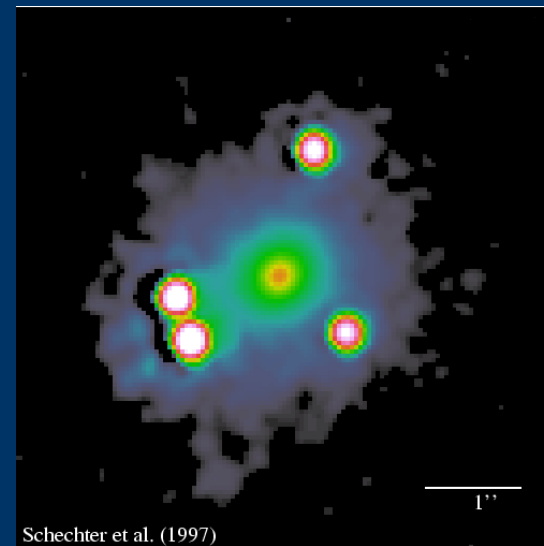
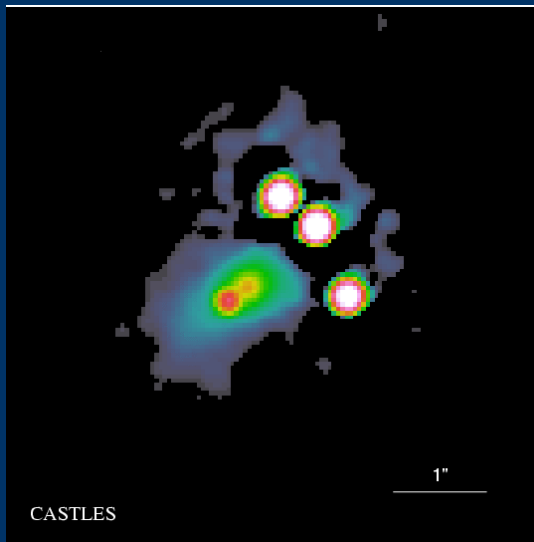


