

# Filamentary Environment and Mass Measurements of Galaxy Clusters

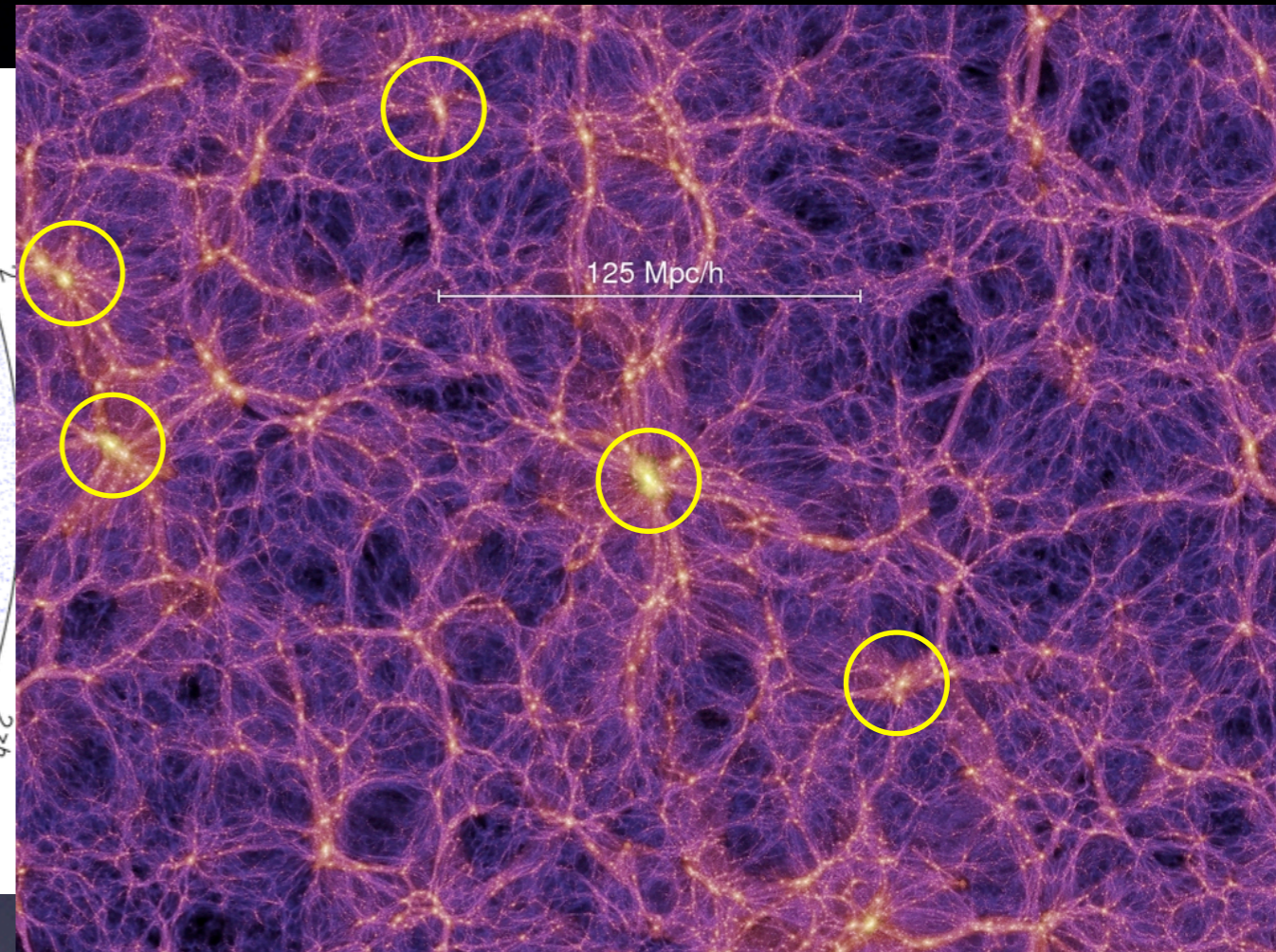
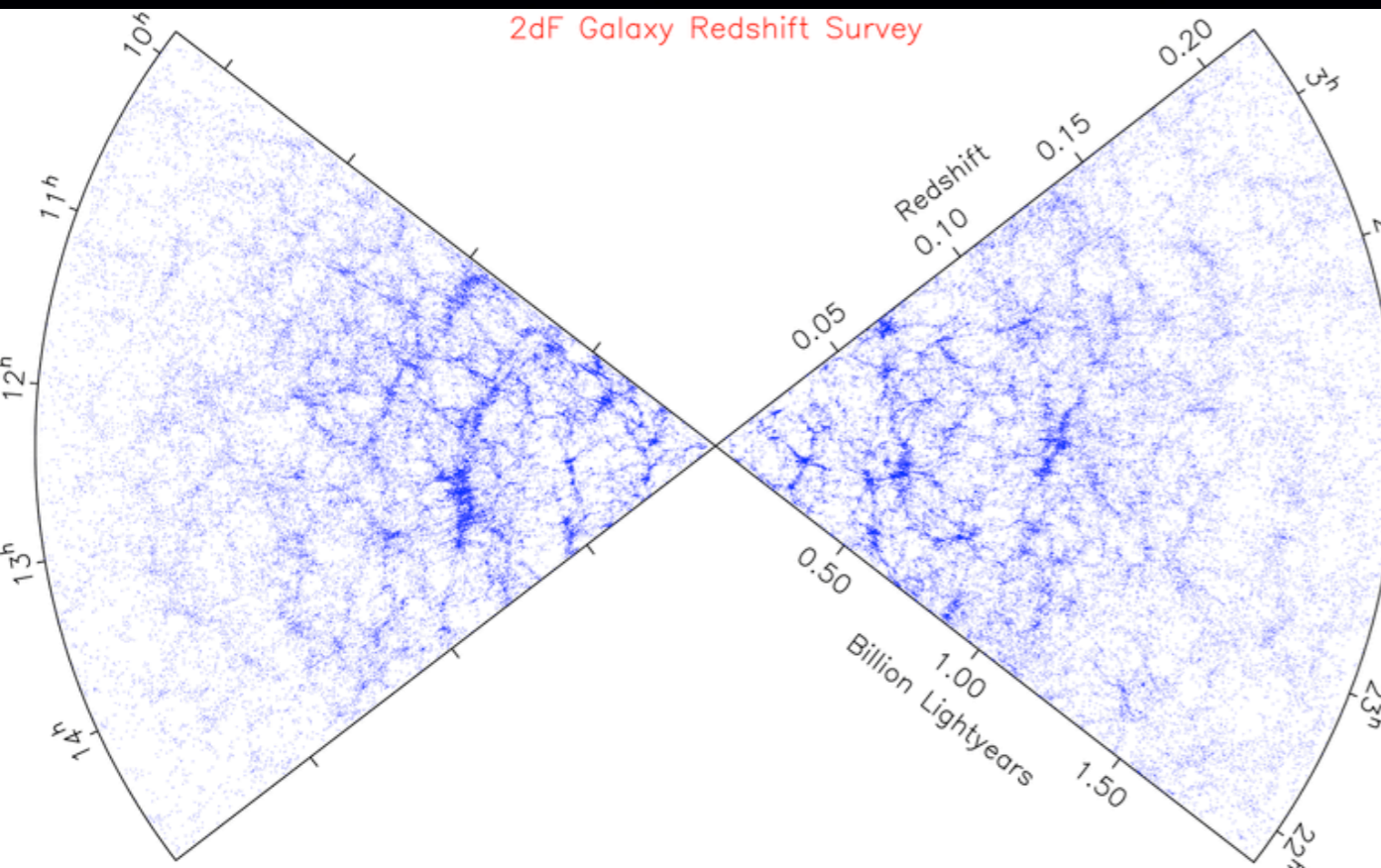
Yookyung Noh (UC Berkeley)

