Leptoquarks: A Tale of Four Searches at the ATLAS Detector



R. Caputo

SUNY, Stony Brook

BNL Seminar April 28, 2011



On Behalf of the ATLAS Collaboration

To Boldly Search...

- The Standard Model and Beyond
 - A Brief Introduction to Leptoquarks
- The LHC and the ATLAS detector
- Reconstruction and Identification
- Leptoquark Analysis
- Results and Conclusion



The Standard Model

- Quantum Field Theory
 - particles are fields
 - gauge invariance
 - SU(3)xSU_L(2)xU_Y(1) yields
 12 gauge bosons
- Forces act on particles
 - fermions quarks/leptons
- Families have identical gauge interactions
- Differ by mass and flavor quantum number



Particles

http://www.ipp.phys.ethz.ch/aboutus/?file=institut

The particle drawings are simple artistic representations

A Brief Introduction to Leptoquarks

- SM provides no communication/symmetry between quarks/leptons
- Leptoquarks: Another Boson
 - baryon and lepton number, couple triplet color charge
 - obey SM group symmetries
 - spin-0 scalar/spin-1 vector
 - 2 couplings: $\ell(v)$ -q
 - 4 couplings: 2 with λ_{G} and κ_{G}
 - Produced singly or in pairs
- Theories predict LQs
 - lepton/quark substructure, Grand Unified Theories (GUTs), technicolor



Production Cross Sections



- Focus: scalar LQ pair production
- Use NLO σ for scalar signal
- Early LHC data sensitive to mass range beyond other accelerators

HERA and the Tevatron

- **Excitement from HERA**
 - 1997: H1 and ZEUS observed excess at e+jet mass of 200 GeV
- **HERA** results
 - later ruled out anomaly
- **Tevatron results** •
 - $-\beta$ is branching fraction to charged leptons





The LHC and the ATLAS Detector



The Large Hadron Collider

- 27 km long collider ring 100 m underground
- √s = 7 TeV
- $\mathcal{L}_{inst} = 2.5 \times 10^{32} \, \text{cm}^{-2} \text{s}^{-1}$
- 200 bunches with 1.15x10¹¹ p/bunch



ATLAS coordinate system



Inner Detector (Tracking)



Calorimeters



Magnet System



Barrel: 3.9 T, End-caps: 4.1 T

Muon System



Triggers



Reconstruction and Identification

- Leptons
 - electrons
 - muons
- Jets
- Missing Energy



Leptons

Electrons

- Energy clusters in EM calorimeter
- E_T>20 GeV, E_T isolation < 20%
- |η|<2.47 with crack region removed
- Efficiency ~70%



Muons

- Tracks: inner detector and muon system then matched
- p_T>20 GeV, p_T isolation < 25%
- |ŋ|<2.4
- Rejection of cosmics
 - |d₀|<0.1 mm and |z₀|<1 cm
- Efficiency ~65%
 - d₀- min distance between muon trajectory and the event primary vertex in xy-plane z₀- parallel to beam direction

Jets and E_T^{miss}

Jets

- Anti- k_{T} algorithm, R=0.4
- p_T>20 GeV, ΔR_{jet,lep}>0.5

 $\Delta R = \sqrt{\Delta \phi^2 + \Delta \eta^2}$

- |ŋ|<2.8
- "good" jet requirements
 - rejects noise induced jets, vertex confirmation

M. Cacciari, G.P. Salam, Phys Lett. B 641 (2006)

$\mathbf{E}_{\mathrm{T}}^{\mathrm{miss}}$

- Negative vector sum of E_T and muon p_T
- $E_T^{miss} > 25 \text{ GeV}$
- Removed if "bad" jets are present



Leptoquark Analysis



- Background Yield Determination
- Base Event Selection
- Control Regions
- Optimized LQ Selection
- Limit Setting

Background Yield Determination

- Simulated Background and Signal Samples
 - PDF Set: CTEQ 6.6
 - Generators:
 - ALPGEN (V+jets) (Z+jets in dilepton is semi-data driven)
 - HERWIG, MC@NLO (tt, single top, VV)
 - Pythia
- N_{pred} = acceptance* σ * $\mathcal{L}_{integrated}$
- Multijet background determined by data driven methods
- Control regions
 - V+jets and tt enhanced to validate modeling

