

NLO predictions for a Z boson + photons final states at the LHC

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(with John Campbell and Ciaran Williams, arXiv:1208.0566)

Florida State University/Fermilab

September 6, 2012



Fermilab Theory Seminar



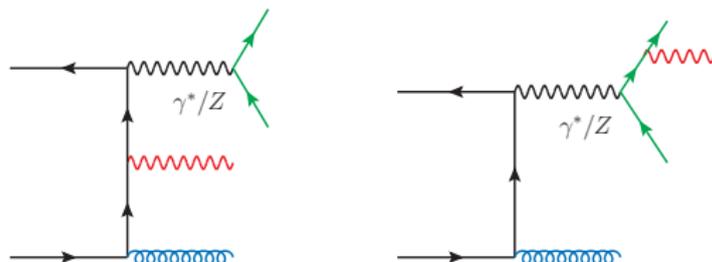
NLO QCD predictions for:

$$p + p \rightarrow \ell\bar{\ell} + \gamma + \text{jet} \quad \text{“}Z\gamma j\text{”}$$

$$p + p \rightarrow \ell\bar{\ell} + \gamma + \gamma \quad \text{“}Z\gamma\gamma\text{”}$$

where $\ell = e, \nu$.

For electron case, the final state radiation of photons from electrons are included.



$Z\gamma\gamma$ production \Rightarrow by-product of $Z\gamma j$ production.

The calculations are implemented in MCFM.

Outline:

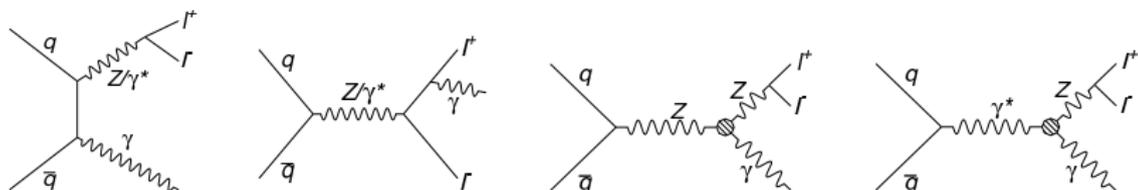
- Introduction
- Some Basic Tools
- $Z\gamma j$ production: Calculation and Results
- $Z\gamma\gamma$ production: Calculation and Results
- Conclusions

Introduction

Introduction

Diboson processes: study of the anomalous Three Gauge Couplings (aTGCs). For example:

- $W\gamma$ process $\Rightarrow WW\gamma$ coupling
- WZ process $\Rightarrow WWZ$ coupling
- WW process $\Rightarrow WW\gamma$ and WWZ couplings
- $Z\gamma$ process $\Rightarrow Z\gamma\gamma$ and $Z\gamma Z$ couplings



$Z\gamma\gamma$: background new physics search involving MET+diphotons final states

$Z\gamma Z$ and $Z\gamma\gamma$ non-standard couplings

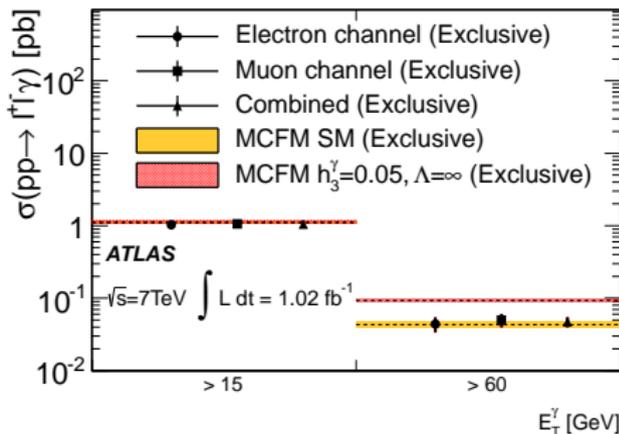
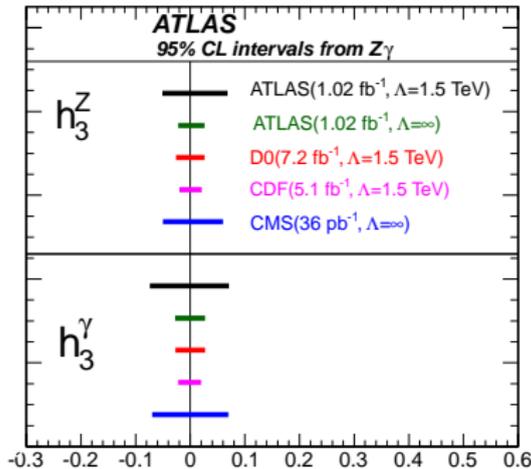
Non-standard $Z\gamma Z$ vertex:

[Hagiwara, Peccei, Zeppenfeld, Hikasa (1987)]

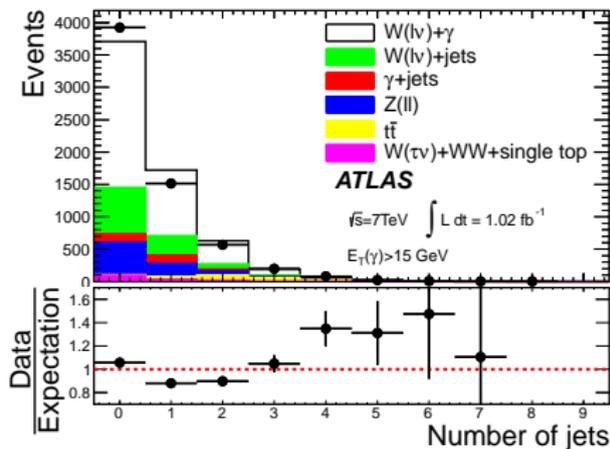
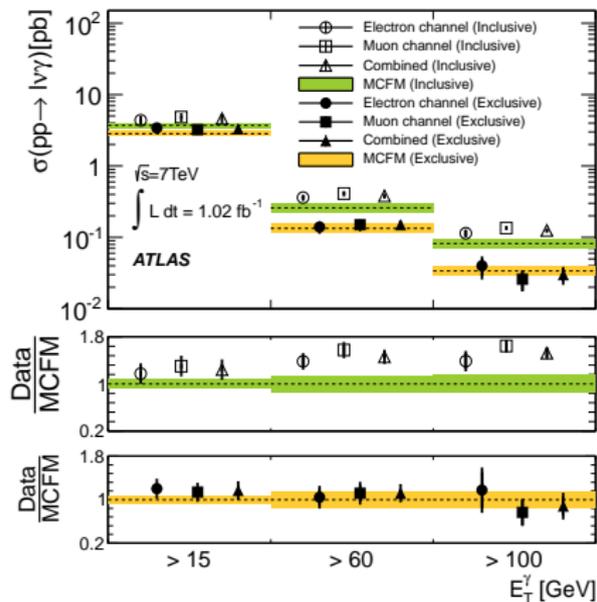
$$\Gamma_{Z\gamma Z}^{\alpha,\beta,\mu}(q_1, q_2, p) = i \frac{p^2 - q_1^2}{M_Z^2} \left[h_1^Z \left(q_2^\mu g^{\alpha\beta} - q_2^\alpha g^{\mu\beta} \right) + \frac{h_2^Z}{M_Z^2} p^\alpha \left(p \cdot q_2 g^{\mu\beta} - q_2^\mu p^\beta \right) \right. \\ \left. - h_3^Z \epsilon^{\mu\alpha\beta\nu} q_{2\nu} - \frac{h_4^Z}{M_Z^2} \epsilon^{\mu\beta\nu\sigma} p^\alpha p_\nu q_{2\sigma} \right]$$

For $Z\gamma\gamma$ vertex, $q_1^2 \rightarrow 0$, $h_i^Z \rightarrow h_i^\gamma$.

$$h_i^{Z/\gamma} \rightarrow \frac{h_i^{Z/\gamma}}{\left(1 + \frac{s}{\Lambda^2}\right)^n}$$

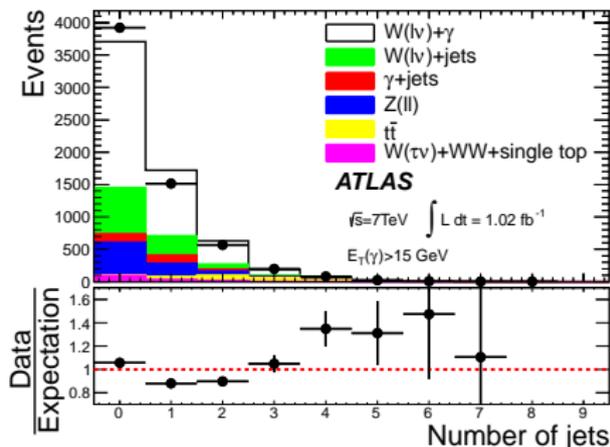
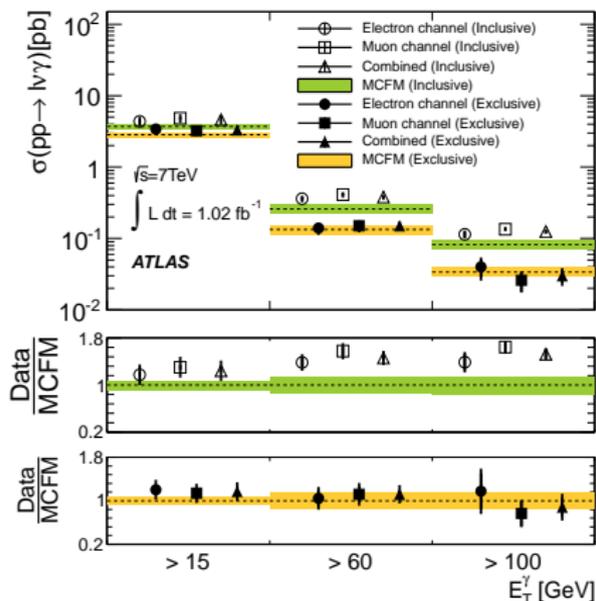


$W\gamma$ measurement (ATLAS 1.02 fb⁻¹, arXiv:1205.2531[hep-ex])



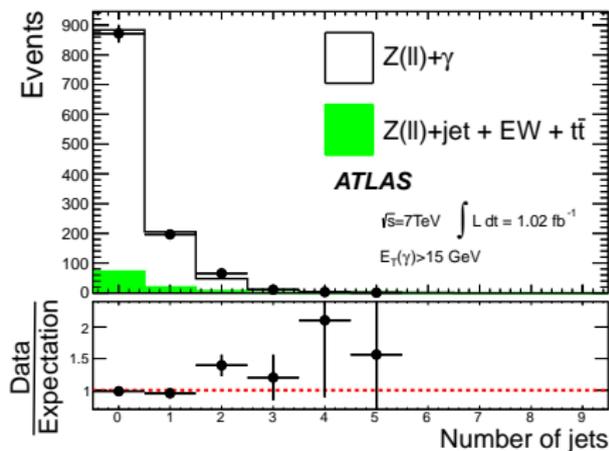
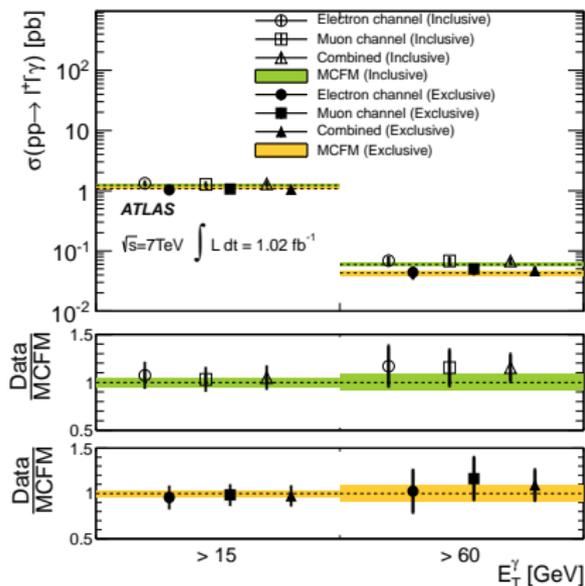
- The measurements are categorized according to p_T^γ : low, intermediate and high- p_T regions.
- Searches divided based on the number of reconstructed jets

