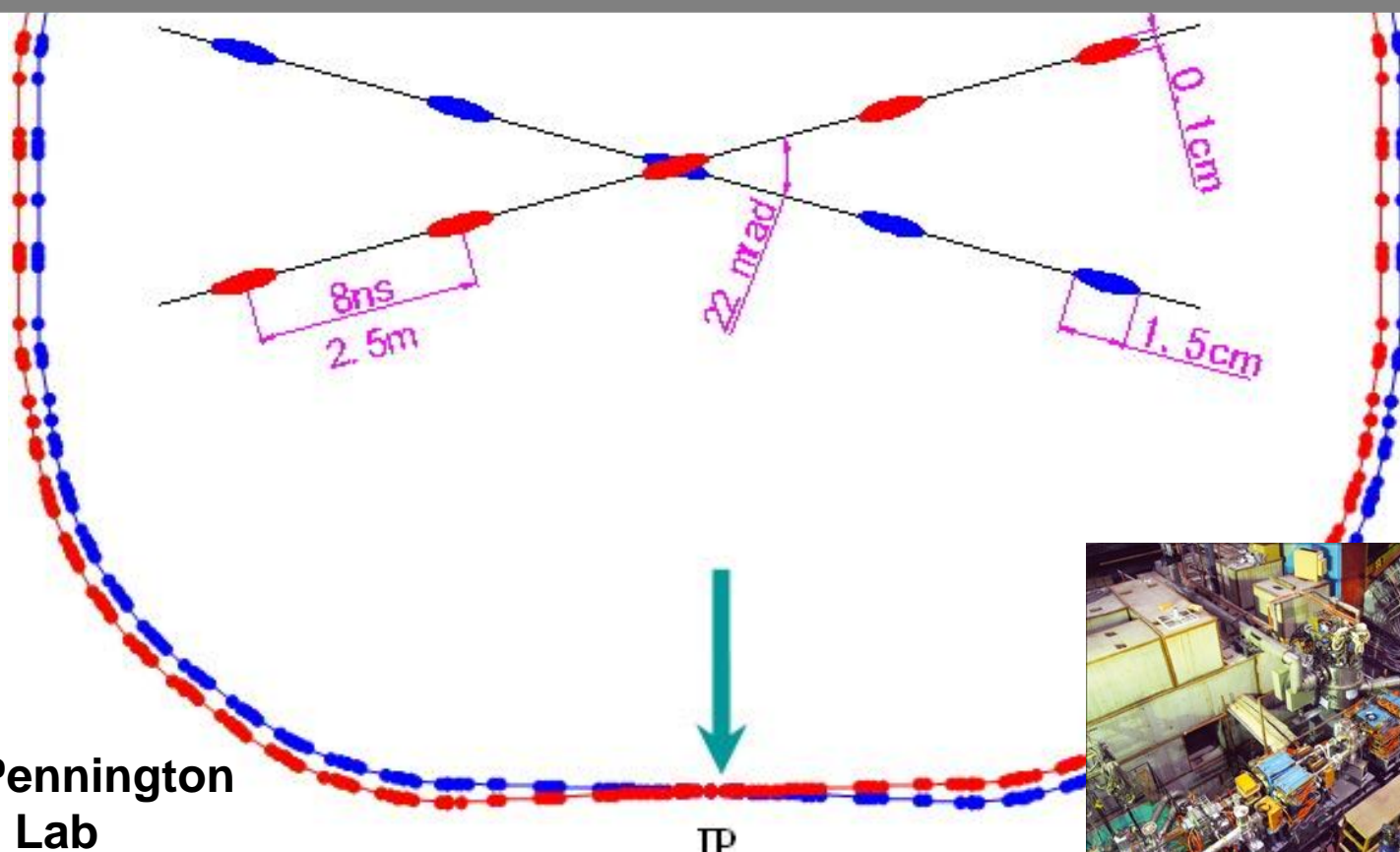
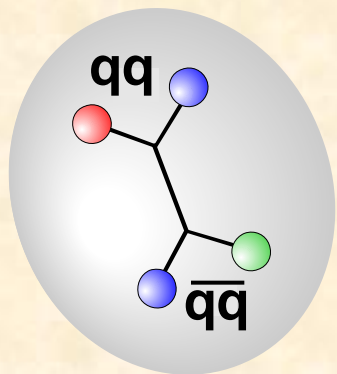
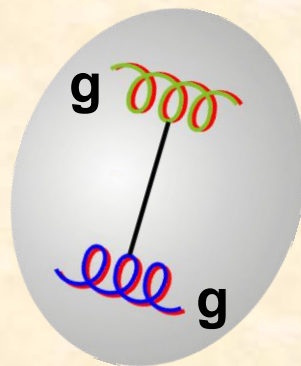


Can BESIII help distinguish between a four quark state, a molecule, a glueball or a $\bar{q}q$ meson ?

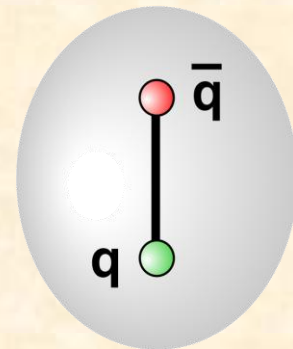


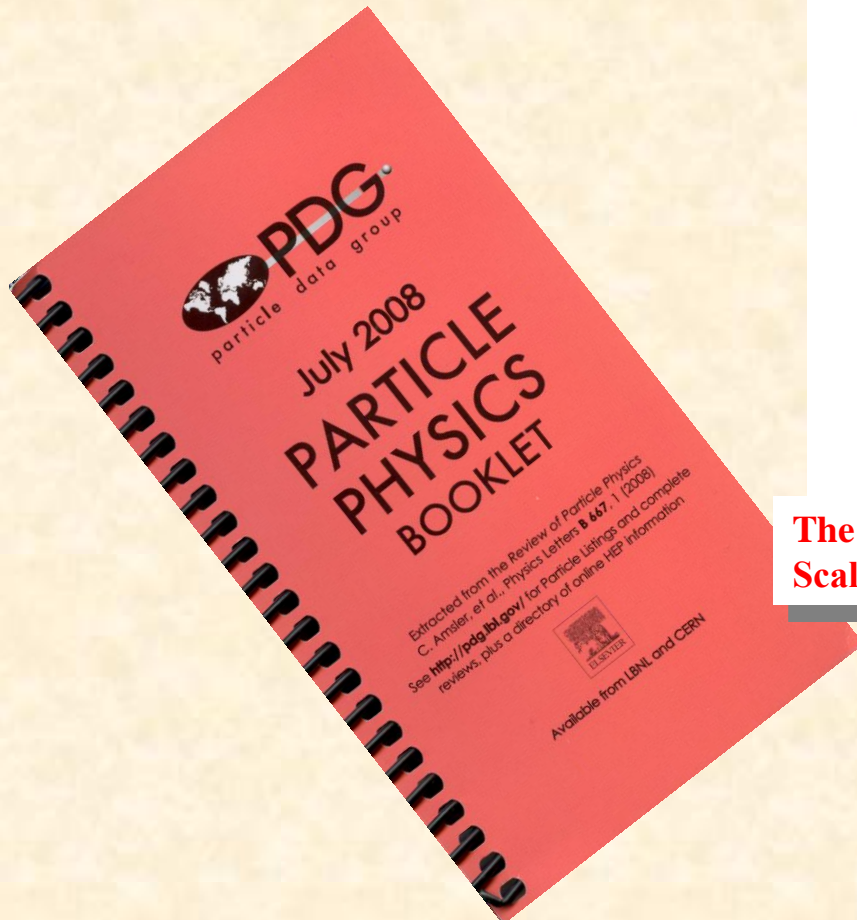
Michael Pennington
Jefferson Lab





Scalars





NOTE ON SCALAR MESONS

Revised January 2008 by S. Spanier (University of Tennessee), N.A. Törnqvist (University of Helsinki), and C. Amsler (University of Zurich).

I. Introduction:

The scalar mesons are especially important to understand because they have the same quantum numbers as the vacuum ($J^{PC} = 0^{++}$). Therefore they can condense into the vacuum and break a symmetry like a global chiral $U(N_f) \times U(N_f)$. The details of how this symmetry breaking is implemented in Nature is one of the most profound problems in particle physics.

The identification of scalar mesons is a long-standing puzzle. Scalar resonances are difficult to resolve ...

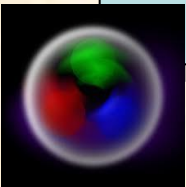
Scalars

color wave-functions

$$\pi^+ = \frac{1}{\sqrt{N_c}} [u\bar{d} + u\bar{d} + u\bar{d} + u\bar{d} + \dots]$$

$$N_c = 3$$

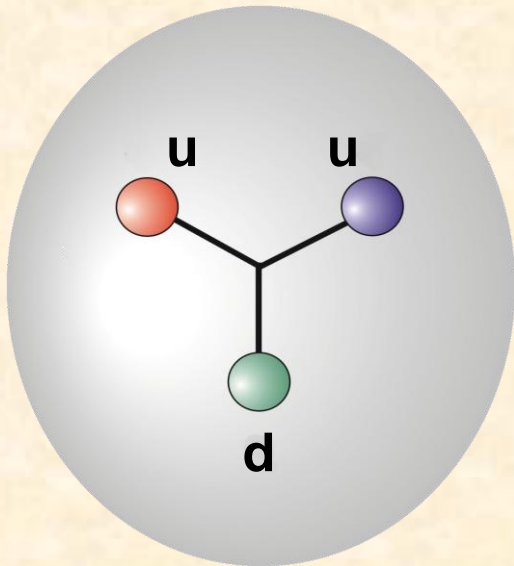
$$p = \frac{1}{\sqrt{6}} [uud + uud + uud \\ - uud - uud - uud]$$



$\Delta(1232)$ color wave-function

$$N_c = 3$$

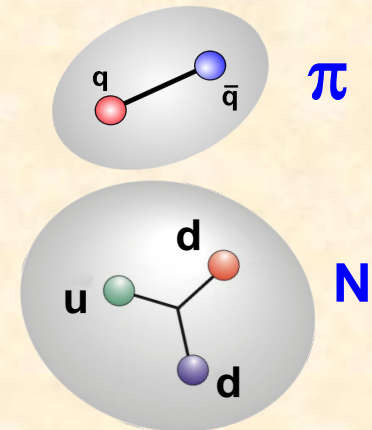
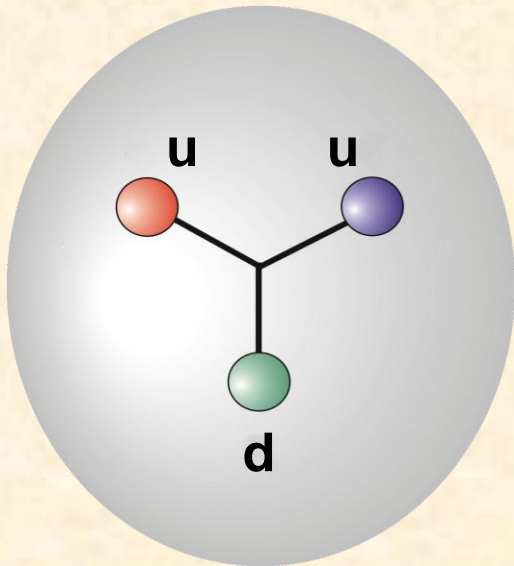
$$\Delta^+ = \frac{1}{\sqrt{6}} \left[\begin{aligned} & \text{uud} + \text{uud} + \text{uud} \\ & - \text{uud} - \text{uud} - \text{uud} \end{aligned} \right]$$



$\Delta(1232)$ color wave-function

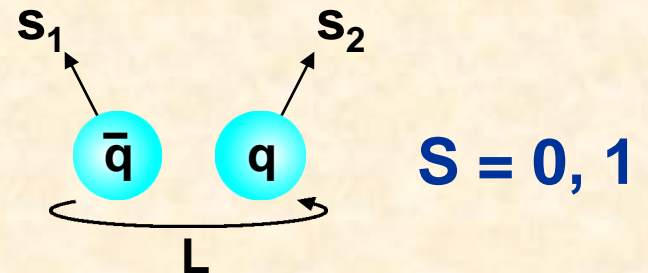
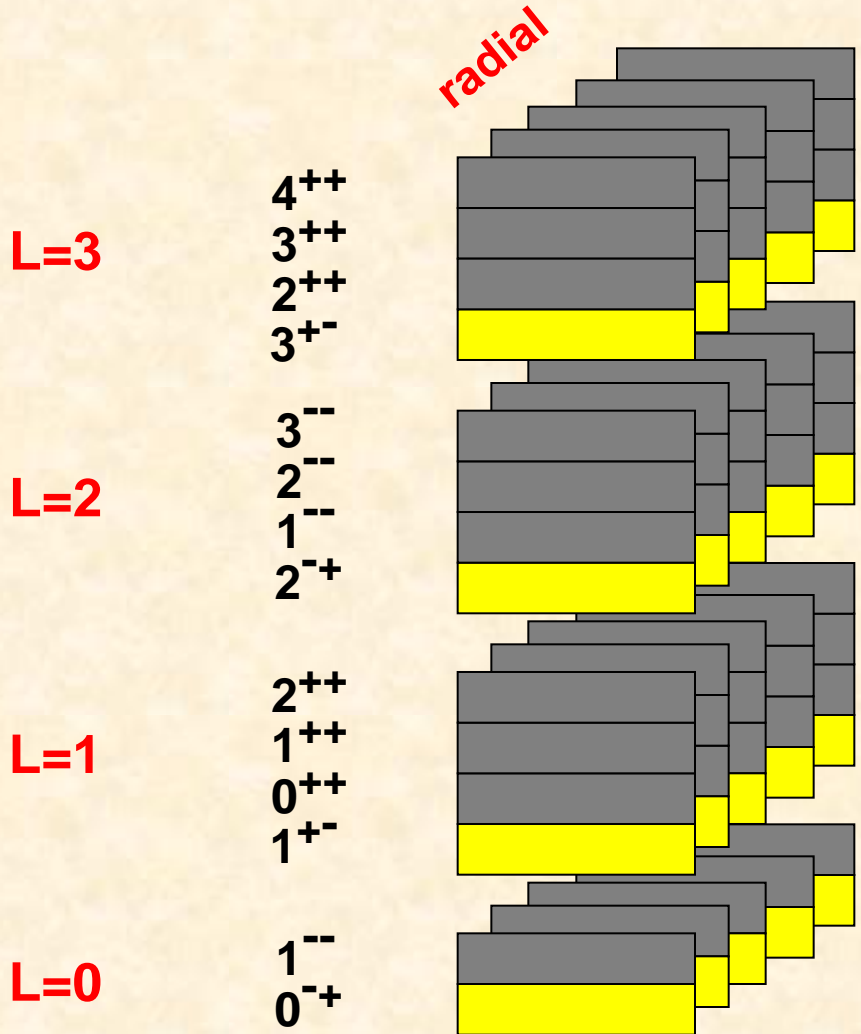
$$N_c = 3$$

$$\Delta^+ = \frac{1}{\sqrt{6}} \left[\begin{aligned} & \text{uud} + \text{uud} + \text{uud} \\ & - \text{uud} - \text{uud} - \text{uud} \end{aligned} \right]$$

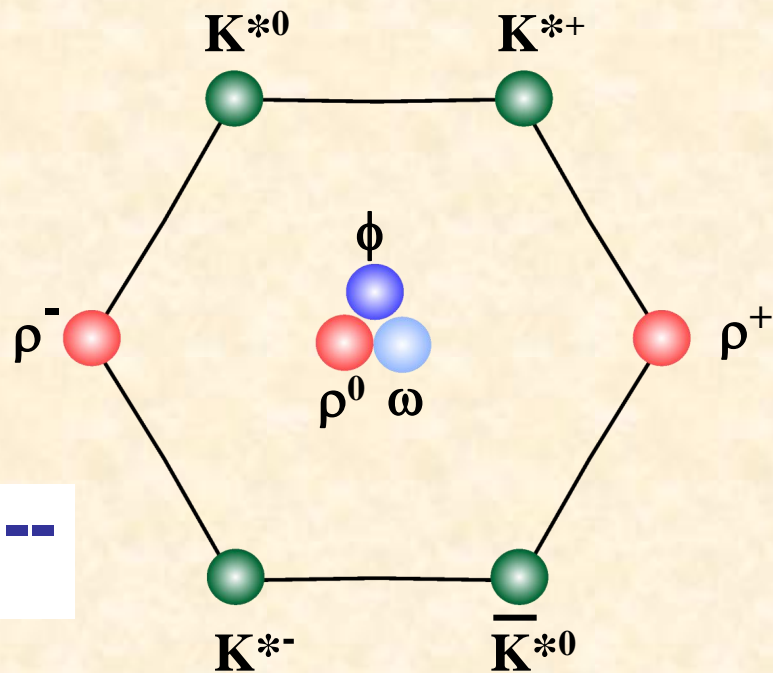
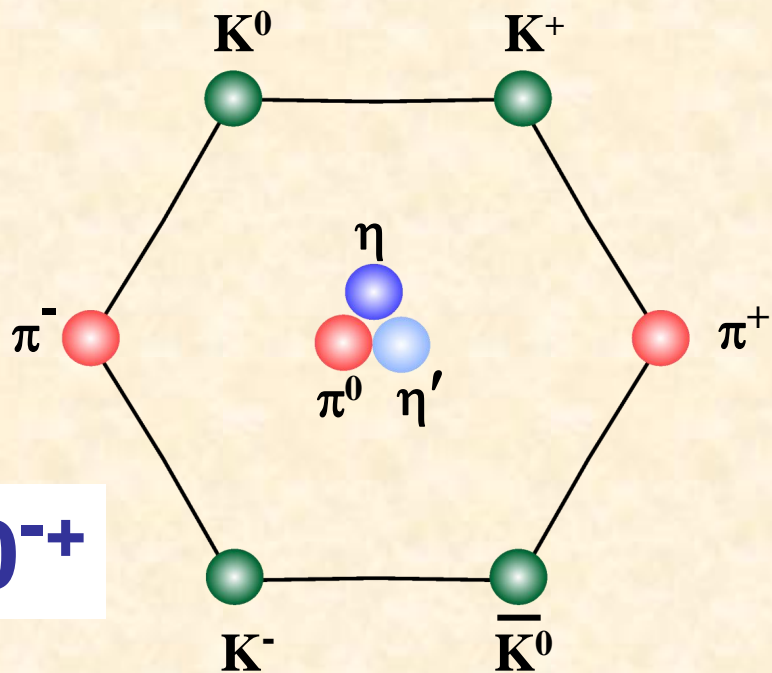


Meson spectrum

J^PC

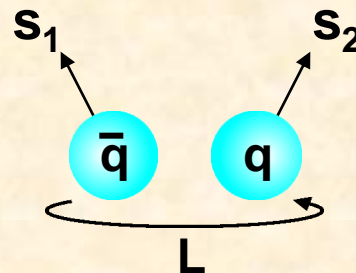
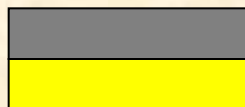


Meson spectrum









$L=0$

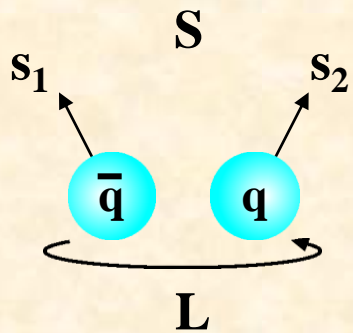
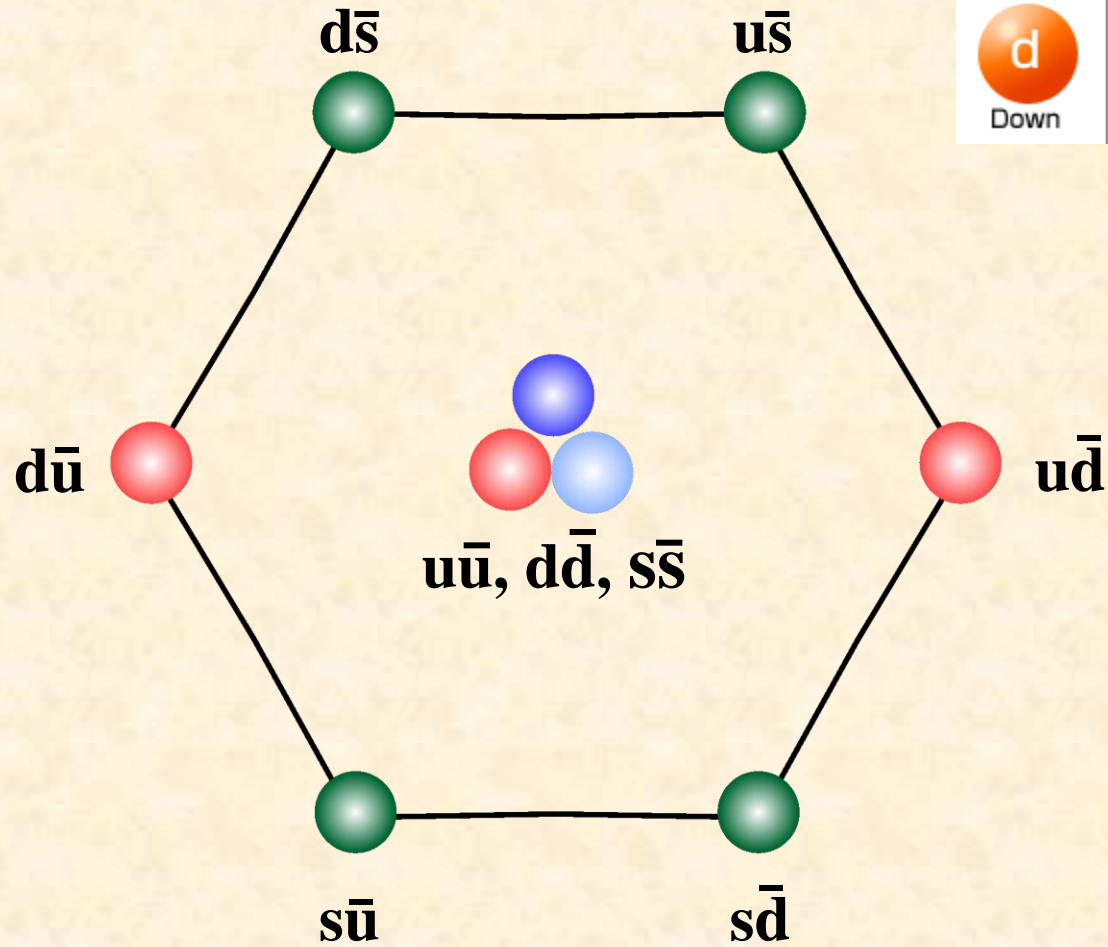
1^{--}
 0^{-+}



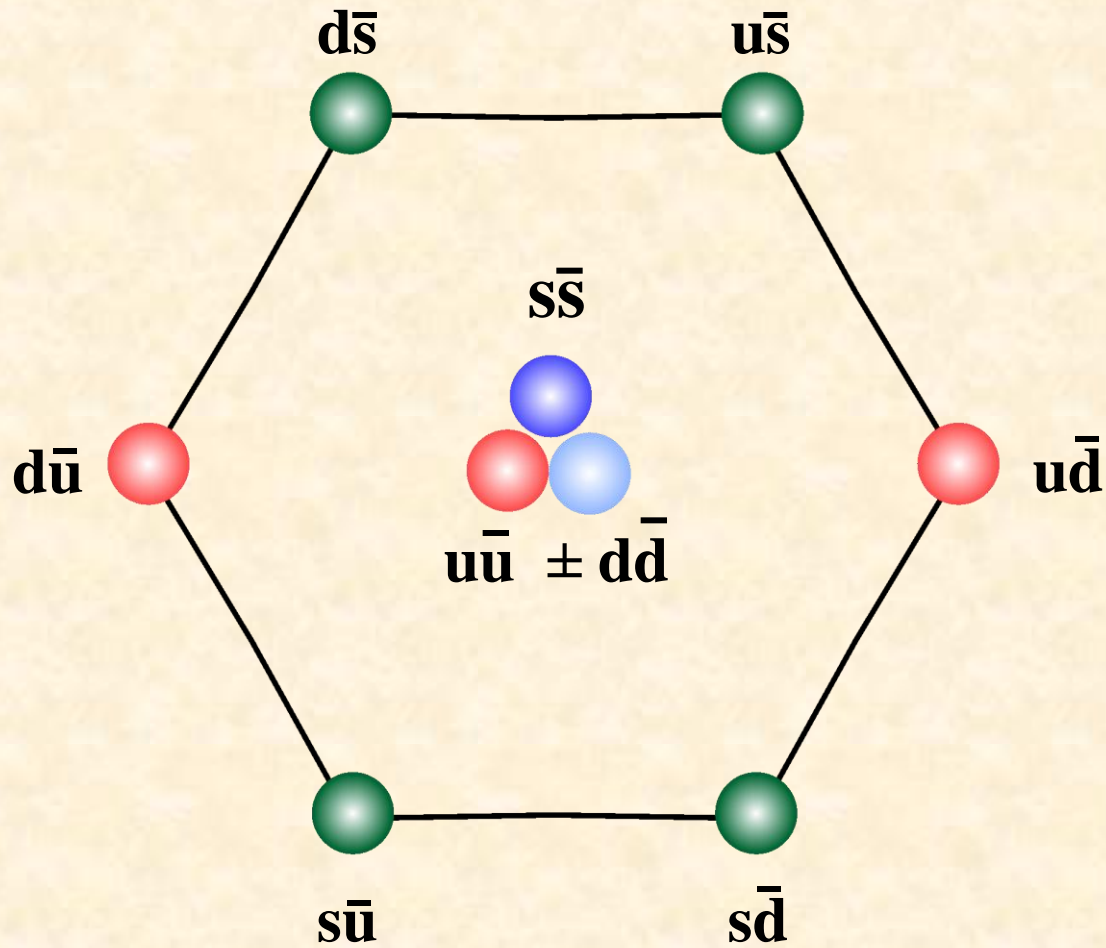
$S = 0, 1$

Meson multiplet

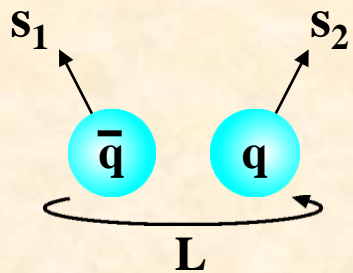
First generation	Second generation	Third generation
 u Up	 c Charm	 t Top
 d Down	 s Strange	 b Bottom



