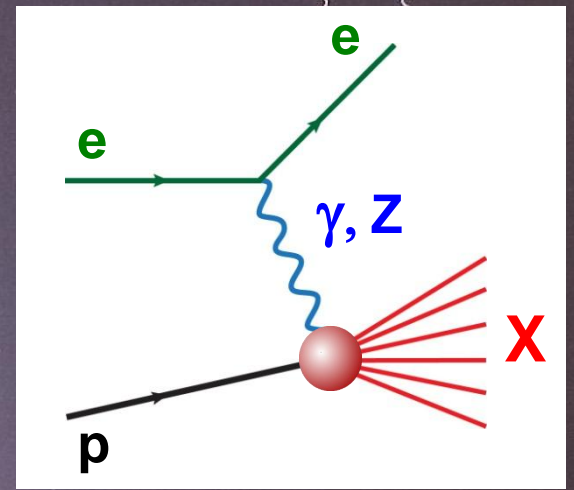
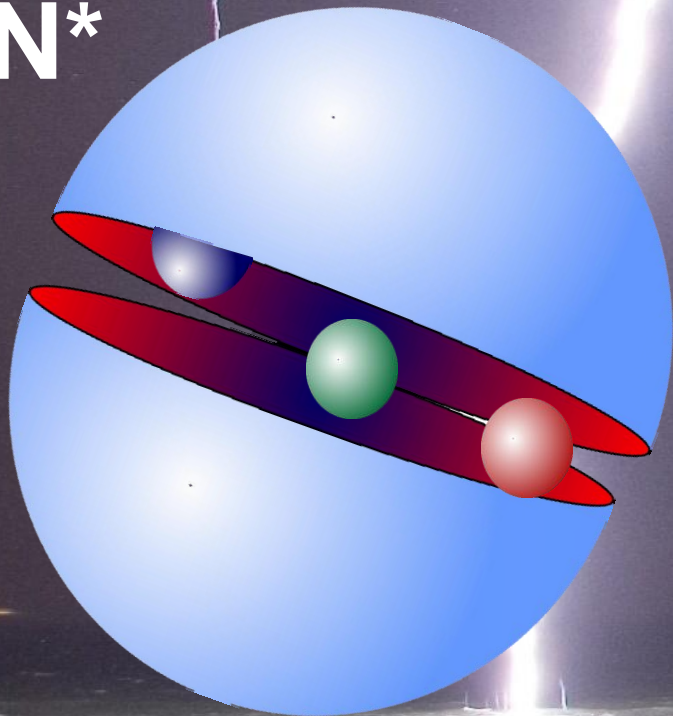
$$X = N^*$$



**p**

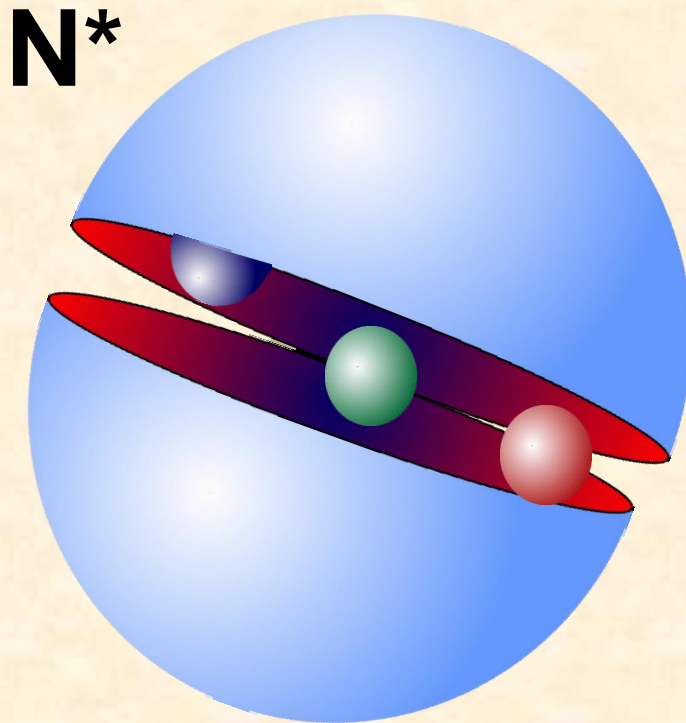
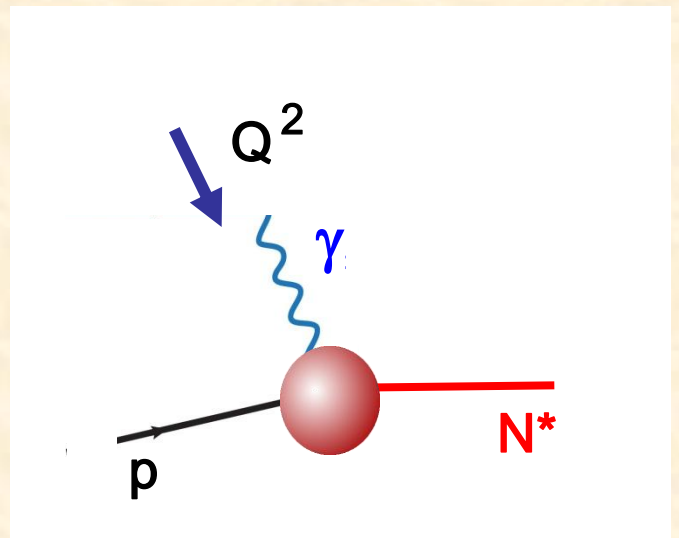


$N^*$

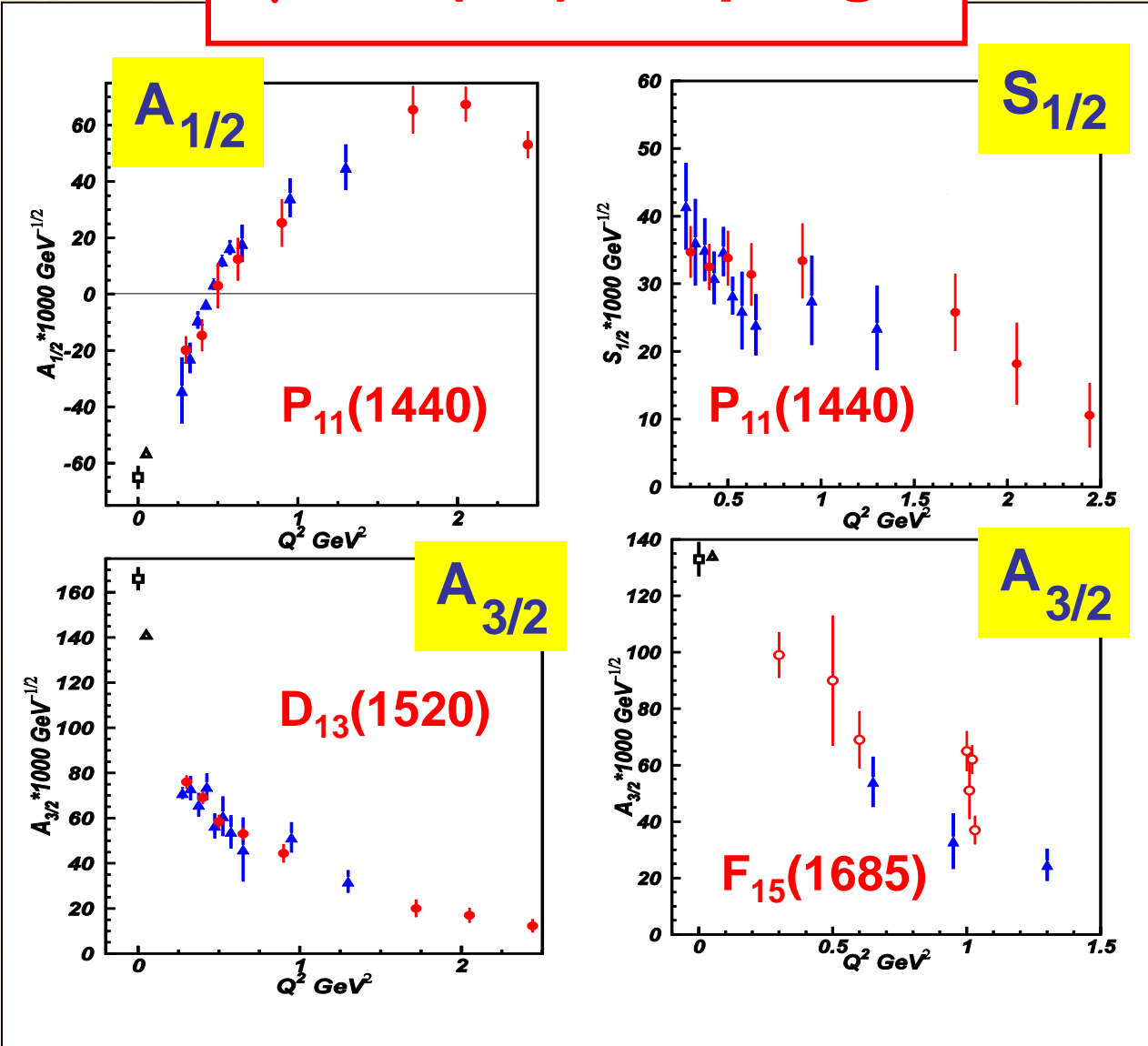


$X = N^*$

**Nucleon Resonance Structure in Exclusive  
Electroproduction at High Photon Virtualities  
with the CLAS 12 Detector Workshop**



# γ\*NN\*(Q<sup>2</sup>) couplings

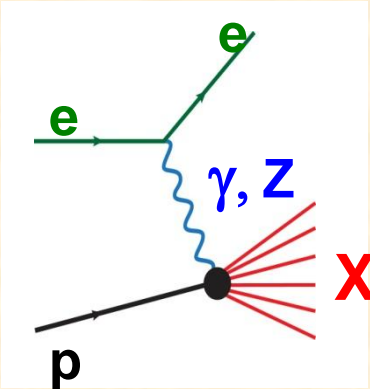


- $N\pi\pi$  CLAS preliminary.
- $N\pi$  Aznauryan et al.
- Burkert et al.
- $N\pi$   $Q^2 = 0$  Dugger et al.

Good agreement between  $N\pi$  and  $N\pi\pi$  channels.

**Moakeev**

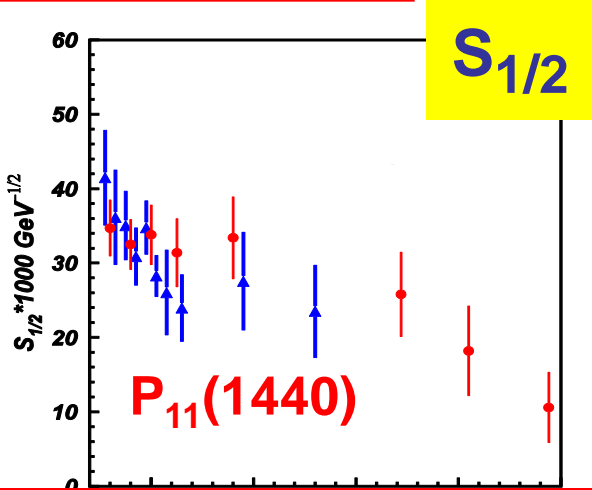
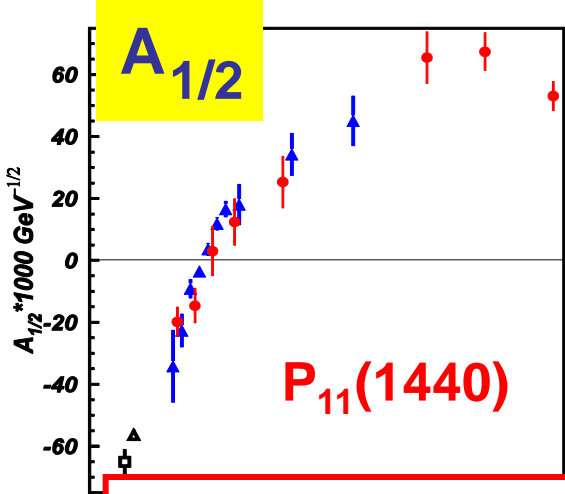
# γ\*NN\*(Q<sup>2</sup>) couplings



▲ Nπ CLAS preliminary.

