

# Probabilistic Genotyping

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**MAFS Workshop**

Milwaukee, WI  
**September 25, 2012**



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Standards and Technology

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Is there a way forward?

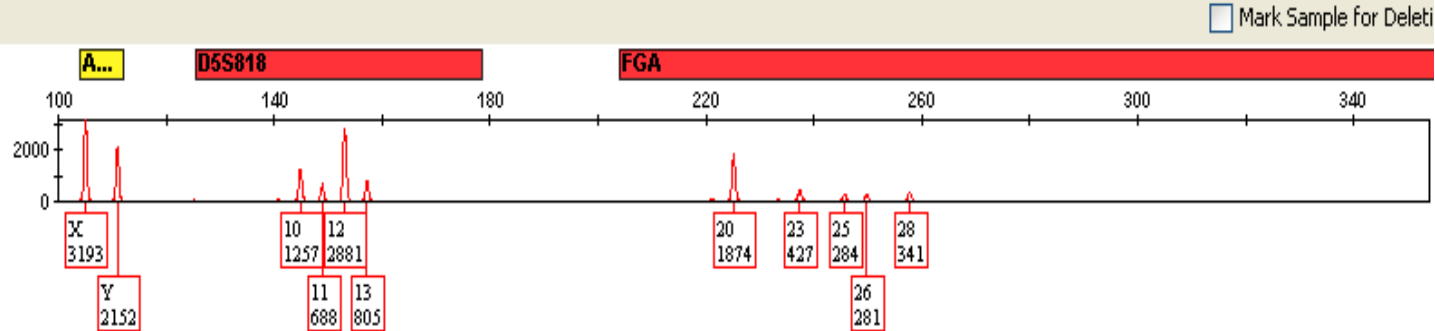
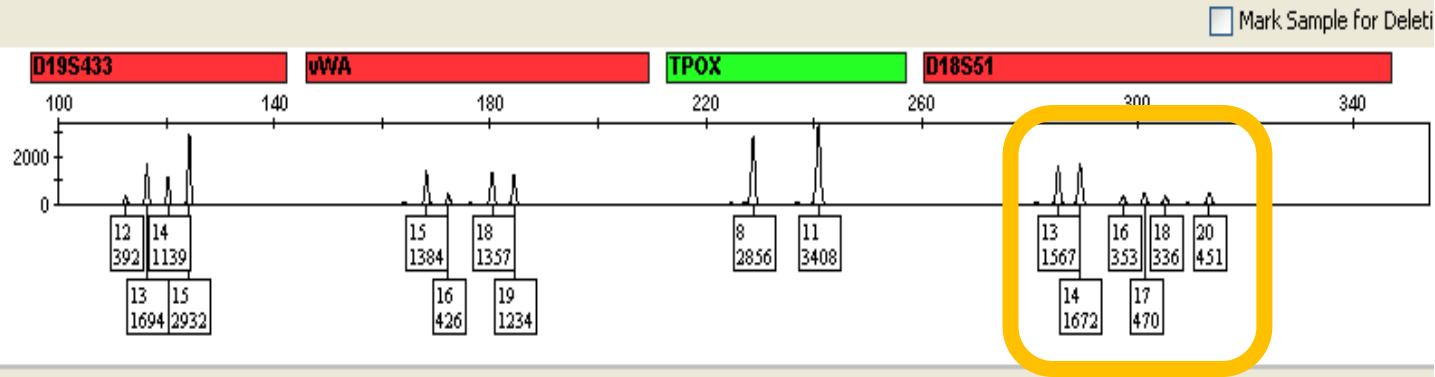
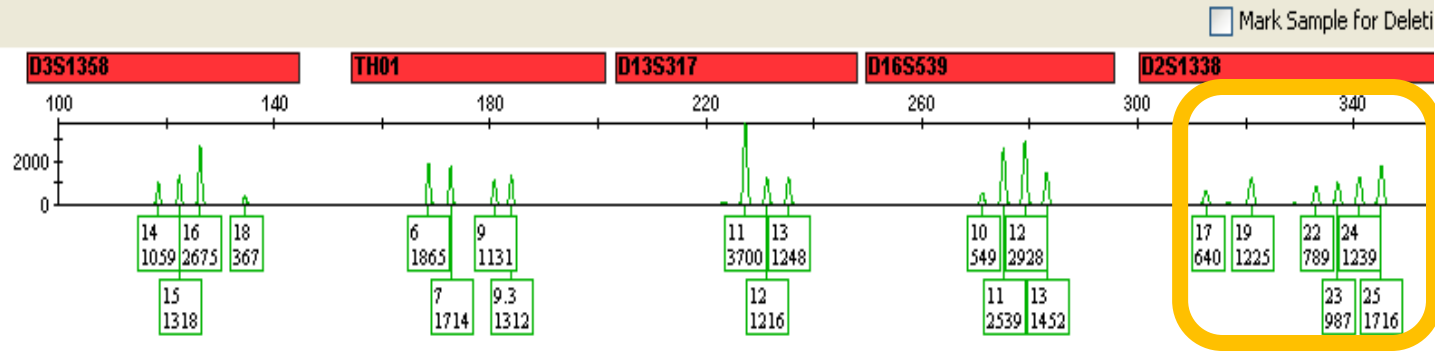
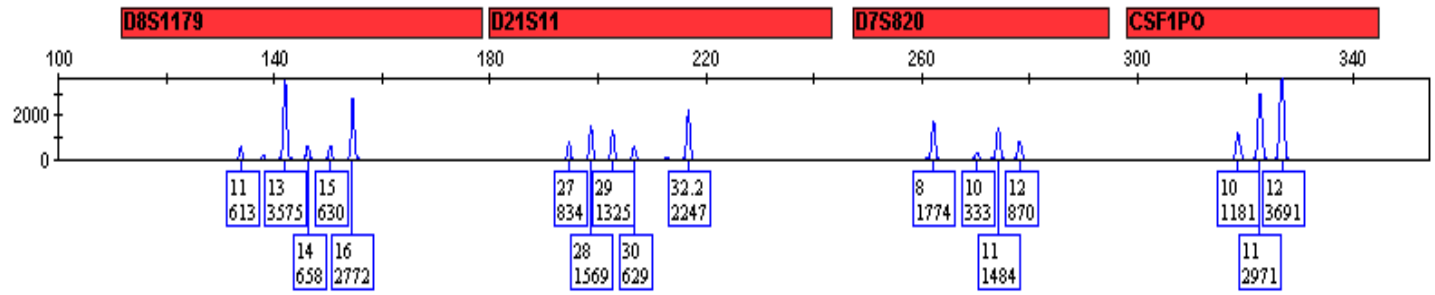
# Three Questions

- What were the last words of Julius Caesar before he died?
- Et tu, Brute? Then fall Caesar!
- What is the capital of Bangladesh?
- Dhaka

# Three Questions

- How many people are in this mixture?

All alleles are above ST



Do you have any uncertainty  
in your answer?

Whatever way uncertainty is approached, probability is the *only* sound way to think about it.

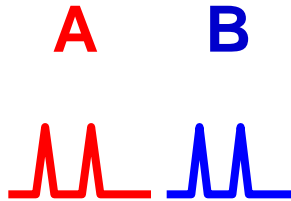


-Dennis Lindley

# Two-Person Mixtures

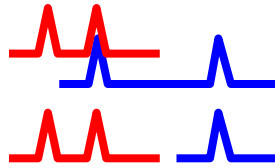
**14 total combinations**

Observed  
profile



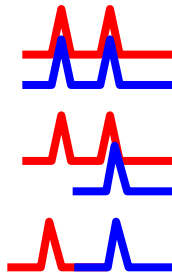
**4 alleles**

All heterozygotes and non-overlapping alleles



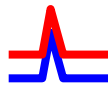
**3 alleles**

Heterozygote + heterozygote, one overlapping allele  
Heterozygote + homozygote, no overlapping alleles



**2 alleles**

Heterozygote + heterozygote, two overlapping alleles  
Heterozygote + homozygote, one overlapping allele  
Homozygote + homozygote, no overlapping alleles



**1 allele**

Homozygote + homozygote, overlapping allele



# 3-Person Mixtures

## Observed profile

**150 total combinations**



### 6 alleles

All heterozygotes and non-overlapping alleles



### 5 alleles

Two heterozygotes and one homozygote

Three heterozygotes, one overlapping allele



### 4 alleles

Six combinations of heterozygotes, homozygotes and overlapping alleles



### 3 alleles

Eight combinations of heterozygotes, homozygotes, and overlapping alleles



### 2 alleles

Five combinations of heterozygotes, homozygotes, and overlapping alleles

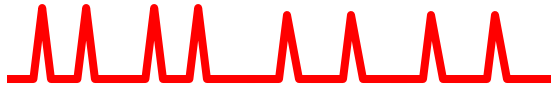


### 1 allele

All homozygotes, overlapping allele

# 4-Person Mixtures

## Observed profile



**8 alleles**

All heterozygotes and non-overlapping alleles

**MANY combinations**



**7 alleles**

Several combinations of heterozygotes, homozygotes, and overlapping alleles



**6 alleles**

Many combinations



**5 alleles**

Many combinations



**4 alleles**

Many combinations



**3 alleles**

Many combinations



**2 alleles**

Many combinations



**1 allele**

All homozygotes, overlapping allele

# Four-Person Mixture Studies Summary

**>70% of 4-person mixtures would NOT be recognized as 4-person mixtures based on allele count**

# “On the Threshold of a Dilemma”

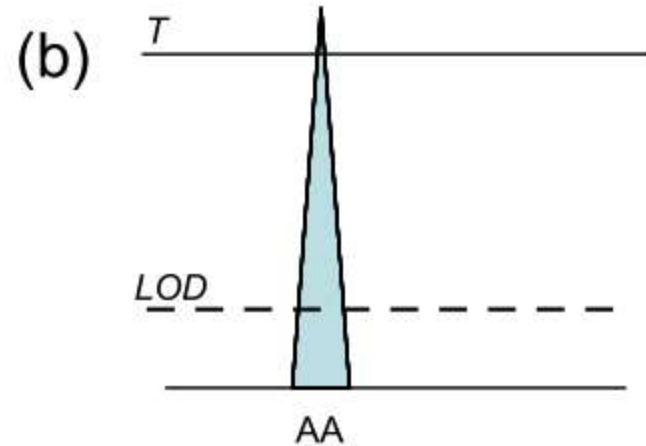
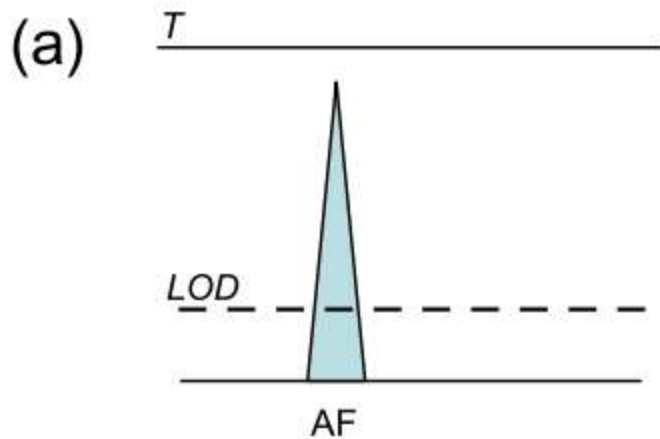
- Gill and Buckleton (2010)
- Although most labs use thresholds of some description, this philosophy has always been problematic because there is an inherent illogicality which we call the falling off the cliff effect.



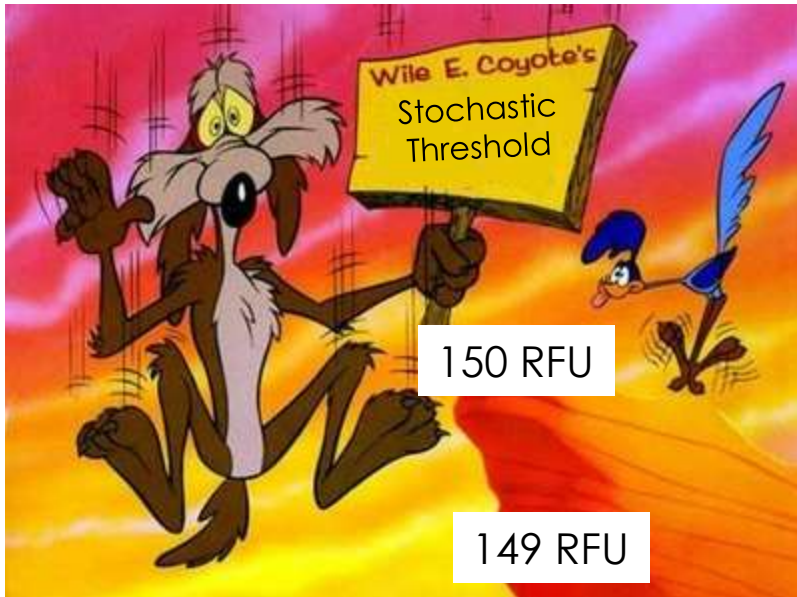
**Commentary on:** Budowle B, Onorato AJ, Callaghan TF, Della Manna A, Gross AM, Guerrieri RA, Luttmann JC, McClure DL. Mixture interpretation: defining the relevant features for guidelines for the assessment of mixed DNA profiles in forensic casework. *J Forensic Sci* 2009;54(4):810–21.

# “Falling off the Cliff Effect”

- If  $T$  = an arbitrary level (e.g., 150 rfu), an allele of 149 rfu is subject to a different set of guidelines compared with one that is 150 rfu even though they differ by just 1 rfu (Fig. 1).



# Falling off the Cliff vs. Gradual Decline



<http://blog.sironaconsulting.com/.a/6a00d8341c761a53ef011168cc5ff3970c-pi>



<http://ultimateescapesdc.files.wordpress.com/2010/08/mountainbiking2.jpg>

# Gill and Buckleton *JFS* **55: 265-268 (2010)**

- “The purpose of the ISFG DNA commission document was to provide a way forward to demonstrate the use of ***probabilistic models to circumvent the requirement for a threshold*** and to safeguard the legitimate interests of defendants.”



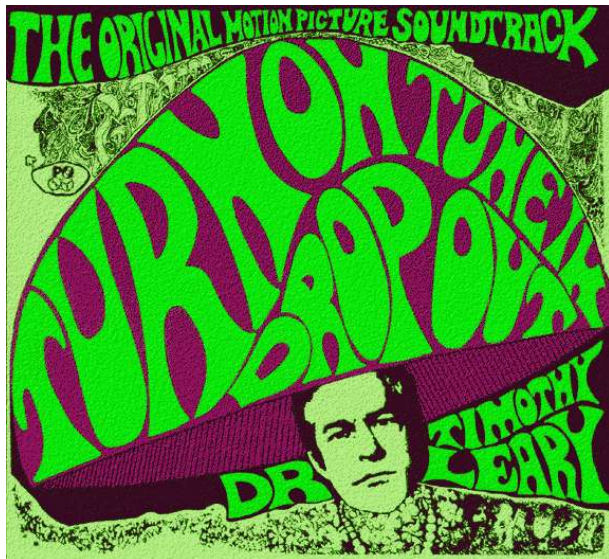
# Psychedelic Mixtures

Turn On...



Tune In...

(Talk about) Drop Out





# Next Issue of FSI-Genetics

Forensic Science International: Genetics xxx (2012) xxx–xxx



Contents lists available at SciVerse ScienceDirect

Forensic Science International: Genetics

journal homepage: [www.elsevier.com/locate/fsig](http://www.elsevier.com/locate/fsig)



Editorial

Focus issue—Analysis and biostatistical interpretation of complex and low template DNA samples

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# Article in press...



ELSEVIER

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Forensic Science International: Genetics

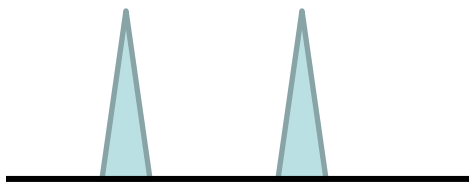
journal homepage: [www.elsevier.com/locate/fsig](http://www.elsevier.com/locate/fsig)



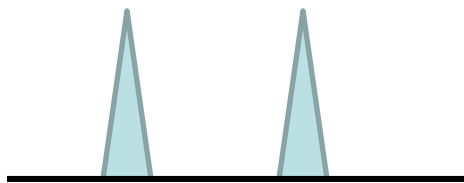
DNA commission of the International Society of Forensic Genetics:  
Recommendations on the evaluation of STR typing results that may  
include drop-out and/or drop-in using probabilistic methods

P. Gill<sup>a,b,\*</sup>, L. Gusmão<sup>c</sup>, H. Haned<sup>d</sup>, W.R. Mayr<sup>e</sup>, N. Morling<sup>f</sup>, W. Parson<sup>g</sup>, L. Prieto<sup>h</sup>,  
M. Prinz<sup>i</sup>, H. Schneider<sup>j</sup>, P.M. Schneider<sup>k</sup>, B.S. Weir<sup>l</sup>

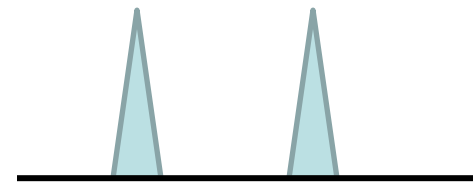
Suspect



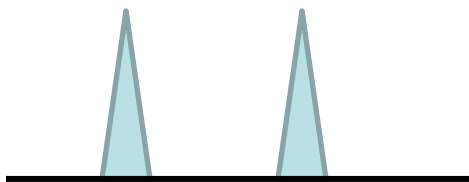
Suspect



Suspect



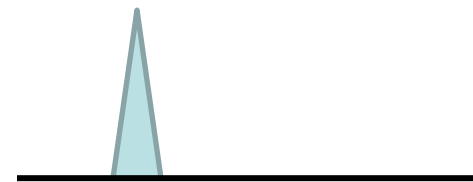
Evidence



Evidence



Evidence



$$LR = \frac{1}{2pq}$$

$$LR = \frac{0}{2pq}$$

$$LR = \frac{?}{2pq}$$

“2p”

$$p^2 + 2p(1 - p)$$

# Haned *et al.*

Forensic Science International: Genetics xxx (2012) xxx–xxx



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Forensic Science International: Genetics

journal homepage: [www.elsevier.com/locate/fsig](http://www.elsevier.com/locate/fsig)



## Exploratory data analysis for the interpretation of low template DNA mixtures

H. Haned<sup>a,\*</sup>, K. Slooten<sup>a,b</sup>, P. Gill<sup>c,d</sup>

<sup>a</sup> Netherlands Forensic Institute, Department of Human Biological traces, The Hague, The Netherlands

<sup>b</sup> VU University Amsterdam, Amsterdam, The Netherlands

<sup>c</sup> Norwegian institute of Public Health, Oslo, Norway

<sup>d</sup> University of Oslo, Norway

# Mitchell *et al.*

Forensic Science International: Genetics xxx (2012) xxx–xxx



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Forensic Science International: Genetics

journal homepage: [www.elsevier.com/locate/fsig](http://www.elsevier.com/locate/fsig)



## Validation of a DNA mixture statistics tool incorporating allelic drop-out and drop-in

Adele A. Mitchell\*, Jeannie Tamariz, Kathleen O'Connell, Nubia Ducasse, Zoran Budimlija, Mechthild Prinz, Theresa Caragine

Department of Forensic Biology, Office of Chief Medical Examiner of The City of New York, 421 E 26th Street, New York, NY 10016, United States

# The Drop-out Model

The interpretation of low level DNA mixtures

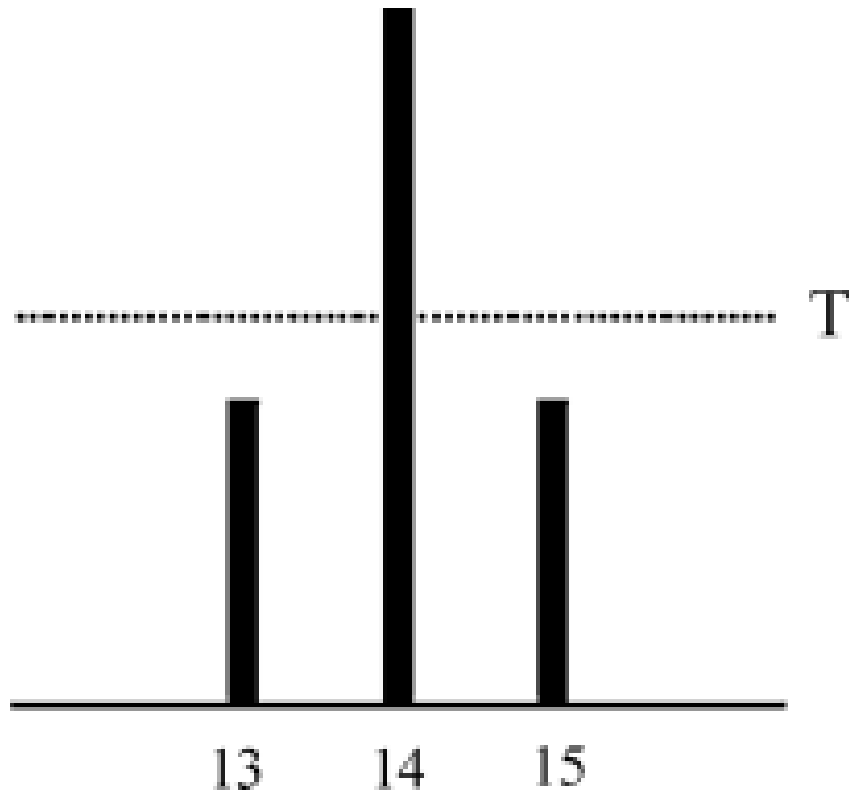
Hannah Kelly <sup>a,\*</sup>, Jo-Anne Bright <sup>a</sup>, James Curran <sup>b</sup>, John Buckleton <sup>a</sup>

<sup>a</sup> ESR, PB 92021 Auckland, New Zealand

<sup>b</sup> Department of Statistics, University of Auckland, PB 92019 Auckland, New Zealand

FSI - Genetics 6 (2012) 191–197

# First – Convert Peaks to Alleles



Assume 2 Contributors  
3 peaks – 4 alleles

Allelic Vector

13

14

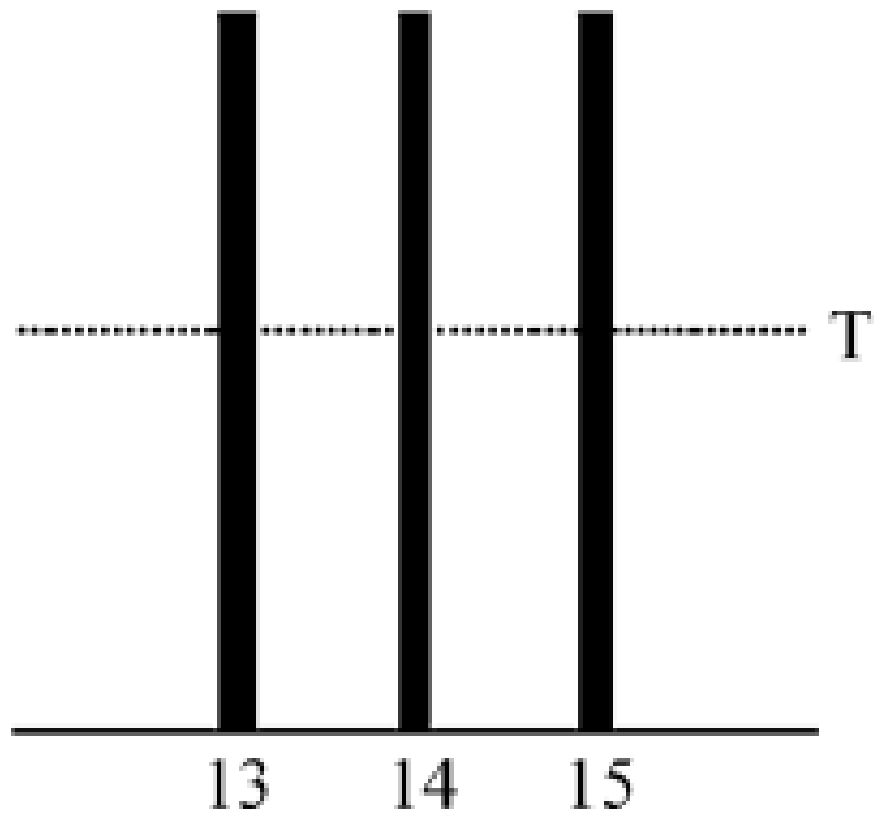
14

15

13,14,14,15

# Ambiguity in Determining Vectors

Assume 2 Contributors



## Allelic Vectors

13, 13, 14, 15

13, 14, 14, 15

13, 14, 15, 15

3 possibilities



# Permutations

- The number of permutations is the number of ways that the alleles can be arranged as pairs.

