
**Extraction of nucleon resonances from global
analysis of meson production reactions at
EBAC**

Hiroyuki Kamano

(Excited Baryon Analysis Center, Jefferson Lab)

In collaboration with

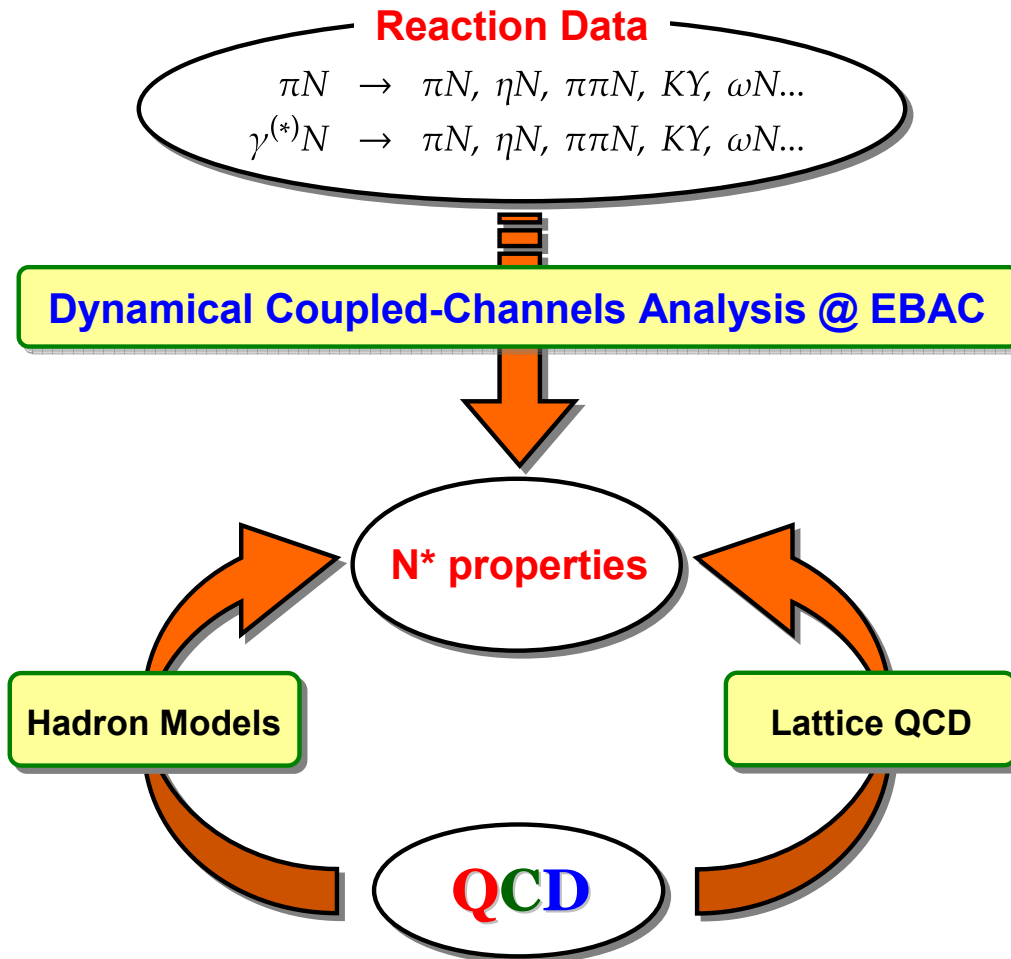
**B. Julia-Diaz, T.-S. H. Lee, A. Matsuyama,
S. Nakamura, T. Sato, N. Suzuki**

BARYONS'10, December 7th – 11th, Osaka, Japan

Excited Baryon Analysis Center (EBAC) of Jefferson Lab

Founded in January 2006

<http://ebac-theory.jlab.org/>



Objectives and goals:

Through the **comprehensive analysis** of world data of πN , γN , $N(e,e')$ reactions,

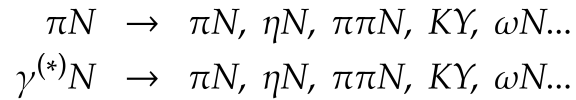
- ✓ Determine N^* spectrum (pole positions)
- ✓ Extract N^* form factors
(e.g., N - N^* e.m. transition form factors)
- ✓ Provide **reaction mechanism information** necessary for interpreting N^* properties, structures and dynamical origins

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Reaction Data



Dynamical Coupled-Channels Analysis @ EBAC

“Dynamical coupled-channels model of meson production reactions”

A. Matsuyama, T. Sato, T.-S.H. Lee Phys. Rep. 439 (2007) 193

QCD

Objectives and goals:

Through the **comprehensive analysis** of world data of πN , γN , $N(e,e')$ reactions,

... determine N^* spectrum (pole positions)

✓ Provide **reaction mechanism information** necessary for interpreting N^* properties, structures and dynamical origins

Dynamical coupled-channels model of EBAC (EBAC-DCC model)

For details see Matsuyama, Sato, Lee, Phys. Rep. 439,193 (2007)

- ✓ Partial wave (LSJ) amplitude of $a \rightarrow b$ reaction:

$$T_{a,b}^{(LSJ)}(p_a, p_b; E) = V_{a,b}^{(LSJ)}(p_a, p_b) + \sum_c \int_0^\infty q^2 dq V_{a,c}^{(LSJ)}(p_a, q) G_c(q; E) T_{c,b}^{(LSJ)}(q, p_b; E)$$

coupled-channels effect

- ✓ Reaction channels:

$$a, b, c = (\gamma^{(*)}N, \pi N, \eta N, \pi\Delta, \sigma N, \rho N, K\Lambda, K\Sigma, \dots)$$

$\pi\pi N$

- ✓ Transition potentials:

$$V_{a,b} = v_{a,b} + \sum_{N^*} \frac{\Gamma_{N^*,a}^\dagger \Gamma_{N^*,b}}{E - M_{N^*}}$$

exchange potentials
of ground state
mesons and baryons

bare N^* states

Dynamical coupled-channels model of EBAC (EBAC-DCC model)

For details see Matsuyama, Sato, Lee, Phys. Rep. 439,193 (2007)

7. $\pi(k, i) + N(p) \rightarrow \rho(k', j) + N(p')$:

$$\bar{V}(7) = \bar{V}_a^7 + \bar{V}_b^7 + \bar{V}_c^7 + \bar{V}_d^7 + \bar{V}_e^7$$

with

$$\bar{V}_a^7 = i \frac{f_{\pi NN}}{m_\pi} g_{\rho NN} \Gamma_{\rho'} S_N(p+k) \not{k} \gamma_5 \tau^i,$$

$$\bar{V}_b^7 = i \frac{f_{\pi NN}}{m_\pi} g_{\rho NN} \not{k} \gamma_5 \tau^i S_N(p-k') \Gamma_{\rho'},$$

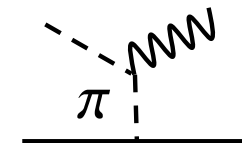
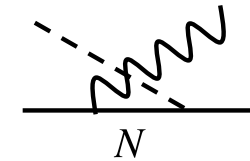
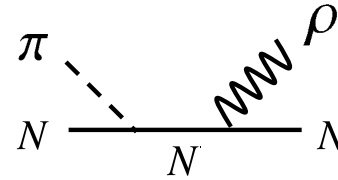
$$\bar{V}_c^7 = \frac{f_{\pi NN}}{m_\pi} g_{\rho\pi\pi} \epsilon_{ijl} \tau^l \frac{(q-k) \cdot \epsilon_{\rho'}^* \not{q} \gamma_5}{q^2 - m_\pi^2},$$

$$\bar{V}_d^7 = -\frac{f_{\pi NN}}{m_\pi} g_{\rho NN} \not{\epsilon}_{\rho'}^* \gamma_5 \epsilon_{jil} \tau^l,$$

$$\bar{V}_e^7 = \frac{g_{\omega NN} g_{\omega\pi\rho}}{m_\omega} \delta_{ij} \frac{\epsilon_{\alpha\beta\gamma\delta} \epsilon_{\rho'}^{*\alpha} k'^\beta k^\gamma}{q^2 - m_\omega^2} \left[\gamma^\delta + \frac{\kappa_\omega}{4m_N} (\gamma^\delta \not{q} - \not{q} \gamma^\delta) \right],$$

where

$$\Gamma_{\rho'} = \frac{\tau^j}{2} \left[\not{\epsilon}_{\rho'}^* + \frac{\kappa_\rho}{4m_N} (\not{\epsilon}_{\rho'}^* \not{k}' - \not{k}' \not{\epsilon}_{\rho'}^*) \right].$$



Dynamical coupled-channels model of EBAC (EBAC-DCC model)

For details see Matsuyama, Sato, Lee, Phys. Rep. 439,193 (2007)

