

Jefferson Lab PAC36 August 24, 2010

# Longitudinal structure of hadrons

Wally Melnitchouk



- Spin-averaged nucleon structure
  - $\rightarrow$  d/u ratio at large x, with *minimal* nuclear corrections
  - → new global QCD analysis ("CTEQ6X") with large-x focus – importance of  $1/Q^2$  corrections
  - resonance region structure / quark-hadron duality
     recent first confirmation for *neutron*

Spin- <i>dependent</i> nucleon structure	E12-06-109 E12-06-121
	E12-06-122
$\rightarrow A_1$ (or $\Delta u/u$ , $\Delta d/d$ ) at large x	PR12-06-110

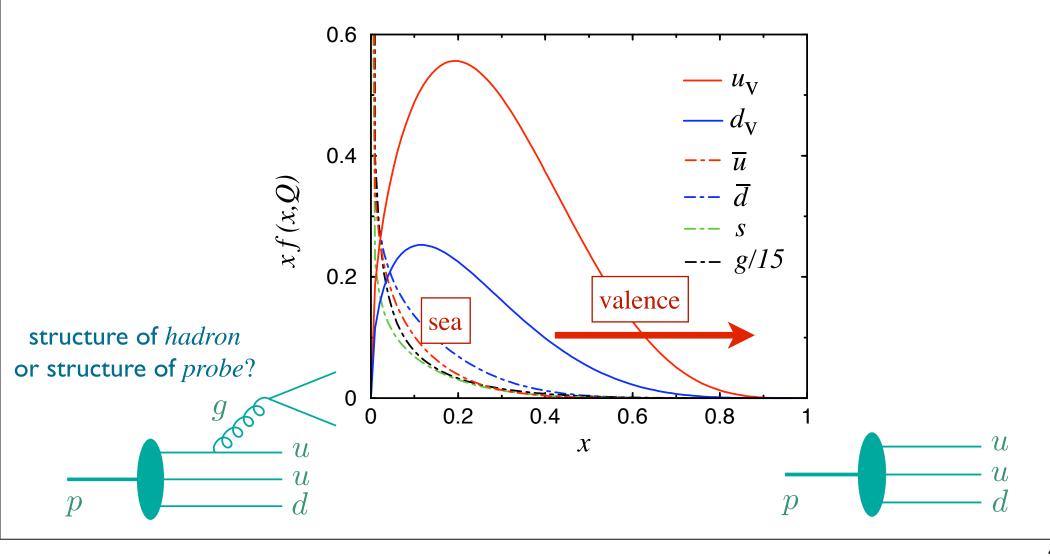
- $\rightarrow$  nuclear corrections for neutron extraction from <sup>3</sup>He or d
- $\rightarrow$  finite  $Q^2$  corrections / higher twist extraction

E12-06-104 E12-10-002 PR12-06-113 PR12-06-118

# Nucleon structure at large *x*: *spin-averaged*

Why is nucleon structure at large x interesting?

- Most direct connection between quark distributions and nonperturbative structure of nucleon is via *valence* quarks
  - $\rightarrow$  most cleanly revealed at x > 0.4



Why is nucleon structure at large x interesting?

- Most direct connection between quark distributions and nonperturbative structure of nucleon is via valence quarks
- Predictions for  $x \rightarrow 1$  behavior of *e.g.* d/u ratio
  - $\rightarrow$  scalar diquark dominance: d/u = 0 Feynman (1972)
  - $\rightarrow$  hard gluon exchange: d/u = 1/5 Farrar, Jackson (1975)
  - $\rightarrow$  SU(6) symmetry: d/u = 1/2 1960s
- Needed to understand backgrounds in searches for new physics beyond the Standard Model at LHC or in v oscillation experiments
  - $\rightarrow$  DGLAP evolution feeds low-x, high- $Q^2$  from high-x, low- $Q^2$

At large x, valence u and d distributions determined from p and n structure functions, e.g. at LO

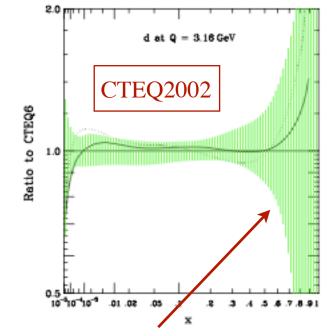
$$\frac{1}{x}F_2^p \approx \frac{4}{9}u_v + \frac{1}{9}d_v$$
$$\frac{1}{x}F_2^n \approx \frac{4}{9}d_v + \frac{1}{9}u_v$$

- *u* quark distribution well determined from *proton*
- *d* quark distribution requires *neutron* structure function

$$\implies \quad \frac{d}{u} \approx \frac{4 - F_2^n / F_2^p}{4F_2^n / F_2^p - 1}$$

No <u>FREE</u> neutron targets (neutron half-life ~ 12 mins)

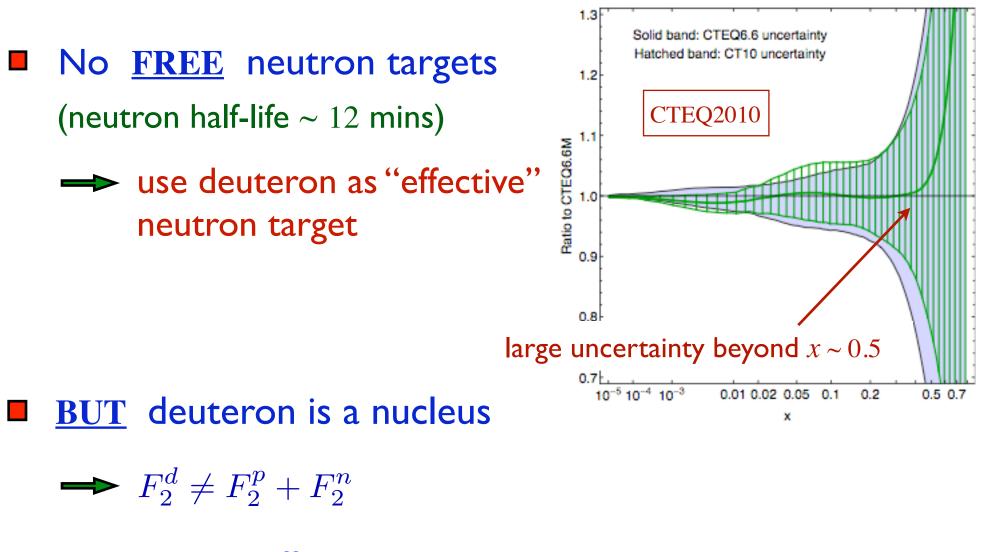
use deuteron as "effective" neutron target



large uncertainty beyond  $x \sim 0.5$ 

- BUT deuteron is a nucleus
  - $\implies$   $F_2^d \neq F_2^p + F_2^n$
  - nuclear effects (nuclear binding, Fermi motion, shadowing) obscure neutron structure information
  - → need to correct for "nuclear EMC effect"

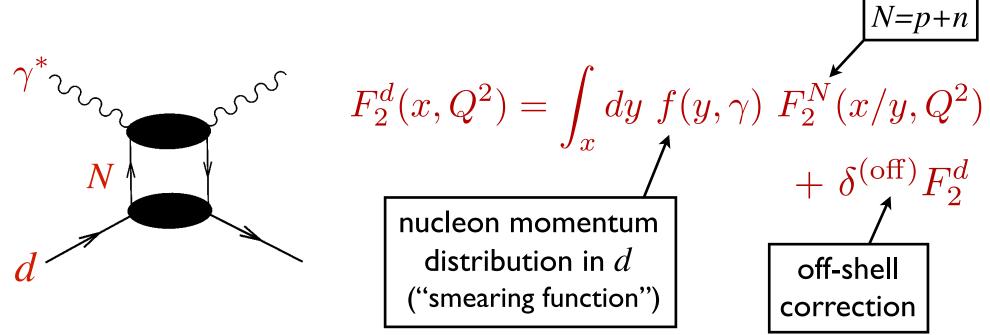
d/u at Q=85 GeV



nuclear effects (nuclear binding, Fermi motion, shadowing) obscure neutron structure information

