



New parton distributions from high- x data: implications for JLab to the LHC

Wally Melnitchouk



Outline

- Why are large- x quarks in the nucleon important (and problematic)?
 - d/u PDF ratio, neutron structure & nuclear corrections
- New global “CJ” (CTEQ–Jefferson Lab) analysis
 - first serious foray into high- x , low- Q^2 region
 - implications of PDF uncertainties for LHC physics
- Outlook

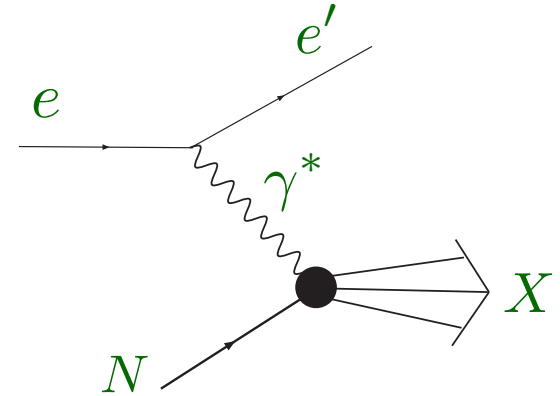
Electron scattering & structure functions

■ Inclusive cross section for $e N \rightarrow e X$

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{4\alpha^2 E'^2 \cos^2 \frac{\theta}{2}}{Q^4} \left(2 \tan^2 \frac{\theta}{2} \frac{F_1}{2M} + \frac{F_2}{\nu} \right)$$

$$\left. \begin{aligned} \nu &= E - E' \\ Q^2 &= \vec{q}^2 - \nu^2 = 4EE' \sin^2 \frac{\theta}{2} \end{aligned} \right\} x = \frac{Q^2}{2M\nu}$$

Bjorken scaling variable



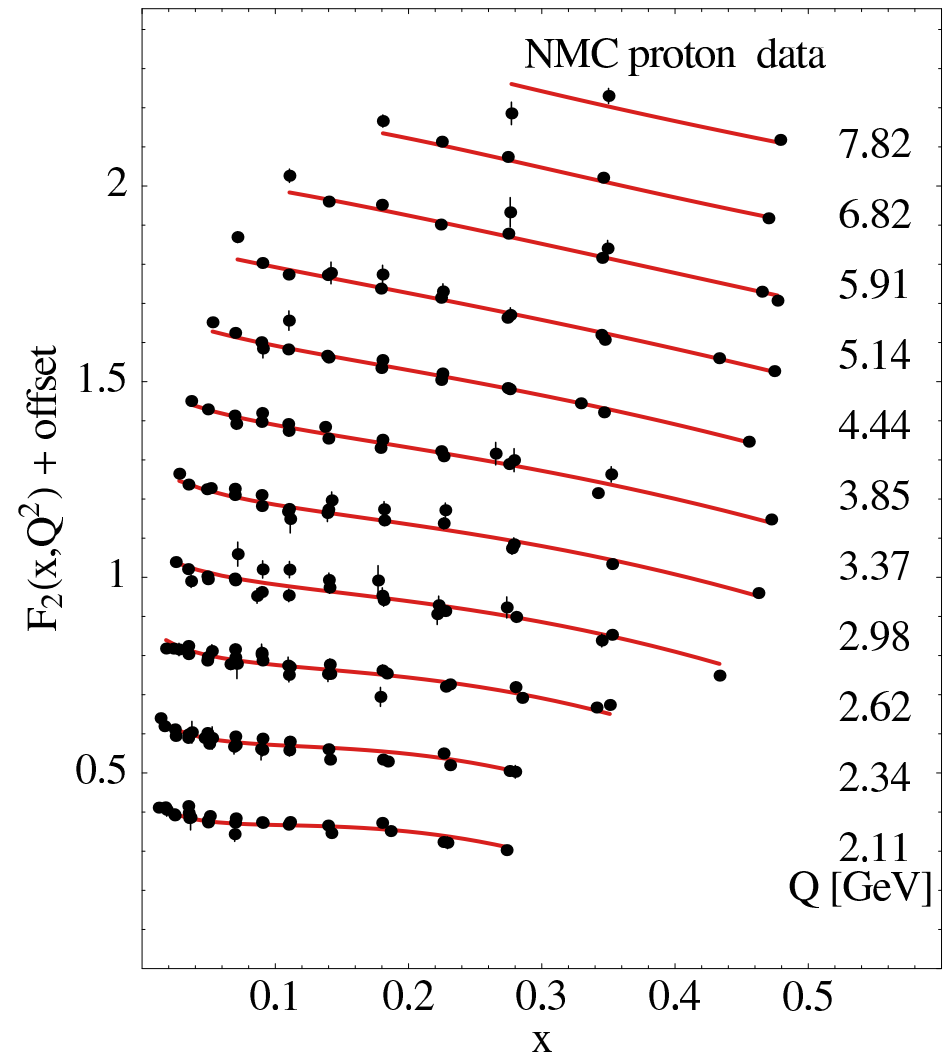
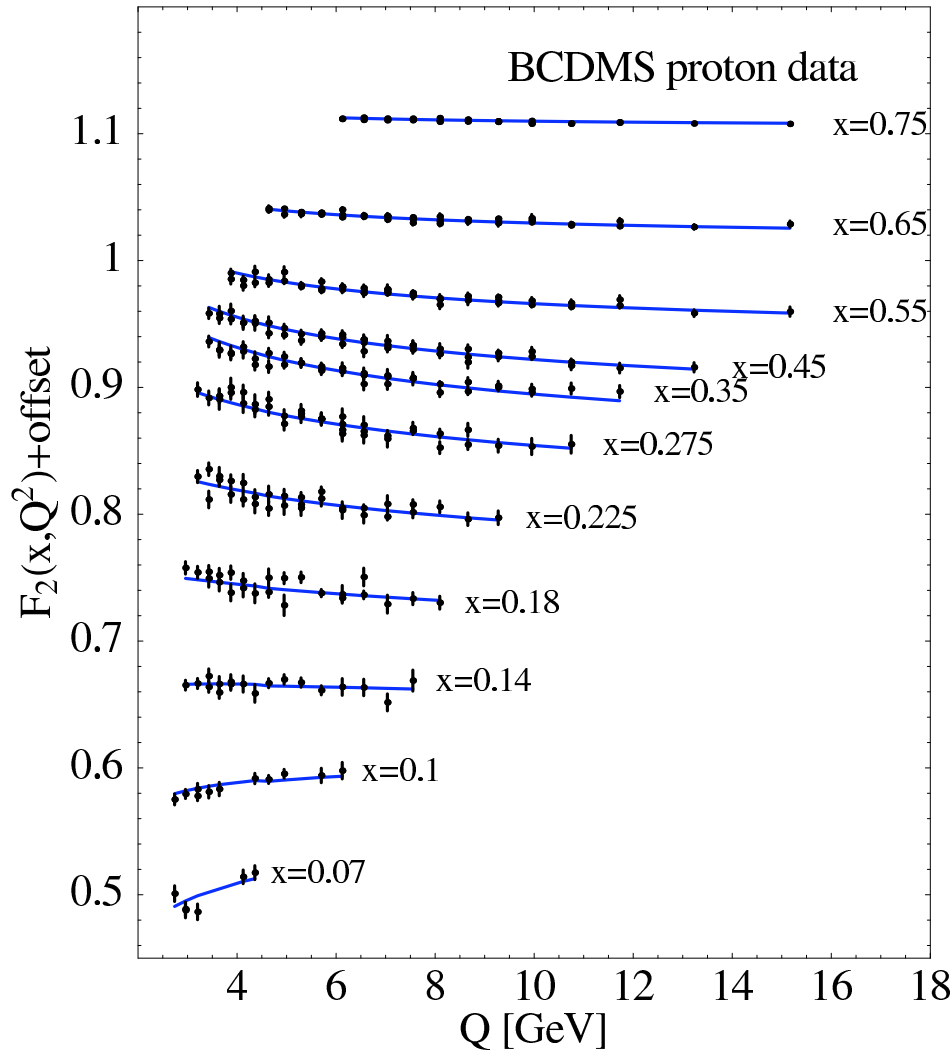
■ Structure functions F_1 , F_2

→ contain all information about structure of nucleon
e.g. at leading order (parton model)

$$F_2(x, Q^2) = x \sum_q e_q^2 q(x, Q^2) \quad (q=u, d, s, \dots)$$

$q(x, Q^2)$ = probability (in infinite momentum frame & light-cone gauge)
 to find quark q with (light-cone) momentum fraction x

Electron scattering & structure functions



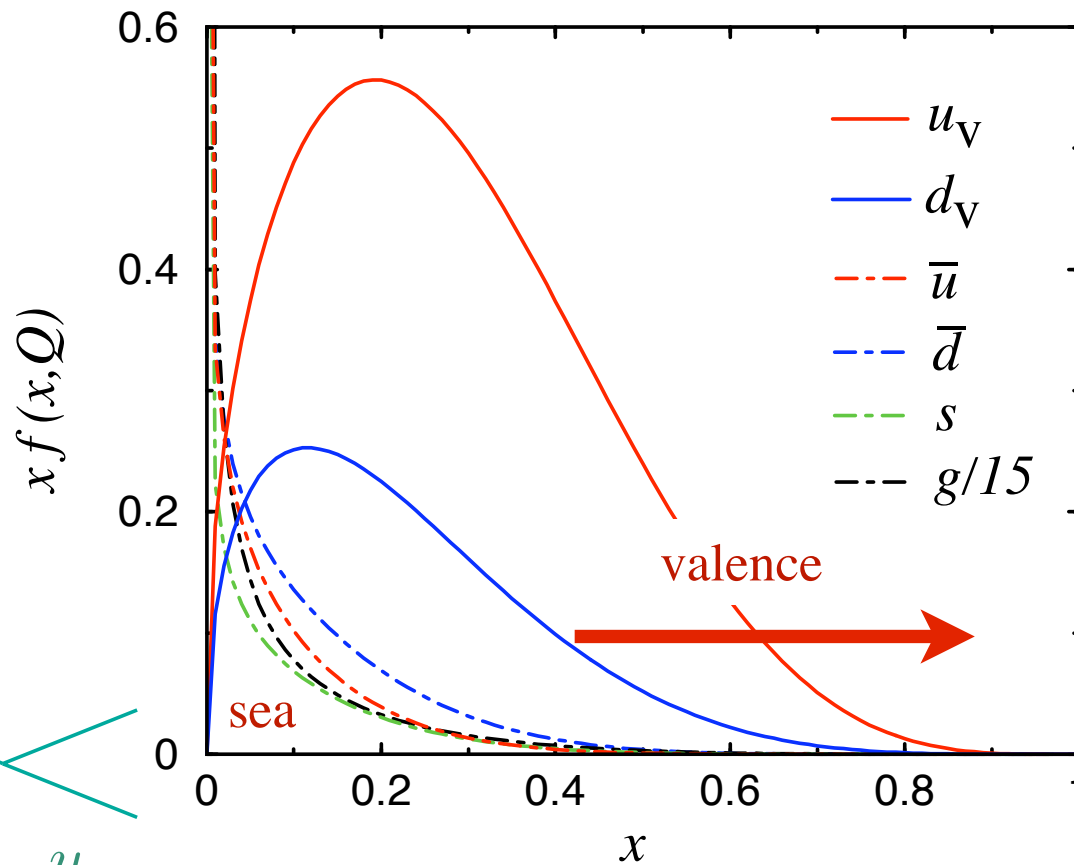
Lai et al., EPJC 12 (2000) 375

→ predicted $\log Q^2$ scaling violations confirmed experimentally
(important early confirmation of QCD!)

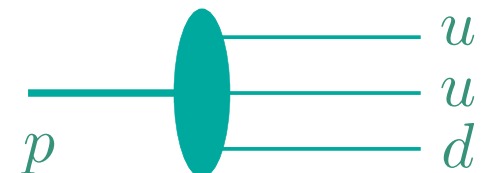
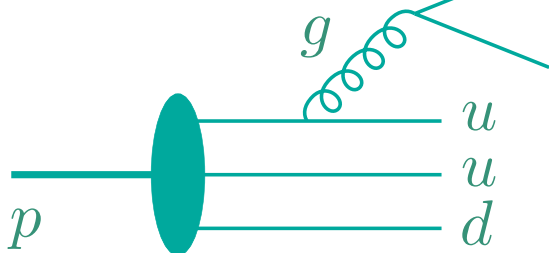
Why are PDFs at *large* x important?

Large- x PDFs

- Most direct connection between quark distributions and models of nucleon structure is via *valence* quarks
 - most cleanly revealed at $x > 0.4$



structure of *hadron*
or structure of *probe*?



