

# ***Gluon distribution from jet analysis in EIC***

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- Gluon distribution from jets
  - Difficulty in inclusive events  $\Rightarrow$  looking at 2+1 jet events
  - What to expect: kinematic reach
  - What to expect: statistical errors
  
- Other jet-related processes
  - Diffractive jets
  - DGLAP vs. BFKL in forward jets (saturation?)

Standard way of extracting the gluon distribution:

- consider the inclusive  $F_2$  (plus other inclusive quantities as Drell-Yan cross-sections)
- PDF parametrised at  $Q^2 = Q_0^2$  and evolved with DGLAP

At LO:

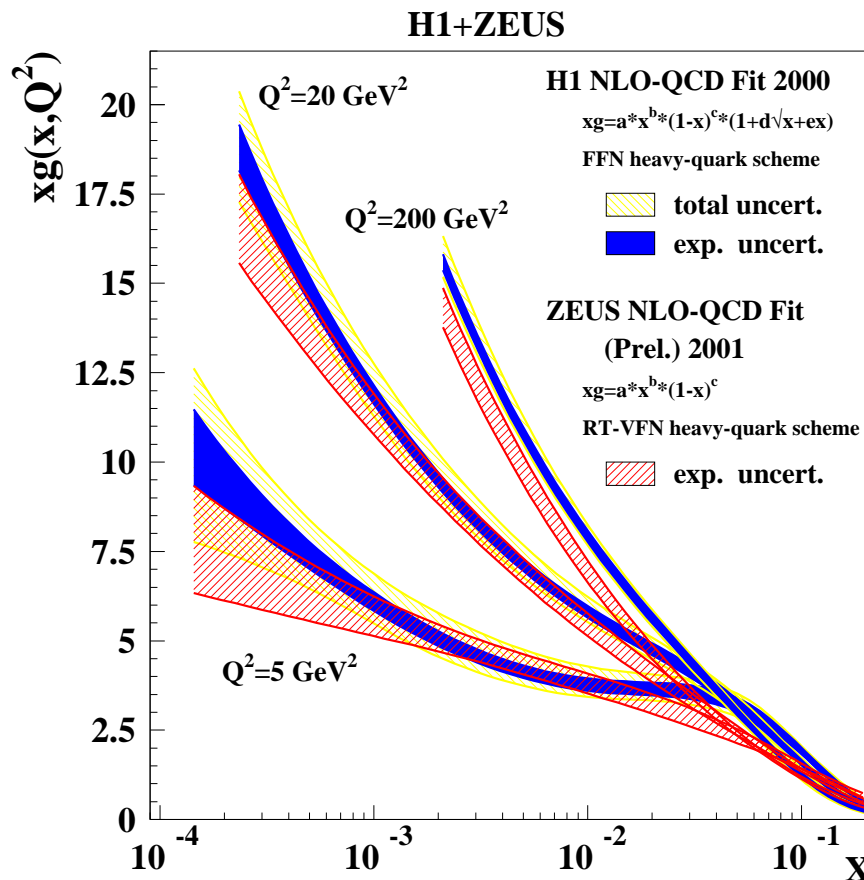
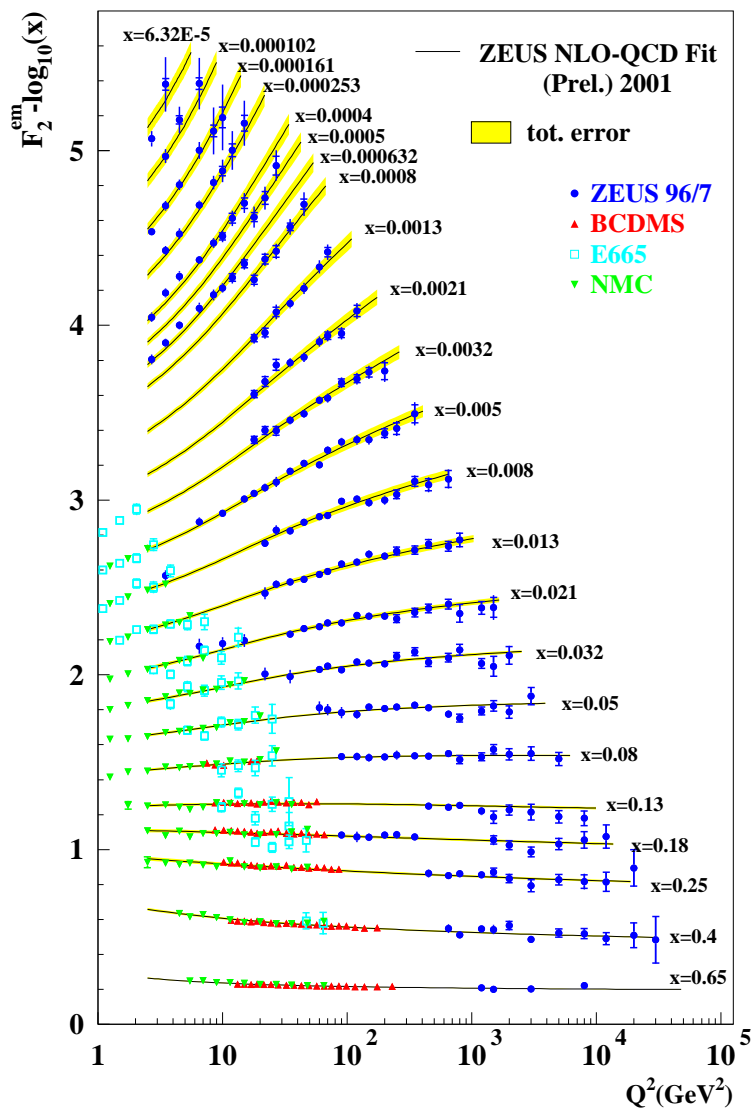
$$F_2(x, Q^2) \propto xq(x, Q^2)$$
$$\partial_{\log(Q^2)} q(x, Q^2) = \alpha_s [P_{qq} \otimes q(\xi, Q^2) + P_{qg} \otimes g(\xi, Q^2)]$$
$$\partial_{\log(Q^2)} g(x, Q^2) = \alpha_s [P_{gq} \otimes q(\xi, Q^2) + P_{gg} \otimes g(\xi, Q^2)]$$