Data Driven Background

- Data Driven method
 - tails not modeled well by MC
 - not enough events generated
- Iljj (Z+jets)
 - signal region: tails of Z+jet dist
 - fitting method for 1 lepton and a fake (relative iso variable)
- evjj (QCD): Fit to $M_T N_D^{sig} = N_D^Z \frac{N_{MC}^{sig}}{N_{MC}^Z}$
 - $-\Sigma bkgs = data yield$
 - minimize LLR

 $M_T(l, E_T^{miss}) = \sqrt{2p_T^l E_T^{miss}(1 - \cos(\Delta \phi))}$

- μvjj (QCD): ABCD method
 - E_T^{miss} and $|d_0|$ (uncorrelated)
 - signal region: high E_T^{miss} and low $|d_0|$
 - Assumes EWK contribution in region C is negligible, QCD
 shape same in C and D

Data and Total Background



4/28/10

Data Driven Background

- Data Driven method
 - tails not modeled well by MC
 - not enough events generated
- Iljj (Z+jets)
 - signal region: tails of Z+jet dist
 - fitting method for 1 lepton and a fake (relative iso variable)
- evjj (QCD): Fit to $M_T N_D^{sig} = N_D^Z \frac{N_{MC}^{sig}}{N_{MC}^Z}$
 - Σbkgs = data yield
 - minimize LLR

 $M_T(l, E_T^{miss}) = \sqrt{2p_T^l E_T^{miss}(1 - \cos(\Delta \phi))}$

- μvjj (QCD): ABCD method
 - E_T^{miss} and $|d_0|$ (uncorrelated)
 - signal region: high E_T^{miss} and low $|d_0|$
 - Assumes EWK contribution in region C is negligible, QCD
 shape same in C and D





 N_A , N_B , and N_C are yields from data in regions A, B, and C after EWK contribution is eliminated (using MC)

4/28/10

Base Event Selection

- Event Selection
 - At least 1 good primary vertex
 - ≥ 3 ID tracks
 - |z_{vtx}| < 15 cm
 - = 1 good lepton (=2 for dilepton analysis)
 - ≥ 2 good jets
- Event Selection for lvjj
 - pass E_T^{miss}
 - M_T(I,E_T^{miss}) > 40 GeV
 - triangle cut for QCD removal - extra rejection of residual events with badly measured jets (evjj) ($\Delta \phi(E_T^{miss}, jet)$ vs. E_T^{miss})
 - opposite lepton veto



Base Event Selection Plots



R. Caputo, BNL HEP Seminar

Control Regions: Electron channels

eejj	Z+≥2jets	ttbar				
V+jets	150±23	0.3±0.1				
Тор	2.0±0.3	24±4				
diboson	2.0±0.3	0.8±0.1				
QCD	4.0+144.	0.+0.1-0.				
Total	158±25	25±4				
Data	140	22				
10^5 ATLAS Preliminary • Data 2010 ($\sqrt{s} = 7$ To						

20 GeV	10 ⁵	ATLAS	Prelimi	nary] • ا	Data 2010 /+jets	(√s = 7 T	eV)	
Events /	10 ³	eejj:	Z+≥2	jets		Fop QCD Diboson			
	10 1 10 ⁻¹			┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝ ┝	•				
	10 ⁻²	200	300	400	500	600	700	800	
							S ^e T [G	ieV]	, Bľ

evjj	W+=2 jets	W+≥3jets	ttbar
V+jets	2080±680	580±190	180±60
Тор	21±4	44±9	210±40
diboson	17±4	8.3±1.9	2.1±0.5
QCD	64±14	68±15	29±7
Total	2180±710	700±200	420±80
Data	2344	722	425



Control Regions: Electron channels

eejj	Z+≥2jets	ttbar
V+jets	150±23	0.3±0.1
Тор	2.0±0.3	24±4
diboson	2.0±0.3	0.8±0.1
QCD	4.0+144.	0.+0.1-0.
Total	158±25	25±4
Data	140	22



evjj	W+=2 jets	W+≥3jets	ttbar
V+jets	2080±680	580±190	180±60
Тор	21±4	44±9	210±40
diboson	17±4	8.3±1.9	2.1±0.5
QCD	64±14	68±15	29±7
Total	2180±710	700±200	420±80
Data	2344	722	425