work with Joanne Cohn

12/10/2012

Fermilab Particle Astrophysics Seminar

# Cosmic Web



In observed galaxies

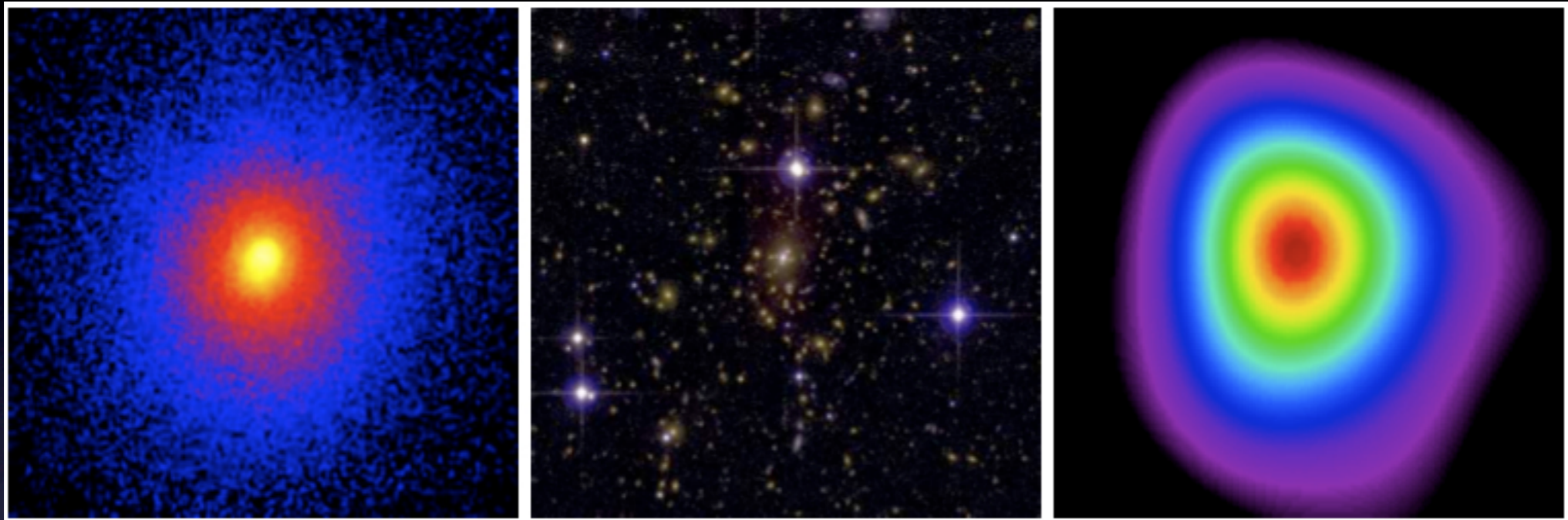
In simulated dark matter

Clusters are the largest, most massive virialized objects lying at the nodes of cosmic web

( $M \approx 10^{14}-10^{15} M_{\odot}/h$ ,  $R \approx 1 \text{ Mpc}$ )

# Clusters in Multi-wavelength Observations

**Abell 1835**  
 $z=0.25$   
5.2 arcmin  
( $\sim 1.2$  Mpc)  
 $M \sim 10^{15} M_{\odot}$



Mantz  
Linden++  
Marrone

## X-ray

Luminous, spatially extended objects due to hot gas

## Optical

Large populations of galaxies

## Microwave

Sunyaev-Zeldovich Effect (SZE)

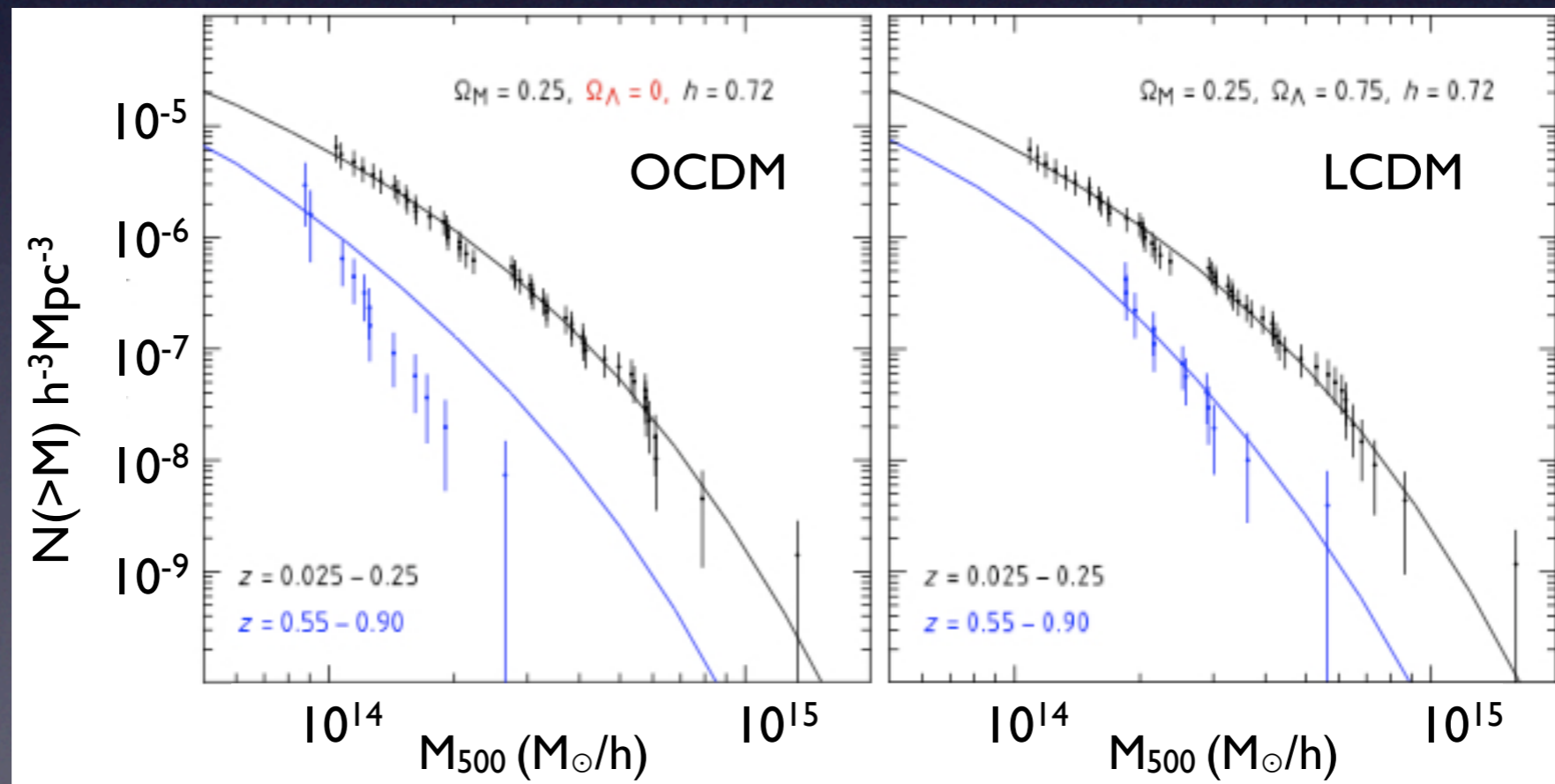
Decrement or increment of the background CMB

# Why do we study clusters?

- Cosmological probe
- Special environment of galaxies
- Hosting extreme astrophysical phenomena

Voit 05,  
Allen++11, etc.

Example:



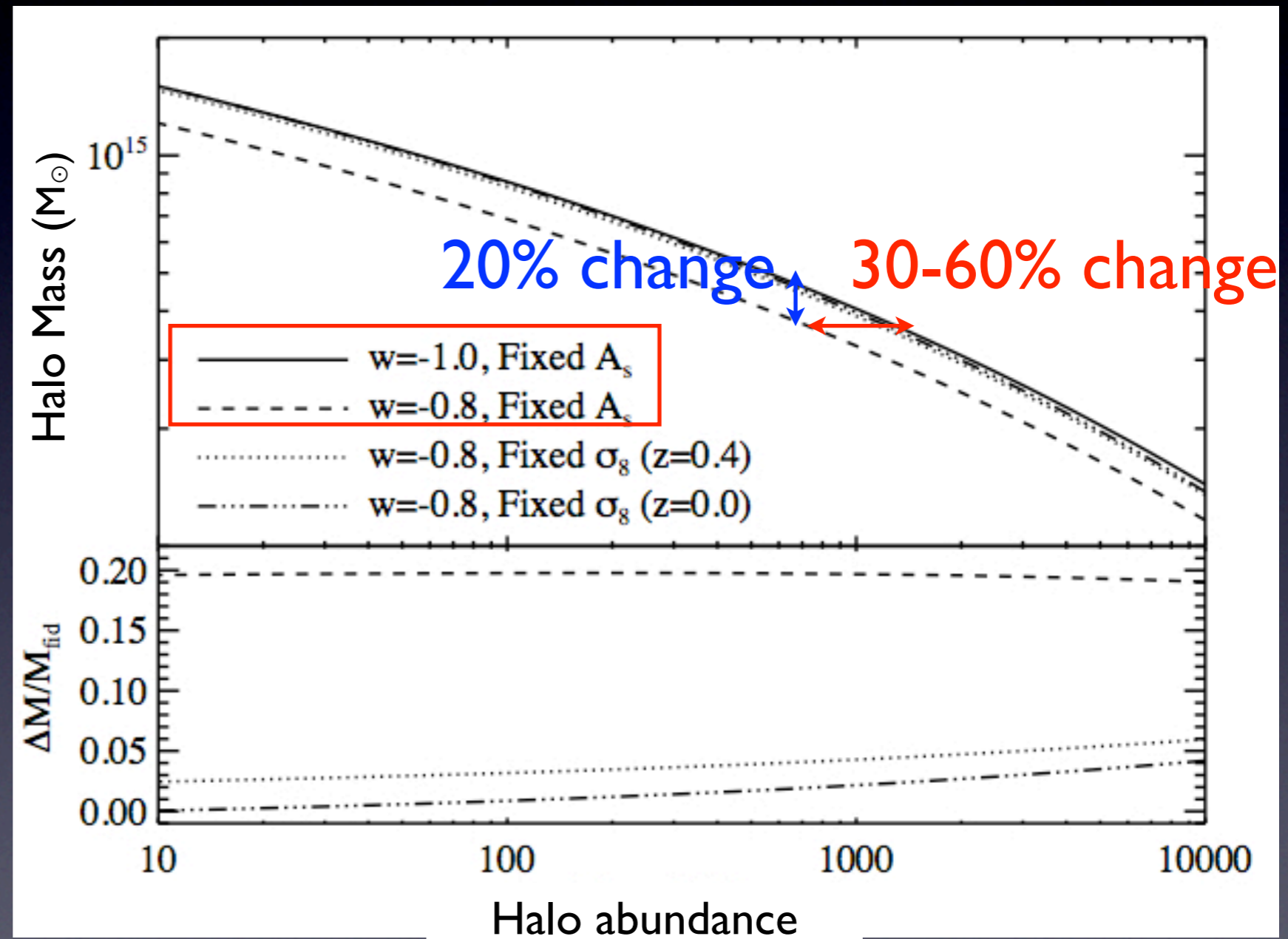
Vikhlinin++09

# Cluster mass is a crucial property!

Change from

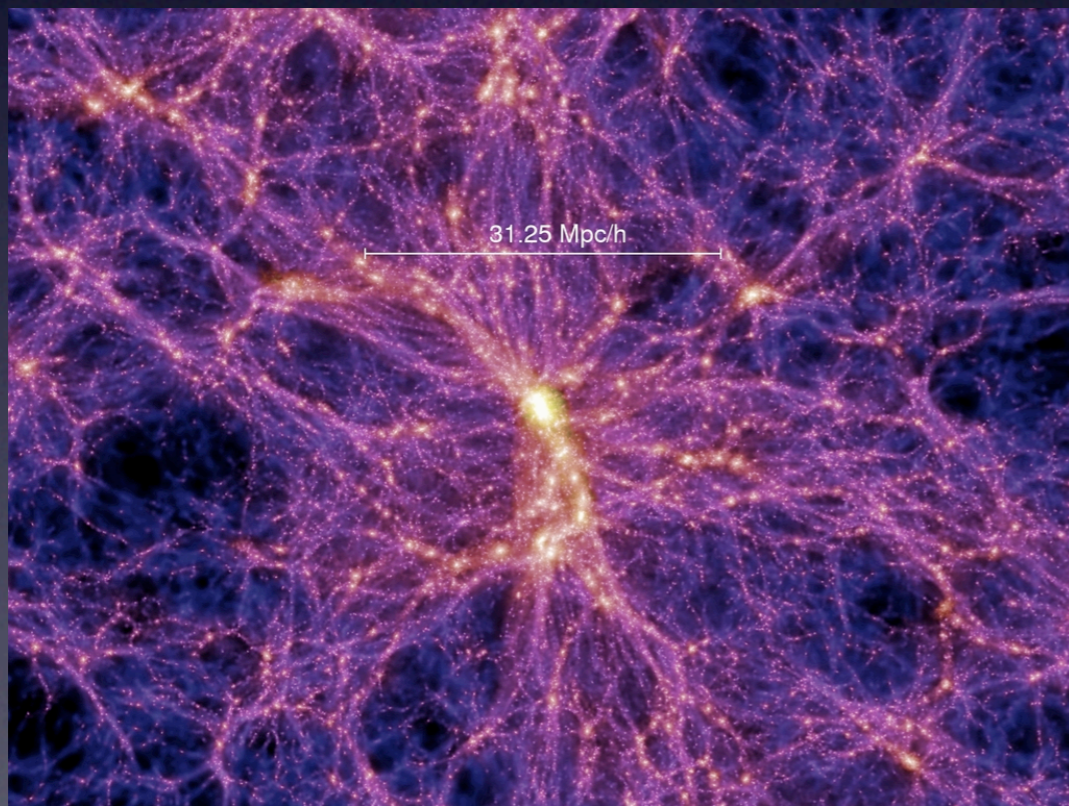
$w=-1$  to  $w=-0.8$

- 30-60% change in the predicted abundance
- only 20% change in the mass threshold

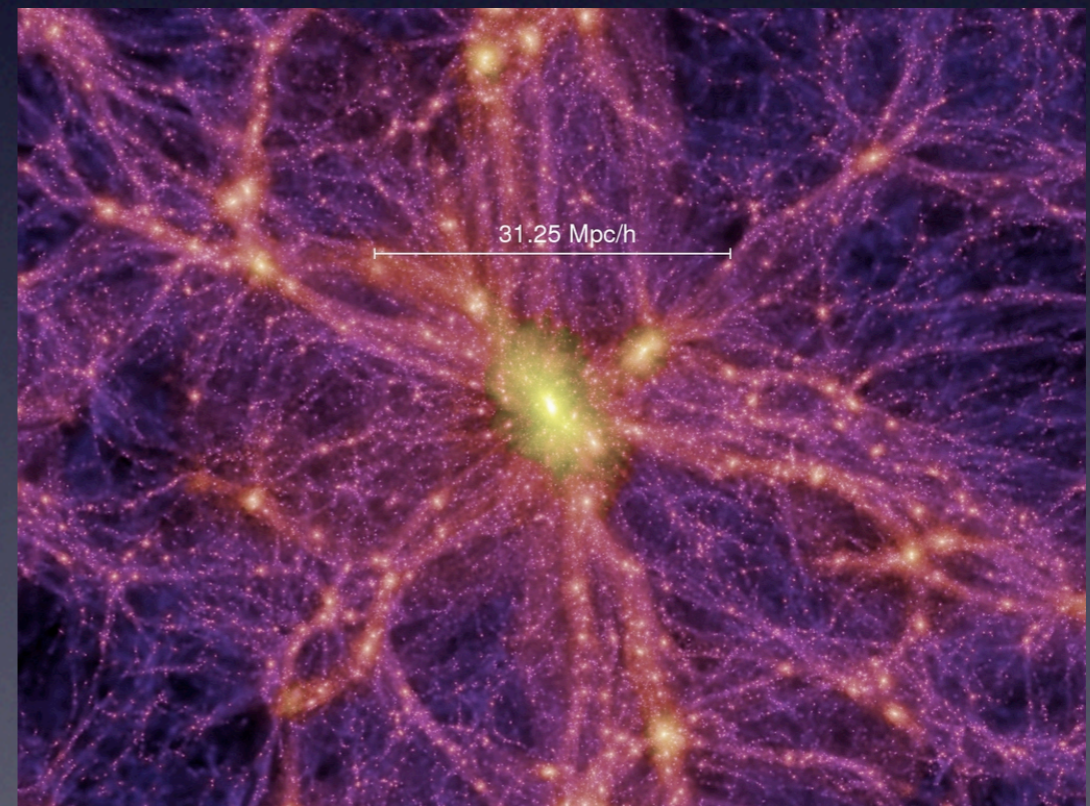


# Challenges in Mass Measurements

- Measure cluster mass indirectly
- Measurements include the cosmic web around the cluster