# Light Bending and Dark Matter:

## Gravitational Lensing as a Probe of Galaxy Structure



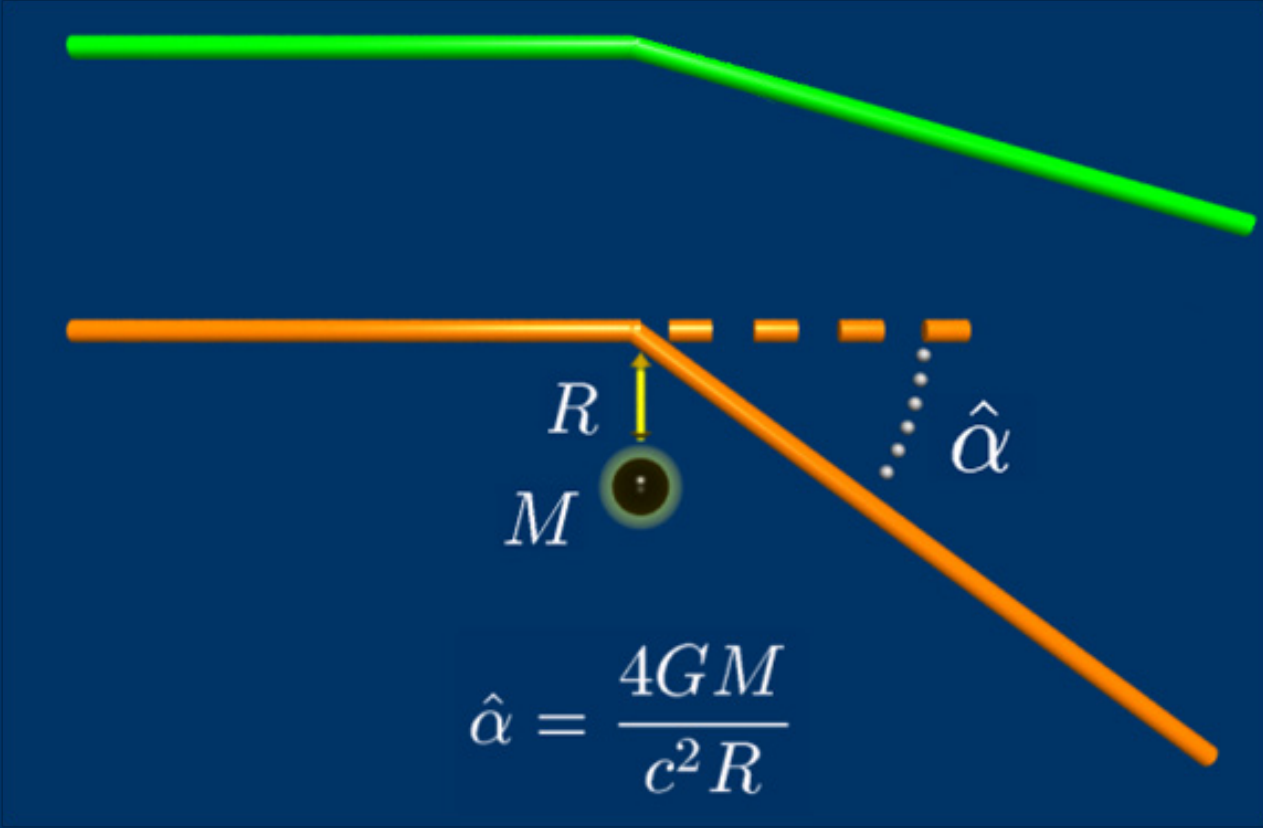
*Arthur Congdon • JPL*

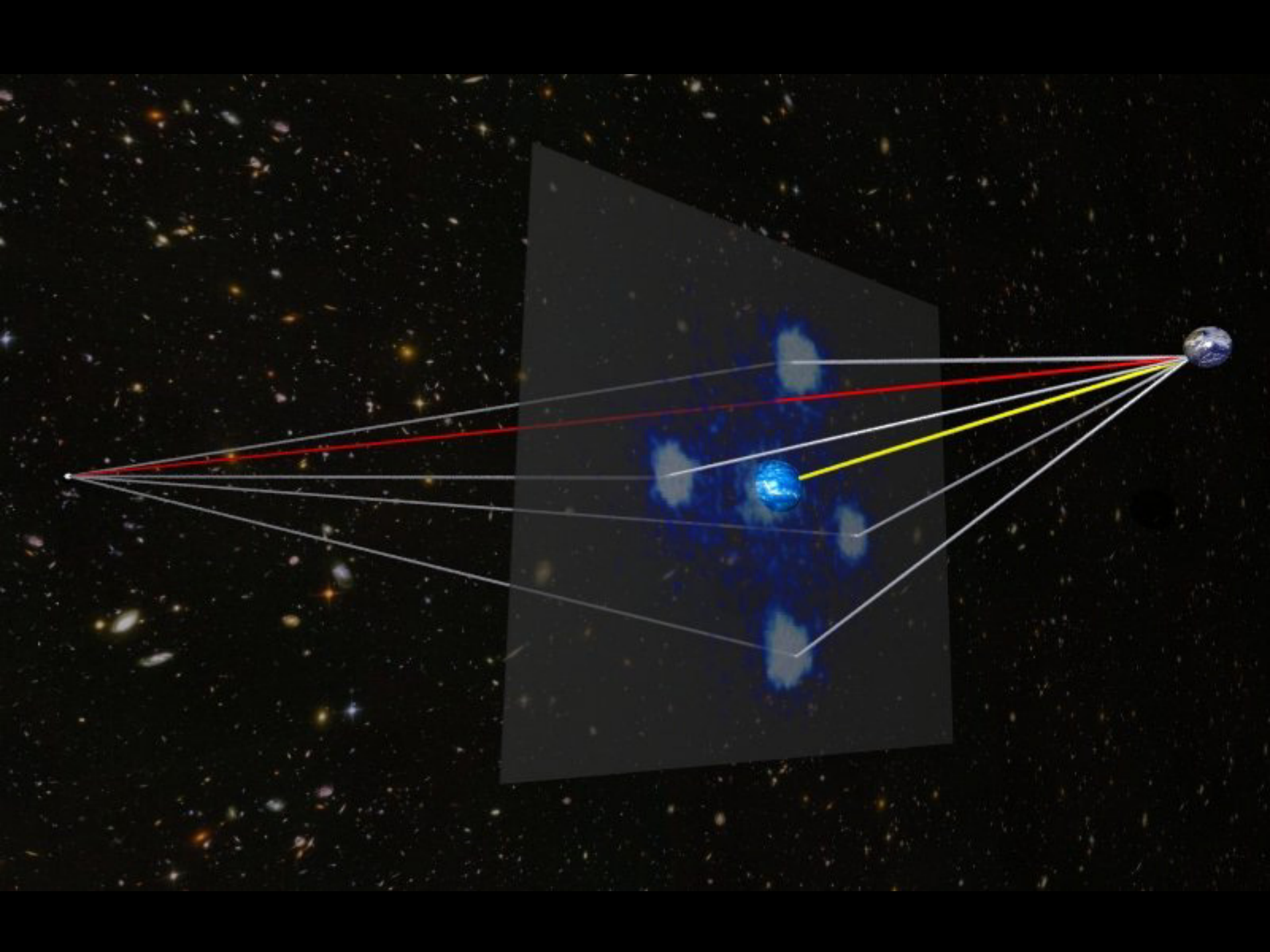
# Acknowledgments

I would like to thank my collaborators,  
Chuck Keeton and Erik Nordgren

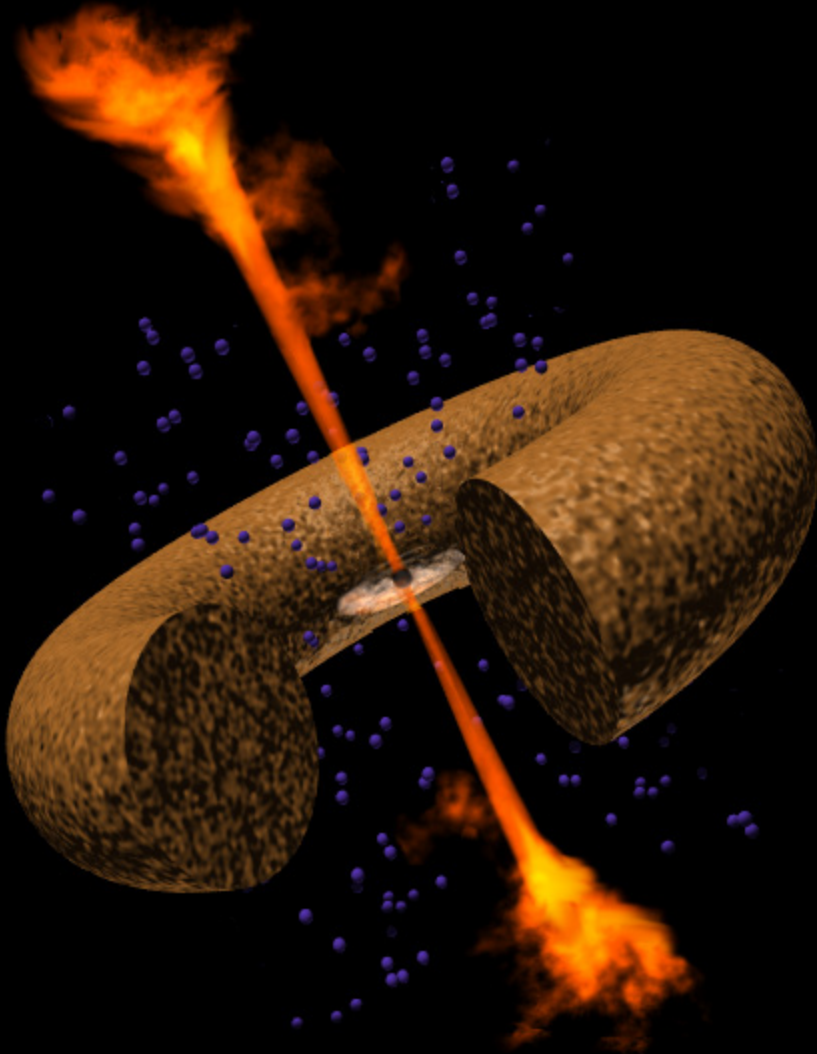
# What Is Gravitational Lensing?

- Bending of light by mass
- Larger deflection for larger mass or smaller distance from lens
- Multiple images if source and lens are nearly aligned – strong lensing
- Positions, fluxes and/or arrival times of images constrain properties of source and lens





# Quasars as Lensed Sources



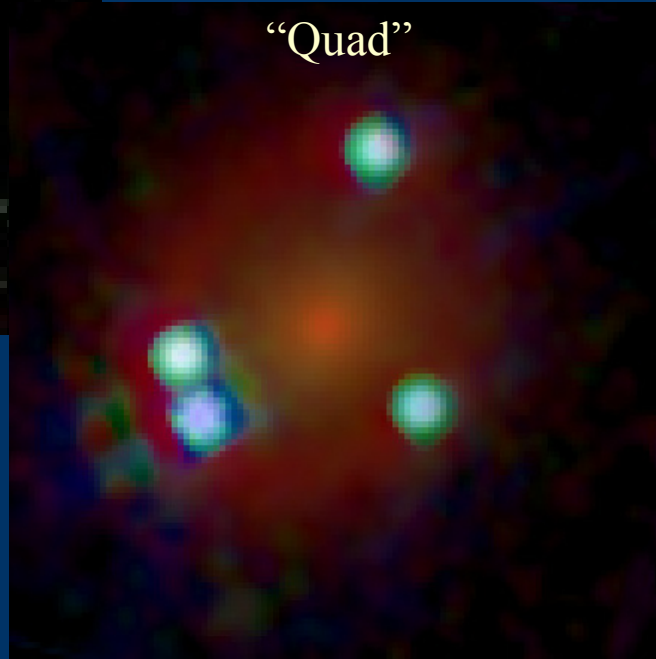
- Radio emission comes from extended jets
- Optical, UV and X-ray emission comes mainly from the central accretion disk

# Lensing by Galaxies: Hubble Space Telescope Images

“Double”



“Quad”



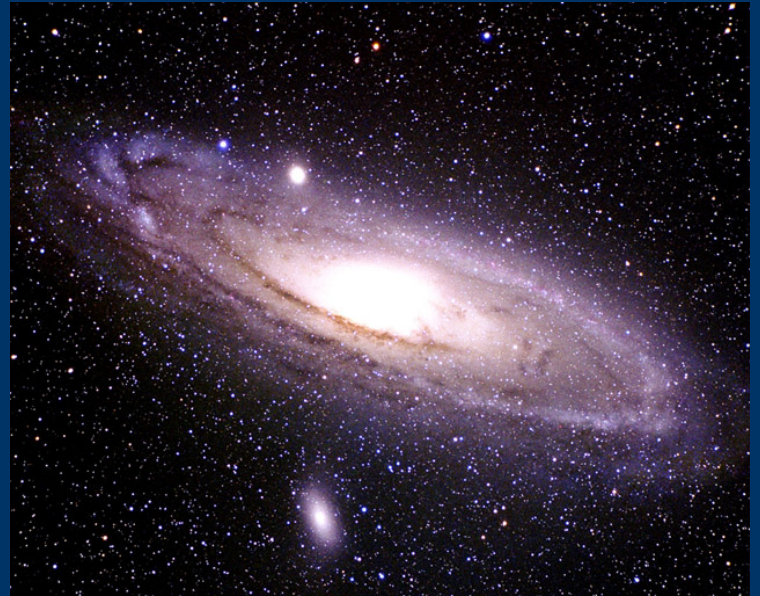
“Ring”





# Galaxies as Lensing Objects

- Two major galaxy types
- Most lens galaxies are elliptical
- Galaxies contain dark matter





# Does Dark Matter Really Exist?

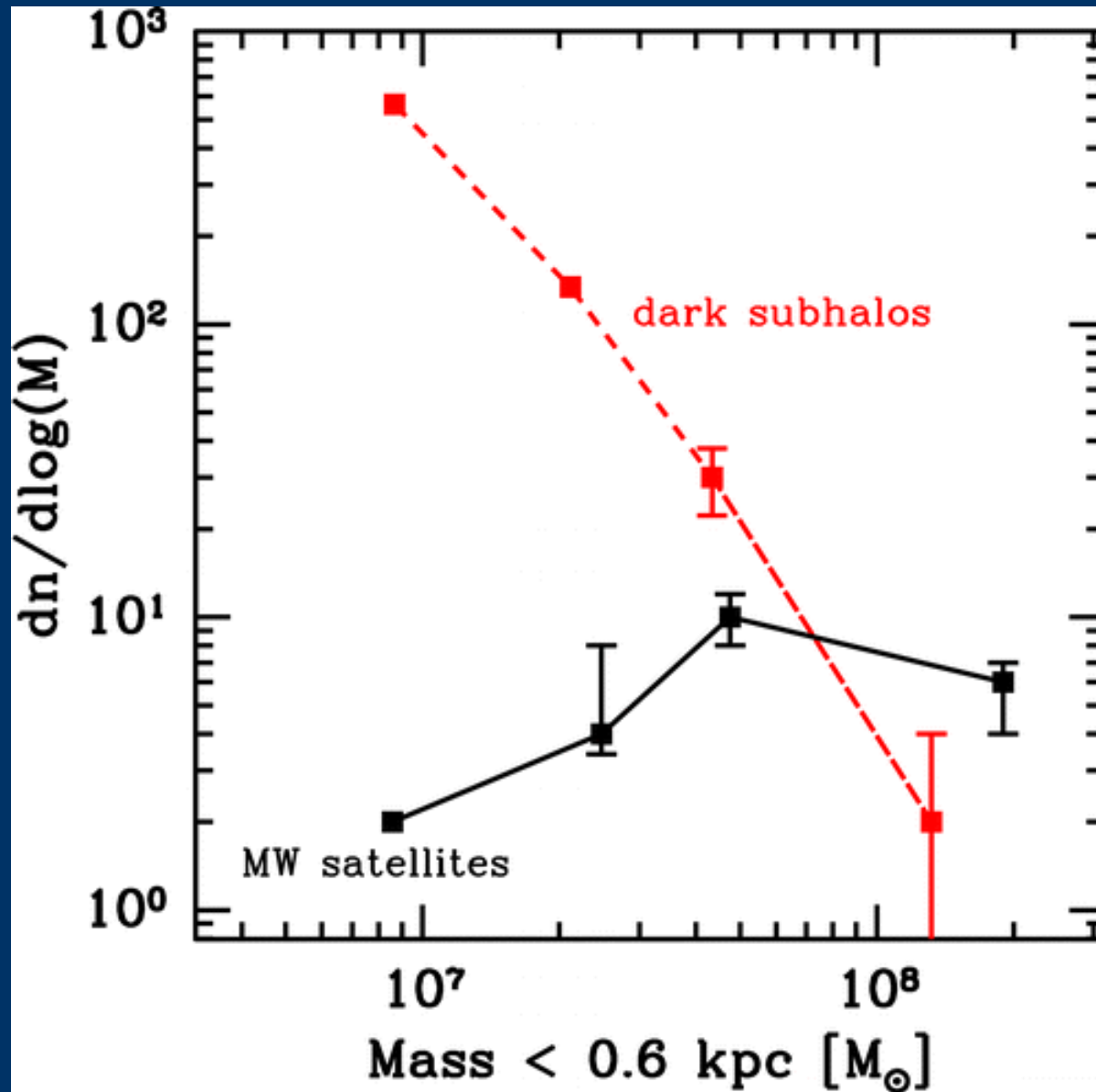


- Use rotation curve to find enclosed mass
- Not enough visible matter to explain observations
- Need more mass — dark matter