Large- x PDFs

- Most direct connection between quark distributions and models of nucleon structure is via *valence* quarks

→ most cleanly revealed at $x > 0.4$

$$F_2^p \approx \frac{4}{9}xu_v + \frac{1}{9}xd_v$$

$$F_2^n \approx \frac{1}{9}xu_v + \frac{4}{9}xu_v$$

- Needed to understand backgrounds in searches for physics *beyond the Standard Model* in high-energy colliders *e.g.* the LHC

→ Q^2 evolution feeds *high x , low Q^2* to *low x , high Q^2* where *e.g.* Higgs, SUSY most likely to produce signals

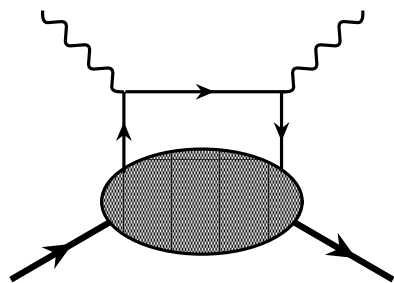
Large- x PDFs

- Ratio of d to u quark distributions particularly sensitive to quark dynamics in nucleon
- SU(6) spin-flavor symmetry

proton wave function

$$\begin{aligned}
 p^\uparrow = & -\frac{1}{3}d^\uparrow(uu)_1 - \frac{\sqrt{2}}{3}d^\downarrow(uu)_1 \\
 & + \frac{\sqrt{2}}{6}u^\uparrow(ud)_1 - \frac{1}{3}u^\downarrow(ud)_1 + \frac{1}{\sqrt{2}}u^\uparrow(ud)_0
 \end{aligned}$$

50%	$S=0$	(qq)
50%	$S=1$	(qq)



interacting
quark

spectator
"diquark"

diquark spin

Large- x PDFs

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- SU(6) spin-flavor symmetry

proton wave function

$$p^\uparrow = -\frac{1}{3}d^\uparrow(uu)_1 - \frac{\sqrt{2}}{3}d^\downarrow(uu)_1 + \frac{\sqrt{2}}{6}u^\uparrow(ud)_1 - \frac{1}{3}u^\downarrow(ud)_1 + \frac{1}{\sqrt{2}}u^\uparrow(ud)_0$$

50%	$S=0$	(qq)
50%	$S=1$	(qq)

→ $u(x) = 2 d(x)$ for all x

→ $\frac{F_2^n}{F_2^p} = \frac{2}{3}$

Large- x PDFs

- But SU(6) symmetry is broken

e.g. scalar diquark dominance

$M_{\Delta} > M_N \implies (qq)_1$ has larger energy than $(qq)_0$

\implies scalar diquark dominant in $x \rightarrow 1$ limit

since only u quarks couple to *scalar* diquarks

$$\longrightarrow \frac{d}{u} \rightarrow 0$$

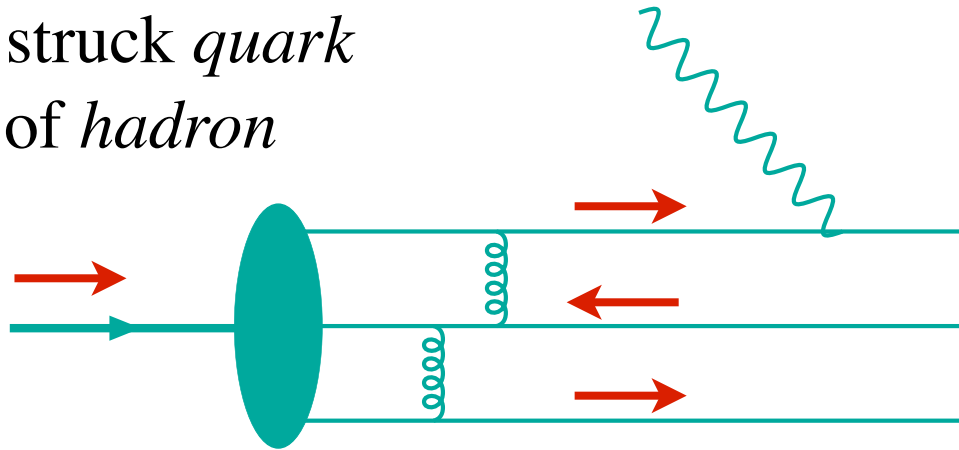
$$\longrightarrow \frac{F_2^n}{F_2^p} \rightarrow \frac{1}{4}$$

Feynman (1972), Close (1973), Close/Thomas (1988)

Large- x PDFs

- Alternatively, $SU(6)$ can be broken by hard gluon exchange

helicity of struck *quark*
= helicity of *hadron*



$$q^\uparrow \gg q^\downarrow$$

\implies helicity-zero diquark dominant in $x \rightarrow 1$ limit

$$\longrightarrow \frac{d}{u} \rightarrow \frac{1}{5}$$

$$\longrightarrow \frac{F_2^n}{F_2^p} \rightarrow \frac{3}{7}$$

Farrar/Jackson (1975)

Large- x PDFs

■ Nonperturbative & perturbative QCD predictions for d/u ratio in $x \rightarrow 1$ limit:

- $d/u \rightarrow 1/2$ SU(6) symmetry

- $d/u \rightarrow 0$ $S = 0$ qq dominance

- $d/u \rightarrow 1/5$ $S_z = 0$ qq dominance

- $d/u \rightarrow \frac{4 \mu_n^2 / \mu_p^2 - 1}{4 - \mu_n^2 / \mu_p^2}$ local quark-hadron duality*
($\mu_{p,n}$ magnetic moments)

see e.g. WM, Ent, Keppel
Phys. Rep. **406**, 127 (2005)

*structure function at $x \rightarrow 1$ given by
elastic form factor at $Q^2 \rightarrow \infty$

Large- x PDFs

- Nonperturbative & perturbative QCD predictions for $\Delta q/q$ ratio in $x \rightarrow 1$ limit:

- $\Delta u/u \rightarrow 2/3$
 $\Delta d/d \rightarrow -1/3$ SU(6) symmetry
- $\Delta u/u \rightarrow 1$
 $\Delta d/d \rightarrow -1/3$ $S = 0$ qq dominance
- $\Delta u/u \rightarrow 1$
 $\Delta d/d \rightarrow 1$ $S_z = 0$ qq dominance
or local duality

→ sign of d quark polarization is uncertain!

Deuteron corrections

- u quark distribution well determined from *proton* data
- d quark distribution requires *neutron* structure function

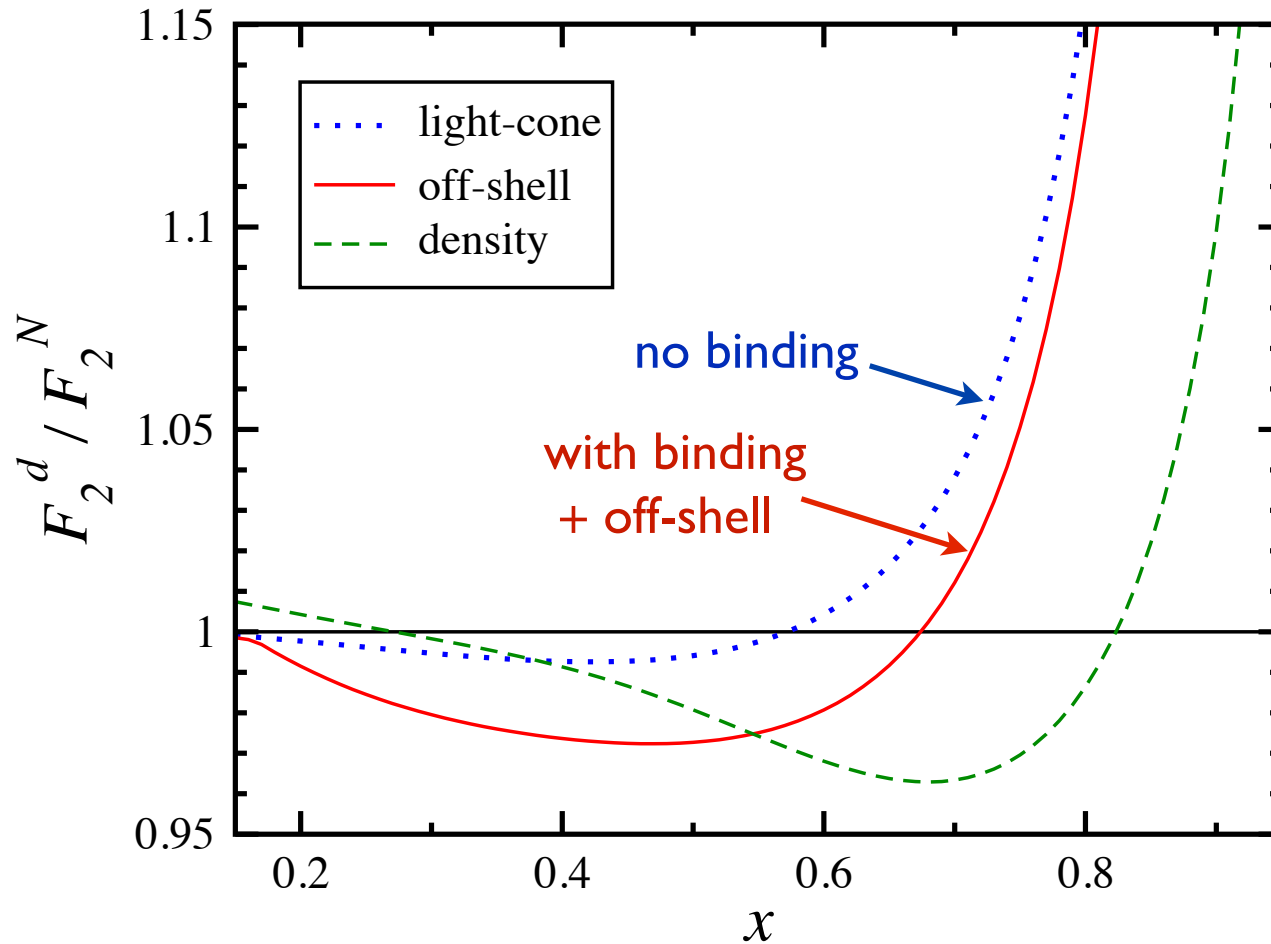
$$\longrightarrow \frac{d}{u} \approx \frac{4 - F_2^n / F_2^p}{4F_2^n / F_2^p - 1}$$

- Absence of free neutron targets

- use *deuterons* (weakly bound state of p and n)
- must account for nuclear effects in deuteron

$$F_2^d \neq F_2^p + F_2^n$$

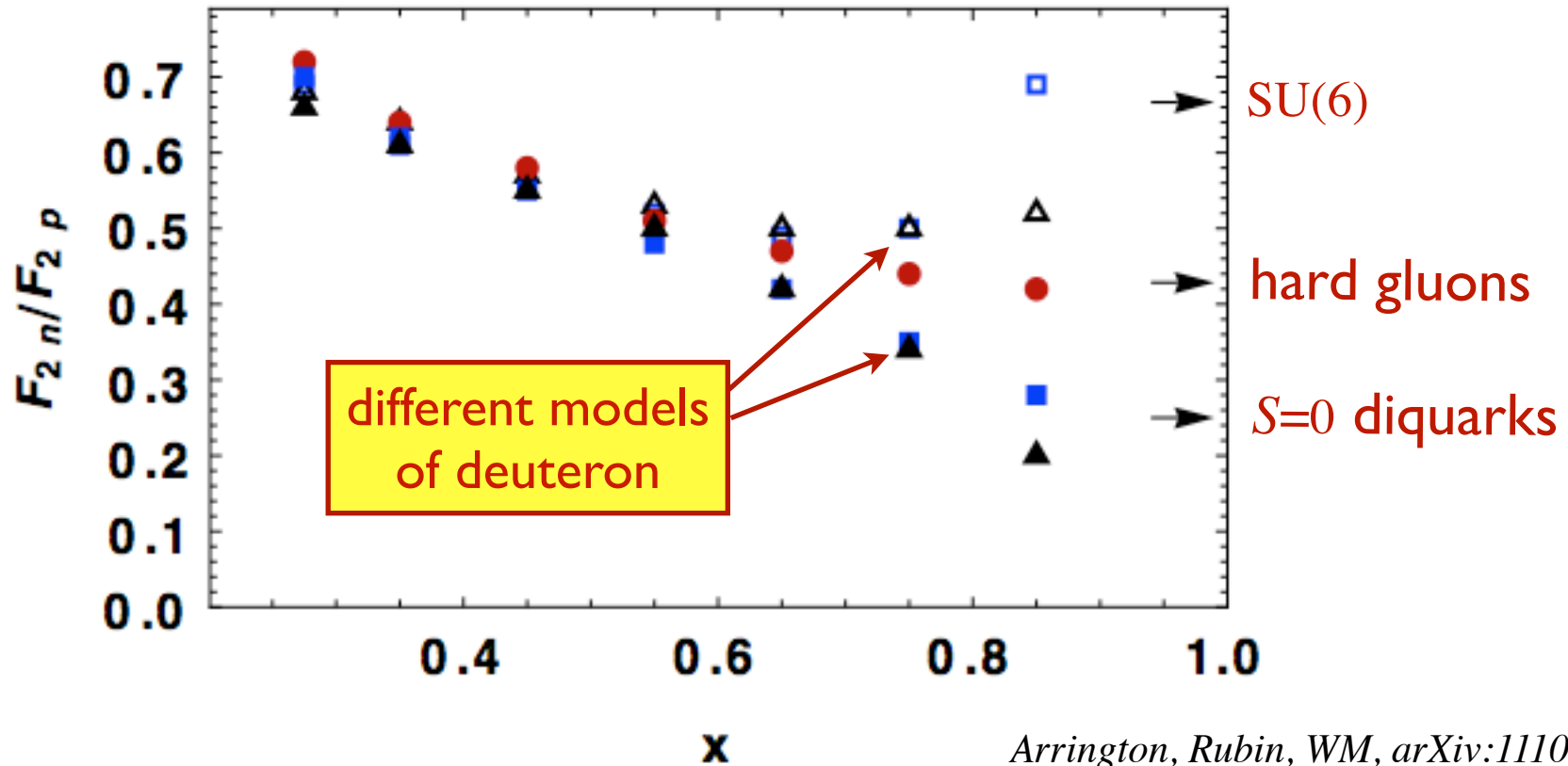
Deuteron corrections



*WM, Thomas
PLB 377, 11 (1996)*

- $\sim 2-3\%$ reduction of F_2^d / F_2^N at $x \sim 0.5-0.6$ with steep rise for $x > 0.6-0.7$
- larger EMC effect at $x \sim 0.5-0.6$ with binding + off-shell corrections *cf.* light-cone

Deuteron corrections



- significant deuteron model uncertainty at large x (short-range NN interaction)
- obscures free neutron structure information

New global PDF analysis: CTEQ-JLab (“CJ”) collaboration

A. Accardi, J. Owens, WM (theory)
E. Christy, C. Keppel, P. Monaghan, L. Zhu (expt.)

- Next-to-leading order (NLO) analysis of expanded set of *proton* and *deuterium* data, including large- x , low- Q^2 region
 - also include new CDF & D0 W -asymmetry, and E866 DY data
- Systematically study effects of Q^2 & W cuts
 - as low as $Q \sim m_c$ and $W \sim 1.7$ GeV
- Correct for *nuclear* effects in the deuteron (binding + off-shell)
 - most global analyses assume *free* nucleons; some use density model, a few assume Fermi motion only
- Include subleading $1/Q^2$ corrections
 - target mass corrections & dynamical higher twists
- Dependence on choice of PDF parametrization

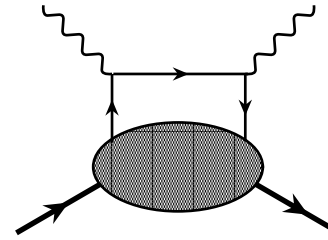
Higher twists

■ $1/Q^2$ expansion of structure function moments

$$M_n(Q^2) = \int_0^1 dx x^{n-2} F_2(x, Q^2) = A_n^{(2)} + \frac{A_n^{(4)}}{Q^2} + \frac{A_n^{(6)}}{Q^4} + \dots$$

matrix elements of operators with specific “twist” (= dimension – spin)

→ twist = 2 corresponds to single-quark scattering



e.g. $\bar{\psi} \gamma_\mu \psi$

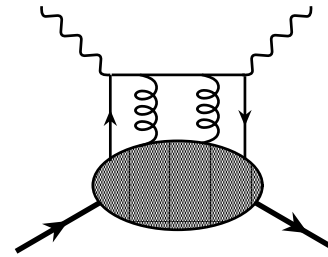
Higher twists

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matrix elements of operators with specific “twist” (= dimension – spin)