The gluon distribution is accessed

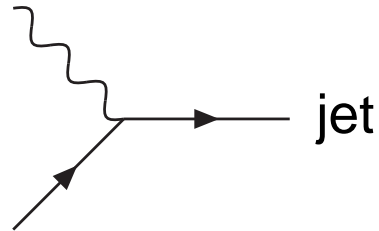
- through a convolution (with the splitting function)
- through the slope of  $F_2$

The gluon distribution is accessed through the slope of  $F_2$

- more difficult to estimate
- particularly at small  $x$  where the  $Q^2$  range is smaller

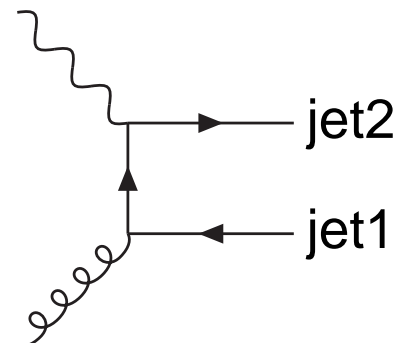
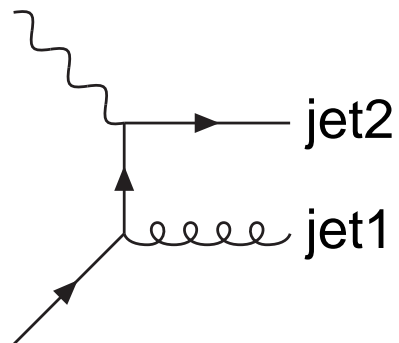


“1+1 jet” dominated by



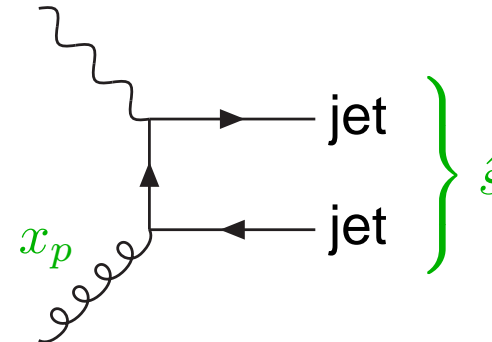
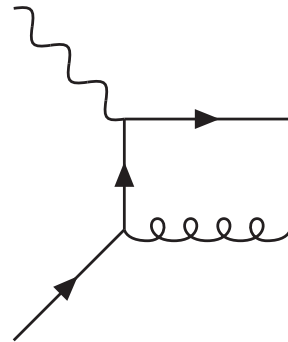
i.e. dominated by quarks (gluons start at NLO)

“2+1 jets” becomes more interesting



- involve quarks and gluons
- dominated by gluons at small  $x$

“2+1 jets” becomes more interesting



Main formula:

$$\frac{d^2\sigma^{2+1}}{dx_p dQ^2} = \alpha_s [a g(x_p, Q^2 + \hat{s}) + b q(x_p, Q^2 + \hat{s})]$$