# Permutations

- An easier way to compute using factorials.

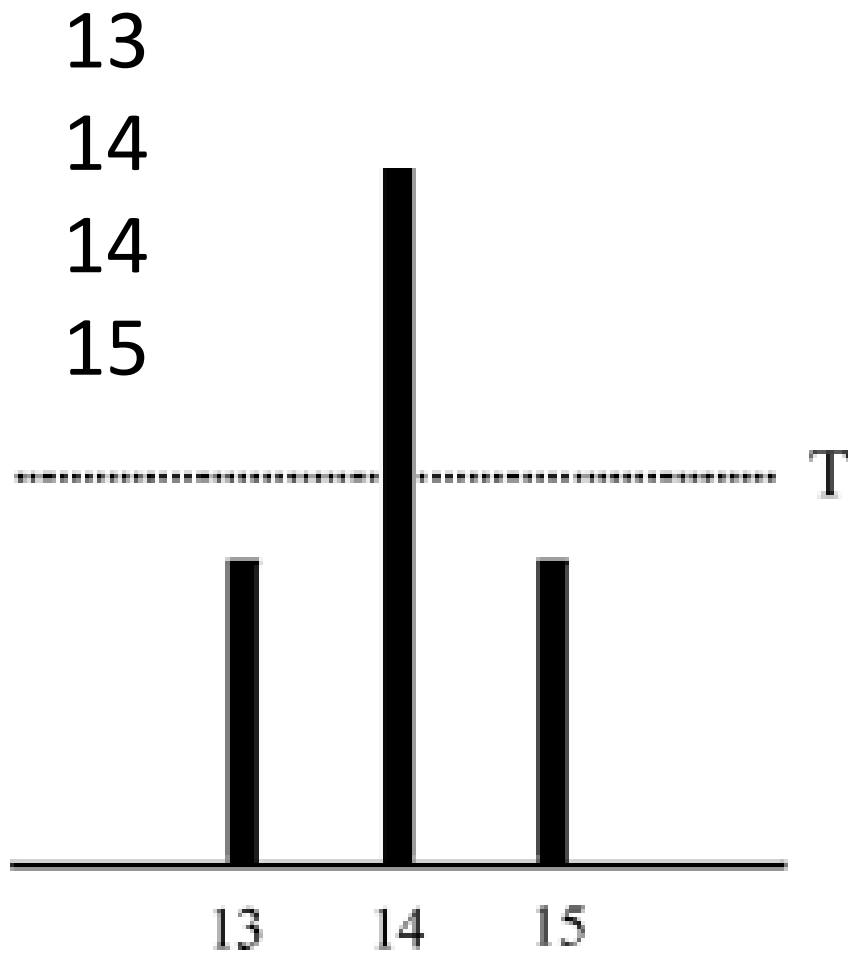
$$\binom{n}{m_1, m_2, \dots, m_k} = \frac{n!}{m_1! m_2! \dots m_k!}$$

$n$  = total number of alleles at the locus.

$m$  = number of times each allele is seen.

# Determine the Permutations for this example

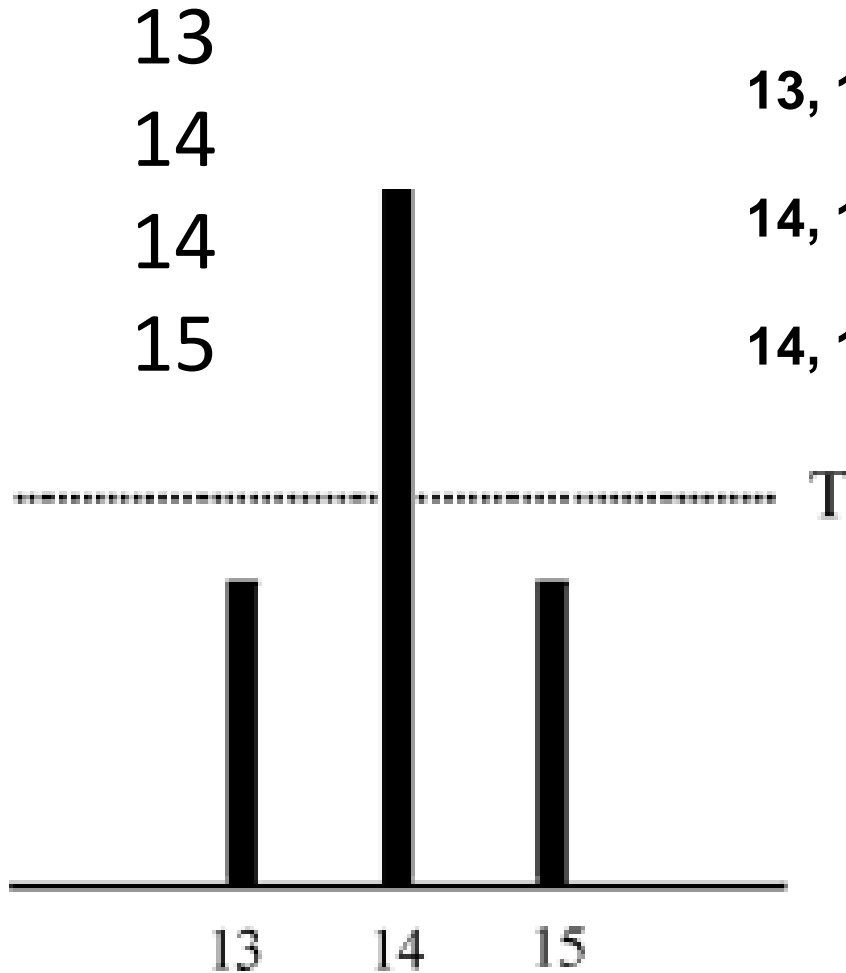
## Allelic Vectors



$$\begin{aligned}
 & \frac{4!}{1!2!1!} \\
 & = \frac{4 \times 3 \times 2 \times 1}{1 \times 2 \times 1} \\
 & = 12
 \end{aligned}$$

# Let's Prove It!

## Allelic Vectors



$$13, 14 \text{ and } 14, 15 = 2ab \times 2bc = 4ab^2c$$

$$13, 15 \text{ and } 14, 14 = 2ac \times b^2 = 2ab^2c$$

$$14, 15 \text{ and } 13, 14 = 2bc \times 2ab = 4ab^2c$$

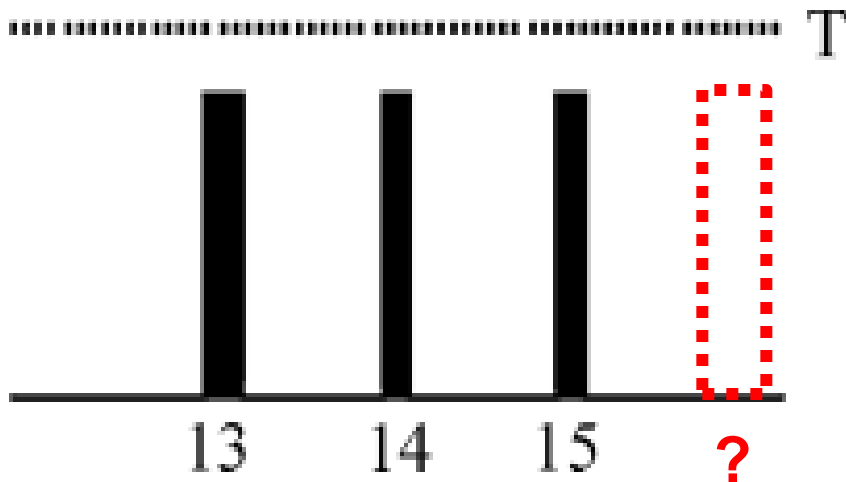
$$14, 14 \text{ and } 13, 15 = b^2 \times 2bc = 2ab^2c$$

$$= 12ab^2c$$

$$= 12$$

# Assign Allele Designations

- Use “F” as a placeholder to consider alleles that may have dropout.

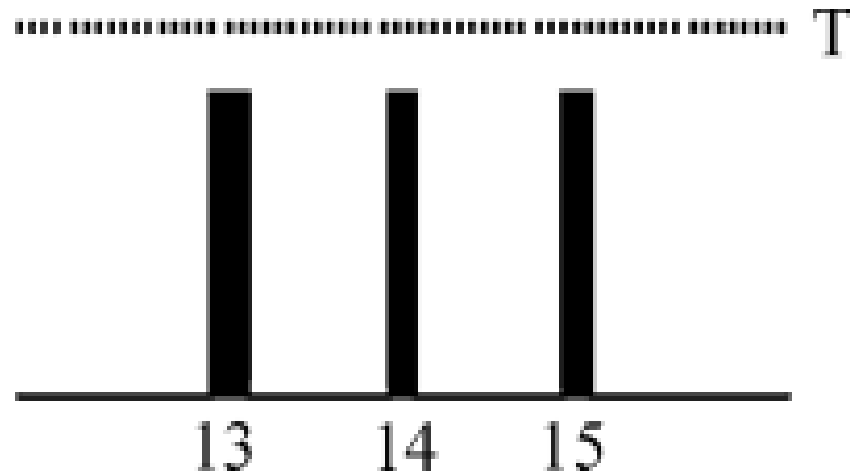


Assume 2 Contributors  
3 peaks – 3 alleles

Allelic Vector  
13,14,15,F

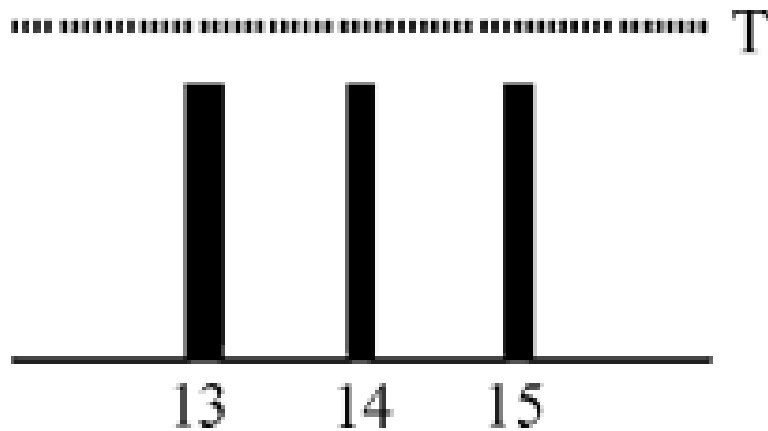
# Assign Probability using the F-model

- Calculate the number of permutations using “F” as a placeholder and then drop it from the equation.



# Assign Probability using the F-model

$$\Pr(13,14,15,F|X) = \frac{4!}{1!1!1!1!} \Pr(13,14,15,F|X)$$



$$= 24\Pr(13,14,15|X)$$

# Apply the Sampling Formula (Balding and Nichols 1994)

$$\frac{x \theta + (1 - \theta)p_a}{1 + (n - 1) \theta}$$

$x$  = value calculated from the F-model.

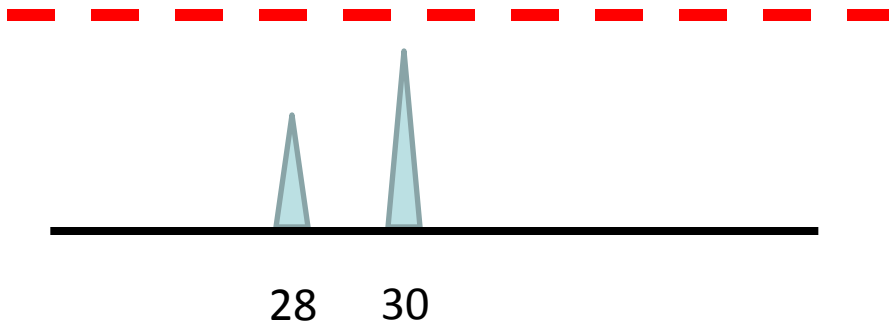
$p_a$  = frequency of the “a” allele.

$\theta$  = coancestry coefficient ( $F_{ST}$ ).

$n$  = number of alleles.



# A Worked Example



POI = 28, 30

2 peaks – 4 alleles

D21

Assume 2 contributors

Allele 28 = 107 RFU

Allele 30 = 198 RFU

ST = 200 RFU

Allelic Vector

28,30,F,F

# Permutations and Probability

$$\Pr(28,30,F,F \mid 28,30) =$$

$$\frac{4!}{1!1!2!} \Pr(28,30,F,F \mid 28,20)$$

$$= 12\Pr(28,30 \mid 28,30)$$

# Apply the Sampling Formula (Balding and Nichols 1994)

$$\Pr(A|X) = \frac{x\theta + (1 - \theta) p_a}{1 + (n - 1)\theta}$$

$$\Pr(E|H_p) = 1$$

$$\Pr(E|H_d) = 12\Pr(28,30|28,30)$$

$$\frac{12(\theta(1 - \theta) p_{28})(\theta + (1 - \theta) p_{30})}{(1 + \theta)(1 + 2\theta)}$$

$$\text{LR} = 1.86$$

# Kelly *et al.*

- Other models including the “Q” method and the Unconstrained Combinatorial “UC” method (no peak height info).
- The UC method overestimates the LR and is not appropriate. The “Q” model performs better than the “F” model, but is more mathematically intense...

# The “Q” Model for D21 (28,30)

Allelic vector (28,30)

$\Pr(E|Hp) = 1$

$$4\Pr(28, 28, 28, 30|28, 30) + 6\Pr(28, 28, 30, 30|28, 30) + 4\Pr(28, 30, 30, 30|28, 30) + 12\Pr(28, 28, 30, Q|28, 30) \\ + 12\Pr(28, 30, 30, Q|28, 30) \\ + 12\Pr(28, 30, Q, Q|28, 30)$$

$$\Pr(E|Hd) = 2\Pr(28, 30|28, 30) \times \left[ \begin{array}{l} 6 - 6\Pr(28|28, 28, 30, 30) - 6\Pr(30|28, 28, 30, 30) + 2\Pr(28, 28|28, 28, 30, 30) \\ + 2\Pr(30, 30|28, 28, 30, 30) \\ + 3\Pr(28, 30|28, 28, 30, 30) \end{array} \right]$$

$$\frac{2(\theta(1-\theta)p_{28})(\theta + (1-\theta)p_{30})}{(1+\theta)(1+2\theta)} \times \left[ \begin{array}{l} 6 - \frac{6(2\theta + (1-\theta)p_{28})}{(1+3\theta)} - \frac{6(2\theta + (1-\theta)p_{30})}{(1+3\theta)} + \frac{2(2\theta + (1-\theta)p_{28})(3\theta + (1-\theta)p_{28})}{(1+3\theta)(1+4\theta)} + \frac{2(2\theta + (1-\theta)p_{30})(3\theta(1-\theta)p_{30})}{(1+3\theta)(1+4\theta)} \\ + \frac{3(2\theta + (1-\theta)p_{28})(2\theta + (1-\theta)p_{30})}{(1+3\theta)(1+4\theta)} \end{array} \right]$$

# LR with Pr(Drop-out)

Forensic Science International: Genetics 4 (2009) 1–10



Contents lists available at ScienceDirect

Forensic Science International: Genetics

journal homepage: [www.elsevier.com/locate/fsig](http://www.elsevier.com/locate/fsig)



## Interpreting low template DNA profiles

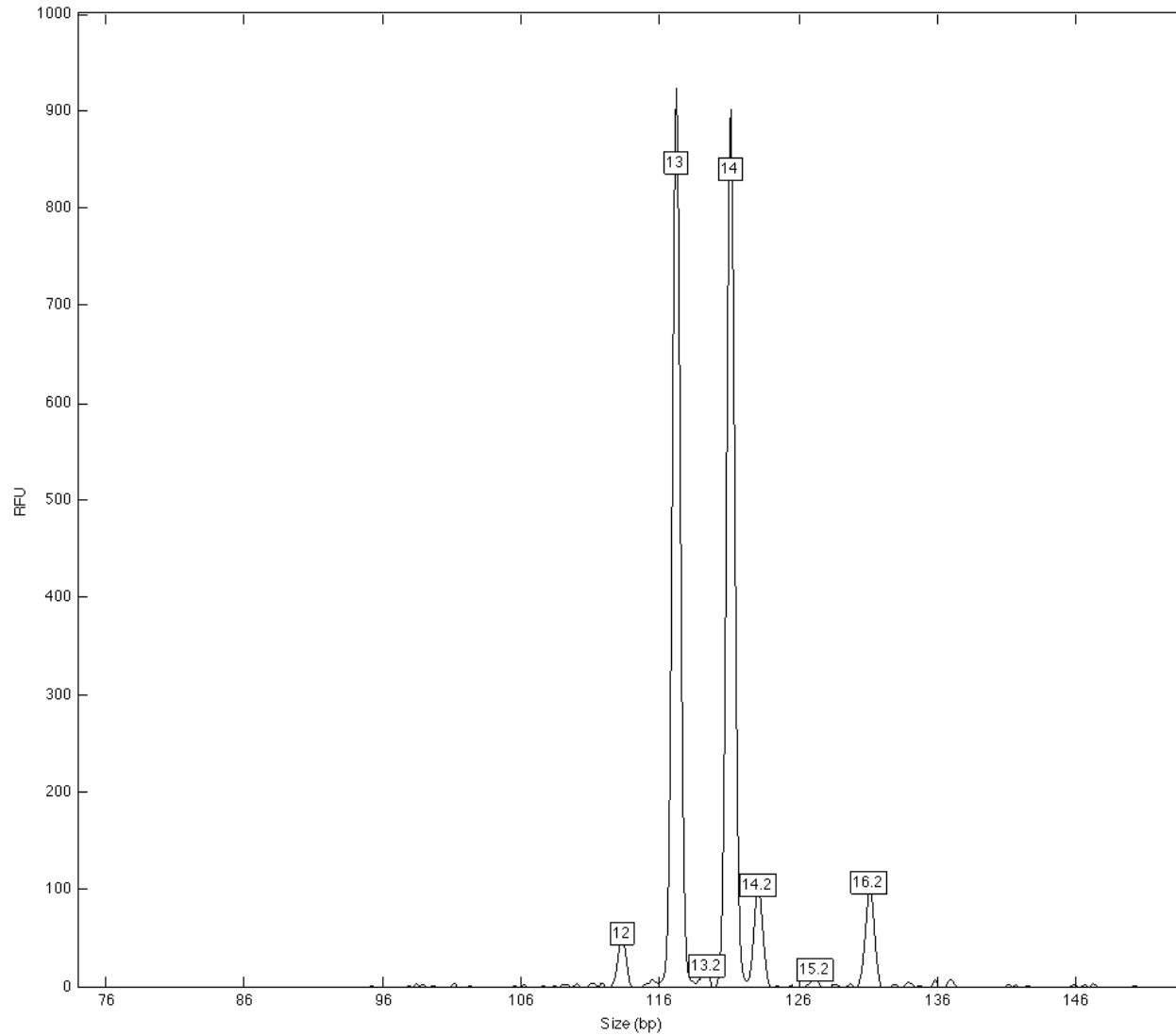
David J. Balding<sup>a,\*</sup>, John Buckleton<sup>b</sup>

<sup>a</sup> Department of Epidemiology and Public Health, Imperial College, St Mary's Campus, Norfolk Place, London W2 1PG, UK

