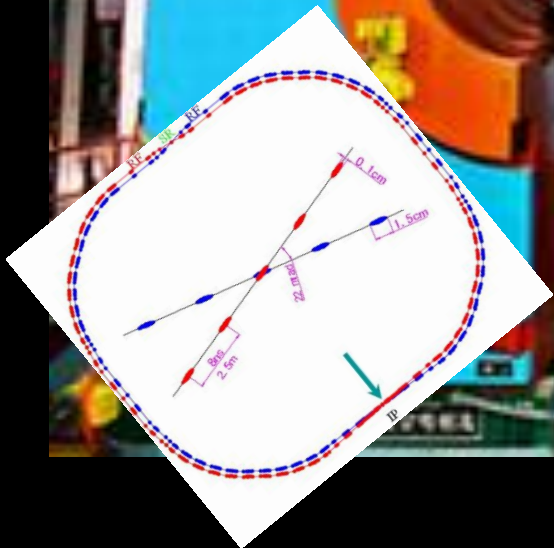
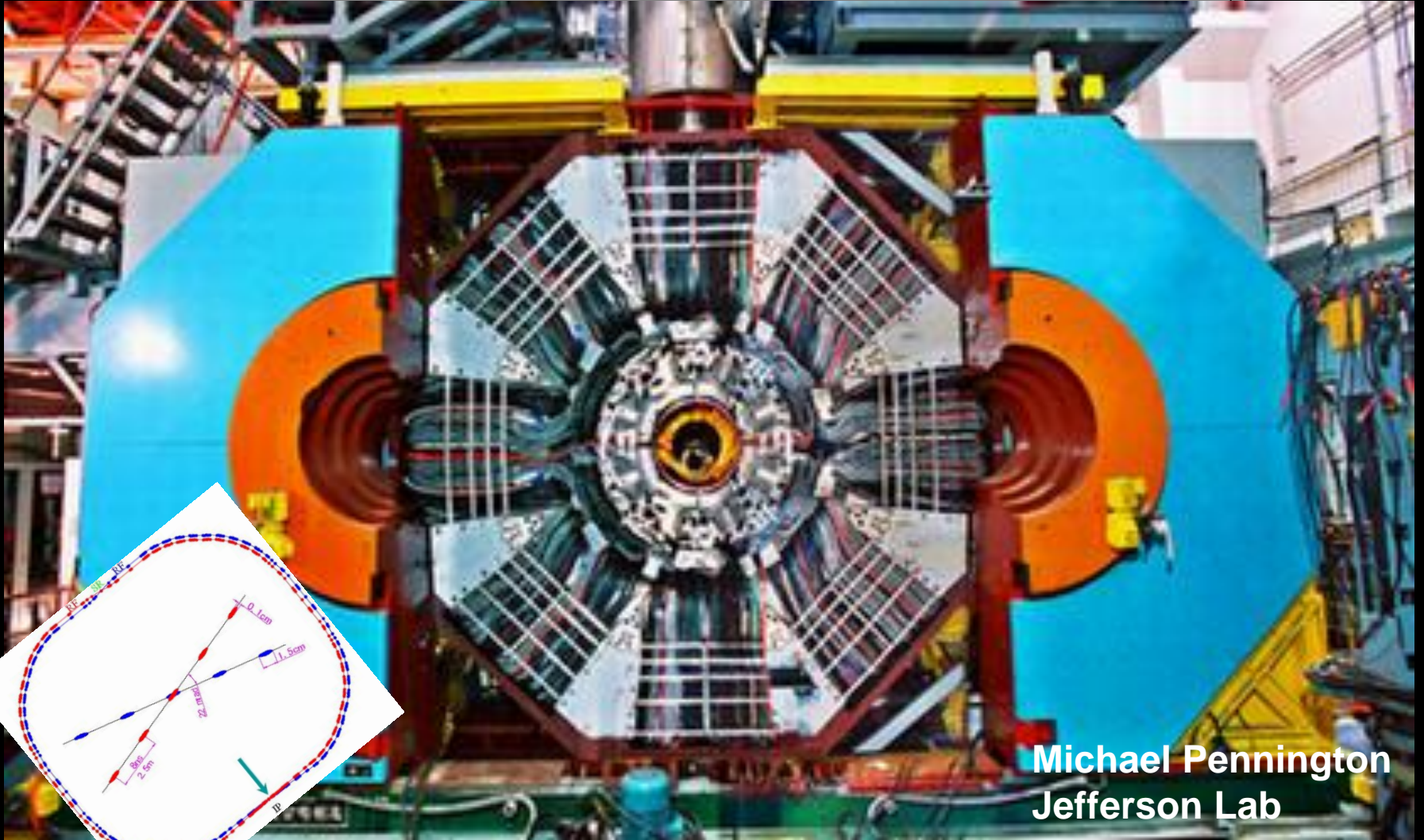


$\pi\pi$, $K\pi$ final state interactions: examples from BES



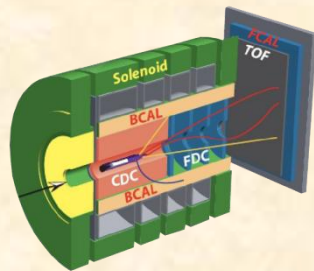
Michael Pennington
Jefferson Lab



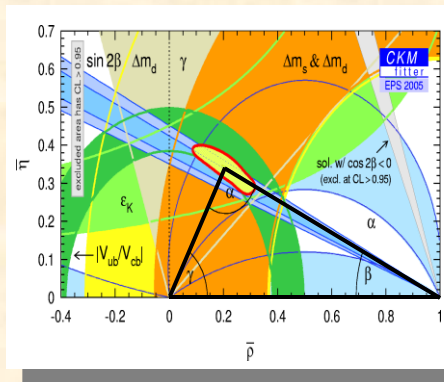
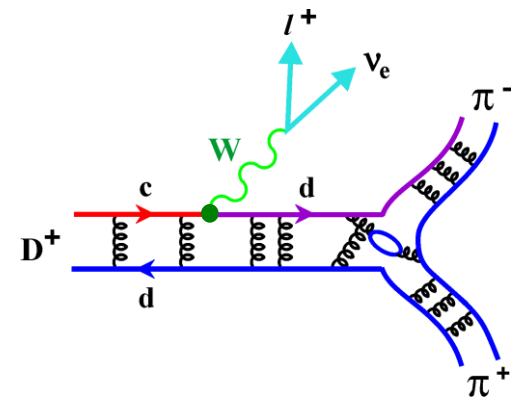
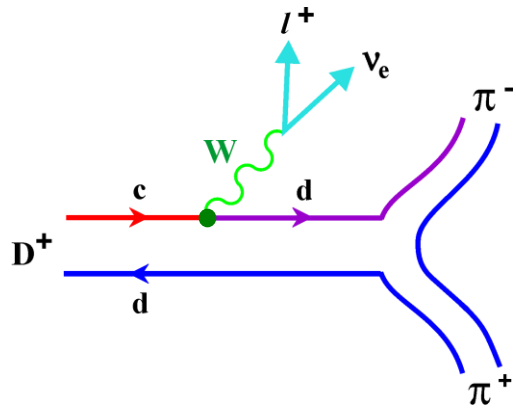
CLEO-c



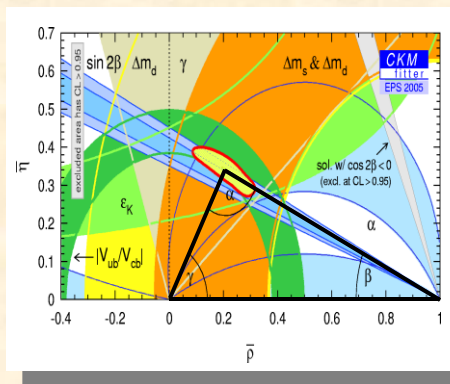
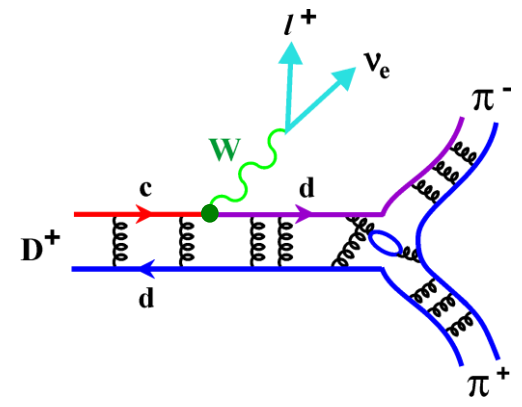
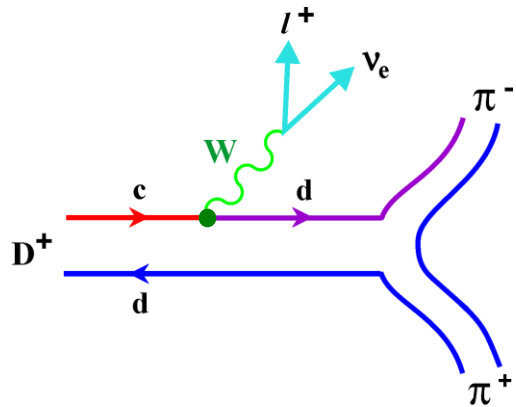
GLUEX CITATIONS
PERIMENT
Hall D@JLab



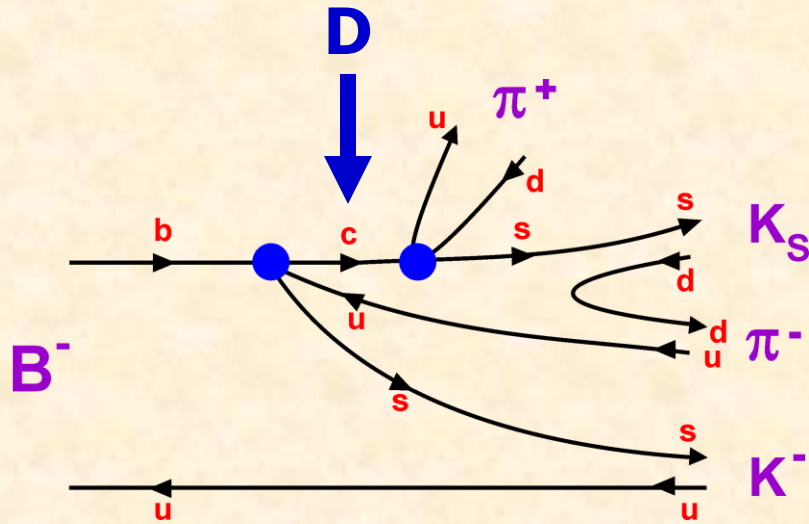
CKM matrix elements



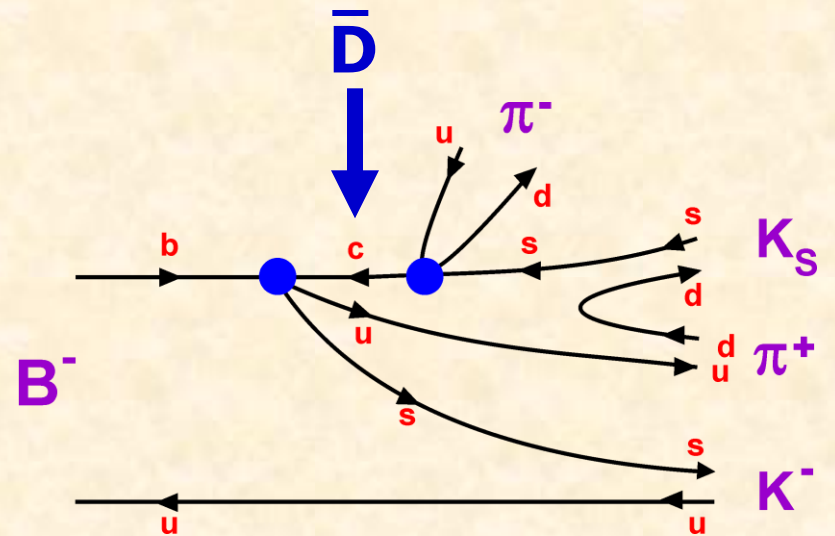
CKM matrix elements



$B \rightarrow D\bar{K} \rightarrow \bar{K}K\pi\pi$

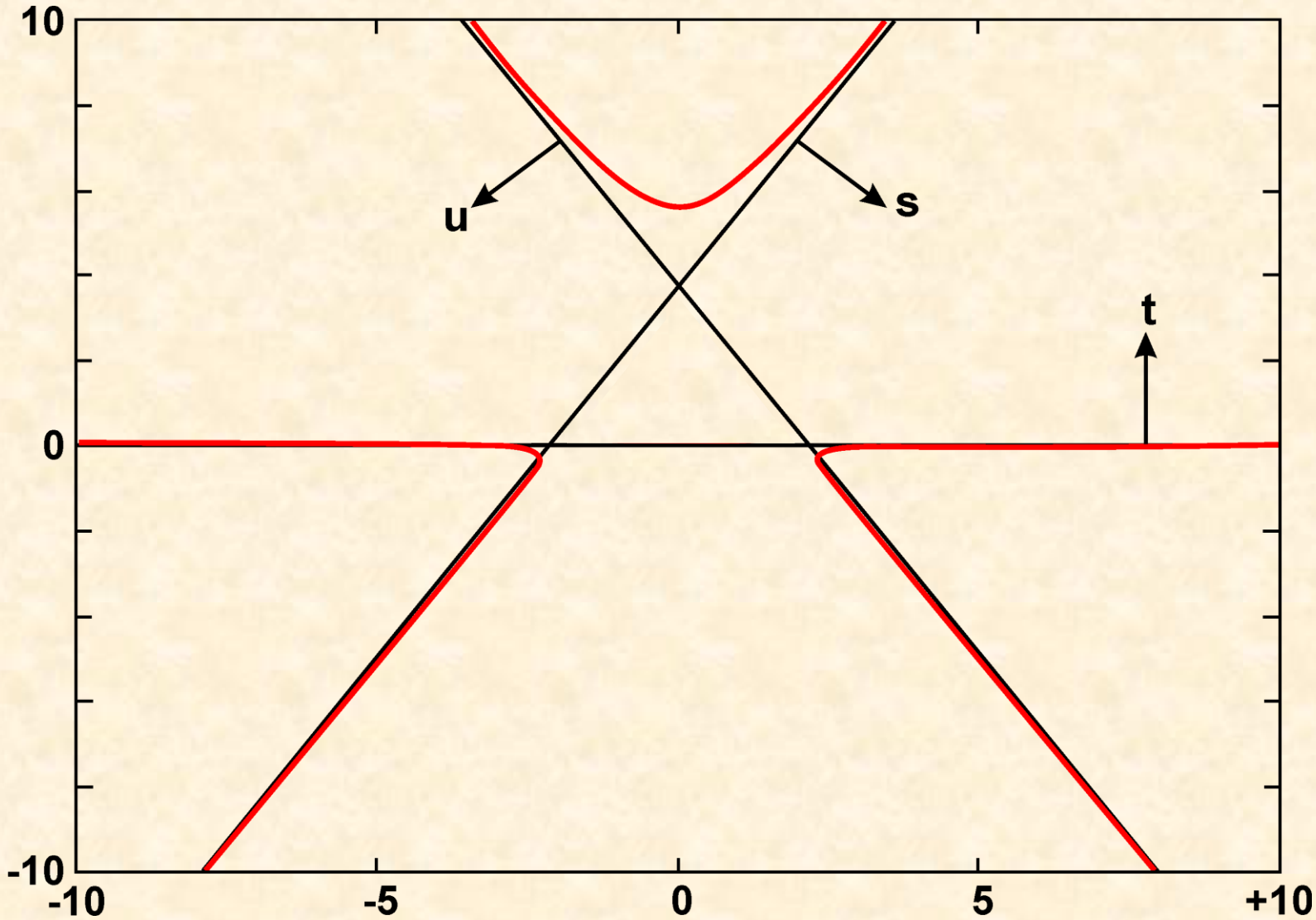


$B \rightarrow \bar{D}K \rightarrow \bar{K}K\pi\pi$

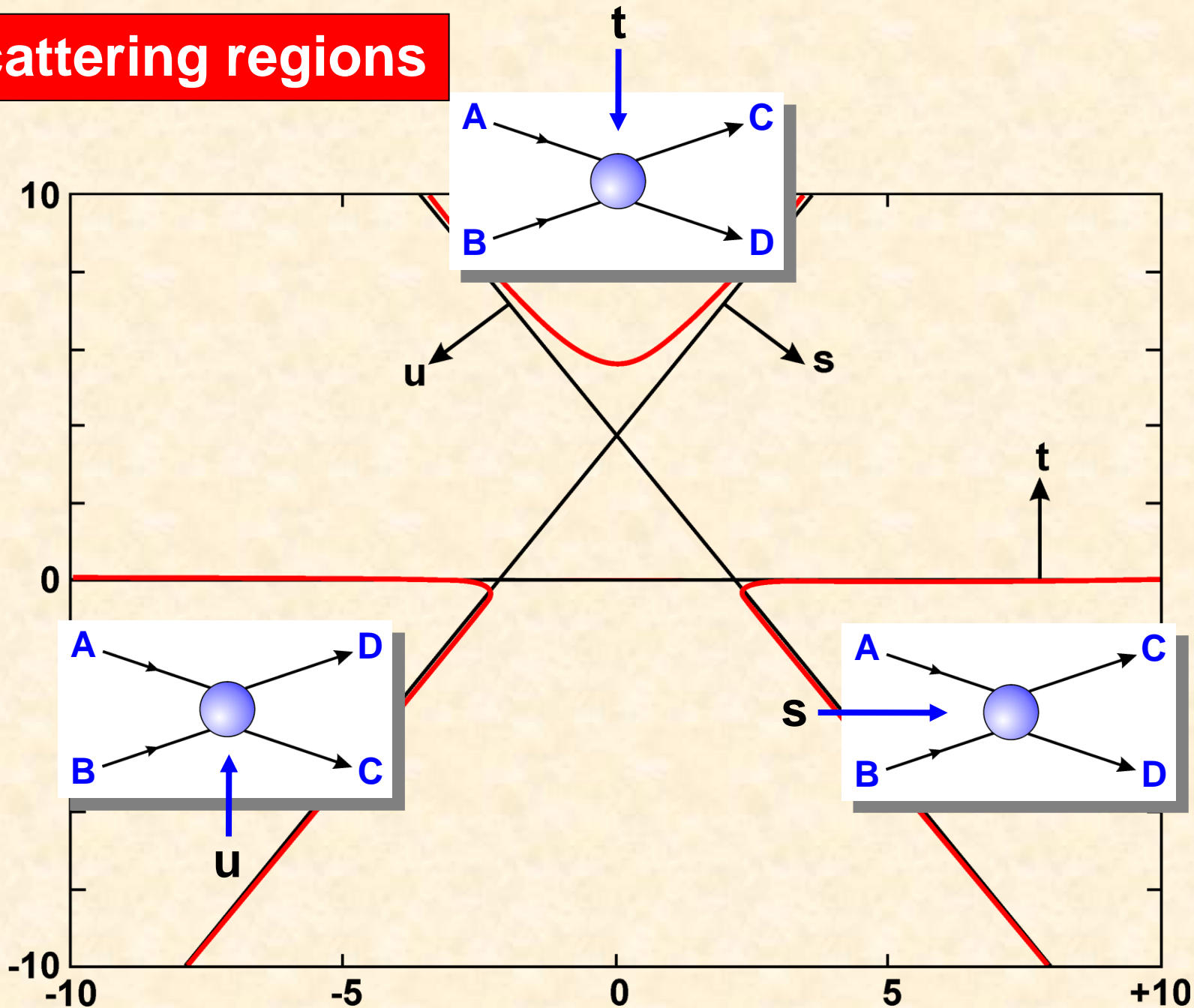


~~CP~~

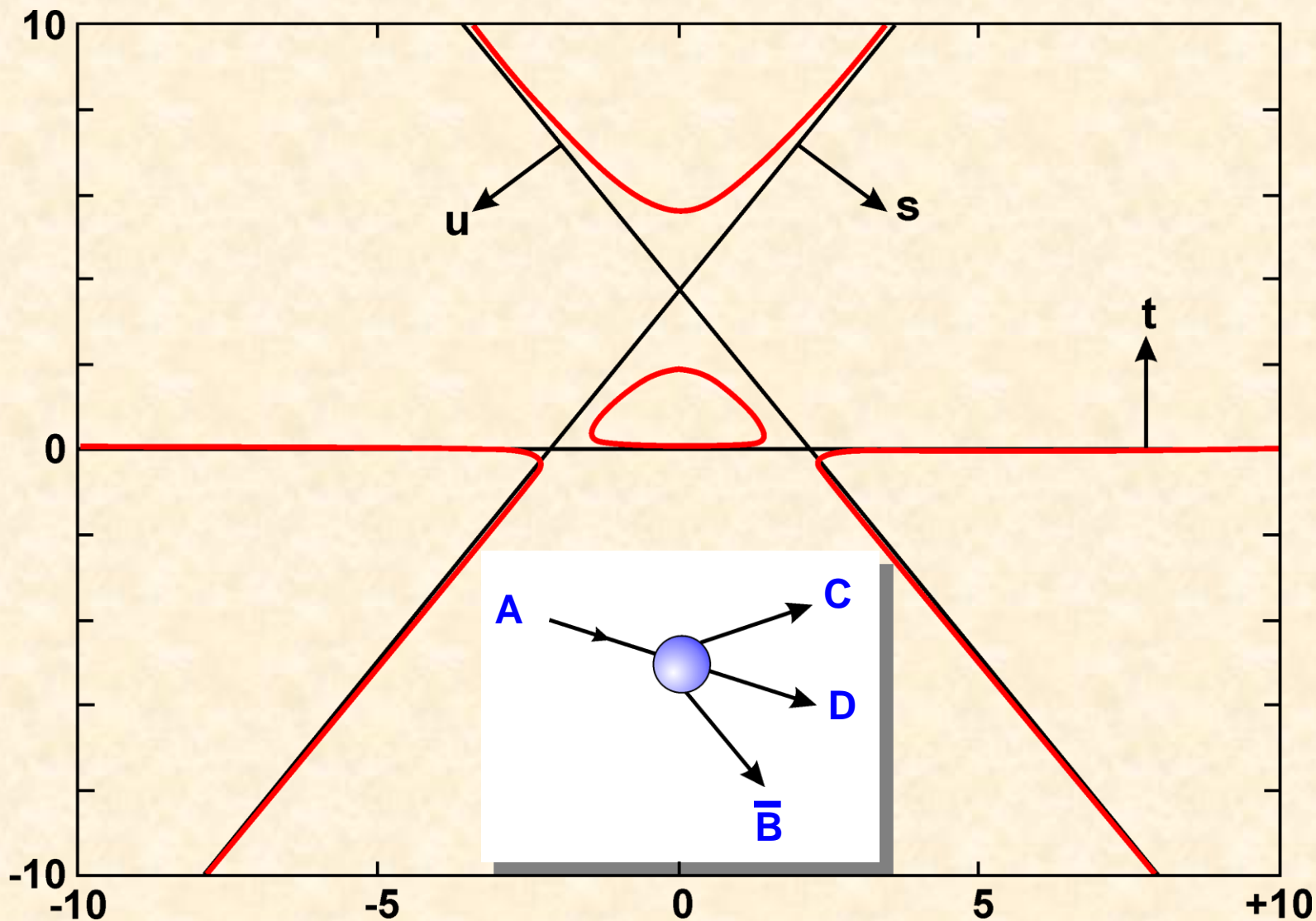
scattering & decay regions



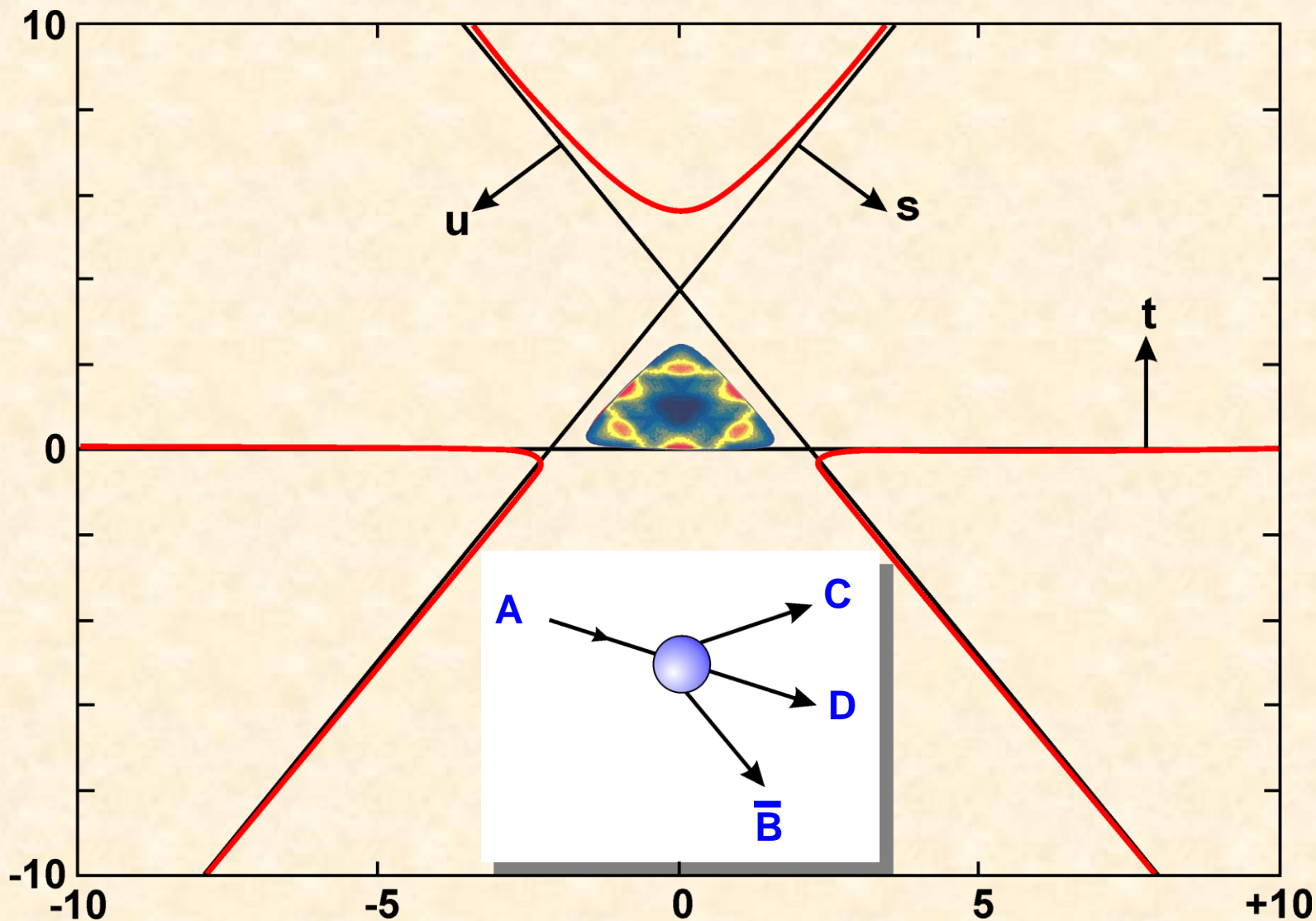
scattering regions



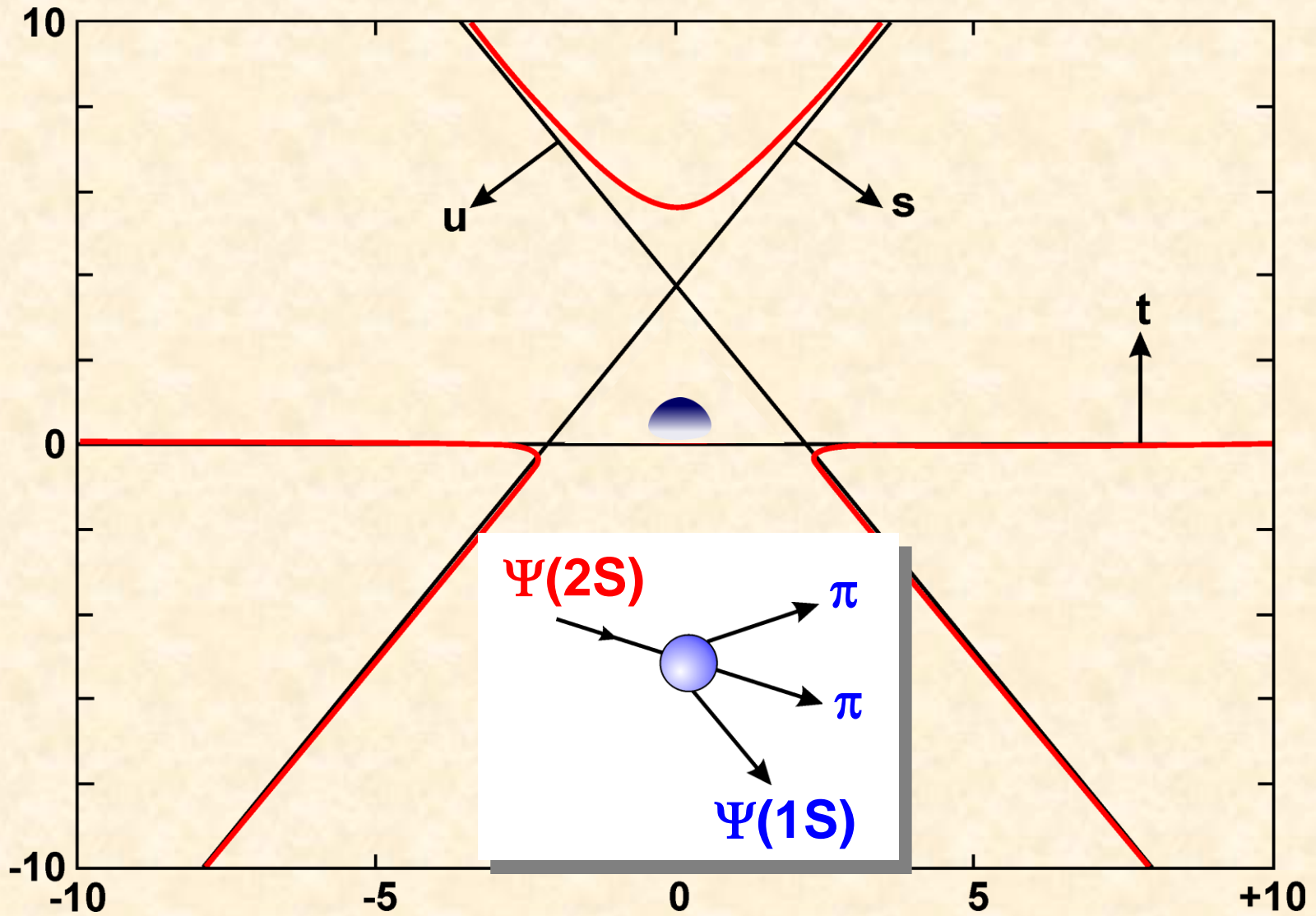
decay region



decay region

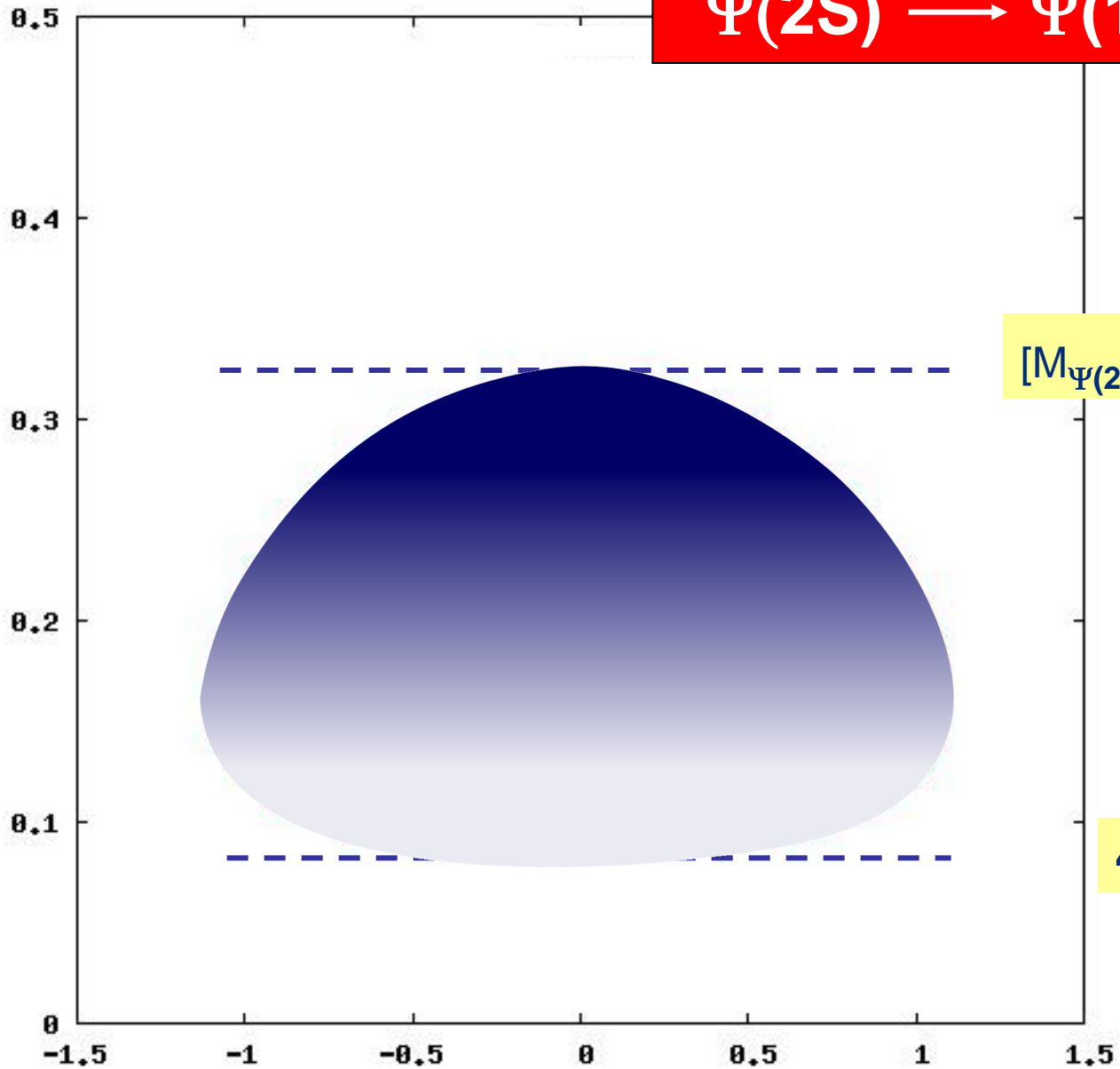


decay region



$\Psi(2S) \longrightarrow \Psi(1S) \pi^+ \pi^-$

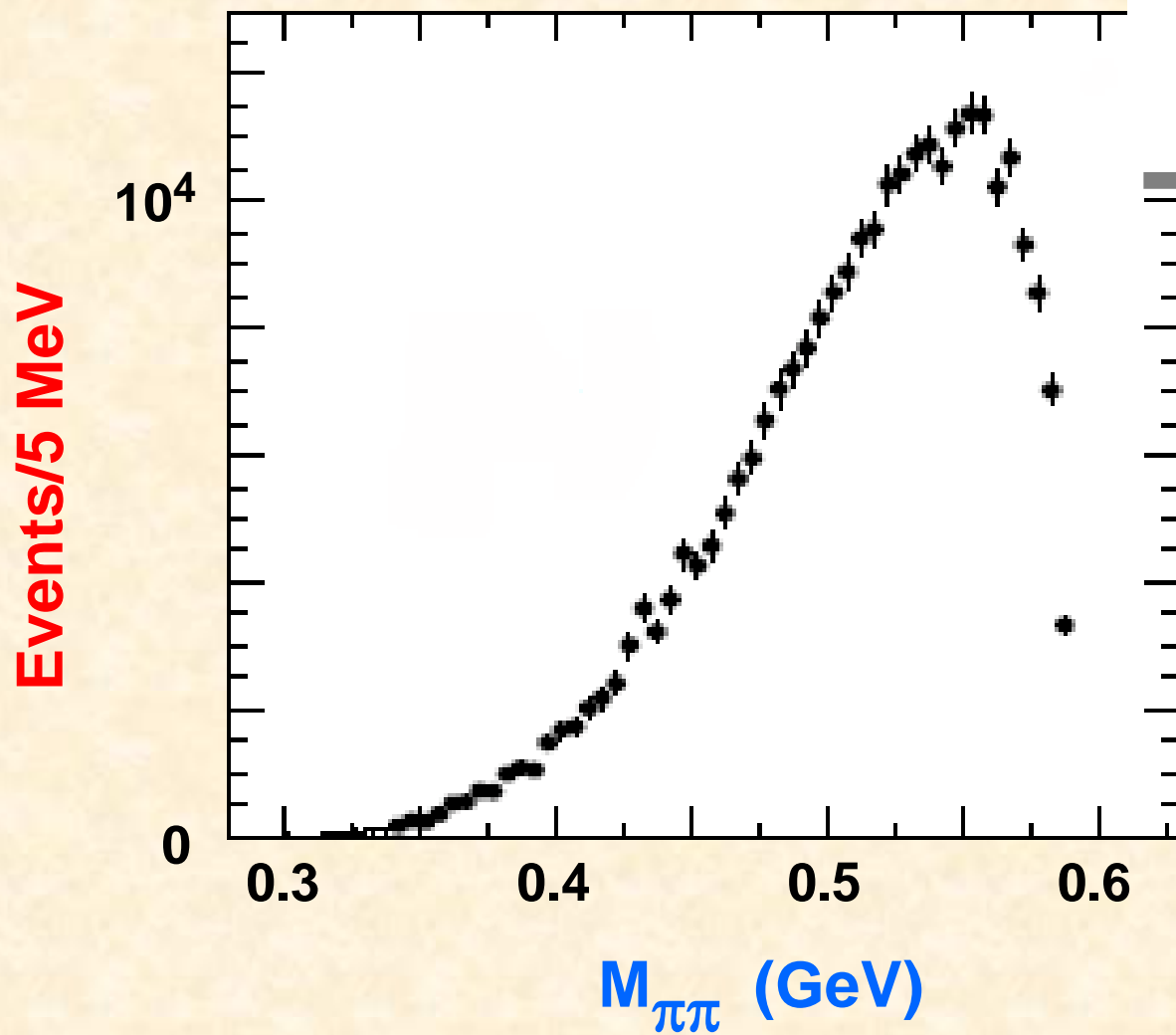
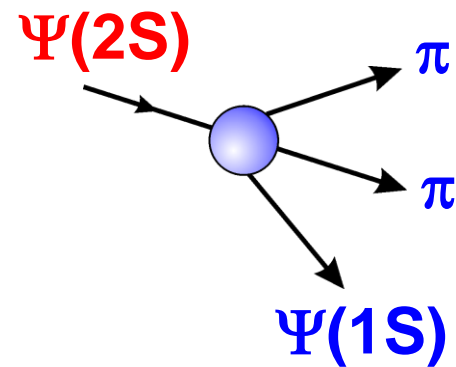
$M_{\pi\pi}^2$



