

INTRODUCTION TO NEUTRON SCATTERING

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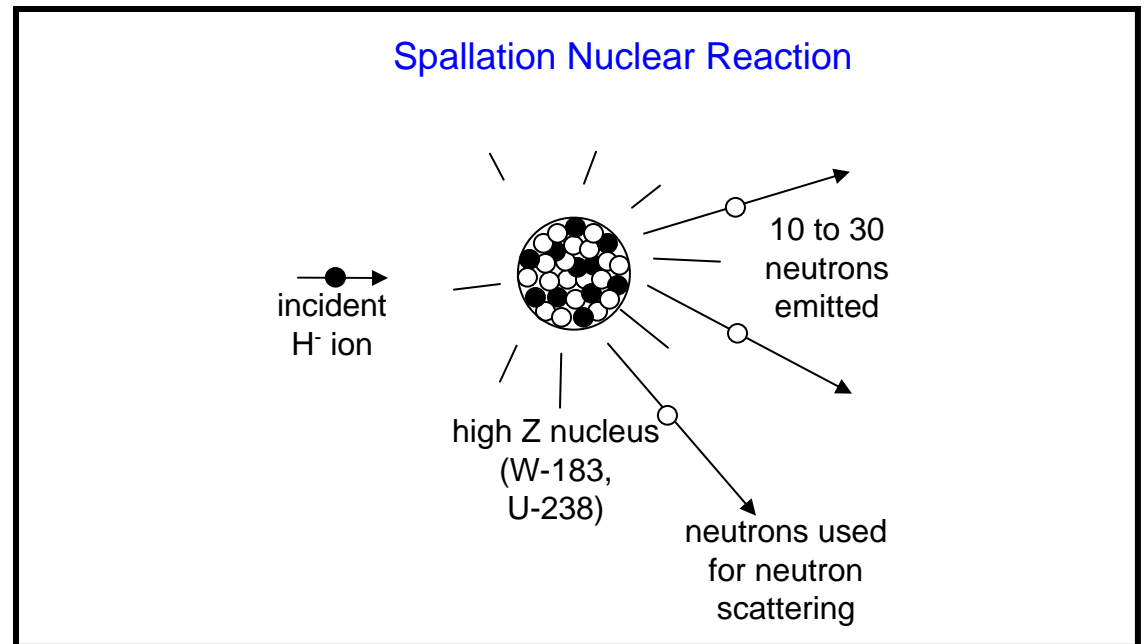
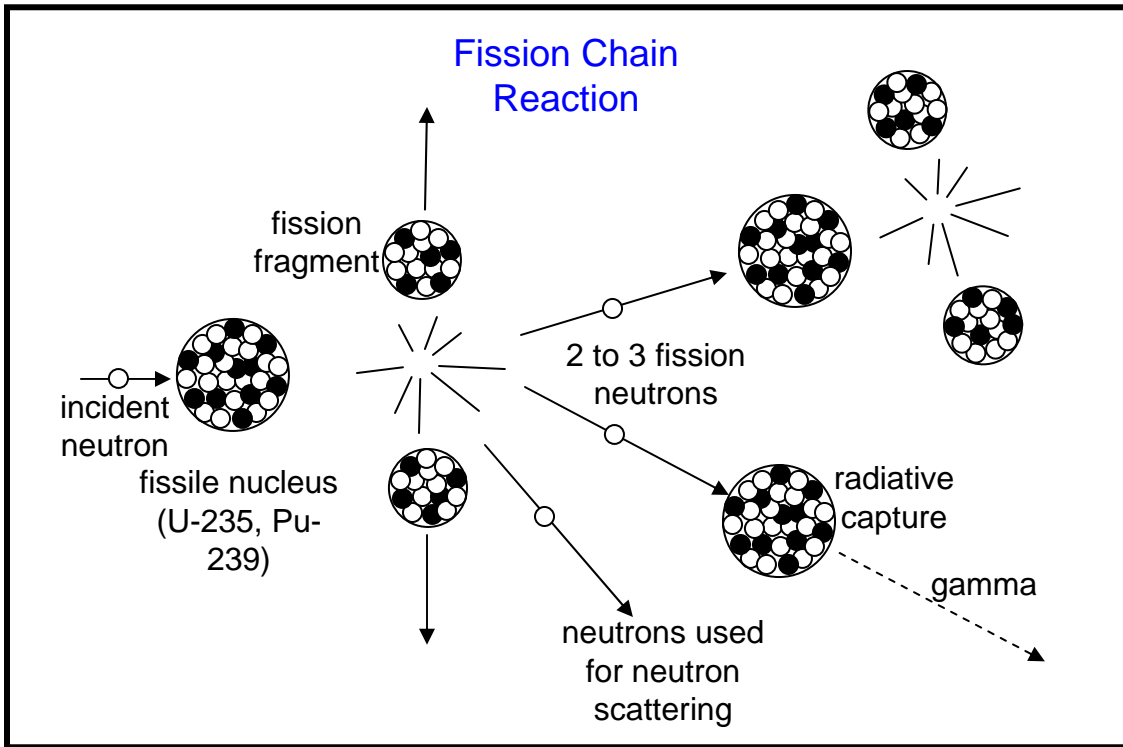
National Institute of Standards and Technology
Center for Neutron Research

- Why Use Neutrons?
- Neutron Sources
- Continuous vs Time-of-Flight
- Neutron Sources in the US
- The NIST Neutron Scattering Facilities
- Neutron interactions
- Elastic vs Inelastic Scattering
- Coherent and Incoherent Scattering
- Neutron Scattering Lengths and Contrast Factors
- Introduction to SANS

WHY USE NEUTRONS?

