

The Lapack for Clusters (LFC) Project

Presented by

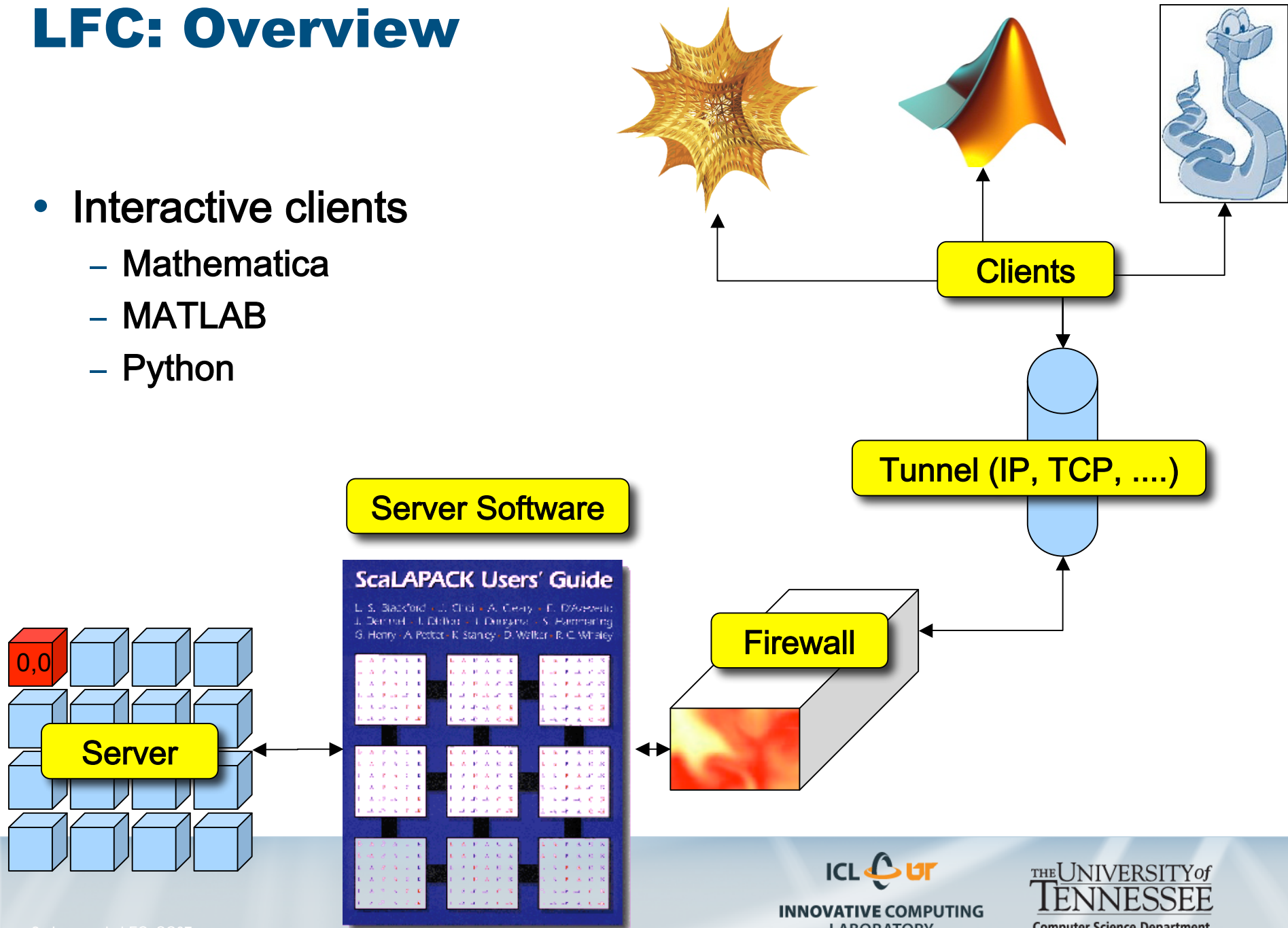
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LFC: Overview

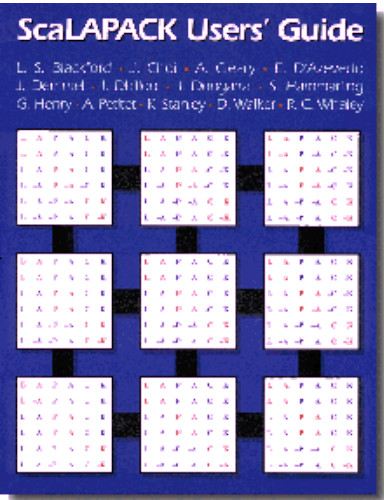
- Interactive clients
 - Mathematica
 - MATLAB
 - Python