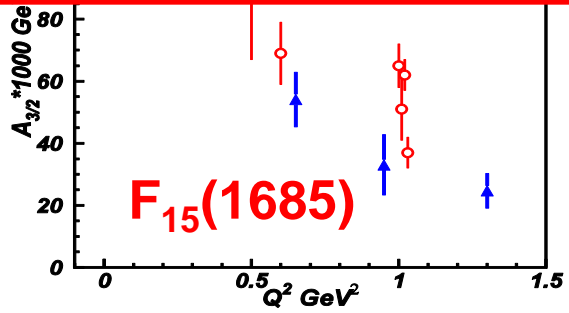
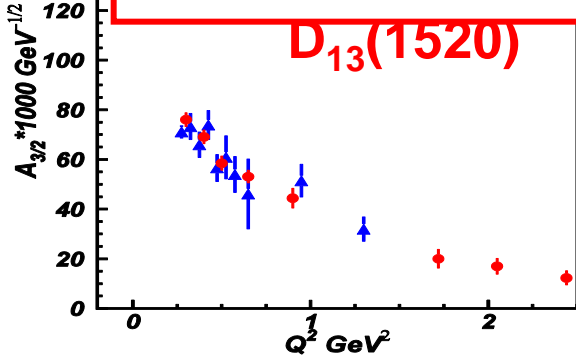
○ Burkert et al

△ Nπ Q<sup>2</sup> = 0 Dugger et al.



$$\mathcal{L}_{\text{QCD}} = \sum_{q=u,d,s,c,b} \bar{\psi}_q (i \gamma_\mu D^\mu - m_q) \psi_q - \frac{1}{4} \mathcal{F}_{\mu\nu} \mathcal{F}^{\mu\nu}$$

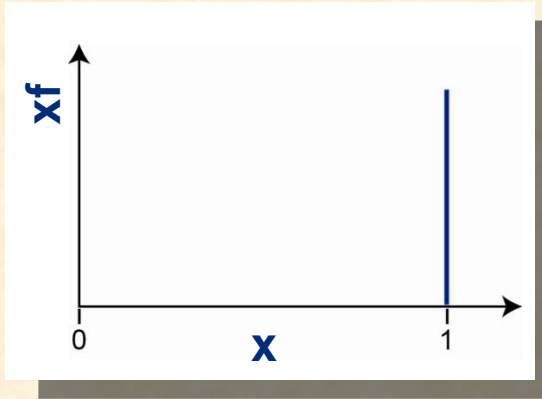
an et al.



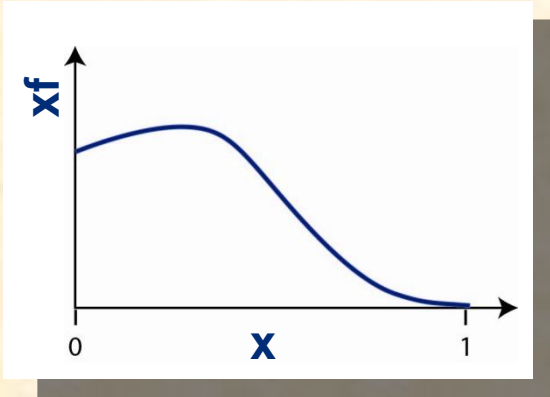
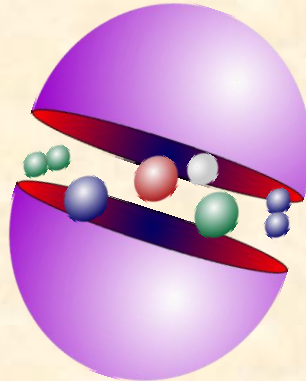
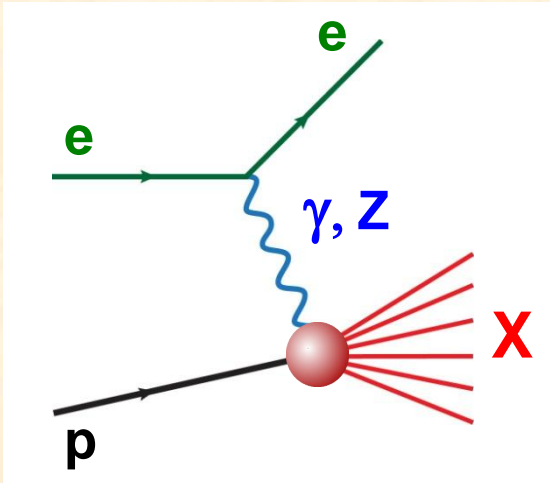
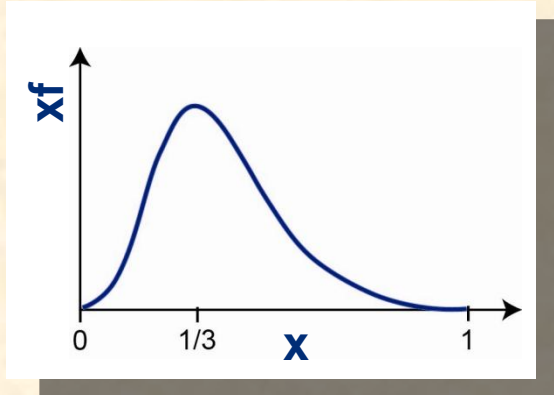
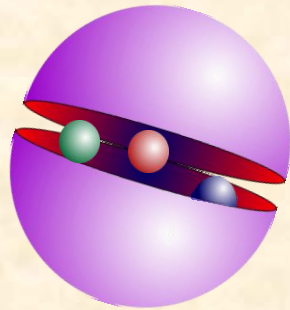
Good agreement between Nπ and Nππ channels.

Mokeyev

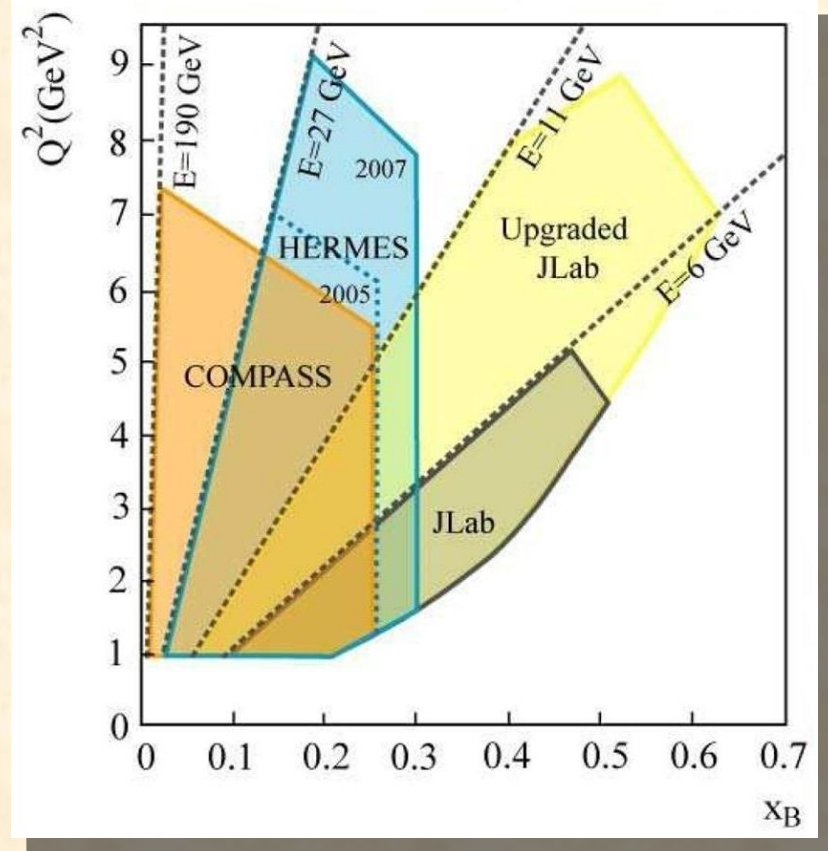
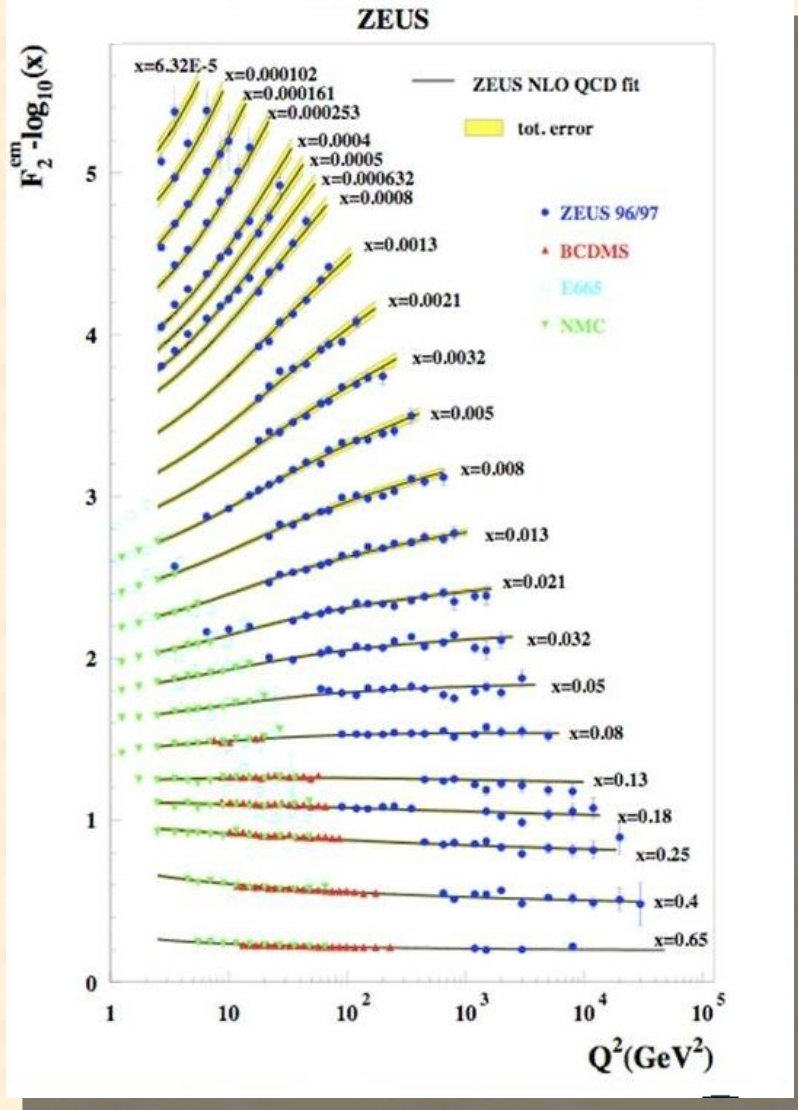