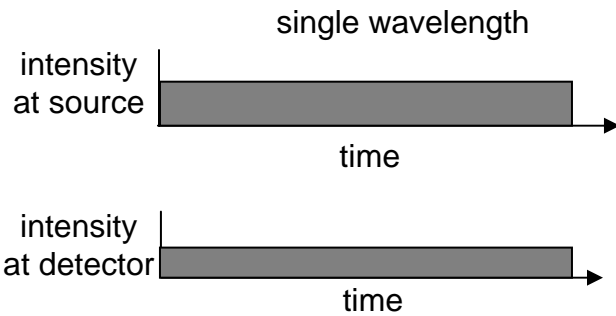
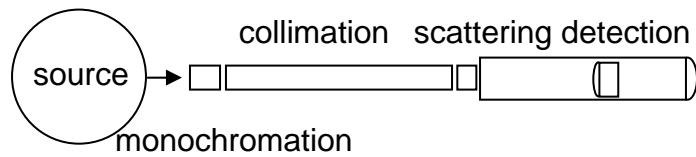
- Neutrons interact through short-range nuclear interactions. They have no charge and are **very penetrating** and **do not destroy samples**.
- **Neutron wavelengths** are comparable to **atomic sizes** and interdistance spacings.
- Neutrons interactions with **hydrogen** and **deuterium** are widely different making the **deuterium labeling method** an advantage.

NEUTRON SOURCES



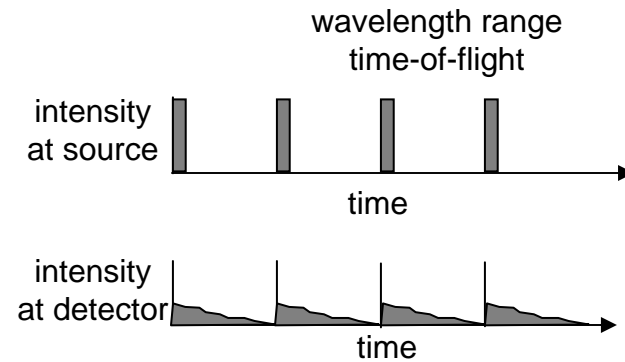
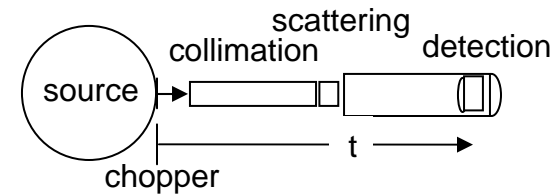
CONTINUOUS VS TIME-OF-FLIGHT

Continuous Reactors



Measure some of the neutrons all of the time

Pulsed Sources



Measure all of the neutrons some of the time

NEUTRON SOURCES IN THE US

Continuous Sources:

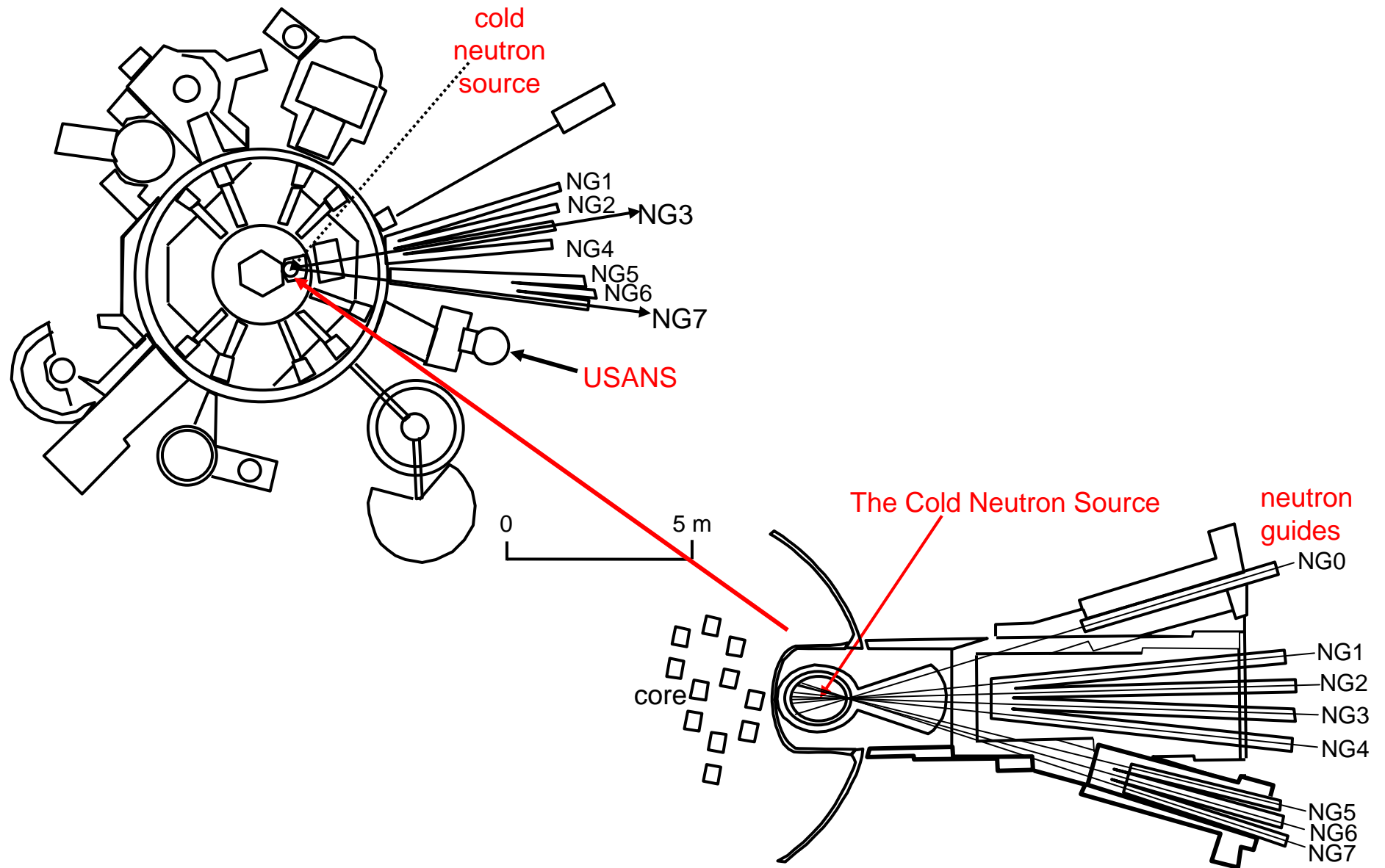
- **HFIR-Oak Ridge** National Laboratory. <http://neutrons.ornl.gov>.
- **NIST**-National Institute of Standards and Technology. <http://www.ncnr.nist.gov>.