→ twist > 2 reveals long-range multi-parton correlations



e.g. $\bar{\psi} \tilde{F}_{\mu\nu} \gamma_\nu \psi$

- Phenomenologically important at large x and low Q^2

→ parametrize x dependence by

$$F_2(x, Q^2) = F_2^{\text{LT}}(x, Q^2) \left(1 + \frac{C(x)}{Q^2} \right)$$

Target mass corrections

■ Kinematical corrections arising from derivative operators

e.g. $\bar{\psi} \gamma_\mu D_{\mu_1} \cdots D_{\mu_n} \psi \rightarrow \text{twist} = 2!$

→ give rise to corrections $\sim Q^2/\nu^2 = 4M^2x^2/Q^2$
(hence “target mass”)

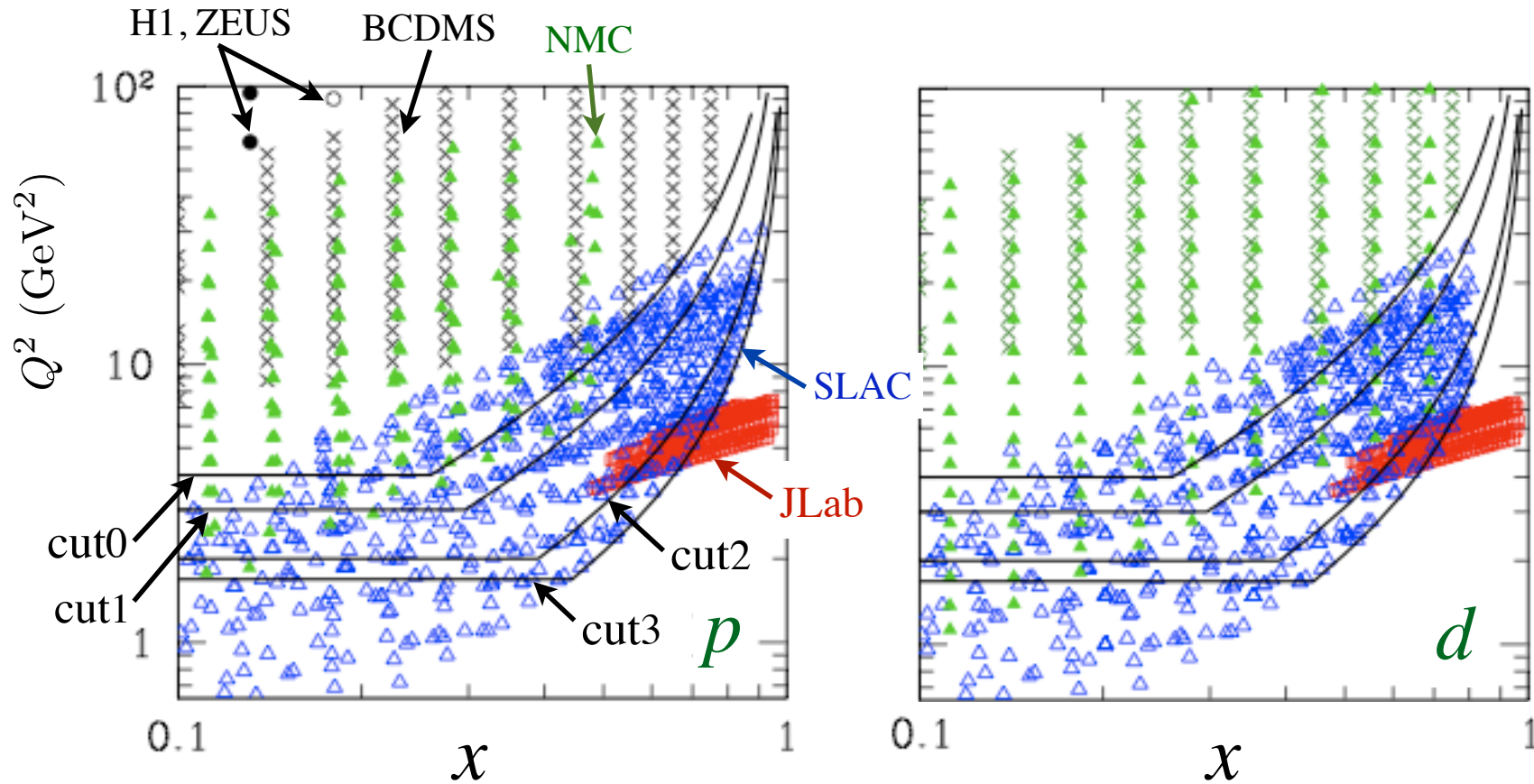
→ target mass corrected structure function

$$F_2^{\text{TMC}}(x, Q^2) = \frac{x^2}{\xi^2 \gamma^3} F_2^{(0)}(\xi, Q^2) + \frac{6M^2 x^3}{Q^2 \gamma^4} \int_\xi^1 du \frac{F_2^{(0)}(u, Q^2)}{u^2} \\ + \frac{12M^4 x^4}{Q^4 \gamma^5} \int_\xi^1 dv (v - \xi) \frac{F_2^{(0)}(v, Q^2)}{v^2}$$

● $F_2^{(0)}$ = structure function in massless (Bjorken) limit

● new “Nachtmann” scaling variable $\xi = \frac{2x}{1 + \sqrt{1 + 4M^2x^2/Q^2}}$

Kinematic cuts



cut0: $Q^2 > 4 \text{ GeV}^2$, $W^2 > 12.25 \text{ GeV}^2$

cut1: $Q^2 > 3 \text{ GeV}^2$, $W^2 > 8 \text{ GeV}^2$

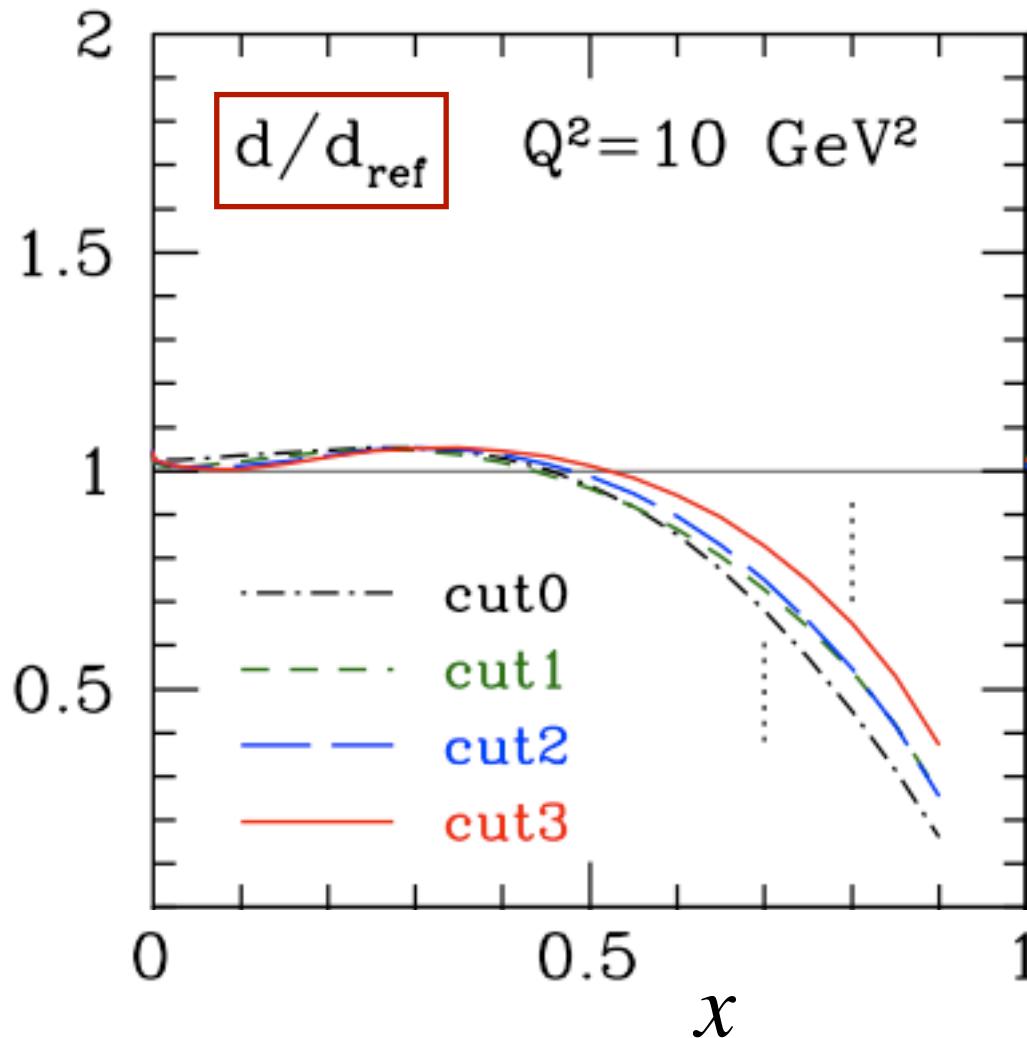
cut2: $Q^2 > 2 \text{ GeV}^2$, $W^2 > 4 \text{ GeV}^2$

cut3: $Q^2 > m_c^2$, $W^2 > 3 \text{ GeV}^2$

factor 2 increase
in DIS data from
cut0 \rightarrow cut3

Kinematic cuts

- Systematically reduce Q^2 & W cuts
- Fit includes TMCs, HT term, nuclear corrections

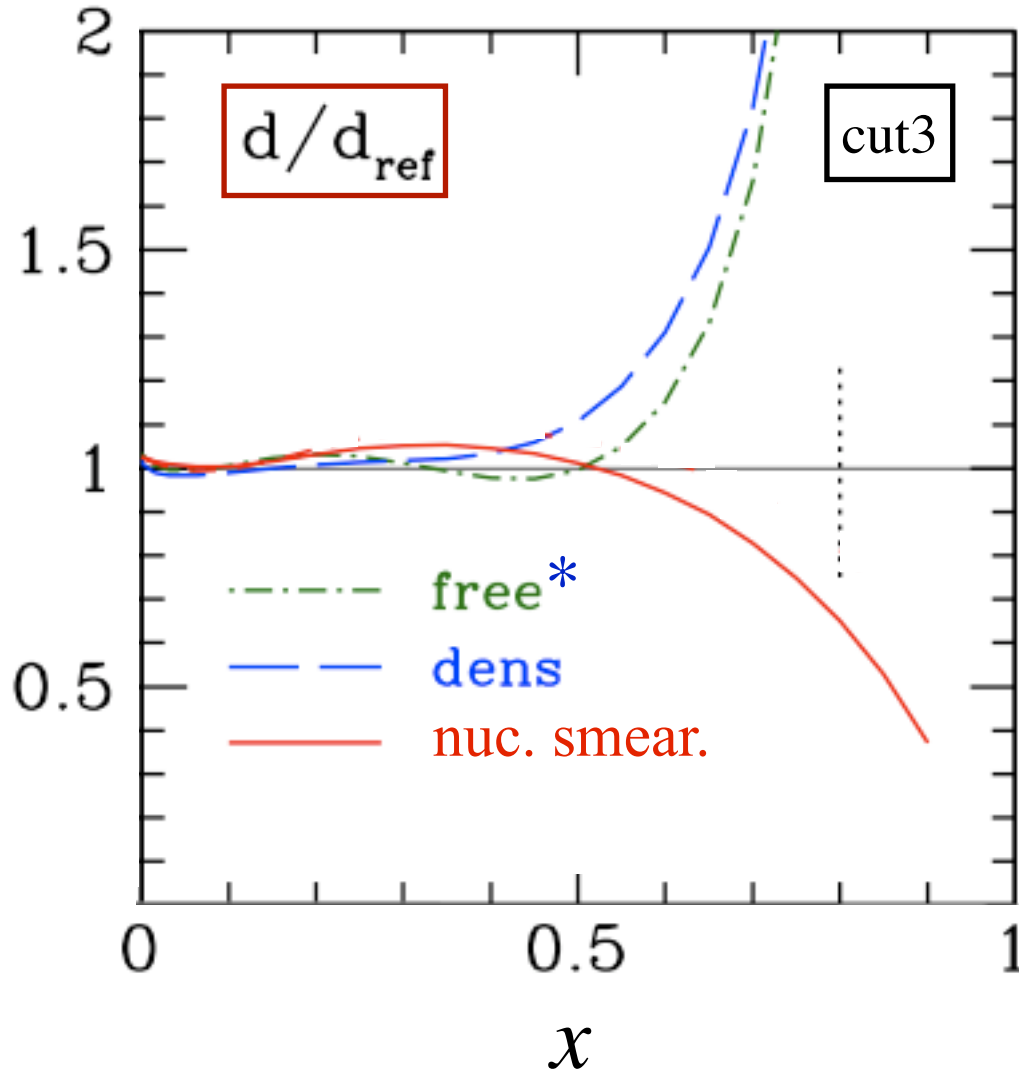


→ *stable* with respect to cut reduction

→ d quark suppressed by $\sim 50\%$ for $x > 0.5$ (driven by nuclear corrections)

Accardi et al., PRD 81, 034016 (2010)

Nuclear corrections



* assumes $F_2^d = F_2^p + F_2^n$ as in CTEQ6.1 and most other global fits

→ increased d quark for no nuclear effects
(compensates for nuclear smearing in deuteron → increased F_2^d)