$z=1.4$

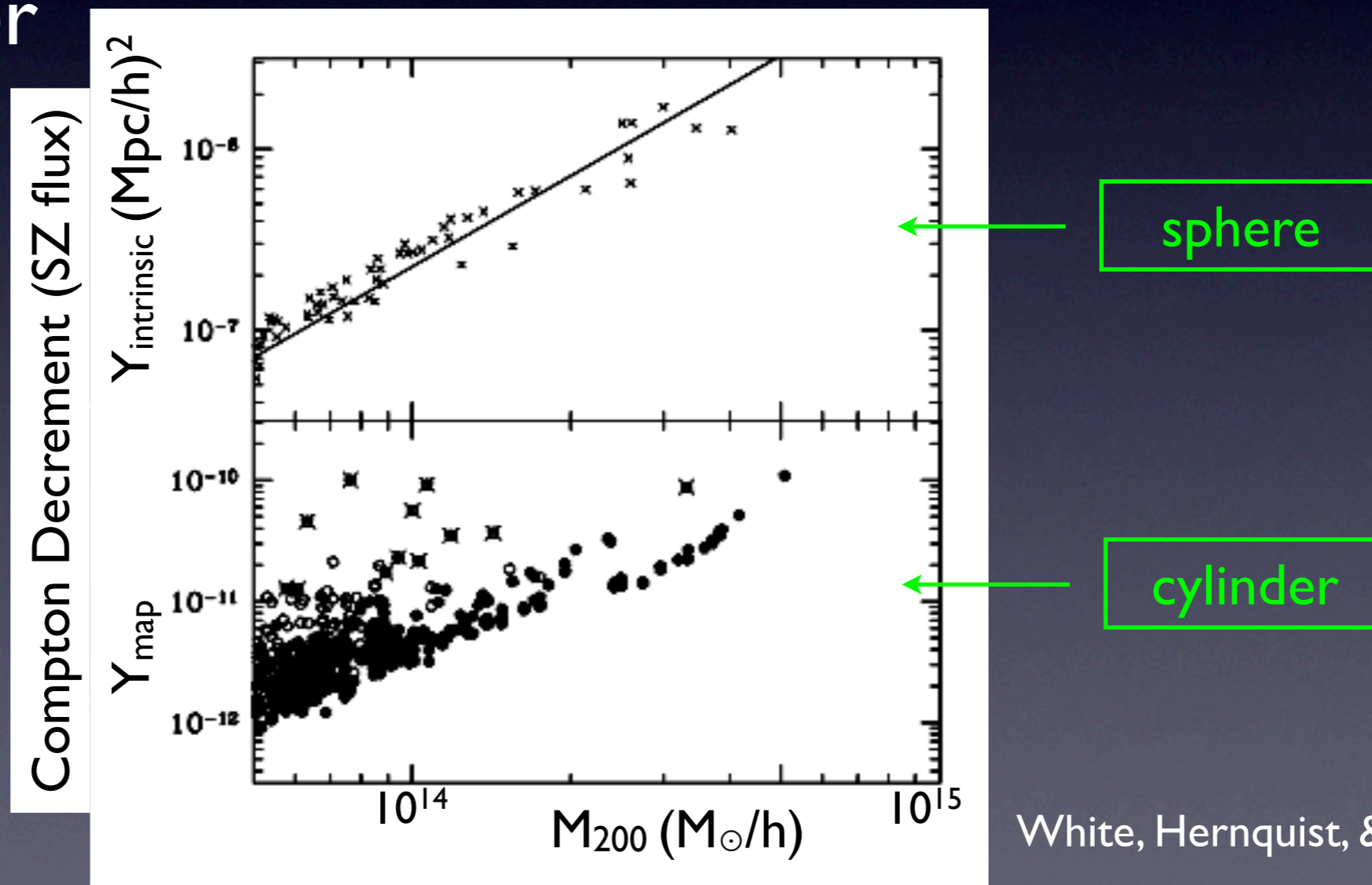


$z=0.0$

millennium simulation

# Challenges in Mass Measurements

- Measure cluster mass indirectly
- Measurements include the cosmic web around the cluster



White, Hernquist, & Springel 02

# Questions about Filaments around Galaxy Clusters

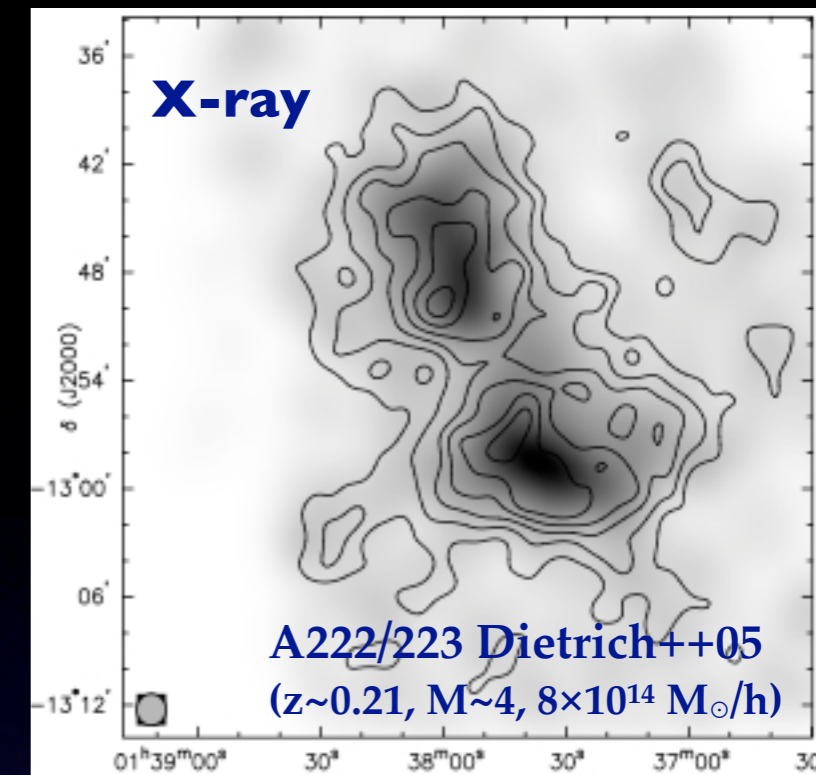
- What are the properties of filaments which surround clusters?

Extending the work of Colberg, Krughoff & Connolly 05, Aragon-calvo, Shandarin, & Szalay 10

- How do filaments affect cluster observations?

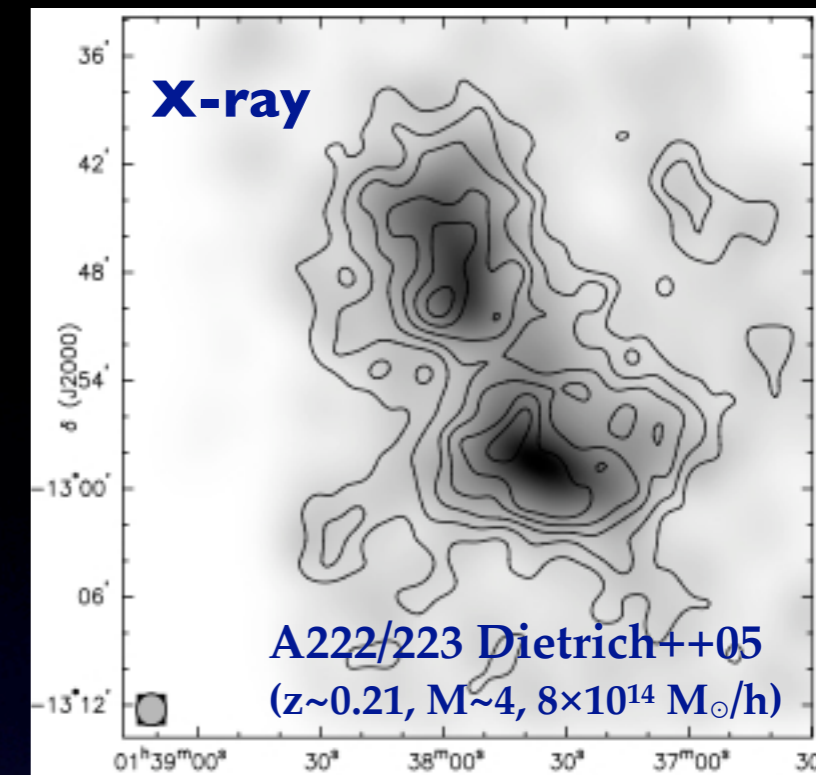


# What are Filaments? (No Unique DEFIN)



- Observations
  - Extended warm hot gas between clusters ( $T \sim 10^5 - 10^7$  K, 40% of total baryon)
  - Overdensities of galaxies, Orientations of galaxies, etc
- Filament finders
  - Halo based: e.g. Minimal spanning trees (e.g. Barrow++85)
  - Density based: e.g. Hessian of the potential or density (e.g. Hahn++07, Bond++10)