Pulsed Sources:

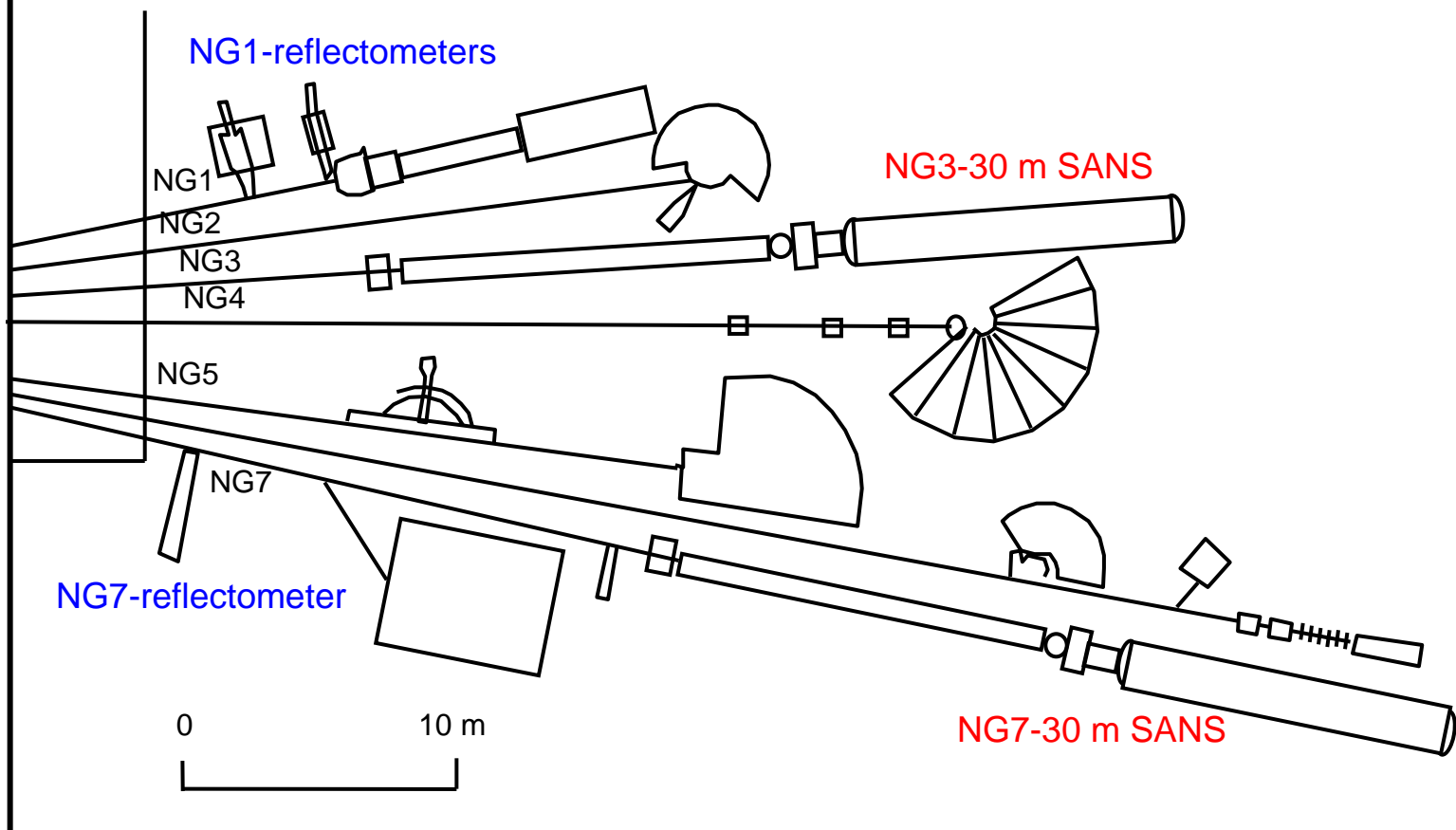
- WNR/PSR LANSCE (**Los Alamos**). <http://lansce.lanl.gov>
- **SNS** (**Oak Ridge** National Lab). <http://www.sns.gov>.