- ✓ Partial wave (LSJ) amplitude of a → b reaction:

$$T_{a,b}^{(LSJ)}(p_a, p_b; E) = V_{a,b}^{(LSJ)}(p_a, p_b) + \sum_c \int_0^\infty q^2 dq V_{a,c}^{(LSJ)}(p_a, q) G_c(q; E) T_{c,b}^{(LSJ)}(q, p_b; E)$$

coupled-channels effect

- ✓ Reaction amplitude

$$a, \quad \Gamma_{N^*,a(LS)}(p) = \frac{1}{(2\pi)^{3/2}} \frac{1}{\sqrt{m_N}} \left[\frac{p}{m_\pi} \right]^L C_{N^*,a} \left[\frac{\Lambda_{N^*,a(LS)}^2}{\Lambda_{N^*,a(LS)}^2 + p^2} \right]^{(2+L)}$$

- ✓ Transition potentials:

$$V_{a,b} = v_{a,b} + \sum_{N^*} \frac{\Gamma_{N^*,a}^\dagger \Gamma_{N^*,b}}{E - M_{N^*}}$$

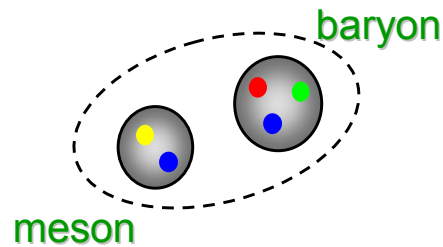
exchange potentials
of ground state
mesons and baryons

bare N* states

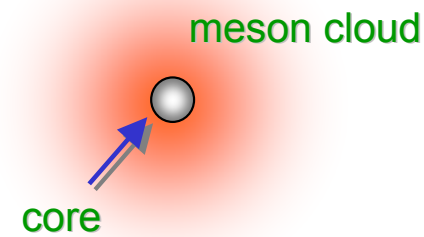
Dynamical coupled-channels model of EBAC (EBAC-DCC model)

For details see Matsuyama, Sato, Lee, Phys. Rep. 439,193 (2007)

Physical N^* s will be a “superposition” of the two pictures:



$$|N^*\rangle = |MB\rangle$$



$$|N^*\rangle = |qqq\rangle + |m.c.\rangle$$

transition potentials.

 $V_{a,b}$
 $=$
 $v_{a,b}$
 $+$

$$\sum_{N^*} \frac{\Gamma_{N^*,a}^\dagger \Gamma_{N^*,b}}{E - M_{N^*}}$$

exchange potentials
of ground state
mesons and baryons

bare N^* states

Strategy for N^* study at EBAC

Stage 1

Construct a reaction model through the comprehensive analysis of meson production reactions

Requires careful **analytic continuation** of amplitudes to **complex energy plane**

→ Suzuki, Sato, Lee PRC79 025205; PRC82 045206

Stage 2

Extract resonance information from the constructed reaction model

- N^* pole positions; $N^* \rightarrow \gamma N$, MB transition form factors
- Confirm/reject N^* with low-star status; Search for new N^*

Stage 3

Make a connection to hadron structure calculations; Explore the structure of the N^* states.

- Quark models, DSE, Large N_c , Holographic QCD,...

EBAC-DCC analysis (2006-2009)

$\pi N, \eta N, \pi\pi N$ ($\pi\Delta, \rho N, \sigma N$) coupled-channels calculations were performed.

Hadronic part

- ✓ $\pi N \rightarrow \pi N$: Used for constructing a hadronic model **up to $W = 2$ GeV**.
Julia-Diaz, Lee, Matsuyama, Sato, PRC76 065201 (2007)
- ✓ $\pi N \rightarrow \eta N$: Used for constructing a hadronic model **up to $W = 2$ GeV**
Durand, Julia-Diaz, Lee, Saghai, Sato, PRC78 025204 (2008)
- ✓ $\pi N \rightarrow \pi\pi N$: First full dynamical coupled-channels calculation **up to $W = 2$ GeV**.
Kamano, Julia-Diaz, Lee, Matsuyama, Sato, PRC79 025206 (2009)

Electromagnetic part

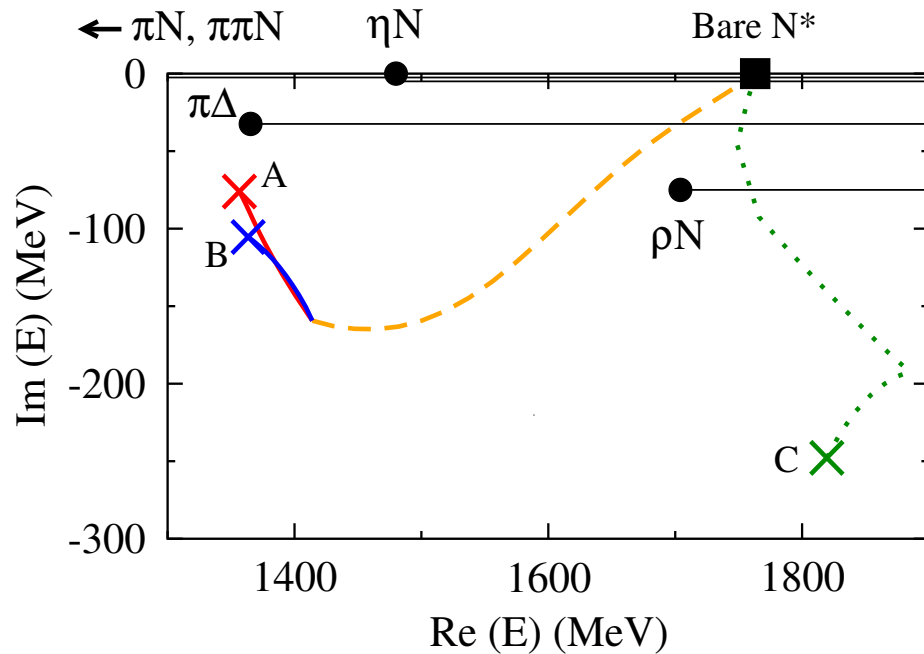
- ✓ $\gamma^{(*)} N \rightarrow \pi N$: Used for constructing a E.M. model **up to $W = 1.6$ GeV and $Q^2 = 1.5$ GeV²**
(photoproduction) Julia-Diaz, Lee, Matsuyama, Sato, Smith, PRC77 045205 (2008)
(electroproduction) Julia-Diaz, Kamano, Lee, Matsuyama, Sato, Suzuki, PRC80 025207 (2009)
- ✓ $\gamma N \rightarrow \pi\pi N$: First full dynamical coupled-channels calculation **up to $W = 1.5$ GeV**.
Kamano, Julia-Diaz, Lee, Matsuyama, Sato, PRC80 065203 (2009)

Dynamical coupled-channels effect on N^* poles and form factors

Suzuki, Julia-Diaz, Kamano, Lee, Matsuyama, Sato, PRL104 065203 (2010)

Suzuki, Sato, Lee, PRC82 045206 (2010)

Dynamical origin of P11 resonances



N-1st D13 e.m. transition form factor

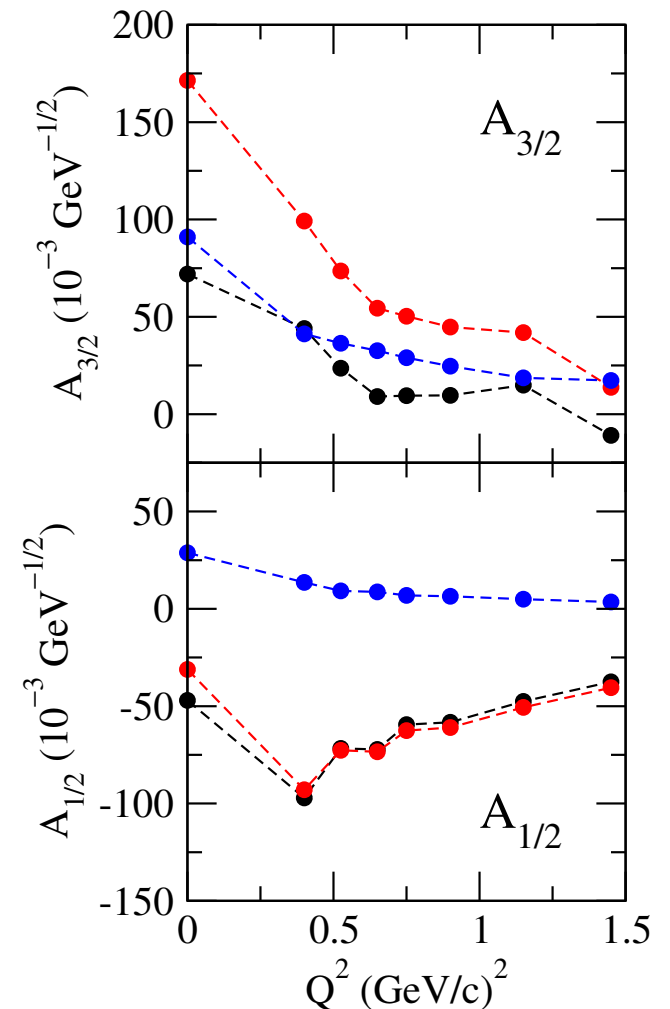
Re(Dressed vertex)



