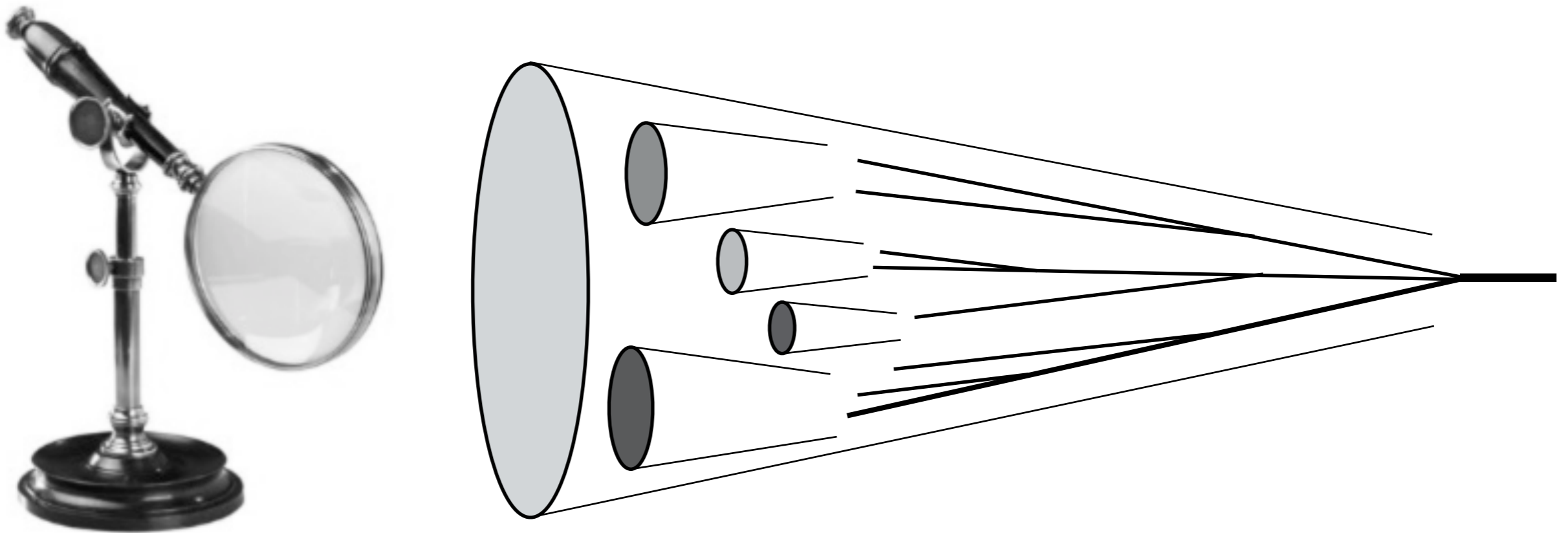


# Jet substructure via angular correlations



**Martin Jankowiak**

**Stanford/SLAC**

based on 1104.1646, 1201.2688 (with Andrew Larkoski)

May 17th 2012

# Outline

- introduction: why jet substructure?
- the unclustering paradigm
- angular correlation function
- top-tagging
- underlying event

# Jet substructure

- the excellent resolution of the ATLAS & CMS detectors means that we can “peer inside” jets and measure how energy is distributed within jets

## What is this good for?

- as a probe of QCD
- event discrimination

# Jet substructure

## as a probe of QCD

- make jet substructure measurements in data and compare to perturbative QCD calculations
- use to tune Monte Carlo event generators

# Jet substructure

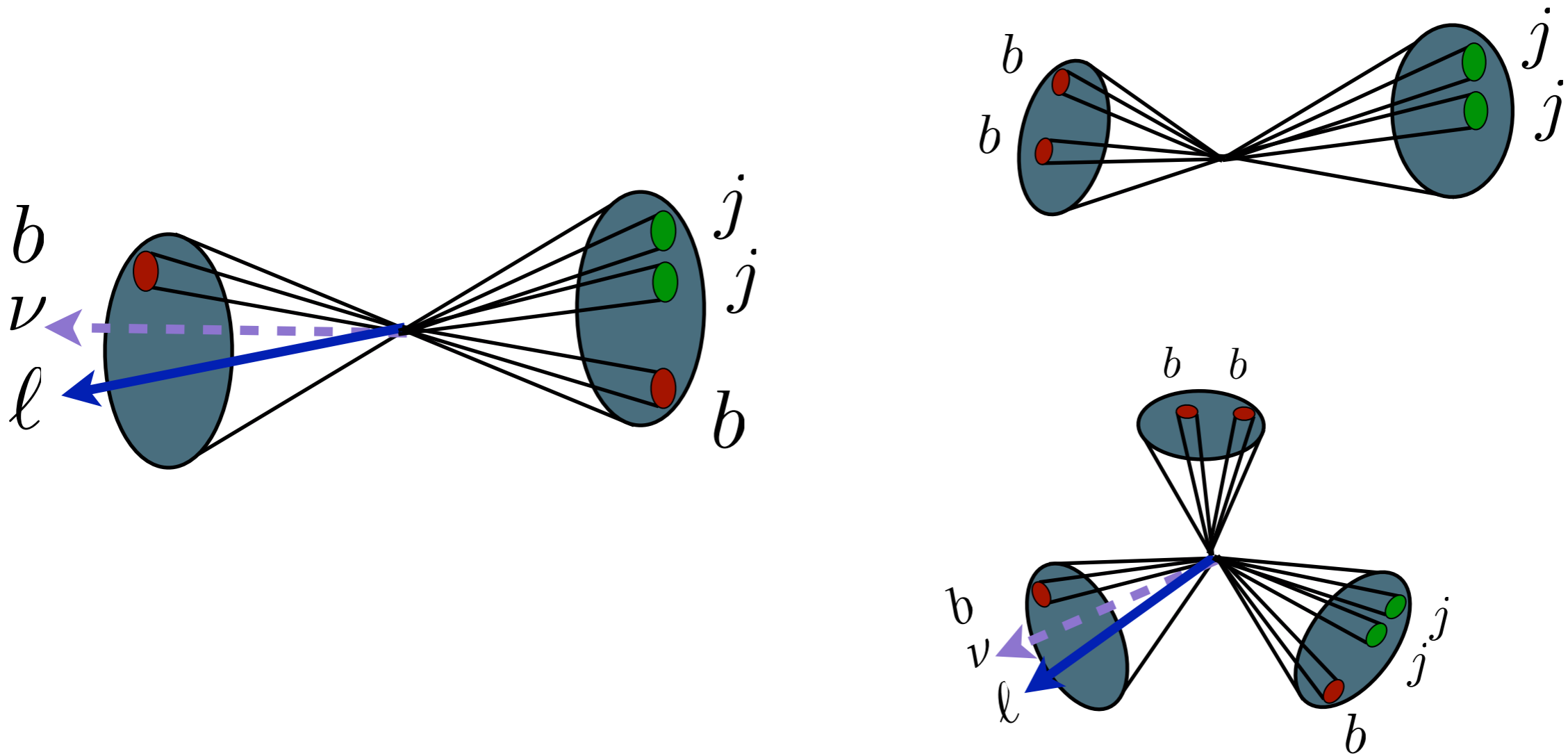
## for event discrimination

- the LHC inverse problem:
  - how do we connect what we measure (jets) to the hard scattering ?
- use the characteristic energy distribution of signal jets (e.g. top jets) to discriminate against background jets (e.g. QCD jets initiated by light partons)
- especially relevant for boosted objects

# Jet substructure

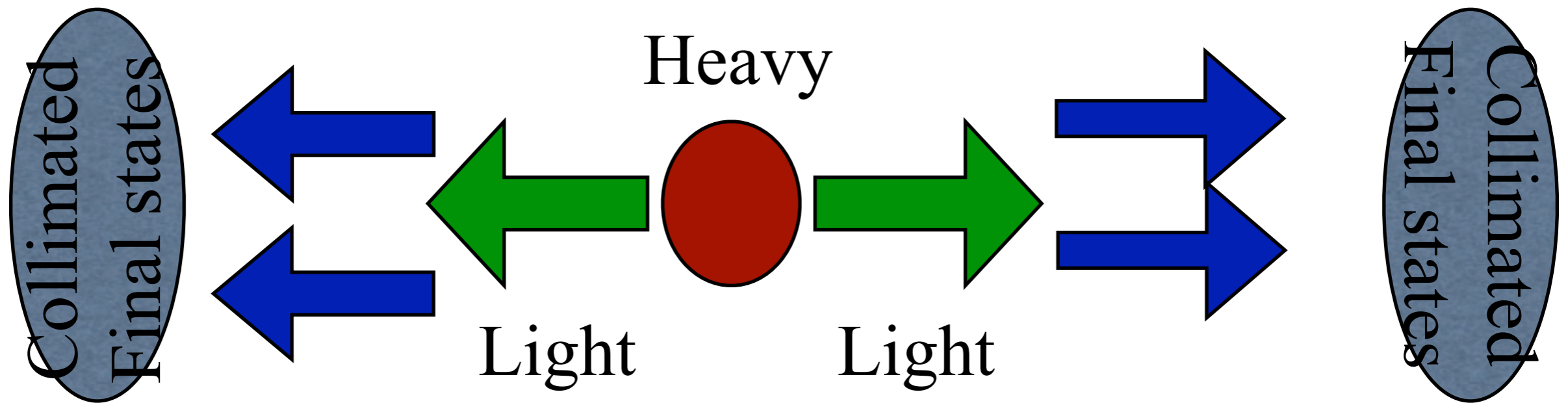
for event discrimination

want to separate complex signal topologies  
from QCD backgrounds



# Jet substructure for boosted objects

The LHC has access to much higher energy scales:  
cascade decays can lead to collimated final states



# Jet substructure

## for boosted objects

- requires rethinking cuts (e.g. isolation)
- a way of classifying complicated signatures
- reduces combinatoric backgrounds
- can be a unifying framework for peculiar signatures that were falling between cracks

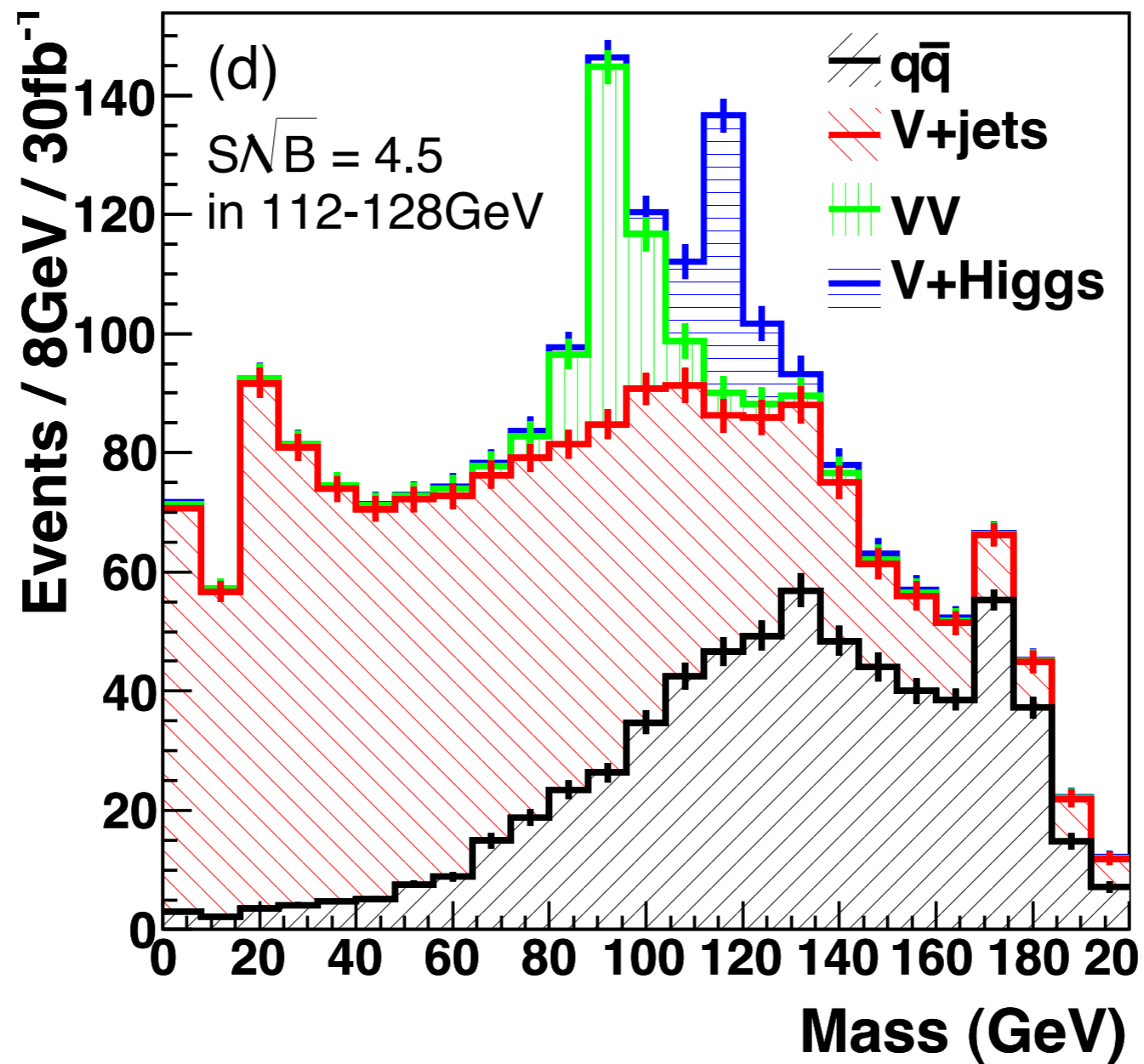


# Jet substructure

## for boosted higgs

- for  $p_T \gtrsim m_H$  the decay products of the higgs will typically be close together and reconstructed as a single jet
- about 5% of the cross-section for VH has  $p_T > 200$  GeV
- backgrounds (V+jets, VV, top pairs) fall faster with  $p_T$  than the signal
- can pay to go to the boosted regime if substructure techniques can reduce backgrounds/combinatorics
- discovery for a light higgs with  $\sim 30$  inverse fb

# Jet substructure for boosted higgs

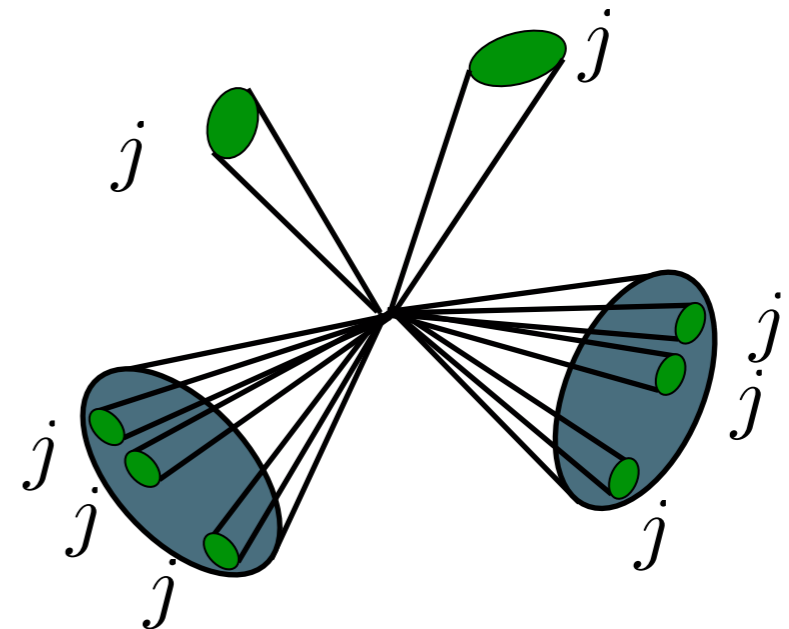
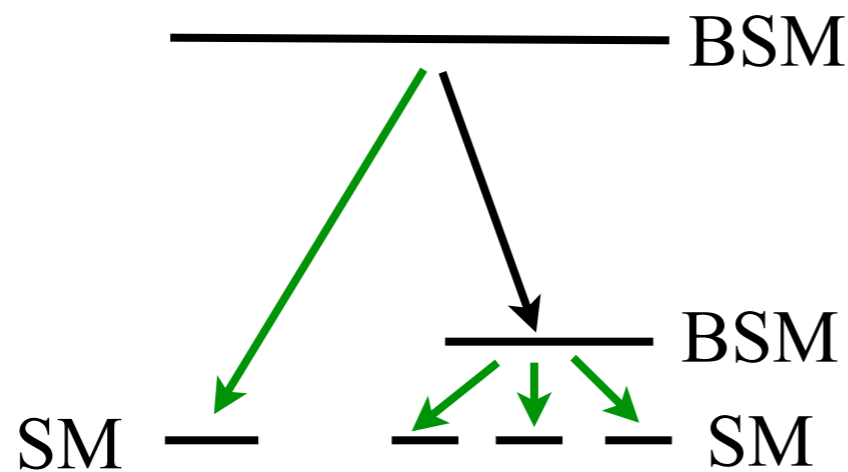


Jon Butterworth, Adam Davison, Mathieu Rubin, Gavin Salam arXiv/hep-ph:0802.2470

# Jet substructure for boosted bsm physics

R-Parity Violation  $\tilde{q} \rightarrow \tilde{\chi}^0 q$  Butterworth et al. 0906.0728

$$W_{\text{RPV}} = U^c D^c D^c \quad \Rightarrow \quad \tilde{\chi}^0 \rightarrow 3q$$



No significant MET, can reconstruct everything

# Sequential jet clustering algorithms

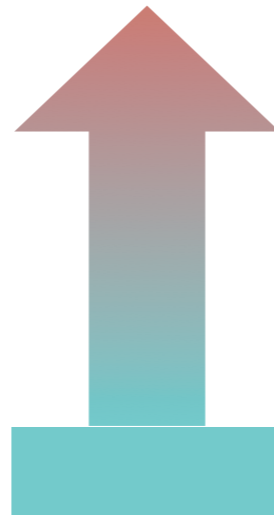
- need a way to define jets from the four-momenta measured in the detector
- do this by sequentially combining four-momenta