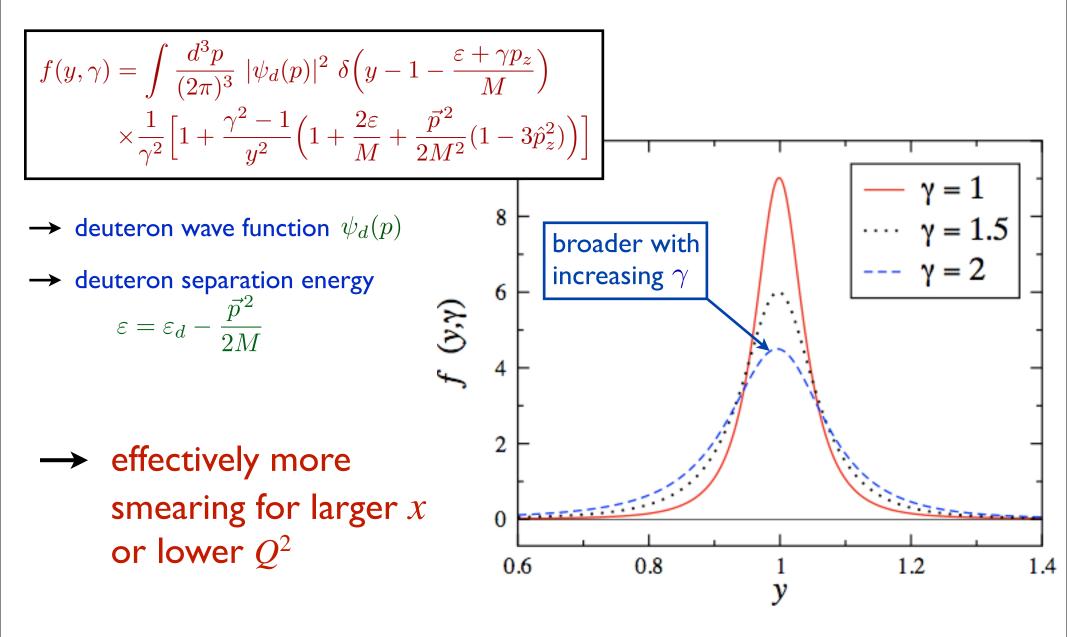
need to correct for "nuclear EMC effect"

Incoherent scattering from individual nucleons in d (good approx. at x >> 0)

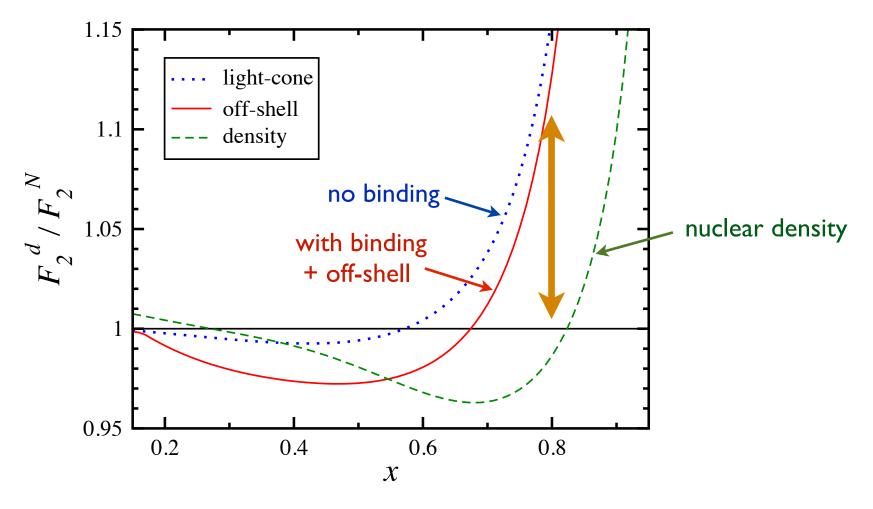


- $\rightarrow$   $y = p \cdot q / P \cdot q$  light-cone momentum fraction of d carried by N
- $\rightarrow$  at finite  $Q^2$ , smearing function depends also on parameter

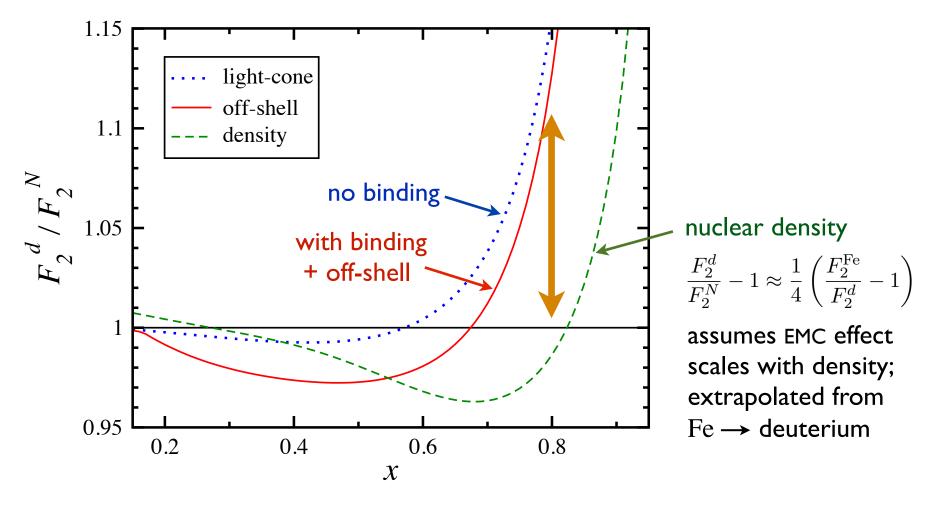
$$\gamma = |\mathbf{q}|/q_0 = \sqrt{1 + 4M^2 x^2/Q^2}$$



Kulagin, Petti, NPA **765**, 126 (2006) Kahn et al., PRC **79**, 035205 (2009)



- → using off-shell model, will get *larger* neutron cf. light-cone model
- → but will get *smaller* neutron *cf. no nuclear effects* or *density* model



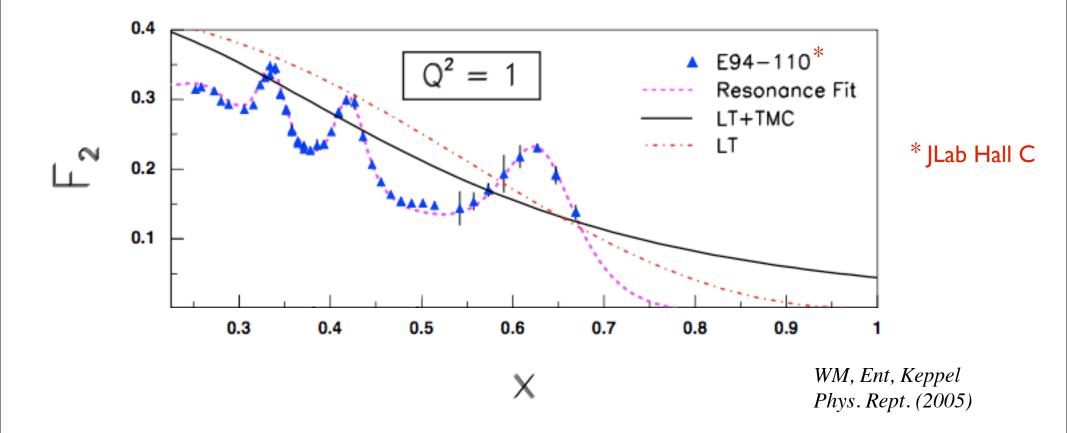
- → ~2-3% reduction of  $F_2^d/F_2^N$  at  $x \sim 0.5-0.6$ with steep rise for x > 0.6-0.7
- → larger EMC effect at  $x \sim 0.5-0.6$  with binding + off-shell corrections *cf.* light-cone

- In OPE insertion of covariant derivatives in quark bilinears leads to terms ~  $Q^2/\nu^2$  ~  $M^2x^2/Q^2$ 
  - → kinematical *target mass corrections* (formally leading twist)
  - $\rightarrow$  gives rise to new "Nachtmann" scaling variable

$$\xi = \frac{2x}{1+\gamma}, \quad \gamma^2 = 1 + Q^2/\nu^2$$

Target mass corrected structure function (in OPE approach)

$$F_{2}(x,Q^{2}) = \frac{x^{2}}{\xi^{2}\gamma^{3}}F_{2}^{(0)}(\xi,Q^{2}) + \frac{6M^{2}x^{3}}{Q^{2}\gamma^{4}}\int_{\xi}^{1} du \frac{F_{2}^{(0)}(u,Q^{2})}{u^{2}} + \frac{12M^{4}x^{4}}{Q^{4}\gamma^{5}}\int_{\xi}^{1} dv(v-\xi)\frac{F_{2}^{(0)}(v,Q^{2})}{v^{2}}$$
massless limit function
Georgi, Politzer (1976)



#### -> TMC important for verification of quark-hadron duality

- <u>But</u> TMCs not unique: e.g. in collinear factorization
  - → work directly in *momentum* space at partonic level (avoids Mellin transform; applicable also to non-DIS processes)
  - $\rightarrow$  expand parton momentum k around its *on-shell* and *collinear* component  $(k_{\perp}^2 \rightarrow 0)$

Ellis, Furmanski, Petronzio (1983)

