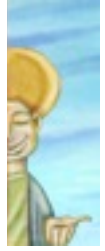


*University of New Hampshire
Colloquium, March 19, 2012*

Quark-Hadron Duality in Electron-Nucleon Scattering

Wally Melnitchouk





Outline

- Historical perspective
 - examples from Nature

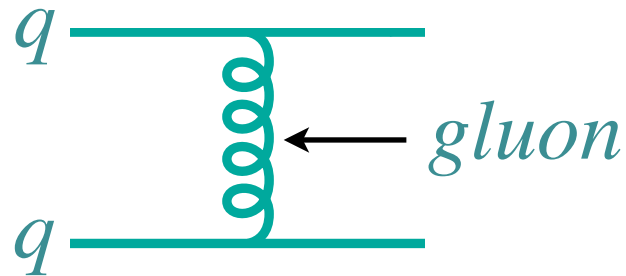
- Duality and Quantum ChromoDynamics
 - twists and moments
 - nonperturbative models

- Implications for quark distributions

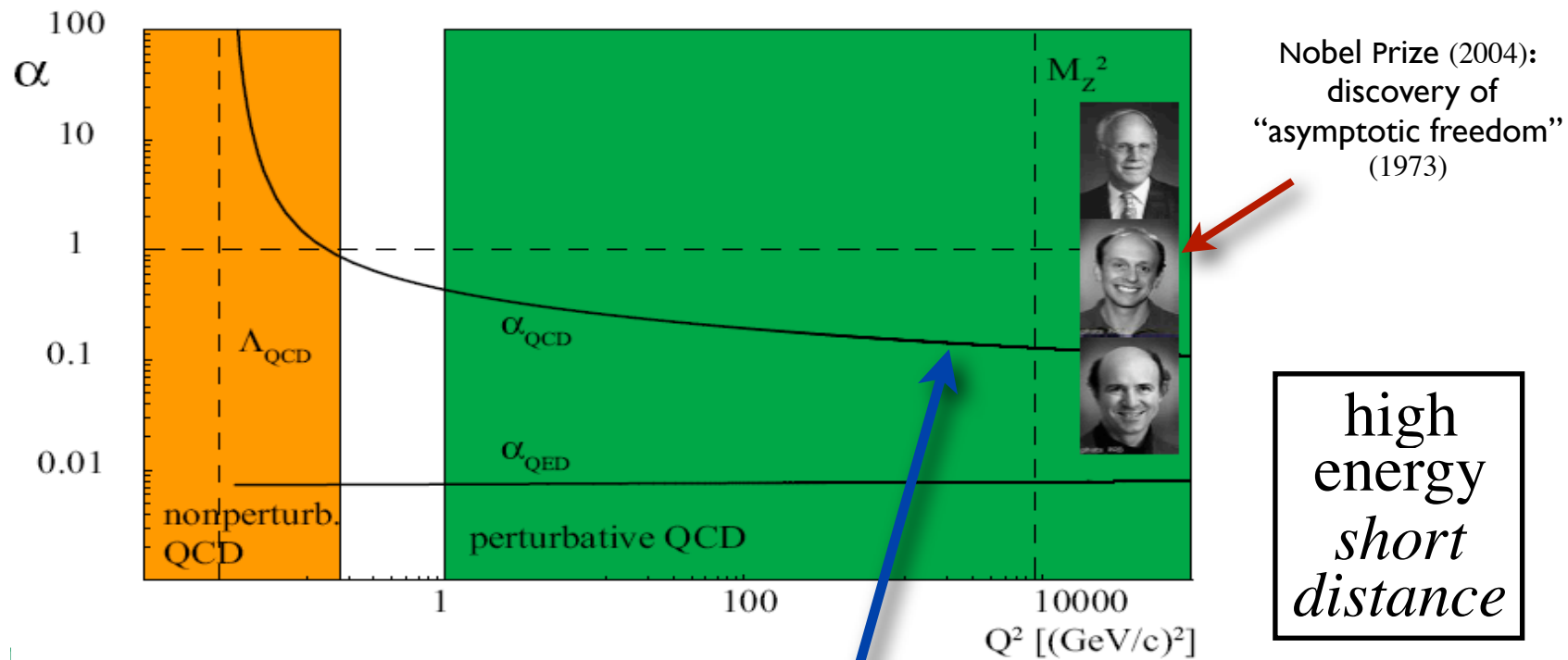
- Outlook

■ Strong nuclear force described (in principle) by theory of Quantum ChromoDynamics (QCD)

→ governed by size of quark-gluon coupling constant α_{QCD} (or α_s)



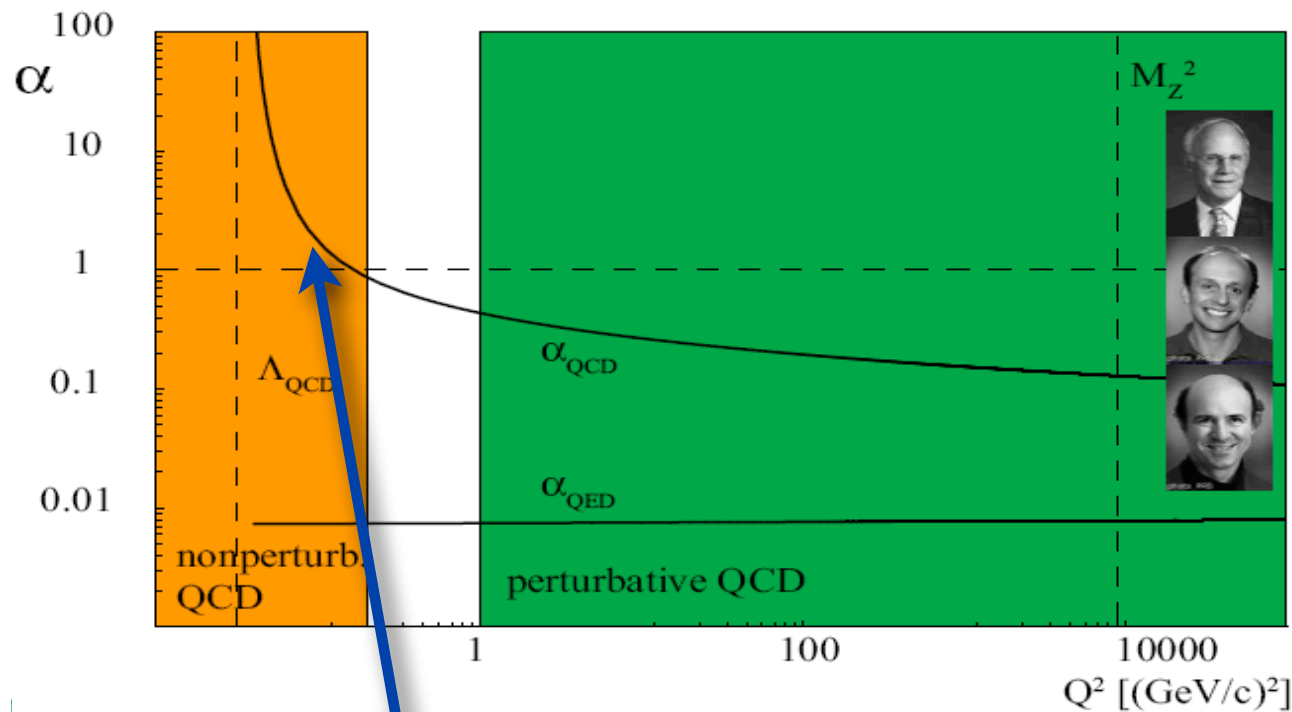
→ in practice, full understanding of *hadron & nuclear* structure and interactions in terms of *quarks & gluons* remains a challenge even after 40 years!



“strong” coupling constant α_s small

→ calculate physical observables in terms of quarks and gluons using perturbation theory

low
energy
long
distance

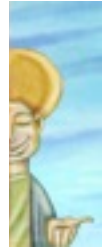


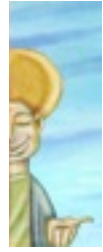
high
energy
short
distance

α_s large, cannot describe observables
in terms of quarks perturbatively

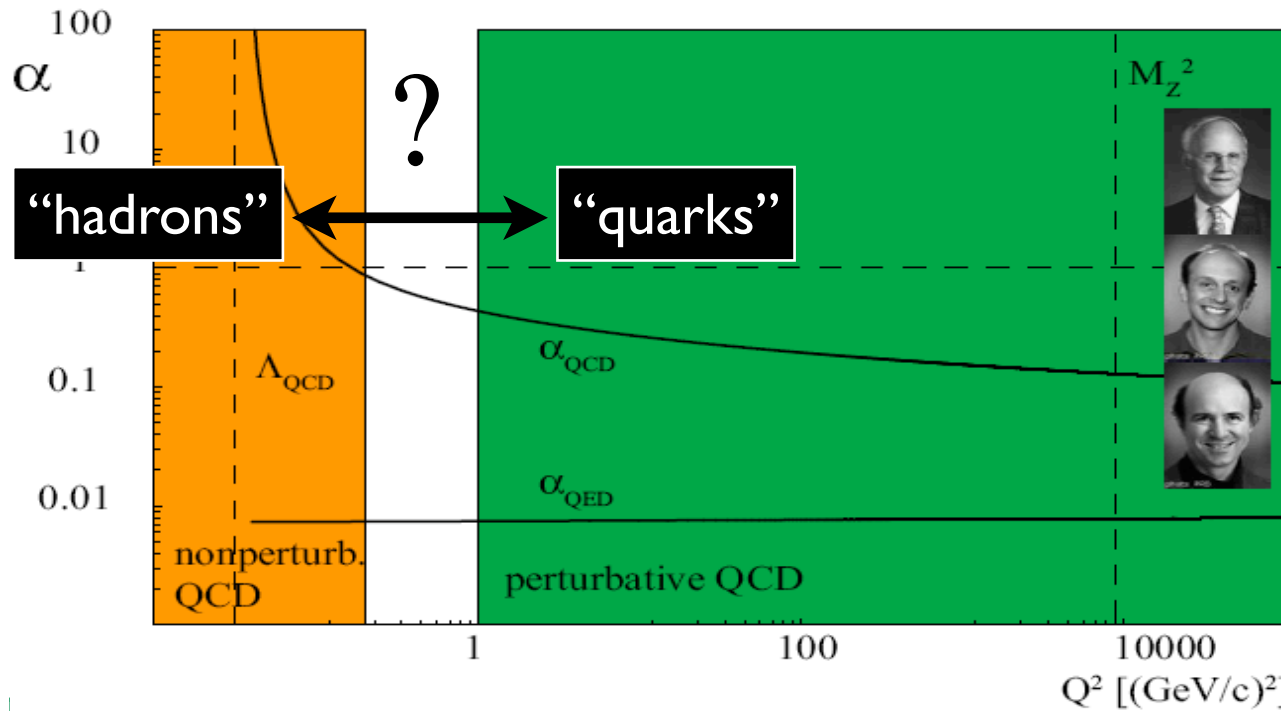
→ requires nonperturbative methods
such as *lattice* QCD