Im(Dressed vertex)



Bare vertex (Real)



Critical role of **non-trivial multi-channel reaction mechanisms** for interpreting the structure and dynamical origin of **nucleon resonances !!**

EBAC-DCC analysis: 2010 ~

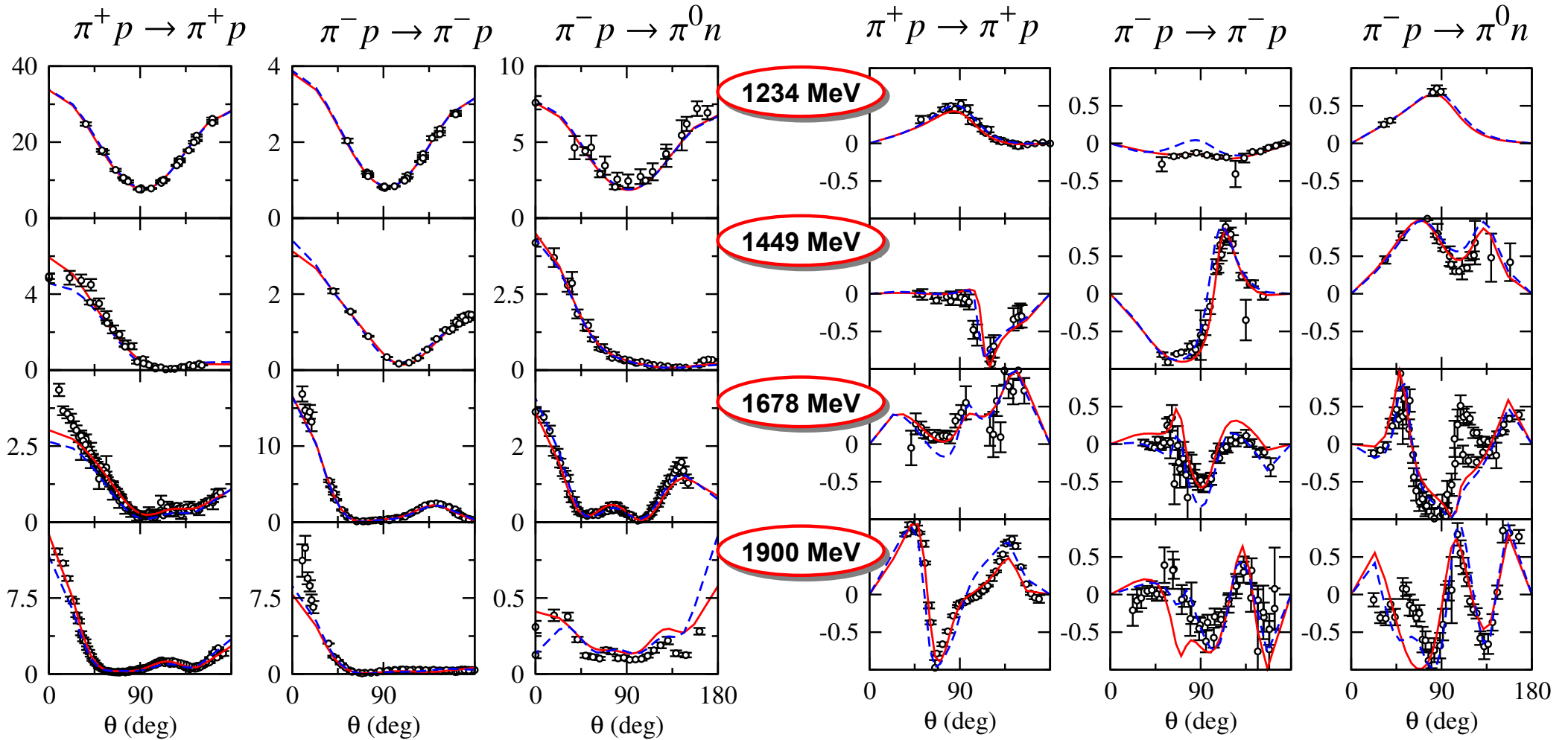
Full-combined analysis of γN , $\pi N \rightarrow \pi N$, ηN , KY reactions !!

	2006 ~ 2009	2010 ~
✓ # of coupled channels	5 channels ($\pi N, \eta N, \pi \Delta, \rho N, \sigma N$)	7 channels ($\pi N, \eta N, \pi \Delta, \rho N, \sigma N, K\Lambda, K\Sigma$)
✓ $\pi N \rightarrow \pi N$	< 2 GeV	< 2 GeV
✓ $\gamma N \rightarrow \pi N$	< 1.6 GeV	< 2 GeV
✓ $\pi N \rightarrow \eta N$	< 2 GeV	< 2 GeV
✓ $\gamma N \rightarrow \eta N$	—	< 2 GeV
✓ $\pi N \rightarrow KY$	—	< 2.1 GeV
✓ $\gamma N \rightarrow K\Lambda$	—	< 2.1 GeV

Pion-nucleon elastic scattering

Angular distribution $d\sigma/d\Omega$ (mb/sr)

Target polarization



Current model

(full combined analysis, **PRELIMINARY**)

Previous model (fitted to $\pi N \rightarrow \pi N$ data only)

[PRC76 065201 (2007)]



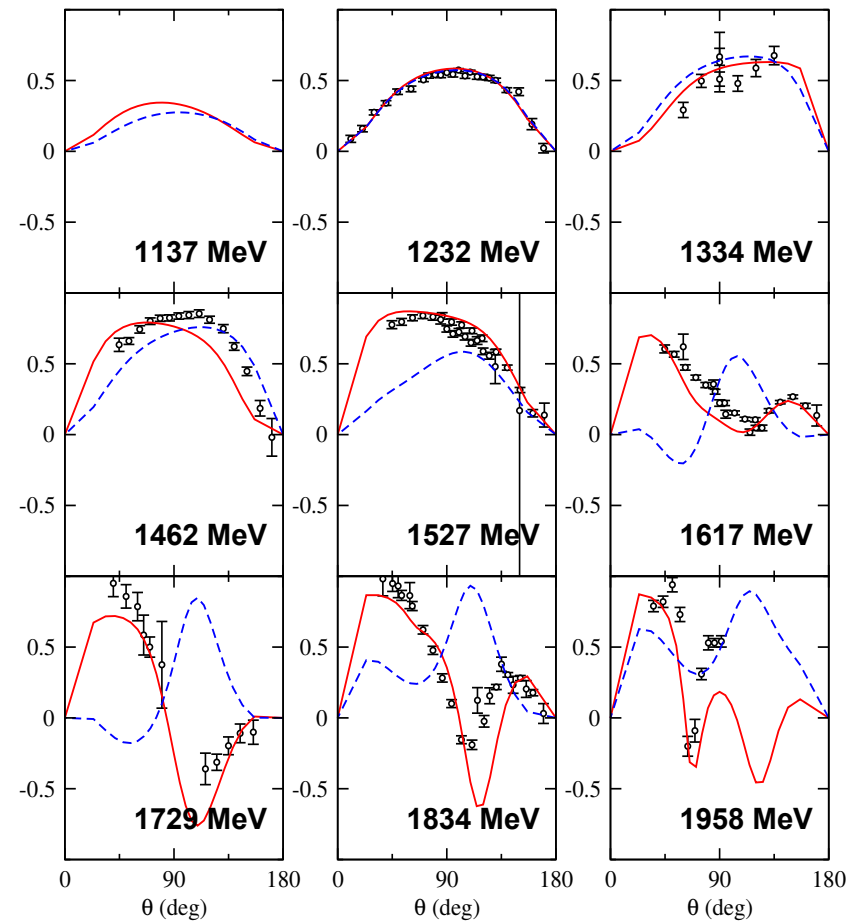
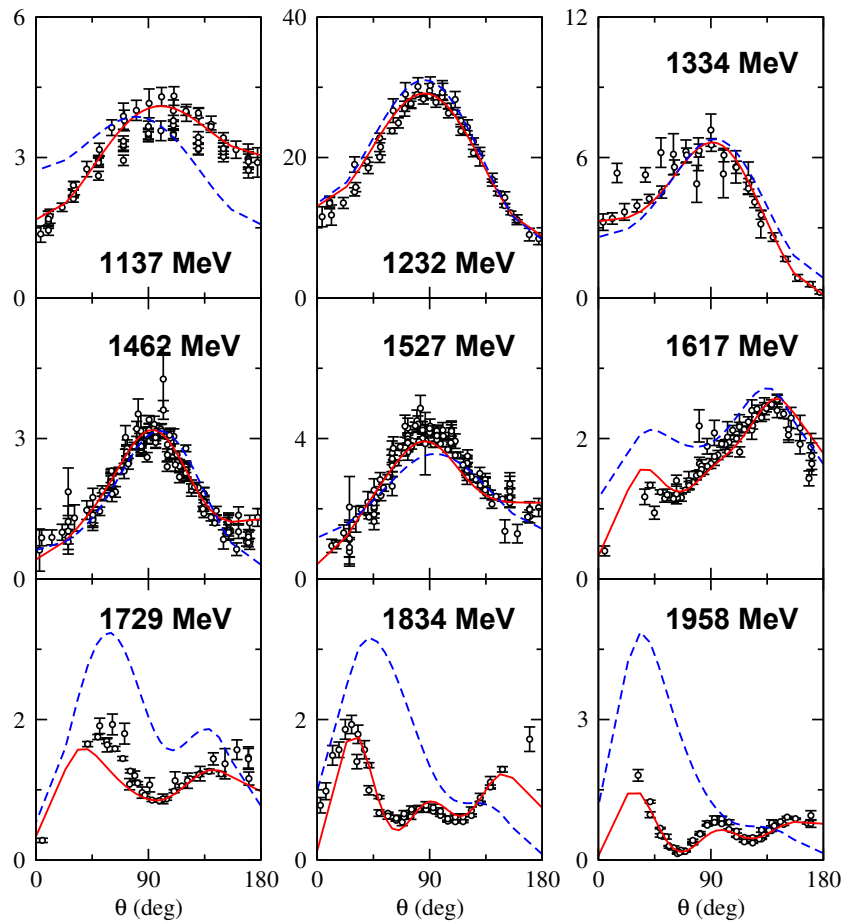
Single pion photoproduction