<sup>b</sup> ESR Private Bag 92021, Auckland, New Zealand

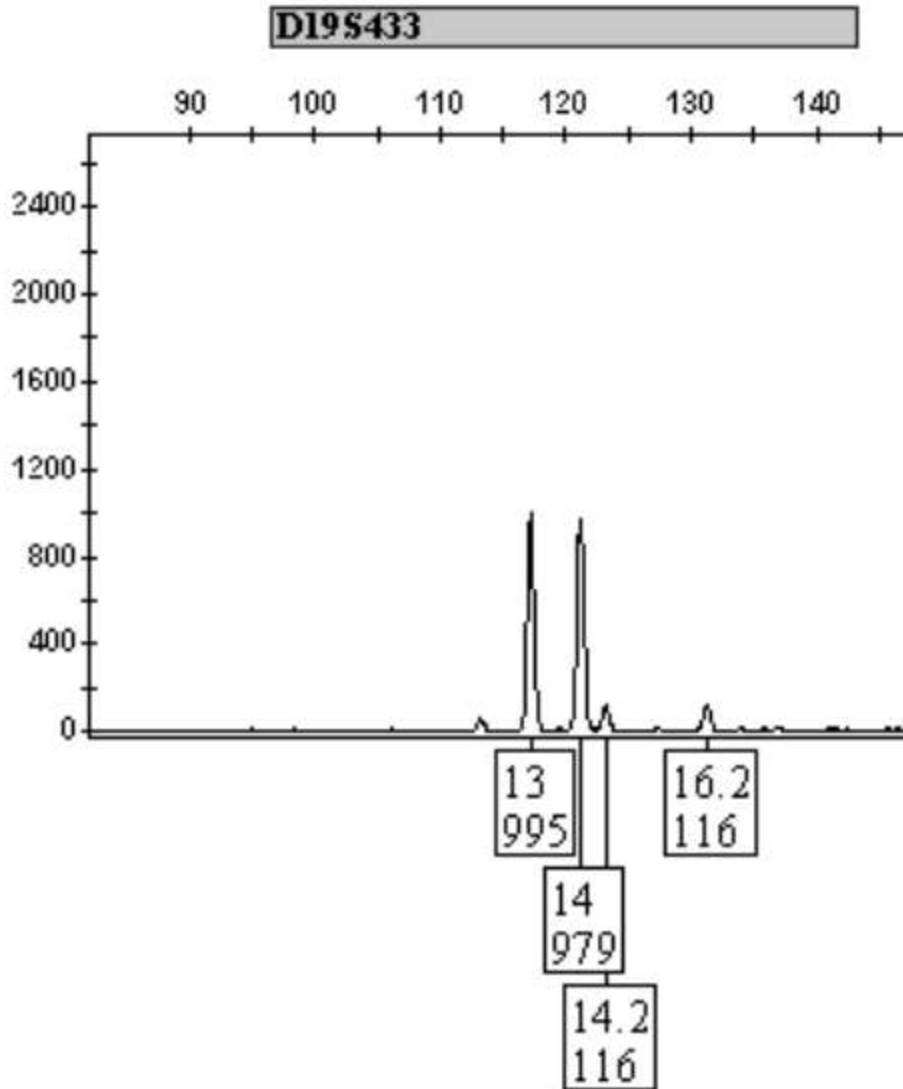


# 3 person mixture – 1 major, 2 minor



D19S433

# 3 Person Mixture



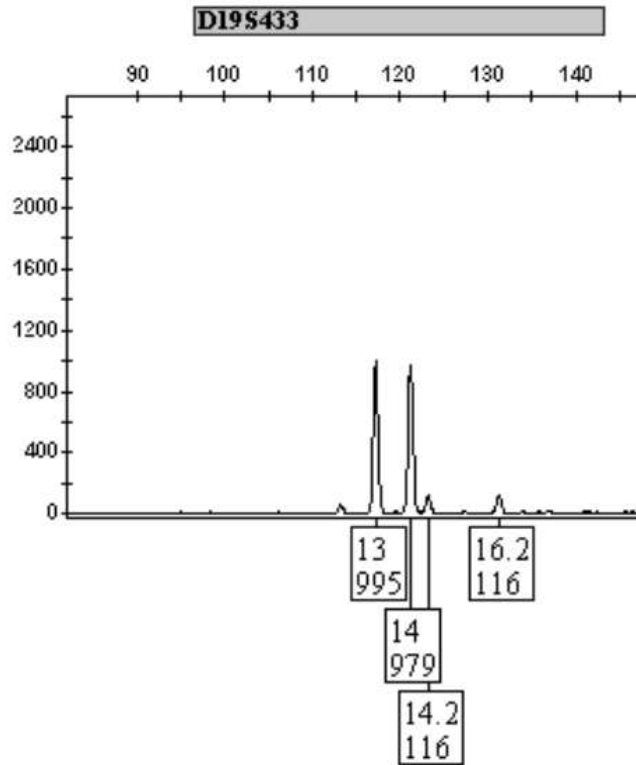
$$V = 13, 14$$

$$CP = 13, 14.2$$

$$S = \mathbf{15}, 16.2$$

$$\frac{P(E | H_1)}{P(E | H_2)}$$





$$V = 13, 14$$

$$CP = 13, 14.2$$

$$S = 15, 16.2$$

$$\Pr(\text{Drop-out}) = 10\%$$

$$\Pr(\text{Drop-in}) = 1\%$$

$$P(E | H_1) = \Pr(\text{No Drop-out at 16.2}) \Pr(\text{Drop-out at 15}) \Pr(\text{No Drop-in})$$

$$=$$

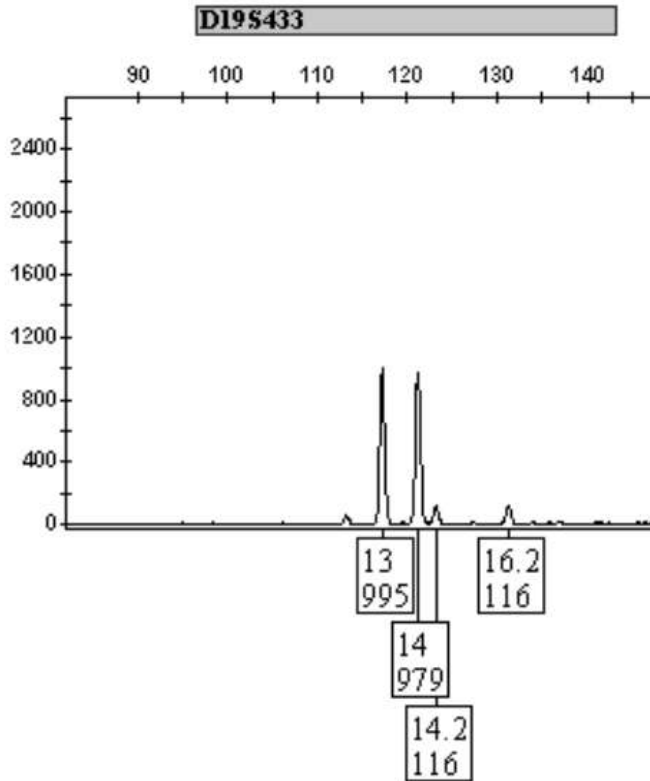
$$0.90$$

$$0.10$$

$$0.99$$

$$= 0.0891$$

# 3 Person Mixture



$$V = 13, 14$$

$$CP = 13, 14.2$$

$$S = 15, 16.2$$

$$\frac{P(E | H_1)}{P(E | H_2)} = 0.0891$$

Keith Inman, Norah Rudin and Kirk Lohmueller have modified the Balding program to incorporate your own data for estimating  $\Pr(\text{Drop-out})$ .

PAPER

*J Forensic Sci*, 2011  
doi: 10.1111/j.1556-4029.2011.01859.x  
Available online at: [onlinelibrary.wiley.com](http://onlinelibrary.wiley.com)

## CRIMINALISTICS

*Mark W. Perlin,<sup>1</sup> M.D., Ph.D.; Matthew M. Legler,<sup>1</sup> B.S.; Cara E. Spencer,<sup>1</sup> M.S.; Jessica L. Smith,<sup>1</sup> M.S.; William P. Allan,<sup>1</sup> M.S.; Jamie L. Belrose,<sup>2</sup> M.S.; and Barry W. Ducean,<sup>3</sup> Ph.D.*

Validating TrueAllele<sup>®</sup> DNA Mixture Interpretation<sup>\*,†</sup>

- Quantitative computer interpretation using Markov Chain Monte Carlo testing
- Models peak uncertainty and infers possible genotypes
- Results are presented as the Combined LR



# Monte Carlo



# What is a Markov Chain?

“A mathematical system that undergoes transitions from one state to another, between a finite or countable number of possible states. It is a random process usually characterized as memoryless: the next state depends only on the current state and not on the sequence of events that preceded it.”



Andrey Markov

<http://en.wikipedia.org/wiki/File:AAMarkov.jpg>



# Is Blackjack a Markov Chain?



# Monopoly is a Markov Chain



# Monopoly simulation

- [http://www.bewersdorff-online.de/amonopoly/monopoly\\_m.htm](http://www.bewersdorff-online.de/amonopoly/monopoly_m.htm)



2.83% 2.61% 1.04% 2.57% 2.99% 2.89% 2.54% 2.52% 2.65% 2.44%

Higher Prob.  
of being in jail



9.46%  
in jail

2.14% just vis. 2.17% 2.19% 0.82% 2.19% 2.8% 2.19% 2.04% 1.77% 2.01% 2.91%

# True Allele also uses a Bayesian Analysis of the data



# Bayes' Theorem

$$\frac{P(H_1|E)}{P(H_2|E)} = \frac{P(H_1)}{P(H_2)} \cdot \frac{P(E|H_1)}{P(E|H_2)}$$

Posterior  
Probability

Prior  
Probability

Likelihood  
Ratio



**Prior Prob = 0.5   LR = 10,000/1**

**Yes - White      Posterior Prob =  
No - Black      0.5 x 10,000  
                         = 99.98%**

**9,999 days later**

# Little Orphan Alien...



The sun'll come out tomorrow

With a 99.98% probability

tomorrow there'll be sun

# Real-life Example

# Air France Flight 447

- June 1, 2009, Air France Flight 447, (Rio de Janeiro to Paris) with 228 passengers and crew disappeared over the South Atlantic.
- 33 bodies were located from June 6-10, 2009.
- By June 17, 50 bodies had been recovered in two distinct groups more than 50 miles apart.



# Air France Flight 447

- Initial searches conclude at the end of August.
- More searches in 2009 and 2010.
- In July 2010, the US-based search consultancy Metron was asked by BEA (France) to examine the results. Metron uses a Bayesian approach to find the potential crash site.
- <http://www.informs.org/ORMS-Today/Public-Articles/August-Volume-38-Number-4/In-Search-of-Air-France-Flight-447>



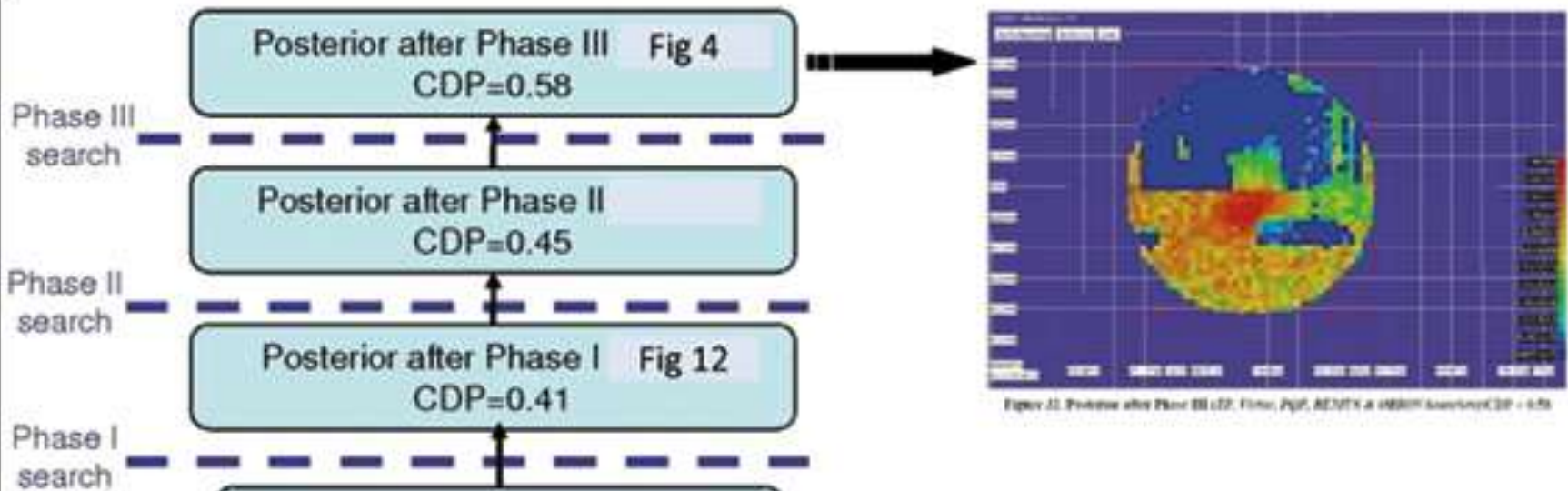
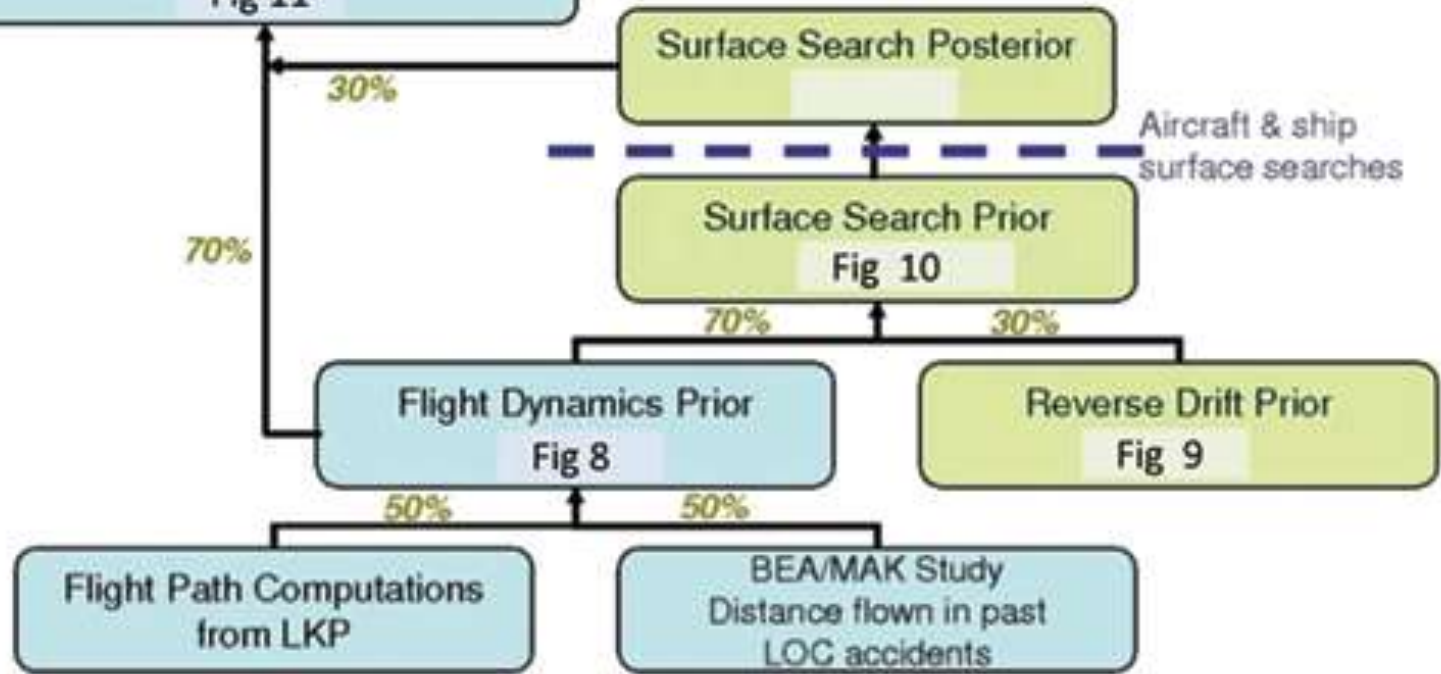
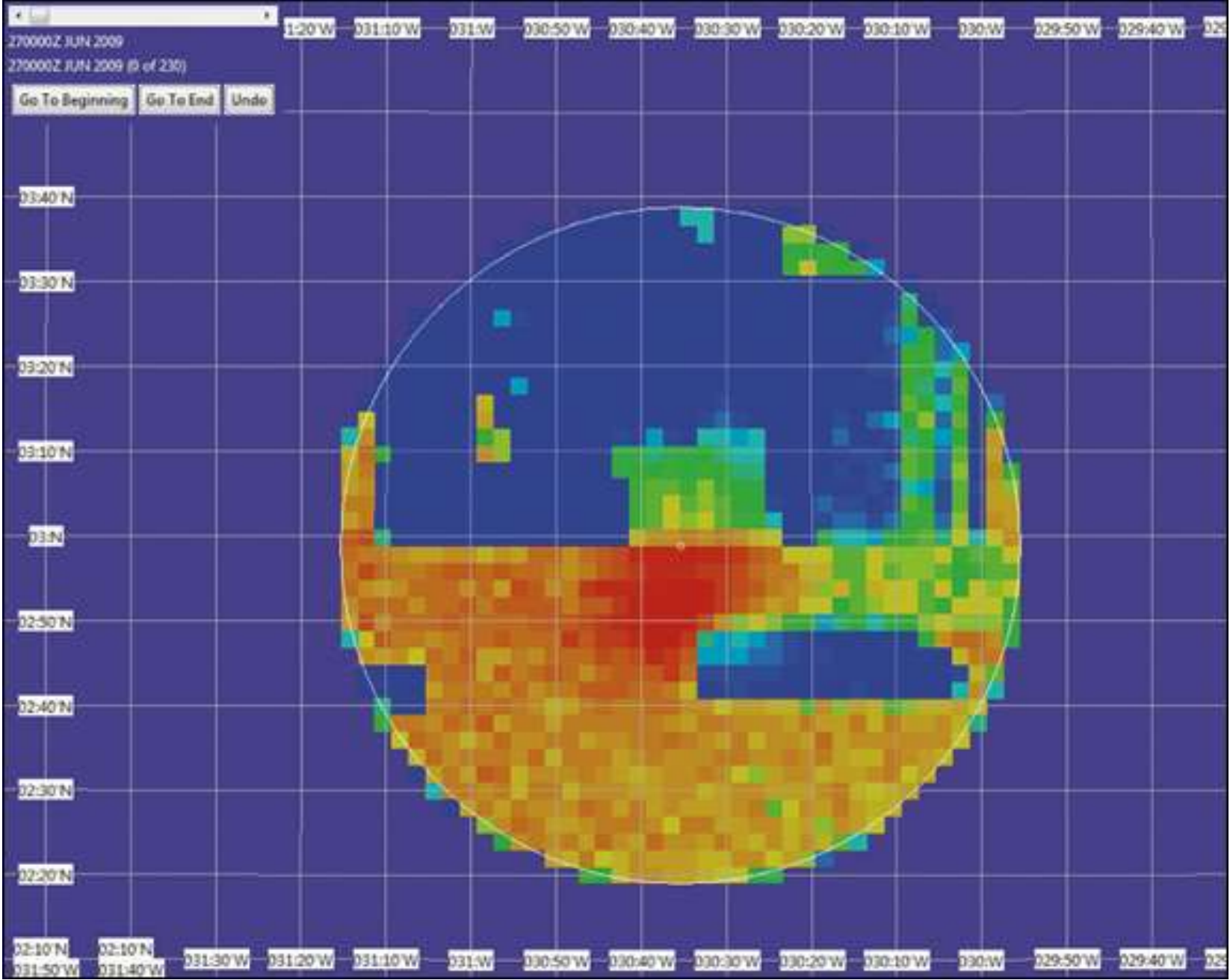


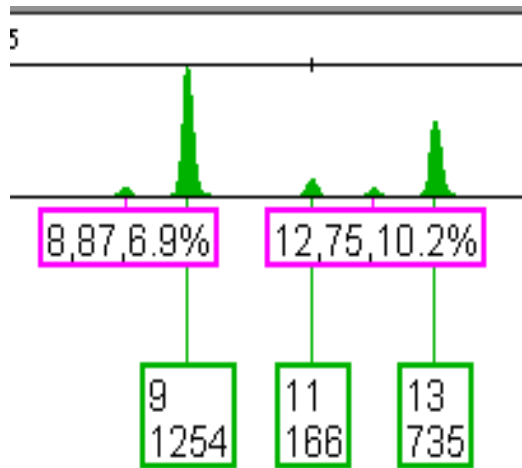
Figure 11. Posterior after Phase III CDP. From: Pugh, AEWMA & IMA/AT&T Associates CDP - 0.58



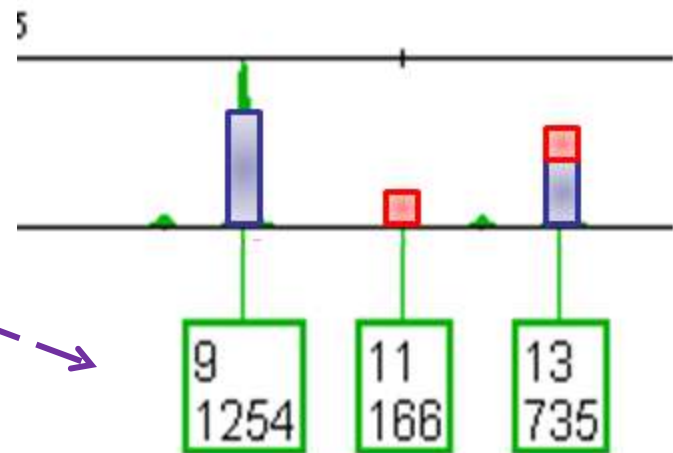


# Air France Flight 447

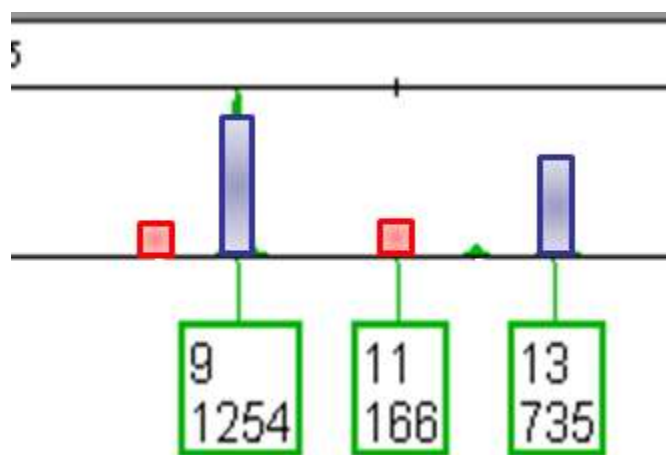
- January 2011 – Metron published their findings on the BEA website using a Bayesian approach to find the potential crash site.
- Fourth phase initiated in April 2011 – debris field was found within a week. Flight recorders were found in May 2011.
- <http://www.informs.org/ORMS-Today/Public-Articles/August-Volume-38-Number-4/In-Search-of-Air-France-Flight-447>



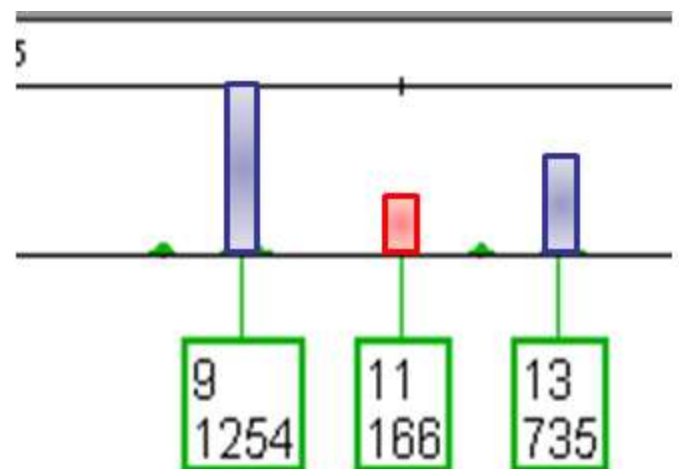
9	11	13
1254	166	735



9	11	13
1254	166	735



9	11	13
1254	166	735



9	11	13
1254	166	735

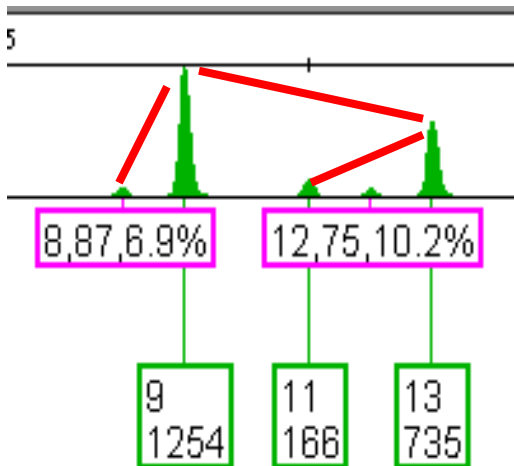
# Probabilistic Modeling of TA

Mathematical Modeling  
of the Data

50-100,000  
Simulations  
(MCMC) →

Probable **Genotypes**  
to explain the mixture

PHR, Mix Ratio, Stutter etc...