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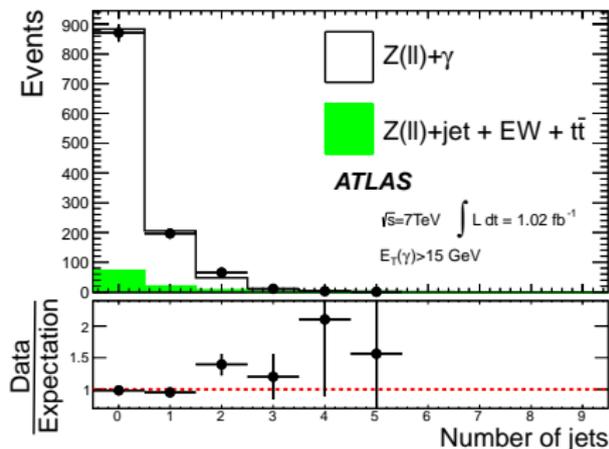
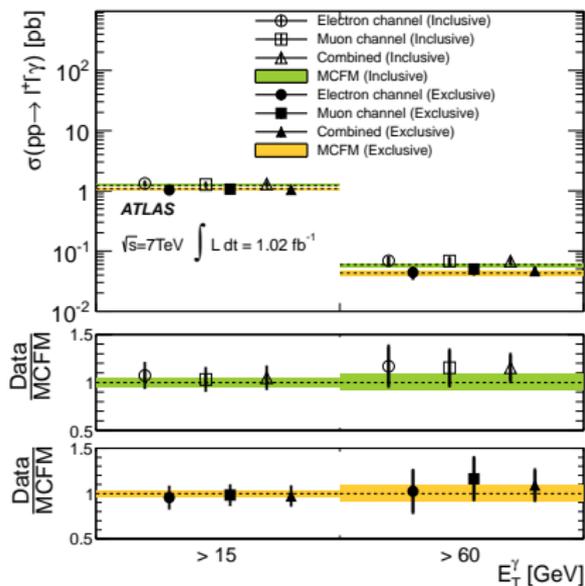
- good agreement between measured cross sections and theoretical predictions for exclusive cross sections
- Inclusive measurements are somewhat higher compare to theoretical predictions

$Z\gamma$ measurement (ATLAS 1.02 fb⁻¹, arXiv:1205.2531[hep-ex])



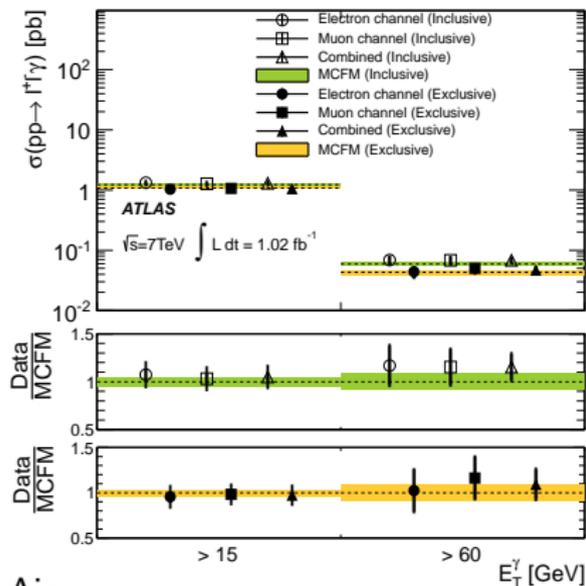
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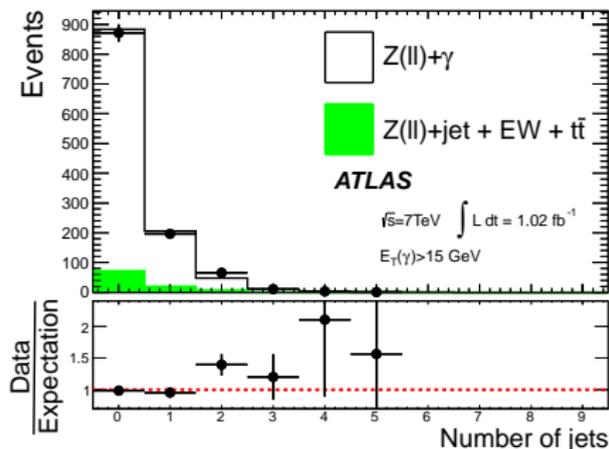
- good agreement between measured cross sections and theoretical predictions
- Note that: uncertainties in exclusive predictions smaller or comparable to that on the inclusive predictions

$Z\gamma$ measurement (ATLAS 1.02 fb⁻¹, arXiv:1205.2531[hep-ex])



Aim:

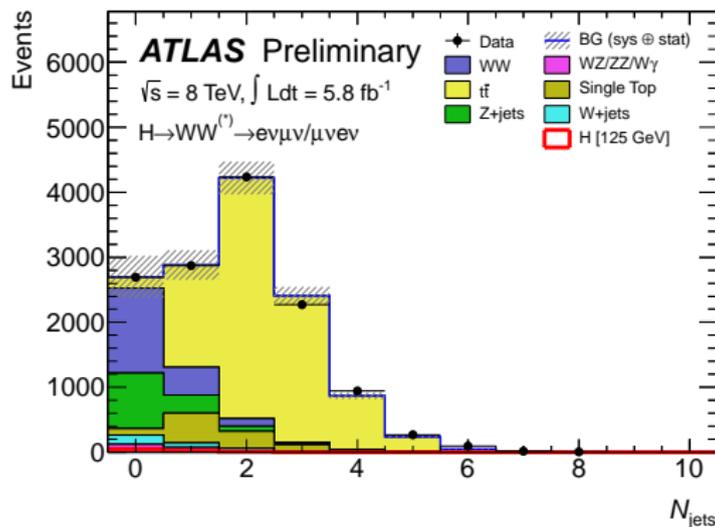
- Reasses the uncertainties for exclusive predictions
- Provide the prediction for 1-jet bin at NLO accuracy (have the $Z\gamma j$, working on $W\gamma j$)



Searches using Jet Bin

Example: Higgs search in WW channel

[ATLAS-CONF-2012-098]



- background composition depend on the number of jets in the final state
- the overall sensitivity can be increased
- How do we estimate theory uncertainties in the presence of jet veto?

Exclusive Cross Section: perturbative uncertainties

Evaluating uncertainties:

[Stewart,Tackmann: arXiv:1107.2117]

- Directly varying the μ_r and μ_f for each σ_N

Potentially underestimate the uncertainties in individual jet bin due to numerical cancellation.

$$\begin{aligned} \sigma_{\text{total}} &\simeq \sigma_B \left[1 + \alpha_s + \alpha_s^2 + \mathcal{O}(\alpha_s^3) \right], & L = \ln(p_T^{\text{cut}}/Q) \\ \sigma_{\geq 1}(p_T^{\text{cut}}) &\simeq \sigma_B \left[\alpha_s(L^2 + L + 1) + \alpha_s^2(L^4 + L^3 + L^2 + L + 1) + \mathcal{O}(\alpha_s^3 L^6) \right] \\ \sigma_0(p_T^{\text{cut}}) &= \sigma_{\text{total}} - \sigma_{\geq 1}(p_T^{\text{cut}}) \end{aligned}$$

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- Combine uncertainties in inclusive N -jet cross section

$$\Delta_0^2 = \Delta_{\text{total}}^2 + \Delta_{\geq 1}^2$$

→ Δ_{total} and $\Delta_{\geq 1}$ are treated as independent

→ takes into account large logarithmic corrections

→ Applied to $H + 0,1$ jets, $WW + 0$ jets, $W + 0,1,2$ jets

Existing calculations:

- NLO prediction for $W\gamma$ and $Z\gamma$
 Ohnemus (1993); Baur, Han, Ohnemus (1998); de Florian, Signer (2000)
 Hollik, Meier (2004); Accomando, Denner, C. Meier (2005)
 Ametller, Gava, Paver, Treleani (1985); van der Bij, Glover (1988)
 Adamson, de Florian, Signer (2003); Campbell, Ellis, Williams (2010)
 (EW corrections, $gg \rightarrow Z\gamma$)
- NLO prediction for $W\gamma j$
 Campanario, Englert, Spannowsky, Zeppenfeld (2009)
- NLO prediction for $Z\gamma\gamma$
 Bozzi, Campanario, Rauch, Zeppenfeld (2011)
- Two-loop QCD helicity amplitudes for $q\bar{q}' \rightarrow W^\pm\gamma$ and $q\bar{q} \rightarrow Z\gamma$
 Gehrmann, Tancredi (2012)

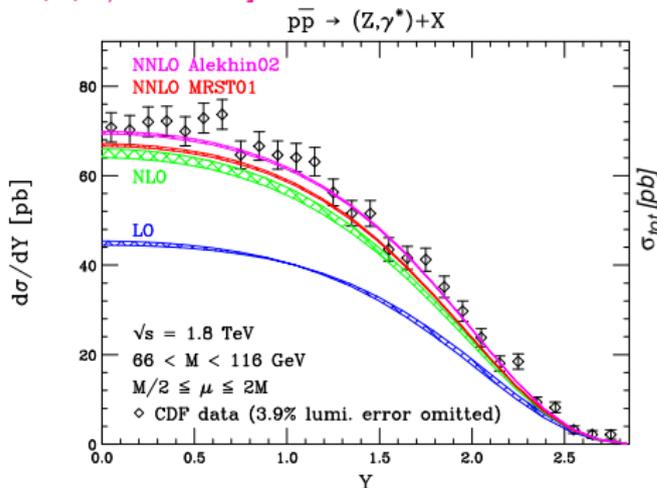
Some Basic Tools

Going Beyond Leading Order

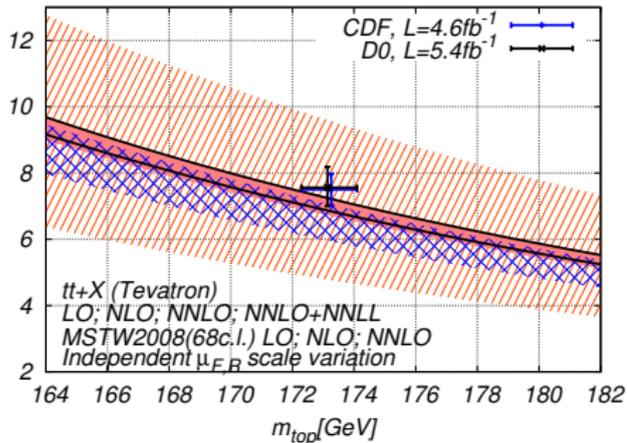
What do we gain?