→ meson & baryon degrees of freedom
prominent





low energy
long distance

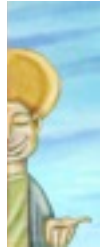
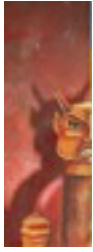


high energy
short distance

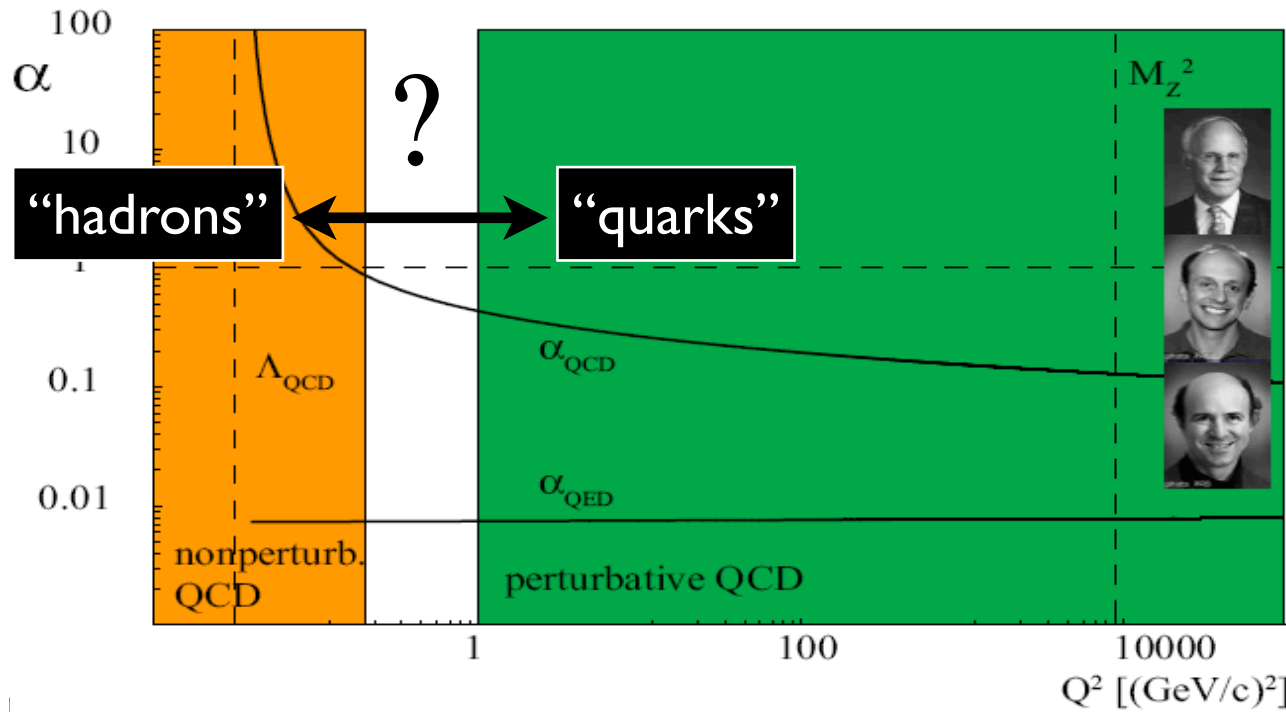
- Duality hypothesis: complementarity between *quark* and *hadron* descriptions of observables

$$\sum_{hadrons} = \sum_{quarks}$$

→ can use either set of *complete* basis states to describe physical phenomena



low
energy
long
distance



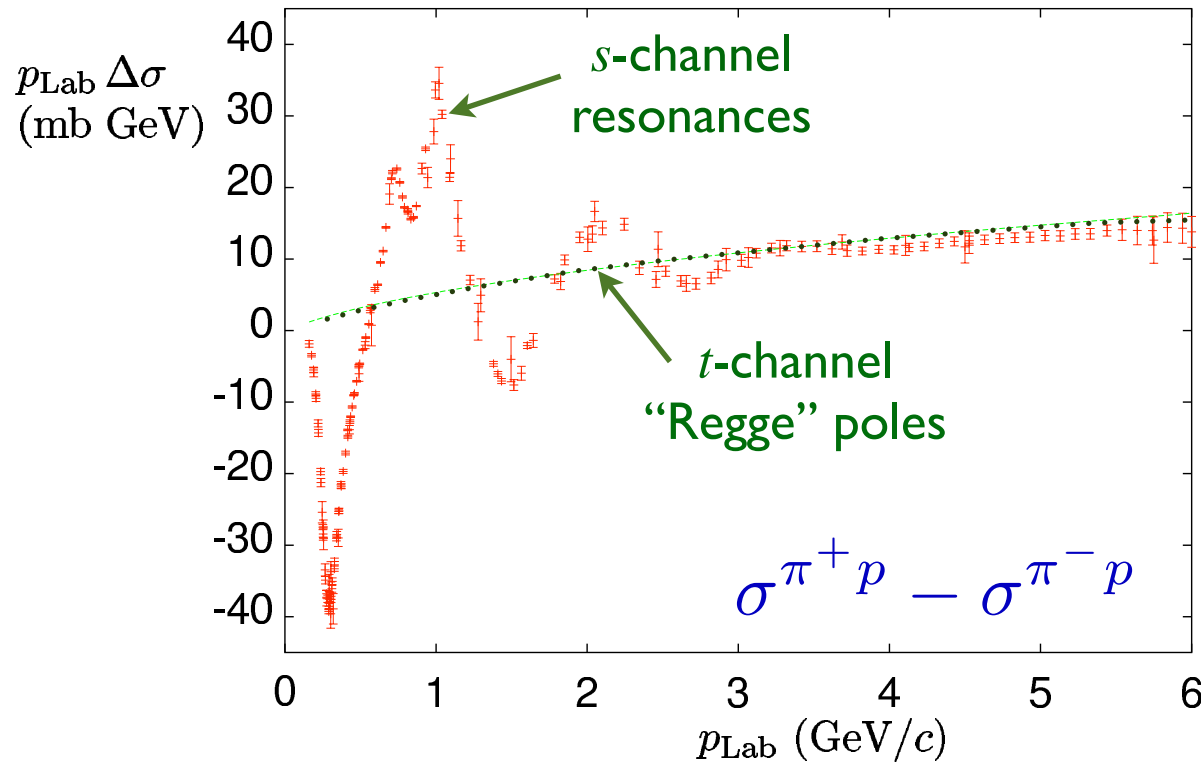
high
energy
short
distance

- In practice, at finite energy typically have access only to *limited* set of basis states

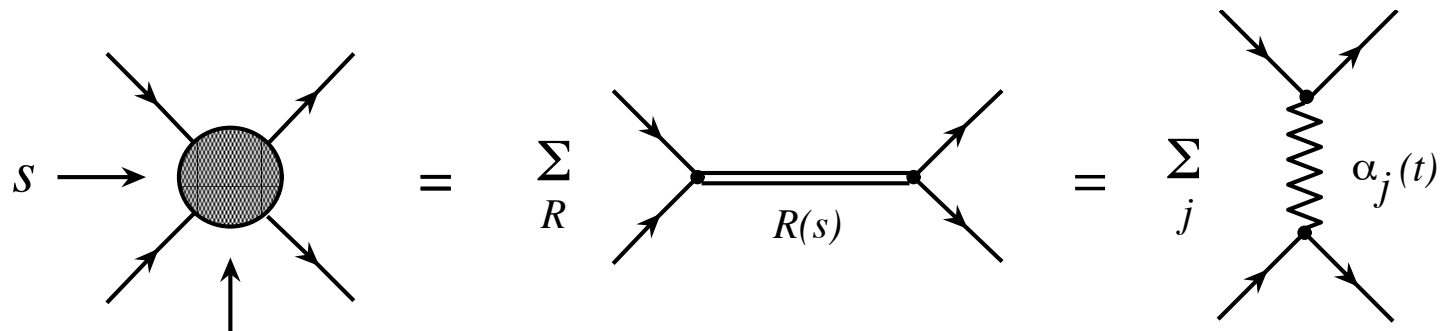


- In practice, at finite energy typically have access only to *limited* set of basis states
- Question is not *why* duality exists, but *how* it arises where it exists

Duality in hadron-hadron scattering

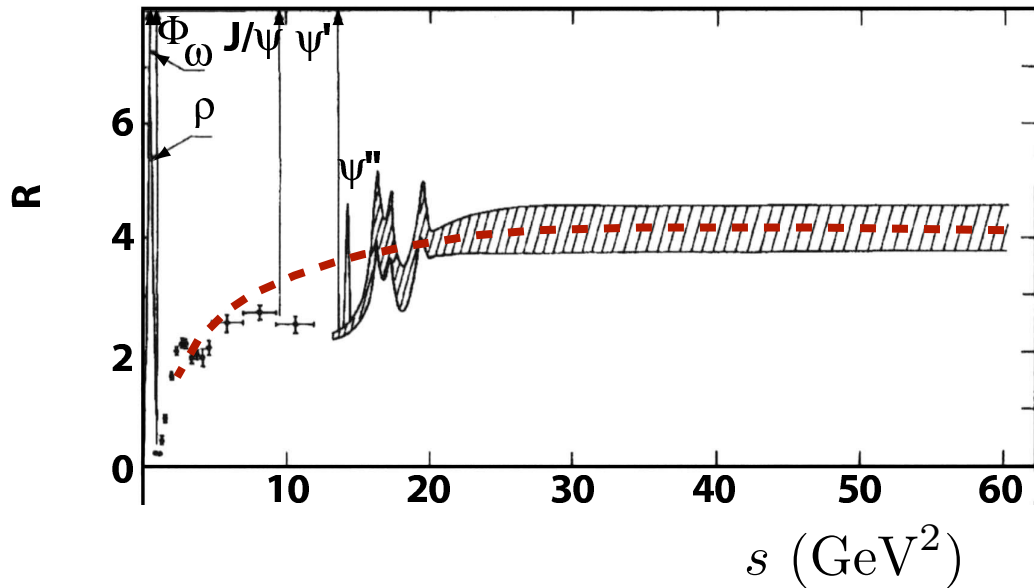


Igi (1962)
Dolen, Horn, Schmidt (1968)



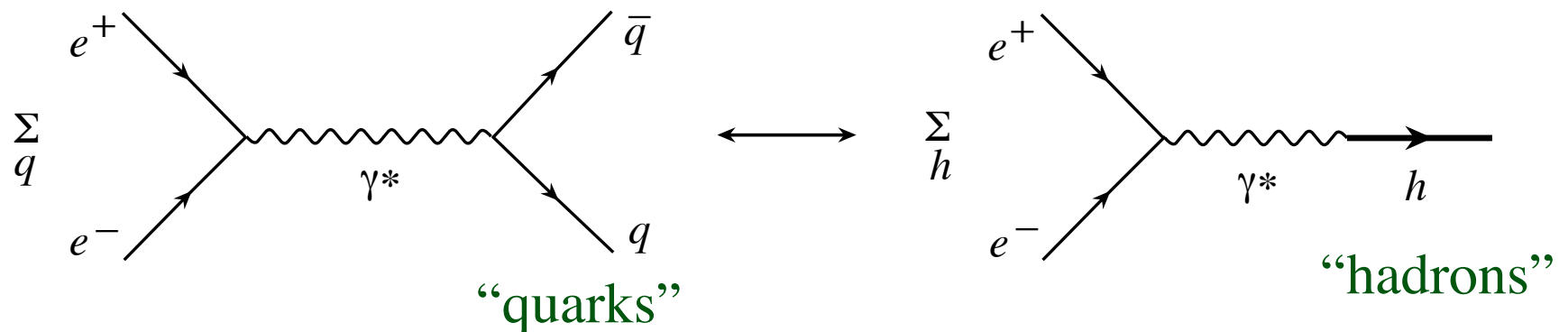
"*s-t* channel duality"

Duality in $e^+ e^-$ annihilation

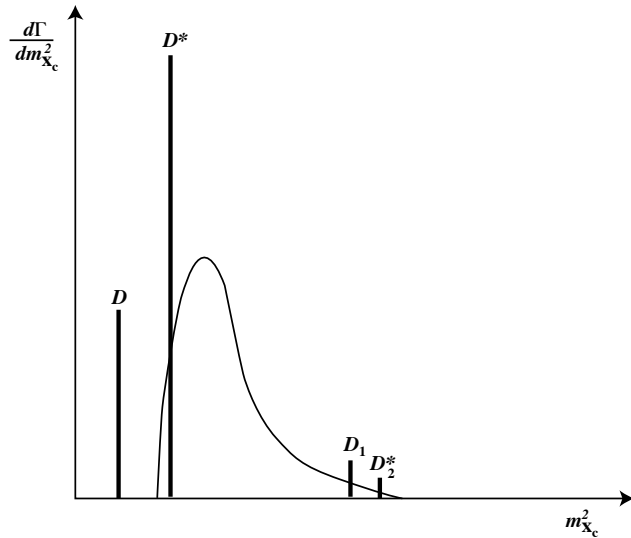


$$R = \frac{\sigma(e^+ e^- \rightarrow \text{hadrons})}{\sigma(e^+ e^- \rightarrow \mu^+ \mu^-)}$$