Genotypes	Probability
<b>9,11</b>	<b>76%</b>
<b>11,11</b>	<b>15%</b>
<b>11,13</b>	<b>2%</b>
<b>8,11</b>	<b>2%</b>
<b>11,12</b>	<b>2%</b>
<b>9,9</b>	<b>1%</b>
<b>9,12</b>	<b>&lt;1%</b>
<b>10,11</b>	<b>&lt;1%</b>
<b>8,12</b>	<b>&lt;1%</b>
<b>8,9</b>	<b>&lt;1%</b>

# True Allele Software (Cybergenetics)

- We purchased the software in September 2010.
- Three day training at Cybergenetics (Pittsburgh, PA) in October.
- Software runs on a Linux Server with a Mac interface.



# True Allele Casework Workflow

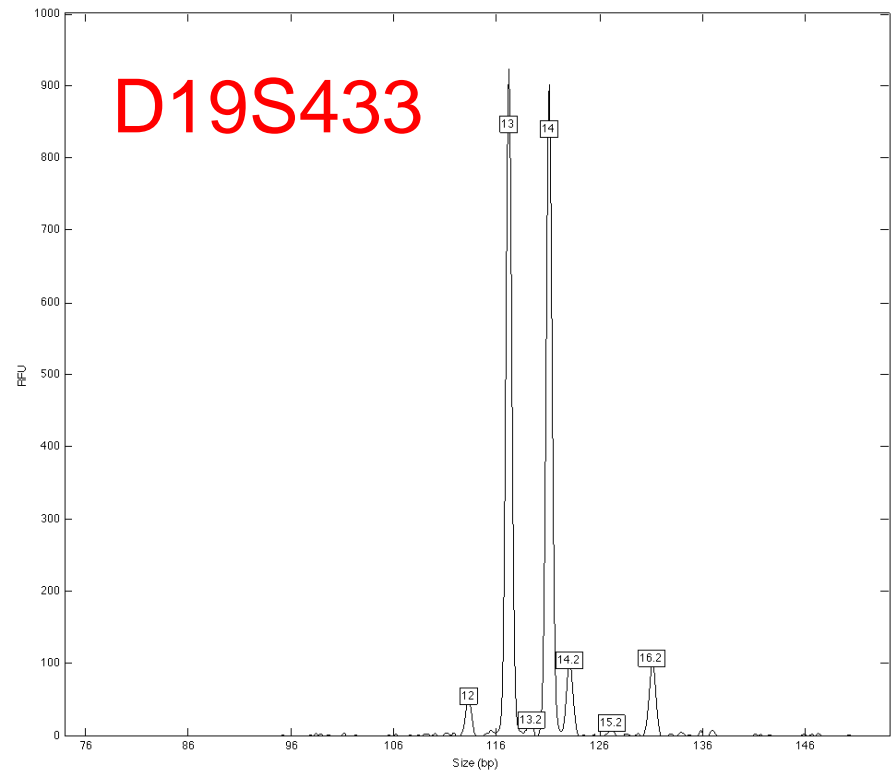
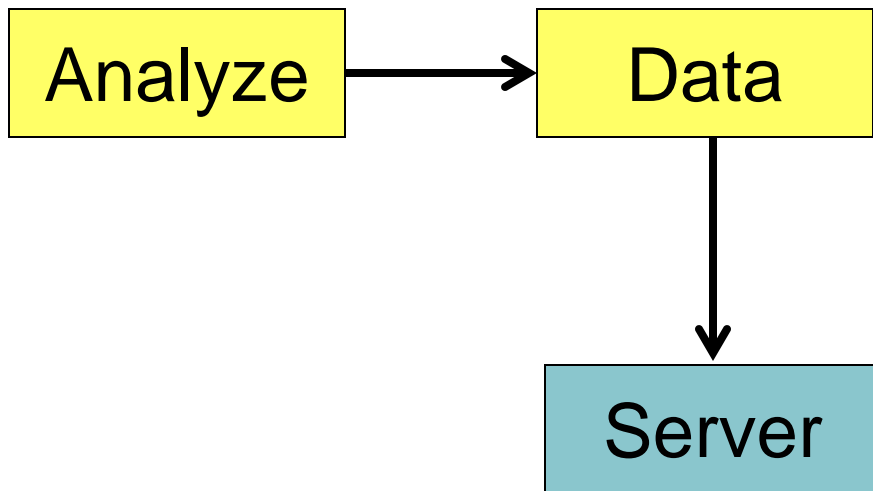
## 5 Modules

Analyze

.fsa files imported  
Size Standard check  
Allelic Ladder check  
Alleles are called

# True Allele Casework Workflow

## 5 Modules

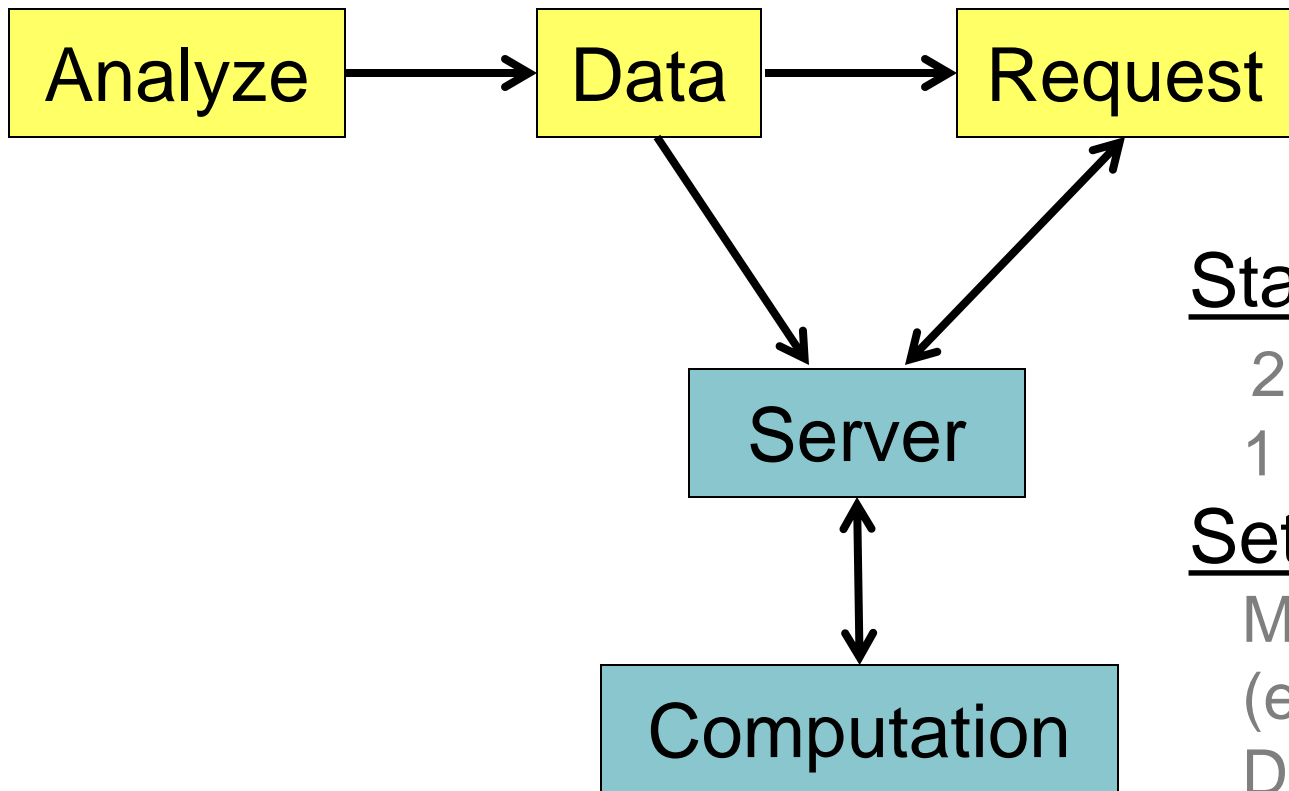


*All Peaks above 10 RFU are considered*



# True Allele Casework Workflow

## 5 Modules



### State Assumptions

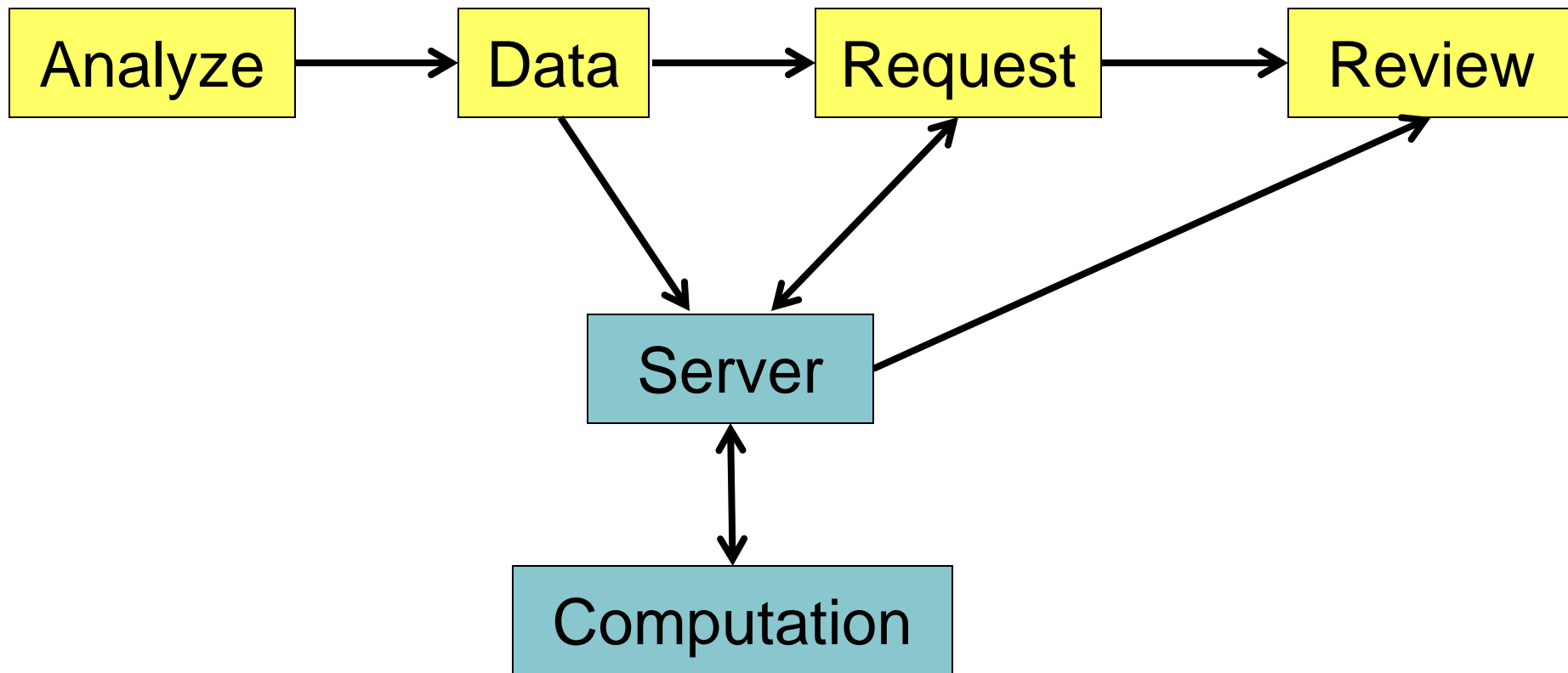
2, 3, 4 unknowns  
1 Unk with Victim?

### Set Parameters

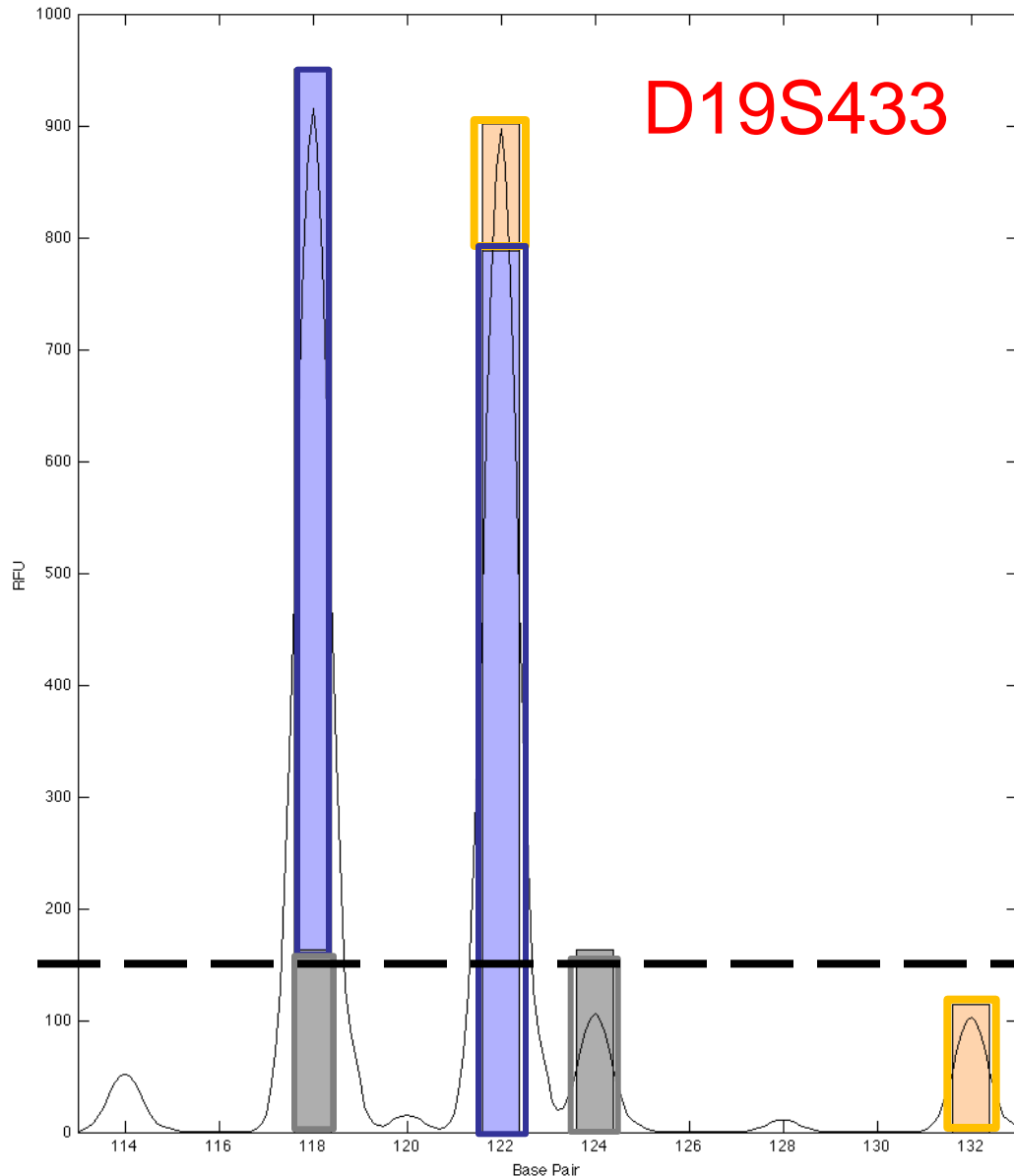
MCMC modeling  
(e.g. 50K)  
Degradation?

# True Allele Casework Workflow

## 5 Modules



# Review of One Replicate (of 50K)



3P mixture,  
2 Unknowns,

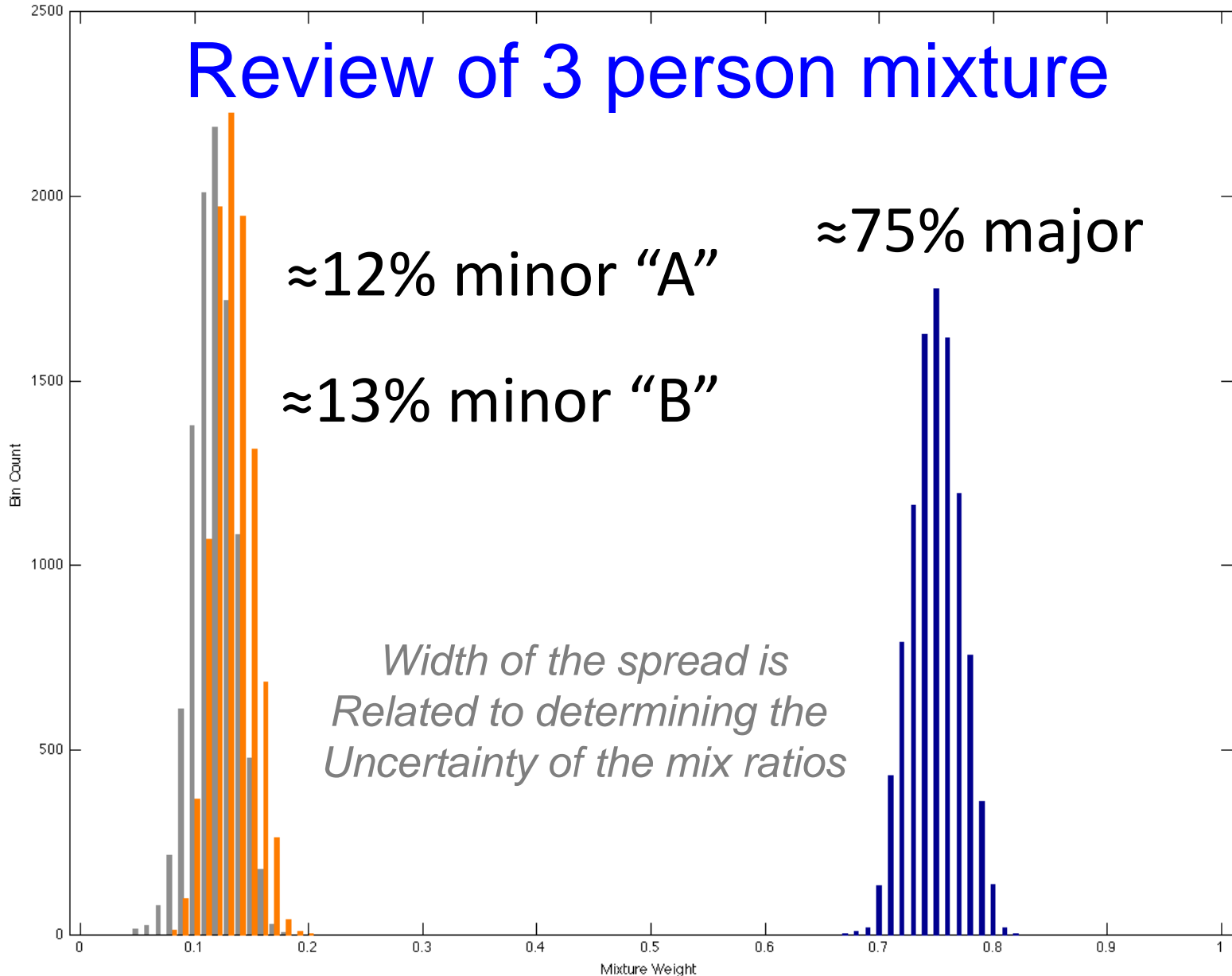
Conditioned  
on the Victim  
(major)