→ decreased d quark for nuclear smearing models

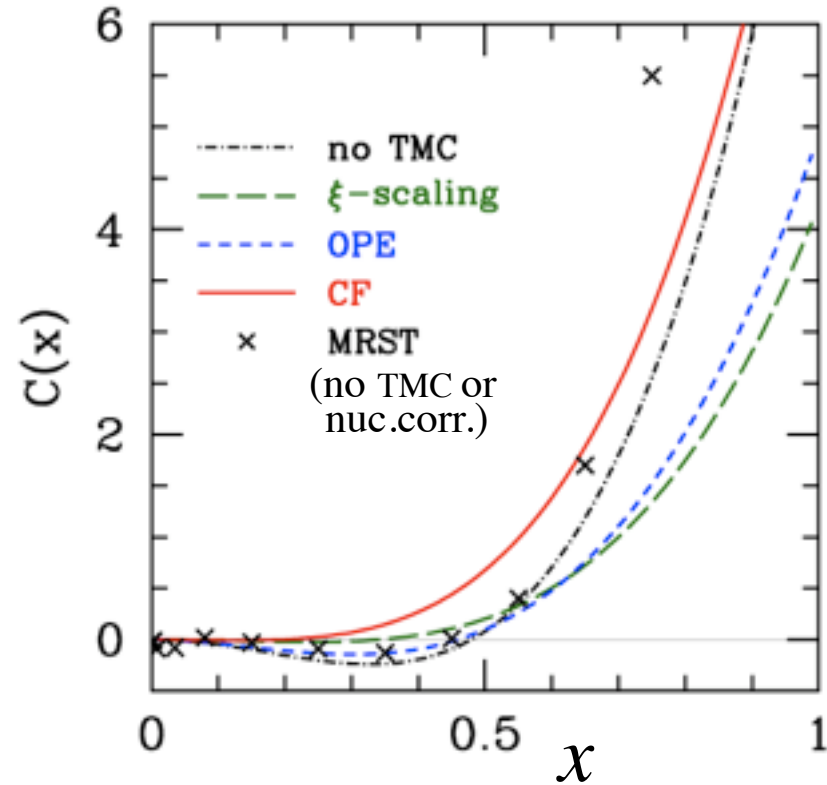
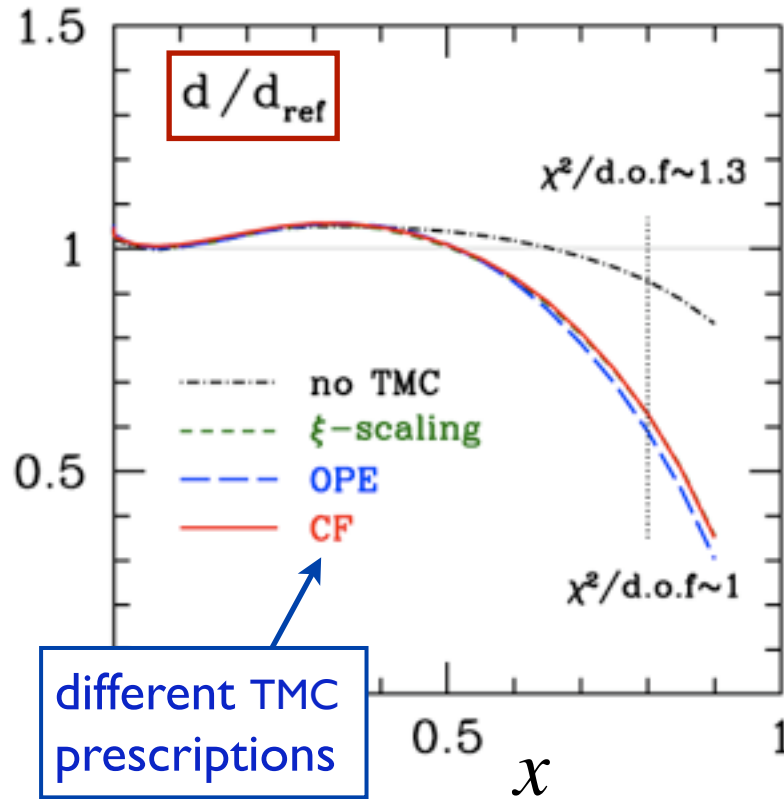


$F_2^d / F_2^N > 1$ for $x \sim 0.6-0.8$
while $F_2^d / F_2^N < 1$ for “free” and “density” models

$$F_2^d / F_2^N \uparrow \longleftrightarrow F_2^n / F_2^p \downarrow$$

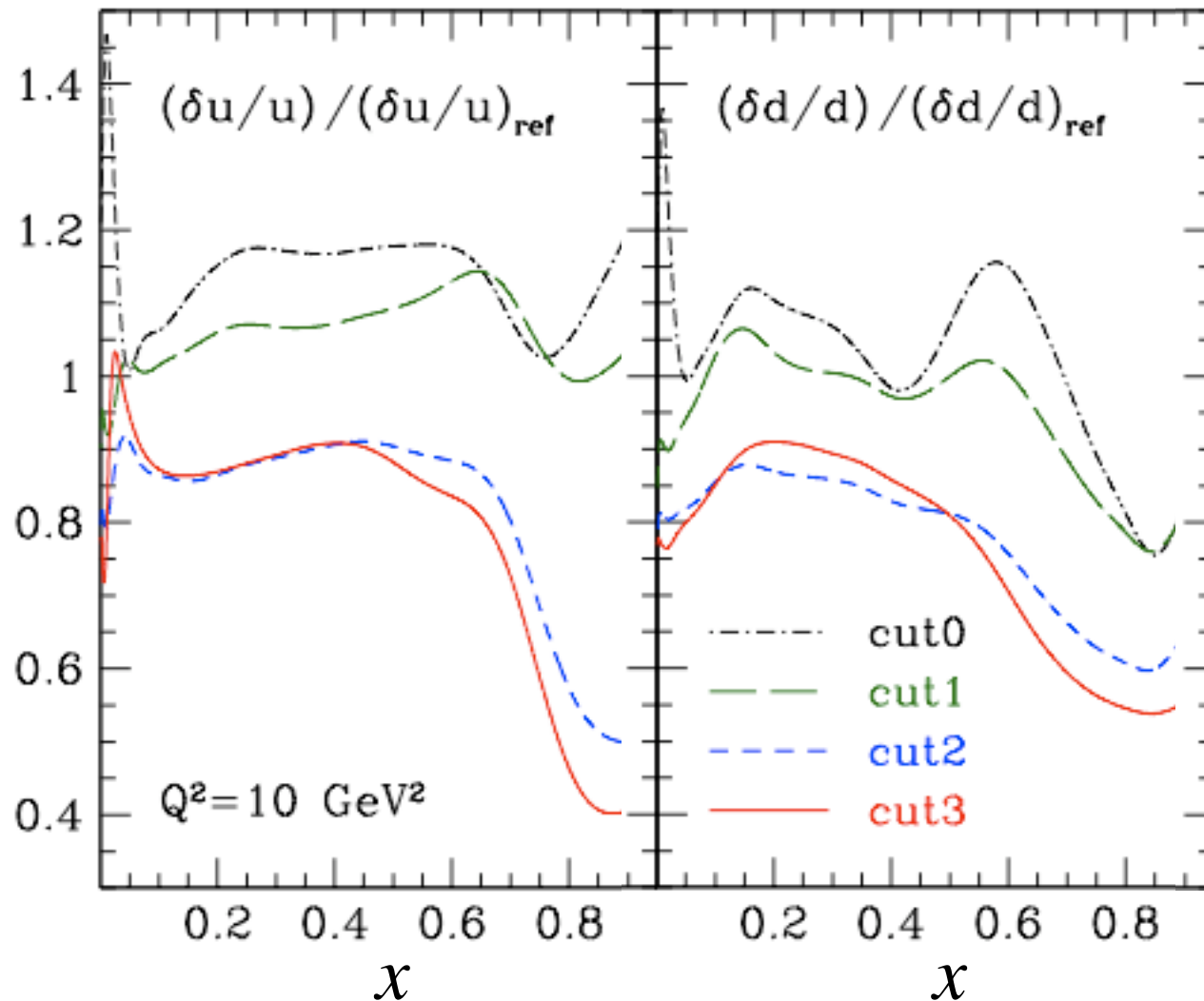
$$\longleftrightarrow d/u \downarrow$$

Effect of $1/Q^2$ corrections



- $1/Q^2$ correction $F_2 = F_2^{\text{LT}} \left(1 + \frac{C(x)}{Q^2} \right)$, $C(x) = c_1 x^{c_2} (1 + c_3 x)$
- important interplay between TMCs and higher twist: HT alone *cannot* accommodate full Q^2 dependence
- stable leading twist when both TMCs and HTs included

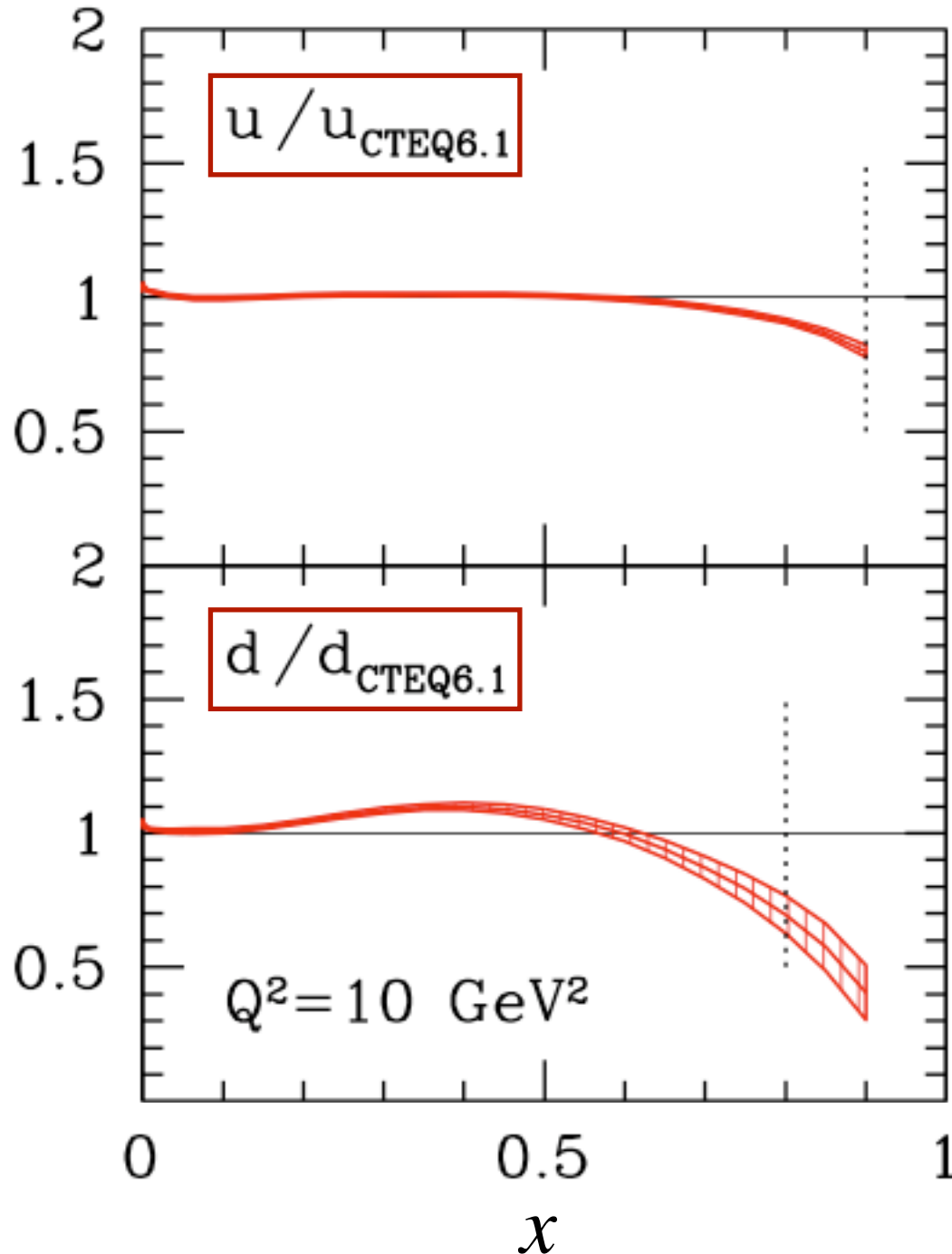
CJ10 PDF results



Accardi et al.
PRD 81, 034016 (2010)

→ larger database with weaker cuts leads to significantly *reduced errors*, esp. at large x

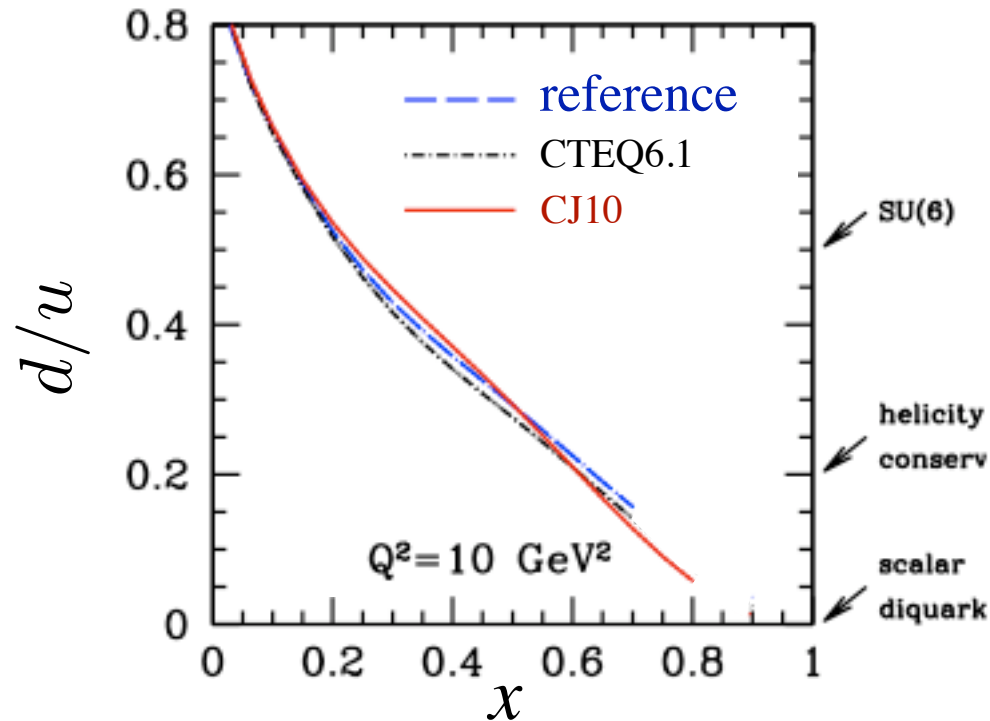
CJ10 PDF results



→ full fit appears to favor smaller d/u ratio

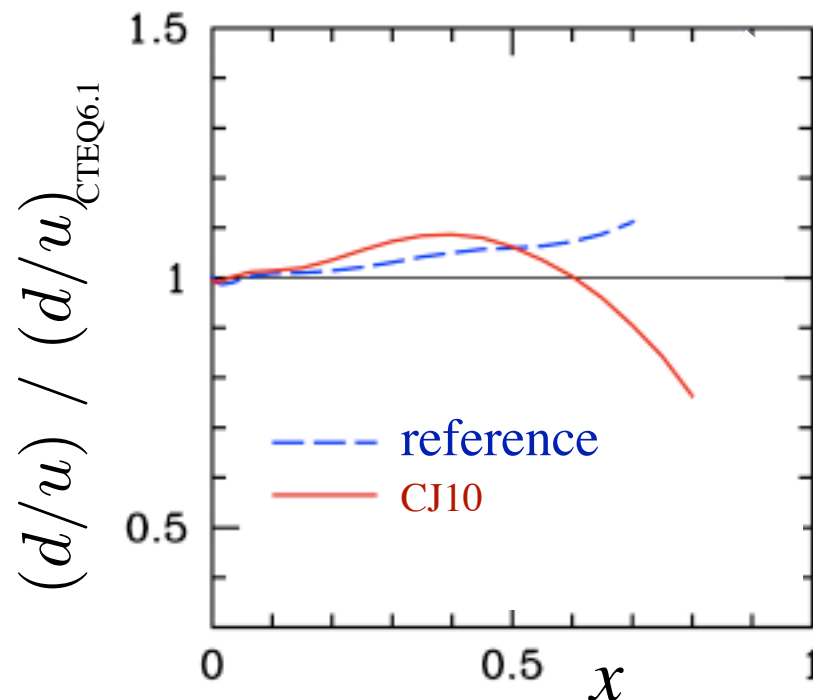
Accardi et al., PRD 81, 034016 (2010)

CJ10 PDF results



→ full fit appears to favor smaller d/u ratio

→ dominance of non-pQCD physics (*cf.* hard g exchange)?