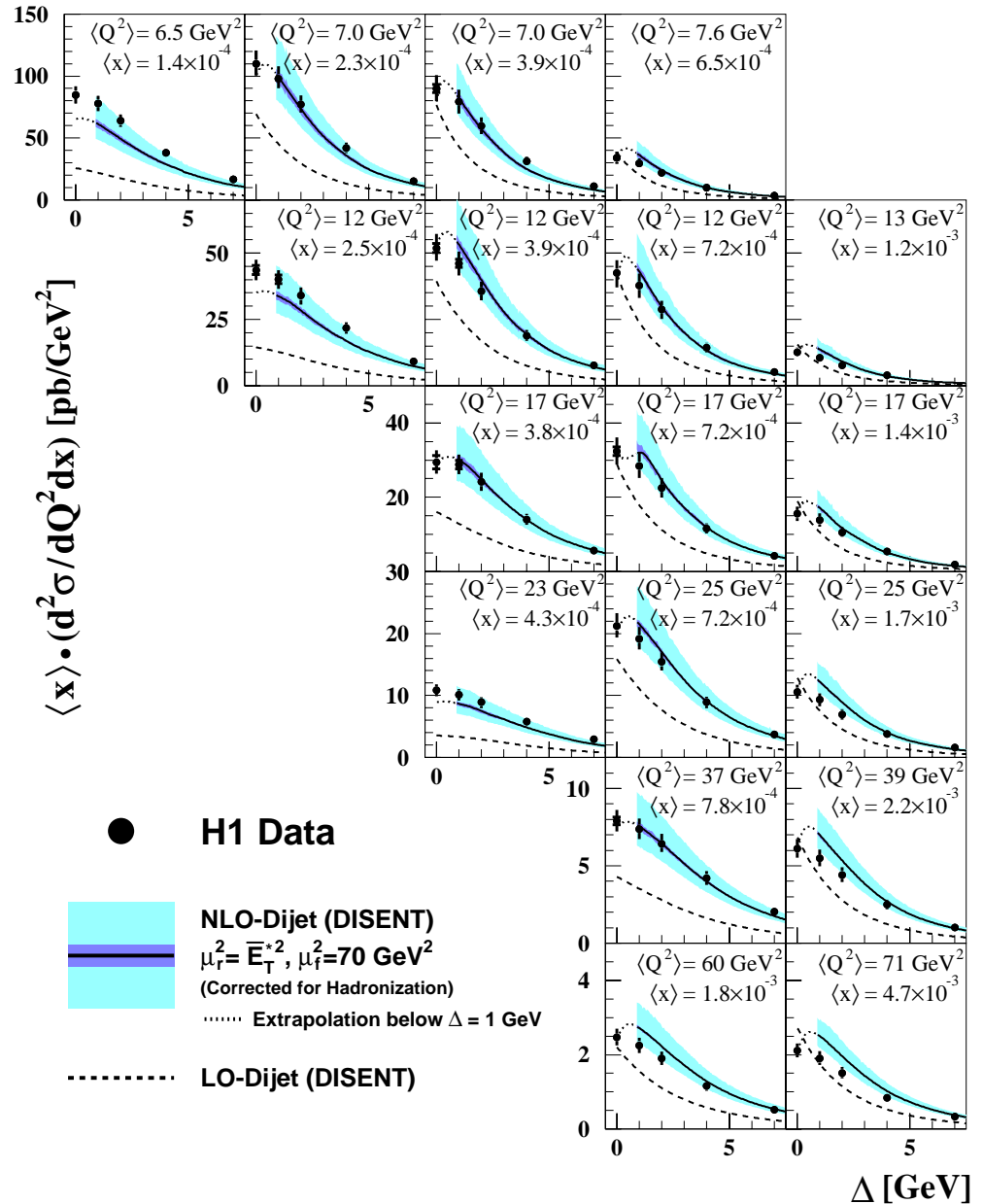
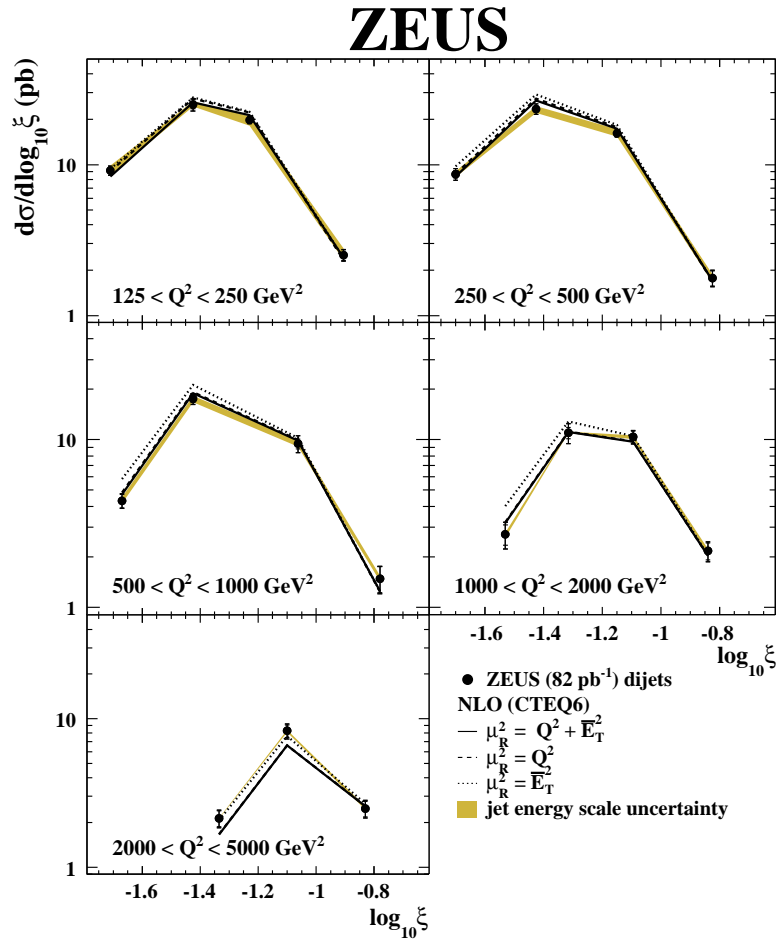
Technique:

1.  $a$  and  $bq$ : matrix elements & quark piece from Monte Carlo

2.  $x_p = x \left(1 + \frac{\hat{s}}{Q^2}\right)$

3. Extract the gluon distrib:  $g_{\text{extr.}} = \frac{1}{a_{\text{MC}}} (\sigma_{\text{meas.}} - b_{\text{MC}}q)$

Measured at HERA





Can, in principle, be computed from pQCD

Monte Carlo allows to

- put experimental cuts (e.g. outgoing electron energy)
- account for parton shower and hadronisation
- account for jet-clustering effects
- compute quark and gluon parts

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- Consequences:

- minimal  $x = \frac{Q^2}{Q^2 + 4P(E - E'_{\min})}$
- minimal  $\hat{s} = 2p_{t,\min}^2 [1 - \cos(R)]^2$

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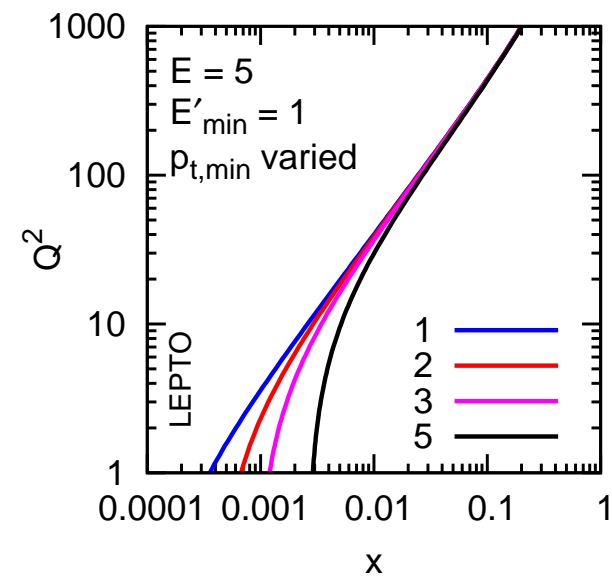
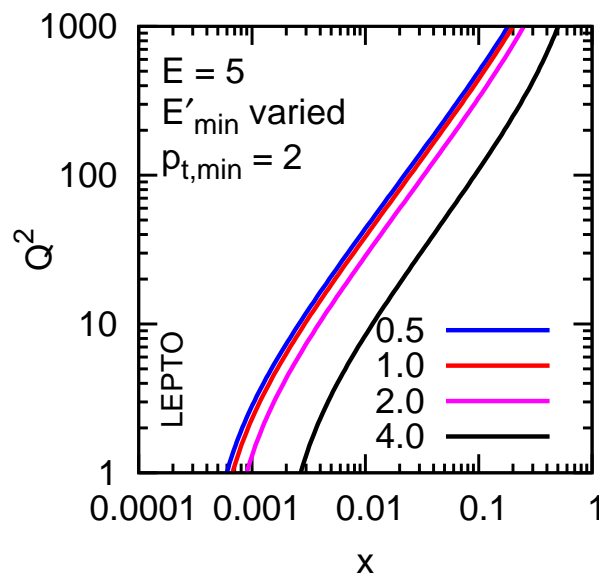
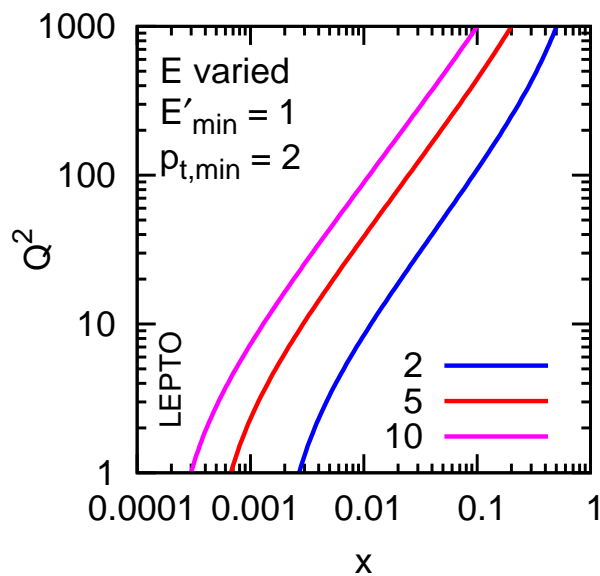
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Reach small  $x$ :

