SANDIA REPORT

SAND89-1397 • UC-905 Unlimited Release Printed September 1989





8232-2//069541



0000001

Analytical Framework for the LIFE2 Computer Code

Herbert J. Sutherland

SF2900Q(8-81)

Sandia National Laboratories
Albuquerque, New Mexico 97:85 and Livermore, California 94550
for the United States Department of Energy
under Contract DE-AC04-78DP00789

Issued by Sandia National Laboratories, operated for the United States Department of Energy by Sandia Corporation.

NOTICE: This report was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor any agency thereof, nor any of their employees, nor any of their contractors, subcontractors, or their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government, any agency thereof or any of their contractors or subcontractors. The views and opinions expressed herein do not necessarily state or reflect those of the United States Government, any agency thereof or any of their contractors.

Printed in the United States of America. This report has been reproduced directly from the best available copy.

Available to DOE and DOE contractors from Office of Scientific and Technical Information PO Box 62 Oak Ridge, TN 37831

Prices available from (615) 576-8401, FTS 626-8401

Available to the public from National Technical Information Service US Department of Commerce 5285 Port Royal Rd Springfield, VA 22161

NTIS price codes Printed copy: A03 Microfiche copy: A01

SAND89-1397 Unlimited Release Printed September 1989

ANALYTICAL FRAMEWORK FOR THE LIFE2 COMPUTER CODE*

by

Herbert J. Sutherland

Wind Energy Research Division Sandia National Laboratories Albuquerque, New Mexico 87185

ABSTRACT

The LIFE2 computer code is a fatigue/fracture analysis code specifically designed for the analysis of wind turbine components. It is a PC-compatible Fortran code that is written in a top-down modular format. In this numerical formulation, an "S-n" fatigue analysis is used to describe the initiation, growth and coalescence of micro-cracks into macro-cracks. A linear, "da/dn" fracture analysis is used to describe the growth of a macro-crack. This paper presents the numerical formulations used to implement these analyses.

^{*}This work is supported by the U.S. Department of Energy at Sandia National Laboratories under contract DE-AC04-76DP00789.

TABLE OF CONTENTS

INTRODUCTION	1
NUMERICAL PHILOSOPHY	,
Memory Allocation	-
Computation Times	2
Computation Times	3
Units Alternating Stress Levels	4
NUMERICAL FRAMEWORK	5
WIND REGIME	7
Round-Off Error	8
	0
Weibull and Rayleigh Distributions	9
Plotting Routines	10
Plotting Routines	
Interpolation	11
Summary Statement	11
CONSTITUTIVE FORMULATION	11
S-n Fatigue Constitutive Relations	12
Tabular Hibut	12
Constitutive Relations	12
Maximum and Minimum Values	13
Interpolation	13
da/dn Fracture Mechanics Relations	13
Tabular Innut	14
Tabular Input Constitutive Relations	
Internalation	14
Interpolation	15
Plotting Routines	15
Summary Statement	15
STRESS STATES	16
Operational Stresses	
Tabular Input	16 16
Narrow-Band Gaussian Model	
Parked Stresses	17
Start-Ston Stresses	18
Start-Stop Stresses	18

Stress Interval	19
Summary Statement	19
OPERATIONAL PARAMETERS	19
Operation Regime	19
Operation RegimeParked Stress Cycles	19
Start-Stop Cycles	20
Stress Concentration Factors	20
DAMAGE CALCULATION	20
Annual Average Cycle Count	22
Operational and Parked Cycle Count Matrices	22
Start-Stop Cycle Count Matrices	22
Alternating Stress Parameter	23
Operational Wind Speeds	23
Fatigue Analysis	23
Stress Concentration Factor	23
Cycles to Failure	24
Damage Calculation	24
Fracture Analysis	25
Current Crack Length	25
Stress Intensity Factor	26
Crack Growth Rate	27
Damage Calculation for the Current Crack Length	27
Summary Statement	28
SUMMARY	28
ACKNOWLEDGMENTS	29
REFERENCES	30
ADDENDIV Formen Constitutive Model	32

LIST OF TABLES

TABLE I.	Constitutive Parameters for the S-n Formulations	13
TABLE II.	Specialized Values for the Exponents in the Forman Constitutive Equation	15
TABLE A-I.	Cross-Reference for the Forman Constitutive Constants	34

LIST OF SYMBOLS

а	Crack length.
	The initial crack length.
a _i	The final crack length.
a _f	The final value of the crack length used in the computations, see
a_{W}	Eq. 42.
$\mathbf{a}_{\mathbf{w}}$	The maximum crack length in the w th crack interval.
$\hat{\hat{\mathbf{a}}}_{\mathbf{W}}^{w}$	The average crack length in the w th crack interval, see Eq. 43.
a(∆t)	The current crack length.
a_0	The initial value of the crack length used in the computations,
	see Eq. 41.
A(•)	The cumulative density function for the annual wind speed
	distribution, see Eq.18.
A 0	Forman calculational constant, see Eq. A-7.
A 1	Forman calculational constant, see Eq. A-8.
A2	Forman calculational constant, see Eq. A-10.
A3	Forman calculational constant, see Eq. A-9.
A_k	Forman calculational constant, see Eq. A-4.
B_k	Forman calculational constant, see Eq. A-3.
C	Forman material parameter, see Eq. 24.
C(•)	The complementary cumulative density function for the annual
` /	wind speed distribution, see Eq. 17
d	Forman calculational constant, see Eq. A-16.
da/dn	The crack growth rate at the stress intensity state (κ_m, κ_a) .
dâ/dn	The adjusted crack growth rate at the adjusted stress intensity
	state $[(\kappa_m)_r, (\kappa_a)_s)$, see Eq. 37.
$\mathrm{D}(ullet)$	The average annual damage rate for the turbine.
f_0	The dominate frequency of blade vibration or the rate of mean
Ū	level crossings, see Eq. 28. The LIFE2 code assumes units of
	Hz for this variable.
G(i)	Constants for determining the value of the Γ function, see Eq.
()	15.
i.I	Index.
j,J	Index.
k,K	Index for the mean stress terms of the constitutive formulation.
Κ̈́c	Forman calculational constant, see Eq. A-3.
K_{Ic}	Critical stress intensity factor for mode I failure.
L,l	Index for the alternating stress terms of the constitutive
,	formulation.
$\mathbf{n}(\boldsymbol{\cdot})$	The number of stress cycles imposed on the turbine component
` /	in time Δt with a wind velocity \hat{V} and at the stress state $(\hat{S_m}, \hat{S_a})$.
	÷

 $(\hat{n}_{rs})_q$ The annual average cycle count imposed on the turbine component for the qth wind velocity interval and for the (Sm,Sa) stress state interval, see Eq. 33 and 34. $N(\cdot)$ The total number of cycles required to fail the material at the stress state (S_m, S_a) . $\hat{N}(\cdot)$ The adjusted number of cycles required to fail the material at the adjusted stress state $[(\hat{S}_m)_r, (\hat{S}_a)_s)$, see Eq. 37. The conditional probability density function for the vibratory PS V stress, see Eq. 26. The probability density function for the annual wind speed pγ distribution. The conditional probability density function for the vibratory $(P_S|_V)_s$ stress integrated over the sth stress interval, see Eq. 27. $(P_V)_i$ The probability density function for the annual wind speed distribution in the ith interval, see Eq. 16. Index for the summation over wind speed. q,Q r.R Index for the summation over mean stresses. R Stress ratio, see Eq. A-1. s,S Index for the summation over alternating stresses. S Stress state. The alternating stress. $(\hat{S}_a)_s$ The adjusted alternating stress in the sth interval, see Eq. 37. S_c The component stress state. S_{m} The mean stress. The adjusted mean stress in the rth interval, see Eq. 37. $(S_m)_r$ S_{max} The maximum stress in a stress cycle. $[S_{max}/\sigma_{o}]$ Forman calculational constant, set equal to 0.3, see Eq. A-7. The minimum stress in a stress cycle. S_{min} Forman calculational constant, see Eqs. A-11 and A-15. $[S_o/S_{max}]$ $[S_0/S_{max}]_R$ Forman calculational constant, see Eq. A-12. Thickness of the component, see Eq. A-4. Forman calculational constant, see Eq. A-5. t_0 Т The total number of seconds in one year. It equals 365.25 $day/yr \cdot 24 hr/day \cdot 60 min/hr \cdot 60 sec/min = 31,557,600 sec.$ $(T_{aa})_q$ The annual average time the turbine is subjected to the qth wind velocity interval, see Eq. 32. T_{f} The service lifetime of the component. v,VThe wind speed. V_{m} The mean wind speed for the Weibull distribution, see Eq.14.. V_{ci}

The cut-in wind speed.

The cut-out wind speed.

The maximum wind speed in the qth interval.

Forman calculational constant, see Eq. A-4.

Index for the summation over crack length.

 V_{co}

 V_{q}

w,W

W

Yo	The geometric shape factor for the stress intensity factor, see Eqs. 44 and 45.
α	The shape factor for the Weibull distribution, see Eqs. 13 and 14.
$\alpha_{ m F}$	Forman calculational constant, see Eqs. A-7 and A-8.
β	The amplitude factor for the Weibull distribution, see Eqs. 13 and 14.
γ	The stress concentration factor, see Eqs. 30 and 31.
γA	The range/amplitude multiplier, see Eqs. 36 and 48.
γf	The stress concentration factor used for fatigue analysis, see
	Eqs. 35 and 36.
γĠ	The exponent for Goodman's or Gerber's rule, see Eq. 22 and Table I.
γi	The i th stress concentration factor, see Eq. 29.
$\gamma_{ m r}$	The stress concentration factor used for fracture analysis, see Eqs. 46, 47 and 48.
γ SF	The safety factor.
γ_{t}	The total stress concentration factor resulting from various phenomenons, see Eq 29.
$\Gamma(ullet)$	The gamma function.
$\eta_{ m q}$	The number of start-stop events counted for the stress cycle matrix that describes the q th class of start-stop events, see Eq. 34.
$\hbar_{\mathbf{q}}$	The annual average number of the q th class of start-stop events, see Eq. 34.
∆a _w	Crack extension in the w th interval, see Eqs. 6 and 40.
Δκ	The range of the stress intensity factor for a stress cycle, see Eq. 24.
$[\Delta \kappa]_{\mathrm{eff}}$	Forman calculational constant, see Eq. A-13.
$\Delta \kappa_{\rm O}$	Forman calculational constant, see Eq. A-6.
$\Delta \kappa_{ ext{th}}$	Forman material parameters, see Eq.24.
Δκ1	Forman calculational constant, see Eq. A-13.
$\Delta \mathbf{t}$	Time period.
∆t _a	The q th time interval.
$\Delta ilde{ ext{V}}_{ ext{q}}$	The q th wind speed interval, see Eq. 25.
κ_a	The alternating stress intensity factor.
$\kappa_{ m C}$	Forman material parameter, see Eq.24.
$\kappa_{ m m}$	The mean stress intensity factor.
μ	Forman material parameter, see Eq.24 and Table II.
η	Forman material parameter, see Eq.24 and Table II.
π	Pi. The effective cyclic stress amplitude for Goodman's or Gerber's
$\sigma_{\mathbf{e}}$	rule, see Eq. 22 and Table I.