Vector multiplet

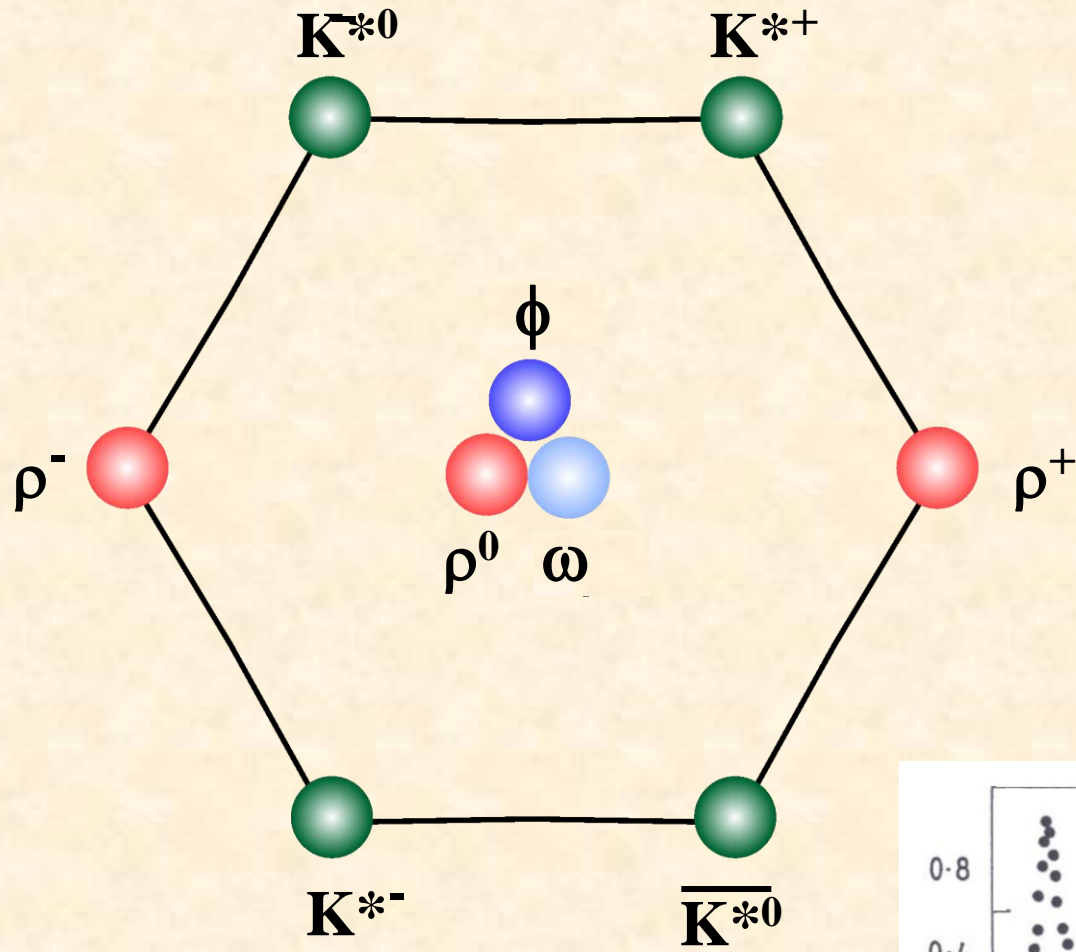


$$J^{PC} = 1^{--}$$

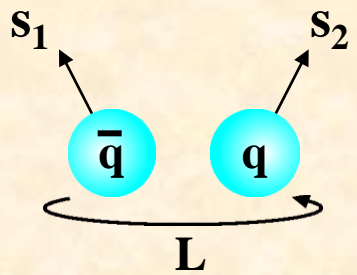


$$S = 1, L = 0$$

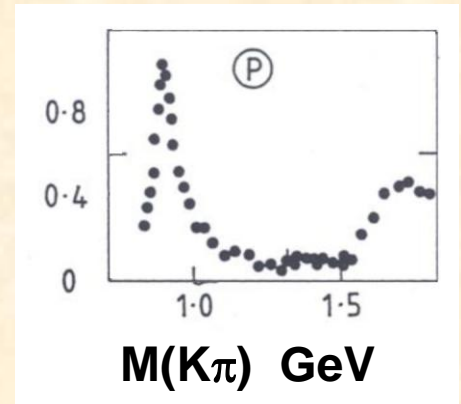
Vector multiplet



$$J^{PC} = 1^{--}$$

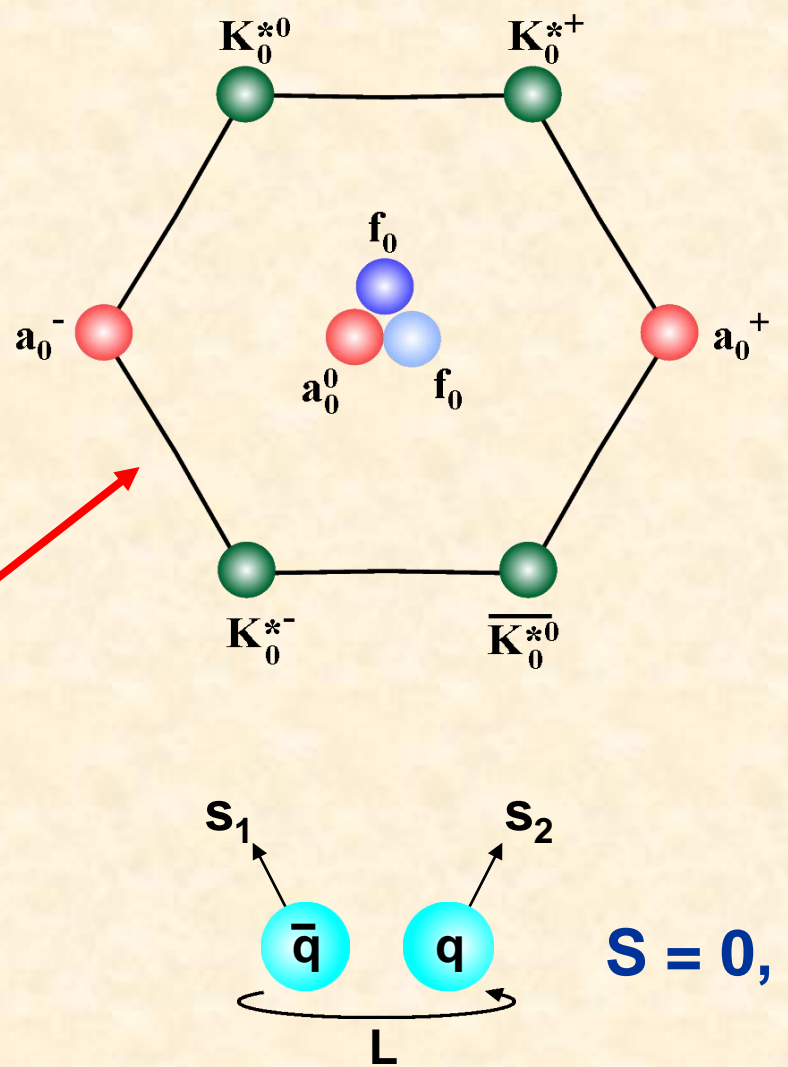
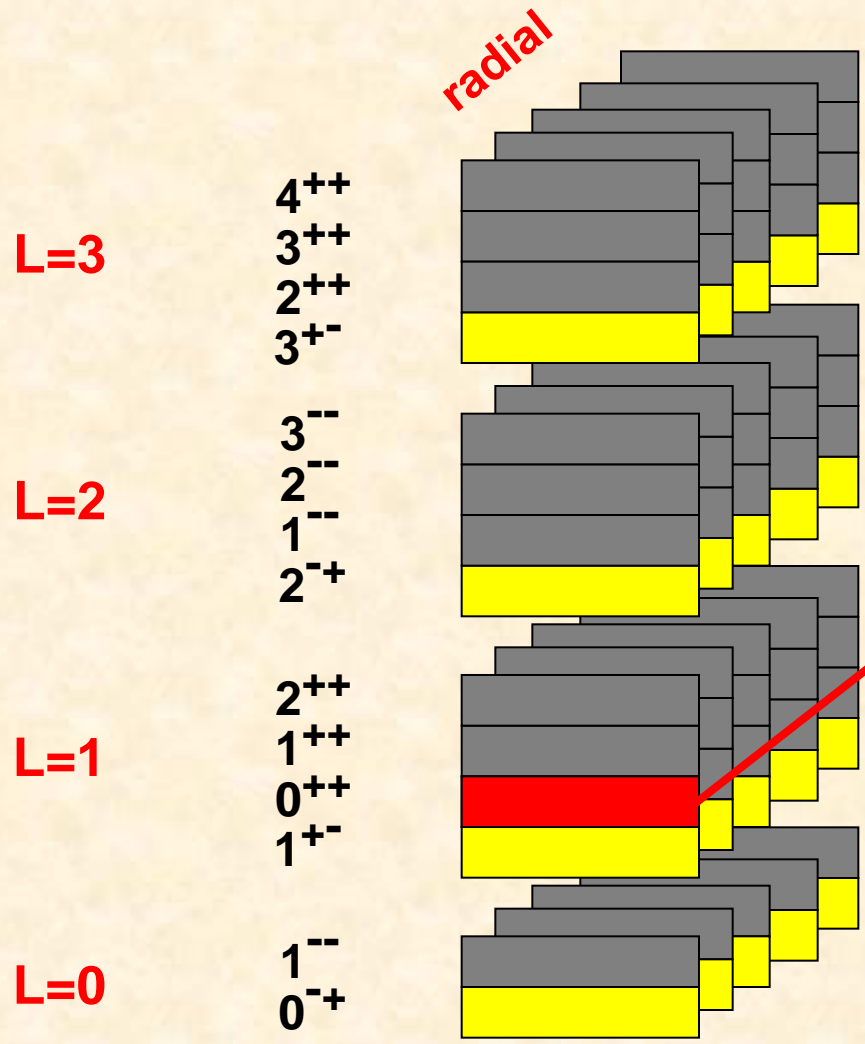