parton structure  
of the nucleon

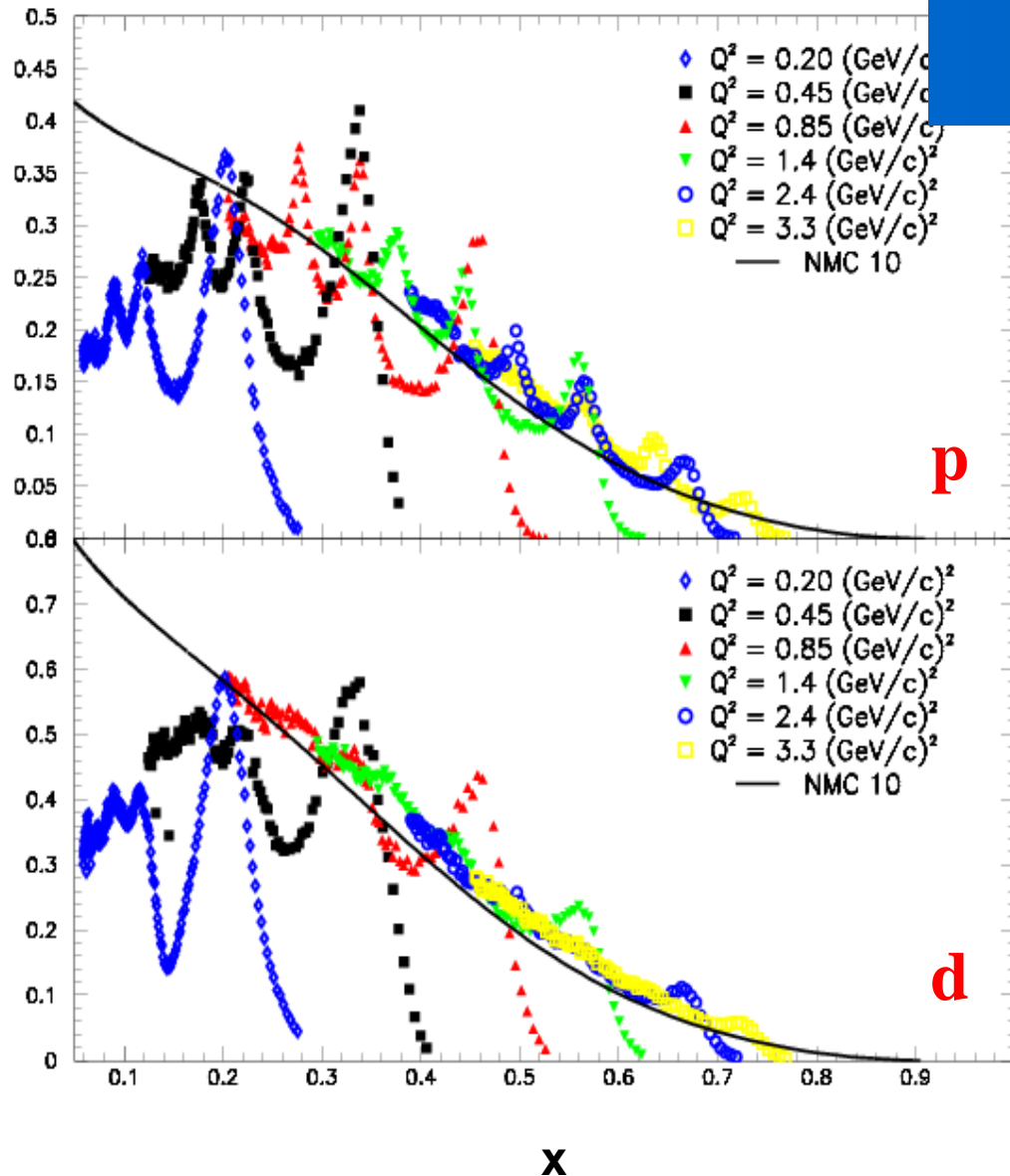


# Parton Distribution Functions

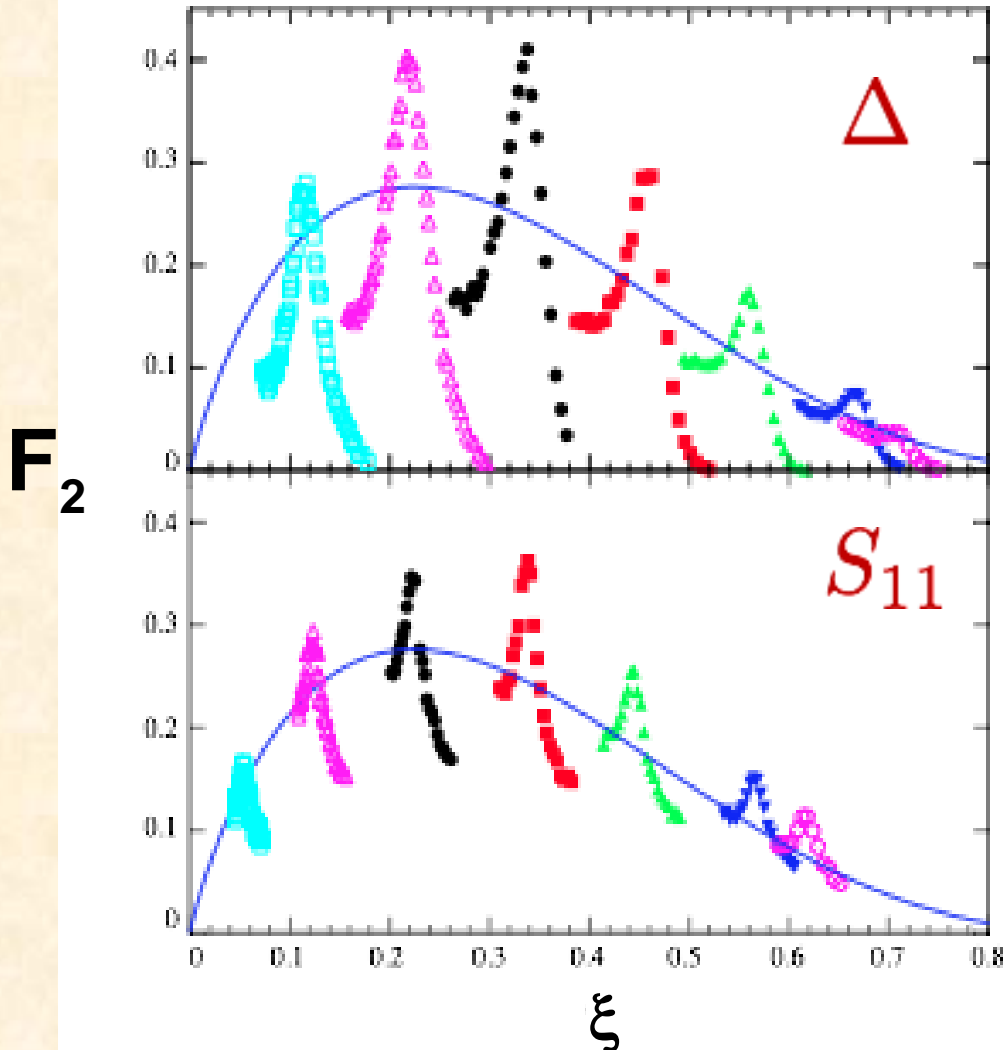


# quark-hadron duality

$F_2$



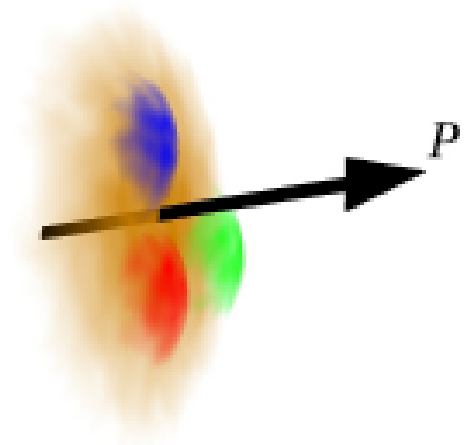
# quark-hadron duality



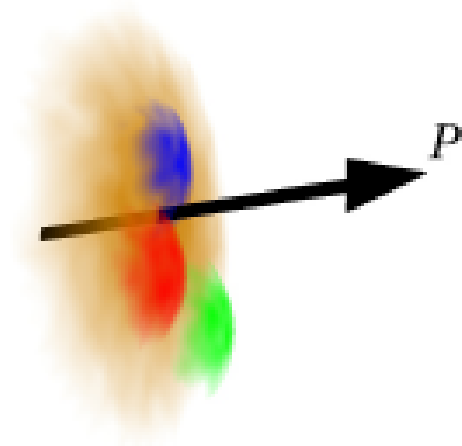
Nachtmann scaling variable

$$\xi = \frac{2x}{1 + \sqrt{1 + 4M^2x^2/Q^2}}$$

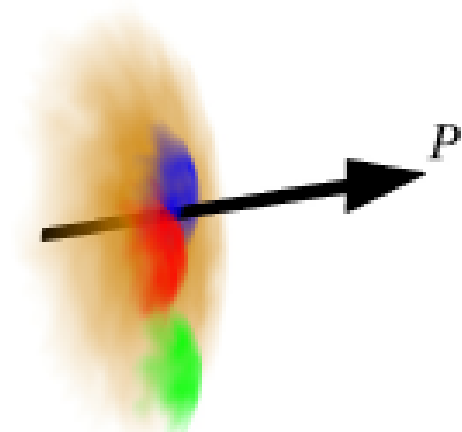
# Parton densities



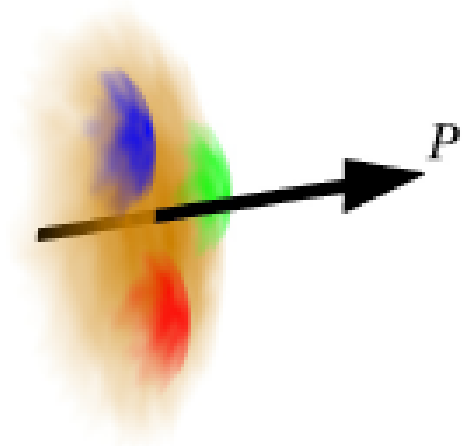
# Parton densities



# Parton densities

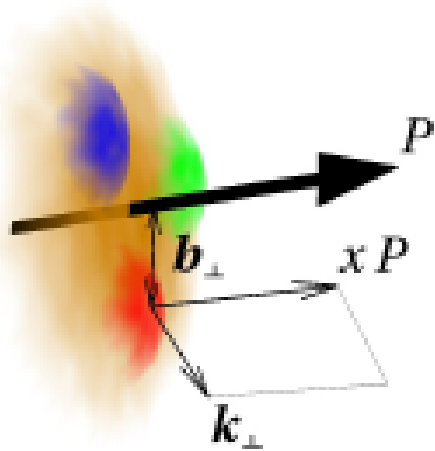


# Parton densities

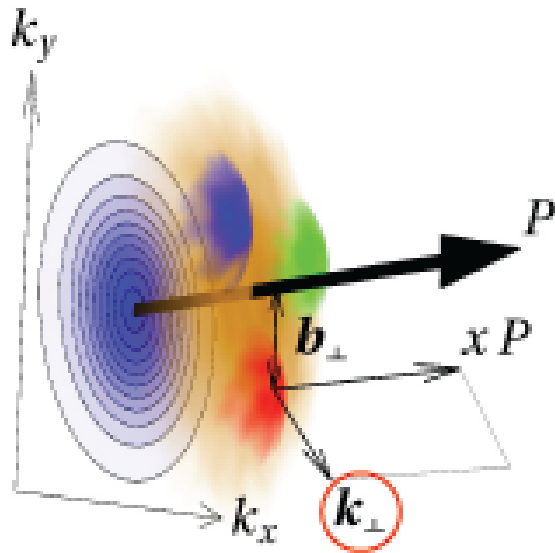




# Parton densities

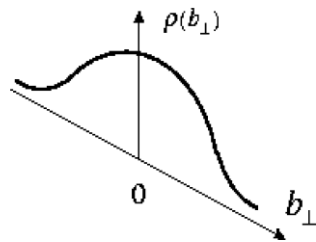
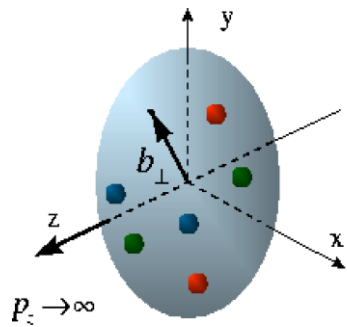


# Parton densities

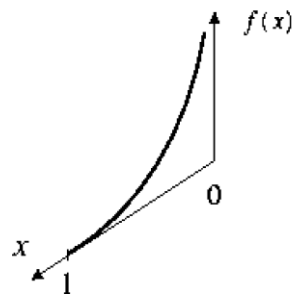
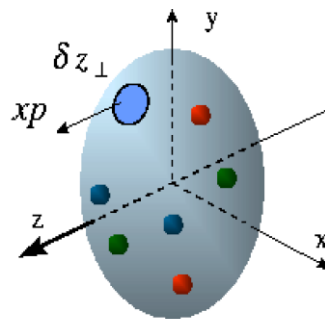


- $x$  (longitudinal momentum fraction)  $\Rightarrow$  **PDFs**
- $x, b_\perp$  (impact parameter)  $\Rightarrow$  **GPDs**
- $x, k_\perp$  (intrinsic transverse momentum)  $\Rightarrow$  **TMDs**

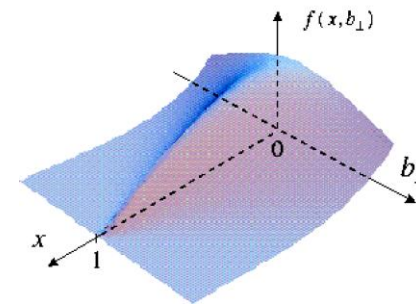
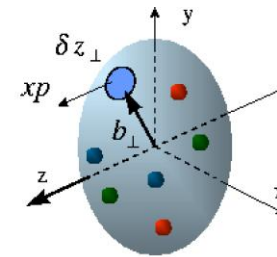
# Internal Landscape of the Hadron



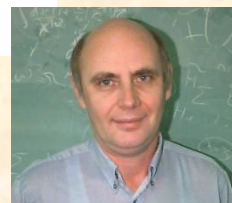
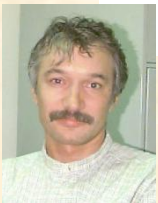
**Form Factors**  
transverse quark  
distribution in  
Coordinate space



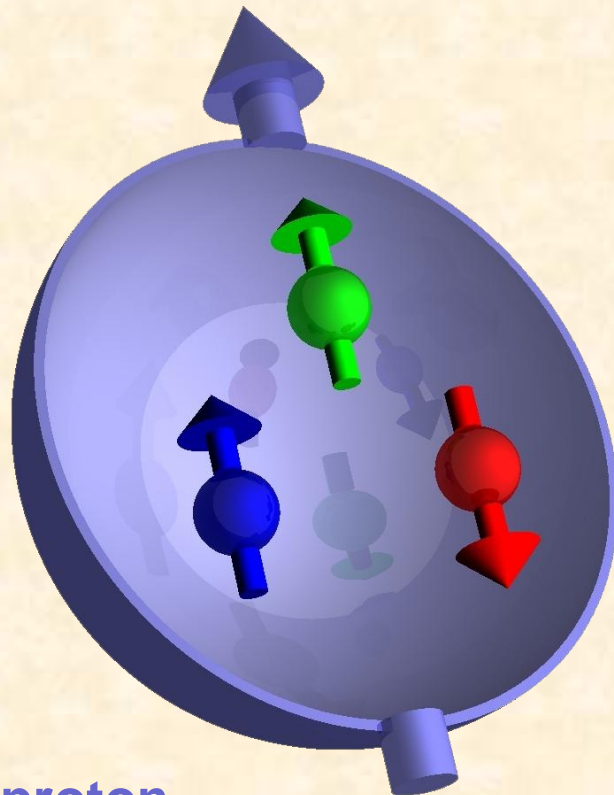
**Structure Functions**  
longitudinal  
quark distribution  
in momentum space