Good fit of the  
data to the model

— 150 RFU

# Review of 3 person mixture

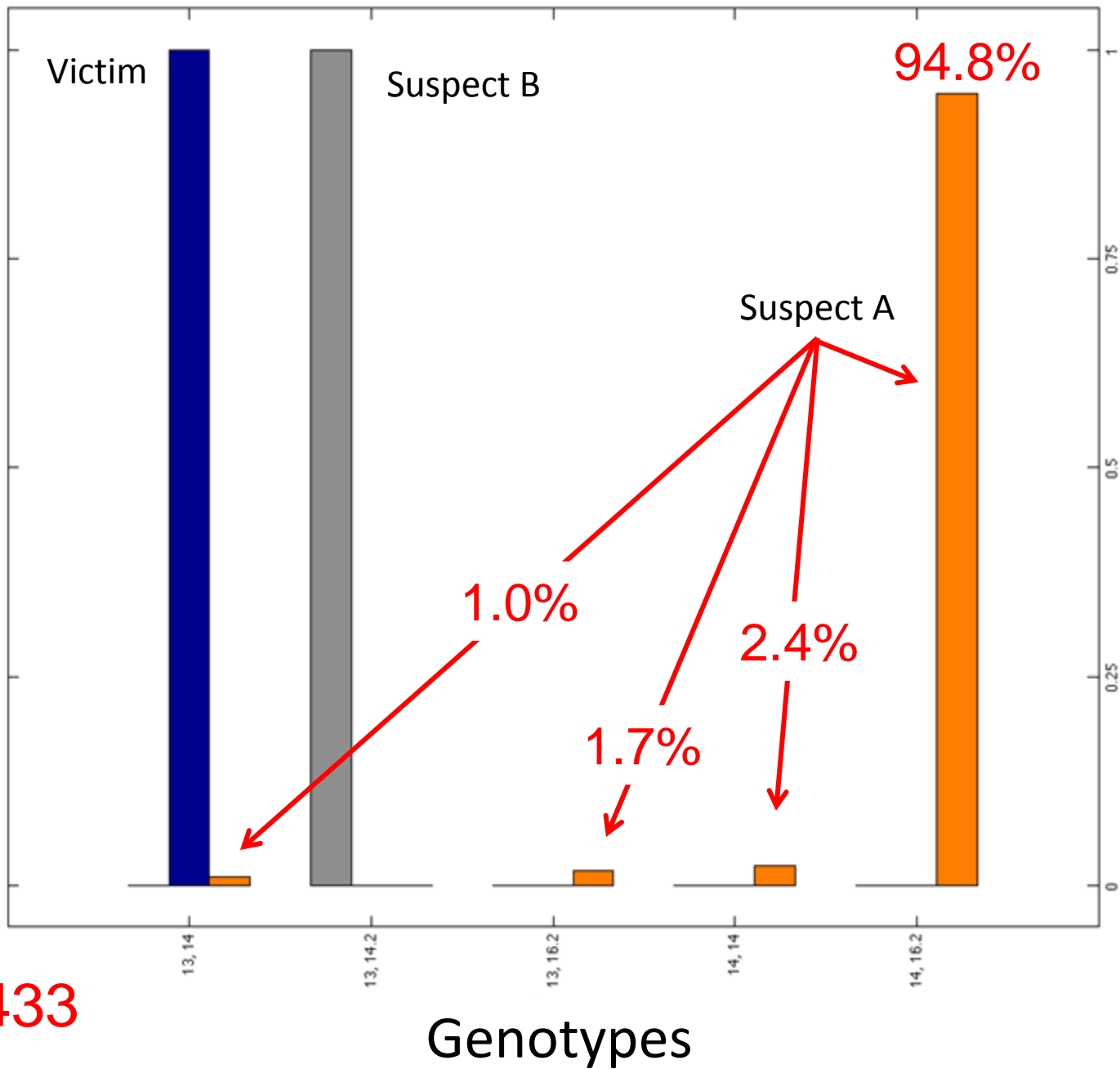
Bin Count



Mixture Weight

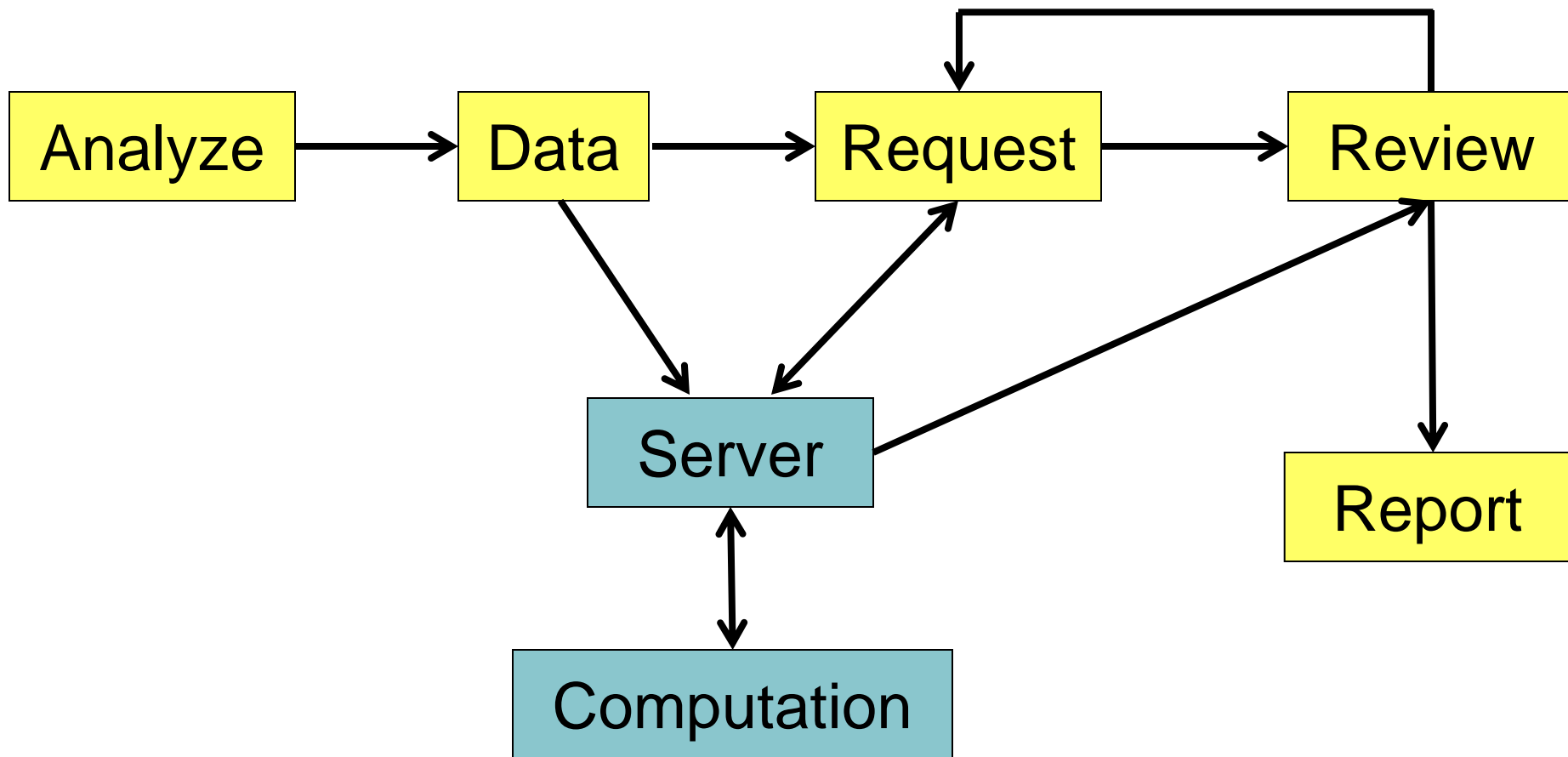
D19S433

Genotype Probability



# True Allele Casework Workflow

## 5 Modules



# Determining the LR for D19S433

Suspect A = 14, 16.2

$$H_p = 0.967$$

	Allele Pair	Probability Before Conditioning
→	14, 16.2	0.967
	14, 14	0.003
	13, 16.2	0.026
	13, 14	0.001

$$LR = \frac{0.967}{\quad}$$

# Determining the LR for D19S433

Suspect A = 14, 16.2

$H_P = 0.967$

Allele Pair	Probability Before Conditioning	Genotype Frequency	Probability * Genotype Freq
14, 16.2	0.967	0.0120	0.01164
14, 14	0.003	0.0498	0.00013
13, 16.2	0.026	0.0131	0.00034
13, 14	0.001	0.1082	0.00009
		sum	<b>0.0122</b>

$$LR = \frac{0.967}{0.0122} = 79.26 \quad H_D$$



# Combined LR = 5.6 Quintillion

locus	allele pair x	Likelihood l(x)	Genotype Probability Distribution			Weighted Likelihood		Likelihood Ratio	
			Questioned q(x)	Reference r(x)	Suspect s(x)	Numerator l(x)*s(x)	Denominator l(x)*r(x)	LR	log(LR)
CSF1PO	11, 12	0.686	0.778	0.1448	1	0.68615	0.1292	5.31	0.725
D13S317	9, 12	1	1	0.0291	1	0.99952	0.02913	34.301	1.535
D16S539	9, 11	0.985	0.995	0.1238	1	0.98451	0.12188	8.036	0.905
D18S51	13, 17	0.999	1	0.0154	1	0.99915	0.01543	64.677	1.811
D19S433	14, 16.2	0.967	0.948	0.012	1	0.96715	0.01222	79.143	1.898
D21S11	28, 30	0.968	0.98	0.0872	1	0.96809	0.08648	11.194	1.049
D2S1338	23, 24	0.998	1	0.0179	1	0.99831	0.01787	55.866	1.747
D3S1358	15, 17	0.988	0.994	0.1224	1	0.98759	0.12084	8.14	0.911
D5S818	11, 11	0.451	0.394	0.0537	1	0.45103	0.07309	6.17	0.79
D7S820	11, 12	0.984	0.978	0.0356	1	0.98383	0.03617	27.198	1.435
D8S1179	13, 14	0.203	0.9	0.1293	1	0.20267	0.02993	6.771	0.831
FGA	21, 25	0.32	0.356	0.028	1	0.31986	0.01906	16.783	1.225
TH01	7, 7	0.887	0.985	0.1739	1	0.88661	0.15588	5.687	0.755
TPOX	8, 8	1	1	0.1375	1	1	0.13746	7.275	0.862
vWA	15, 20	0.998	0.996	0.0057	1	0.99808	0.00569	174.834	2.243

# Results

- Results are expressed as logLR values

$$\text{LR} = 1,000,000 = 10^6$$

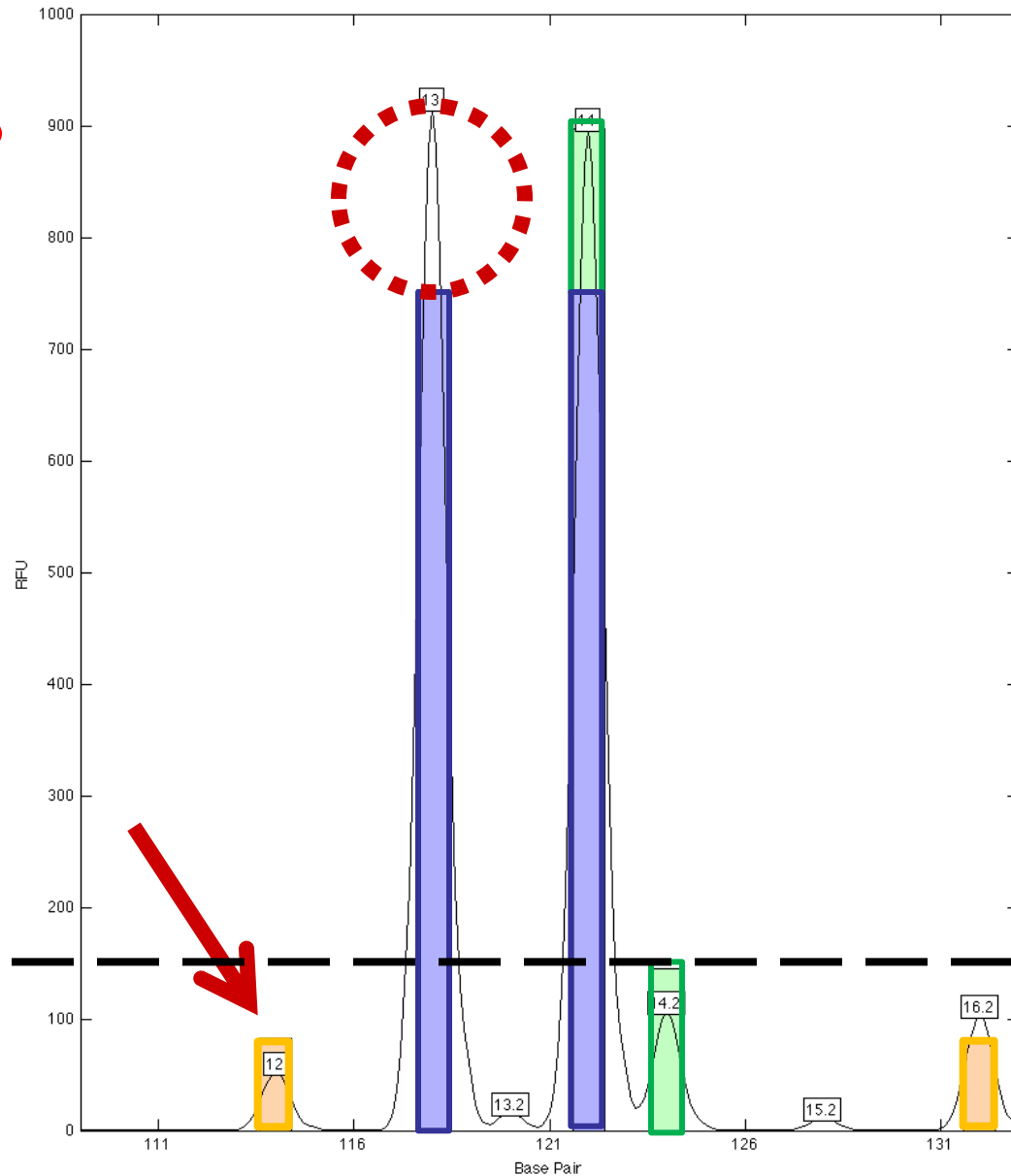
$$\log(\text{LR}) = \log 10^6$$

$$\log(\text{LR}) = 6 * \log 10 (1)$$

$$\log(\text{LR}) = 6$$

# Review of One Replicate (of 50K)

D19S433



3P mixture,  
3 Unknowns

Poor fit of the  
data to the  
model

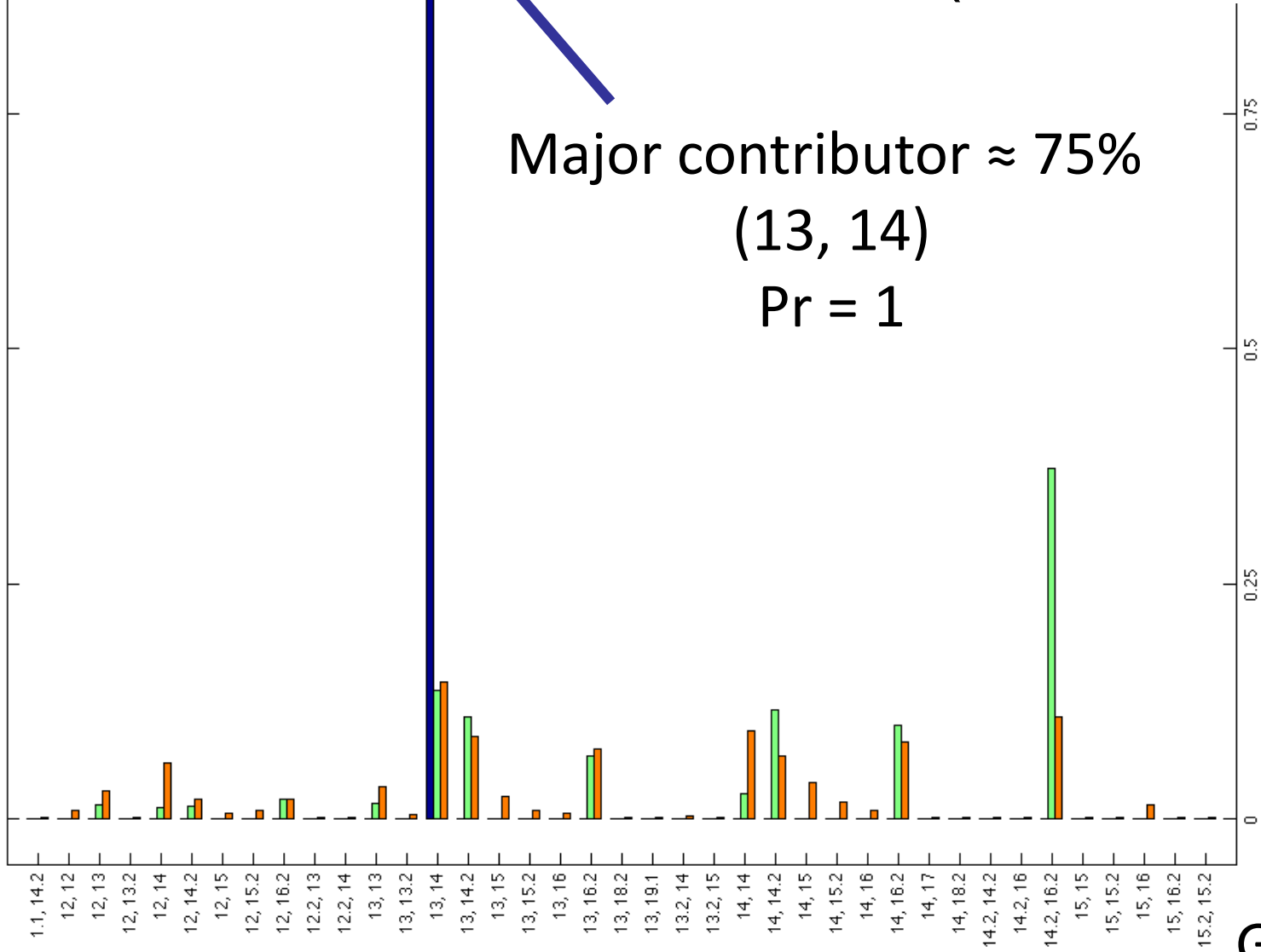
150 RFU

# No Conditioning (3 Unknowns)

D19S433

Genotype Probability

Major contributor  $\approx 75\%$   
(13, 14)  
Pr = 1

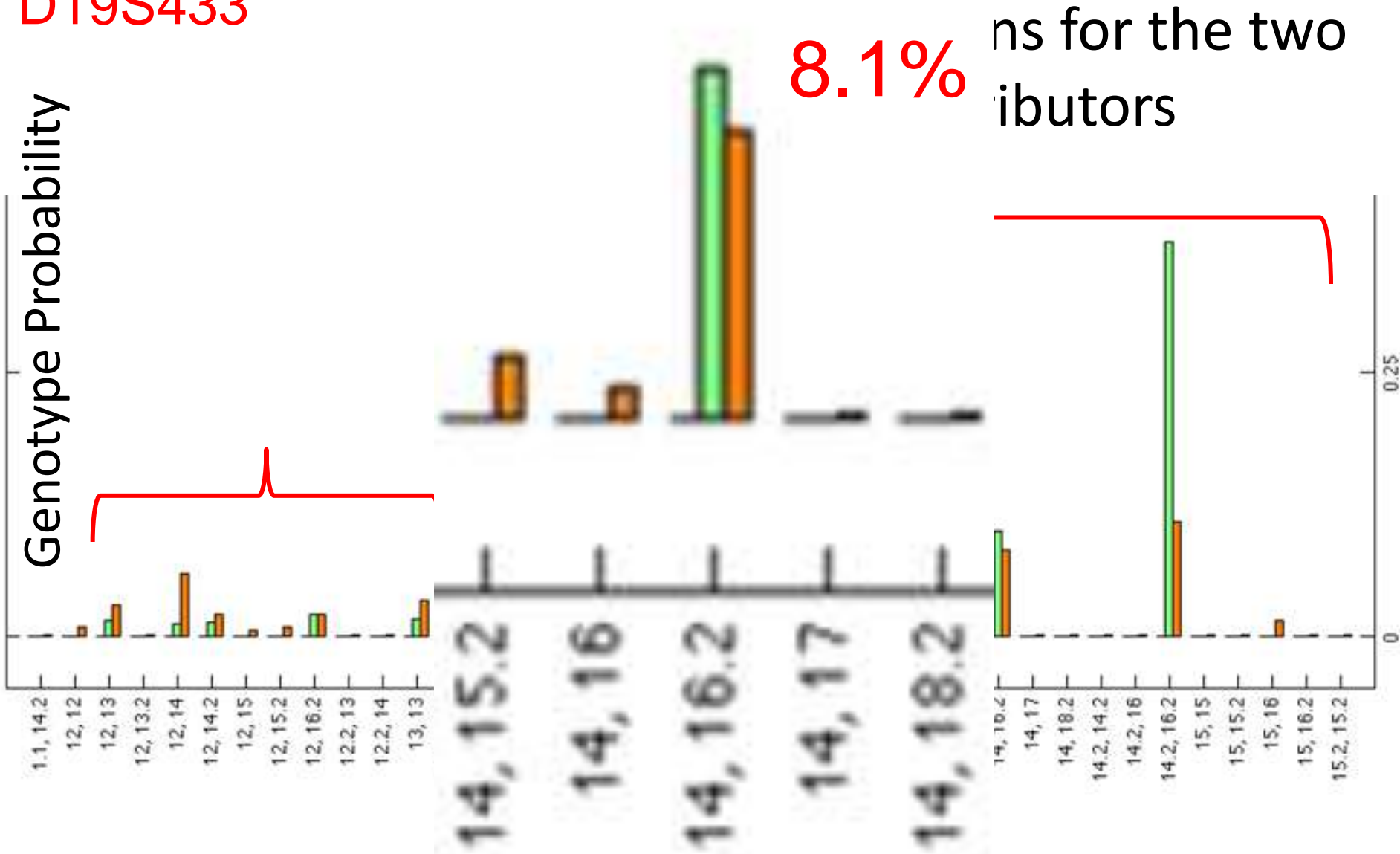


Genotypes

# No Conditioning (3 Unknowns)

D19S433

Genotype Probability



locus	allele pair	L	Q	R	S	L*S	L*R	LR	log(LR)
D19S433	13 , 14	0.002	0.146	0.1082			0.00020		
	14.2, 16.2	0.270	0.109	0.0044			0.00118		
	14 , 14	0.002	0.093	0.0498			0.00008		
	13 , 14.2	0.017	0.088	0.0392			0.00068		
	14 , 16.2	0.013	0.081	0.0120	1	0.01295	0.00016		
	13 , 16.2	0.018	0.074	0.0131			0.00023		
	14 , 14.2	0.009	0.067	0.0361			0.00031		
	12 , 14	0.002	0.059	0.0498			0.00012		
	14 , 15	0.001	0.038	0.0343			0.00002		
	13 , 13	0.001	0.034	0.0587			0.00007		
	12 , 13	0.002	0.029	0.0541			0.00010		
	13 , 15	0.001	0.024	0.0373			0.00002		
	12 , 16.2	0.017	0.021	0.0060			0.00010		
	12 , 14.2	0.013	0.020	0.0180			0.00023		
	14 , 15.2	0.001	0.018	0.0275			0.00003		
	15 , 16	0.002	0.015	0.0006			0.00000		
	13 , 15.2	0.001	0.009	0.0299			0.00003		
	12 , 15.2	0.003	0.009	0.0137			0.00004		
	14 , 16	0.000	0.009	0.0017			0.00000		
	12 , 12	0.004	0.009	0.0125			0.00004		
	12 , 15	0.001	0.006	0.0172			0.00001		
	13 , 16	0.000	0.006	0.0019			0.00000		
	13 , 13.2	0.001	0.004	0.0261			0.00003		
	13.2, 14	0.001	0.003	0.0240			0.00002		
	13.2, 15	0.001	0.002	0.0083			0.00001		
	14 , 18.2	0.002	0.002	0.0017			0.00000		
	13 , 19.1	0.019	0.002	0.0000			0.00000		
	12 , 13.2	0.002	0.002	0.0120			0.00003		
	14.2, 16	0.001	0.002	0.0006			0.00000		
	12.2, 13	0.001	0.002	0.0168			0.00002		
	13 , 18.2	0.002	0.001	0.0019			0.00000		
	12.2, 14	0.001	0.001	0.0155			0.00001		
	14.2, 14.2	0.004	0.001	0.0065			0.00003		
	15 , 15	0.000	0.001	0.0059			0.00000		
	15 , 15.2	0.000	0.001	0.0095			0.00000		
	14 , 17	0.001	0.001	0.0000			0.00000		
	15 , 16.2	0.000	0.001	0.0042			0.00000		
	15.2, 15.2	0.001	0.001	0.0038			0.00000		
	1.1, 14.2	0.072	0.001	0.0097			0.00069		
						0.01295	0.00385	3.367	0.527