- *Hierarchical structure formation:*  
small objects form first, then  
aggregate into larger objects
- Large halos contain the remnants of  
their many progenitors - substructure
- Theory predicts more substructure  
than we see – “missing satellites”  
problem



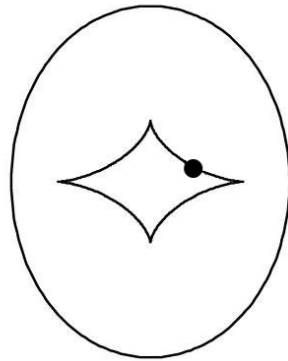
# Missing Satellites Problem



*Strigari et al (2007)*

# Four-Image Lenses

Source  
plane



Fold

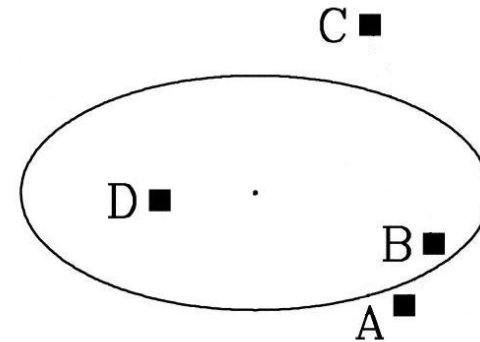
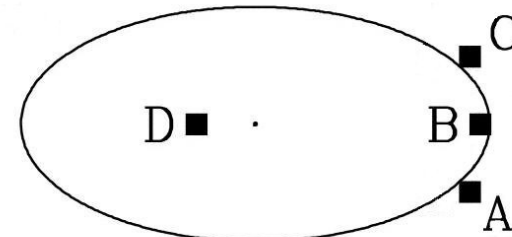
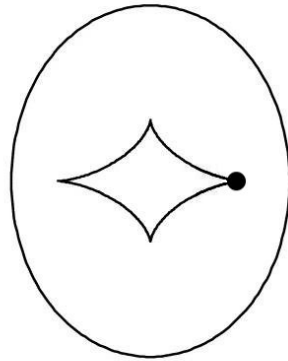
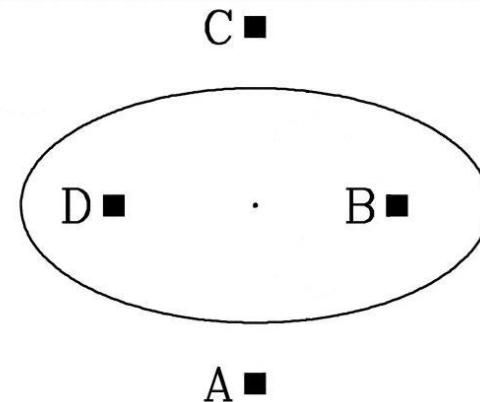
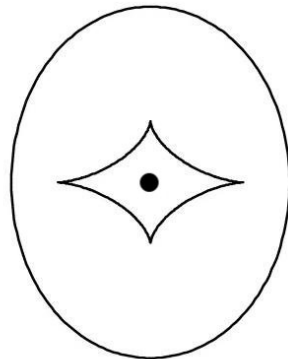