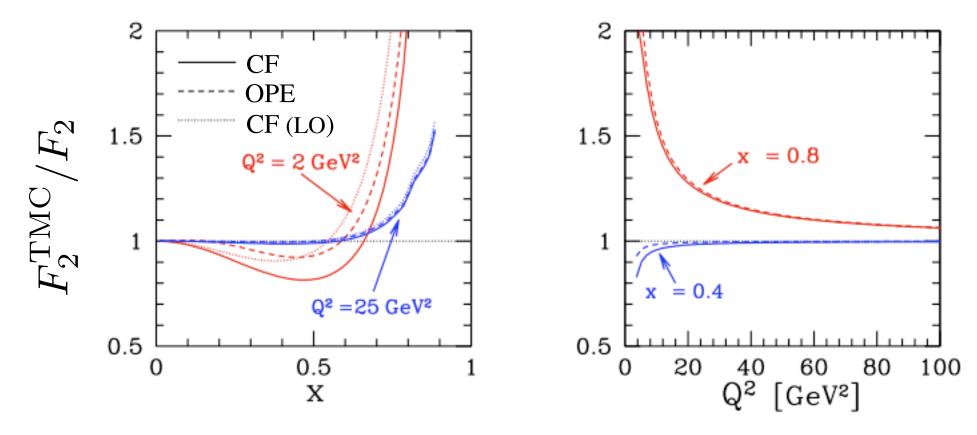
$$F_{T,L}(x,Q^2) = \sum_{q} \int_{\xi}^{\xi/x} \frac{dy}{y} C_{T,L}^{q} \left(\frac{\xi}{y},Q^2\right) q(y,Q^2)$$
Accardi, Qiu (2008)

 $\rightarrow$  at leading order

$$\begin{split} F_2^{\text{CF}}(x,Q^2) &= \frac{x}{\xi\gamma^2} \ F_2^{(0)}(\xi,Q^2) \\ &\approx \frac{\xi\gamma}{x} \ F_2^{\text{OPE}}(x,Q^2) \end{split} \qquad \text{Kretzer, Reno} \end{split}$$

(2004)

<u>But</u> TMCs not unique: e.g. in collinear factorization



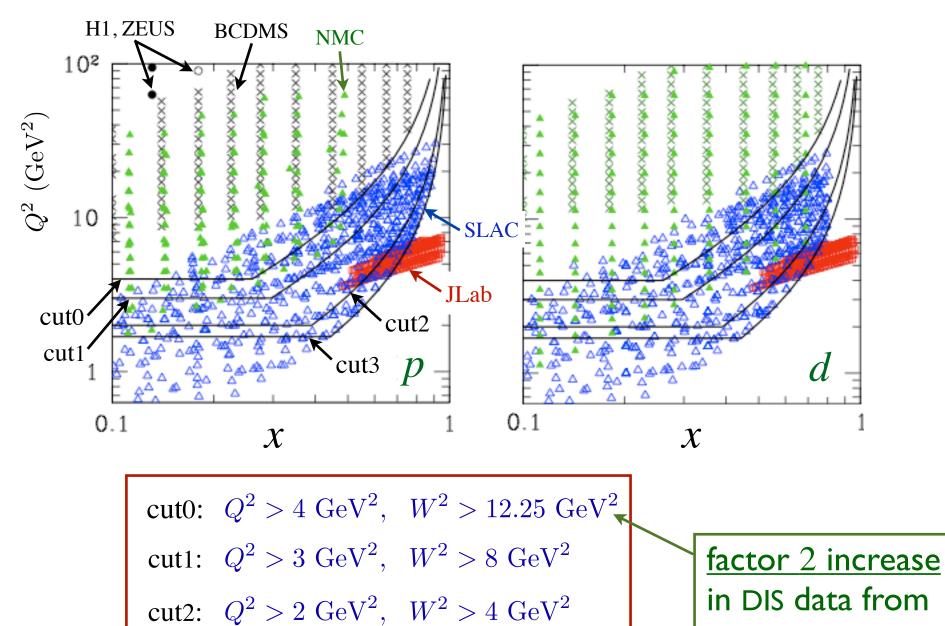
Accardi, Qiu (2008)

→ TMC important at large x even for large  $Q^2$ 

# CTEQ6X global PDF fit

- New global QCD (next-to-leading order) analysis of expanded set of p and d data, including large-x, low-Q<sup>2</sup> region
  - → joint JLab-CTEQ theory/experiment collaboration (with Hampton, FSU, FNAL, Duke)
- Systematically study effects of  $Q^2 \& W$  cuts
  - $\rightarrow$  as low as  $Q \sim m_c$  and  $W \sim 1.7 \text{ GeV}$
- $\blacksquare Include large-x corrections$ 
  - $\rightarrow$  TMCs & higher twists  $F_2(x,Q^2) = F_2^{LT}(x,Q^2)(1+C(x)/Q^2)$
  - → realistic nuclear effects in deuteron (binding + off-shell) (most analyses use either no correction, or density model)

#### CTEQ6X – kinematic cuts

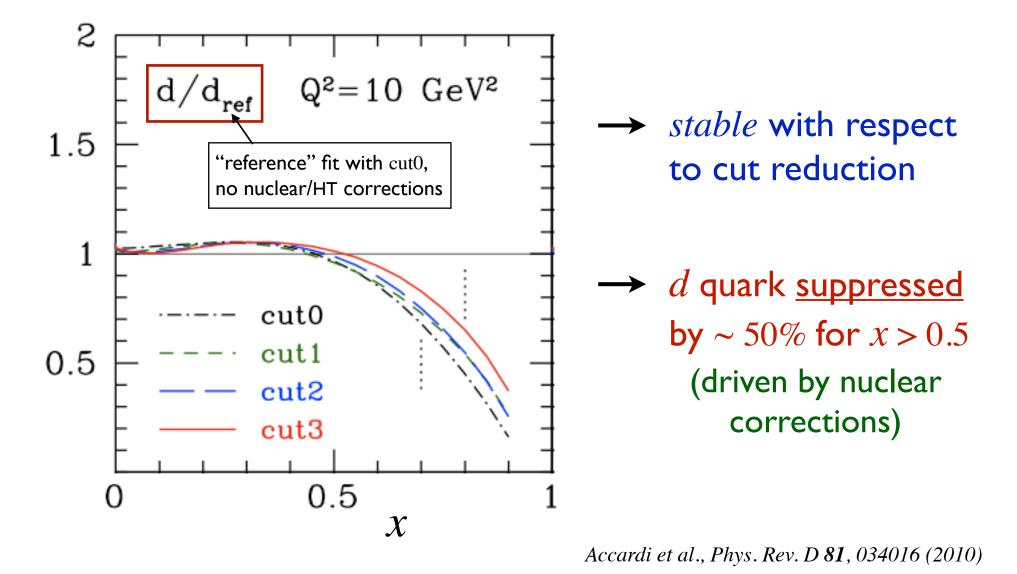


cut3:  $Q^2 > m_c^2$ ,  $W^2 > 3 \text{ GeV}^2$ 

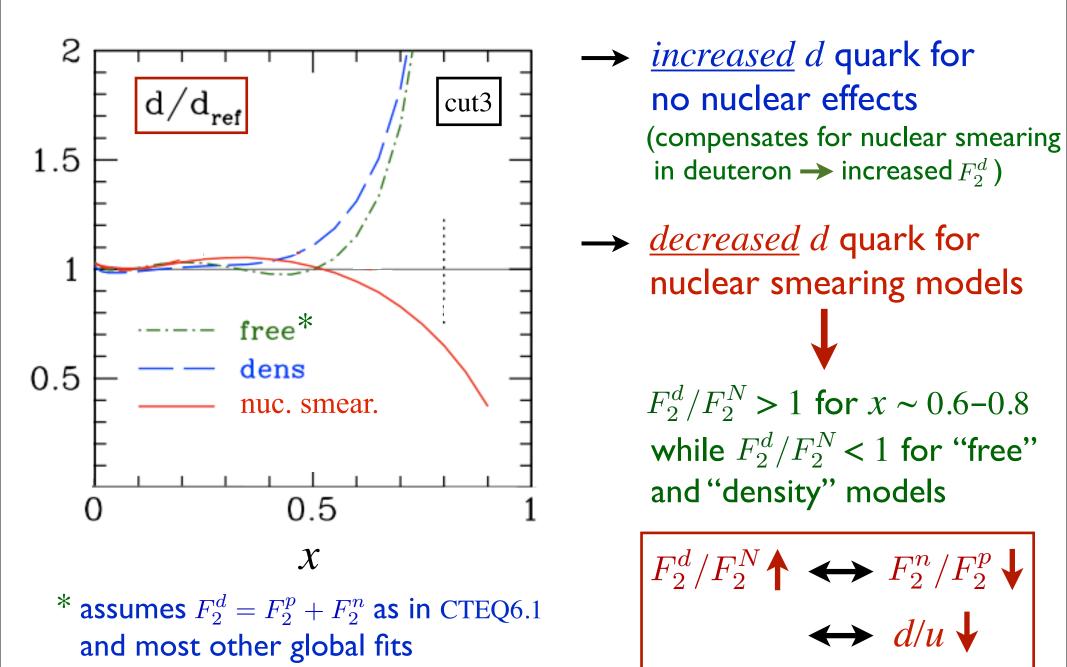
 $cut0 \rightarrow cut3$ 

#### CTEQ6X – kinematic cuts

Systematically reduce Q<sup>2</sup> and W cuts, including TMC, HT
 & nuclear corrections