# Sequential jet clustering algorithms

find smallest  
 $d_{ij}$  or  $d_i$



Combine  $i$  &



Call  $i$  a jet

$p = 0 \Rightarrow$  Cambridge-Aachen

$p = 1 \Rightarrow$  kT

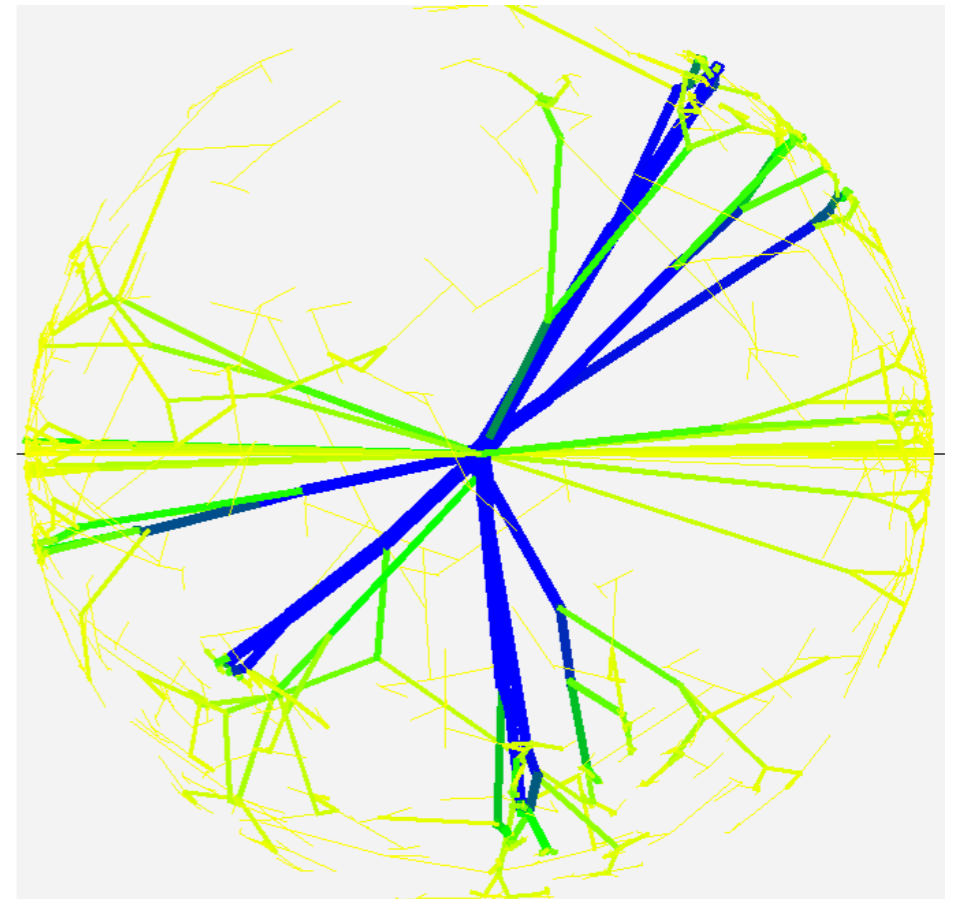
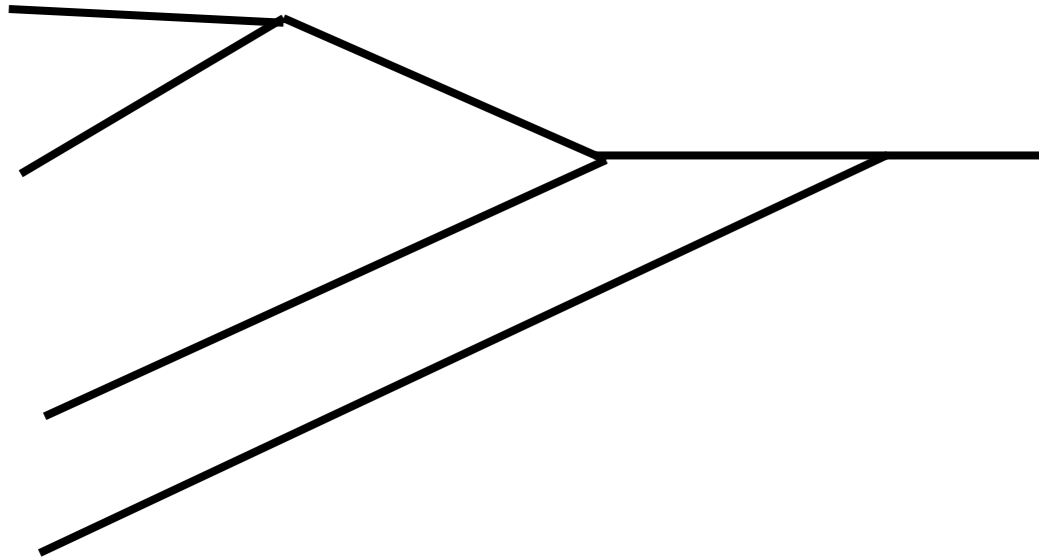
$p = -1 \Rightarrow$  anti-kT

$$d_{ij} = \min(p_{ti}^{2p}, p_{tj}^{2p}) \frac{\Delta R_{ij}^2}{R^2}$$

$$d_{iB} = p_{ti}^{2p}$$

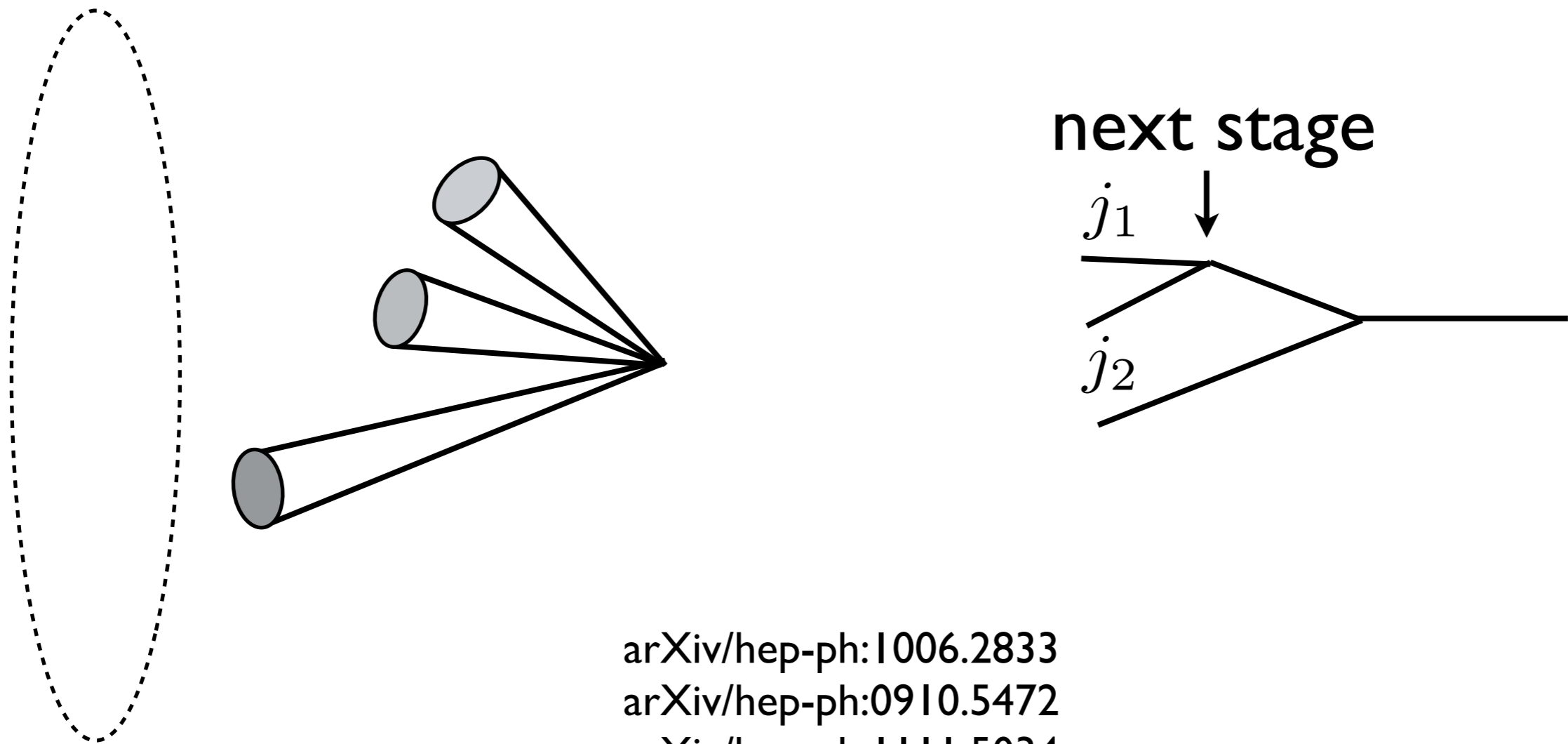
# Unclustering

- sequential jet clustering algorithms give us more than a list of jet four-momenta
- they also give us a *clustering tree*: lots of information inside
- **main idea**: use the clustering tree to identify and characterize substructure in jets



# HEPTopTagger

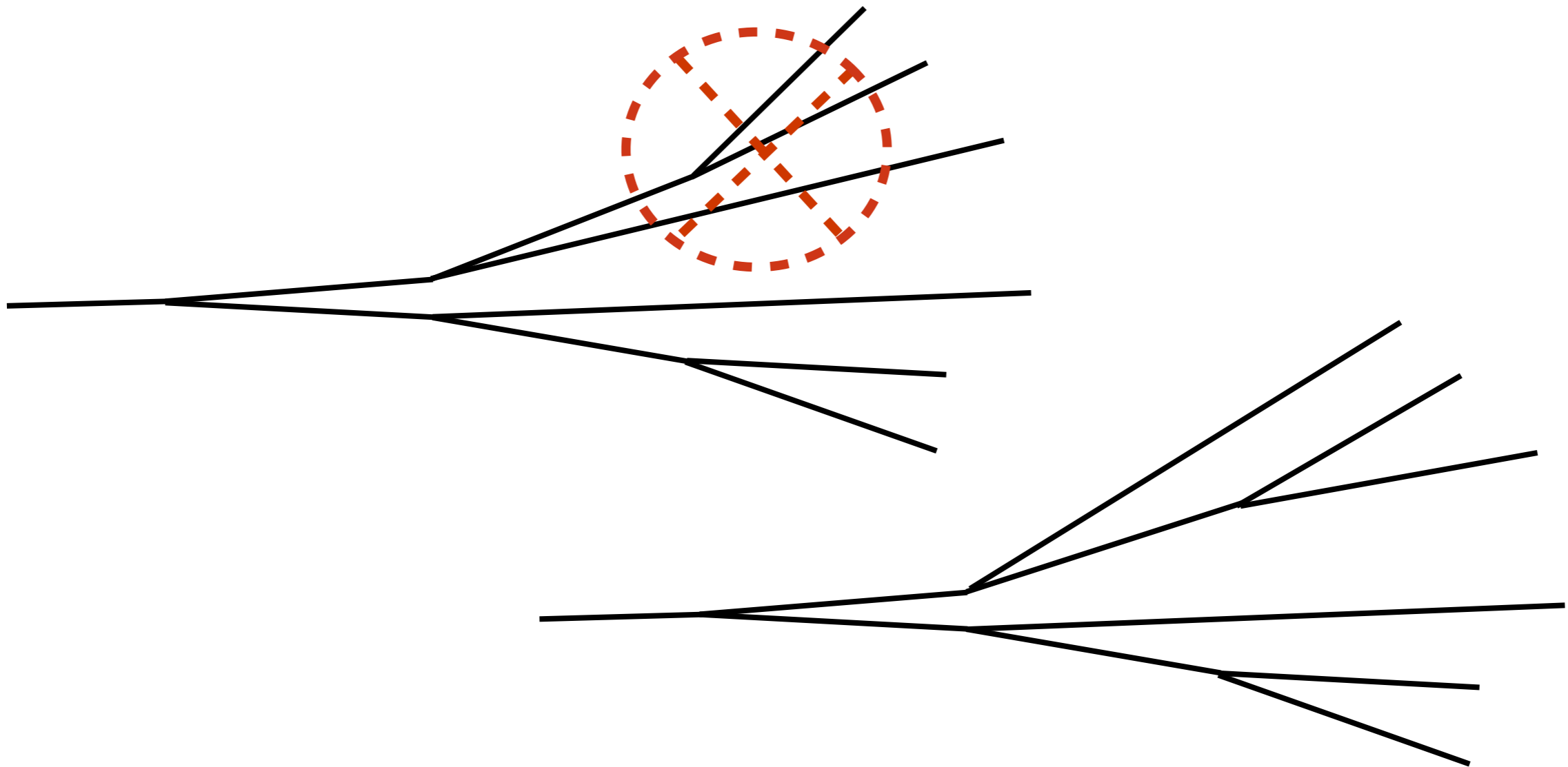
2. Break each fat jet into hard subjets using the following mass-drop criterion. Undo the last stage of clustering to yield two subjets  $j_1$  and  $j_2$  (with  $m_{j_1} > m_{j_2}$ ), keeping both  $j_1$  and  $j_2$  if  $m_{j_1} < 0.8m_j$  and otherwise dropping  $j_2$ . Repeat this procedure recursively, stopping when the  $m_{j_i}$  drop below 30 GeV.



arXiv/hep-ph:1006.2833  
arXiv/hep-ph:0910.5472  
arXiv/hep-ph:1111.5034

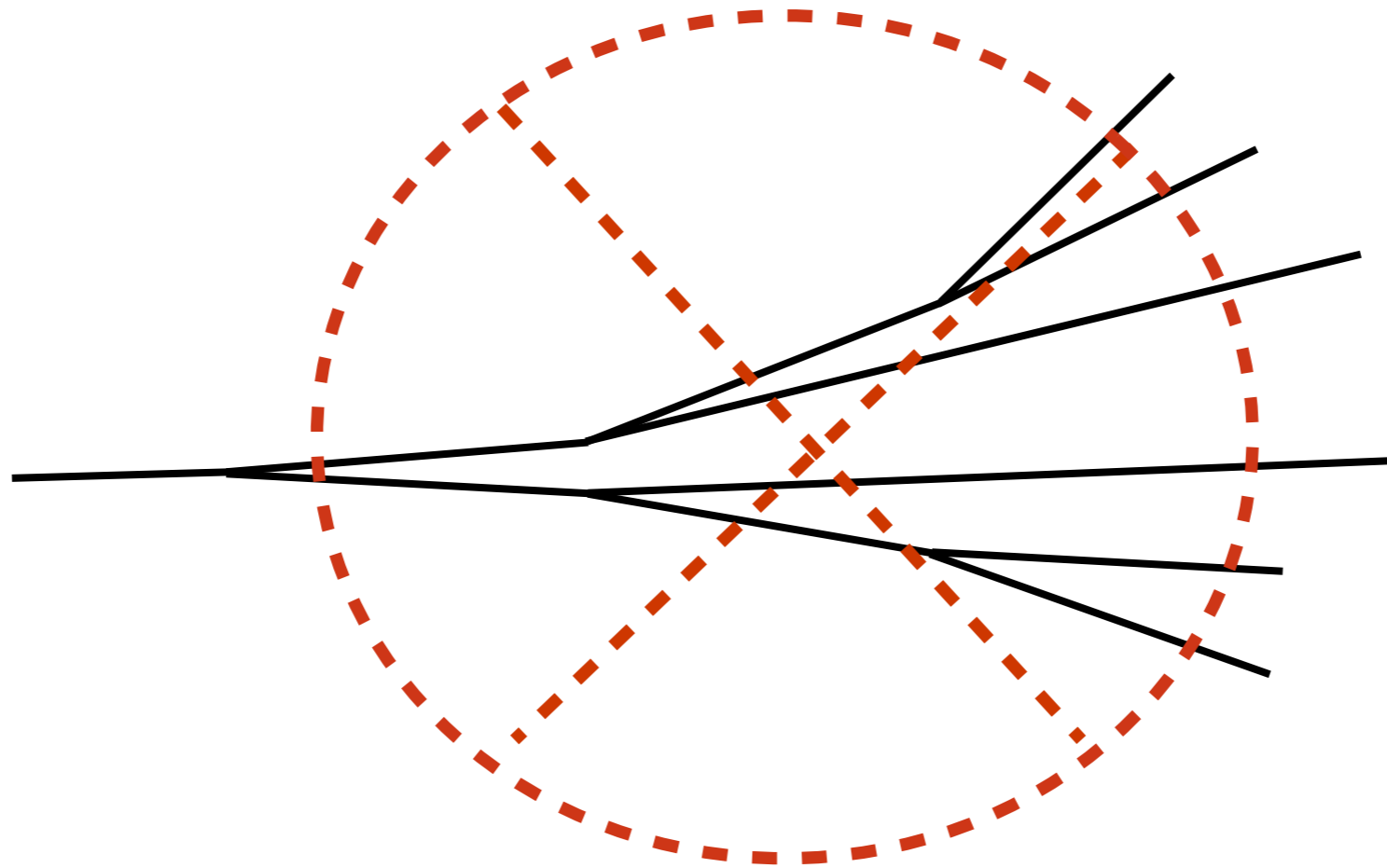
# Unclustering

we might worry that we've reconstructed the wrong parton shower history





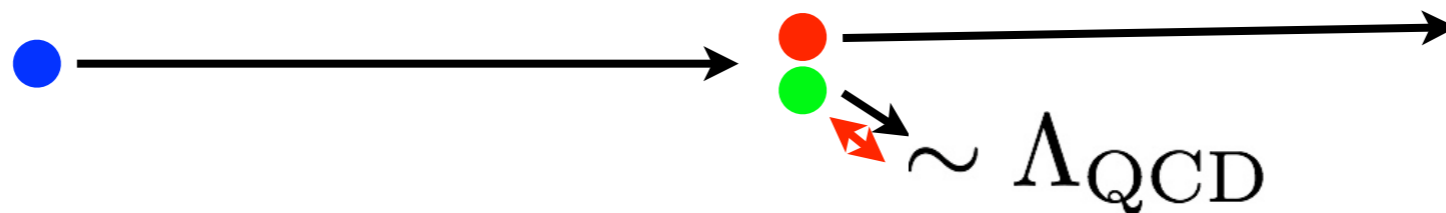
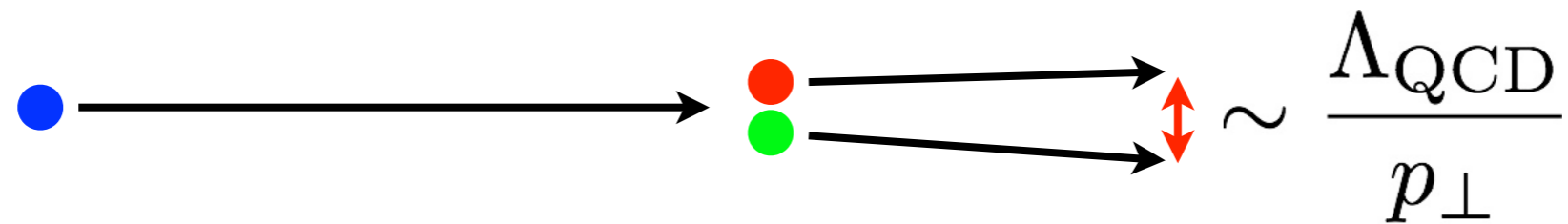
# angular correlation function