$[M_{\Psi(2S)} - M_{\Psi(1S)}]^2$

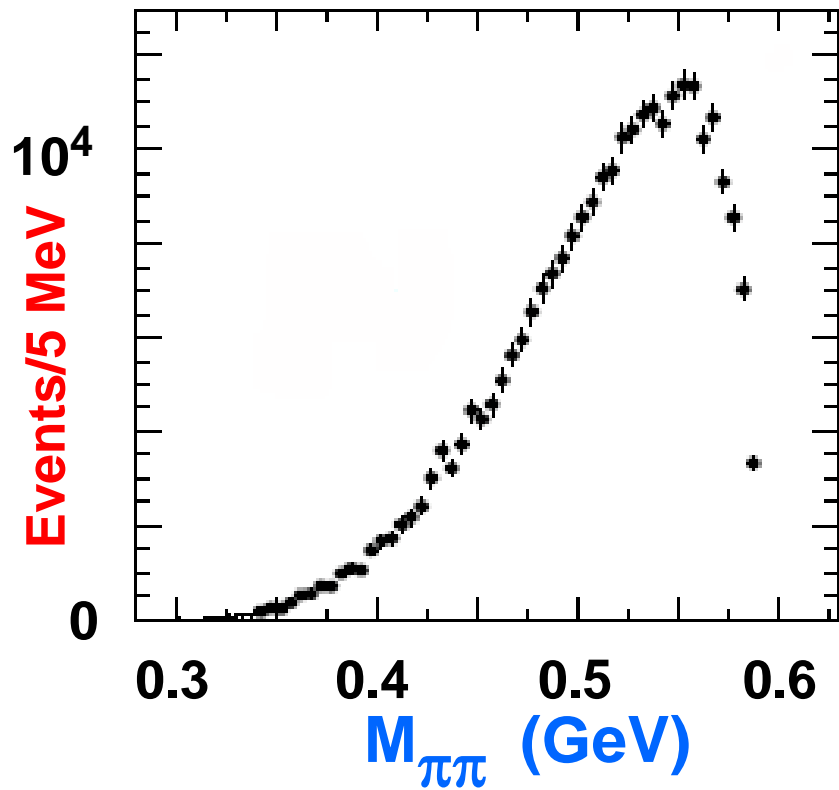
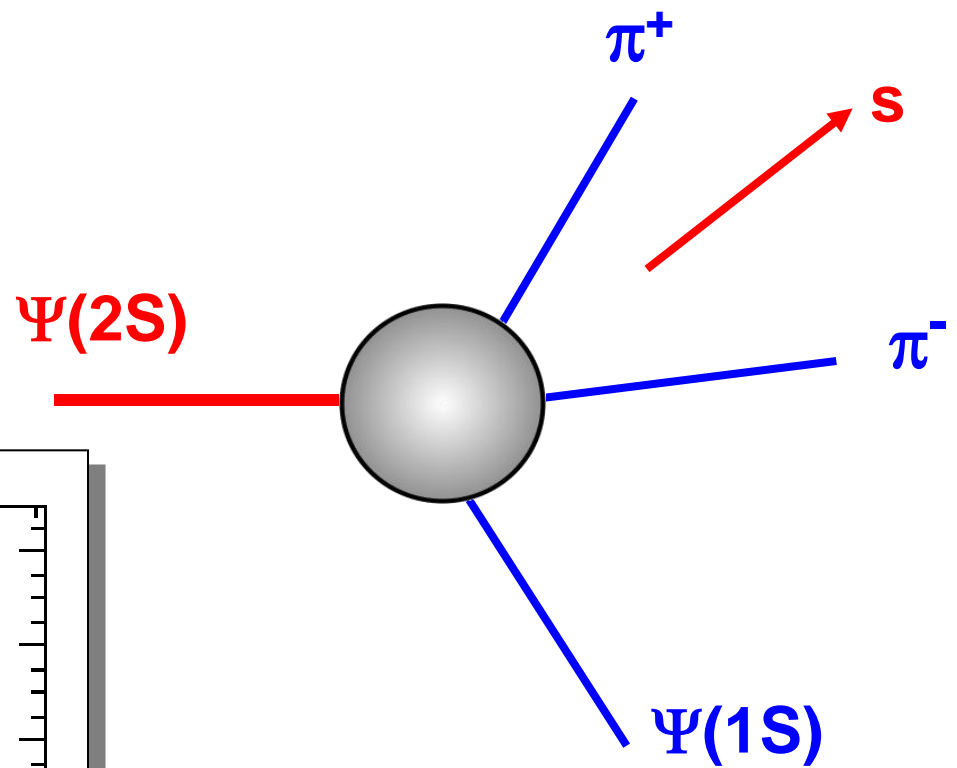
$4m_{\pi}^2$

$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$



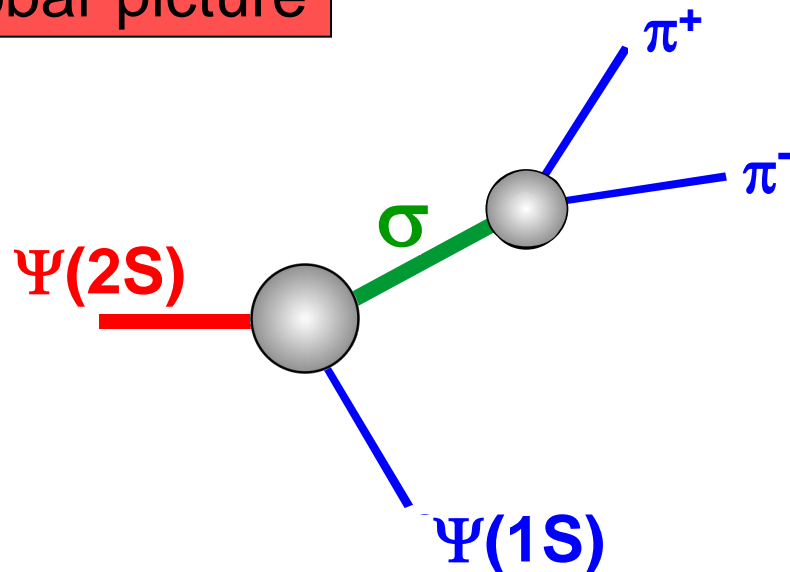
BESII

$$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$$



$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$

isobar picture



Events/5 MeV

0

10^4

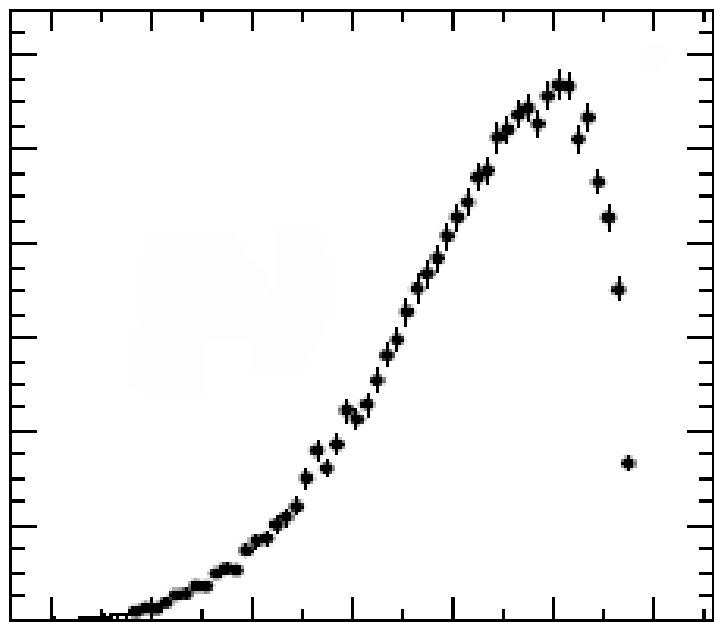
0.3

0.4

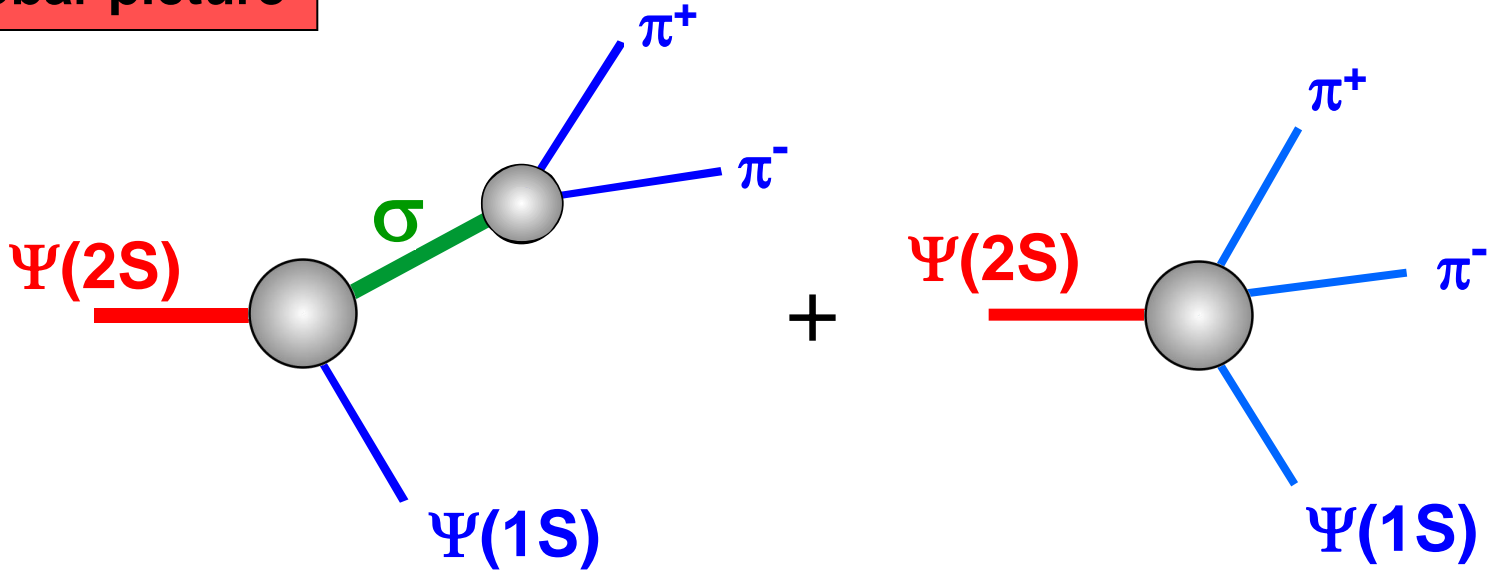
0.5

0.6

$M_{\pi\pi}$ (GeV)



isobar picture

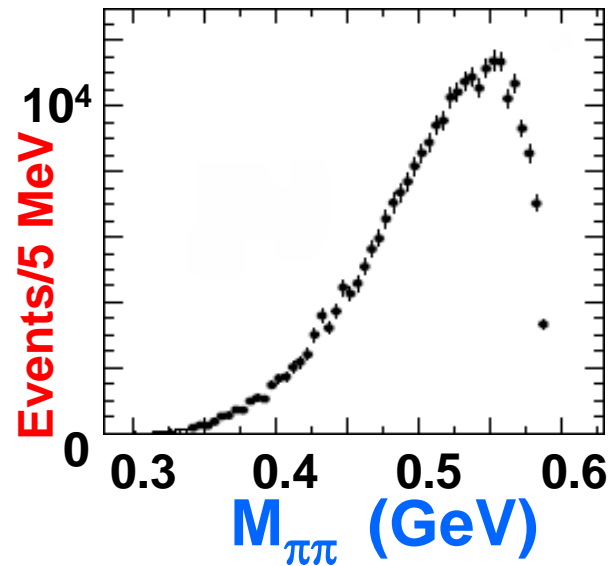


Breit-Wigner

$$\frac{1}{M^2 - s - iM\Gamma}$$

Ablikim *et al*

Phys Lett B645 (2007)1



$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$

$\text{Im } s \text{ (GeV)}^2$

$4m_\pi^2$

0

-0.1

-0.2

-0.3

0

0.1

0.2

0.3

0.4

0.5

$s = E^2$

$\text{Re } s \text{ (GeV)}^2$

pku

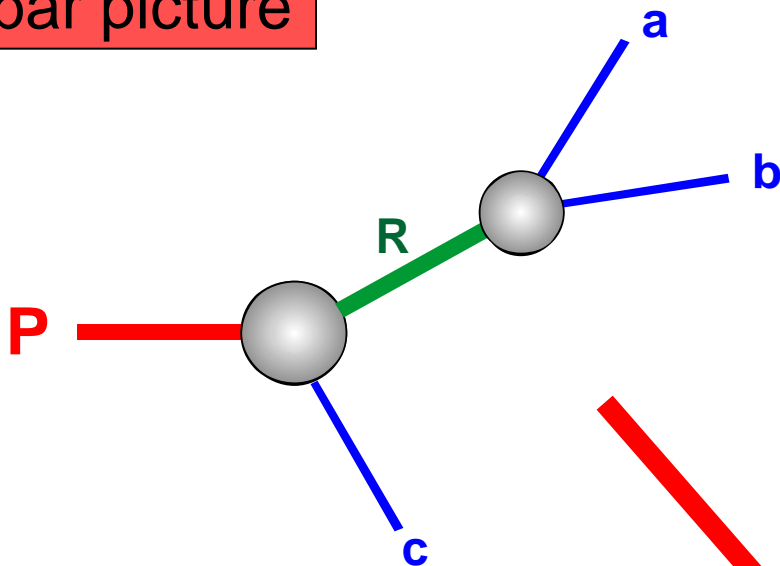
2

3

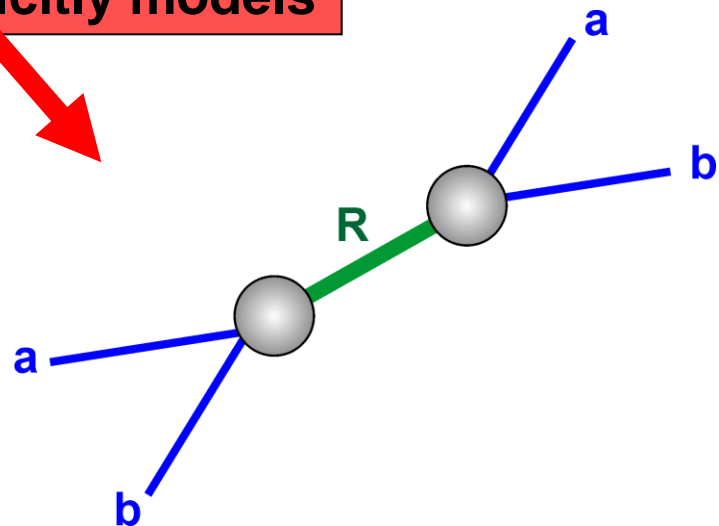
4

1

isobar picture



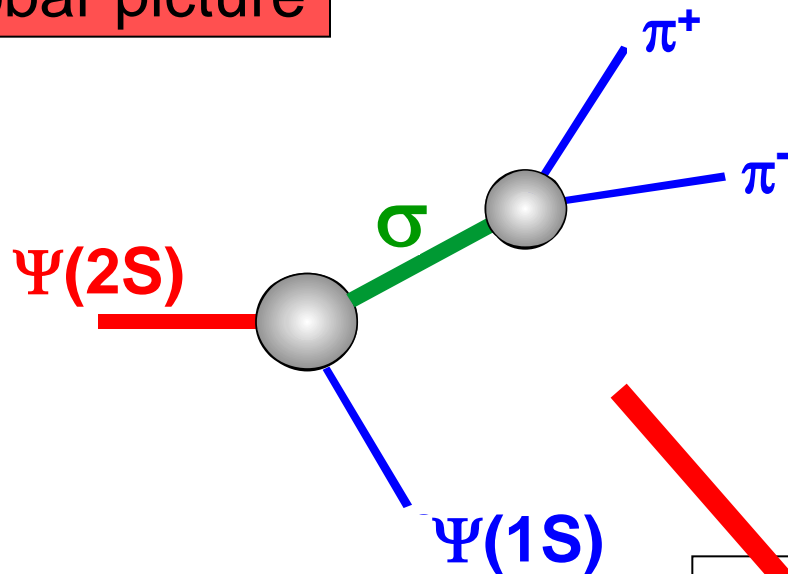
implicitly models



Universality
of final state interactions

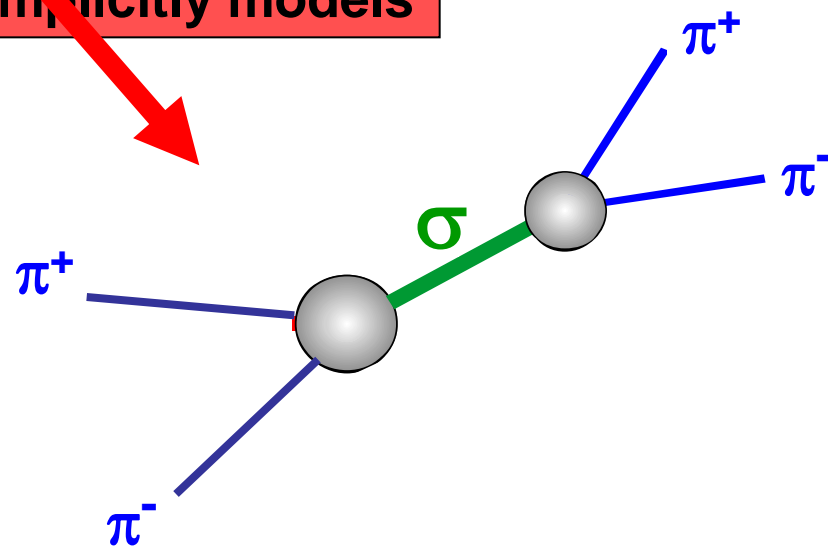
P → **a b c**

isobar picture



Universality
of final state interactions

implicitly models



$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$

$\text{Im } s \text{ (GeV)}^2$

0

-0.1

-0.2

-0.3

0

0.1

0.2

0.3

0.4

0.5

$\text{Re } s \text{ (GeV)}^2$

CCL

pku

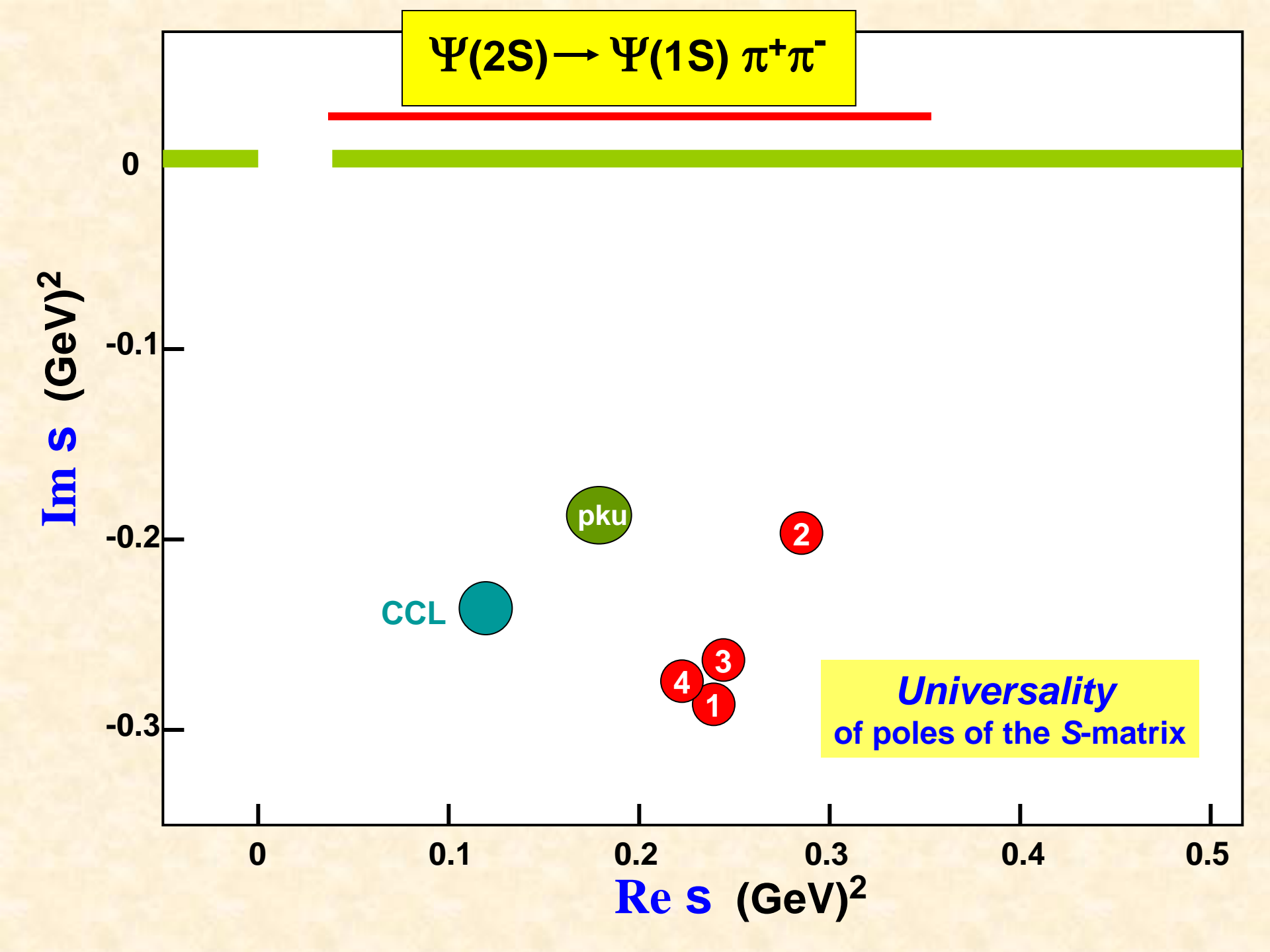
2

4

3

1

Universality
of poles of the S-matrix



$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$

Are the BESII data on $\Psi(2S)$ decay
inconsistent with $\pi\pi$ scattering?

$\text{Im } s \text{ (GeV)}^2$

0
-0.1
-0.2
-0.3

CCL

pku

2

4

3

1

Universality
of poles of the S-matrix

0

0.1

0.2

0.3

0.4

0.5

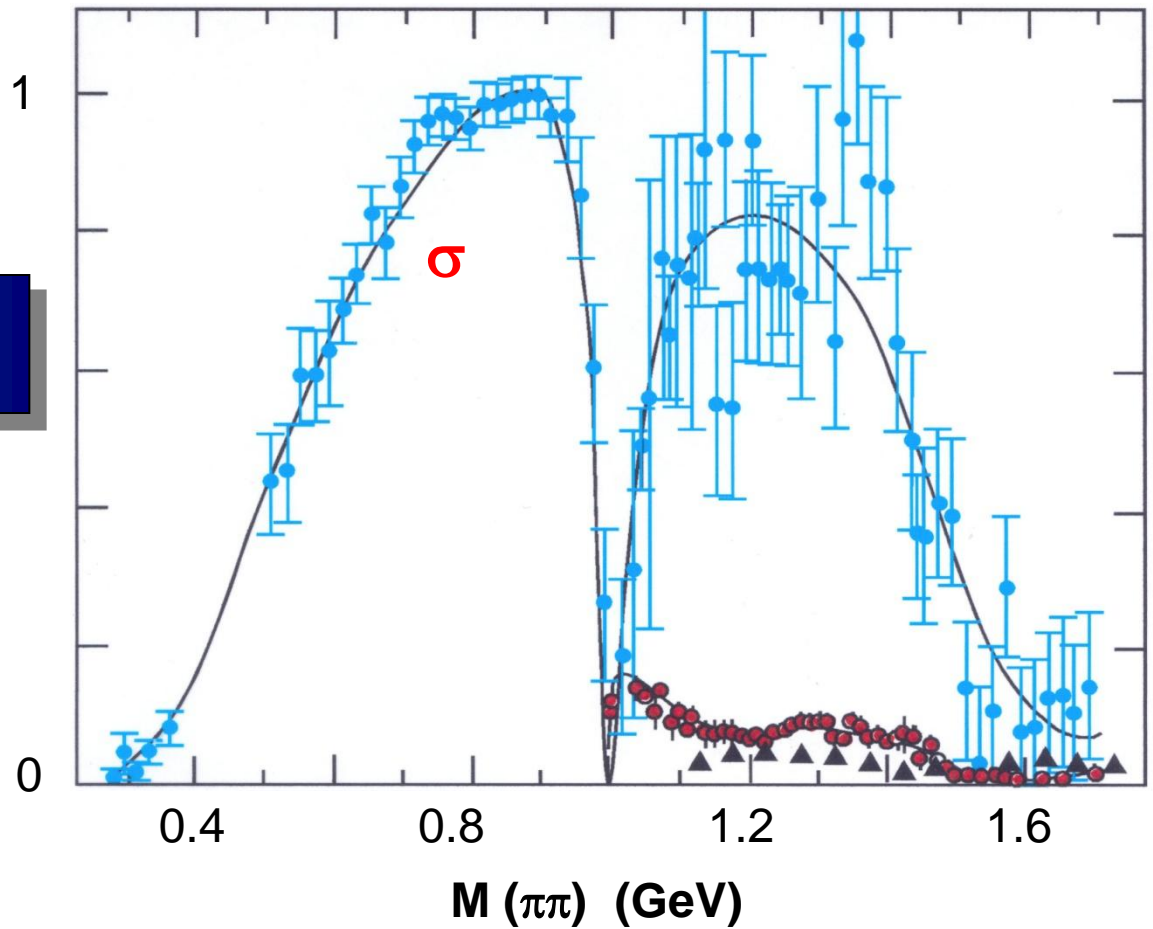
$\text{Re } s \text{ (GeV)}^2$

Scalar mesons

$\pi\pi \rightarrow \pi\pi$

$f_0(600)$

$I = J = 0$

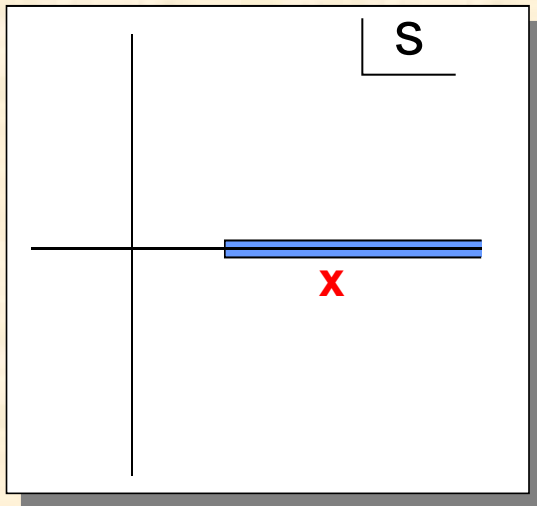
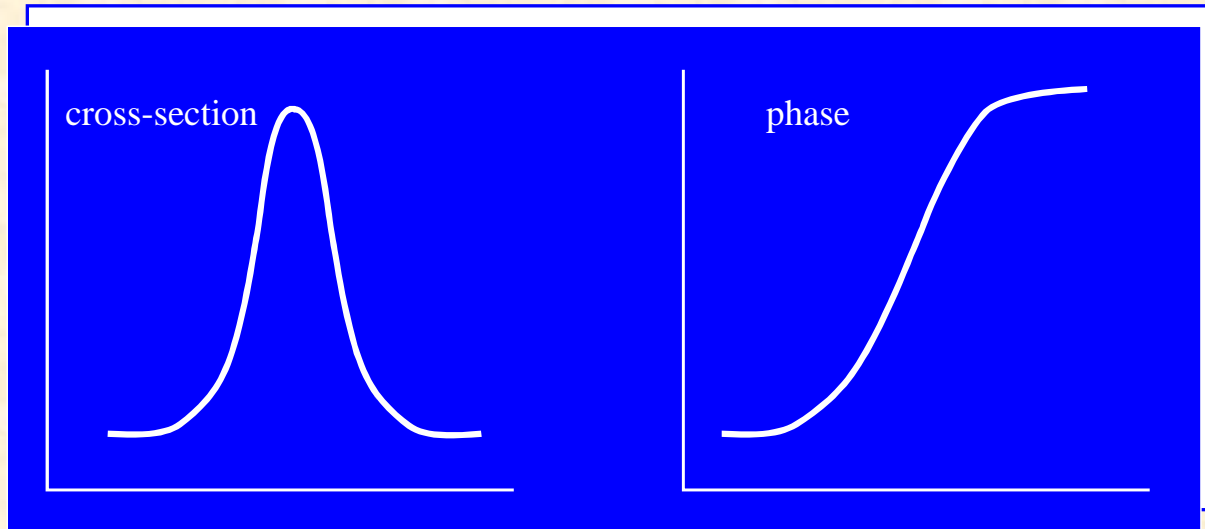