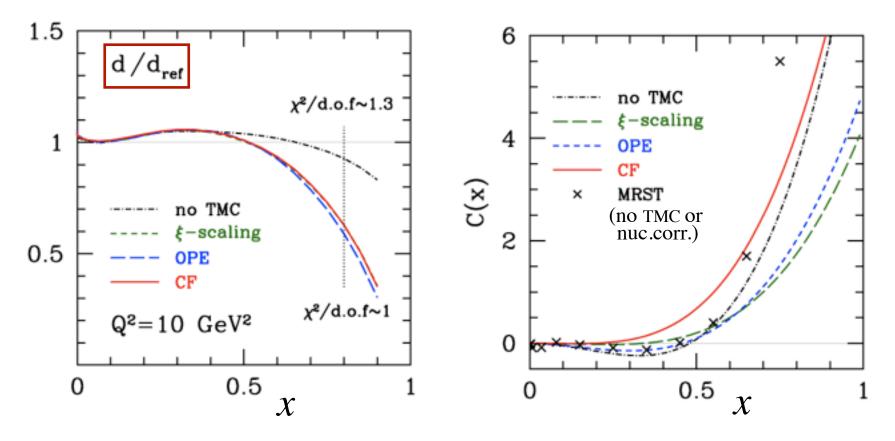


## CTEQ6X – nuclear effects



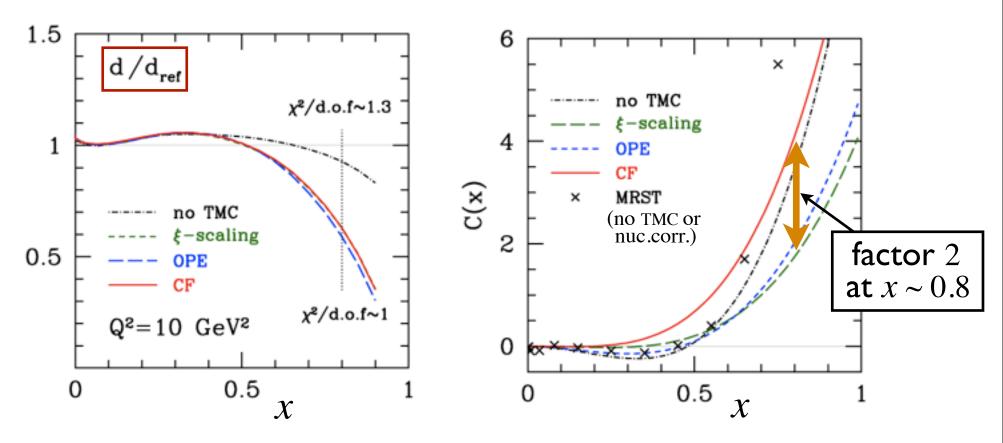
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CTEQ6X –  $1/Q^2$  corrections



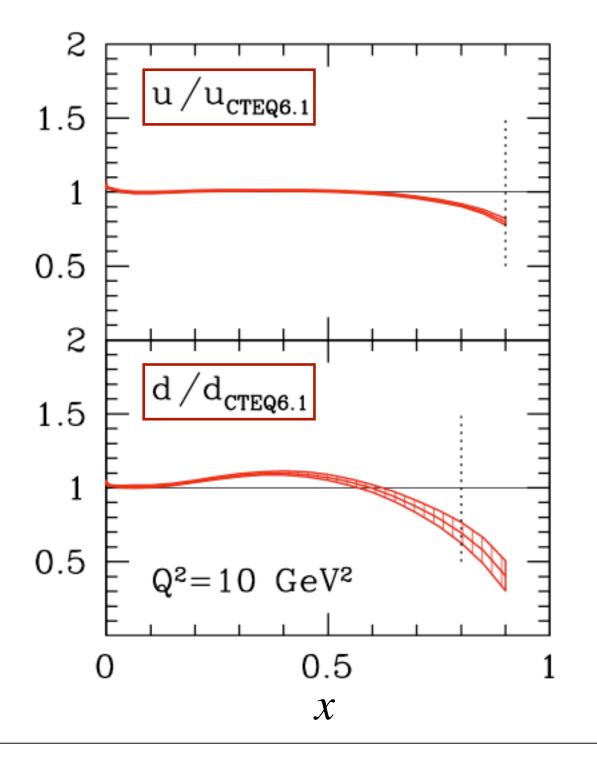
- important interplay between TMCs and higher twist:
   HT alone *cannot* accommodate full Q<sup>2</sup> dependence
- stable leading twist when <u>both</u> TMCs and HTs included

CTEQ6X –  $1/Q^2$  corrections



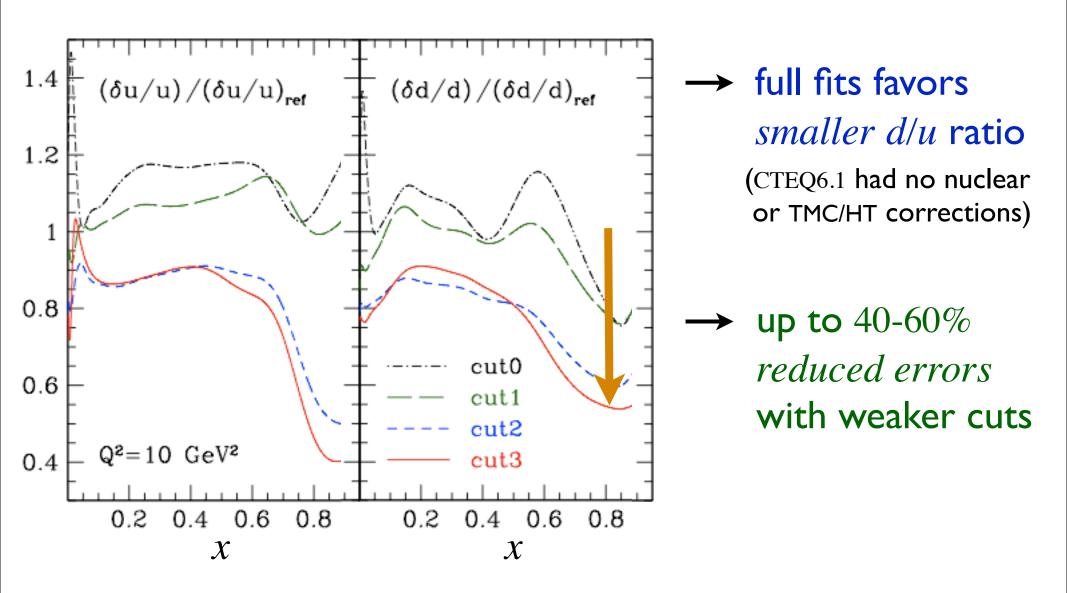
- important interplay between TMCs and higher twist:
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- stable leading twist when <u>both</u> TMCs and HTs included
- prescription dependence of TMCs may limit extraction of higher twist contributions

CTEQ6X – final PDF results



### → full fits favors smaller d/u ratio (CTEQ6.1 had no nuclear or TMC/HT corrections)

### CTEQ6X – final PDF results

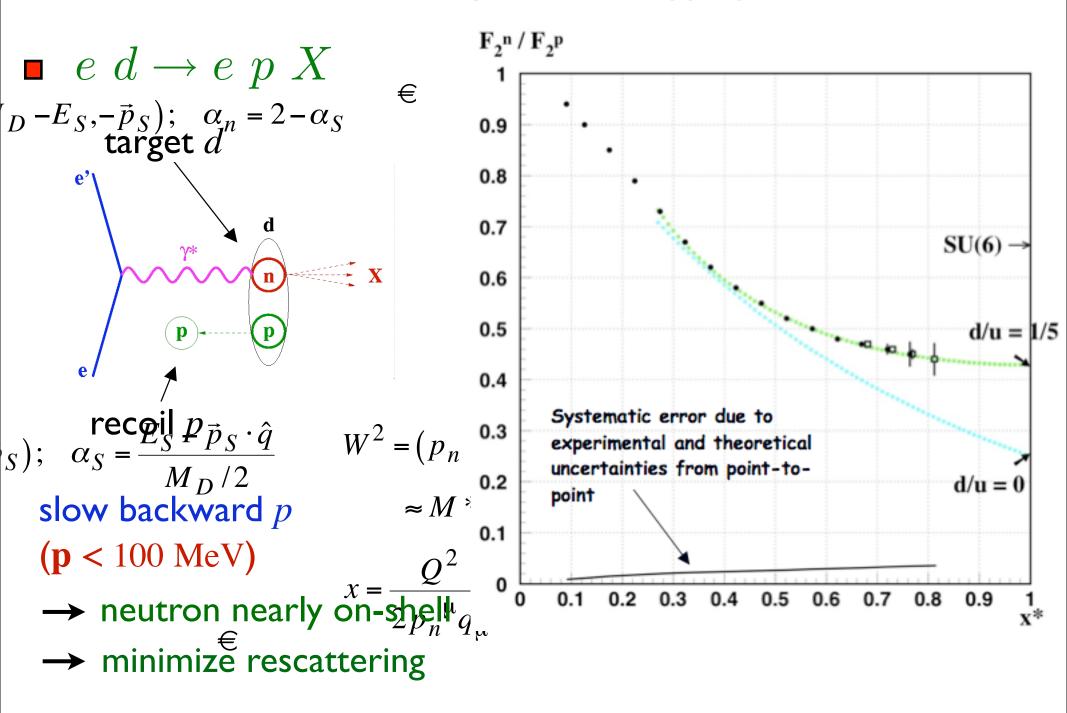


Accardi et al., Phys. Rev. D 81, 034016 (2010)