$$S = 1, L = 0$$



Meson spectrum

0^{++}

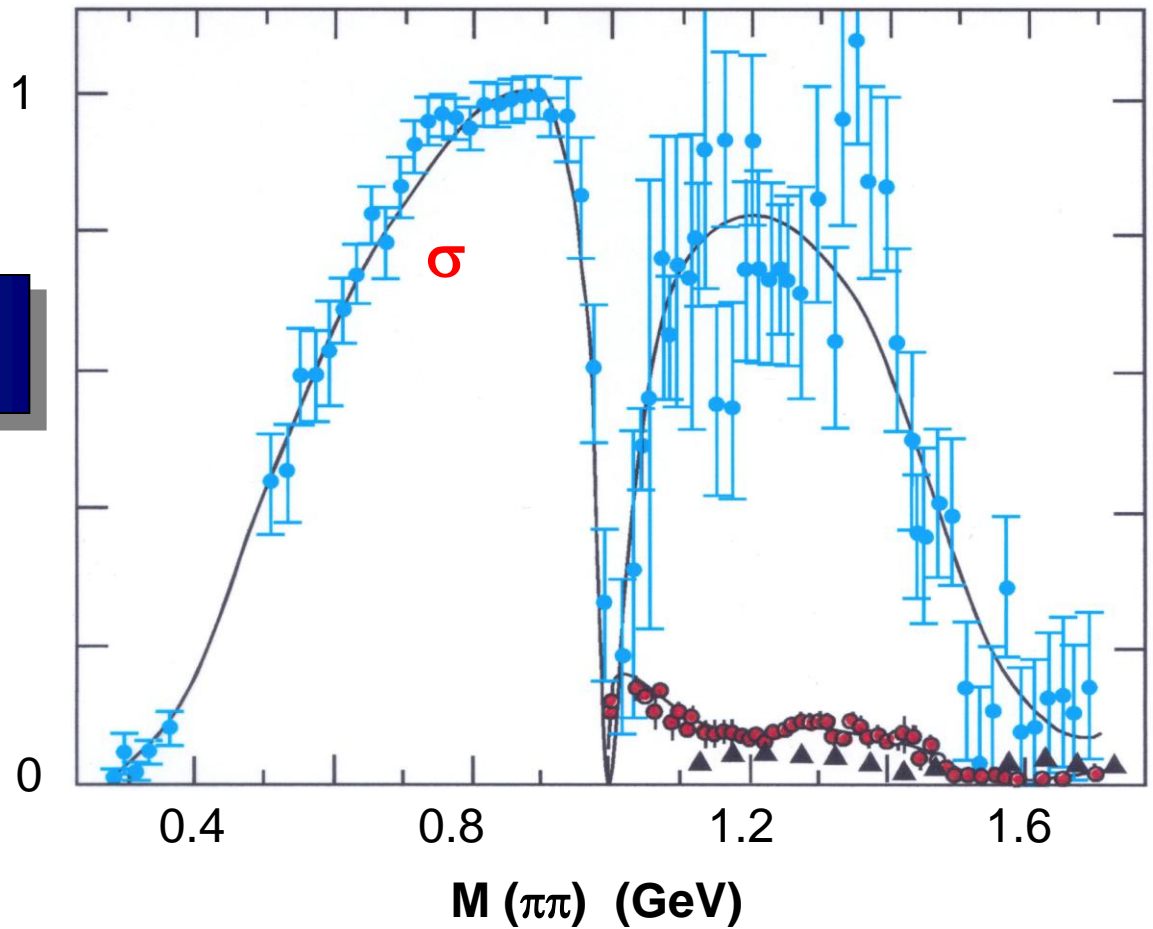


Scalar mesons

$\pi\pi \rightarrow \pi\pi$

$f_0(600)$

$I = J = 0$



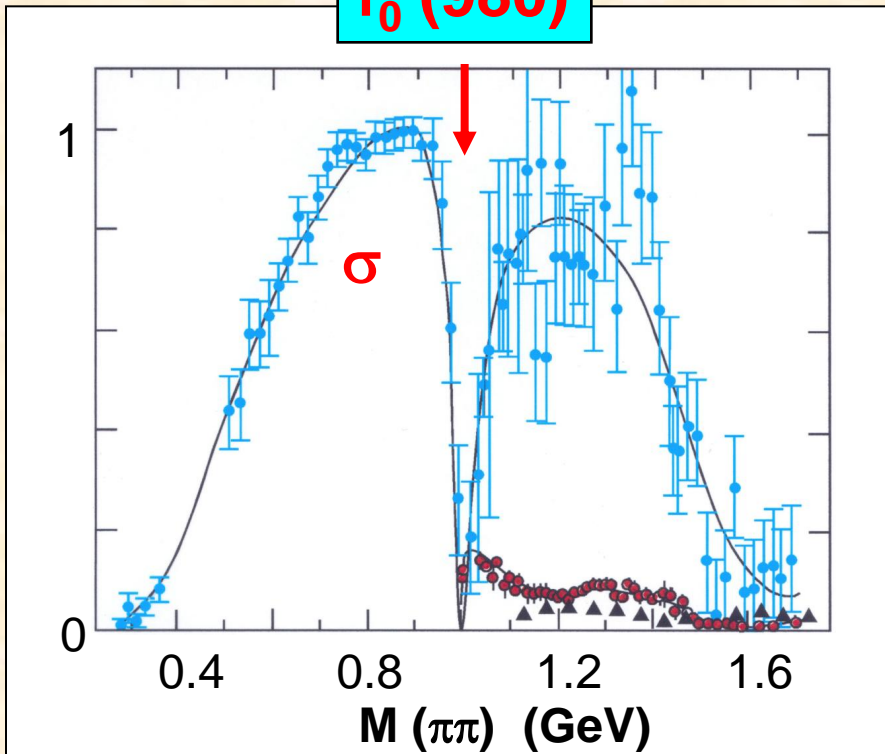
● $\pi\pi \rightarrow \pi\pi$

● $\pi\pi \rightarrow K\bar{K}$

▲ $\pi\pi \rightarrow \eta\eta$

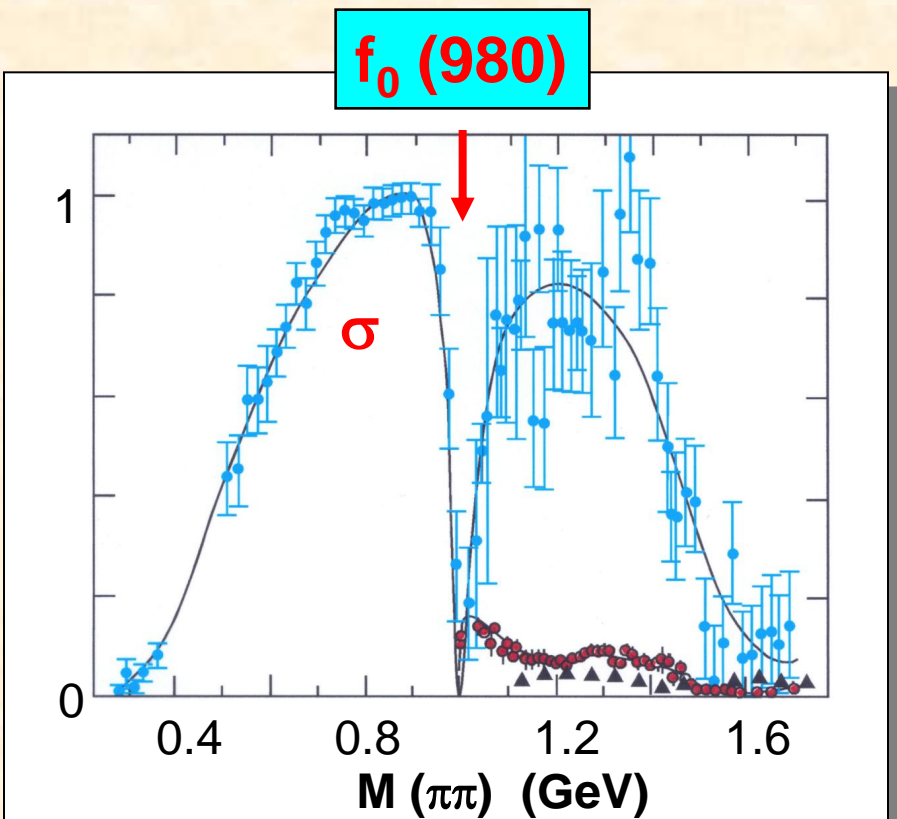
$\pi\pi \rightarrow \pi\pi, \bar{K}K$

$f_0(980)$



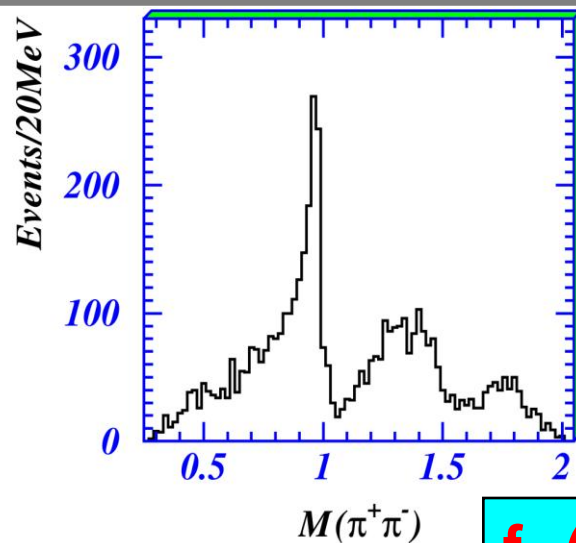
CERN-Munich, ANL, BNL

$\pi\pi \rightarrow \pi\pi, \bar{K}K$

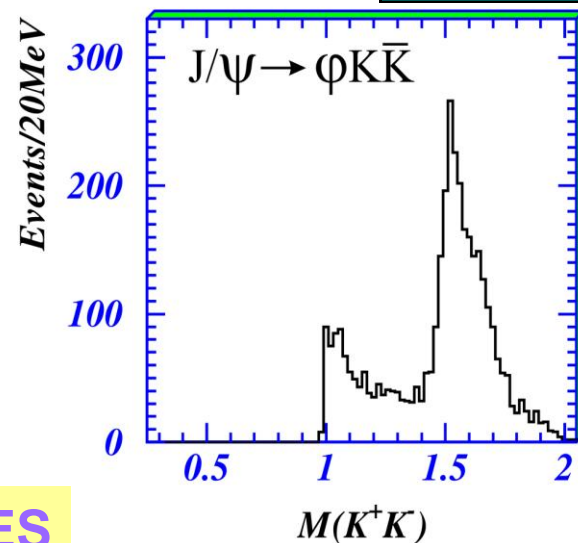


CERN-Munich, ANL, BNL

$J/\psi \rightarrow \phi (\pi\pi, \bar{K}K)$

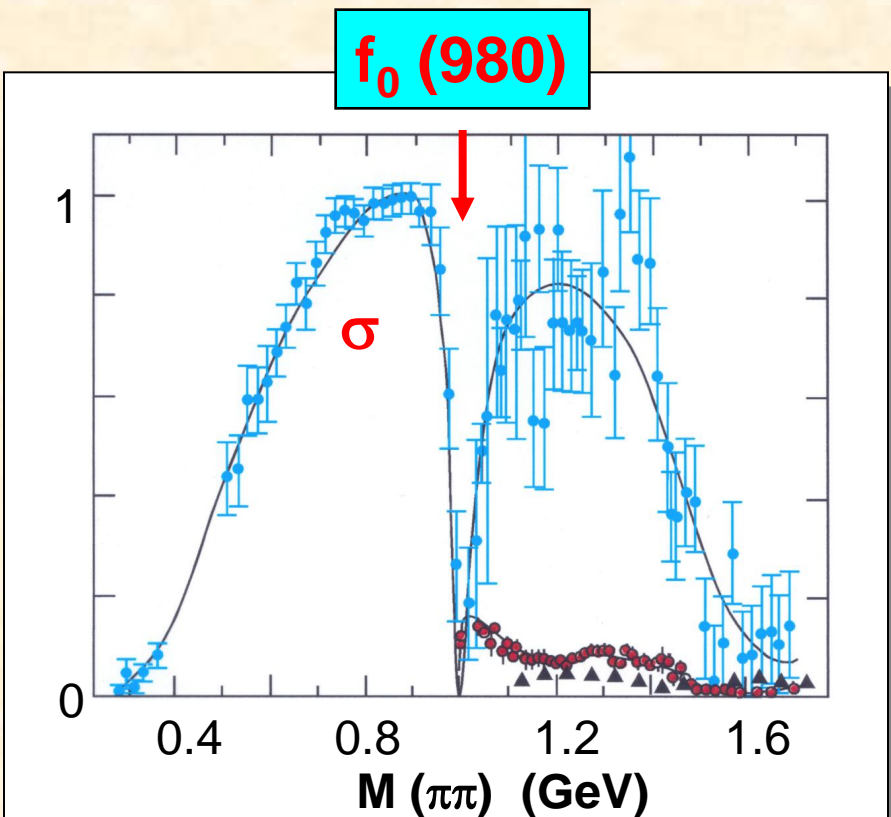


$f_0(980)$



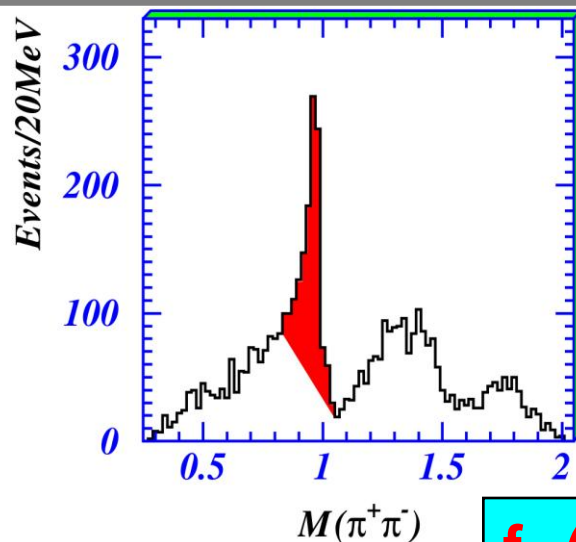
BES

$\pi\pi \rightarrow \pi\pi, \bar{K}K$

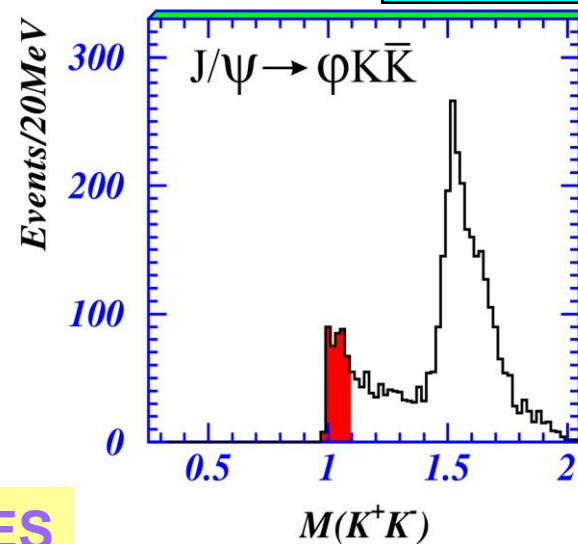


CERN-Munich, ANL, BNL

$J/\psi \rightarrow \phi (\pi\pi, \bar{K}K)$



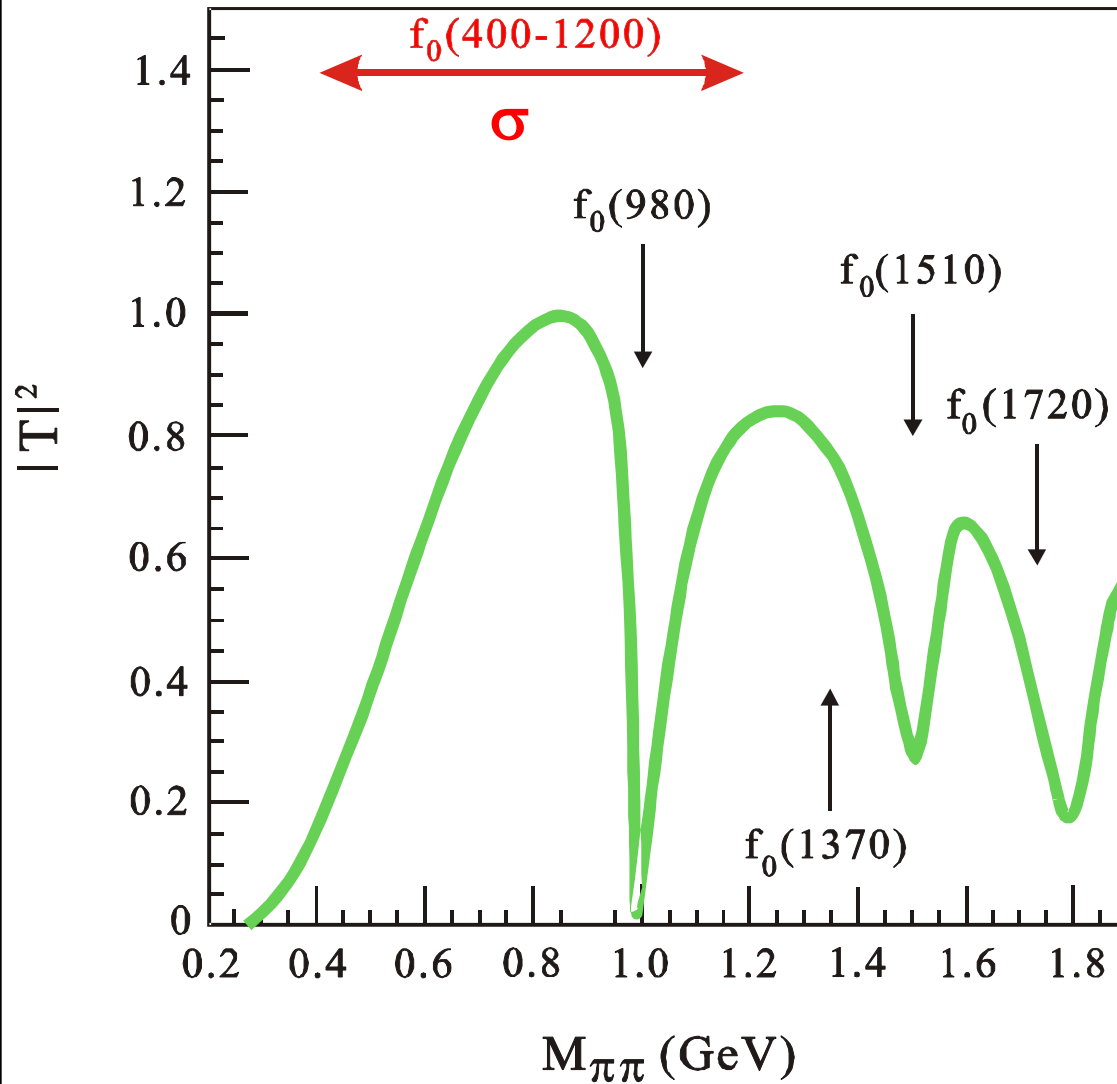
$f_0(980)$



BES

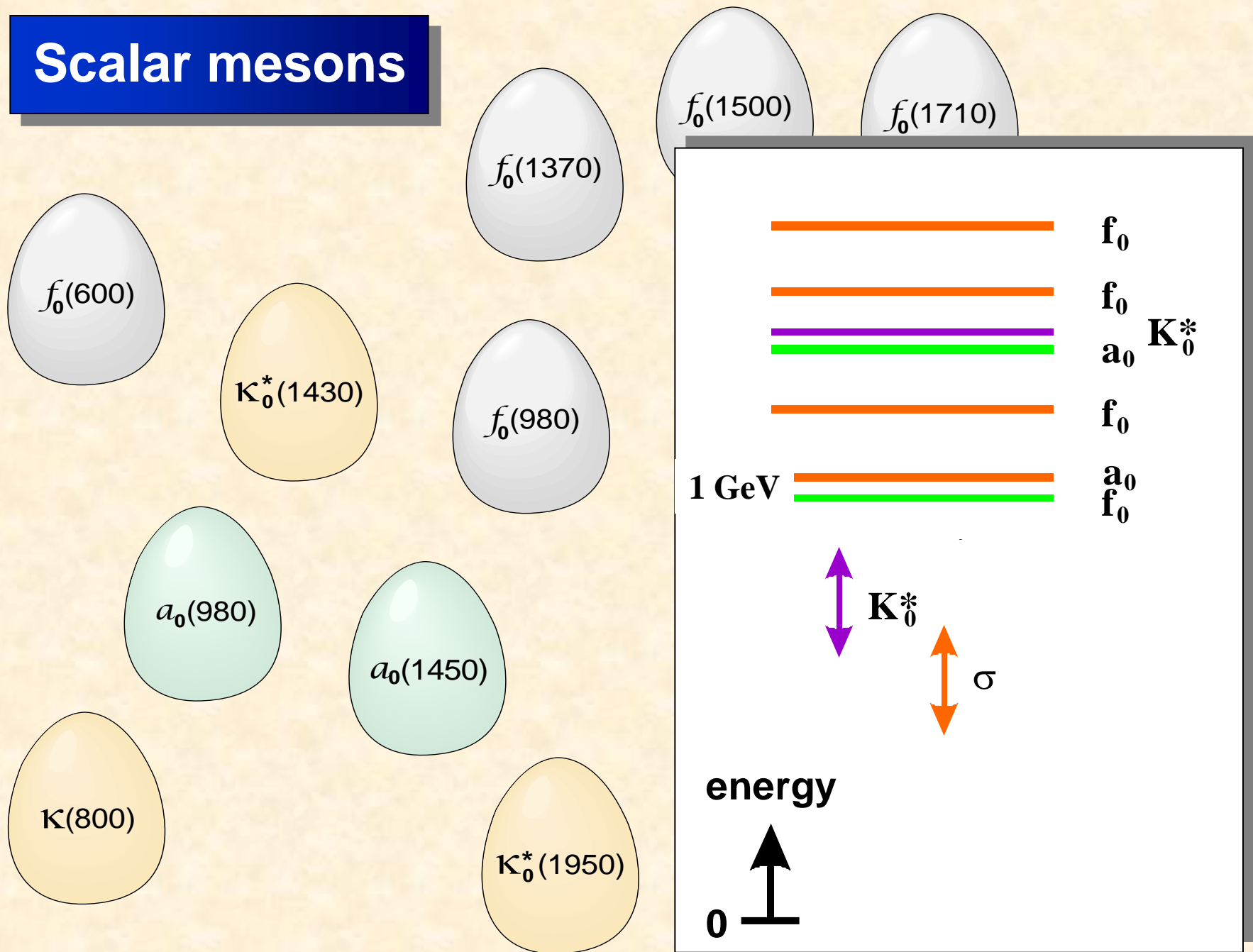
$\pi\pi \rightarrow \pi\pi$

$I = J = 0$

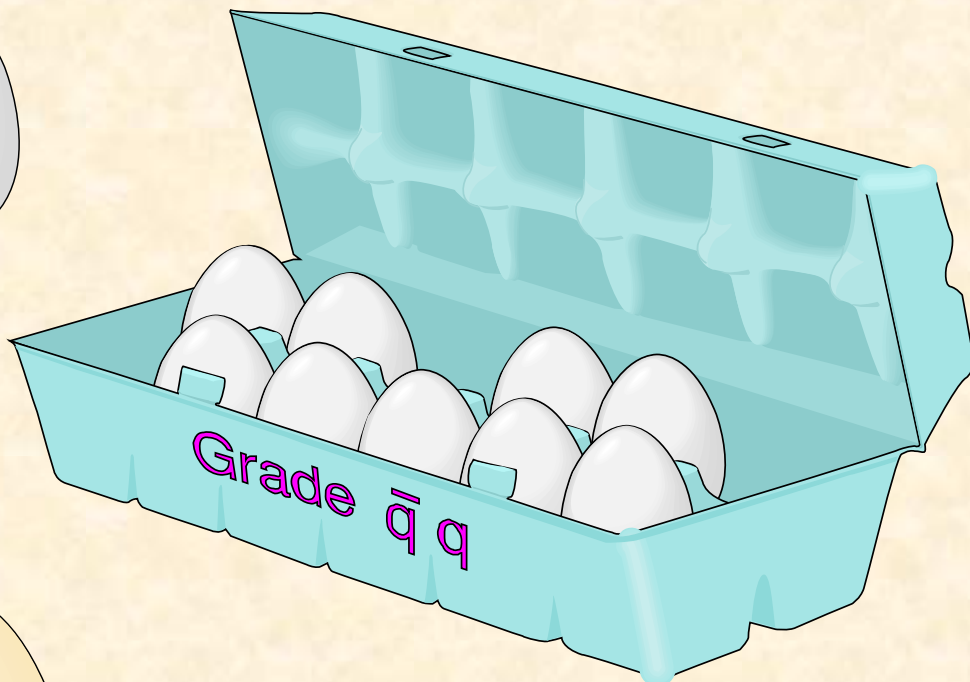
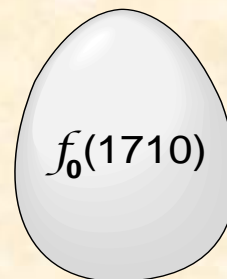
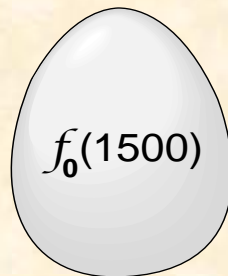
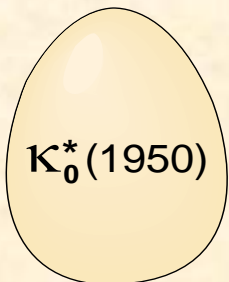
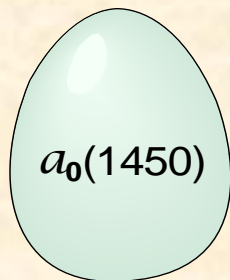
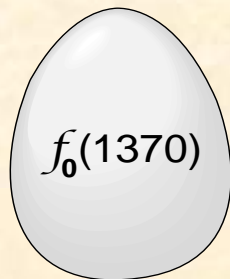
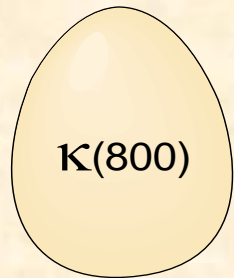
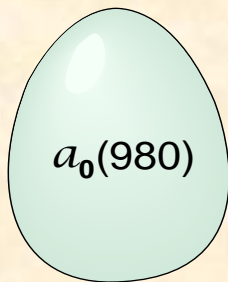
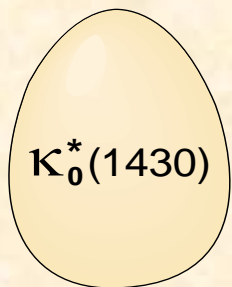
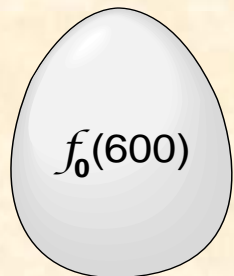


Zou

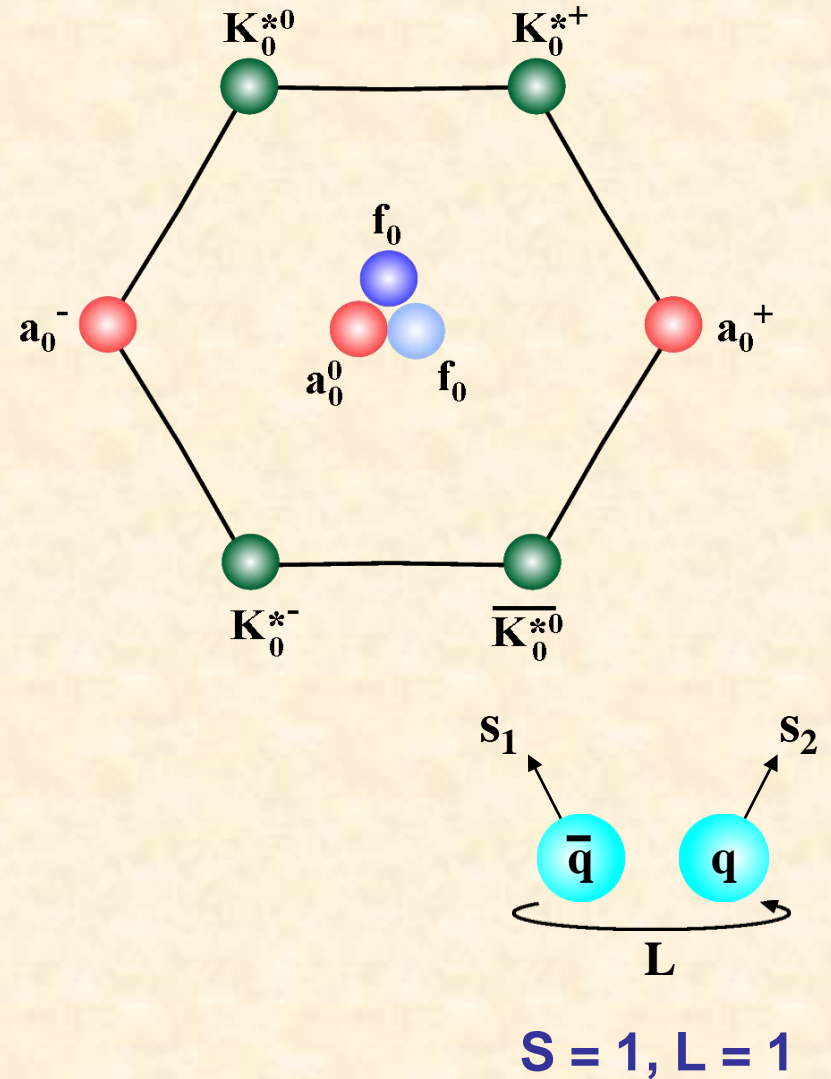
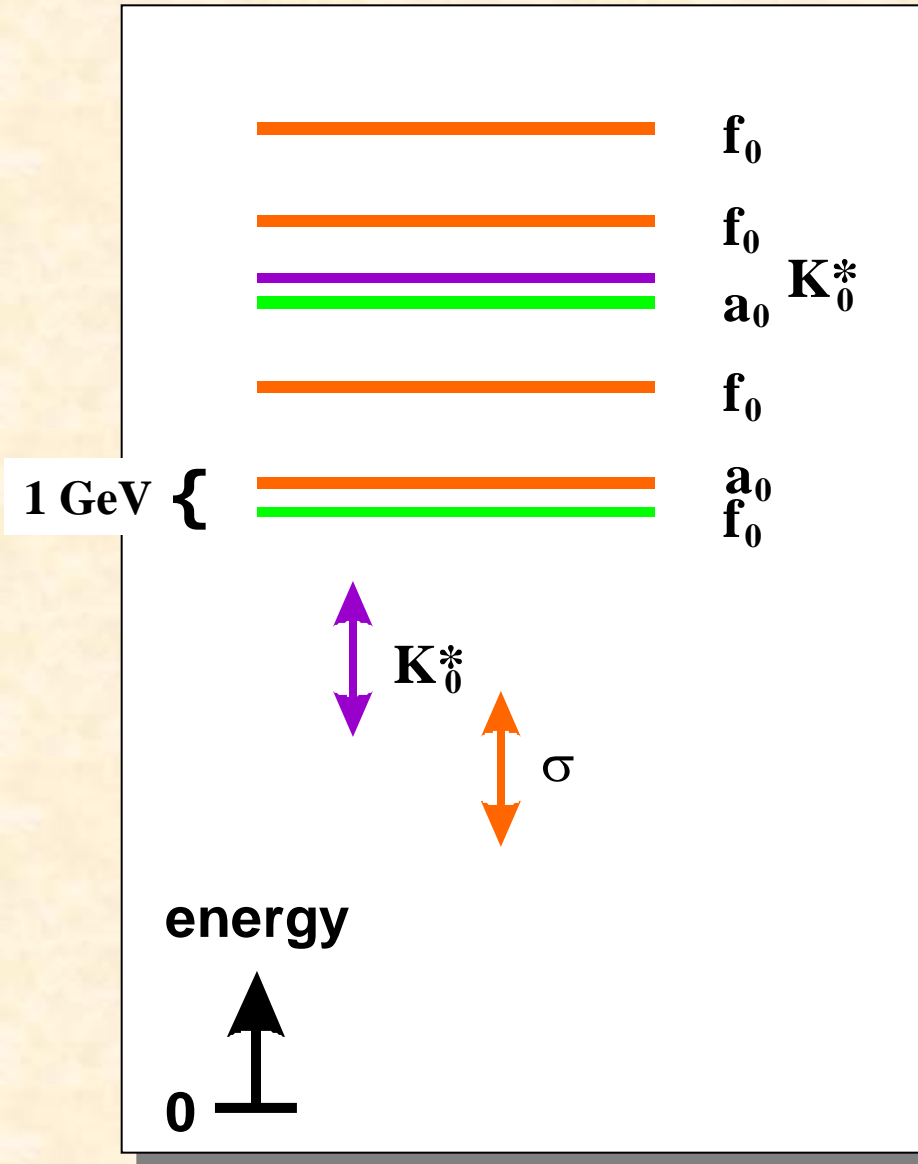
Scalar mesons



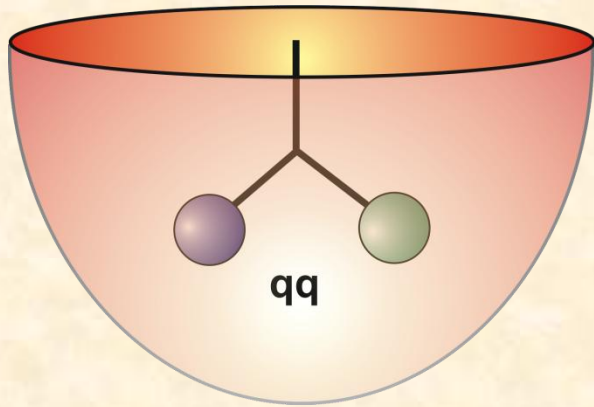
Scalar mesons



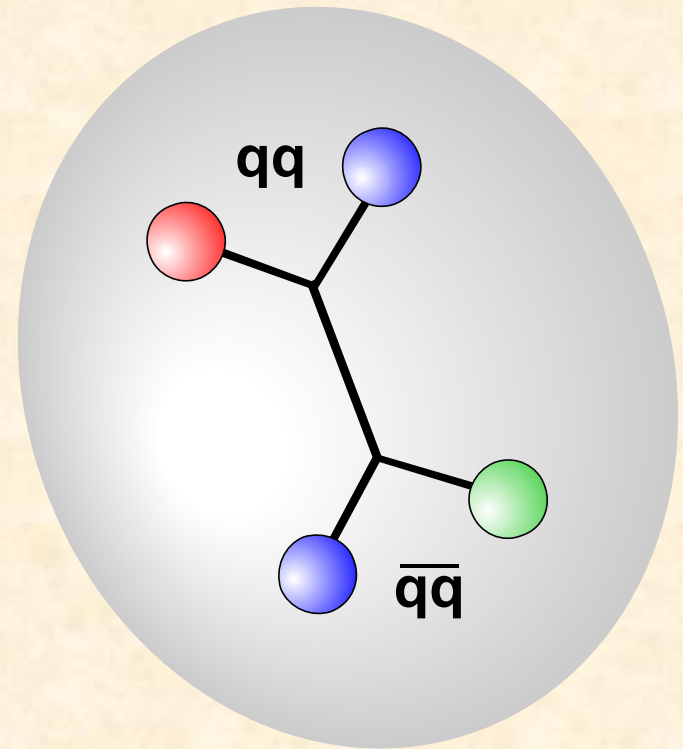
Scalar multiplet



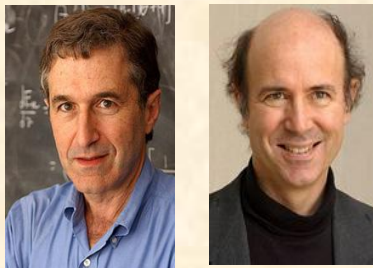
diquarks: color



tetraquark



Jaffe & Wilczek



Scalar diquarks

[ud] [us] [ds]
[cd] [cu] [cs]

Scalar meson multiplets

$q\bar{q}$

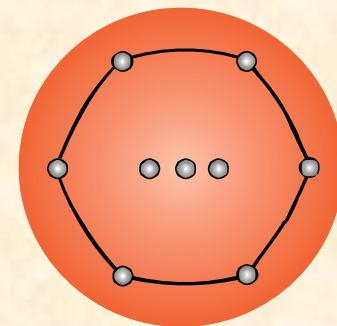
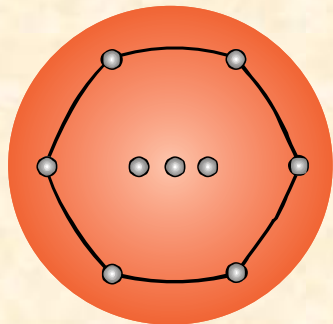
$q\bar{q}q\bar{q}$

$\bar{s}s$ ————— f_0
 $\bar{s}n$ ————— K_0
 $\bar{n}n$ ————— a_0/f_0

$\bar{s}s\bar{n}n$ ————— a_0/f_0
 $\bar{s}n\bar{n}n$ ————— K_0 \mathbf{K}
 $\bar{n}n\bar{n}n$ ————— f_0 $\mathbf{\sigma}$

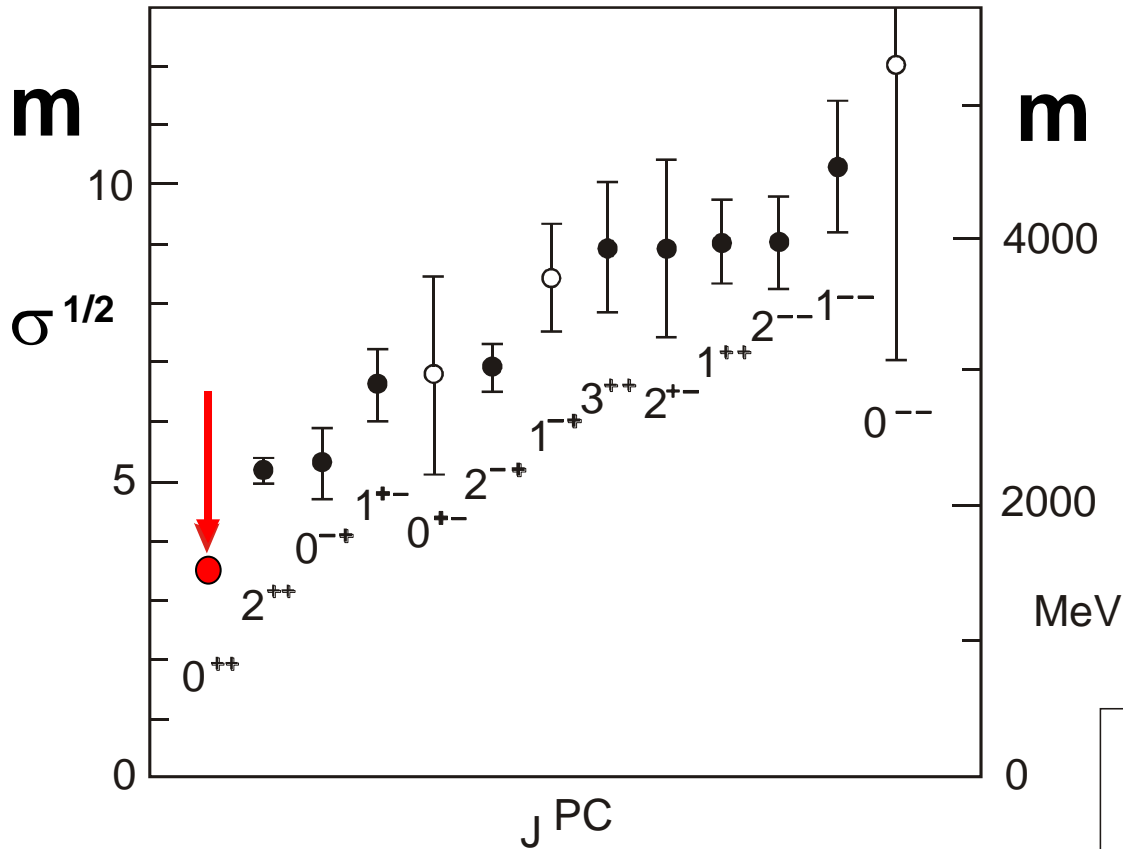
$n = u, d$

Jaffe



Lattice QCD

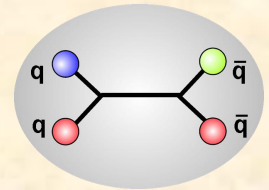
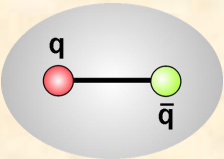
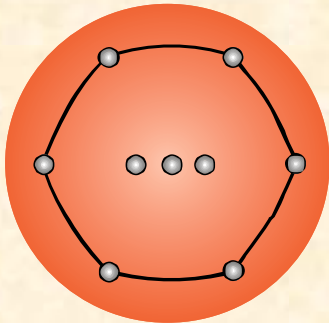
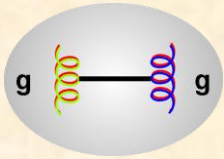
glueball spectrum in a world without quarks



UKQCD
GF11
MP
GF11 (reanal)

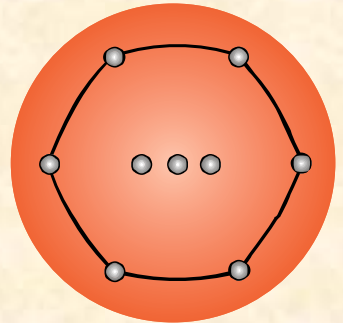
$$m = \begin{cases} 1568 \pm 89 \\ 1740 \pm 71 \\ 1630 \pm 100 \\ 1648 \pm 58 \end{cases}$$

Scalar mesons



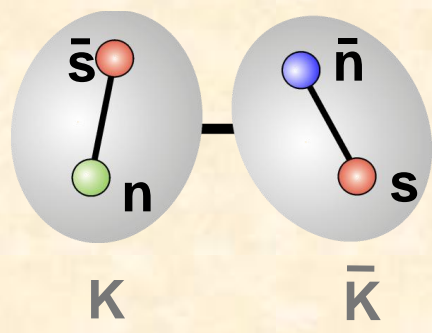
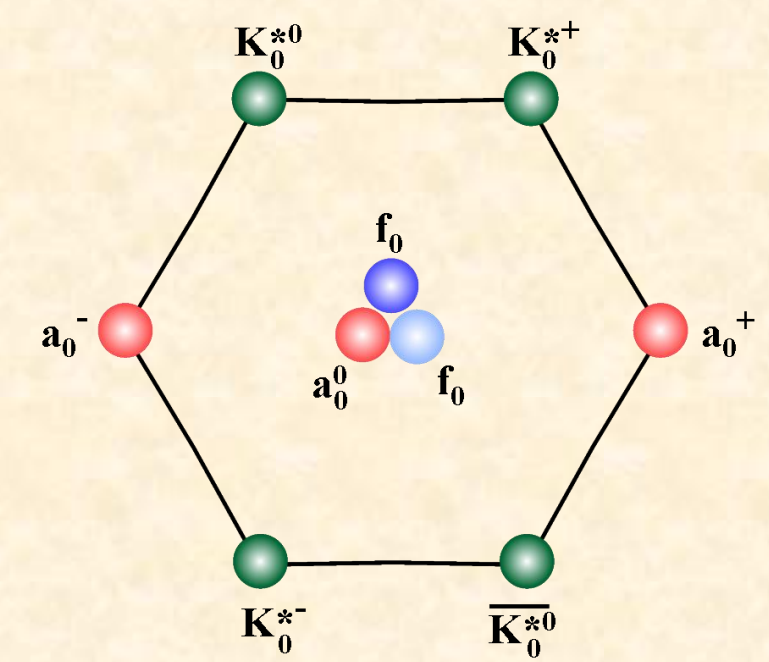
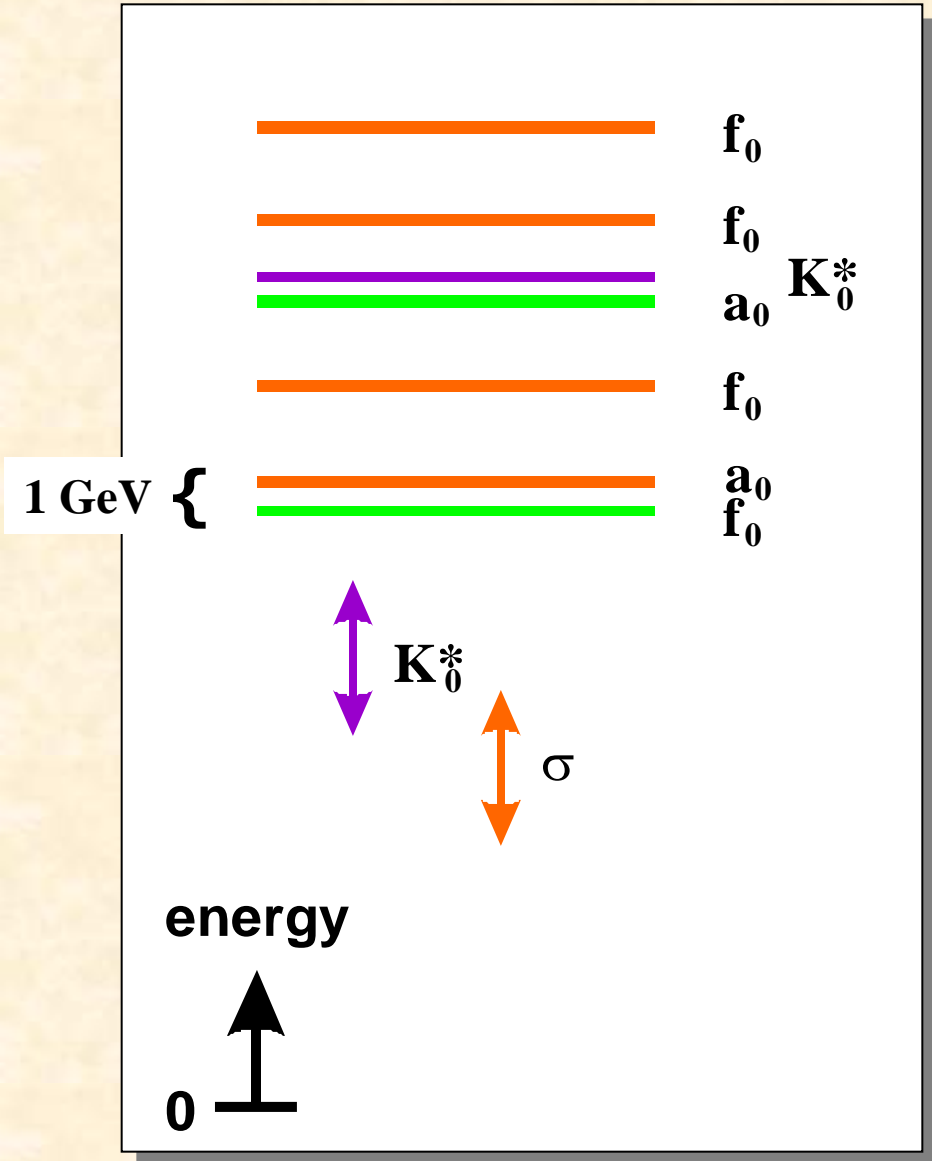
gg	—————	f_0
$\bar{s}s$	—————	f_0
$\bar{s}n$	—————	K_0
$\bar{n}n$	—————	a_0/f_0

$\bar{s}s\bar{n}n$	—————	a_0/f_0
$\bar{s}n\bar{n}n$	—————	K_0 \mathbf{K}
$\bar{n}n\bar{n}n$	—————	f_0 $\mathbf{\sigma}$

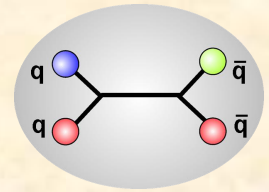
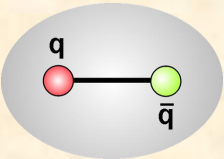
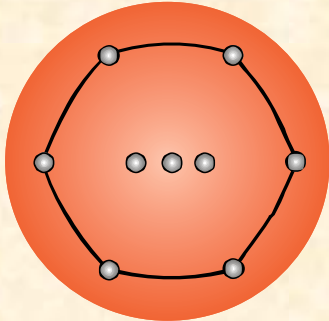
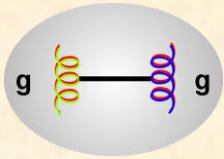


$n = u, d$

Scalar multiplet

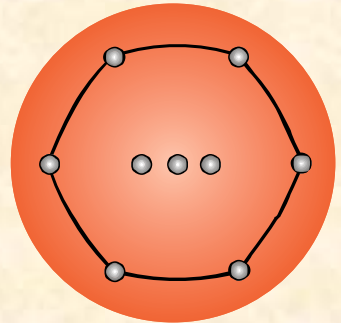


Scalar mesons



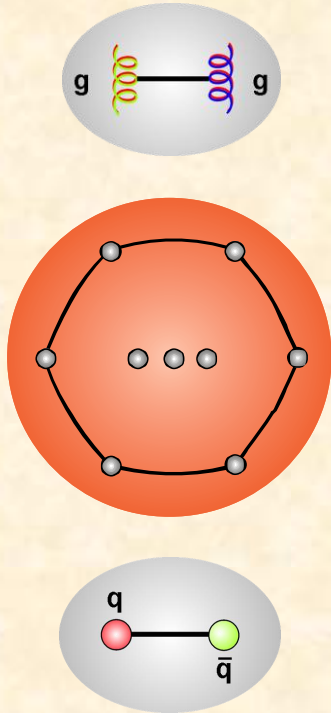
gg	—————	f_0
$\bar{s}s$	—————	f_0
$\bar{s}n$	—————	K_0
$\bar{n}n$	—————	a_0/f_0