LFC: Behind the scenes



```
x = lfc.gesv(A, b)
```

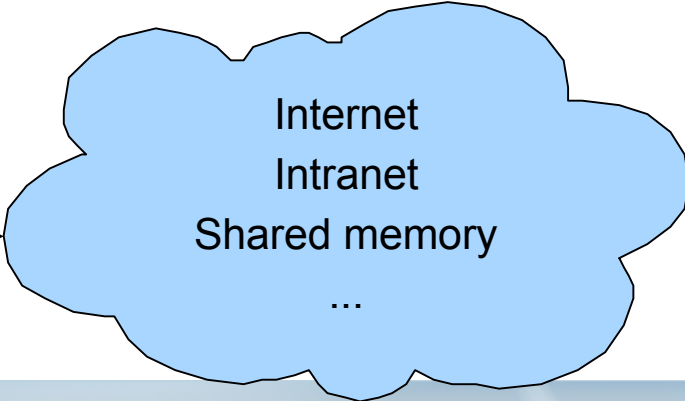


Batch mode bypass

```
x = b.copy()  
command('pdgesv', A.id, x.id)
```

```
call pdgesv(A, x)
```

```
send(c_sckt, buf)
```

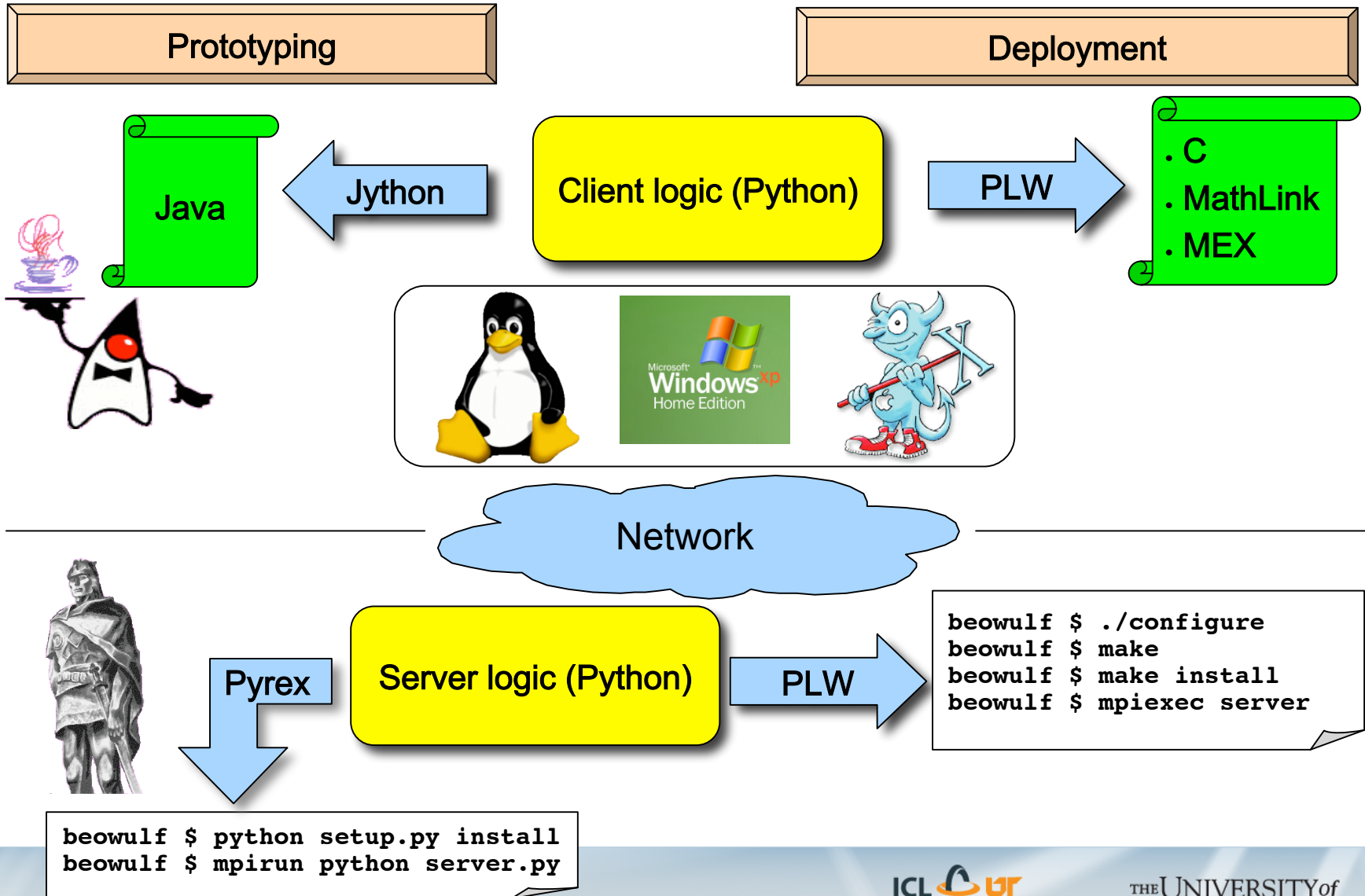


```
recv(s_sckt, buf)
```

LFC: Current functionality

- Linear systems (via factorizations)
 - Cholesky: $A = UTU$ $A = LLT$
 - Gaussian: $PA = LU$
 - Least Squares: $A = QR$
- Singular- and eigen-value problems
 - $A = U\Sigma V^T$ (thin SVD)
 - $AV = V\Lambda = AHV$ (symmetric AEP)
 - $AV = V\Lambda$ (non-symmetric AEP)
- Norms, condition-number estimates
- Precision, data types
 - Single, double
 - Real, complex
 - Mixed precision (by upcasting)
- User data routines
 - Loading/Saving
 - MPI I/O
 - ...
- Generating
 - Plug-ins
 - Moving
- More to come...
 - Now working on sparse matrices support

LFC: Design and implementation



LFC: Implemented MATLAB functionality