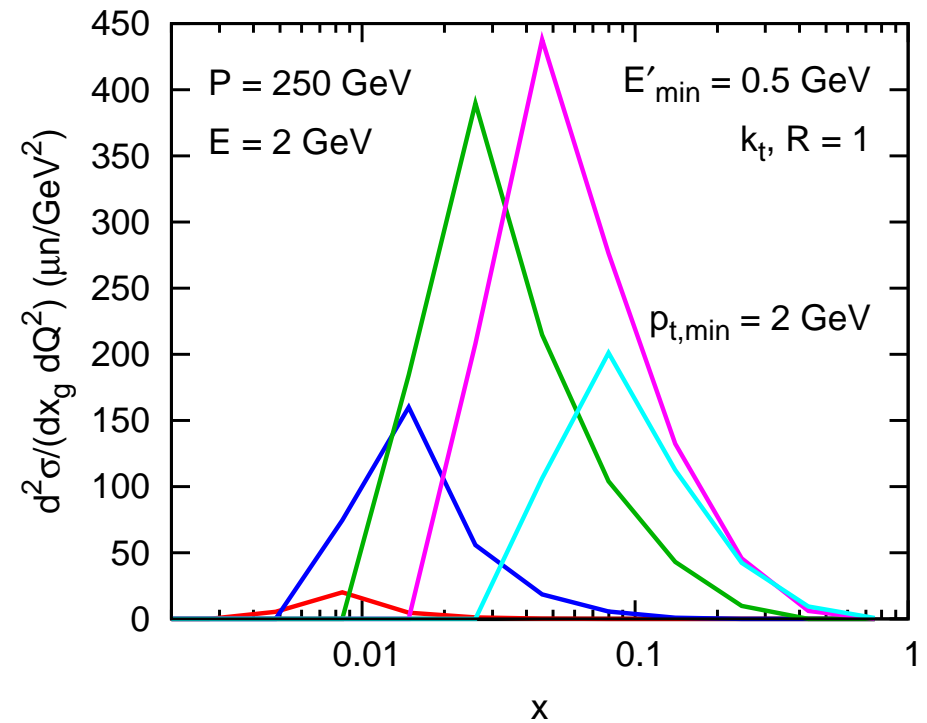
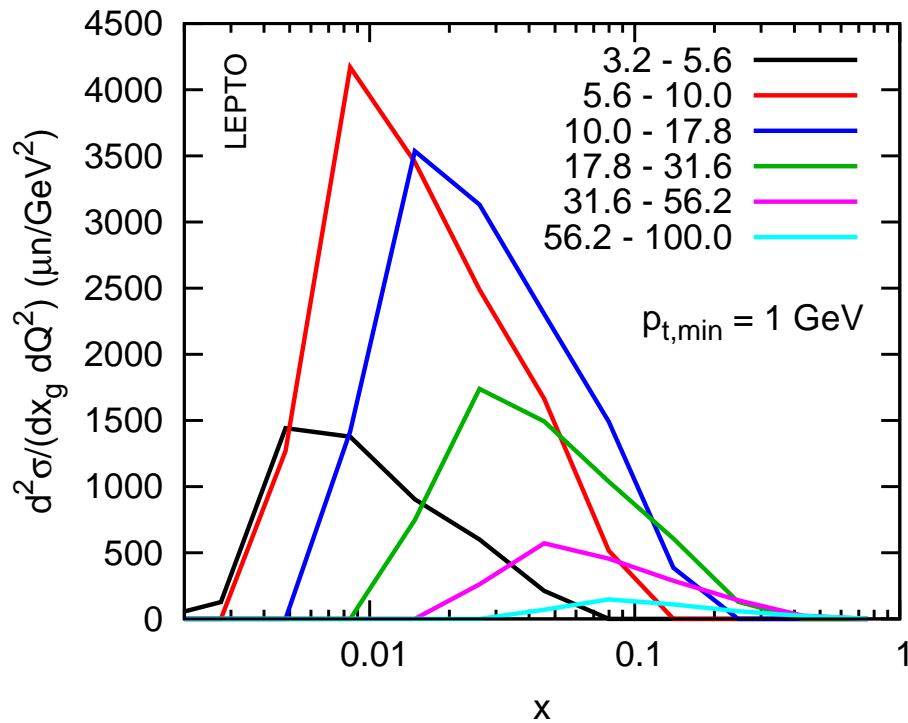
- decrease  $p_{t,\min}$  or  $E'_{\min}$  / increase beam energies – experimental issue
- decrease  $R$  – more systematic errors