● $\pi\pi \rightarrow \pi\pi$

● $\pi\pi \rightarrow K\bar{K}$

▲ $\pi\pi \rightarrow \eta\eta$

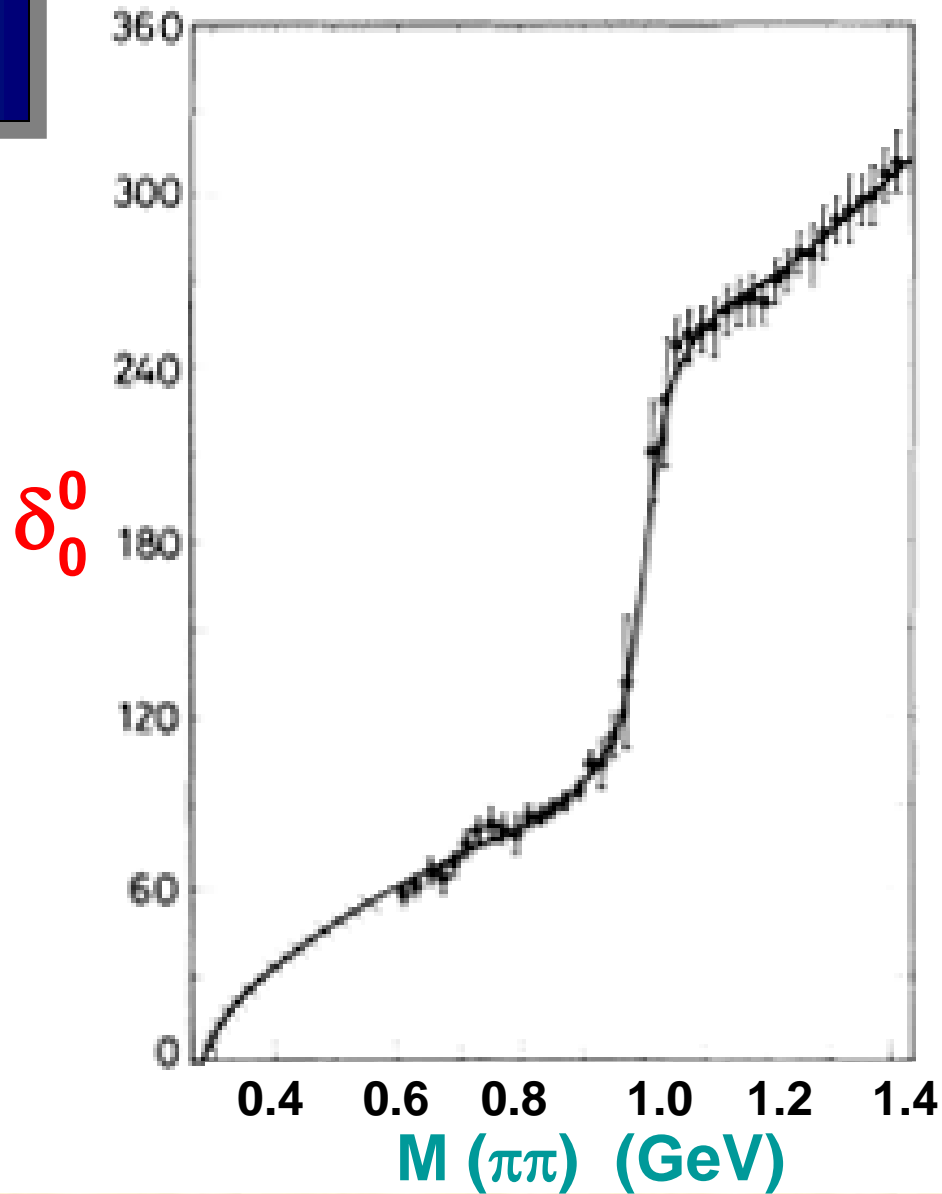
Hadron States



Breit-Wigner

$$\frac{1}{M^2 - s - iM\Gamma}$$

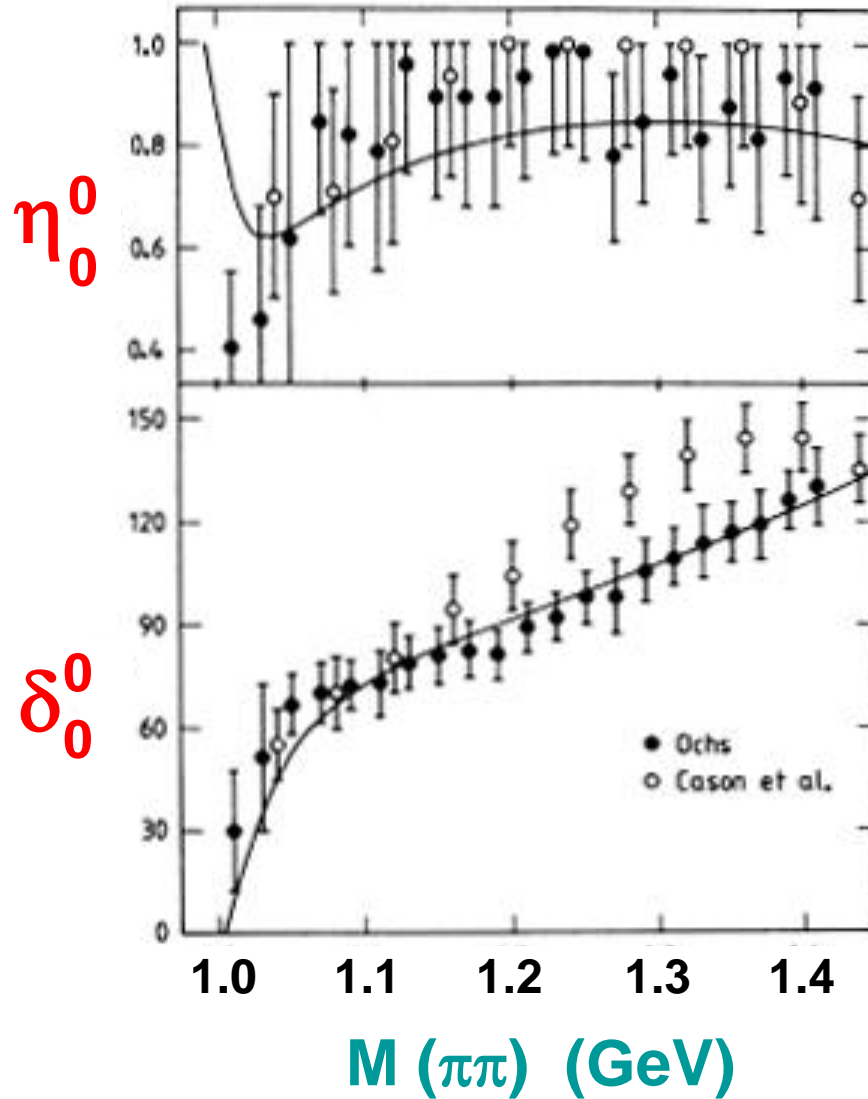
$\pi\pi \rightarrow \pi\pi$



$I = J = 0$

Ochs
CERN/Munich

$\pi\pi \rightarrow \pi\pi$



$I = J = 0$

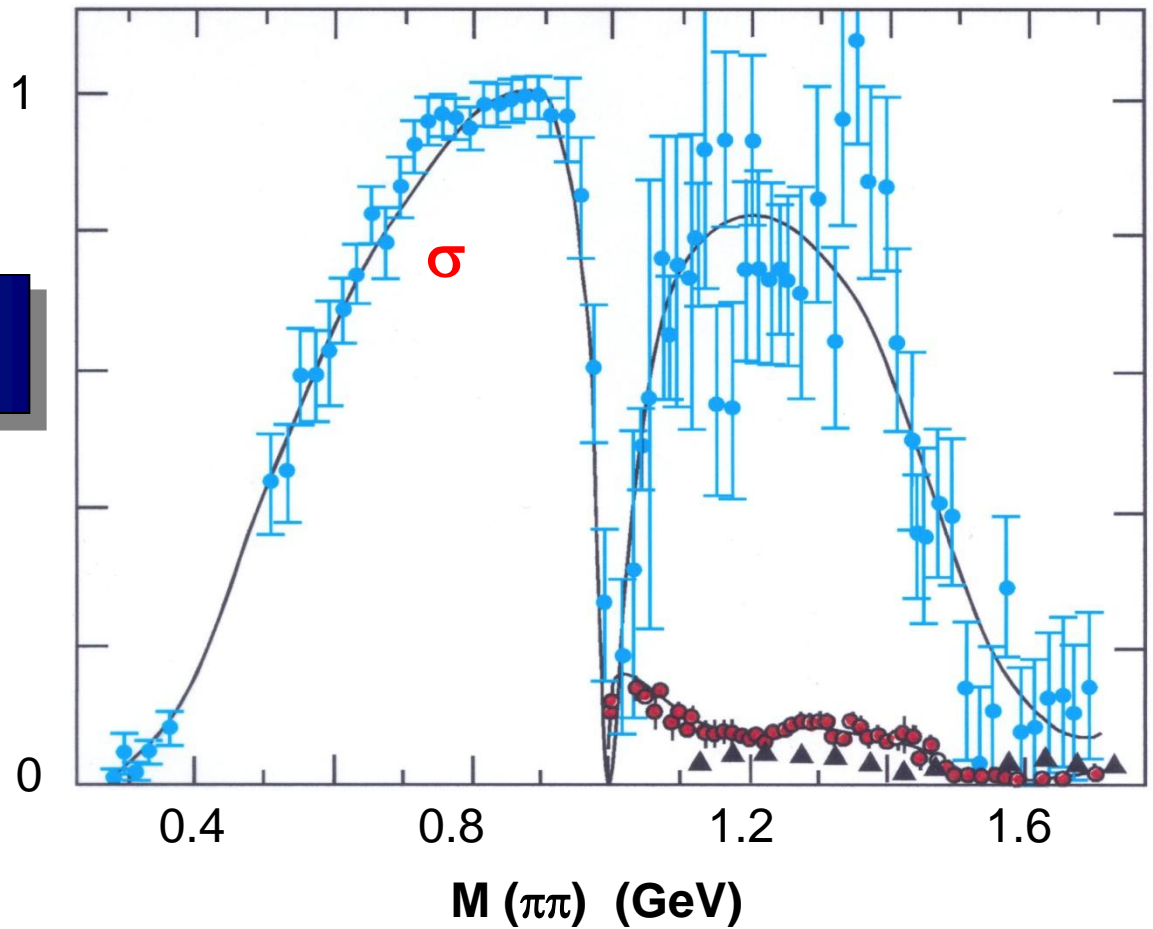
Sarantsev et al

Scalar mesons

$\pi\pi \rightarrow \pi\pi$

$f_0(600)$

$I = J = 0$



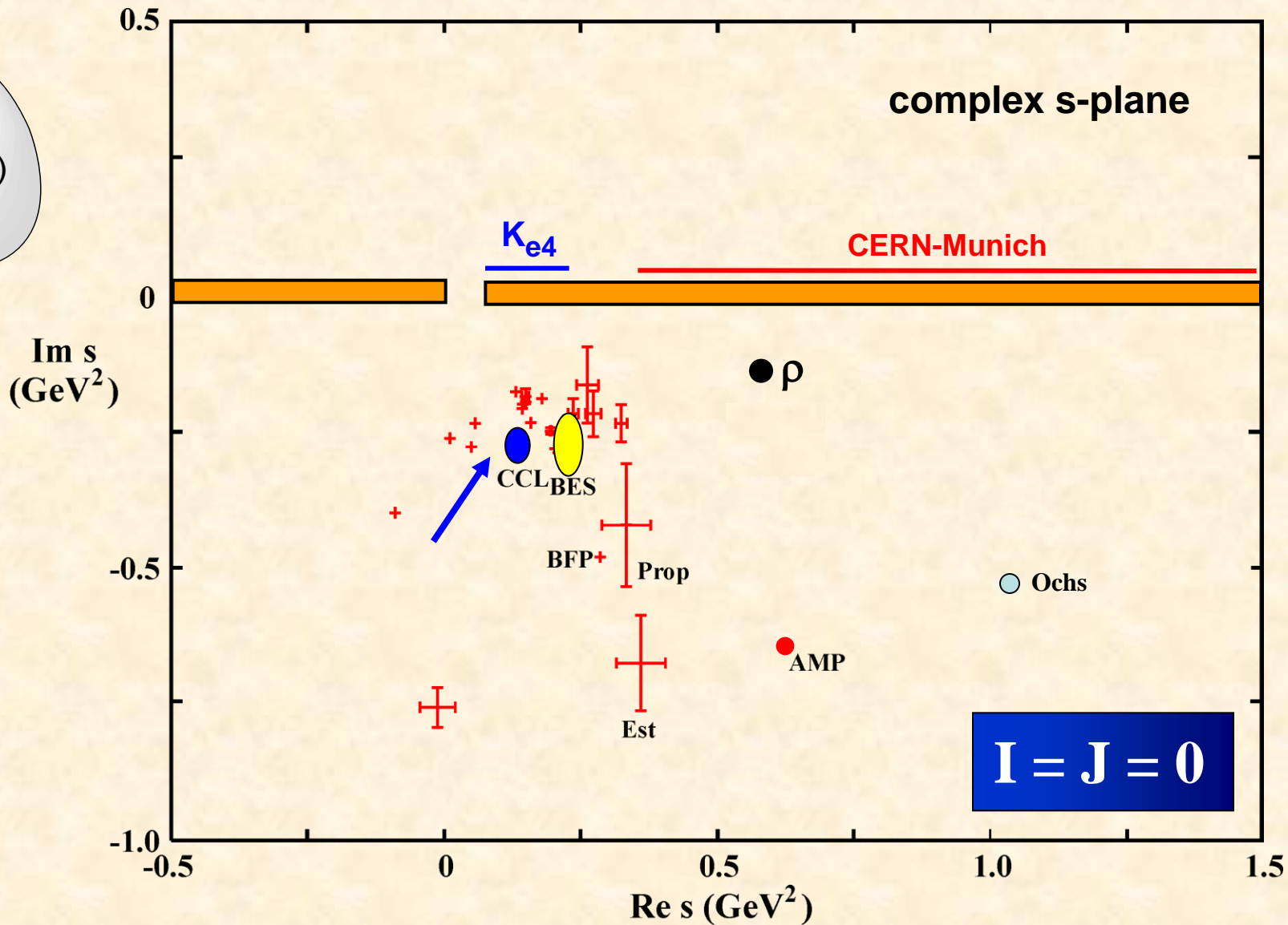
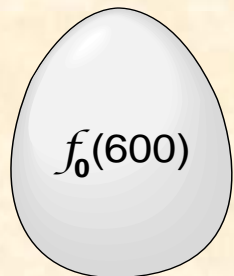
● $\pi\pi \rightarrow \pi\pi$

● $\pi\pi \rightarrow K\bar{K}$

▲ $\pi\pi \rightarrow \eta\eta$

Scalar mesons

$$s = E^2$$

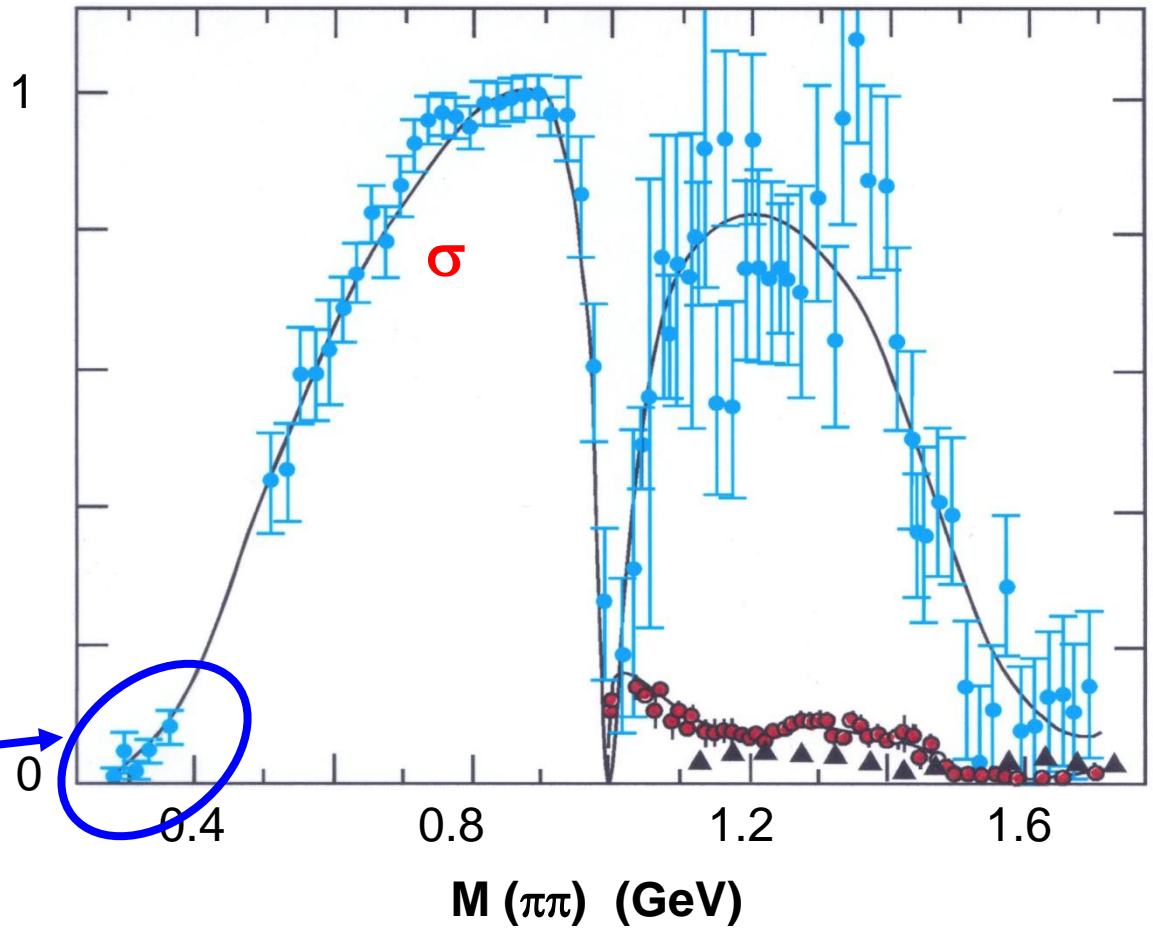


Scalar mesons

$\pi\pi \rightarrow \pi\pi$

$f_0(600)$

$K \rightarrow e\nu\pi\pi$



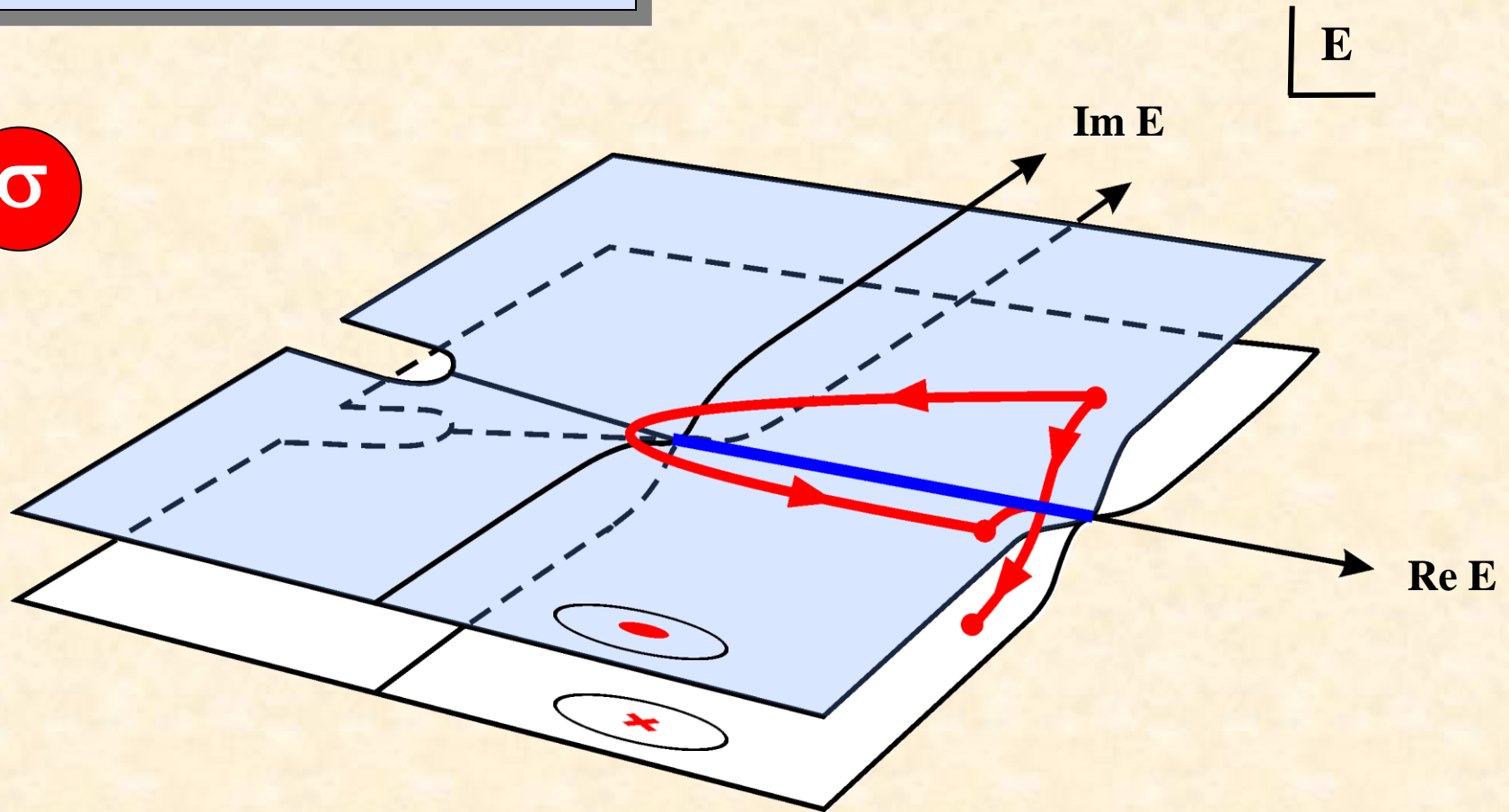
● $\pi\pi \rightarrow \pi\pi$

● $\pi\pi \rightarrow K\bar{K}$

▲ $\pi\pi \rightarrow \eta\eta$

Into the complex plane

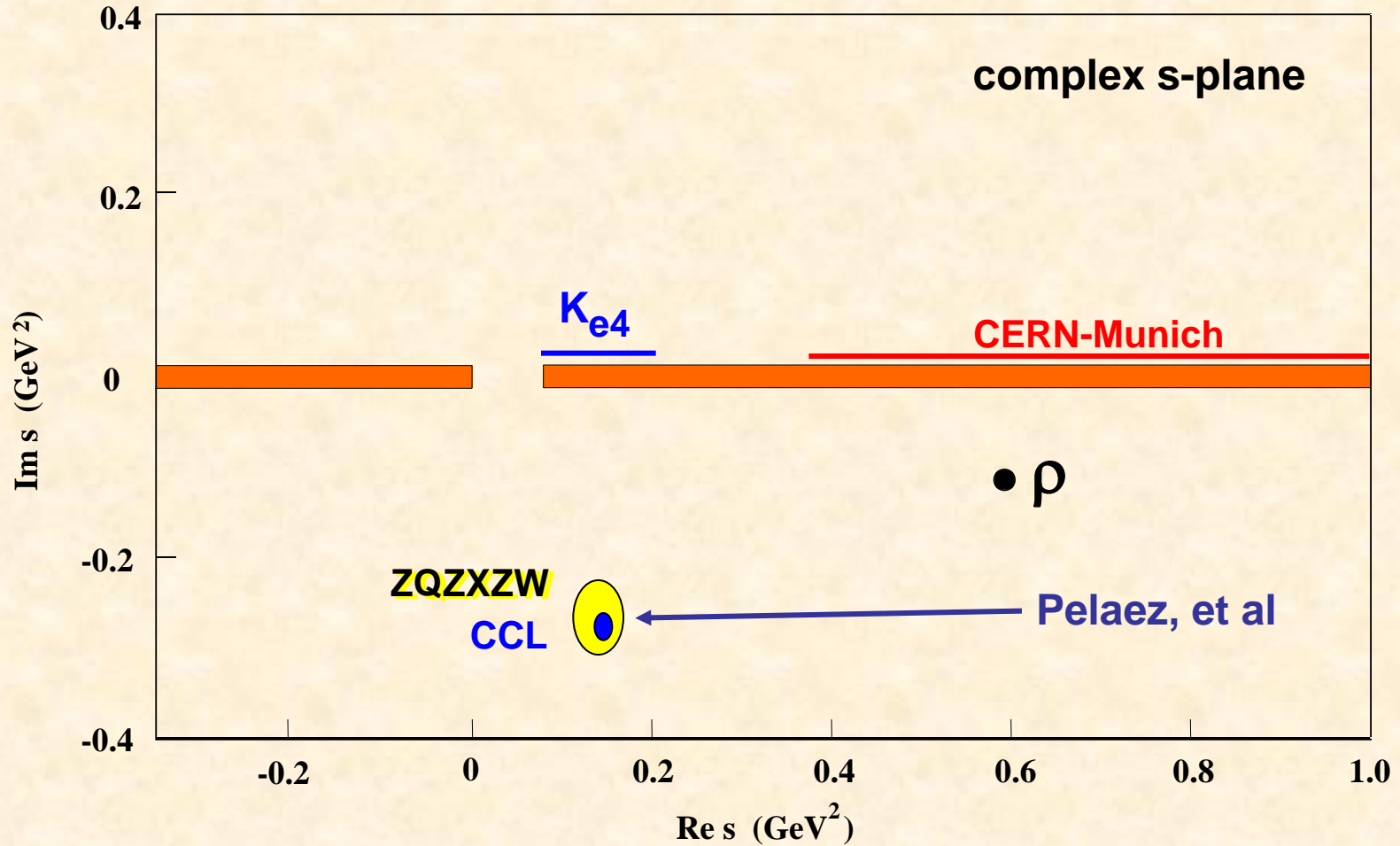
6



Caprini, Colangelo, & Leutwyler

$$\mathbf{E}_R = 441 - i 272 \text{ MeV}$$

$\pi\pi : I = 0, J = 0$



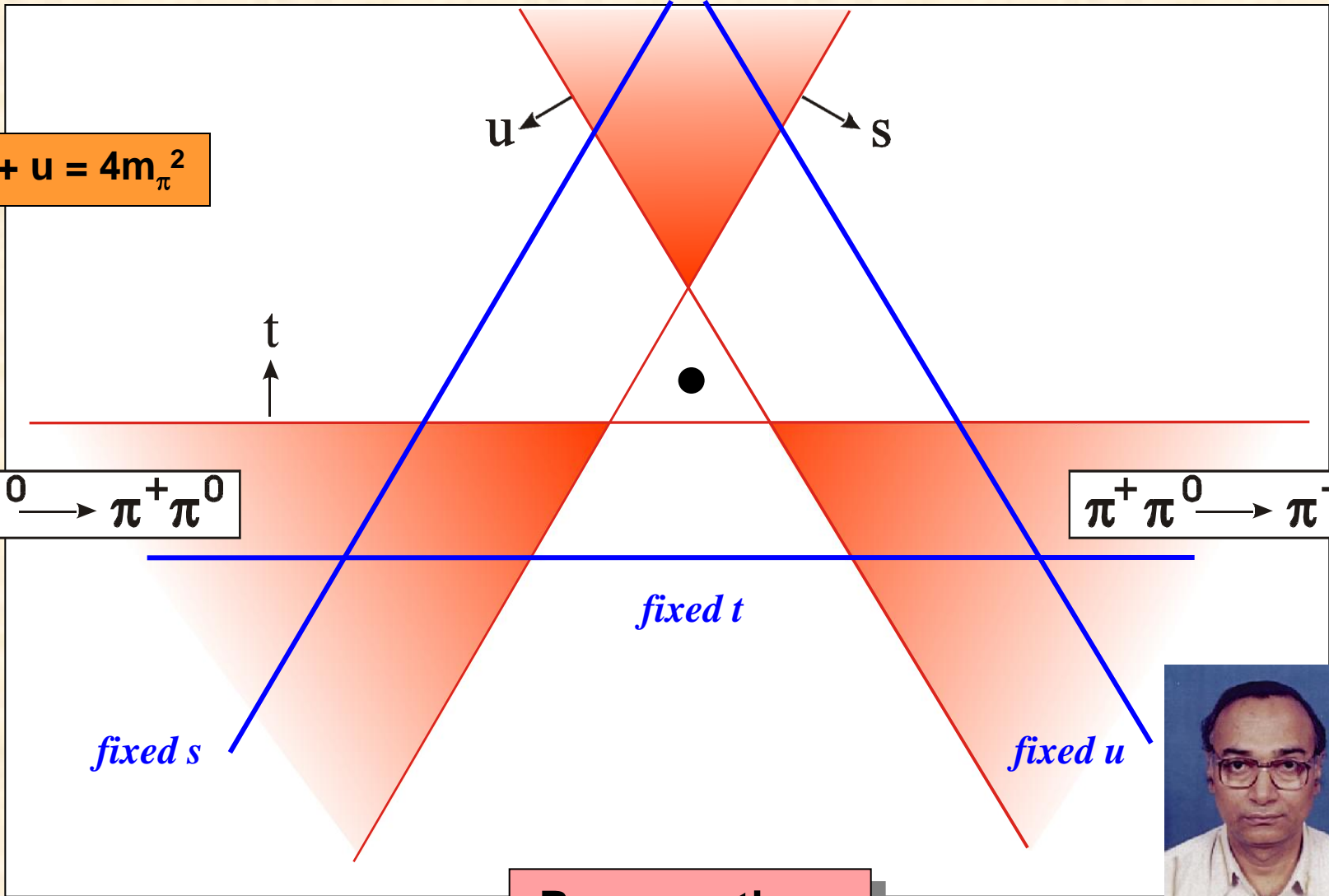
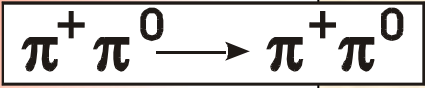
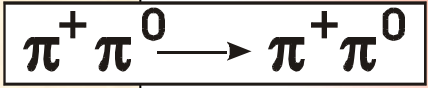
Caprini, Colangelo, & Leutwyler

Zhou, Qin, Zhang, Xiao, Zheng & Wu

$$E_R = 441 - i 272 \text{ MeV}$$



$$s + t + u = 4m_\pi^2$$



Roy equations



S M Roy

$\text{Im } s \text{ (GeV)}^2$

0
-0.2
-0.4
-0.6

0

0.2

0.4

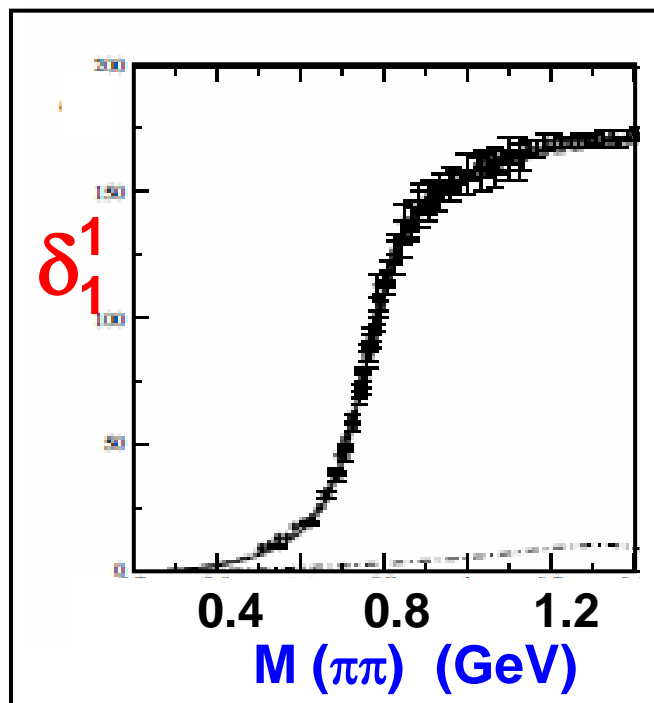
0.6

0.8

1.0

$\text{Re } s \text{ (GeV)}^2$

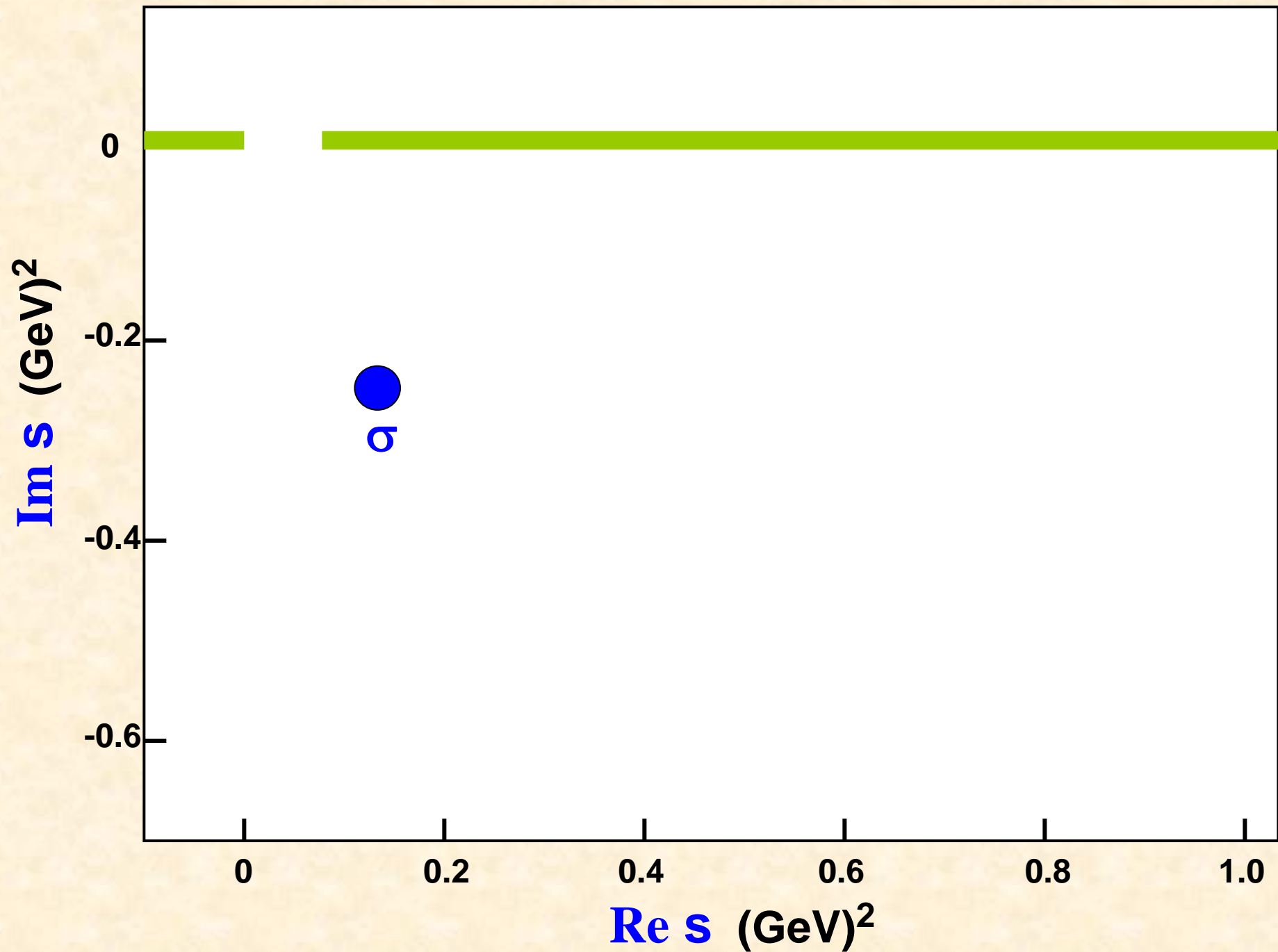
ρ ●



δ_1^1

0.4 0.8 1.2

$M(\pi\pi) \text{ (GeV)}$



$\text{Im } s \text{ (GeV)}^2$

0
-0.2
-0.4
-0.6

9

0

0.2

$\text{Re } s \text{ (GeV)}^2$

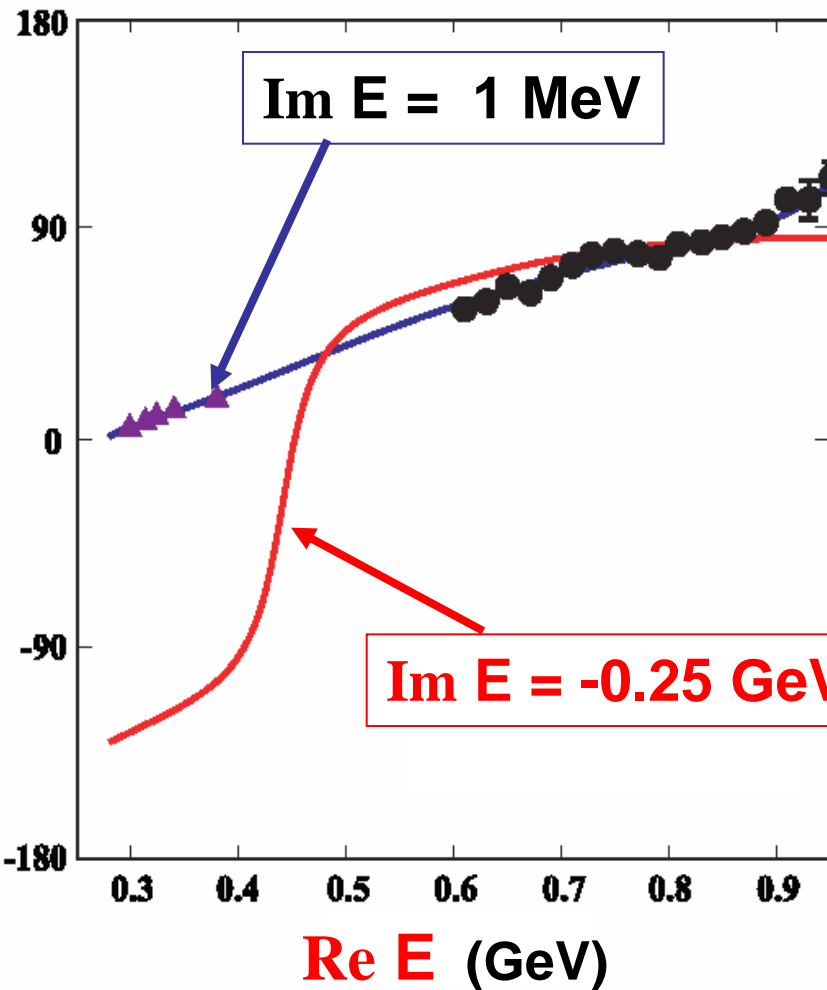
0.4

0.6

0.8

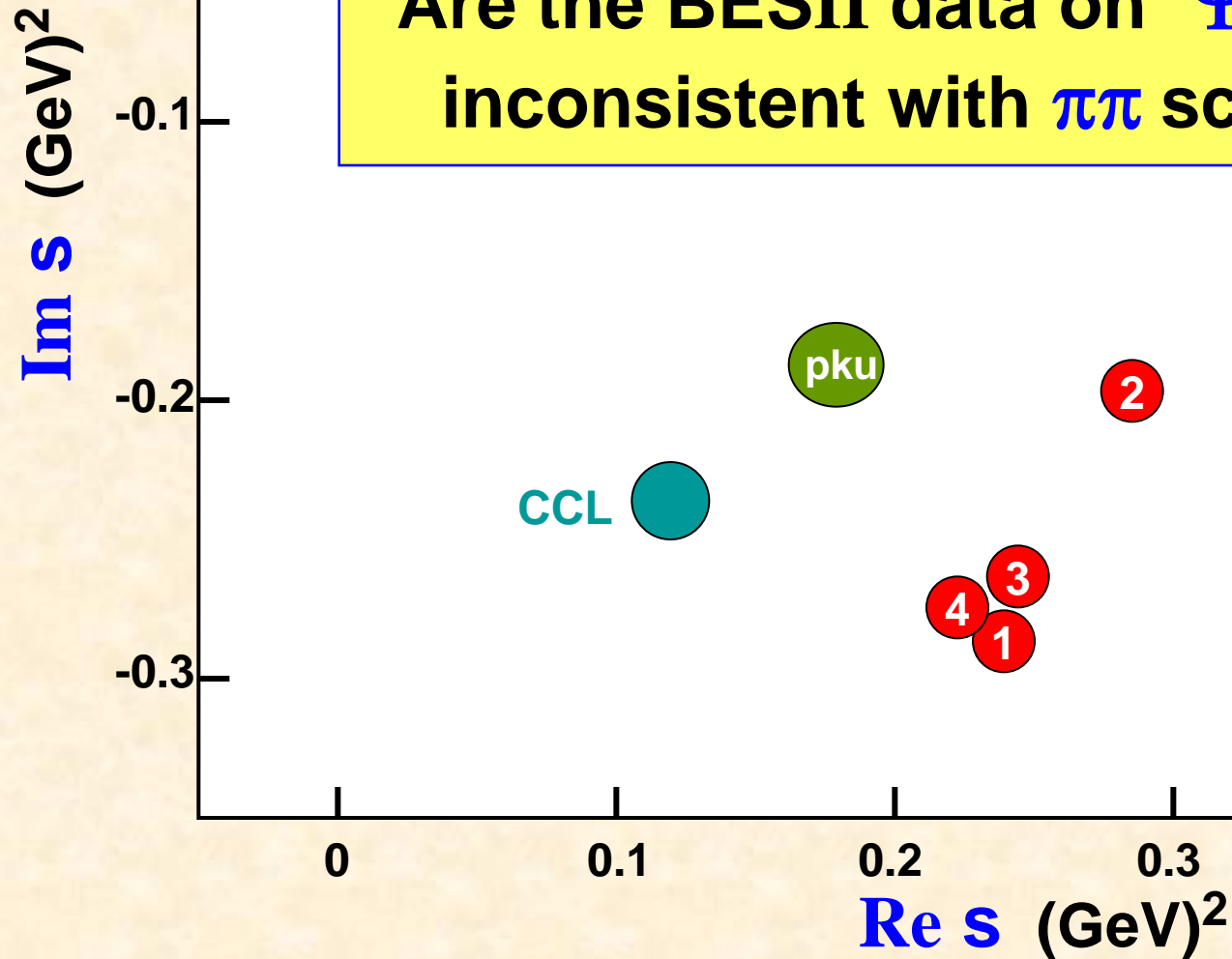
1.0

phase (degrees)