$\sigma_{\mathbf{i}}$	The stress in the i th interval, see Eq. 23.
$\sigma_{ m ref}$	The reference stress for Goodman's or Gerber's rule, see Eq. 22 and Table I.
$\sigma_{ m V}$	The yield stress of a material.
$\sigma_{\mathbf{u}}$	The ultimate stress of a material.
σ_{V}	The standard deviation of the vibratory stresses, see Eq. 26.
ν	Forman material parameter, see Eq.24.
ψ	Forman material parameter, see Eq.24 and Table II.

INTRODUCTION

The LIFE2 computer code is a fatigue/fracture analysis code specifically designed for the analysis of wind turbine components. The code was originally written by Sutherland, Ashwill and Naassan, and it was subsequently modified by Sutherland and Schluter. The code is written in a top-down modular format using Fortran. It is designed to run on an IBM personal micro-computer (PC) or compatible.

The service lifetime of a wind turbine component may be divided into three phases: 1) micro-crack initiation, 2) growth and coalescence of micro-cracks into macro-cracks and 3) growth of a macro-crack. In the LIFE2 formulation, an "S-n" fatigue analysis is used to describe the first two phases and a linear, "da/dn" fracture mechanics analysis is used to describe the third phase.

The code is divided into five main sections. The first four describe the wind resource, the constitutive properties of the turbine material, the stress state in which the turbine operates and operational parameters for the turbine system. The fifth uses the data files written by the first four sections to calculate the service lifetime of a turbine component. In addition to the main sections, auxiliary sections are included to permit the storage of input data and code calculations and to permit the plotting of results.

The wind resource is described in the LIFE2 code as the probability density function for the yearly wind speed distribution. Rayleigh and Weibull distributions³ may be calculated directly by the code. Other distributions may be entered in tabular form.

Two sets of constitutive properties are used by the code. The first is the classical "S-n" fatigue characterization that describes the number of stress cycles required to fail the component.⁴ Each stress cycle is described as a function of applied stress state. The stress state is characterized by both its mean stress level and its alternating stress level. This functional relation may be entered in tabular form or by using a constitutive description. The constitutive relations include Goodman's rule (using either the yield or the ultimate stress), Gerber's rule and the modified Gerber rule.⁴ The second set of constitutive properties describes the rate of crack growth as a function of the cyclic change in the stress intensity factor. The growth rate is assumed to be dependent on the mean stress intensity factor and the alternating stress intensity factor. Again, the relationship between these variables may be entered in tabular form. A Forman constitutive model is also included in the code.⁵

The third section of the code describes the cyclic content of the stress state imposed on the turbine component. Classes of stress states include operational stresses, parked stresses (i.e., the stresses due to the wind buffeting a parked blade) and start-stop stresses. The first two are taken to be functions of the annual wind speed distribution and the third is taken to be a function of specific events. For each of these stress states, the code accepts a cycle count matrix in which the number of stress cycles (for a specified time period) is characterized as a function of the mean stress and the alternating stress. This matrix, commonly called a "rain-flow" matrix, is accepted in

tabular form. A narrow-band Gaussian model for operational stresses⁶ is also included in the code.

The fourth section of the code describes the operational parameters for the turbine. This section records the miscellaneous parameters required for the calculations. Typical inputs include such parameters as the cut-in wind speed, the cut-out wind speed and the stress concentration factor(s).

The fifth section of the code has two calculational modules. The S-n fatigue analysis module uses Miner's Rule⁴ to determine the initial portion of the service lifetime of a turbine component; namely, this module describes the initiation of micro-cracks and their growth and coalescence into macro-cracks. In this formulation, the damage rule is integrated over all stress cycles to determine the annual average rate at which damage is being accumulated. The lifetime of the component is inversely proportional to this damage accumulation rate.

In the second calculational module, the crack propagation characteristics of a preexisting macro-crack are analyzed using a da/dn constitutive rule.⁴ In this formulation, the crack growth rate, da/dn, is integrated over all stress cycles. As da/dn is a function of the crack length, the calculation is divided into a finite number of steps. For each step, the crack length is taken to be a constant, and an average growth rate is determined and the time required for the crack to grow across that integration segment is calculated. The sum over all of the integration segments yields the time of growth for the crack from its initial size to its final size.

This report describes the computational framework used in the LIFE2 code to evaluate the damage rules cited above. It is designed to be a companion report to the "User's Manual" that was written by Schluter and Sutherland.⁷ Example problems to illustrate its capabilities are presented in the Ref. 7.

NUMERICAL PHILOSOPHY

From its inception, the LIFE2 code has been designed to run on an IBM personal micro-computer (PC) or compatible. This decision was made to insure that it could be used by the maximum number of wind turbine designers. To implement the numerical formulations discussed below onto this relatively small computer required that special formulations and techniques be incorporated into the code. The main differences between this code and a code written for a larger, faster machine are dictated because the smaller machines have limited memory, have comparatively slow processors and have comparatively few significant digits.

MEMORY ALLOCATION

For a PC, the available memory for a program and all of its data is limited to a total of 640K of operational random-access memory (RAM). This relatively small memory placed a rather severe limitation on the program and forced several programming compromises to be incorporated into the code. The first compromise was to use program overlays. In this technique, the program resides in external memory (e.g., a hard disk, a floppy disk, a RAM disk in extended memory, etc.) and only those subprograms required by the current calculations are loaded into the operational RAM. When another subprogram is required, it is automatically loaded into the operational RAM and "overlays" the memory locations of a subprogram that is no longer required. These operations are transparent to the operator.

Further reductions in total memory requirements were achieved by limiting the size of the matrices used in the code. We have tried to make the matrices as large as possible and still have the program fit within the 640K memory limit of a standard PC. Also, data overlays are used throughout the program; namely, one matrix is used to store several different variables at different times during the course of the computations. This numerical philosophy requires extensive read/write statements to disk that significantly increase the time for the code to complete a task. However, these compromises are required for the program to maintain PC compatibility and a reasonable degree of accuracy.

The program does not use expanded memory directly, because this feature is not available in all PC's. However, expanded memory may be used in this formulation by using a "virtual disk" for reading and writing computational data files. In this manner, the I/O (input/output) time for data files can be reduced significantly.

COMPUTATION TIMES

As the PC uses a relatively slow processor, computational times may become excessively long when all computations are preformed at one time. To permit the use and storage of previous calculations and to permit a calculation to be terminated in mid-stream without the loss of the calculations that have been completed to that point, extensive "library" functions (i.e., data storage to permanent files) have been incorporated into the code. The transfer of data between calculational modules is accomplished by read/write statements to permanent files.

This "open architecture" for data transfer between modules has several benefits. First, this formulation inherently yields calculational modules that are independent of one another. This aspect of the program implies that new calculational modules may be added to the code with relative ease. When a new module is added, only that module needs to be validated, rather than the whole code. Second, data from sources other than the code may be incorporated into the calculations by simply placing them in the proper format and then adding them to the code's library. Third, parameter studies may be conducted relatively quickly because a large portion of the computations do not

have to be duplicated. And, finally, all computations may be archived for future reference.

The major problem with this formulation is that the program uses tables (matrices) to transfer computations between modules. This formulation implies that the numerical framework relies heavily on interpolations. Thus, the accuracy of the calculations decreases. Unfortunately, the decision to make this code PC compatible has severely limited our ability to address this problem. Our primary technique for addressing it is to keep all data transfer tables (matrices) as large as possible and to have them cover only those ranges required by the calculations. Additional techniques for increasing accuracy have been incorporated into the code. These techniques are discussed below in the sections that described the individual computation modules.

UNITS

With the one exception of variables with units of time, the LIFE2 code assumes that a consistent set of units are being analyzed by it. Namely, units are not checked for consistency by the code; no units are changed by the calculational modules. Thus, all variables with equivalent units must be entered with the same units (e.g., if stresses are entered in KPa in one place than they must be entered in KPa everywhere). If mixed units are entered into the code, the code will not preform correctly. To help alleviate the problem of mixed units, subroutines are provided in the code to change units, as required. These subroutines are invoked at the discretion of the operator.

Time variables are the one exception to this rule. As the service lifetime of a turbine component (i.e., the ultimate answer produced by the code) has units of time, the code must know the time units entered into it. The LIFE2 code always assumes that all time variables (i.e., those variable that have exclusive units of time) have units of seconds. If other units are used, they must be changed to seconds (using the appropriate subroutines) before calculations can proceed. The code prompts have been written to specify units of seconds for the appropriate time variables and Hertz for the appropriate frequency variables.

ALTERNATING STRESS LEVELS

Throughout this paper, the oscillating portion of the stress state, S_a , is described as the alternating stress level. Two definitions may be used for the alternating stress level: the range of the stress oscillation or the amplitude of the stress oscillation.⁴ The range is equal to the maximum stress in the cycle, S_{max} , minus the minimum stress in the cycle, S_{min} , and the amplitude equals half the range.

As the numerical formulations are, in general, not dependent on the definition used, either may be used by the operator. However, the operator must insure the consistency of the calculation. Namely, if the constitutive equation is defined using the range, then the operating stresses must also be defined using the range; and if the constitutive equation

is defined using the amplitude then the operating stresses must also be defined using the amplitude. Typically, the S-n constitutive relations are defined using the amplitude of the oscillating stress. And, the "da/dn" vs stress intensity factor are based on the range. Thus, the operator must be careful when entering the alternating stress data into the code.

Notes have been placed throughout the program input prompts to inform the operator when a particular formulation assumes that the alternating stress is an amplitude or a range variable. The operator is given the opportunity to change the alternating stress variable between these two definitions in the calculational module.

NUMERICAL FRAMEWORK

The LIFE2 computer code has been developed to compute the fatigue lifetime of a turbine component. It uses either Miner's Rule⁴ or linear fracture mechanics⁴ to analyze the behavior of the component. In the case of the former, the damage law used in the computations is given by the relation

$$D(\Delta t) = \int_{V_{ci}}^{V_{co}} p_{V} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{n(S_{m}, S_{a}, V, \Delta t)}{N(S_{m}, S_{a})} dS_{m} dS_{a} dV , \qquad (1)$$

where p_V is the probability density function for the annual wind speed distribution, S_m is the mean stress, S_a is the alternating stress, $N(\cdot)$ is the total number of cycles required to fail the material at the stress state (S_m, S_a) and $n(\cdot)$ is the number of stress cycles imposed on the turbine component in time Δt with a wind velocity V. V_{ci} and V_{co} are the cut-in and the cut-out wind speeds, respectively. In this form, D is the average annual damage rate for the turbine. When the damage rate D integrates over time to one, the component is expected to fail. As this formulation is linear, the service lifetime T_f of the component is given by:

$$1 = \int_{0}^{T_{f}} D(\Delta t) dt = D(\Delta t) T_{f}, \qquad (2)$$

or,

$$T_{f} = \frac{1}{D(\Delta t)} \qquad . (3)$$

We have assumed apriori that the stress cycles are a function of the velocity of the wind impinging on the turbine and that the annual wind speed distribution may be described by a probability density function. Eq. 1 has been discretized to the following finite summation:

$$D(\Delta t) = \sum_{q=1}^{Q} \sum_{r=1}^{R} \sum_{s=1}^{S} (P_{V})_{q} \frac{n_{qrs}[(S_{m})_{r}, (S_{a})_{s}, V_{q}, \Delta t]}{N_{rs}[(S_{m})_{r}, (S_{a})_{s}]} . \tag{4}$$

The index q is for the summation over wind speed, r is for the summation over mean stresses and s for the summation over alternating stresses. The exact formulation of each term in this sum will be defined later in this report.