“Jet Substructure Without Trees”

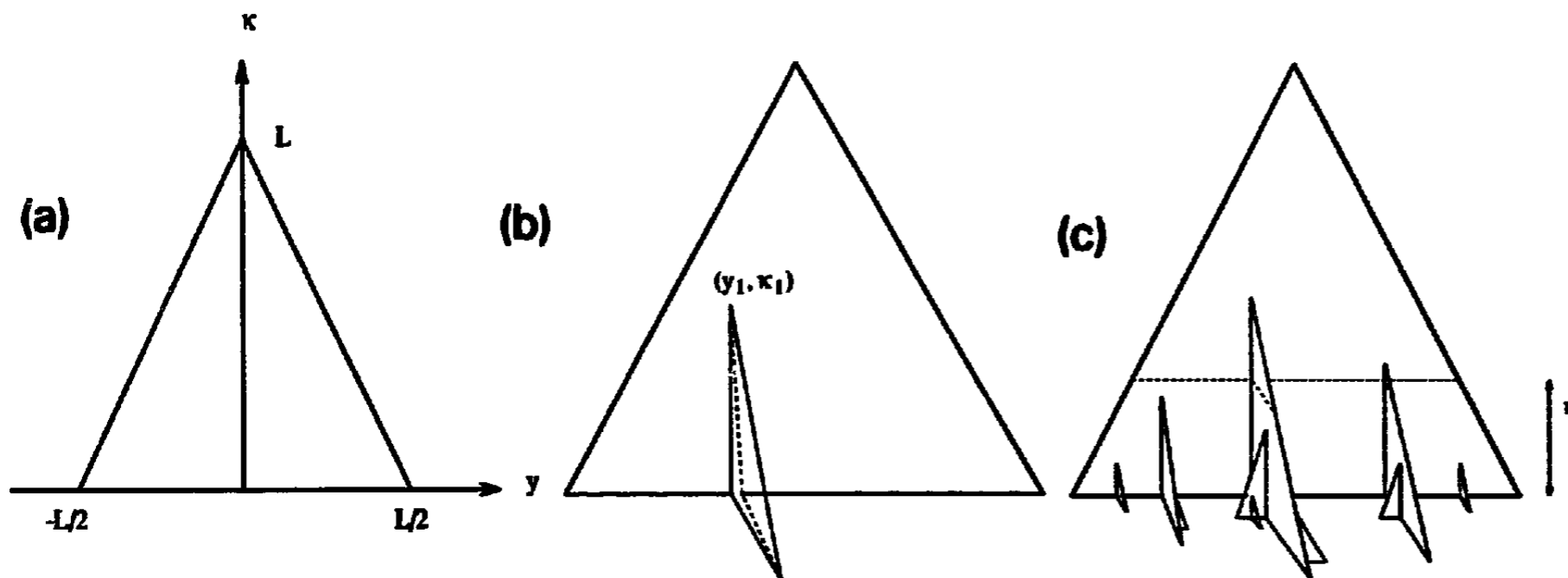
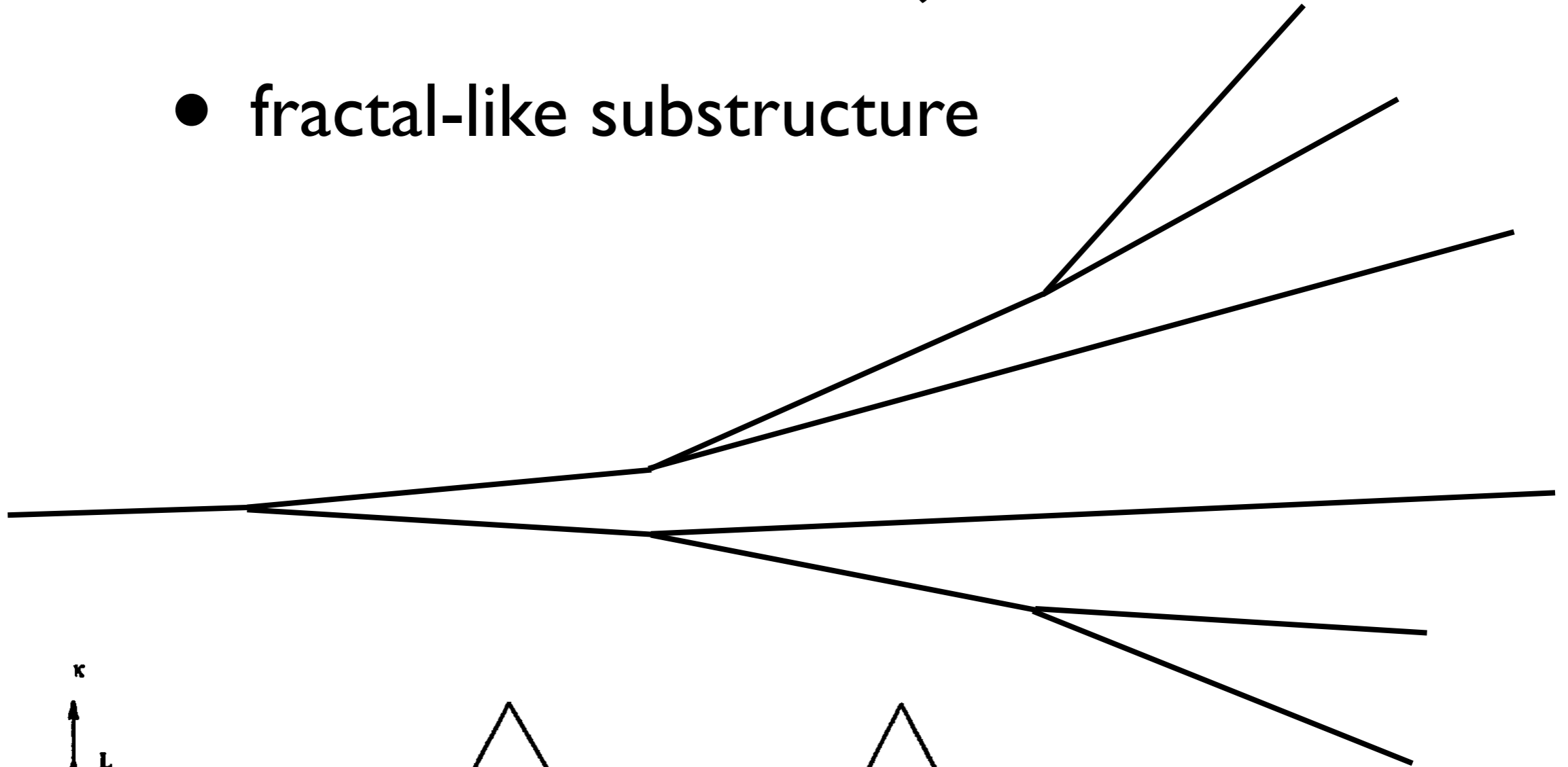
# What are QCD jets like?

- QCD is an approximately scale-invariant non-Abelian gauge theory at high energies
- consequences:
  - soft & collinear singularities



# What are QCD jets like?

- fractal-like substructure

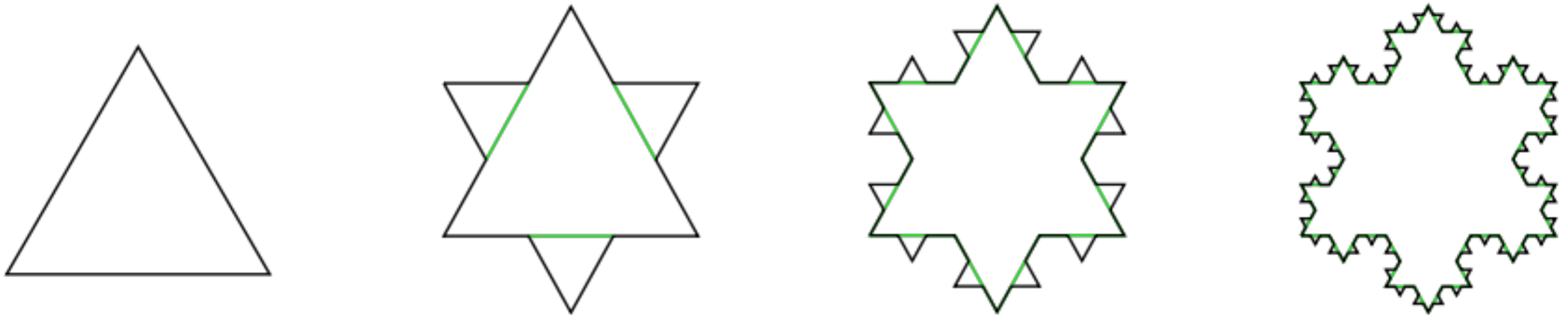


# Defining an Observable

- goal: define an observable that can distinguish between approximately scale invariant objects and objects that have an intrinsic, high energy scale
- observable will be a function that encodes the scaling behavior of the system
- the argument of the function is a resolution parameter

# Defining an Observable

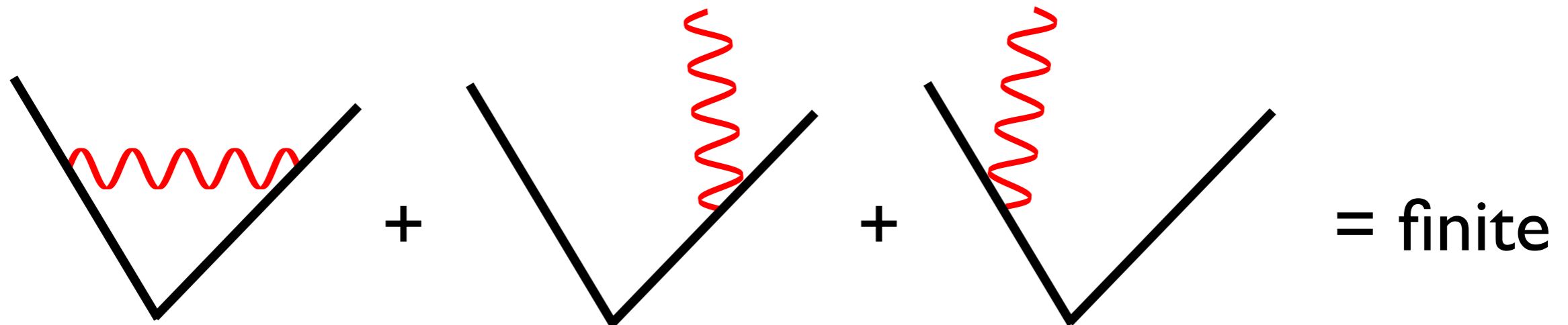
- define an angular correlation function between jet constituents



increasing resolution  $\longrightarrow$

# Defining an Observable

- requirements from theory:
  - infrared and collinear safety
  - want to compute in pert. theory



# Defining an Observable

- correlation function should be z-boost invariant
- jet mass is the prototypical 2-particle ‘correlation function’

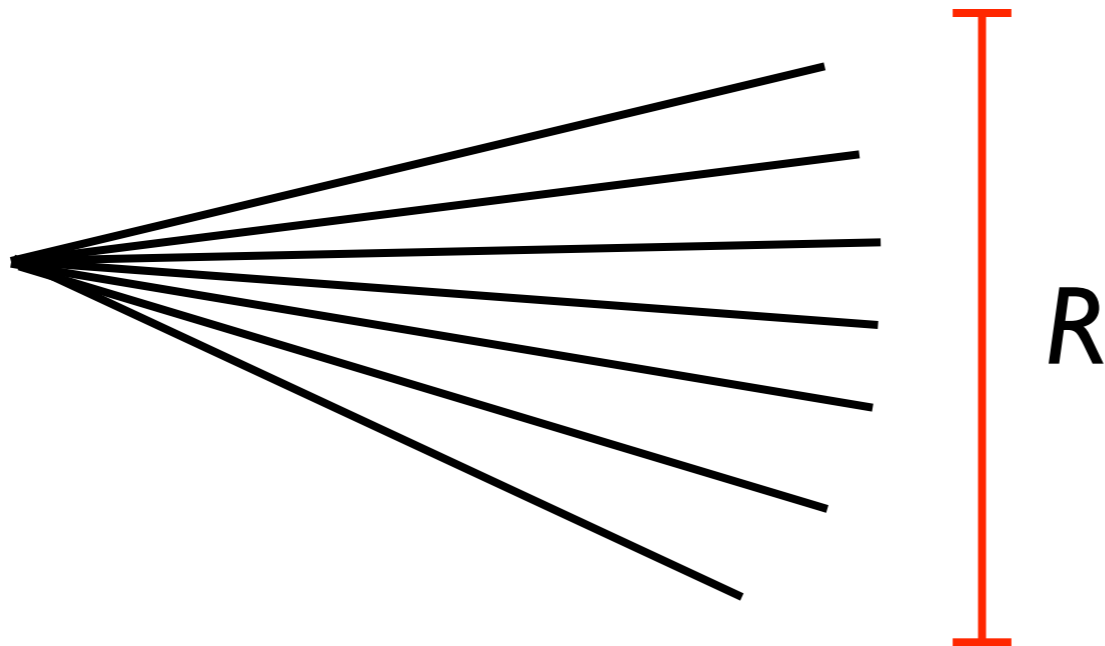
$$\mathcal{G}(R) \equiv \sum_{i \neq j} p_{\perp i} p_{\perp j} \Delta R_{ij}^2 \Theta[R - \Delta R_{ij}]$$

$$\Delta R_{ij}^2 = (\eta_i - \eta_j)^2 + (\phi_i - \phi_j)^2$$

- angular correlation function (ACF)

# Angular Correlation Function

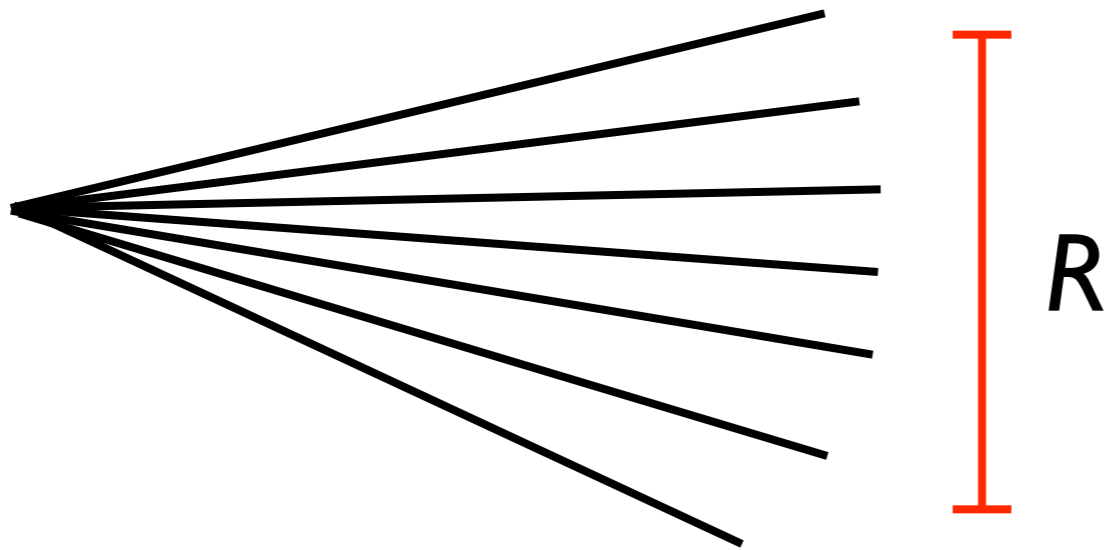
- expectations
  - ACF in QCD  $\sim R^2$