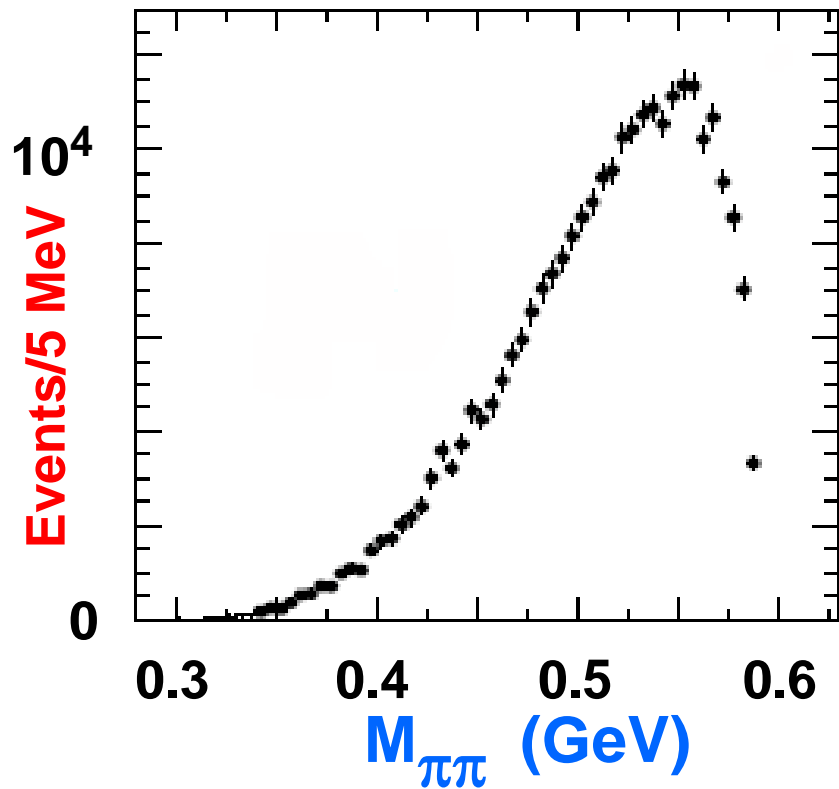
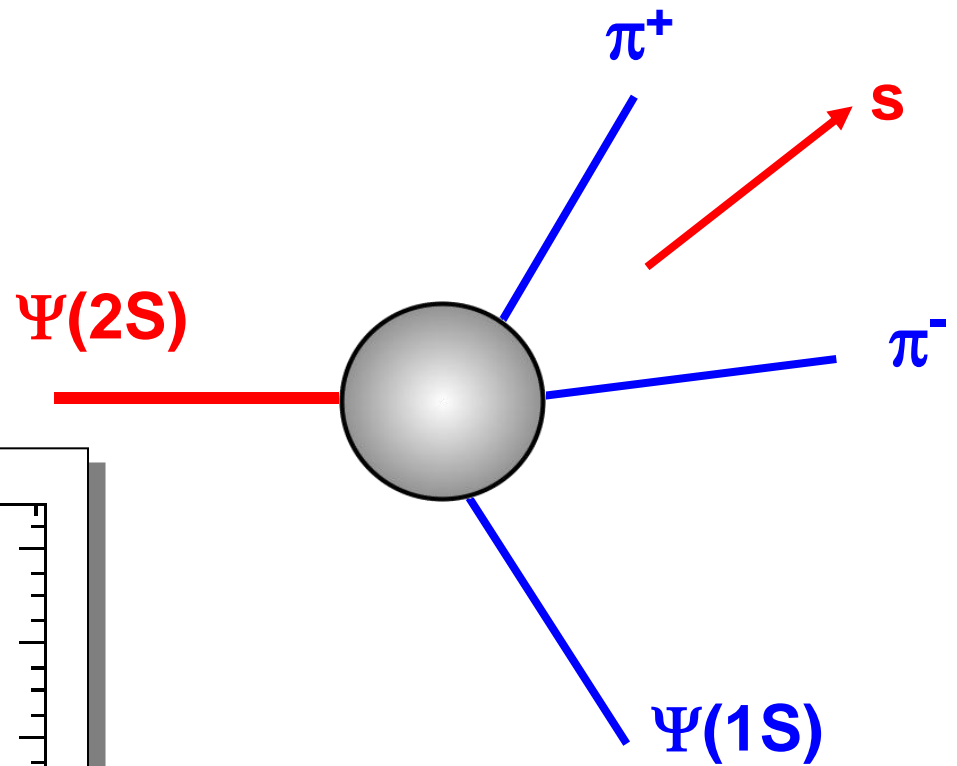


$$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$$

Are the BESII data on $\Psi(2S)$ decay
inconsistent with $\pi\pi$ scattering?

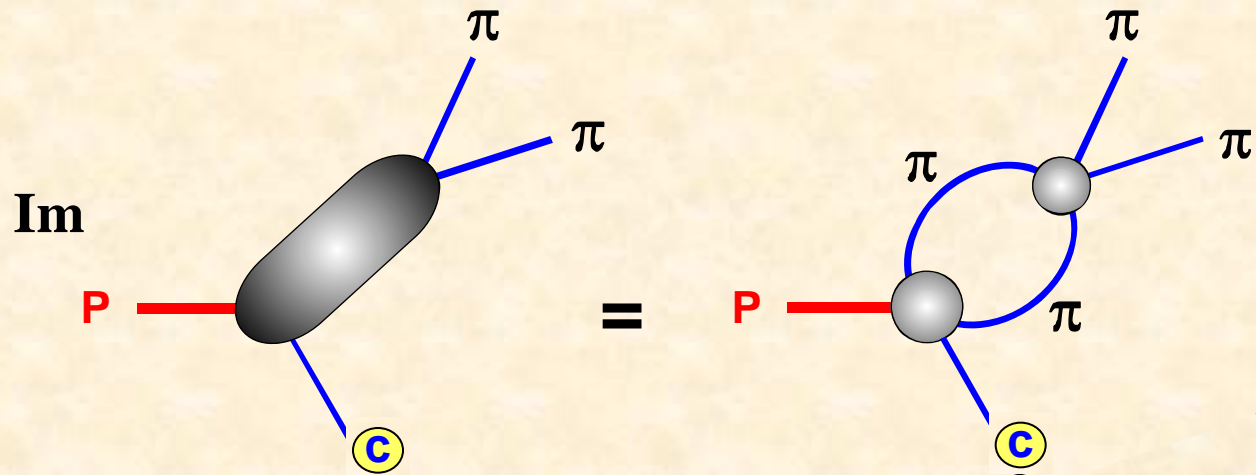


$$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$$



no need for isobar picture

Unitarity : decays in spectator picture

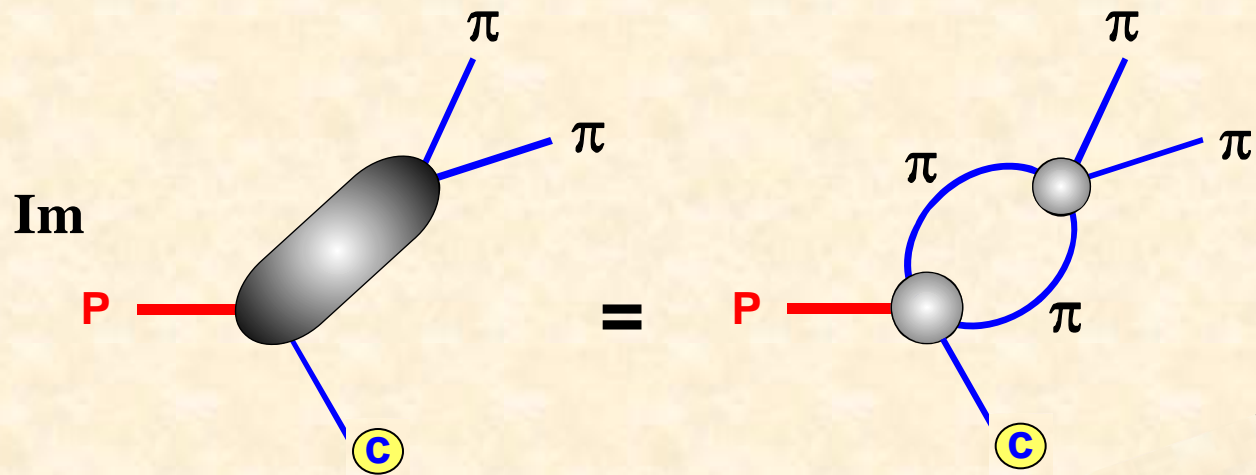


$$T = \frac{K}{1 - i\rho K}$$

$$F = \frac{P}{1 - i\rho K} = \alpha T$$

C spectator

Unitarity : decays in spectator picture



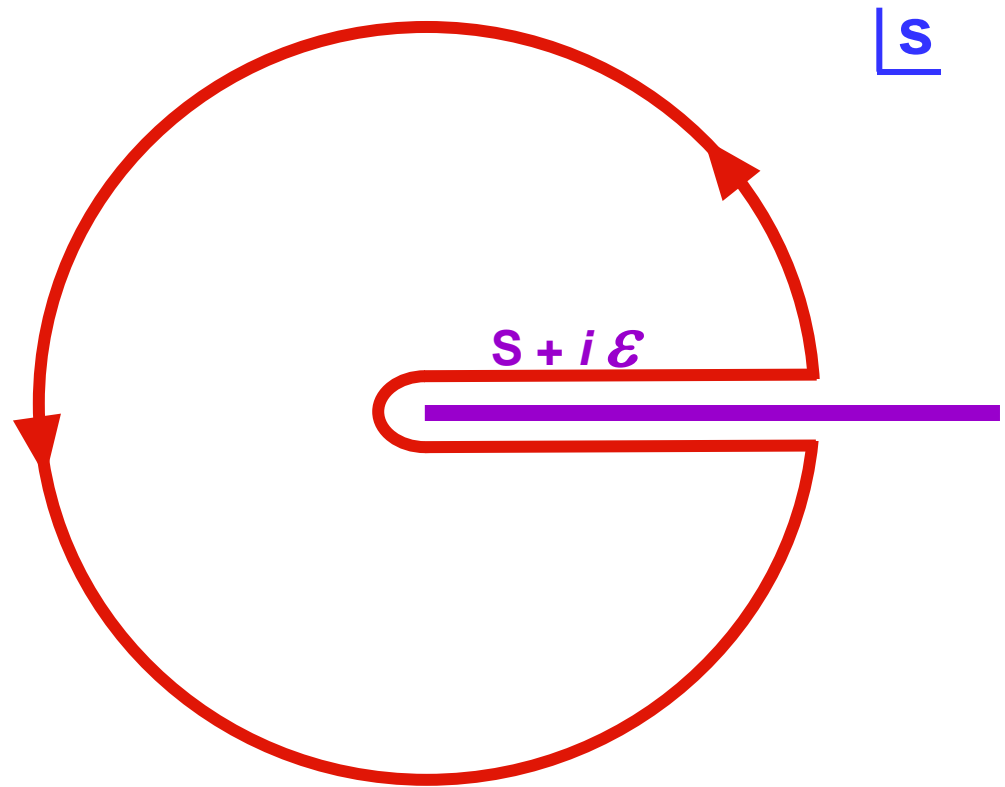
$F = \alpha T \longrightarrow$
Watson's theorem
 elastic
 phases simply related
 if no rescattering

Universality
 of final state interactions
 on the real energy axis

 spectator

$$f(s) = \frac{1}{\pi} \int_{s_t}^{\infty} \frac{ds' \operatorname{Im} f(s')}{(s' - s)}$$

Cauchy's theorem



$$\mathbf{F}(s) = |\mathbf{F}(s)| \exp \left[i\Phi(s) \right]$$

$$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$$

Step 1: define

$$\Omega(s) = |\Omega(s)| \exp \left[i\Phi(s) \right]$$

only has right hand cut

where $\Phi(s) = \Phi(\pi\pi \rightarrow \pi\pi)$ with same \mathbf{I}, \mathbf{J} in elastic region

$$F(s) = |F(s)| \exp \left[i \Phi(s) \right]$$

$$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$$

Step 1: define

$$\Omega(s) = |\Omega(s)| \exp \left[i \Phi(s) \right]$$

only has right hand cut

where $\Phi(s) = \Phi(\pi\pi \rightarrow \pi\pi)$ with same **I, J** in elastic region

Step 2: then

$$F(s) = P(s) \cdot \Omega(s)$$

where $P(s)$ is real for $s > s_t$

Step 1: define

$$\Omega(s) = |\Omega(s)| \exp \left[i \Phi(s) \right]$$

only has right hand cut

where $\Phi(s) = \Phi(\pi\pi \rightarrow \pi\pi)$ with same **I, J** in elastic region

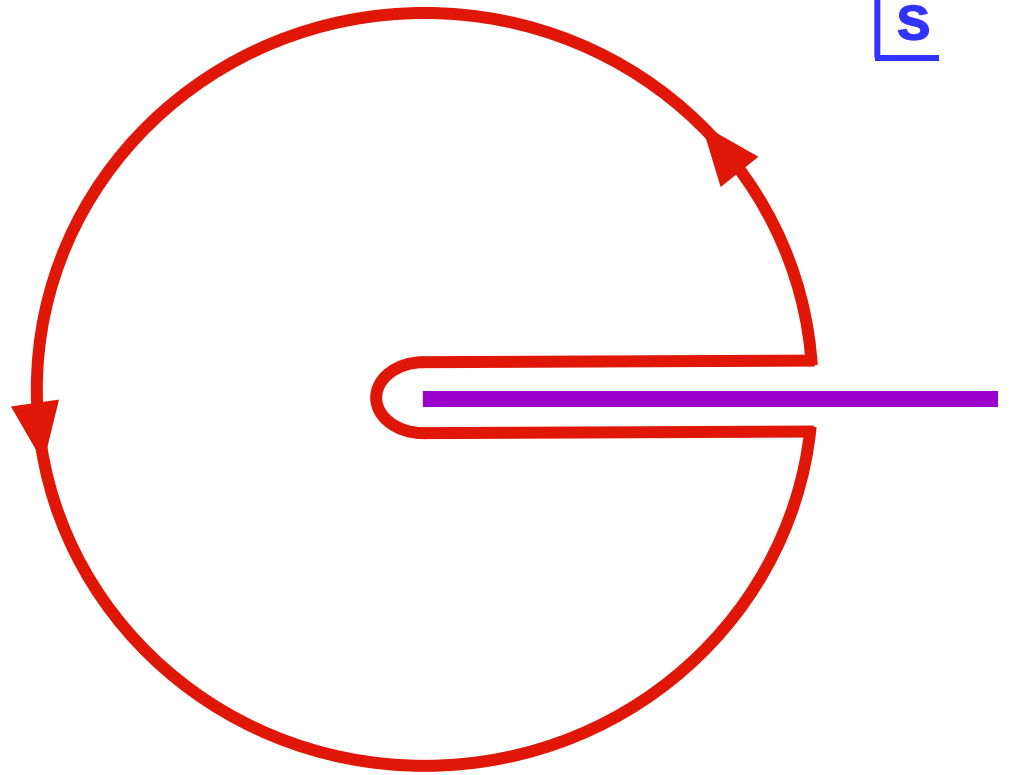
$$f(s) = \frac{1}{\pi} \int_{s_t}^{\infty} \frac{ds' \operatorname{Im} f(s')}{(s' - s)}$$

only has right hand cut

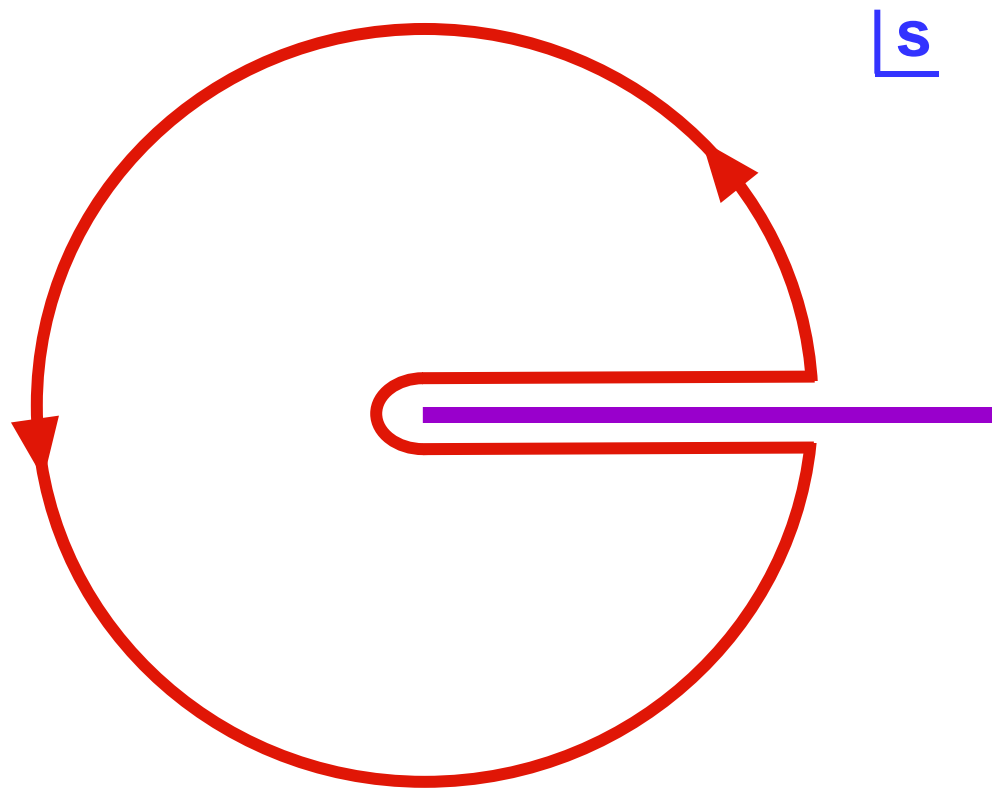
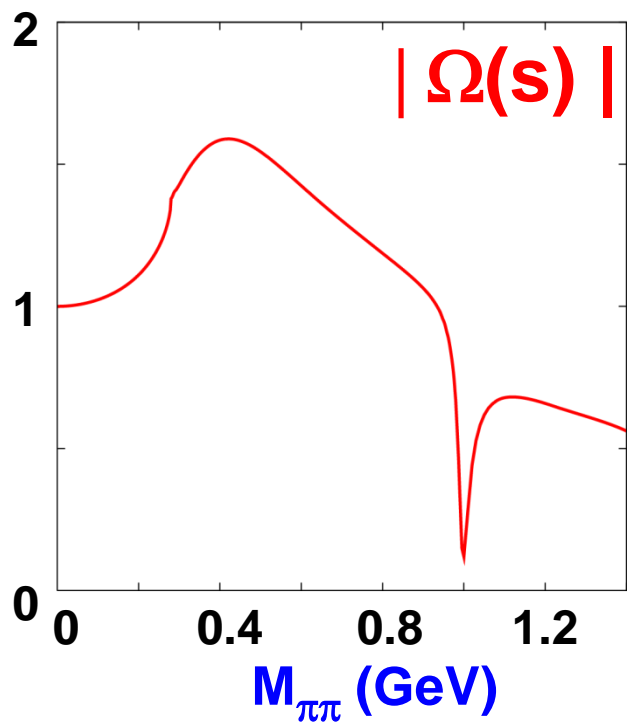
let

$$f(s) = \ln \Omega(s)$$

$$\Omega(s) = \exp \left[\frac{is}{\pi} \int_{s_t}^{\infty} \frac{ds' \Phi(s')}{s'(s' - s)} \right]$$



$$\Omega(s) = \exp \left[\frac{is}{\pi} \int_{s_t}^{\infty} \frac{ds' \Phi(s')}{s'(s'-s)} \right]$$



Step 2: then

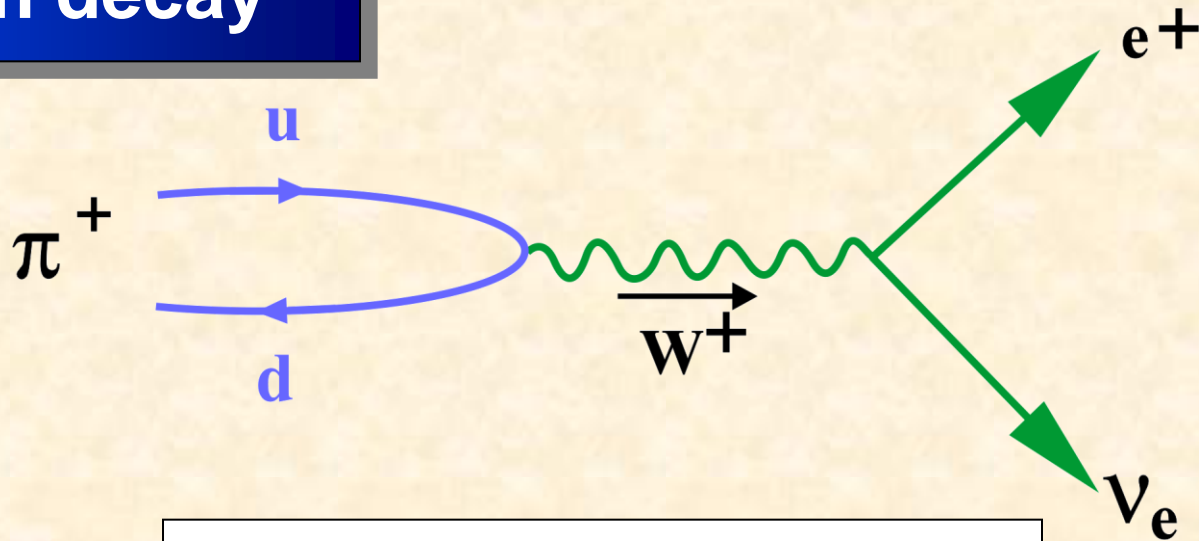
$$F(s) = P(s) \cdot \Omega(s)$$

where $P(s)$ is real for $s > s_t$

what is $P(s)$ for

$$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^- \quad ?$$

Pion decay



$$\langle \pi(p) | A_\mu | O \rangle = i f_\pi p_\mu$$

$$\langle \pi(p) | \partial^\mu A_\mu | O \rangle = i f_\pi p_\mu (-i p^\mu)$$

$$= f_\pi m_\pi^2$$

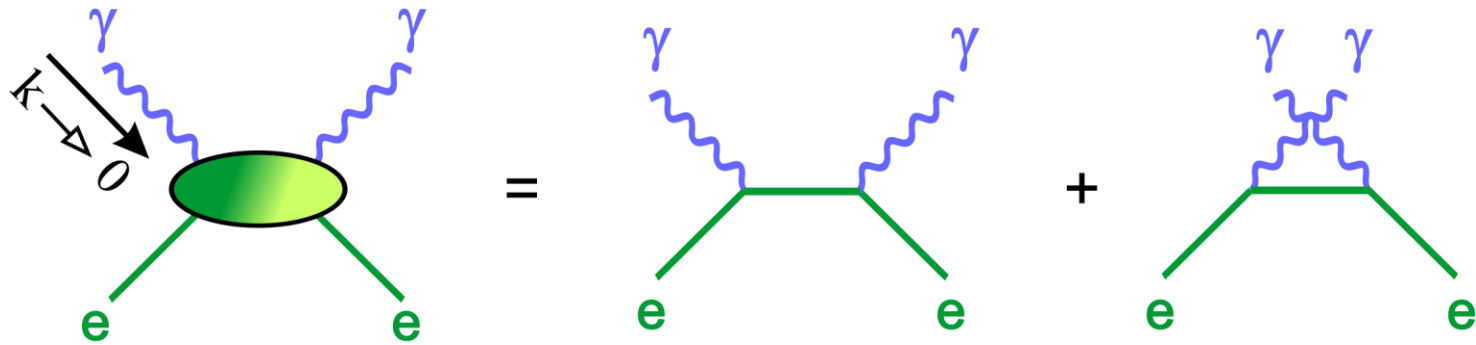
$$m_\pi \rightarrow 0$$

$$\partial^\mu A_\mu = 0$$

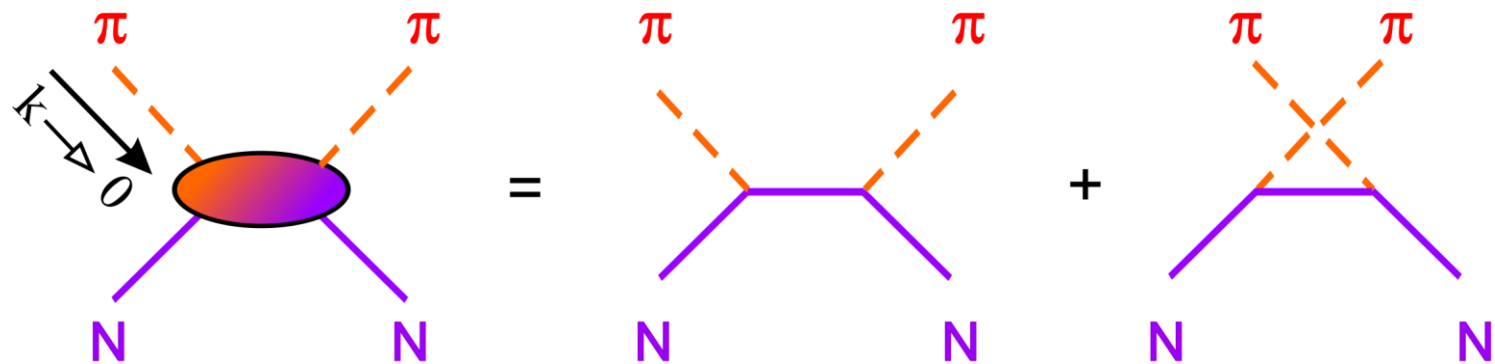
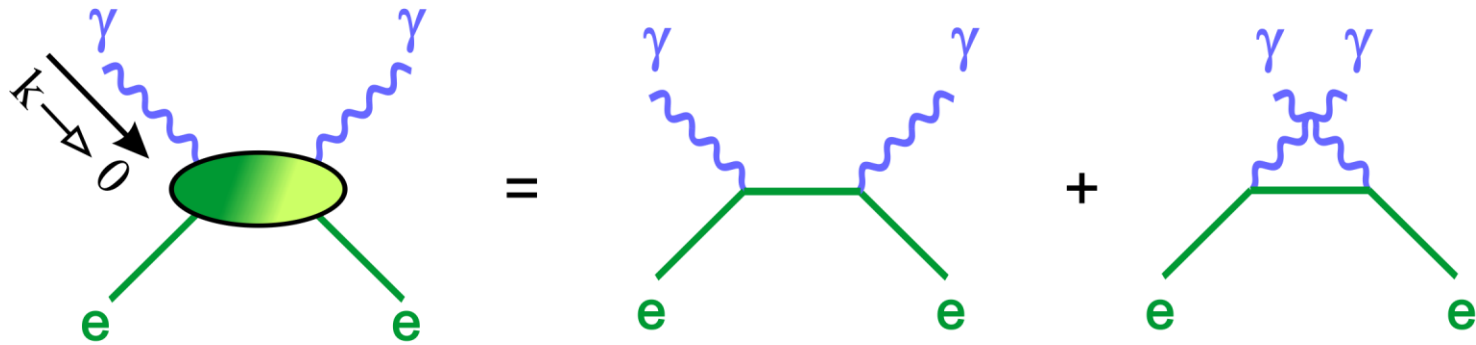
CAC

PCAC

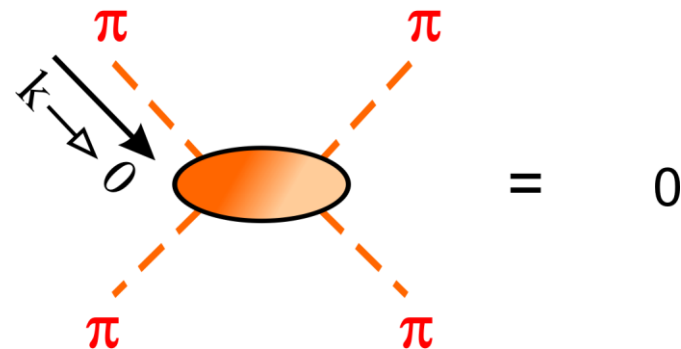
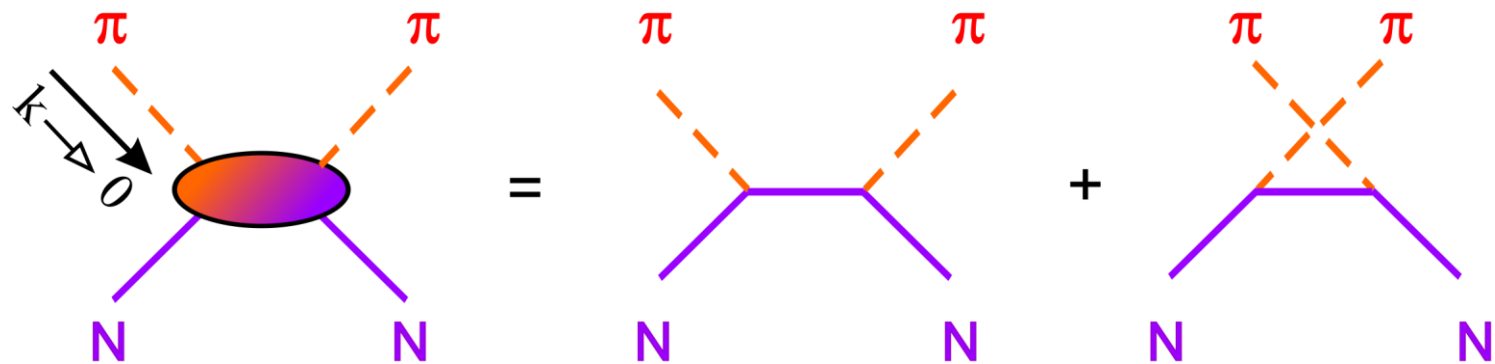
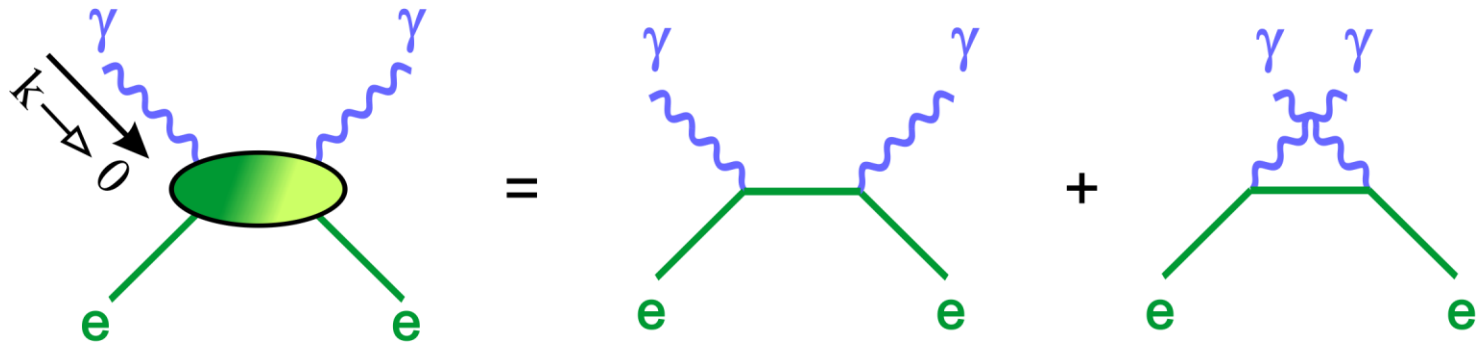
Low energy theorems



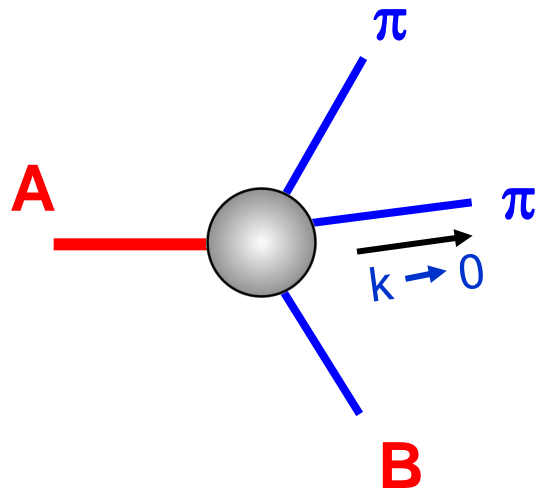
Low energy theorems



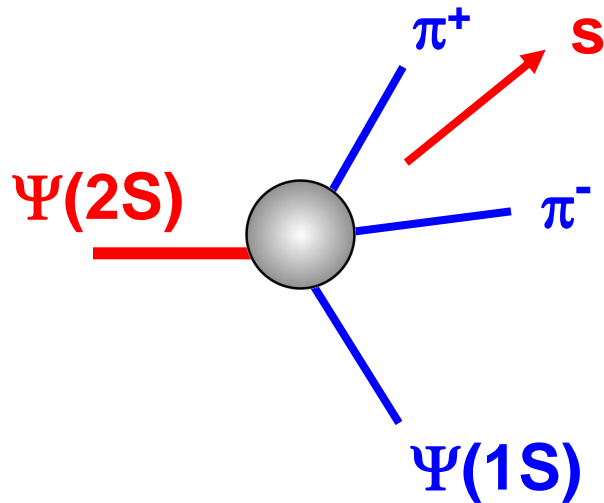
Low energy theorems



CAC **PCAC**



= Born amplitude



= 0

$$s = O(m_\pi^2)$$

PHYSICAL REVIEW D

VOLUME 12, NUMBER 5

1 SEPTEMBER 1975

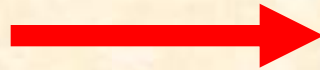
$\psi' \rightarrow \psi \pi \pi$ decay as a test of partial conservation of axial-vector current

D. Morgan and M. R. Pennington

Rutherford Laboratory, Chilton, Didcot, Berkshire, OX11 0QX, England
(Received 14 April 1975)

The shape of the $\pi^+ \pi^-$ mass distribution in the recently analyzed $\psi' \rightarrow \psi \pi \pi$ decay is explained. Although the explanation assumes the known general features of the $\pi \pi$ s-wave amplitude, detailed alternatives are not distinguished; rather, it is the on-shell appearance of the Adler zero which is crucial. The extension of this description to other dipion production processes is illustrated with a discussion of low energy $\pi^- p \rightarrow \pi^+ \pi^- n$.

$$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$$



$$P(s) = N \cdot (s - \lambda m_\pi^2)$$

PHYSICAL REVIEW
LETTERS

VOLUME 35

7 JULY 1975

NUMBER 1

Chiral Symmetry and $\psi' \rightarrow \psi \pi \pi$ Decay

Lowell S. Brown

Fermi National Accelerator Laboratory, Batavia, Illinois 60510, and
Physics Department, University of Washington, Seattle, Washington 98195

and

Robert N. Cahn

Physics Department, University of Washington, Seattle, Washington 98195
(Received 23 April 1975)

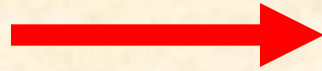
Unbroken chiral symmetry (with a vanishing σ term) relates the $\psi' \rightarrow \psi \pi \pi$ decay amplitude to three basic parameters. Two of these parameters put strong angular correlations in the amplitude which, apparently, are not observed. Taking these two parameters to vanish, we obtain an isotropic decay which is strongly peaked in the region where the invariant mass of the $\pi \pi$ system is large.