→ how robust is this result?

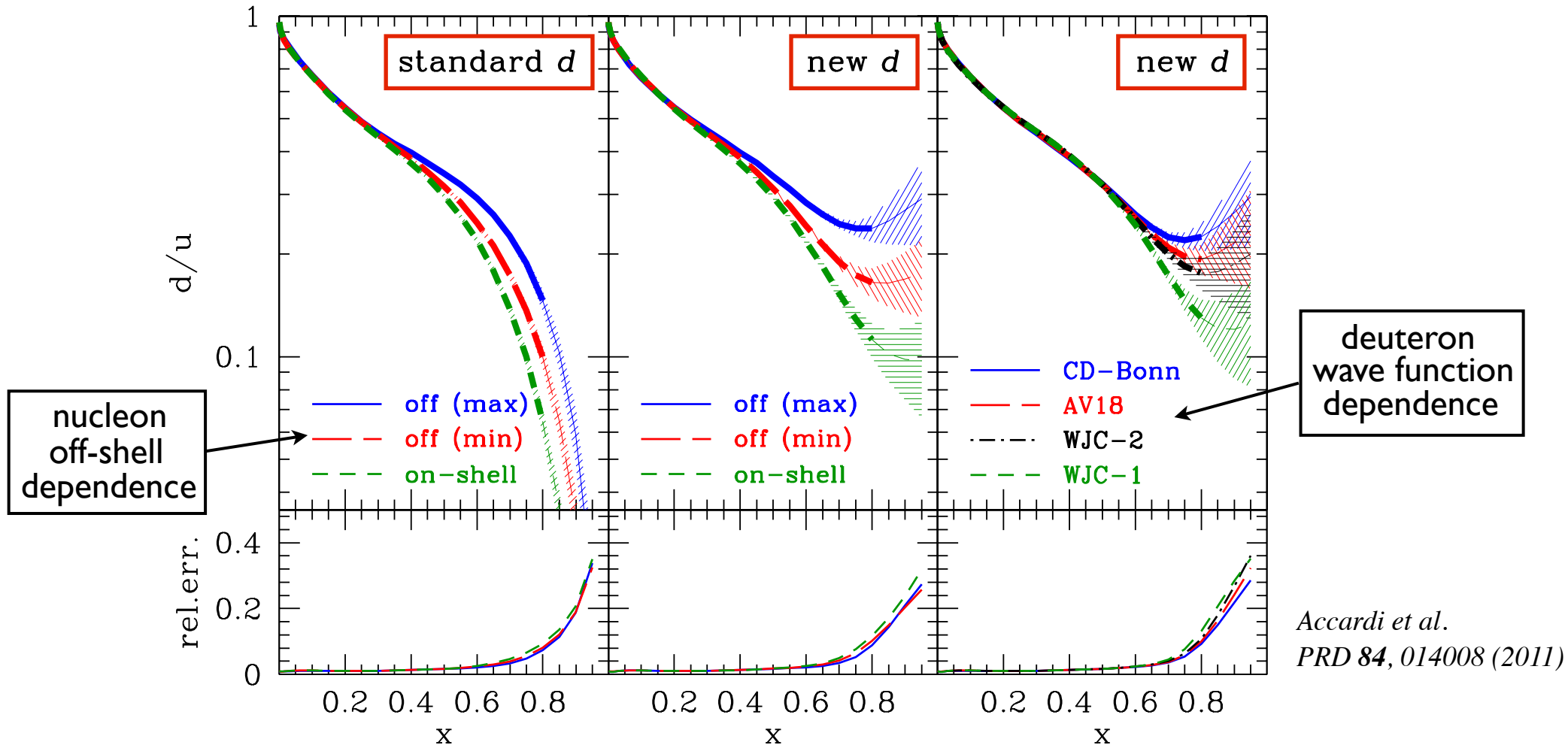
Accardi et al., PRD 81, 034016 (2010)

New CJ11 PDF analysis

- Explore dependence of PDF fits on deuteron wave functions and nucleon off-shell corrections
 - use only “high-precision” wave functions (AV18, CD-Bonn, WJC-1, WJC-2)
 - model nucleon off-shell correction with reasonable range of parameters
- Dependence of d/u ratio on choice of parametrization
 - allow for finite, nonzero ratio in $x = 1$ limit

$$d(x, Q^2) \rightarrow d(x, Q^2) + a x^b u(x, Q^2)$$

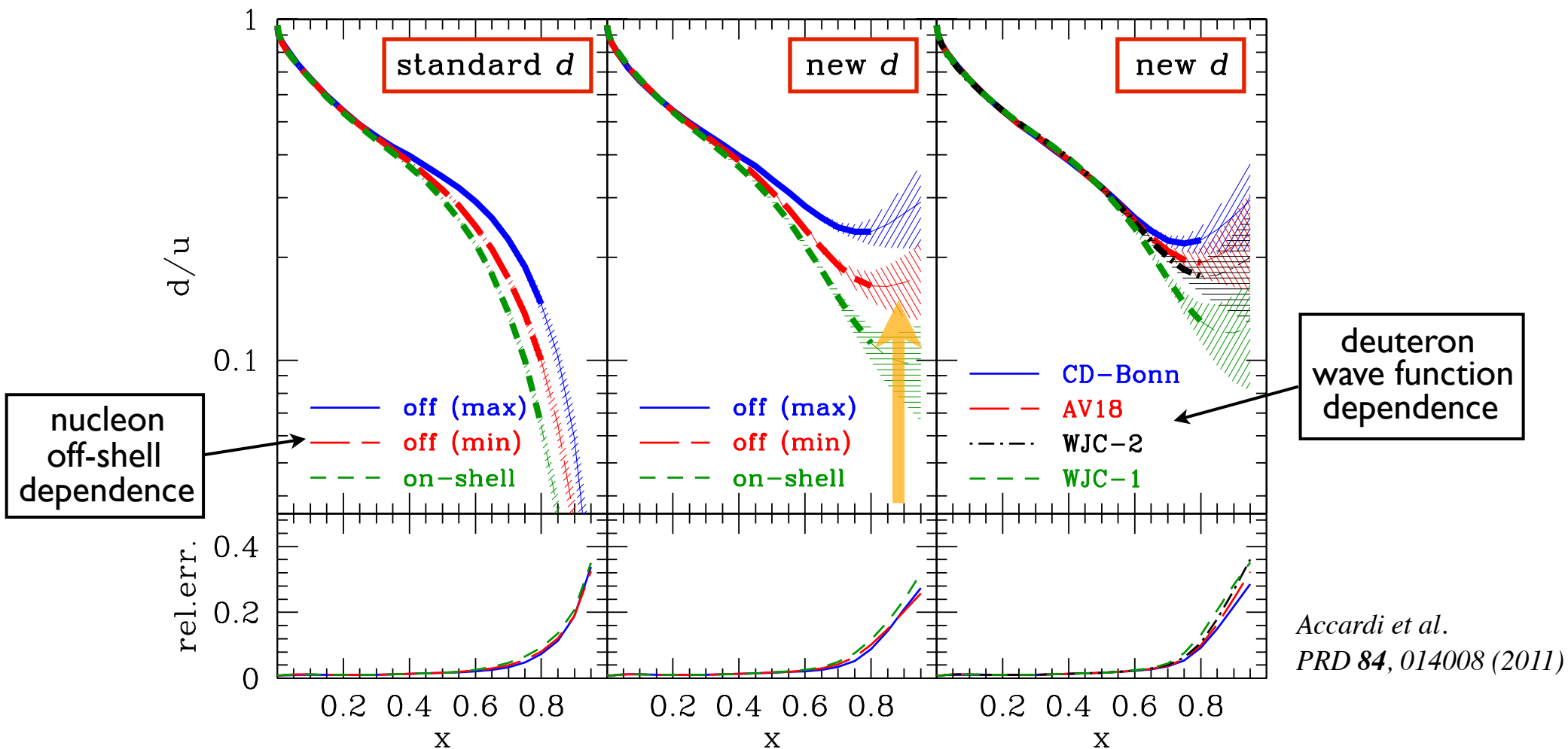
CJ global analysis



→ large nuclear correction uncertainties at $x > 0.5$

→ $x \rightarrow 1$ limiting value depends on deuteron model

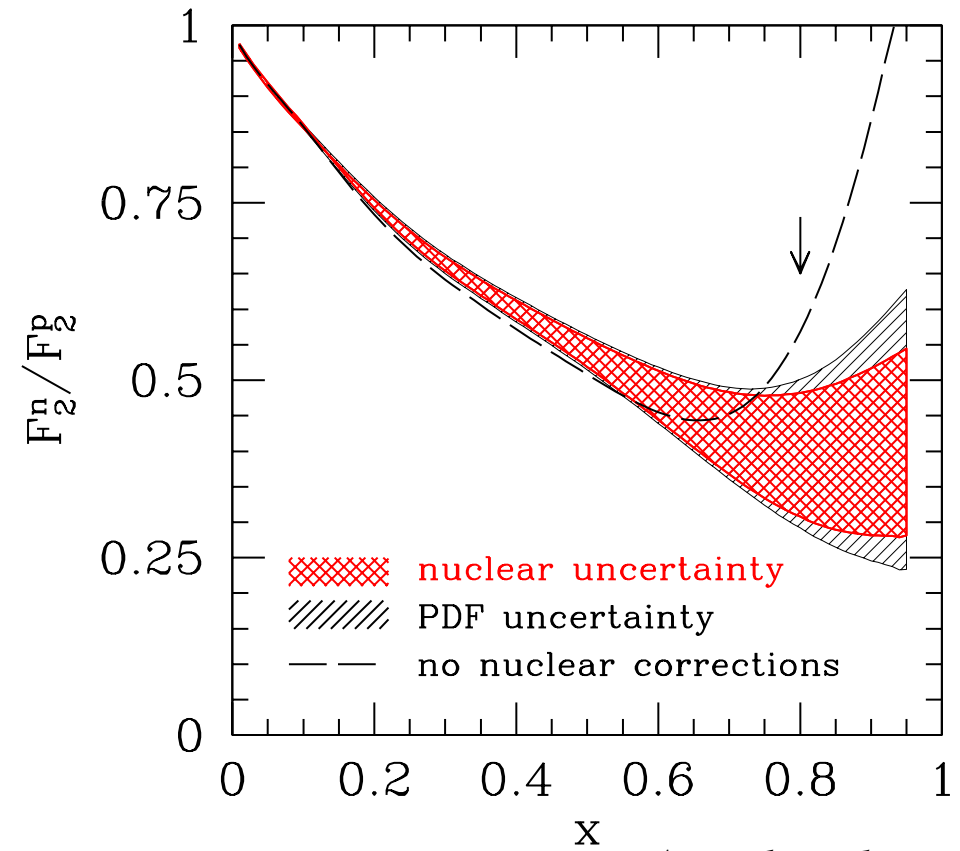
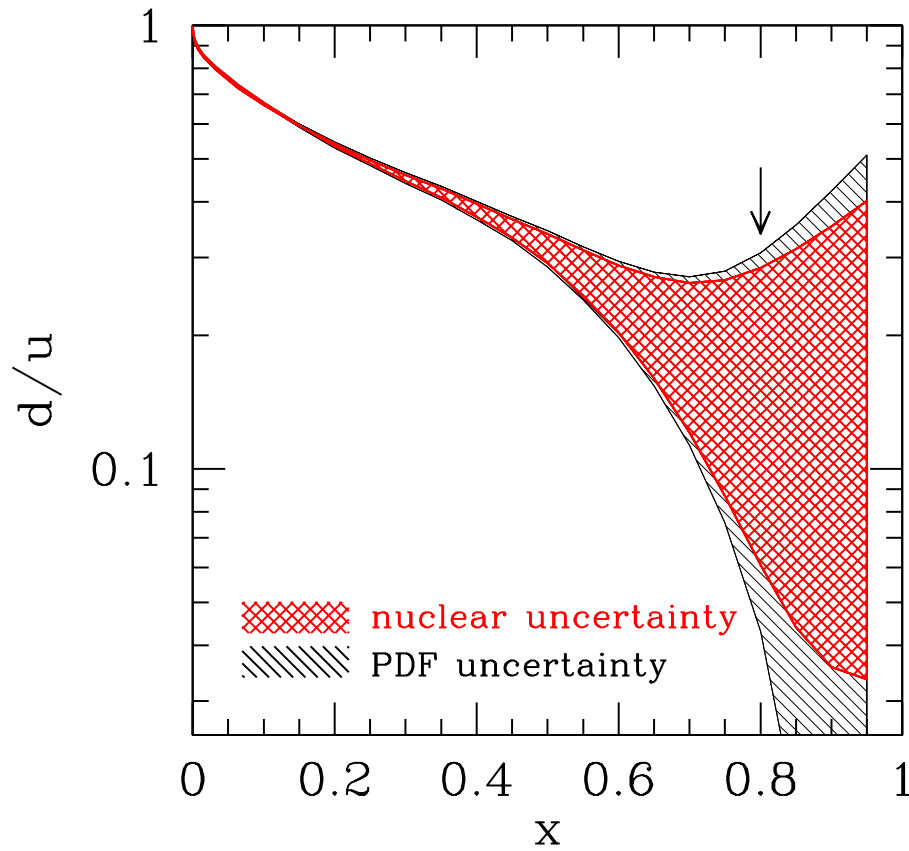
CJ global analysis



Accardi et al.
PRD **84**, 014008 (2011)