$\bar{s}s\bar{n}n$	—————	a_0/f_0
$\bar{s}n\bar{n}n$	—————	K_0 \mathbf{K}
$\bar{n}n\bar{n}n$	—————	f_0 $\mathbf{\sigma}$



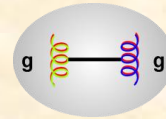
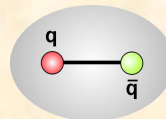
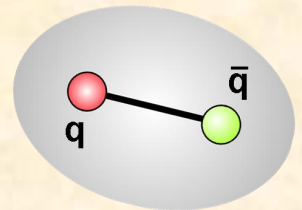
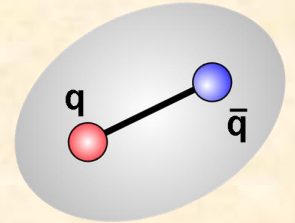
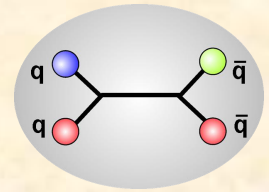
$n = u, d$

Scalar mesons

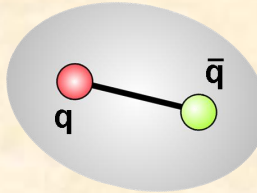
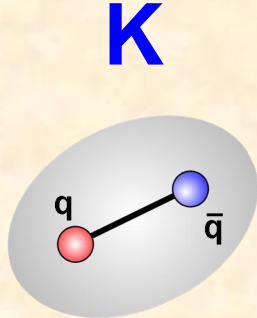
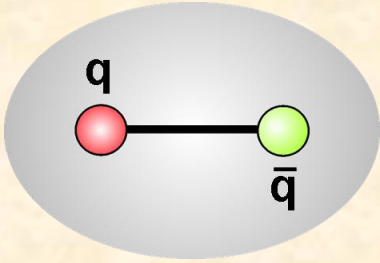


gg ————— f_0
 $\bar{s}s$ ————— f_0
 $\bar{s}n$ ————— K_0
 $\bar{n}n$ ————— a_0/f_0

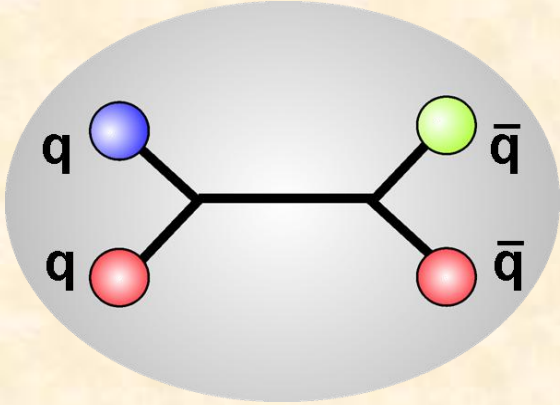
$\bar{s}s\bar{n}n$ ————— a_0/f_0
 $\bar{s}n\bar{n}n$ ————— K_0 \mathbf{K}
 $\bar{n}n\bar{n}n$ ————— f_0 $\mathbf{\sigma}$



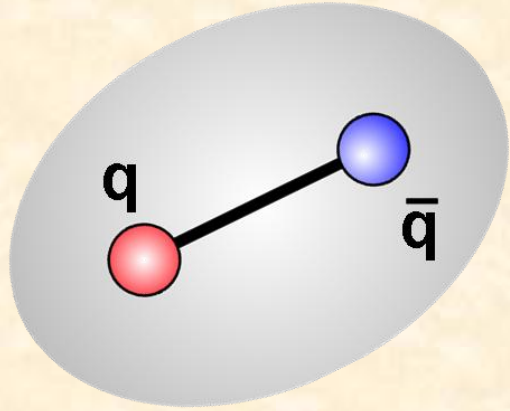
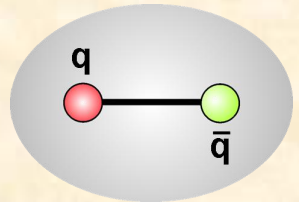
$f_0(980)$



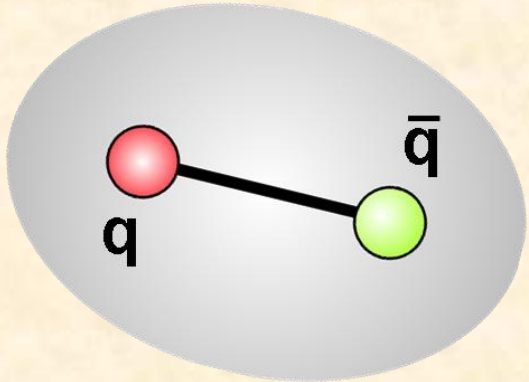
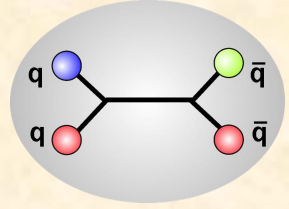
K-bar



$f_0(980)$



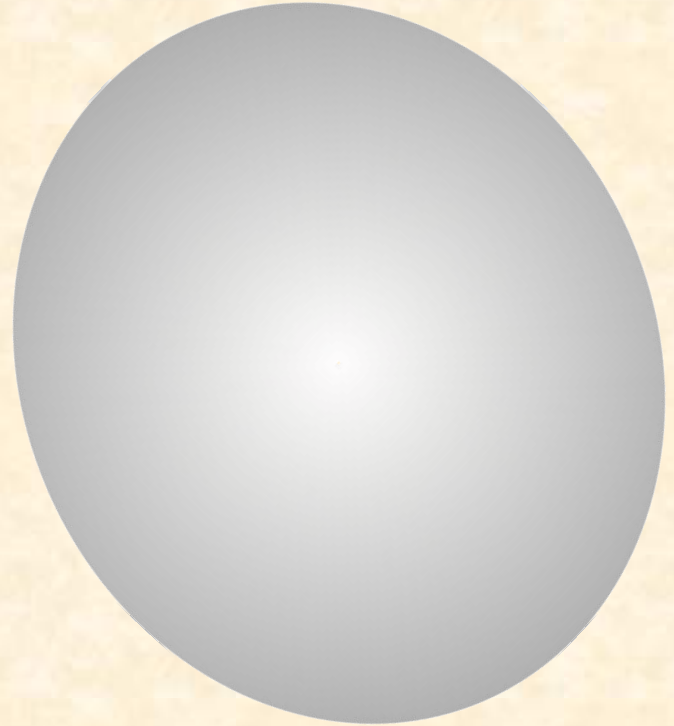
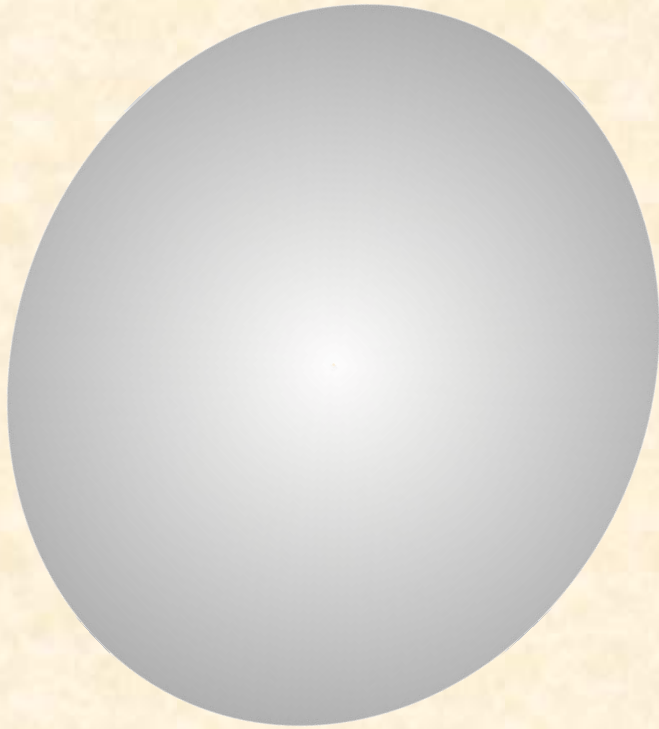
K



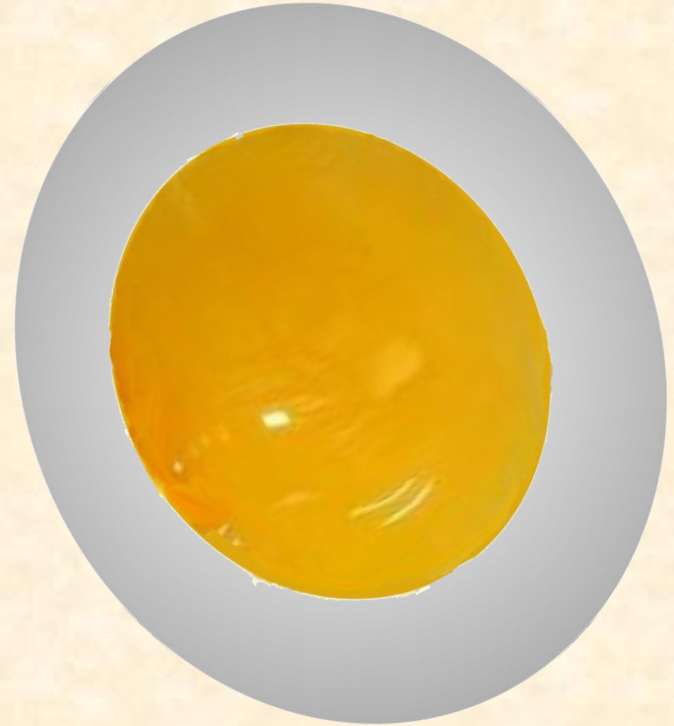
\bar{K}



Molecule v Quark State

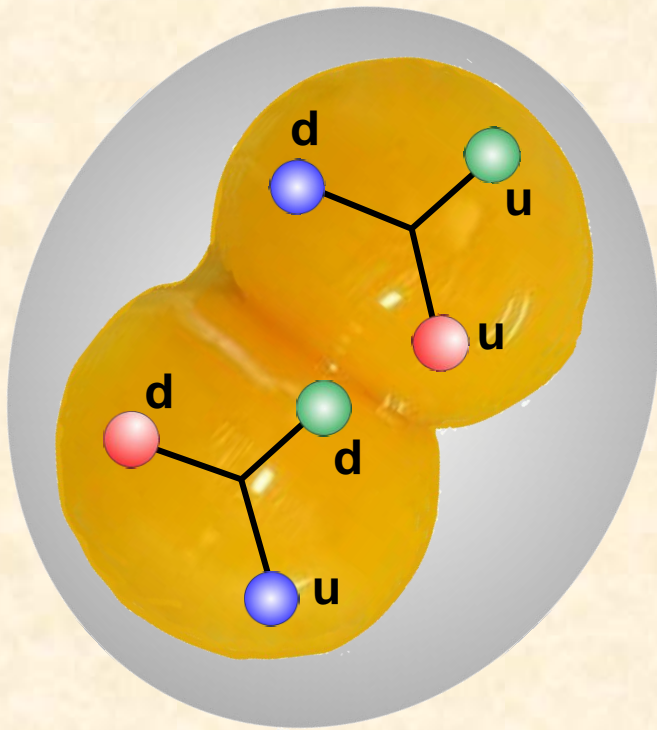


Molecule v Quark State

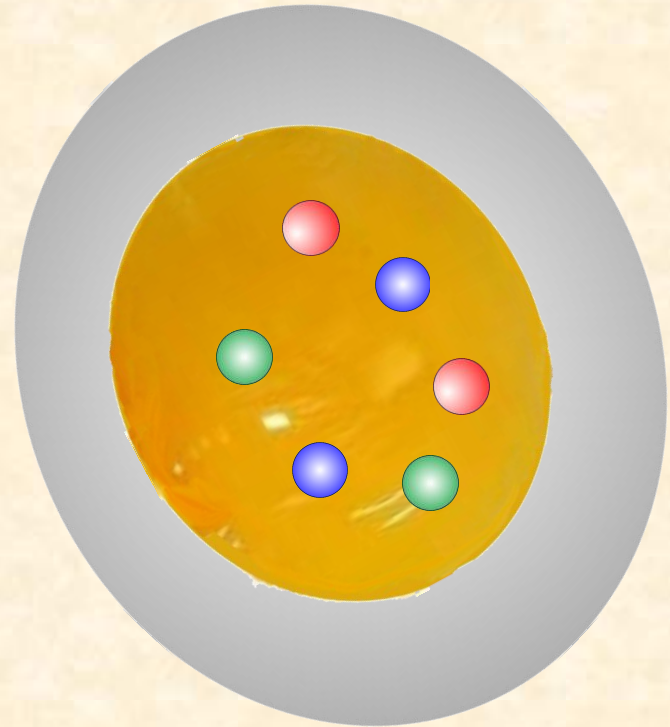


what is the deuteron?

Molecule v Quark State



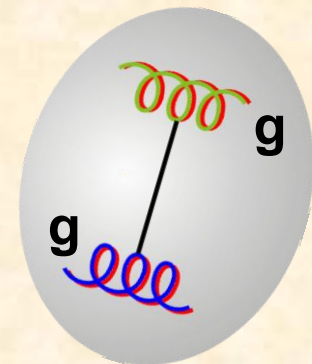
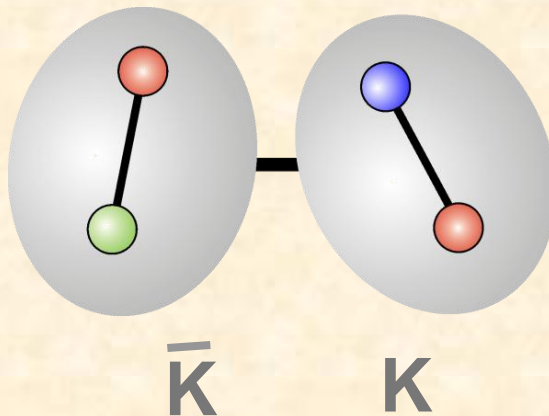
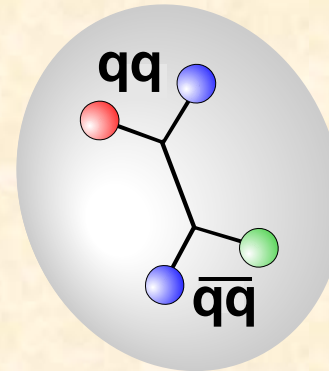
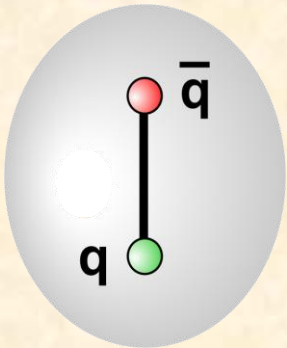
Weinberg



what is the deuteron?

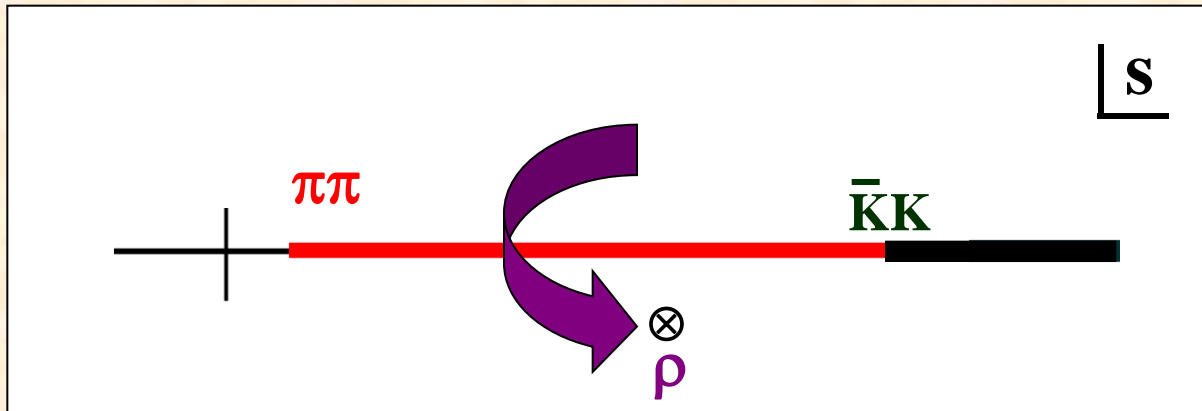
2 three or **1 six** quark bag ?

Can experiment distinguish between
a four quark state, a molecule,
a glueball or a $\bar{q}q$ meson ?



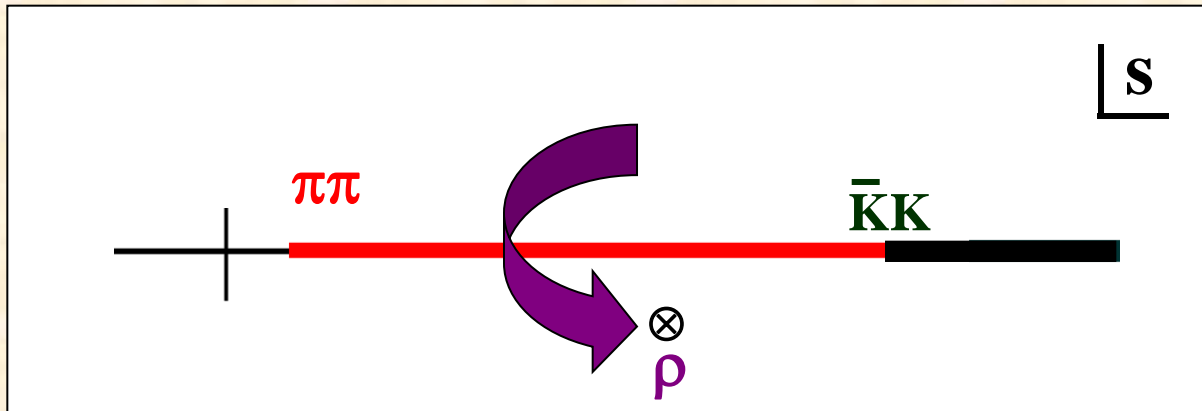
Vector meson

poles in complex plane



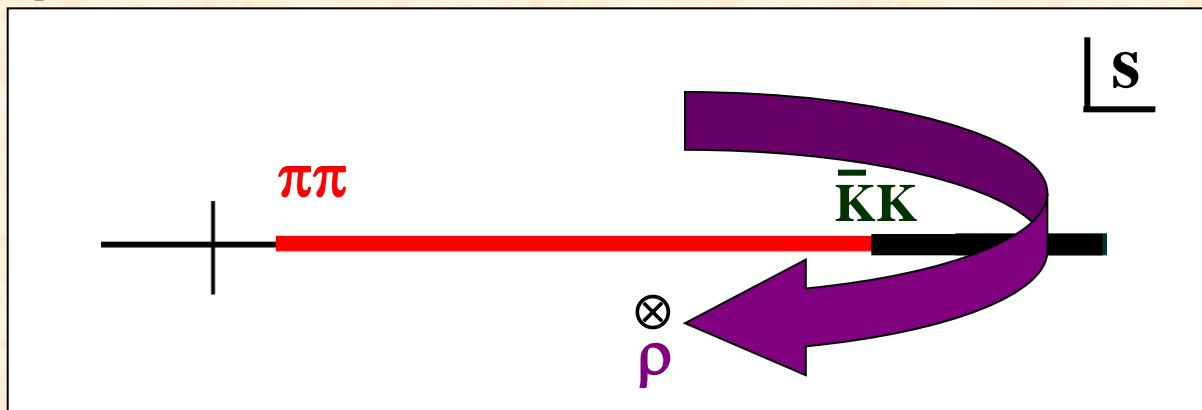
Vector meson

poles in complex plane



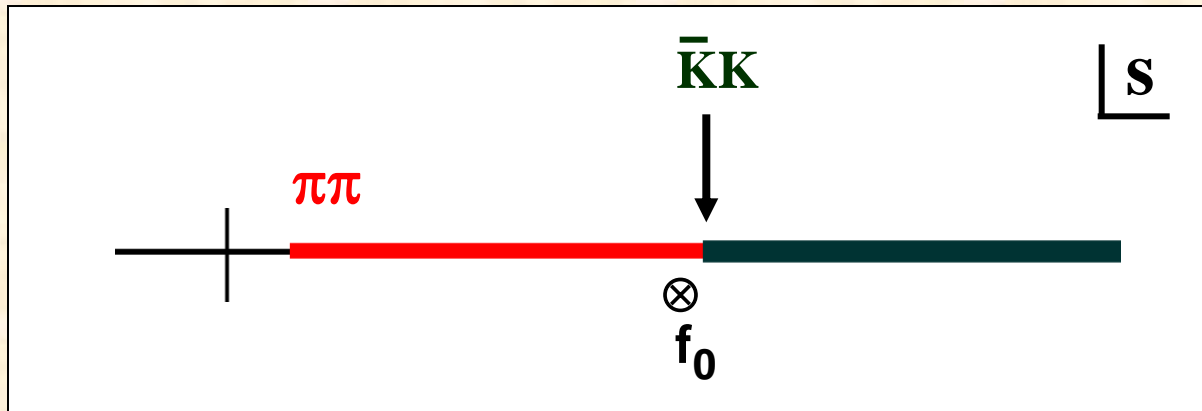
shadow pole

mirror pole



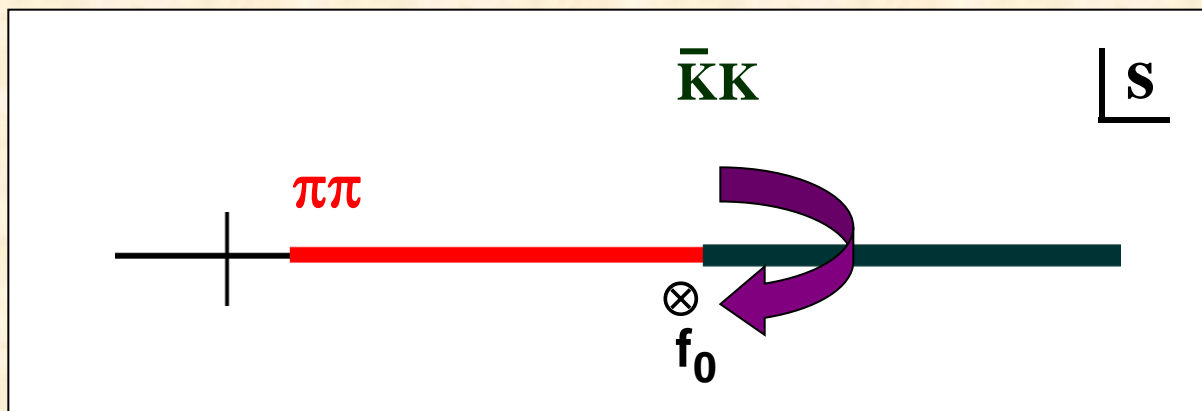
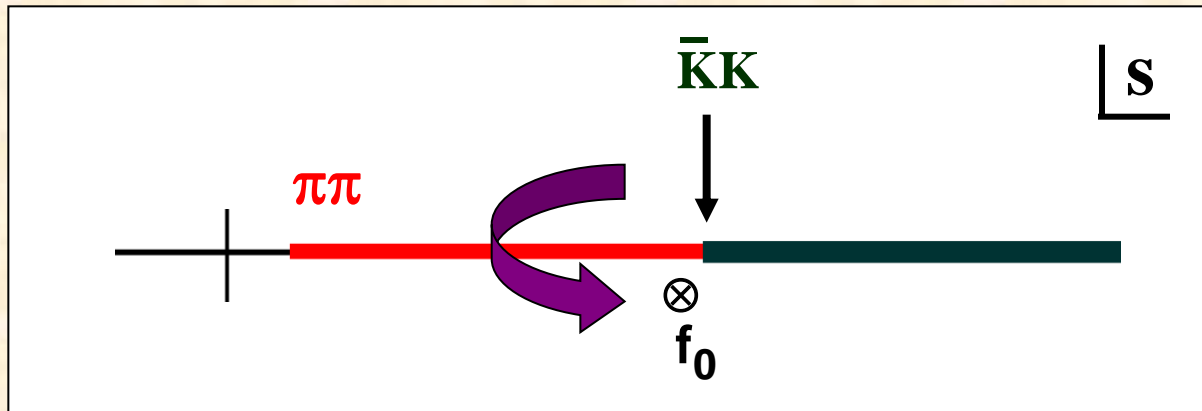
Scalar meson