Suspect "A"  
Genotype

39 probable  
genotypes

D19S433

Suspect A = 14, 16.2

$$H_P = 0.013$$

Allele Pair	Probability	Genotype Frequency	Prob * GenFreq
13,14	0.002	0.1082	0.00020
14.2, 16.2	0.270	0.0044	0.00118
14, 14	0.002	0.0498	0.00008
13, 14.2	0.017	0.0392	0.00068
14, 16.2	0.013	0.0120	0.00016
13, 16.2	0.018	0.0131	0.00023
etc...	etc...	etc...	etc...
		<b>Sum</b>	<b>0.00385</b>

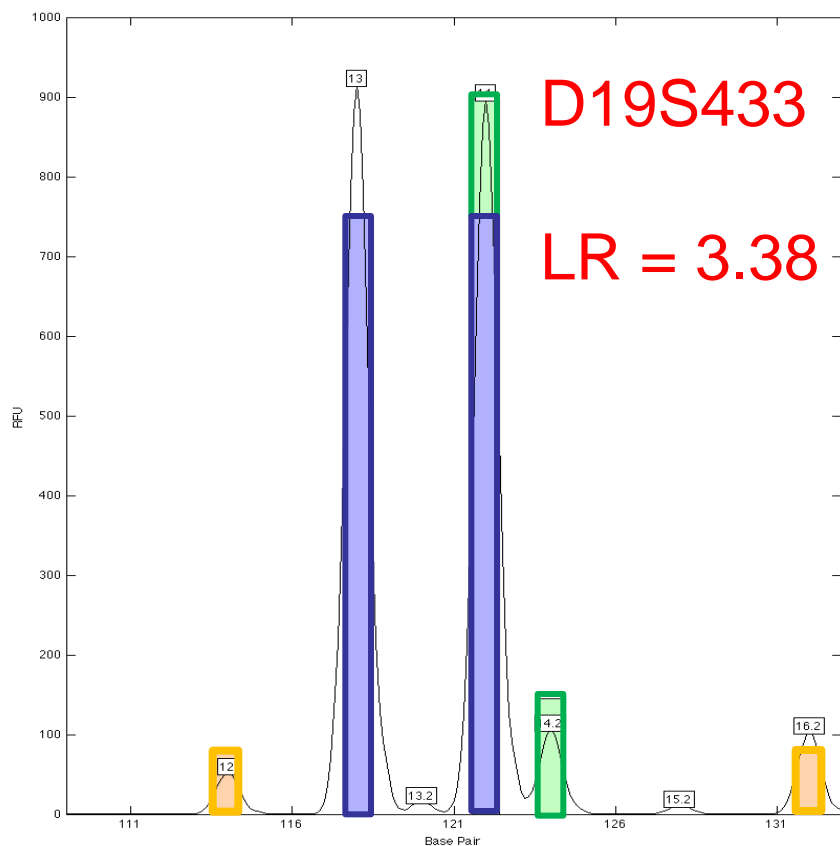
$$LR = \frac{0.013}{0.00385} = 3.38$$

$H_D$

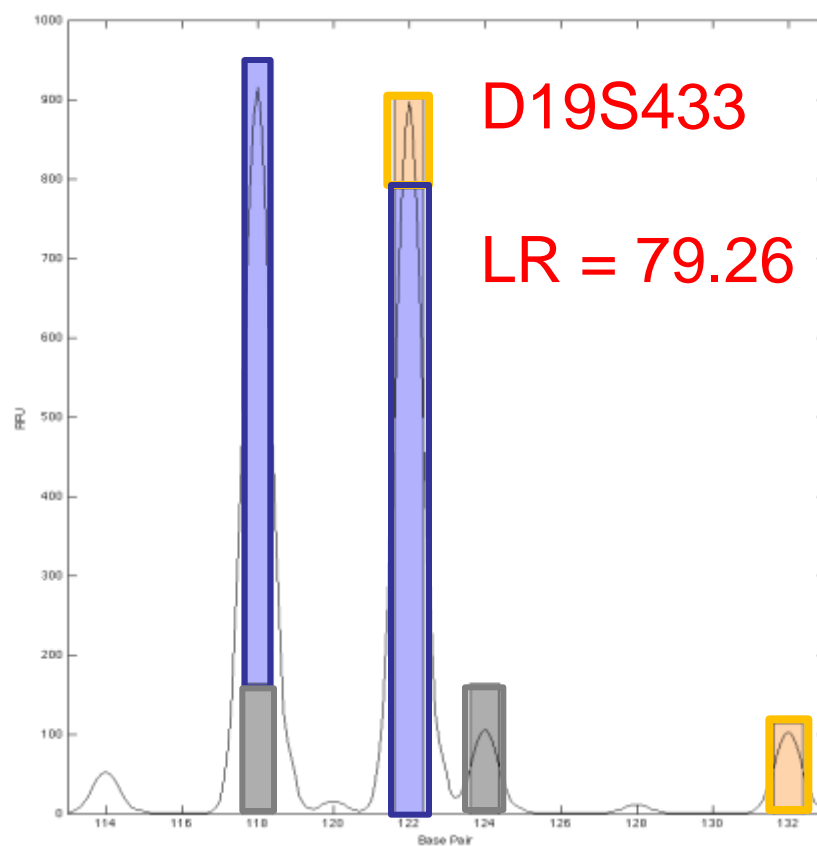
D19S433

*No Conditioning (3 Unknowns)*

# No Conditioning



# Conditioned on Victim



Profile - Combined  $\log(\text{LR})$

Suspect A  $\log(\text{LR}) = 8.03$

Suspect B  $\log(\text{LR}) = 7.84$

Profile - Combined  $\log(\text{LR})$

Suspect A  $\log(\text{LR}) = 18.72$

Suspect B  $\log(\text{LR}) = 19.45$



# Exploring the Capabilities

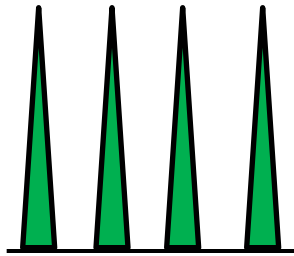
- **Degree of Allele Sharing**
- **Mixture Ratios**
- DNA Quantity

# Mixture Data Set

- Mixtures of pristine male and female DNA amplified at a total concentration of 1.0 ng/ $\mu$ L using Identifiler (standard conditions).
- Mixture ratios ranged from 90:10, 80:20, 70:30, 60:40, 50:50, 40:60, 30:70, 20:80, and 10:90
- Each sample was amplified twice.

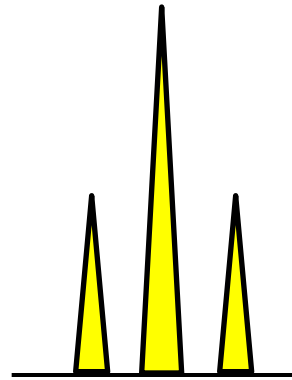
# Mixture Data Set

- Three different combinations:



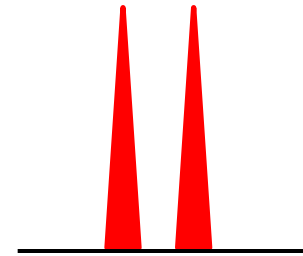
“Low” Sharing

4 alleles – 10 loci  
3 alleles – 5 loci  
2 alleles – 0 loci  
1 allele – 0 loci



“Medium” Sharing

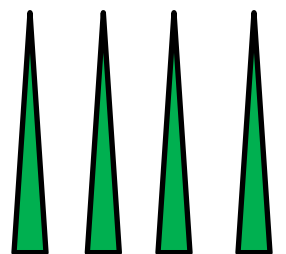
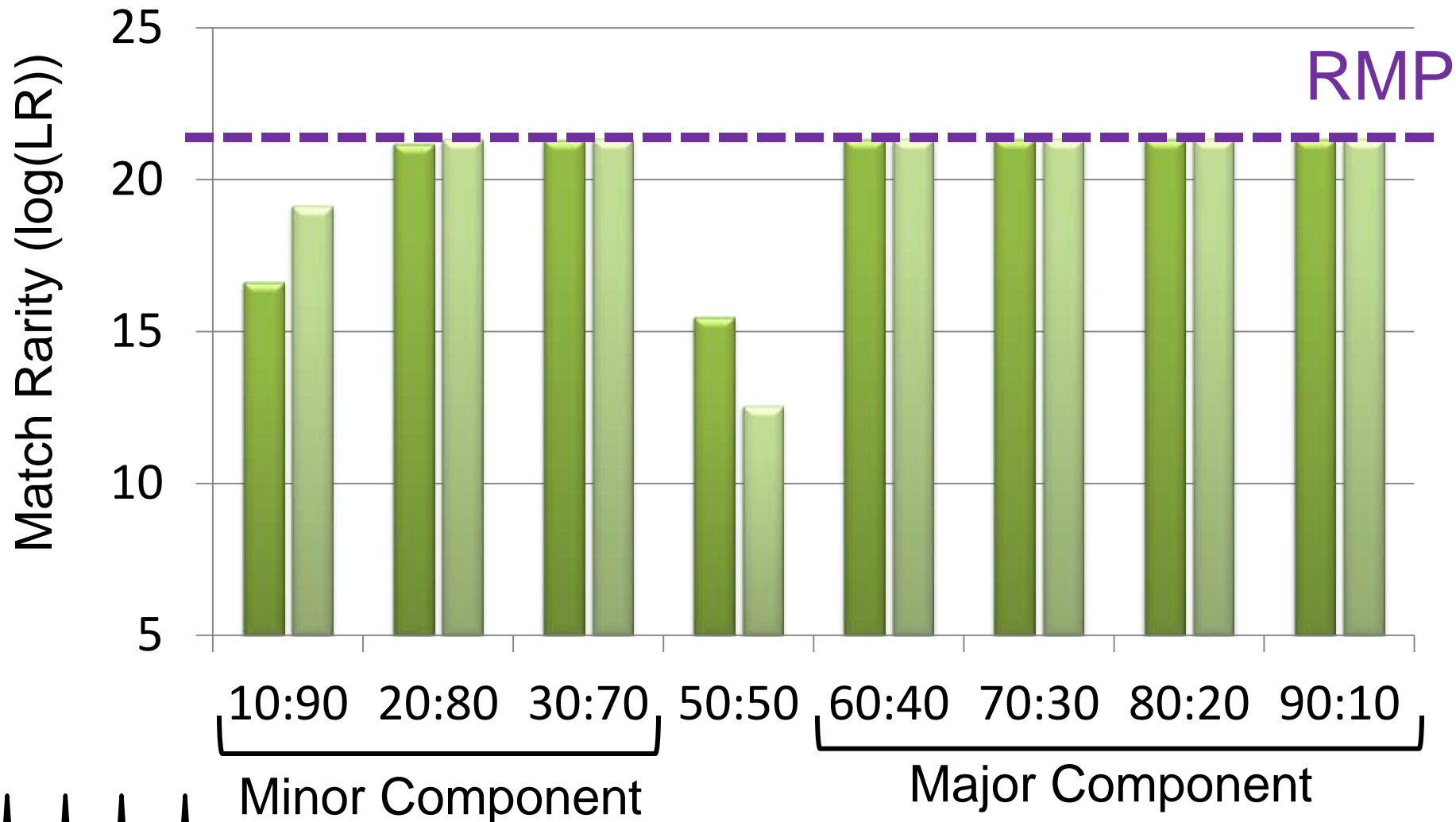
4 alleles – 3 loci  
3 alleles – 8 loci  
2 alleles – 4 loci  
1 allele – 0 loci



“High” Sharing

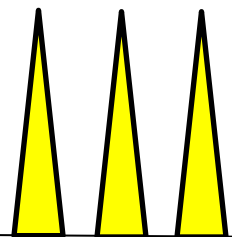
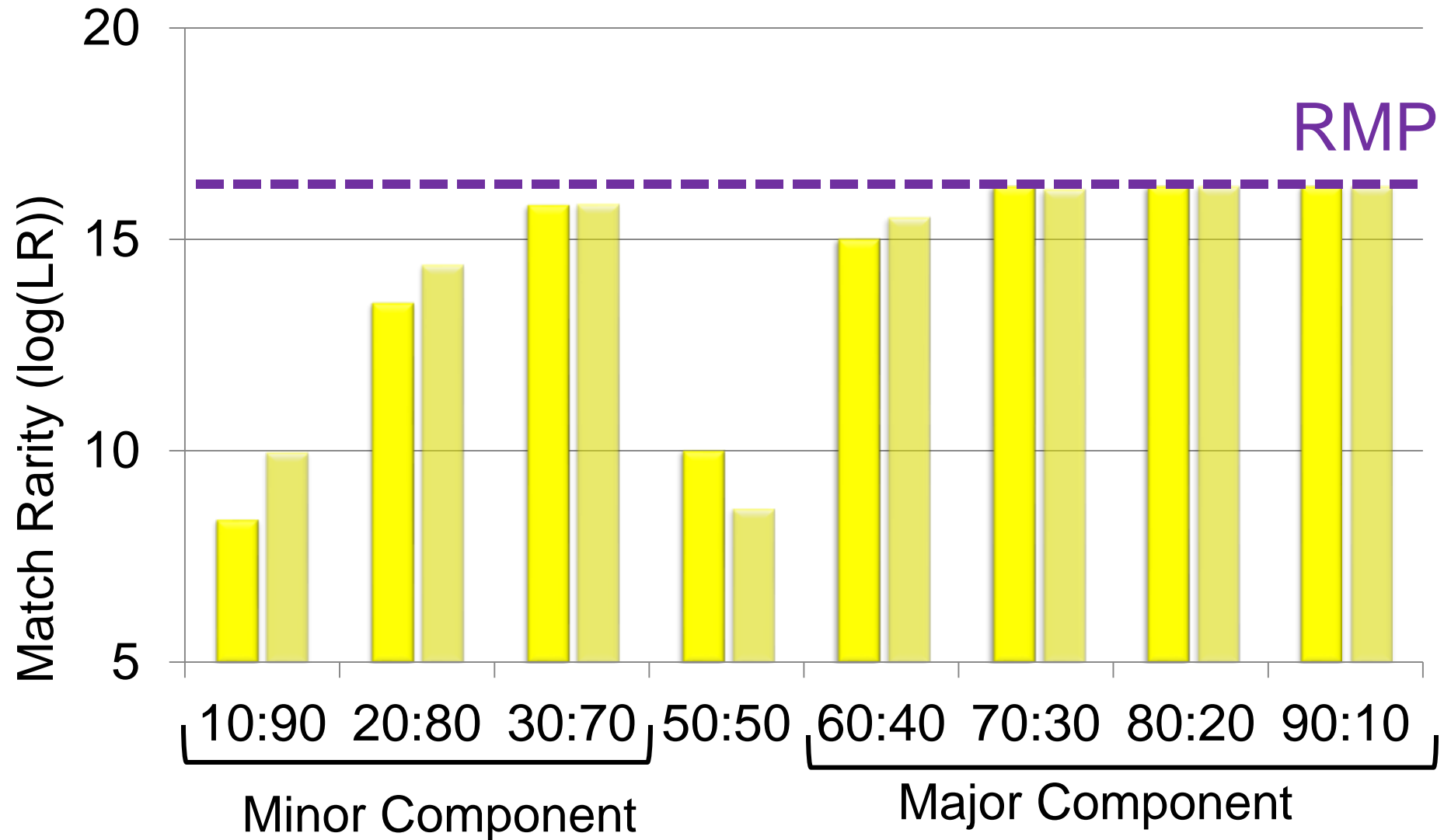
4 alleles – 0 loci  
3 alleles – 6 loci  
2 alleles – 8 loci  
1 allele – 1 loci