→ total hadronic cross section at high energy averages resonance cross section



Duality in heavy meson decays



$$Q \rightarrow Q' l \bar{\nu}_l$$

$$\Gamma^q = \frac{G_F^2 \delta m^5}{15\pi^2} |V_{QQ'}|^2$$

$$(Q\bar{q}) \rightarrow X_{Q'} l \bar{\nu}_l$$

$$\Gamma^{\text{PS}} = \frac{G_F^2 \delta m^5}{60\pi^2} |V_{QQ'}|^2$$

$$\Gamma^{\text{V}} = \frac{G_F^2 \delta m^5}{20\pi^2} |V_{QQ'}|^2$$

$$m_Q + m_{Q'} \gg m_Q - m_{Q'} \gg \Lambda_{\text{QCD}}$$

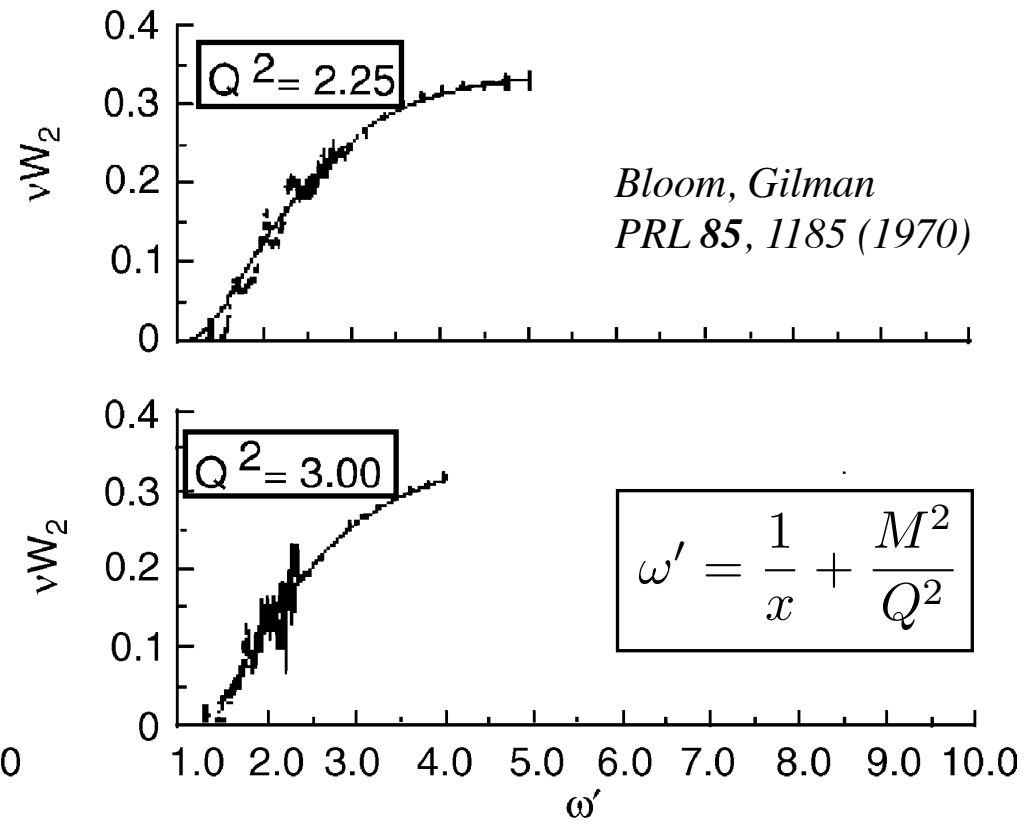
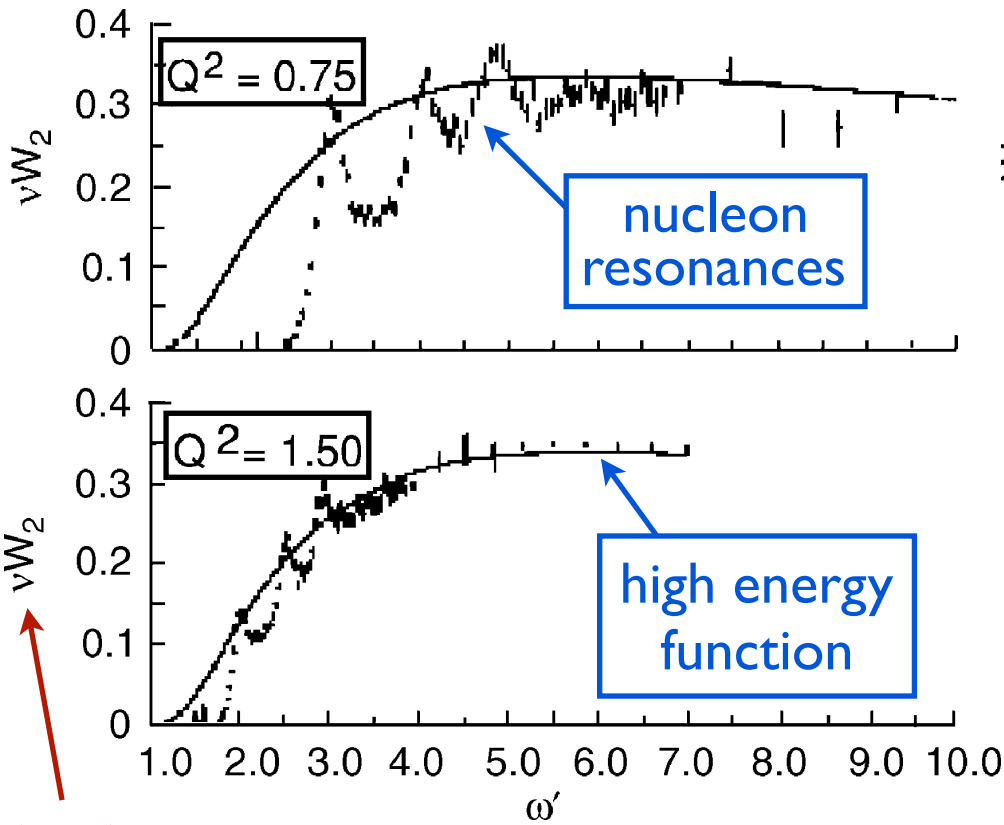
$$\delta m = m_Q - m_{Q'} \approx M_{(Q\bar{q})} - M_{Q'\bar{q}}$$

→ sum over hadronic-level decay rates
= quark-level decay rate

$$\Gamma^{\text{PS}} + \Gamma^{\text{V}} \longleftrightarrow \Gamma^q$$

Duality in electron-nucleon scattering

“Bloom-Gilman duality”



“structure function”

$$\frac{2M}{Q^2} \int_0^{\nu_m} d\nu \nu W_2(\nu, Q^2) = \int_1^{\omega'_m} d\omega' \nu W_2(\omega')$$

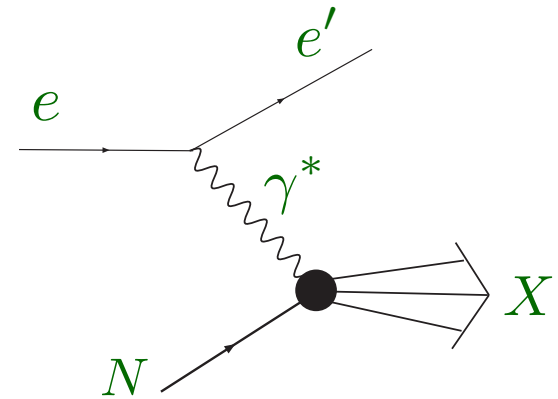
“hadrons”

“quarks”

Electron-nucleon scattering

- Inclusive cross section for $eN \rightarrow eX$

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{4\alpha^2 E'^2 \cos^2 \frac{\theta}{2}}{Q^4} \left(2 \tan^2 \frac{\theta}{2} \frac{F_1}{2M} + \frac{F_2}{\nu} \right)$$



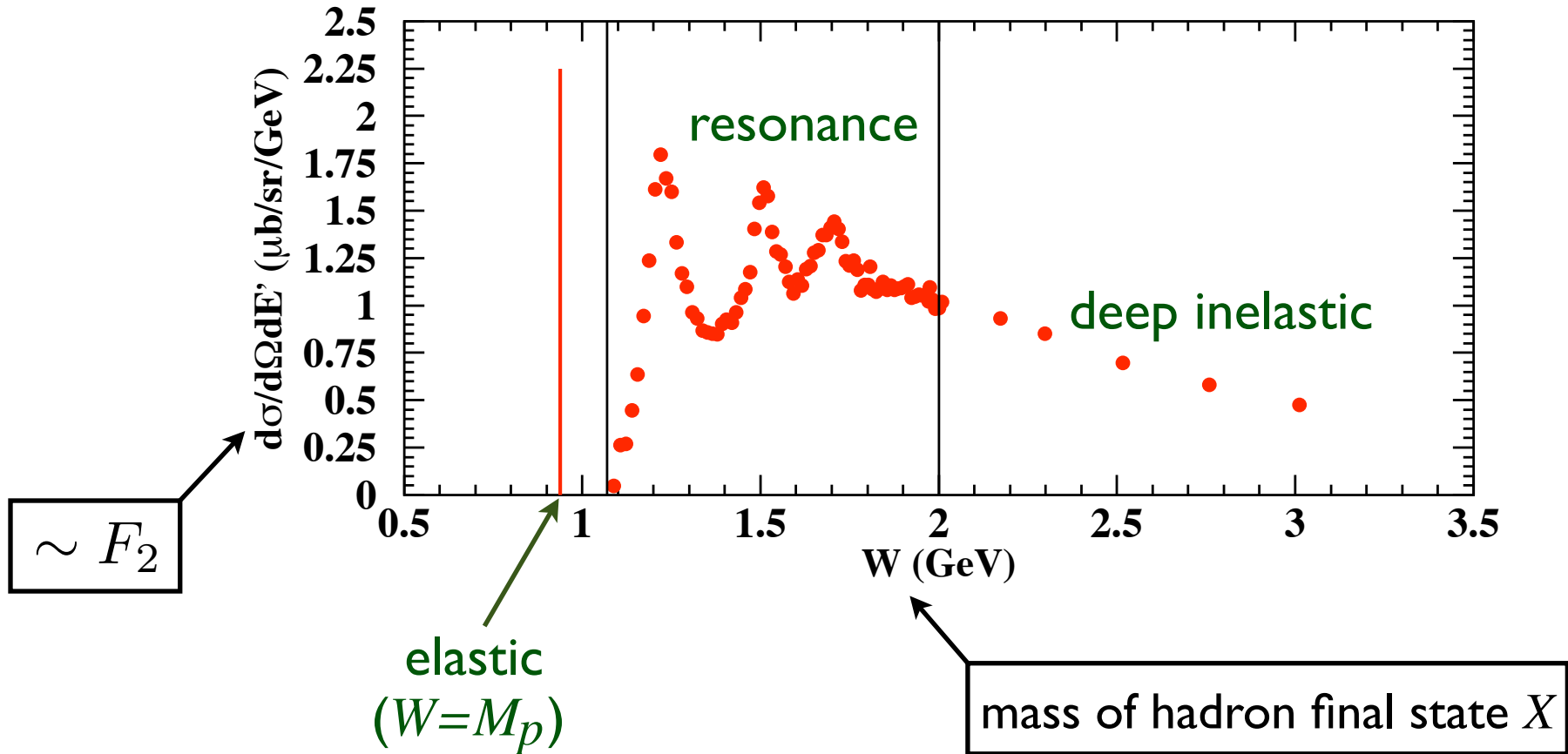
$$\left. \begin{aligned} \nu &= E - E' \\ Q^2 &= \vec{q}^2 - \nu^2 = 4EE' \sin^2 \frac{\theta}{2} \end{aligned} \right\} x = \frac{Q^2}{2M\nu}$$

Bjorken scaling variable

- F_1 , F_2 structure functions

→ contain all information about structure of nucleon

Electron-nucleon scattering



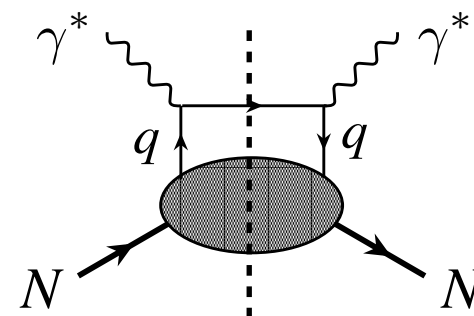
Bjorken variable in terms of Q^2 & W :
$$x = \frac{Q^2}{W^2 - M^2 + Q^2}$$

- In *deep-inelastic* region ($W \gtrsim 2 \text{ GeV}$, $Q^2 \gtrsim 1 \text{ GeV}^2$), structure function given by quark & antiquark (“parton”) distributions

$$\begin{aligned}
 F_2(x, Q^2) &= x \sum_q e_q^2 q(x, Q^2) \\
 &= \frac{4}{9} x(u + \bar{u}) + \frac{1}{9} x(d + \bar{d}) + \frac{1}{9} x(s + \bar{s}) + \dots
 \end{aligned}$$

→ $q(x, Q^2)$ = probability to find quark type “ q ” in nucleon, carrying momentum fraction x