→ dramatic increase in d PDF in $x \rightarrow 1$ limit
with more flexible parametrization
(range $\sim 0 - 0.4$)

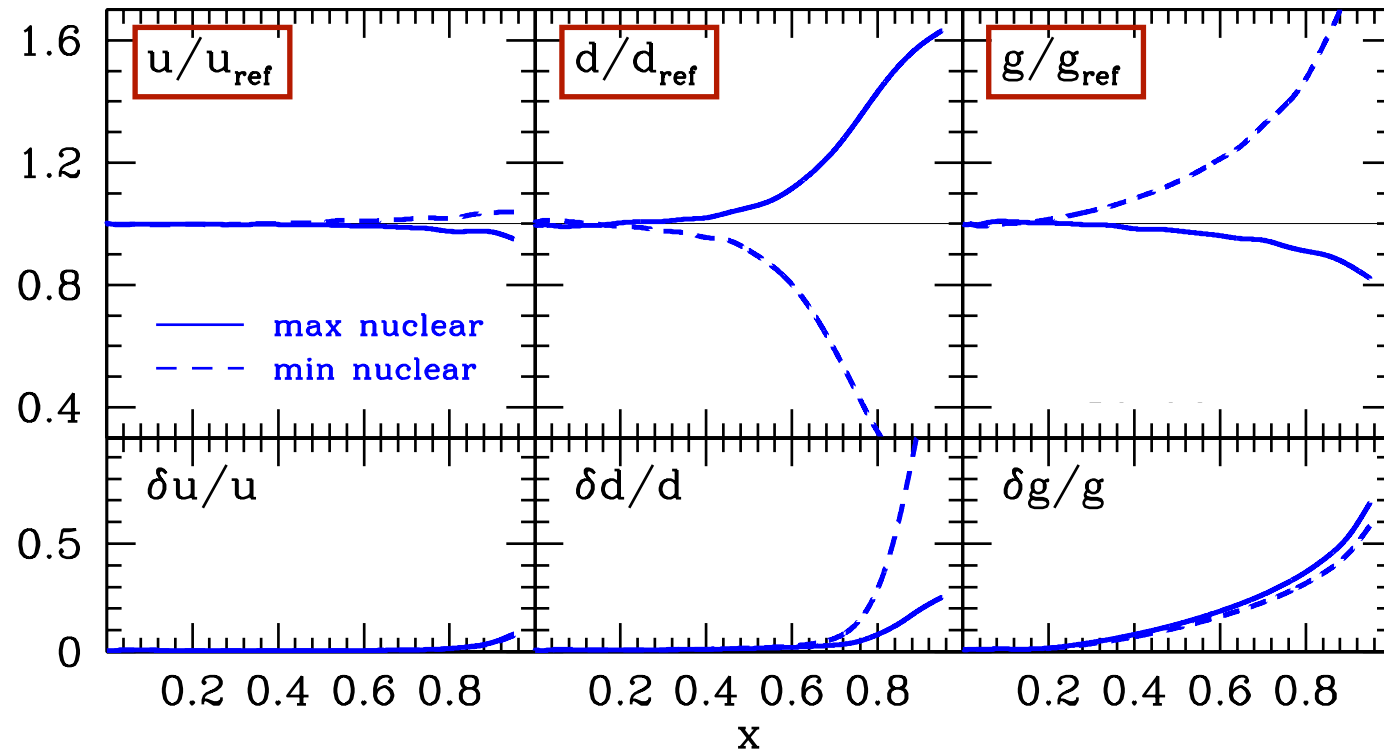
New CJ11 PDF analysis



Accardi et al.
PRD 84, 014008 (2011)

- combined nuclear correction uncertainties sizable at $x > 0.5$
- $x \rightarrow 1$ limiting value depends critically on deuteron model
- n/p ratio smaller at large x *cf.* no nuclear corrections fit

New CJ11 PDF analysis



Accardi et al.
PRD 84, 014008 (2011)

- **very little effect on u quark PDF**
(tightly constrained by DIS & DY proton data)
- **gluon PDF anticorrelated with d quark**
(g compensates for smaller d quark contribution in jet data)
- **uncertainty in d feeds into larger uncertainty in g at high x**

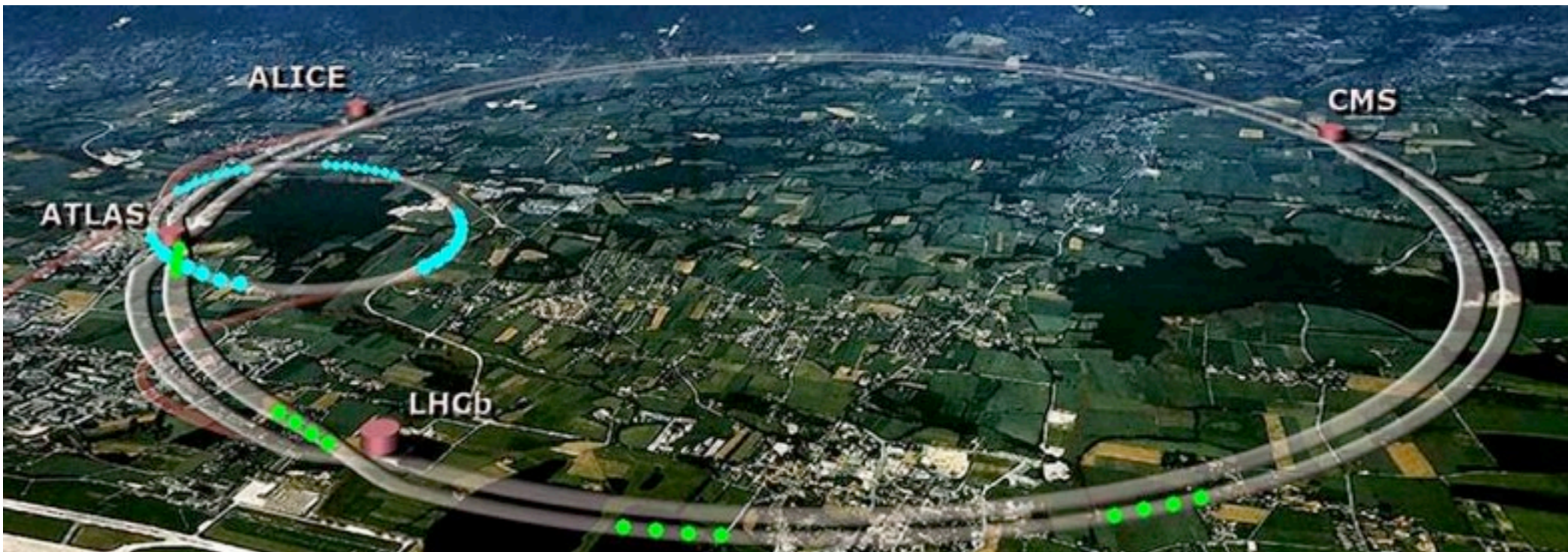
Implications for high-energy colliders

(Tevatron, LHC)

Large Hadron Collider (CERN): discovery of *Higgs boson*,
new physics beyond
the Standard Model?



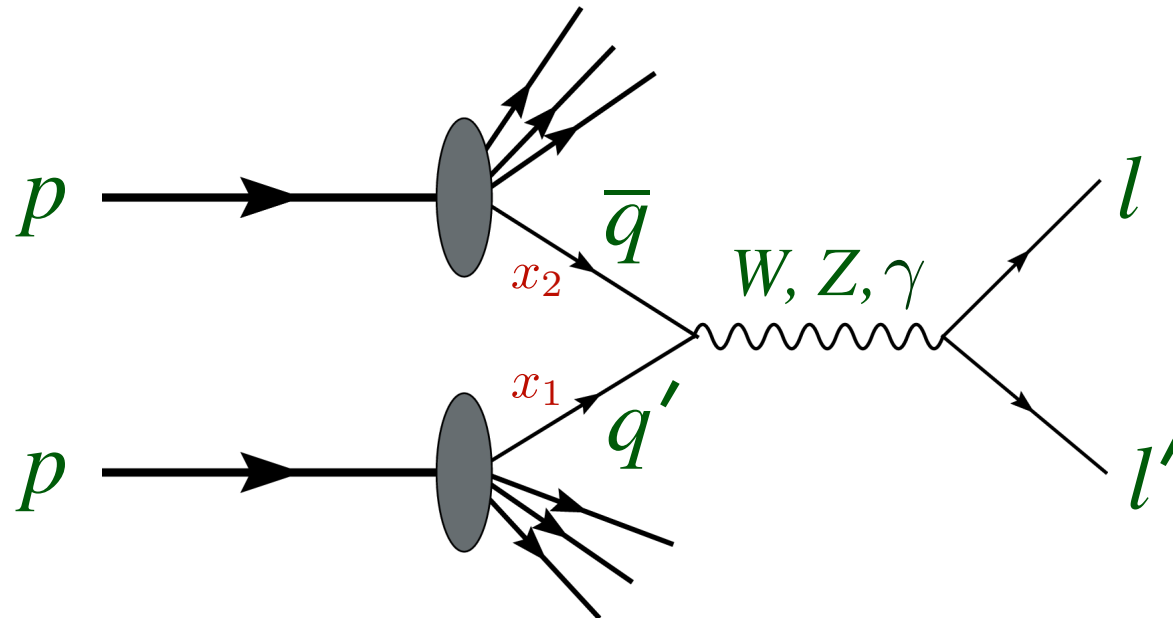
→ pp collisions at $\sqrt{s} = 7$ TeV



Large Hadron Collider (CERN): discovery of *Higgs boson*, new physics beyond the Standard Model?



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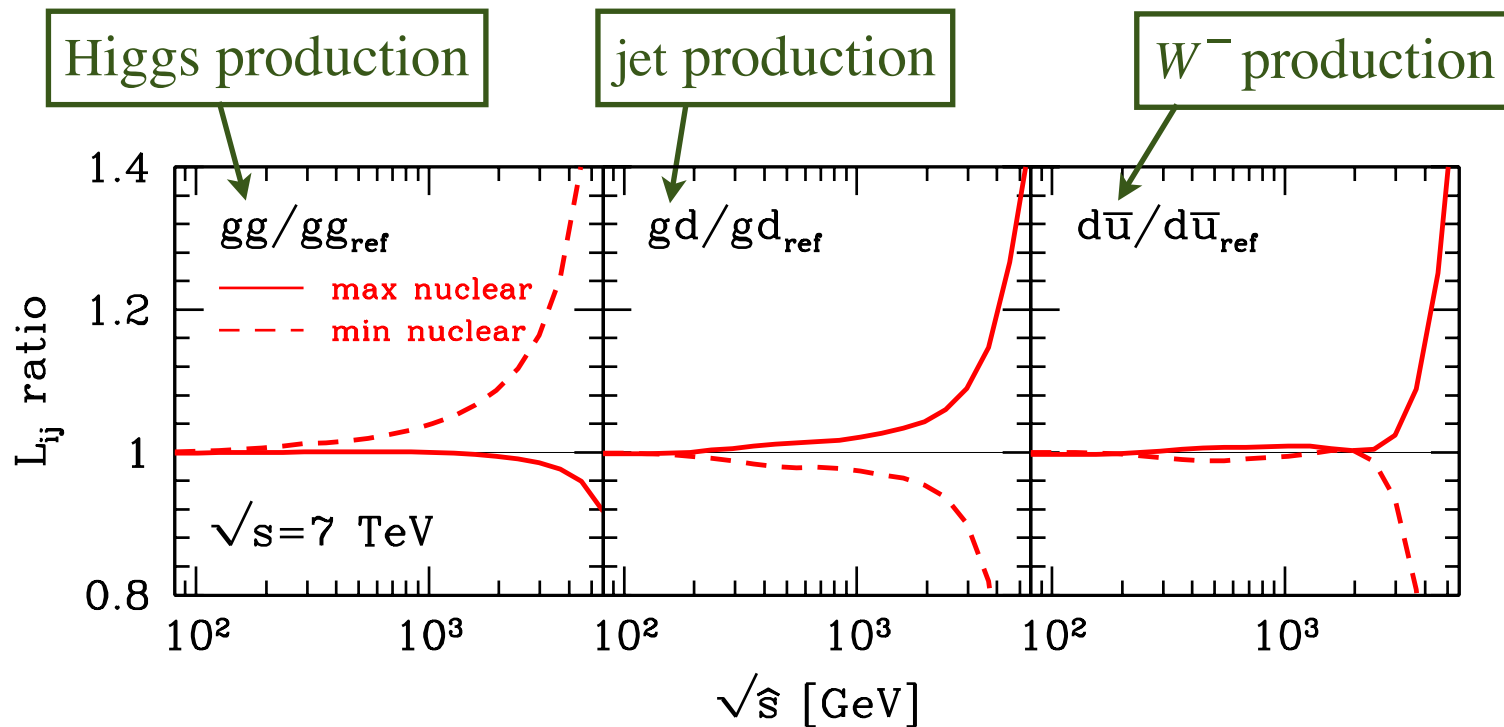


Parton luminosities

- Impact of CJ11 PDFs on parton “luminosities” at colliders

$$L_{ij} = \frac{1}{s(1 + \delta_{ij})} \int_{\hat{s}/s}^1 \frac{dx}{x} f_i(x, \hat{s}) f_j(\hat{s}/xs, \hat{s}) + (i \leftrightarrow j)$$