- reliable prediction for total rates and shape of the distributions
- reduced scale dependence
- test the convergence of the perturbative series

[Anastasiou, Dixon, Melnikov, Petriello:
hep-ph/0312266]



[Baernreuther, Czakon, Mitov:
arXiv:1204.5201]

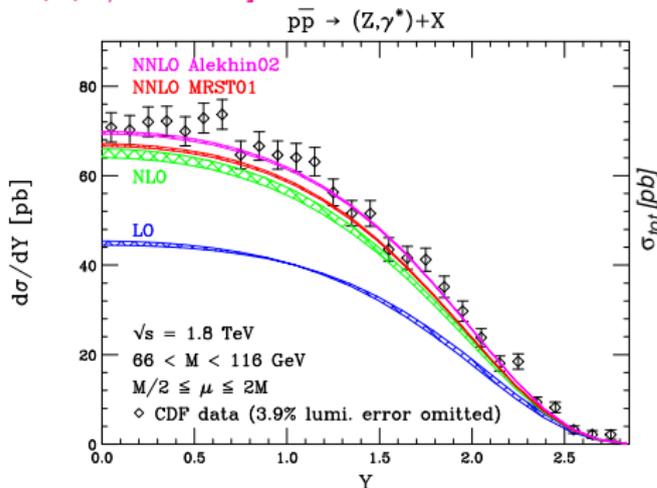


Going Beyond Leading Order

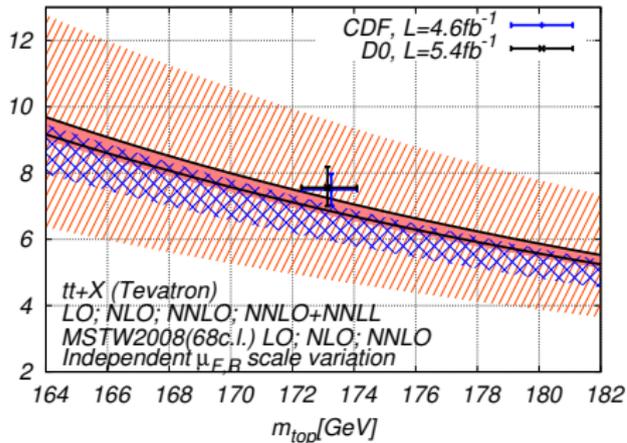
In fixed order calculations, there are some regions of phase space that don't match the data/not well behaved

- Resummation
- Shower MC: NLO+PS

[Anastasiou, Dixon, Melnikov, Petriello:
hep-ph/0312266]



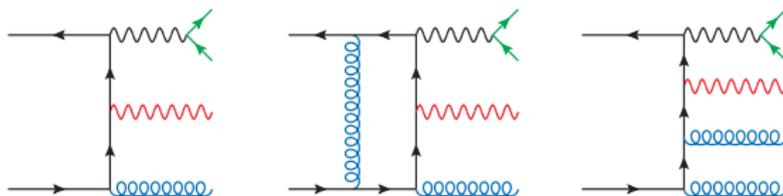
[Baernreuther, Czakon, Mitov:
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NLO calculation (1)

NLO cross section:

$$\sigma^{NLO} = \int_n d\sigma^B + \int_n d\sigma^V + \int_{n+1} d\sigma^R$$



- Virtual corrections contain UV and IR singularities
 Extract the singularities: dimensional regularization, compute loop diagrams in $d = 4 - 2\epsilon$ dimensions.
 Singularities manifest in the $1/\epsilon^2$ and $1/\epsilon$ poles.
 UV singularities are removed by renormalization
- Real corrections suffer from IR singularities when massless partons become soft or collinear

NLO calculation (2)

Subtraction Method

$$\sigma^{NLO} = \int_n d\sigma^B + \int_n \left[d\sigma^V + \int_1 d\sigma^A \right]_{\epsilon=0} + \int_{n+1} \left[d\sigma_{\epsilon=0}^R - d\sigma_{\epsilon=0}^A \right] + \int_n d\sigma^C$$

[Catani,Seymour]

- $d\sigma^A$ composed from the underlying Born process $d\sigma^B$ and the dipoles dV_{dipole} by summing over all possible dipole contributions

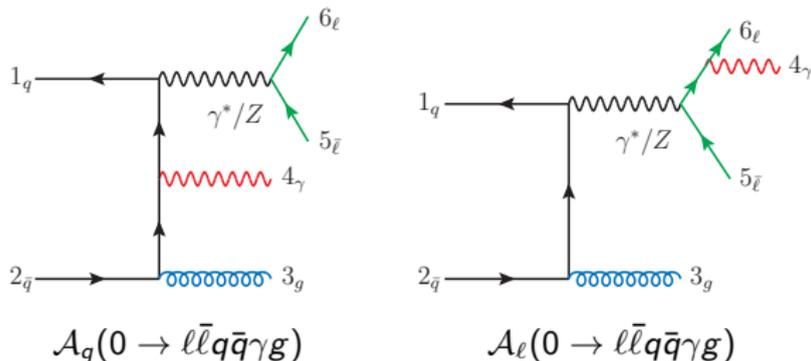
$$d\sigma^A = \sum_{\text{dipole}} d\sigma^B \otimes dV_{\text{dipole}}$$

- Each dipole cancels the singularity at a particular kinematic region
- $d\sigma^A$ has the same singular behavior as $d\sigma^R$ at each PS point

- $d\sigma^A$ exactly integrable analytically over one-parton PS in d -dim
 ⇒ has to be simple functions

After analytically integrated over 1-parton PS in $d = 4 - 2\epsilon$ dimensions, the IR singularities manifest in $1/\epsilon^2$ and $1/\epsilon$ poles.

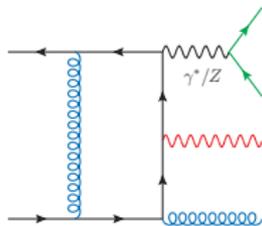
Z γ +jet: Calculation

Z γ j production at LO

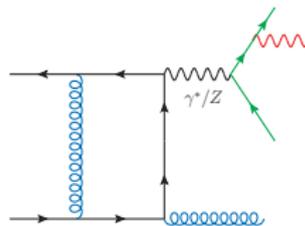
- Two separately gauge invariant classes of diagrams:
 - γ from quark line (“q-type”)
 - γ from lepton line (“l-type”)
- **only** q-type diagrams for neutrino final state
- Matrix elements are computed using spinor helicity formalism
- Checked against MadGraph/MadEvent

Zγj production: $\mathcal{O}(\alpha_s)$ virtual correction

→ self energy, vertex, box and pentagon one-loop corrections



$$A_q(0 \rightarrow \ell \bar{\ell} q \bar{q} \gamma g)$$



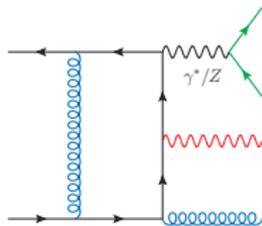
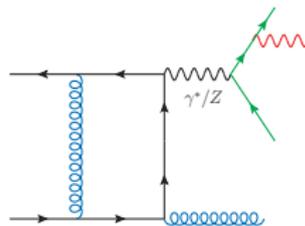
$$A_\ell(0 \rightarrow \ell \bar{\ell} q \bar{q} \gamma g)$$

Decomposition of one-loop amplitude:

$$\begin{aligned}
 A^{(1)}(1_q, 2_{\bar{q}}, 3_g, 4_\gamma, 5_{\bar{\ell}}, 6_\ell) &= 2\sqrt{2}e^3 g_s^3 c_F T_{i_1 i_2}^{a_3} \times \left\{ \begin{aligned}
 &Q_q \left(-Q_q + v_{L,R}^q v_{L,R}^\ell \mathcal{P}_Z(s_{56}) \right) \mathcal{A}_{q;1}^{(1)}(1_q, 2_{\bar{q}}, 3_g, 4_\gamma, 5_{\bar{\ell}}, 6_\ell) \\
 &+ Q_q \sum_{i=1}^{n_f} \left(-Q_i + \frac{1}{2} v_{L,R}^\ell (v_L^i + v_R^i) \mathcal{P}_Z(s_{56}) \right) \mathcal{A}_{q;2}^{(1)}(1_q, 2_{\bar{q}}, 3_g, 4_\gamma, 5_{\bar{\ell}}, 6_\ell) \\
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Zγj production: $\mathcal{O}(\alpha_s)$ virtual correction

→ self energy, vertex, box and pentagon one-loop corrections


 $\mathcal{A}_q(0 \rightarrow \ell \bar{\ell} q \bar{q} \gamma g)$

 $\mathcal{A}_\ell(0 \rightarrow \ell \bar{\ell} q \bar{q} \gamma g)$

Decomposition of one-loop amplitude:

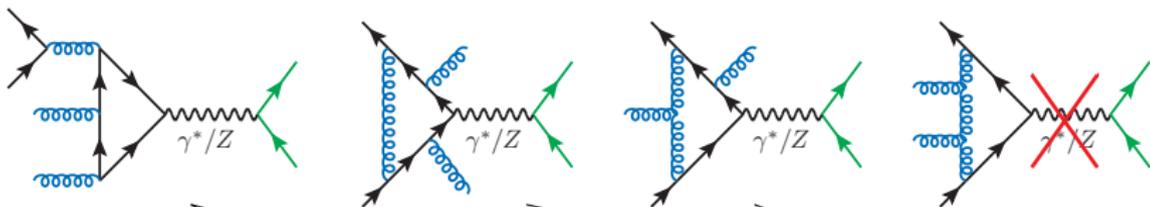
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 \end{aligned}$$



Zγj production: $\mathcal{O}(\alpha_s)$ virtual correction

$\mathcal{A}_q(0 \rightarrow \ell\bar{\ell}q\bar{q}\gamma\gamma)$ are obtained from $e^+e^- \rightarrow q\bar{q}gg$ one-loop amplitudes

[Bern,Dixon,Kosower:hep-ph/9708239]

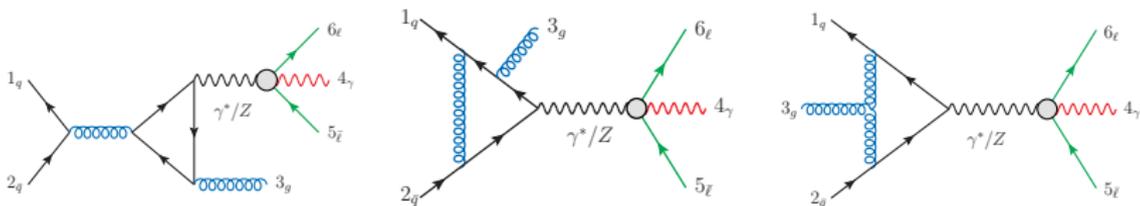


Decomposition of the one-loop amplitude:

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 \end{aligned}$$

Zγj production: $\mathcal{O}(\alpha_s)$ virtual correction

Need to compute $\mathcal{A}_\ell(0 \rightarrow \ell\bar{\ell}q\bar{q}\gamma g)$



Decomposition of the one-loop amplitude:

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 \end{aligned}$$

Interlude: Spinor Helicity Formalism

For massless four-vector p_i , define spinor products:

$$\langle ij \rangle = \bar{u}_-(p_i) u_+(p_j), \quad [ij] = \bar{u}_+(p_i) u_-(p_j), \quad \langle ij \rangle [ji] = 2p_i \cdot p_j.$$

where

$$u_+(p) = P_R u(p) \quad u_-(p) = P_L u(p)$$

Spinor sandwiches

$$\langle i | m \cdots n | j \rangle = \bar{u}_-(p_i) \not{p}_m \cdots \not{p}_n u_-(p_j) \quad (\text{odd \# of } p)$$

$$\langle i | m \cdots n | j \rangle = \bar{u}_-(p_i) \not{p}_m \cdots \not{p}_n u_+(p_j) \quad (\text{even \# of } p)$$

$$[i | m \cdots n | j] = \bar{u}_+(p_i) \not{p}_m \cdots \not{p}_n u_-(p_j) \quad (\text{even \# of } p)$$

Polarization vectors

$$\epsilon_+^\mu(k, q) = \frac{\langle q | \gamma^\mu | k \rangle}{\sqrt{2} \langle qk \rangle}, \quad \epsilon_-^\mu(k, q) = \frac{[q | \gamma^\mu | k]}{\sqrt{2} [qk]}.$$

Useful relations

$$\langle ij \rangle = -\langle ji \rangle, \quad [ij] = -[ji], \quad \langle ii \rangle = 0, \quad [ii] = 0$$

$$\not{p}_i = |i\rangle \langle i| + |i\rangle [i|$$

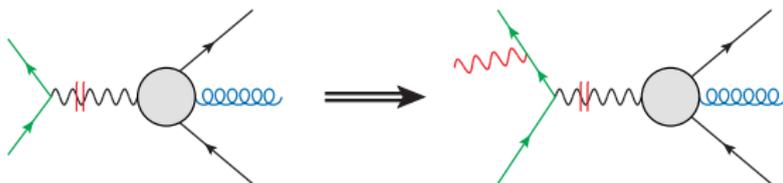
$$\langle i | \gamma_\mu | j \rangle \langle k | \gamma^\mu | l \rangle = 2 \langle ik \rangle [lj] \quad (\text{Fierz id.})$$

$$\langle ij \rangle \langle kl \rangle + \langle ik \rangle \langle lj \rangle + \langle il \rangle \langle jk \rangle = 0 \quad (\text{Schouten id.})$$

Work with $\mathcal{A}(\langle ij \rangle, [ij])$ instead of $|\mathcal{A}|^2(p_i \cdot p_j)$.

$$\mathcal{A}_\ell(0 \rightarrow \ell\bar{\ell}q\bar{q}\gamma g):$$

Replace lepton current in $e^+e^- \rightarrow q\bar{q}g$ 1-loop amplitudes by $\ell\bar{\ell}\gamma$ current.



$$\mathcal{M} = L_\mu^{e^+e^-} V^\mu \quad \rightarrow \quad L_\mu^{\gamma e^+e^-} V^\mu$$

→ applies to tree and virtual amplitudes

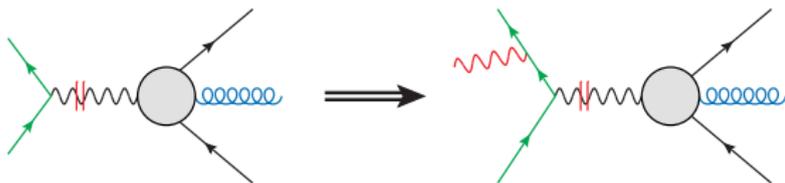
Example at tree level:

$$J_{\ell\bar{\ell}}^\mu(5_\ell^-, 6_\ell^+) = -\frac{\langle 5|\gamma^\mu|6\rangle}{s_{56}}$$

$$\mathcal{A}_q^{(0)}(1_q^+, 2_{\bar{q}}^-, 3_g^+, 5_\ell^-, 6_\ell^+) = -i \frac{\langle 25\rangle^2}{\langle 13\rangle \langle 23\rangle \langle 56\rangle}$$

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then use

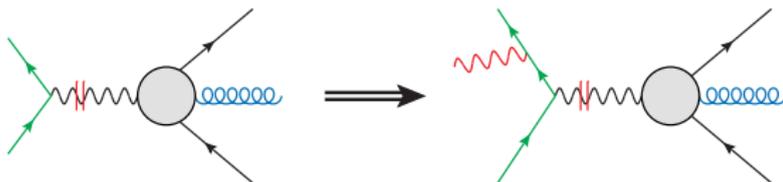
$$\langle 56\rangle [65] = s_{56}$$

$$\langle 25\rangle [56] = \langle 2|5|6\rangle \quad \text{from } |5\rangle\langle 5| + |5\rangle[5] = \not{p}_5$$

$$= -\langle 2|(1+3)|6\rangle \quad \text{mom. conservation}$$

$$\mathcal{A}_\ell(0 \rightarrow \ell\bar{\ell}q\bar{q}\gamma g):$$

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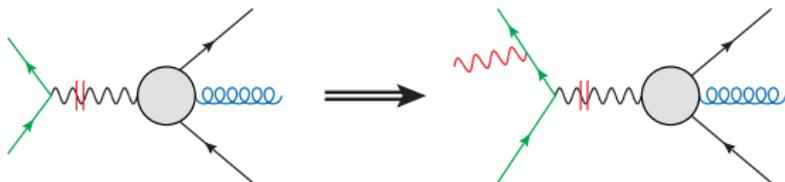
→ applies to tree and virtual amplitudes

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→ applies to tree and virtual amplitudes

Example at tree level:

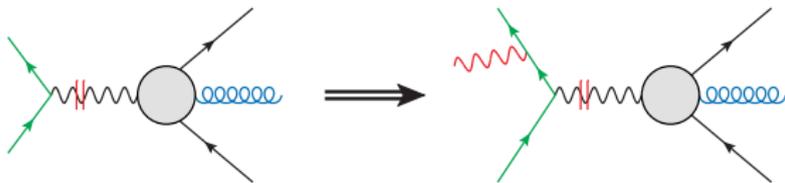
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undo the Fierz identity

$$\langle ik \rangle [lj] = \frac{1}{2} \langle i|\gamma_\mu|j\rangle \langle k|\gamma^\mu|l\rangle$$

$$\mathcal{A}_\ell(0 \rightarrow \ell\bar{\ell}q\bar{q}\gamma g):$$

Replace lepton current in $e^+e^- \rightarrow q\bar{q}g$ 1-loop amplitudes by $\ell\bar{\ell}\gamma$ current.



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→ applies to tree and virtual amplitudes

Example at tree level:

$$\begin{aligned} \mathcal{A}_q^{(0)}(1_q^+, 2_{\bar{q}}^-, 3_g^+, 5_{\bar{\ell}}^-, 6_\ell^+) &= -i \frac{\langle 25 \rangle^2}{\langle 13 \rangle \langle 23 \rangle \langle 56 \rangle} \\ &= -i \frac{\langle 2 | (1+3) | 6 \rangle \langle 25 \rangle}{\langle 13 \rangle \langle 23 \rangle s_{56}} \\ &= i \frac{\langle 2 | (1+3) | \gamma_\mu | 2 \rangle}{2 \langle 13 \rangle \langle 23 \rangle} \times \left(-\frac{\langle 5 | \gamma^\mu | 6 \rangle}{s_{56}} \right) \\ &= \tilde{\mathcal{A}}_\mu(1_q^+, 2_{\bar{q}}^-, 3_g^+) \times J_{\ell\bar{\ell}}^\mu(5_{\bar{\ell}}^-, 6_\ell^+) \end{aligned}$$

Currents with photon radiation from leptons

$$J_{\ell\bar{\ell}\gamma}^{\mu}(4_{\gamma}^{+}, 5_{\bar{\ell}}^{-}, 6_{\ell}^{+}) = \frac{\langle 5|\gamma^{\mu}|(4+6)|5\rangle}{t_{456} \langle 45\rangle \langle 46\rangle}$$

$$J_{\ell\bar{\ell}\gamma}^{\mu}(4_{\gamma}^{-}, 5_{\bar{\ell}}^{-}, 6_{\ell}^{+}) = \frac{[6|\gamma^{\mu}|(4+5)|6]}{t_{456} [45] [46]}$$

Currents with photon radiation from leptons

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$$J_{\ell\bar{\ell}\gamma}^{\mu}(4_{\gamma}^{-}, 5_{\bar{\ell}}^{-}, 6_{\ell}^{+}) = \frac{\langle 6|\gamma^{\mu}|(4+5)|6\rangle}{t_{456} [45] [46]}$$

Compute $\mathcal{A}_{\ell}^{(0)}(1_q, 2_{\bar{q}}, 3_g, 4_{\gamma}, 5_{\bar{\ell}}, 6_{\ell})$

$$\begin{aligned} \mathcal{A}_{\ell}^{(0)}(1_q^{+}, 2_{\bar{q}}^{-}, 3_g^{+}, 4_{\gamma}^{+}, 5_{\bar{\ell}}^{-}, 6_{\ell}^{+}) &= \tilde{\mathcal{A}}_{\mu}(1_q^{+}, 2_{\bar{q}}^{-}, 3_g^{+}) \times J_{\ell\bar{\ell}\gamma}^{\mu}(4_{\gamma}^{+}, 5_{\bar{\ell}}^{-}, 6_{\ell}^{+}) \\ &= i \frac{\langle 2|(1+3)|\gamma_{\mu}|2\rangle}{2 \langle 13\rangle \langle 23\rangle} \frac{\langle 5|\gamma^{\mu}|(4+6)|5\rangle}{t_{456} \langle 45\rangle \langle 46\rangle} \\ &= i \frac{\langle 25\rangle^2}{\langle 13\rangle \langle 23\rangle \langle 45\rangle \langle 46\rangle} \end{aligned}$$

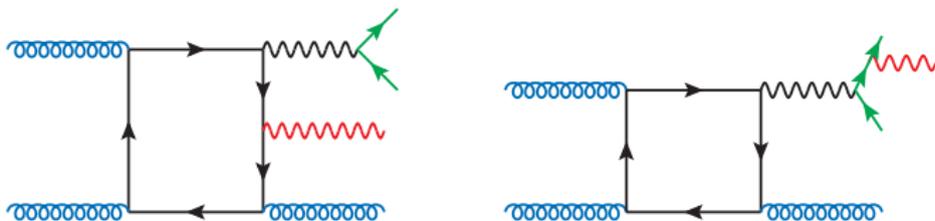
→ analytic expression for $\mathcal{A}_{\ell}(0 \rightarrow \ell\bar{\ell}q\bar{q}\gamma g)$.

$$\mathcal{A}_{\ell}^{(1)}(1_q^{+}, 2_{\bar{q}}^{-}, 3_g^{+}, 4_{\gamma}^{+}, 5_{\bar{\ell}}^{-}, 6_{\ell}^{+})$$

$$\mathcal{A}_{\ell}^{(1)}(1_q^{+}, 2_{\bar{q}}^{-}, 3_g^{+}, 4_{\gamma}^{-}, 5_{\bar{\ell}}^{-}, 6_{\ell}^{+})$$

- Renormalization to cancel UV singularities.
- IR singularities cancelled by corresponding singularities from the real part.
- Pole cancellations are checked numerically.