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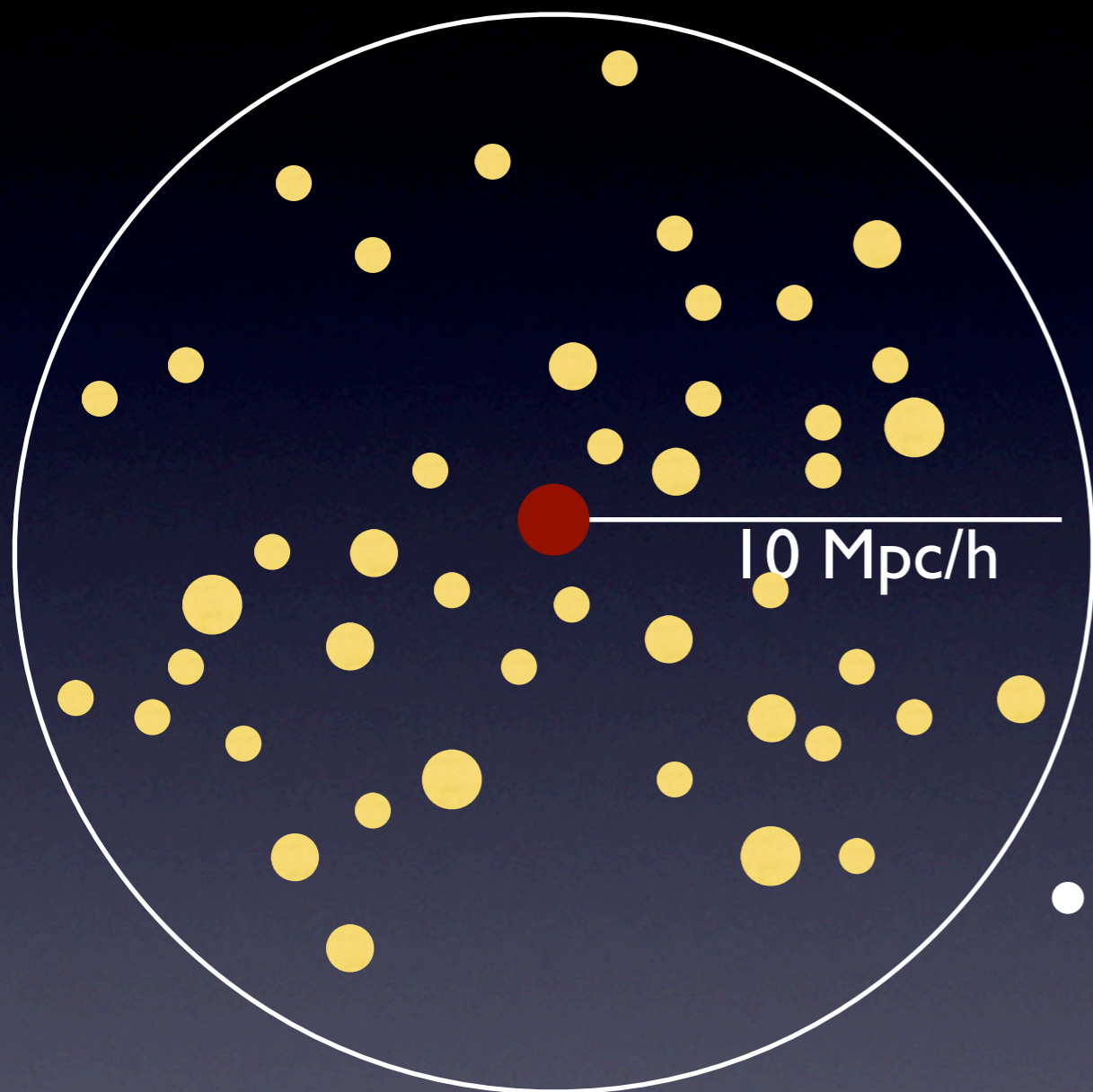


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# Simulation

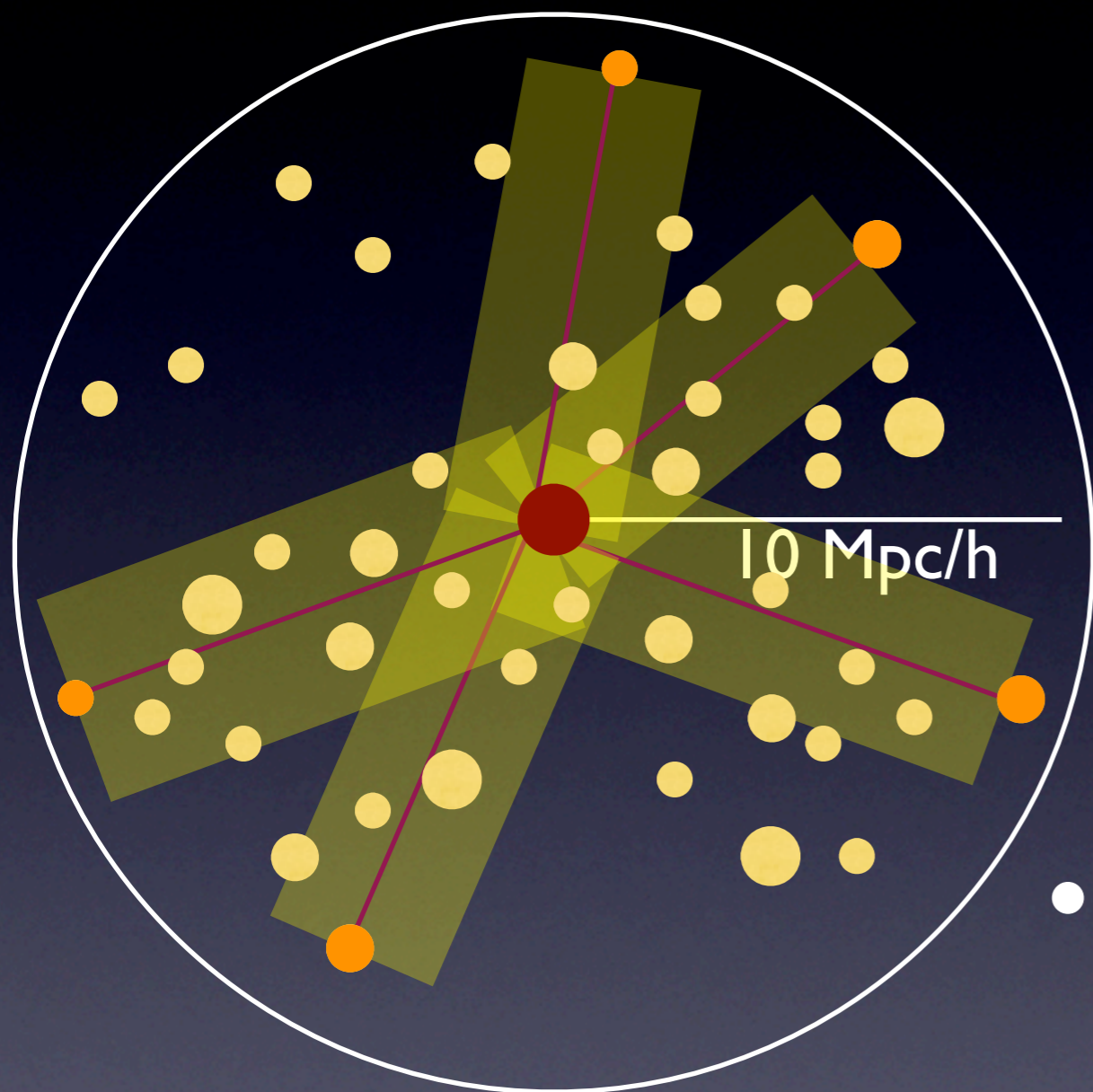
- N-body simulation (TreePM code, White 2002)
  - 250 Mpc/h box,  $2048^3$  particles
  - $\Omega_m = 0.274$ ,  $h = 0.72$ ,  $n = 0.95$ ,  $\sigma_8 = 0.8$
  - Halos via FoF with linking length  $\sim 0.168$
  - Focus here on  $z=0.1$
- Mock observations
  - Based on dark matter and subhalo distribution