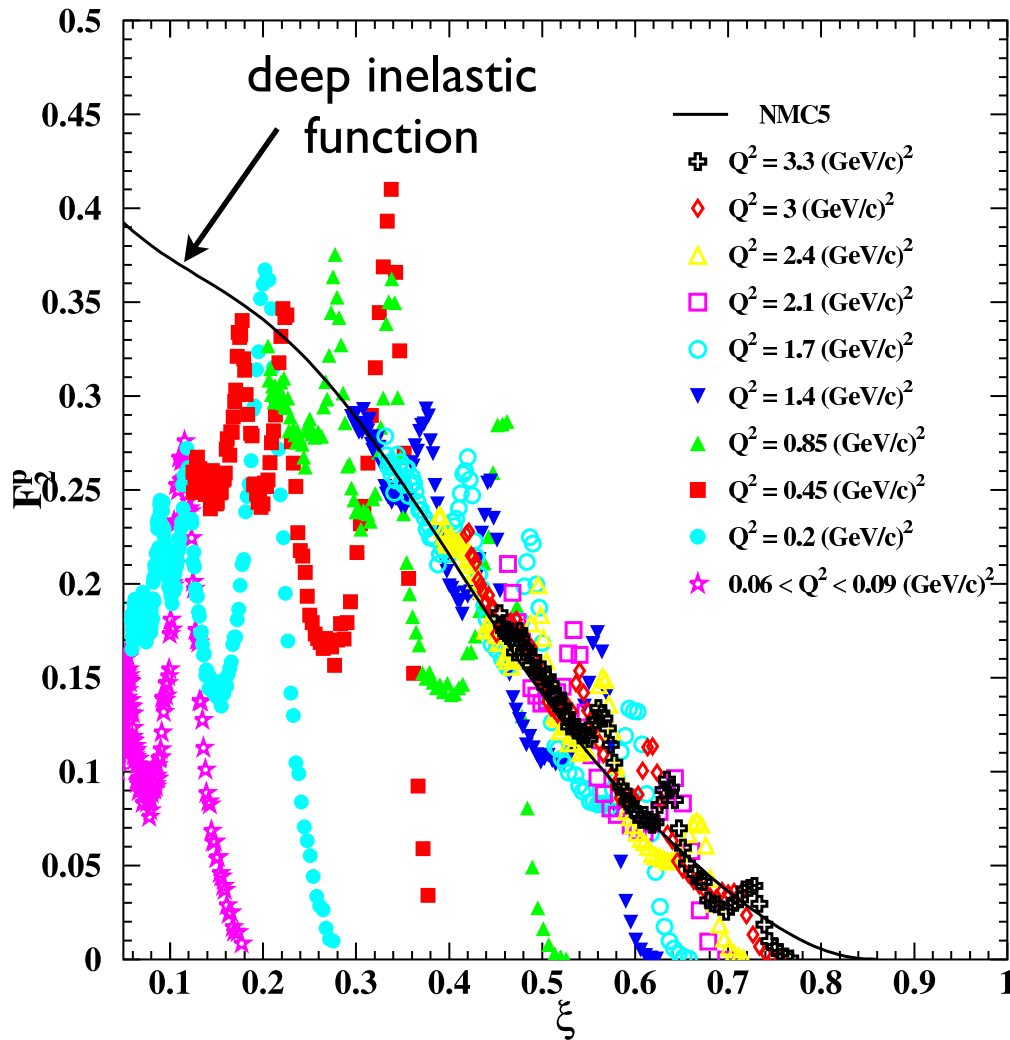
“PDF”



- In *resonance* region ($W \lesssim 2 \text{ GeV}$), or at low Q^2 ($Q^2 \lesssim 1 \text{ GeV}^2$) can no longer resolve individual quark structure

→ see *gross features* of hadron (complex, multi-parton effects)

Duality in electron-nucleon scattering



average over
(strongly Q^2 dependent)
resonances
 $\approx Q^2$ independent
scaling function

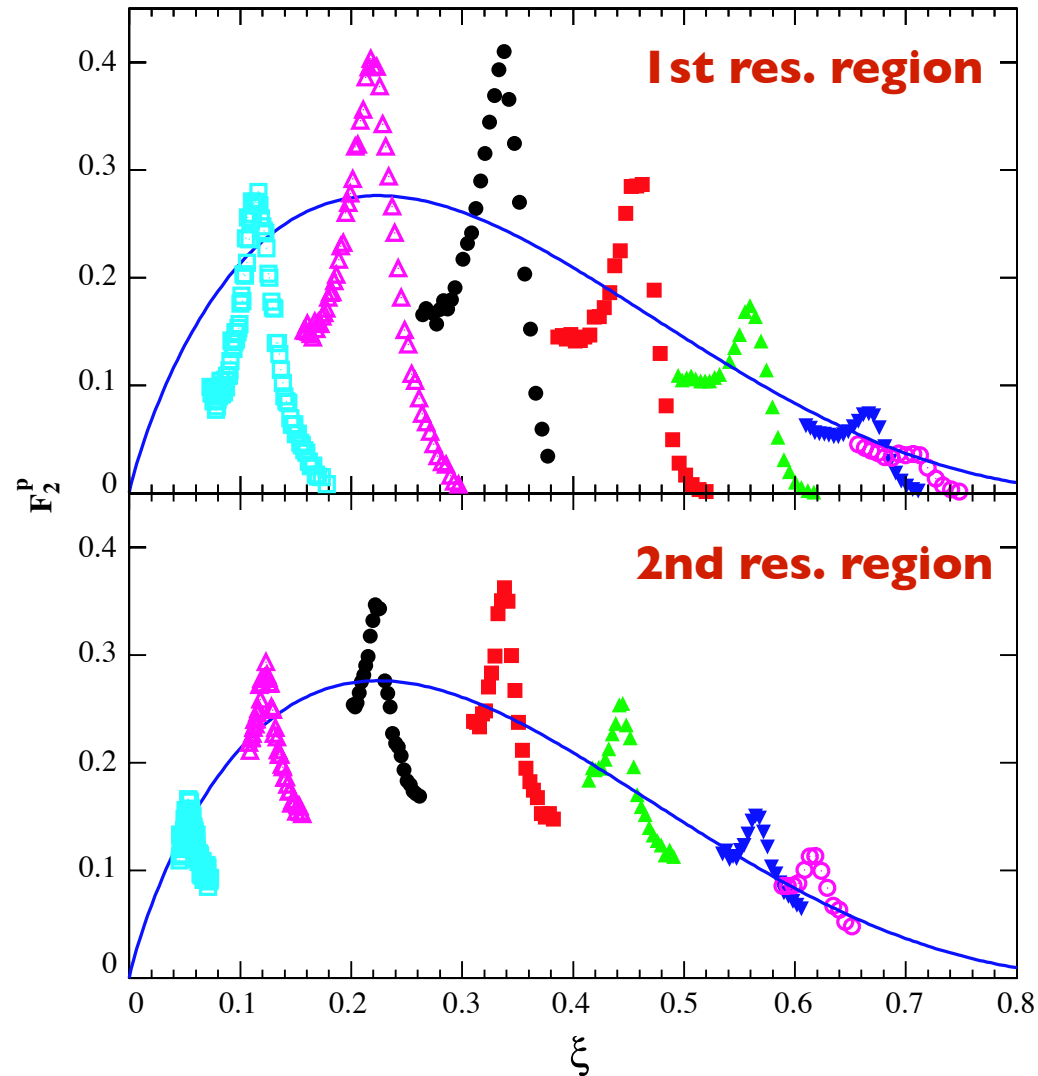
“Nachtmann” scaling variable

$$\xi = \frac{2x}{1 + \sqrt{1 + 4M^2 x^2 / Q^2}}$$

Niculescu et al., PRL 85, 1182 (2000)

WM, Ent, Keppel, PRep. 406, 127 (2005)

Duality in electron-nucleon scattering



→ also exists *locally* in individual resonance regions

Duality and QCD

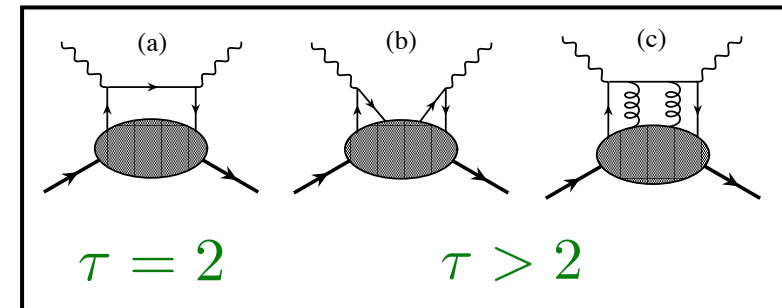
■ Operator product expansion

→ expand *moments* of structure functions in powers of $1/Q^2$

$$\begin{aligned} M_n(Q^2) &= \int_0^1 dx x^{n-2} F_2(x, Q^2) \\ &= A_n^{(2)} + \frac{A_n^{(4)}}{Q^2} + \frac{A_n^{(6)}}{Q^4} + \dots \end{aligned}$$

matrix elements of operators with specific “twist” τ

$\tau = \text{dimension} - \text{spin}$



Duality and QCD

■ Operator product expansion

→ expand *moments* of structure functions in powers of $1/Q^2$

$$\begin{aligned} M_n(Q^2) &= \int_0^1 dx x^{n-2} F_2(x, Q^2) \\ &= A_n^{(2)} + \frac{A_n^{(4)}}{Q^2} + \frac{A_n^{(6)}}{Q^4} + \dots \end{aligned}$$

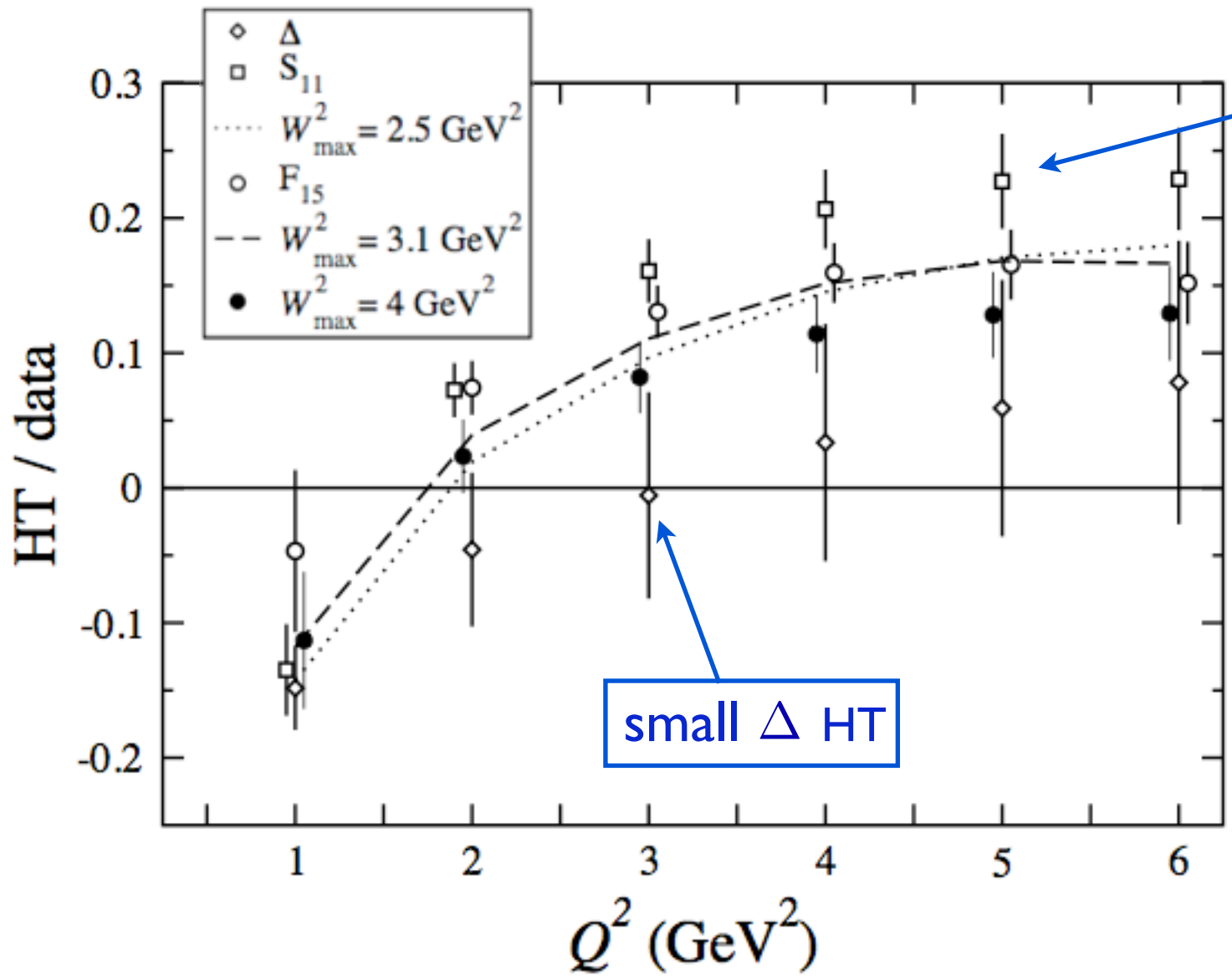
*de Rujula, Georgi, Politzer
Ann. Phys. 103, 315 (1975)*