Step 2: then

$$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$$

$$F(s) = P(s) \cdot \Omega(s)$$

where $P(s)$ is real for $s > s_t$



$$P(s) = N \cdot (s - \lambda m_\pi^2)$$

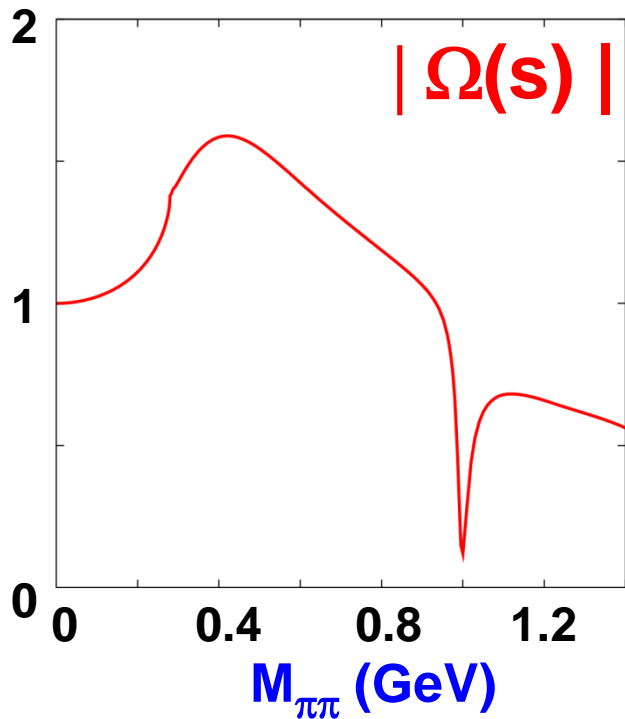
Step 2: then

$$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$$

$$F(s) = P(s) \cdot \Omega(s)$$

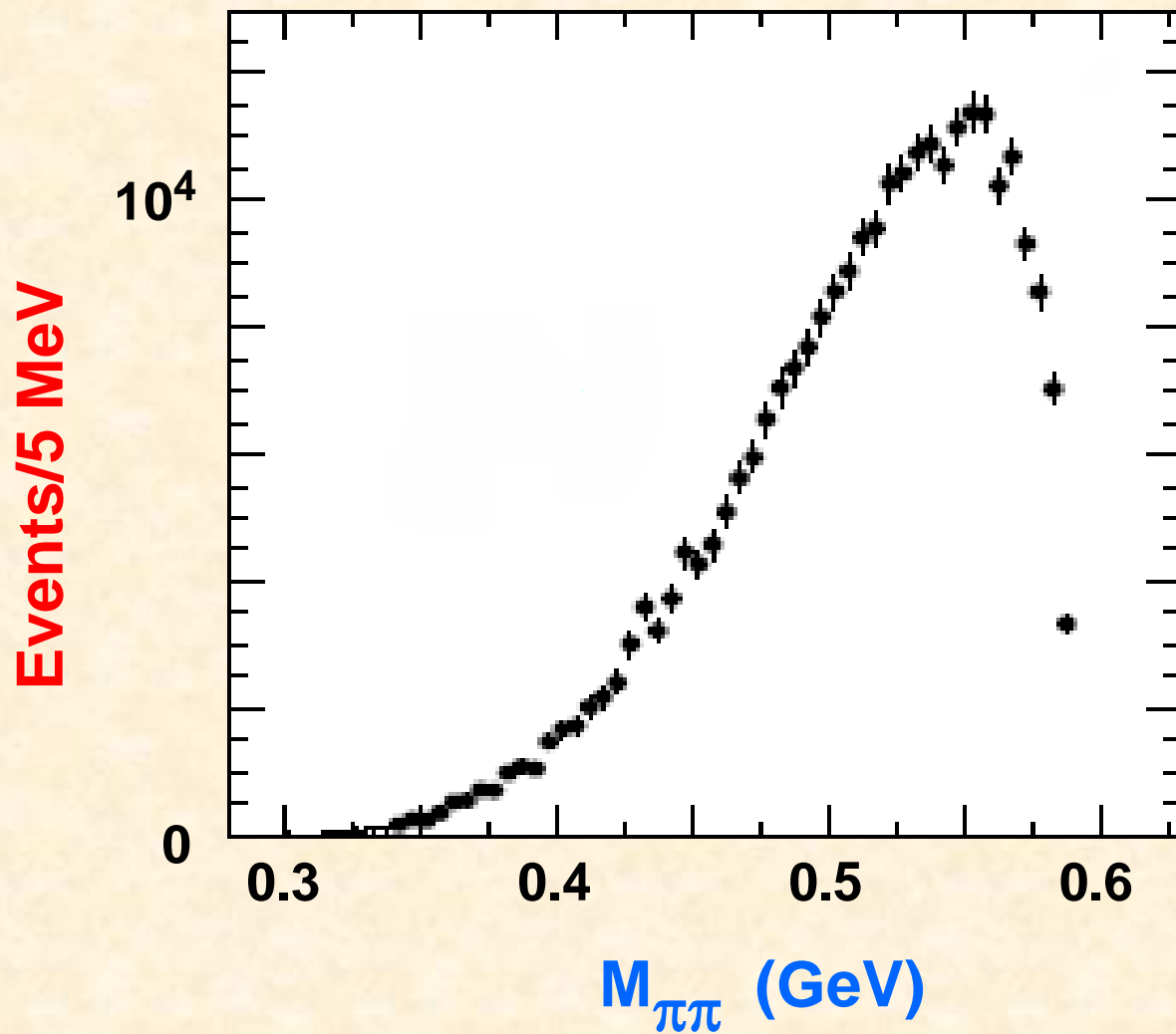
where $P(s)$ is real for $s > s_t$

$$P(s) = N \cdot (s - \lambda m_\pi^2)$$

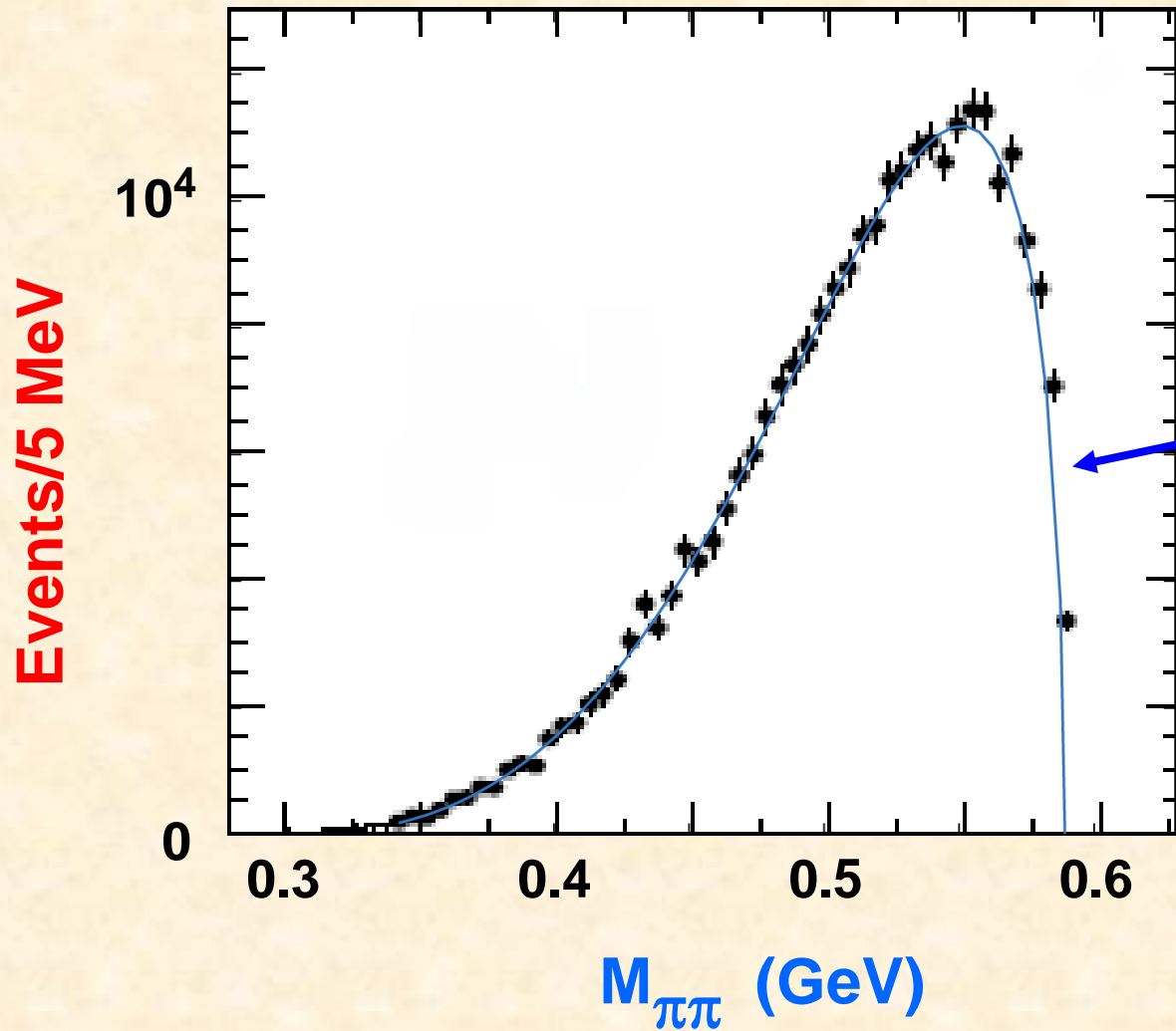


$|\Omega(s)|$ encodes σ

$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$

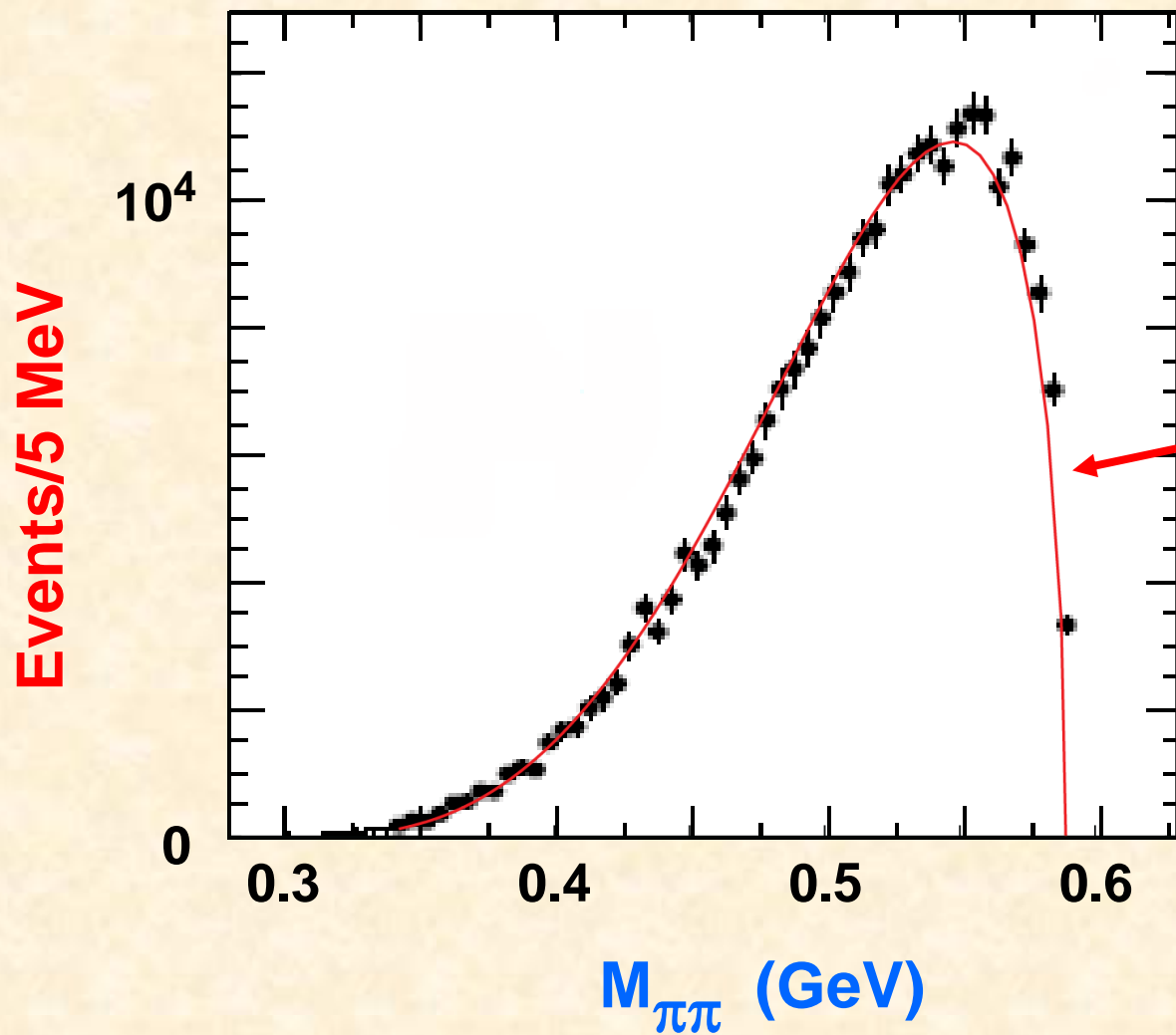


$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$



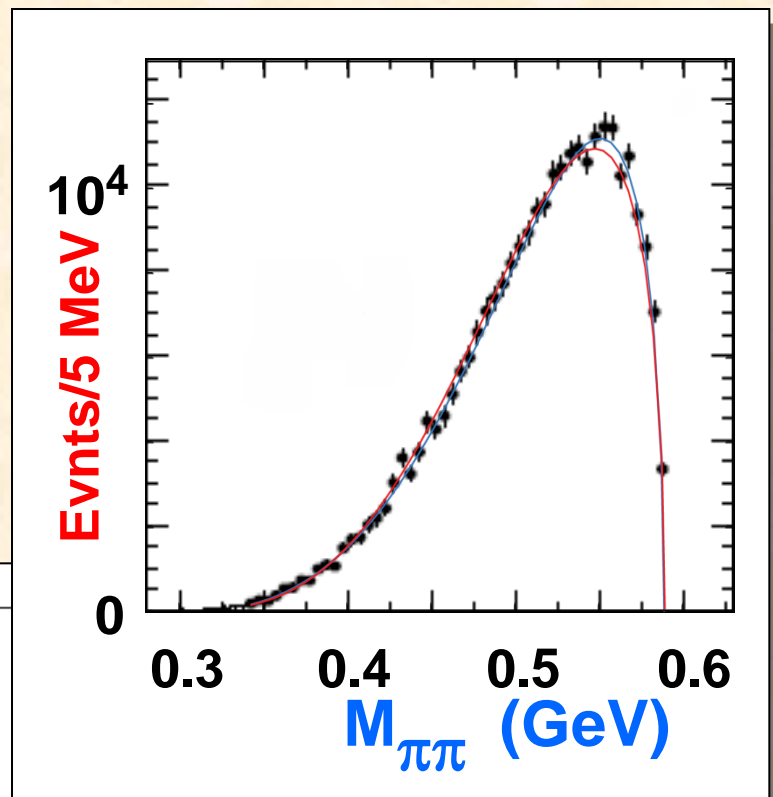
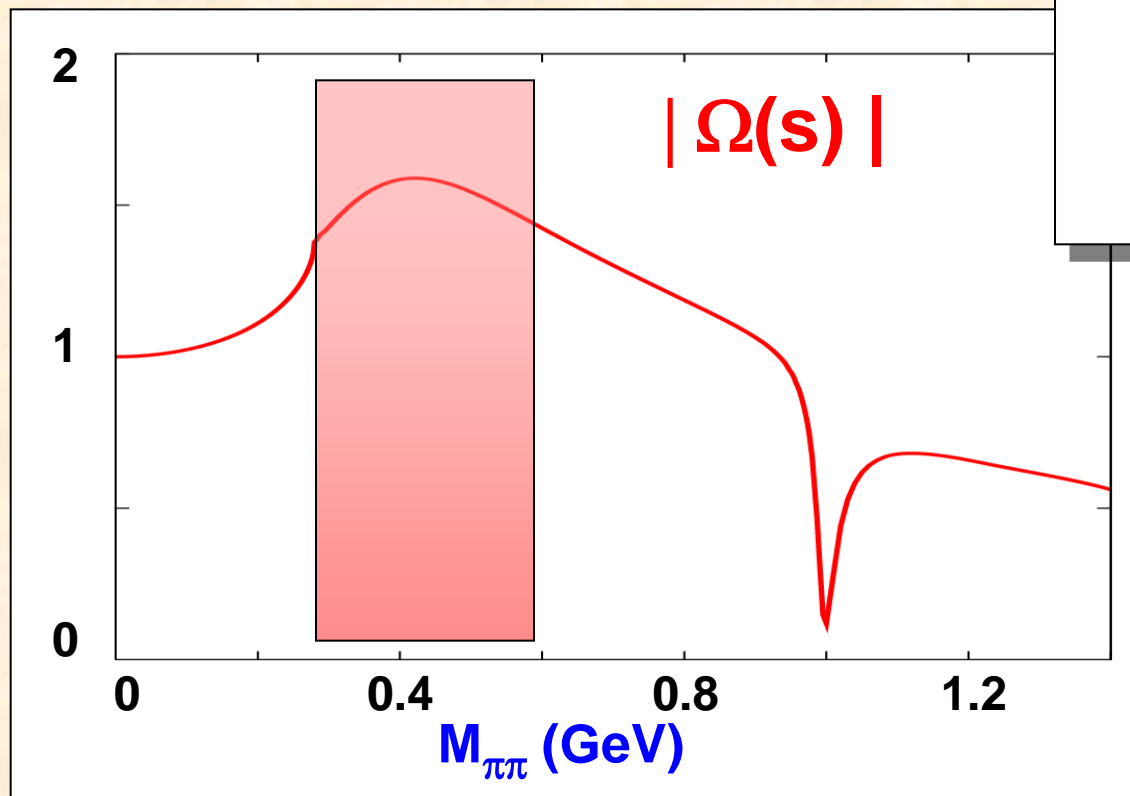
$|\Omega(s)| = 1$
no σ

$$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$$

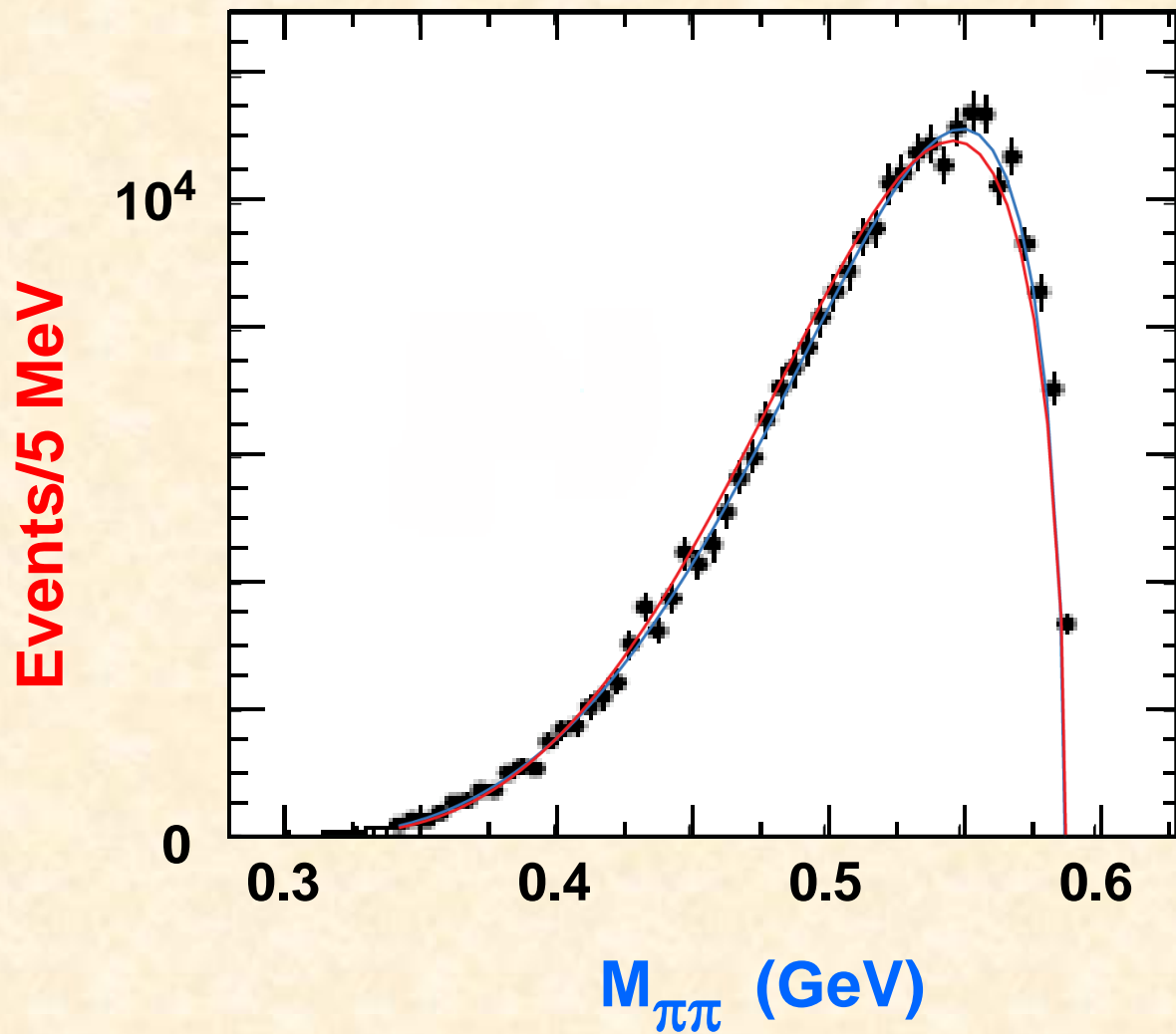


$|\Omega(s)|$
with σ

$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$



$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$



$\Psi(2S) \rightarrow \Psi(1S) \pi^+ \pi^-$

$\text{Im } s \text{ (GeV)}^2$

0
-0.1
-0.2
-0.3

$\text{Re } s \text{ (GeV)}^2$

0

0.1

0.2

0.3

0.4

0.5

CCL

pku

4
3
1

10^4
EVI
2/5 MeV

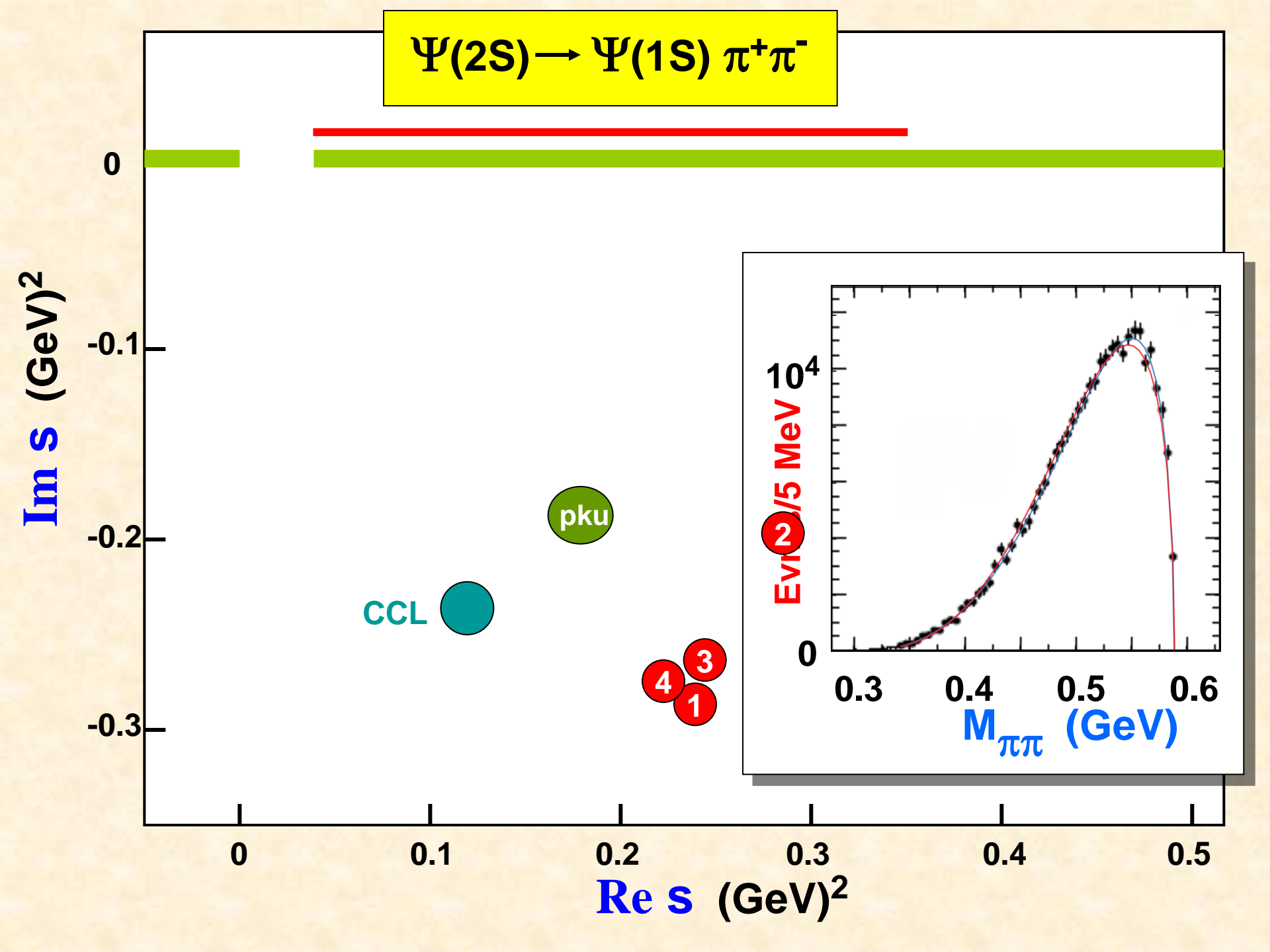
$M_{\pi\pi} \text{ (GeV)}$

0.3

0.4

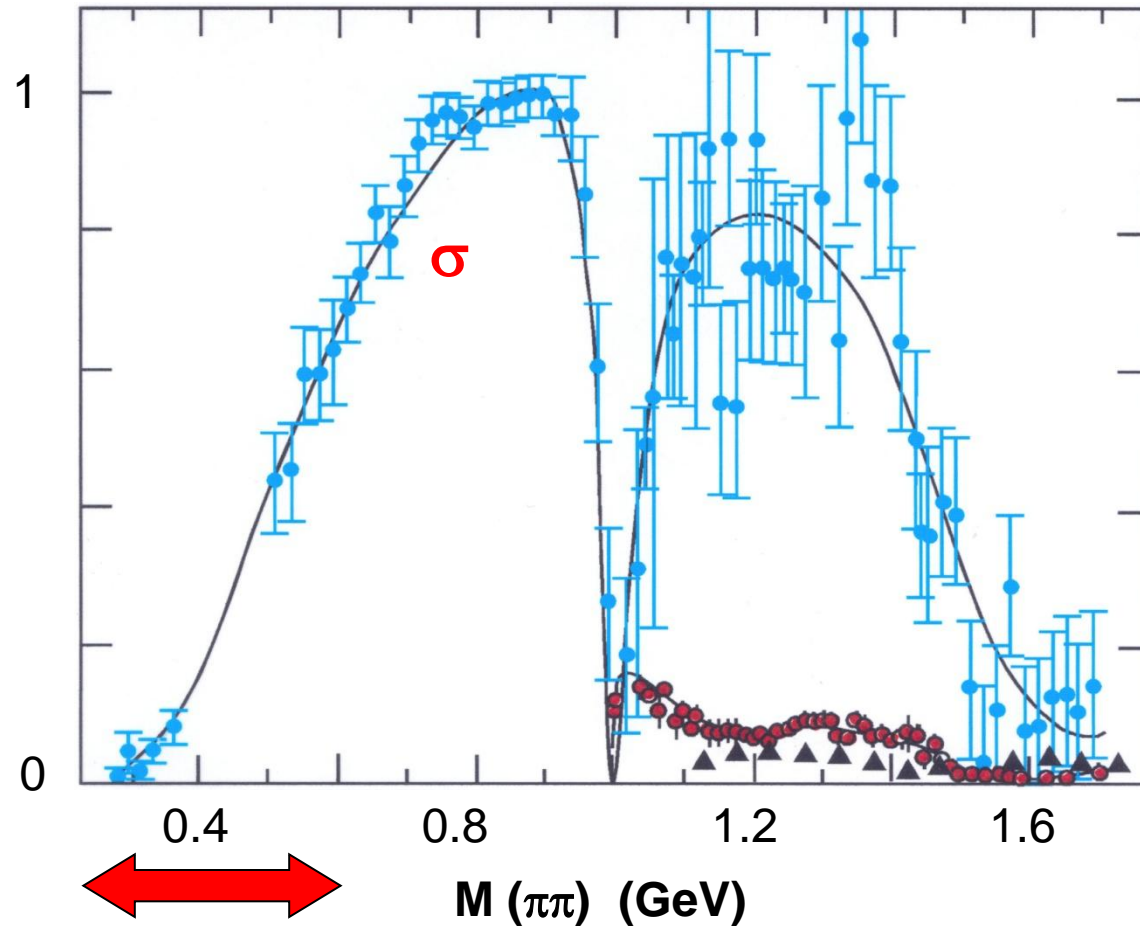
0.5

0.6



$\pi\pi \rightarrow \pi\pi$

$I = J = 0$



● $\pi\pi \rightarrow \pi\pi$

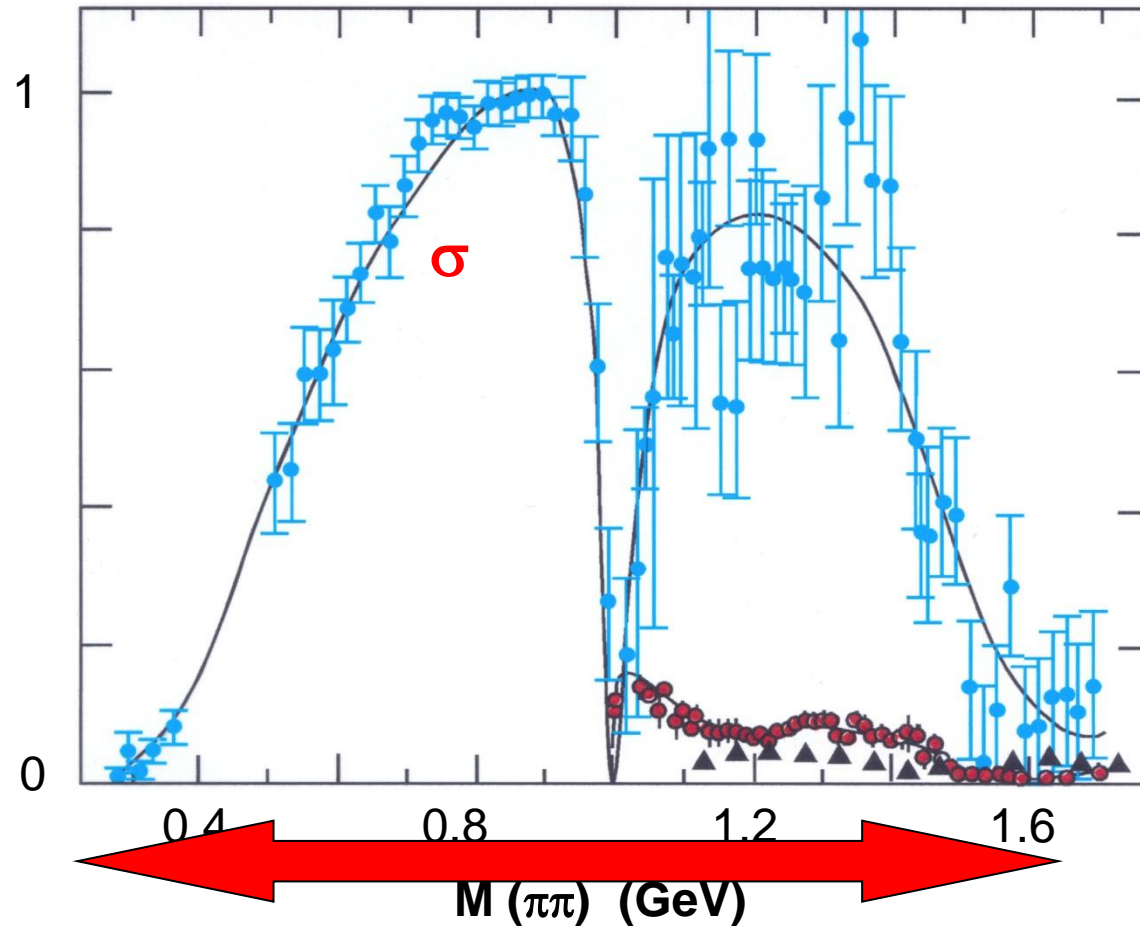
● $\pi\pi \rightarrow K\bar{K}$

▲ $\pi\pi \rightarrow \eta\eta$

BES III can add to our knowledge

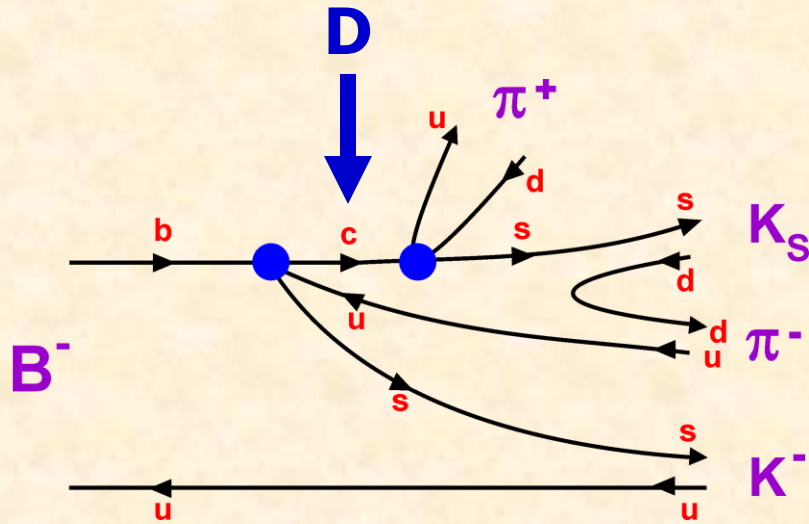
$\pi\pi \rightarrow \pi\pi$

$I = J = 0$

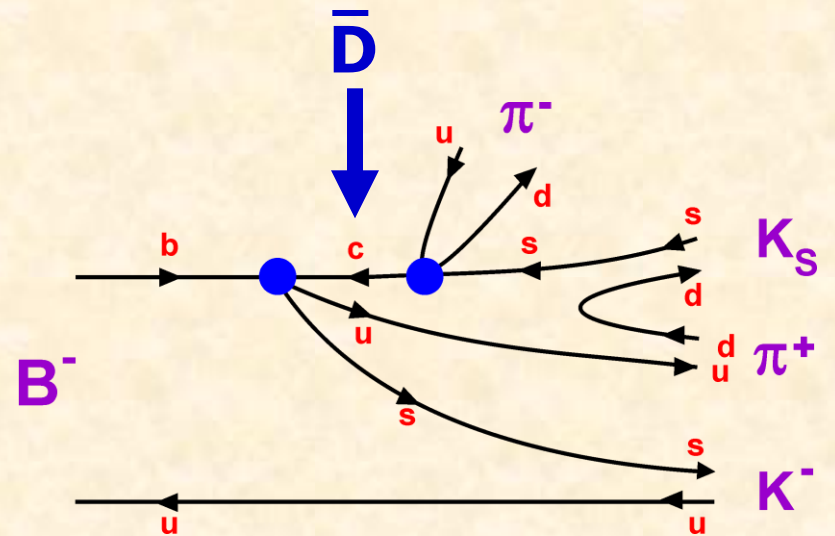


BES III can add to our knowledge

$B \rightarrow D\bar{K} \rightarrow \bar{K}K\pi\pi$



$B \rightarrow \bar{D}K \rightarrow \bar{K}K\pi\pi$



~~CP~~



PHYSICS LETTERS B

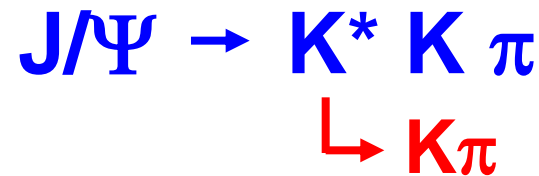
www.elsevier.com/locate/physletb

Physics Letters B 633 (2006) 681–690

Evidence for κ meson production in $J/\psi \rightarrow \bar{K}^*(892)^0 K^+ \pi^-$ process