# Our Method



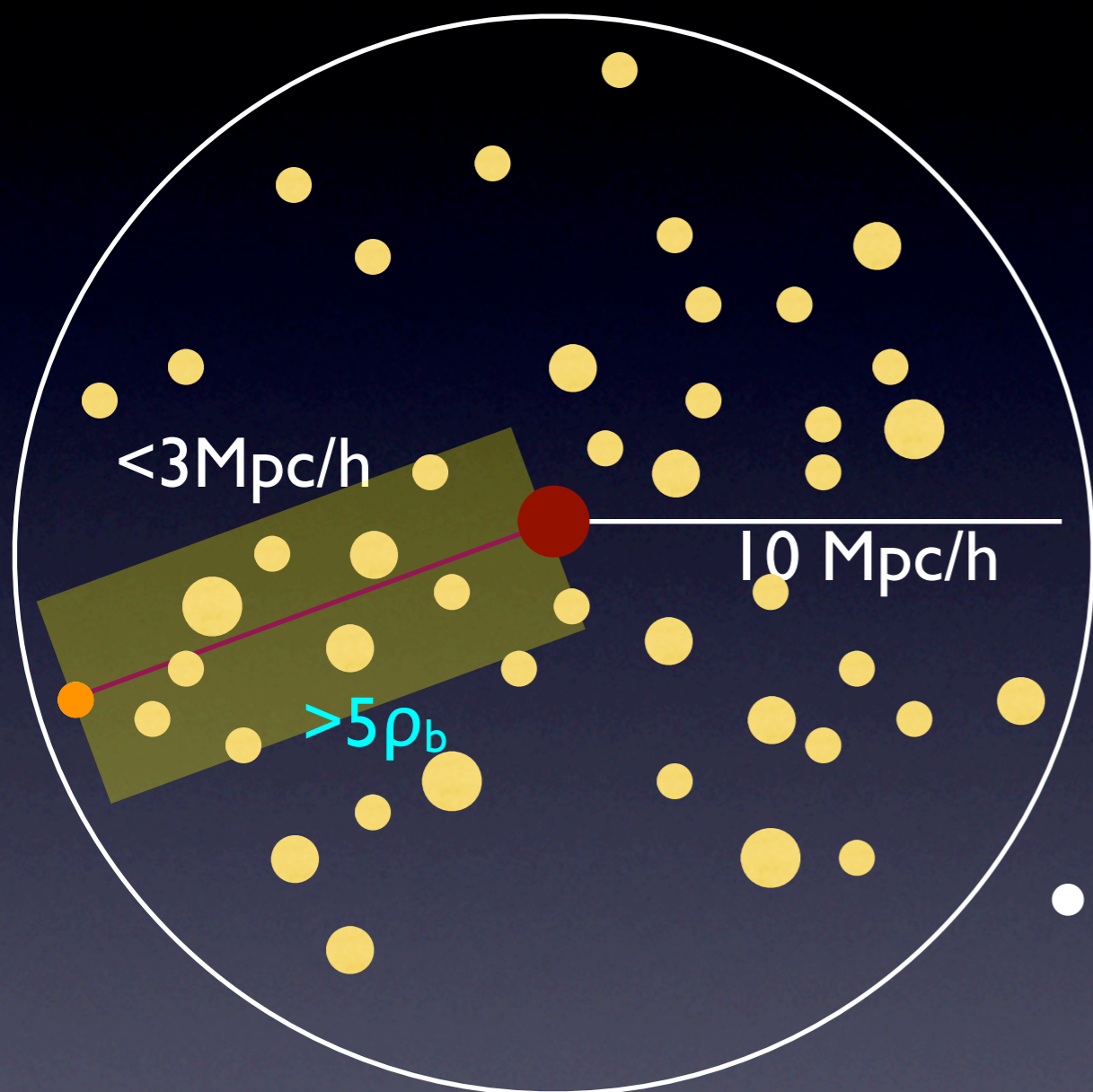
- Based on halos (Zhang et al. 2009) (min. halo mass:  $3 \times 10^{10} M_{\odot}$ )
  - Take each massive halo
  - Look at neighbors ( $< 10 \text{ Mpc}/h$ )
  - See which bridge is densest in terms of halos ( $> 5 \rho_b$ )
  - Cut at the most massive halo in filament ( $> 3 \text{ Mpc}/h$ )
- Add various refinements
  - Analogous to spherical overdensity of the cluster
  - Merge nearby filaments, etc..

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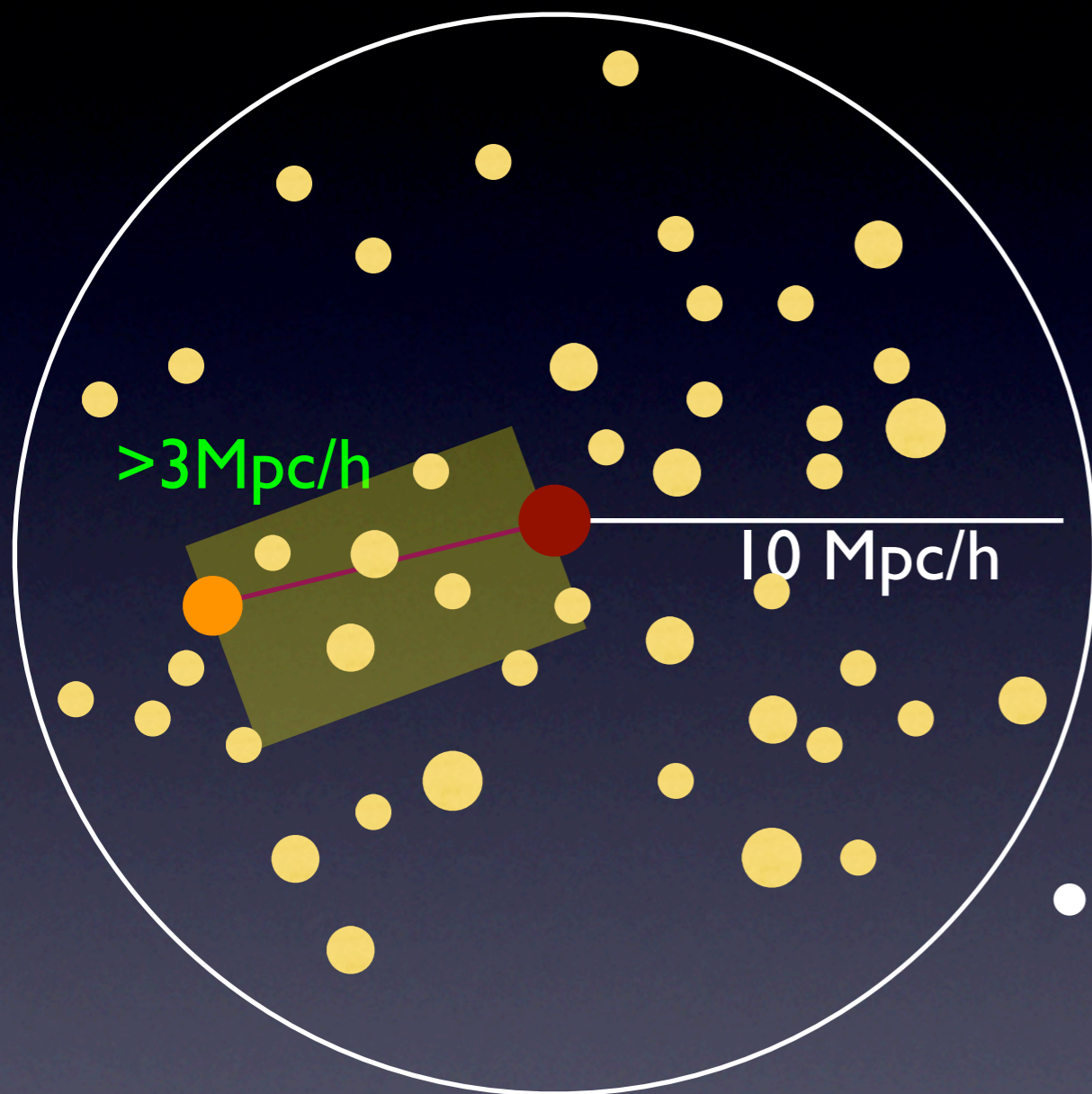
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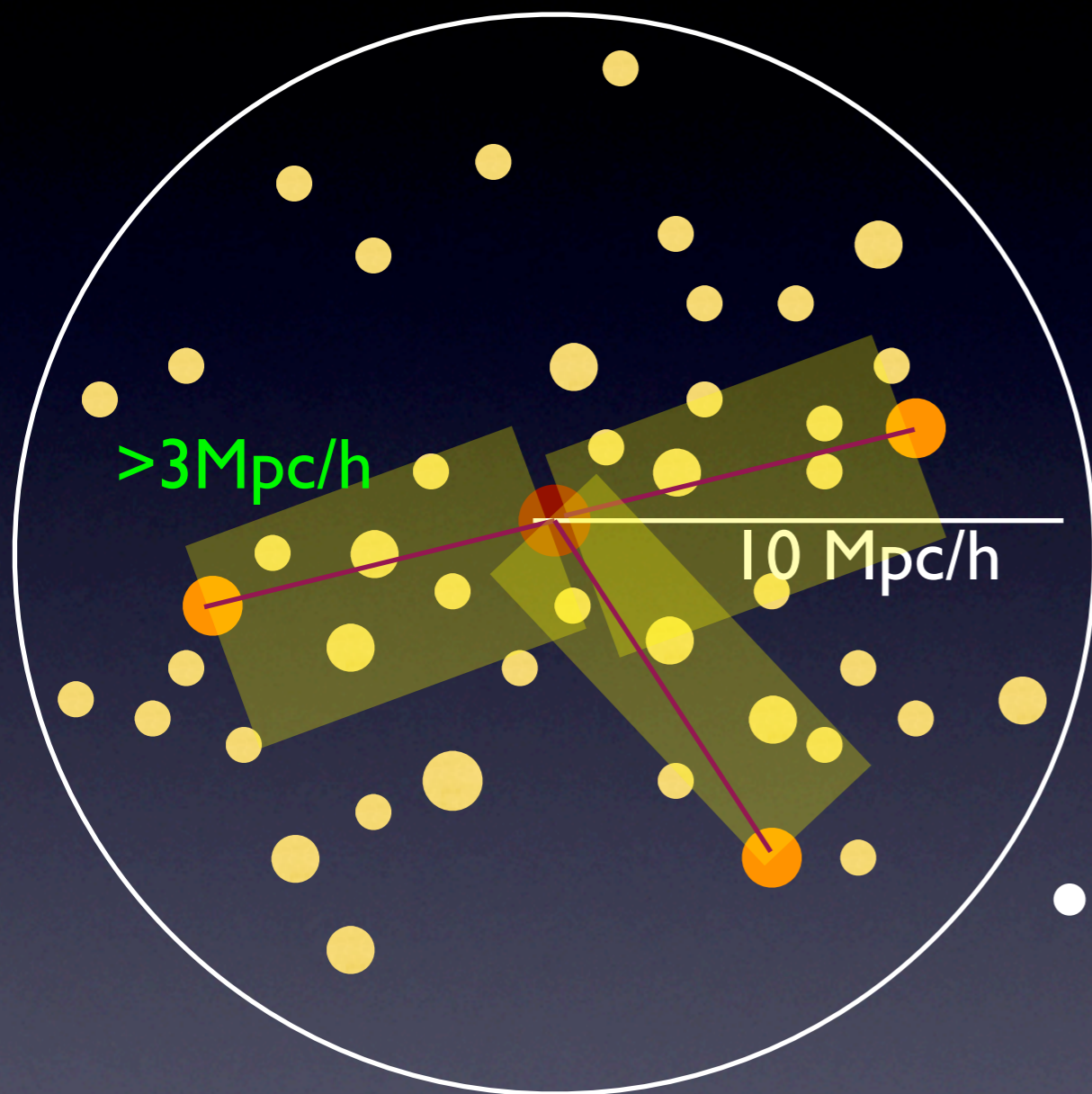
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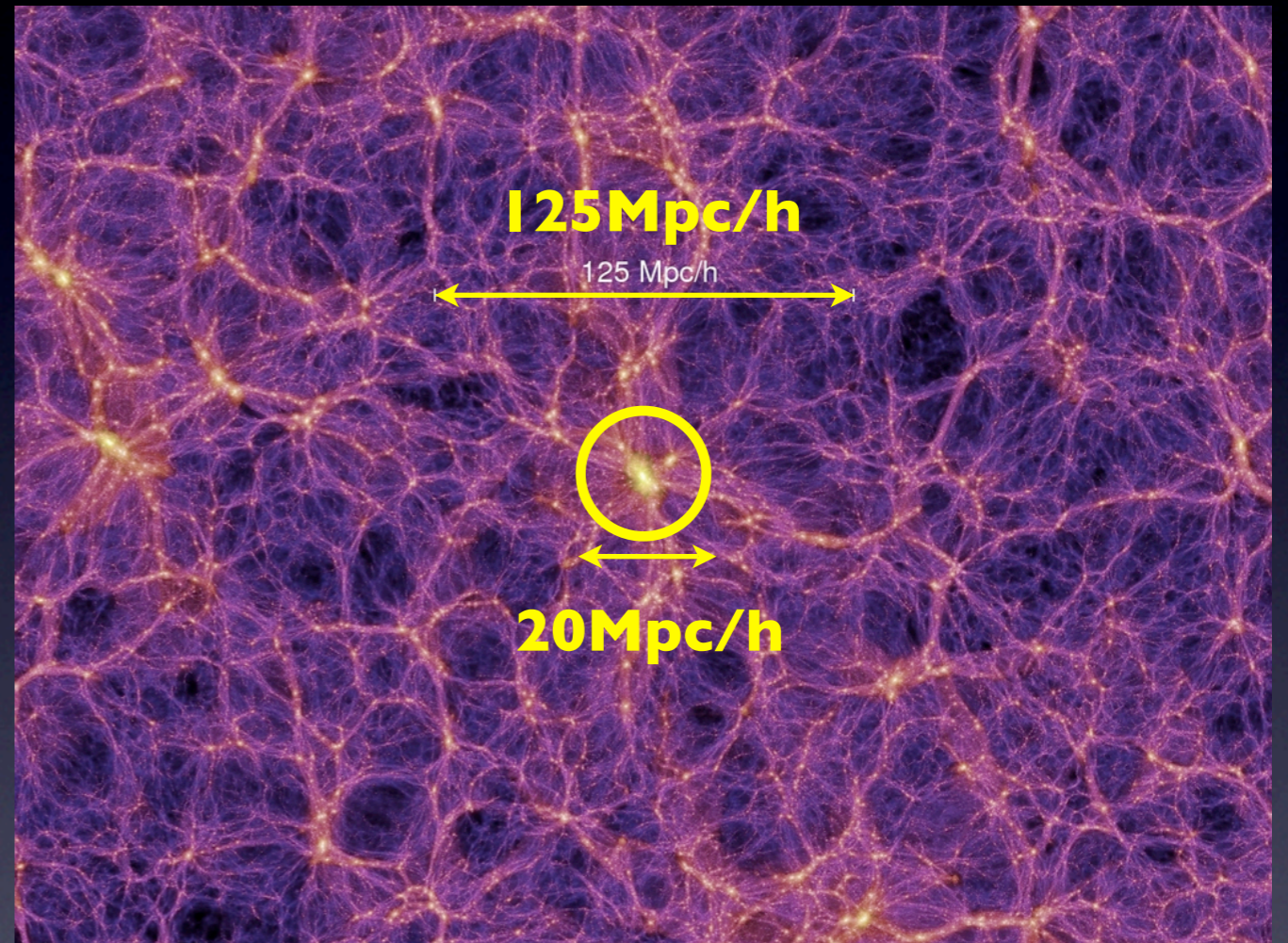