**GPDs**  
Fully-correlated  
quark distribution in  
both coordinate and  
momentum space



# Internal Landscape of the Hadron



proton

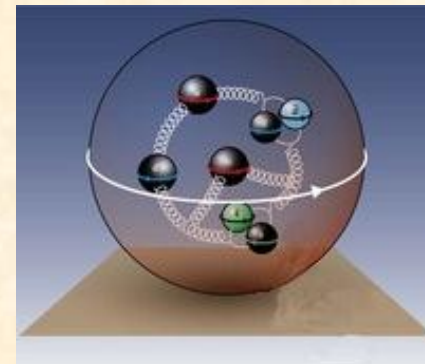
**Spatial**

**Momentum**

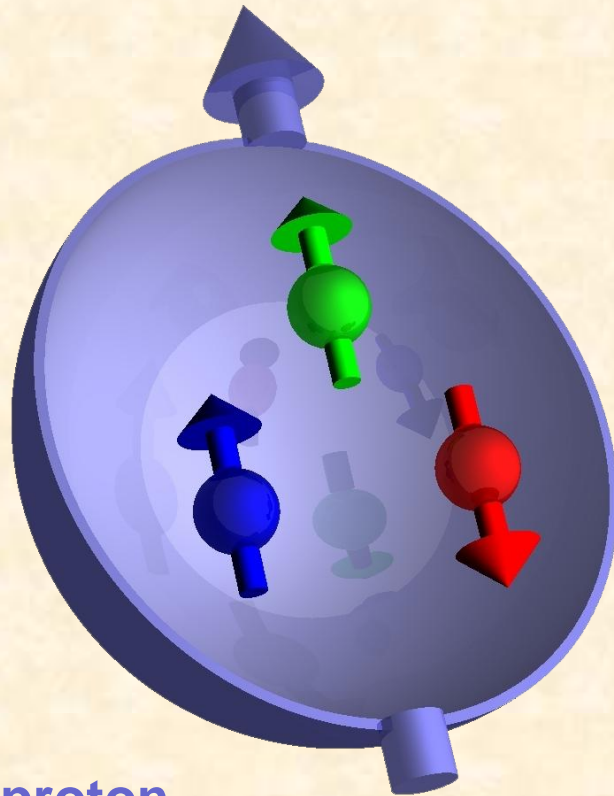
**Flavor**

**Angular momentum**

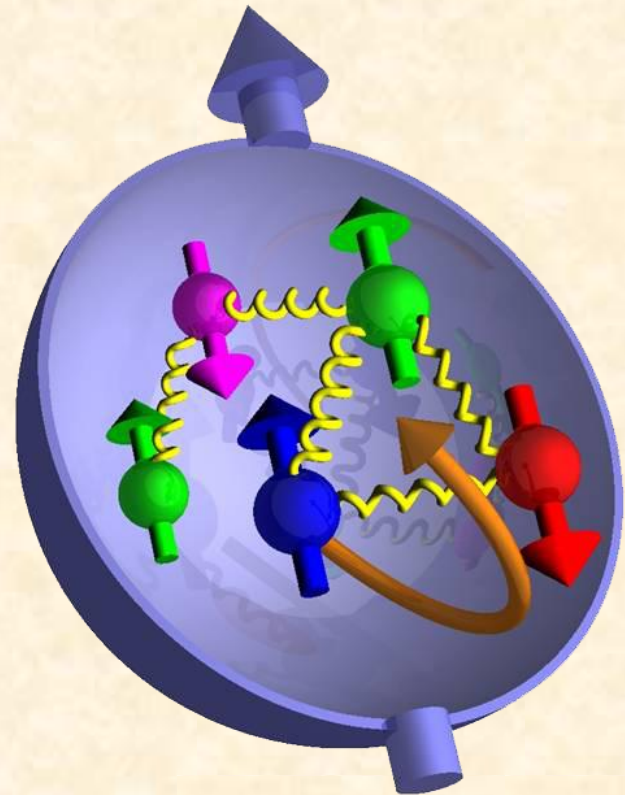
**Parton Distribution Functions**



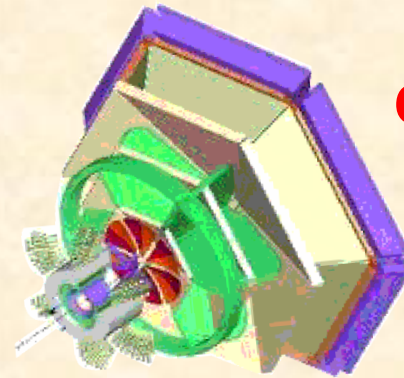
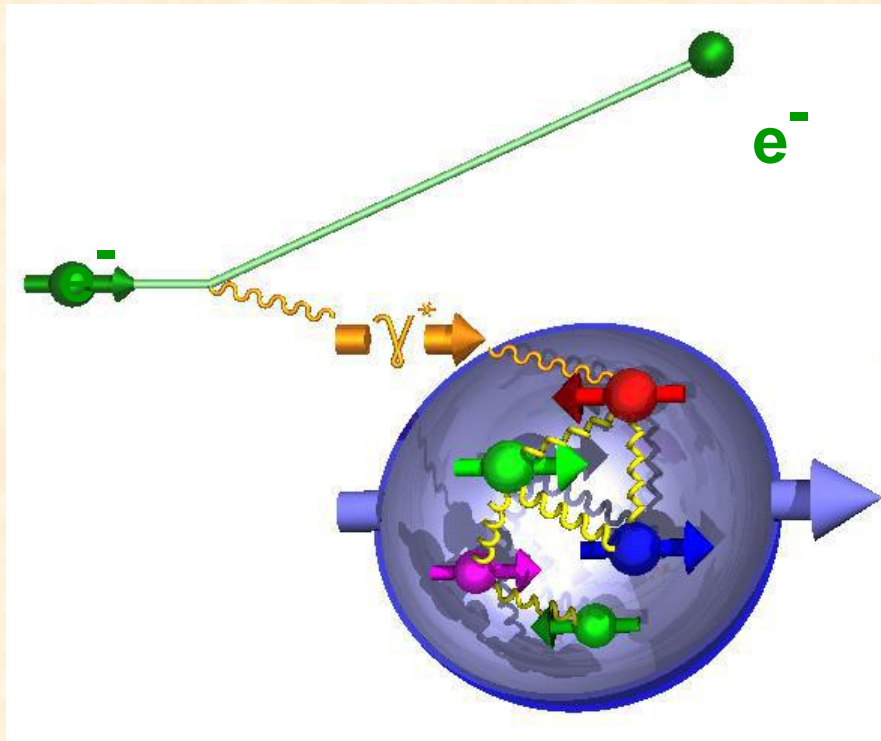
# Spin of the proton



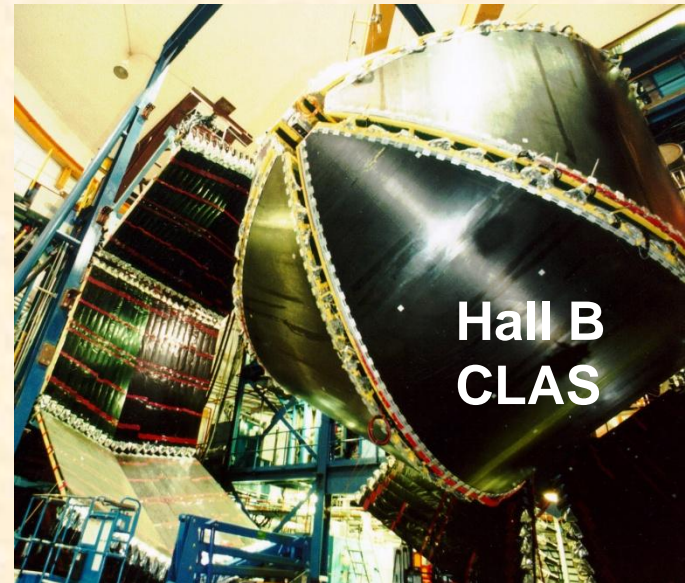
proton



# Semi-Inclusive Deep Inelastic Scattering

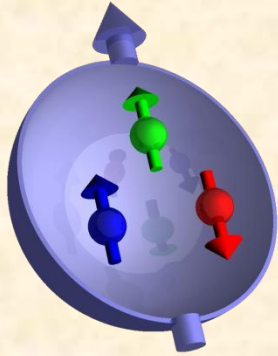


**CLAS12**



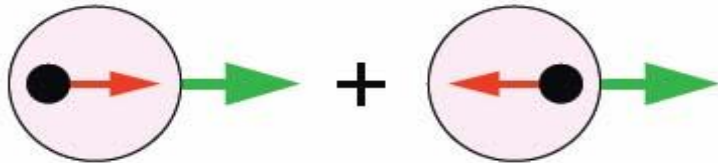
**Hall B  
CLAS**

# Spin of the proton

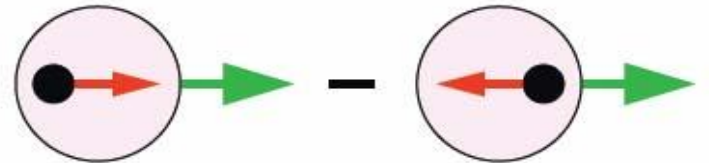


$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$

$$q(x) = q^\uparrow(x) + q^\downarrow(x)$$



$$\Delta q(x) = q^\uparrow(x) - q^\downarrow(x)$$



$$\Delta\Sigma \equiv \int dx (\Delta u(x) + \Delta d(x) + \Delta s(x) + \Delta\bar{u}(x) + \Delta\bar{d}(x) + \Delta\bar{s}(x))$$

evolves with  $Q^2$  : here  $Q^2 > 5 \text{ GeV}^2$

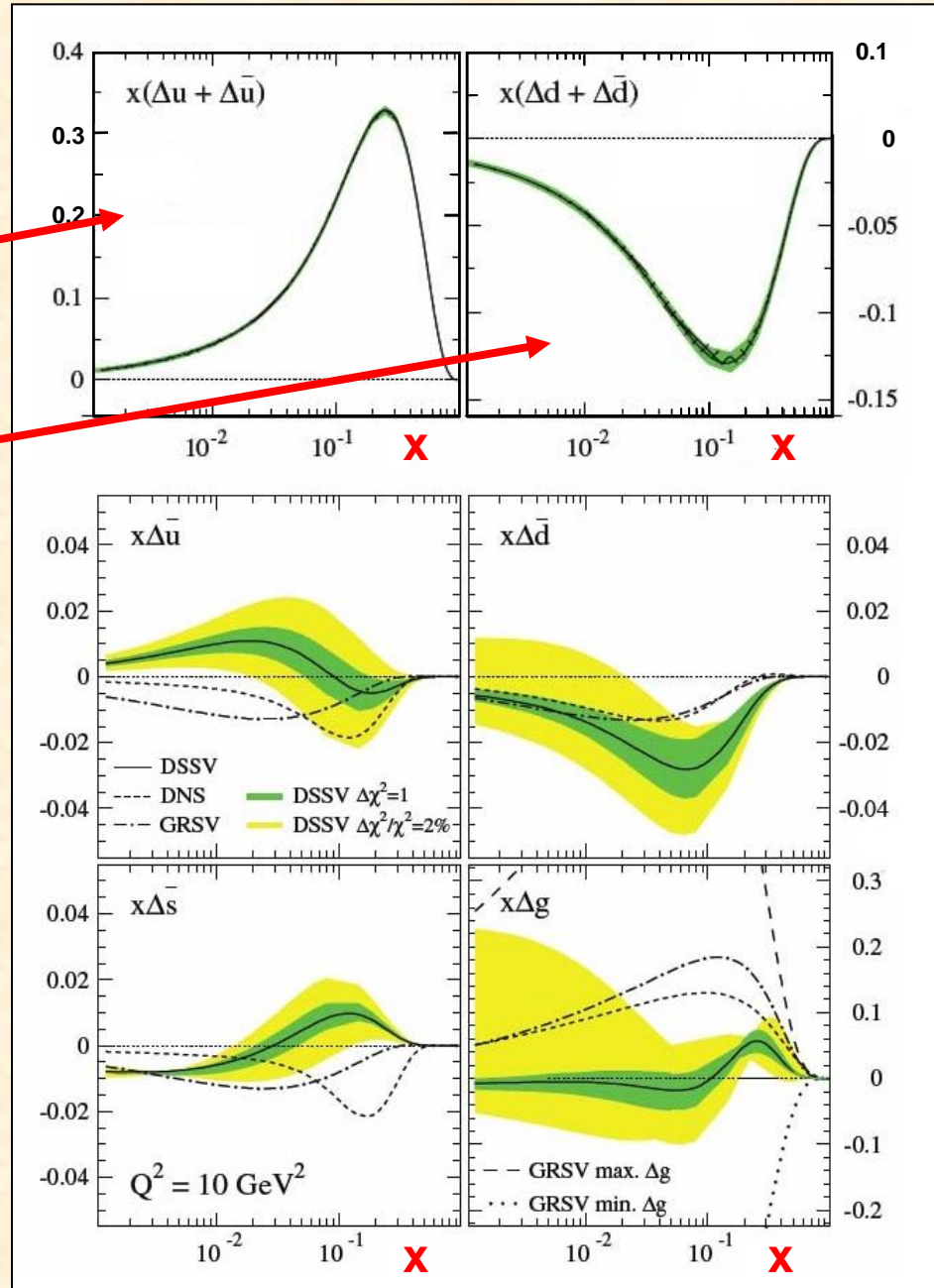
$\sim 20\%$

# Spin of the proton

$$\int dx \Delta(u + \bar{u}) = +0.81$$

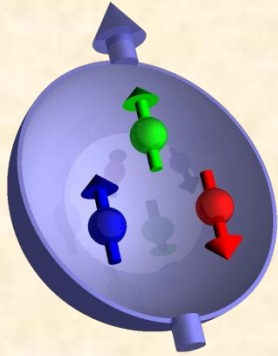
$$\int dx \Delta(d + \bar{d}) = -0.46$$

	meas: x > .001	extrap: all x	error
$\Delta\Sigma$	0.37	<b>0.24</b>	+0.04 -0.06
$\Delta\bar{u}$	0.03	<b>0.04</b>	$\pm 0.06$
$\Delta\bar{d}$	-0.09	<b>-0.12</b>	$\pm 0.09$
$\Delta s$	-0.01	<b>-0.06</b>	$\pm 0.03$
$\Delta G$	0.01	<b>-0.08</b>	+0.7 -0.3