■ If moment \approx independent of Q^2

→ “higher twist” terms $A_n^{(\tau>2)}$ small

■ Duality \longleftrightarrow suppression of higher twists

■ Analysis of JLab F_2^p resonance region data



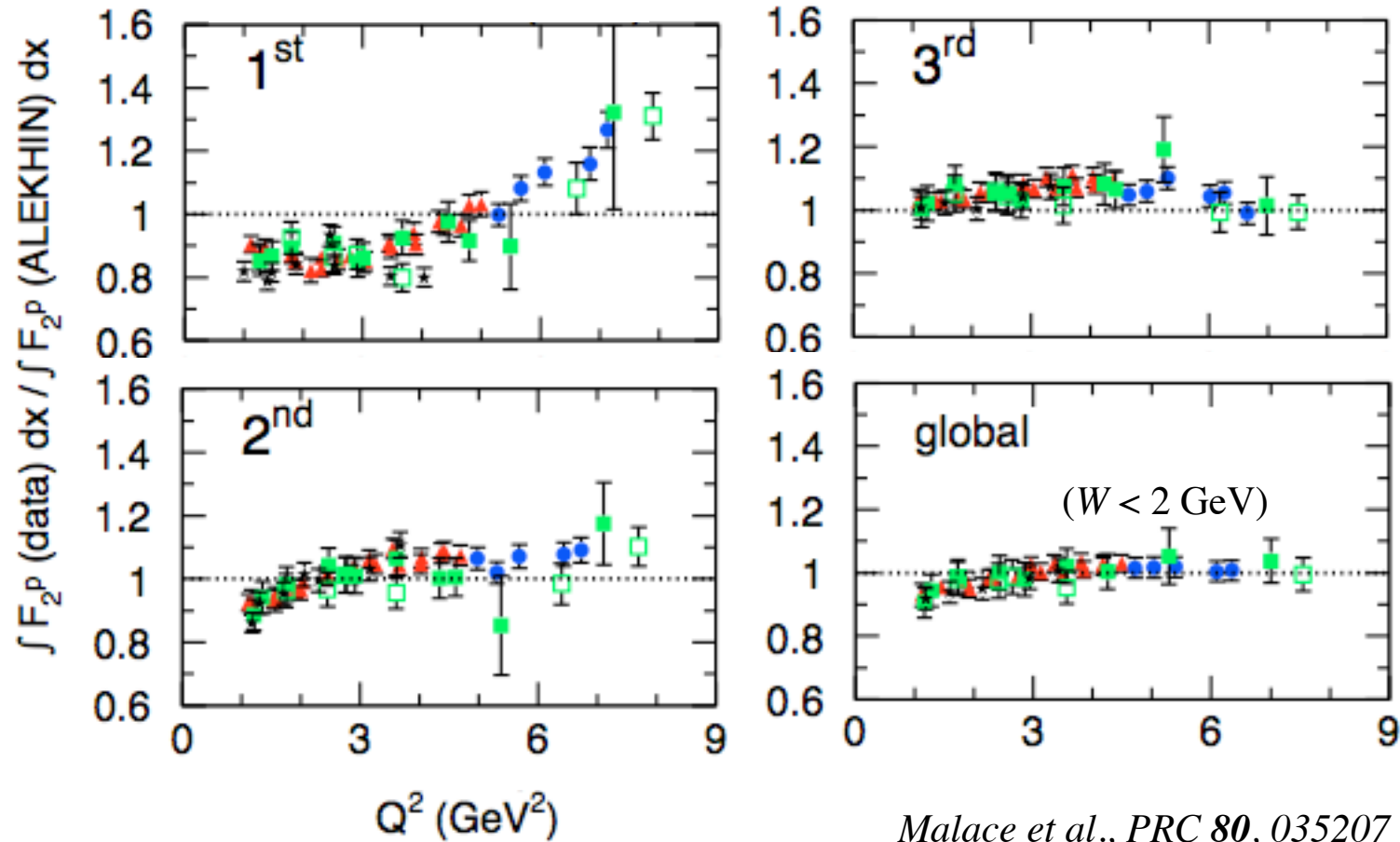
larger S_{11} HT

small Δ HT

*Psaker et al.,
PRC 78, 025206 (2008)*

→ higher twists < 10–15% for $Q^2 > 1 \text{ GeV}^2$

■ Analysis of (latest) JLab F_2^p resonance region data



Malace et al., PRC 80, 035207 (2009)

→ higher twists < 10–15% for $Q^2 > 1 \text{ GeV}^2$

Resonances & twists

- Total “higher twist” is *small* at scales $Q^2 \sim \mathcal{O}(1 \text{ GeV}^2)$
 - On average, nonperturbative interactions between quarks and gluons not dominant (at these scales)
 - nontrivial interference between resonances
-

- Can we understand this dynamically, at quark level?
 - is duality an accident?
- Can we use resonance region data to learn about *leading twist* structure functions?
 - expanded data set has potentially significant implications for global quark distribution studies

- Consider simple quark model with spin-flavor symmetric wave function

low energy

→ *coherent* scattering from quarks $d\sigma \sim \left(\sum_i e_i \right)^2$

high energy

→ *incoherent* scattering from quarks $d\sigma \sim \sum_i e_i^2$

- For duality to work, these must be equal

→ how can square of a sum become sum of squares?

■ Dynamical cancellations

→ *e.g.* for toy model of two quarks bound in a harmonic oscillator potential, structure function given by

$$F(\nu, \mathbf{q}^2) \sim \sum_n |G_{0,n}(\mathbf{q}^2)|^2 \delta(E_n - E_0 - \nu)$$

→ charge operator $\sum_i e_i \exp(i\mathbf{q} \cdot \mathbf{r}_i)$ excites
even partial waves with strength $\propto (e_1 + e_2)^2$
odd partial waves with strength $\propto (e_1 - e_2)^2$

→ resulting structure function

$$F(\nu, \mathbf{q}^2) \sim \sum_n \{ (e_1 + e_2)^2 G_{0,2n}^2 + (e_1 - e_2)^2 G_{0,2n+1}^2 \}$$

→ if states degenerate, *cross terms* ($\sim e_1 e_2$) *cancel* when averaged over nearby *even and odd parity states*

Close, Isgur, PLB 509, 81 (2001)

■ Dynamical cancellations

→ duality is realized by summing over at least one complete set of even and odd parity resonances

Close, Isgur, PLB 509, 81 (2001)

→ in NR Quark Model, even & odd parity states generalize to **56** ($L=0$) and **70** ($L=1$) multiplets of spin-flavor SU(6)

representation	${}^2\mathbf{8}[\mathbf{56}^+]$	${}^4\mathbf{10}[\mathbf{56}^+]$	${}^2\mathbf{8}[\mathbf{70}^-]$	${}^4\mathbf{8}[\mathbf{70}^-]$	${}^2\mathbf{10}[\mathbf{70}^-]$	Total
F_1^p	$9\rho^2$	$8\lambda^2$	$9\rho^2$	0	λ^2	$18\rho^2 + 9\lambda^2$
F_1^n	$(3\rho + \lambda)^2/4$	$8\lambda^2$	$(3\rho - \lambda)^2/4$	$4\lambda^2$	λ^2	$(9\rho^2 + 27\lambda^2)/2$

λ (ρ) = (anti) symmetric component of ground state wave function

Close, WM, PRC 68, 035210 (2003)

■ Dynamical cancellations

→ in $SU(6)$ limit $\lambda = \rho$, with relative strengths of $N \rightarrow N^*$ transitions

$SU(6) :$	$[56, 0^+]^2 8$	$[56, 0^+]^4 10$	$[70, 1^-]^2 8$	$[70, 1^-]^4 8$	$[70, 1^-]^2 10$	<i>total</i>
F_1^p	9	8	9	0	1	27
F_1^n	4	8	1	4	1	18

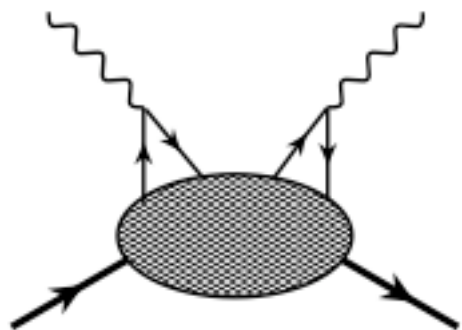
→ summing over all resonances in 56^+ and 70^- multiplets

$$\frac{F_1^n}{F_1^p} = \frac{18}{27} = \frac{2}{3}$$

→ at the quark level, n/p ratio is

$$\frac{F_1^n}{F_1^p} = \frac{4d + u}{d + 4u} = \frac{6}{9} = \frac{2}{3} \quad ! \quad \text{if } u = 2d$$

■ Accidental cancellations of charges?



cat's ears diagram (4-fermion higher twist $\sim 1/Q^2$)

$$\propto \sum_{i \neq j} e_i e_j \sim \left(\sum_i e_i \right)^2 - \sum_i e_i^2$$