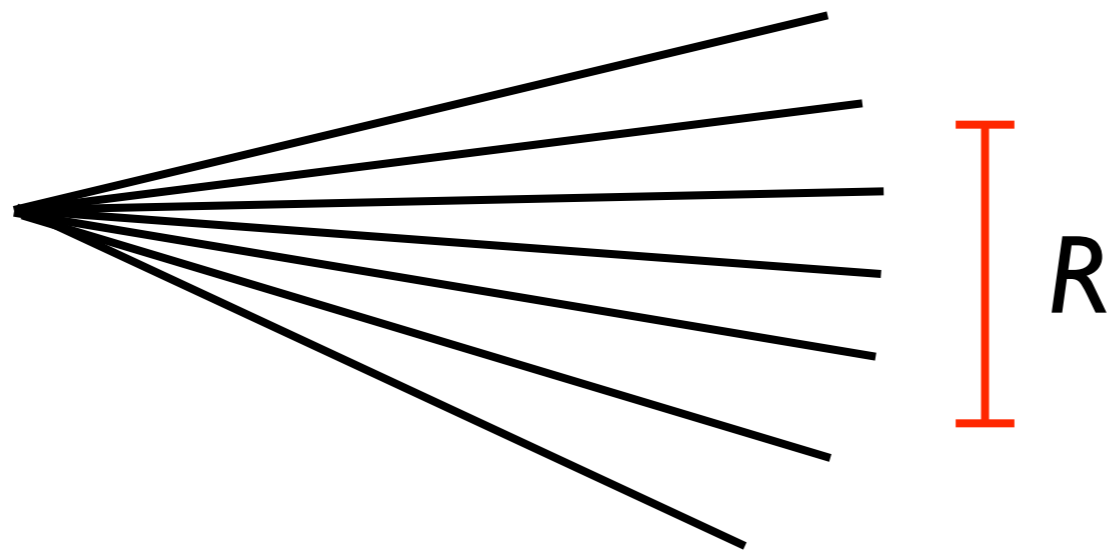
# Angular Correlation Function

- expectations
  - ACF in QCD  $\sim R^2$



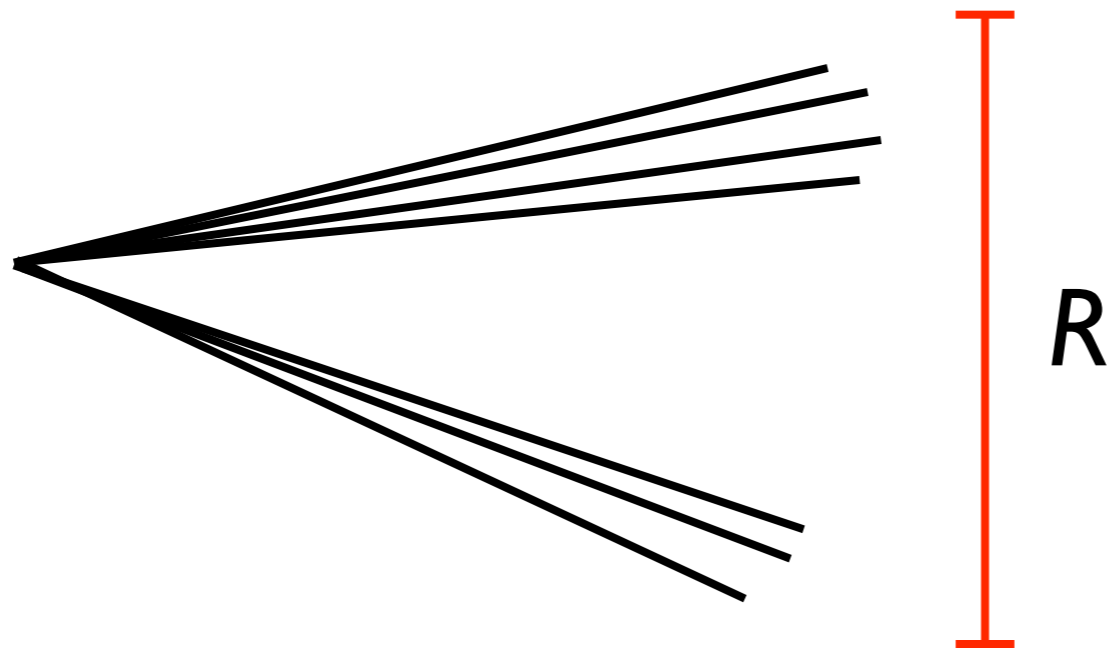
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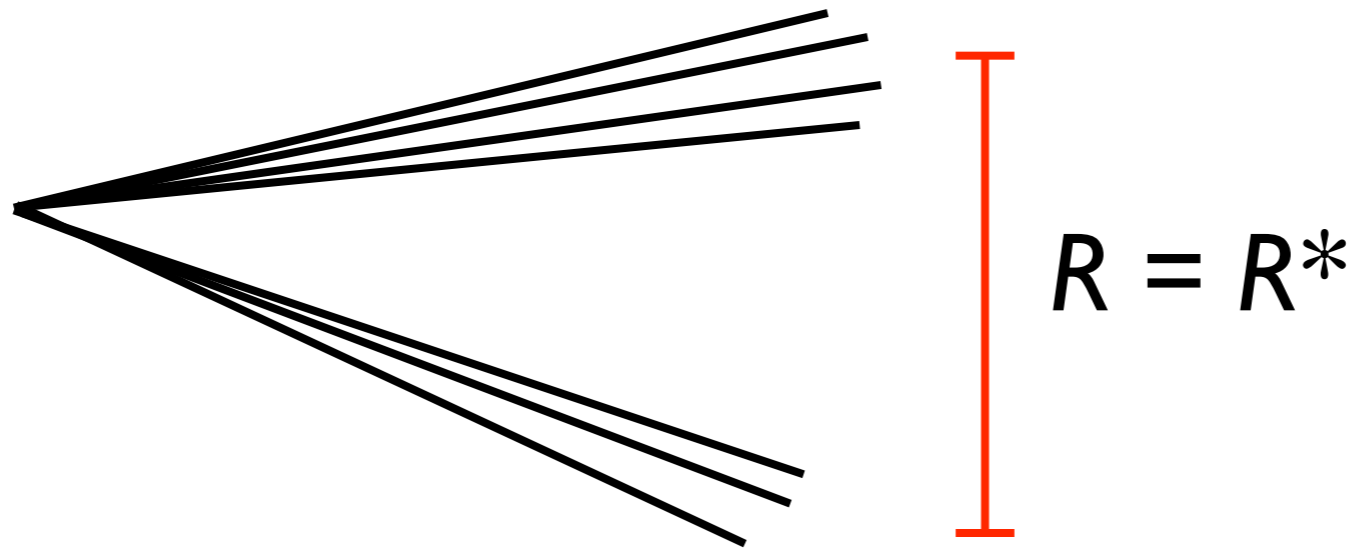
# Angular Correlation Function

- expectations
  - ACF for heavy particle jet will have “cliffs” at characteristic values of  $R$



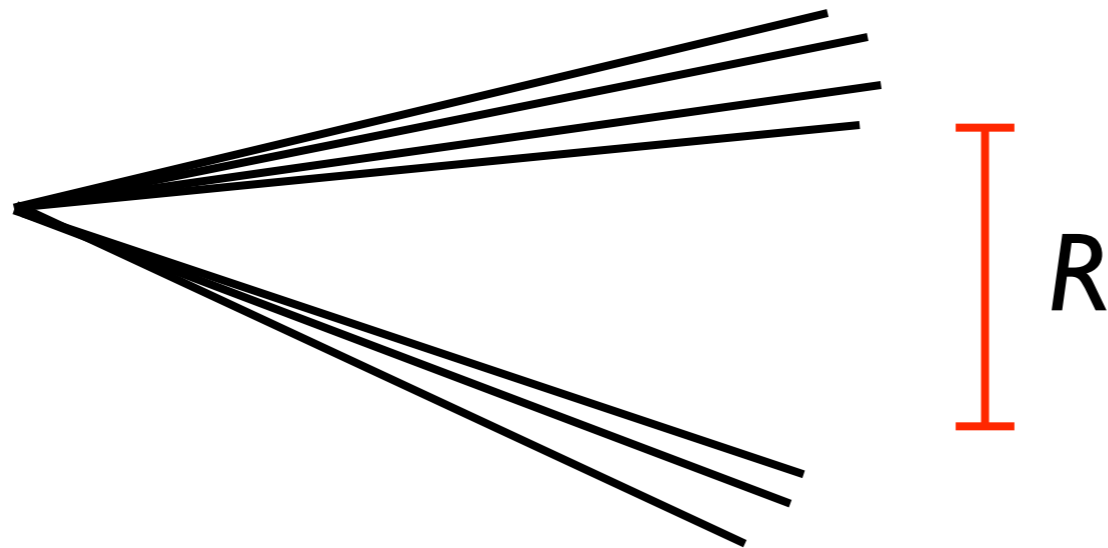
# Angular Correlation Function

- expectations
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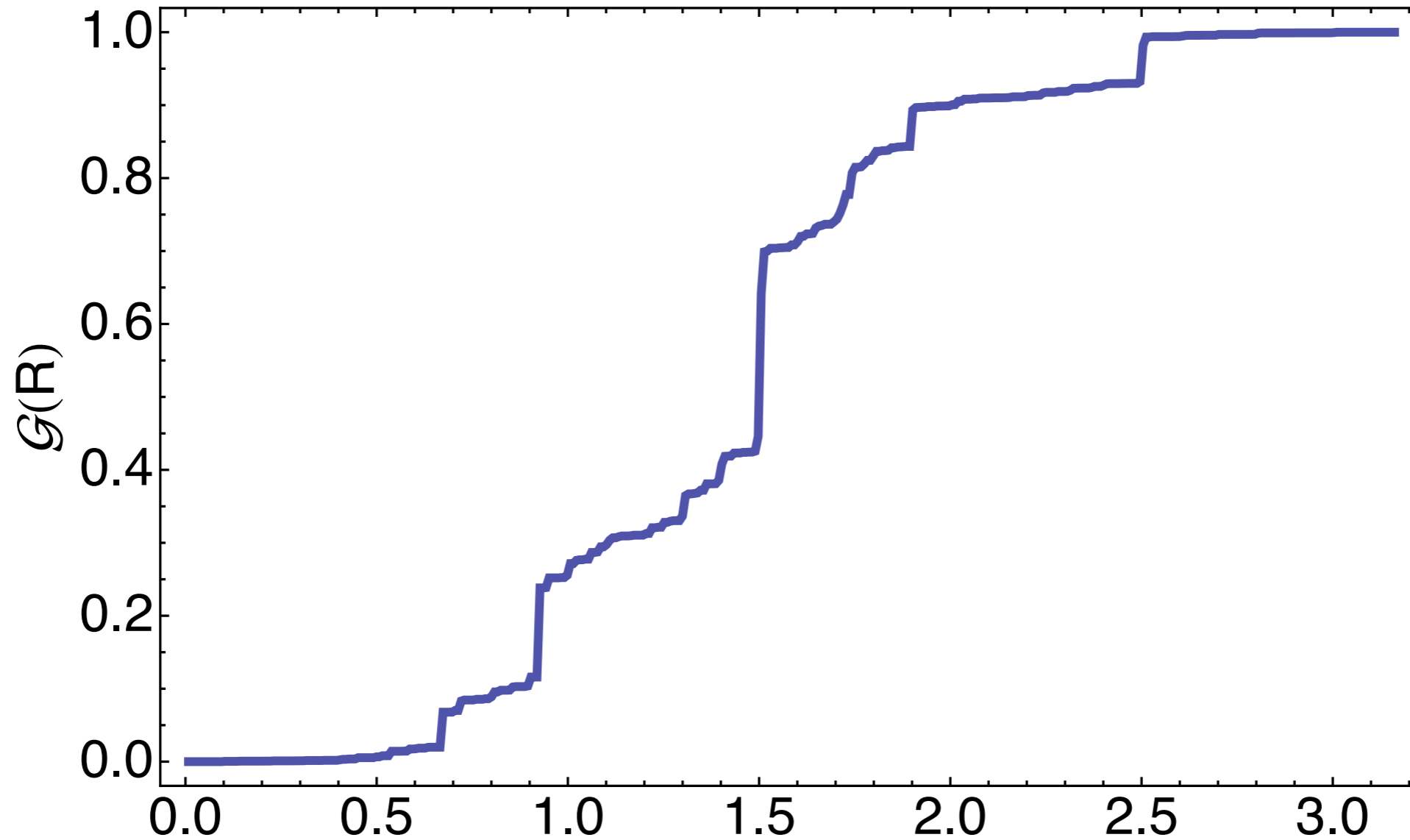


# Angular Correlation Function

- expectations
  - ACF for heavy particle jet will have “cliffs” at characteristic values of  $R$



- cliffs in  $\mathcal{G}(R) =$  separation of hard subjets



- $\mathcal{G}(R)$  for a top quark jet<sup>R</sup>

# Angular Structure Function

- how to extract a dimension:
  - “standard way”:

$$D = \lim_{R \rightarrow 0} \frac{\log \mathcal{G}(R)}{\log R}$$

- problem: can't access this limit!

# Angular Structure Function

- how to extract a dimension:
  - better: take a derivative

$$D = \frac{d \log \mathcal{G}(R)}{d \log R}$$

- benefits: defined for all  $R$ , cliffs in ACF manifest themselves as peaks in derivative



# Angular Structure Function

- define angular structure function (ASF):

$$\begin{aligned}\Delta\mathcal{G}(R) &\equiv \frac{d \log \mathcal{G}(R)}{d \log R} \\ &= R \frac{\sum_{i \neq j} p_{\perp i} p_{\perp j} \Delta R_{ij}^2 \delta[R - \Delta R_{ij}]}{\sum_{i \neq j} p_{\perp i} p_{\perp j} \Delta R_{ij}^2 \Theta[R - \Delta R_{ij}]}\end{aligned}$$

# Angular Structure Function

- delta-function is inappropriate for finite data
- smooth ASF by replacing delta-function:

$$\Delta\mathcal{G}(R) = R \frac{\sum_{i \neq j} p_{\perp i} p_{\perp j} \Delta R_{ij}^2 K[R - \Delta R_{ij}]}{\sum_{i \neq j} p_{\perp i} p_{\perp j} \Delta R_{ij}^2 \Theta[R - \Delta R_{ij}]}$$

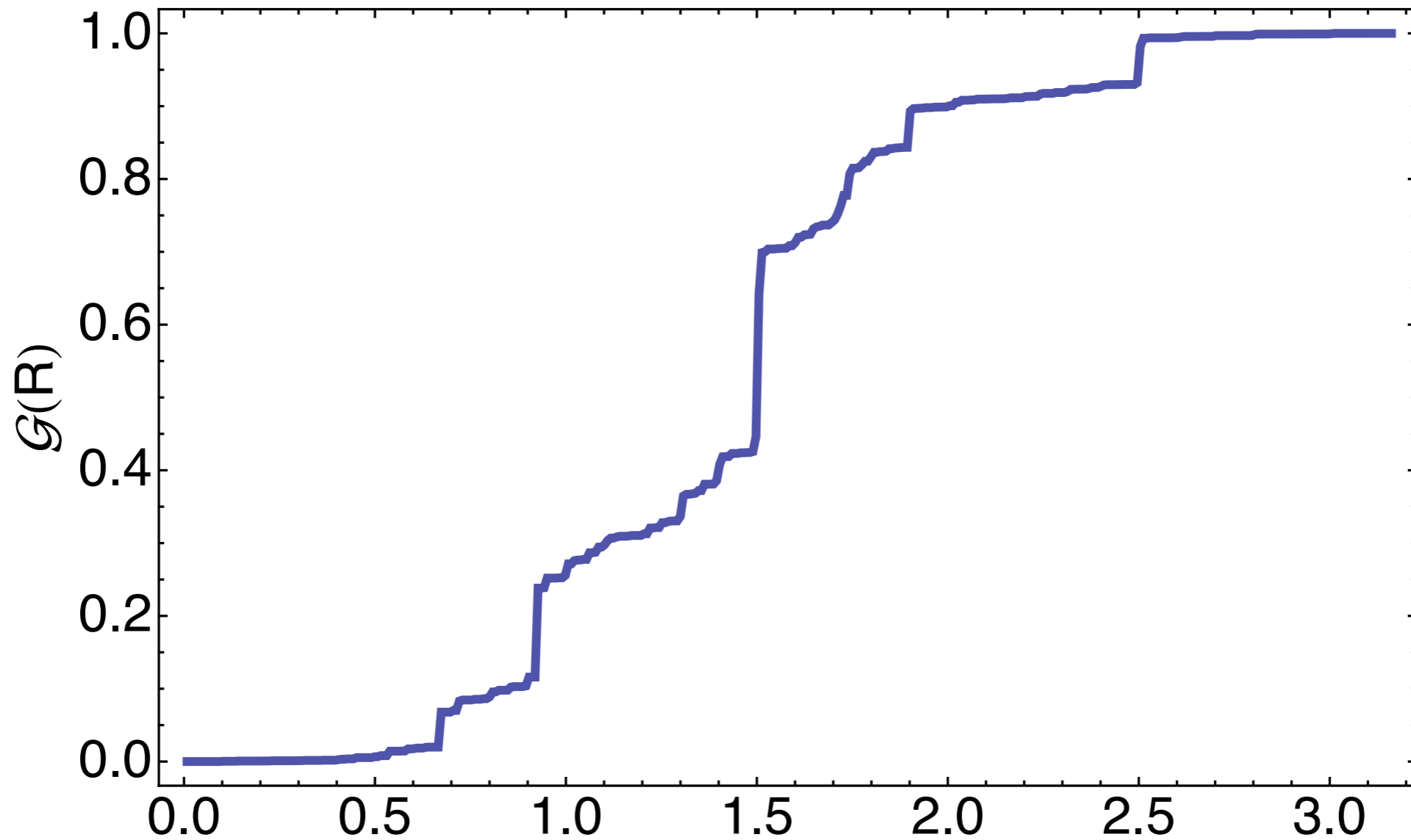
- $K$  is taken to be a smooth gaussian kernel:

$$\delta(R - \Delta R_{ij}) \simeq \frac{e^{-\frac{(R - \Delta R_{ij})^2}{2dR^2}}}{dR\sqrt{2\pi}}$$