# CTEQ6X – implications

- Stable leading twist PDFs for  $W \gtrsim 1.7 \text{ GeV } \& Q^2 \gtrsim 1.5 \text{ GeV}^2$ - provided nuclear and subleading  $1/Q^2$  corrections included
  - → advocates using (high statistics) low-W data to constrain large-x PDFs
- Prescription dependence of TMCs limits extraction of higher twist matrix elements
  - $\rightarrow$  TMC / HT interplay needs to be better understood
- *Nuclear corrections* in deuteron significant at for  $x \gtrsim 0.6$ 
  - $\rightarrow$  completely obscure *d* quark extraction at large-*x*, require new methods free of nuclear uncertainties

# New methods – spectator<sup>2</sup> tagging $Q^{2}$ (BONUS')

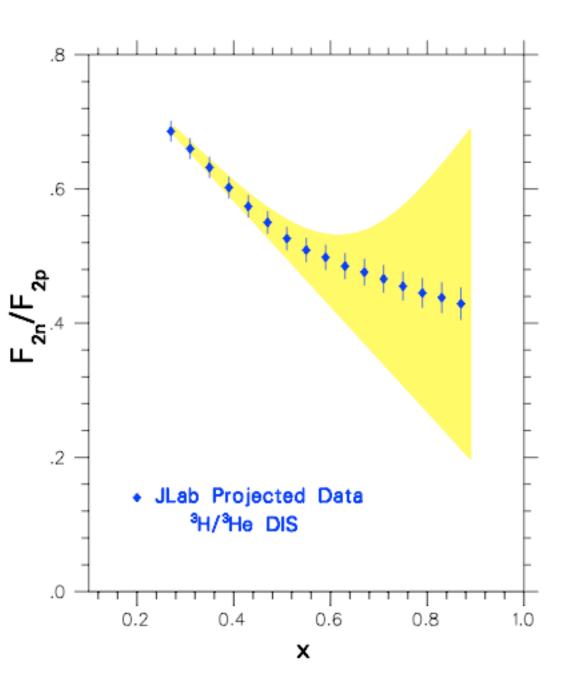


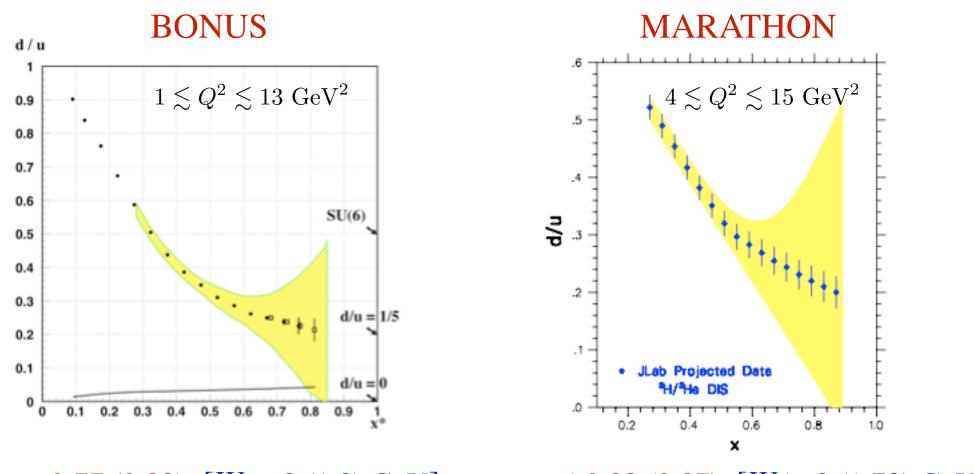
New methods – DIS from *A*=3 ("MARATHON")

extract n/p ratio from ratio of A=3 structure functions

$$\frac{F_2^n}{F_2^p} = \frac{2\mathcal{R} - F_2^{^{3}\text{He}}/F_2^{^{3}\text{H}}}{2F_2^{^{3}\text{He}}/F_2^{^{3}\text{H}} - \mathcal{R}}$$

→ ratio of <sup>3</sup>He to <sup>3</sup>H EMC ratios cancels to ~1% for x < 0.85





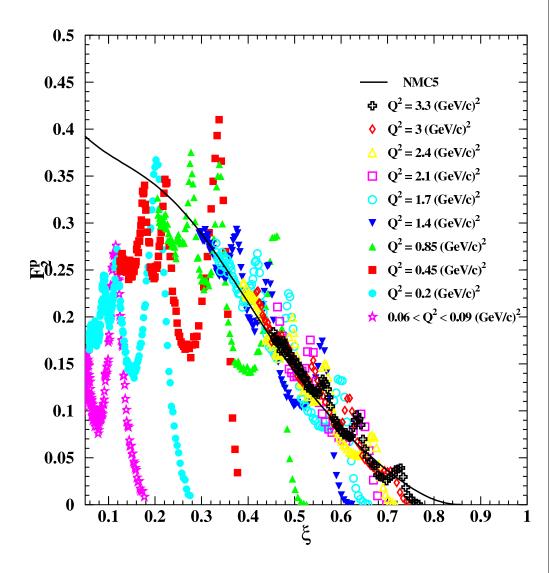
 $x \le 0.77 \ (0.83) \ [W \ge 2 \ (1.8) \ \text{GeV}]$ 

 $x \le 0.83 \ (0.87) \ [W \ge 2 \ (1.73) \ \text{GeV}]$ 

• theoretical uncertainties similar to  $x \sim 0.85$ 

other: π structure function; <sup>3</sup>A(e,e'd)X; (ideally) neutron tagging for cross-check! other: EMC effect in A=3; isospin-dependence of nuclear corrections; SIDIS

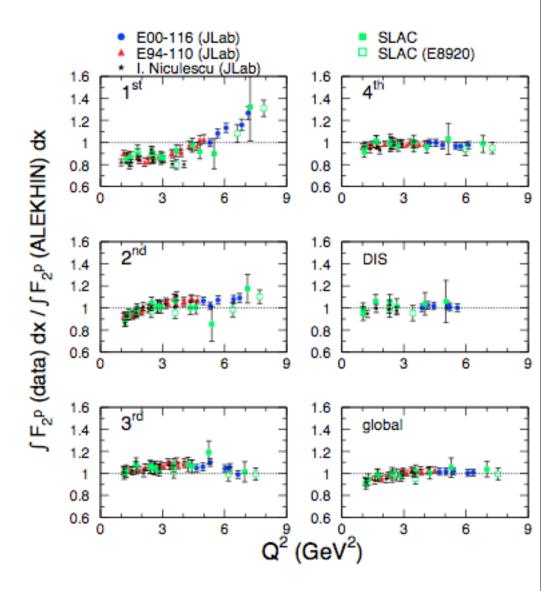
average over resonances (strongly  $Q^2$  dependent)  $\approx$  leading twist str. fn. (~  $Q^2$  independent)



Niculescu et al., PRL 85, 1182 (2000)

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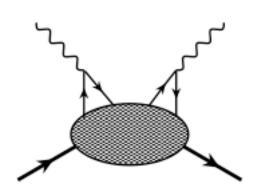
■ duality violation for proton  $\lesssim 10\%$ , integrated over *x* 



Malace et al., PRC 80, 035207 (2009)

Is duality in the proton a coincidence?

 $\rightarrow$  consider model with symmetric nucleon wave function



<u>cat's ears diagram</u> (4-fermion higher twist ~  $1/Q^2$ )  $\propto \sum_{i \neq j} e_i e_j \sim \left(\sum_i e_i\right)^2 - \sum_i e_i^2$ 

coherent

incoherent

Is duality in the proton a coincidence?