For the linear fracture mechanics model, the propagation of a pre-existing, finite length crack is determined by integrating the crack growth rate da/dn over all stress cycles N. As the growth rate is a function of the current crack length $a(\Delta t)$, this integration is typically divided into a finite number of integration steps of the form:

$$a_f = a_i + \sum_{w=1}^{W} \Delta a_w \qquad , \qquad (5)$$

where a_i is the initial length of the crack and a_f is the "final" length of the crack produced by the N stress cycles occurring in time Δt . The growth rate at each step is determined by integrating the annual average growth rate over the unknown number of stress cycles N required to grow the crack an incremental length of Δa_w ; namely:

$$\Delta a_{W} = \int_{0}^{N} \operatorname{avg}[(da/dn)_{W}] dn = \operatorname{avg}[(da/dn)_{W}] N .$$
 (6)

Expanding this integral to illustrate its functional dependence,

$$\Delta a_{\mathbf{w}} = \int_{\mathbf{V}_{\mathbf{c}i}}^{\mathbf{V}_{\mathbf{c}o}} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{\mathrm{d}a(\kappa_{\mathbf{m}}, \kappa_{\mathbf{a}})}{\mathrm{d}n} \, n(S_{\mathbf{m}}, S_{\mathbf{a}}, \mathbf{V}, \Delta t) \, dS_{\mathbf{m}} \, dS_{\mathbf{a}} \, dV \quad . \quad (7)$$

(Note: this form of the crack growth equation is parallel in construction to the damage accumulation integral for fatigue shown in Eq. 1.)

As seen in this formulation, the crack growth rate da/dn is a function of the stress intensity state (κ_m, κ_a) and the cycle count n is a function of the stress state (S_m, S_a) . To map the stress state into the stress intensity state requires a knowledge of the current

crack length a. Thus, the integrand is a function of the independent variable a. To integrate this equation numerically, let us assume that the crack length a may be divided into W discrete intervals (as discussed above) and that the crack length, a_w , in each interval may be considered to be a constant. Then, Eqs. 5 and 7 may be combined to yield the following:

$$a(\Delta t) = a_{f} = a_{i} + \sum_{w=1}^{W} \int_{V_{ci}}^{V_{co}} p_{V} \int_{-\infty}^{\infty} \left[\frac{da(\kappa_{m}, \kappa_{a})}{dn} \right]$$

$$\left[n[(\kappa_{m})_{w}, (\kappa_{a})_{w}, V, \Delta t)] \right] d\kappa_{m} d\kappa_{a} dV$$
(8)

where the two components of the stress state have been mapped into the current stress intensity state using the current crack length a_w . In this formulation, the final crack length a_f is equivalent to the current crack length $a(\Delta t)$ because the integration is conducted over the stress cycles occurring in a time Δt . Discretizing Eq. 8 for numerical evaluation yields:

$$a(\Delta t) = a_{i} + \sum_{w=1}^{W} \sum_{q=1}^{Q} \sum_{r=1}^{R} \sum_{s=1}^{S} (P_{V})_{q} \left[\frac{da[(\kappa_{m})_{wr}, (\kappa_{a})_{ws}]}{dn} \right] \bullet$$

$$\left[n[(\kappa_{m})_{wr}, (\kappa_{a})_{ws}, V_{q}, \Delta t)] \right] . \tag{9}$$

The index w is for the summation over crack length, q is for the summation over wind speed, r is for the summation over mean stress intensity factors and s is for the summation over alternating stress intensity factors. Again, each term will be defined in detail later in this report.

WIND REGIME

The annual wind speed distribution which acts upon the turbine is assumed to be described by a probability density function p_V , see Eqs. 4 and 9. This function may take the form of a table or it may be described with an equation(s). If we assume that the stress state terms in Eqs. 1 and 8 are independent of this distribution, then the integration over the wind speed distribution may take the form:

$$(P_{V})_{i} = \int_{V_{i-1}}^{V_{i}} p_{V} dv \qquad , \qquad (10)$$

where the integration has been divided into I intervals. An alternative formulation of this equation is given by:

$$(P_{V})_{i} = C(V_{i-1}) - C(V_{i})$$
 (11)

where C(•) is the complementary cumulative density function defined by:

$$C(V) = \int_{V}^{\infty} p_{V} dv \qquad . \tag{12}$$

C(V) was chosen as the storage parameter for transferring this term to the calculation module because this form permits the calculational module to interpolate a tabular C(V) function rather than numerically integrating a probability density tabular function. This procedure decreases computation times and it permits the yearly wind speed distribution to be entered in tabular form.

ROUND-OFF ERROR

To illustrate the problems with PC compatibility and accuracy, Eq. 11 is analyzed in detail here. Eq. 11 takes the difference of two numbers that are typically small (in comparison to one) and close together at high wind speeds. As most PC's are limited to 6 or 8 significant digits in floating points operations and approximately 15 digits in double precision, this difference can be significantly influenced by numerical round-off if not handled carefully.

To minimize round-off errors caused by this term in the computation of total damage rates, let us consider the stress states of a wind turbine. In general, the stress state (and, thus, the damage) imposed on a wind turbine increases with increasing wind velocity. Therefore, the numerical formulation chosen to evaluate P_V should have high accuracy at large wind speeds. For the form chosen in Eq. 11, P_V is evaluated as the difference between two numbers that are relatively close to zero for high wind conditions; and, thereby, maximizes the accuracy of the calculation.

Also, the accuracy of this numerical formulation has been increased by taking the $C(V_i)$ matrix to be double precision.

TABULAR INPUT

To handle wind distributions that are not described by a functional relation supported by the code, tabular inputs may be used. The LIFE2 code will accept the complementary cumulative density function C(V) in tabular form. The function C(V) has a range that is limited to $0.0 \le C(V) \le 1.0$. To insure that this range is not violated, the code checks C(V) to insure that it always falls in the proper range. If it does not, the operator is asked to re-enter the data.

WEIBULL AND RAYLEIGH DISTRIBUTIONS

Two mathematical descriptions of the wind regime are supported by the code at this time. They are the Weibull and the Rayleigh distributions. The formulation for the Weibull distribution is given by:

$$p_{V} = \begin{bmatrix} \frac{\alpha}{\beta} \end{bmatrix} \begin{bmatrix} \frac{V}{\beta} \end{bmatrix}^{\alpha-1} \exp \left\{ - \begin{bmatrix} \frac{V}{\beta} \end{bmatrix}^{\alpha} \right\} , \qquad (13)$$

where p_V is the probability density function, α and β are the shape factor and the amplitude factor of the distribution, respectively. The Rayleigh distribution is a special case of the Weibull distribution, with $\alpha = 2$.

Typically, the shape factor α and the average wind speed V_m are used to describe the annual wind speed distribution at turbine sites (e.g., see Ref. 9). α and β are related to the average wind speed (velocity) V_m through the gamma function Γ :3

$$V_{\rm m} = \beta \Gamma \left[1 + \frac{1}{\alpha} \right] \qquad (14)$$

To maintain consistency, α and V_m are used as input variables. Eq. 14 is used to change them into the computational appropriate framework of α and β .

For this analysis, the gamma function Γ is evaluated using the following expression:10

$$\Gamma(1 + X) = 1 + \sum_{i=1}^{5} G(i) X^{i-1}$$
, (15)

where G(i), i = 1 to 5, are constants defined to be -0.5748646, 0.9512363, -0.6998588, 0.4245549 and -0.1010678, respectively. This expansion yields an absolute error that is always less the $5x10^{-5}$ for $0 \le X \le 1$.

C(V) is determined by numerically integrating the probability density function p_V . Let the i^{th} wind velocity intervals be defined as the interval between V_i and V_{i-1} , then the total probability for that interval $(P_V)_i$ may be approximated by:

$$(P_{V})_{i} = \int_{V_{i-1}}^{V_{i}} p_{V} dv \approx (p_{V})_{i} (V_{i} - V_{i-1})$$
, (16)

where $(p_V)_i$ is evaluated at the midpoint of the velocity interval, i.e., at $[(V_i + V_{i-1})/2]$. $C(V_i)$ is then determined using:

$$C(V_i) = 1.0 - \sum_{k=1}^{i} (P_V)_k$$
 (17)

Here, we assume that $(P_V)_1$ covers the entire interval from V = 0 to $V = V_1$.

PLOTTING ROUTINES

The code supports two classes of plots for the wind regime. They are the cumulative density function A(V) and the probability density function p_V . The first plot uses the relation:

$$C(V) = 1.0 - A(V)$$
 , (18)

to determine A(V) from C(V).

For the second plot, C(V) is numerically differentiated using the relation:

$$(p_{V})_{i} = \frac{\left[C(V_{i-1}) - C(V_{i}) \right]}{V_{i} - V_{i-1}}$$
 (19)

This term is centered at the average velocity of $(V_i + V_{i-1}) / 2$. This form is numerically equivalent to that used in Eqs. 10, 11, 16 and 17 to determine $C(V_i)$ from p_V .

INTERPOLATION

The computational modules use linear interpolation to determine $(P_V)_q$ in Eqs. 4 and 9. To evaluate each term in Eq. 11, the set of I ordered pairs $[V_i, C(V_i)]$ are interpolated using

$$C(V) = \frac{V - V_{i-1}}{V_{i} - V_{i-1}} \left[C(V_{i}) - C(V_{i-1}) \right] + C(V_{i-1}) . \qquad (20)$$

Here, the value of i is chosen using the relation:

$$i = \begin{cases} 2 & \text{for} & V \leq V_2 \\ j & \text{for} & V_{j-1} < V \leq V_j & \text{and} & j=2,3,..., \text{ or I-1.} \end{cases}$$

$$[1] \quad \text{for} \quad V_{j-1} < V \leq V_j \quad \text{and} \quad \text{if} \quad \text{if}$$

SUMMARY STATEMENT

The wind resource is described in the LIFE2 code as the probability density function, py, for the annual wind speed distribution. To increase the accuracy of the calculations and to accommodate the PC framework of the code, a tabular representation of the complementary cumulative density function has been chosen to transfer the annual wind speed distribution to the computation modules. Rayleigh, Weibull and tabular distributions are supported by the code. The code has the capability of displaying the annual wind speed distribution in graphical form.

CONSTITUTIVE FORMULATION

As discussed above, the LIFE2 code accepts two classes of constitutive formulations. The first is the classical "S-n" fatigue characterization that describes the number of stress cycles required to fail the component and the second is a linear fracture mechanics analysis that describes the rate of crack growth as a function of the cyclic change in the stress intensity factor.