$$\gamma p \rightarrow \pi^0 p$$

Preliminary!!

Angular distribution $d\sigma/d\Omega$ ($\mu\text{b/sr}$)

Photon asymmetry Σ



— Current model
(full combined analysis, *preliminary*)

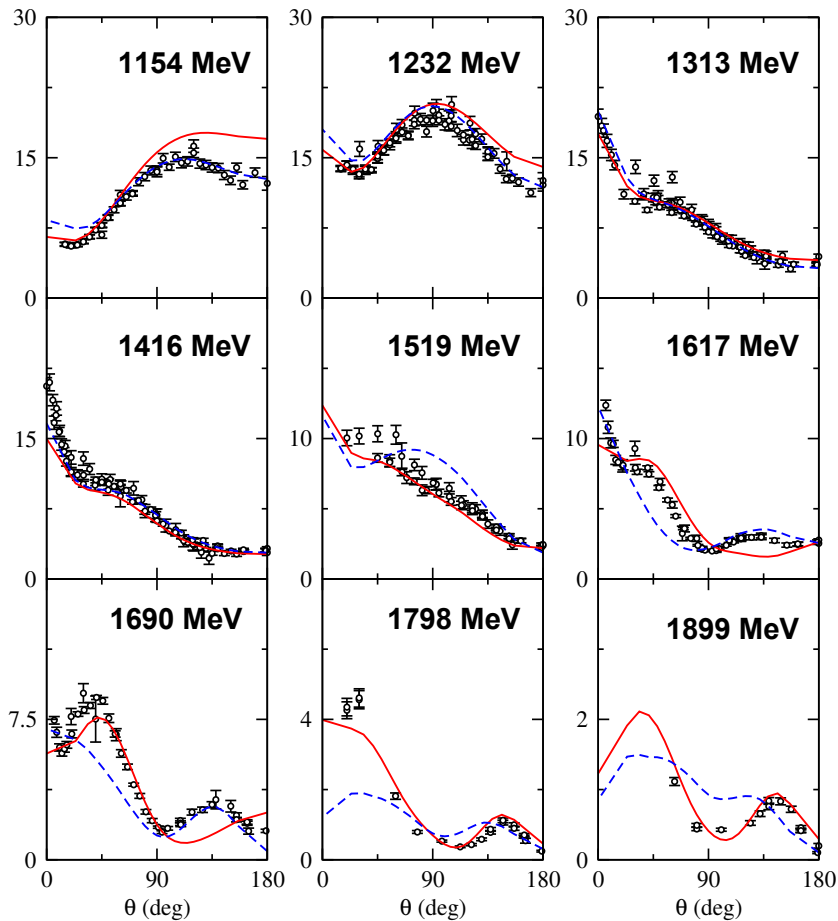
- - - Previous model (fitted to $\gamma N \rightarrow \pi N$ data *up to 1.6 GeV*)
[PRC77 045205 (2008)]

Single pion photoproduction

$$\gamma p \rightarrow \pi^+ n$$

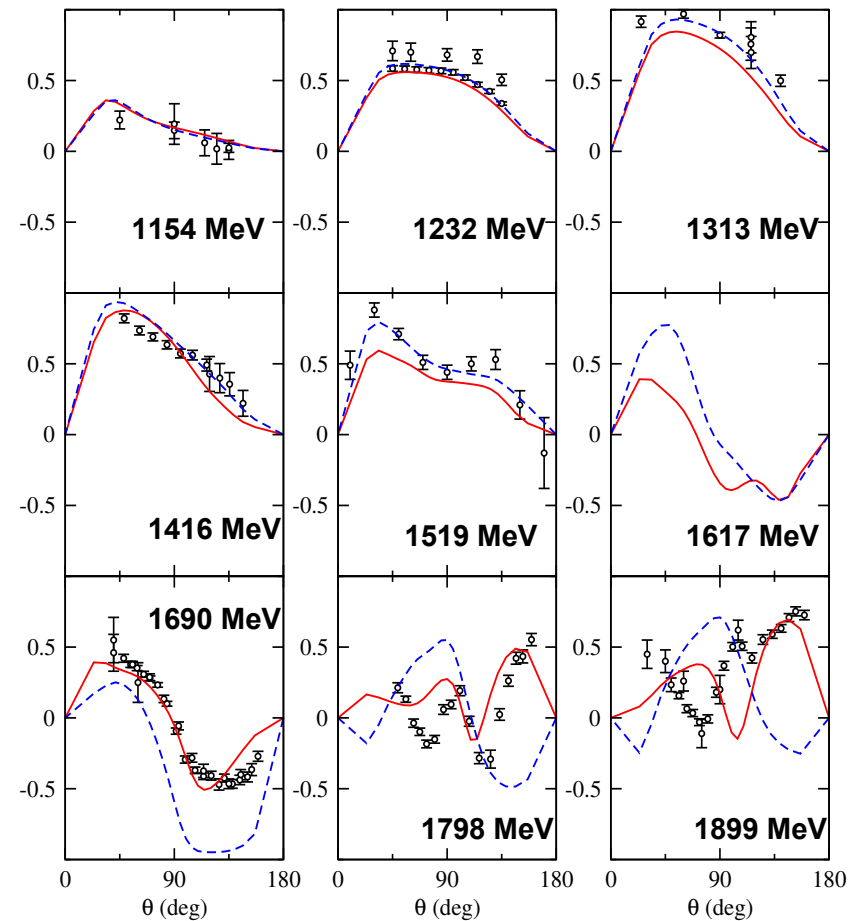
Preliminary!!

Angular distribution $d\sigma/d\Omega$ ($\mu\text{b/sr}$)