 $\rightarrow$  consider model with symmetric nucleon wave function

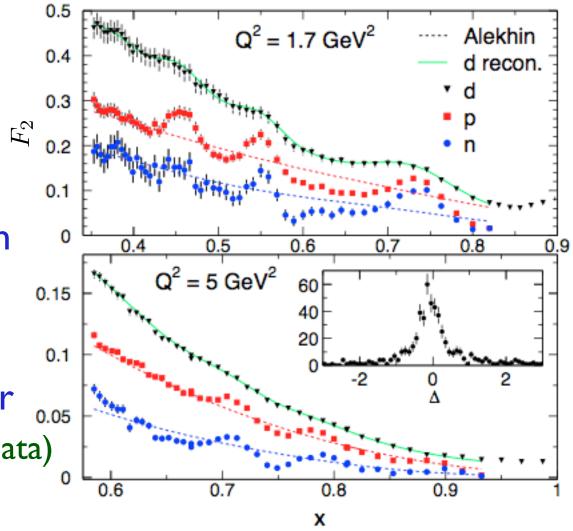
<u>cat's ears diagram</u> (4-fermion higher twist  $\sim 1/Q^2$ )  $\propto \sum_{i \neq j} e_i e_j \sim \left(\sum_i e_i\right)^2 - \sum_i e_i^2$ coherent incoherent HT ~ 1 -  $\left(2 \times \frac{4}{9} + \frac{1}{9}\right) = 0!$ proton HT ~ 0 -  $\left(\frac{4}{9} + 2 \times \frac{1}{9}\right) \neq 0$ 

Brodsky, hep-ph/0006310

need to test duality in the neutron!

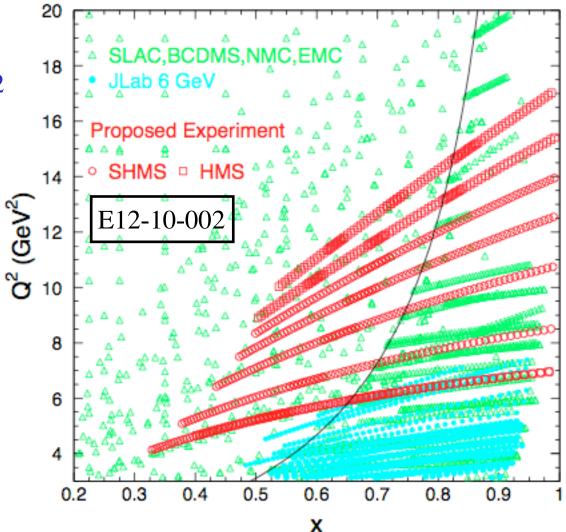
neutron

- average over resonances (strongly  $Q^2$  dependent)  $\approx$  leading twist str. fn. (~  $Q^2$  independent)
- duality violation for proton  $\lesssim 10\%$ , integrated over *x* 
  - recently confirmed also for *neutron* (from inclusive *p*, *d* data)
     → duality *not* accidental!



Malace et al., PRL 104, 102001 (2010)

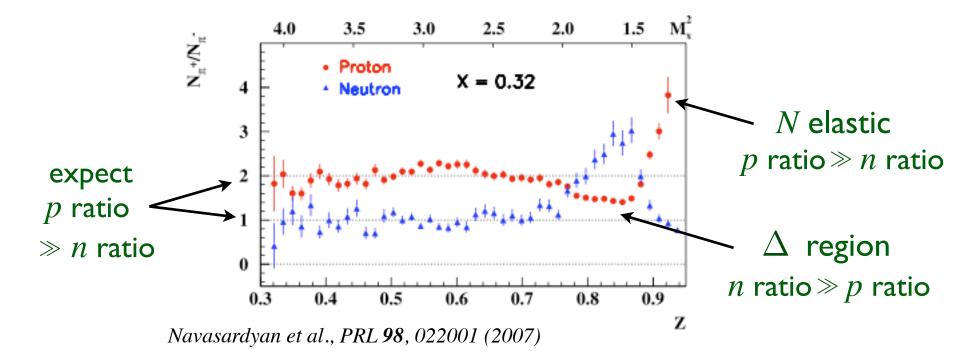
- currently duality studies limited to  $Q^2 \lesssim 6 \text{ GeV}^2$ , beyond which no resonance data exist
- with 12 GeV will map out resonances to Q<sup>2</sup>~17 GeV<sup>2</sup>
- high-precision low-W
   data base will constrain
   PDFs at larger x values
  - → input into CTEQ6Xlike global QCD fits



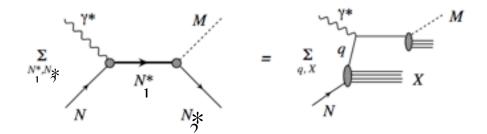
# Semi-inclusive DIS

- Semi-inclusive DIS at 12 GeV offers tremendous opportunity for determining
  - → flavor-spin decomposition of nucleon PDFs (*e.g. d/u*,  $\overline{d}/\overline{u}$ ,  $\Delta \overline{d} - \Delta \overline{u}$ )
  - → new distributions, not accessible in inclusive DIS (*e.g.* transversity, Sivers function, *etc*)
  - → <u>vital issue</u>: does factorization of scattering & fragmentation processes (needed for pQCD treatment) hold at these energies?
    - must establish *empirically* before method can be reliably utilized

#### 6 GeV data hint at intriguing quark-hadron duality in SIDIS



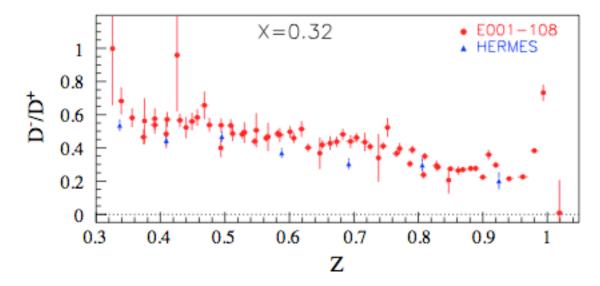
trends consistent with resonance model predictions



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	<sup>2</sup> 8,56 <sup>+</sup>	$^{4}10,56^{+}$	<sup>2</sup> 8,70 <sup>-</sup>	48,70-	$^{2}10,70^{-}$	sum					
$\gamma p \rightarrow \pi^+ N_2^{\star}$	100 (100)	32 (-16)	64(64)	16 (-8)	4 (4)	216 (144)					
$\gamma p \to \pi^- N_2^\star$	0 (0)	24 (-12)	0 (0)	0 (0)	3 (3)	27 (-9)					
$\gamma n \to \pi^+ N_2^\star$	0 (0)	96(-48)	0 (0)	0 (0)	12(12)	108 (-36)					
$\gamma n \to \pi^- N_2^*$	25 (25)	8 (-4)	16 (16)	4 (-2)	1 (1)	54 (36)					

Close, WM, PRC 79, 055202 (2009)

#### 6 GeV data hint at intriguing quark-hadron duality in SIDIS

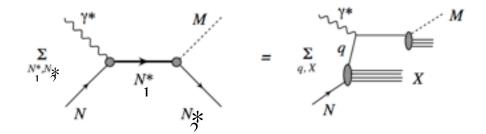


$$\frac{D^-}{D^+} = \frac{4 - N_\pi^+ / N_\pi^-}{4N_\pi^+ / N_\pi^- - 1}$$

resonance contributions to ratio cancel in quark model!

Navasardyan et al., PRL 98, 022001 (2007)

#### trends consistent with resonance model predictions



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Close, WM, PRC 79, 055202 (2009)

■ In parton model cross section has simple factorization:  $\frac{d\sigma}{dx \, dQ^2 \, dz_h} \sim \sum_q e_q^2 \, q(x, Q^2) \, D_q^h(z_h, Q^2)$   $\sum_{h=1}^{n} \frac{p_h \cdot p}{q \cdot p} \to \frac{E_h}{\nu}$ 

• At finite  $Q^2$  hadronic mass corrections (target & fragment):

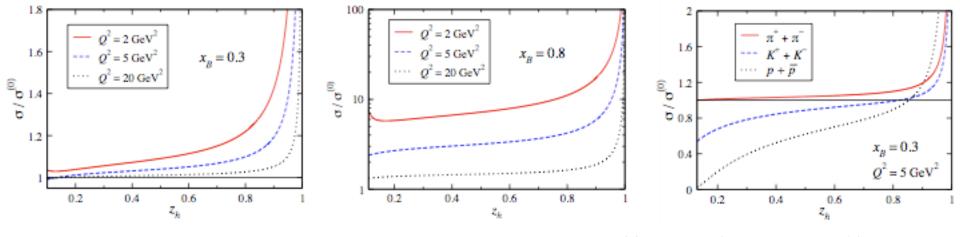
$$\frac{d\sigma}{dx \, dQ^2 \, dz_h} \sim \sum_{q} e_q^2 \, q(\xi_h, Q^2) \, D_q^h(\zeta_h, Q^2)$$
  
$$\xi_h = \xi \left( 1 + \frac{m_h^2}{\zeta_h Q^2} \right) \qquad \zeta_h = \frac{z_h}{2} \frac{\xi}{x} \left( 1 + \sqrt{1 - \frac{4x^2 M^2 m_h^2}{z_h^2 Q^4}} \right)$$

Mulders (2001), Albino et al. (2007), Hobbs et al. (2009)

→ *hadron* mass dependence in quark *distribution* function

→ factorization breakdown (quantifiable!)