NIST Thermal Instruments

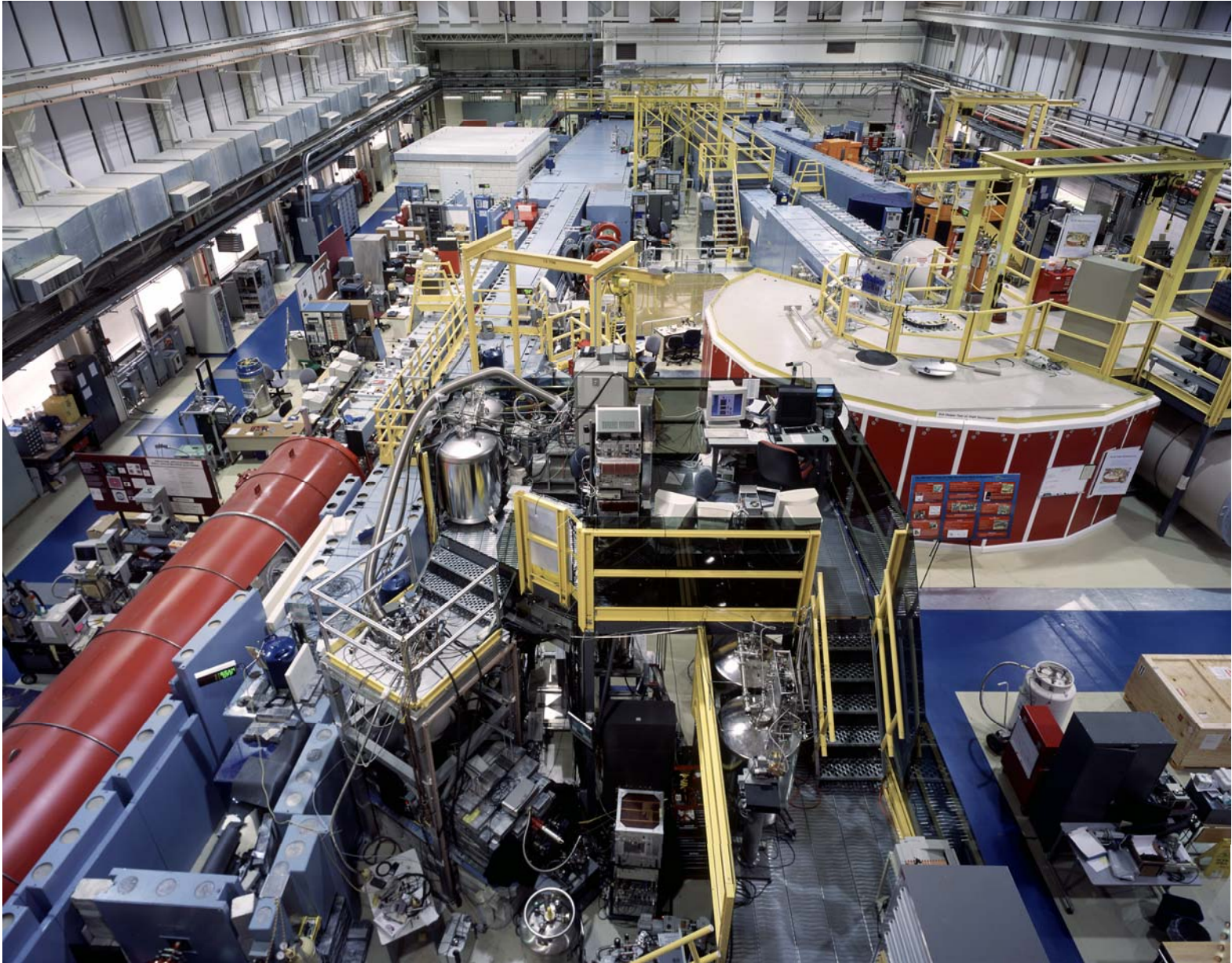
THE NIST NEUTRON SOURCE



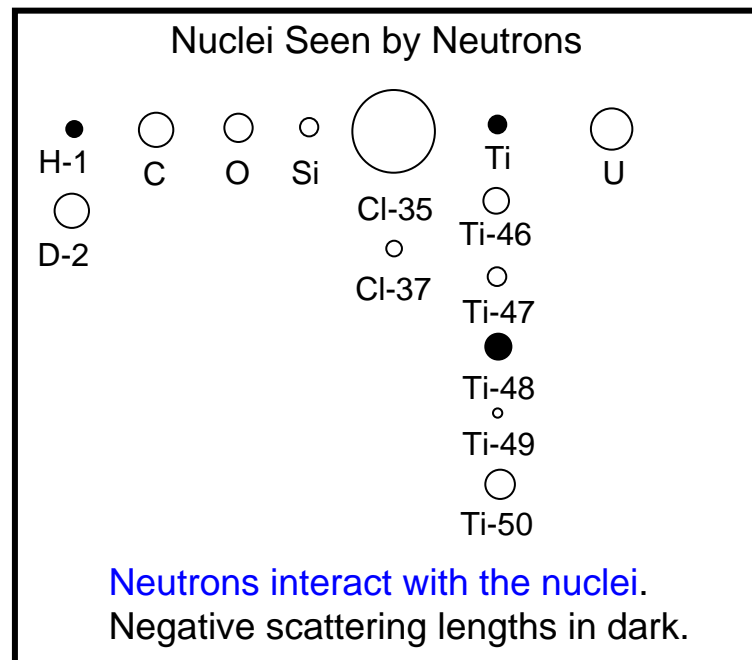
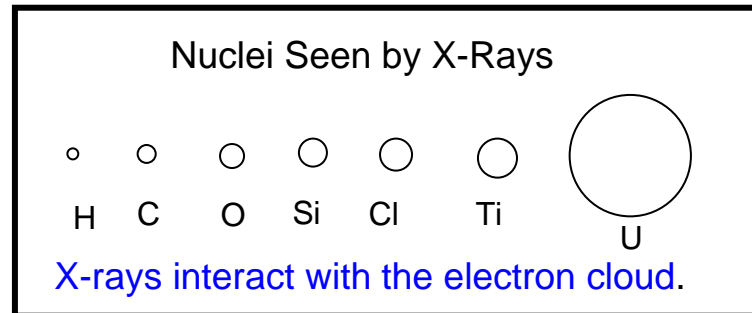
The NIST Guide Hall