Control Regions: Muon channels

μμϳϳ	Z+≥2jets	ttbar
V+jets	190±24	0.3±0.1
Тор	2.7±0.5	24±4
diboson	0.2±0.1	0.8±0.1
QCD	6.+115.5	0.+0.1-0.
Total	200±25	25±4
Data	216	22



μvjj	W+=2 jets	W+≥3jets	ttbar
V+jets	3250±1060	900±30	250±80
Тор	14±3	53±1	260±50
diboson	28±6	14±3	3.0±0.7
QCD	300±100	130±50	54±32
Total	3590±1080	1100±330	570±120
Data	3588	1120	547



Control Regions: Muon channels

μμϳϳ	Z+≥2jets	ttbar
V+jets	190±24	0.3±0.1
Тор	2.7±0.5	24±4
diboson	0.2±0.1	0.8±0.1
QCD	6.+115.5	0.+0.1-0.
Total	200±25	25±4
Data	216	22



μvjj	W+=2 jets	W+≥3jets	ttbar
V+jets	3250±1060	900±30	250±80
Тор	14±3	53±1	260±50
diboson	28±6	14±3	3.0±0.7
QCD	300±100	130±50	54±32
Total	3590±1080	1100±330	570±120
Data	3588	1120	547



Optimized Leptoquark Selection

- Grid Search
 - systematic Search over a grid of points
 - regular grid inefficient
- Search region: value of MC signal events
 - use every signal event to form grid
 - n-Dimensional
- Significance calculated and plotted
 - matched to each cut
- Minimize Poisson probability
 - background fluctuation is signal
 + background





Optimization on LQ signal

- 4-D grid space
 - dilepton channels:
 - M(l,l) Invt. mass of leptons
 - M_{ave}(LQ) Ave. LQ mass
 - p_T^{all}
 - $S_T \Sigma p_T(2 \text{ jets}, 2 \text{ leptons})$
 - single lepton channels:
 - M_T(I,E_T^{miss})
 - M(LQ) Invt. LQ mass
 - M_T(LQ) Transverse LQ mass
 - $S_T \Sigma p_T(2 \text{ jets, lepton,} E_T^{miss})$



$eejj$ and $\mu\mu jj$	e u jj	$\mu u jj$
$M_{ll} > 120 { m ~GeV}$	$M_{\rm T} > 200 { m ~GeV}$	$M_{\rm T} > 160 { m ~GeV}$
$\overline{M_{\rm LQ}} > 150 {\rm ~GeV}$	$M_{\rm LQ} > 180~{\rm GeV}$	$M_{\rm LQ} > 150 { m ~GeV}$
$p_{\mathrm{T}}^{\mathrm{all}} > 30~\mathrm{GeV}$	$M_{ m LQ}^{ m T} > 180~{ m GeV}$	$M_{\rm LQ}^{\rm T} > 150 { m ~GeV}$
$S_{\mathrm{T}}^{\ell} > 450 \ \mathrm{GeV}$	$S_{\mathrm{T}}^{\nu} > 410 \; \mathrm{GeV}$	$S_{\mathrm{T}}^{\nu} > 400 \ \mathrm{GeV}$

Systematics

	V+jets		Top		Dibo	son	LQ (30	0 GeV)
Channel	lljj	$l\nu jj$	lljj	$l\nu j j$	lljj	$l\nu jj$	lljj	$l\nu jj$
Production Cross Section	—	4	13	13	5	5	18	18
Modeling	34*, 45**	40	35	35		_	—	_
Electron Energy Scale & Resolution [*]	+13, -0.2	5	10	2	7	1	8	1
Muon Momentum Scale & Resolution**	20	5	7	2	8	1	6.7	1
Jet Energy Scale	6	+22, -13	+9, -18	32	+16, -6	+17, -24	2	3
Jet Energy Resolution	16	10	0.3	26	4	14	0.3	3
Luminosity	0.3	11	11	11	11	11	11	11
Pile up	< 0.1	5	< 0.1	4	< 0.1	6	< 0.1	2
Total Systematics	39*	+49, -45	47^{*}	57	(+22, -16)	+26,-31	22	22