poles in complex plane

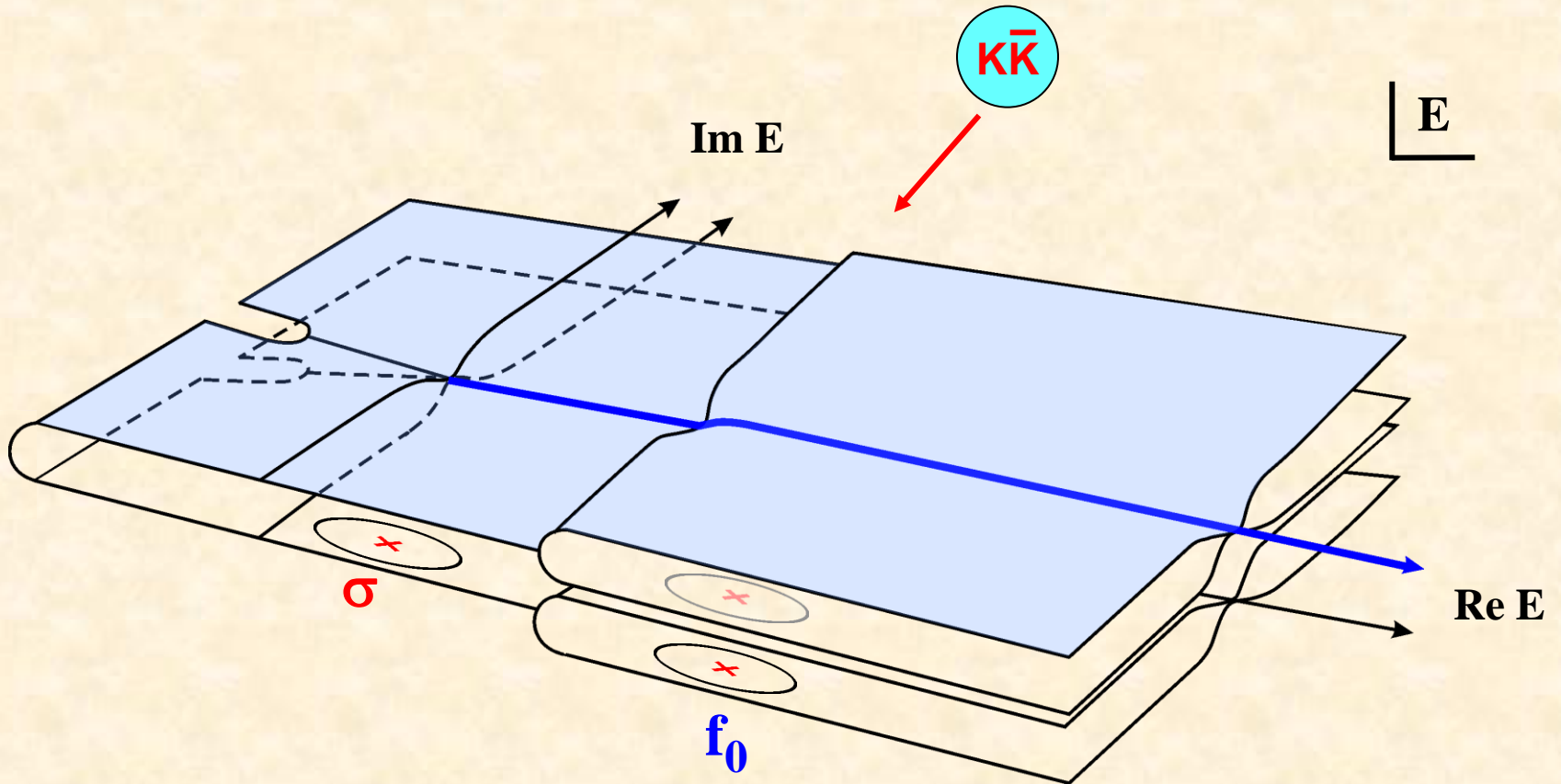


Scalar meson

poles in complex plane

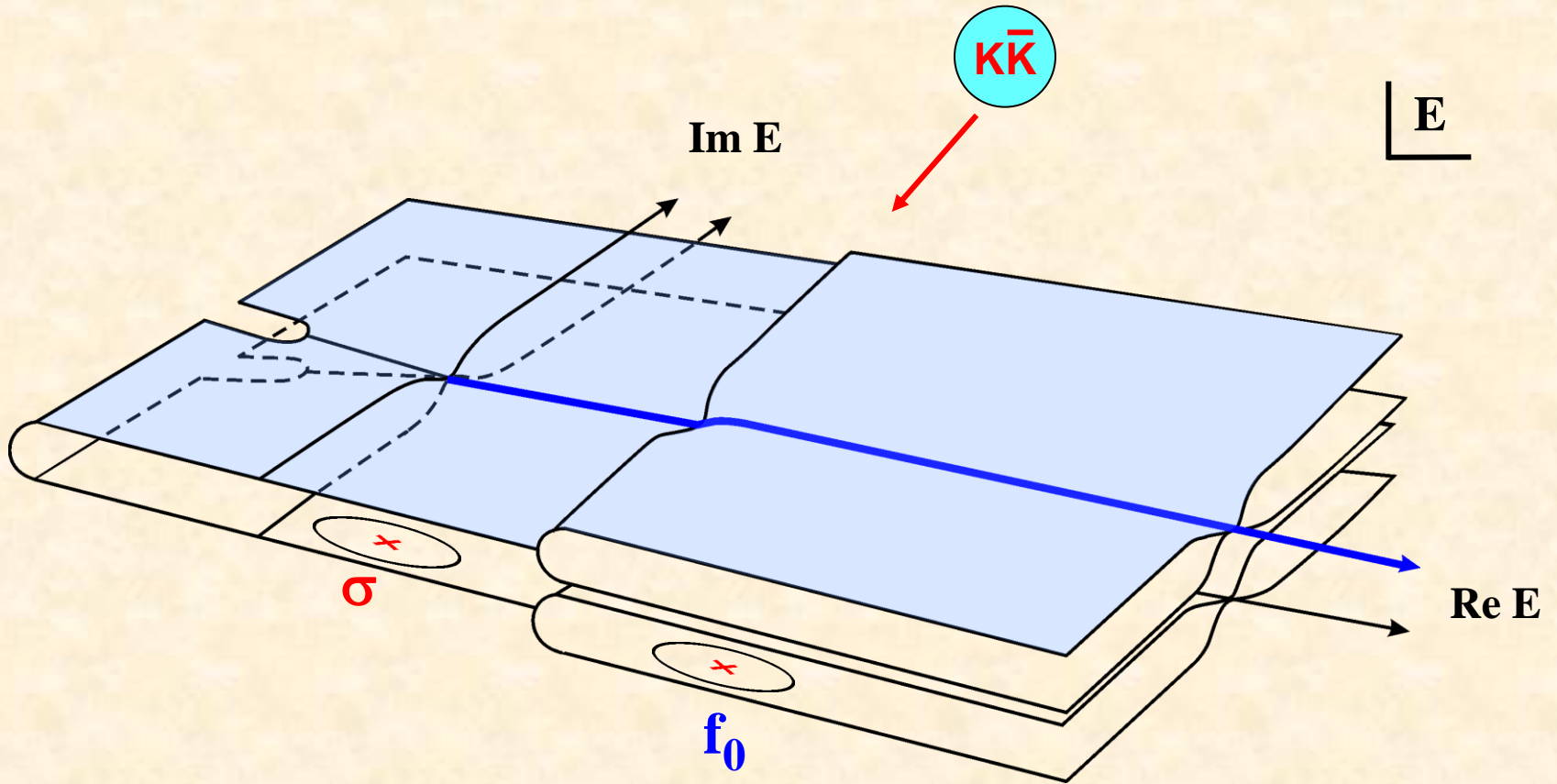


Quark state v Molecule



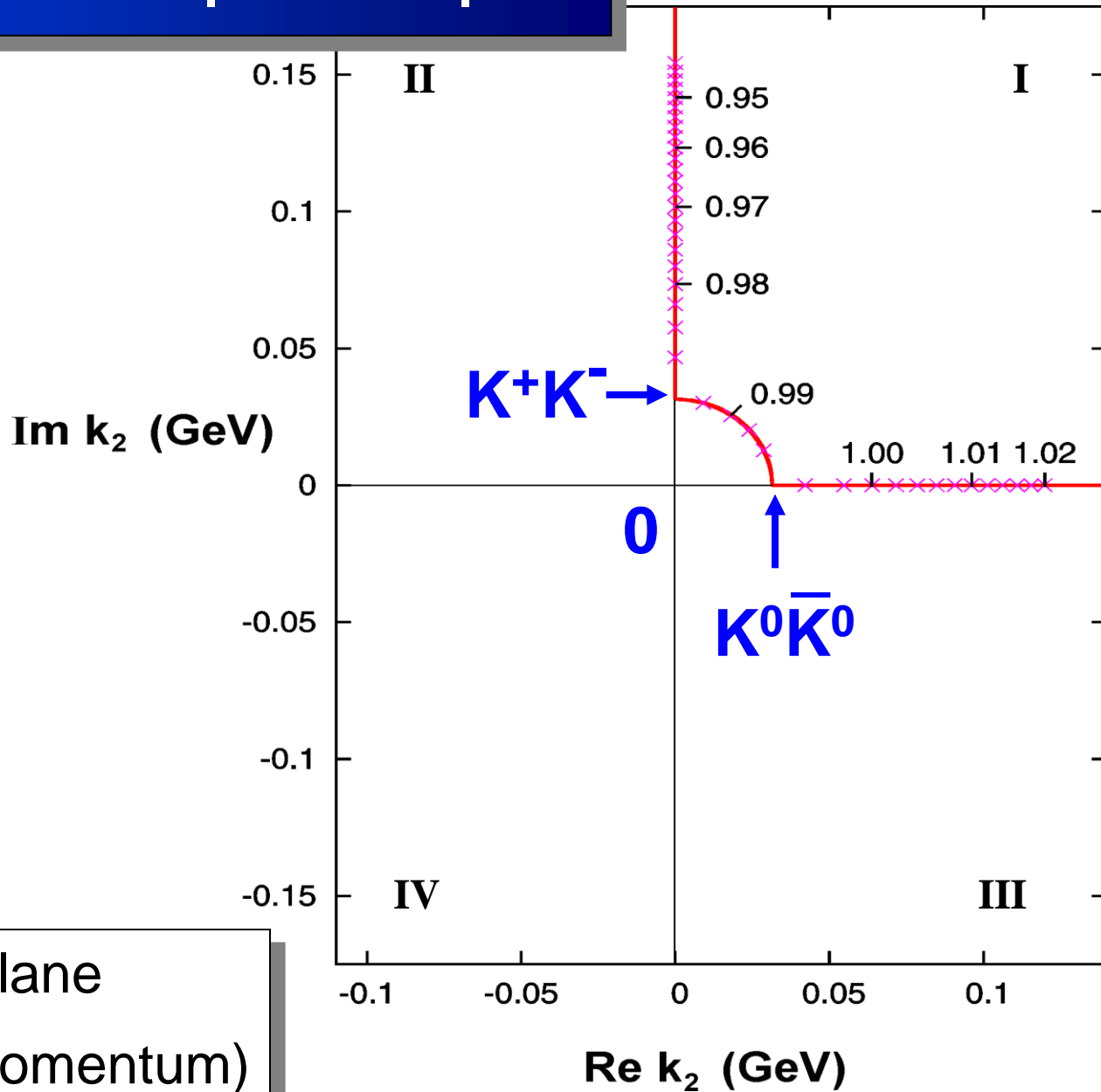
Weinberg
Morgan

Quark state v Molecule



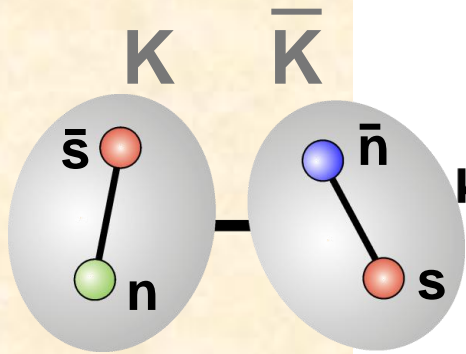
Weinberg
Morgan

Jost function: 1 pole v 2 pole

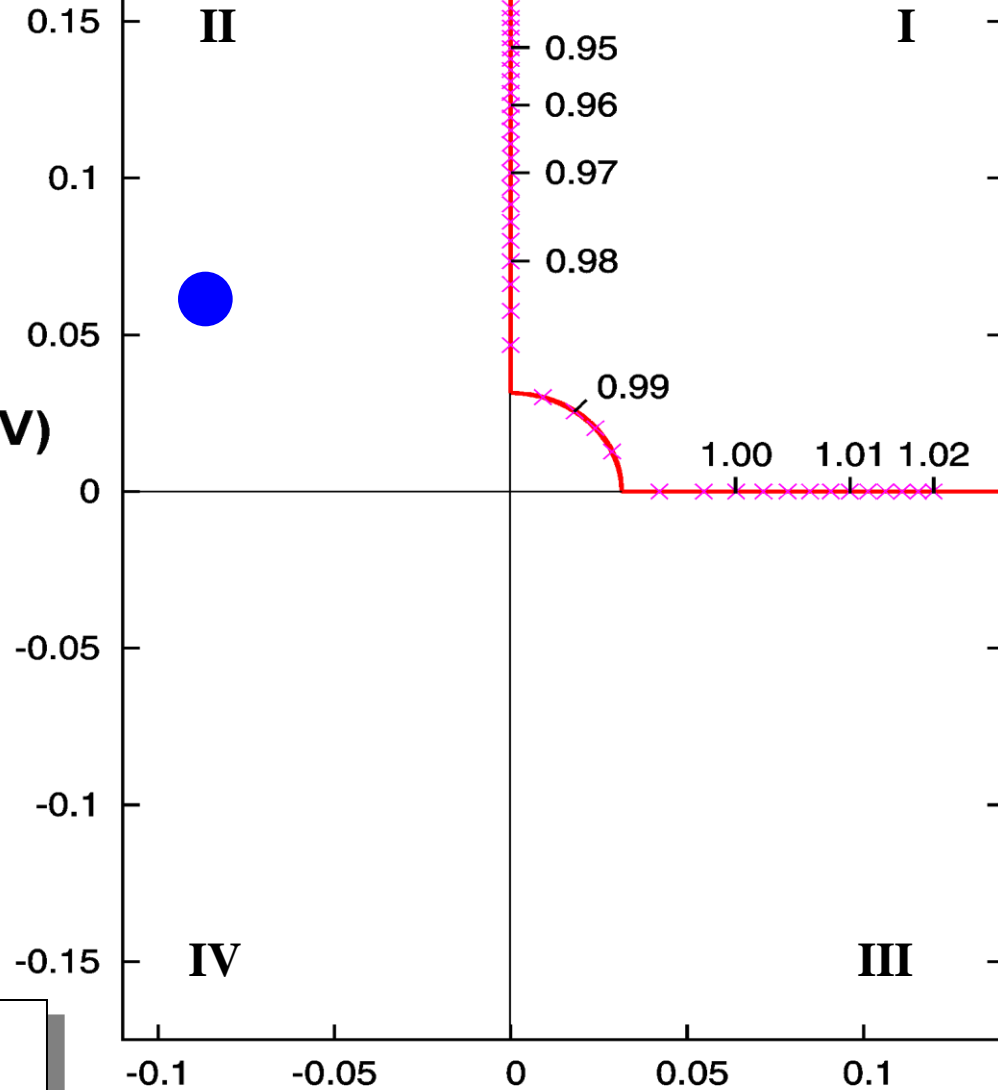


k_2 plane
($K\bar{K}$ c.m. momentum)

Jost function: 1 pole v 2 pole



k_2 (GeV)

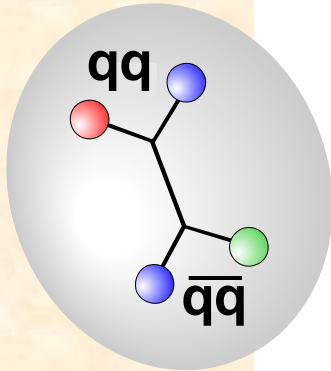
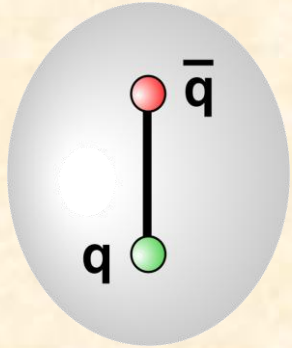


k_2 plane
($K\bar{K}$ c.m. momentum)

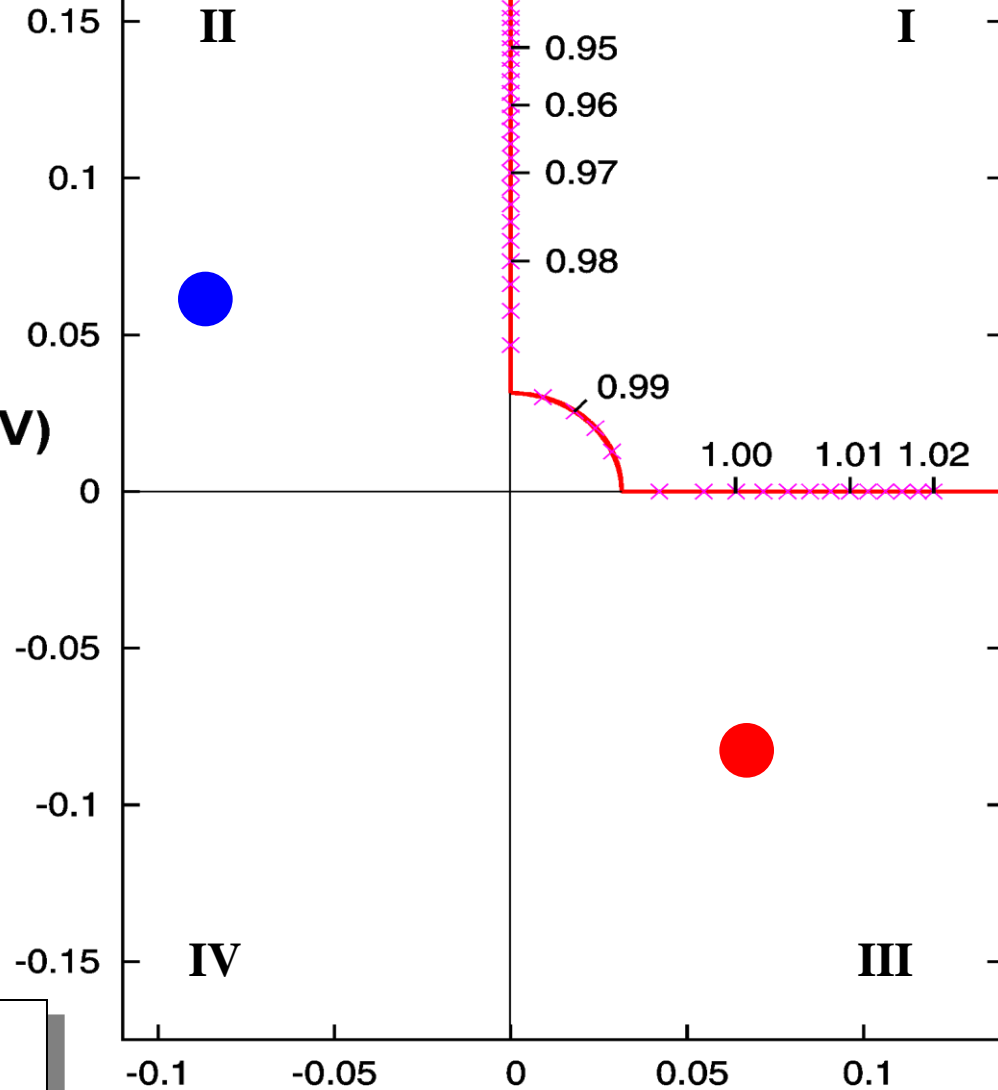
$\text{Re } k_2$ (GeV)

Weinberg
Morgan

Jost function: 1 pole v 2 pole



Im k_2 (GeV)

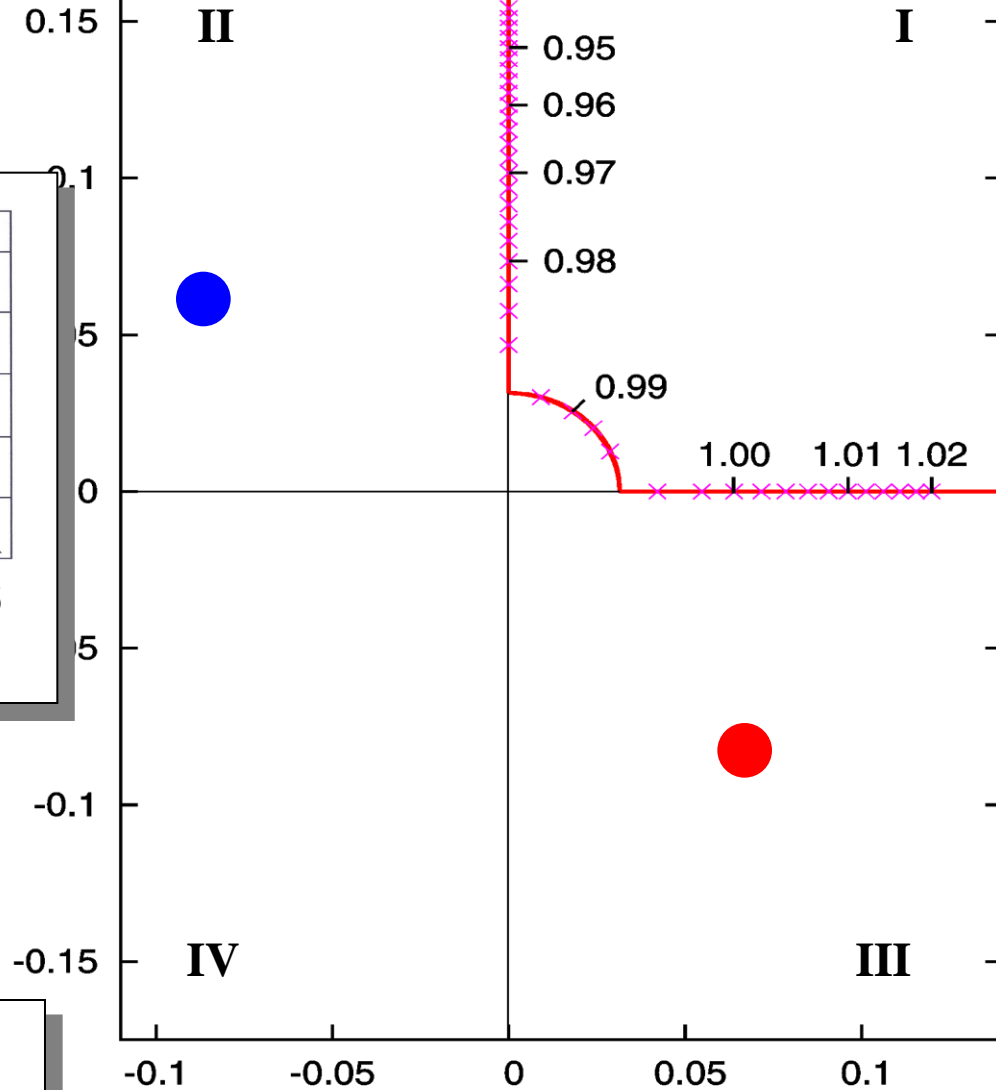
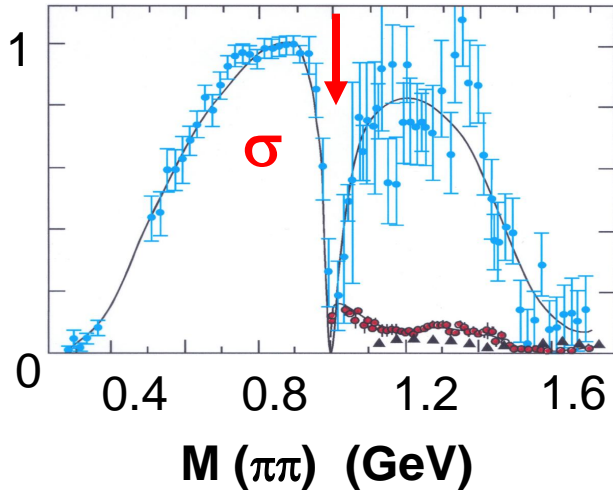


k_2 plane
($K\bar{K}$ c.m. momentum)

Weinberg
Morgan

Jost function: 1 pole v 2 pole

$f_0(980)$

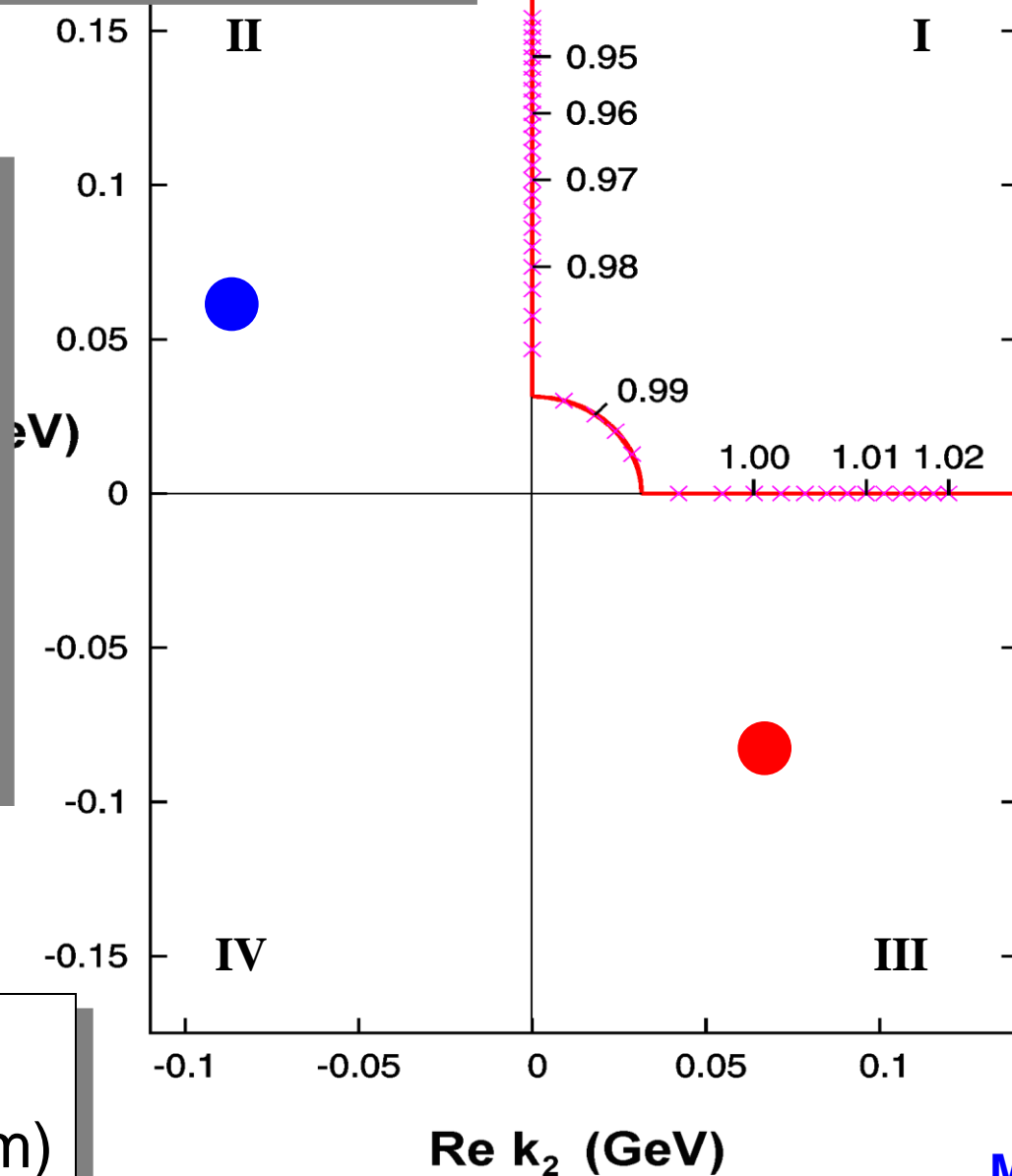
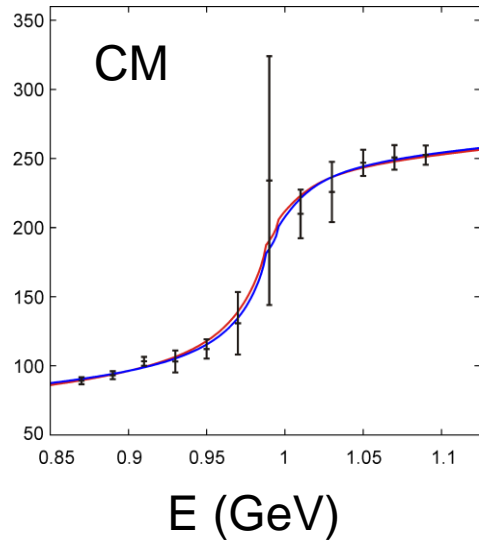


k_2 plane
($K\bar{K}$ c.m. momentum)

Weinberg
Morgan

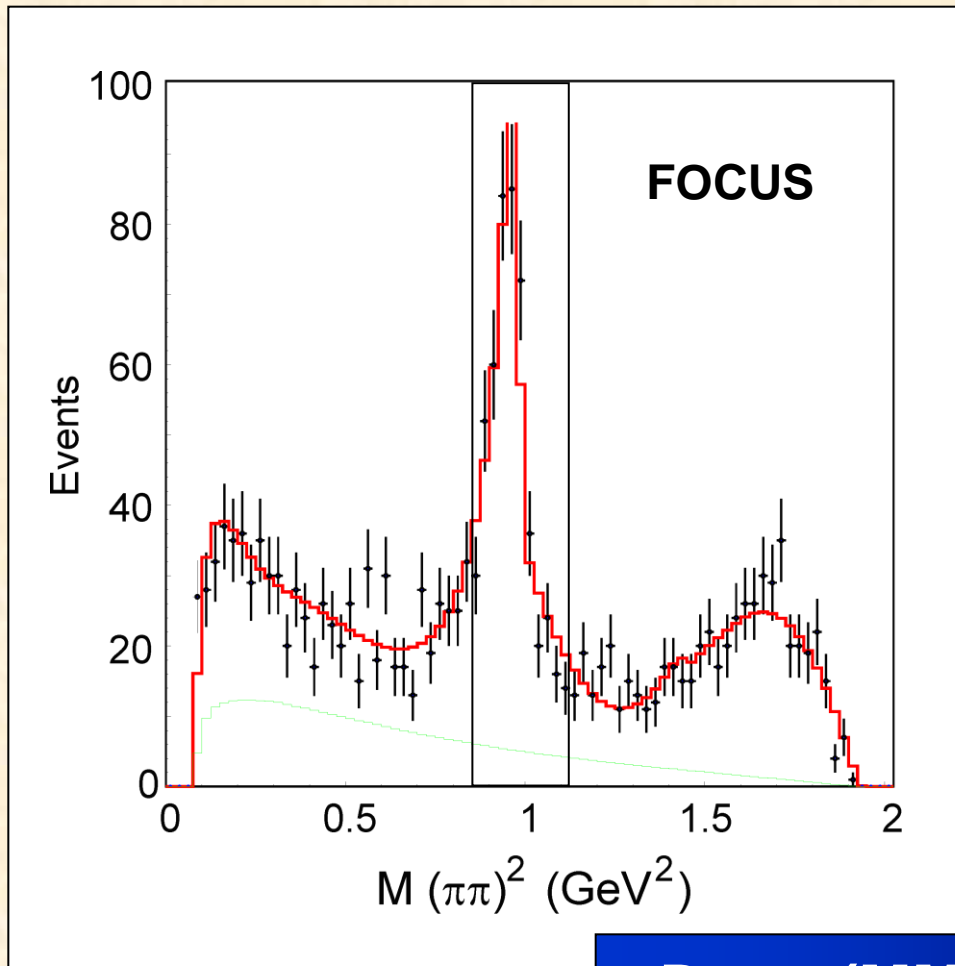
Jost function: 1 pole v 2 pole

$\pi\pi$ phase-shift

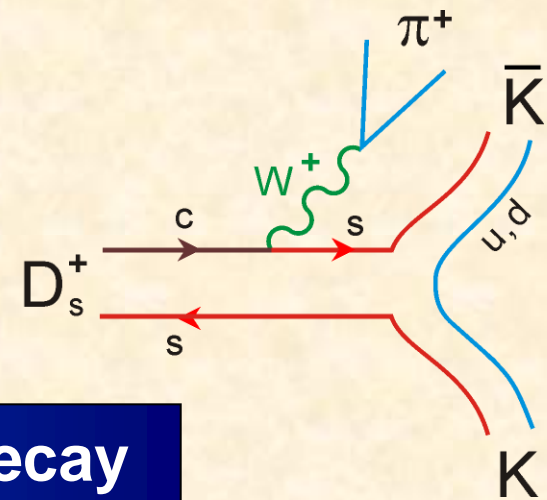
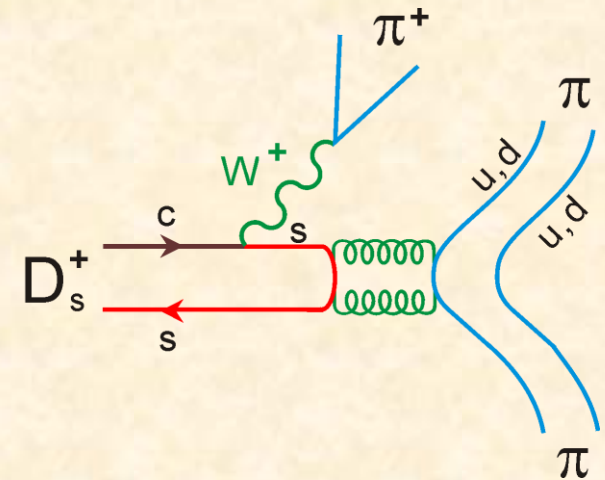


k_2 plane
($K\bar{K}$ c.m. momentum)