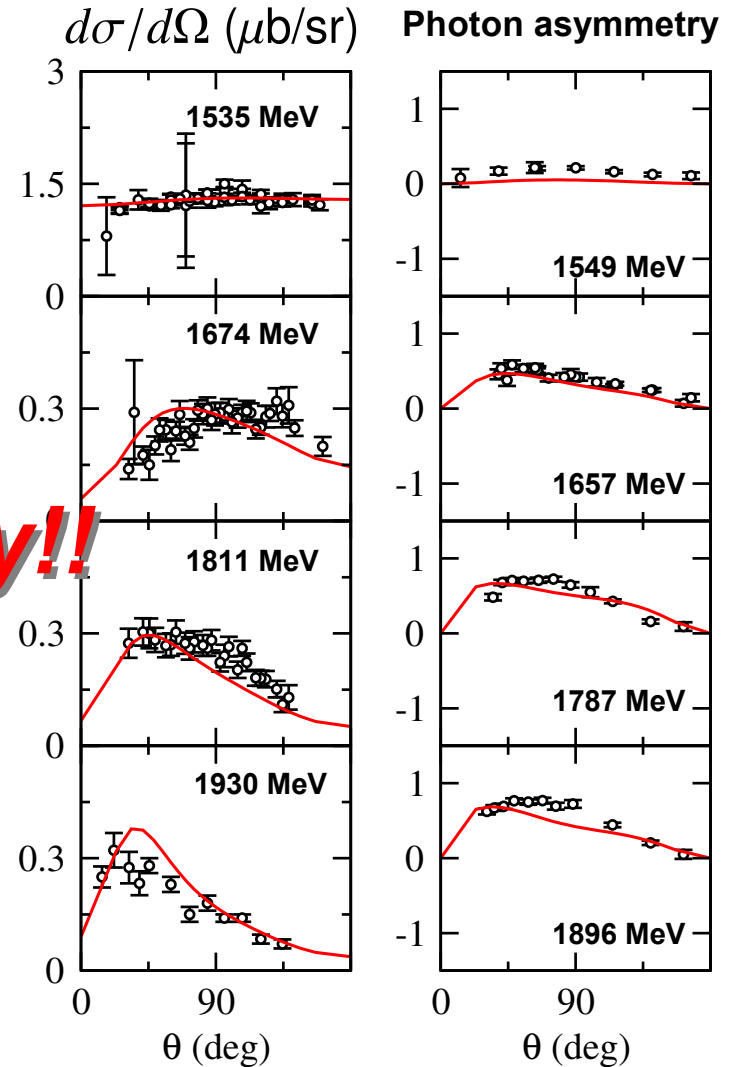
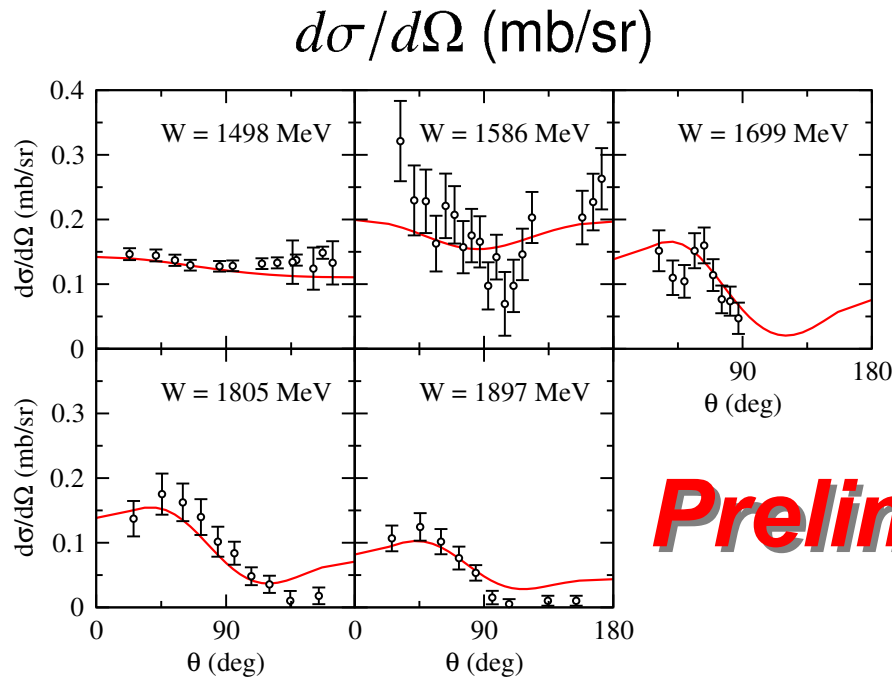
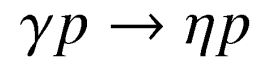
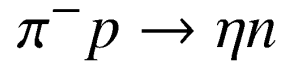
— Current model
(full combined analysis, *preliminary*)

Photon asymmetry Σ



--- Previous model (fitted to $\gamma N \rightarrow \pi N$ data *up to 1.6 GeV*)
[PRC77 045205 (2008)]

Eta production reactions



Preliminary!!

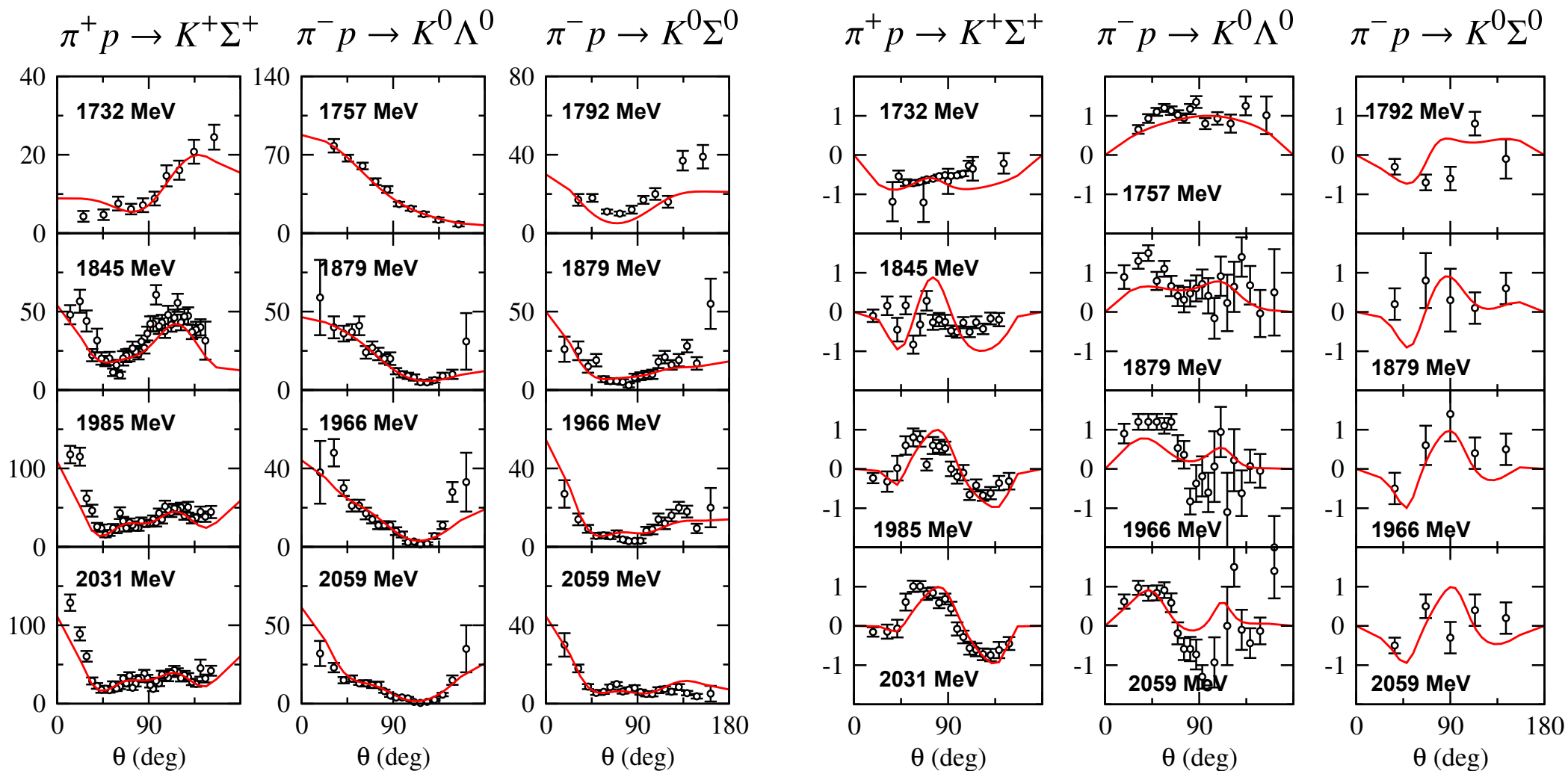
- ✓ Analyzed data up to **W = 2 GeV**.
- ✓ $\pi^- p \rightarrow \eta n$ data are selected following Durand et al. PRC78 025204.

$\pi N \rightarrow KY$ reactions

Preliminary!!

Angular distribution $d\sigma/d\Omega$ ($\mu\text{b/sr}$)

Recoil polarization



gamma p \rightarrow K⁺ Lambda

Preliminary!!