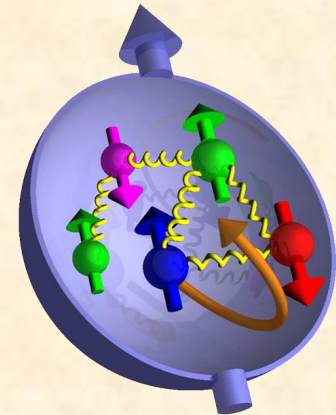
# Spin of the proton



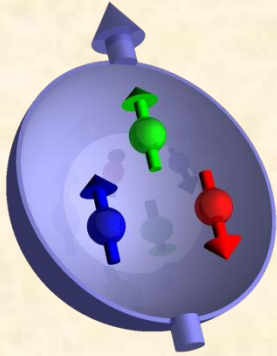
$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$

$$\Delta G \equiv \int dx \Delta g(x)$$

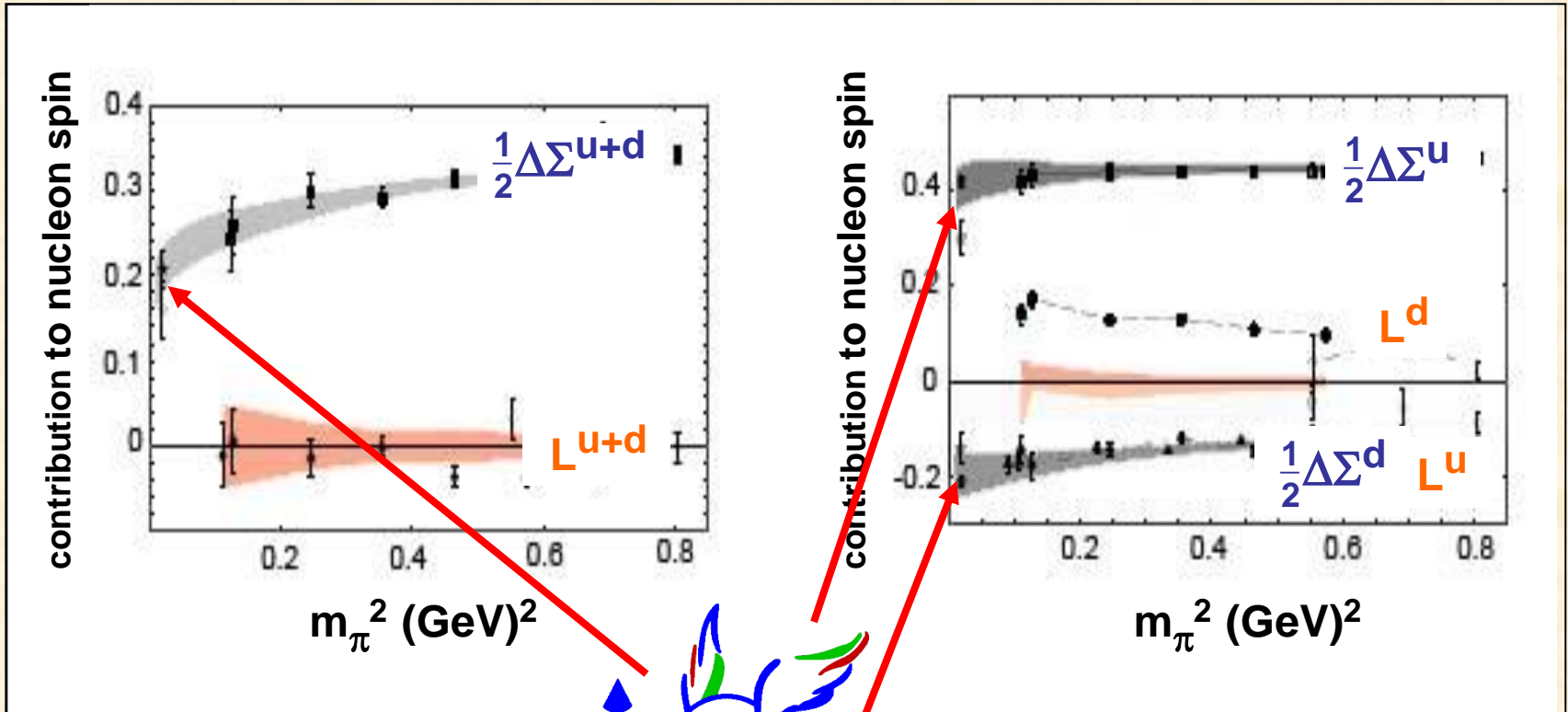
$$L_z \equiv L_q + L_g$$



# Spin of the proton: Lattice v Experiment



$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$



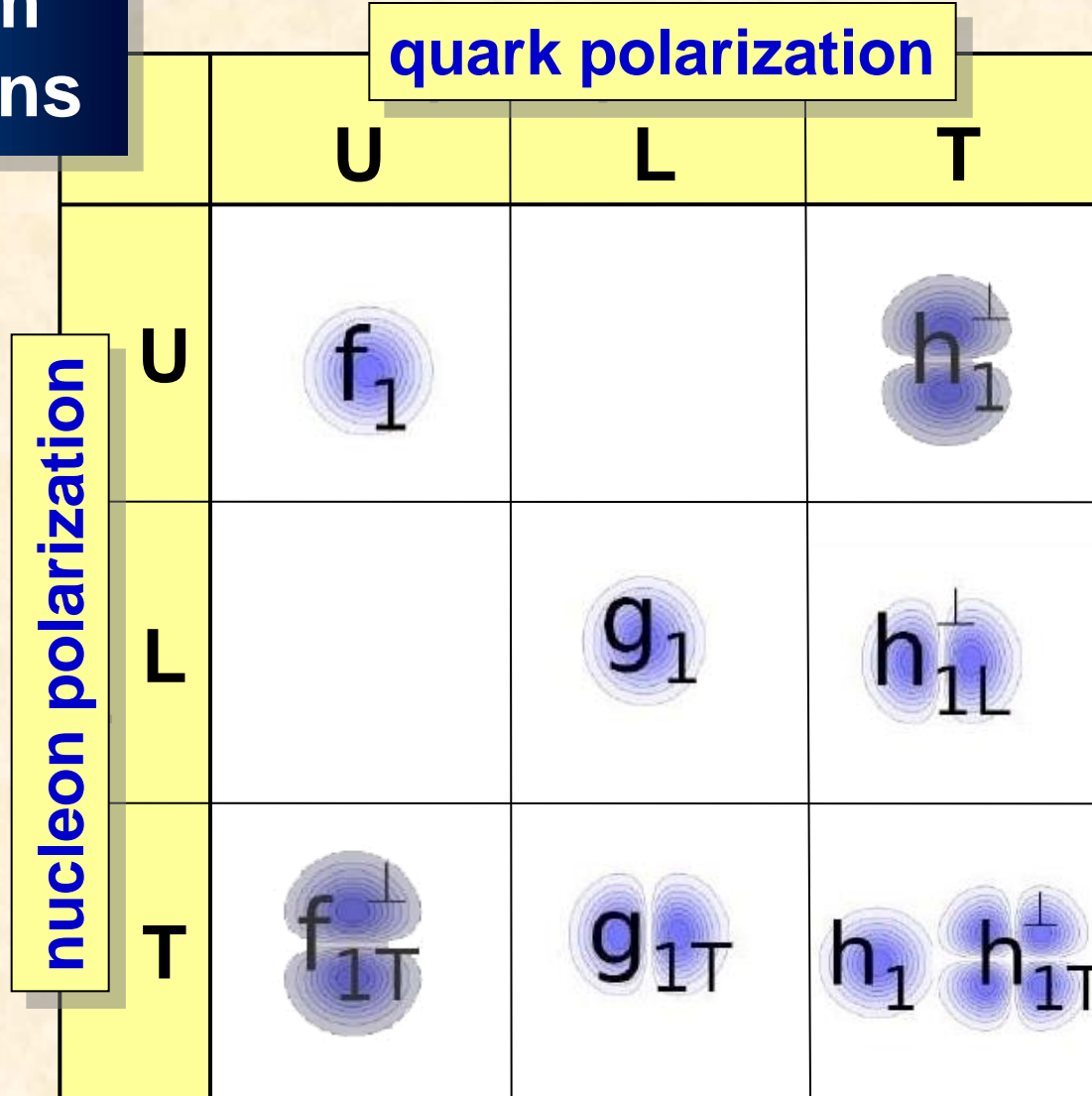
LHPC, Haegler *et al.*



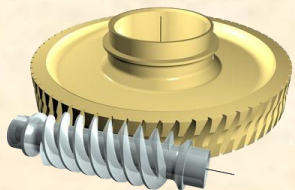
No disconnected contributions

# Transverse Momentum Distributions

quark polarization



nucleon polarization

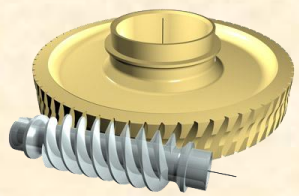
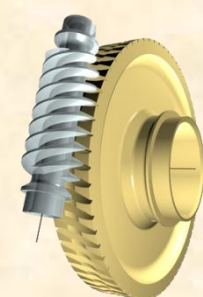


at leading twist

# Transverse Momentum Distributions

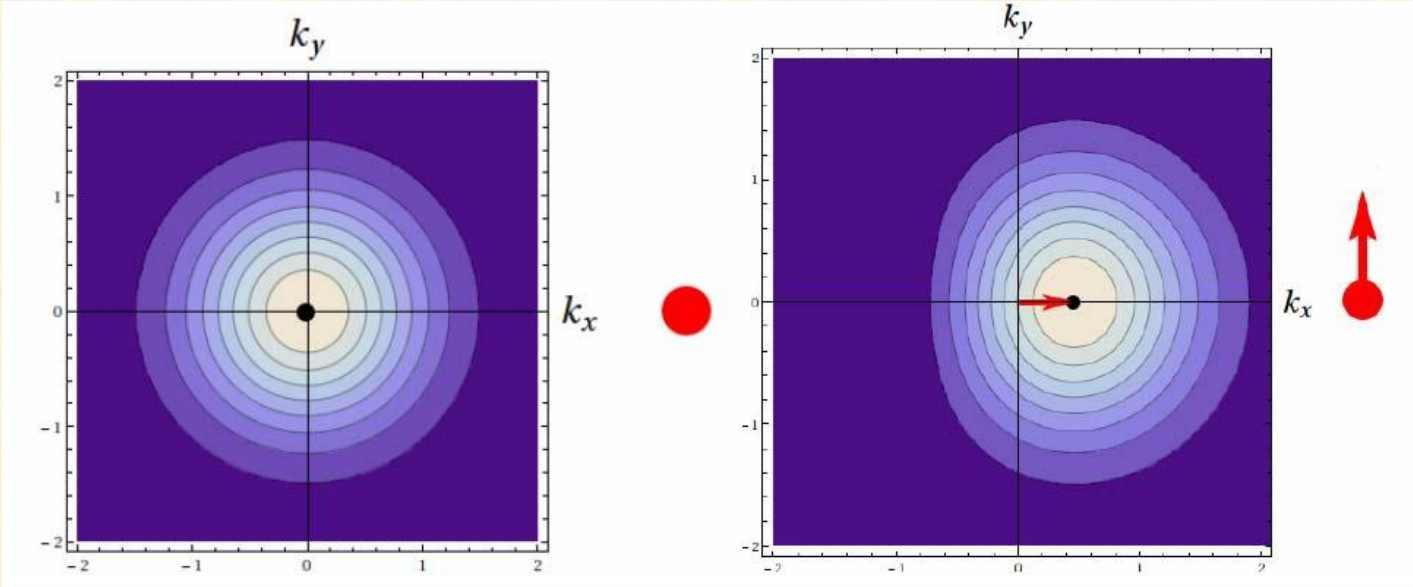
quark polarization

		quark polarization		
		U	L	T
nucleon polarization	U	$f_1$		$h_1$ Boer-Mulders
	L		$g_1$ helicity	$h_{1L}$ worm-gear
	T	$f_{1T}$ Sivers	$g_{1T}$ worm-gear	$h_1$ $h_{1T}$ transversity pretzelosity