↑ *coherent*
↑ *incoherent*

proton HT $\sim 1 - \left(2 \times \frac{4}{9} + \frac{1}{9} \right) = 0!$

neutron HT $\sim 0 - \left(\frac{4}{9} + 2 \times \frac{1}{9} \right) \neq 0$

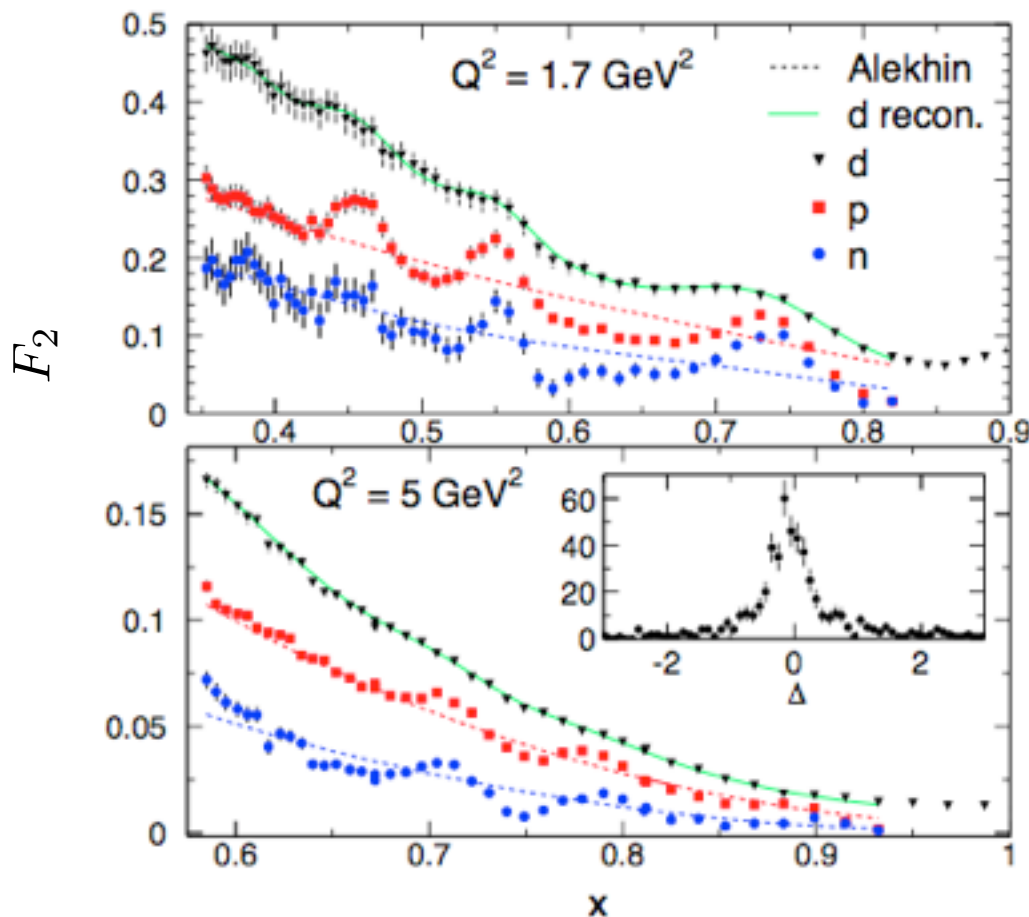
*Brodsky
hep-ph/0006310*

→ duality in proton a *coincidence!*

→ should not hold for neutron

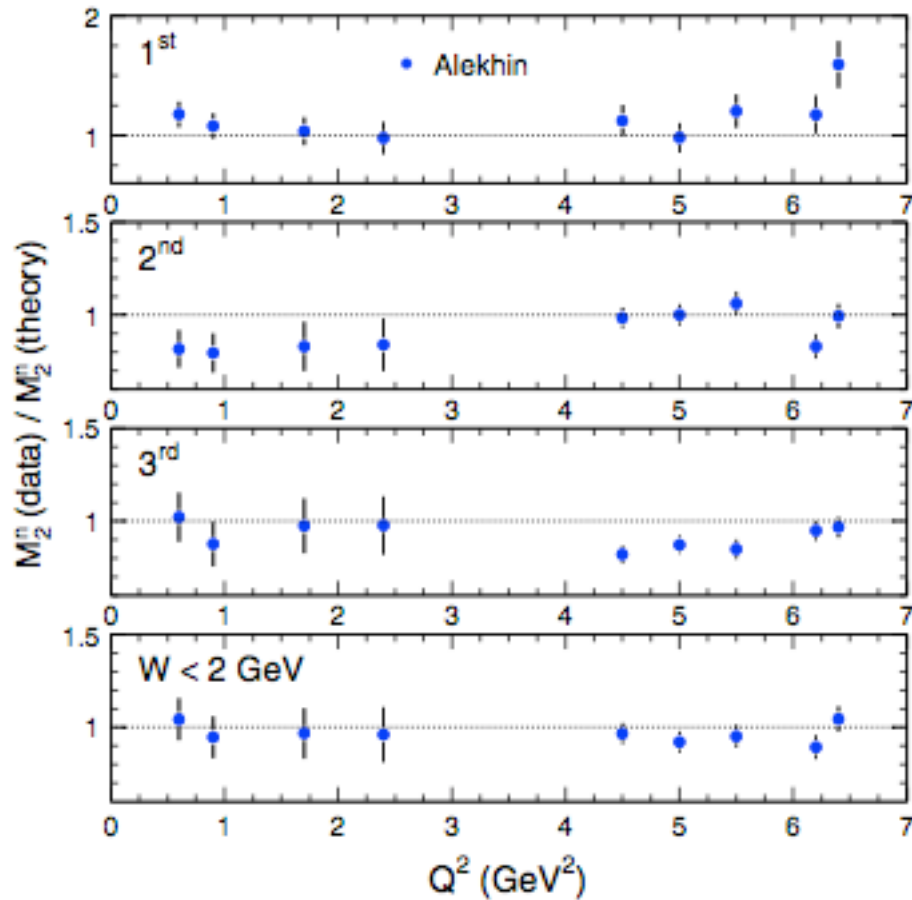
Neutron: the smoking gun

- Duality in *neutron* more difficult to test because of absence of free neutron targets
- New extraction method (using iterative procedure for solving integral convolution equations) has allowed first determination of F_2^n in resonance region & test of neutron duality



Malace, Kahn, WM, Keppel
PRL **104**, 102001 (2010)

Neutron: the smoking gun



→ “theory”: fit to $W > 2 \text{ GeV}$ data

Alekhin et al., 0908.2762 [hep-ph]

→ *locally*, violations of duality in resonance regions $< 15\text{--}20\%$ (largest in Δ region)

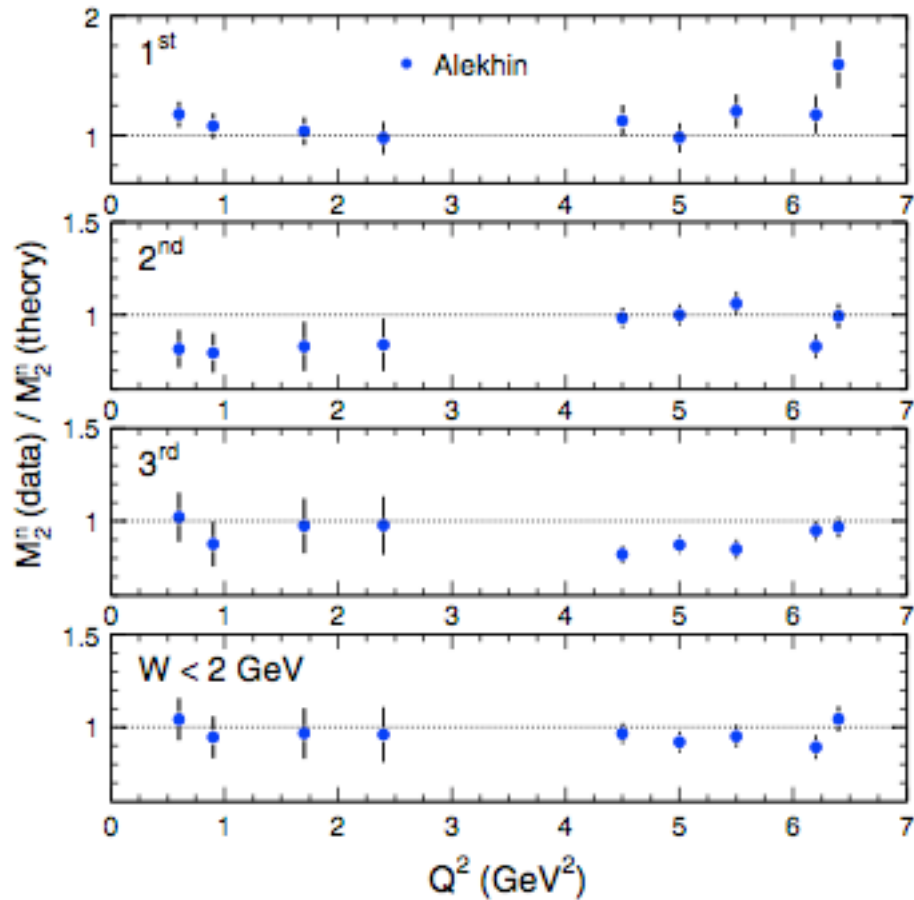
→ *globally*, violations $< 10\%$

Malace, Kahn, WM, Keppel
PRL 104, 102001 (2010)



duality is *not accidental*, but a general feature of resonance–scaling transition!

Neutron: the smoking gun



→ “theory”: fit to $W > 2$ GeV data

Alekhin et al., 0908.2762 [hep-ph]

→ *locally*, violations of duality in resonance regions < 15–20% (largest in Δ region)

→ *globally*, violations < 10%

*Malace, Kahn, WM, Keppel
PRL 104, 102001 (2010)*



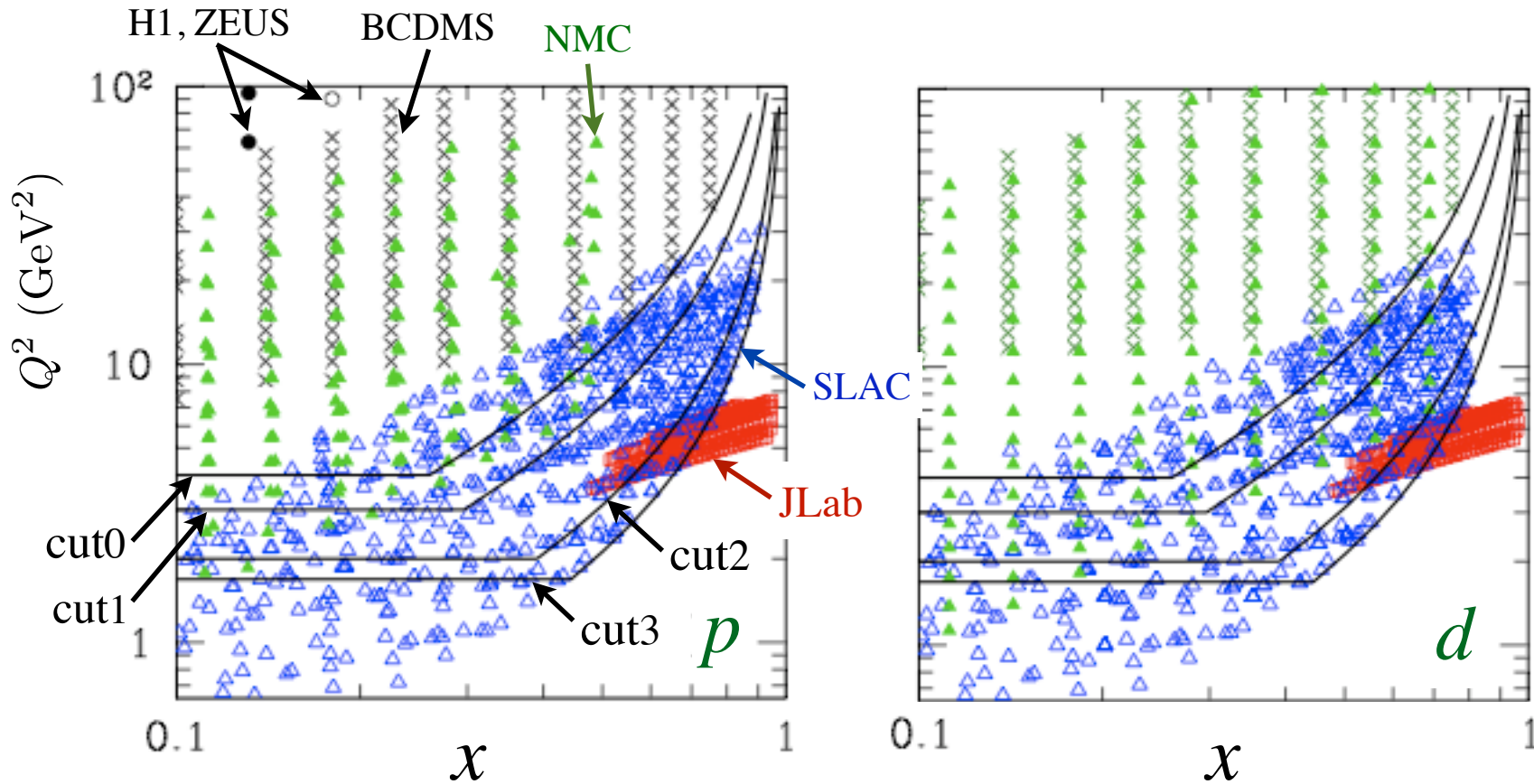
use resonance region data to learn about *leading twist* structure functions?