Image  
plane

Cusp



Cross

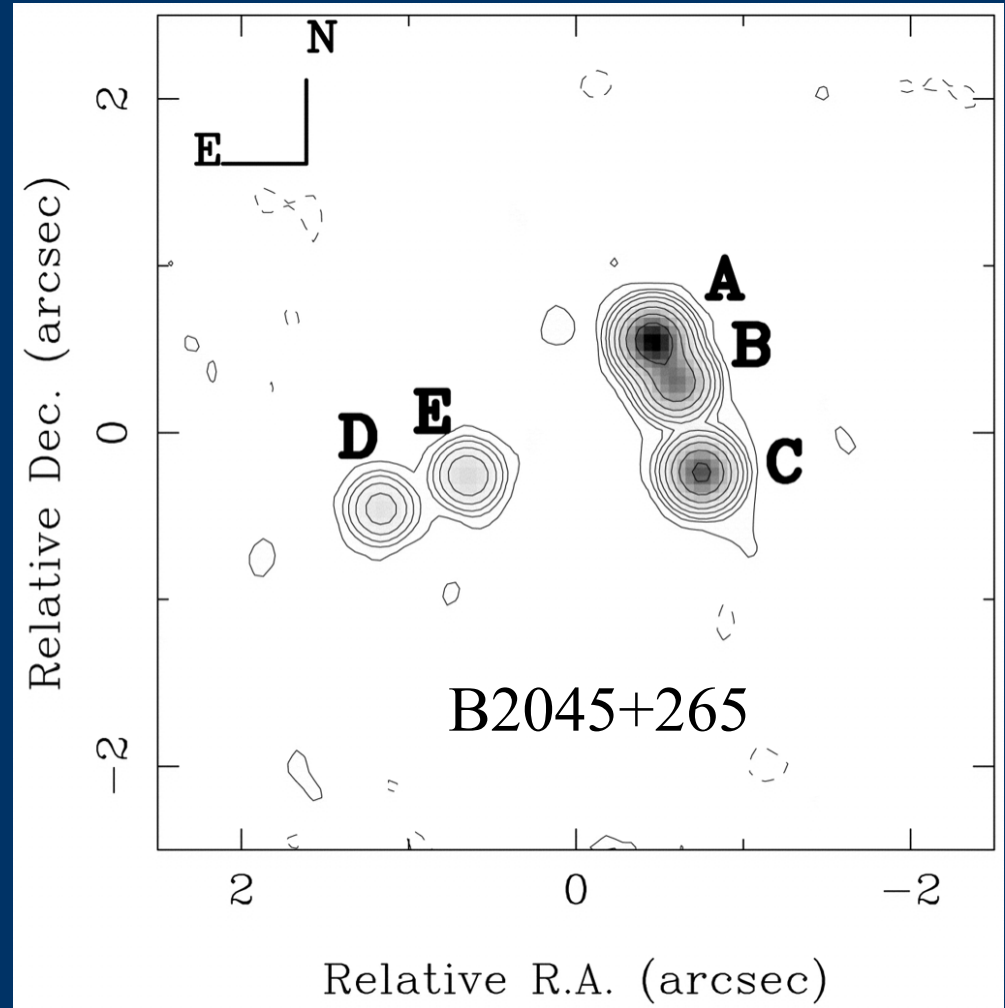


# Flux Anomalies

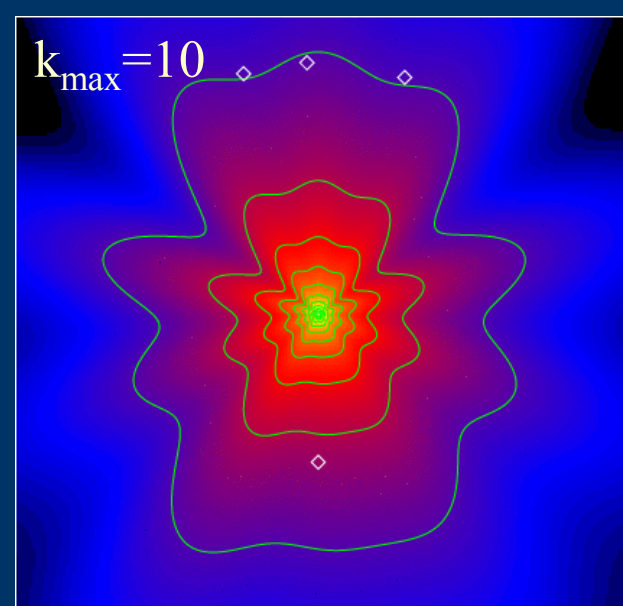
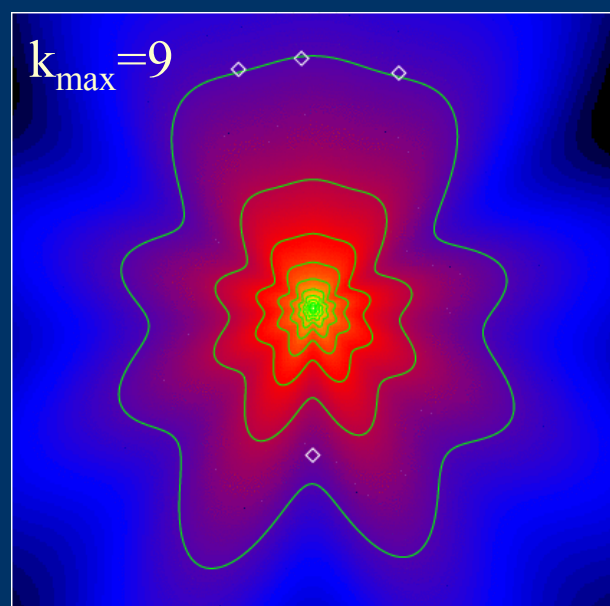
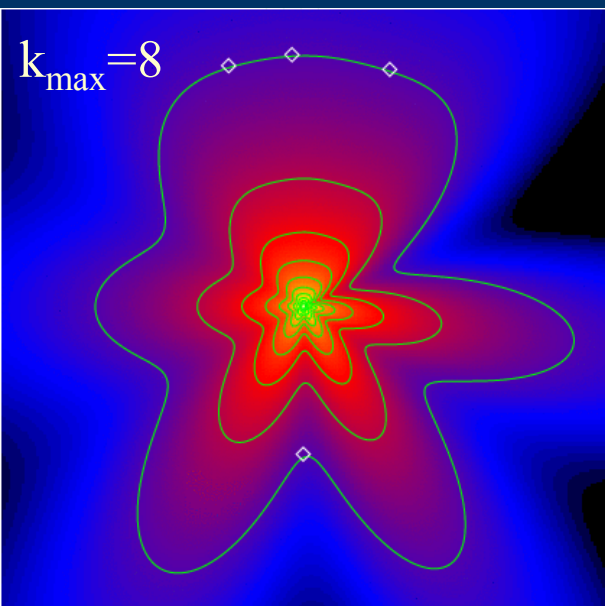
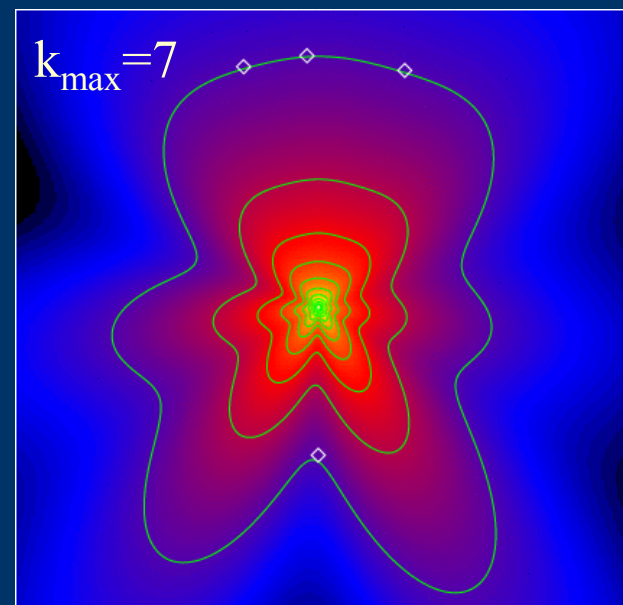
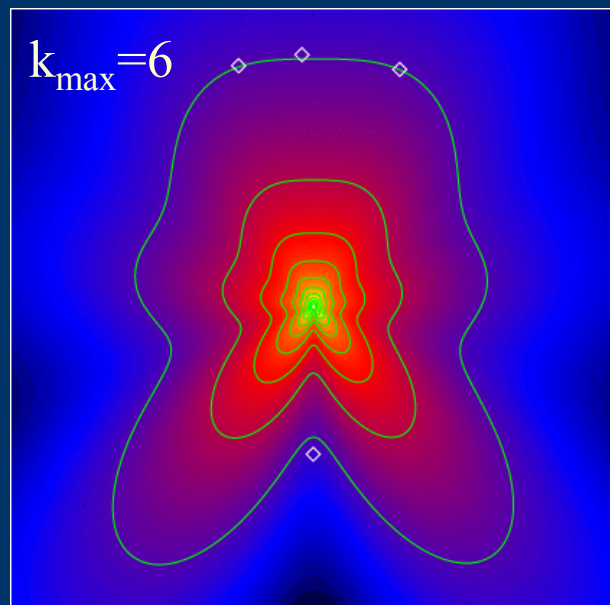
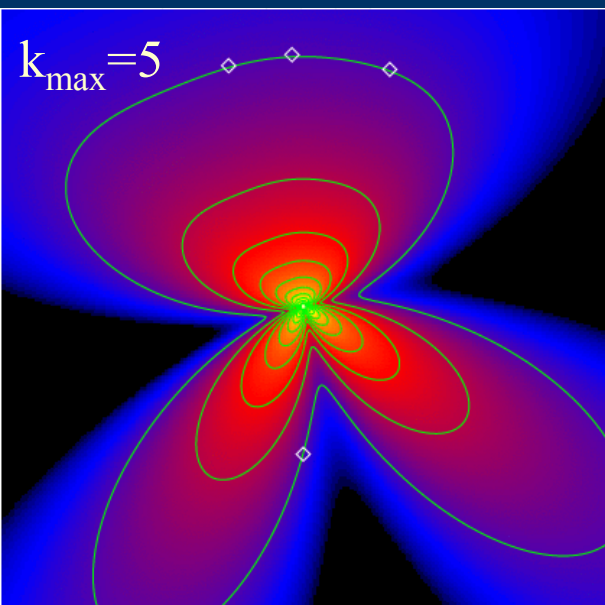
- Many lenses require small-scale structure  
*(Mao & Schneider 1998; Keeton, Gaudi & Petters 2003, 2005)*
- Could be CDM substructure  
*(Metcalf & Madau 2001; Chiba 2002)*
- Fitting the lenses requires  $0.006 < f_{\text{sub}} < 0.07$   
*(Dalal & Kochanek 2002)*
- Broadly consistent with CDM
- Is substructure the only viable explanation?

# “Minimum Wiggle” Model

- Allow many multipoles, up to mode  $k_{\max}$
- Models underconstrained  $\Rightarrow$  large solution space
- Minimize departures from elliptical symmetry