Hadron beam:  $P = 250$  GeV

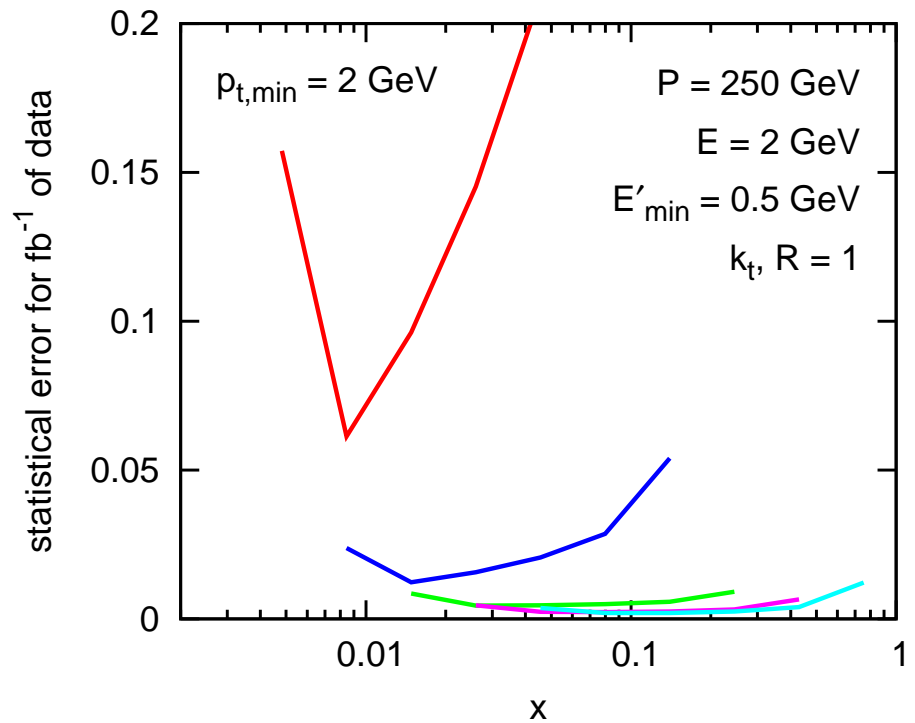
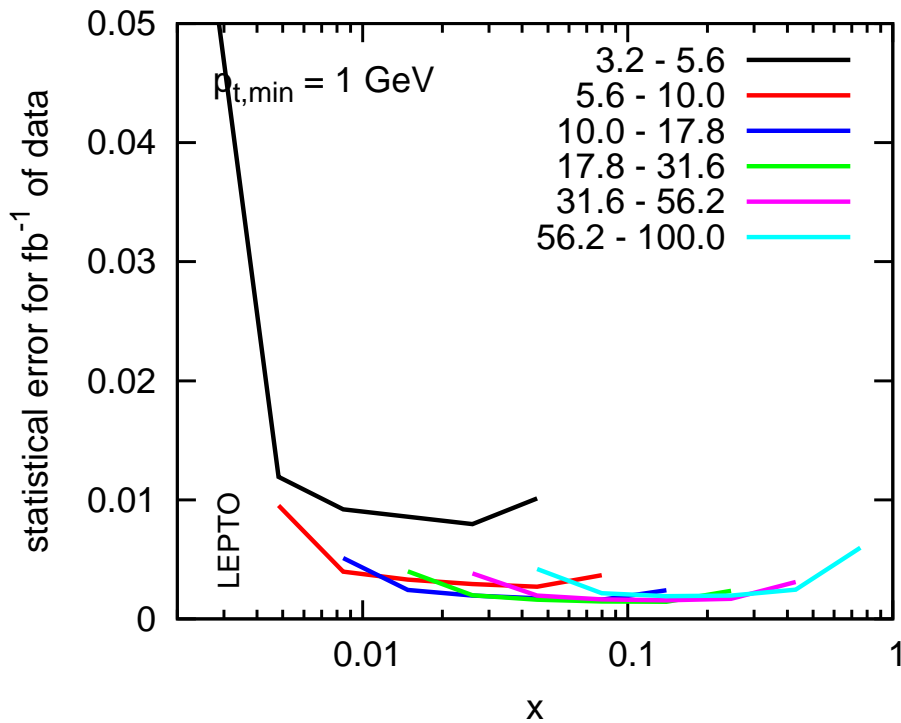
Clustering:  $k_t$  algorithm with  $R = 1$



Hard to reach  $x_g < 10^{-3}$



- Over optimistic cuts
- Less optimistic reduces  $x_{\text{min}}$ ,  $Q_{\text{min}}^2$  and the cross-section



- Fine with over optimistic cuts
- Less optimistic increases errors

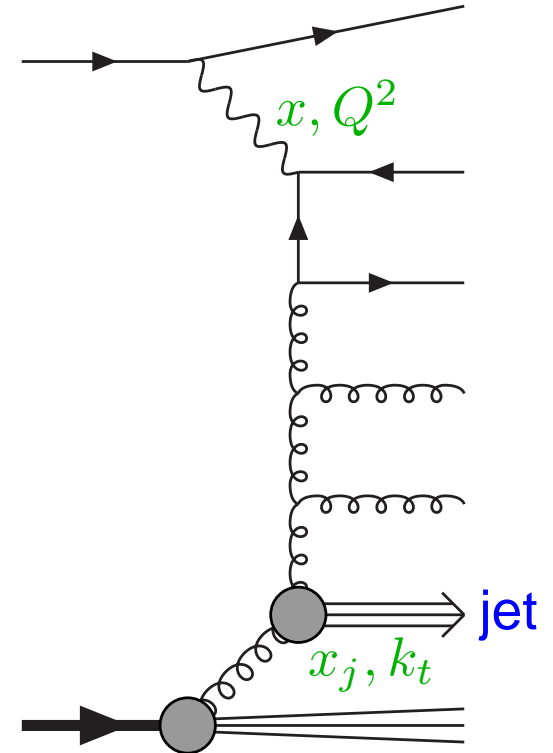


Some of the systematics come from theory:

- Scale in  $g$ :  $Q^2 + \hat{s}?$ ,  $Q^2?$
- Matrix element computation: effects of the cuts
- Errors on the quark contrib.: from incl. measurements
- Clustering effects: vary/optimize jet algorithm and parameter

## ***Other useful jet measurement(s)***

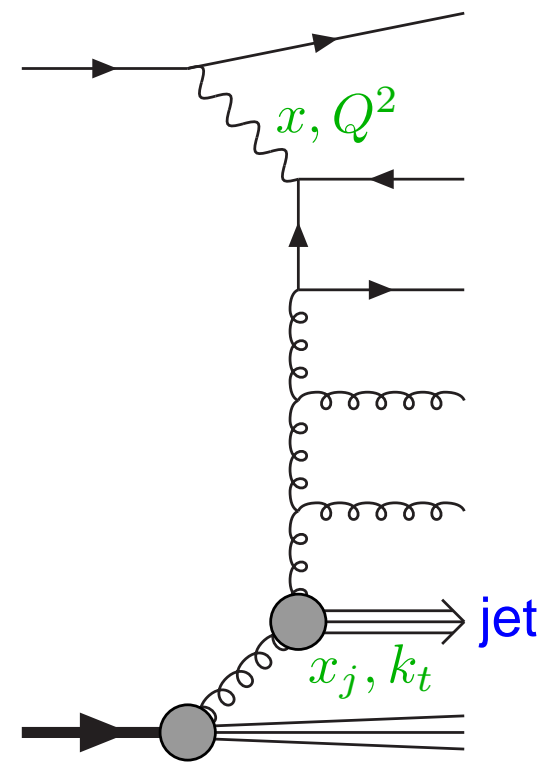
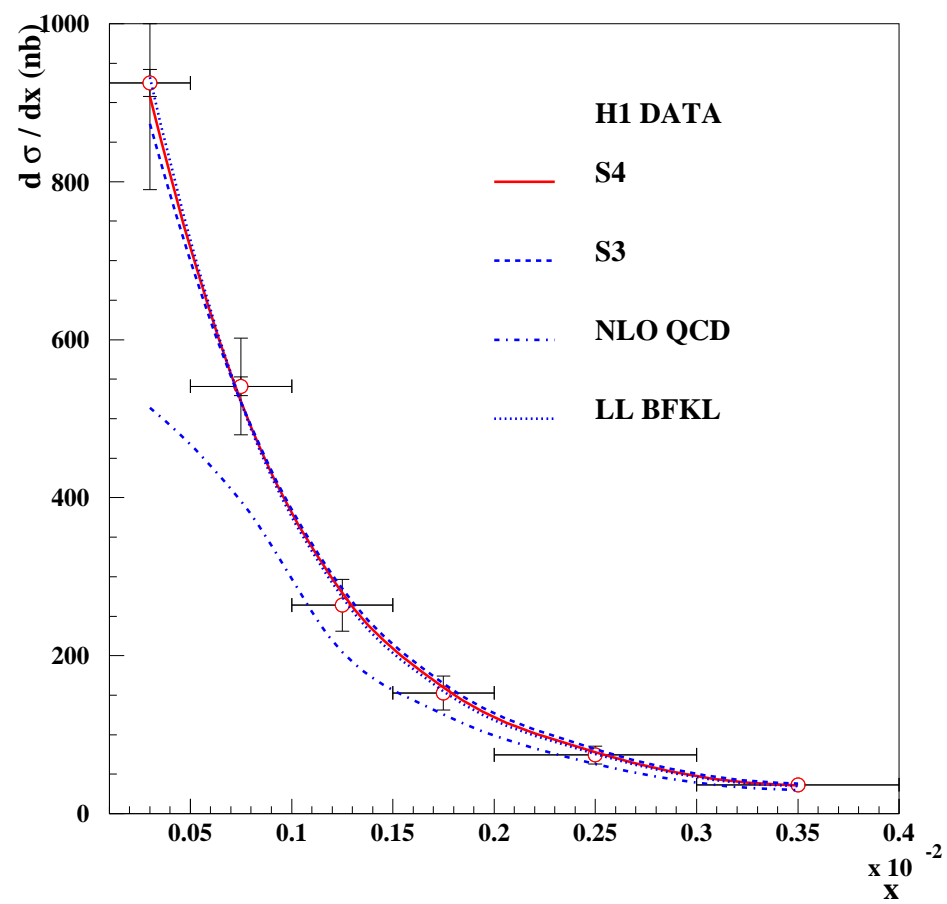
Tag a forward jet with  $x \ll x_j$ .