Name	Single	Double	S-Complex	D-Complex	Description
chol	√	√	√	√	Cholesky factorization: LL^T , U^TU
lu	√	√	√	√	LU factorization: $PA=LU$
qr	√	√	-1	-1	QR factorization: $A = QR$
qrp	-1	-1	-1	-1	QR factorization+pivoting: $PA=QR$
Svd	√	√	√	√	Singular-value decomposition: $A=U\Sigma V^T$
Eig	-1	-1	-1	-1	Eigenvalue problem: $AX=X\Lambda$
Syev	√	√	n/a	n/a	Symmetric eigenvalue problem
Heev	n/a	n/a	√	√	Hermitian eigenvalue problem
Diag	√	√	√	√	Diagonal matrix/vector
Trans	√	√	√	√	Matrix/vector transpose
Herm	n/a	n/a	√	√	Matrix/vector hermitian transpose
Norm	√	√	√	√	Matrix/vector norm
Cond	√	√	√	√	Condition number estimate
Inv	0	0	0	0	Explicit matrix inverse

Sample LFC code: Linear system solve

- MATLAB with LFC (parallel):

```
n = lfc(1000);  
nrhs = 1;  
A = rand(n);  
b = rand(n, 1);  
x = A \ b;  
r = A*x - b;  
norm(r, 'fro')
```

- MATLAB – no LFC (sequential):

```
n = 1000;  
nrhs = 1;  
A = rand(n);  
b = rand(n, 1);  
x = A \ b;  
r = A*x - b;  
norm(r, 'fro')
```