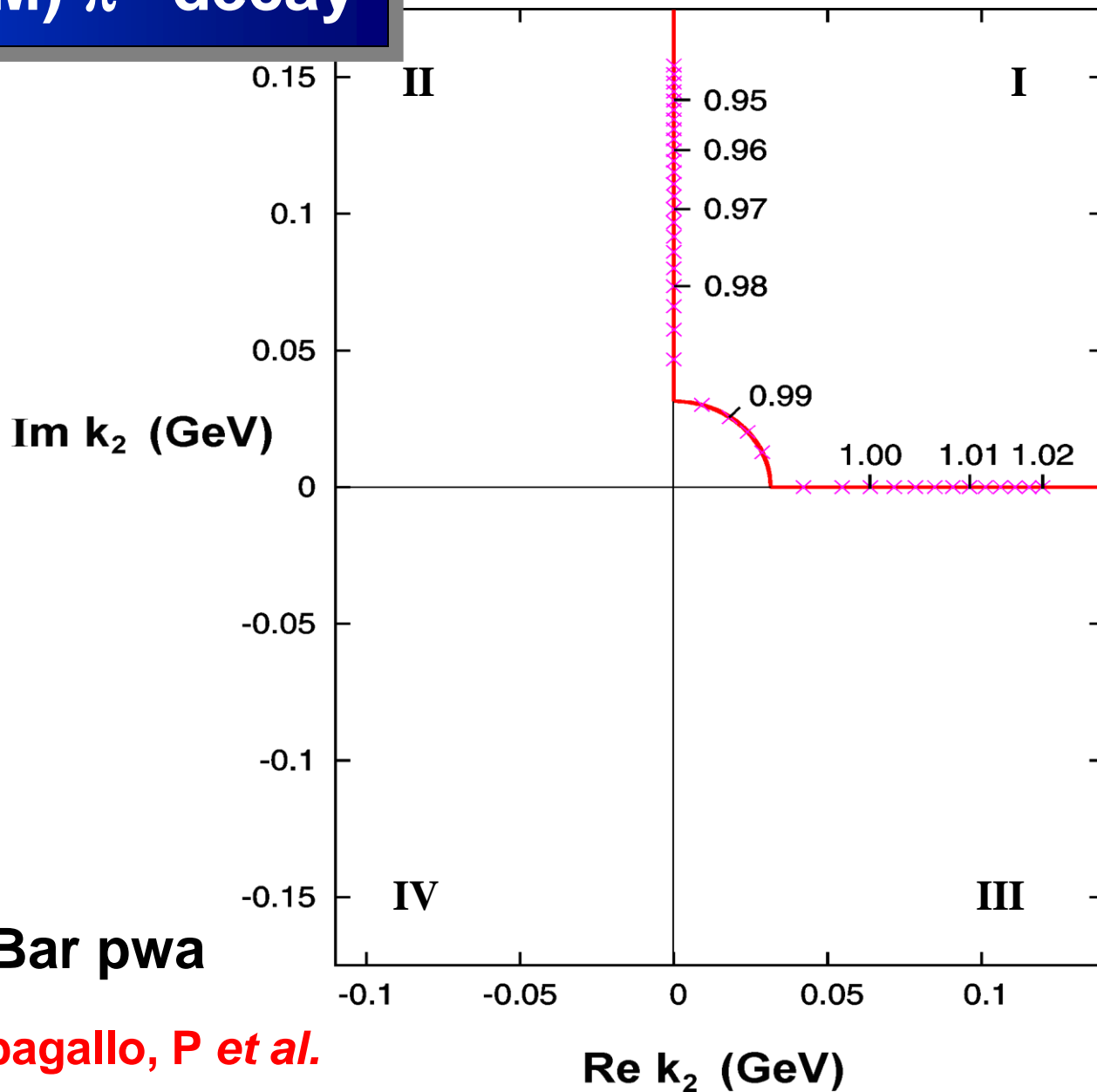
Heavy flavor decays



$D_s \rightarrow (MM) \pi$ decay



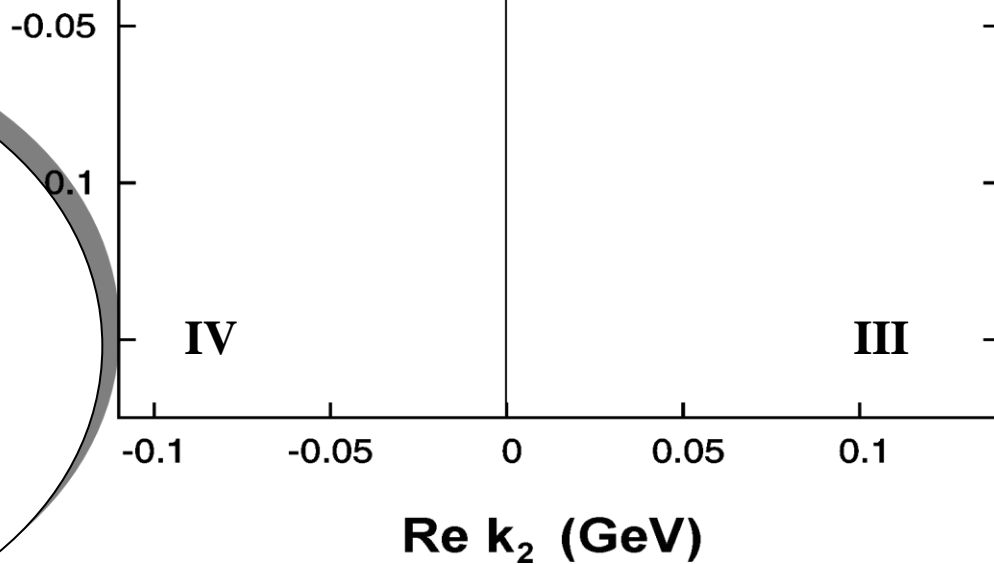
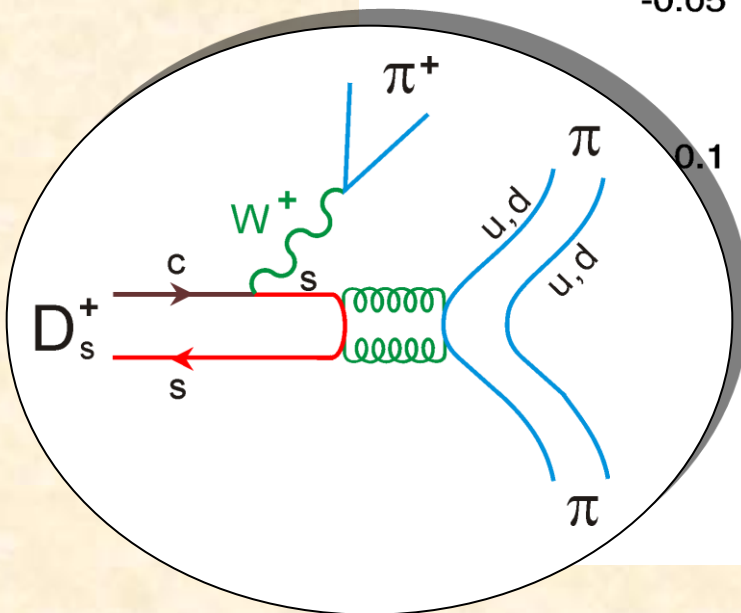
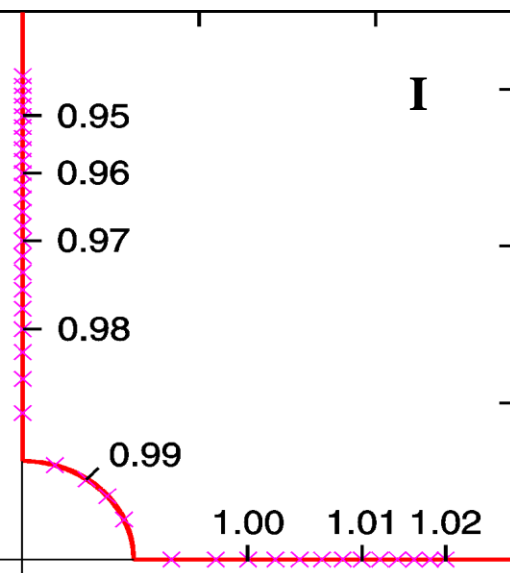
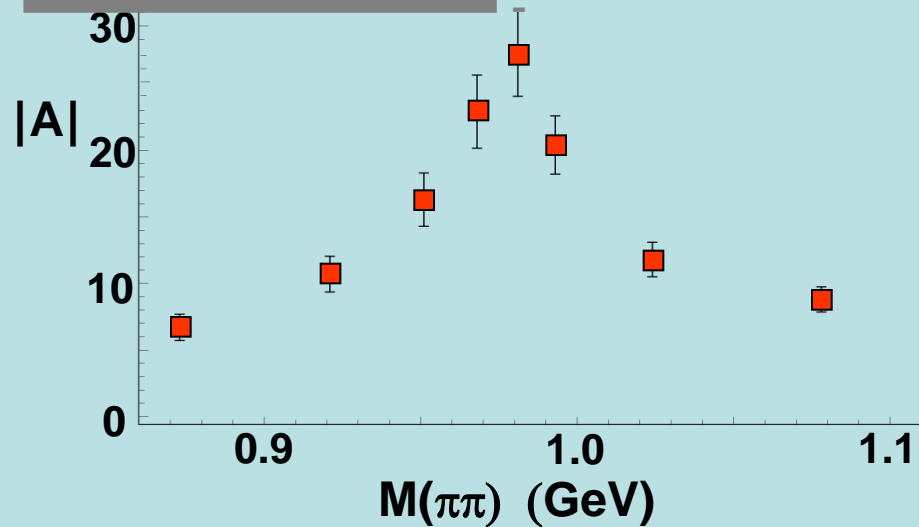
$D_s \rightarrow (MM) \pi$ decay



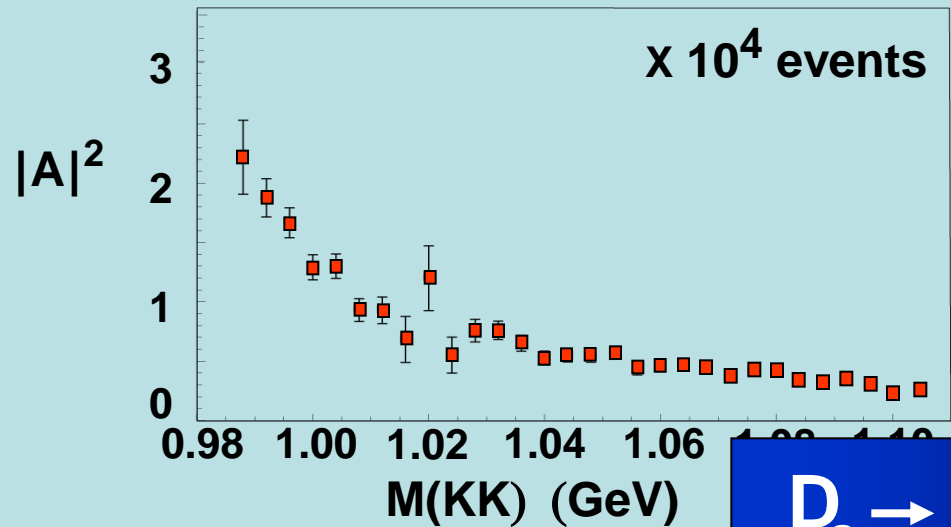
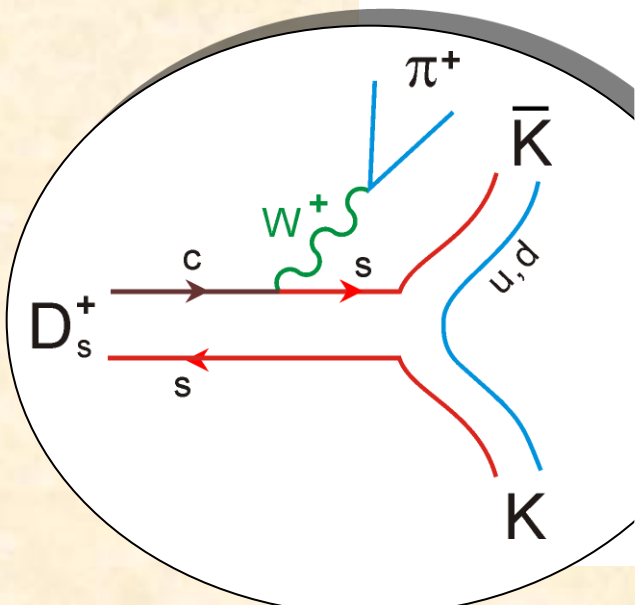
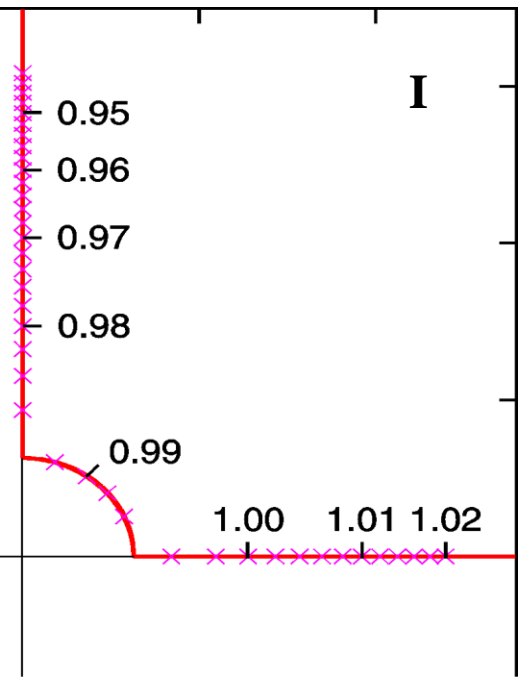
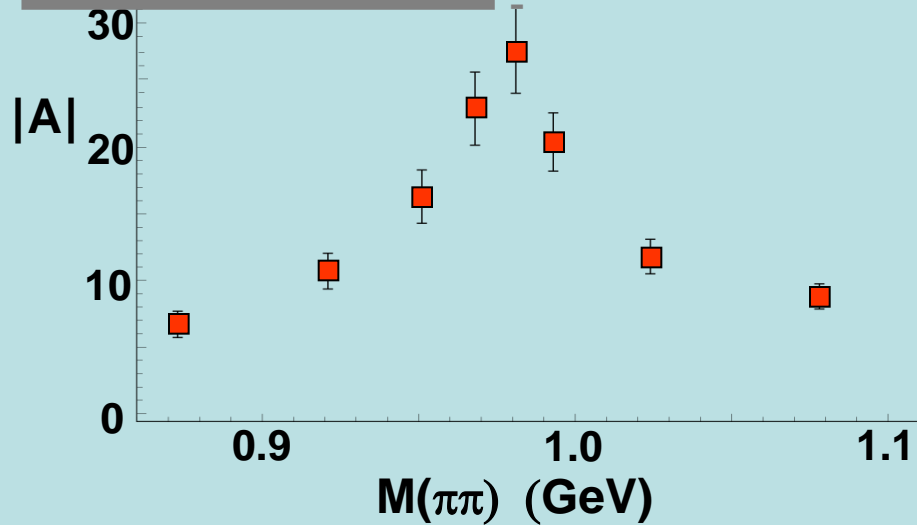
BaBar pwa

Pappagallo, P *et al.*

$$D_s \rightarrow \pi(\pi\pi)$$

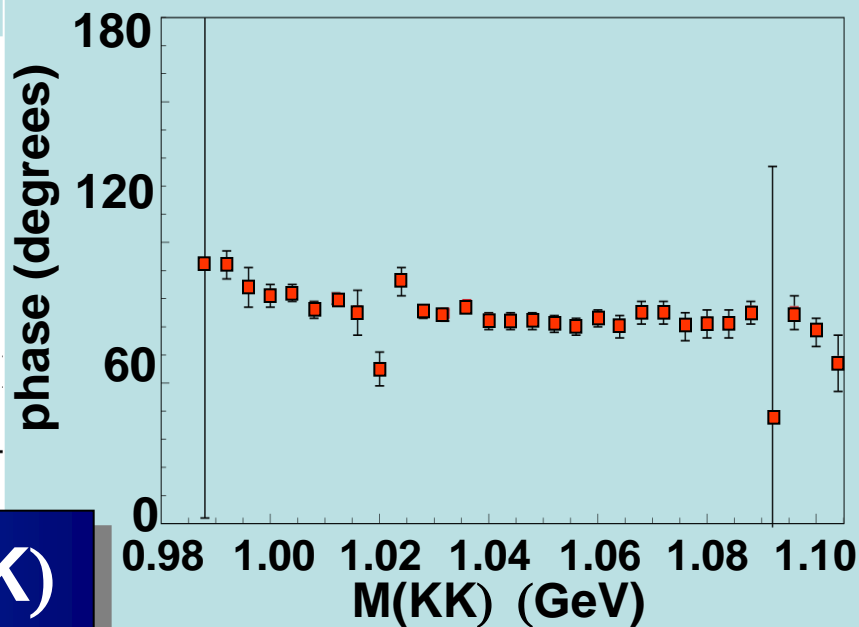
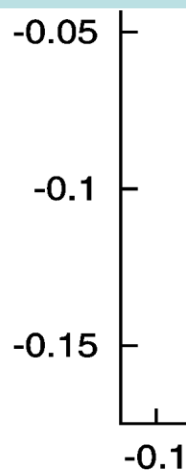
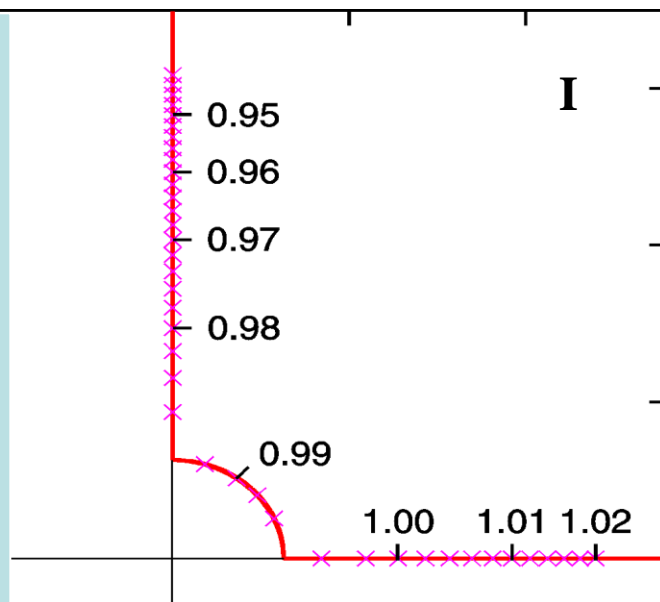
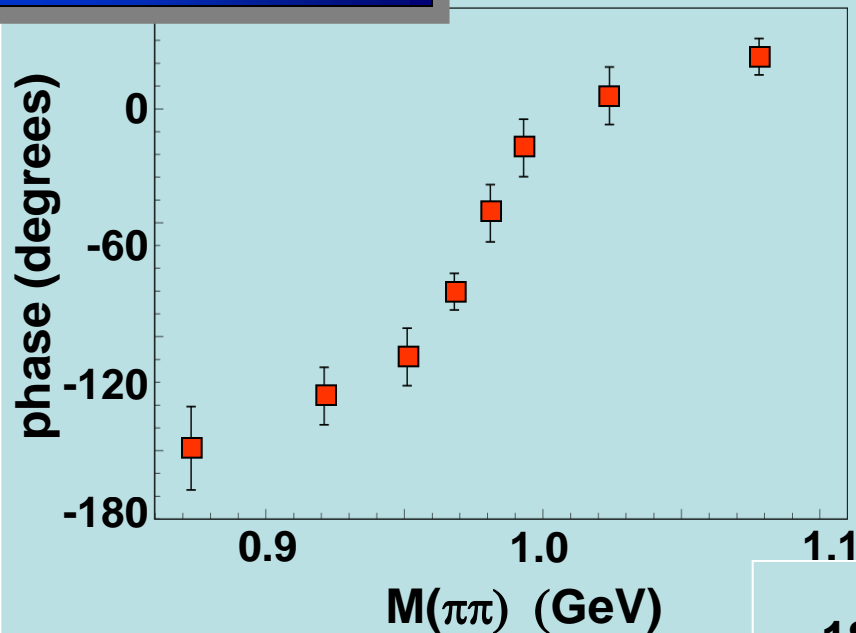


$D_s \rightarrow \pi(\pi\pi)$



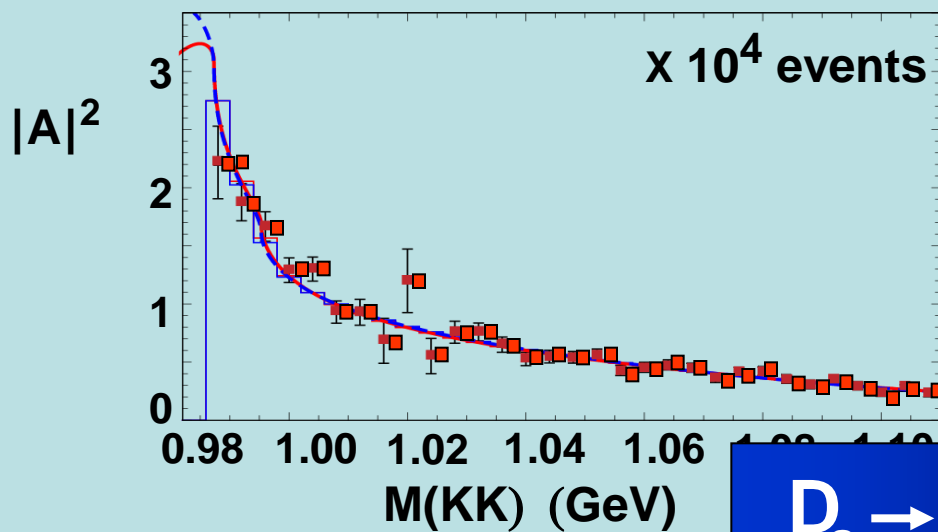
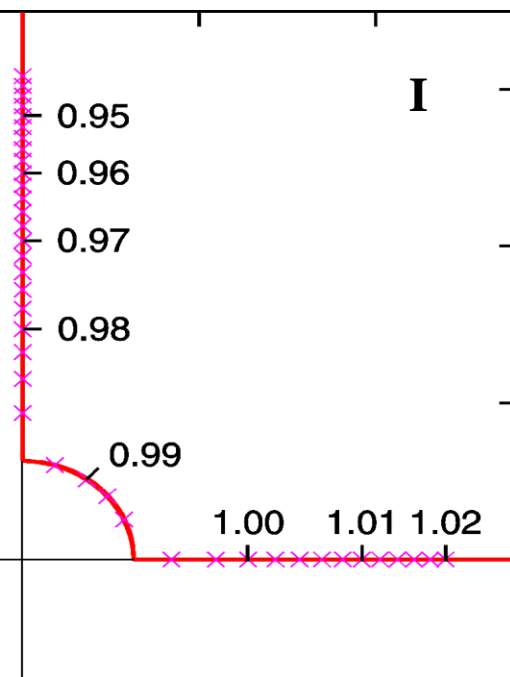
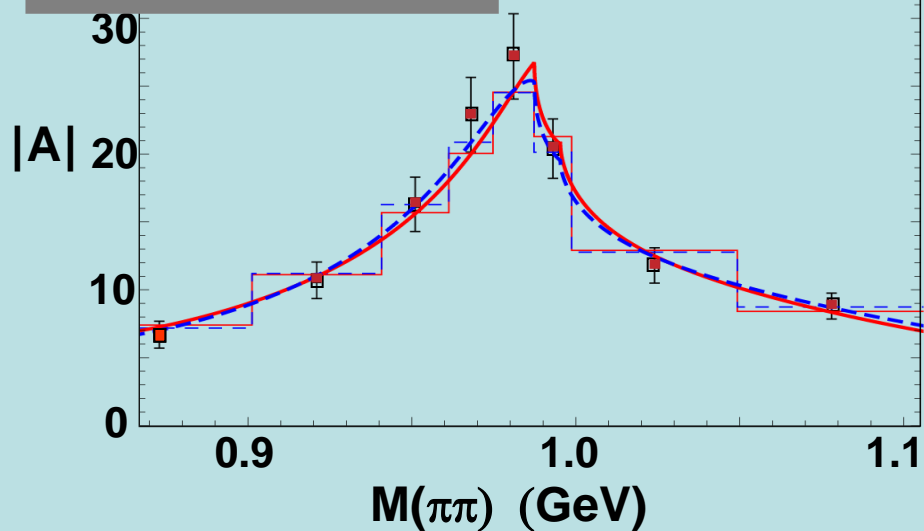
$D_s \rightarrow \pi(KK)$

$D_s \rightarrow \pi(\pi\pi)$



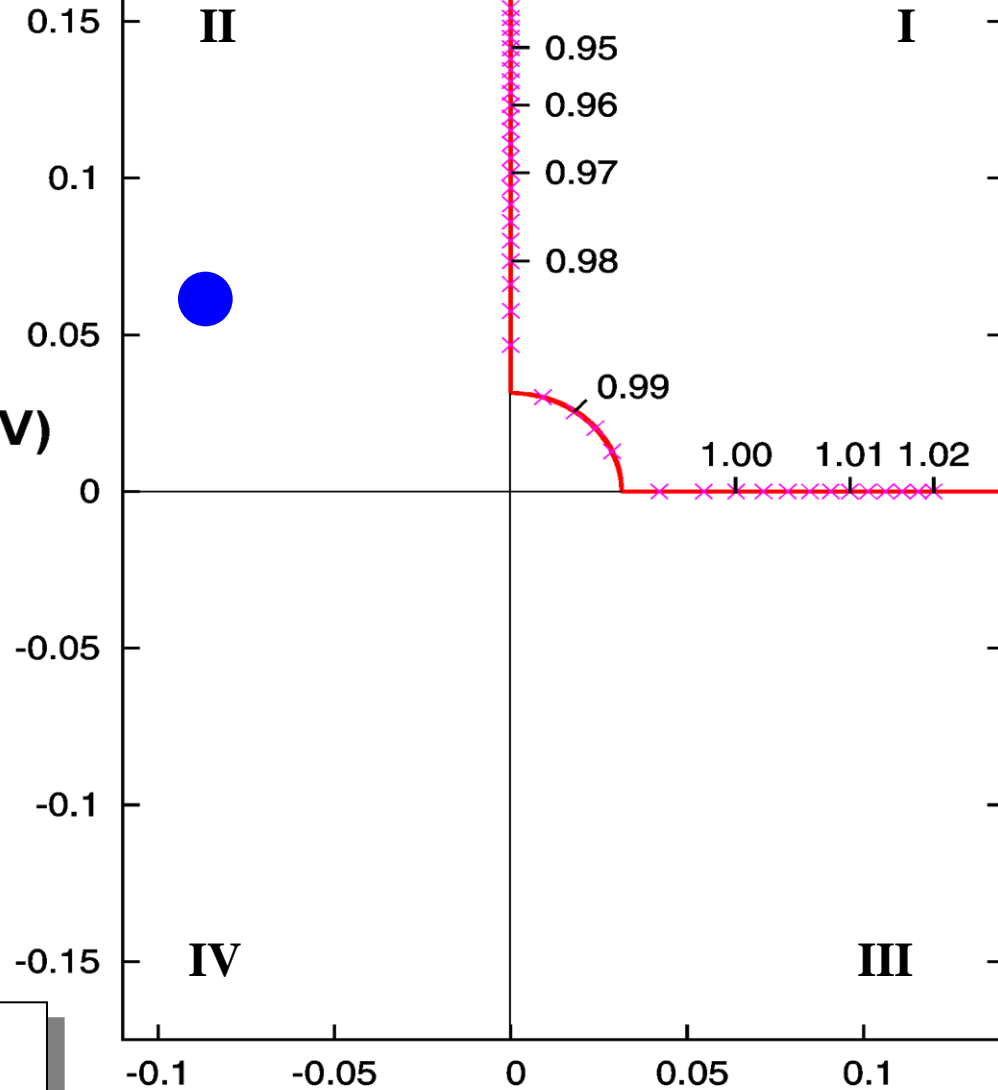
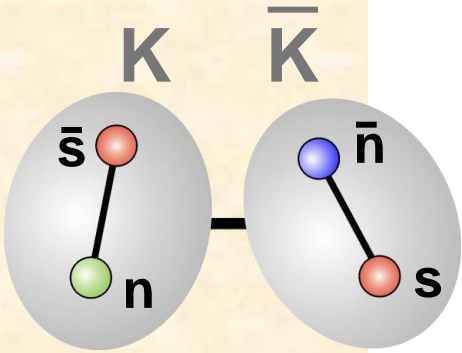
$D_s \rightarrow \pi(KK)$