**first application**

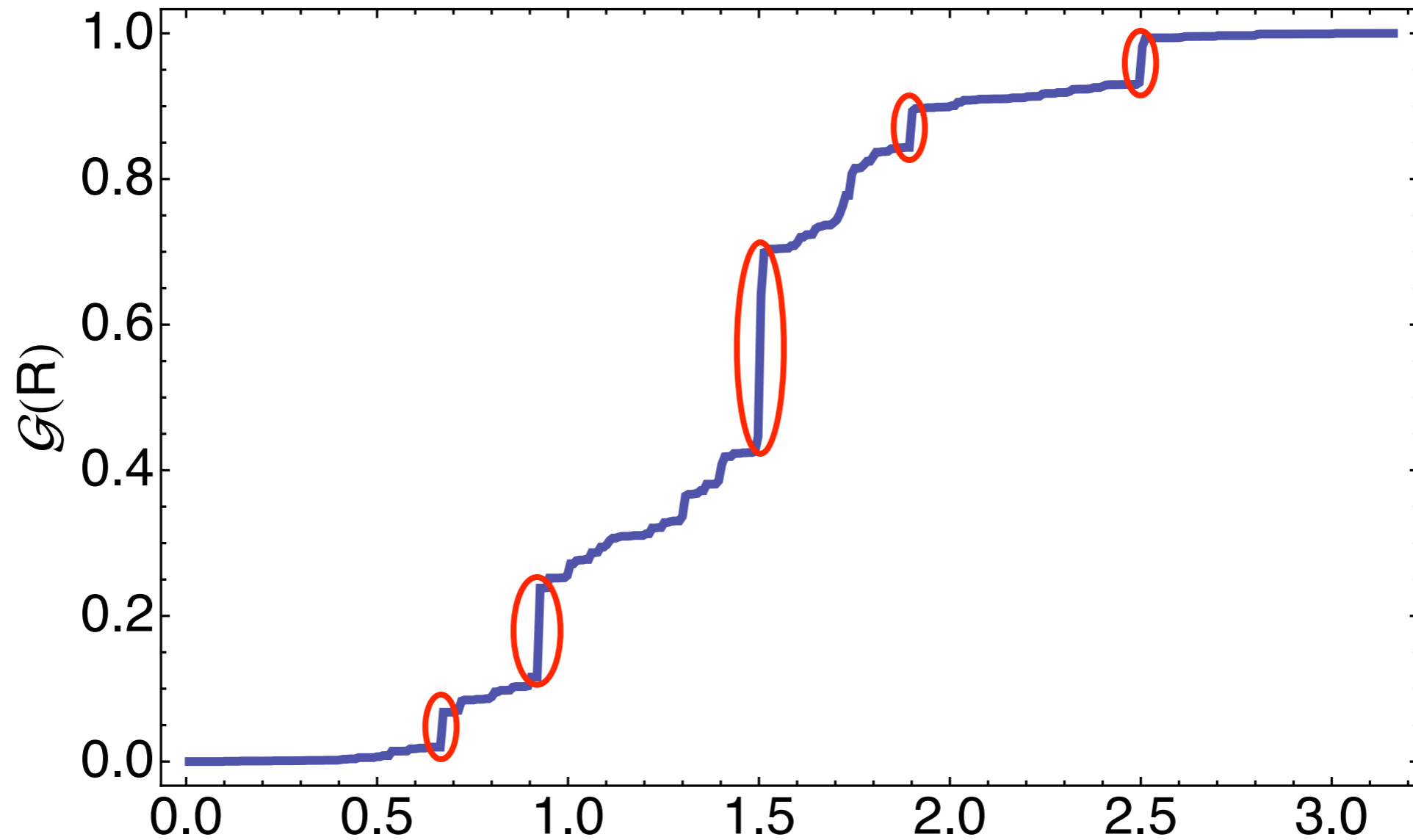
ASF event by event:  
Top Tagging

- cliffs in  $\mathcal{G}(R) =$  separation of hard subjets



- $\mathcal{G}(R)$  for a top quark jet<sup>R</sup>

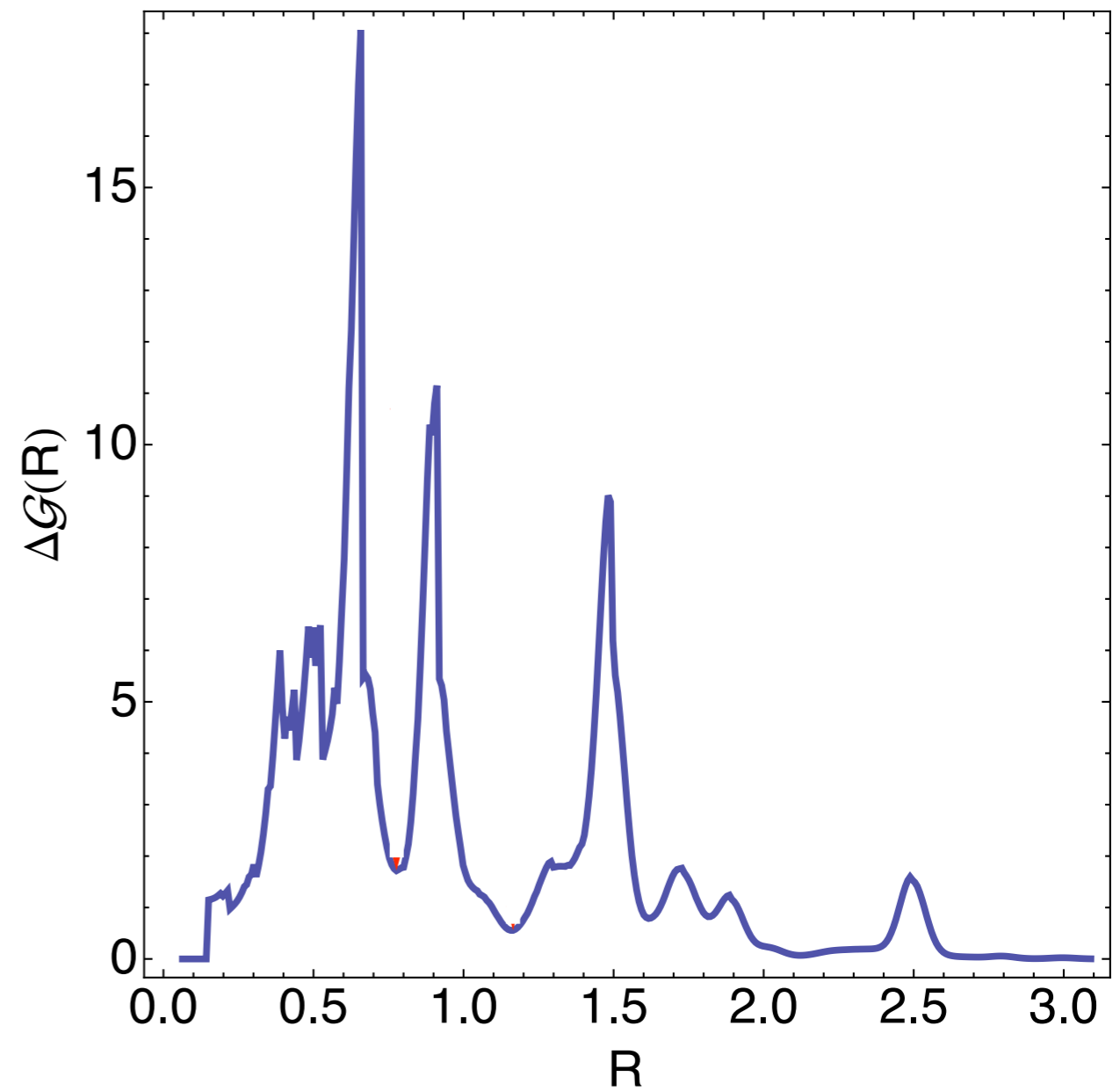
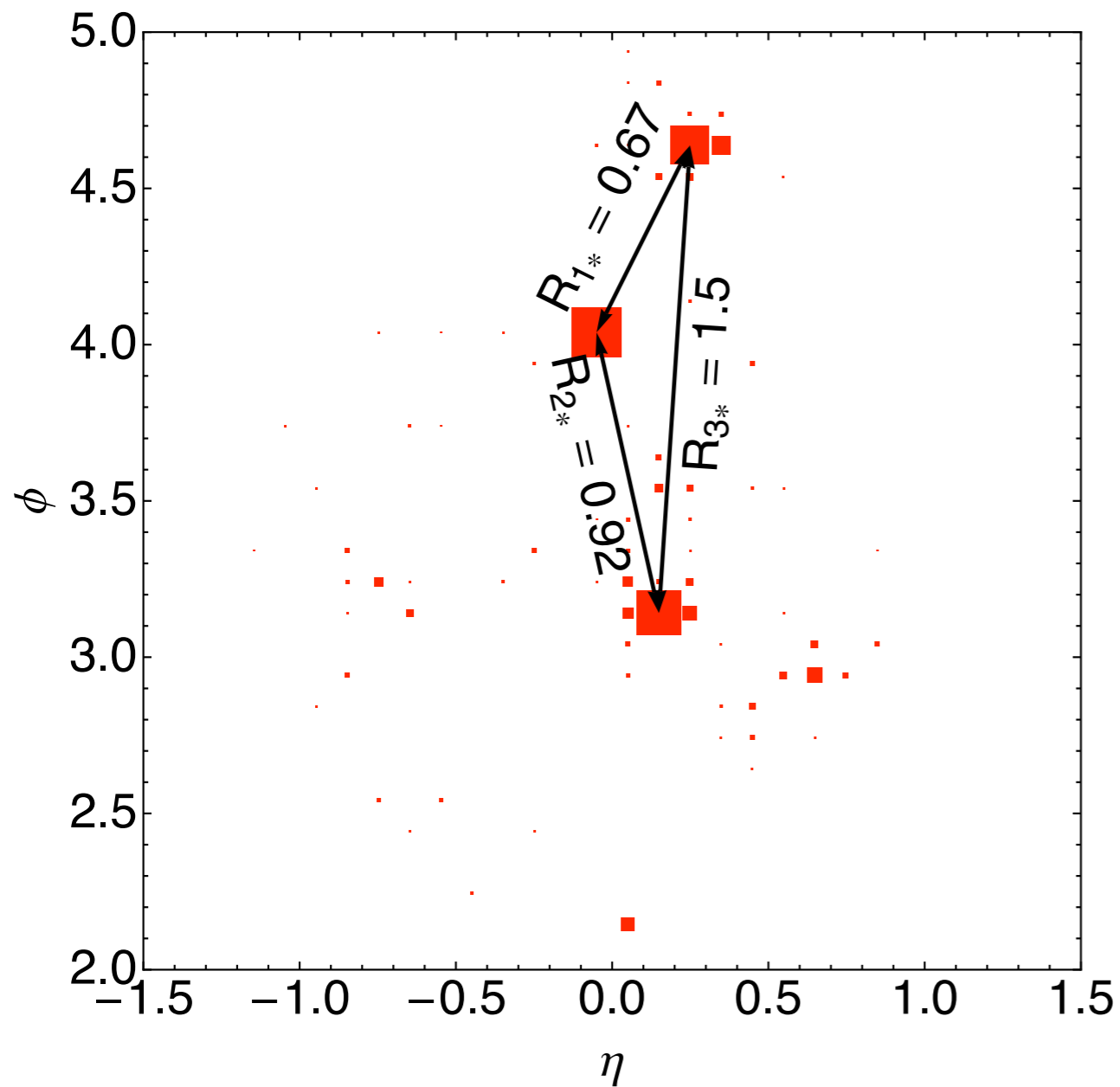
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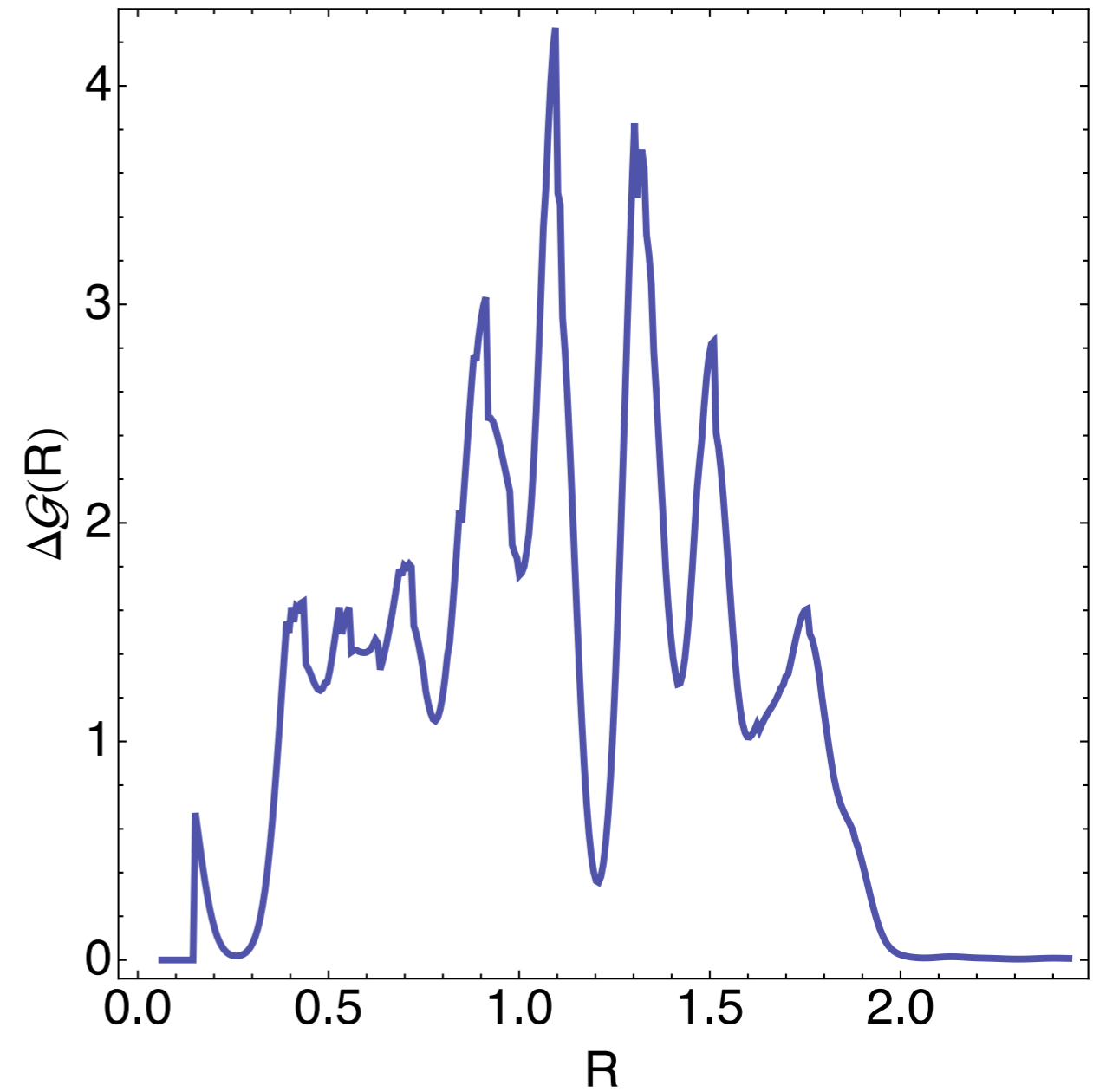
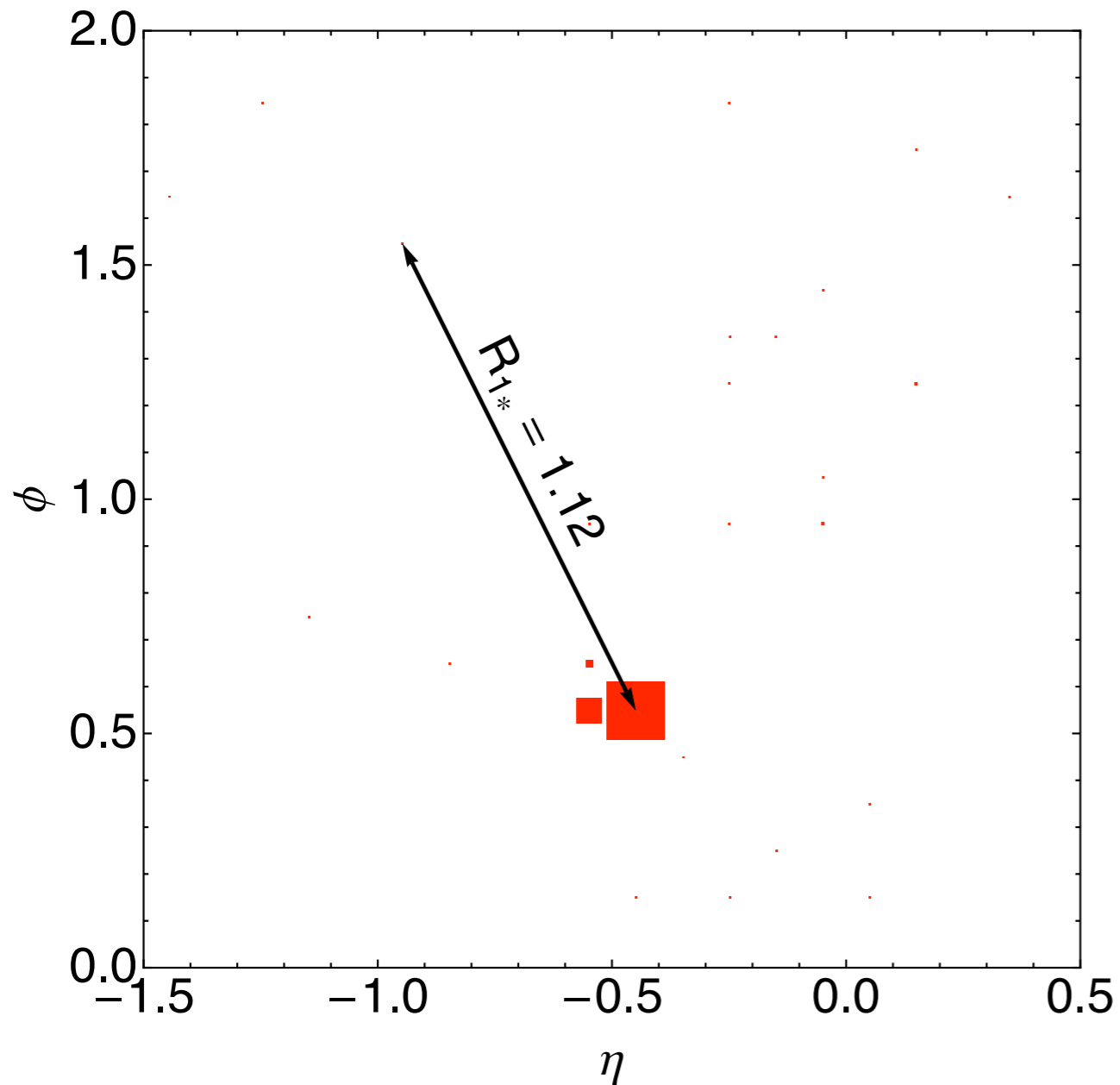
# “Jet Substructure Without Trees”