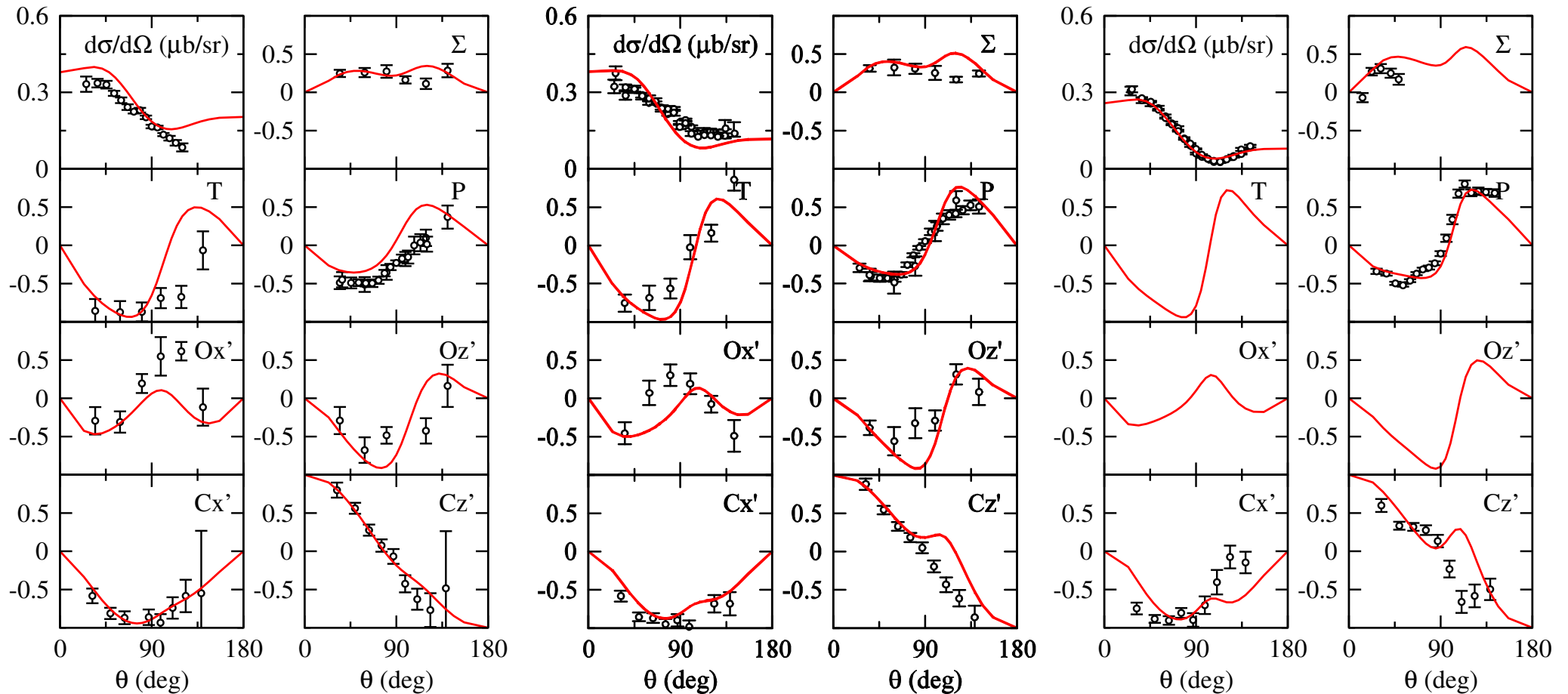
Formulae for calculating polarization observables

\rightarrow Sandorfi, Hoblit, Kamano, Lee arXiv:1010.0455

1781 MeV

1883 MeV

2041 MeV

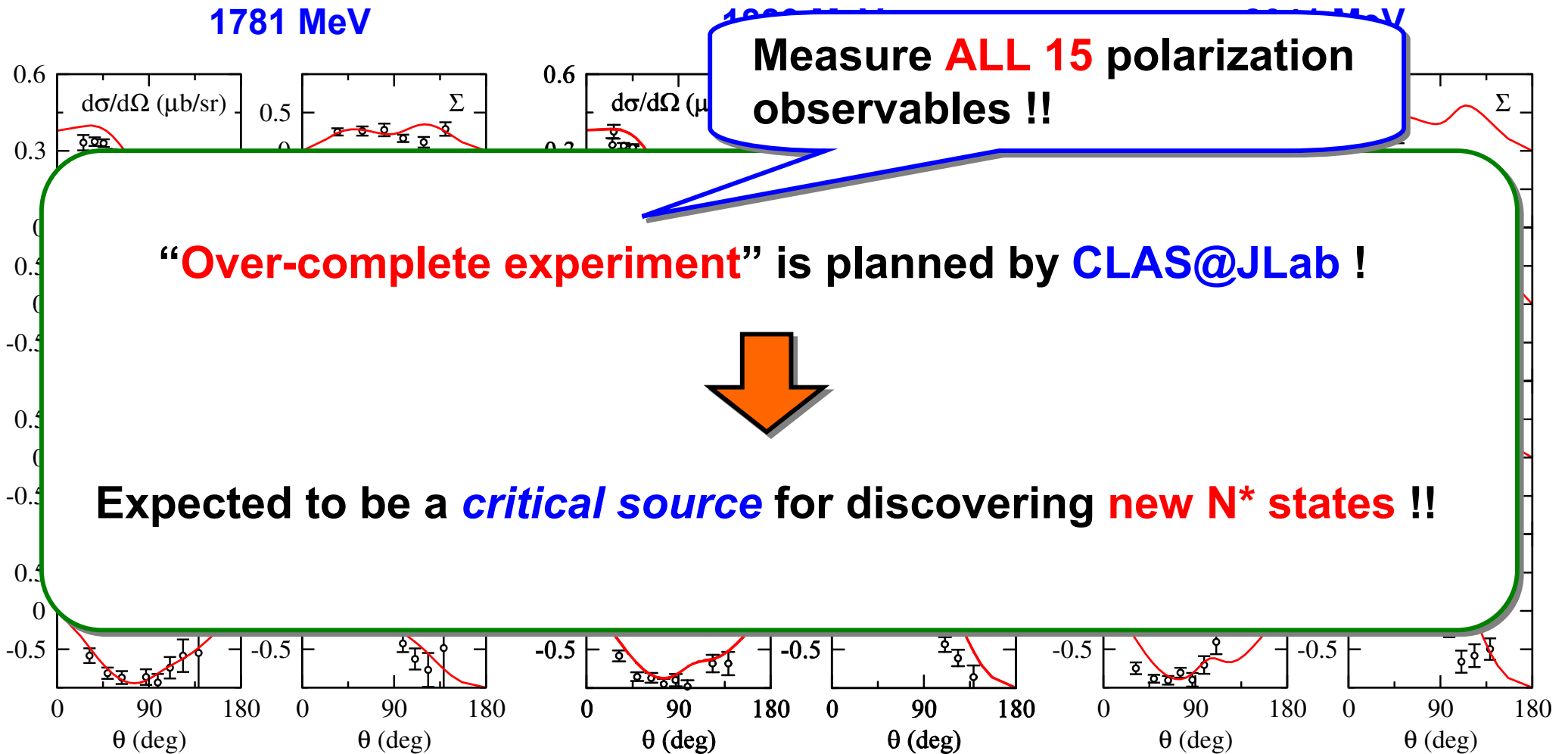


gamma p \rightarrow K⁺ Lambda

Preliminary!!

Formulae for calculating polarization observables

\rightarrow Sandorfi, Hoblit, Kamano, Lee arXiv:1010.0455



Summary and outlook

✓ **Full-combined** analysis of $\pi N, \gamma N \rightarrow \pi N, \eta N, KY$ reactions is underway.

➤ Re-examine resonance poles

Previous model: $Q^2 < 1.5 \text{ GeV}^2$

➤ Analyze CLAS $ep \rightarrow e\pi N$ data with $Q^2 < 6 \text{ GeV}^2$; extract N-N* e.m. transition f.f.s

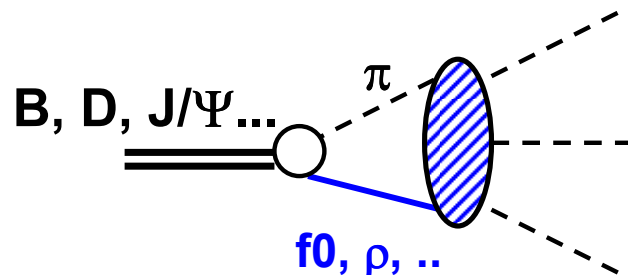
➤ Include $\pi N, \gamma N \rightarrow \pi\pi N, \omega N, \dots$ reactions to the combined analysis.