$s(\hat{s}) = \text{hadronic (partonic) c.m. energy squared}$



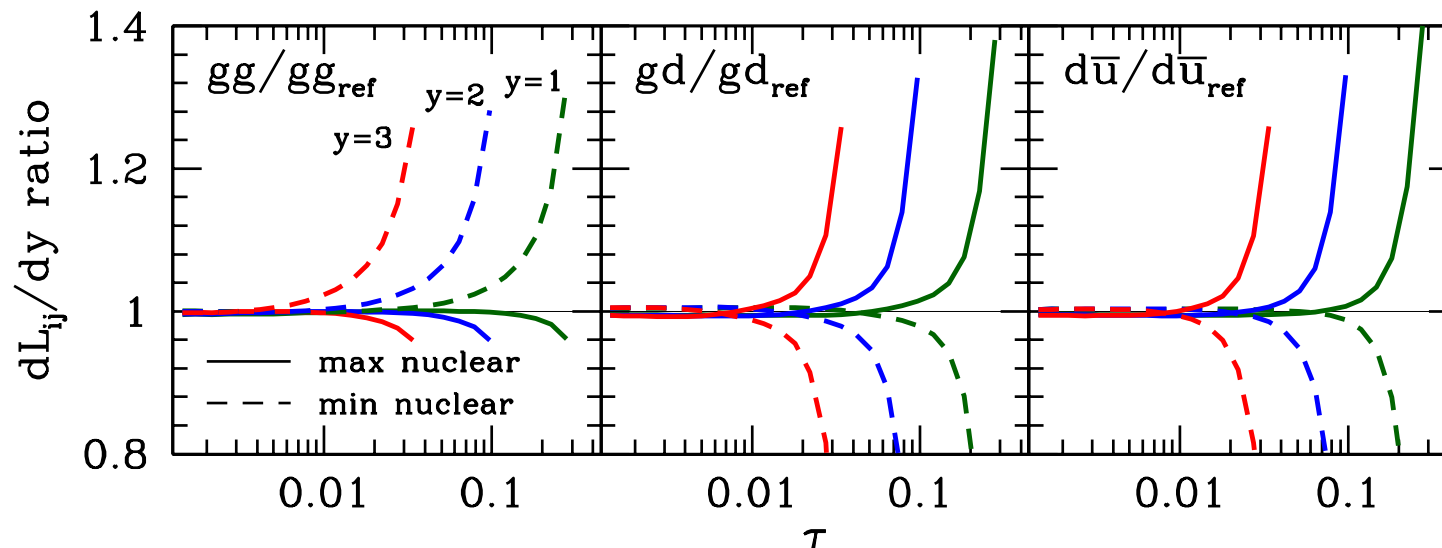
→ nuclear uncertainties important for $\sqrt{\hat{s}} \gtrsim 1 \text{ TeV}$ mass range

Parton luminosities

■ Impact of CJ11 PDFs on differential parton luminosities

$$\frac{dL_{ij}}{dy} = \frac{1}{s(1 + \delta_{ij})} f_i(x_1, \hat{s}) f_j(x_2, \hat{s}) + (i \leftrightarrow j)$$

$$x_{1,2} = \tau e^{\pm y}, \quad \tau = \sqrt{\hat{s}/s} \text{ for rapidity } y$$



Accardi et al.
arXiv:1101.1234

→ greater sensitivity to high- x region at larger rapidities

W boson asymmetries

- Large- x PDF uncertainties affect observables at large rapidity y , with

$$y = \frac{1}{2} \ln \left(\frac{E + p_z}{E - p_z} \right) \rightarrow x_{1,2} = \frac{M}{\sqrt{s}} e^{\pm y}$$

e.g. W^{\pm} asymmetry

$$A_W(y) = \frac{\sigma_{W^+} - \sigma_{W^-}}{\sigma_{W^+} + \sigma_{W^-}} \approx \frac{d(x_2)/u(x_2) - d(x_1)/u(x_1)}{d(x_2)/u(x_2) + d(x_1)/u(x_1)} \quad [x_1 \gg x_2]$$

where

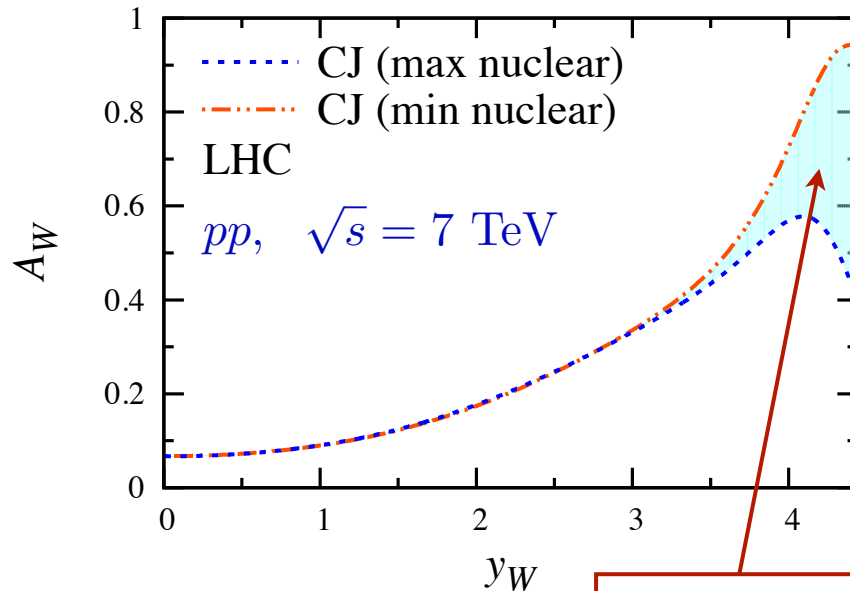
$$\sigma_{W^+} \equiv \frac{d\sigma}{dy}(pp \rightarrow W^+ X) = \frac{2\pi G_F}{3\sqrt{2}} x_1 x_2 (u(x_1)\bar{d}(x_2) + \dots)$$

W boson asymmetries

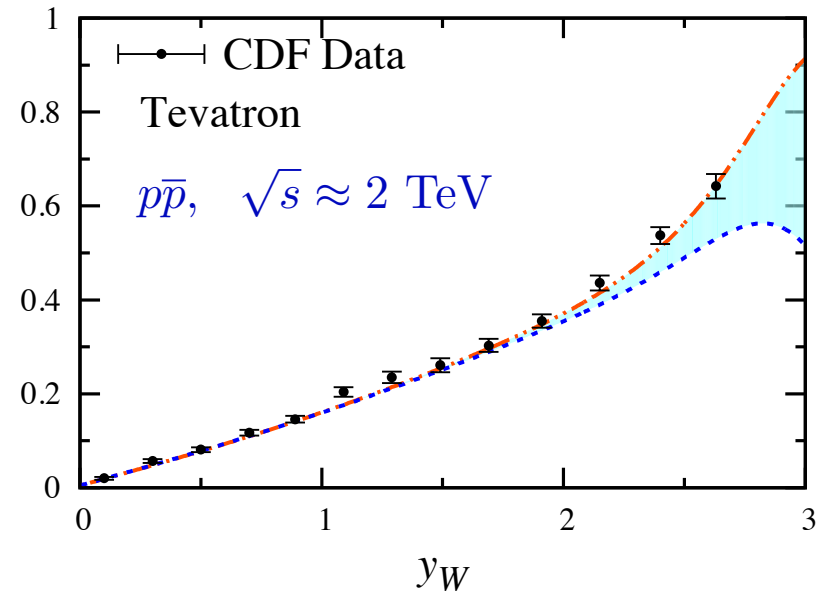
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e.g. W^{\pm} asymmetry



sensitive to
 d at high x



Brady, Accardi, WM, Owens
arXiv:1110:5398 [hep-ph]

Heavy Z' , W' boson production

- Some extensions of Standard Model predict heavy versions of W , Z bosons

→ Sequential Standard Model (SSM)

... assume same couplings as SM W , Z bosons

→ Grand Unified Theories *e.g.* E_6

London, Rosner (1986)

$$E_6 \rightarrow SO(10) \times U(1)_\chi \rightarrow SU(5) \times U(1)_\psi \times U(1)_\chi$$

→ more exotic scenarios, *e.g.*

- scalar excitations in R -parity violating supersymmetric models

Hewett, Rizzo (1998)

- spin-1 Kaluza-Klein excitations of SM bosons in presence of extra dimensions

Antoniadis (1990)

- spin-2 excitations of the graviton

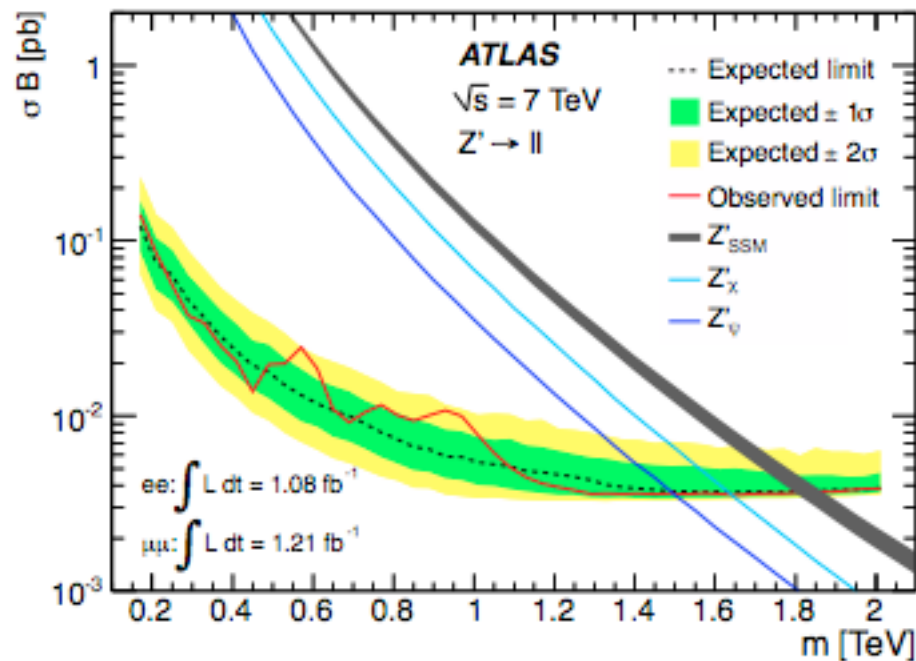
Randall, Sundrum (1999)

Heavy Z' , W' boson production

- Current limits on masses (for SSM; lower for other models)

→ $M_{Z'} > 1.83 \text{ TeV}$

$M_{W'} > 2.15 \text{ TeV}$ ATLAS @ LHC



arXiv:1108.1582 [hep-ex]

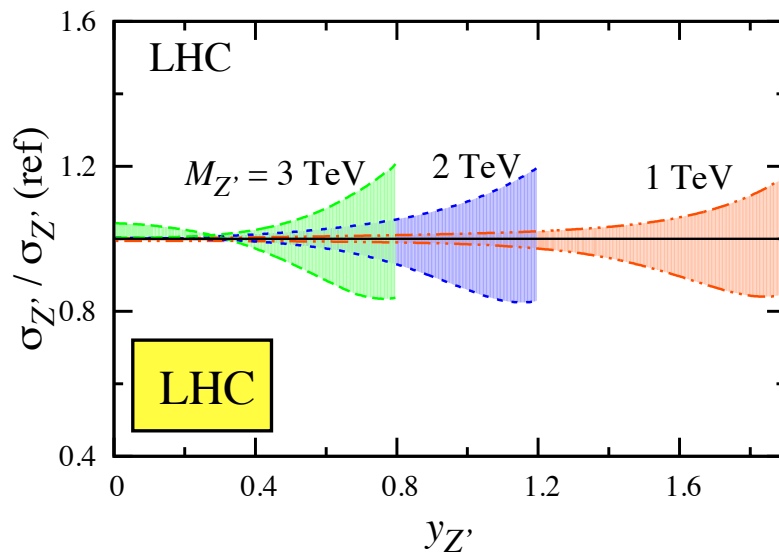
Heavy Z' , W' boson production

- Observation of new physics signals requires accurate determination of QCD backgrounds — depend on PDFs!
(since $x_{1,2} \sim M_{Z',W'}$, large- x uncertainties scale with mass)

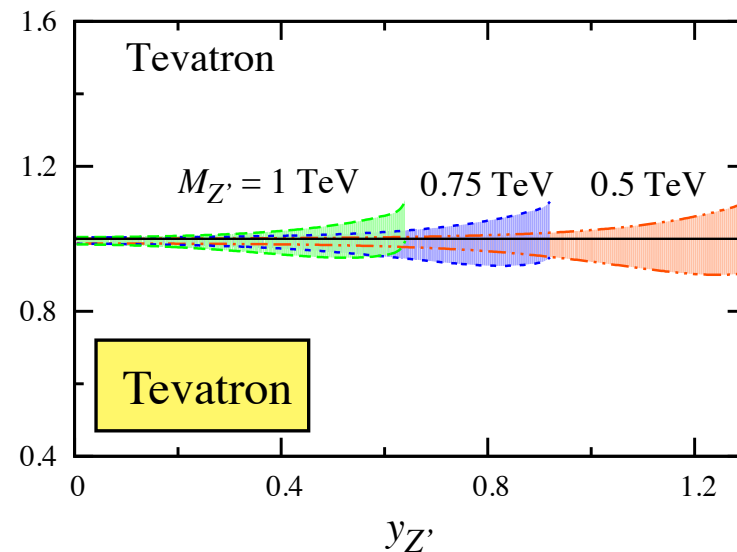
- for Z' production

couplings similar for u and d

$$\frac{d\sigma^{pp}}{dy} \sim \sum_q \left[(g_V^q)^2 + (g_A^q)^2 \right] \left(q(x_1)\bar{q}(x_2) + \bar{q}(x_1)q(x_2) \right)$$



→ dominated by $u * \bar{u}$
– rel. small uncertainties

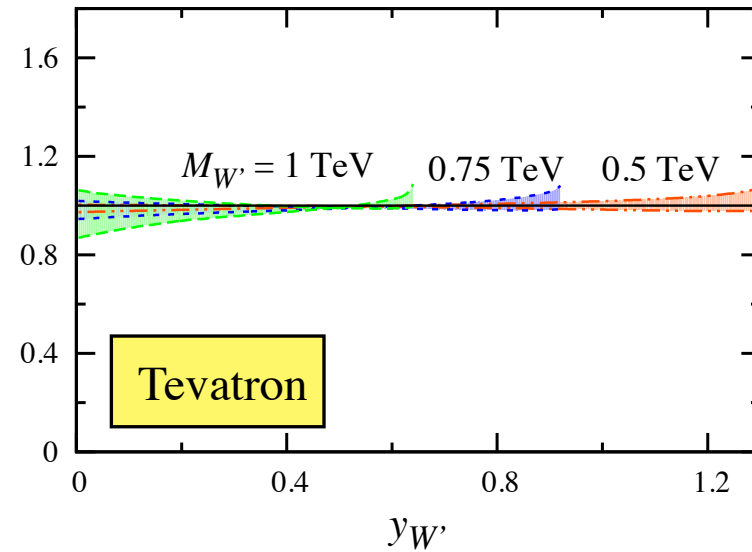
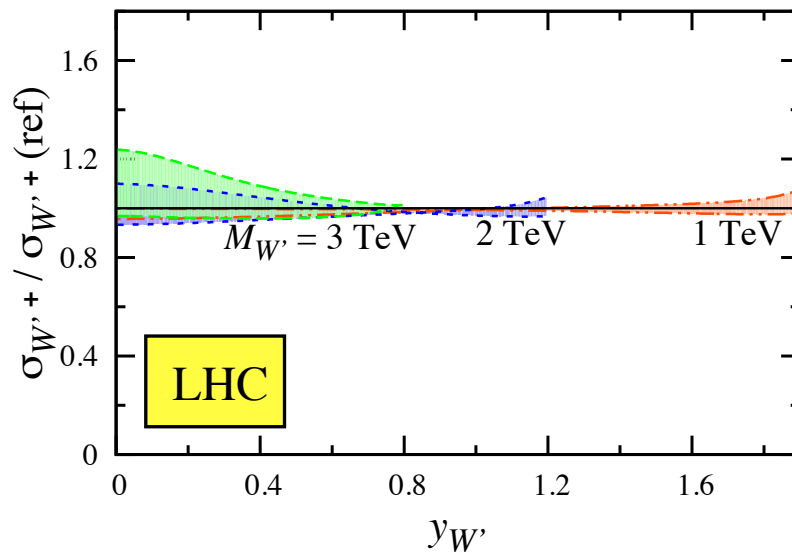


→ dominated by $u * u$
– well constrained

Heavy Z' , W' boson production

- Observation of new physics signals requires accurate determination of QCD backgrounds — depend on PDFs!
(since $x_{1,2} \sim M_{Z',W'}$, large- x uncertainties scale with mass!)