## Top Jet



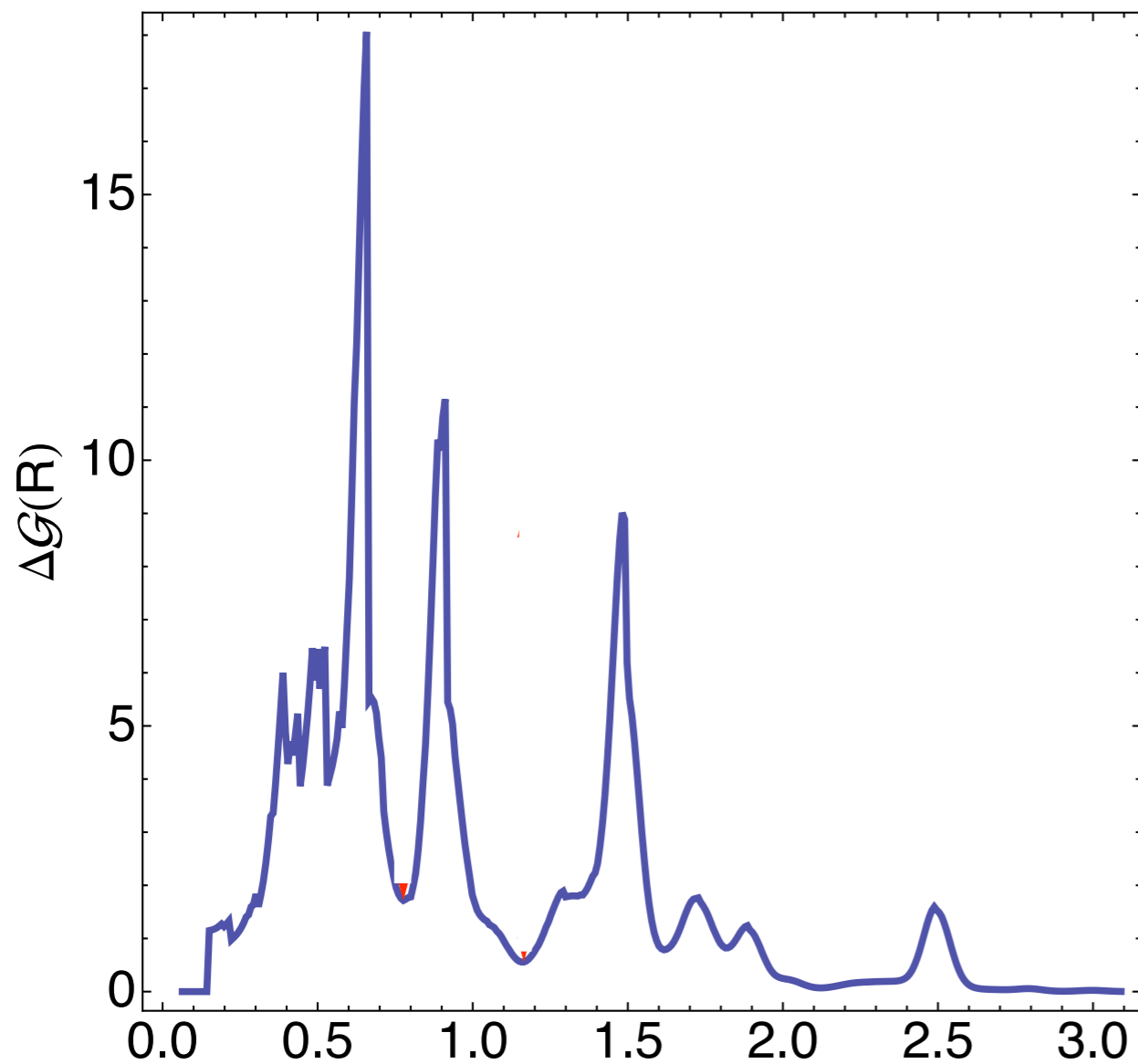
# “Jet Substructure Without Trees”

QCD Jet



# Defining Observables

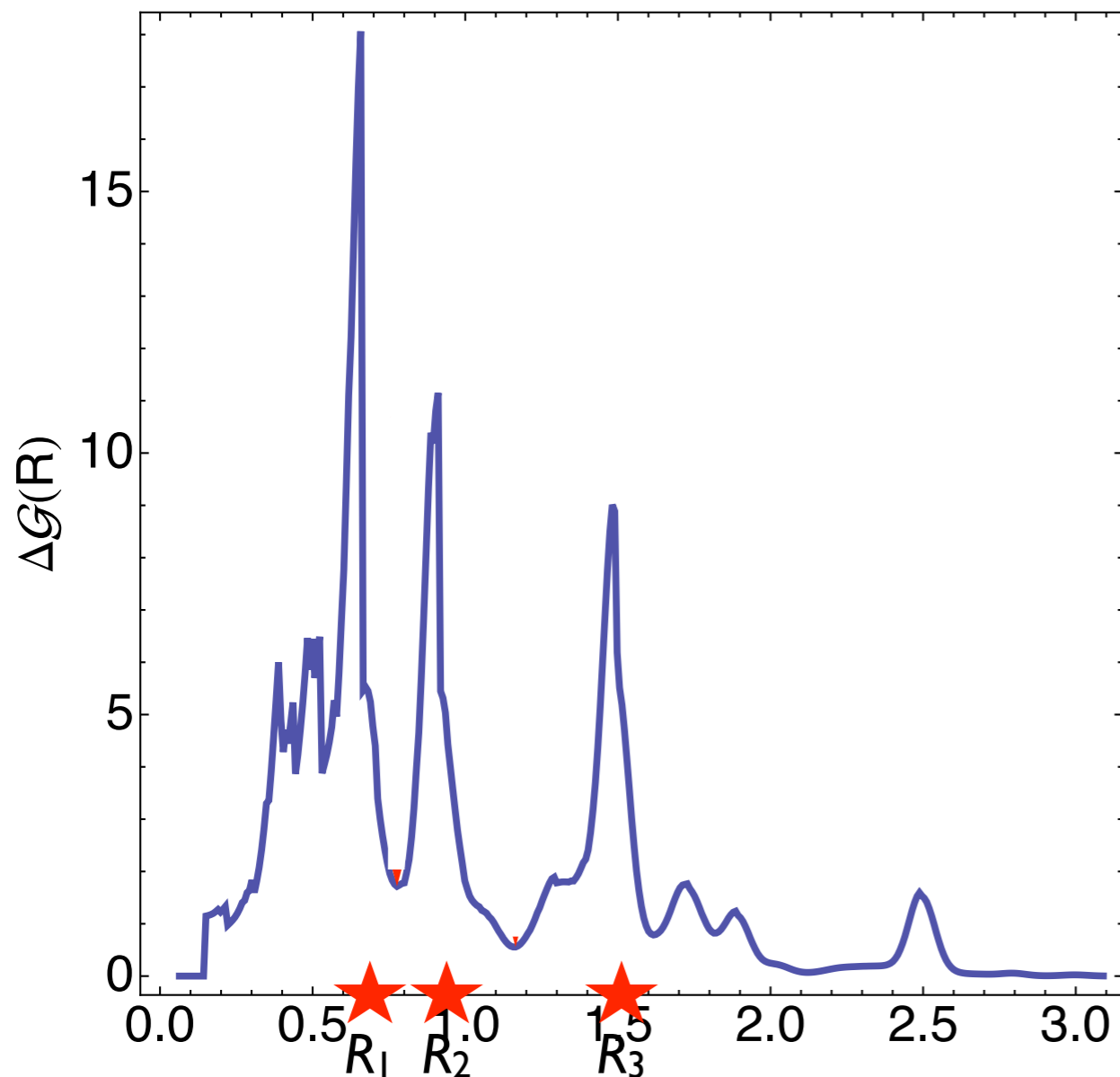
- IRC safe observables from  $\Delta\mathcal{G}(R)$ :





# Defining Observables

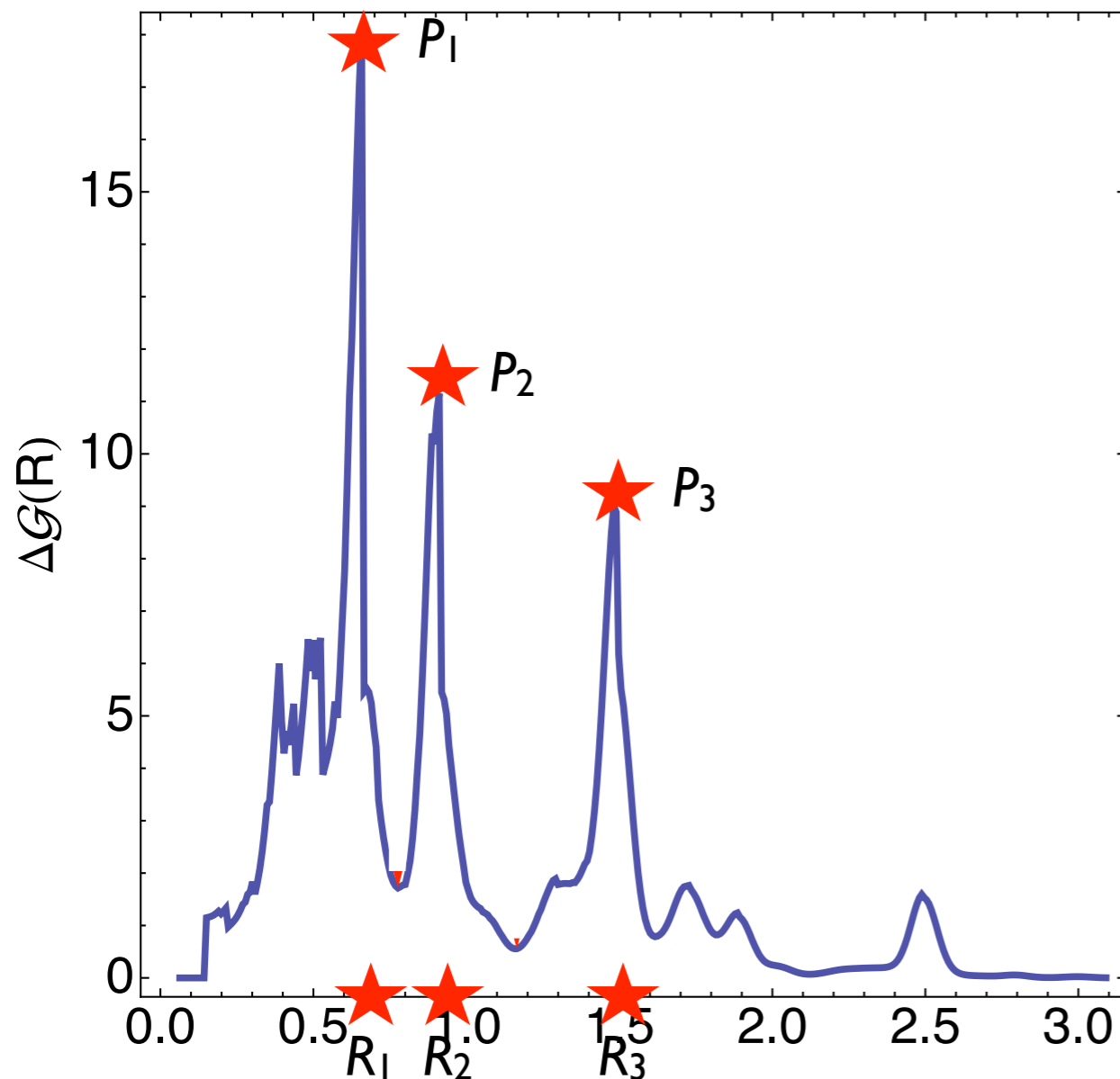
- IRC safe observables from  $\Delta\mathcal{G}(R)$ :



- location of peaks in  $R$

# Defining Observables

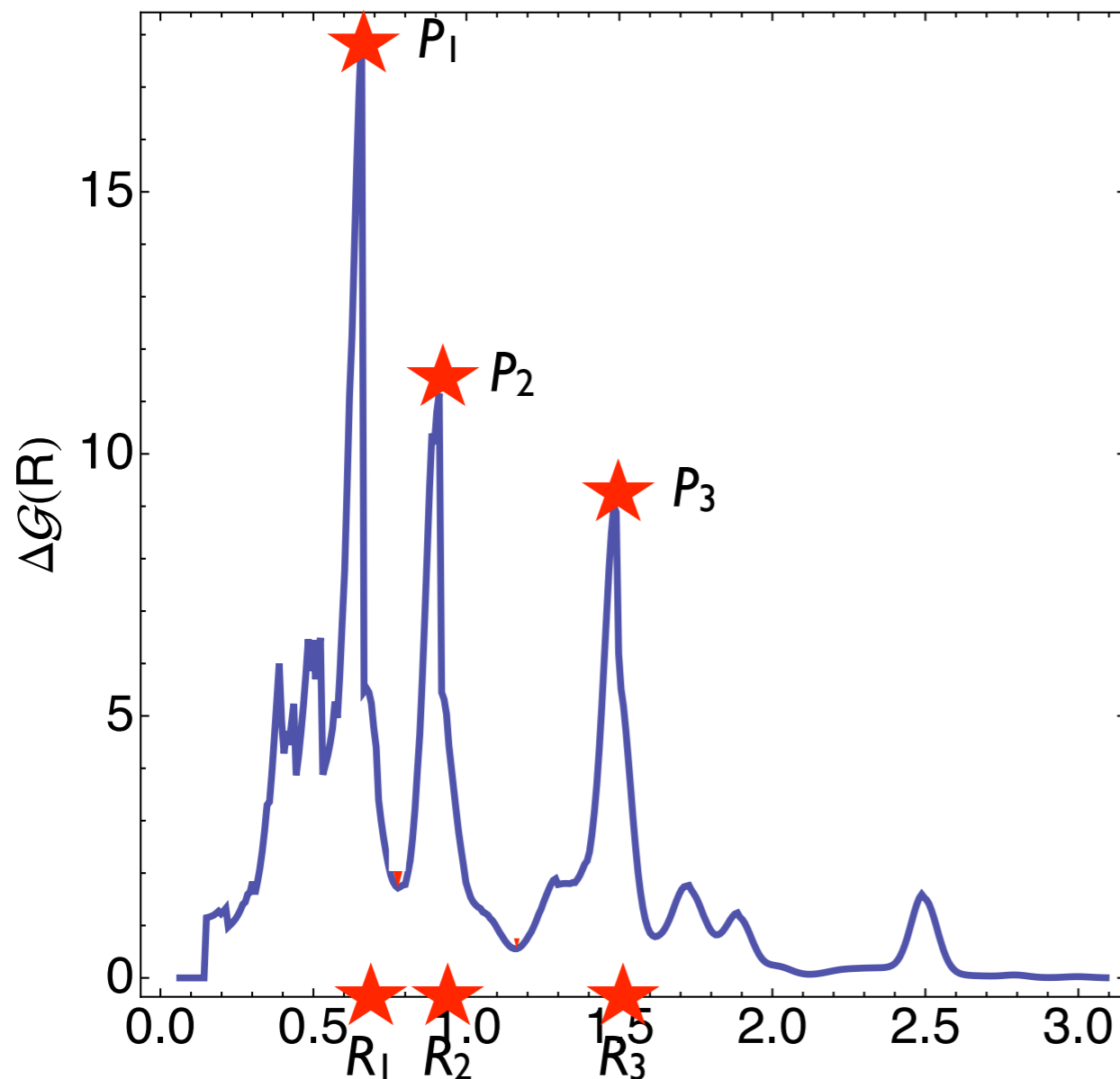
- IRC safe observables from  $\Delta\mathcal{G}(R)$ :



- location of peaks in  $R$
- height of peaks

# Defining Observables

- IRC safe observables from  $\Delta\mathcal{G}(R)$ :