Numbers are in percentages

Systematics

	V+	jets	Top		Dibo	oson	LQ (30	00 GeV)
Channel	lljj	$l\nu jj$	ll j j	lvjj	lljj	$l\nu j j$	lljj	$l\nu jj$
Production Cross Section		4	13	13	5	5	18	18
Modeling	$34^*, 45^{**}$	40	35	35	—	_	—	_
Electron Energy Scale & Resolution [*]	+13, -0.2	5	10	2	7	1	8	1
Muon Momentum Scale & Resolution**	20	5	7	2	8	1	6.7	1
Jet Energy Scale	6	+22, -13	+9, -18	32	+16, -6	+17, -24	2	3
Jet Energy Resolution	16	10	0.3	26	4	14	0.3	3
Luminosity	0.3	11	11	11	11	11	11	11
Pile up	< 0.1	5	< 0.1	4	< 0.1	6	< 0.1	2
Total Systematics	39*	+49, -45	47*	57	(+22, -16)	+26,-31	22	22

Numbers are in percentages

Systematics

- Modeling
 - varying event generator-level parameters
- Jet Energy Scale and Resolution
 - varied by uncertainties
 - 5% added (quark/gluon response)
 - included in E_T^{miss}
- Pile-up
 - multiple minimum bias events per bunch crossing
 - sub-detectors sensitive to bunch crossings before and after interesting physics interaction



Confidence Level Evaluation



- Overview
- Semi-Frequentist approach
- Log-Likelihood Ratio Test
- Confidence levels

Semi-Frequentist approach

- "Frequency" a result will occur
- Collie (COnfidence Level LImit Evaluator)
 - likelihood Ratio test
 - "as Frequentist as possible"
 - Bayesian treatment of systematics
 - T. Junk, arXiv:hep-ex/9902006v1

$$L(b \mid x) = \frac{(b)^{x} e^{-b}}{x!}$$

$$\Lambda(\vec{x}) = \prod_{i}^{channel} \prod_{j}^{bin} \frac{L((s+b)_{ij} \mid x_{ij})}{L(b_{ij} \mid x_{ij})}$$

$$s = signal$$

$$b = background$$

$$x = data$$

$$L = likelihood$$

Log-Likelihood Ratio Test

- Generate Null and Test hypothesis
- Distributions of LLR(s+b) and LLR(b)

 $LLR(x) = -2\log(\Lambda)$



W. Fisher, Fermilab-TM-2386-E

$$LLR(x) = \sum_{i}^{channels \ bins} \sum_{j}^{bins} s_{ij} - x_{ij} \ln\left(1 + \frac{s_{ij}}{b_{ij}}\right)$$

4/28/10

Confidence levels

- Confidence levels integral of LLR distribution
- CL relative to outcome
 - observed/expected limits
- Expected data
 - median bkg outcome
 - CL_b is 50% if bkg is well modeled
- Poor modeling -> CL_s method
- Exclusion: 95% CL
 - increase parameter until 1-CL_s=0.95



Source	eejj	e u jj	$\mu\mu j j$	$\mu u j j$
V+jets	0.50 ± 0.28	0.65 ± 0.38	0.28 ± 0.22	2.6 ± 1.4
Тор	$0.51~\pm~0.23$	$\left 0.67 \pm 0.39 \right $	0.52 ± 0.23	$1.6~\pm~0.9$
Diboson	0.03 ± 0.01	$0.10~\pm~0.03$	0.04 ± 0.01	0.10 ± 0.03
Other Bkg.	$0.02 \ \ {}^+_{-} \ \ {}^{0.03}_{0.02}$	$0.06~\pm~0.01$	$0.00 \ \ {}^+ \ \ {}^{0.01}_{0.00}$	$0.0~\pm~0.0$
Total Bkg	1.1 ± 0.4	1.4 ± 0.5	0.8 ± 0.3	4.4 ± 1.9
Data				
LQ(250 GeV)	38 ± 8	9.6 ± 2.1	45 ± 10	13 ± 3
LQ(300 GeV)	17 ± 4	5.1 ± 1.1	$21~\pm~5$	6.4 ± 1.4
LQ(350 GeV)	7.7 ± 1.7	2.6 ± 0.6	9.4 ± 2.1	$3.0~\pm~0.7$
LQ(400 GeV)	$3.5~\pm~0.8$	_	$ 4.4 \pm 1.0$	