S-n FATIGUE CONSTITUTIVE RELATIONS

The classical S-n fatigue characterization of a material describes the number of stress cycles N required to "fail" the material at a particular stress state. Each stress cycle is described by two terms, its mean stress S_m and its alternating stress S_a .⁴ The mean stress is defined to be the sum of the maximum and minimum values of the stress cycle divided by two, and the alternating stress is defined to be the range or the amplitude of the stress cycle (see discussion above).

As discussed above, the functional form chosen for the description of the constitutive material property $N(S_m,S_a)$ is tabular. Namely, the ranges of the mean stress and the alternating stress are divided into K and L intervals, respectively. At each ordered pair $[(S_m)_k, (S_a)_l]$, the table contains the number of cycles to failure at this stress state, N_{kl} . This two dimensional (2D) matrix may be entered into the code as a table or it may be calculated using standard formulations.

Tabular Input

To input the S-n constitutive table into the LIFE2 code, the values of $(S_m)_k$, k=1,K and $(S_a)_l$, l=1,L are entered. The code then prompts the user for each N_{kl} . The program assumes that all points in this matrix are defined.

If the S-n properties of a particular material are independent of mean stress, only the dependence of N on alternating stress must be defined in the input table.

Constitutive Relations

Four constitutive relationships for defining the S-n fatigue characterization matrix are supported by the LIFE2 code at this time. They are Goodman's rule using the yield stress, Goodman's rule using the ultimate stress, Gerber's rule and the modified Gerber rule.⁴ The general formulation for these rules is given by:

$$S_{a} = \sigma_{e} \left\{ 1 - \left[\frac{S_{m}}{\sigma_{ref}} \right]^{\gamma_{G}} \right\}$$
 (22)

where, σ_e is the effective cyclic stress amplitude, and the reference stress σ_{ref} and the exponent γ_G are constitutive parameters that are listed in Table I for the four different formulations. In this table, σ_y and σ_u are the yield stress and the ultimate stress of the material, respectively.

The number of cycles to failure at the effective stress σ_e is equal to the number of cycles to failure at stress state $S_m = 0$ and $S_a = \sigma_e$; i.e., $N(0,\sigma_e)$. Thus, the S-n material characterization for zero mean stress must be known. For the LIFE2 code, this relation is entered in tabular form. The set of ordered pairs that form this table are $[\sigma_i, N_i]$ for i=1,I.

TABLE I. Constitutive Parameters for the S-n Formulations.

Constitutive Relations	Constitutive Parameter		
	$\sigma_{ t ref}$	γ_{G}	
Goodman (Yield)	σ_{y}	1	
Goodman (Ultimate)	$\sigma_{ m u}$	1	
Gerber	$\sigma_{ m u}$	2	
Modified Gerber	$\sigma_{ m u}$	material constant	

This constitutive table that is transferred to the computational modules is set up automatically. First, a set of values for $(S_m)_k$ and $(S_a)_l$ are chosen. Then, σ_e is computed for each ordered pair $[(S_m)_k,(S_a)_l]$ using Eq. 22 and the appropriate constants from Table I. N_{kl} is determined by interpolating on the tabular values at zero mean stress. For this interpolation, an exponential (logarithmic) interpolation is used. The form used here is given by:

$$\log(N_{k1}) = \frac{\log(\sigma_{e}) - \log(\sigma_{i-1})}{\log(\sigma_{i}) - \log(\sigma_{i-1})} \left[\log(N_{i}) - \log(N_{i-1}) \right] + \log(N_{i-1}) . (23)$$

Here, the value of i is chosen using an equivalent relation to that described in Eq. 21.

Maximum and Minimum Values

For this code to be PC compatible, special attention must be given to the calculations described in Eq. 23. In particular, the range of single-precision real numbers that can be handled by a PC is approximately -1E-38 to 3E38.8 As these values could be exceeded by the interpolation, the code automatically limits the maximum value of N_{kl} to 1E37. The minimum value is limited to 1; i.e., one stress cycle is always required to fail the material.

Interpolation

The computational modules use logarithmic interpolation to determine $N_{rs}(\cdot)$ at $[(S_m)_r, (S_a)_s]$, see Eq. 4. To evaluate N_{kl} at $[(Sm)_k, (S_a)_l]$ from the constitute matrix transferred by the code, a two dimensional interpolation scheme must be used. The technique is equivalent to that cited in Eq. 23.

da/dn FRACTURE MECHANICS RELATIONS

The classical da/dn fracture mechanics characterization of a material describes the crack growth rate of a macro-crack as a function of the stress intensity factor. The relationship between the stress state and the crack length is discussed below. Typically, the stress intensity factor is taken to have two components, a mean and an alternating stress intensity factor, κ_m and κ_a , respectively. As discussed above, the functional form chosen to describe the constitutive material property da/dn(κ_m , κ_a) is tabular. Namely, the ranges of the mean and the alternating stress intensity factors are divided into K and L intervals, respectively. The table contains the crack growth rate at each ordered pair $[(\kappa_m)_k, (\kappa_a)_l]$ of stress intensity factors. This matrix may be entered as a table or it may be calculated using standard formulations.

Tabular Input

To input the da/dn constitutive table into the LIFE2 code, the values of $(\kappa_m)_k$, k=1,K and $(\kappa_a)_l$, l=1,L are entered; the code then prompts the user for each $(da/dn)_{kl}$. The program assumes that all points in this matrix are defined.

If the da/dn properties of a particular material are independent of mean stress, only the dependence of da/dn on alternating stress must be defined in the input table.

Constitutive Relations

Many constitutive equations have been proposed for the description of crack propagation in metallic materials. One general form proposed by Forman^{5,11} is supported by the LIFE2 code at this time. The governing equation for this formulation is given by:

$$\frac{\mathrm{da}}{\mathrm{dn}} = \frac{C (1 - R)^{\mu} \Delta \kappa^{\nu} [\Delta \kappa - \Delta \kappa_{\mathrm{th}}]^{\eta}}{[(1 - R) \kappa_{\mathrm{c}} - \Delta \kappa]^{\psi}}, \qquad (24)$$

where a is the current crack length; n is the number of stress cycles; R is the stress ratio⁴; $\Delta \kappa$ is the change in the stress intensity factor κ at the crack tip for cycle n; and C, μ , ν , η , ψ , $\Delta \kappa_{th}$ and κ_{c} are material parameters (constants) defined by Forman.⁵

As noted by Forman⁵ this formulation may be reduced to other commonly used forms by setting the exponents μ , η and ψ to the values listed in Table II.

In Table II, m_W is another material constant. Ref. 11 lists a set of constants, for various materials, that may be used in this formulation. The appendix describes the procedure for obtaining the constitutive table required here from these parameters.

TABLE II. Specialized Values for the Exponents in the Forman Constitutive Equation.

Proposed Constitutive	Exponent		
Relation	μ	η	ψ
Paris	0	. 0	0
Forman	0	0	1
Walker	(m _W -1)ν	0	0

Interpolation

The computational modules use logarithmic interpolation to determine $(da/dn)_{rs}$ at $[(\kappa_m)_r, (\kappa_a)_s]$. The technique is equivalent to that cited in Eq. 23. To evaluate this term, from the 2D matrix transferred from the code, $(da/dn)_{kl}$ at $[(\kappa_m)_k, (\kappa_a)_l]$, a two dimensional interpolation scheme must be used. This scheme is identical to that used to determine N_{rs} at $[(S_m)_r, (S_a)_s]$ from N_{kl} at $[(Sm)_k, (S_a)_l]$. As the interpolation scheme is discussed above, it is not duplicated here.

PLOTTING ROUTINES

The code supports plots of these constitutive relations. For the S-n formulations, a family of curves is presented. Each curve is a plot of the cycles-to-failure versus the alternating stress level for a constant mean stress. For the da/dn formulations, two classes of plots are supported. The first class is a family of curves of da/dn versus κ_a at constant κ_m and the second is a family of curves of da/dn versus κ_a at constant R. The latter class of plots is for illustration purposes only. As noted to the operator by a prompt from the code, these data must not be used for the calculation of the service lifetime.

SUMMARY STATEMENT

The constitutive properties of a material are described in the LIFE2 code using the classical S-n fatigue characterization and a da/dn fracture mechanics characterization. The form chosen for the transfer of this information to the computational modules is a 2D matrix. For the S-n characterization, the cycles to failures are specified over a range of mean stresses and alternating stress. Four constitutive relations are supported. For the da/dn characterization, the crack growth rate is specified over a range of mean

and alternating stress intensity factors. A generalized constitutive relation is supported. Any constitutive characterization may be input in tabular form.

STRESS STATES

The LIFE2 code accepts three classes of stress states for the turbine. They are the operational stresses, parked stresses (i.e., the stresses due to the wind buffeting a parked blade) and start-stop stresses. The first two are taken to be functions of time and the last as specific events. All three stress states are characterized using three dimensional (3D) cycle count matrices of the form n_{qrs} . Each of these matrices contains the stress cycle count associated with a fixed time period (or a fixed number of events) and a particular operating condition of the turbine. Thus, they describe, on the average, the stress cycles imposed upon the turbine whenever it is in this particular operating condition.

In each matrix (commonly called a "rain flow" matrix), each stress cycle is characterized as a function of its mean stress $(S_m)_r$ and its alternating stress $(S_a)_s$. To save memory in the operational RAM, the 3D cycle count matrix n_{qrs} is defined as a set of Q 2D-matrices, $(n_{rs})_q$, and only one of these matrices is held in the operational RAM at any one time.

It should be noted here that the stress states [$(S_m)_r$, $(S_a)_s$] are not required to be equivalent to the state states [$(S_m)_k$, $(S_a)_l$] or the stress intensity factor states [$(\kappa_m)_r$, $(\kappa_a)_s$] that are used to describe the constitutive properties of the material, see above.

OPERATIONAL STRESSES

The operational stress states are input into the LIFE2 code as a series of cyclic count matrices. Each matrix is defined for a specific wind interval ΔV_q and a time interval Δt_q , where:

$$\Delta V_{q} = V_{q} - V_{q-1} \qquad (25)$$

The code assumes that the first interval covers the wind interval from zero to V₁.

For each of these velocity intervals, the code accepts a cycle count matrix n_{rs} that is determined from the stress-time history of the component when the wind turbine is being operating with an average wind speed of $(V_q + V_{q-1})/2$ for a time of Δt_q .

Tabular Input

To input the operational stress matrices into the LIFE2 code, the code prompts the user for V_q , the time Δt_q , $(S_m)_r$ for r=1,R and $(S_a)_s$ for s=1,S. Then the values for n_{rs} are

entered. This process is repeated for each wind speed interval. The program assumes that all points in each one of these matrices are defined. The values of $(S_m)_r$ and $(S_a)_s$ may be different for each velocity interval V_q .

Narrow-Band Gaussian Model

One technique for modeling the operational stresses is supported by the LIFE2 code at this time. This technique was used by Veers⁶ to model the operational stress states of a vertical axis wind turbine (VAWT) component. The technique is based on the assumption that the amplitude of the vibrational stresses at any wind speed follows the distribution of peak values of a narrow-band Gaussian process; i.e., a Rayleigh distribution. The conditional probability density function $p_S \mid_V$ of the vibratory stress S_a occurring at a particular wind speed V may be written as:

$$p_{S|V} = \begin{bmatrix} \frac{s_a}{\sigma_V^2} \\ \sigma_V \end{bmatrix} \exp \begin{bmatrix} \frac{-s_a^2}{2\sigma_V^2} \\ \end{bmatrix} , \qquad (26)$$

where σ_V is the standard deviation of the vibratory stresses. Here, we assume that σ_V is only a function of the wind speed V.