- location of peaks in  $R$
- height of peaks
- number of peaks

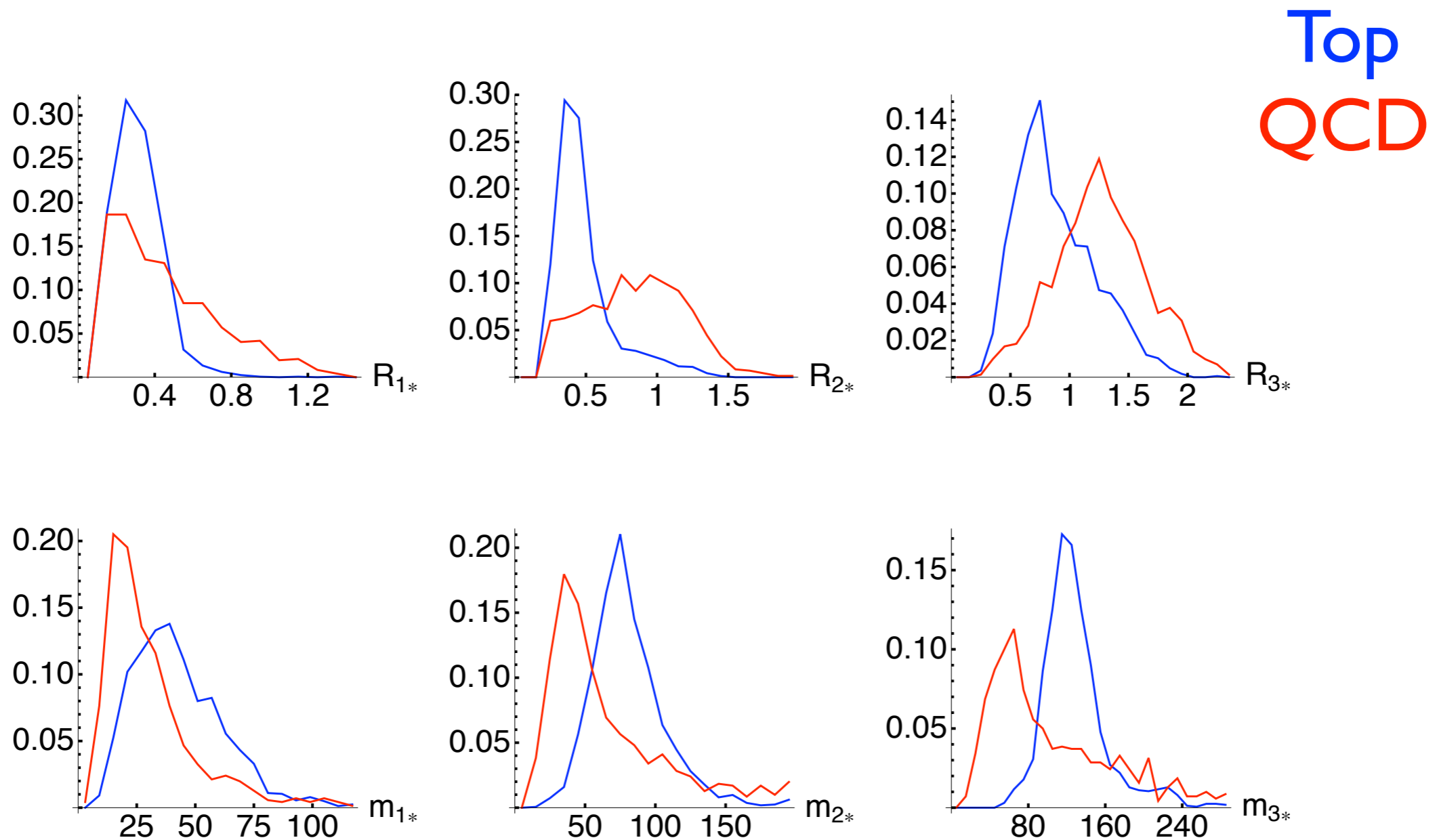
# Top Tagger

- top tagging approach:
  - bin jets by the number of peaks
  - in each bin place rectangular cuts on the available observables (mass and angular scales)

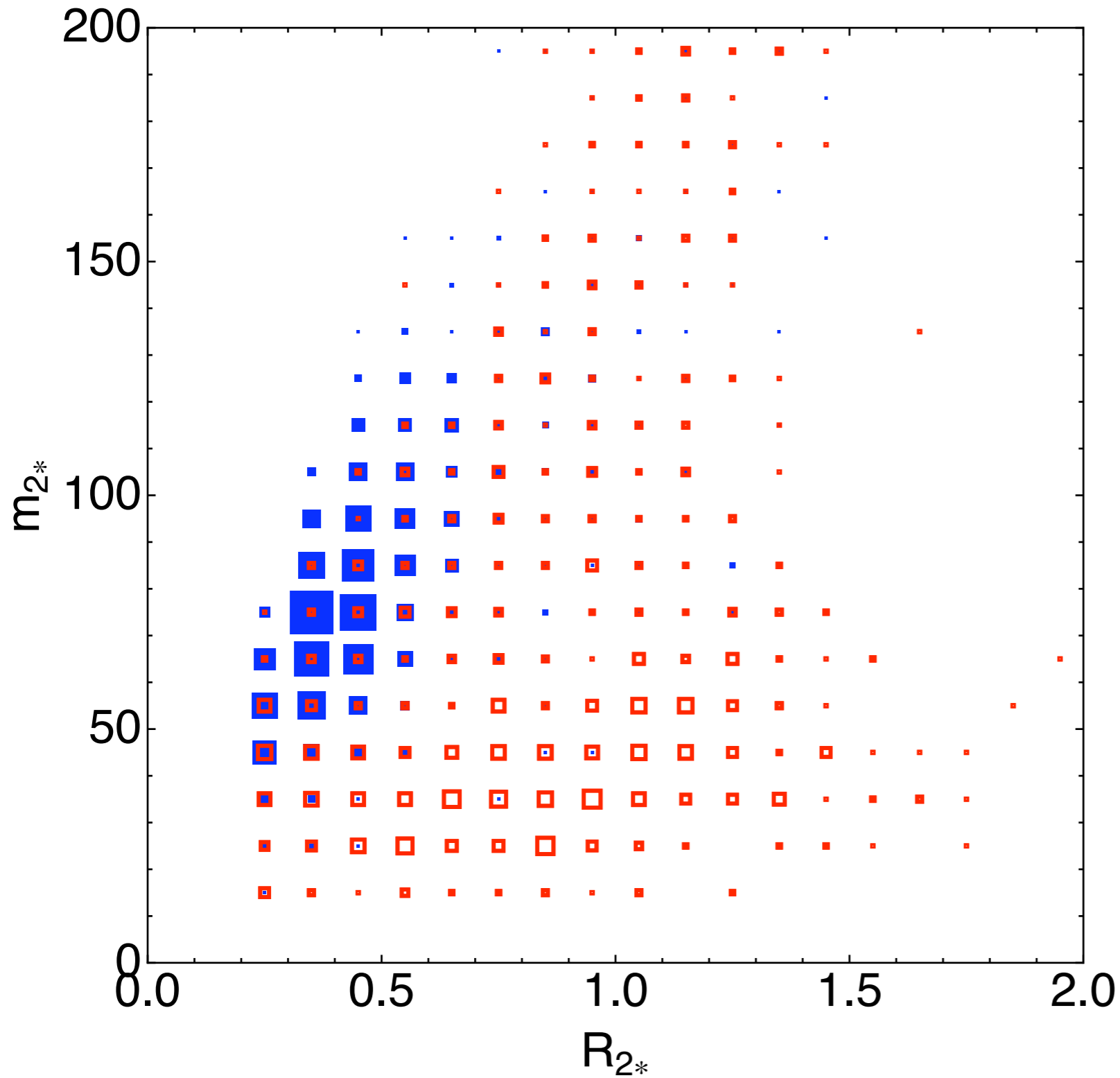
$$m_{R_*}^2 \equiv \text{Numerator}[\Delta\mathcal{G}(R_*)] = \sum_{i \neq j} p_{Ti} p_{Tj} \Delta R_{ij}^2 K(R_* - \Delta R_{ij})$$

# Top Tagger

- observables for  $dR = 0.06$ , min height = 4.0, npeaks = 3



# Top Tagger

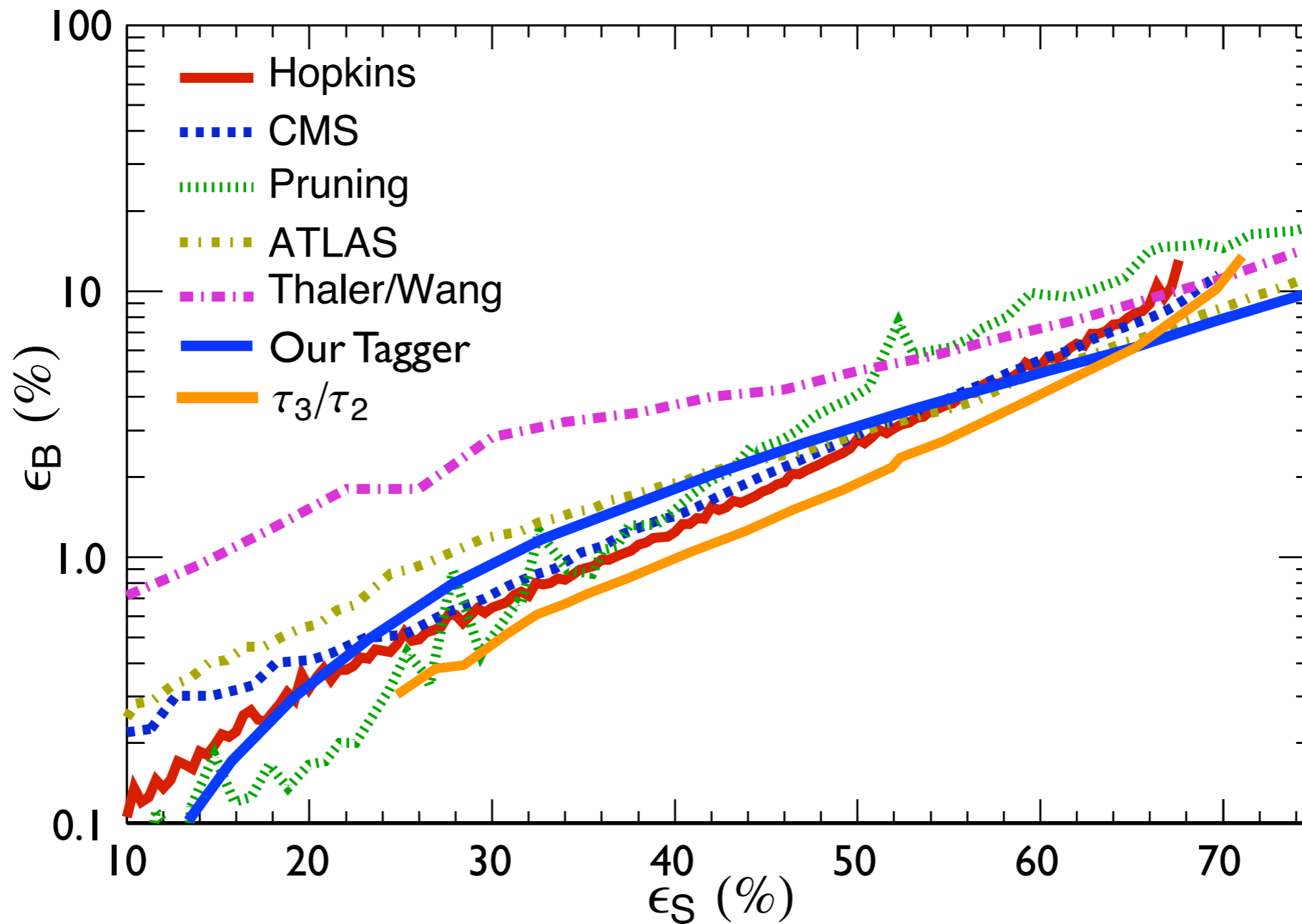


Top  
QCD

- Top:  $m \sim R$
- QCD:  $m, R$  uncorrelated

# Top Tagger

- comparison to other top taggers



**second application**

ensemble averaged ASF:  
the underlying event



# Ensemble Averages

average ACF  $\langle \mathcal{G}(R) \rangle \equiv \frac{1}{n} \sum_{k=1}^n \mathcal{G}(R)_k$

$$\langle \Delta \mathcal{G}(R) \rangle \equiv R \frac{\frac{d}{dR} \langle \mathcal{G}(R) \rangle}{\langle \mathcal{G}(R) \rangle}$$

$$= R \frac{\sum_{k=1}^n \mathcal{G}'(R)_k}{\sum_{k=1}^n \mathcal{G}(R)_k}$$

$$\equiv R \frac{\sum_{k=1}^n \sum_{i \neq j} p_{Tk,i} p_{Tk,j} \Delta R_{ij}^2 \delta_{dR}(R - \Delta R_{ij})}{\sum_{k=1}^n \sum_{i \neq j} p_{Tk,i} p_{Tk,j} \Delta R_{ij}^2 \text{erf}(R - \Delta R_{ij})}$$

$$\neq \frac{1}{n} \sum_{k=1}^n \Delta \mathcal{G}(R)_k$$

average ASF

# Simple calculation

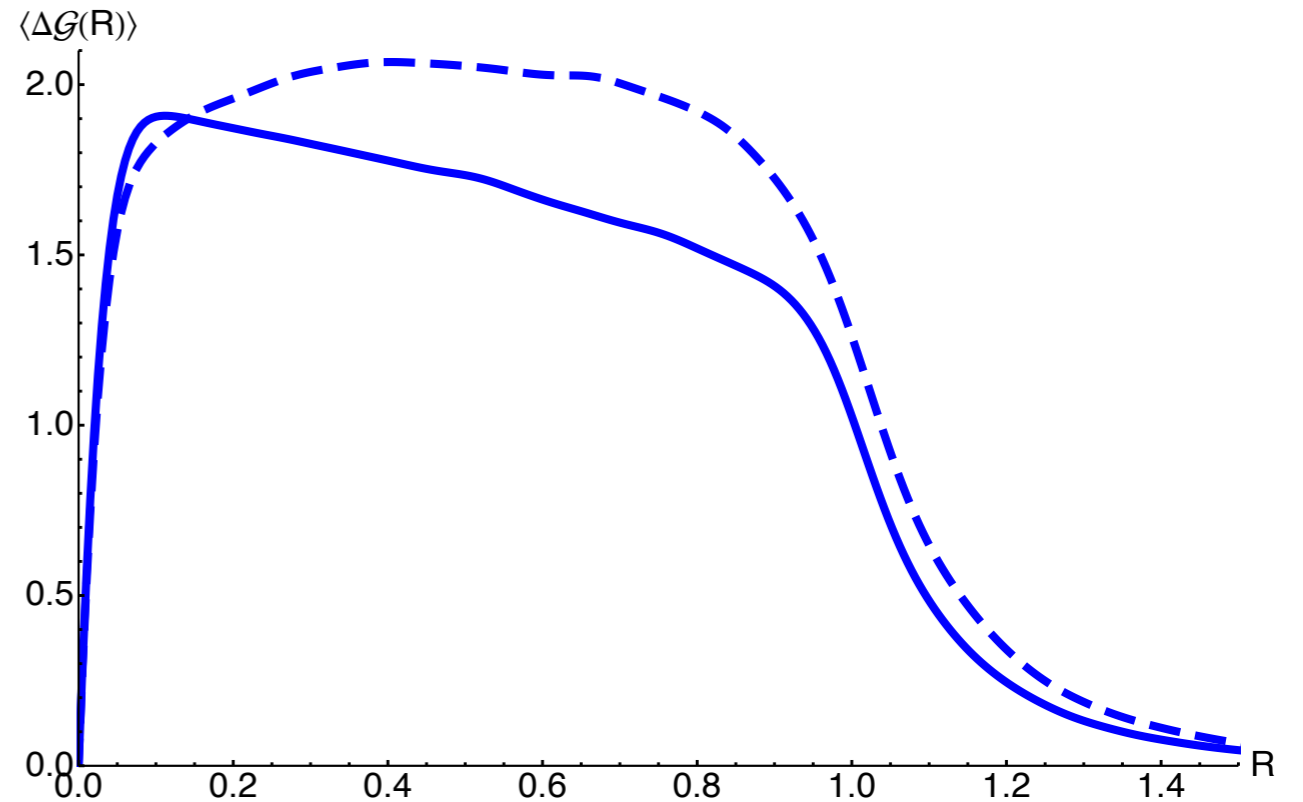
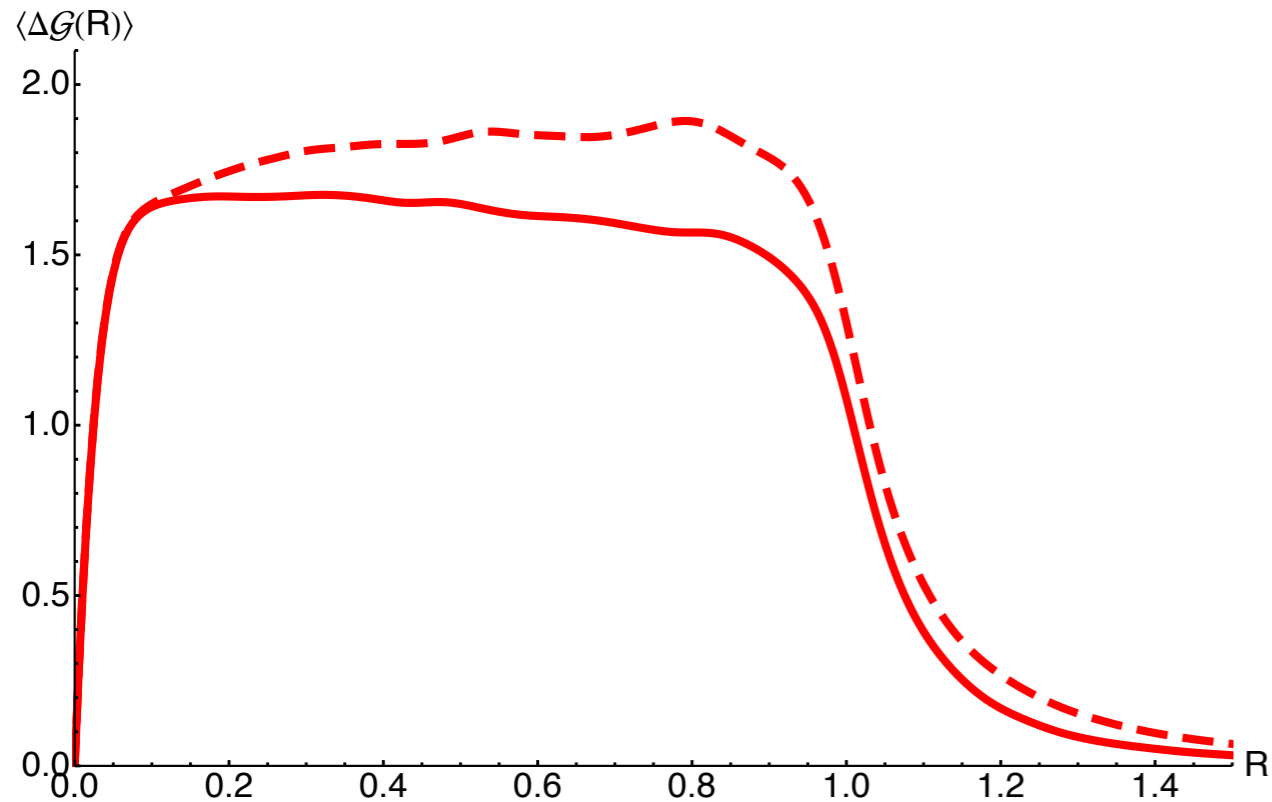
$$\langle \mathcal{G}(R) \rangle \simeq \frac{\alpha_s}{2\pi} \int^{R_0^2} \frac{d\theta^2}{\theta^2} \int dz P(z) p_T^2 z(1-z) \theta^2 \Theta(R - \theta)$$

$$\langle \mathcal{G}(R) \rangle = \frac{\alpha_s}{2\pi} p_T^2 R^2 \begin{cases} \frac{3}{4} C_F & \text{quark jets} \\ \frac{7}{10} C_A + \frac{1}{10} n_F T_R & \text{gluon jets} \end{cases}$$

$$\langle \Delta \mathcal{G}(R) \rangle = 2$$

expect higher order effects to be  $\mathcal{O}(\alpha_s) \sim 10\%$

# Monte Carlo



Pythia8 (solid) vs. Herwig++ (dashed): no UE or ISR

red = quark jets

blue = glue jets

# Simple calculation continued

- leading order integral can be computed analytically with a running coupling

$$\alpha_s(p_T\theta(1-z)) = \frac{\alpha_0}{\log\left(\frac{p_T\theta(1-z)}{\Lambda_{QCD}}\right)}$$

