## Methods for Modeling Decisions under Uncertainty for Integrated Assessment Models

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## Introduction

Most current IAMs are structured for deterministic analyses



### But...

- The climate change policy problem is *inherently* stochastic. For example:
  - uncertainty in rate of clean capital technological improvement
  - uncertainty in climate system response to temperature change
- We can learn about these uncertainties over time and revise decisions
- We lack good stochastic climate policy (IAM) models due to computational limitations

# **Overview:** Sequential decision making under uncertainty (1 of 2)

**Decision:** µ = GHG (or carbon) emission control rate **Uncertainty:** High/Med/Low = "clean" energy technology improvement rate **State Variable**: "holds" information about the past needed to make a new decision





<u>Objective of the Stochastic Problem</u> choose  $\mu(t)$  to maximize **Bellman Value** (Total Reward) in each time period:

$$V_{t}^{*}(S_{t}) = \max_{\mu(t)} (C_{t}(S_{t}, \mu_{t}) + E[V_{t+1}(S_{t+1})|S_{t}, \mu_{t}])$$
  
Current Expected Future Reward Reward

# **Motivation:** DICE stochastic dynamic program results and "curse of dimensionality"

## The "curse of dimensionality"

- limited decisions and stages (1 decision made at 100/100/150 years)
- coarse state and action resolutions
- long run times
  - <u>3-stage DICE SDP</u> took ~12 days to solve on a new 64-bit desktop PC (2010)

Climate policy decisions need to be made at <u>shorter intervals</u> and at <u>finer resolutions</u>.

A much simpler model than the one we need already takes far too long to run!

## Stochastic Dynamic Programming (SDP) v. Approximate Dynamic Programming (ADP)

Two Components to ADP: Sampling and Value Function Approximation



## New DICE ADP Model (1 of 2)

- Working Paper here: <u>http://esd.mit.edu/WPS/2011/esd-wp-2011-12.pdf</u>
- Implementation: ADP for 7-period stochastic DICE (50-year steps)
  - objective: maximize  $(C_t(S_t, \mu_t) + E[V_{t+1}(S_{t+1})|S_t, \mu_t]) \leftarrow \text{"Bellman Value"}$
  - single decision:  $\mu(t)$  Current Utility
  - single uncertainty (with and without path-dependency): abatement cost

**Expected Future Utility** 

- state variable: K(t)—capital stock level, TE(t)—current temperature
- Solves in ~1-3 mins!
- New Model Validation



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## New DICE ADP Model (2 of 2)

#### Results of Numerical Experiments with DICE ADP Model

Uncertainty (REF) v. path-dependent uncertainty (PD) in abatement costs



## **Conclusions:** ADP Advantages and Challenges

### Main Advantages

- Overcomes the "curse of dimensionality" (ability to model several decisions, types and numbers of uncertainties, and time-periods in a fraction of time for a comparable SDP)
- Explicitly represents uncertainty with learning/adaptation
- Method of forward sampling (through uncertainties and decisions) lends to more easily representing sequential path-dependent decisions over other comparable approaches.

#### Main Challenges

- Falls under the general class of heuristic methods for global optimization
- Value function approximation methods are sensitive to complexity and type of decision problem
- Final solution can be sensitive to initial value function approximation. More research needs to be done studying the tradeoff between "explore v. exploit" methods.

## **Upcoming Related Work**

#### ADP formulation of DICE extensions

(Webster & Santen-MIT, Popp-Syracuse/NBER, and Fisher-Vanden-PSU)

- ENTICE/ENTICE-BR<sup>4,5</sup> modifies DICE to include endogenous technological change and investments in clean energy R&D
- We will be modeling these additional R&D investment decisions, and
- including uncertainties about breakthrough technological change activity
  & climate sensitivity
- MIT Integrated Global System Modeling Framework (MIT IGSM) ADP (Jennifer Morris, MIT ESD PhD Candidate, Dissertation Topic)

<sup>5</sup> Popp, D. (2006). "ENTICE-BR: Backstop Technology in the ENTICE Model of Climate Change." Energy Economics 28 (2): 188-222.

<sup>&</sup>lt;sup>4</sup> Popp, D. (2004). "ENTICE: Endogenous Technological Change in the DICE Model of Global Warming." *Journal of Environmental Economics and Management 48(1): 742-768.* 





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## Webster Research Group Sample Doctoral Students' Research Projects

**Research Question:** Under a long-term climate stabilization target, how do uncertain technology costs, and the ability to learn and adapt decisions over time, affect near-term emission mitigation decisions? - Jennifer Morris, MIT ESD

- Integrated Assessment Models (IAMs) couple human and climate systems and are valuable decision support tools
- However, most IAM analyses are deterministic
- How can we capture technological uncertainty and ability to revise decisions over time in an IAM?
- **Curse of Dimensionality** limits application of Dynamic Programming
- Approximate Dynamic Programming to the rescue!!!
- ADP IAM can provide important insight into near-term mitigation strategies and climate policy design



MIT Integrated Global System Modeling Framework (IGSM)

#### Environmental and R&D policy portfolio optimization under technology change uncertainty: the case of the U.S. electricity sector Nidhi R. Santen, ESD Ph.D. Candidate

#### **Research Question:**

"What is the optimal balance between near-term regulatory policy and clean electricity technology R&D expenditures, given the uncertainty in returns to R&D?"

#### **Objectives:**

- Develop an integrated policy and long-range generation capacity planning modeling framework to evaluate the impact of uncertain electricity technology improvements on optimal policy planning.
- Evaluate the trade-offs between "development-focused" and "adoption-focused" climate and technology policies, considering uncertainty (& breakthroughs) in R&D returns.

#### Approach:

- Couple a policy-induced technology change model with a national-level electricity generation capacity planning model. Use patent citation data to empirically calibrate relationships between R&D and generation technology costs.
- Use stochastic optimization techniques to model a range of sequential environmental and R&D policy decisions under uncertain (endogenous) R&D returns, and study optimal nearterm policies. Study associated electricity generation capacity and carbon-dioxide emission evolutions.
  - Use approximate dynamic programming (ADP) to capture the large number of decisions and uncertainties at each stage, and the long time-horizon of the policy and generation capacity planning processes (while keeping the problem tractable).





# Operating Constraints in Stochastic Electricity Planning By Bryan Palmintier

Operational Flexibility Key for Renewables and Emissions Assessment

New methods for

ops + planning:

- Efficient Long-term Unit Commitment
- Multi-Fidelity Approximate
   Dynamic
   Programming



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