$D_s \rightarrow \pi(\pi\pi)$



$D_s \rightarrow \pi(KK)$

Jost function: 1 pole v 2 pole

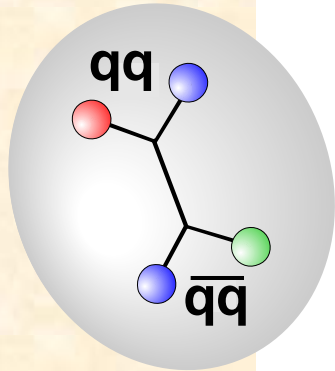
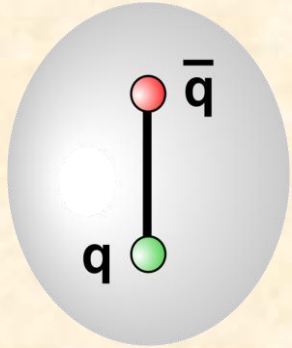


k_2 plane
($K\bar{K}$ c.m. momentum)

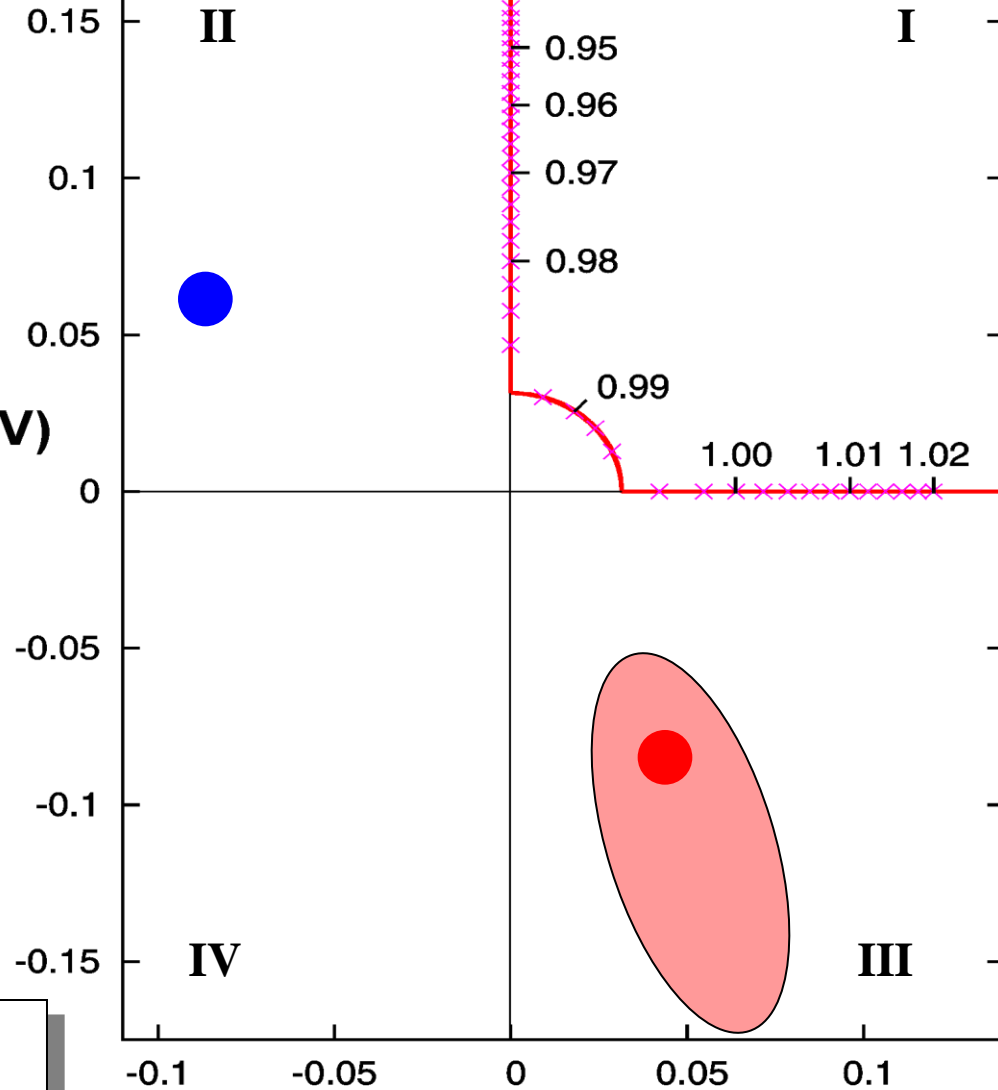
$\text{Re } k_2$ (GeV)

Wilson & P

Jost function: 1 pole v 2 pole



Im k_2 (GeV)

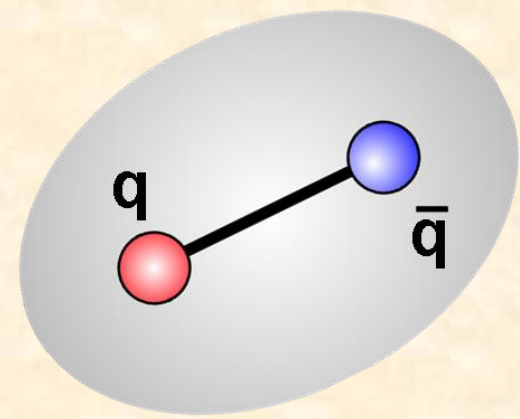
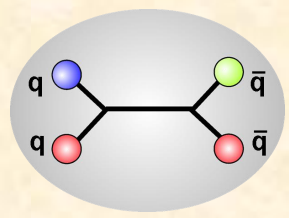
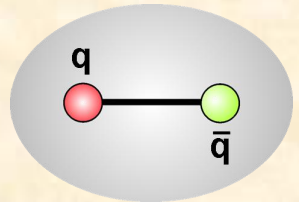


k_2 plane
($K\bar{K}$ c.m. momentum)

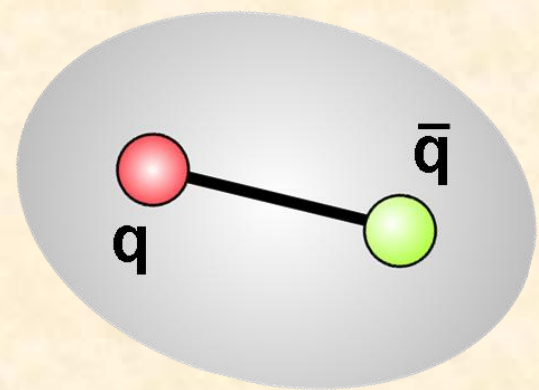
Re k_2 (GeV)

Wilson & P

$f_0(980)$

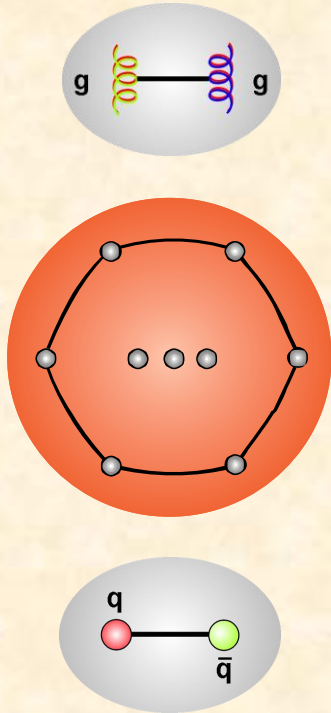


K



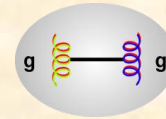
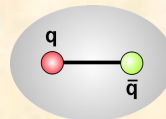
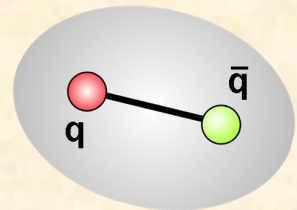
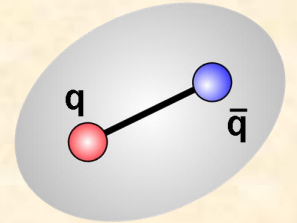
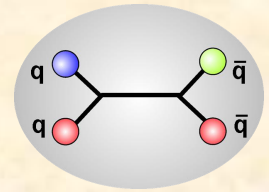
\bar{K}

Scalar mesons



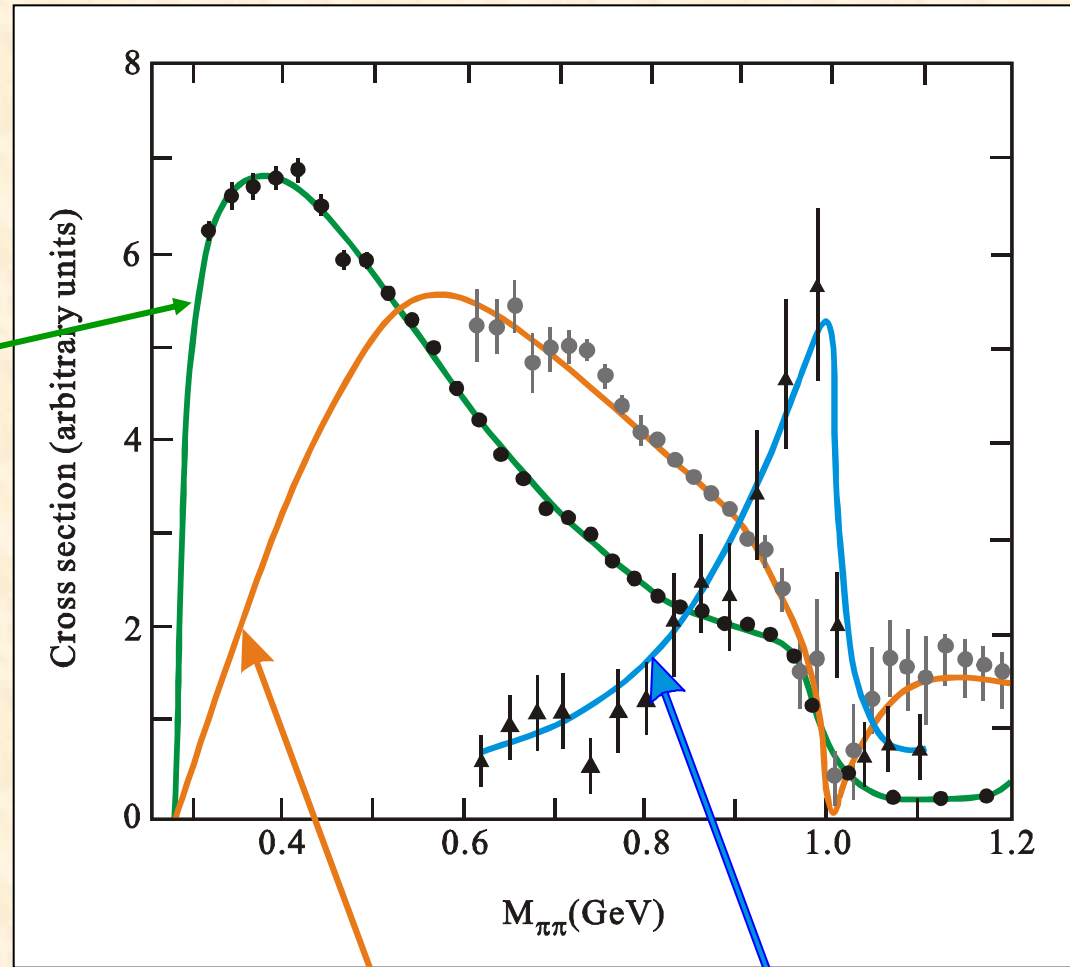
gg ————— f_0
 $\bar{s}s$ ————— f_0
 $\bar{s}n$ ————— K_0
 $\bar{n}n$ ————— a_0/f_0

$\bar{s}s\bar{n}n$ ————— a_0/f_0
 $\bar{s}n\bar{n}n$ ————— K_0 \mathbf{K}
 $\bar{n}n\bar{n}n$ ————— f_0 $\mathbf{\sigma}$



Universality of final state interactions

$pp \rightarrow pp (\pi\pi)$



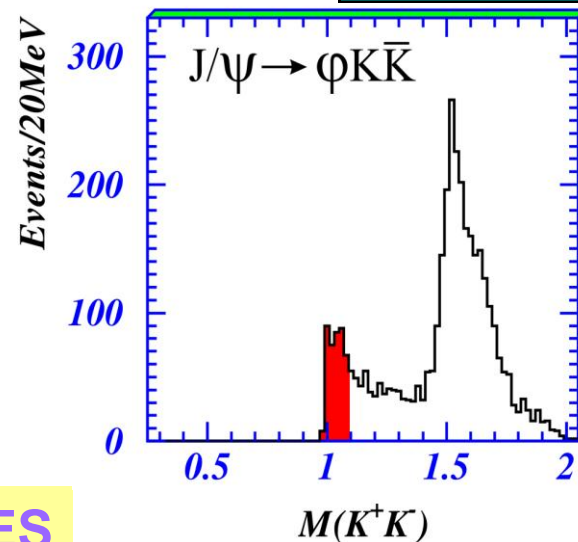
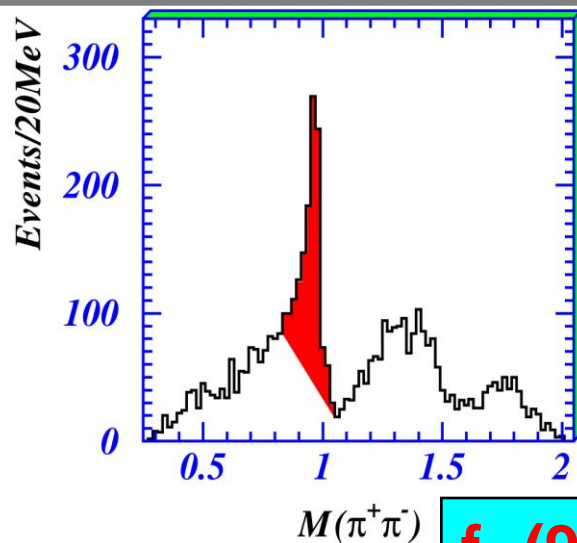
$\pi\pi \rightarrow \pi\pi$

$\psi \rightarrow \phi(\pi\pi)$



BESIII data
partial wave analyzed
in **2-4 MeV** bins
would help

$$J/\psi \longrightarrow \varphi (\pi\pi, \bar{K}K)$$



BES

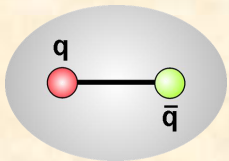
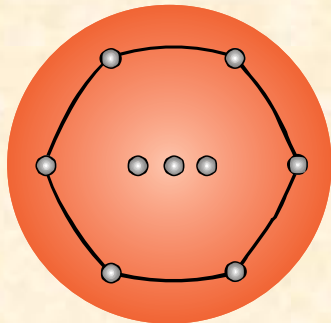
Modeling scalar mesons



van Beveren
Rupp



+Tornqvist



$\bar{s}s$ ————— f_0
 $\bar{s}n$ ————— K_0
 $\bar{n}n$ ————— a_0/f_0



————— a_0/f_0
 ————— K_0 \mathcal{K}
 ————— f_0 σ

$n = u, d$

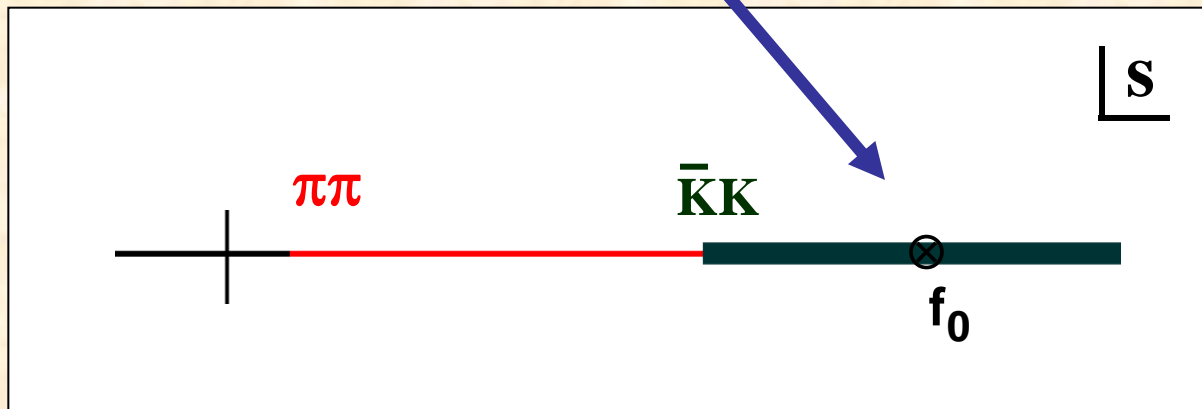
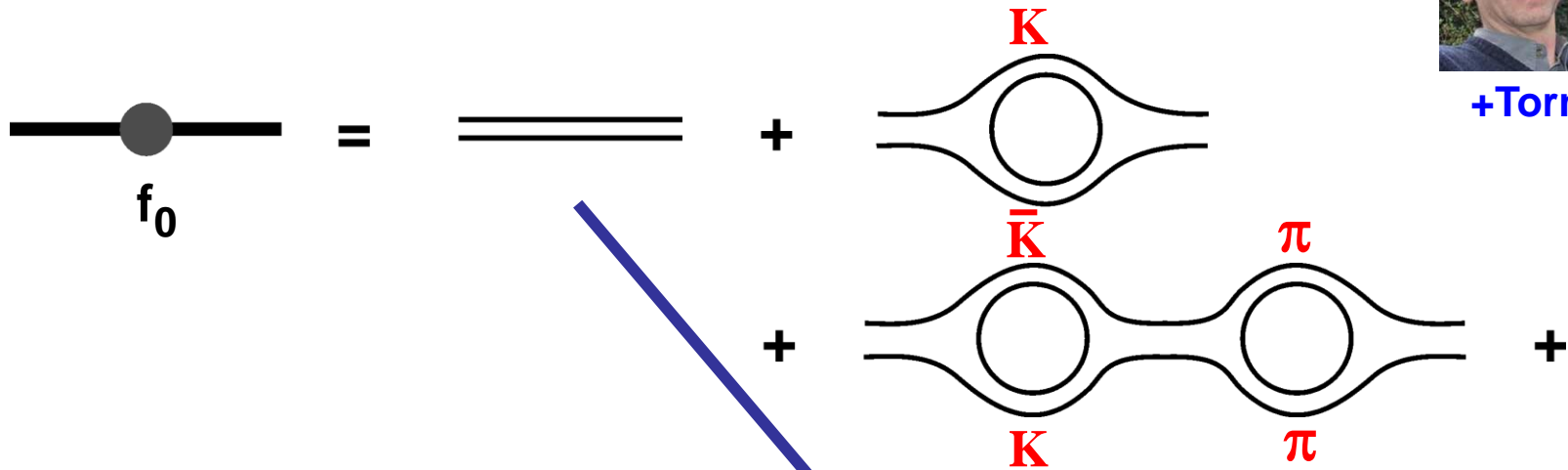
Scalar multiplet



van Beveren
Rupp

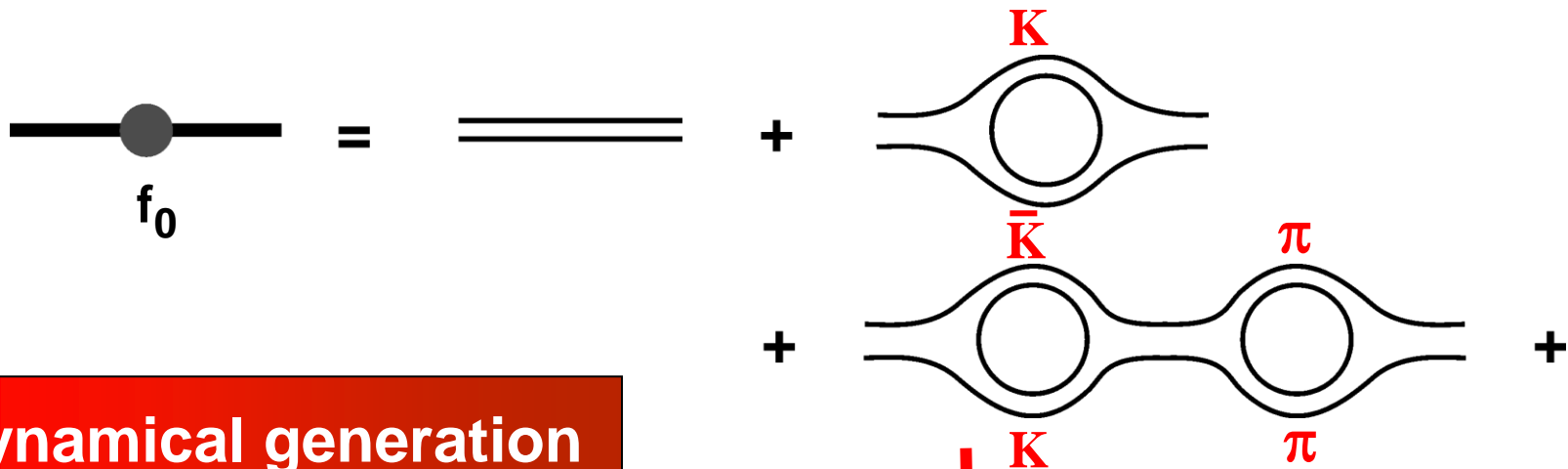


+Tornqvist



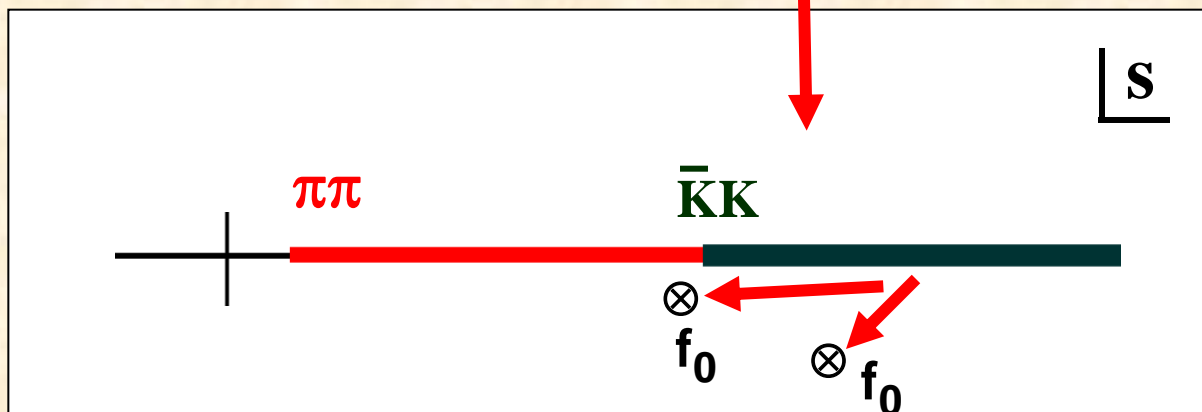
Scalar multiplet

shifting of masses



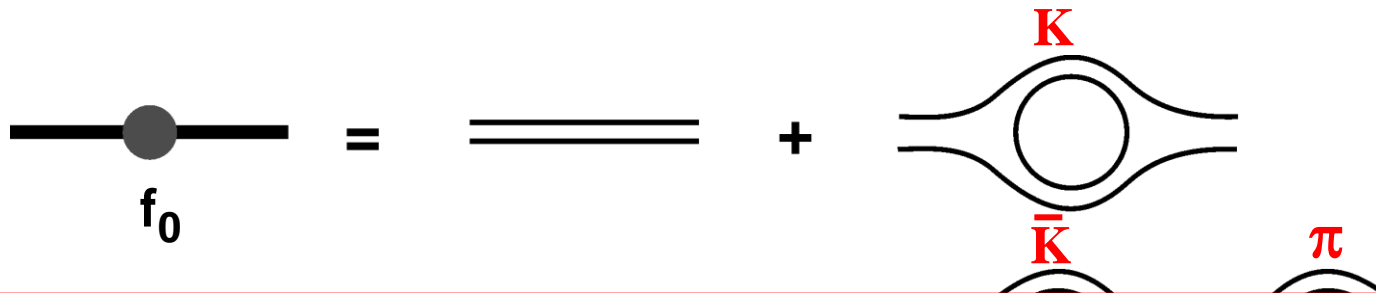
dynamical generation

$\bar{s}s$



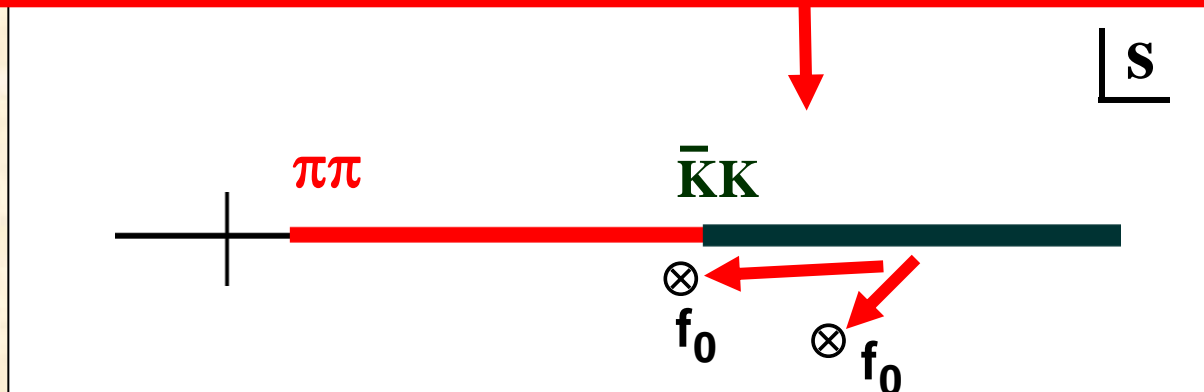
Scalar multiplet

shifting of masses



$$\mathcal{L}_{\text{QCD}} = \sum_{q=u,d,s,c,b} \bar{\psi}_q (i \gamma_\mu D^\mu - m_q) \psi_q - \frac{1}{4} \mathcal{F}_{\mu\nu} \mathcal{F}^{\mu\nu}$$

$\bar{s}s$



Scalar meson multiplets

$q\bar{q}$

$q\bar{q}q\bar{q}$

$\bar{s}s$ ————— f_0
 $\bar{s}n$ ————— K_0
 $\bar{n}n$ ————— a_0/f_0

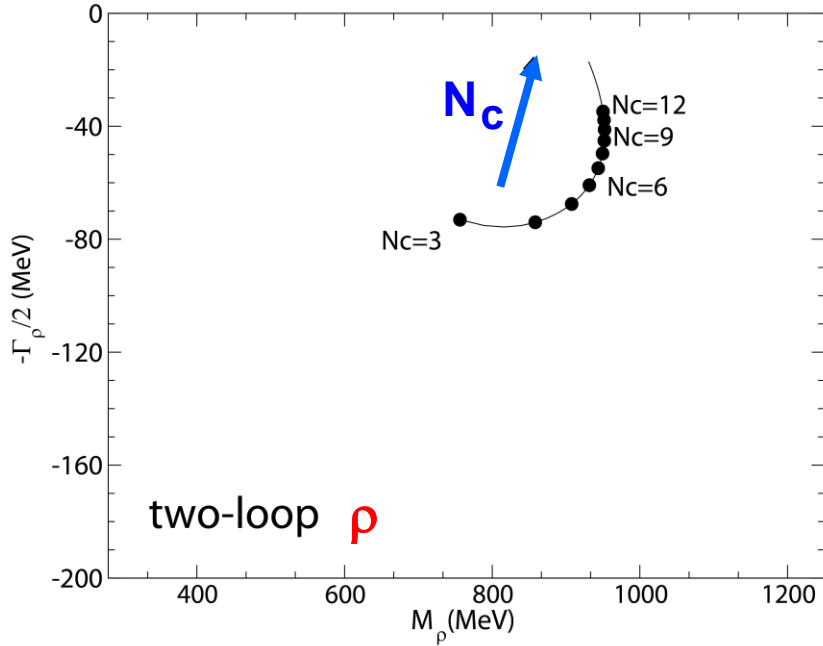
$\bar{s}s\bar{n}n$ ————— a_0/f_0
 $\bar{s}n\bar{n}n$ ————— K_0 \mathbf{K}
 $\bar{n}n\bar{n}n$ ————— f_0 $\mathbf{\sigma}$