The functional relationship between the wind speed and σ_V is input in tabular form as a set of ordered pairs of the form $[V_i, (\sigma_V)_i]$ For values of V that lie between the tabulated points, linear interpolation, see Eq. 20 and 21, is used to determine the value of σ_V .

To determine the cyclic count matrix from this formulation, the probability density function in Eq. 26 is integrated over a series of S cyclic count intervals, at each wind speed V_q . Namely,

$$(P_{S|V})_{s} = \begin{bmatrix} (S_{a})_{s} \\ \frac{S_{a}}{\sigma_{V}^{2}} \end{bmatrix} \exp \left[\frac{-S_{a}^{2}}{2\sigma_{V}^{2}} \right] dS_{a}$$

$$(27)$$

The integration is centered in the wind speed interval by evaluating σ_V at the midpoint between V_{q-1} and V_q .

This formulation assumes that the mean stress S_m is a constant at all wind speeds, i.e., the turbine is operated at constant rotational speed (the magnitude of this mean stress is an input parameter to the code).

Thus, a probability matrix has been determined for the stress cycles at each wind speed interval V_q . Each one of these matrices is composed of one column of S elements. The sth element is the probability of occurrence of a stress cycle with a mean stress of S_m and an alternating stresses in the range between $(S_a)_{s-1}$ and $(S_a)_s$.

To convert these probabilities into cycle count matrices, the rate at which the stress cycles occur must be known. Veers assumes that the stress cycle rate is, on the average, equal to the dominant frequency of blade vibration f_0^6 or the rate of mean level crossings.¹² Thus, the time Δt for the average stress cycle is given by:

$$\Delta t = \frac{1}{f_0} \qquad (28)$$

To maintain correct units of time, the LIFE2 code assumes that the frequency f_o has units of Hz.

Thus, the probability matrices become cycle count matrices by setting their count period Δt_q to Δt .

PARKED STRESSES

The parked stress states are also input as a series of cyclic count matrices. Each matrix is defined for a specific wind interval ΔV_q . For each of these velocity intervals, the code accepts a cycle count matrix n_{qrs} in which the number of stress cycles are characterized as a function of the mean stress and the alternating stress. Each stress cycle count matrix is based on the count from a specific time period Δt_q . At this time, only tabular inputs may be used to define these cyclic count matrices.

START-STOP STRESSES

The start-stop stress states are also input as a series of 2D cyclic count matrices. Each matrix is based on the count from a specific number of start-stop events, η_q . For each state, the code accepts a cycle count matrix n_{rs} in which the number of stress cycles (for a specified number of starts or stops) are characterized as a function of the mean stress and the alternating stress. Each input matrix is defined for a class of starts and/or stops, e.g. normal start, high wind start, normal stop, high wind stop, emergency stop, "lost of grid stop", etc. At this time, only tabular inputs may be used to define these cyclic count matrices.

STRESS INTERVAL

One should note that in the formulation cited here, a stress cycle that is counted in the interval described by its end points $[(S_m)_r$, $(S_a)_s]$ has an actual stress state anywhere between $[(S_m)_{r-1}$, $(S_a)_{s-1}]$ and $[(S_m)_r$, $(S_a)_s]$. To assure conservative results, all stress cycles are assumed to occur at the maximum stress levels for that interval; i.e., at $[(S_m)_r$, $(S_a)_s]$.

SUMMARY STATEMENT

The operational stress states are described in the LIFE2 code as a series of cycle count matrices. Three classes of stress states are analyzed by the code. They are the operational stress states, the parked stress states, and the start-stop stress states. The first two states are taken to be functions of wind speed and the last state is taken to be a series of discrete events. A narrow band Gaussian model⁶ is supported for the determination of operational stresses. Tabular data is accepted for all three stress states.

OPERATIONAL PARAMETERS

The forth section of the LIFE2 code describes the miscellaneous operational parameters for the turbine that are required for the calculations.

OPERATION REGIME

The first two parameters are the minimum and maximum wind speed at which the turbine is operated, commonly called the "cut-in" wind speed V_{ci} and the "cut-out" wind speed V_{co} .

PARKED STRESS CYCLES

The next set of parameters describes the annual average time spent in each interval of the parked stress matrices. The parameter P_V is the annual average fraction of time for the q^{th} parked stress matrix. This number is entered by the operator rather than being calculated from the wind speed distribution.)

START-STOP CYCLES

The next set of parameters describes the number of start-stop events for each cycle count matrix recorded in the start-stop stress matrices. The parameter \hbar_q is the yearly average number of events for the q^{th} start-stop matrix.

STRESS CONCENTRATION FACTORS

The final two parameters relate the stress state used in the cycle count matrices to the actual stress state anticipated in the turbine component. These two parameters are used to describe the stress concentration factor γ_t and the safety factor γ_{SF} used in the analysis. Typically, the γ_t is divided into its contributing factors through the relation 11

$$\gamma_{t} = \gamma_{1} * \gamma_{2} * \cdots * \gamma_{n} \qquad . \tag{29}$$

Each γ_i is the stress concentration factor due to a particular phenomenon. Typical stress concentration factors that should be considered for turbine applications include the type of loading, size effects, surface roughness, surface treatment, penetrations, notch sensitivity, etc. A description of various factors is given in Refs. 4, 13, 14, and 15.

If we define the total "stress concentration factor" γ to be:

$$\gamma = \gamma_{t} * \gamma_{SF} , \qquad (30)$$

Then, the nominal stress state S is related to the component stress state S_c by:

$$S_{c} = \gamma S \qquad . \tag{31}$$

As γ is different for a fatigue and fracture analyses, see below, two parameters are defined here, γ_f for the fatigue analysis and γ_r for the fracture analysis. The implementation of Eq. 31 into the service lifetime calculation is described below in Eqs. 35, 36, 47 and 48.

DAMAGE CALCULATION

The fifth section of the code uses the inputs from the other four sections to determine the service lifetime of the turbine component. At this time, the service lifetime may be computed using either one of two damage rules. The first is Miner's rule,⁴ see Eq. 4, and the second is based on linear fracture mechanics, see Eq. 9.

The computations for each technique proceed along similar lines. The computational steps are:

- 1. The code reads into current memory the files generated by the other four modules and creates a "summary file" to record the input parameters that are being used for this particular calculation.
- 2. The code reads in each cycle count matrix $(n_{rs})_q$ and adjusts it to an equivalent annual cycle count. The operational and the parked cycle count matrices are adjusted to an annual average using the time parameter Δt_q and the fraction of the time, $(P_V)_q$, at which the turbine operates in the wind velocity interval V_{q-1} to V_q . For operational stresses, the time fraction is determined from the wind speed distribution. For the parked stresses, the time fraction is set explicitly by the operator. The start-stop cycle count matrices are adjusted to an annual average using the count parameters η_q and \hbar_q .
- 3. The nominal stress levels in each matrix are adjusted to the component stress levels (stress intensity factors) by using the appropriate "stress concentration factor"; i.e., γ_f or γ_r and the range-to-amplitude or amplitude-to-range variable (see below).
- 4. The constitutive relation is interpolated to determine the damage rate per cycle at each adjusted stress (or stress intensity) state.
- 5. The damage rule and adjusted damage rate per cycle are used with the cycle count matrix to determine the annual average damage rate for each stress (or stress intensity) state in that cycle count matrix.
- 6. The damage rates are summed for all stress (or stress intensity) states in that cycle count matrix.
- 7. Steps 2 through 6 are repeated for each of the operational, parked and start-stop cycle count matrix.
- 8. Each damage rate is summed over the wind velocity interval from V_{ci} to V_{co} for the operational stress; for all velocities greater than V_{co} for the parked stresses; and for all start-stop stresses.
- 9. Fatigue calculation:

The sum computed in step 8 is the total annual average damage rate for the turbine. This average damage rate is inversely proportional to the service lifetime of the component.

Fracture analysis:

- a. The sum computed in step 8 is the annual average growth rate for the current crack length. This crack growth rate defines the time for the crack to grow from a_{w-1} to a_w.
- b. Steps 2 through 8 are repeated for the each interval of crack growth.

c. The time for the crack to grow across each interval is summed to determine the time required for the crack to grow from its initial length a_0 to its specified final length a_f .

Thus, the code computes the triple sum described in Eq. 4 for the fatigue analysis and the quadruple sum in Eq. 9 for the fracture analysis. The particular order of calculations described above was chosen to facilitate archiving intermediate calculations for future reference.

ANNUAL AVERAGE CYCLE COUNT

Operational and Parked Cycle Count Matrices

The adjustment for the operational and parked cycle count matrices to the annual average cycle count is identical for both damage rules. In the procedure used by the LIFE2 code, the annual average time, $(T_{aa})_q$, that the turbine is subjected to a wind velocity interval V_{q-1} to V_q is determined first. This time equals:

$$(T_{aa})_{q} = T (P_{V})_{q} , \qquad (32)$$

where T is the total time contained in one year and $(P_V)_q$ is the annual average probability for this wind interval. For operational stress states, the later parameter is determined using the interpolating technique on C(V) described in Eqs. 20 and 21. For parked stress states, P_V is an input variable.

To determine the total number of stress cycles for one year of operation, each cycle count $(n_{rs})_q$ is multiplied by T_{aa} and divided by Δt_q (the time length for the cycle count matrix). Thus, the annual average cycle count for a operational and parked stress cycle count matrices, $(\hat{n}_{rs})_q$

$$\left(\hat{n}_{rs}\right)_{q} = \frac{\left(T_{aa}\right)_{q}}{\Delta t_{q}} \left(n_{rs}\right)_{q} = \left(P_{V}\right)_{q} \frac{T}{\Delta t_{q}} \left(n_{rs}\right)_{q} . \tag{33}$$

The implementation of this relation requires that the units of Δt_q be known. The LIFE2 code assumes that Δt_q has the units of seconds. Thus, T = 365.25 day/yr • 24 hr/day • 60 min/hr • 60 sec/min = 31,557,600 sec.

Start-Stop Cycle Count Matrices

The adjustment for each start-stop cycle count matrix is the equivalent relationship:

$$\left(\hat{\mathbf{n}}_{rs}\right)_{q} = \frac{\dot{\eta}_{q}}{\eta_{q}} \left(\mathbf{n}_{rs}\right)_{q} . \tag{34}$$

ALTERNATING STRESS PARAMETER

As discussed above, the alternating stress may be described as either a range variable or an amplitude variable. During the initial set-up of both damage calculations, the operator is given the option of changing the operational stresses, parked stresses and start-stop stresses between the two. The range/amplitude multiplier γ_A is set equal to 1.0 for no change, to 0.5 for changing from range to amplitude, or to 2.0 for changing from amplitude to range. This variable is then incorporated into the damage calculation as describe in Eqs. 36 and 48.