# Statistics of Total Filaments ( $z=0.1$ )

- Number of filaments in total:  $\sim 30000$
- Number of nodes:  $\sim 44000$
- Halo mass fraction in filaments:  $\sim 45\%$
- Halo number fraction in filaments:  $\sim 36\%$

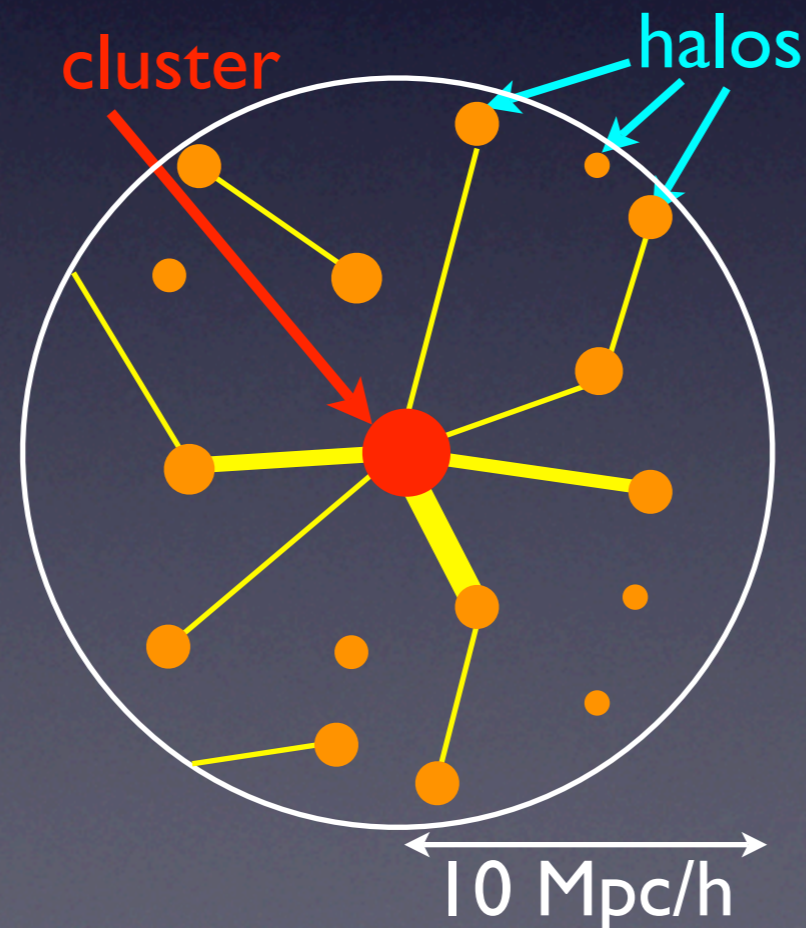
# Filaments Surrounding Clusters

- Finder restricts to **local** filamentary environment of the cluster
- Filaments may be longer (e.g. Colberg++05, Gonzalez&Padilla10)