# Match Score in Duplicate Runs



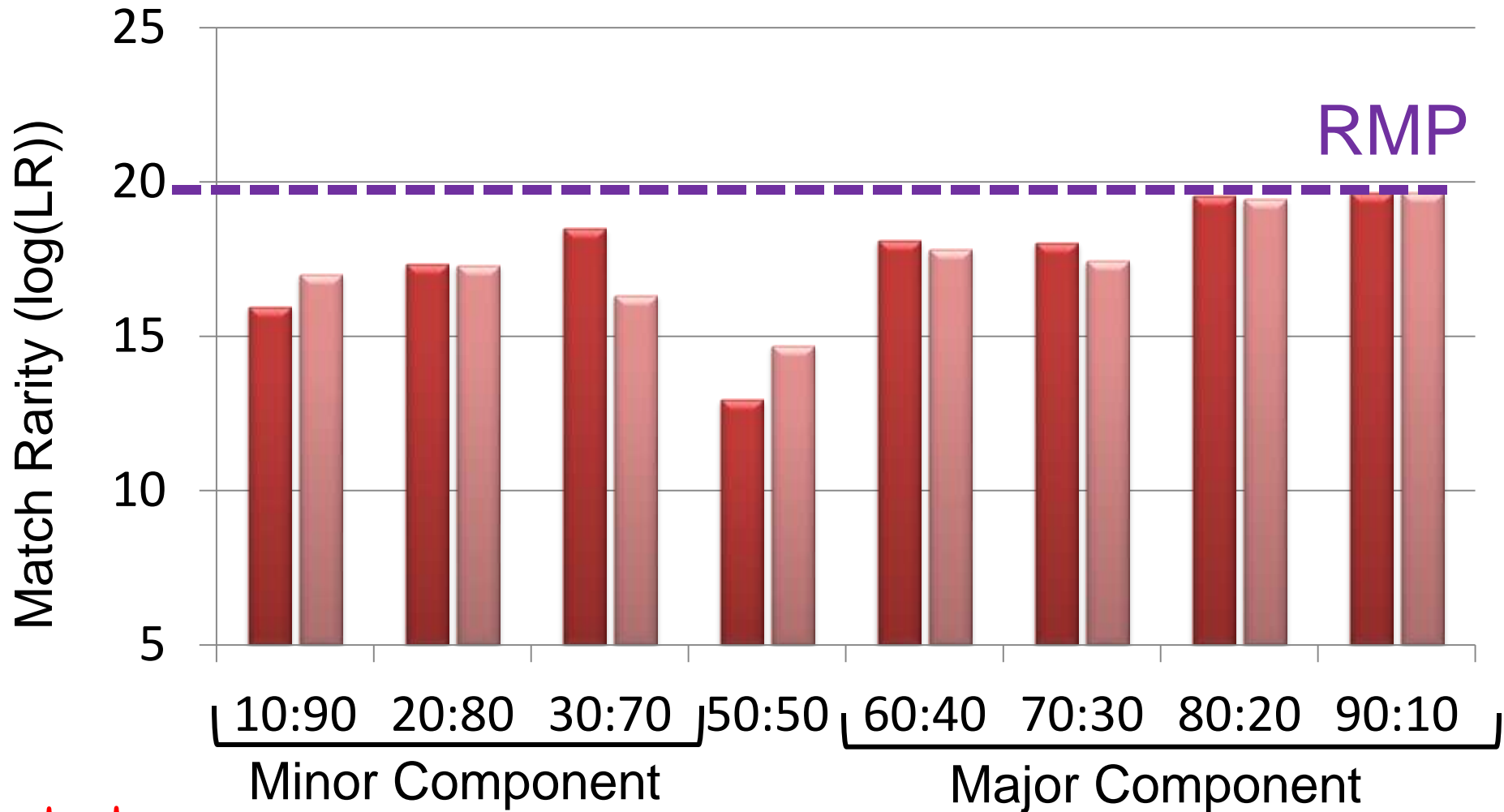
“Easy” for  
Deconvolution

# Match Score in Duplicate Runs

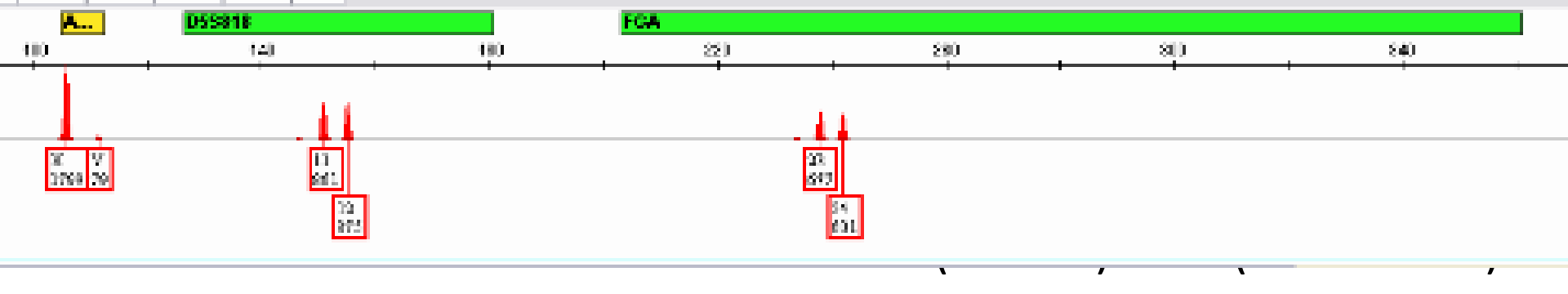
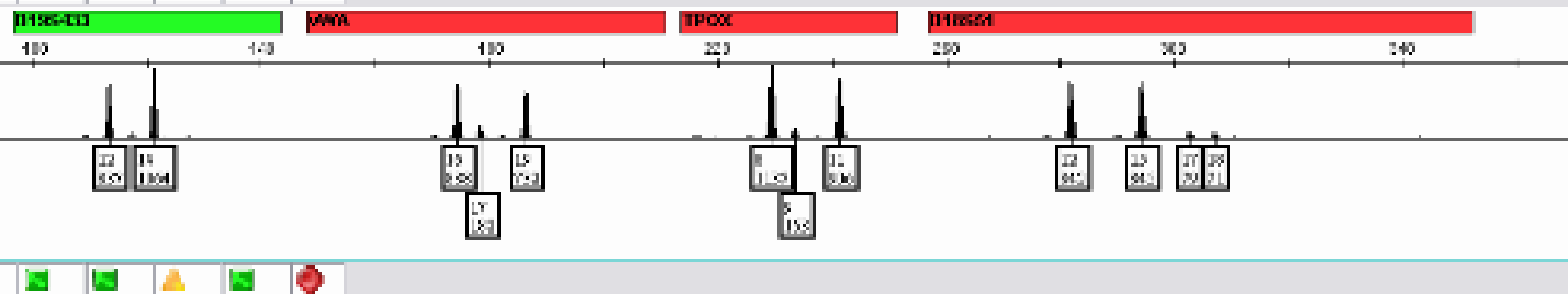
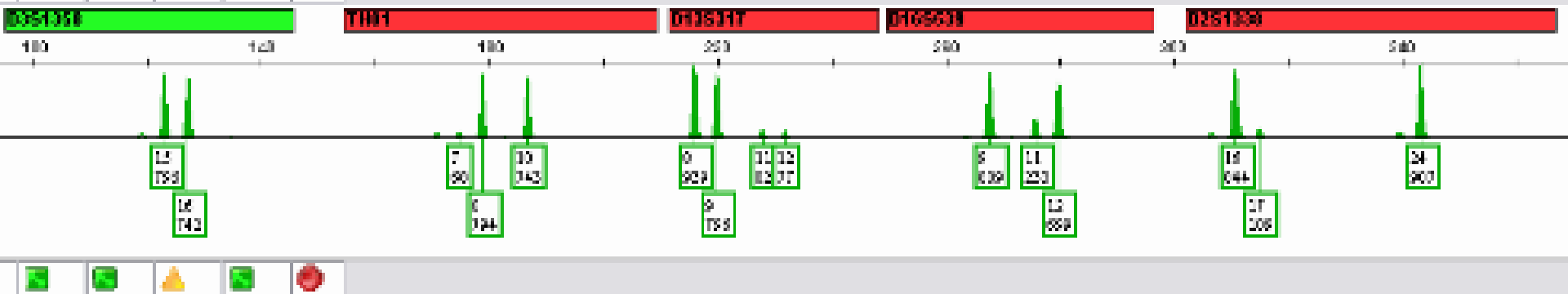
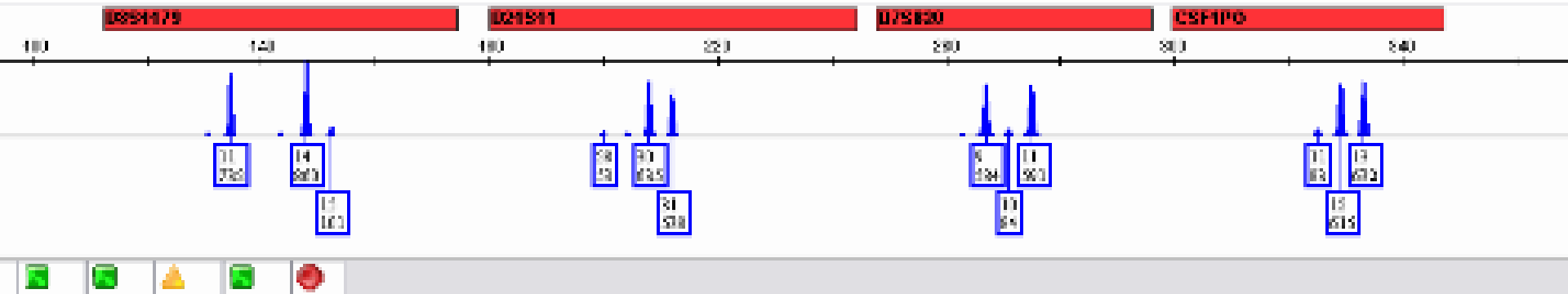


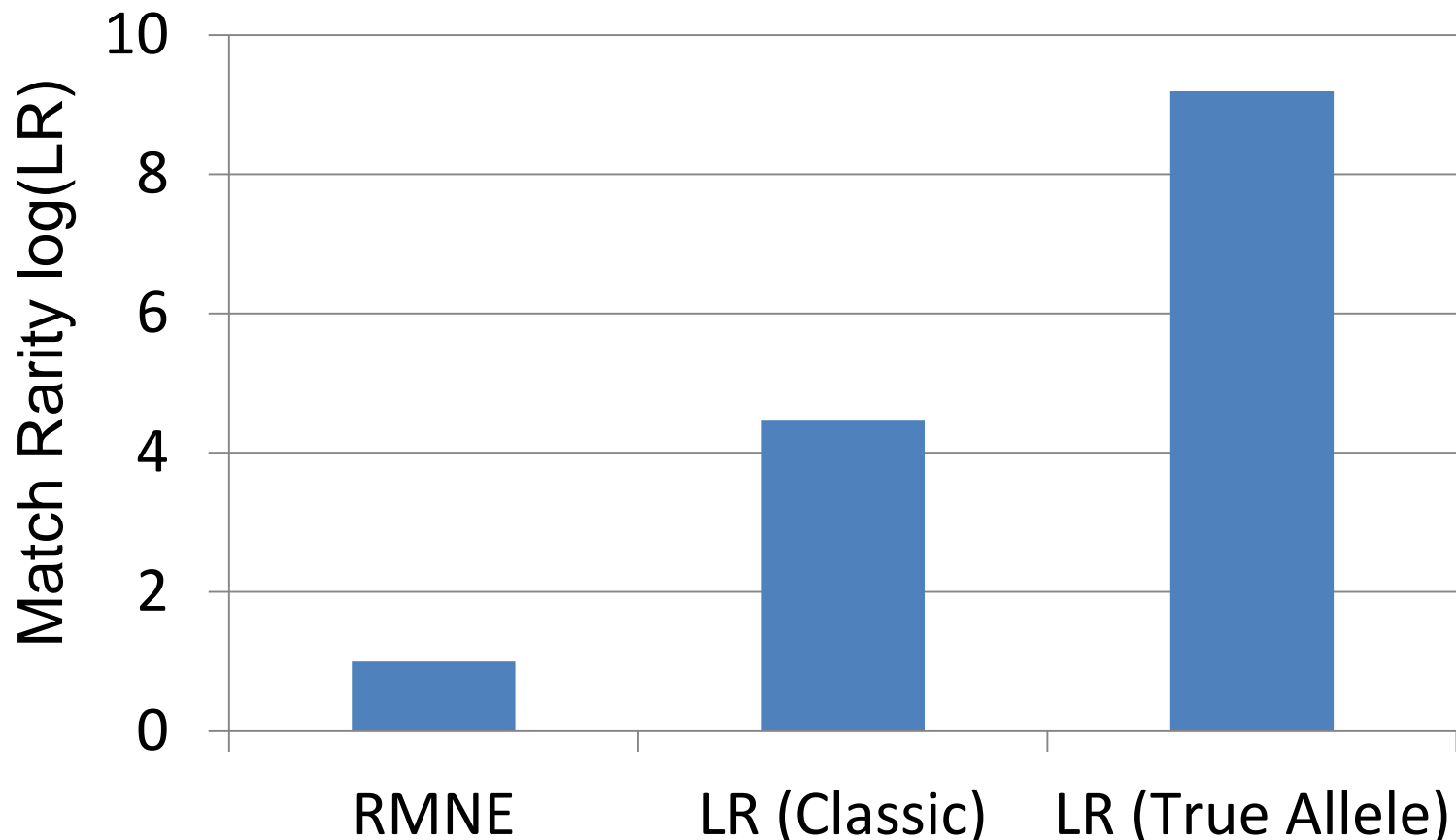
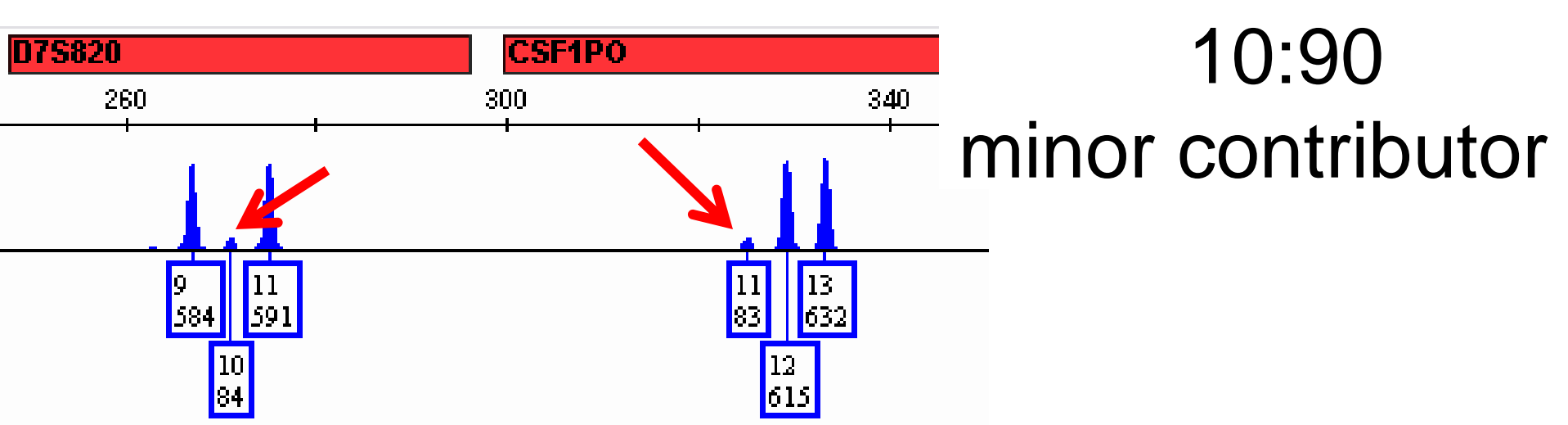
“Challenging” for  
Deconvolution

# Match Score in Duplicate Runs



“Difficult” for  
Deconvolution







# Exploring the Capabilities

- Degree of Allele Sharing
- Mixture Ratios
- **DNA Quantity**

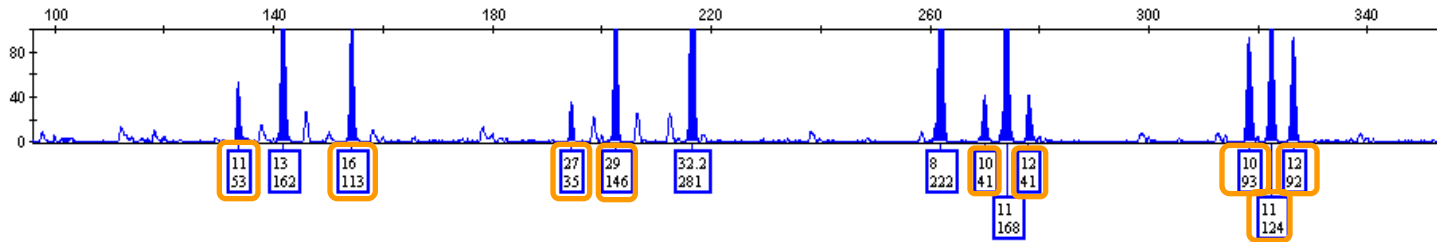
Identifiler

125 pg total DNA

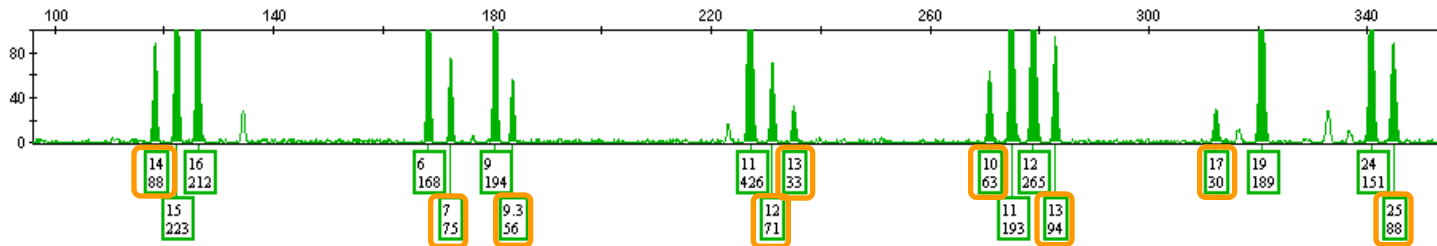
AT = 30 RFU

ST = 150 RFU

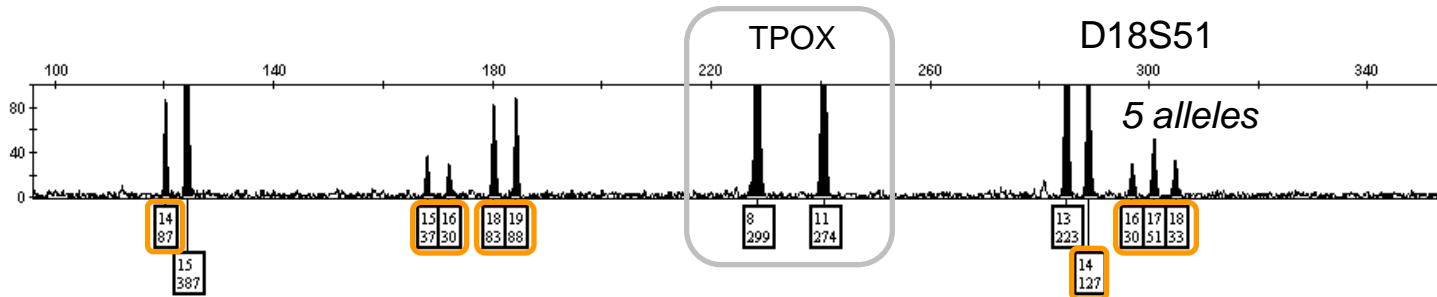
Stutter filter off



Peaks below stochastic threshold



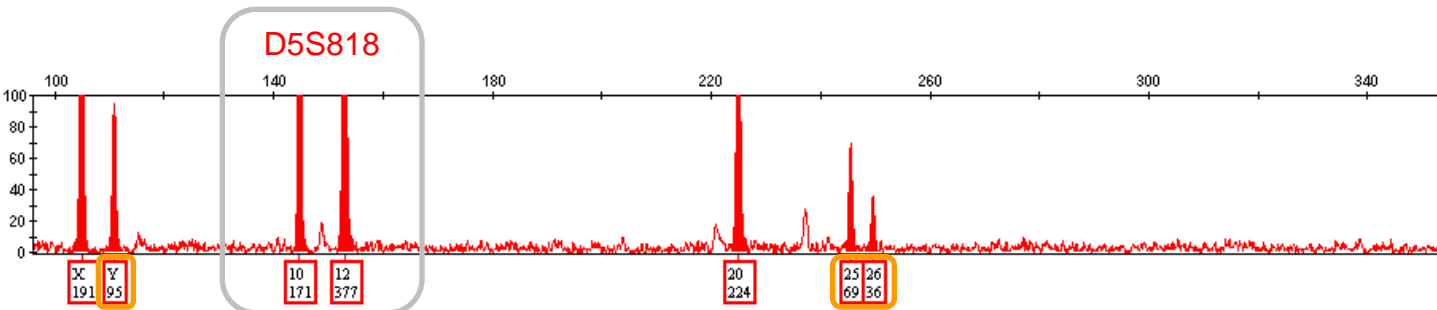
y-axis  
zoom to  
100 RFU



TPOX

D18S51

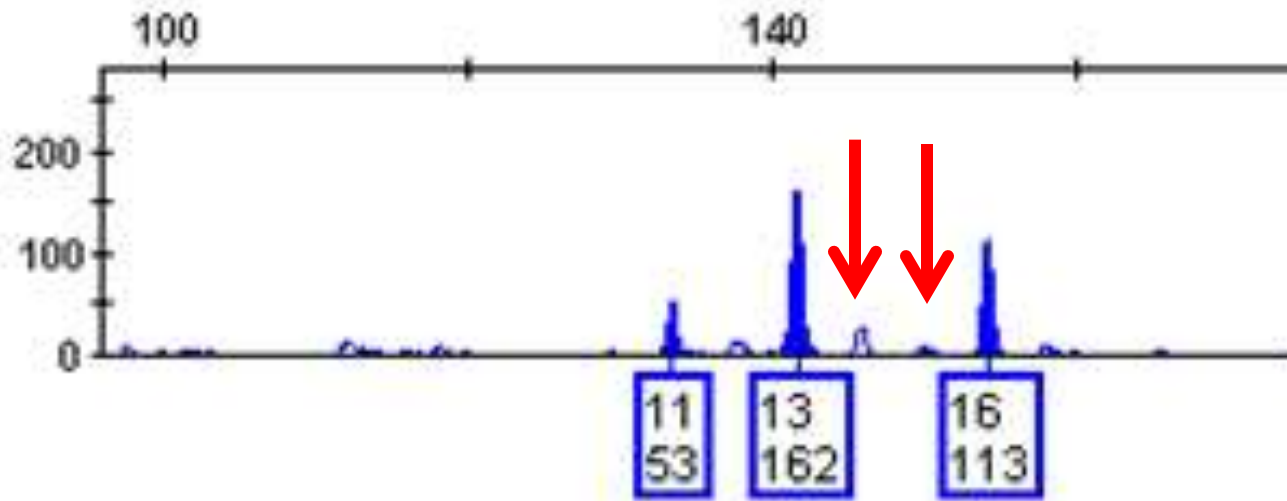
5 alleles



D5S818

# D8S1179

“True Genotypes”

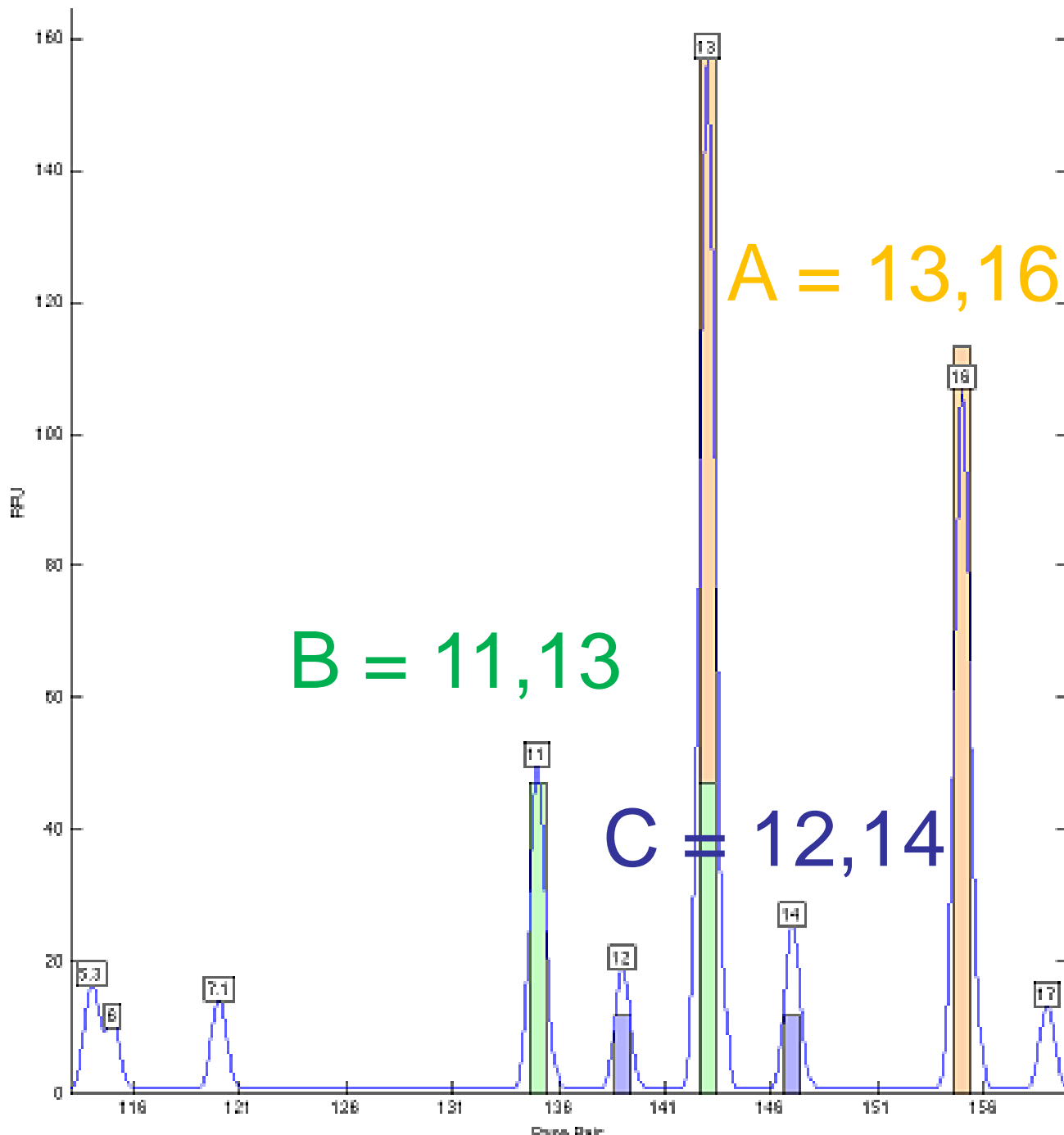


A = 13, 16

B = 11, 13

C = 14, 15

3 person Mixture – No Conditioning  
Major Contributor  $\approx$  83 pg input DNA  
2 Minor Contributors  $\approx$  21 pg input DNA