CTEQ-JLab (CJ) global PDF analysis *

- New global NLO analysis of expanded set of p and d data (DIS, pp , pd) including large- x , low- Q^2 region
- Systematically study effects of Q^2 & W cuts
→ down to $Q \sim m_c$ and $W \sim 1.7$ GeV
- Correct for *nuclear* effects in the deuteron, subleading $1/Q^2$ corrections (target mass, higher-twists)
- Dependence on choice of PDF parametrization

* CJ collaboration: A. Accardi, J. Owens, WM (theory)
E. Christy, C. Keppel, P. Monaghan, L. Zhu (expt.)
<http://www.jlab.org/CJ/>

CJ kinematic cuts



cut0: $Q^2 > 4 \text{ GeV}^2, W^2 > 12.25 \text{ GeV}^2$

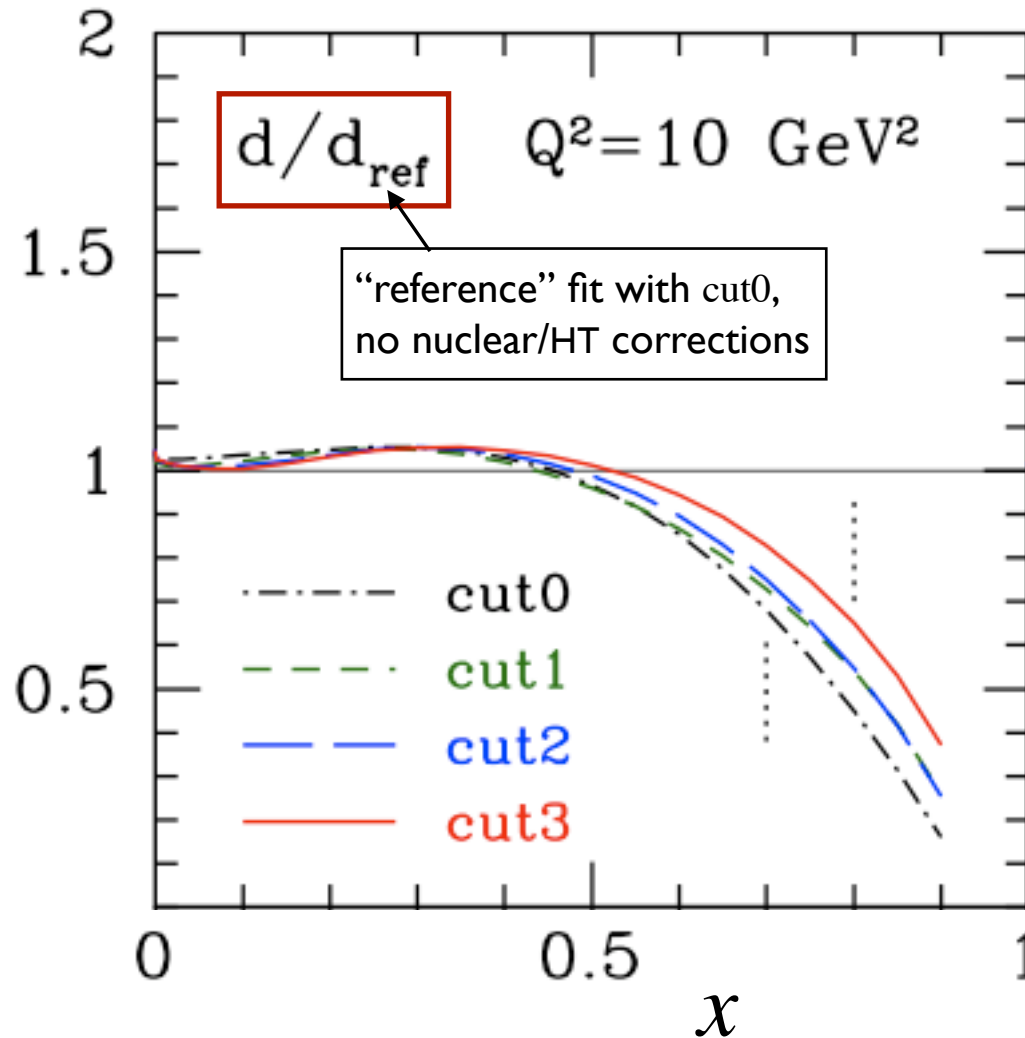
cut1: $Q^2 > 3 \text{ GeV}^2, W^2 > 8 \text{ GeV}^2$

cut2: $Q^2 > 2 \text{ GeV}^2, W^2 > 4 \text{ GeV}^2$

cut3: $Q^2 > m_c^2, W^2 > 3 \text{ GeV}^2$

factor 2 increase
 in DIS data from
 cut0 \rightarrow cut3

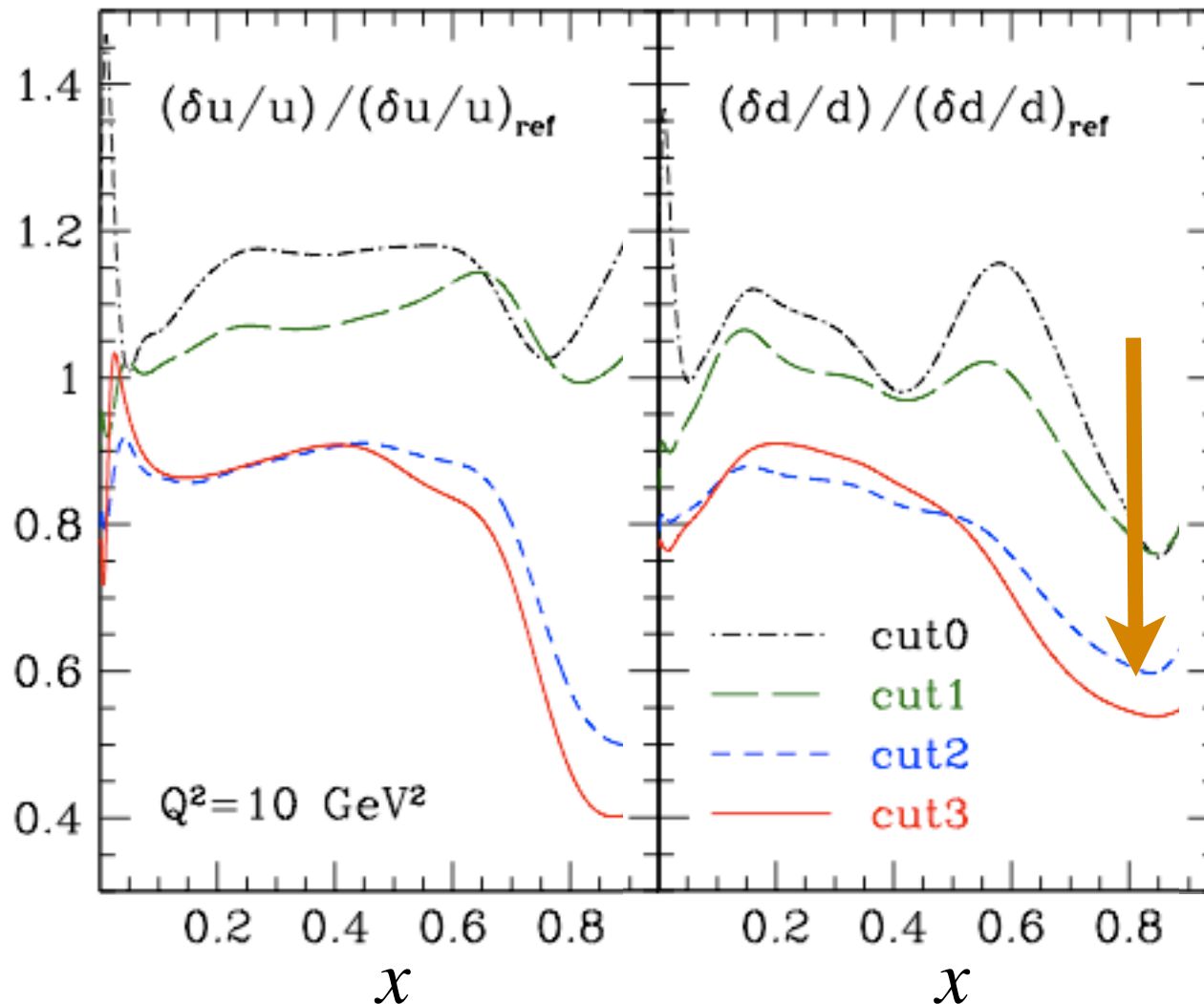
- PDFs remarkably *stable* with respect to cut reduction, as long as finite- Q^2 corrections included



Accardi et al.
PRD 81, 034016 (2010)

→ d quark behavior driven by nuclear corrections at high x

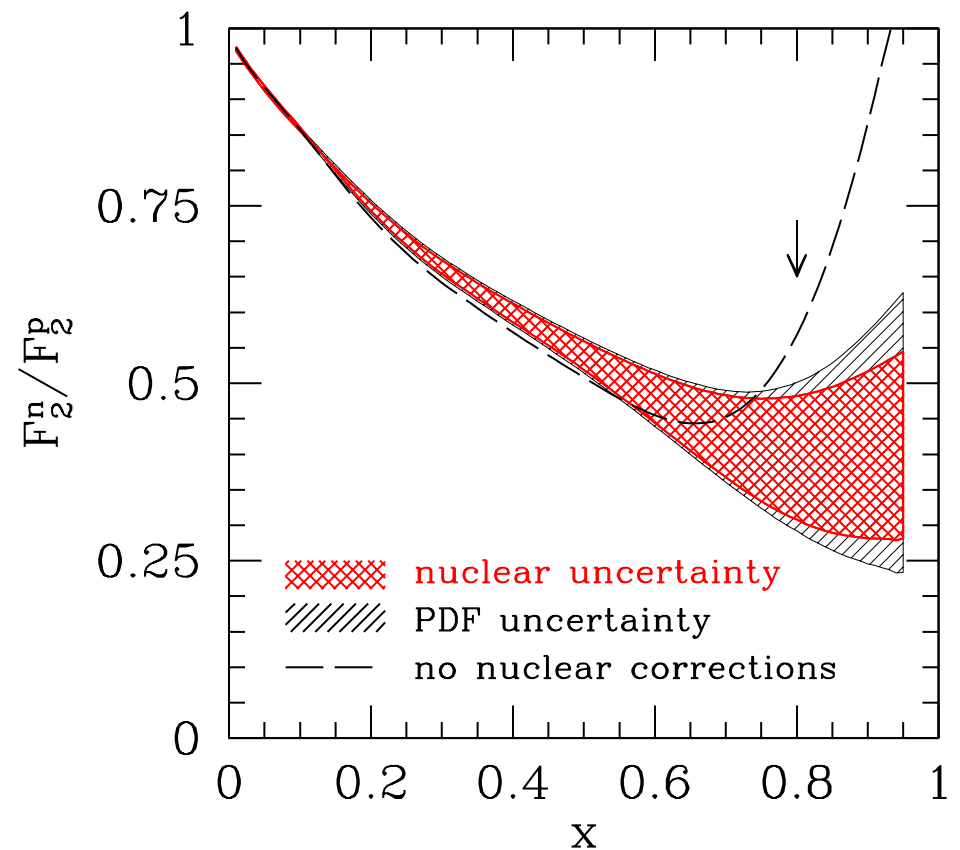
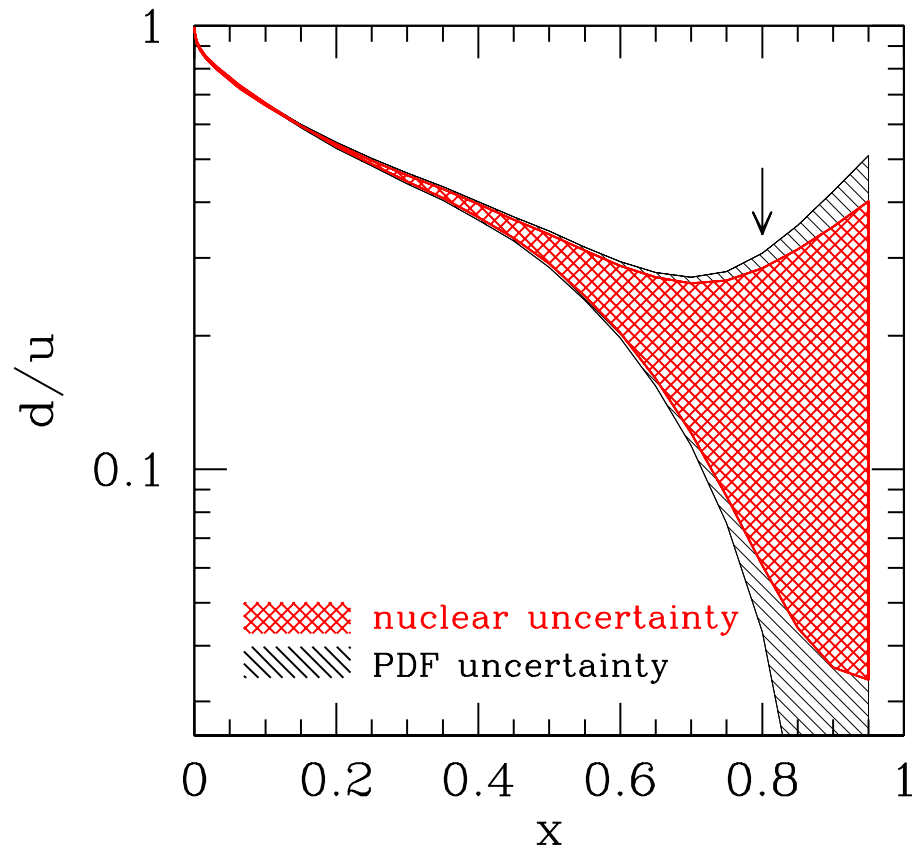
- Larger database with weaker cuts leads to significantly reduced errors, especially at large x



Accardi et al.
PRD 81, 034016 (2010)

→ up to 40–60% error reduction when cuts extended into resonance region

- Vital for large- x analysis, which currently suffers from large uncertainties (mostly due to nuclear corrections)



Accardi et al., PRD 84, 014008 (2011)