BES Collaboration

M. Ablikim^a, J.Z. Bai^a, Y. Ban^a, J.G. Bian^a, X. Cai^a, H.F. Chen^a, H.S. Chen^a, H.X. Chen^a, J.C. Chen^a, Jin Chen^a, Y.B. Chen^a, S.P. Chi^a, Y.P. Chu^a, X.Z. Cui^a, Y.S. Dai^a, Z.Y. Deng^a, Q.F. Dong^a, S.X. Du^a, Z.Z. Du^a, J. Fang^a, S.S. Fang^a, C.D. Fu^a, C.S. Gao^a, Y.N. Gao^a, S.D. Gu^a, Y.T. Gu^a, Y.N. Guo^a, Y.Q. Guo^a, Z.J. Guo^a, Z.J. Guo^a, F.A. Harris^a, K.L. He^a, M. He^a, Y.K. Heng^a, H.M. Hu^a, T. Hu^a, G.S. Huang^a, X.P. Huang^a, X.T. Huang^a, X.T. Huang^a, S. Ishida^a, X.B. Ji^a, X.S. Jiang^a, J.B. Jiao^a, D.P. Jin^a, S. Jin^a, Y. Jin^a, T. Komada^a, S. Kurokawa^a, Y.F. Lai^a, G. Li^a, H.B. Li^a, H.H. Li^a, J. Li^a, R.Y. Li^a, S.M. Li^a, F. Liu^a, Fang Liu^a, H.H. Liu^a, H.J. Liu^a, J.G. Lu^a, J.B. Liu^a, Y.F. Liang^a, H.B. Liao^a, C.X. Liu^a, F. Lu^a, G.R. Lu^a, G.R. Lu^a, H.J. Lu^a, J.G. Lu^a, J.G. Lu^a, C.L. Luo^a, F.C. Ma^a, J.P. Liu^a, R.G. Liu^a, Z.A. Liu^a, F. Lu^a, G.R. Lu^a, H.M. Liu^a, H.M. Liu^a, J. Liu^a, J. Liu^a, J.B. Liu^a, H.L. Ma^a, L.L. Ma^a, Q.M. Ma^a, X.B. Ma^a, Z.P. Mao^a, T. Matsuoka^a, X.H. Mo^a, J. Nie^a, H.P. Peng^a, N.D. Qi^a, H. Qin^a, J.F. Qiu^a, Z.Y. Ren^a, G. Rong^a, L. Shang^a, D.L. Shen^a, X.Y. Shen^a, H.Y. Sheng^a, F. Shi^a, X. Shi^a, H.S. Sun^a, J.F. Sun^a, K. Takamatsu^a, Z.Q. Tan^a, X. Tang^a, Y.R. Tian^a, G.L. Tong^a, L. Wang^a, L.S. Wang^a, M. Wang^a, P. Wang^a, P. Wang^a, P.L. Wang^a, W. Z.Y. Wang^a, Zhe Wang^a, Zheng Wang^a, C.L. Wei^a, D.H. Wei^a, B. Xin^a, G.F. Xu^a, Y. Xu^a, K. Yamada^a, I. Yamauchi^a, J. Yang^a, Y.X. Yang^a, M.H. Ye^a, Y.K. Ye^a, Z.Y. Yi^a, G.W. Y. Zeng^a, Yu Zeng^a, B.X. Zhang^a, B.Y. Zhang^a, C.C. J.Y. Zhang^a, X.Y. Zhang^a, Y.Y. Zhang^a, Z.X. Zhang^a, Z.P. Zhang^a, D.X. Zhao^a, J.W. Zhao^a, M.G. Zhao^a, Z.Q. Zheng^a, J.P. Zheng^a, Z.P. Zheng^a, L. Zhou^a, N. H.Q. Zheng^a, Y.S. Zhu^a, Yingchun Zhu^a, Z.A. Zhu^a



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A study of charged κ in $J/\psi \rightarrow K^\pm K_S \pi^\mp \pi^0$

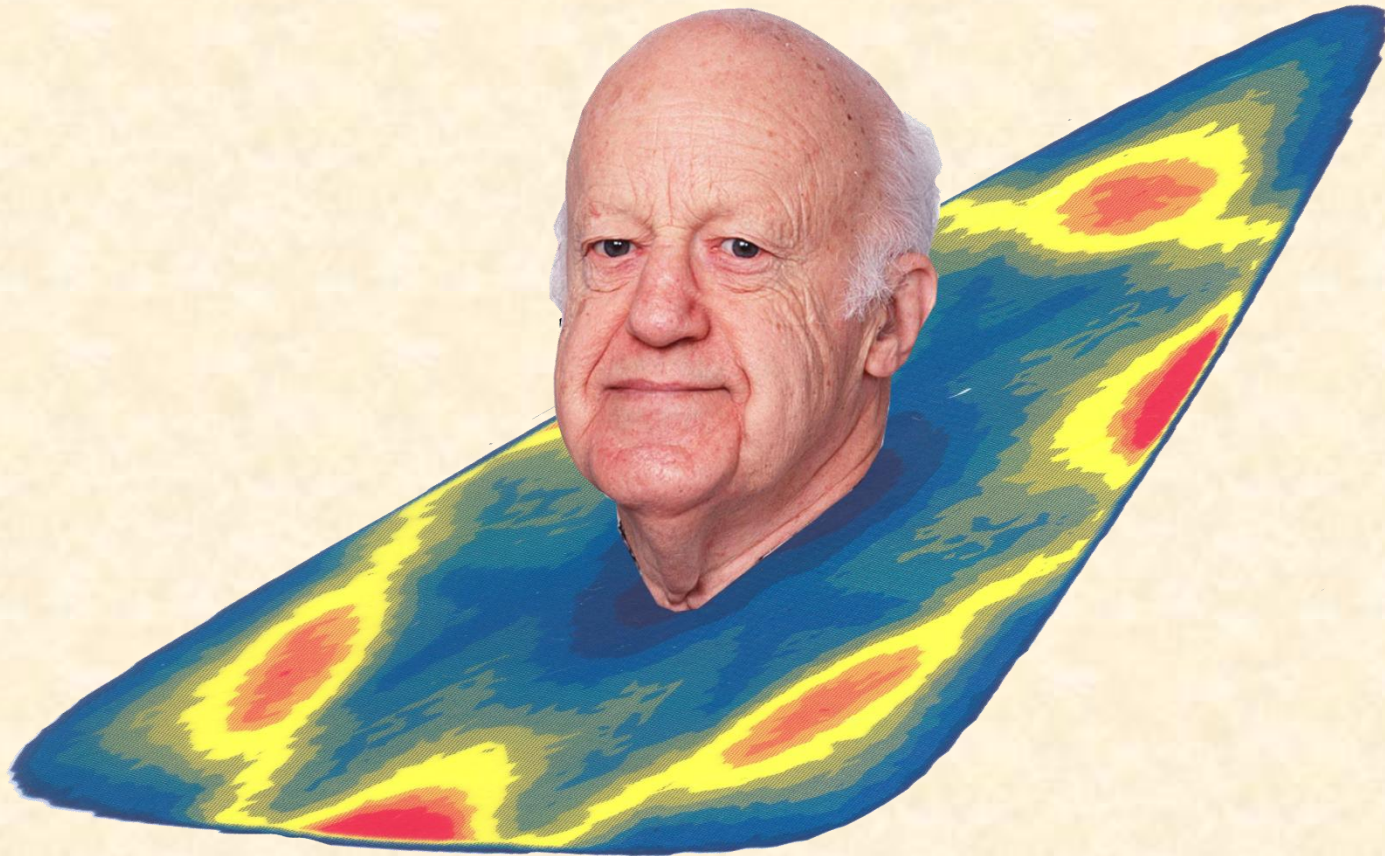
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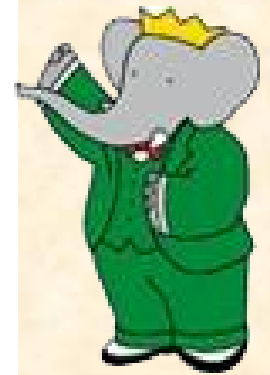
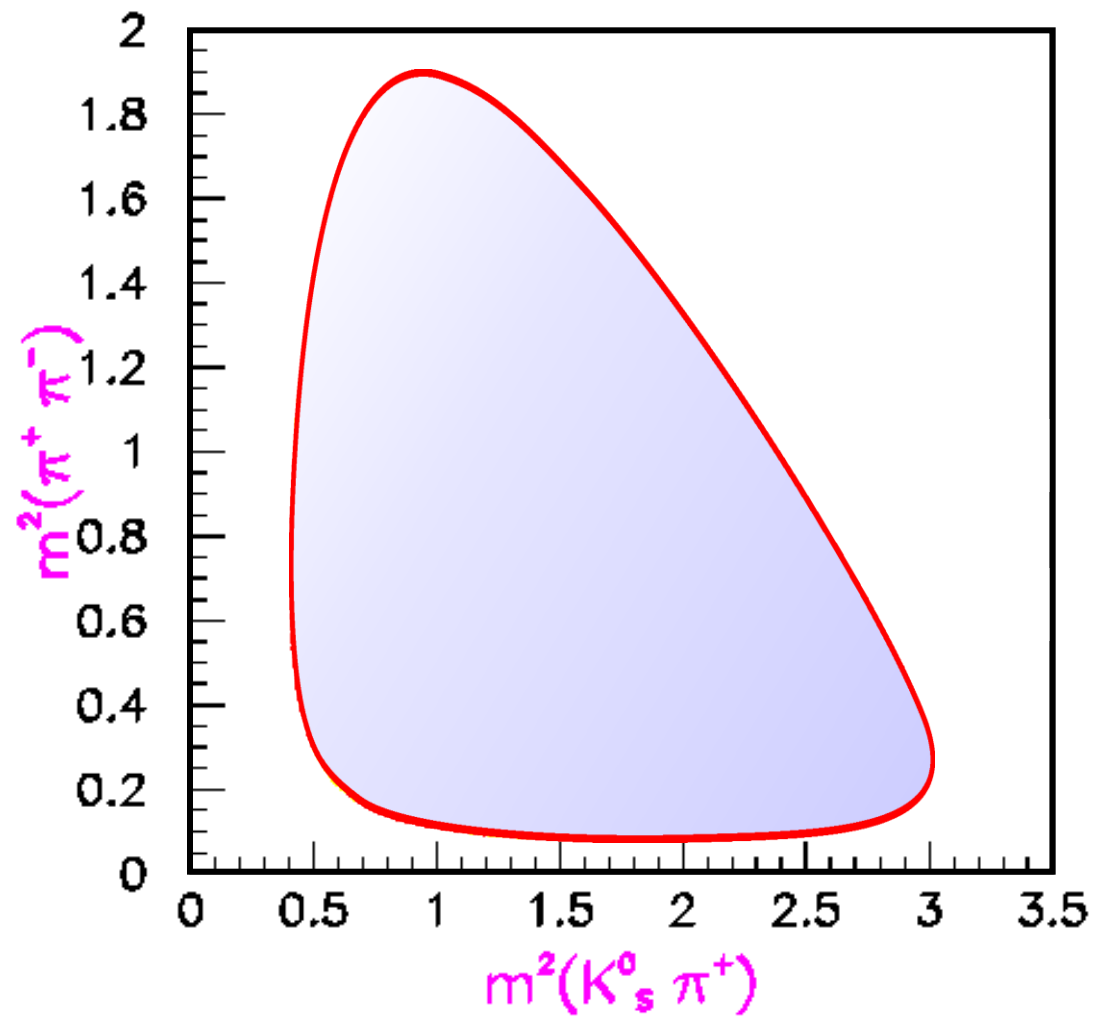




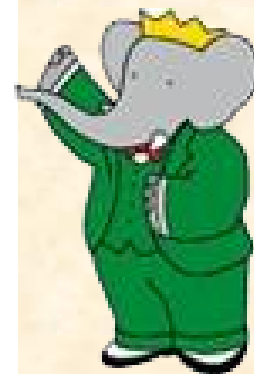
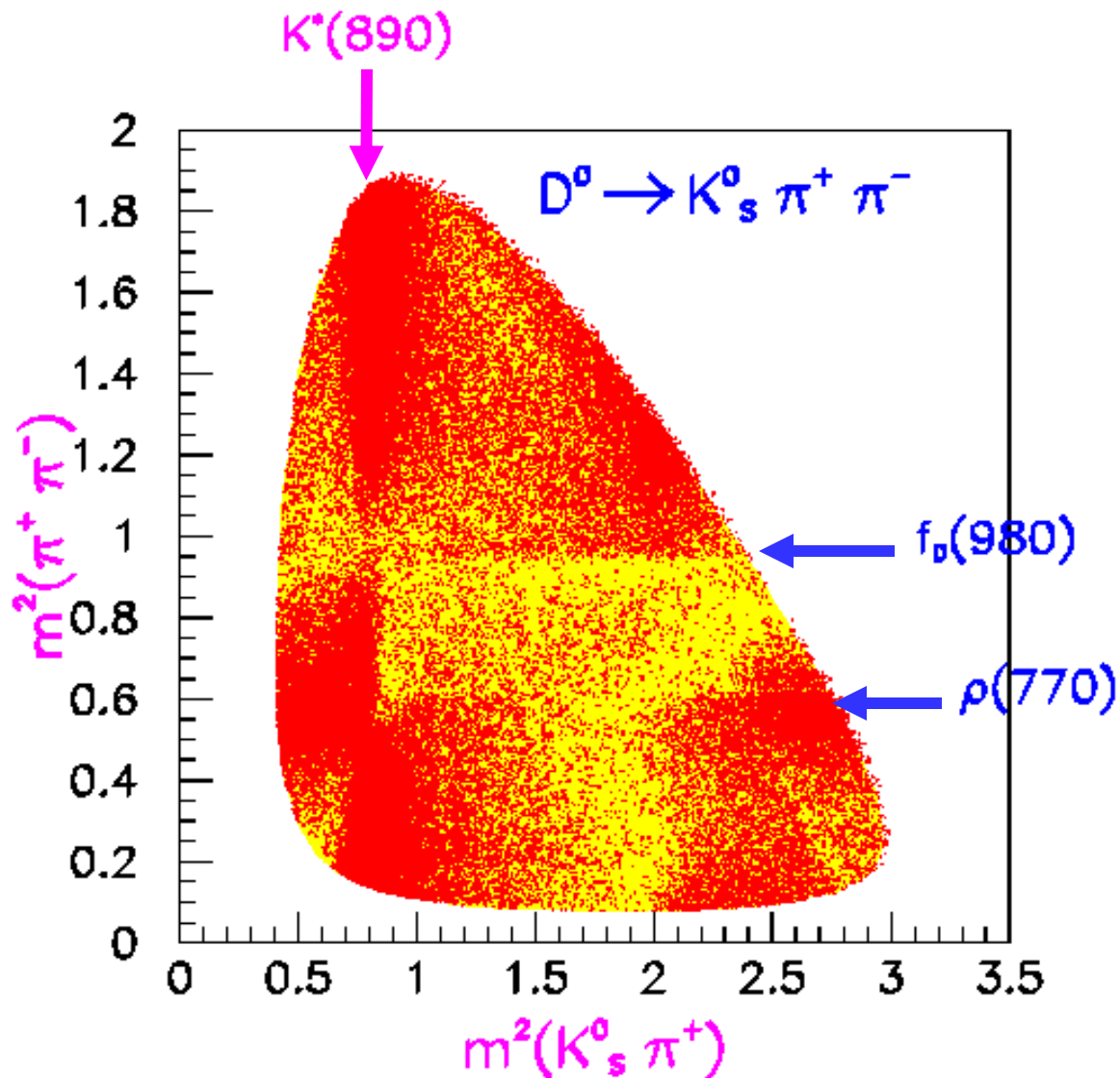
Dalitz Analysis



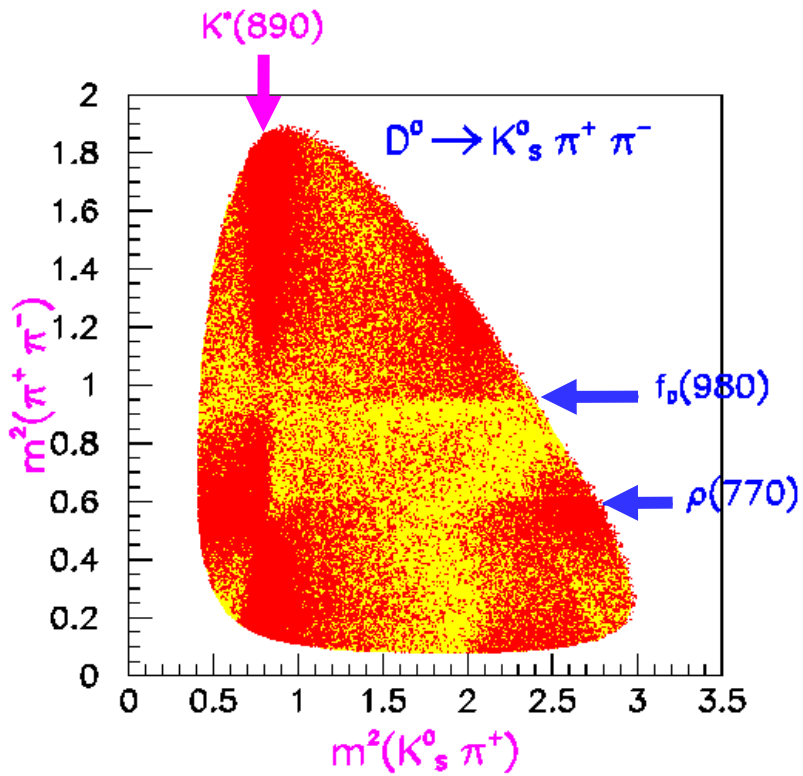
Dalitz plot of $D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$.



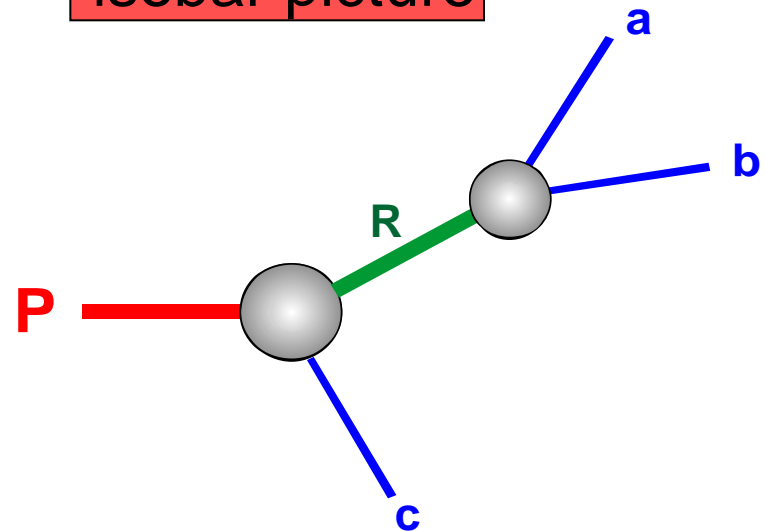
Dalitz plot of $D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$.



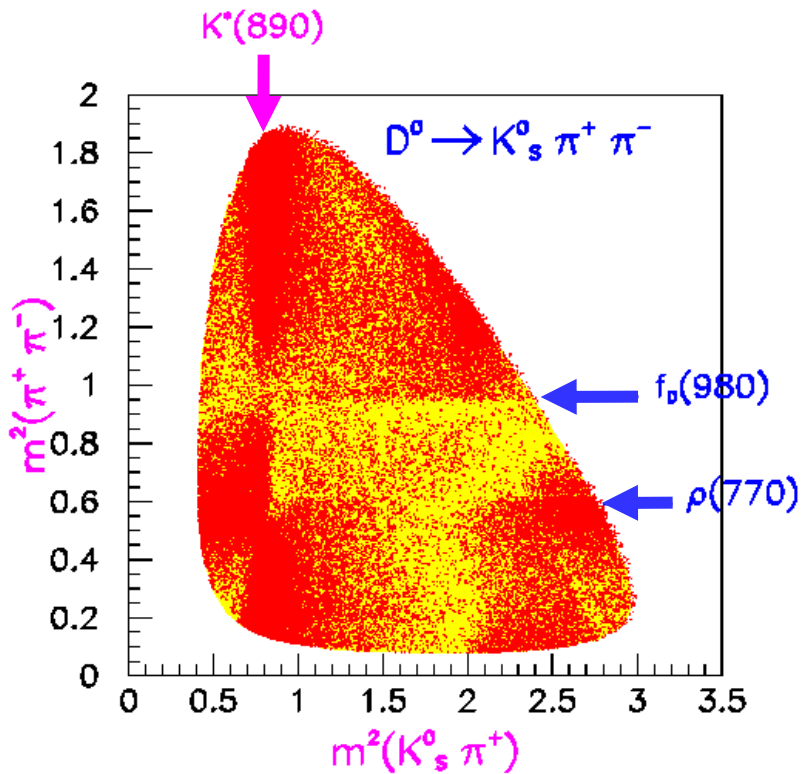
Dalitz plot of $D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$.



isobar picture



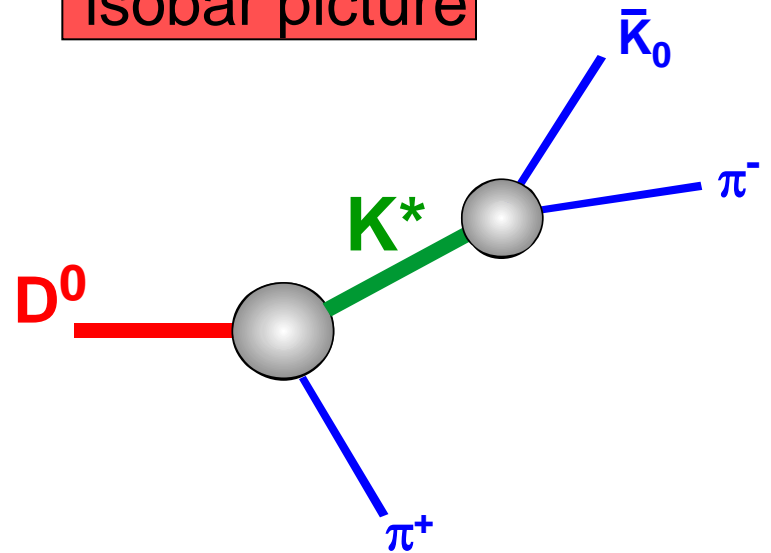
Dalitz plot of $D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$.



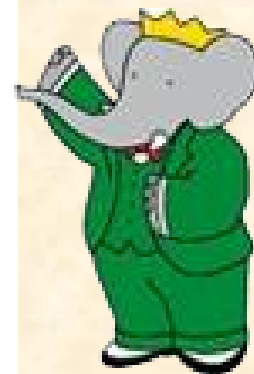
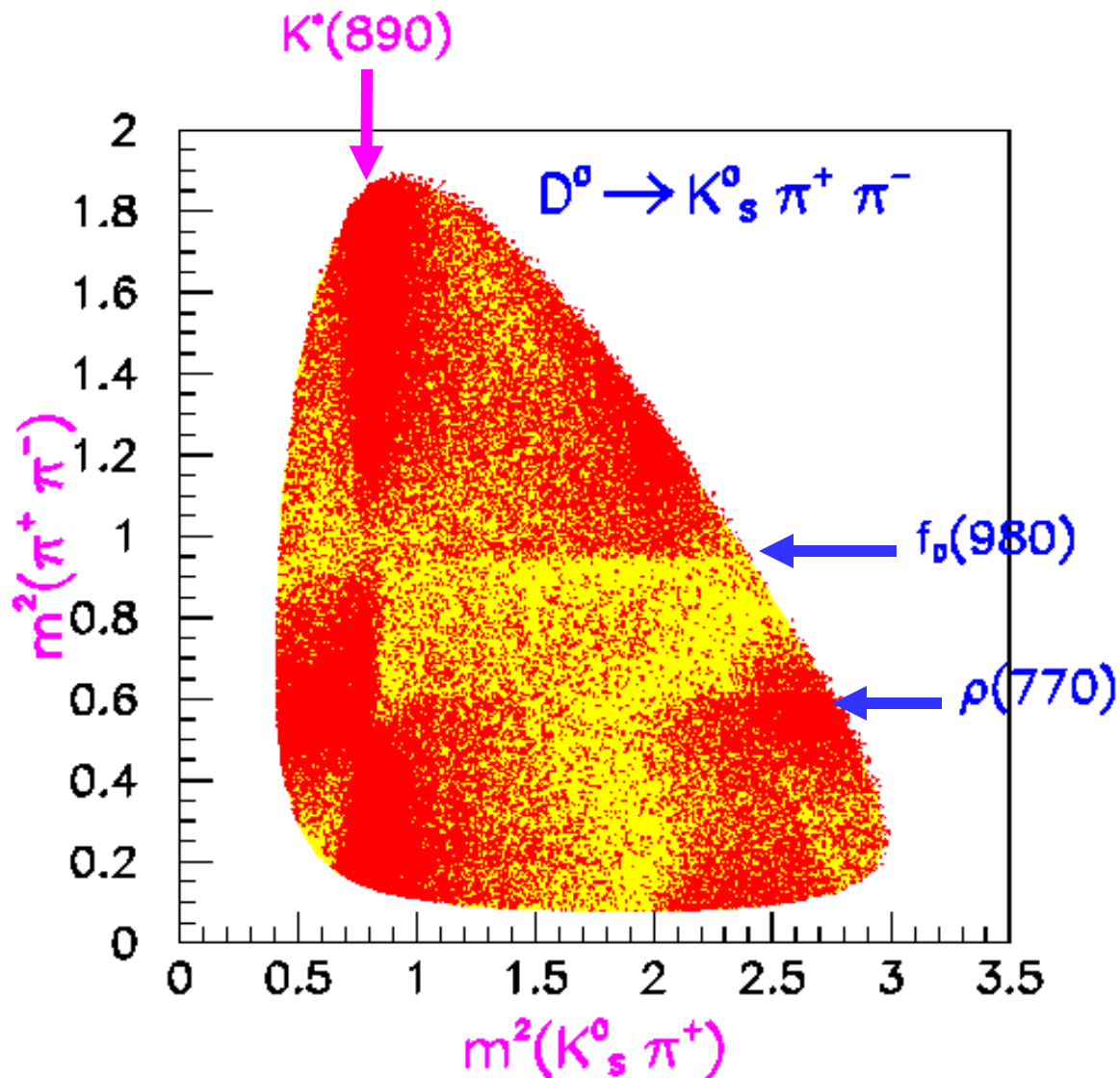
Universality
of final state interactions

beyond

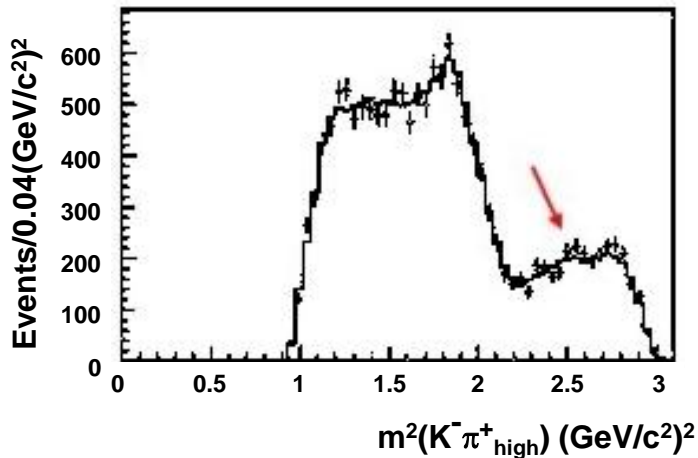
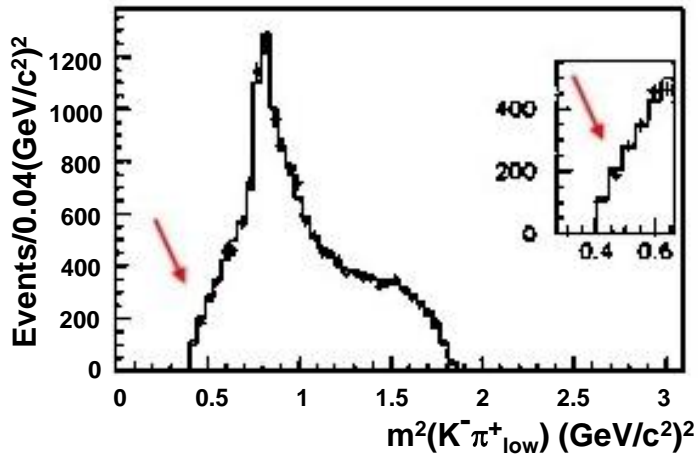
isobar picture



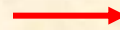
Dalitz plot of $D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$.