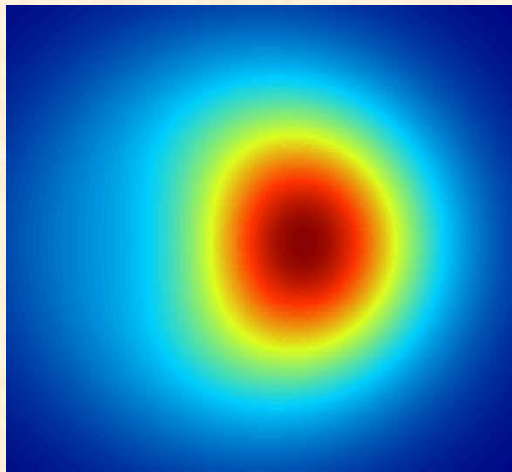


transversity      pretzelosity

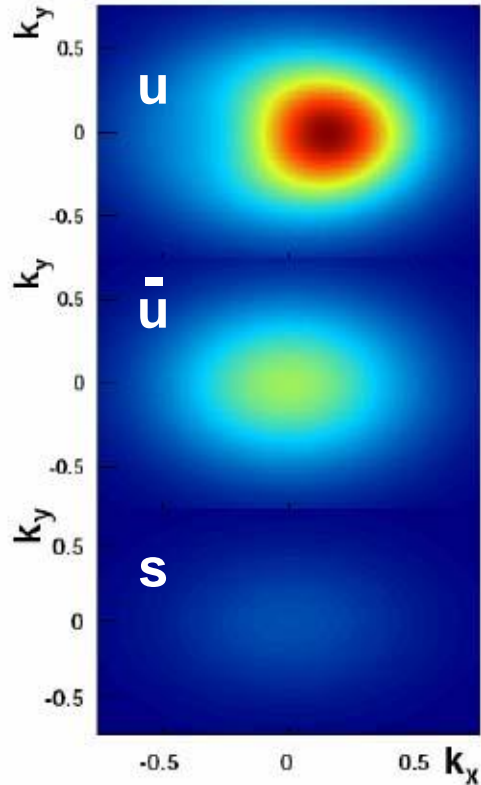
$$f(x, z, Q^2, p_T)$$



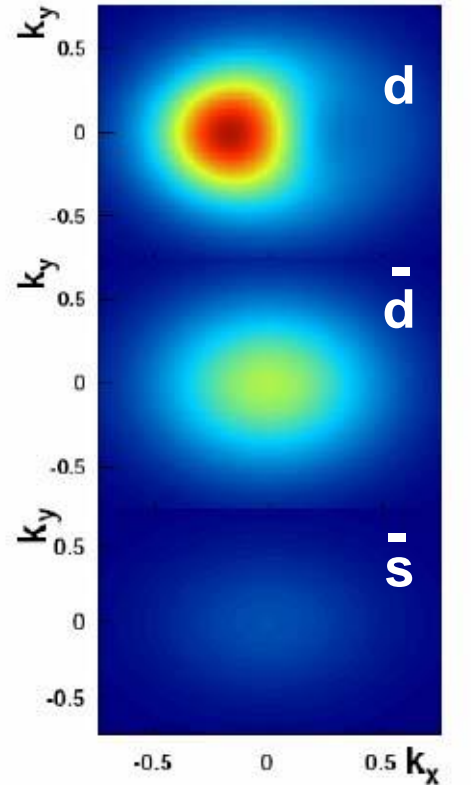
experiment



$\times f_1(x, k_T, S_T)$

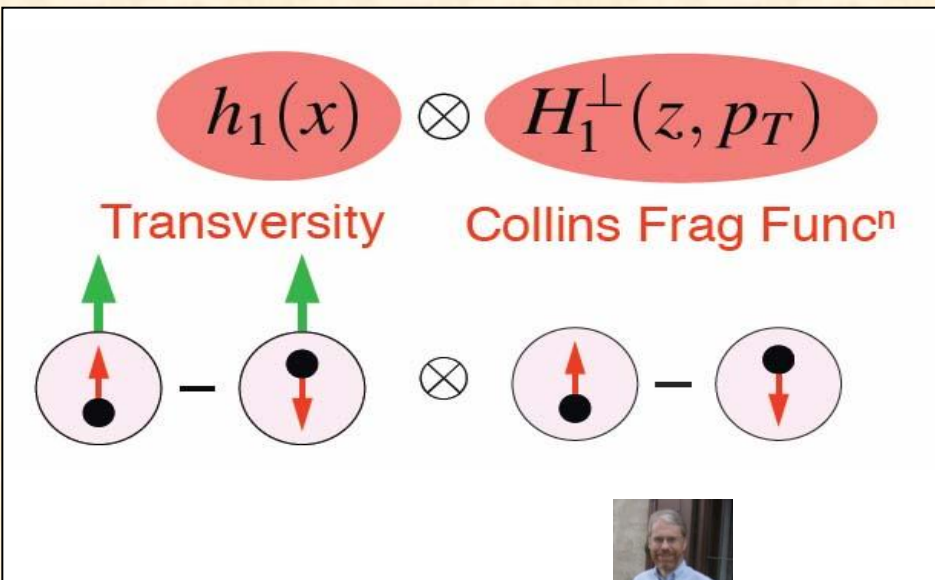


$k_x$  (GeV)

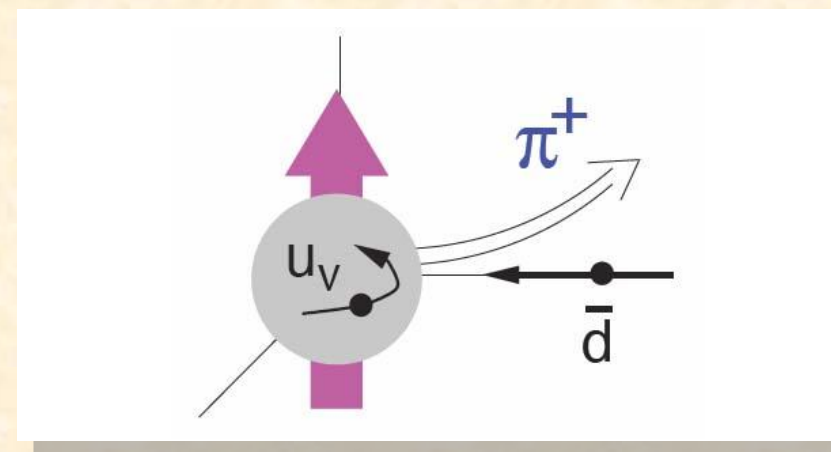
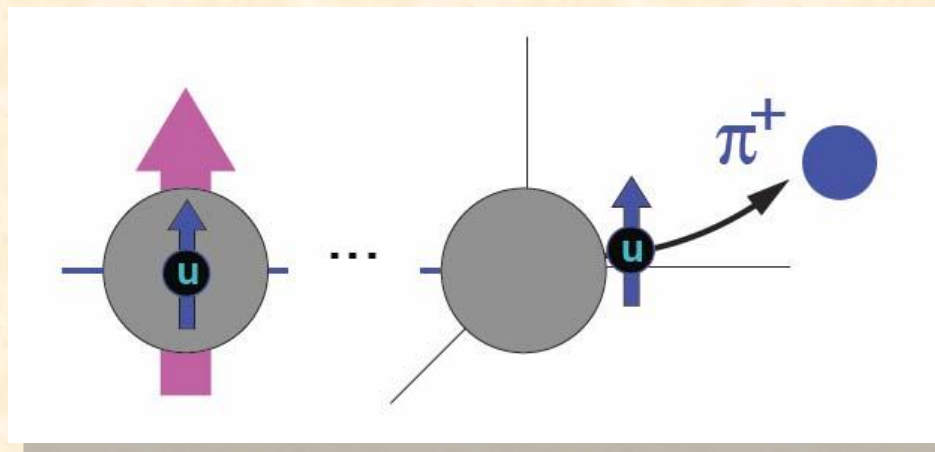
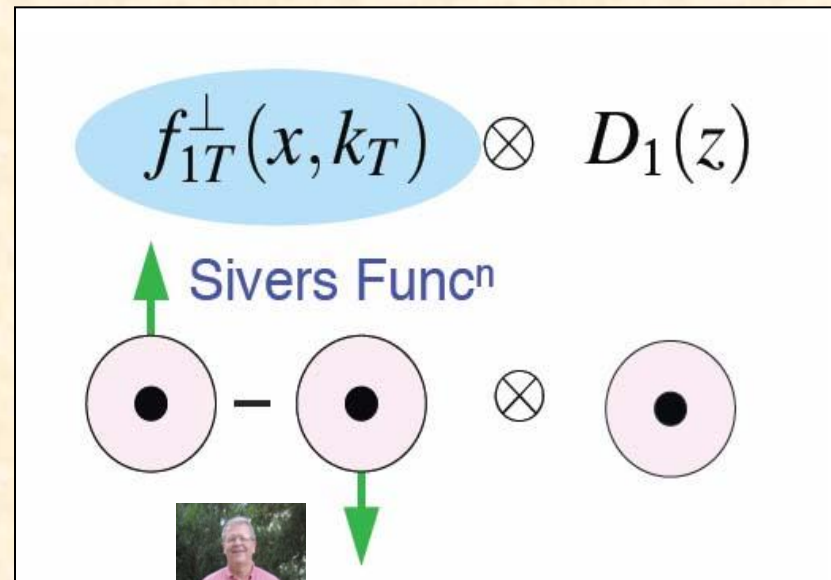


$k_x$  (GeV)

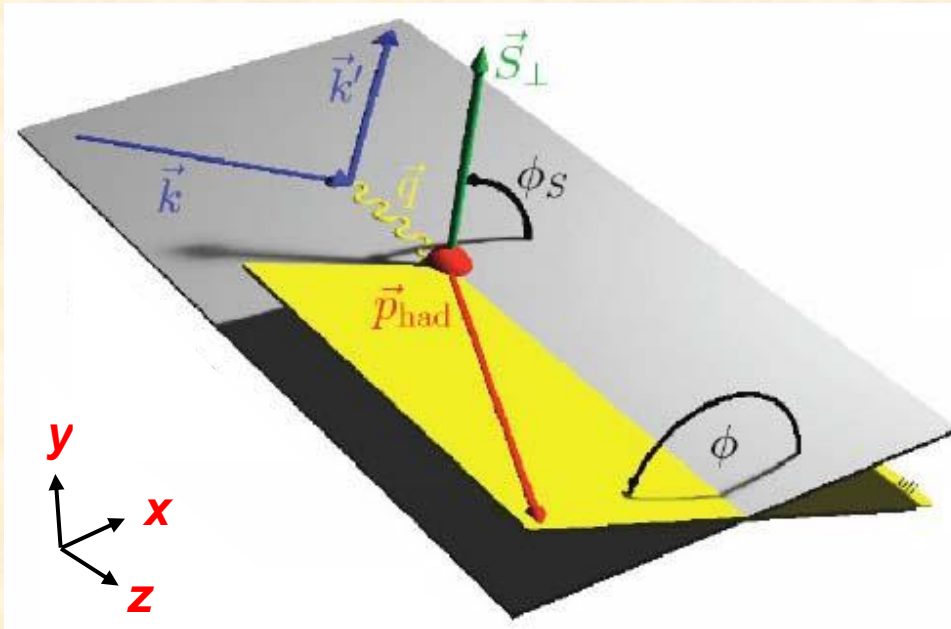
# Collins Frag Fn



# Sivers Dist Fn



# $\pi$ electroproduction with transverse target



- $(\phi_h^l - \phi_S^l) =$  angle of pion relative to **initial** quark spin
- $(\phi_h^l + \phi_S^l) =$  angle of pion relative to **final** quark spin