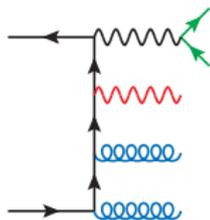
What we don't include: virtual $gg \rightarrow Z\gamma g$



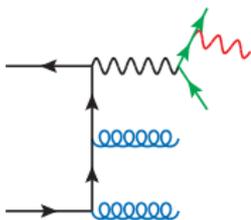
Formally NNLO correction $\mathcal{O}(\alpha^3\alpha_s^3)$

[Agarwal, Shivaji: arXiv:1207.2927]

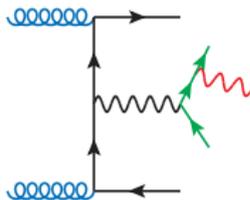
- On-shell Z-boson, no decay to leptons
- Contribute $\sim 2\%$

Z γ j production: $\mathcal{O}(\alpha_s)$ real correction

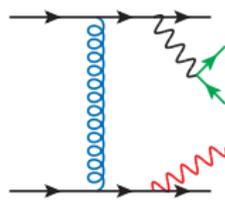
$$\mathcal{A}_q(0 \rightarrow \ell\bar{\ell}q\bar{q}\gamma gg)$$



$$\mathcal{A}_\ell(0 \rightarrow \ell\bar{\ell}q\bar{q}\gamma gg)$$



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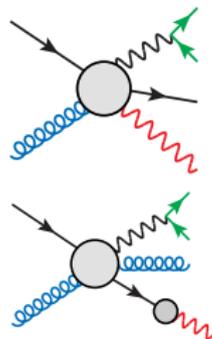
$$\mathcal{A}_q(0 \rightarrow \ell\bar{\ell}q\bar{q}Q\bar{Q}\gamma)$$

- Tree level contributions open up at $\mathcal{O}(\alpha^3\alpha_s^2)$:
 - gg initial state
 - $qq, \bar{q}\bar{q}$ initial state from 4 quarks amplitude
- \mathcal{A}_q helicity amplitudes from $e^+e^- \rightarrow q\bar{q}ggg$ and $e^+e^- \rightarrow q\bar{q}Q\bar{Q}g$
 [Nagy, Trocsanyi:hep-ph/9806317]
- Need to compute \mathcal{A}_ℓ
- Cross checked against MadGraph/MadEvent
- Dipole subtraction to cancel soft and collinear singularities

Photon isolation and fragmentation

Production of photons:

- Prompt photons:
 - \Rightarrow photons **directly** produced from hard scattering:
 - \Rightarrow photons from **fragmentation** of QCD partons:



Probability for a parton i to fragment into a photon: $D_{i \rightarrow \gamma}(z, M_F)$
 Photon FFs must be extracted from data due to their non-perturbative nature

- Secondary photon: hadronic activities (e.g. $\pi^0 \rightarrow \gamma\gamma$)
 Removed by isolation cuts

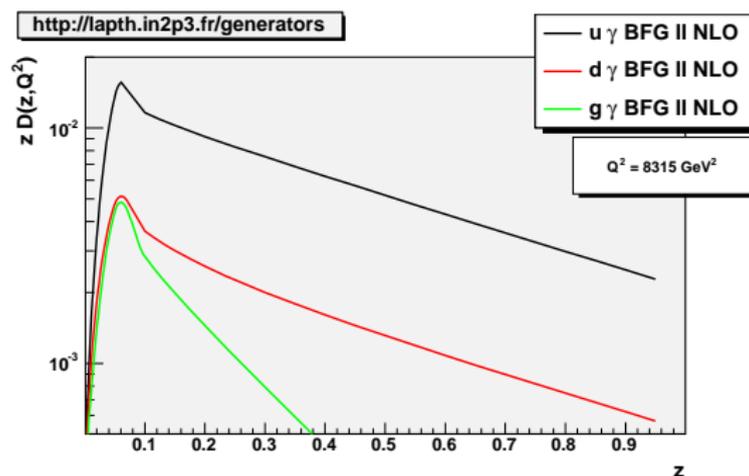
$$\sum_{\in R_0} E_T(\text{had}) < E_T^{\text{max}} \text{ with } R_0 = \sqrt{\Delta\phi^2 + \Delta\eta^2}$$

Photon Fragmentation Functions

- BFG (set I and II)
- GdRG

[Bourhis,Fontannaz,Guillet:hep-ph/9704447]

[Gehrmann-De Ridder,Glover:hep-ph/9806316]



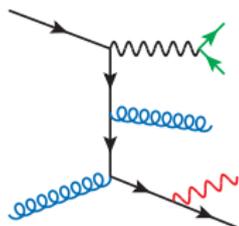
$z \rightarrow$ fraction of parton momentum that is carried by the photon

FFs dominant in the low z region

After isolation cut, z is typically large

\rightarrow Isolation drops the fragmentation contribution substantially

Quark-photon FS collinear singularities

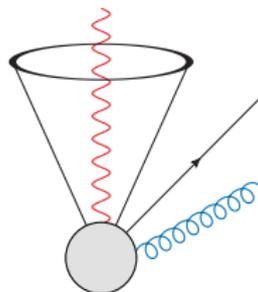
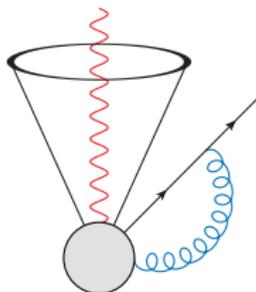


Impose photon-jet separation cut
to remove singularities

$$R(\gamma, j) > R_{\min}$$

→ OK at LO

→ What about NLO?



Naive separation cut between photon and jet restrict the gluon phase space,
thus spoils IR cancellations.

- Absorb the singularities into photon FFs.

→ Using variant of CS dipole subtraction method

[Catani,Fontannaz,Guillet,Pilon:hep-ph/0204023]

→ Integral of subtraction terms has the form

$$D_q^\gamma = -\frac{1}{\epsilon} \frac{\Gamma(1-\epsilon)}{\Gamma(1-2\epsilon)} \left(\frac{4\pi\mu^2}{M_F^2} \right)^\epsilon \frac{\alpha}{2\pi} Q_q^2 P_{\gamma q}(z)$$

→ Perform isolation in an IR-safe way

The NLO cross section:

$$\sigma_{NLO}^\gamma = \sigma_{NLO,direct}^\gamma(M_F) + \int_0^1 dz \sum_a \sigma_f^a D_{a \rightarrow \gamma}(z, M_F)$$

$M_F \Rightarrow$ Fragmentation Scale

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$M_F \Rightarrow$ Fragmentation Scale

- Frixione's smooth cone isolation

[Frixione:hep-ph/9801442]

$$\sum_{\text{had}} E_T^{\text{had}} \theta(R - R_{\text{had},\gamma}) < \epsilon_h E_T^\gamma \left(\frac{1 - \cos R}{1 - \cos R_0} \right)^n \quad \text{for all } R \leq R_0$$

→ Soft radiation is allowed inside the cone but collinear singularities are removed

→ Remove fragmentation contributions

→ Useful for theoretical calculation, difficult to implement experimentally

MCFM (<http://mcfm.fnal.gov>)

- MCFM = Monte Carlo for FeMtobarn processes
- parton level Monte Carlo program (with NLO accuracy) written in Fortran
 - ⇒ “one-stop shopping” for many NLO predictions.
 - ⇒ Latest version: v6.3, August 2012
- Authors: [J. Campbell](#), [R. K. Ellis](#), [C. Williams](#)
- Includes SM processes involving γ , W , Z + jets, top quarks, Higgs.
- Decays of unstable particles are included, maintaining spin correlations and (sometimes) including NLO effects.
- Anomalous couplings for $W\gamma$ and $Z\gamma$ processes.
- **Photon fragmentation** and realistic isolation included.
- Cross sections and **differential distributions**, flexible cuts.
- Analytic **helicity amplitudes** calculated from scratch or taken from literature.
- Slightly-modified implementation of Catani-Seymour **dipole subtraction**

Z γ +jet: Results

Setup

Standard Cuts:

Photon : $|\eta_\gamma| < 2.37, R_{\ell\gamma} > 0.7,$

$p_T^\gamma > 15$ GeV (low- p_T),

$p_T^\gamma > 60$ GeV (intermediate- p_T),

$p_T^\gamma > 100$ GeV (high- p_T).

$R_0 = 0.3$ and $E_T^{\max} = 6$ GeV (isolation).

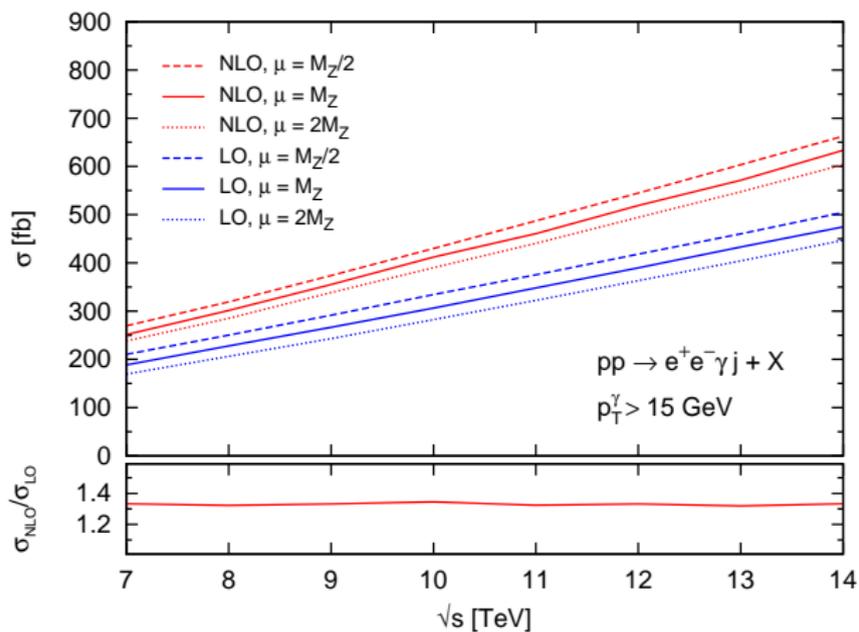
Leptons : $m_{\ell\ell} > 40$ GeV, $p_T^\ell > 25$ GeV, $|\eta_\ell| < 2.47, R_{\ell j} > 0.6,$
 $E_T^{\text{miss}} > 25$ GeV.

Jets : $p_T^j > 30$ GeV, $|y_j| < 4.4,$ k_T algorithm with $R = 0.4$.