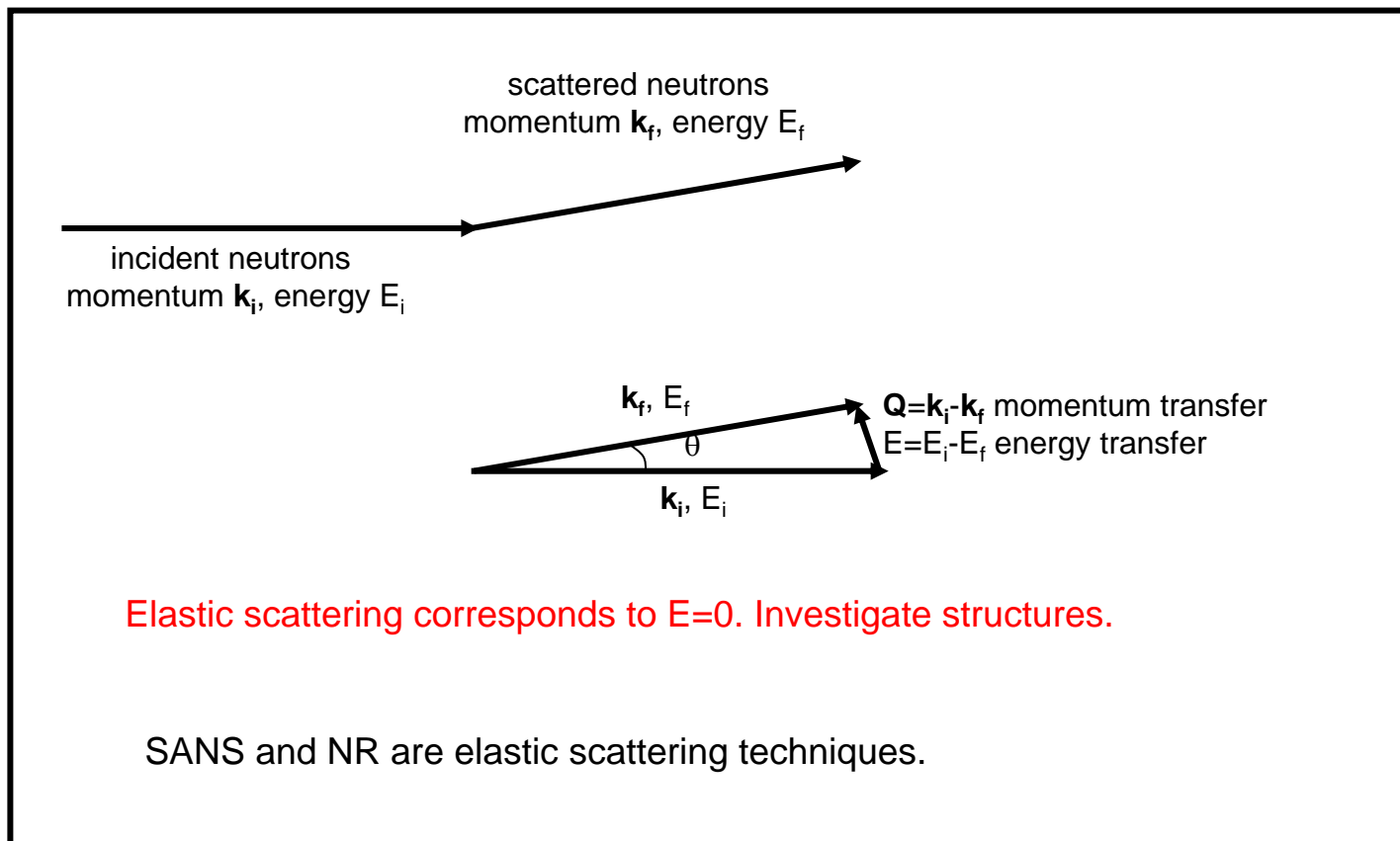
The NIST Guide Hall



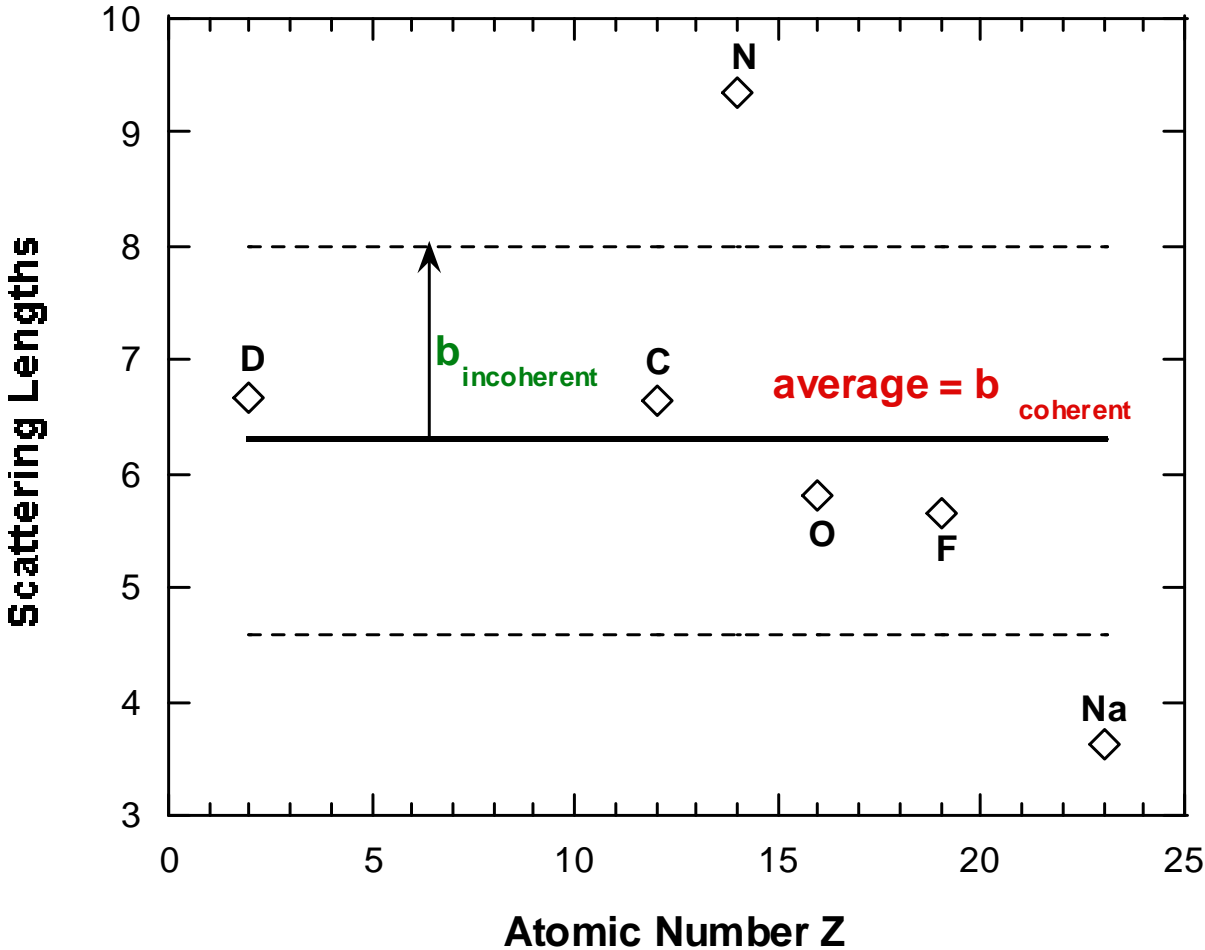
NEUTRON INTERACTIONS



ELASTIC vs INELASTIC NEUTRON SCATTERING



COHERENT AND INCOHERENT SCATTERING



NEUTRON SCATTERING LENGTHS AND CROSS SECTIONS

	Scattering Lengths		Scattering Cross Sections		
	Coherent	Incoherent	Coherent	Incoherent	Absorption
Element	b_c Fermi	b_i Fermi	σ_c Barn	σ_i Barn	σ_a Barn
H-1	-3.739	25.278	1.757	80.30	0.333
D-2	6.671	4.04	5.592	2.05	0.000
C-12	6.646	0	5.550	0.001	0.003
N-14	9.36	2.0	11.01	0.50	1.90
O-16	5.803	0	4.232	0.000	0.000
F-19	5.654	0	4.232	0.001	0.000
Na-23	3.63	3.59	1.66	1.62	0.530

1 Fermi = 10^{-13} cm.

1 Barn = 10^{-24} cm².

Case of D₂O:

Mass $m_{D_2O} = 20$ g/mole, Density $d_{D_2O} = 1.111$ g/cm³.

Specific Volume = $v_{D_2O} = m_{D_2O}/d_{D_2O} = 18$ cm³/mole.

Scattering Length: $b_{D_2O} = 2b_D + b_O = (2 \cdot 6.671 + 5.803) \cdot 10^{-13} = 19.145 \cdot 10^{-13}$ cm.

Scattering Length Density: $b_{D_2O}/v_{D_2O} = 1.064 \cdot 10^{-13}$ cm²/mole = $6.38 \cdot 10^{-6}$ Å⁻².

Microscopic coherent scattering cross section $\sigma_c = 4\pi \langle b \rangle^2$ units of barns.

Macroscopic coherent scattering cross section: $\Sigma_c = (N/V) \sigma_c$ units of cm⁻¹.

Contrast factor (mixture of A in B): $(b_A/v_A - b_B/v_B)^2$ in units of cm⁻⁴.