	Z+je	ets .	W+jets	
		t	ор	
Source	eejj	$e \nu j j$	$\mu\mu j j$	$\mu u j j$
V+jets	0.50 ± 0.28	0.65 ± 0.38	0.28 ± 0.22	$2.6~\pm~1.4$
Тор	$0.51~\pm~0.23$	0.67 ± 0.39	0.52 ± 0.23	$1.6~\pm~0.9$
Diboson	0.03 ± 0.01	$0.10~\pm~0.03$	0.04 ± 0.01	0.10 ± 0.03
Other Bkg.	$0.02 \ \ {}^+ \ \ {}^{0.03}_{0.02}$	$0.06~\pm~0.01$	$0.00 \ \ {}^+ \ \ {}^{0.01} _{- \ \ 0.00}$	$0.0~\pm~0.0$
Total Bkg	1.1 ± 0.4	1.4 ± 0.5	0.8 ± 0.3	4.4 ± 1.9
Data				
LQ(250 GeV)	38 ± 8	9.6 ± 2.1	45 ± 10	13 ± 3
LQ(300 GeV)	17 ± 4	5.1 ± 1.1	$21~\pm~5$	6.4 ± 1.4
LQ(350 GeV)	$7.7~\pm~1.7$	2.6 ± 0.6	$9.4~\pm~2.1$	$3.0~\pm~0.7$
LQ(400 GeV)	$\mid~3.5~\pm~0.8$	_	$ 4.4 \pm 1.0$	

Source	eejj	e u jj	$\mu\mu j j$	$\mu u j j$
V+jets	0.50 ± 0.28	0.65 ± 0.38	0.28 ± 0.22	2.6 ± 1.4
Тор	$0.51~\pm~0.23$	$\left 0.67 \pm 0.39 \right $	0.52 ± 0.23	$1.6~\pm~0.9$
Diboson	0.03 ± 0.01	0.10 ± 0.03	$0.04~\pm~0.01$	$0.10~\pm~0.03$
Other Bkg.	$0.02 \ \ {}^+ \ \ {}^{0.03}_{0.02}$	$0.06~\pm~0.01$	$0.00 \ \ {}^+ \ \ {}^{0.01}_{0.00}$	$0.0~\pm~0.0$
Total Bkg	1.1 ± 0.4	1.4 ± 0.5	0.8 ± 0.3	4.4 ± 1.9
Data	2	2	0	4
LQ(250 GeV)	38 ± 8	9.6 ± 2.1	45 ± 10	13 ± 3
LQ(300 GeV)	17 ± 4	5.1 ± 1.1	$21~\pm~5$	$6.4~\pm~1.4$
LQ(350 GeV)	7.7 ± 1.7	2.6 ± 0.6	$9.4~\pm~2.1$	$3.0~\pm~0.7$
LQ(400 GeV)	$3.5~\pm~0.8$		4.4 ± 1.0	

4/28/10



 $S_T = \sum p_T(jet_1, jet_2, lepton_1, E_T^{miss} / lepton_2)$



Cross Section Limits

- ATLAS combined result
 - observed: red
 - expected: blue dashed
- Max Sensitivity lacksquare
 - dilepton: β =1
 - single lepton: β =0.5
- Stronger exclusion in dimuon channel
- CMS •
 - dilepton results published
 - publishing single-lepton channel and combined results



Cross Section Limits



In Summary

- Data in high signal-to-background matches background-only predictions
 - 95% CL upper bounds on production cross section
- 1st generation:

- MLQ > 376 (319) GeV for β =1 (0.5)

- 2nd generation:
 - MLQ > 422 (362) GeV for β =1 (0.5)
- LHC set world's most stringent from direct LQ pair production searches with 2010 data
- Future Prospects: order of a TeV LQ (discovery hopefully) 2011 with 5 fb⁻¹

Backups!