Scale: $\mu_r = \mu_f = M_F = M_Z$

PDFs: CTEQ6L1 for LO, CT10 for NLO

Photon FFs: BFG set II

Z γ j inclusive cross section vs LHC operating energy.

Exclusive cross section: $pp \rightarrow e^+ e^- \gamma + (0,1) \text{ jet}$

Evaluating uncertainties:

[Stewart,Tackmann: arXiv:1107.2117]

- Directly varying the μ_r and μ_f for each σ_N

Potentially underestimate the uncertainties in individual jet bin due to numerical cancellation.

$$\begin{aligned}\sigma_{\text{total}} &\simeq \sigma_B \left[1 + \alpha_s + \alpha_s^2 + \mathcal{O}(\alpha_s^3) \right], & L = \ln(p_T^{\text{cut}}/Q) \\ \sigma_{\geq 1}(p_T^{\text{cut}}) &\simeq \sigma_B \left[\alpha_s(L^2 + L + 1) + \alpha_s^2(L^4 + L^3 + L^2 + L + 1) + \mathcal{O}(\alpha_s^3 L^6) \right] \\ \sigma_0(p_T^{\text{cut}}) &= \sigma_{\text{total}} - \sigma_{\geq 1}(p_T^{\text{cut}})\end{aligned}$$

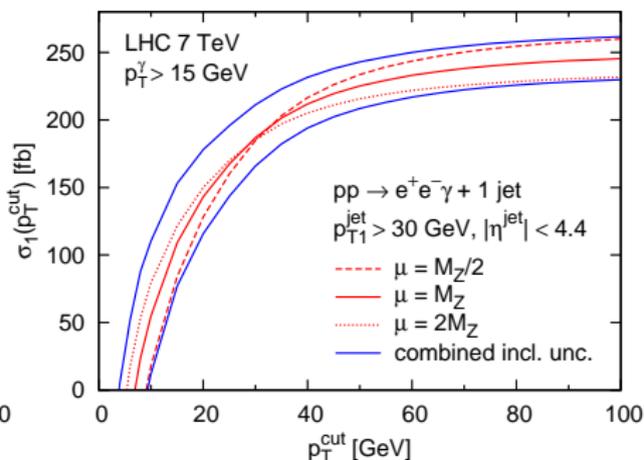
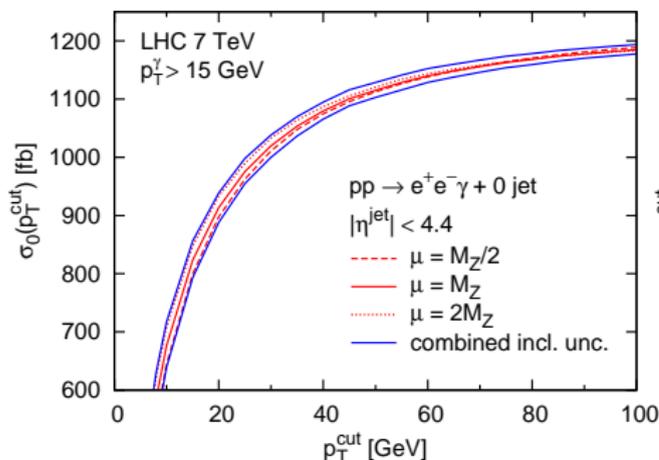
- Combine uncertainties in inclusive N -jet cross section

$$\Delta_0^2 = \Delta_{\text{total}}^2 + \Delta_{\geq 1}^2, \quad \Delta_1^2 = \Delta_{\geq 1}^2 + \Delta_{\geq 2}^2$$

→ Δ_{total} and $\Delta_{\geq 1}$ are treated as independent

→ takes into account large logarithmic corrections

→ Applied to $H + 0,1$ jets, $WW + 0$ jets, $W + 0,1,2$ jets

Exclusive cross section: $pp \rightarrow e^+ e^- \gamma + (0,1) \text{ jet}$ 

$e^+ e^- \gamma + (0,1) \text{ jets: } (p_T^{\text{jet}} \geq 30 \text{ GeV})$

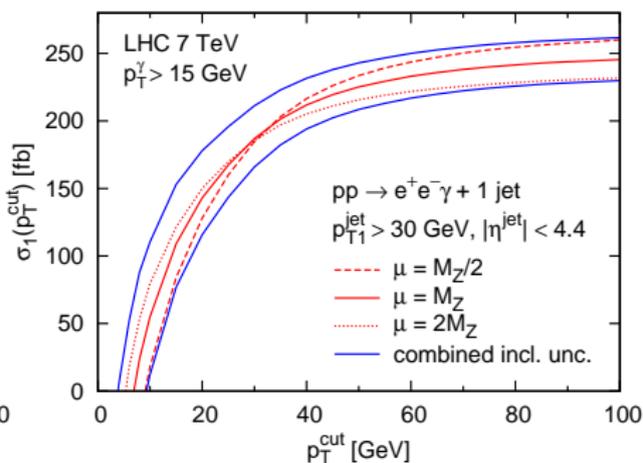
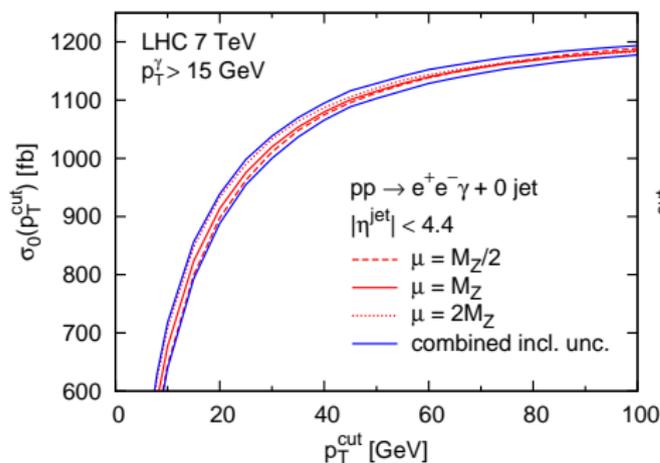
$$\delta(\sigma_{\text{tot}}) = \begin{matrix} +0.7\% \\ -0.5\% \end{matrix}, \quad \delta(\sigma_{\geq 1}) = \begin{matrix} +7.4\% \\ -5.2\% \end{matrix}, \quad \delta(\sigma_{\geq 2}) = \begin{matrix} +28.0\% \\ -21.6\% \end{matrix}$$

$$\delta(\sigma_0) = \begin{matrix} +1.8\% \\ -1.9\% \end{matrix}, \quad \delta(\sigma_1) = \begin{matrix} +13.0\% \\ -11.2\% \end{matrix}$$

$$\delta(\sigma_0) = \begin{matrix} +1.3\% \\ -0.9\% \end{matrix}, \quad \delta(\sigma_1) = \begin{matrix} -0.8\% \\ -1.2\% \end{matrix}$$

(combined incl. uncertainties)

(direct scale variation)

Exclusive cross section: $pp \rightarrow e^+ e^- \gamma + (0,1) \text{ jet}$ 

$e^+ e^- \gamma + 1 \text{ jet}: (\mu = M_Z)$

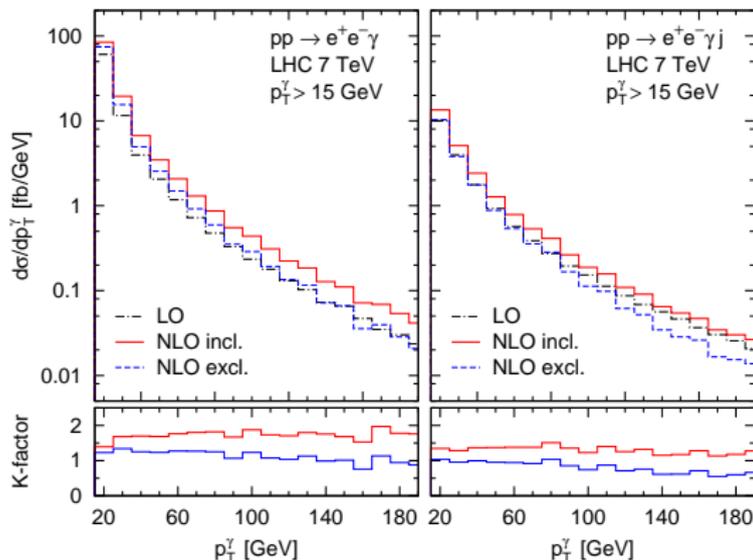
$$\sigma_{\geq 1}(p_{T1}^{\text{jet}} \geq 30 \text{ GeV}) = (188 \text{ fb})[1 + 2.89\alpha_s + \mathcal{O}(\alpha_s^2)]$$

$$\sigma_{\geq 2}(p_{T1,2}^{\text{jet}} \geq 30 \text{ GeV}) = (188 \text{ fb})[2.93\alpha_s + \mathcal{O}(\alpha_s^2)]$$

$$\sigma_1(p_{T1,2}^{\text{jet}} \geq 30 \text{ GeV}) = \sigma_{\geq 1}(p_{T1}^{\text{jet}} \geq 30 \text{ GeV}) - \sigma_{\geq 2}(p_{T1,2}^{\text{jet}} \geq 30 \text{ GeV})$$

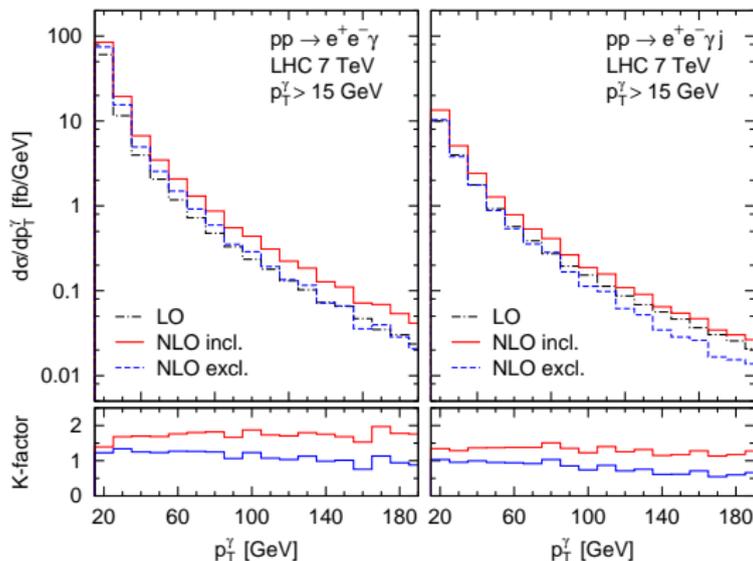
→ sizeable numerical cancellation for α_s term

Photon p_T distributions



- deviation from the SM prediction may indicate the presence of anomalous couplings
- searches in MET+photon channel use photon as a probe (e.g. DM production at colliders)

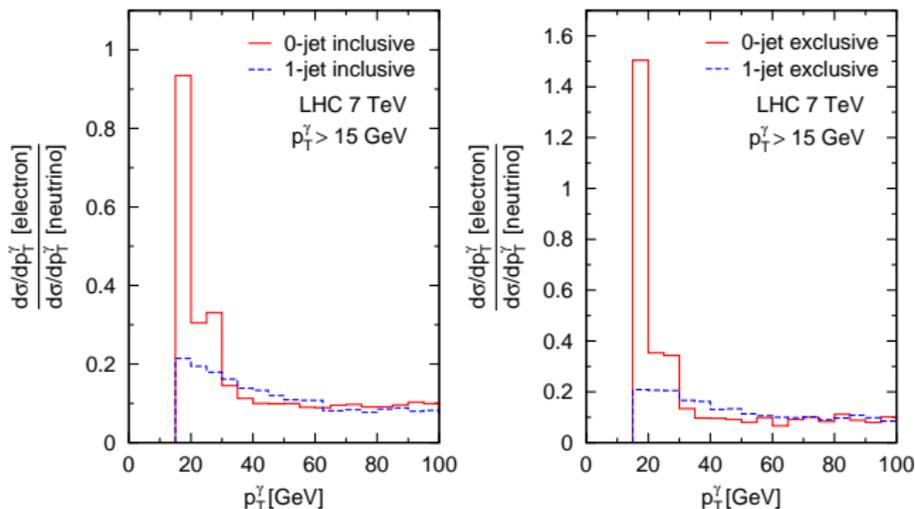
Photon p_T distributions



- Increased K factor for 0-jet inclusive but smaller and flatter for 0-jet exclusive, 1-jet inclusive and exclusive.