New direction

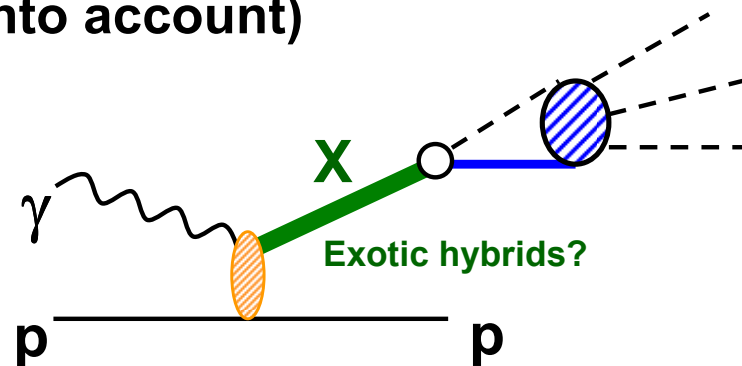
(Presented by S. Nakamura at SP01 session)

✓ Application of the **EBAC-DCC approach** to **meson physics**:

(**3-body unitarity effects** are fully taken into account)



Heavy meson decays



GlueX experiment @ Hall D of JLab

Back up

N* states and PDG *s

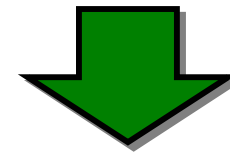
Particle	$L_{2I,2J}$ status	$N\pi$	$N\eta$	$N\omega$	$N\phi$	$N\rho$	$N\sigma$	$N\omega'$
N(939)	P_{11}	****						
N(1440)	P_{11}	****	****	*				
N(1520)	D_{13}	****	****	***				
N(1535)	S_{11}	****	****	****				
N(1650)	S_{11}	****	****	*	***	**		
N(1675)	D_{15}	****	****	*	*		****	
N(1680)	F_{15}	****	****	*	*		****	
N(1700)	D_{13}	***	***	*	**	*	**	*
N(1710)	P_{11}	***	***	?	**	*	**	**
N(1720)	P_{13}	****	****	*	**	*	*	*
N(1900)	P_{13}	**	**	?				
N(1990)	F_{17}	**	**	*	*			
$\Delta(1232)$	P_{33}	****	****	F				
$\Delta(1600)$	P_{33}	***	***	o?			***	
$\Delta(1620)$	S_{31}	****	****	r			****	
$\Delta(1700)$	D_{33}	****	****	b	*		***	
$\Delta(1750)$	P_{31}	*	*	?				
$\Delta(1900)$	S_{31}	**	**	d	*	*		
$\Delta(1905)$	F_{35}	****	****	d	*	**		
$\Delta(1910)$	P_{31}	****	****	e	*	*		
$\Delta(1920)$	P_{33}	***	***	n	*	**		
$\Delta(1930)$	D_{35}	***	***	?	*			
$\Delta(1940)$	D_{33}	*	*	F				
$\Delta(1950)$	F_{37}	****	****	o	*	****		

All of these studies essentially agree on the existence and (most) properties of the 4-star states. For the 3-star and lower states, however, even a statement of existence is problematic.

— Arndt, Briscoe, Strakovsky, Workman PRC 74 045205 (2006)

Most of the N*s were extracted from

$$\pi N \rightarrow \pi N, \quad \gamma N \rightarrow \pi N$$

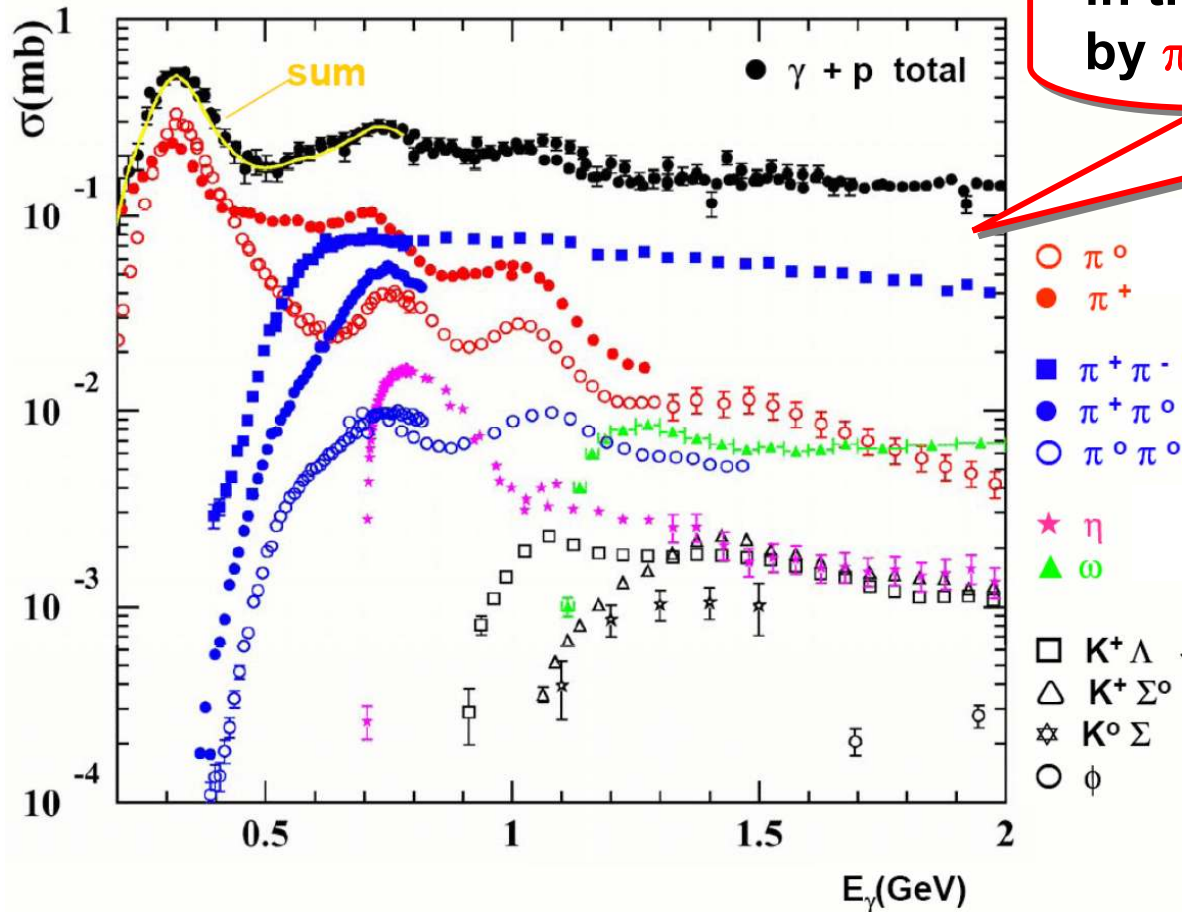


Need **comprehensive analysis** of

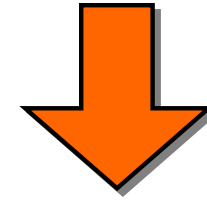
$$\pi N, \eta N, \pi\pi N, KY, \omega N, \dots$$

channels !!

“Priority” of coupled-channels effect



γN (also πN) reaction cross sections in the resonance region are dominated by πN and $\pi\pi N$ final states.



At least, the couplings of πN and $\pi\pi N$ channels should be taken into account in the analyses of **any** γN (πN) \rightarrow MB reactions.

Figure: E. Pasyuk's talk at Hall-B/EBAC meeting

“Complete Experiment” of pseudoscalar meson photoproduction reactions

“Complete Experiment” = Measure **ALL** polarization observables needed to determine **amplitudes** up to overall phase

unpolarized diff. crs. sec.

$$\rightarrow d\sigma/d\Omega$$

single spin

$$\rightarrow P, \Sigma, T$$

beam-target

$$\rightarrow E, F, G, H$$

beam-recoil

$$\rightarrow C_{x'}, C_{z'}, O_{x'}, O_{z'}$$

target-recoil

$$\rightarrow T_{x'}, T_{z'}, L_{x'}, L_{z'}$$

8 /16 observables needed!

Chiang, Tabakin PRC55 2054 (1997)

- ✓ Measurement of $\gamma N \rightarrow KY$ pol. obs. is very active.
- ✓ **OVER-complete** experiments planned by **CLAS** for $\gamma p \rightarrow K^+ \Lambda$, $\gamma n \rightarrow KY$.



Provides critical information on **$N^* \rightarrow KY$** decays !!
Much room for new N^* state searches

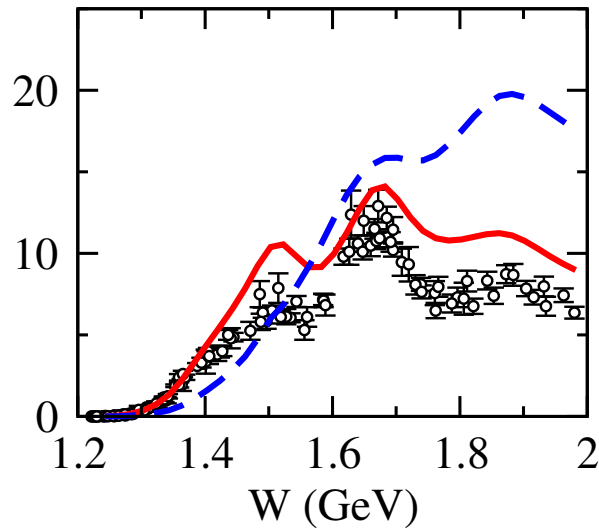
$\pi N \rightarrow \pi \pi N$ reaction

Kamano, Julia-Diaz, Lee, Matsuyama, Sato, PRC79 025206 (2009)