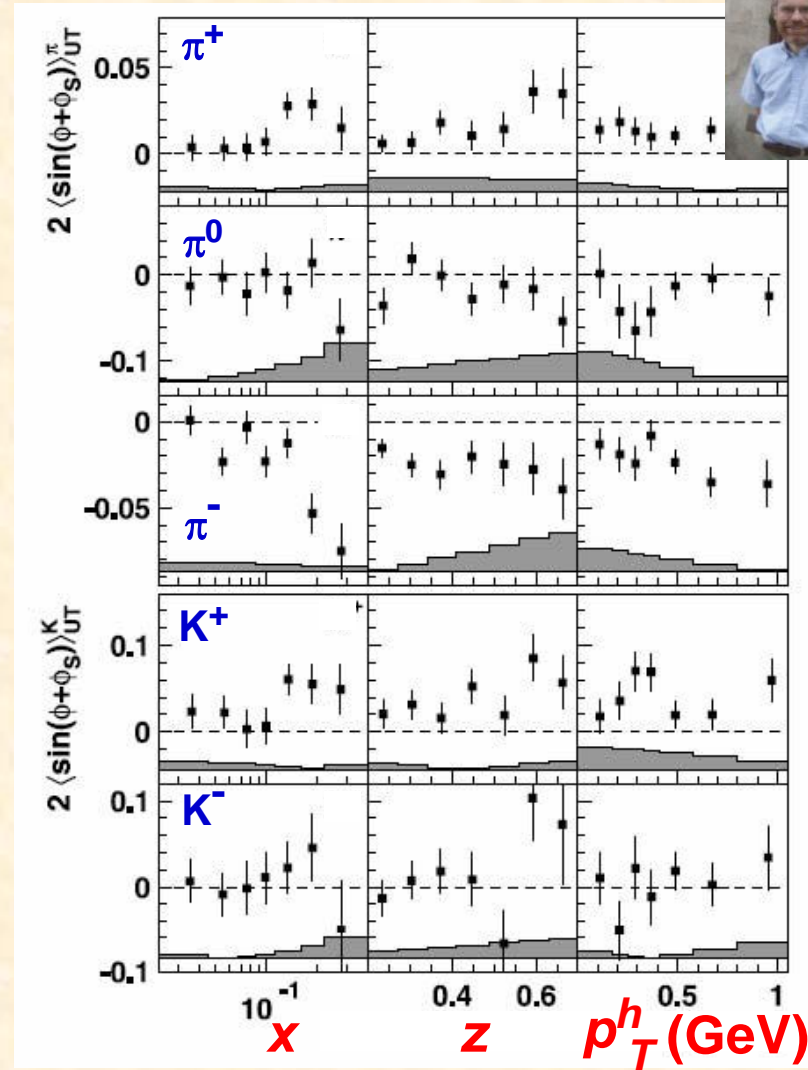
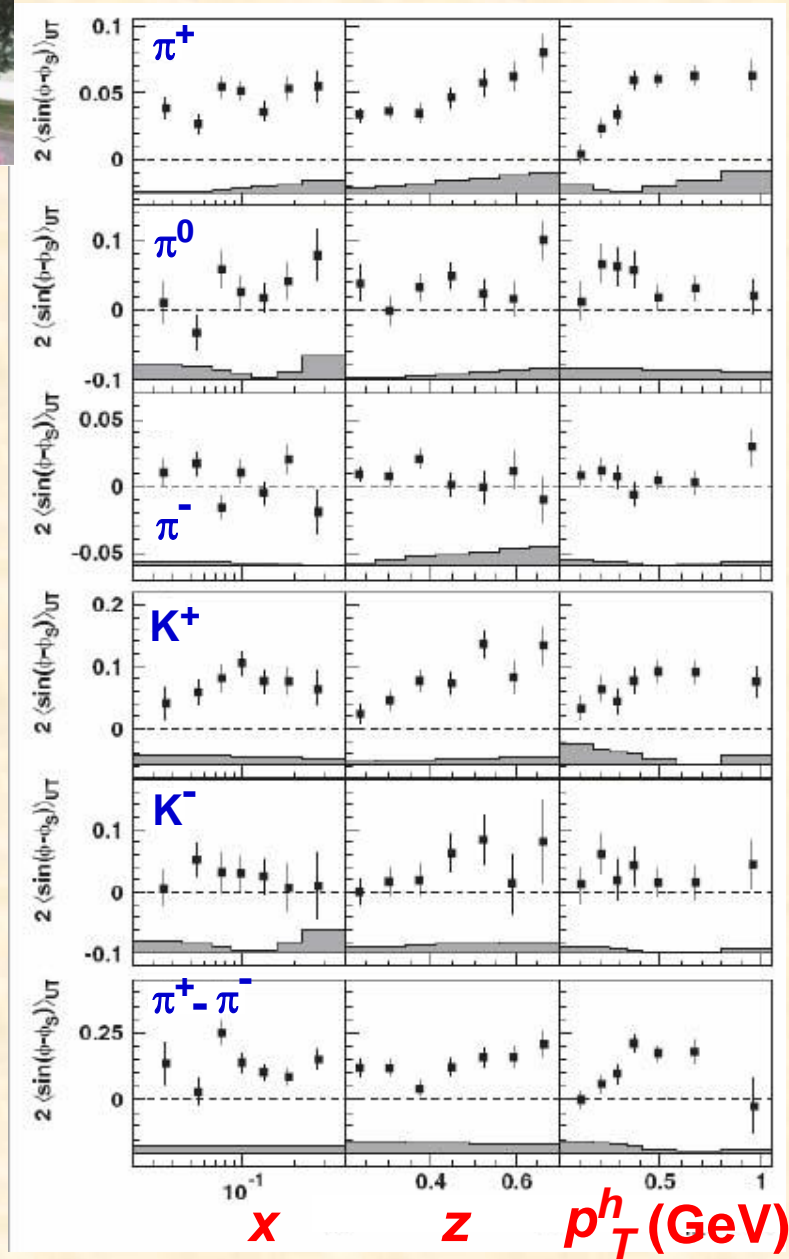


# $\pi$ electroproduction with transverse target

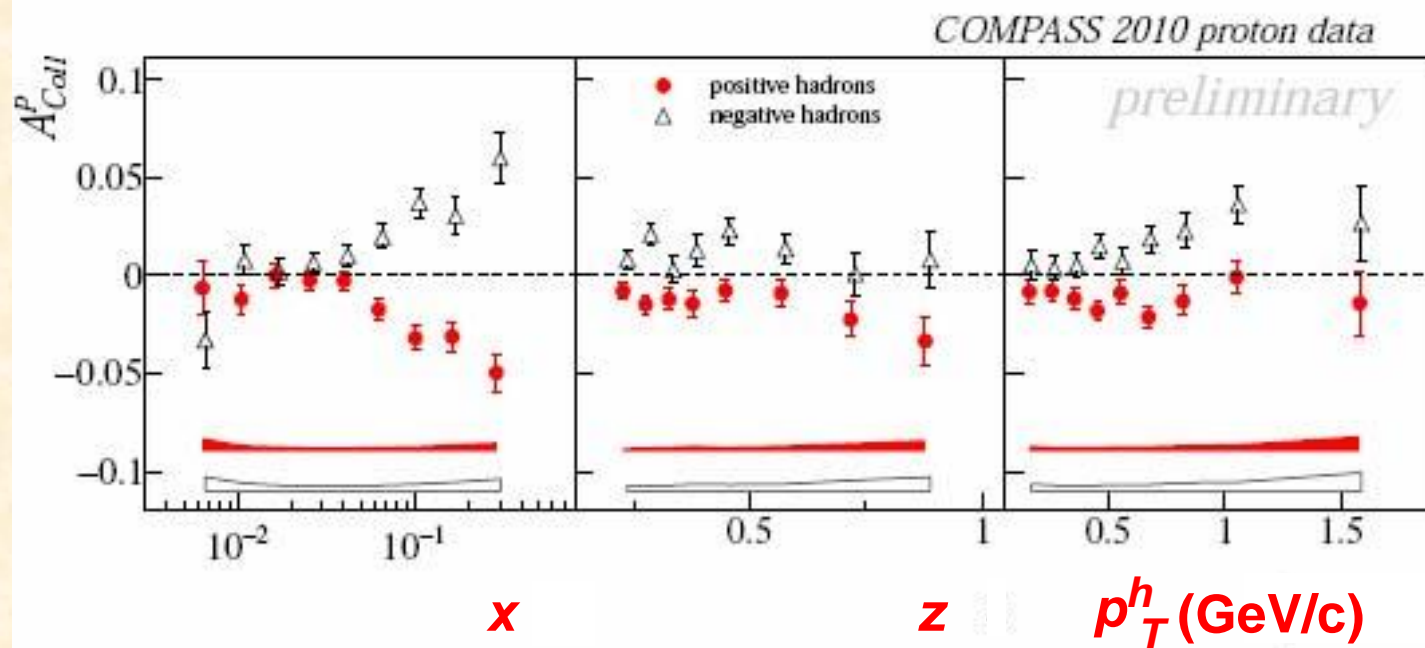
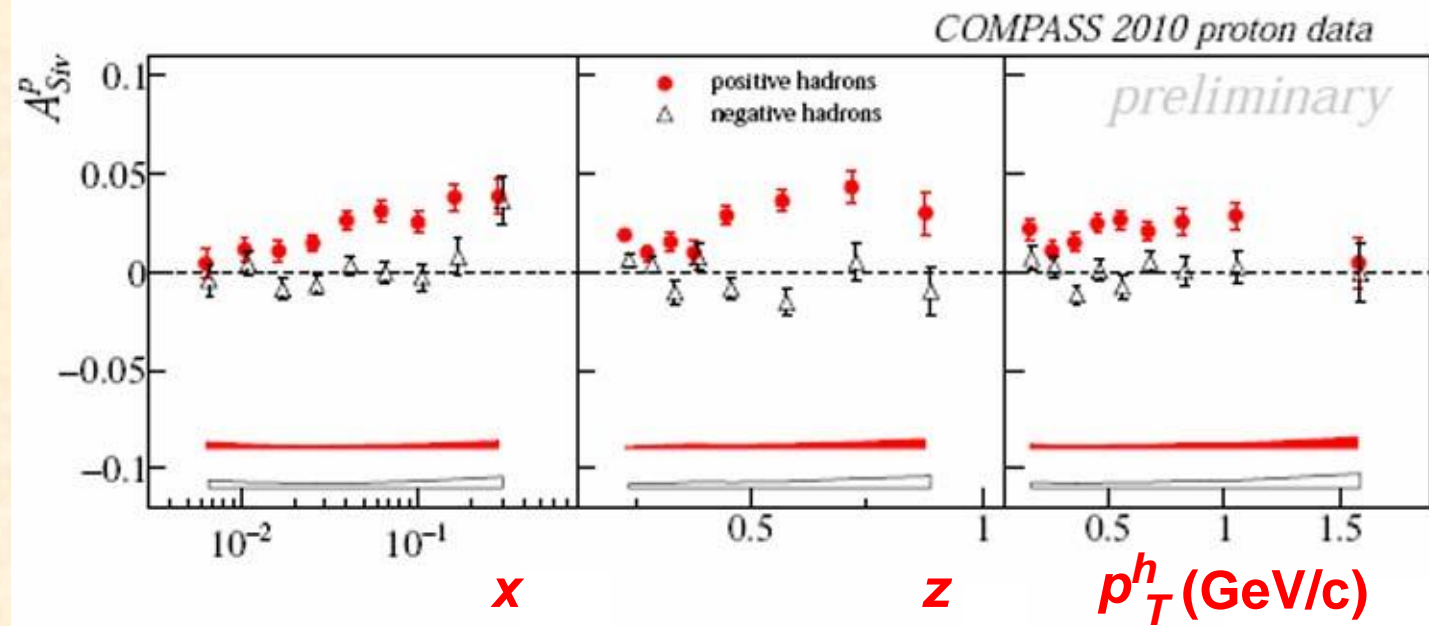
$$\sin(\phi_h^l + \phi_S^l) \Rightarrow h_1 = \begin{array}{c} \uparrow \\ \circ \\ \uparrow \\ \bullet \end{array} - \begin{array}{c} \uparrow \\ \circ \\ \downarrow \\ \bullet \end{array} \otimes H_1^\perp = \begin{array}{c} \uparrow \\ \circ \\ \bullet \end{array} - \begin{array}{c} \bullet \\ \circ \\ \downarrow \end{array}$$

$$\sin(\phi_h^l - \phi_S^l) \Rightarrow f_{1T}^\perp = \begin{array}{c} \uparrow \\ \circ \\ \bullet \end{array} - \begin{array}{c} \bullet \\ \circ \\ \downarrow \end{array} \otimes D_1 = \begin{array}{c} \bullet \\ \circ \\ \bullet \end{array}$$

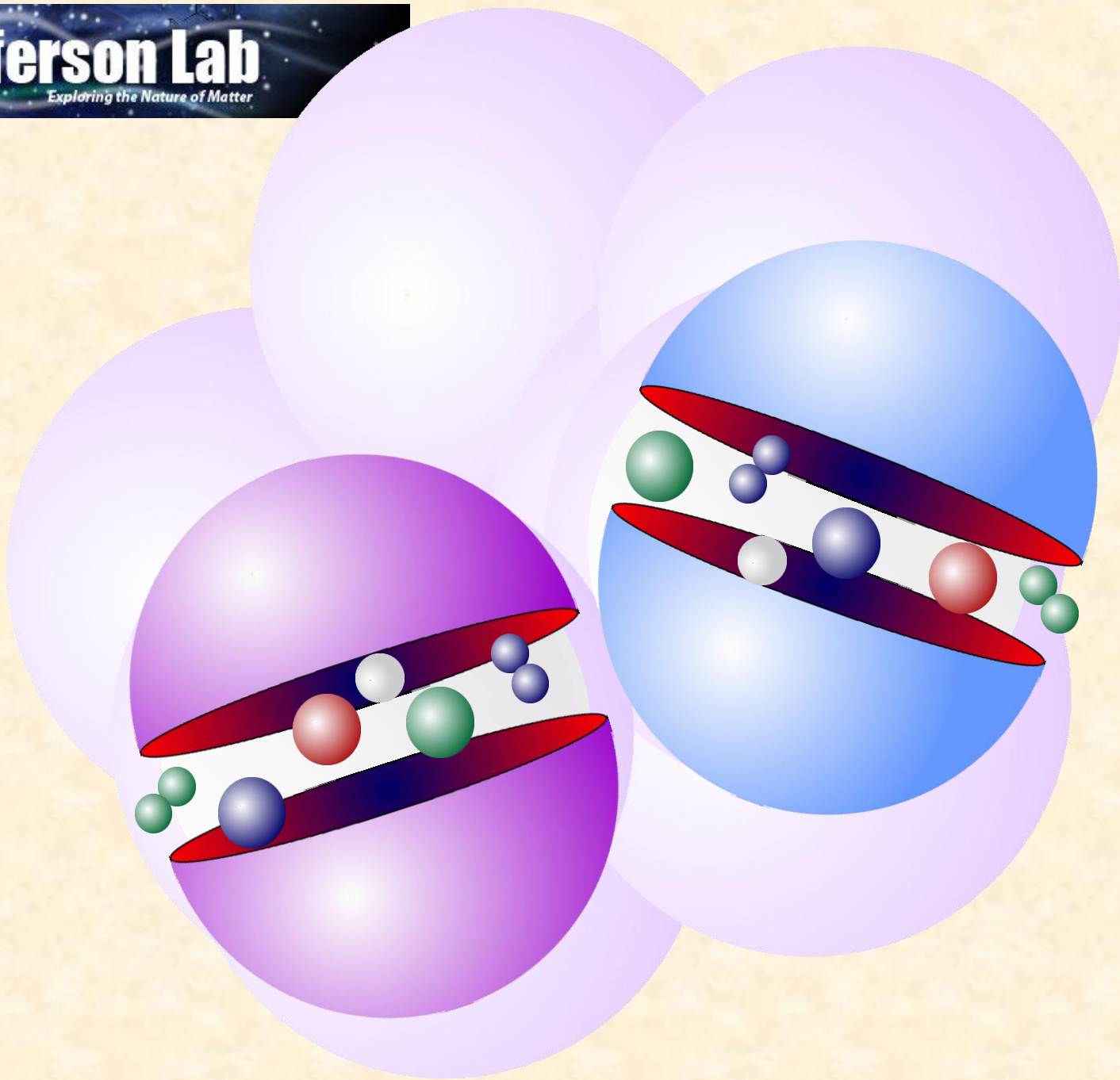
- $(\phi_h^l - \phi_S^l)$  = angle of pion relative to **initial** quark spin
- $(\phi_h^l + \phi_S^l)$  = angle of pion relative to **final** quark spin