Example of Poly(ethylene oxide)/Deuterated Water (hPEO/D₂O) Solution:

hPEO: C₂H₄O, $b_{hPEO} = 4.139 \cdot 10^{-13}$ cm, $V_{hPEO} = 38.94$ cm³/mole

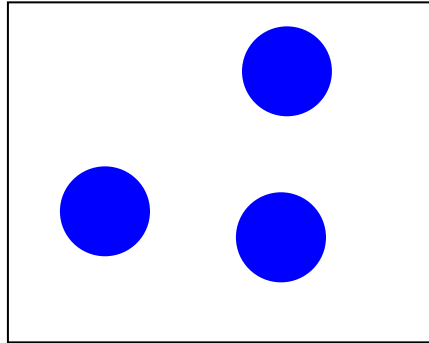
d-water: D₂O, $b_{D_2O} = 19.14 \cdot 10^{-13}$ cm, $V_{D_2O} = 18$ cm³/mole

Contrast factor: $(b_{hPEO}/v_{hPEO} - b_{D_2O}/v_{D_2O})^2 N_{av} = 5.498 \cdot 10^{-3}$ mole/cm⁴. N_{av} is Avogadro's #.

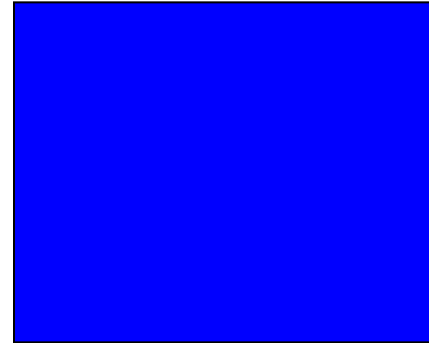
Online Scattering Length Density/Cross Section Calculator:

<http://www.ncnr.nist.gov/resources/sldcalc.html>

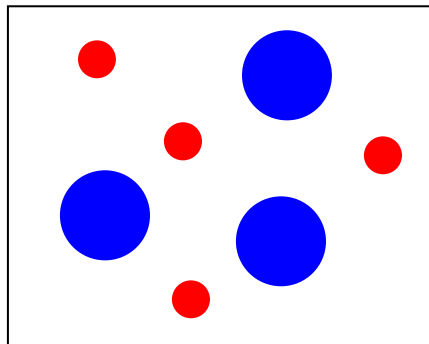
The Contrast Match Method



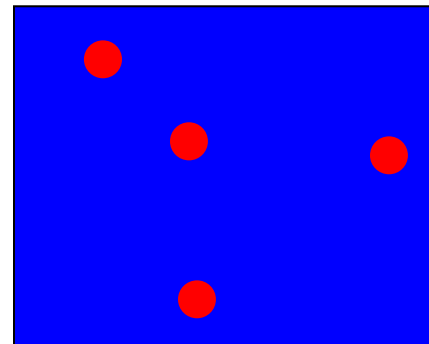
Finite contrast



Zero contrast

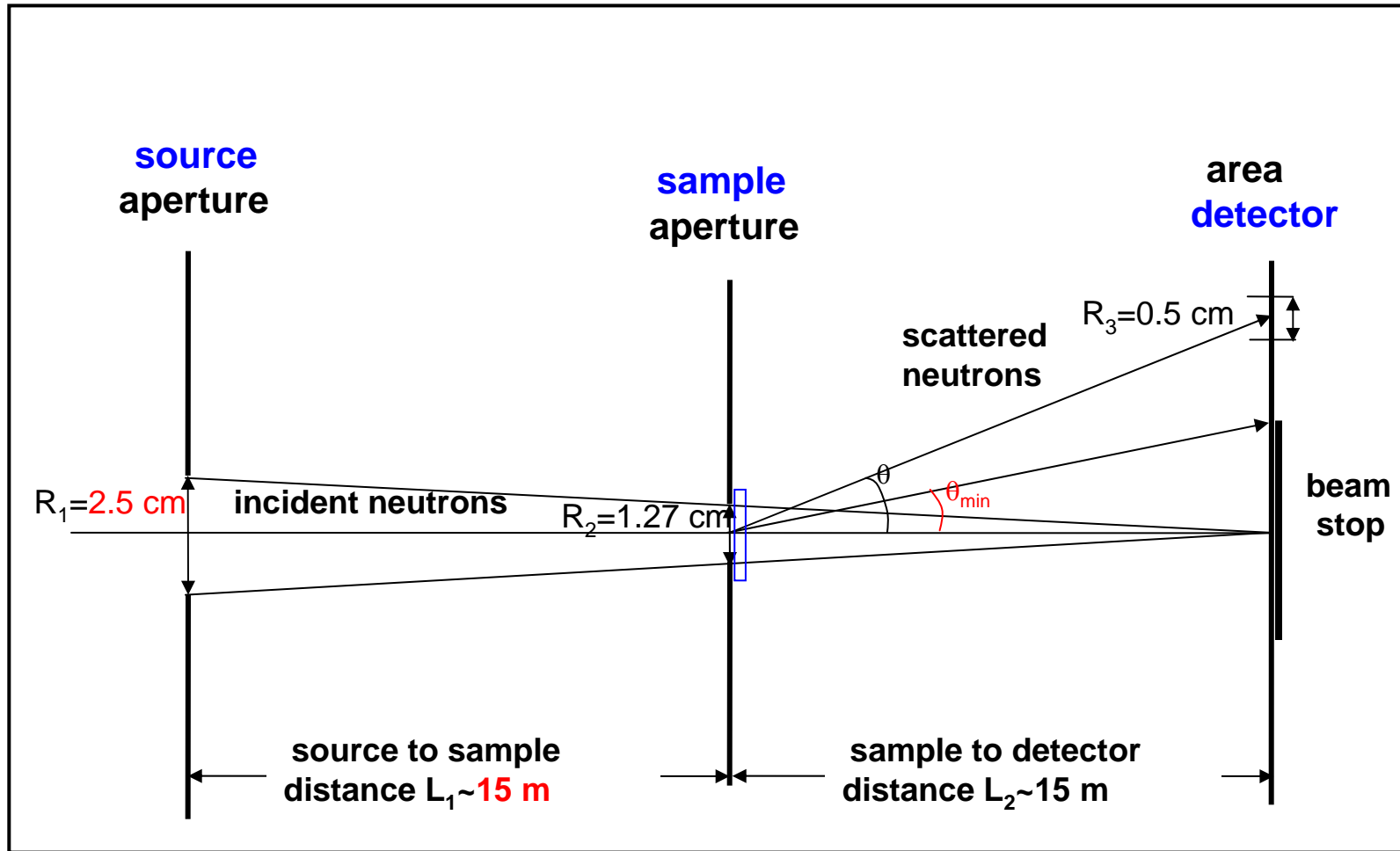


Multiple contrasts



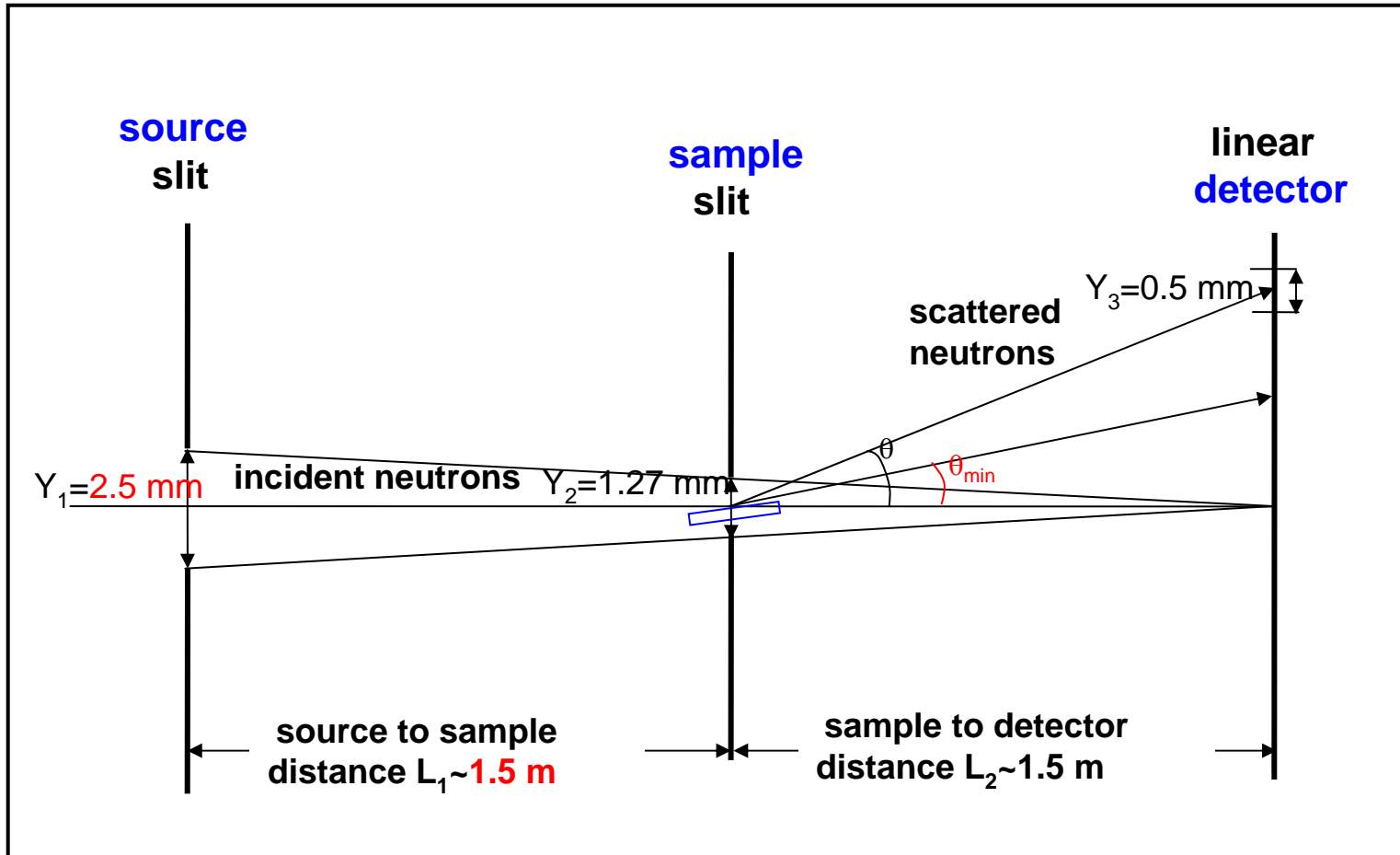
Contrast match

SANS GEOMETRY



$$\theta_{\min} = (R_1 + R_2)/L_1 + R_2/L_2 + R_3/L_2 \sim 3.7 \cdot 10^{-3} \text{ Rad} \sim 0.2^\circ$$

REFLECTOMETRY GEOMETRY



$$\theta_{\min} = (R_1 + R_2)/L_1 + R_2/L_2 + R_3/L_2 \sim 3.7 \cdot 10^{-3} \text{ Rad} \sim 0.2^\circ$$