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- DGLAP and fixed-order fail
- BFKL works

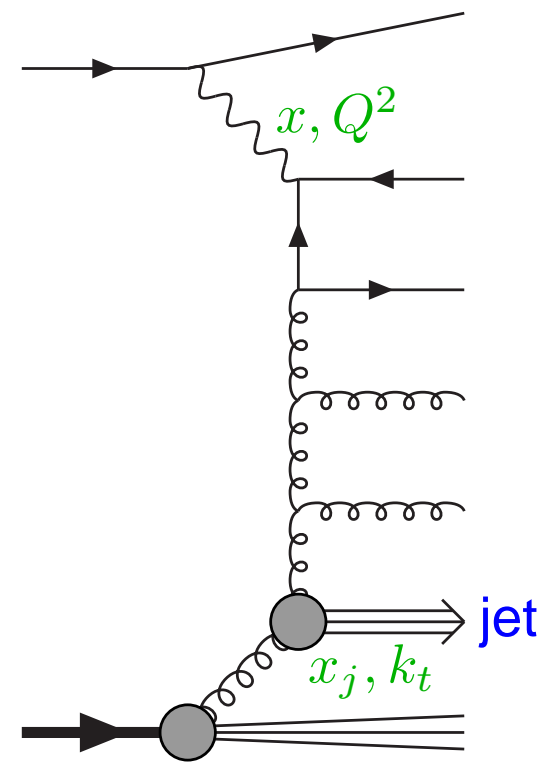
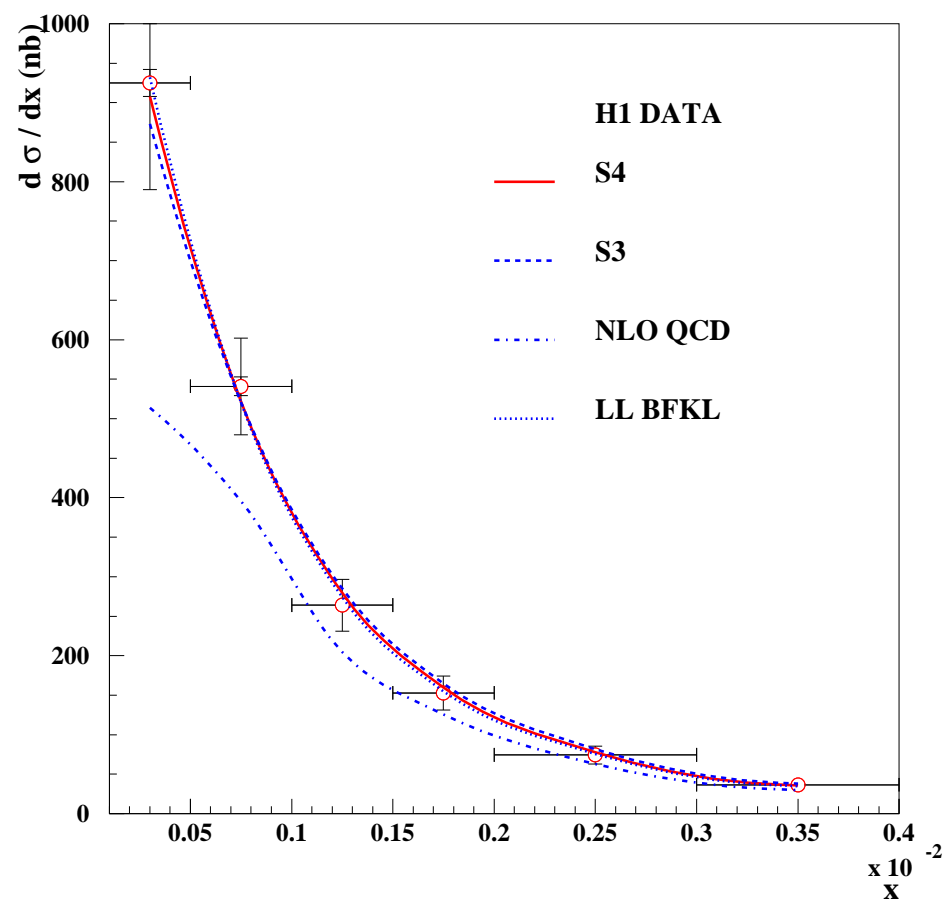


[Kepka, Marquet, Peschanski, Royon]

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Question for EIC:  
 Hints for BFKL, saturation & multiple interactions effects in  $eA$  collisions?

## What can we learn from jet physics at EIC

- gluon PDF
  - from 2+1 jets
  - Kinematics and statistical errors
    - Low-energy option: probably needs over-optimistic cuts
    - Larger-energy option promising
  - $ep$  vs.  $eA$ : multiple interactions effect (+shadowing)
- Other jet measurements
  - diffractive 2+1 jets  $\longrightarrow$  diffractive PDF
  - BFKL (and saturation) tests from forward jets