“True Genotypes”

A = 13,16

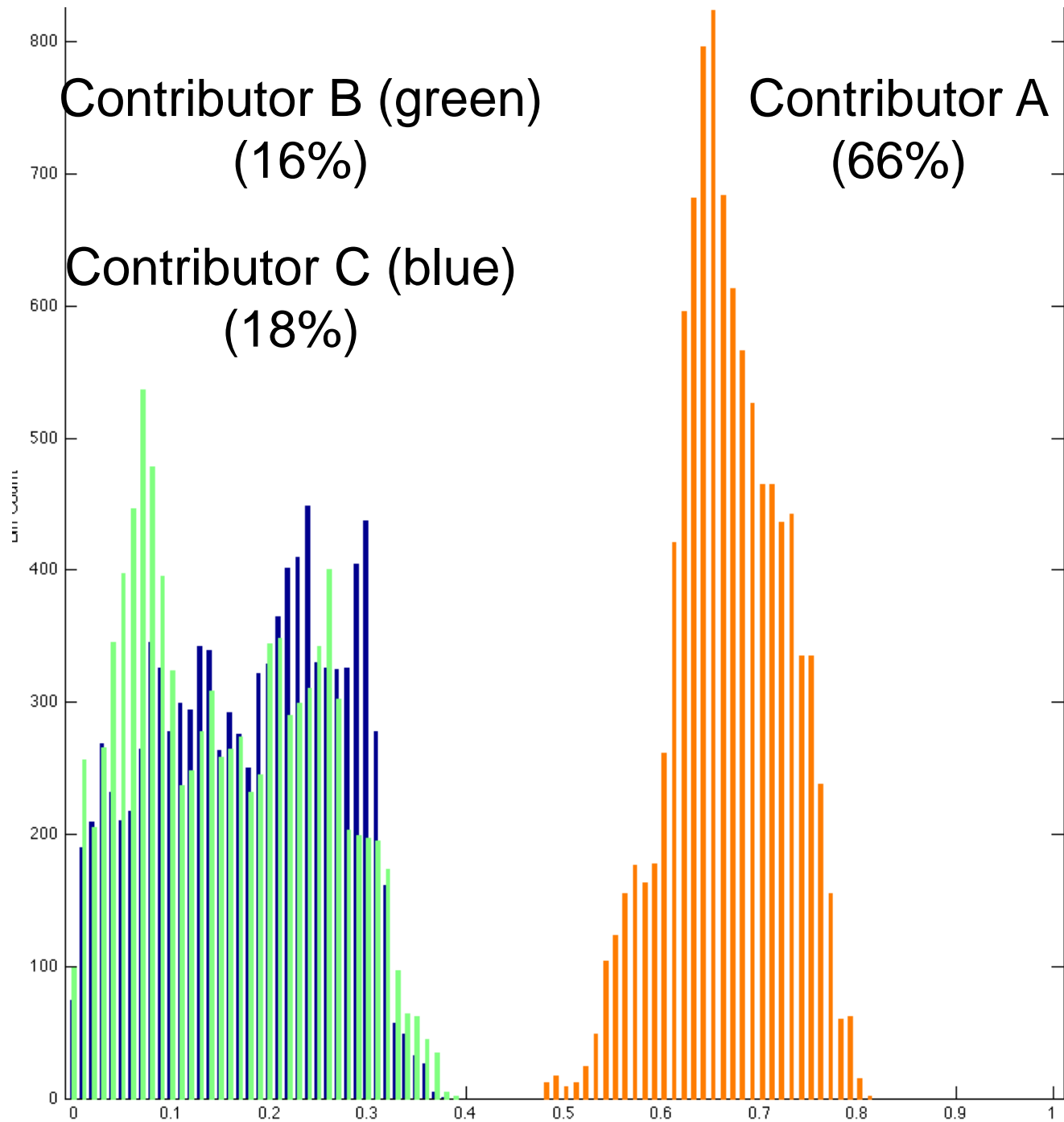
A = 13,16

B = 11,13

B = 11,13

C = 12,14

C = 14,15

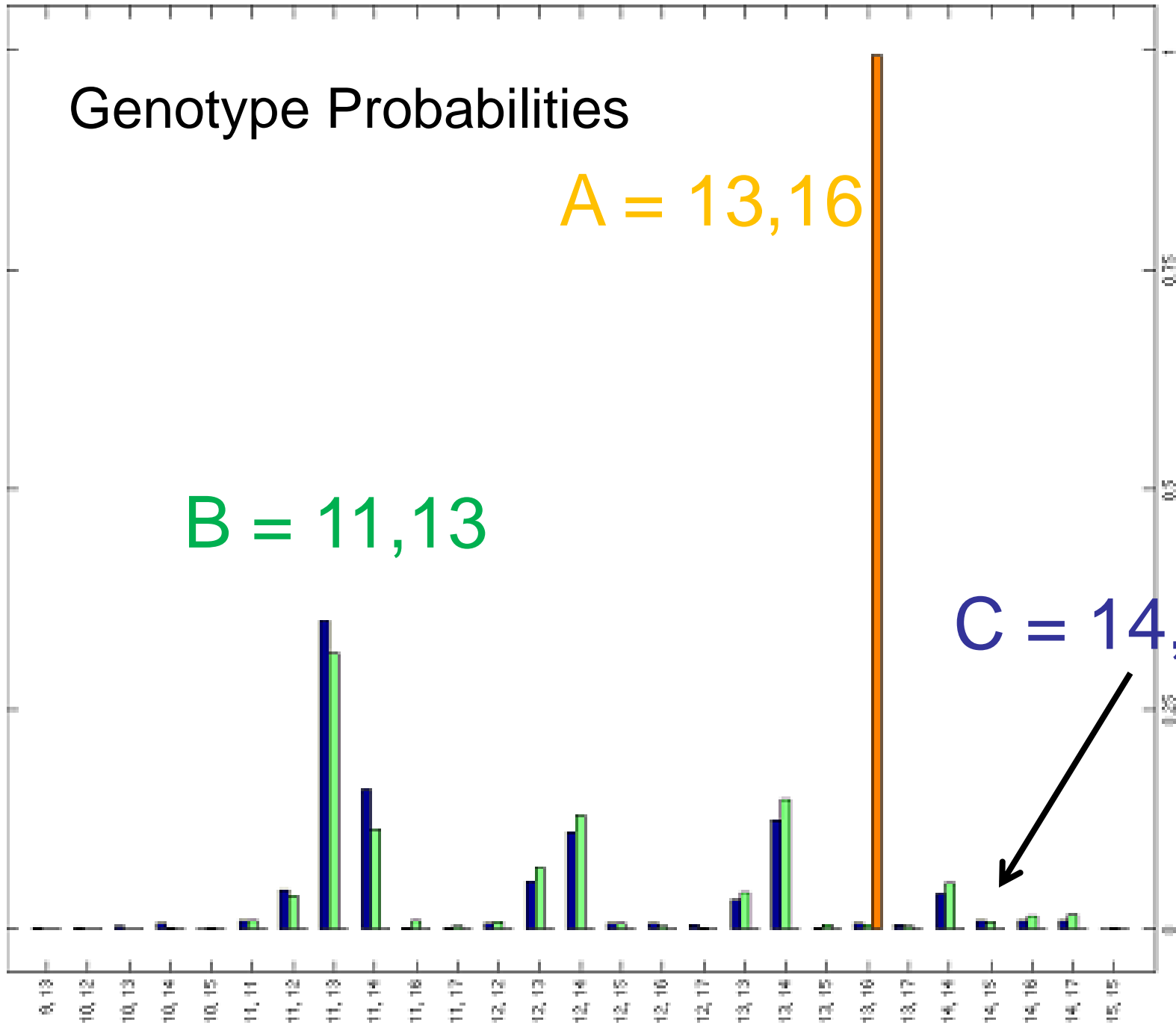


# Genotype Probabilities

A = 13,16

B = 11,13

C = 14,15



# Results for Contributor A (male)

		Probability	Genotype		H <sub>p</sub>	H <sub>d</sub>	
Locus	Allele Pair	Likelihood	Frequency	Suspect	Numerator	Denominator	LR
CSF1PO	10, 11	0.572	0.1292			0.07395	
	11, 12	0.306	0.2133	1	0.30563	0.0652	
	10, 12	0.12	0.1547			0.01861	
					0.30563	0.15791	1.935
D13S317	11, 11	1	0.1149	1	1	0.11488	8.704
D8S1179	13, 16	0.998	0.0199	1	0.99786	0.0199	49.668

The match rarity between the evidence and suspect is 1.21 quintillion

# Results for Contributor B (female)

Locus	Allele Pair	Probability	Genotype	Suspect	$H_p$	$H_d$	LR
		Likelihood	Frequency		Numerator	Denominator	
D8S1179	11, 13	0.073	0.0498	1	0.07338	0.00366	
	11, 14	0.034	0.0271			0.00092	
	13, 14	0.006	0.0996			0.00065	
	12, 14	0.011	0.0606			0.00068	
	12, 13	0.005	0.1115			0.0006	
	11, 12	0.018	0.0303			0.00054	
	14, 14	0.004	0.0271			0.00012	
	13, 13	0.003	0.0916			0.00031	
	14, 16	0.003	0.0108			0.00003	
	14, 15	0.001	0.0379			0.00003	

etc...

9.197

The match rarity between the evidence and suspect is 1.43 million



# Results for Contributor C (male)

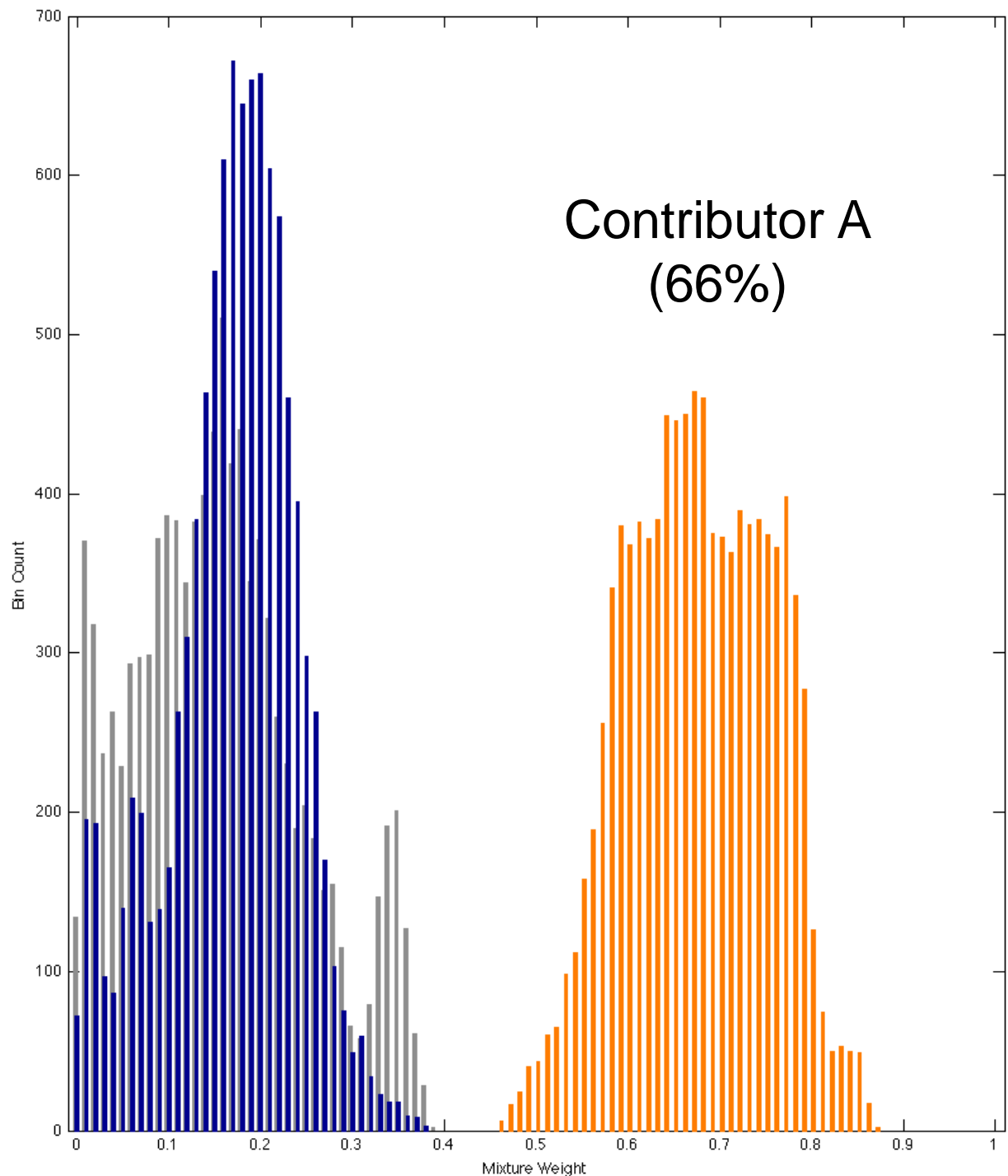
		Probability	Genotype		H <sub>p</sub>	H <sub>d</sub>	
Locus	Allele Pair	Likelihood	Frequency	Suspect	Numerator	Denominator	LR
D8S1179	11, 13	0.056	0.0498			0.00279	
	13, 14	0.007	0.0996			0.00066	
	12, 14	0.011	0.0606			0.00068	
	11, 14	0.021	0.0271			0.00056	
	12, 13	0.006	0.1115			0.00066	
	14, 14	0.005	0.0271			0.00013	
	etc...	etc...	etc...			etc...	
	14, 15	0.001	0.0379	1	0.00056	0.00002	
	12, 15	0.001	0.0424			0.00003	
	etc...	etc...	etc...			etc...	
	10, 15	0	0.0227			0.00001	
					0.00056	0.00665	<b>0.084</b>

The match rarity between the evidence and suspect is 9.16 thousand

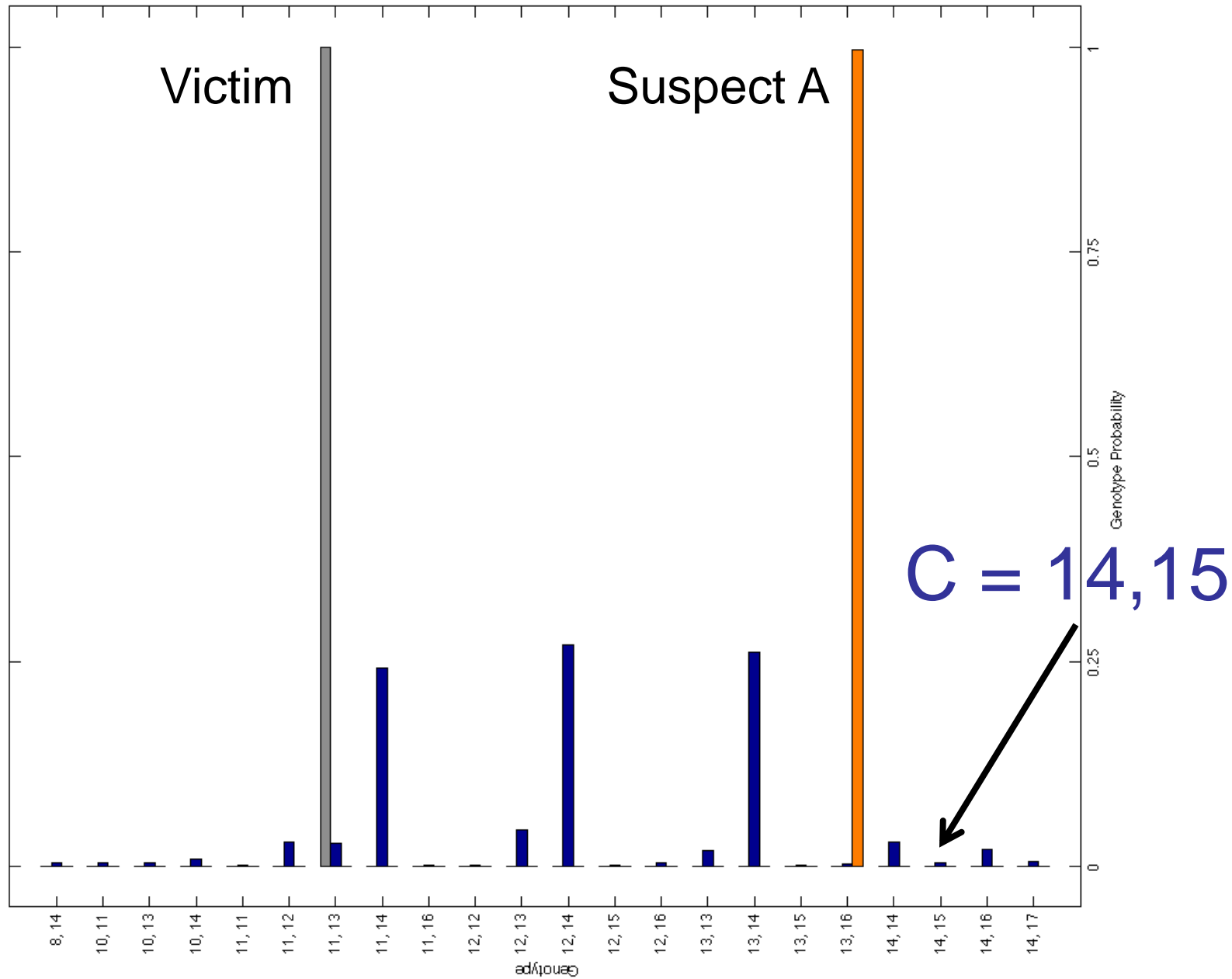
Contributor B (gray)  
(16%)

Contributor C (blue)  
(18%)

Conditioned on the Victim



# The Power of Conditioning



# The Power of Conditioning

	<b>LR (no conditioning, 3unk)</b>
<b>Contributor A</b>	<b>1.21 Quintillion</b>
<b>Contributor B (victim)</b>	<b>1.43 Million</b>
<b>Contributor C</b>	<b>9.16 Thousand</b>

	<b>LR (conditioned on victim + 2unk)</b>
<b>Contributor A</b>	<b>1.32 Quintillion</b>
<b>Contributor B (victim)</b>	<b>2.19 Million</b>
<b>Contributor C</b>	<b>59.8 Thousand</b>



Ranged from 1.13 to 800K

# Summary

- True Allele utilizes probabilistic genotyping and makes better use of the data than the RMNE approach.
- However, the software is computer intensive. On our 4 processor system, it can take 12-16 hours to run up to four 3-person mixture samples.

# Summary

- **Allele Sharing:** Stacking of alleles due to sharing creates more uncertainty.
- **Mixture Ratio:** With “distance” between the two contributors, there is greater certainty. Generally, True Allele performs better than RMNE and the classic LR with low level contributors.

# Summary

- **DNA Quantity:** Generally, with high DNA signal, replicates runs on True Allele are very reproducible.
- However, with low DNA signal, higher levels of uncertainty are observed (as expected).
- There is a need to determine an appropriate threshold for an inclusion  $\log(\text{LR})$ .

# Summary

- We need to move away from the interpretation of mixtures from an “allele-centric” point of view.
- Methods to incorporate probability will be necessary as we make this transition and confront the issues of low-level profiles with drop-out.
- “Just as logic is reasoning applied to truth and falsity, probability is reasoning with uncertainty”  
-Dennis Lindley



# Summary

- The LR is a method to evaluate evidence that can overcome many of the limitations we are facing today. ISFG Recommendations for incorporating drop-out are in press.
- This will require (obviously) software solutions... however, we need to better understand and be able to explain the statistics as a community.

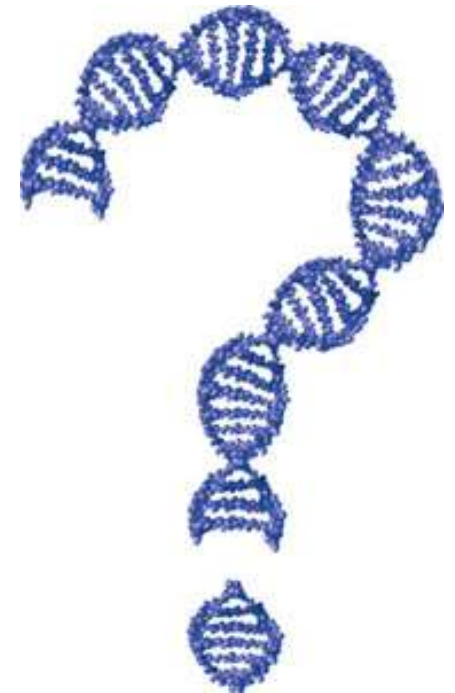
# Thank You!

Our team publications and presentations are available at:  
<http://www.cstl.nist.gov/biotech/strbase/NISTpub.htm>

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**Questions?**



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