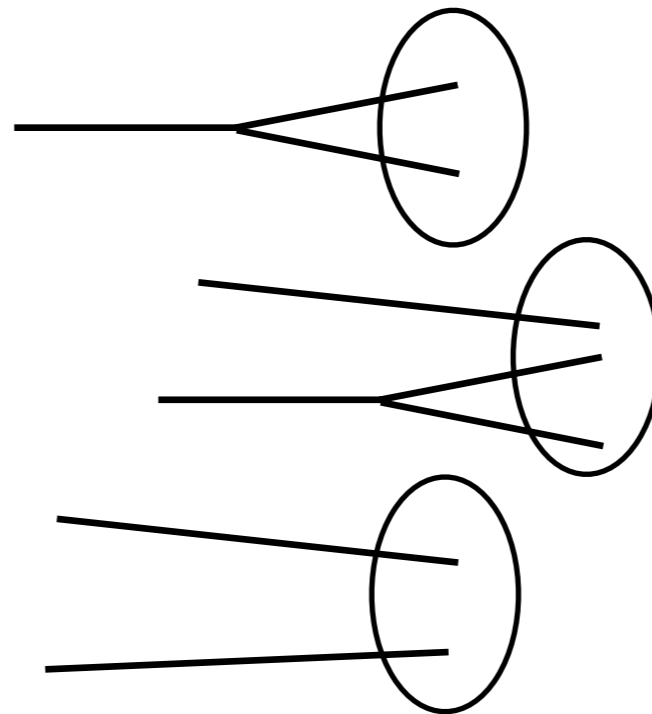
$$\langle\Delta\mathcal{G}(R)\rangle \simeq 2 - \frac{1}{\log\left(\frac{p_T R}{\Lambda_{QCD}}\right)} + \mathcal{O}\left(1/\log^2\left(\frac{p_T R}{\Lambda_{QCD}}\right)\right)$$

# Contributions from the underlying event

- schematically, the ACF can be written as:

$$\text{ACF} = (\text{Pert-Pert correlations}) + (\text{Pert-UE correlations}) + (\text{UE-UE correlations})$$

- **Red**  $\sim p_T^2$
- **Blue**  $\sim p_T \Lambda_{\text{UE}}$
- **Green**  $\sim \Lambda_{\text{UE}}^2$

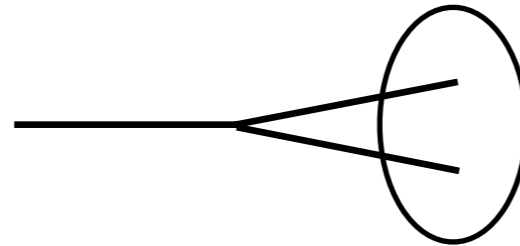


# Contributions from the underlying event

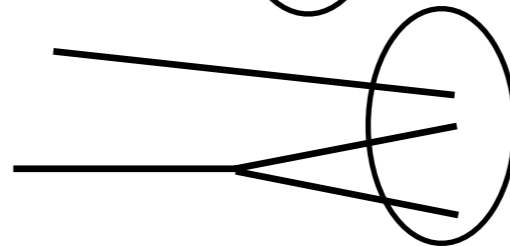
- schematically, the ACF can be written as:

$$\text{ACF} \sim (\text{Pert-Pert correlations}) + (\text{Pert-UE correlations})$$

- **Red**  $\sim p_T^2$



- **Blue**  $\sim p_T \Lambda_{UE}$



# Contributions from the underlying event

- Correlation between jet and UE:

$$\langle \mathcal{G}(R)_{\text{jet-UE}} \rangle = p_{\perp \text{jet}} \Lambda_{\text{UE}} \int_0^{2\pi} d\phi \int_0^R R' dR' R'^2 = \frac{\pi}{2} p_{\perp \text{jet}} \Lambda_{\text{UE}} R^4$$

- ACF including UE ansatz:

$$\langle \mathcal{G}(R)_{\text{with UE}} \rangle = \langle \mathcal{G}(R)_{\text{no UE}} \rangle + \frac{\pi}{2} p_{\perp \text{jet}} \Lambda_{\text{UE}} R^4$$

$$\langle \Delta \mathcal{G}(R)_{\text{no UE}} \rangle = \frac{R \langle \mathcal{G}'(R)_{\text{with UE}} \rangle - 2\pi p_{\perp \text{jet}} \Lambda_{\text{UE}} R^4}{\langle \mathcal{G}(R)_{\text{with UE}} \rangle - \frac{\pi}{2} p_{\perp \text{jet}} \Lambda_{\text{UE}} R^4}$$

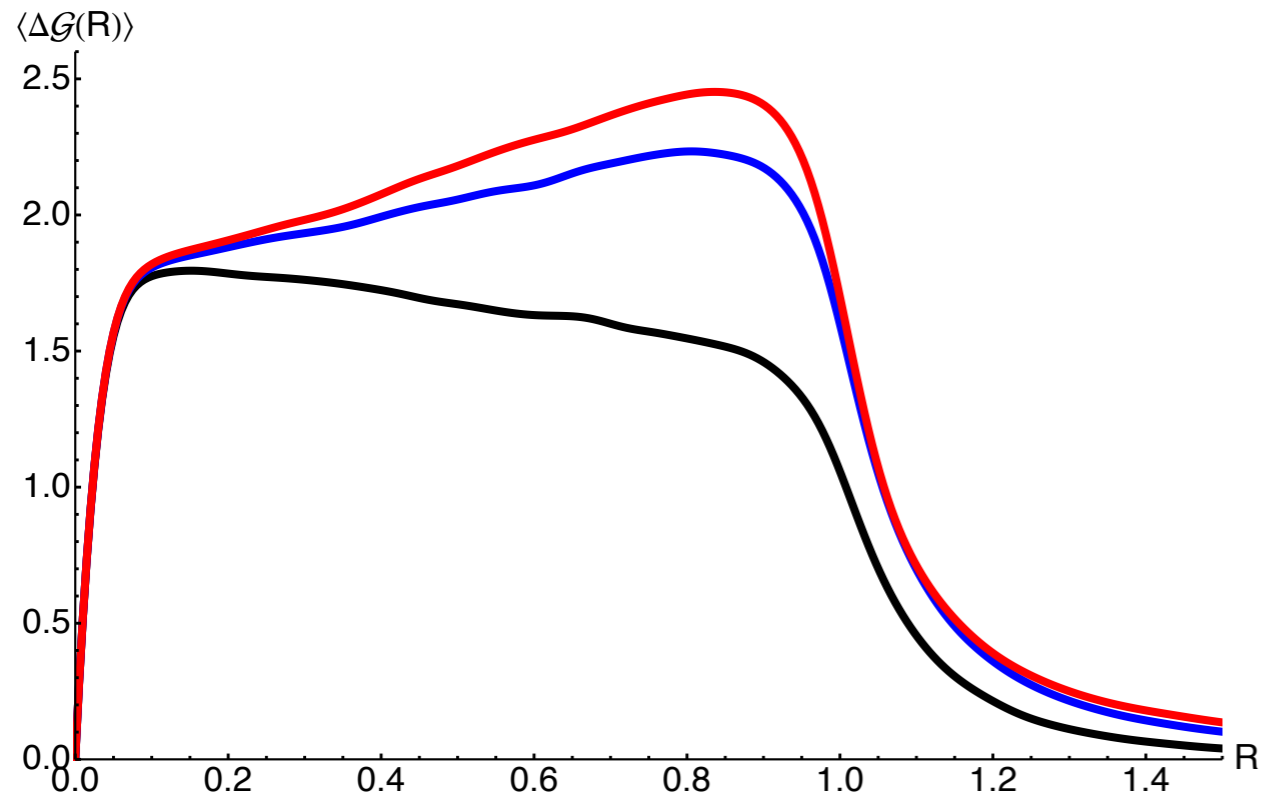
# Extracting UE Energy Density

$$\Lambda_{\text{UE}} = \frac{2\langle \mathcal{G}(R)_{\text{with UE}} \rangle \langle \Delta \mathcal{G}(R)_{\text{with UE}} \rangle - C(R)}{\pi p_{\perp \text{jet}} R^4 (4 - C(R))}$$

- $C(R)$  is the ansatz for perturbative ASF
- Data-driven approach:
  - Match  $C(R)$  to ASF at small  $R$
  - Compute UE energy density function
  - Flatness of UE energy density validates ansatz



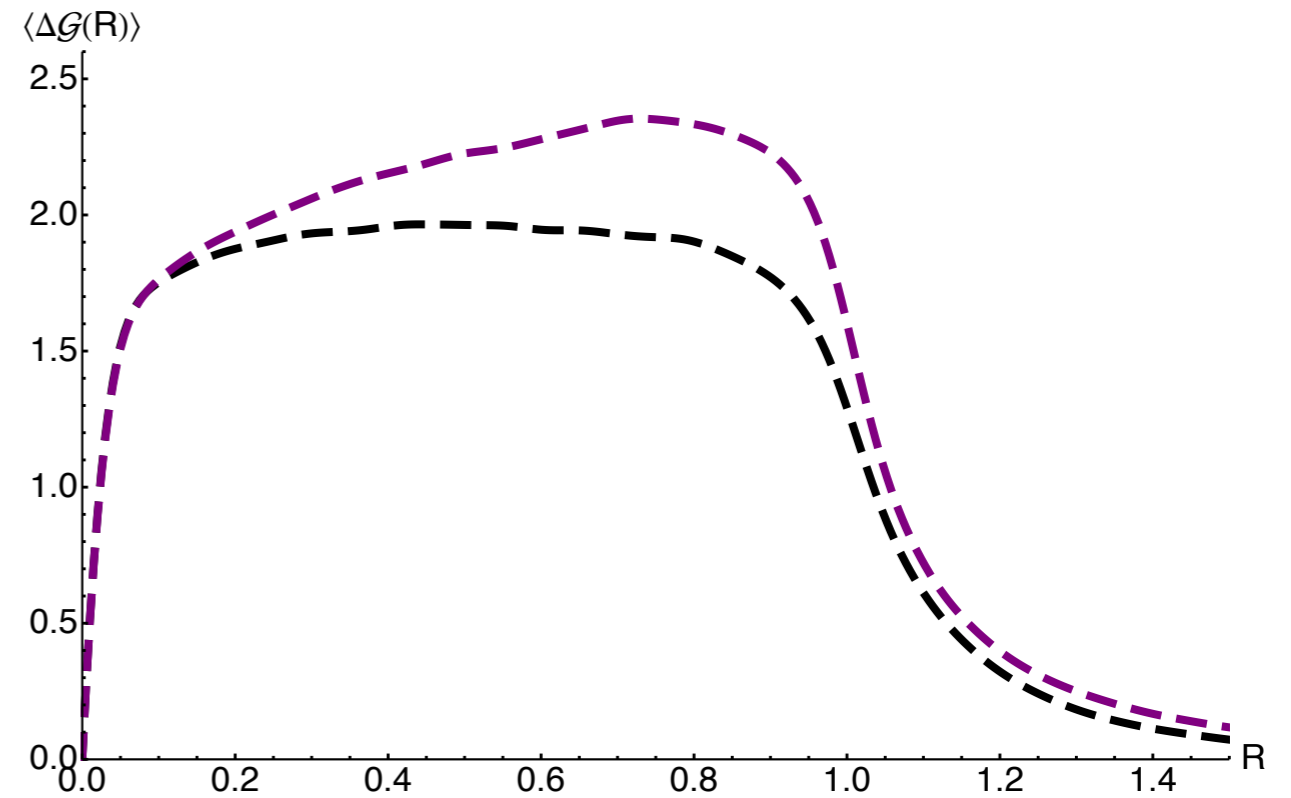
# Extracting UE Energy Density



Pythia8: with UE & ISR  
(blue, red);

red = 2x MPI cross section;

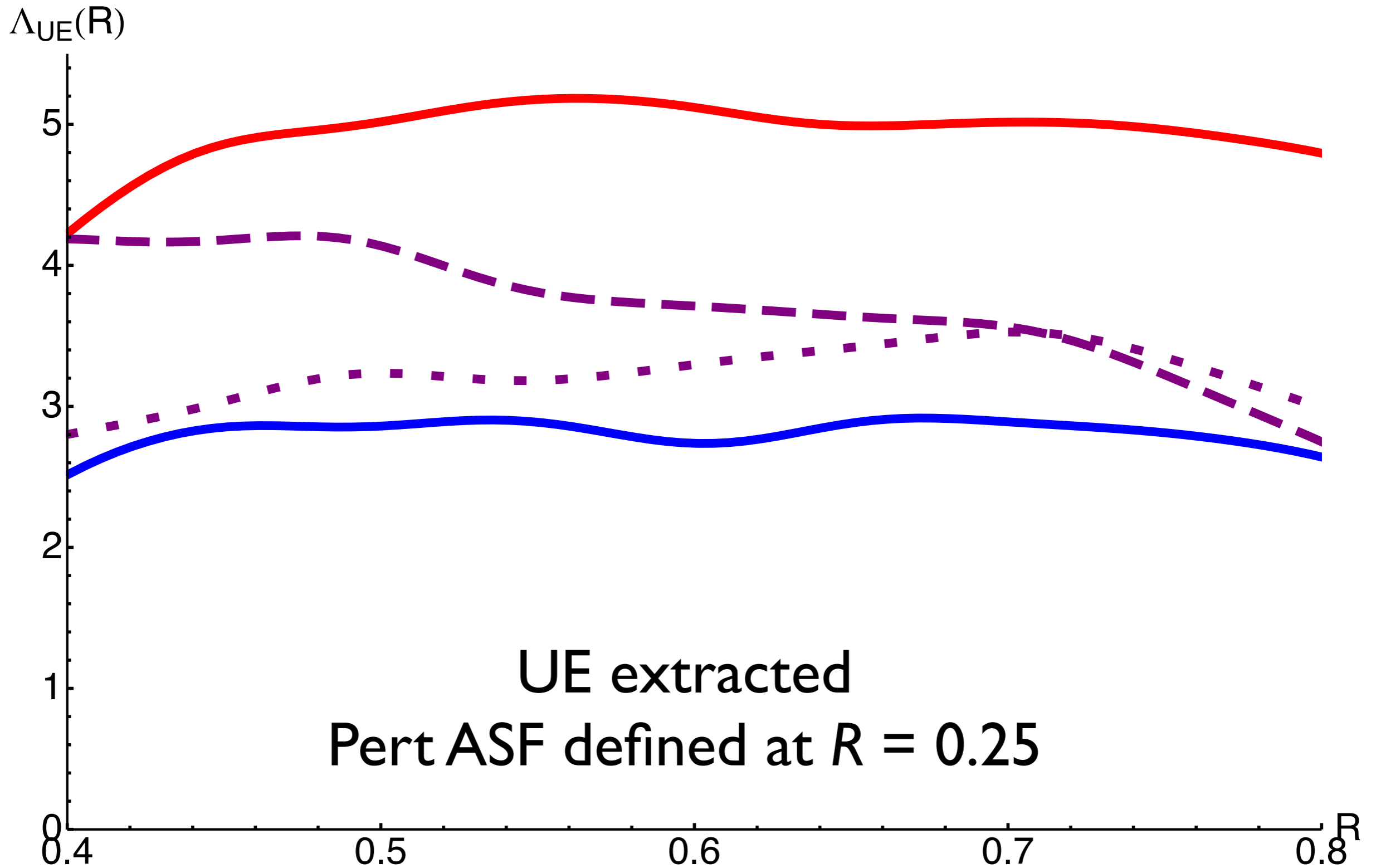
Tune 4C



Herwig: with UE & ISR  
(purple);

Tune LHC7-UE-2

# Extracting UE Energy Density



UE extracted  
Pert ASF defined at  $R = 0.25$

# Conclusions

- worth thinking about alternatives to the clustering paradigm
- ASF offers interesting event-by-event observables
- average ASF is an interesting observable sensitive to the whole of a jet's dynamics (parton shower, underlying event, ISR, ...)

# Conclusions

- many jet substructure techniques proposed to date - time to see them validated at the LHC
- so far focus has been on simpler topologies (e.g. top tagging). how well can we probe more complicated signals?
- more broadly: should searches for “spectacular” signatures fail to find anything, can we use jet substructure to increase sensitivity to and (especially) coverage of new physics?

**thank you**