Photon p_T distributions

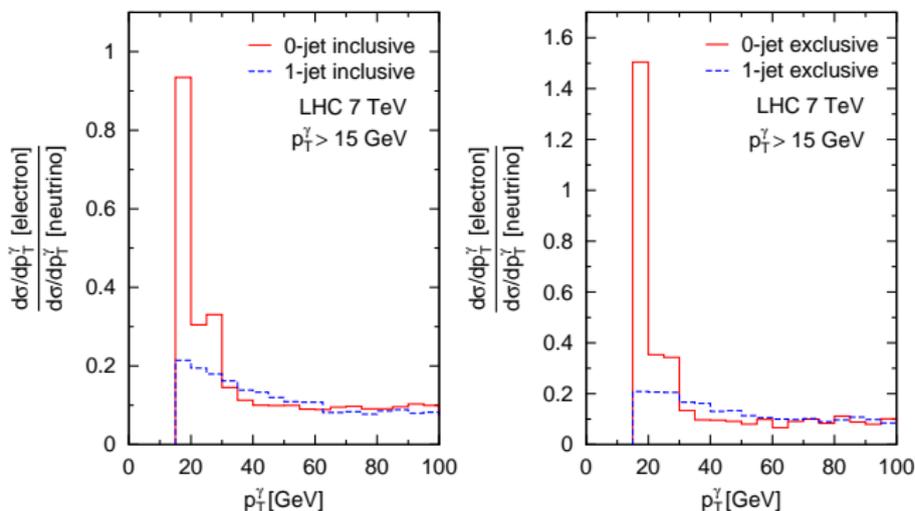
Ratio of p_T distributions between electron and neutrino final state



- In SM the ratio is sensitive to photon radiated from leptons
- Expect cancellation of some systematic errors in experiment
- Sensitive to models that modify the spectrum in one of the channels
 - ⇒ DM scenarios → only MET+photon channel is modified
 - ⇒ Anomalous couplings → both channel are modified

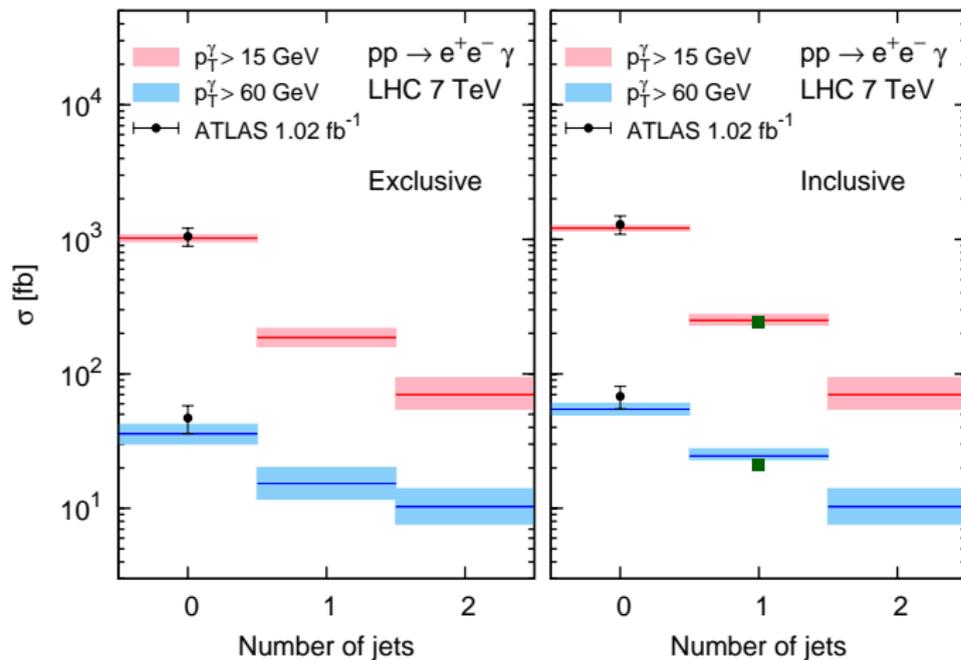
Photon p_T distributions

Ratio of p_T distributions between electron and neutrino final state



- Strong peak in the 0-jet ratio \rightarrow soft photon from FS leptons
- This peak is diminished in 1-jet ratio: hard jet that balances the Z-boson
- The tail of the ratio tends to a constant.
Smaller than $\text{BR}(Z \rightarrow e^+e^-)/\text{BR}(Z \rightarrow 3\nu\bar{\nu}) \sim 1/6$ due to selection cuts

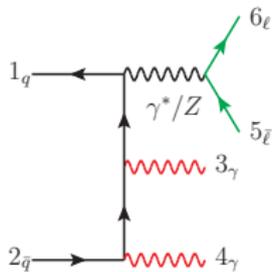
MCFM at Work



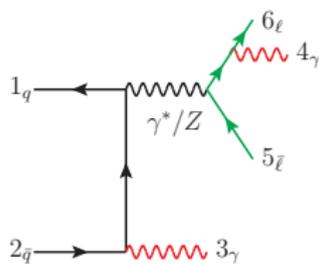
Theoretical uncertainties include: scale variation, PDFs and photon fragmentation.

Z $\gamma\gamma$: Calculation

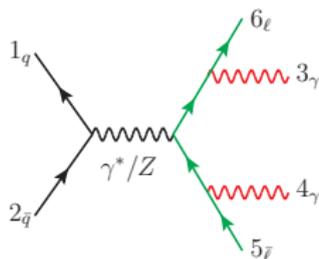
Zγγ production at LO



$$\mathcal{A}_{qq}(0 \rightarrow \bar{l}l q \bar{q} \gamma \gamma)$$



$$\mathcal{A}_{q\ell}(0 \rightarrow \bar{l}l q \bar{q} \gamma \gamma)$$



$$\mathcal{A}_{\ell\ell}(0 \rightarrow \bar{l}l q \bar{q} \gamma \gamma)$$

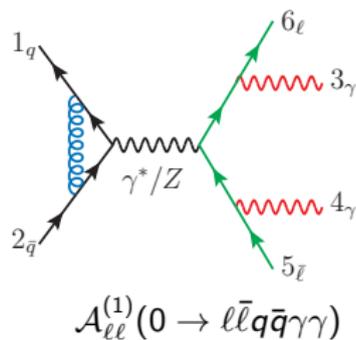
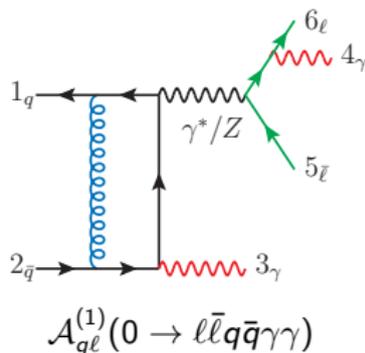
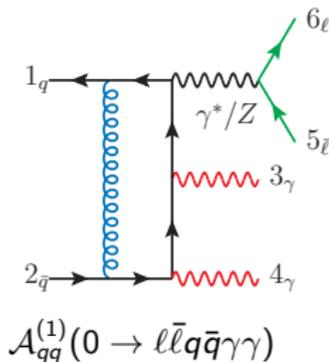
- Three separately gauge invariant classes of diagrams:
 - both photons from quark line (“qq-type”)
 - 1 photon from each line (“ql-type”)
 - both photons from lepton line (“ll-type”)
- **only** qq-type diagrams for neutrino final state
- LO amplitudes:

$$\mathcal{A}_{qq}^{(0)}(1_q, 2_{\bar{q}}, 3_\gamma, 4_\gamma, 5_{\bar{\ell}}, 6_\ell) = \mathcal{A}_q^{(0)}(1_q, 2_{\bar{q}}, 3_g, 4_\gamma, 5_{\bar{\ell}}, 6_\ell)$$

$$\mathcal{A}_{q\ell}^{(0)}(1_q, 2_{\bar{q}}, 3_\gamma, 4_\gamma, 5_{\bar{\ell}}, 6_\ell) = \mathcal{A}_\ell^{(0)}(1_q, 2_{\bar{q}}, 3_g, 4_\gamma, 5_{\bar{\ell}}, 6_\ell)$$

$$\mathcal{A}_{\ell\ell}^{(0)}(1_q, 2_{\bar{q}}, 3_\gamma, 4_\gamma, 5_{\bar{\ell}}, 6_\ell) = \mathcal{A}_{qq}^{(0)}(6_\ell, 5_{\bar{\ell}}, 3_\gamma, 4_\gamma, 2_{\bar{q}}, 1_q)$$

Zγγ production: $\mathcal{O}(\alpha_s)$ virtual correction



- Virtual amplitudes:

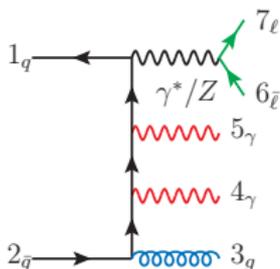
$$\mathcal{A}_{q\bar{q}}^{(1)}(1_q, 2_{\bar{q}}, 3_\gamma, 4_\gamma, 5_{\bar{\ell}}, 6_\ell) = A_6(1_q, 2_{\bar{q}}, 3, 4) + A_6(1_q, 2_{\bar{q}}, 4, 3)$$

$$\mathcal{A}_{q\bar{\ell}}^{(1)}(1_q, 2_{\bar{q}}, 3_\gamma, 4_\gamma, 5_{\bar{\ell}}, 6_\ell) = -A_\ell^{\text{sl}}(1_q, 2_{\bar{q}}, 3_g, 4_\gamma, 5_{\bar{\ell}}, 6_\ell)$$