- for W'^+ production



→ large y : dominated by $u * \bar{d}$
– well constrained

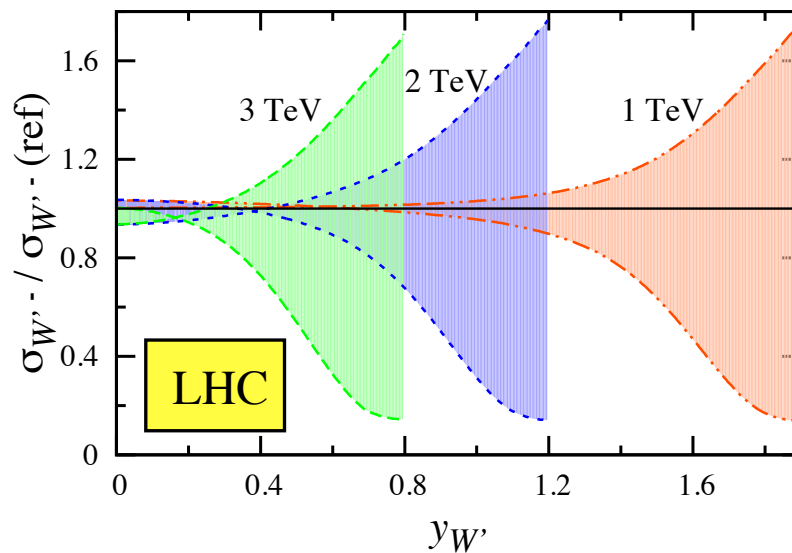
→ small y : uncertainty from \bar{d}
at $x \sim 0.3-0.4$

→ dominated by $u * d$
– well constrained

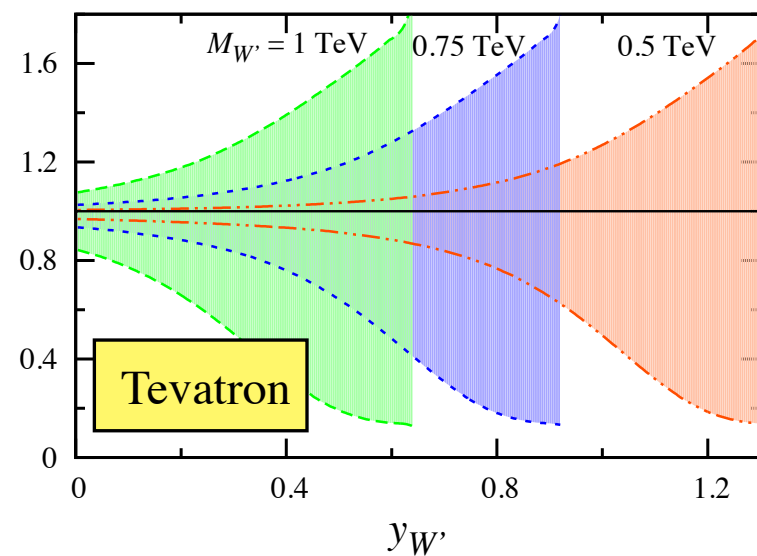
Heavy Z' , W' boson production

- Observation of new physics signals requires accurate determination of QCD backgrounds — depend on PDFs!
(since $x_{1,2} \sim M_{Z',W'}$, large- x uncertainties scale with mass!)

- for W'^- production



→ dominated by $d * \bar{u}$



→ dominated by $d * u + u * d$

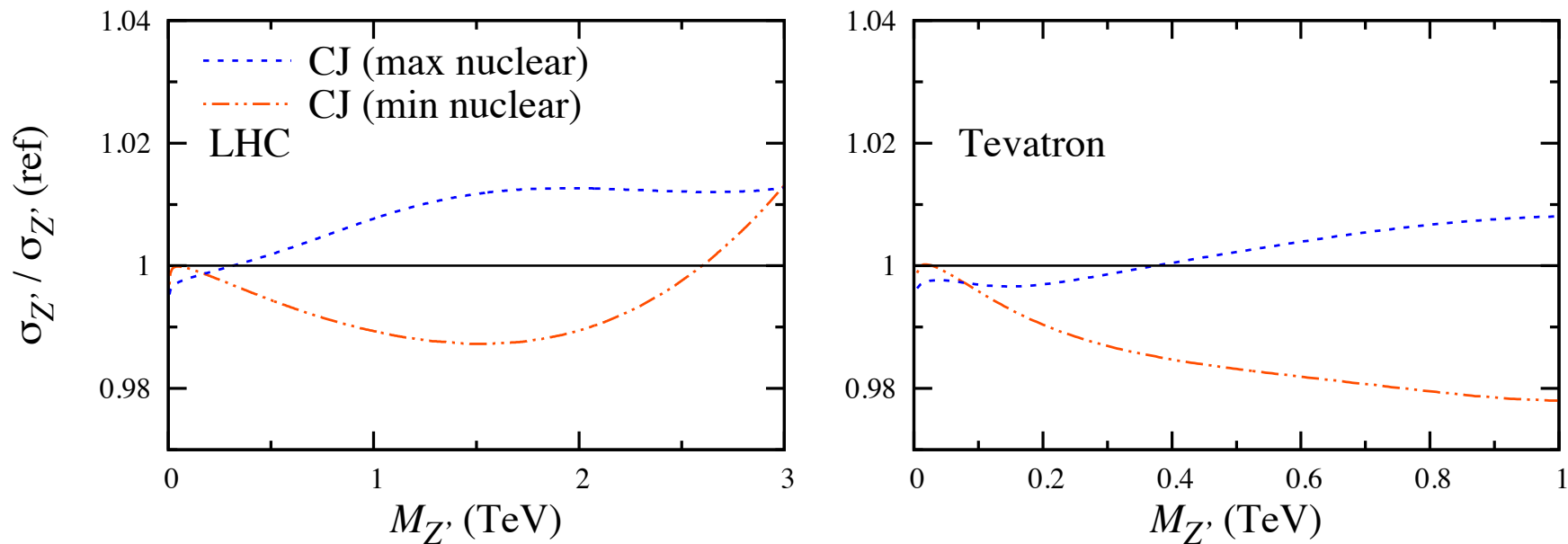
> 100% uncertainties at large y !

Heavy Z' , W' boson production

- Observation of new physics signals requires accurate determination of QCD backgrounds — depend on PDFs!
(since $x_{1,2} \sim M_{Z',W'}$, large- x uncertainties scale with mass!)

- for integrated Z' cross section

→ dominated by contributions from small y

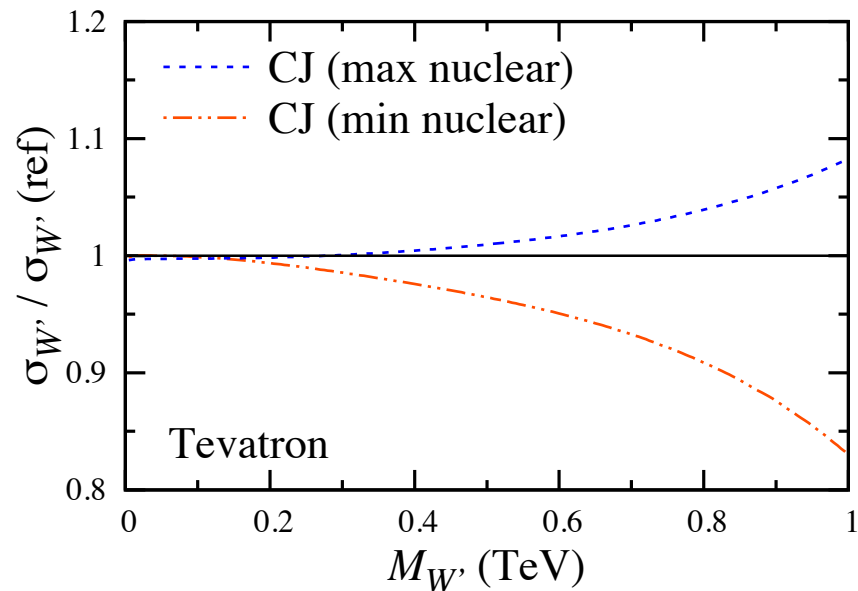
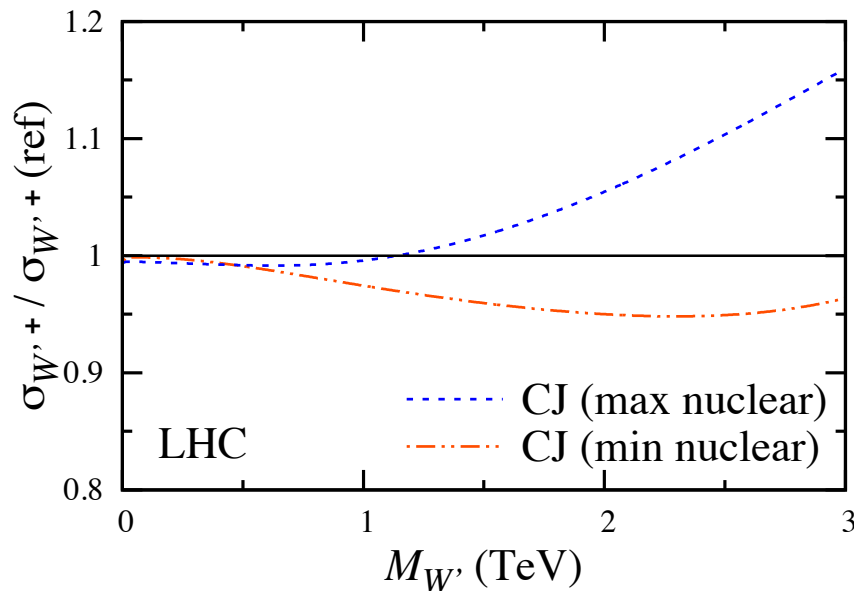


→ increasing uncertainties for large $M_{Z'}$
from antiquark PDFs at high x

Heavy Z' , W' boson production

- Observation of new physics signals requires accurate determination of QCD backgrounds — depend on PDFs!
(since $x_{1,2} \sim M_{Z',W'}$, large- x uncertainties scale with mass!)

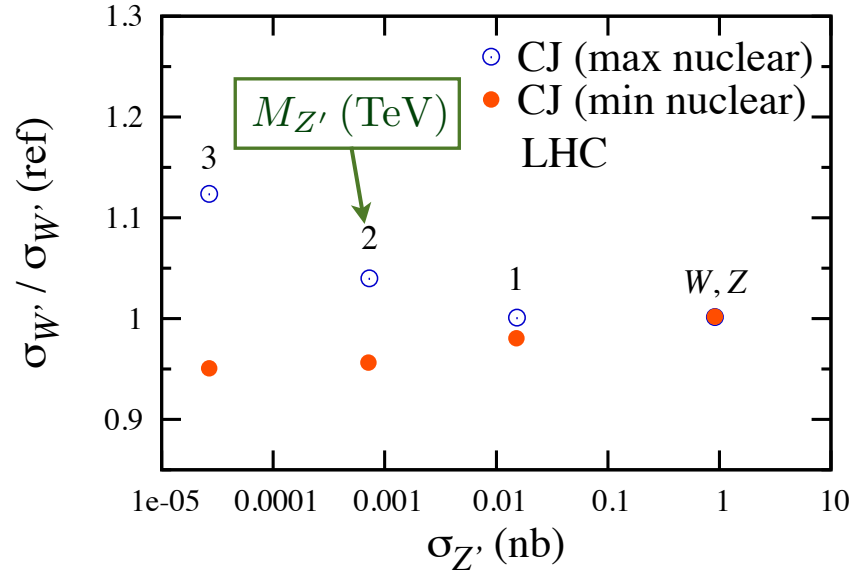
- for integrated W' cross section
→ dominated by contributions from small y



- increasing uncertainties for large $M_{Z'}$
from antiquark PDFs at high x

Heavy Z' , W' boson production

- Observation of new physics signals requires accurate determination of QCD backgrounds — depend on PDFs!
(since $x_{1,2} \sim M_{Z',W'}$, large- x uncertainties scale with mass!)
- for integrated Z' & W' cross sections



- increasing sensitivity to high- x PDF uncertainties
– could affect interpretation of experimental searches

Outlook

Outlook

- Nuclear correction uncertainties expected to be resolved with new experiments at JLab–12 GeV uniquely sensitive to d quarks (up to $x \sim 0.85$)
 - “spectator” protons tagged in SIDIS from deuterium
 $e d \rightarrow e p_{\text{spec}} X$ (“BoNuS”)
 - DIS from ${}^3\text{He}$ -tritium mirror nuclei
 $e {}^3\text{He}({}^3\text{H}) \rightarrow e X$ (“MARATHON”)
 - PVDIS from protons
 $\vec{e}_L(\vec{e}_R) p \rightarrow e X$ (“SOLID”)
- Constraints from W production in pp collisions at high (lepton & W boson) rapidities
 - CDF & D0 at Fermilab, LHCb at CERN

Outlook

- New JLab–12 GeV precisions measurements of A_1^n & A_1^p
hope to constrain $\Delta d/d$ up to $x \sim 0.8$
 - new (non-inclusive DIS) experiments to reduce nuclear dependence
- Parametrization dependence of $x \rightarrow 1$ limit may be eliminated through *e.g.* “neural network” PDFs
 - thus far applied mainly to unpolarized PDFs
- New global analysis of *spin-dependent* PDFs dedicated to large- x , moderate- Q^2 region
 - JLab Angular Momentum (“JAM”) collaboration*
 - initial focus on helicity PDFs; later expand scope to TMDs

* JAM collaboration: P. Jimenez-Delgado, A. Accardi, WM (theory) + JLab Halls A, B, C (expt.)

The End