E791 $D^+ \rightarrow K^- \pi^+ \pi^+$



D^+



non-resonant	$13.0 \pm 5.8 \pm 2.6\%$	$349 \pm 14 \pm 8^\circ$
$\kappa(E791)\pi^+$	$47.8 \pm 12.1 \pm 3.7\%$	$187 \pm 8 \pm 17^\circ$
$K^*(890)\pi^+$	$12.3 \pm 1.0 \pm 0.9\%$	0° (fixed)
$K_0^*(1430)\pi^+$	$12.5 \pm 1.4 \pm 0.4\%$	$48 \pm 7 \pm 10^\circ$
$K_2^*(1430)\pi^+$	$0.5 \pm 0.1 \pm 0.2\%$	$306 \pm 8 \pm 6^\circ$
$K_1^*(1680)\pi^+$	$2.5 \pm 0.7 \pm 0.2\%$	$28 \pm 13 \pm 15^\circ$

$\sim 89\%$

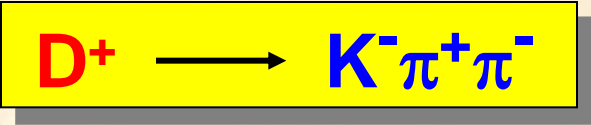
$\chi^2/\text{d.o.f} = 0.73$
(95%)

Probability

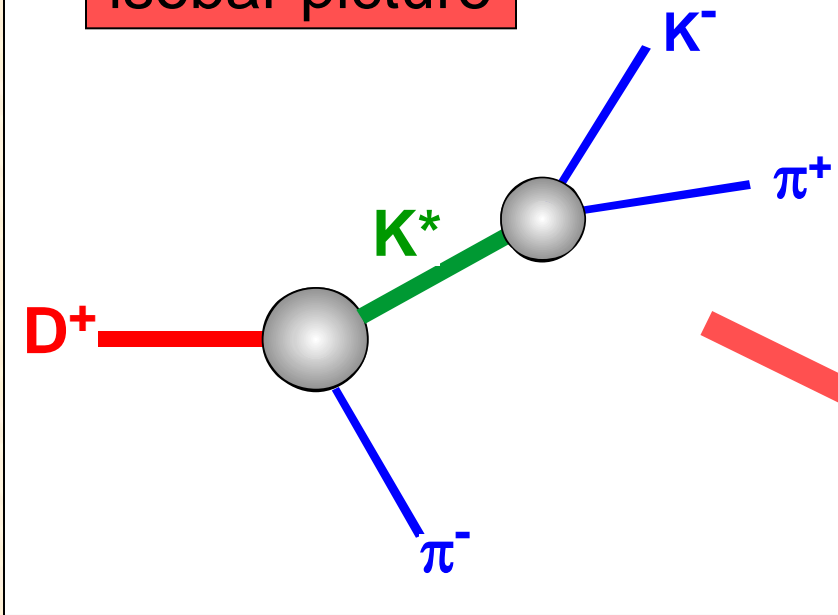
κ

$$M_\kappa = 797 \pm 19 \pm 42 \text{ MeV}$$

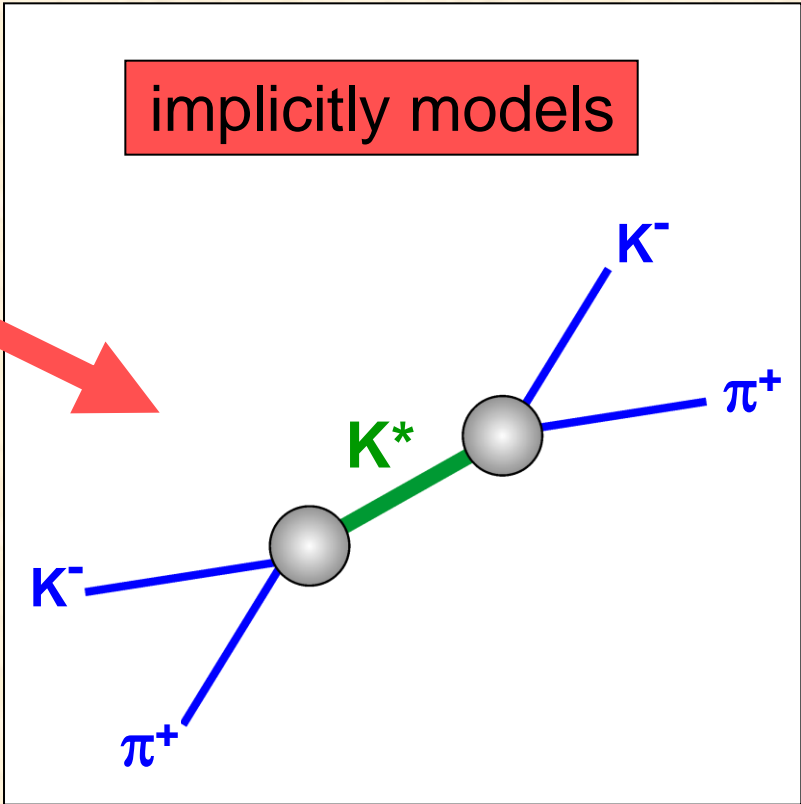
$$\Gamma_\kappa = 410 \pm 43 \pm 85 \text{ MeV}$$



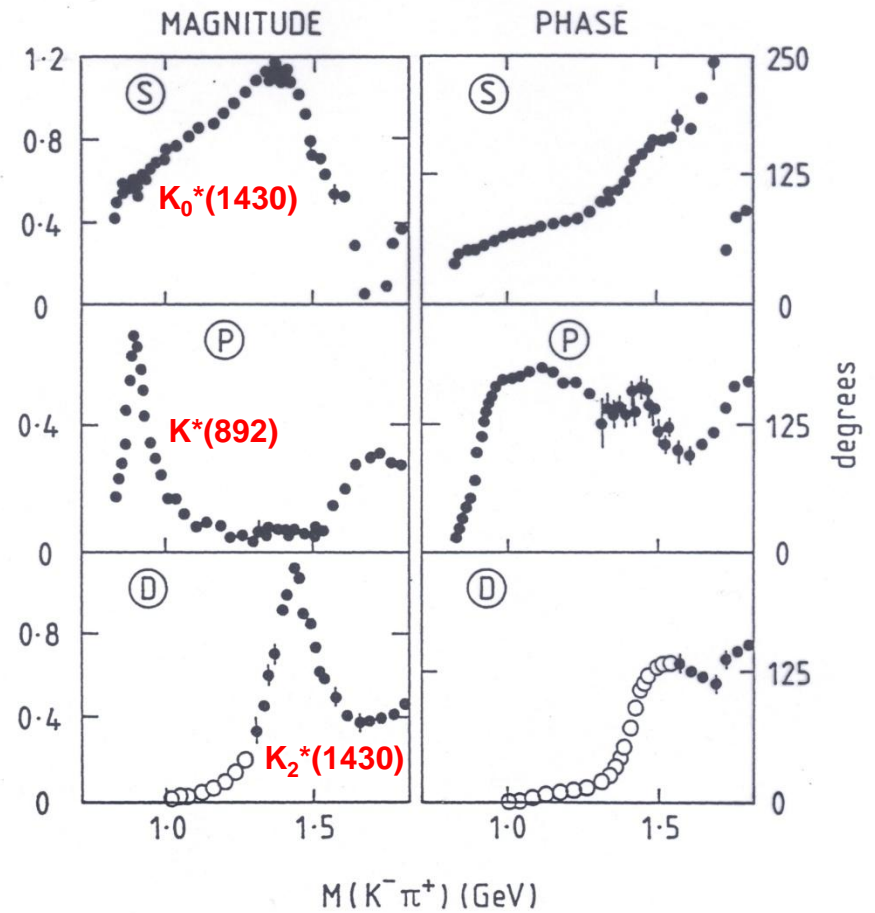
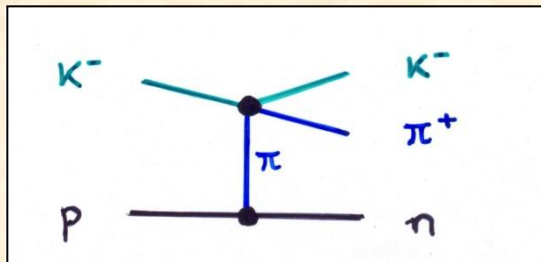
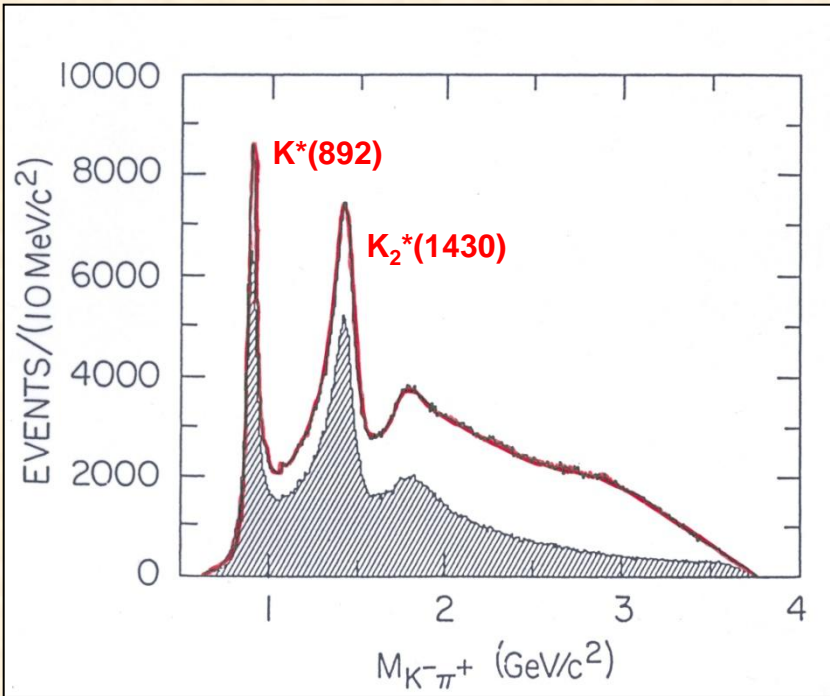
isobar picture



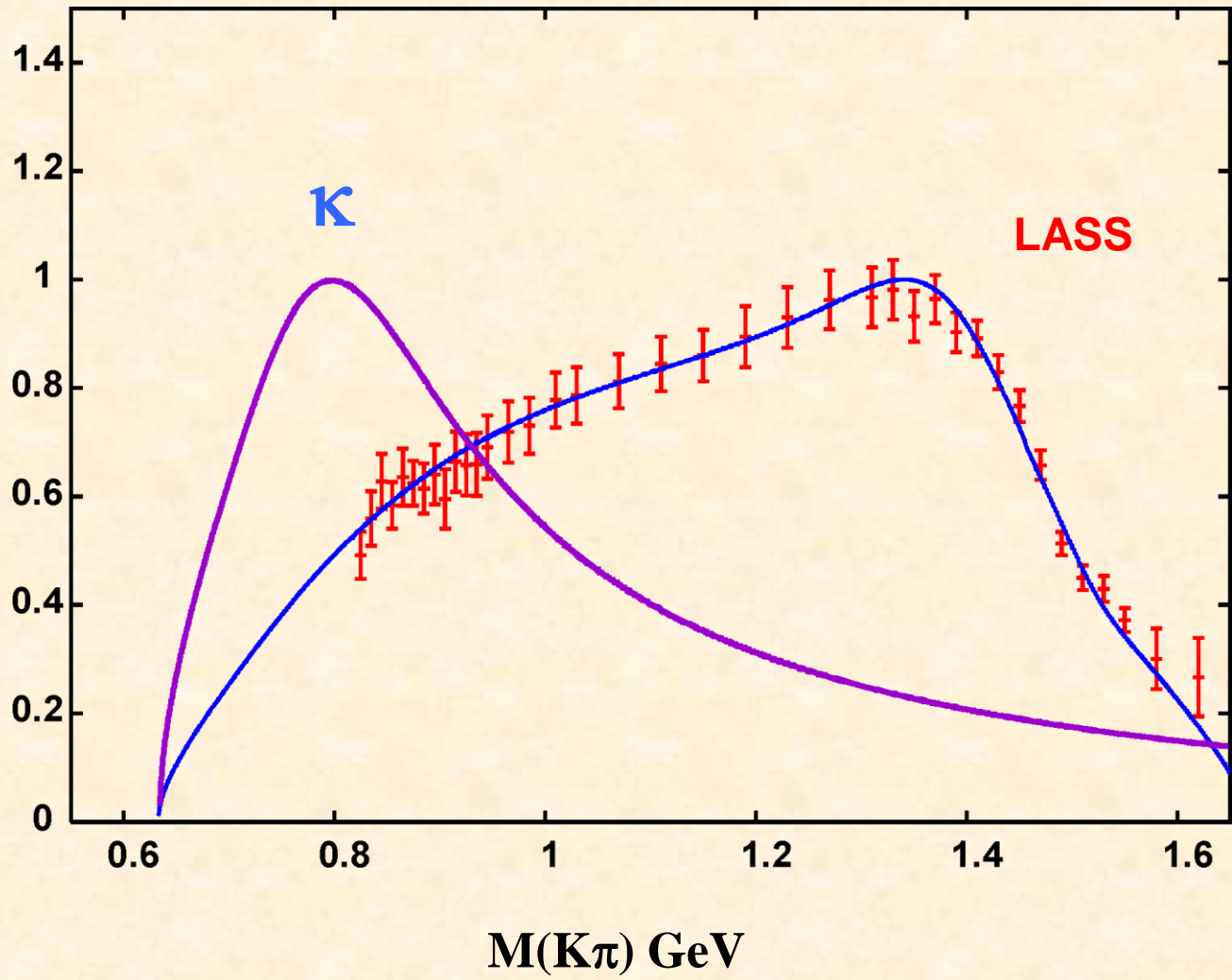
implicitly models



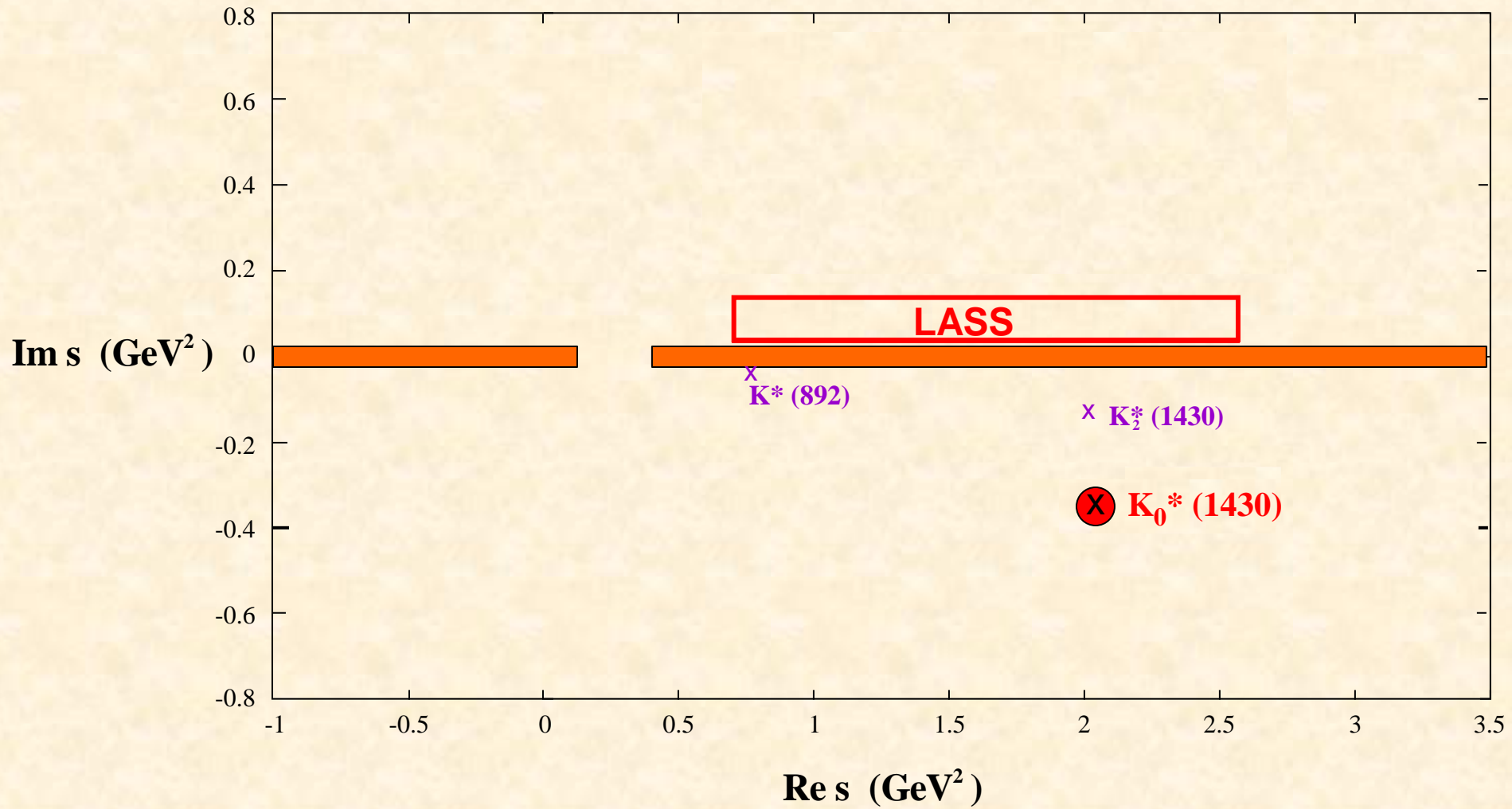
LASS: $K^- p \rightarrow K^- \pi^+ n$



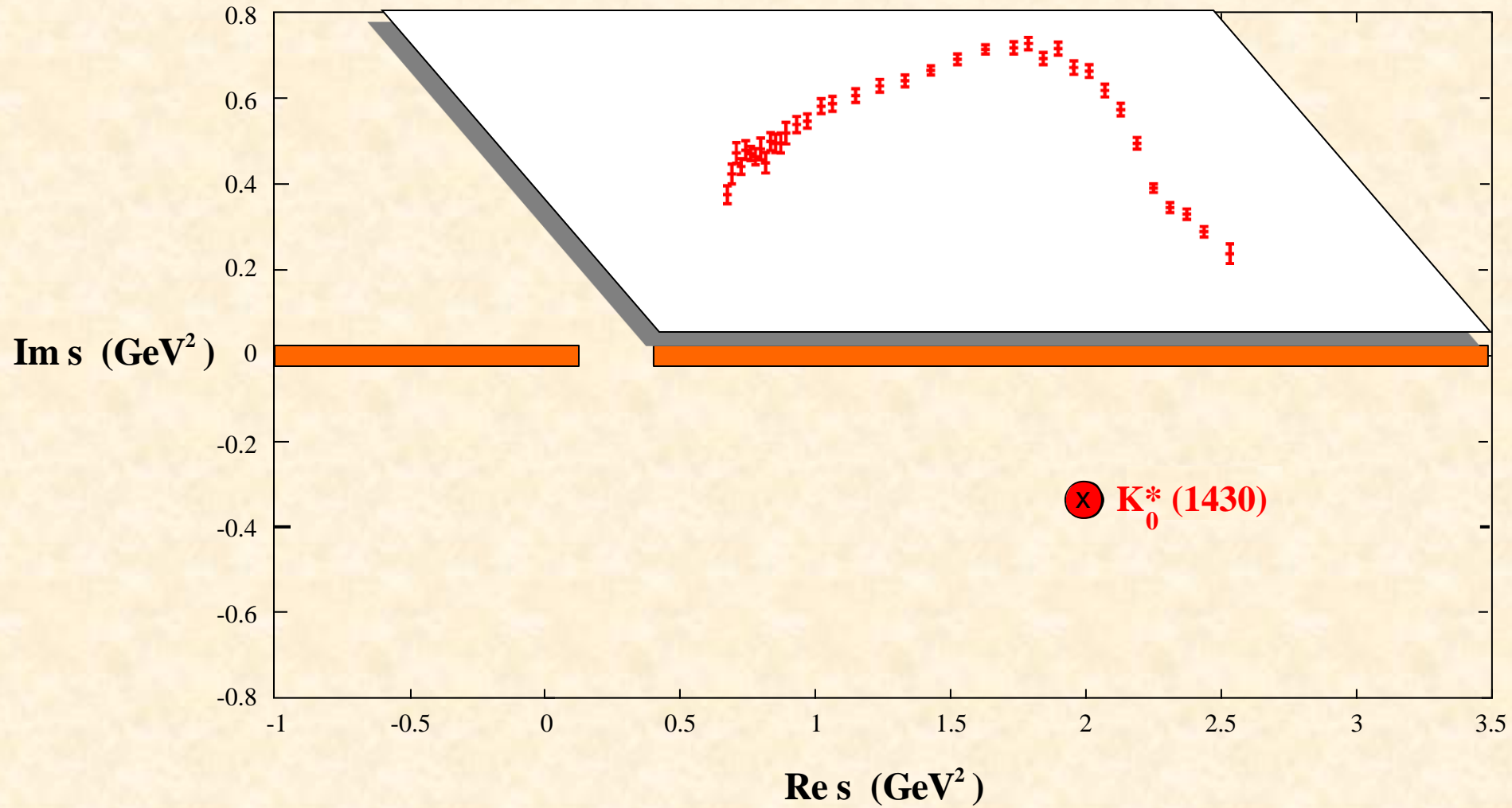
$I=1/2, J=0 : \quad K\pi \rightarrow K\pi$



$\pi K : I = 1/2, J = 0$

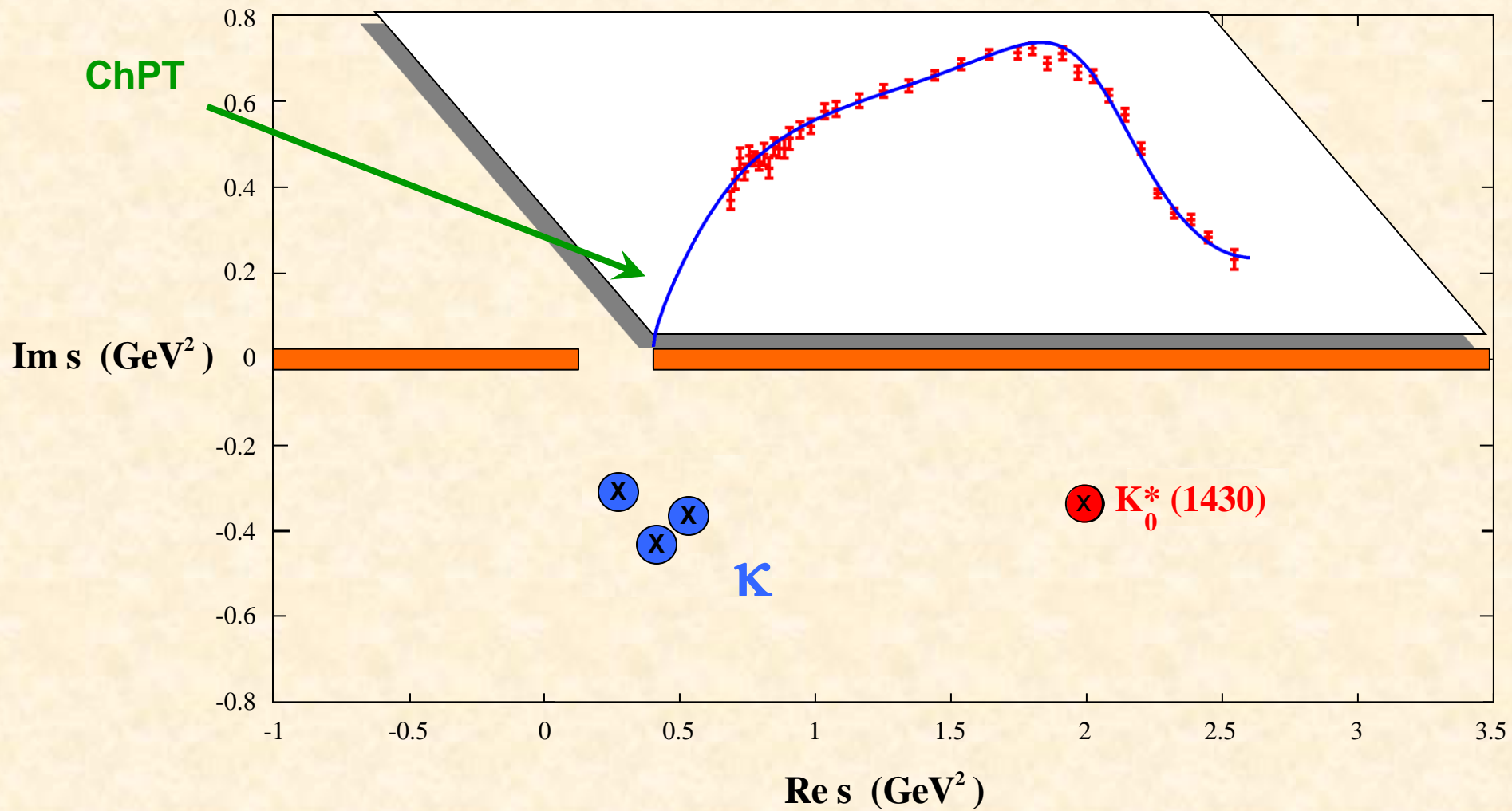


$\pi K : I = 1/2, J = 0$



$\pi K : I = 1/2, J = 0$

ChPT

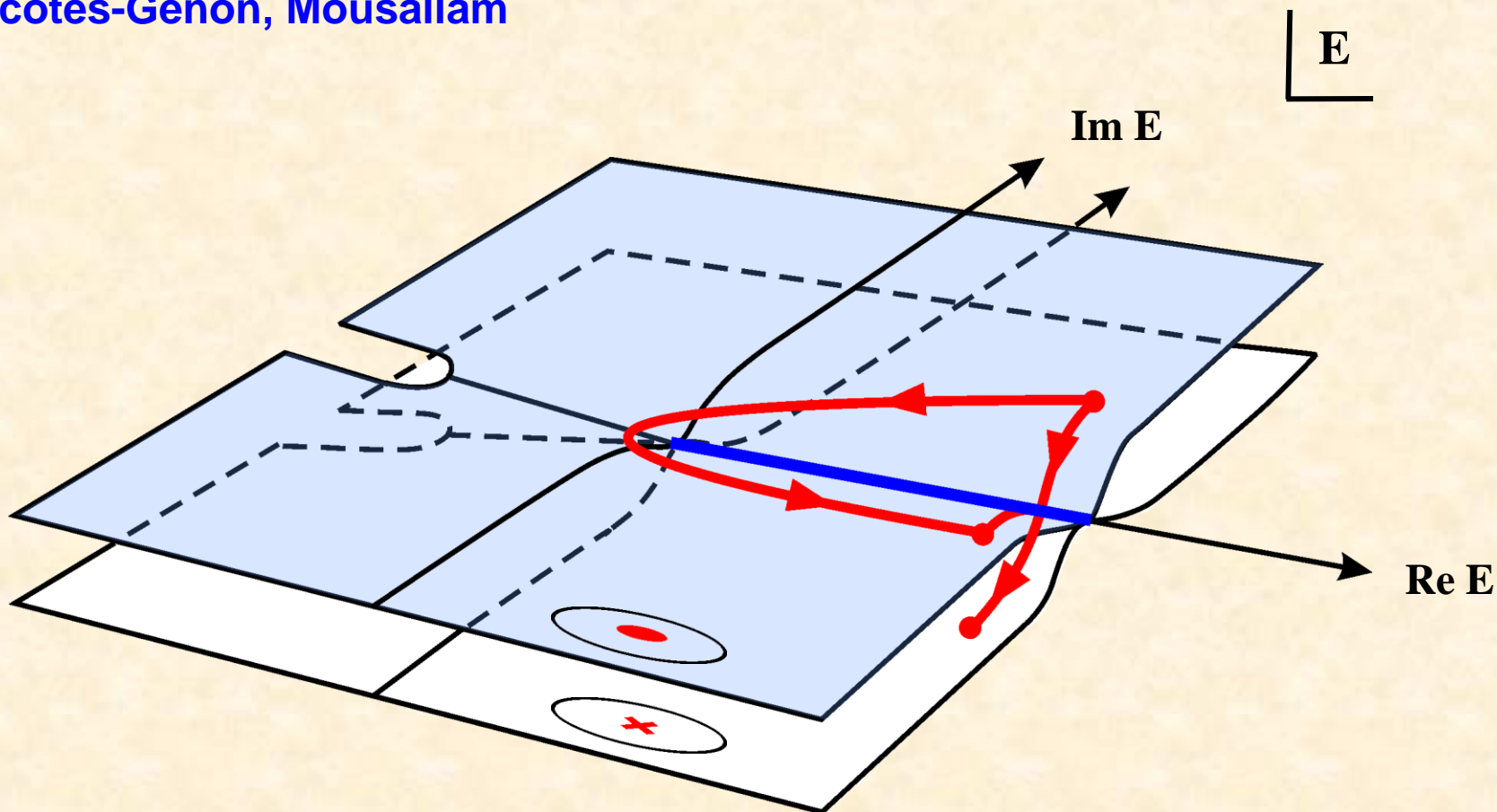


$K\pi$ scattering into the complex plane

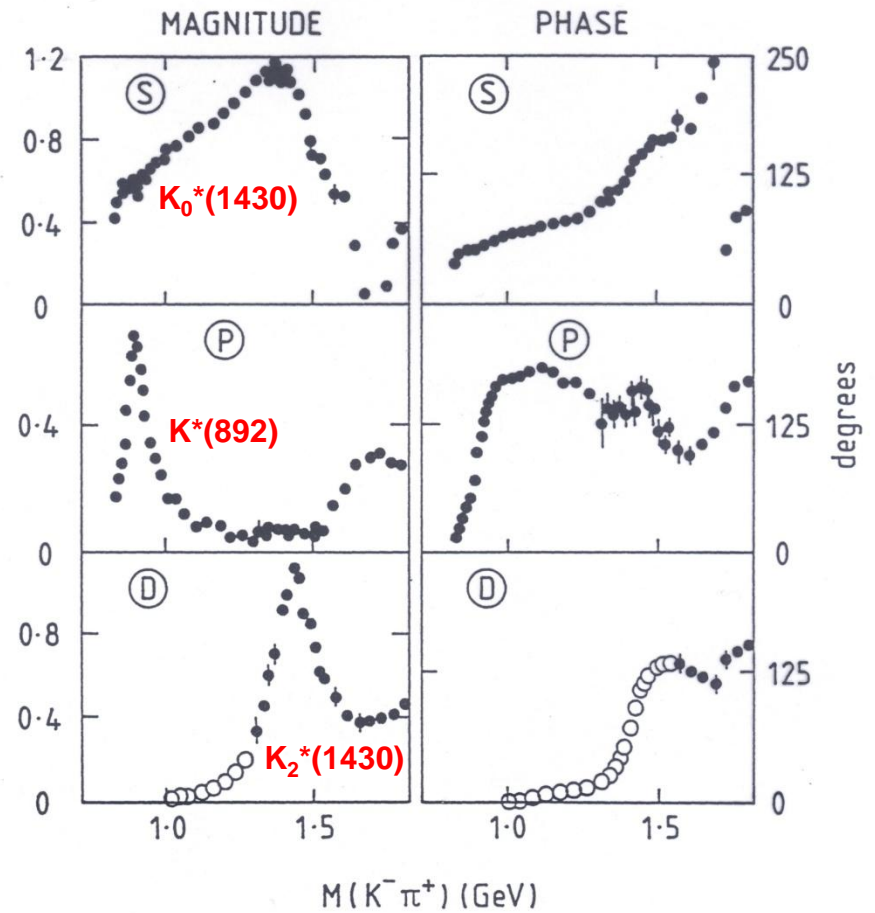
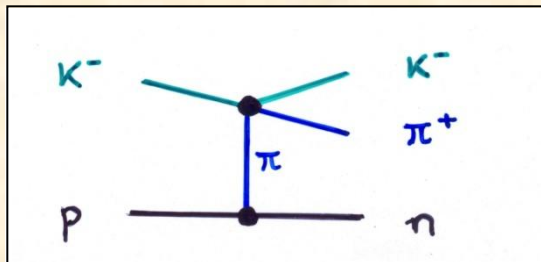
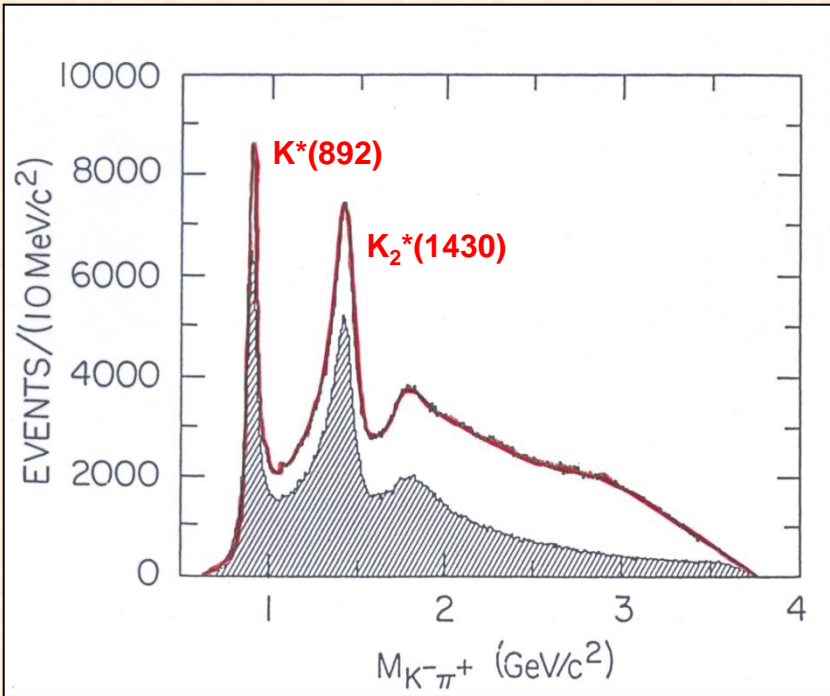


$$E_R = 658 - i 289 \text{ MeV}$$

Descotes-Genon, Mousallam



LASS: $K^- p \rightarrow K^- \pi^+ n$



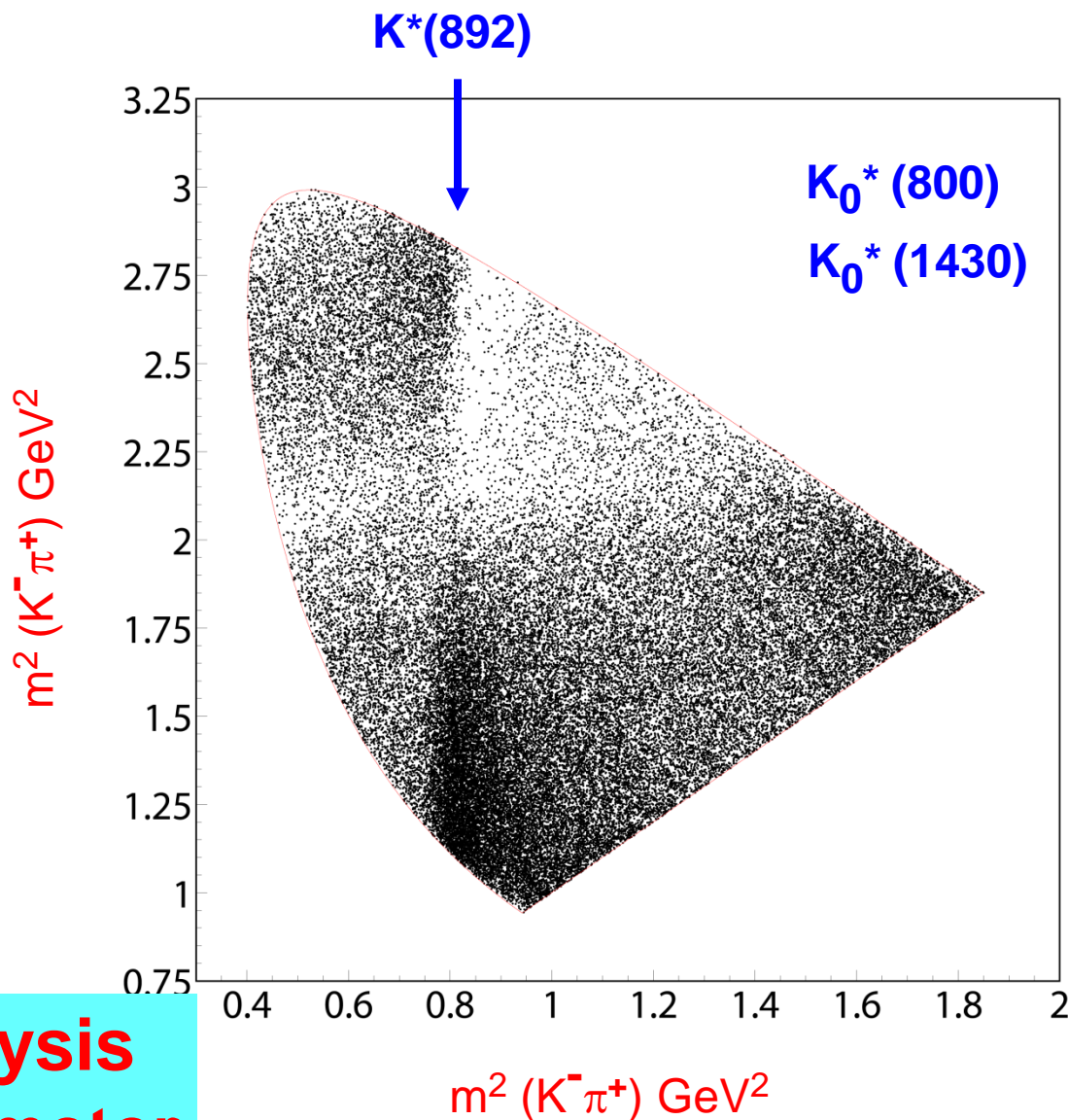
Dalitz plot: $D^+ \rightarrow K^- \pi^+ \pi^+$