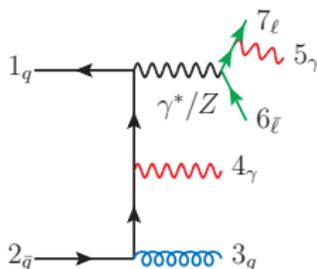
- Only need to compute $\mathcal{A}_{\ell\bar{\ell}}(0 \rightarrow \ell\bar{\ell}q\bar{q}\gamma\gamma)$

$$\mathcal{A}_{\ell\bar{\ell}}^{(1)}(1_q, 2_{\bar{q}}, 3_\gamma, 4_\gamma, 5_{\bar{\ell}}, 6_\ell) = \left(\frac{\mu^2}{-s_{12}}\right)^\epsilon \left[-\frac{1}{\epsilon^2} - \frac{3}{2\epsilon} - 4\right] \mathcal{A}_{\ell\bar{\ell}}^{(0)}(1_q, 2_{\bar{q}}, 3_\gamma, 4_\gamma, 5_{\bar{\ell}}, 6_\ell).$$

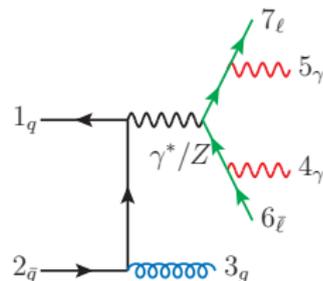
Zγγ production: $\mathcal{O}(\alpha_s)$ real correction



$$\mathcal{A}_{qq}^{(0)}(0 \rightarrow \ell\bar{\ell}q\bar{q}g\gamma\gamma)$$



$$\mathcal{A}_{q\ell}^{(0)}(0 \rightarrow \ell\bar{\ell}q\bar{q}g\gamma\gamma)$$



$$\mathcal{A}_{\ell\ell}^{(0)}(0 \rightarrow \ell\bar{\ell}q\bar{q}g\gamma\gamma)$$

- Real emission amplitudes:

$$\mathcal{A}_{qq}^{(0)}(1_q, 2_{\bar{q}}, 3_g, 4_{\gamma}, 5_{\gamma}, 6_{\bar{\ell}}, 7_{\ell}) = \mathcal{A}_q^{(0)}(1_q, 2_{\bar{q}}, 3_g, 4_g, 5_{\gamma}, 6_{\bar{\ell}}, 7_{\ell}) + \mathcal{A}_q^{(0)}(1_q, 2_{\bar{q}}, 3_g, 5_{\gamma}, 4_g, 6_{\bar{\ell}}, 7_{\ell})$$

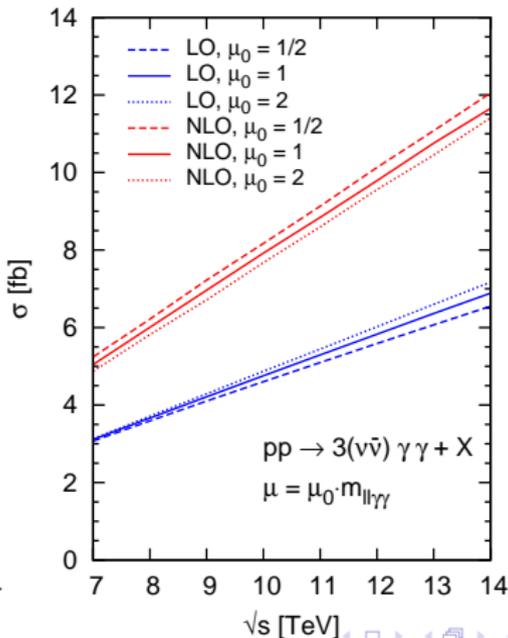
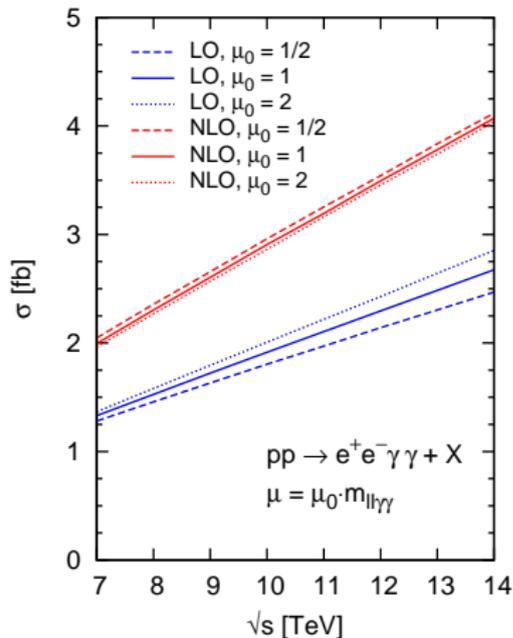
$$\mathcal{A}_{q\ell}^{(0)}(1_q, 2_{\bar{q}}, 3_g, 4_{\gamma}, 5_{\gamma}, 6_{\bar{\ell}}, 7_{\ell}) = \mathcal{A}_{\ell}^{(0)}(1_q, 2_{\bar{q}}, 3_g, 4_g, 5_{\gamma}, 6_{\bar{\ell}}, 7_{\ell}) + \mathcal{A}_{\ell}^{(0)}(1_q, 2_{\bar{q}}, 4_g, 3_g, 5_{\gamma}, 6_{\bar{\ell}}, 7_{\ell})$$

$$\mathcal{A}_{\ell\ell}^{(0)}(1_q, 2_{\bar{q}}, 3_g, 4_{\gamma}, 5_{\gamma}, 6_{\bar{\ell}}, 7_{\ell}) = \mathcal{A}_{q\ell}^{(0)}(7_{\ell}, 6_{\bar{\ell}}, 5_g, 3_{\gamma}, 4_{\gamma}, 2_{\bar{q}}, 1_q)$$

$Z\gamma\gamma$: Results

Z $\gamma\gamma$ inclusive cross section

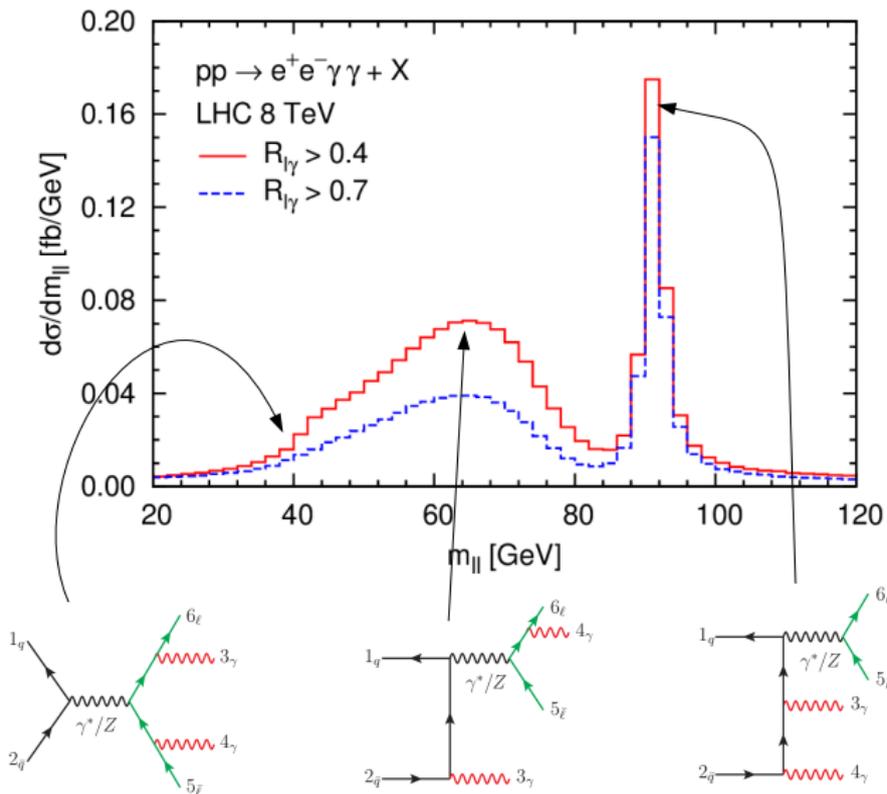
$$\begin{aligned}
 p_T^{\gamma} &> 20 \text{ GeV}, & |\eta_{\gamma}| < 2.5, & R_{\gamma\gamma} > 0.4, \\
 p_T^{\ell_h} &> 25 \text{ GeV}, & p_T^{\ell_s} > 15 \text{ GeV}, & |\eta_e| < 2.5, \\
 m_{\ell\ell} &> 12 \text{ GeV}, & R_{e\gamma} > 0.7, & E_T^{\text{miss}} > 25 \text{ GeV}.
 \end{aligned}$$



$K \sim 1.5$
for $\nu\bar{\nu}\gamma\gamma$

$K \sim 1.6$
for $e^+e^-\gamma\gamma$

$m_{\ell\bar{\ell}}$ distribution



Conclusions

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- We computed NLO QCD corrections to $Z\gamma j$ and $Z\gamma\gamma$ productions at hadron colliders
- We present the phenomenology for the $Z\gamma, Z\gamma+\text{jet}$ and $Z\gamma\gamma$ processes at NLO
- Include the fragmentation contributions
- We studied the perturbative uncertainty of the exclusive cross section following Stewart/Tackmann's method
- $Z\gamma j$ and $Z\gamma\gamma$ processes are available in MCFMv6.3

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THANK YOU

BACKUPs

Predictions for $Z\gamma$ and $Z\gamma+\text{jet}$.

	Inclusive NLO ($e^+e^-\gamma + X$) [pb]
$p_T^\gamma > 15$ GeV	$1.21^{+0.7\%}_{-0.5\%}$ (scale) $\pm 3.5\%$ (PDF) $\pm 0.4\%$ (frag)
$p_T^\gamma > 60$ GeV	$0.0545^{+5.7\%}_{-4.1\%}$ (scale) $\pm 3.7\%$ (PDF) $\pm 1.2\%$ (frag)
	Exclusive NLO ($e^+e^-\gamma + \text{no jets}$) [pb]
$p_T^\gamma > 15$ GeV	$1.02^{+1.8\%}_{-1.9\%}$ (scale) $\pm 3.8\%$ (PDF) $\pm 0.5\%$ (frag)
$p_T^\gamma > 60$ GeV	$0.0357^{+11.6\%}_{-9.4\%}$ (scale) $\pm 4.4\%$ (PDF) $\pm 1.8\%$ (frag)

	Inclusive 1-jet NLO ($e^+e^-\gamma + \text{jet} + X$) [fb]
$p_T^\gamma > 15$ GeV	$252^{+7.4\%}_{-5.2\%}$ (scale) $\pm 2.0\%$ (PDF) $\pm 0.6\%$ (frag)
$p_T^\gamma > 60$ GeV	$24.6^{+8.1\%}_{-6.8\%}$ (scale) $\pm 2.5\%$ (PDF) $\pm 1.9\%$ (frag)
	Exclusive 1-jet NLO ($e^+e^-\gamma + \text{jet}$) [fb]
$p_T^\gamma > 15$ GeV	$188^{+13.0\%}_{-11.2\%}$ (scale) $\pm 2.4\%$ (PDF) $\pm 0.8\%$ (frag)
$p_T^\gamma > 60$ GeV	$15.3^{+25.3\%}_{-17.4\%}$ (scale) $\pm 2.9\%$ (PDF) $\pm 3.1\%$ (frag)