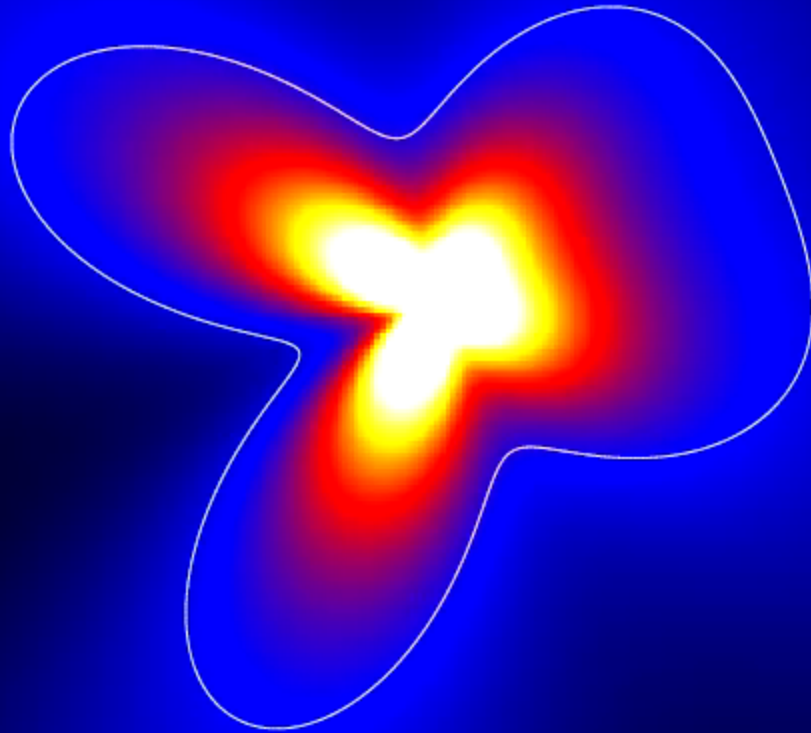




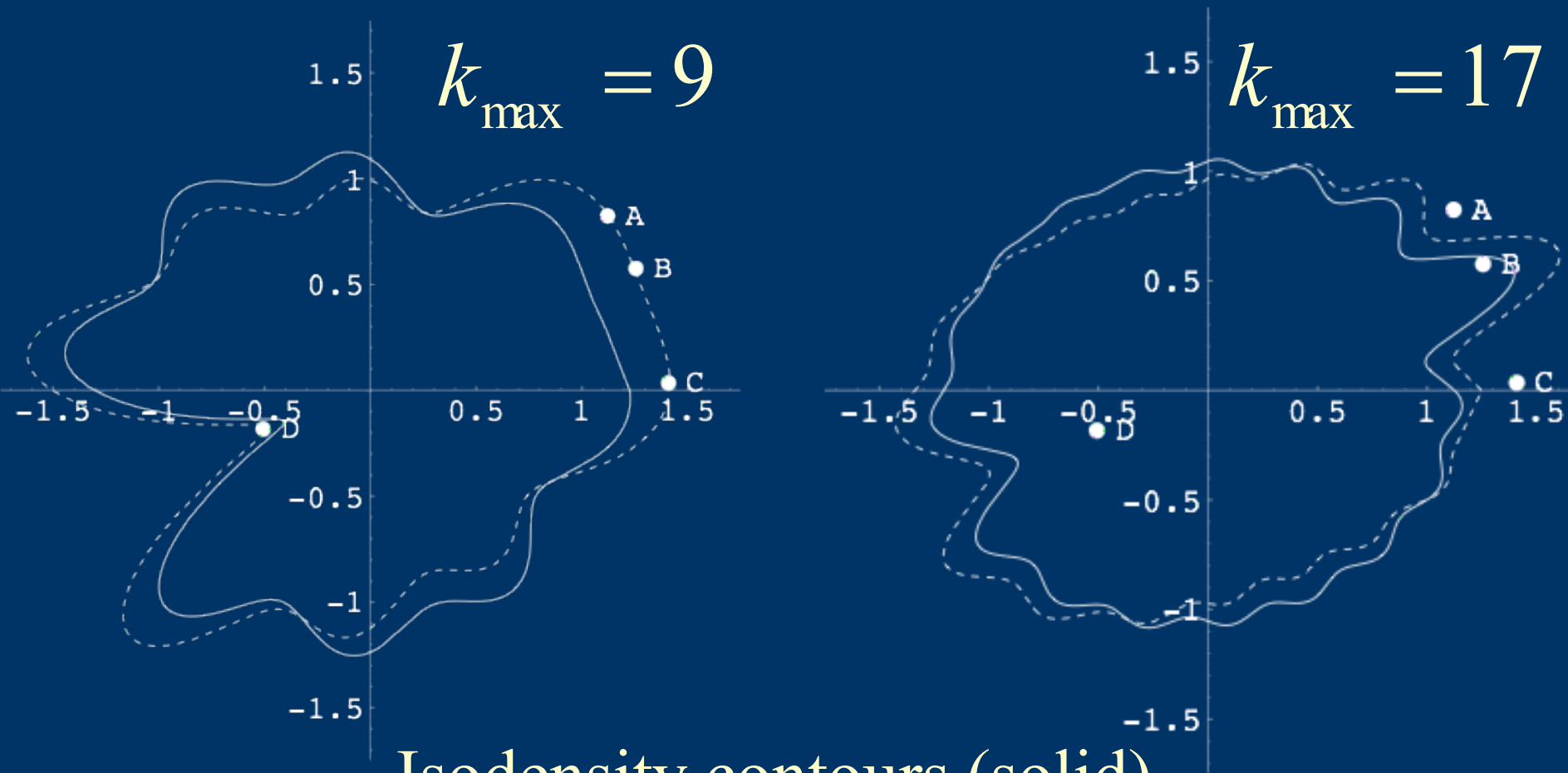


# Solution for B2045+265

kmax=5



# Solution for B2045+265



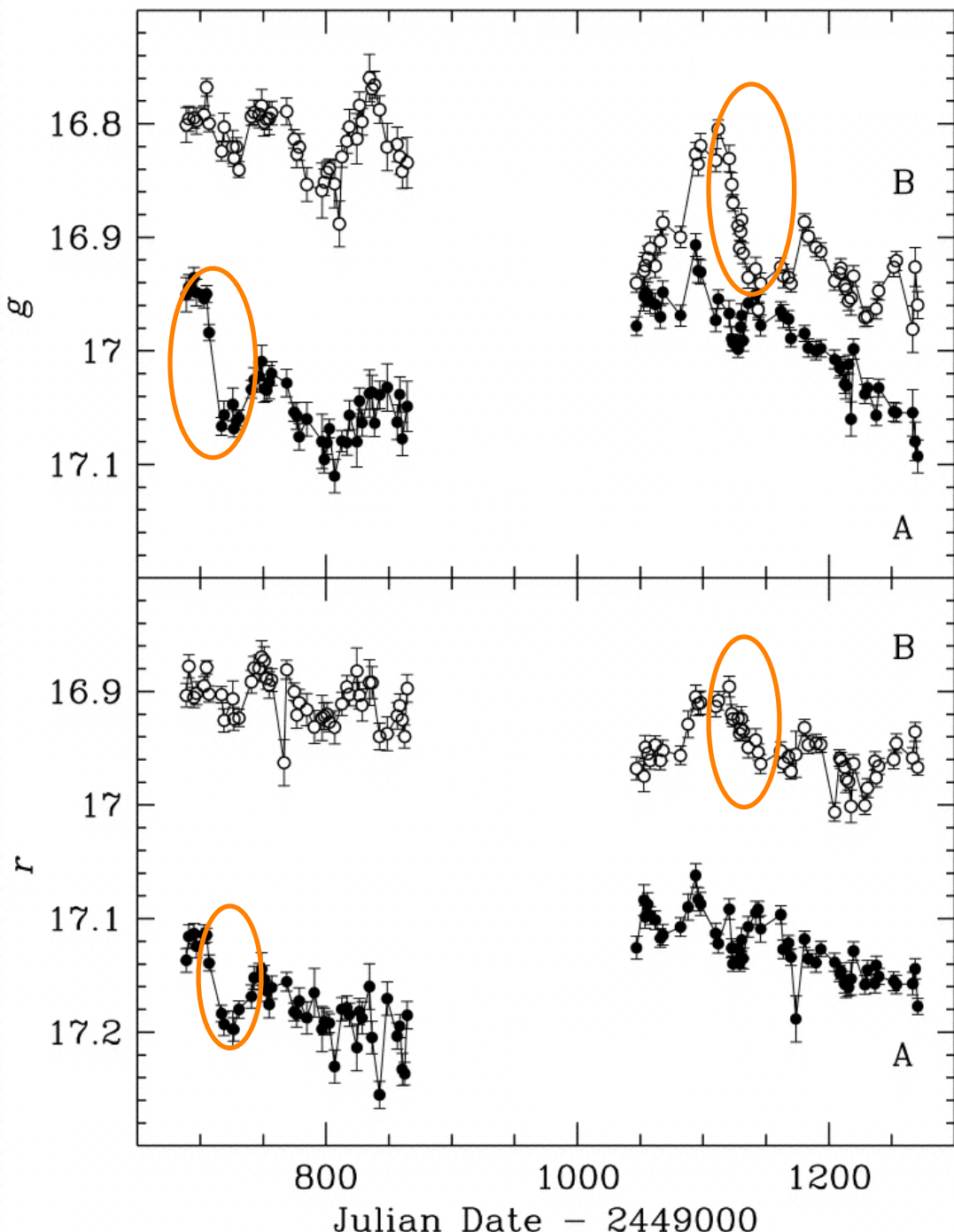
Isodensity contours (solid)  
and critical curves (dashed)

# What Have We Learned from Multipoles?

- Multipole models with shear cannot explain anomalous flux ratios
- Isodensity contours remain wiggly, regardless of truncation order
- Wiggles are most prominent near image positions; implies small-scale structure
- Ruled out a broad class of alternatives to CDM substructure

1995

1996



# Lens Time Delays

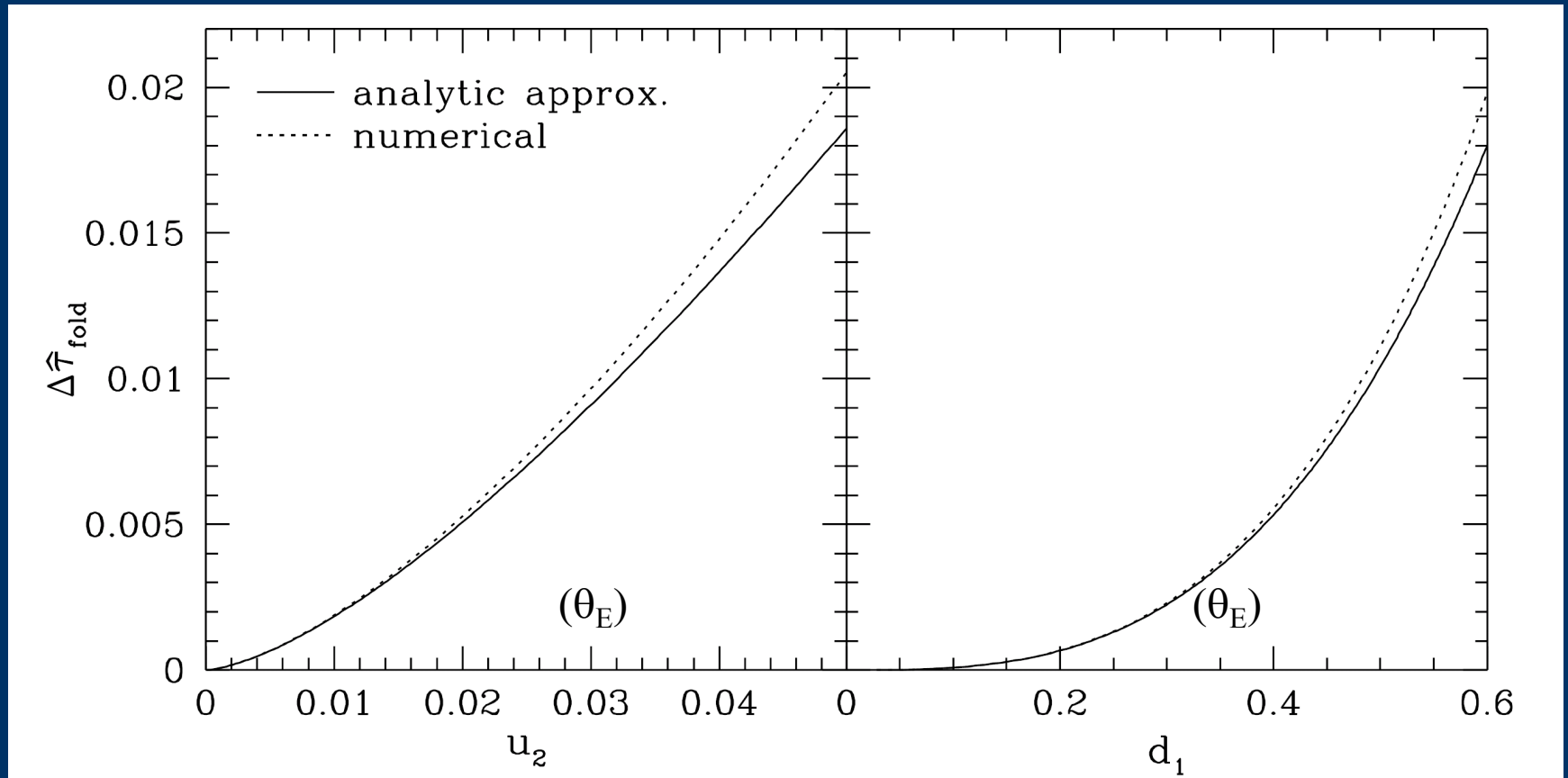
Robust probe of dark matter substructure?

Q0957+561

*Kundić et al. (1997)*

# Time-Delay Relation for Fold Pairs

$$\Delta\tau_{fold} \approx \sqrt{-\frac{16u_2^3}{27h}} \approx -\frac{h}{2}d_1^3$$