OPERATIONAL WIND SPEEDS

The damage calculations for the operational stress states, described below in Eqs. 38 and 50, are evaluated for each operational-stress cycle count matrix. If one operational stress matrix does not correspond to the cut-in wind speed V_{ci} , another to the cut-out wind speed V_{co} , then the linear interpolation is used to determine the damage rates at these end points.

This numerical technique for calculating the end points of these summations was chosen to permit the damage rates for all defined stress matrices to be examined by the operator. However, this choice can produce significant numerical errors in the damage calculation if the stress matrices cover relatively large velocity increments. To alleviate this problem, the stress matrices entered by the operator should have relatively small velocity increments when compared to the cut-in wind speed.

FATIGUE ANALYSIS

The S-n fatigue analysis module in the LIFE2 code uses Miner's Rule⁴ to describe the initiation, growth and coalescence of micro-cracks into macro-cracks.

As described above, the cycle count matrices are read into operational RAM, one at a time, and then adjusted to the annual average cycle count, see Eqs. 32 and 33. At this time the nominal stress levels for each cycle count are adjusted to the component stress levels using the stress concentration factor γ_f and the range/amplitude factor γ_A .

Stress Concentration Factor

The LIFE2 code offers two options for changing the nominal stresses to the component stresses using the stress concentration factor γ_f . The choices are (1) applying γ_f to only the alternating stress; and (2) applying γ_f to both the alternating and mean stress.

For the latter case, the nominal mean stresses $(S_m)_r$ in each cycle count matrix (i.e., all operational stress matrices, all parked stress matrices, and all start-stop matrices) is

multiplied by the fatigue stress concentration factor γ_f to obtain the component mean stress levels $(\hat{S}_m)_s$; namely,

$$(\hat{S}_{m})_{r} \Big|_{q} = \gamma_{f} (S_{m})_{r} \Big|_{q}$$
 (35)

And for both cases, the nominal alternating stresses $(S_a)_s$ in each matrix is multiplied by the same fatigue stress concentration factor γ_f and the range/amplitude multiplier γ_A to obtain the component stress levels $(\hat{S}_a)_s$; namely,

$$(\hat{S}_a)_s \Big|_{q} = \gamma_A \gamma_f (S_a)_s \Big|_{q} . \tag{36}$$

Cycles to Failure

After the cycle count and the stress states in the cycle count matrices have been have been adjusted, the S-n fatigue characterization matrix (i.e., the fatigue constitutive relation matrix) is then interpolated to determine the number of cycles to failure at each stress state in the current cycle count matrix. Thus, the constitutive matrix is mapped into the cycle count matrix's stress states; namely,

$$N[(S_{m})_{k},(S_{a})_{1}] \Rightarrow \hat{N}[(\hat{S}_{m})_{r},(\hat{S}_{a})_{s}] \qquad (37)$$

If all of the cycle count matrices have exactly the same stress states $[(\hat{S}_m)_r, (\hat{S}_a)_s)]$, then this interpolation needs to be conducted only once. The code permits the operator to specify this class of operation. The operator must be careful when using this option because the program does not verify that the stress states are equivalent.

Damage Calculation

With the completion of the mapping described in Eq. 37, the sum described in Eq. 4 can be obtained. As the program holds only one cycle count matrix in current memory at any one time, the summation is conducted in steps. First, the damage for each cycle count matrix is determined. Namely, for each operational, parked and start-stop matrix, the sum

$$D_{q}(T) = \sum_{r=1}^{R} \sum_{s=1}^{S} \frac{\hat{n}_{qrs}[(\hat{s}_{m})_{r}, (\hat{s}_{a})_{s}, T]}{\hat{N}_{rs}[(\hat{s}_{m})_{r}, (\hat{s}_{a})_{s}]} .$$
 (38)

is computed. Then, the average damage accumulated in one year D(T) is determined by summing over all of these operational conditions (i.e., operational stress states from V_{ci} to V_{co} , all parked stress states and all start-stop stress states) using the relation:

$$D(T) = \sum_{q=1}^{Q} D_q(T)$$
 (39)

The predicted service lifetime in years is determined using D(T) and Eq. 3.

FRACTURE ANALYSIS

The linear fracture mechanics analysis module in the LIFE2 code uses a "da/dn" analysis⁴ to describe the propagation of a pre-existing macro-crack. As da/dn is a function of the current crack length, the calculation is divided into a finite number of steps. For each step, the crack length is taken to be a constant, and an average growth rate is determined. This average rate is then used to determine the time required for the crack to grow across that integration segment. The sum over all of the integration segments yields the time of growth for the crack from its initial size to its final size.

As described above, the cycle count matrices are read into operational RAM, one at a time, and then adjusted to the annual average cycle count, see Eqs. 32 and 33. At this time the nominal stress levels for each cycle count are mapped into the component stress intensity factors using the current crack length, the fracture stress concentration factor γ_f and the range/amplitude factor γ_A .

Current Crack Length

As the crack growth rate da/dn is a function of the crack length, the current crack length must be known before the calculation can proceed. The numerical solution to this dependence of the integrand on the independent variable is to divide the calculation into a finite number of steps with the crack length held constant for each step. A logarithmic variation is used in the LIFE2 code for this series. For I equal to the number of intervals per decade, the crack length at the completion of step w, a_w, is given by:

$$\log_{10}(a_{w}) = \log_{10}(a_{0}) + \frac{w}{I}$$
 (40)

The initial value of this series, a₀, is defined to be:

$$\log_{10}(a_0) = AINT[\log_{10}(a_i)],$$
 (41)

where, AINT(•) is the greatest integer function that truncates its argument to an integer. The final term in the series in chosen such that:

$$\log_{10}(a_W) = AINT[\log_{10}(a_f) + 1]$$
 (42)

This choice for the initial and final values of the crack length used in the calculations is based on keeping the calculations as versatile as possible.

For each interval, the current crack size is taken to be at the center of interval:

$$\hat{a}_{W} = \frac{a_{W} + a_{W-1}}{2} . \tag{43}$$

Stress Intensity Factor

The stress intensity factor κ is a function of the stress and the current crack length. The relation between the three is:

$$\kappa = Y_{0} \sqrt{\pi \hat{a}_{W}} S , \qquad (44)$$

where Y_0 is a geometric shape factor. Y_0 may be a constant, or it may be a function of the crack length $a.^{14,15}$ At this time, the LIFE2 code only permits κ to depend upon \sqrt{a} . Therefore, the "fracture stress concentration factor" γ_r is defined to be:

$$\gamma_{\rm r} = Y_{\rm o} \sqrt{\pi} \qquad . \tag{45}$$

And, the LIFE2 code maps the current stress states into the the stress intensity factors through the relation

$$\kappa = \gamma_{r} \sqrt{\hat{a}_{W}} S \qquad . \tag{46}$$

The relations that are used to map the mean stresses and the alternating stresses into the mean and alternating stress intensity factors are:

$$(\kappa_{\mathbf{m}})_{\mathbf{r}} \Big|_{\mathbf{q}} = \gamma_{\mathbf{r}} \sqrt{\hat{\mathbf{a}}_{\mathbf{w}}} (S_{\mathbf{m}})_{\mathbf{r}} \Big|_{\mathbf{q}} ,$$
 (47)

and,

$$(\kappa_a)_s \Big|_q = \gamma_A \gamma_r \sqrt{\hat{a}_w} (S_a)_r \Big|_q$$
, (48)

respectively.

Crack Growth Rate

After the cycle count and the stress states in the cycle count matrices have been have been adjusted, the da/dn crack growth rate matrix (i.e., the fracture mechanics constitutive relation matrix) is then interpolated to determine the crack growth rate at each stress intensity state in the current cycle count matrix. Thus, the constitutive matrix is mapped into the crack growth rate matrix's stress intensity states:

$$\frac{\mathrm{d}a}{\mathrm{d}n} \left[\left(\kappa_{\mathrm{m}} \right)_{\mathrm{k}}, \left(\kappa_{\mathrm{a}} \right)_{1} \right] \Rightarrow \frac{\mathrm{d}\hat{a}}{\mathrm{d}n} \left[\left(\kappa_{\mathrm{m}} \right)_{\mathrm{r}}, \left(\kappa_{\mathrm{a}} \right)_{\mathrm{s}} \right] \qquad (49)$$

Damage Calculation for the Current Crack Length

With the completion of the mapping described in Eq. 49, the sum described in Eq. 9 can be obtained. The summation is conducted in steps, because the program holds only one cycle count matrix in current memory at any one time. First, the extension of crack for each cycle count matrix is determined for each operational, parked and start-stop matrix by computing the sum

$$\Delta a_{\text{wq}}(T) = \sum_{r=1}^{R} \sum_{s=1}^{S} \frac{d\hat{a}_{\text{wrs}}(\kappa_{\text{m}}, \kappa_{a})}{dn} \hat{n}_{\text{wqrs}}[(\kappa_{\text{m}})_{\text{wr}}, (\kappa_{a})_{\text{ws}}, V_{q}, T)] . \quad (50)$$

Then, the total extension of the crack for one year $\Delta a_w(T)$ is determined by summing over the operational conditions (i.e., operational stress states from V_{ci} to V_{co} , all parked stress states and all start-stop stress states) using the relation

$$\Delta a_{\mathbf{w}}(T) = \sum_{\mathbf{q}=1}^{\mathbf{Q}} \Delta a_{\mathbf{w}\mathbf{q}}(T) \qquad . \tag{51}$$

As this crack extension calculation assumes that the current crack length is growing from a_{w-1} to a_w , then the time in years for the crack across this interval is given by:

$$\Delta t_{w} = \frac{a_{w} - a_{w-1}}{\Delta a_{w}(T)} \qquad (52)$$

Thus, the total time, in years, required for the crack to grow from a_i to a_f is the sum of the these times. If a_i does not correspond to a_0 and a_f to a_W , see Eqs. 41 and 42, then linear interpolation is used to determine the initial and the final time steps in this series.

SUMMARY STATEMENT

The damage calculations preformed by the LIFE2 code use the tabular input from the four other modules to determine the service lifetime of a turbine component. Two damage rules are currently available. The first rule uses a classical S-n fatigue analysis that is based on Miner's Rule⁴ to sum the damage over all of the imposed stress states. This formulation is used to describe the initiation of micro-cracks and their growth and coalescence into macro-cracks. The second damage rule uses a linear fracture mechanics analysis⁴ to predict the growth of a pre-existing macro-crack from its initial size to its final size.

SUMMARY

The LIFE2 computer code is a fatigue/fracture analysis code specifically designed for the analysis of wind turbine components. This paper describes the numerical formulations that have been implemented in the code. It is meant to be the companion paper for the user's manual that is published under separate cover⁷.

From its inception, this code has been designed for a PC or compatible computer. This decision has required that the numerical implementation of the analysis techniques used here be formulated to fit on this comparatively small machine. Extensive overlays and read/write statements have been implemented in the code to permit the effective use of available operational RAM. And, as this class of machine has comparatively few significant digits, numerical algorithms had to be chosen carefully to prevent large numerical round-off errors from invalidating the results of the analysis.