# Ratio $\sigma/\sigma^{(0)}$ of corrected to uncorrected (massless limit) $\pi^+ + \pi^-$ cross sections



Hobbs, Accardi, WM, JHEP 11, 084 (2009)

- $\rightarrow$  dramatic rise as  $z_h \rightarrow 1$ , more pronounced at low  $Q^2$
- → downward correction at small  $z_h$  for heavier hadrons driven by suppression of PDF from  $(1 + m_h^2/\zeta_h Q^2)$ factor in  $\xi_h$  (>  $\xi$ )
  - → need to account for HMC at large x or small Q<sup>2</sup> even at 12 GeV

## Nucleon structure at large *x*: *spin-dependent*

Spin structure at large x

- Spin-dependent PDFs are even less well understood at large x than spin-averaged PDFs
- Predictions for  $x \rightarrow 1$  behavior:
  - $\rightarrow$  scalar diquark dominance

$$\frac{\Delta u}{u} \to 1$$
,  $\frac{\Delta d}{d} \to -\frac{1}{3}$   $A_1^{p,n} \to 1$ 

 $\rightarrow$  hard gluon exchange

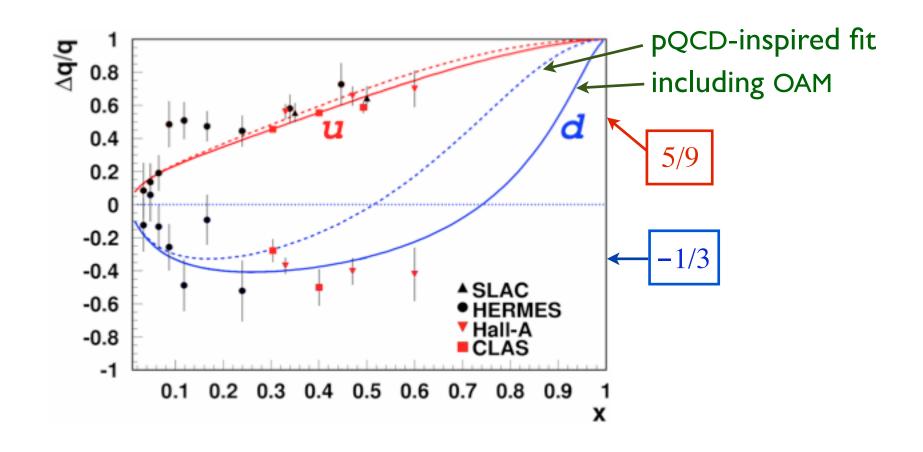
$$\frac{\Delta u}{u} \to 1 \ , \ \ \frac{\Delta d}{d} \to 1 \qquad \qquad A_1^{p,n} \to 1$$

 $\rightarrow$  spin-flavor symmetry

$$\frac{\Delta u}{u} = \frac{2}{3} , \quad \frac{\Delta d}{d} = -\frac{1}{3} \qquad A_1^p = \frac{5}{9} , \quad A_1^n = 0$$

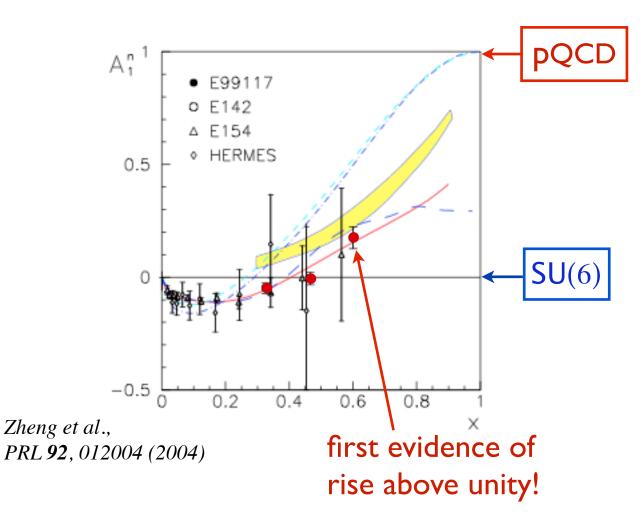
Spin PDFs almost completely unconstrained for  $x \gtrsim 0.6$ 

### Spin structure at large x



- $\rightarrow$  data consistent with SU(6) predictions (*cf.* unpolarized)
- → dramatic behavior expected in  $\Delta d/d$  for  $x \gtrsim 0.6$ reflects upturn in neutron asymmetry  $A_1^n$

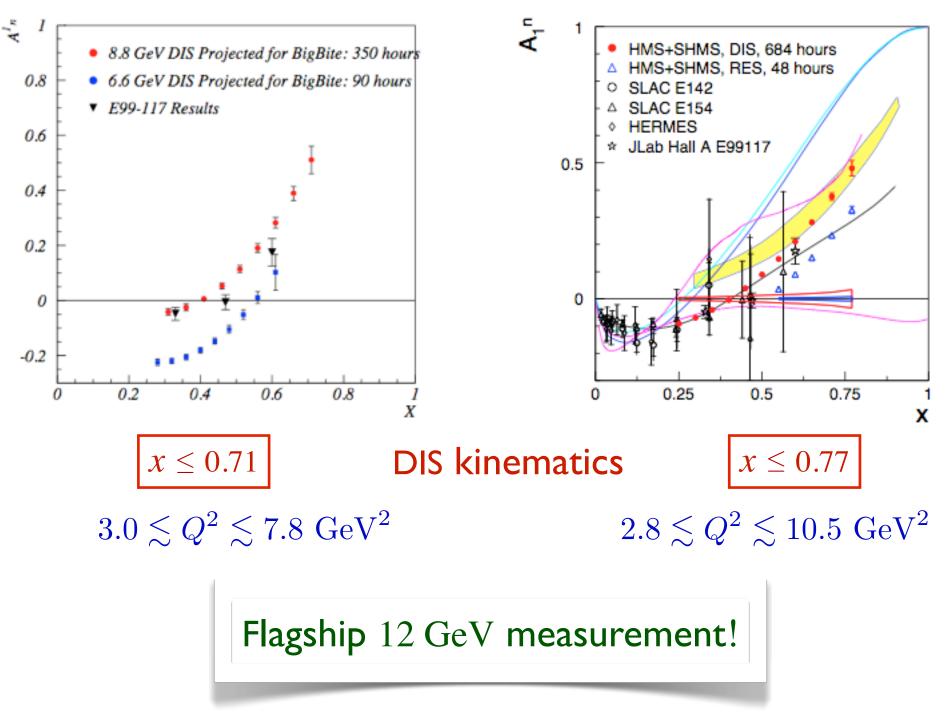
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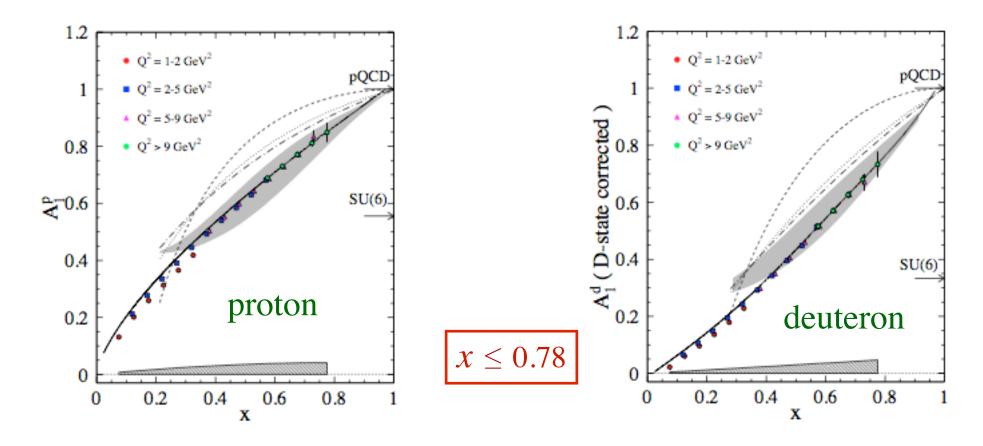
#### E12-06-122 (Hall A)