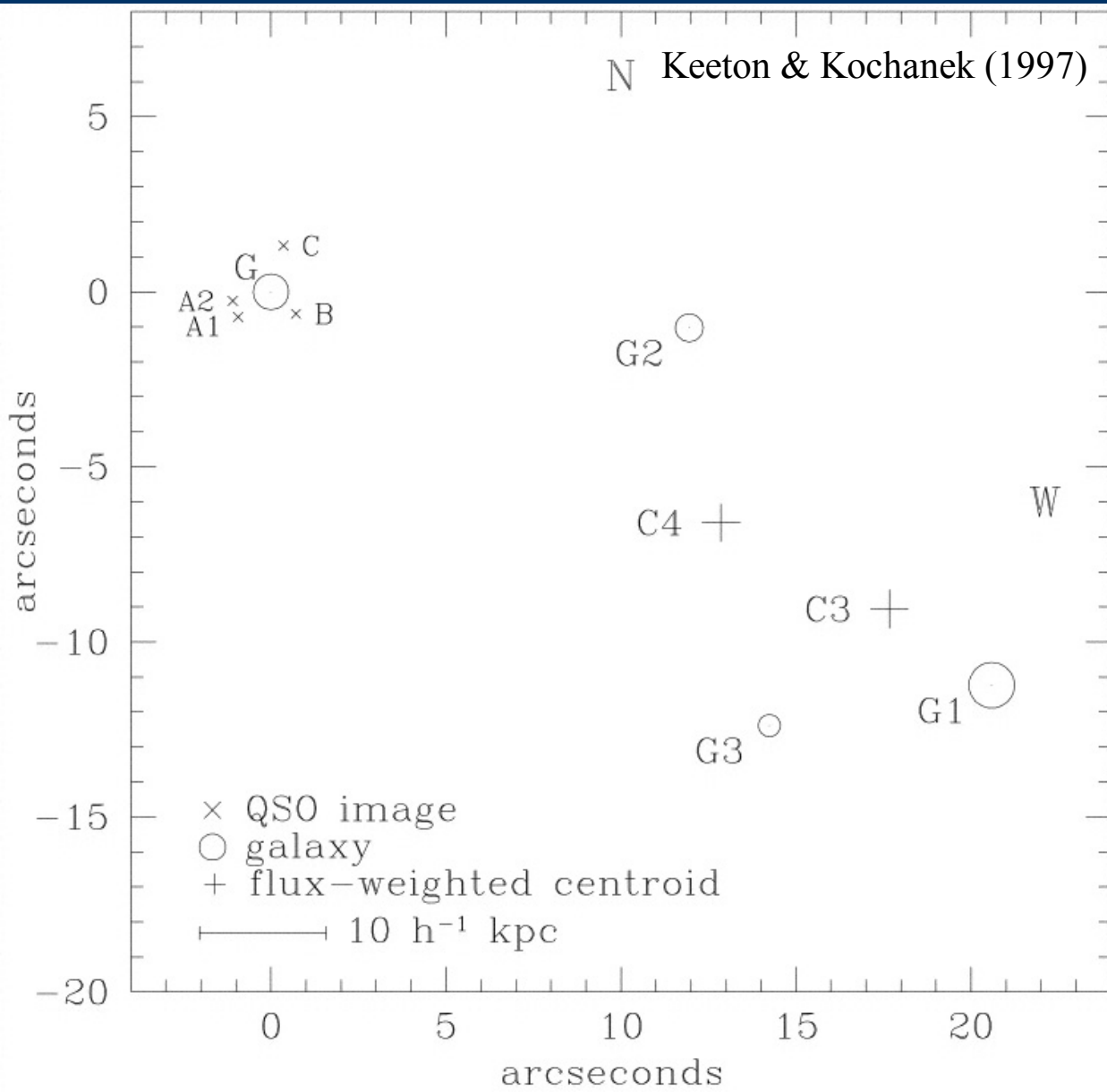
Analytic scaling is astrophysically relevant



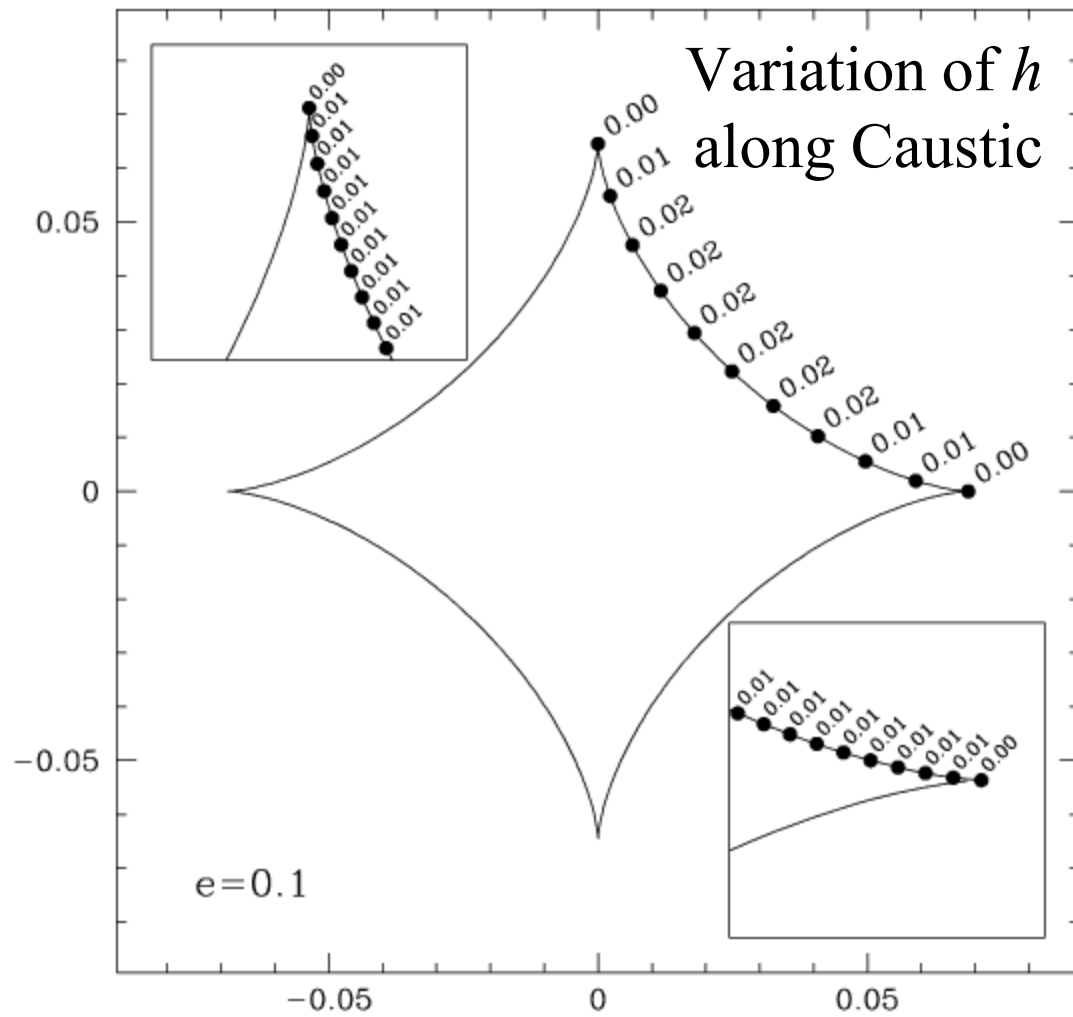
# Dependence of Time Delay on Lens Potential

- Use  $h$  as proxy for time delay
- Model lens as elliptical galaxy with shear
- Higher-order multipoles are not so important here

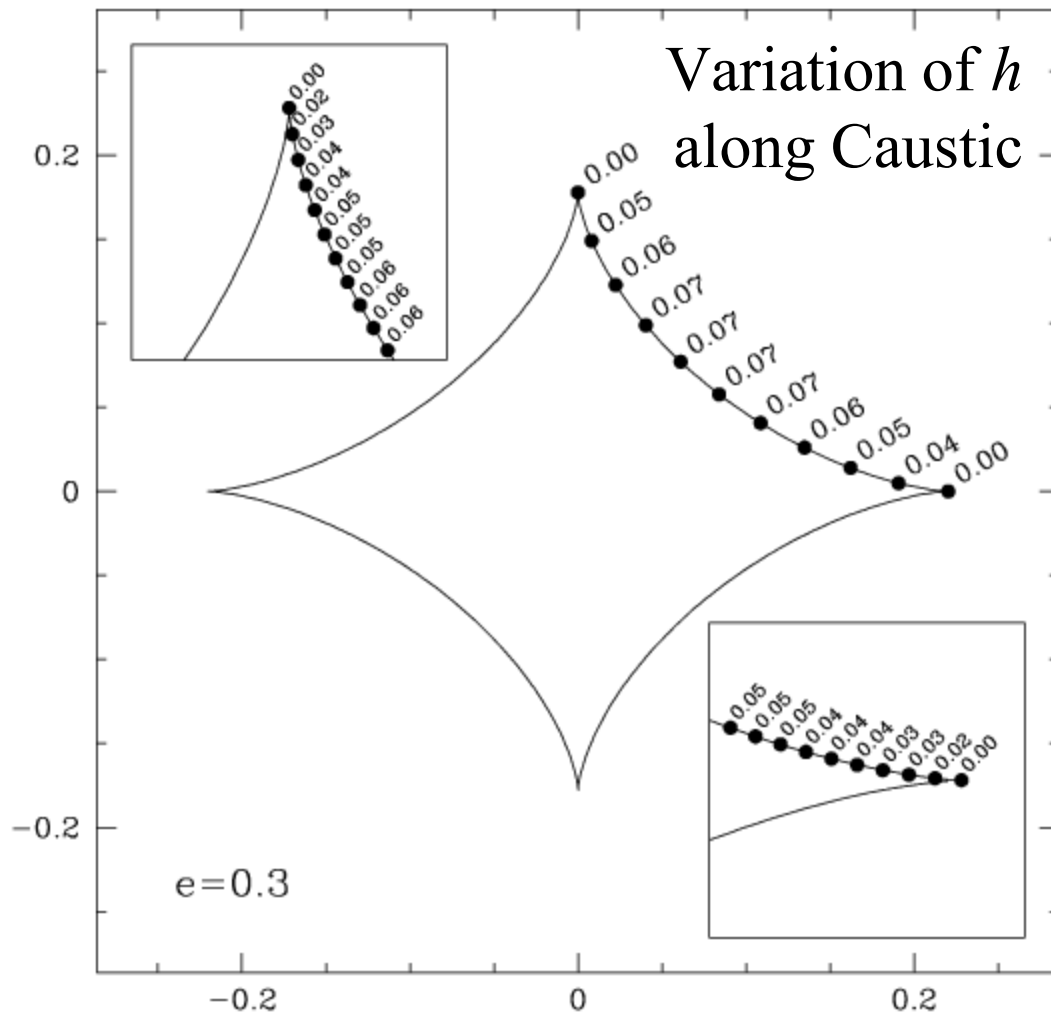
# What Is Shear?