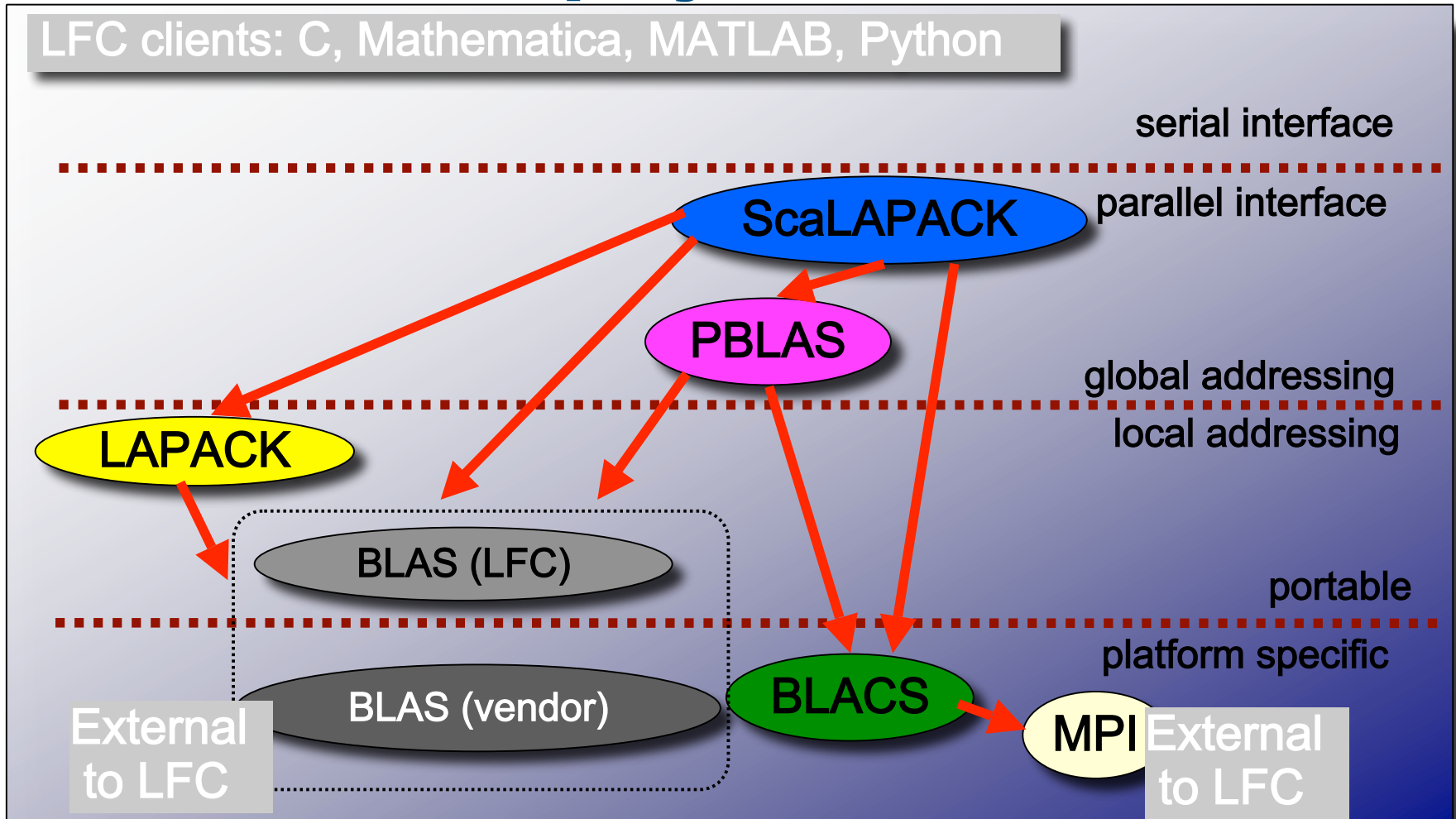
- Python with LFC (parallel):

```
n = 1000  
nrhs = 1  
A = lfc.rand(n)  
b = lfc.rand(n, 1)  
x = lfc.solve(A, b)  
r = A*x - b  
print r.norm('F')
```

LFC's C interface: Sequential calls, parallel execution

- In-memory routines
 - `LFC_gels()`
 - `LFC_gesv()`
 - `LFC_posv()`
- Limitations
 - Data must fit on caller
- Cluster state functions
 - `LFC_hosts_create()`
 - `LFC_hosts_free()`
 - `LFC_get_available_CPU()`
 - `LFC_get_free_memory()`
- Disk-based routines
 - `LFC_gels_file_all()`
 - `LFC_gesv_file_all()`
 - `LFC_posv_file_all()`
- Limitations
 - Must pay I/O cost each time

LFC's ease of deployment



- Only one file to download
- Just type: `./configure && make && make install`

Software technology used by LFC

- Client

- Python
 - Sockets
- MATLAB
 - Embedded Java
 - Jython
 - Reuse of Python code
- C/C++
 - Code:
 - fork()
 - execvp()
 - Shell (implicit)
 - mpirun
 - mpiexec

- Server

- Libraries
 - MPI
 - BLAS
 - BLACS
 - LAPACK
 - ScaLAPACK
- Languages
 - Python
 - Pyrex (C wrappers)
 - PLW
 - Python compiler
 - Translation to C

Contact

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