The code is written in a top-down modular format and data transfer between modules is handled using data transfer files. This open architecture was chosen here because it permits the code to be modified and subroutines to be added to it with relative ease and because it greatly simplifies the validation of the modified code. An additional benefit of this formulation is that calculations are easily archived for future reference. However, this formulation does present a significant problem in that it requires the extensive use of tabular data and interpolation schemes. Thus, the accuracy of the calculations is decreased. Numerical techniques are employed in the code to insure that the decreased accuracy does not become significant.

Two constitutive formulations are currently available in the code. The first uses a conventional S-n fatigue analysis and the second uses linear da/dn fracture mechanics analysis. The former is used to describe the initiation, growth and coalescence of micro-cracks into macro-cracks and the latter is used to describe the growth of macro-cracks.

ACKNOWLEDGMENTS

The LIFE2 code is an outgrowth of the LIFE code. The latter code was initially conceived and written by P. S. Veers⁶ and subsequently modified by H. J. Sutherland, T. D. Ashwill and N. Slack¹⁶. L. L. Schluter, K. A. Naassan, J. R. Wright and D. Vetter have made significant contributions to the coding of this analysis. The author wishes to thank these people for their contributions to the development of the LIFE2 computer code.

REFERENCES

- 1. H. J. Sutherland, T. D. Ashwill, and K. A. Naassan, "Fatigue Analysis Codes for WECS Components", <u>Proceedings of WindPower '87</u>, SERI/CP-217-3315 (Golden: SERI, October 1987), pp. 74-78.
- 2. H. J. Sutherland and L. L. Schluter, "Crack Propagation Analysis of WECS Components Using the LIFE2 Computer Code", <u>Proceedings of the Eighth ASME Wind Energy Symposium</u> (New York: ASME, January 1989), pp.141-145.
- 3. B. L. Amstadter, Reliability Mathematics (New York, McGraw-Hill, 1971).
- 4. C. C. Osgood, Fatigue Design, 2nt Edition (Oxford: Pergamon Press, 1982).
- 5. R. G. Forman, <u>Derivation of Crack Growth Properties of Materials for NASA/FLAGRO</u>, Materials Branch Report 86-ES5-1 (NASA,1986).
- 6. P. S. Veers, <u>A General Method for Fatigue Analysis of Vertical Axis Wind Turbine Blades</u>, SAND82-2543 (Albuquerque: Sandia National Laboratories, 1983).
- 7. L. L. Schluter and H. J. Sutherland, <u>Reference Manual for the LIFE2 Computer Code</u>, SAND89-1396 (Albuquerque: Sandia National Laboratories, 1989).
- 8. Microsoft FORTRAN Optimizing Compiler, Version 4.1, Microsoft Corp. (1987).
- 9. W. R. Barchet, "Wind Energy Data Base," <u>Proceedings of the Fifth Biennial Wind Energy Conference and Workshop II</u>, SERI/CP-635-1340 (Golden: Solar Energy Research Institute, 1981).
- 10. M. Abramowitz and L. A. Stegan, <u>Handbook of Mathematical Functions</u>, NBS Applied Math Series, No. 55 (Washington: US Government Printing Office, 1964).
- 11. R. G. Forman, et al., <u>Fatigue Crack Growth Computer Program</u> "NASA/FLAGRO, JSC-22267 (NASA, 1986).
- 12. P. S. Veers, "Simplified Fatigue Damage and Crack Growth Calculations for Wind Turbines," <u>Proceedings of the Eighth ASME Wind Energy Symposium</u>, SED-Vol. 7 (New York: ASME, 1988).
- 13. R. E. Peterson, <u>Stress Concentration Factors</u>, <u>Charts</u>, <u>and Relations Useful in Making Strength Calculations for Machine Parts and Structural Elements</u> (New York: John Wiley and Sons, 1974).
- 14. H. O. Fuchs and R. I. Stephens, <u>Metal Fatigue in Engineering</u>, 8th Edition (New York: McGraw-Hill, 1978).

- 15. R. W. Hertzberg, <u>Deformation and Fracture Mechanics of Engineering Materials</u> (Wiley, New York, 1977).
- 16. H. J. Sutherland, T. D. Ashwill and N. Slack, <u>The LIFE Computer Code: Fatigue Life Prediction for Vertical Axis Wind Turbine Components</u>, SAND87-0792 (Albuquerque, Sandia National Laboratories, 1987).

APPENDIX

FORMAN CONSTITUTIVE MODEL

The constitutive equation proposed by Forman^{5,11} is presented in Eq. 24 of this report. In his tabulation of materials¹¹, Forman presents the formulation based on a different set of material parameters (see Table A-I for a list of this parameter set). The implementation of the latter set of parameters into the LIFE2 code is described here.

For the LIFE2 code, the fracture constitutive formulation requires that da/dn be written as a function of the mean stress intensity factor κ_m and the alternating stress intensity factor κ_a . As Eq. 24 is written in terms of the stress ratio R, each set of the stress parameters were mapped into their equivalent R value using:

$$R = \frac{\kappa_{\rm m} - \left[\kappa_{\rm a}/2\right]}{\kappa_{\rm m} + \left[\kappa_{\rm a}/2\right]} \tag{A-1}$$

Note that this formulation assumes that κ_a is a range variable as is the convention for this class of constitutive relations.

To simplify the numerical implementation of this constitutive formulation, Eq. 24 is simplified into three regions: R < 0, R = 0 and R > 0. For R = 0, Eq. 24 becomes:

$$\frac{\mathrm{da}}{\mathrm{dn}} = \frac{C \Delta \kappa^{\nu} \left[\Delta \kappa - \Delta \kappa_{\mathrm{th}}\right]^{\eta}}{\left[\kappa_{\mathrm{c}} - \Delta \kappa\right]^{\psi}} . \tag{A-2}$$

In terms of Forman's input parameter set:

$$\kappa_{c} = \kappa_{Ic} \left[1 + B_{k} \exp(-w) \right] ,$$
(A-3)

$$w = \left[A_k \frac{t}{t_0} \right]^2 , \qquad (A-4)$$

$$t_{o} = 2.5 \left[\frac{\kappa_{Ic}}{\sigma_{y}} \right]^{2} , \qquad (A-5)$$

and,

$$\Delta \kappa_{\rm th} = \Delta \kappa_{\rm o}$$
 (A-6)

In these relations, σ_y is the yield strength of the material and t is the thickness of the component being analyzed.

For non-zero values of R, define the following to be:

A0 =
$$(0.085 - 0.34 \alpha_{\rm F} + 0.05 \alpha_{\rm F}^2) \cos \left[\frac{\pi \left[s_{\rm max} / \sigma_{\rm o} \right]}{2} \right]^{1/\alpha_{\rm F}}$$
, (A-7)

A1 =
$$(0.415 - 0.071 \alpha_{F}) [S_{max}/\sigma_{O}]$$
, (A-8)

$$A3 = 2 A0 + A1 - 1.0$$
 , (A-9)

and,

$$A2 = 1.0 - A0 - A1 - A3$$
 , (A-10)

where α_F is a Forman input variable and $[S_{max}/\sigma_0]$ is a material variable that is assumed to be equal to 0.3.

Then, for R < 0 define:

$$[S_{o}/S_{max}] = A0 + A1 R$$
 , (A-11)

$$\left[S_{o}/S_{max}\right]_{R} = A0 \qquad , \tag{A-12}$$

and,

$$[\Delta \kappa]_{\text{eff}} = [\Delta \kappa]_1 \frac{[S_0/S_{\text{max}}]}{[S_0/S_{\text{max}}]_R} (1 - R) . \tag{A-13}$$

The crack growth rate for R < 0 is then given by:

$$\frac{da}{dn} = \frac{\frac{C (\Delta \kappa)^{\nu}_{eff} [(\Delta \kappa)_{eff} - \Delta \kappa_{th}]^{\eta}}{\left[\kappa_{c} - (\Delta \kappa)_{eff}\right]^{\psi}}.$$
(A-14)

For R > 0, define,

$$[S_0/S_{max}] = max\{ R, A0 + A1 R + A2 R^2 + A3 R^3 \}$$
, (A-15)

where max(•) chooses the maximum argument,

$$\Delta \kappa_{\rm th} = \left[1 - C_{\rm o} R \right]^{\rm d} \Delta \kappa_{\rm o} , \qquad (A-16)$$

and, $(\Delta \kappa)_{eff}$ using the definition given in Eq. A-13.

Then, the crack growth rate for R > 0 is given by the equivalent formulation of Eq. A-14, namely:

$$\frac{da}{dn} = \frac{C \left(\Delta\kappa\right)_{eff}^{\nu} \left[\left(\Delta\kappa\right)_{eff}^{\nu} - \Delta\kappa_{th}\right]^{\eta}}{\left[\kappa_{c} - \left(\Delta\kappa\right)_{eff}\right]^{\psi}} \qquad (A-17)$$

Table A-I cross references the symbols used in this report with the symbols used by Forman in Ref. 11. The LIFE2 code asks for these constitutive constants using the symbols that were used by Forman in Ref. 11.

TABLE A-I. Cross-Reference for the Forman Constitutive Constants.

Forman Symbols	LIFE2 Symbols		
YS	$\sigma_{ extsf{y}}$		
KIo	$\kappa_{ extsf{Io}}$		
KIc	K _{Ic}		
Ak	A _k		
Bk	B _k		

Forman Symbols	LIFE2 Symbols
С	С
n	ν
p	η
P	ψ
DKo	Δκο

Forman Symbols	LIFE2 Symbols		
Со	C _o		
đ	d		
DK1	$\Delta \kappa_1$		
α	$lpha_{ m F}$		

DISTRIBUTION:

Alcoa Technical Center (5) Aluminum Company of America

Attn: D. K. Ai

J. T. Huang

J. R. Jombock

M. Klingensmith

J. L. Prohaska

Alcoa Center, PA 15069

Alternative Sources of Energy Attn: L. Stoiaken Milaca, MN 56353

Amarillo College Attn: E. Gilmore Amarillo, TX 79100

American Wind Energy Association 1516 King Street Alexandria, VA 22314

Dr. Mike Anderson VAWT, Ltd. 1 St. Albans Hemel Hempstead Herts HP2 4TA United Kingdom

Dr. M. P. Ansell School of Material Science University of Bath Claverton Down Bath BA2 7AY Avon United Kingdom

Battelle-Pacific Northwest Laboratory Attn: L. Wendell P.O. Box 999 Richland, WA 99352

Bechtel Group, Inc. Attn: B. Lessley P.O. Box 3965 San Francisco, CA 94119 Dr. George Bergeles Dept. of Mechanical Engineering National Technical University 42, Patission Street Athens, GREECE

Canadian Standards Association Attn: T. Watson 178 Rexdale Blvd. Rexdale, Ontario, M9W 1R3 CANADA

Monique Carpentier Energy, Mines and Resources Renewable Energy Branch 460 O'Connor St. Ottawa, Ontario CANADA K1A OE4

Professor V. A. L. Chasteau School of Engineering University of Auckland Private Bag Auckland, NEW ZEALAND

Otto de Vries National Aerospace Laboratory Anthony Fokkerweg 2 Amsterdam 1017 THE NETHERLANDS