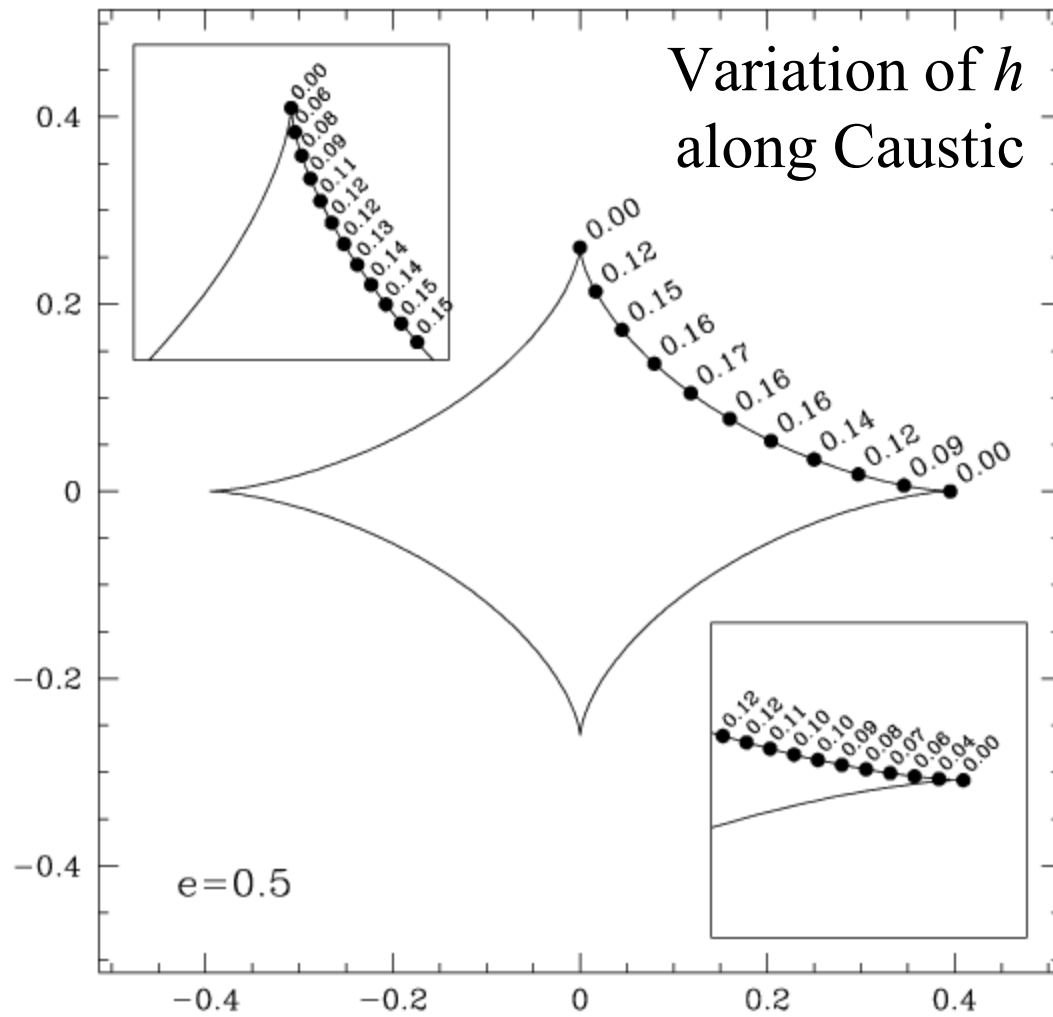
Neighboring galaxies  
perturb lensing  
observables



# Variation of $h$ along Caustic



# Variation of $h$ along Caustic

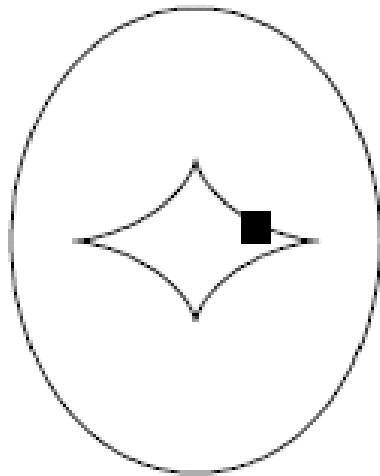


# Time Delays for a Realistic Lens Population

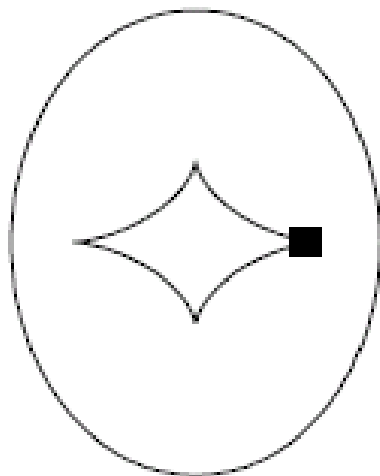
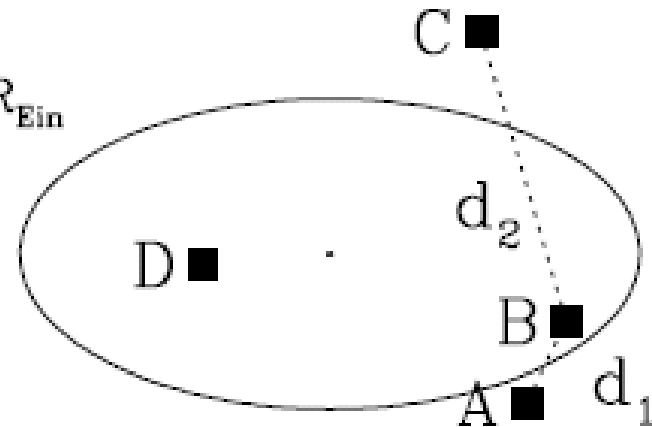
- Perform Monte Carlo simulations:
  - use galaxies with distribution of ellipticity, shear and multipoles
  - use random source positions to create mock four-image lenses
  - use Gravlens software (*Keeton 2001*) to obtain image positions and time delays
  - create time delay histogram for each image pair



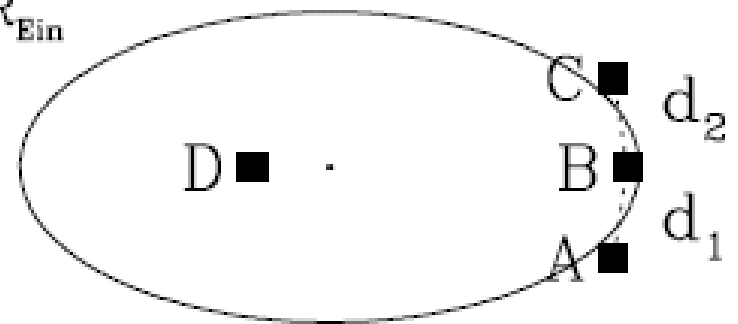
# Matching Mock and Observed Lenses



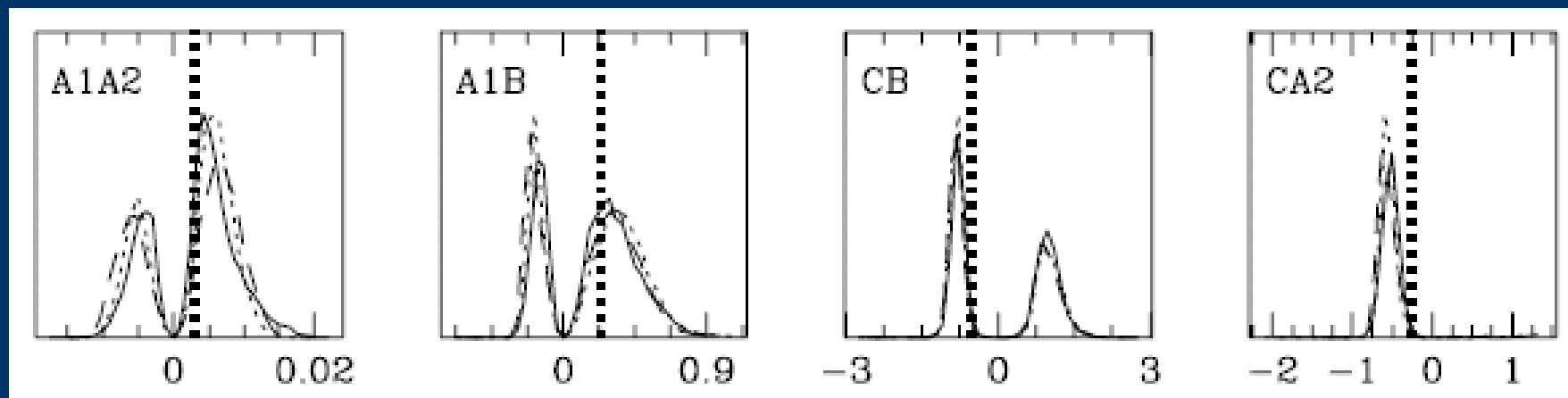
Fold  
 $d_1 \ll d_2 \sim R_{\text{Ein}}$



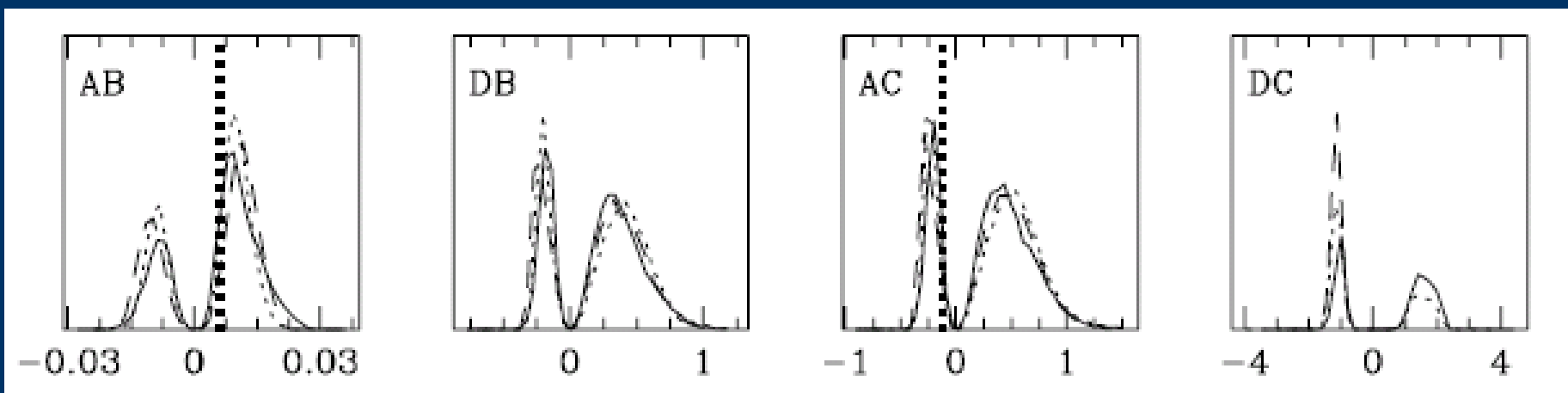
Cusp  
 $d_1 \sim d_2 \ll R_{\text{Ein}}$