N_c large \rightarrow stable

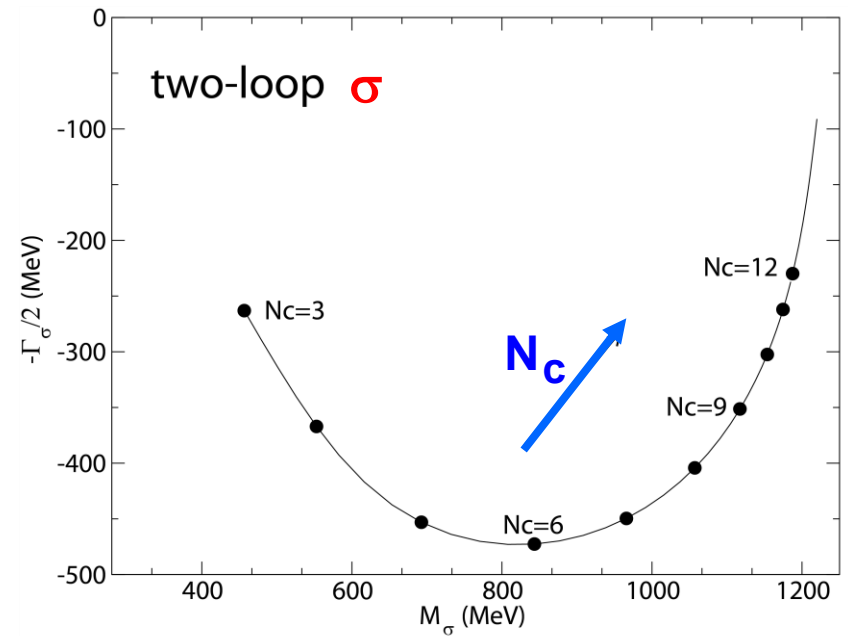
N_c large \rightarrow meson continuum

$1/N_c$ @ two loops

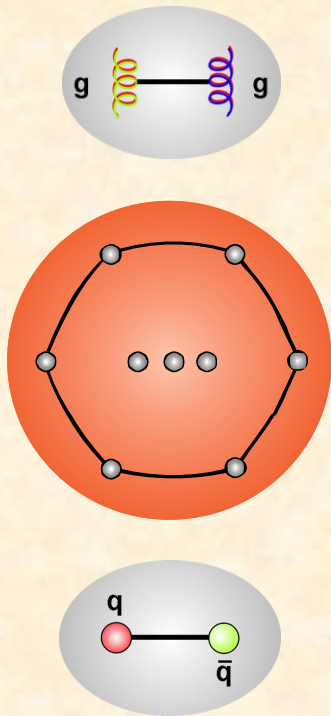
real axis



real axis

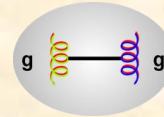
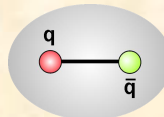
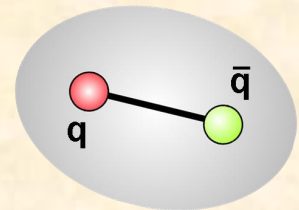
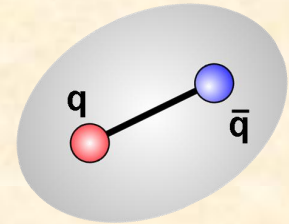
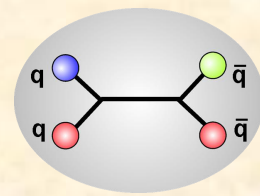


Scalar mesons



gg ————— f_0
 $\bar{s}s$ ————— f_0
 $\bar{s}n$ ————— K_0
 $\bar{n}n$ ————— a_0/f_0

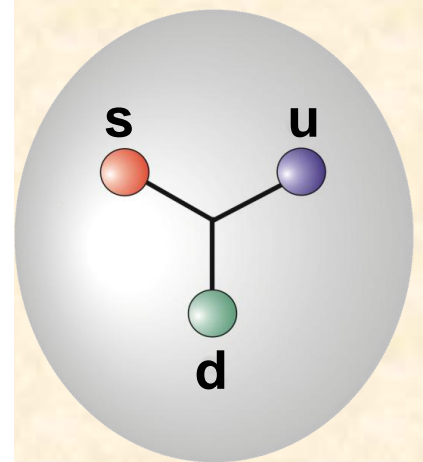
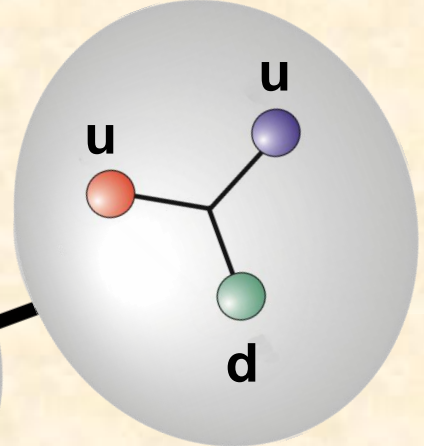
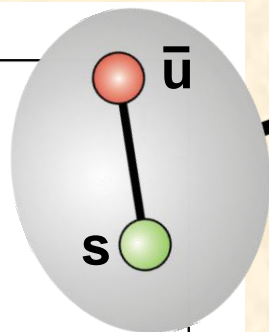
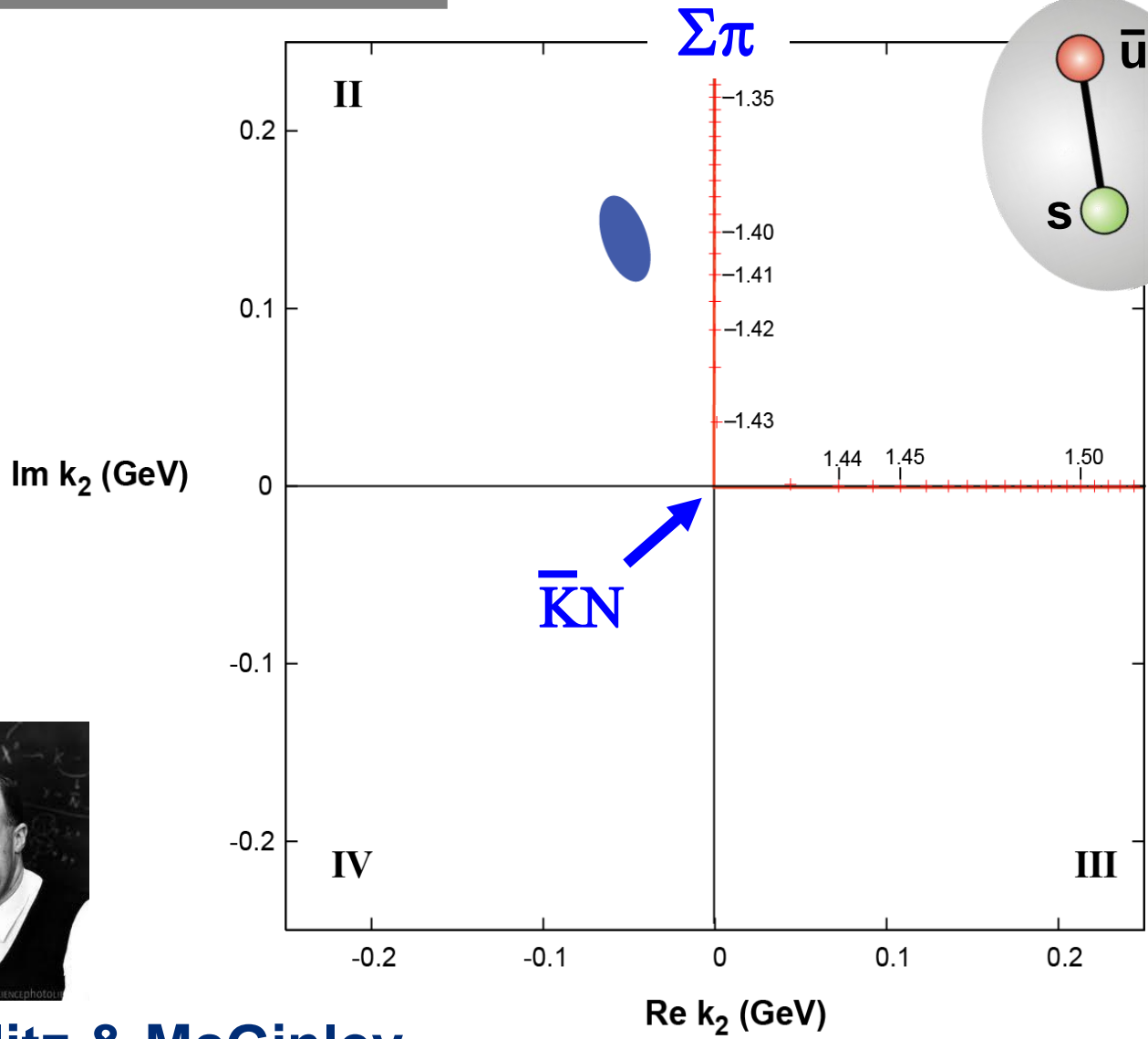
$\bar{s}s\bar{n}n$ ————— a_0/f_0
 $\bar{s}n\bar{n}n$ ————— K_0 \mathbf{K}
 $\bar{n}n\bar{n}n$ ————— f_0 $\mathbf{\sigma}$



Coupled channels

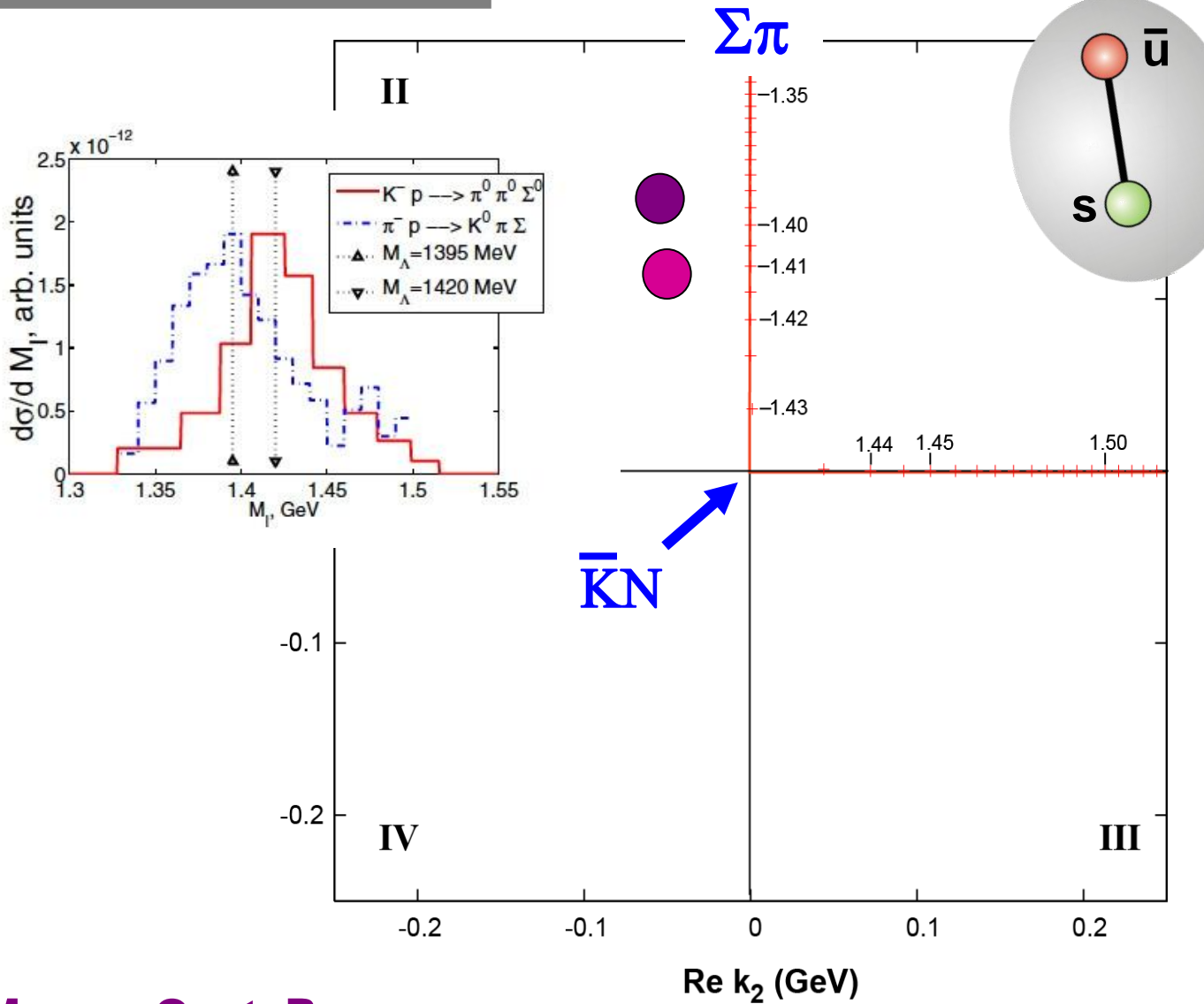


$\Lambda(1405)$

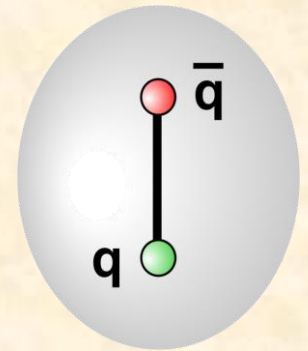
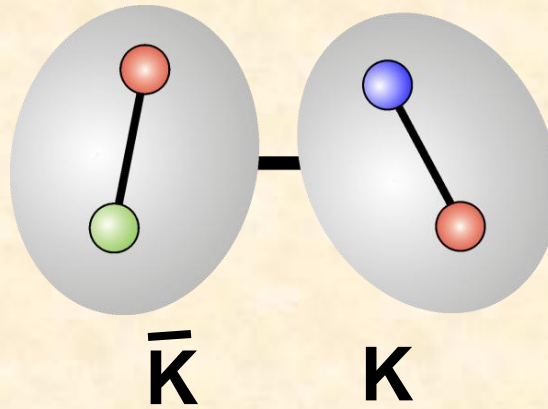
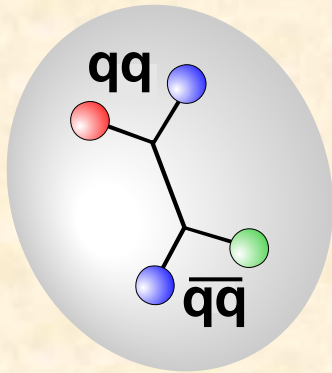


Dalitz & McGinley

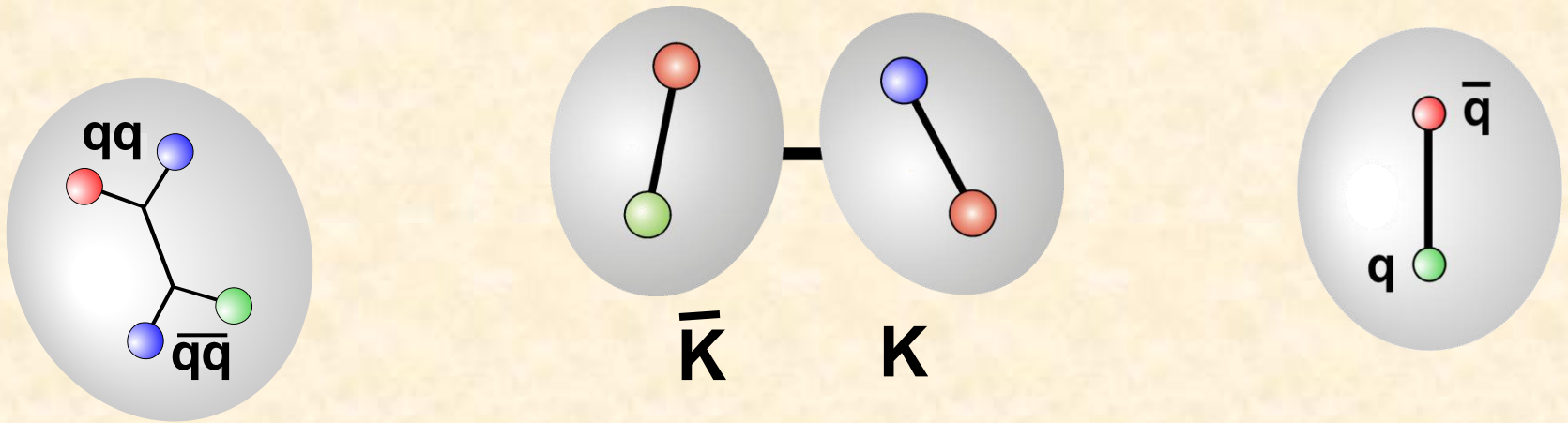
$\Lambda(1405)$



Can BESIII help distinguish between
a four quark state, a molecule,
a glueball or a $\bar{q}q$ meson ?

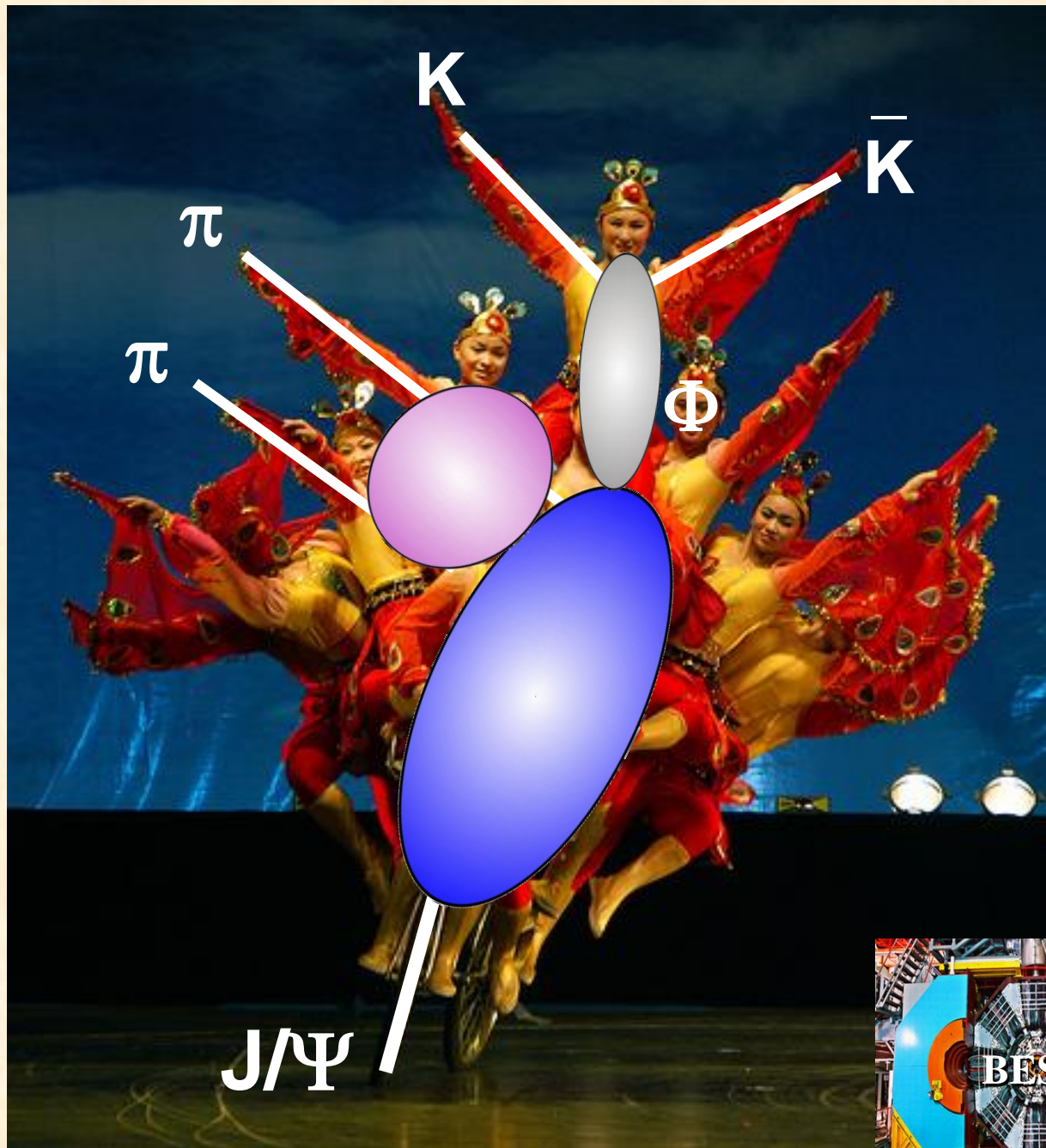


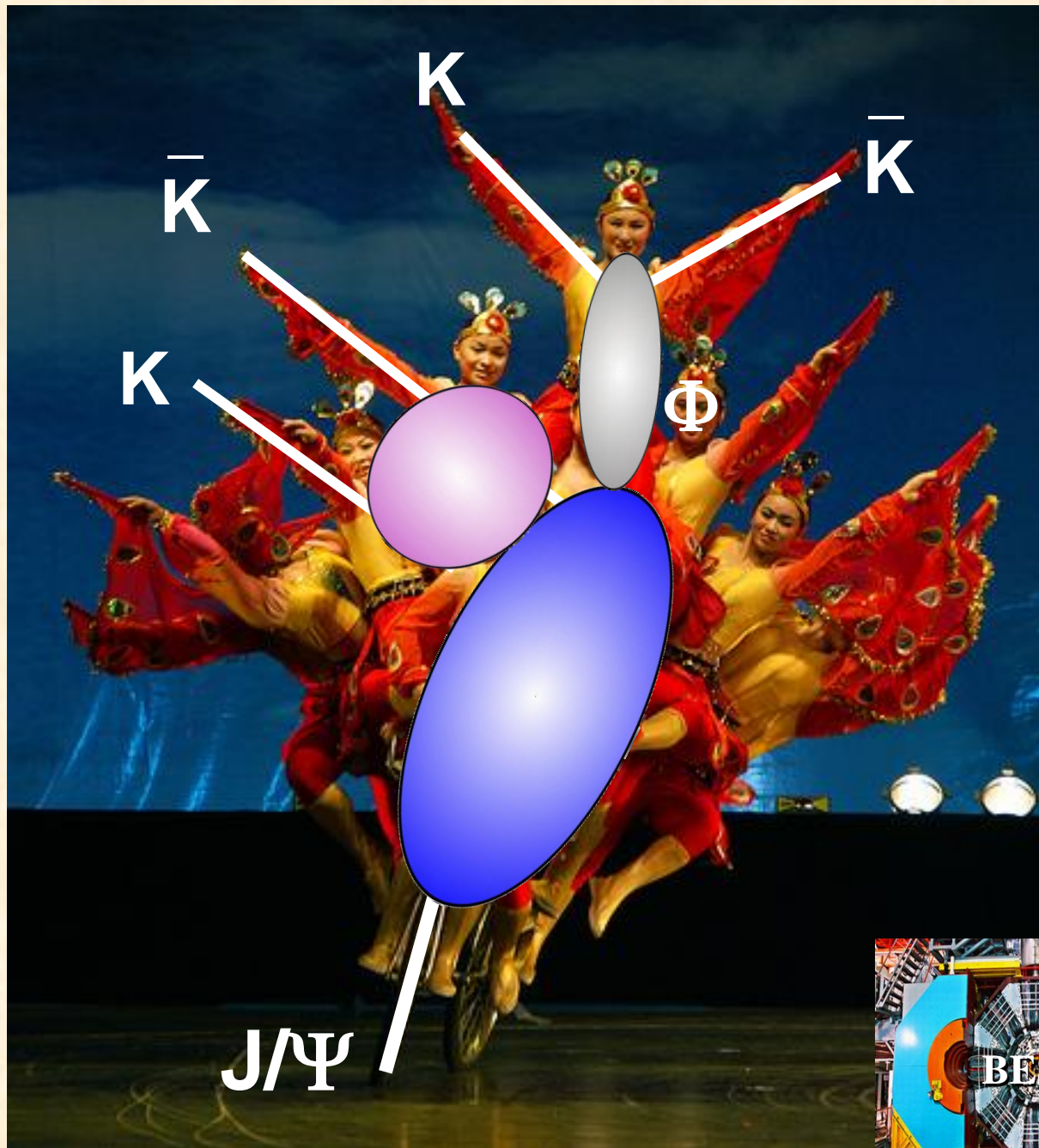
Can BESIII help distinguish between a four quark state, a molecule, a glueball or a $\bar{q}q$ meson ?



BESIII data
partial wave analyzed
in **2-4 MeV** bins







$c\bar{c}$

experiment

E

3^1S_1

3^1S_0

3^3P_2

ψ'''

η''_c

χ'_{c2}

$D^* \bar{D}^*$

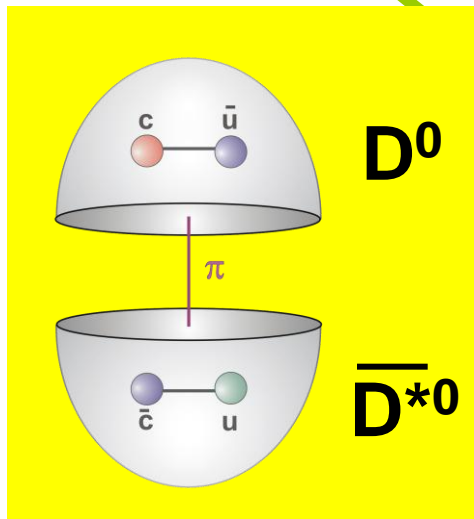
$D_s \bar{D}_s$

$D \bar{D}^*$

$D \bar{D}$

4

3.8



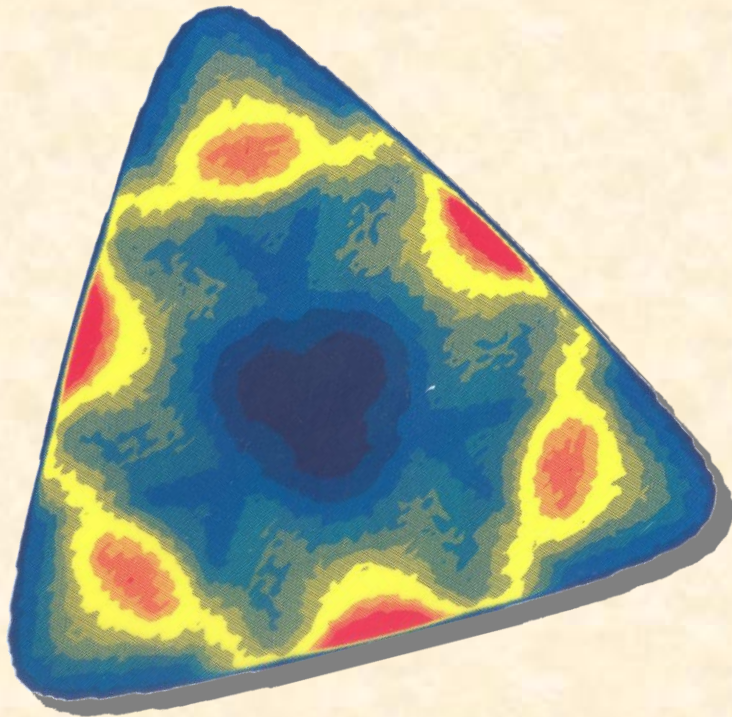
Tornqvist, ...

Barnes & Swanson

Wilson & P

Physics Analysis Center

Techniques of Amplitude Analysis



Jefferson Lab Advanced Study Institute

EXTRACTING PHYSICS FROM PRECISION EXPERIMENTS:

Techniques of Amplitude Analysis

COLLEGE OF WILLIAM & MARY
WILLIAMSBURG, VIRGINIA, USA

Wednesday, May 30th, 2012
through Wednesday, June 13th, 2012

To prepare for the analysis of precision experiments at BESIII, COMPASS, LHCb, JLAB@12 GeV, and PANDA@FAIR, Thomas Jefferson National Accelerator Facility (JLab) is organizing a two week advanced course covering *Techniques of Amplitude Analysis*, aimed at postdoctoral researchers and advanced doctoral students in nuclear and particle physics.

May/June 2012

LECTURERS:

Suh-Urk Chung	(BNL/TUM)
Jozef Dudek	(ODU)
Bastian Kubis	(Bonn)
T-S Harry Lee	(ANL)
Brian Meadows	(Cincinnati)
Antimo Palano	(Bari)
Klaus Peters	(GSI Darmstadt)
Michael Pennington	(JLab)
Ronald Workman	(GWU)

CONTACT:
mfox@jlab.org

For application details and all other information see:

<http://www.jlab.org/conferences/asi2012/>