The Standard Model

- Forces Mediated by integer spin bosons
 - Strong
 - 8 massless gluons, couple only to quarks, confinement
 - relative strength of 1 with 10⁻¹⁵ m (~nucleus) range
 - Electromagnetic
 - photons, couple to charged particles
 - relative strength 10⁻³ with infinite range
 - Weak
 - W[±]/Z, couple to all SM particles
 - relative strength of 10⁻⁶ with 10⁻¹⁸ m (~0.1% dia. proton) range

Strong Electromagnetic Gluons (8) Photon Quarks Atoms Light Chemistry Mesons Electronics Baryons Nuclei Gravitational Weak Bosons (W,Z Graviton ? Solar system Neutron decay Galaxies Beta radioactivity **Black holes** Neutrino interactions Burning of the sun The particle drawings are simple artistic representations [1]

Forces

The ATLAS Detector



Monte Carlo

- Signal and background samples
 - ALPGEN interfaced to HERWIG and JIMMY and PYTHIA
- Designed to model interactions
 - Hard Scatter, Initial and Final State Radiation, Hadronization, Soft Interactions... etc.
- PYTHIA and HERWIG/JIMMY Parton Shower model
- ALPGEN Matrix Element model
 - useful for multi-jet events but other generators handle hadronization and shower more completely
- Detailed detector simulation: GEANT4
 - Ionization and showering in detector, energy deposition in calorimeters, trajectory in magnetic field

GRL and Trigger lists

- Good Runs List
 - All parts of detector working nominally, LHC running nominally
 - General requirements (ptag data10 7TeV and db DATA and partition ATLAS) LHC beam energy at 3.5 TeV (lhc beamenergy 3400-3600)
 - The stable beam flag (lhc stablebeams T)
 - Silicon and muon systems warm starts completed (ready 1)
 - The magnets on (mag s > 6000 and mag t > 18000)
 - Data quality flags (dq GLOBAL STATUS, CP TRACKING, CP EG ELECTRON BARREL, CP EG ELECTRON ENDCAP, CP MU MSTACO, CP JET JETB, CP JET JETEA, CP JET JETEC, CP MET METCALO, CP MET METMUON, LUMI, L1CAL, L1MUE, L1MUB, TRELE, TRMUO)
 - Run period dependent luminosity block and summary flags equal to good status. For periods A and B, this is LBSUMM#DetStatus-v03-repro04-01 g.
 - For other periods this is LBSUMM#DetStatus-v03-pass1-analysis-2010X g with X the period (C-J).
- Electron Trigger
 - E_T>15 GeV
 - "medium" electron requirement

Triangle cut for QCD removal



Data/MC Scale Factors

QCD Estimation: Matrix Method



Methodology

Bin by Bin

 QCD normalization and shape comes from following:

-
$$N_{l}^{i} = N_{ele}^{real i} + N_{QCD}^{fake i}$$

- $N_t^i = \varepsilon_{ele}^{real} N_{ele}^{real i} + \varepsilon_{QCD}^{fake} N_{QCD}^{fake i}$
- fill ith bin

$$\varepsilon_{QCD}^{fake} N_{QCD}^{i} = \varepsilon_{QCD}^{fake} \frac{\varepsilon_{ele}^{real} N_{l}^{i} - N_{t}^{i}}{\varepsilon_{ele}^{real} - \varepsilon_{QCD}^{fake}}$$

Reverse Isolation

- shape from loose-tight
- shape comes from following: normalization from following:

$$\varepsilon_{QCD}^{fake} N_{QCD} = \varepsilon_{QCD}^{fake} \frac{\varepsilon_{ele}^{real} N_l - N_t}{\varepsilon_{ele}^{real} - \varepsilon_{QCD}^{fake}}$$

- depends on tight/loose definition
- ε_{QCD} ~ 45%

data/MC correction factor ~1.0

Multijet Background: M_T fit method

- Data Driven method
 - not modeled well by MC
 - not enough events generated
- Fit to M_T
 - Σbkgs = data yield



$$M_T(l, E_T^{miss}) = \sqrt{2p_T^l E_T^{miss} (1 - \cos(\Delta \phi))}$$

4/28/10

Control Regions

- Iljj
- Z+jets
 - 81 <Z_{mass}<101 GeV
- ttbar
 - both e and μ
 - − ≥2 jets

- Inujj
- W+jets
 - $M_{T} < 150 \text{ GeV}$
 - exactly 2 jets
 - S_T< 175 GeV
 - ≥3 jets
 - S_T < 200 GeV
- ttbar
 - $M_{T} < 150 \text{ GeV}$
 - − ≥4 jets
 - $p_T(j_1)$ < 50 GeV, $p_T(j_2)$ < 40 GeV, $p_T(j_3)$ < 30 GeV