# Histograms for Scaled Time Delay: Folds

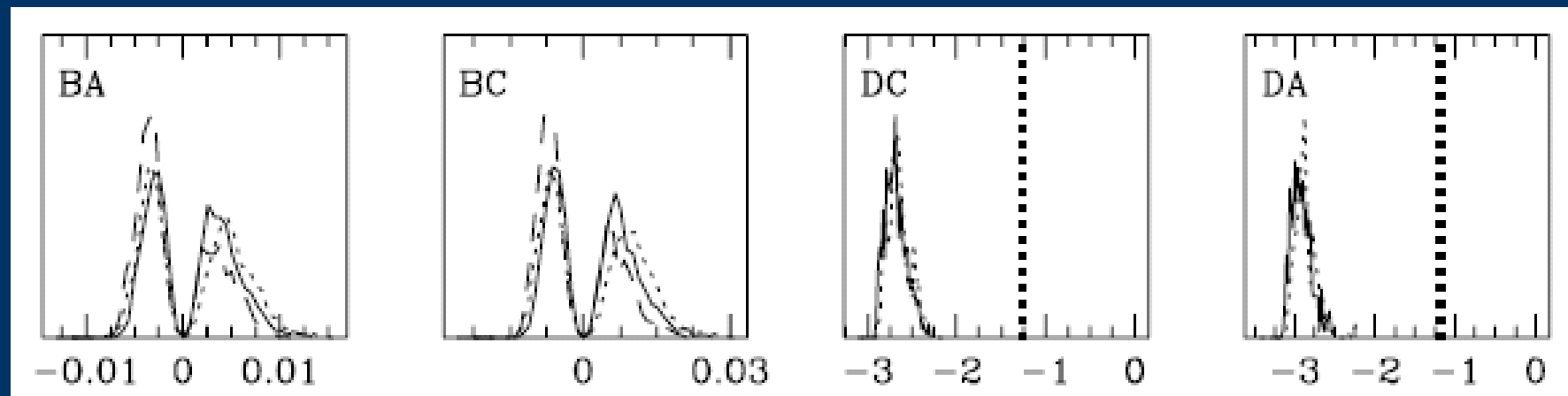


PG 1115+080

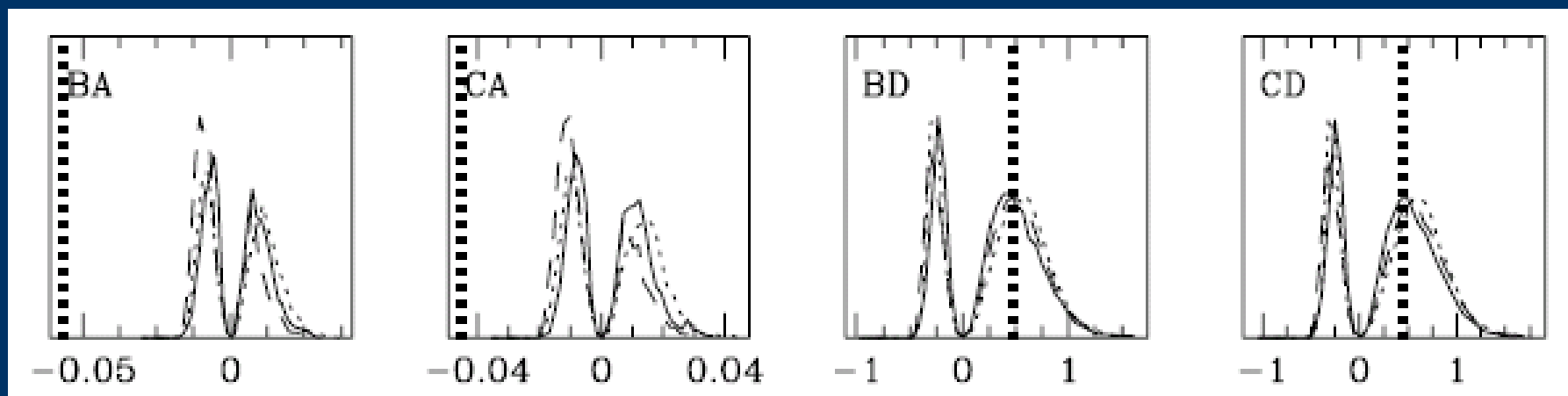


SDSS J1004+4112

# Histograms for Scaled Time Delay: Cusps



RX J0911+0551



RX J1131-1231

# Nature of Dark Matter

- Various explanations of dark matter

sterile neutrino

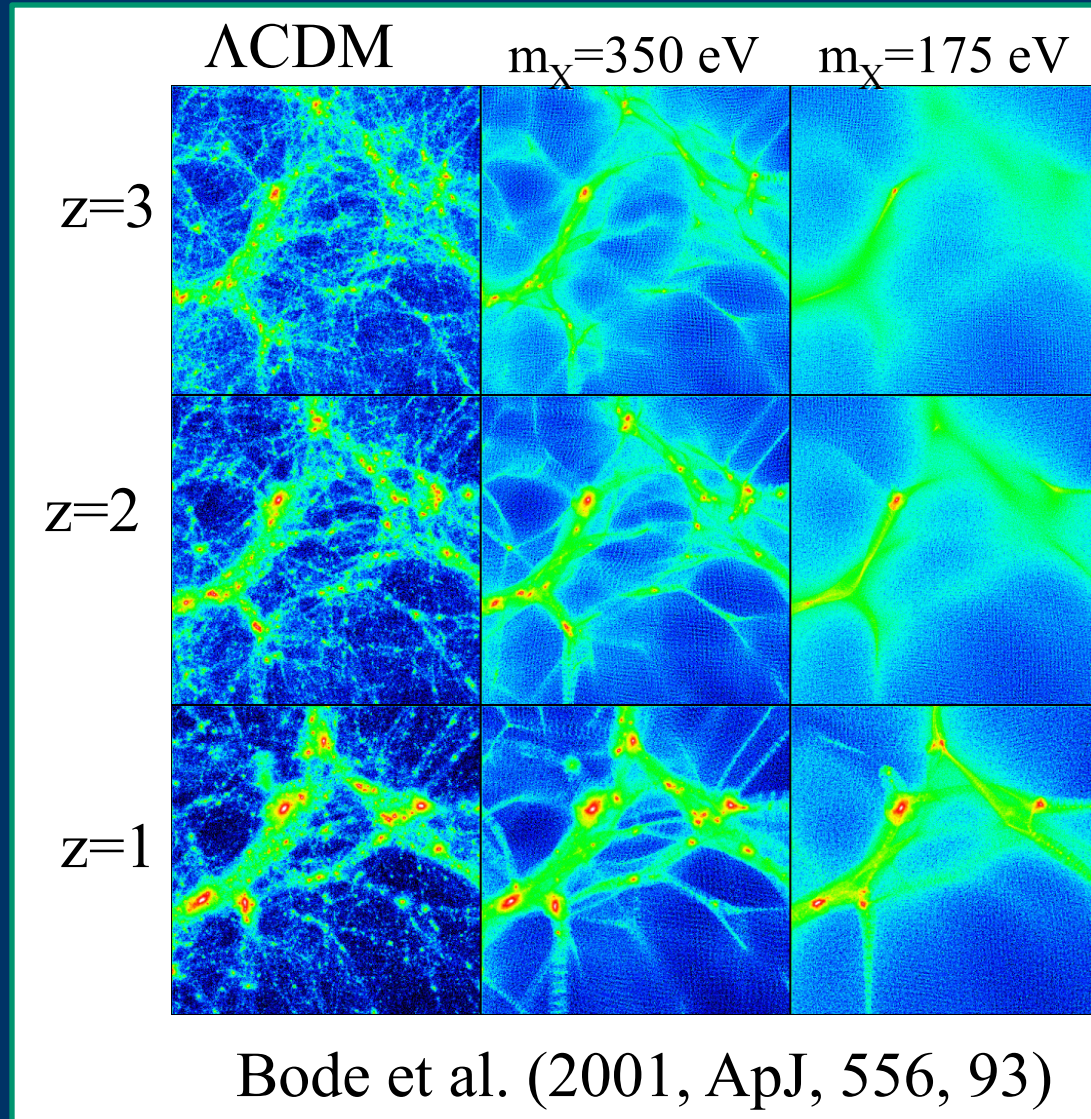
lightest supersymmetric particle

extra dimensions

- Signatures of dark matter

particle annihilation at galactic center or elsewhere

strong lensing?



# Constraining Dark Matter with Strong Lensing

- Different models give different mass functions
- Use lensing observables to constrain mass function and hence particle properties
- Keeton and Moustakas (2008) have shown that time delays are sensitive to substructure

# What Have We Learned from Time Delays?

- Time delay of the close pair in a fold lens scales with the cube of image separation
- Time delay is sensitive to ellipticity and shear, but not higher-order multipoles
- Monte Carlo simulations reveal strong time-delay anomalies in several lenses
- We can use time delays to understand the nature of dark matter