#### E12-06-109 (Hall B)

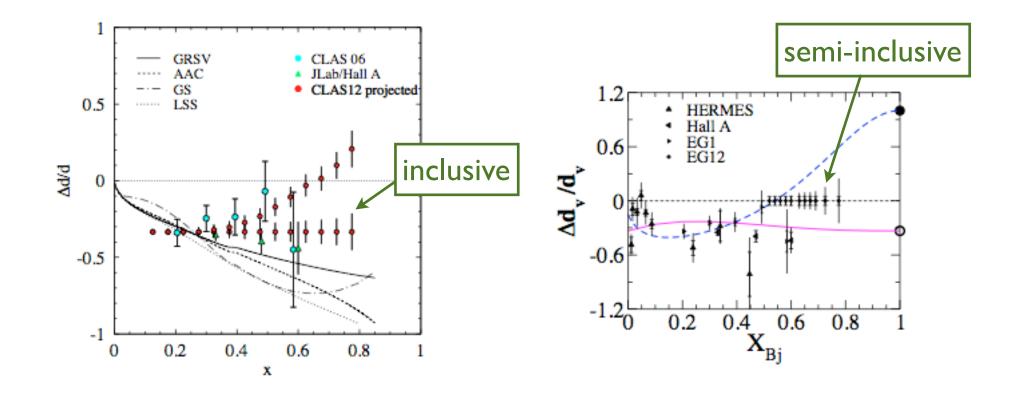
Comprehensive program of *inclusive* and *semi-inclusive* measurements with CLAS12



**Reconstruct large-** $x \Delta u/u \& \Delta d/d$  from any *two* of  $A_1^p, A_1^d, A_1^{^{3}\text{He}}$  (and d/u ratio!)

#### E12-06-109 (Hall B)

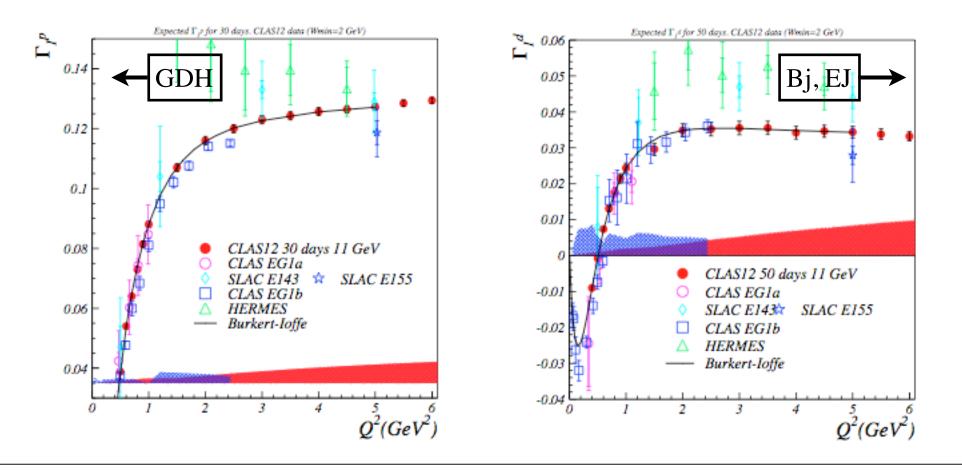
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#### E12-06-109 (Hall B)

- Comprehensive program of *inclusive* and *semi-inclusive* measurements with CLASI2
  - $\rightarrow$  integrals over x allow direct comparison with *lattice* QCD
  - $\rightarrow Q^2$  dependence allows extraction of (leading & higher twist) matrix elements

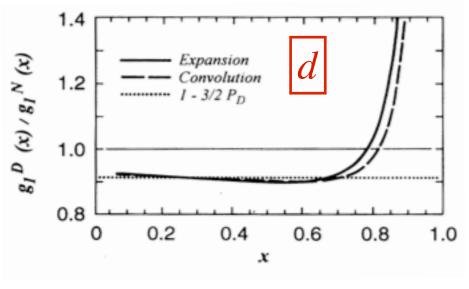


Spin structure at large x – nuclear effects

- Extracting neutron information from <sup>3</sup>He or *d* data requires subtraction of nuclear corrections
- Usual prescription accounts for *effective polarizations* of bound nucleons, assuming  $x \& Q^2$  independent effects

$$g_1^A = \langle \sigma_z \rangle^p \ g_1^p + \langle \sigma_z \rangle^n \ g_1^n$$

- $\rightarrow$  reasonable approximation for  $x \lesssim 0.65$
- $\rightarrow$  breaks down for  $x \gtrsim 0.7$



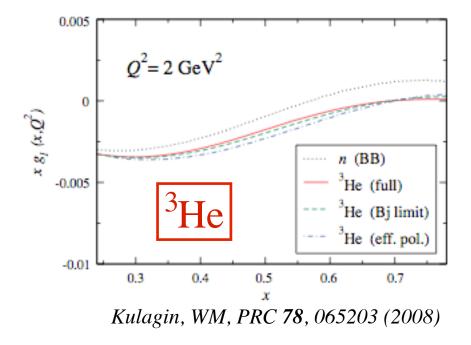
WM, Piller, Kulagin, Thomas, Weise (1995)

Spin structure at large x – nuclear effects

- Extracting neutron information from <sup>3</sup>He or *d* data requires subtraction of nuclear corrections
- Usual prescription accounts for *effective polarizations* of bound nucleons, assuming  $x \& Q^2$  independent effects

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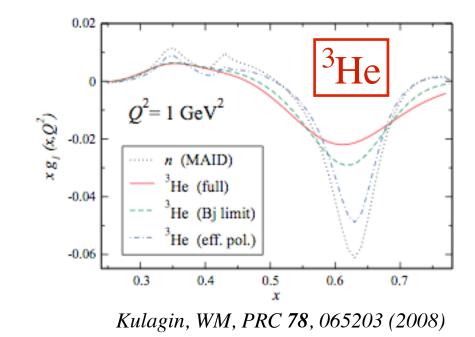


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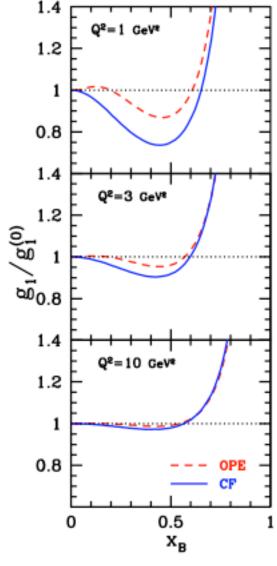
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Spin structure at large x – finite  $Q^2$ 

- Limited  $Q^2$  requires careful treatment of  $1/Q^2$  corrections
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  - → expect cancellation with dynamical HTs for stable LTs (*cf*. CTEQX)



Accardi, WM, PLB **670**, 114 (2008)

Spin structure at large x – finite  $Q^2$ 

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1.2

0.8

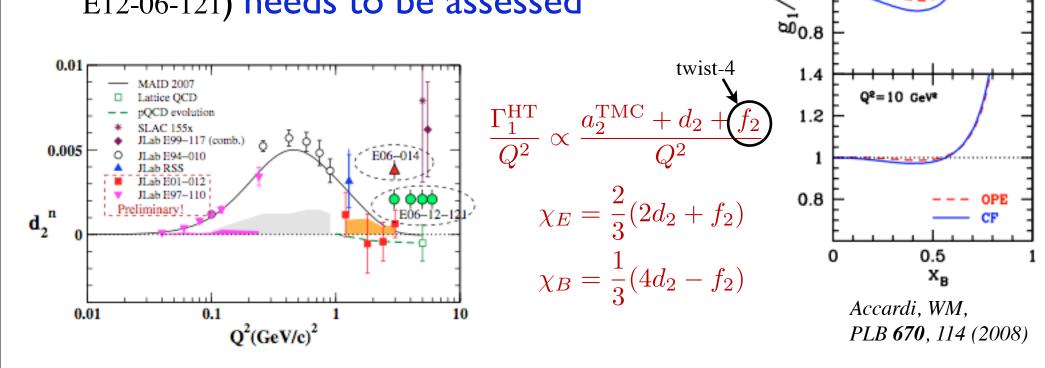
1.4

1.2

g10)

0<sup>2</sup>=3 GeV<sup>8</sup>

- $\rightarrow$  prescription dependence of TMCs
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- Impact on extraction of higher twist matrix elements (e.g. color polarizabilities, E12-06-121) needs to be assessed

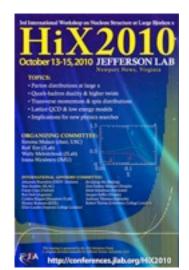


## Summary

- Measurement of structure functions at large x at 12 GeV will resolve long-standing questions about  $x \rightarrow 1$  behavior of PDFs
  - $\rightarrow$  dramatic behavior for  $x \gtrsim 0.6$  best revealed with *highest possible x*
- Need largest  $Q^2$  range possible to constrain subleading  $1/Q^2$  corrections
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- Ongoing interest in & support for high x physics



The End