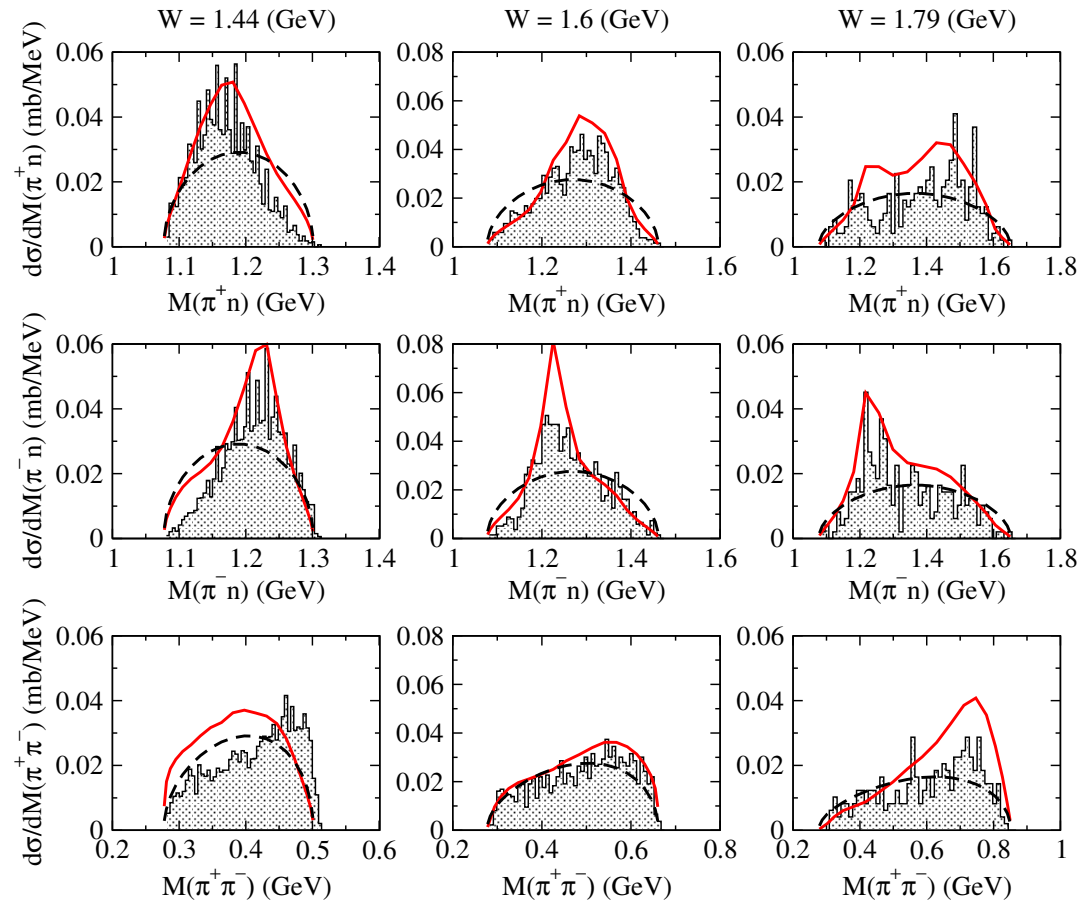
Parameters used in the calculation are from $\pi N \rightarrow \pi N$ analysis.

$$\pi^- p \rightarrow \pi^+ \pi^- n$$

$$\pi^- p \rightarrow \pi^+ \pi^- n$$



— Full result
 - - - - C.C. effect off

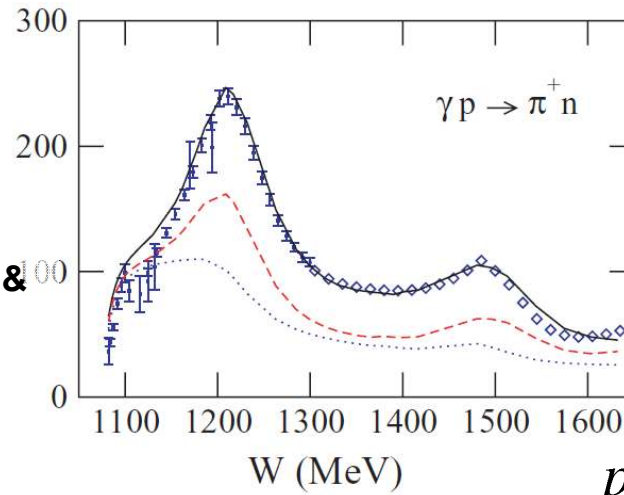
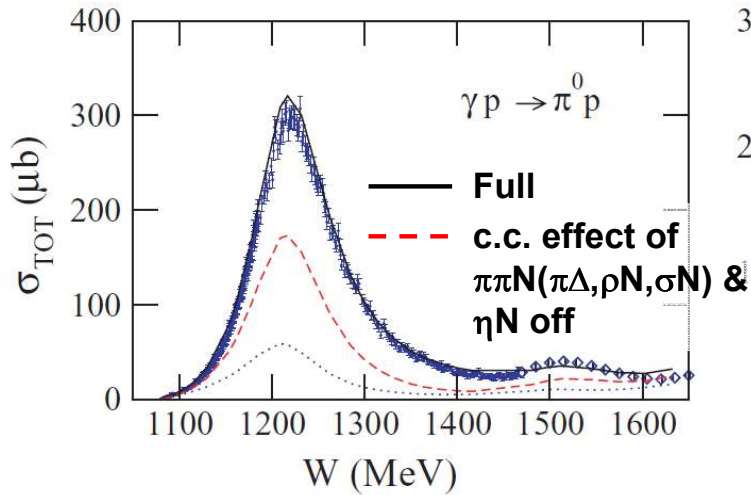


— Full result - - - - Phase space

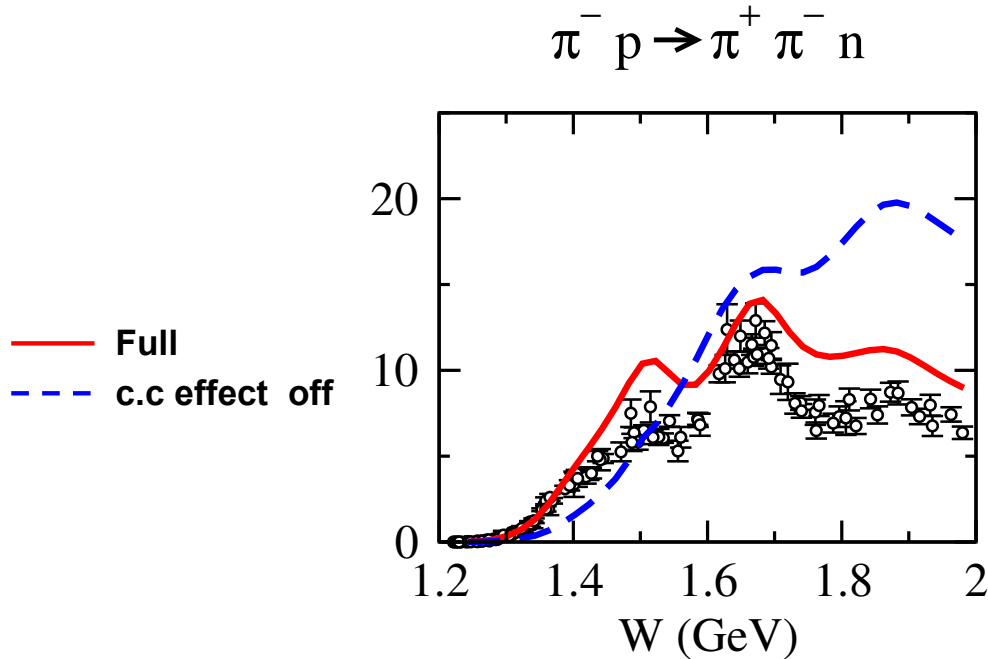
Data handled with the help of R. Arndt



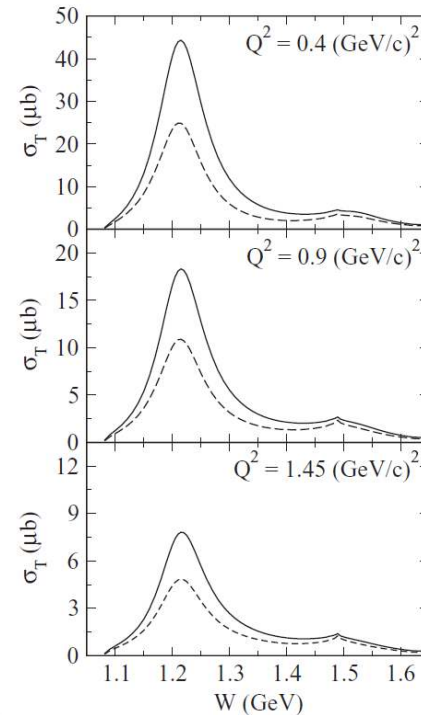
EBAC-DCC analysis (2006-2009)



**Coupled-channels effect
in various reactions**



$p(e, e' \pi^0) p$



— Full
- - - c.c. effect of $\pi\pi N(\pi\Delta, \rho N, \sigma N)$ & ηN off