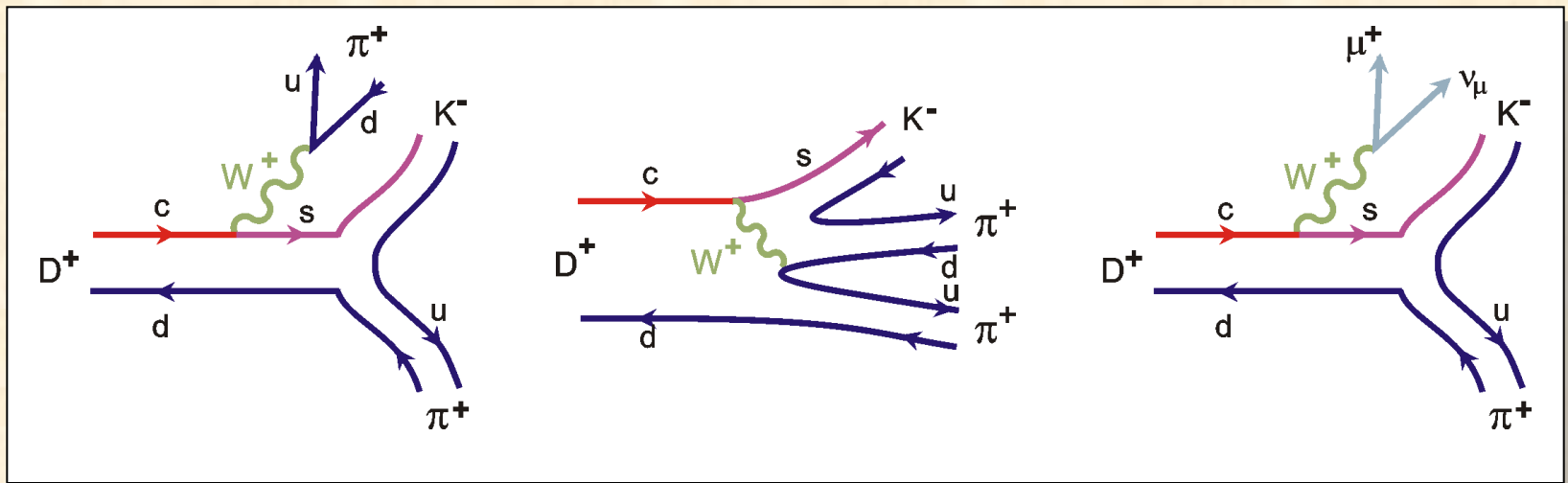
Malvezzi, P

53.6k events

Dalitz plot analysis
as an Interferometer



Dalitz plot: $D^+ \rightarrow K^- \pi^+ \pi^+$

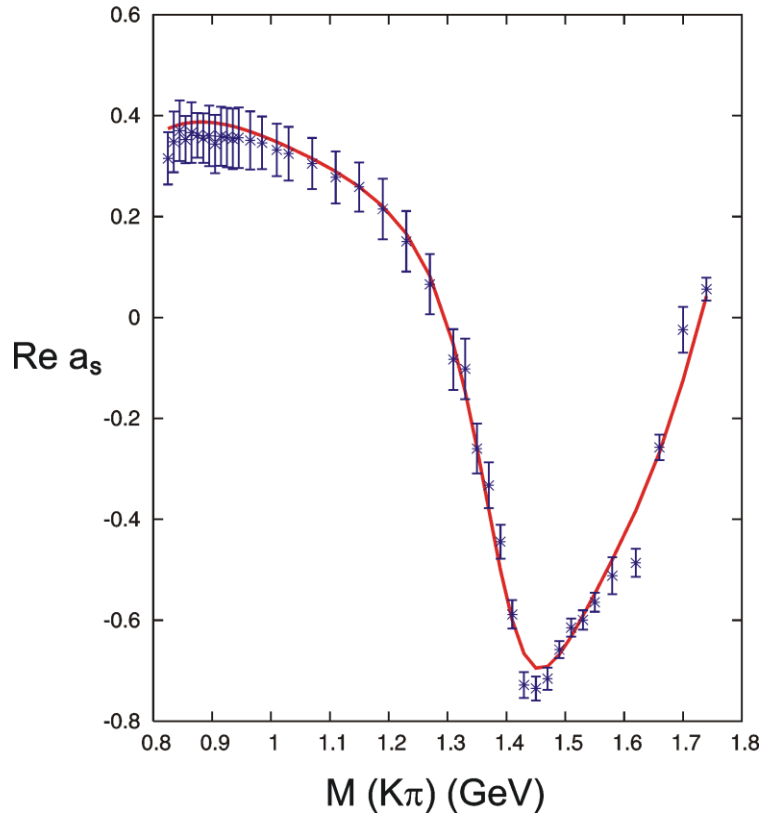


$I = 1/2, 3/2$

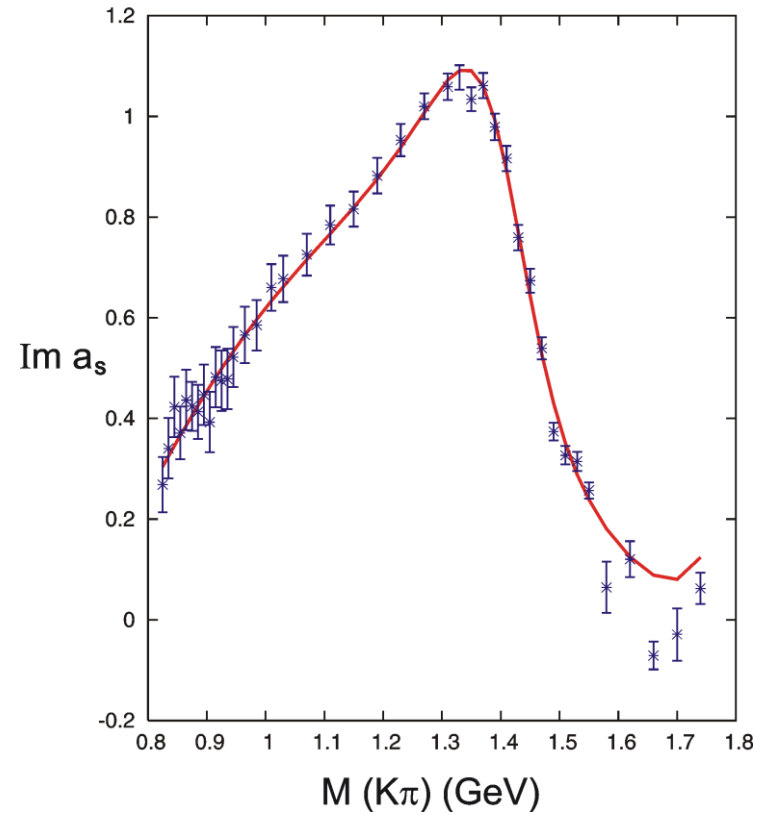
SLAC: $K^- \pi^+ \rightarrow K^- \pi^+$, $K^+ \pi^+ \rightarrow K^+ \pi^+$

SLAC: $K^- \pi^+ \longrightarrow K^- \pi^+$, $K^+ \pi^+ \longrightarrow K^+ \pi^+$

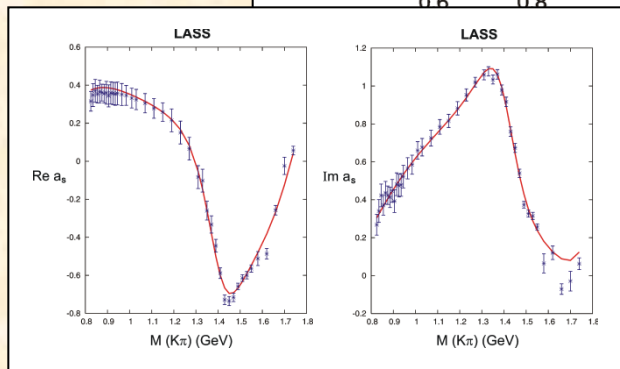
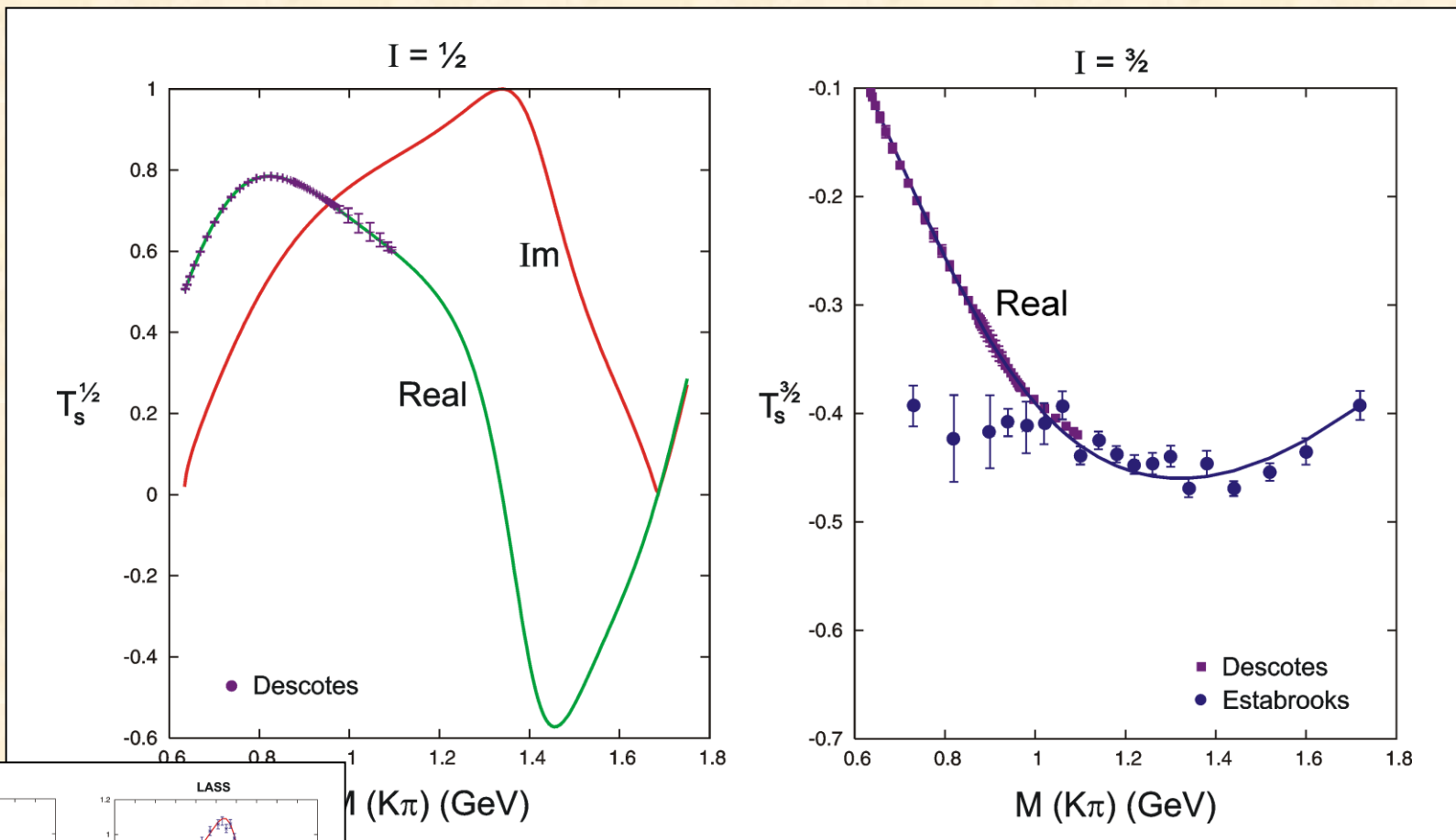
LASS



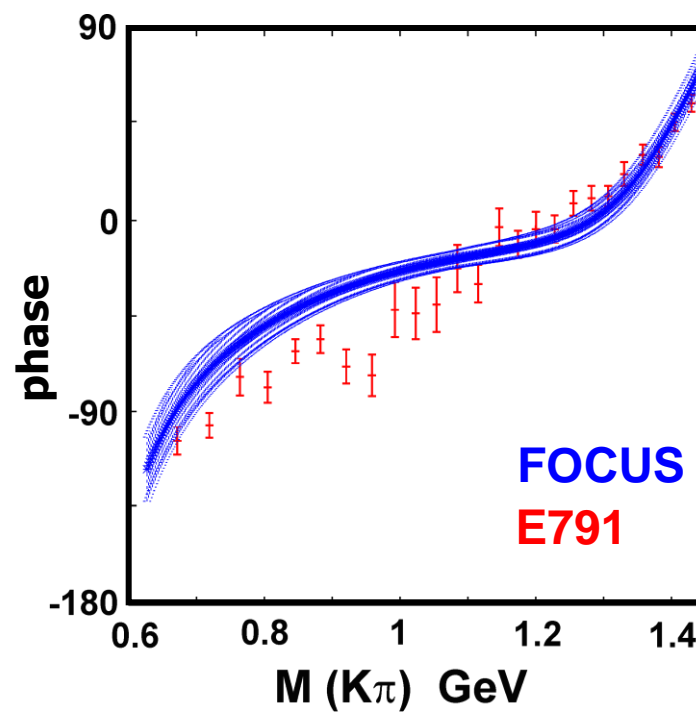
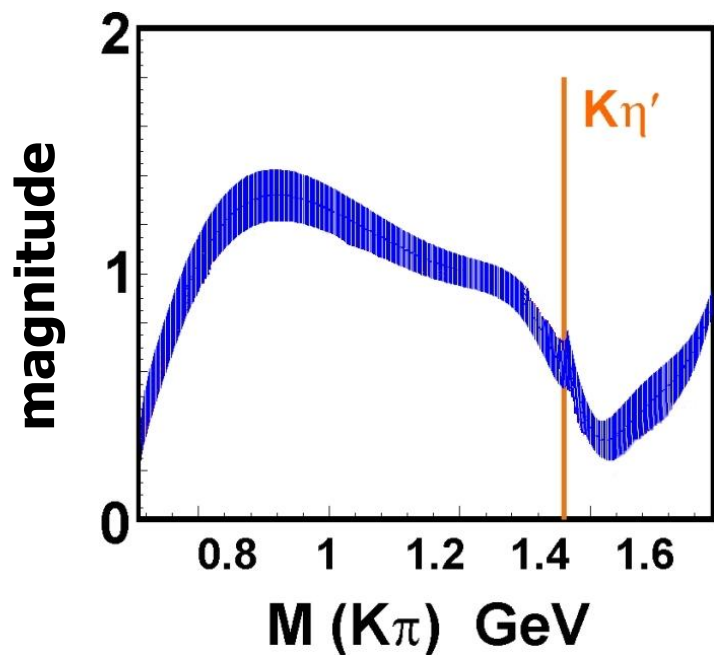
LASS



SLAC: $K^- \pi^+ \rightarrow K^- \pi^+$, $K^+ \pi^+ \rightarrow K^+ \pi^+$



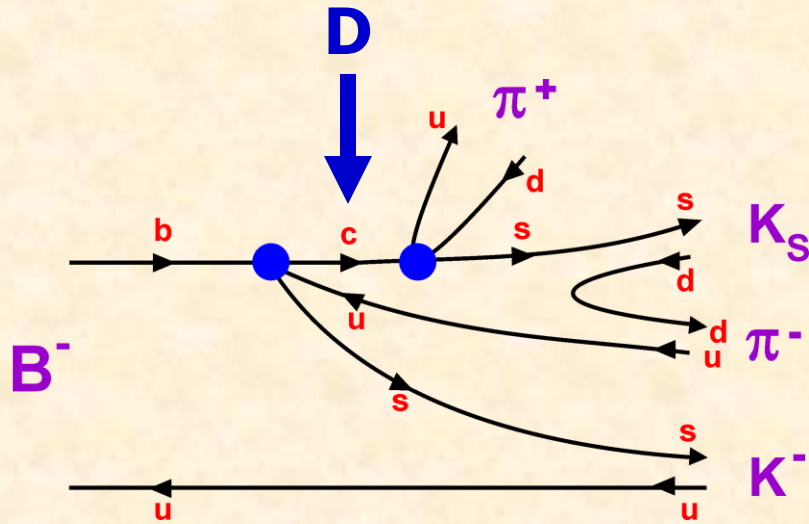
Dalitz plot: $D^+ \rightarrow K^- \pi^+ \pi^+$



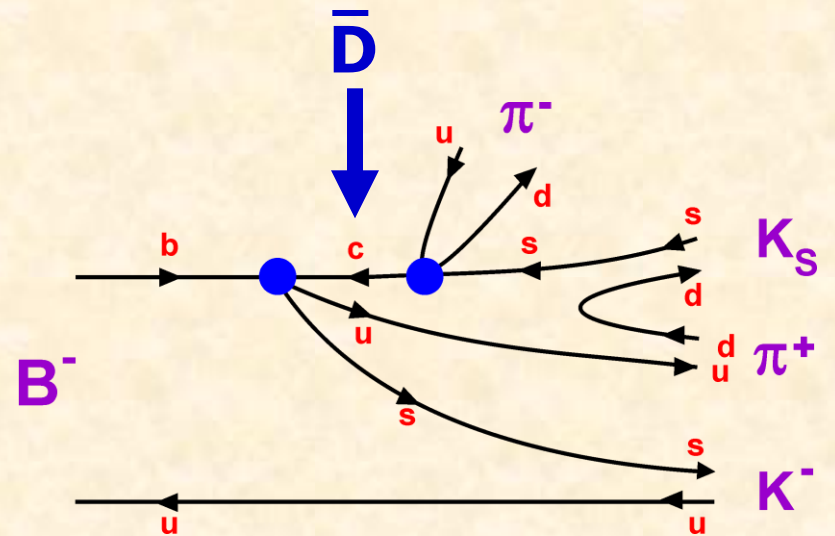
Malvezzi, P
& FOCUS

(Bugg)

$B \rightarrow D\bar{K} \rightarrow \bar{K}K\pi\pi$



$B \rightarrow \bar{D}K \rightarrow \bar{K}K\pi\pi$



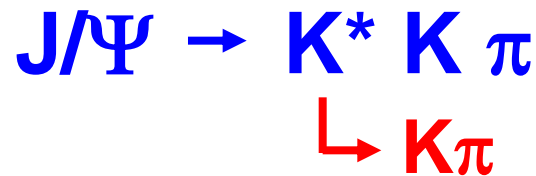
~~CP~~



Evidence for κ meson production in $J/\psi \rightarrow \bar{K}^*(892)^0 K^+ \pi^-$ process

BES Collaboration

M. Ablikim^a, J.Z. Bai^a, Y. Ban^a, J.G. Bian^a, X. Cai^a, H.F. Chen^a, H.S. Chen^a, H.X. Chen^a, J.C. Chen^a, Jin Chen^a, Y.B. Chen^a, S.P. Chi^a, Y.P. Chu^a, X.Z. Cui^a, Y.S. Dai^a, Z.Y. Deng^a, Q.F. Dong^a, S.X. Du^a, Z.Z. Du^a, J. Fang^a, S.S. Fang^a, C.D. Fu^a, C.S. Gao^a, Y.N. Gao^a, S.D. Gu^a, Y.T. Gu^a, Y.N. Guo^a, Y.Q. Guo^a, Z.J. Guo^a, S. Jin^a, Y. Jin^a, T. Komada^a, S. Kurokawa^a, Y.F. Lai^a, G. Li^a, H.M. Hu^a, T. Hu^a, G.S. Huang^a, X.P. Huang^a, X.T. Huang^a, X.T. Huang^a, M. Ishida^a, S. Ishida^a, X.B. Ji^a, X.S. Jiang^a, J.B. Jiao^a, D.P. Jin^a, S. Jin^a, S. Jin^a, Y. Jin^a, T. Komada^a, S. Kurokawa^a, Y.F. Lai^a, G. Li^a, H.B. Li^a, H.H. Li^a, J. Li^a, R.Y. Li^a, S.M. Li^a, F. Liu^a, F. Liu^a, H.H. Liu^a, H.H. Liu^a, H.J. Liu^a, J.G. Lu^a, J.G. Lu^a, J.B. Liu^a, Y.F. Liang^a, H.B. Liao^a, C.X. Liu^a, F. Lu^a, G.R. Lu^a, G.R. Lu^a, H.J. Lu^a, J.G. Lu^a, J.G. Lu^a, J.C. Luo^a, F.C. Ma^a, J.P. Liu^a, R.G. Liu^a, Z.A. Liu^a, F. Lu^a, G.R. Lu^a, G.R. Lu^a, H.J. Lu^a, J.G. Lu^a, J.G. Lu^a, C.L. Luo^a, F.C. Ma^a, H.L. Ma^a, L.L. Ma^a, Q.M. Ma^a, X.B. Ma^a, Z.P. Mao^a, T. Matsuoka^a, X.H. Mo^a, J. Nie^a, H.P. Peng^a, N.D. Qi^a, H. Qin^a, J.F. Qiu^a, Z.Y. Ren^a, G. Rong^a, L. Shang^a, D.L. Shen^a, X.Y. Shen^a, H.Y. Sheng^a, F. Shi^a, X. Shi^a, H.S. Sun^a, J.F. Sun^a, K. Takamatsu^a, Z.Q. Tan^a, X. Tang^a, Y.R. Tian^a, G.L. Tong^a, L. Wang^a, L.S. Wang^a, M. Wang^a, P. Wang^a, P. Wang^a, P.L. Wang^a, W. Z.Y. Wang^a, Zhe Wang^a, Zheng Wang^a, C.L. Wei^a, D.H. Wei^a, B. Xin^a, G.F. Xu^a, Y. Xu^a, K. Yamada^a, I. Yamauchi^a, J. Yang^a, Y.X. Yang^a, M.H. Ye^a, Y.X. Ye^a, Z.Y. Yi^a, G.W. Y. Zeng^a, Yu Zeng^a, B.X. Zhang^a, B.Y. Zhang^a, C.C. J.W. Zhang^a, J.Y. Zhang^a, J.Y. Zhang^a, Z.X. Zhang^a, Z.P. Zhang^a, D.X. Zhao^a, J.W. Zhao^a, M.G. Zhao^a, Z.Q. Zheng^a, J.P. Zheng^a, Z.P. Zheng^a, L. Zhou^a, N. H.Q. Zheng^a, Y.S. Zhu^a, Yingchun Zhu^a, Z.A. Zhu^a



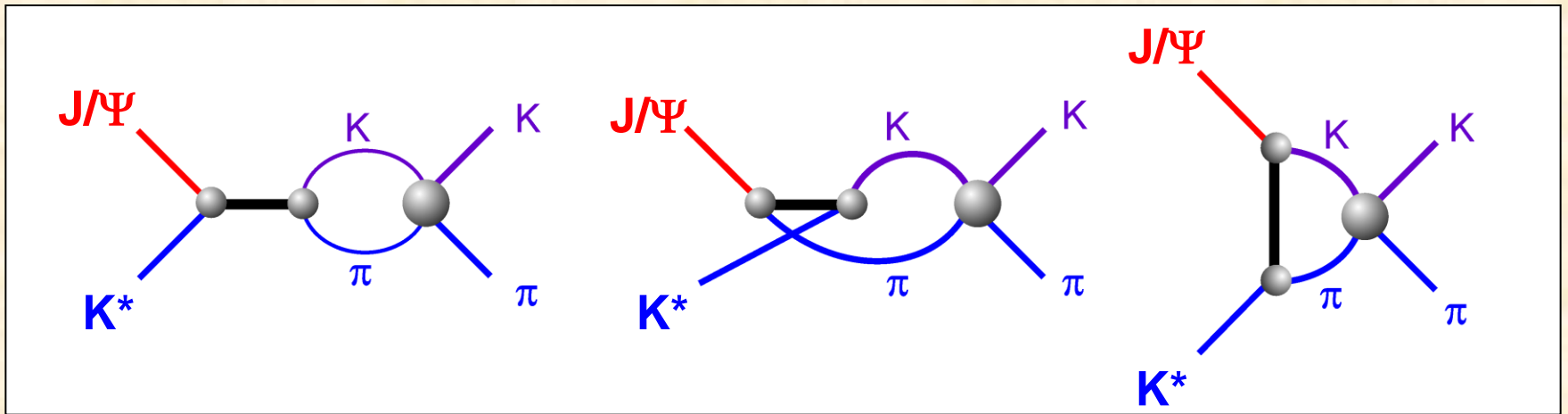
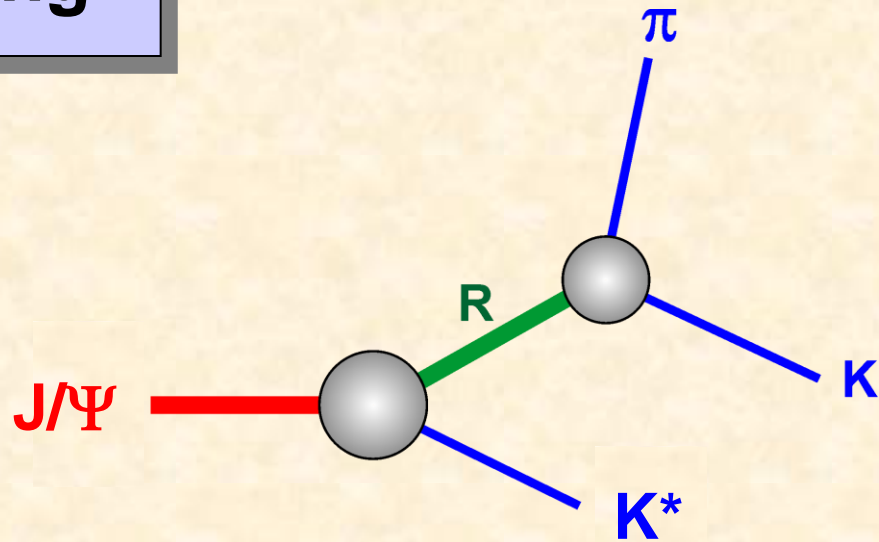
A study of charged κ in $J/\psi \rightarrow K^\pm K_S \pi^\mp \pi^0$

BES Collaboration

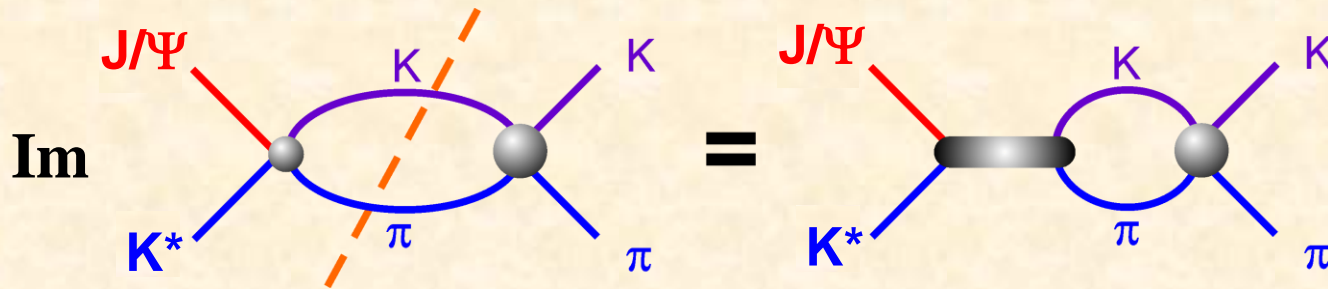
M. Ablikim^a, J.Z. Bai^a, Y. Bai^a, Y. Ban^a, X. Cai^a, H.F. Chen^a, H.S. Chen^a, H.X. Chen^a, J.C. Chen^a, Jin Chen^a, X.D. Chen^a, Y.B. Chen^a, Y.P. Chu^a, Y.S. Dai^a, Z.Y. Deng^a, S.X. Du^{a,1}, J. Fang^a, C.D. Fu^a, C.S. Gao^a, Y.N. Gao^a, S.D. Gu^a, Y.T. Gu^a, Y.N. Guo^a, Z.J. Guo^{a,2}, F.A. Harris^a, K.L. He^a, M. He^a, Y.K. Heng^a, H.M. Hu^a, T. Hu^a, G.S. Huang^{a,3}, X.T. Huang^a, Y.P. Huang^a, X.B. Ji^a, X.S. Jiang^a, J.B. Jiao^a, D.P. Jin^a, S. Jin^a, G. Li^a, H.B. Li^a, J. Li^a, L. Li^a, R.Y. Li^a, H.D. Li^a, W.G. Li^a, X.L. Li^a, X.N. Li^a, X.Q. Li^a, Y.F. Liang^a, B.J. Liu^{a,4}, C.X. Liu^a, Fang Liu^a, Feng Liu^a, H.M. Liu^a, J.P. Liu^a, H.B. Liu^{a,5}, J. Liu^a, Q. Liu^a, R.G. Liu^a, S. Liu^a, Z.A. Liu^a, F. Lu^a, G.R. Lu^a, J.G. Lu^a, C.L. Luo^a, F.C. Ma^a, H.L. Ma^a, Q.M. Ma^a, M.Q.A. Malik^a, Z.P. Mao^a, X.H. Mo^a, J. Nie^a, S.L. Olsen^a, R.G. Ping^a, N.D. Qi^a, J.F. Qiu^a, G. Rong^a, X.D. Ruan^a, L.Y. Shan^a, L. Shang^a, C.P. Shen^a, X.Y. Shen^a, H.Y. Sheng^a, H.S. Sun^a, S.S. Sun^a, Y.Z. Sun^a, Z.J. Sun^a, X. Tang^a, J.P. Tian^a, G.L. Tong^a, G.S. Varner^a, X. Wan^a, L. Wang^a, L.L. Wang^a, L.S. Wang^a, P. Wang^a, P.L. Wang^a, Y.F. Wang^a, Z. Wang^a, Z.Y. Wang^a, C.L. Wei^a, D.H. Wei^a, N. Wu^{a,4}, X.M. Xia^a, G.F. Xu^a, X.P. Xu^a, Y. Xu^a, M.L. Yan^a, H.X. Yang^a, M. Yang^a, Y.X. Yang^a, M.H. Ye^a, Y.X. Ye^a, C.X. Yu^a, C.Z. Yuan^a, Y. Yuan^a, Y. Zeng^a, B.X. Zhang^a, B.Y. Zhang^a, C.C. Zhang^a, D.H. Zhang^a, F. Zhang^{a,6}, H.Q. Zhang^a, H.Y. Zhang^a, J.W. Zhang^a, J.Y. Zhang^a, X.Y. Zhang^a, Y.Y. Zhang^a, Z.X. Zhang^a, Z.P. Zhang^a, D.X. Zhao^a, J.W. Zhao^a, M.G. Zhao^a, P.P. Zhao^a, Z.G. Zhao^a, B. Zheng^a, H.Q. Zheng^a, J.P. Zheng^a, Z.P. Zheng^a, B. Zhong^a, L. Zhou^a, K.J. Zhu^a, Q.M. Zhu^a, X.W. Zhu^a, Y.S. Zhu^a, Z.A. Zhu^a, Z.L. Zhu^a, B.A. Zhuang^a, B.S. Zou^a



Rescattering



Rescattering : Unitarity

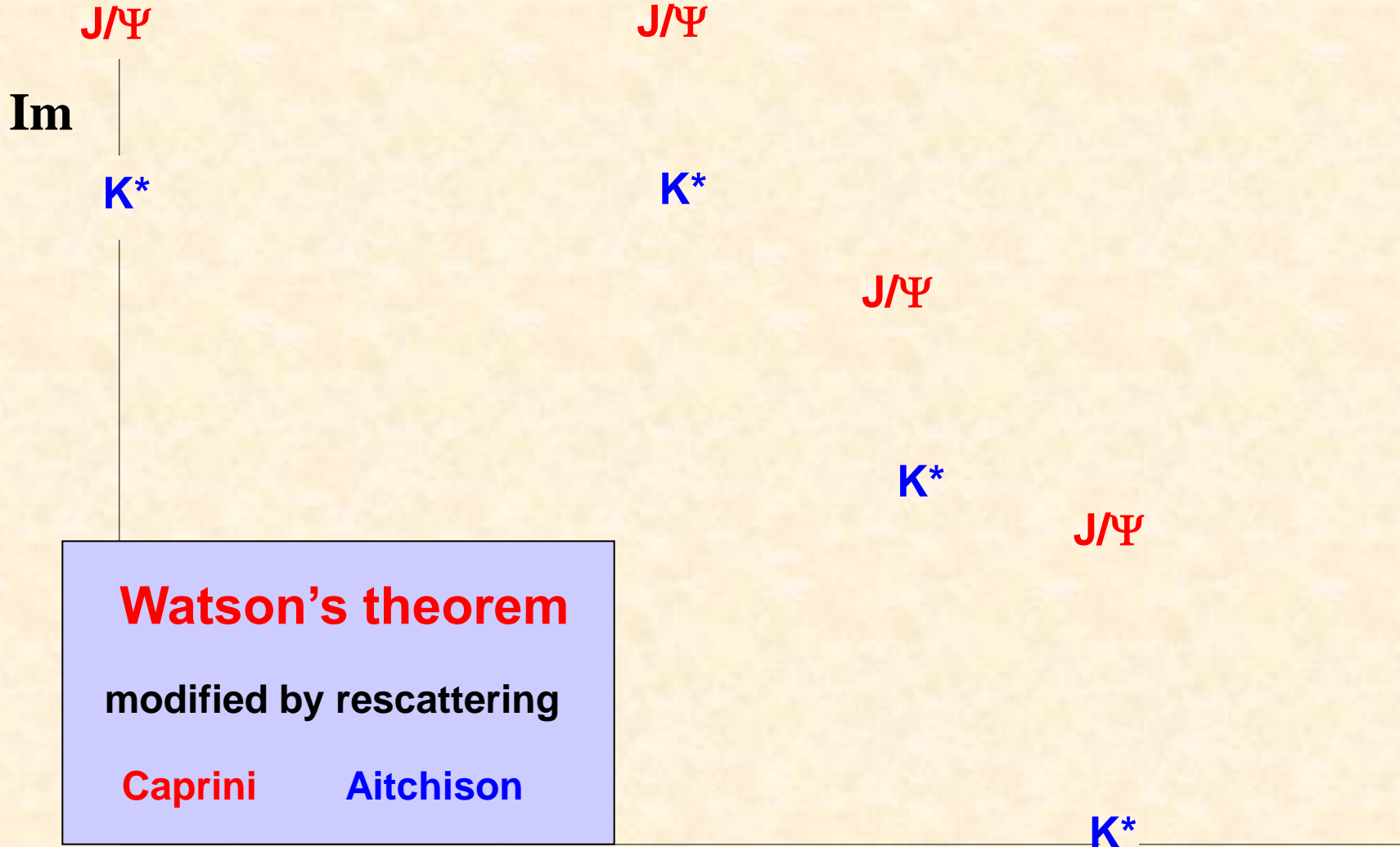


Watson's theorem

elastic

phases simply related
if no rescattering

Rescattering : Unitarity

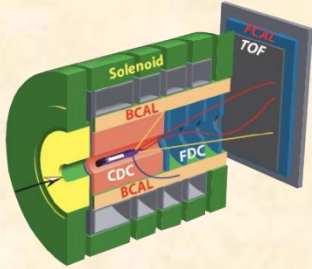




CLEO-c



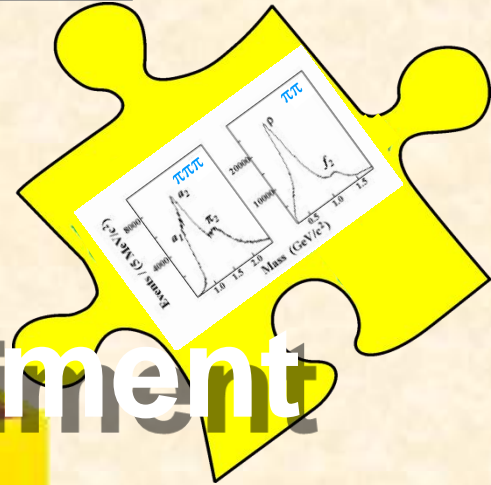
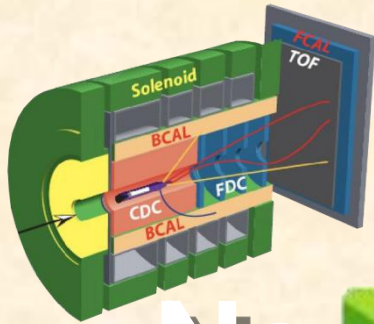
BES III



PANDA



Physics Analysis Center

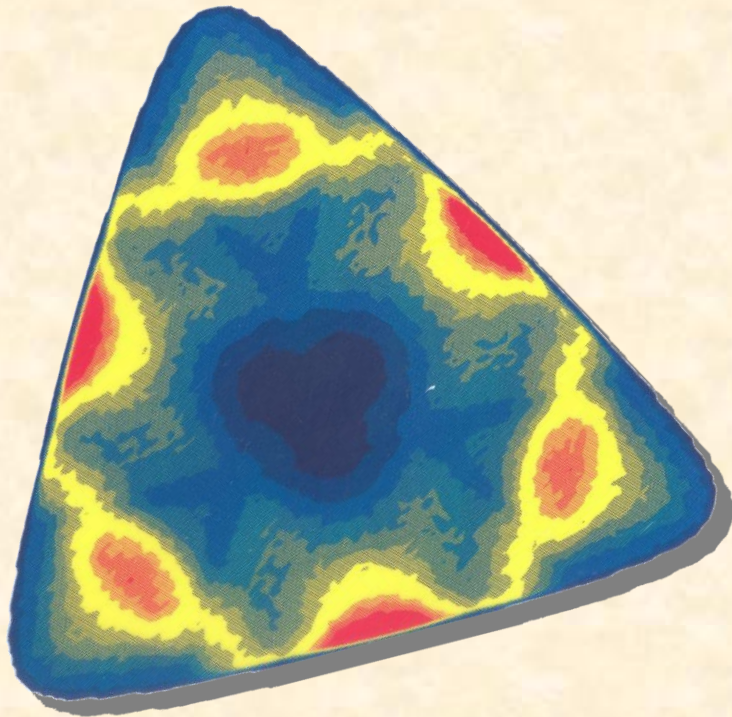


New Theory/Experiment Staff Position



Physics Analysis Center

Techniques of Amplitude Analysis



Jefferson Lab Advanced Study Institute

EXTRACTING PHYSICS FROM PRECISION EXPERIMENTS:

Techniques of Amplitude Analysis

COLLEGE OF WILLIAM & MARY
WILLIAMSBURG, VIRGINIA, USA

Wednesday, May 30th, 2012
through Wednesday, June 13th, 2012

To prepare for the analysis of precision experiments at BESIII, COMPASS, LHCb, JLAB@12 GeV, and PANDA@FAIR, Thomas Jefferson National Accelerator Facility (JLab) is organizing a two week advanced course covering *Techniques of Amplitude Analysis*, aimed at postdoctoral researchers and advanced doctoral students in nuclear and particle physics.

May/June 2012

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Jozef Dudek	(ODU)
Bastian Kubis	(Bonn)
T-S Harry Lee	(ANL)
Brian Meadows	(Cincinnati)
Antimo Palano	(Bari)
Klaus Peters	(GSI Darmstadt)
Michael Pennington	(JLab)
Ronald Workman	(GWU)

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For application details and all other information see:

<http://www.jlab.org/conferences/asi2012/>

End