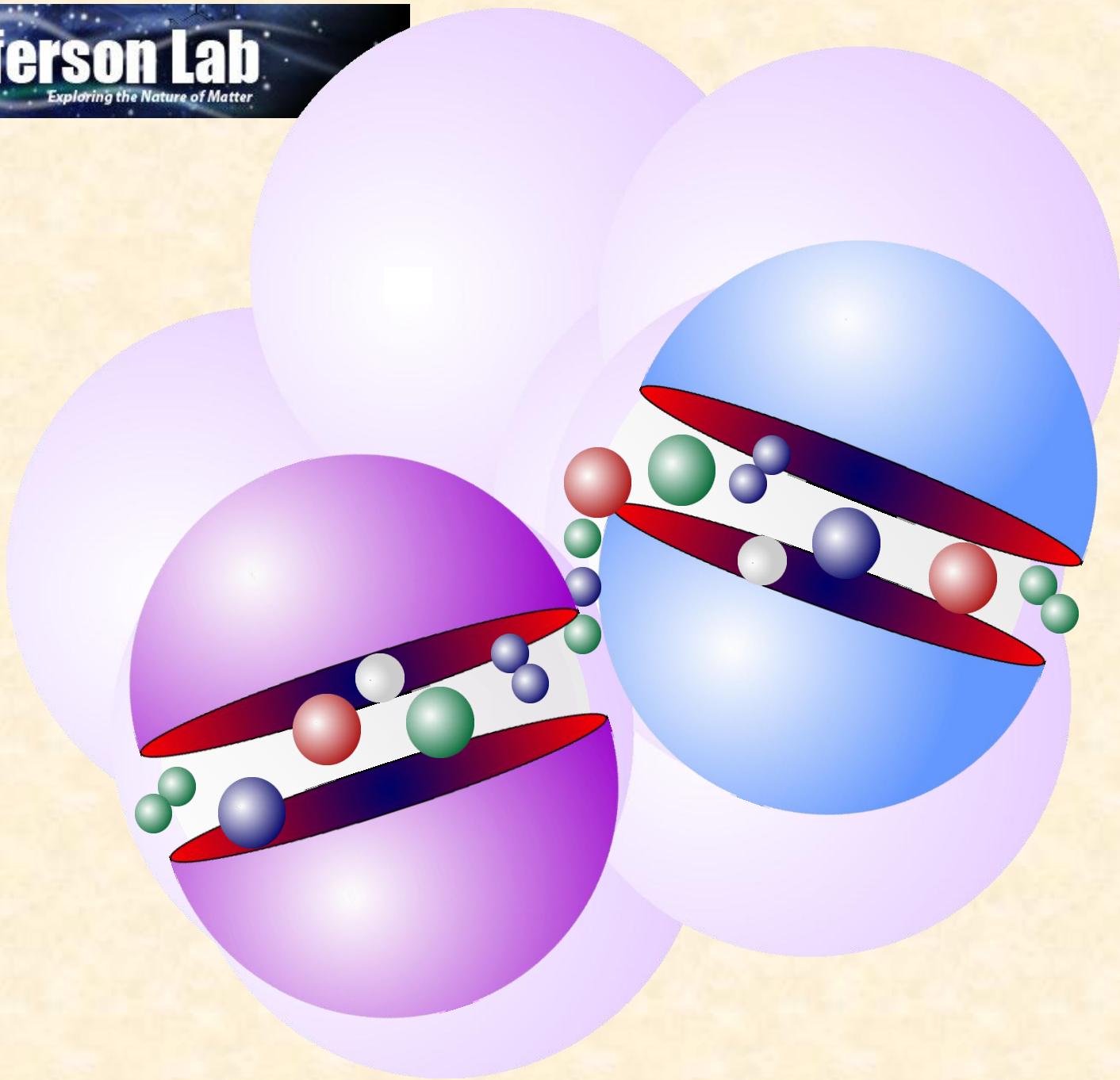


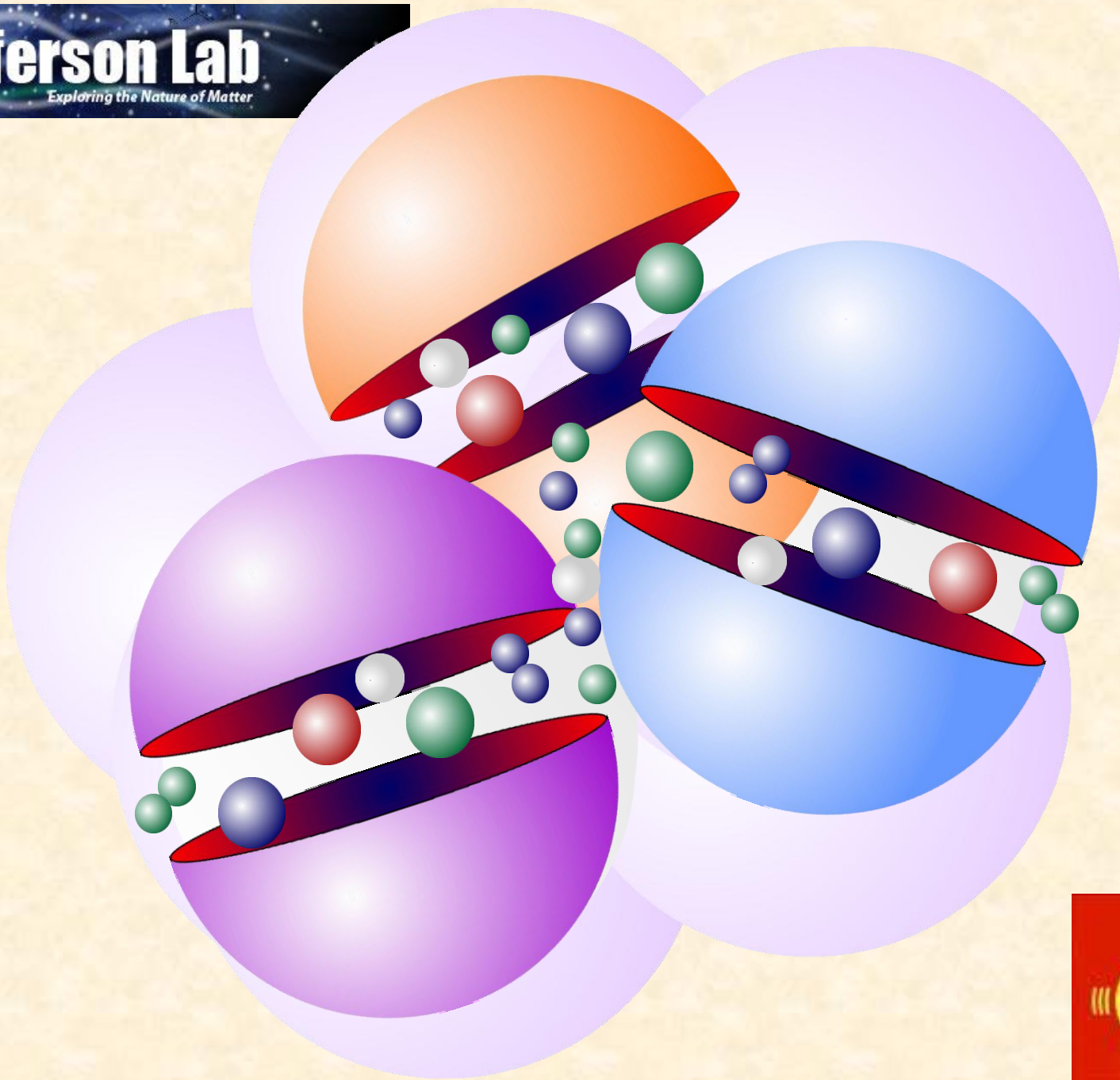
**P<sub>Lab</sub>**  
**27.5 GeV**



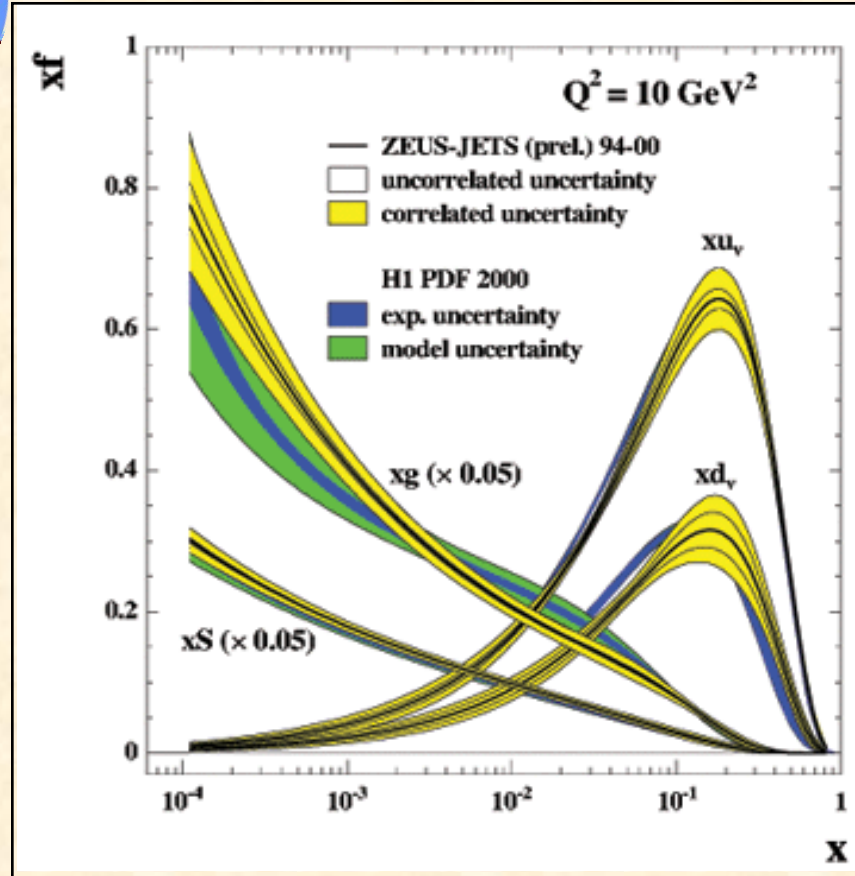
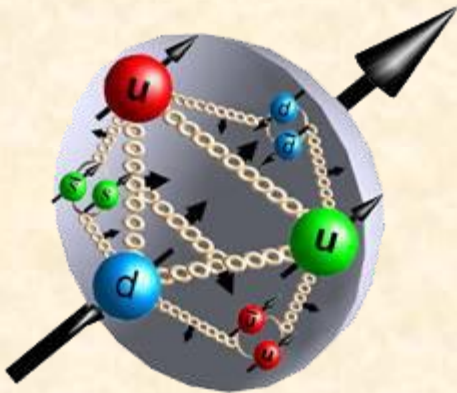
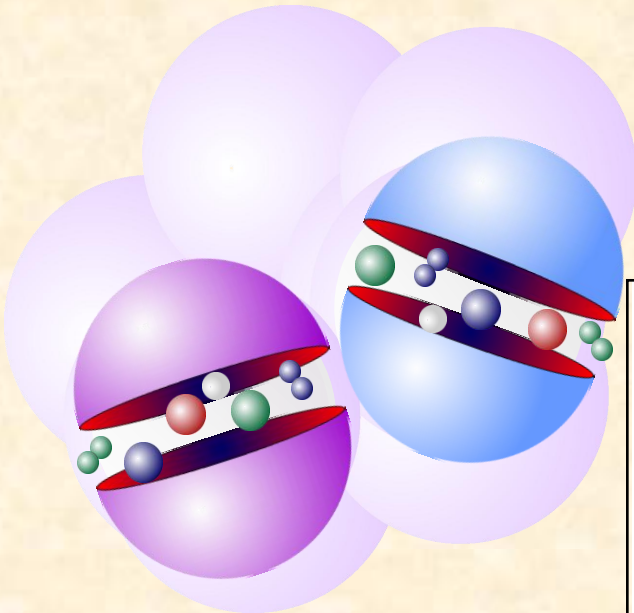
$P_{\text{Lab}}$   
160 GeV







# Electron Ion Collider



New states  
of matter

Color glass  
Condensate?





**Glimpsing colour  
in a world of black & white**





*Skiing*

*with*

*QUARKS*