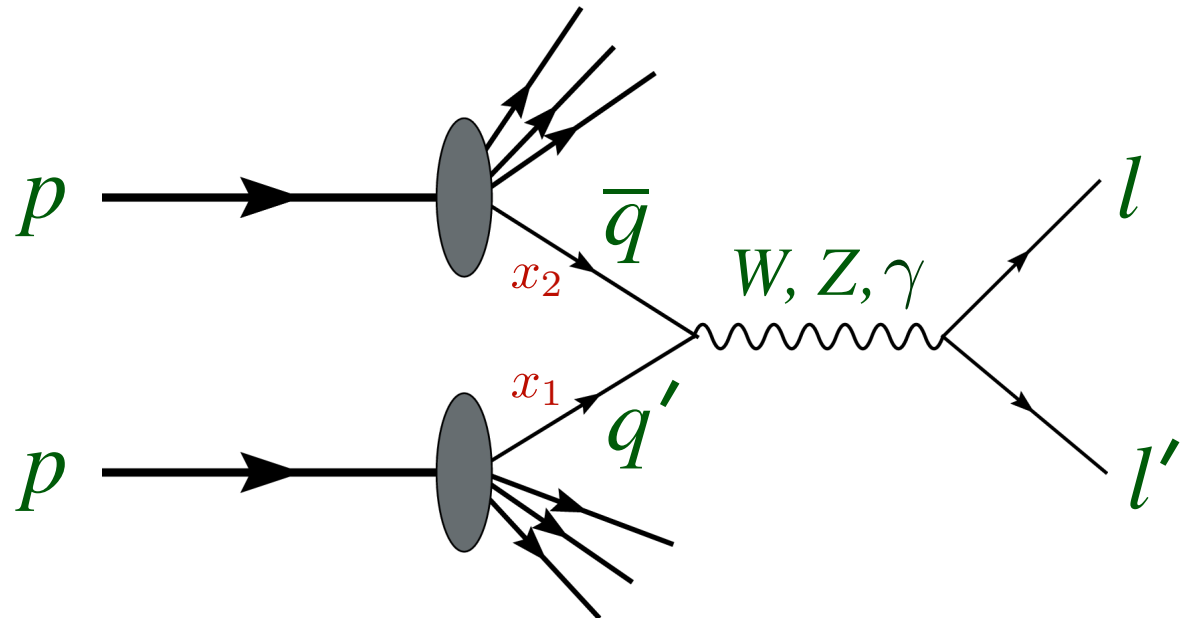
→ uncertainty in d feeds into larger uncertainty in g at high x (important for LHC physics!)

Brady et al., arXiv:1110.5398

Large Hadron Collider (CERN)



pp collisions
at $\sqrt{s} = 7$ TeV



Heavy Z' , W' boson production

- Some extensions of Standard Model predict heavy versions of W , Z bosons

→ Sequential Standard Model (SSM)
(assume same couplings as SM W , Z bosons)

→ Grand Unified Theories *e.g.* E_6 *London, Rosner (1986)*

$$E_6 \rightarrow SO(10) \times U(1)_\chi \rightarrow SU(5) \times U(1)_\psi \times U(1)_\chi$$

→ more exotic scenarios, *e.g.*

- scalar excitations in R -parity violating supersymmetric models

Hewett, Rizzo (1998)

- spin-1 Kaluza-Klein excitations of SM bosons in presence of extra dimensions

Antoniadis (1990)

- spin-2 excitations of the graviton

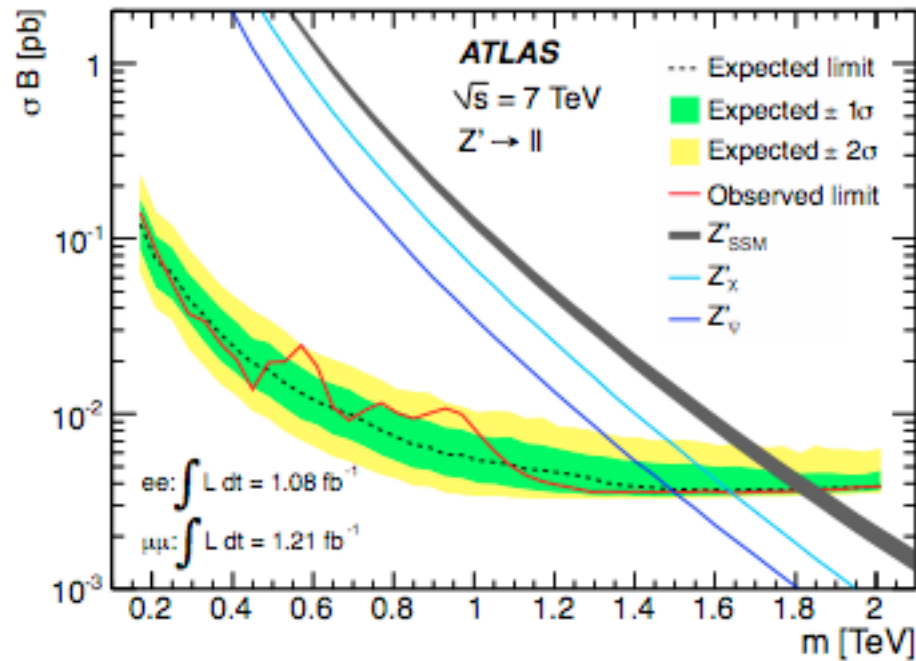
Randall, Sundrum (1999)

Heavy Z' , W' boson production

- Current limits on masses (for SSM; lower for other models)

→ $M_{Z'} > 1.83 \text{ TeV}$

$M_{W'} > 2.15 \text{ TeV}$ ATLAS @ LHC



arXiv:1108.1582 [hep-ex]

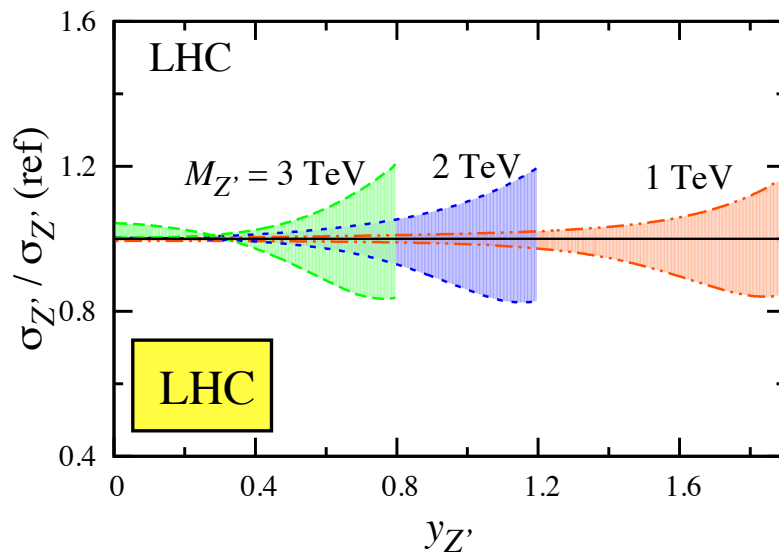
Heavy Z' , W' boson production

- Observation of new physics signals requires accurate determination of QCD backgrounds — depend on PDFs!
(since $x_{1,2} \sim M_{Z',W'}$, large- x uncertainties scale with mass)

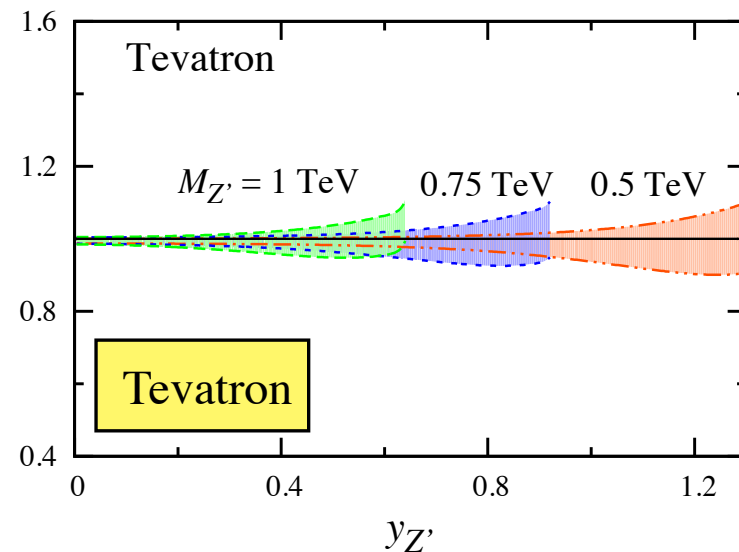
- for Z' production

couplings similar for u and d

$$\frac{d\sigma^{pp}}{dy} \sim \sum_q \left[(g_V^q)^2 + (g_A^q)^2 \right] \left(q(x_1)\bar{q}(x_2) + \bar{q}(x_1)q(x_2) \right)$$



→ dominated by $u * \bar{u}$
– rel. small uncertainties

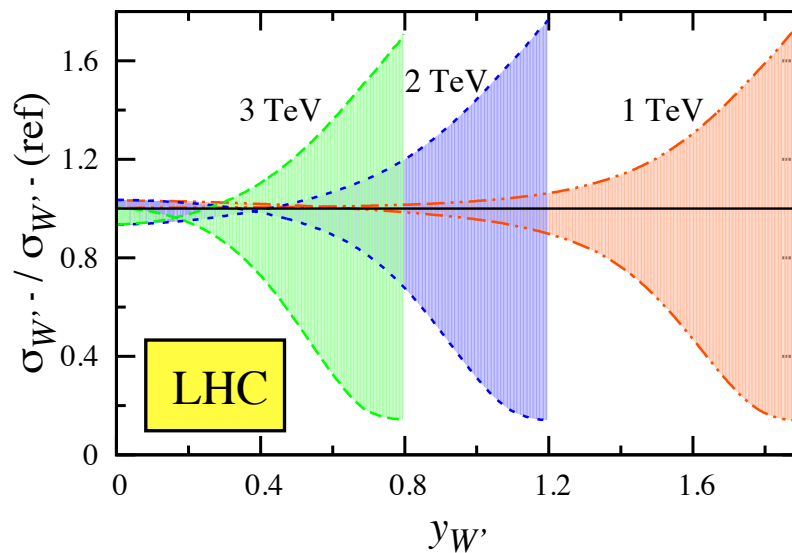


→ dominated by $u * u$
– well constrained

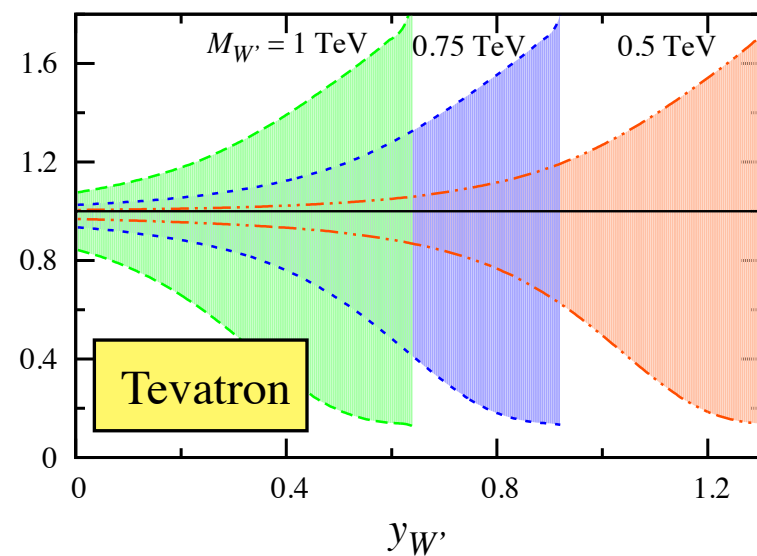
Heavy Z' , W' boson production

- Observation of new physics signals requires accurate determination of QCD backgrounds — depend on PDFs!
(since $x_{1,2} \sim M_{Z',W'}$, large- x uncertainties scale with mass!)

- for W'^- production



→ dominated by $d * \bar{u}$



→ dominated by $d * u + u * d$

> 100% uncertainties at large y !

Summary

- Remarkable confirmation of quark-hadron duality in *proton* and *neutron* structure functions
 - duality-violating higher twists $\sim 10\text{--}15\%$ in few-GeV range
- Confirmation of duality in *neutron* suggests origin in dynamical cancellations of higher twists
 - duality *not* due to accidental cancellations of quark charges
- Practical application of duality
 - use resonance region data to constrain *leading twist* PDFs (global PDF analysis underway)
 - stable fits at low Q^2 and large x with significantly reduced uncertainties

The End