DOE/ALO/ETWMD Attn: G. P. Tennyson Albuquerque, NM 87115

DOE/ALO
Energy Technology Liaison Office
NGD
Attn: Capt. J. L. Hanson, USAF
Albuquerque, NM 87115

DOE Headquarters (5)
Wind/Oceans Technologies Division
Attn: L. J. Rogers
P. R. Goldman
1000 Independence Avenue
Washington, DC 20585

J. B. Dragt
Nederlands Energy Research
Foundation
(E.C.N.)
Physics Department
Westerduinweg 3 Petten (NH)
THE NETHERLANDS

Electric Power Research Institute Attn: E. Demeo 3412 Hillview Avenue Palo Alto, CA 94304

Alcir de Faro Orlando Pontificia Universidade Catolica-PUC/Rj Mechanical Engineering Department R. Marques de S. Vicente 225 Rio de Janeiro, BRAZIL

Fayette Manufacturing Corporation Attn: W. Thompson P.O. Box 1149 Tracy, CA 95378-1149

FloWind Corporation Attn: L. Schienbein 1183 Quarry Lane Pleasanton, CA 94566

A. D. Garrad Garrad Hasson 10 Northampton Square London EC1M 5PA UNITED KINGDOM

H. Gerardin Mechanical Engineering Department Faculty of Sciences & Engineering Universite Laval-Quebec, GlK 7P4 CANADA

Dr. I. J. Graham Southern University Dept. of Mechanical Engineering P.O. Box 9445 Baton Rouge, LA 70813-9445 R. T. Griffiths
University College of Swansea
Dept. of Mechanical Engineering
Singleton Park
Swansea, SA2 8PP
UNITED KINGDOM

Helion, Inc. Attn: J. Park, President Box 445 Brownsville, CA 95919

Indal Technologies, Inc. (2)
Attn: D. Malcolm
C. Wood
3570 Hawkestone Road
Mississauga, Ontario
CANADA L5C 2V8

Iowa State University Agricultural Engineering Attn: L. H. Soderholm Room 213 Ames, IA 50010

K. JacksonDynamic Design123 C StreetDavis, CA 95616

Kaiser Aluminum and Chemical Sales, Inc. Attn: A. A. Hagman 14200 Cottage Grove Avenue Dolton, IL 60419

Kaiser Aluminum and Chemical Sales, Inc. Attn: D. D. Doerr 6177 Sunol Blvd. P.O. Box 877 Pleasanton, CA 94566

R. E. Kelland
The College of Trades & Technology
P.O. Box 1693
Prince Philip Drive
St. John's, Newfoundland, AlC 5P7
CANADA

Kinetics Group, Inc. Attn: J. Sladky, Jr. P.O. Box 1071 Mercer Island, WA 98040

Olle Ljungstrom FFA, The Aeronautical Research Institute Box 11021 S-16111 Bromma, SWEDEN

Peter Lueck CENEMESA 14005 Cordoba Apartado 72 14080 Cordoba SPAIN

Robert Lynette R. Lynette & Assoc., Inc. 15042 NE 40th Street Suite 206 Redmond, WA 98052

Massachusetts Institute of
Technology
Attn: Professor N. D. Ham
W. L. Harris, Aero/Astro
Dept.
77 Massachusetts Avenue
Cambridge, MA 02139

H. S. Matsuda Composite Materials Laboratory Pioneering R&D Laboratories Toray Industries, Inc. Sonoyama, Otsu, Shiga, JAPAN 520

K. F. McAnulty
Energy Technology Support Unit
B156.7 Harwell Laboratory
Oxfordshire OX110RA
United Kingdom

Michigan State University Division of Engineering Research Attn: O. Krauss East Lansing, MI 48825 Napier College of Commerce and Technology Tutor Librarian, Technology Faculty Colinton Road Edinburgh, EH10 5DT ENGLAND

New Mexico Engineering
Research Institute (2)
Attn: G. G. Leigh
D. Morrison
Campus P.O. Box 25
Albuquerque, NM 87131

Ohio State University Aeronautical & Astronautical Dept. Attn: Professor G. Gregorek 2300 West Case Road Columbus, OH 43220

Oklahoma State University Mechanical Engineering Dept. Attn: D. K. McLaughlin Stillwater, OK 76074

Oregon State University
Mechanical Engineering Dept.
Attn: R. E. Wilson
Corvallis, OR 97331

Debby Oscar Massachusetts Institute of Technology 77 Massachusetts Ave. Room 1-303 Cambridge, MA 02139

Ion Paraschivoiu
Dept. of Mechanical Engineering
Ecole Polytecnique
CP 6079
Succursale A
Montreal, Quebec
CANADA H3C 3A7

Jacques Plante Shawinigan Consultants, Inc. 620 Dorchester Blvd. West Montreal, Quebec CANADA H3B 1N8 RANN, Inc. Attn: A. J. Eggers, Jr. 260 Sheridan Ave., Suite 414 Palo Alto, CA 94306

Mr. Bent Rasmussen Overgade 14 DK-7000 Fredericia DENMARK

Markus G. Real, President Alpha Real Ag Feldeggstrasse 89 CH 8008 Zurich Switzerland

The Resources Agency
Department of Water Resources
Energy Division
Attn: R. G. Ferreira
P.O. Box 388
Sacramento, CA 95802

Reynolds Metals Company Mill Products Division Attn: G. E. Lennox 6601 West Broad Street Richmond, VA 23261

R. G. Richards Atlantic Wind Test Site P.O. Box 189 Tignish P.E.I., COB 2BO CANADA

Riso National Laboratory
Attn: Troels Friis Pedersen
Helge Petersen
Peter Hauge Madsen
Postbox 49
DK-4000 Roskilde

DENMARK

Prof. Dr. U. J. Roose
Fachhochschule

Fachhochschule Kanzleistrasse 91-93 2390 Flensburg FEDERAL REPUBLIC OF GERMANY Dr. Ing. Hans Ruscheweyh Institut fur Leichbau Technische Hochschule Aachen Wullnerstrasse 7 FEDERAL REPUBLIC OF GERMANY

Beatrice de Saint Louvent Etablissement d'Etudes et de Recherches Meteorologigues 77 Rue de Serves 92106 Boulogne-Billancourt Cedex FRANCE

Gwen Schreiner Librarian National Atomic Museum Albuquerque, NM 87185

Arnan Seginer
Professor of Aerodynamics
Technion-Israel Institute of
Technology
Aeronautical Engineering Dept.
Haifa
ISRAEL

Mr. Farrell Smith Seiler, Editor Wind Energy News Service P.O. Box 4008 St. Johnsbury, VT 05819

David Sharpe
Dept. of Aeronautical Engineering
Queen Mary College
Mile End Road
London, El 4NS
UNITED KINGDOM

Kent Smith Instituto Technologico Costa Rica Apartado 159 Cartago COSTA RICA

Solar Energy Research Institute Attn: R. W. Thresher 1617 Cole Boulevard Golden, CO 80401 Bent Sorenson Roskilde University Center Energy Group, Bldg. 17.2 IMFUFA P.O. Box 260 DK-400 Roskilde DENMARK

Peter South ADECON 6535 Millcreek Dr., Unit 67 Mississauga, Ontario CANADA L5N 2M2

Southern California Edison Research & Development Dept. Room 497 Attn: R. L. Scheffler P.O. Box 800 Rosemead, CA 91770

G. Stacey
The University of Reading
Department of Engineering
Whiteknights, Reading, RG6 2AY
ENGLAND

Stanford University
Dept. of Aeronautics and
Astronautics Mechanical Engr.
Attn: Holt Ashley
Stanford, CA 94305

Dr. Derek Taylor Alternative Energy Group Walton Hall Open University Milton Keynes, MK7 6AA UNITED KINGDOM

Texas Tech University
Mechanical Engineering Dept.
Attn: J. W. Oler
P.O. Box 4289
Lubbock, TX 79409

US Wind Power
Attn: W. E. Holley
G. M. McNerney
Suite 3050
400 West Cummings Park
Woburn, MA 01803

USDA
Agricultural Research Service
Southwest Great Plains Research
Center
Attn: Dr. R. N. Clark
Bushland, TX 79012

United Engineers and Constructors, Inc. Attn: A. J. Karalis P.O. Box 8223 Philadelphia, PA 19101

Universal Data Systems Attn: C. W. Dodd 5000 Bradford Drive Huntsville, AL 35805

University of Massachusetts
Mechanical and Aerospace
Engineering Dept.
Attn: Dr. D. E. Cromack
Amherst, MA 01003

University of Oklahoma Aero Engineering Department Attn: K. Bergey Norman, OK 73069

University of Sherbrooke
Faculty of Applied Science
Attn: A. Laneville
P. Vittecoq
Sherbrooke, Quebec, J1K 2R1
CANADA

W. A. Vachon W. A. Vachon & Associates P.O. Box 149 Manchester, MA 01944

Dirk Vandenberghe State Univ. of Ghent St. Pietersniewstraat 41 9000 Ghent BELGIUM

F. J. Verheij	400	R. C. Maydew
Dept. of Fluid Mechanics	1520	L. W. Davison
TNO	1522	R. C. Reuter, Jr.
P.O Box 342	1522	D. W. Lobitz
7300 AH Apeldoorn	1522	E. D. Reedy
Laan van Westenenk 501	1523	J. H. Biffle
Apeldoorn	1524	L. W. Davison, Actng.
NETHERLANDS	1524	C. R. Dohrmann
··	1550	C. W. Peterson
Washington & Lee University	1552	J. H. Strickland
Attn: Dr. R. E. Akins	1556	G. F. Homicz
P.O. Box 735	3141	
Lexington, VA 24450	3151	W. I. Klein (3)
Lexington, VA 24450		C. L. Ward (8)
Washington State University	3134 1	For DOE/OSTI (Unlimited
Dept. of Electrical Engineering		Release)
Attn: F. K. Bechtel	3160	J. E. Mitchell
	3100	J. B. MICCHEII
Pullman, WA 99163		•
West Texas State University	3161	P. S. Wilson
Government Depository Library	6000	D. L. Hartley
Number 613	6200	V. L. Dugan
Canyon, TX 79015	6220	D. G. Schueler
Canyon, IX 79013	6225	
West Texas State University	6225	
	6225	
Department of Physics	6225	9
Attn: V. Nelson	6225	•
P.O. Box 248		M. E. Ralph D. C. Reda
Canyon, TX 79016	6225	· · · · · · · · · · · · · · · · · · ·
	6225	<u> </u>
West Virginia University	6225	
Dept. of Aero Engineering	6225	<u>-</u>
Attn: R. Walters	6225	•
1062 Kountz Avenue	6225	
Morgantown, WV 26505	7472	
	7544	
Wichita State University	7544	T. G. Carne
Aero Engineering Department (2)	7544	J. Lauffer
Attn: M. Snyder	8524	J. R. Wackerly
W. Wentz		
Wichita, KS 67208		
Wind Power Digest		
Attn: Michael Evans		
P.O. Box 700		
Bascom, OH 44809		

8232-2/069541

0000001 -

0000001 -

8232-2/069541

0000001 -

Org.	Bldg.	Name	Rec'd by •Or	rg.	Bldg.	Name	Rec'd b
34							
<u> </u>							
-							
		:					
					-		