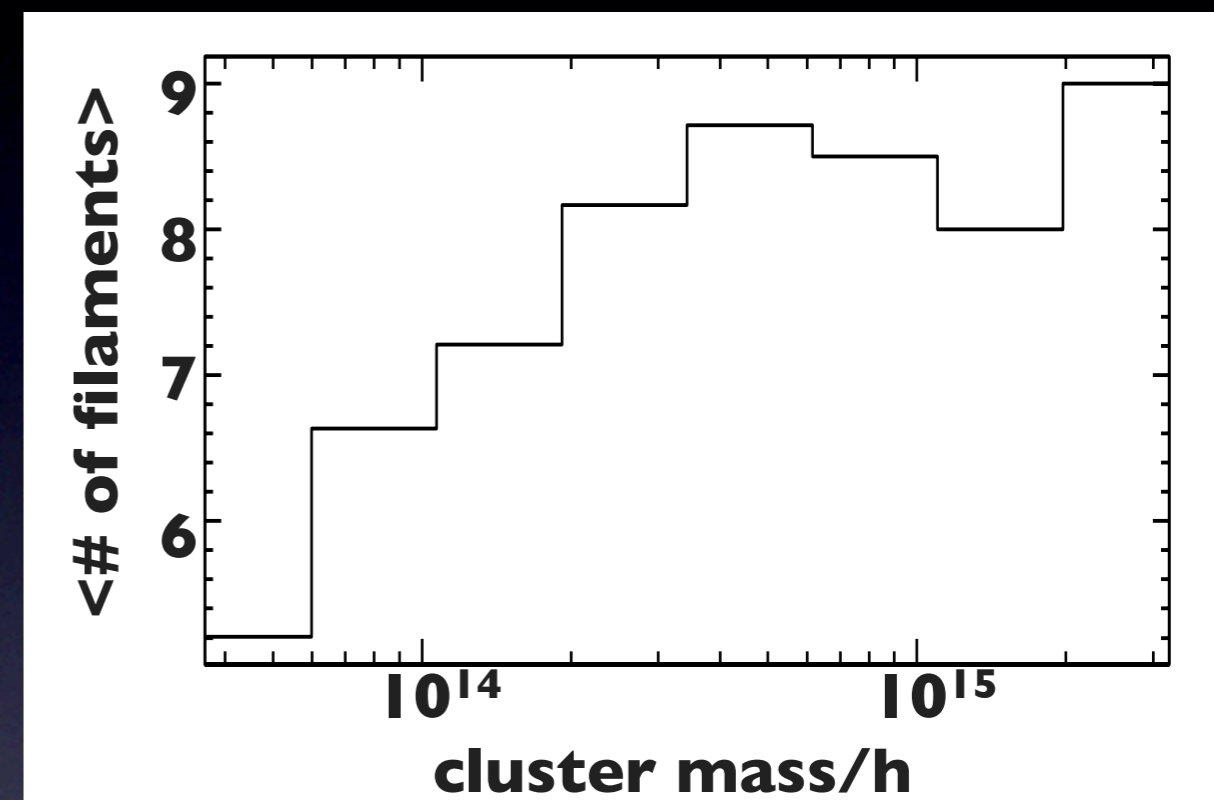
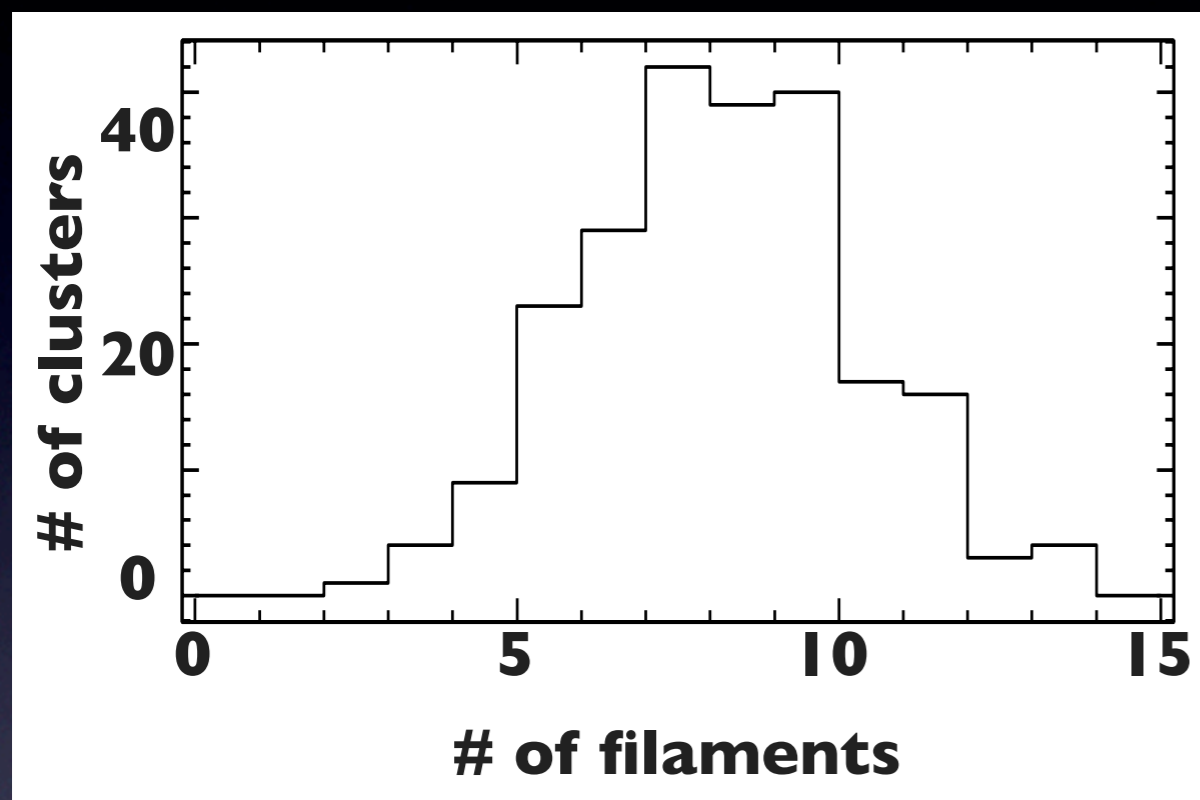


# Filaments Surrounding Clusters

- 243 Clusters ( $M_{\text{halo}} \geq 10^{14} M_{\odot}/h$ ) → 227 nodes
- 10 Mpc/h radius sphere around each cluster
- ~70% halo mass in cluster filaments



# Statistics of Cluster-Filaments



- Typical number of cluster-filaments: ~7-9
  - ~75% of cluster filament mass in the three most massive filaments

- As cluster mass increases, number of cluster-filaments increases
  - Trends agree with previous work (e.g. Colberg++05)

# Geometry

What possibilities are there for the filaments?

Schematic example for 8 filaments from a cluster



3D Isotropic



3D Anisotropic



2D Isotropic

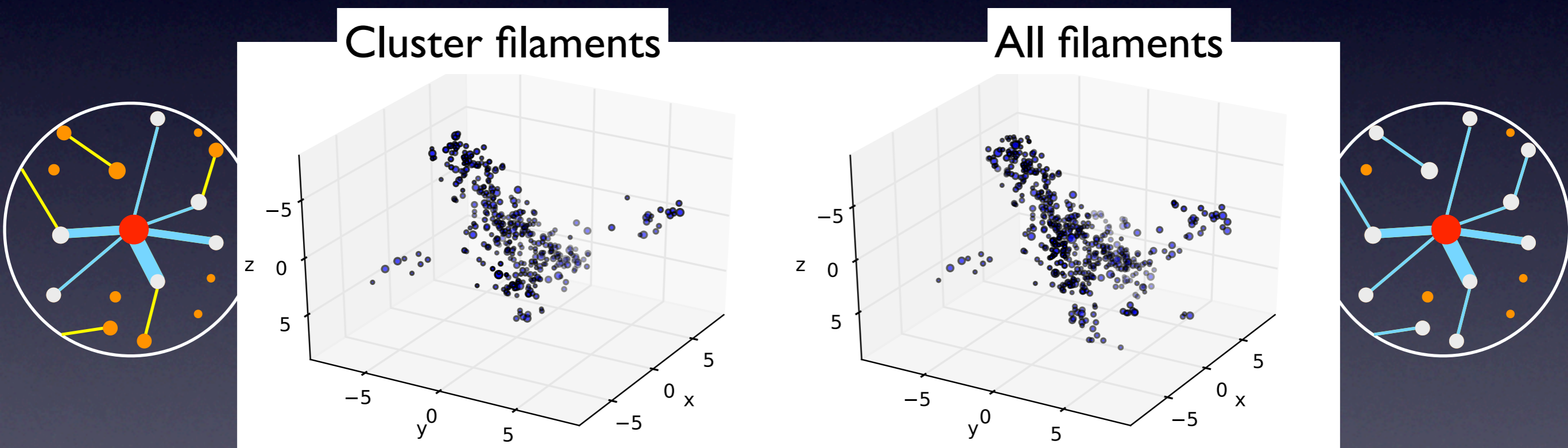
Etc...



# Filament Distribution around Clusters

Example: Filament distribution around one single cluster

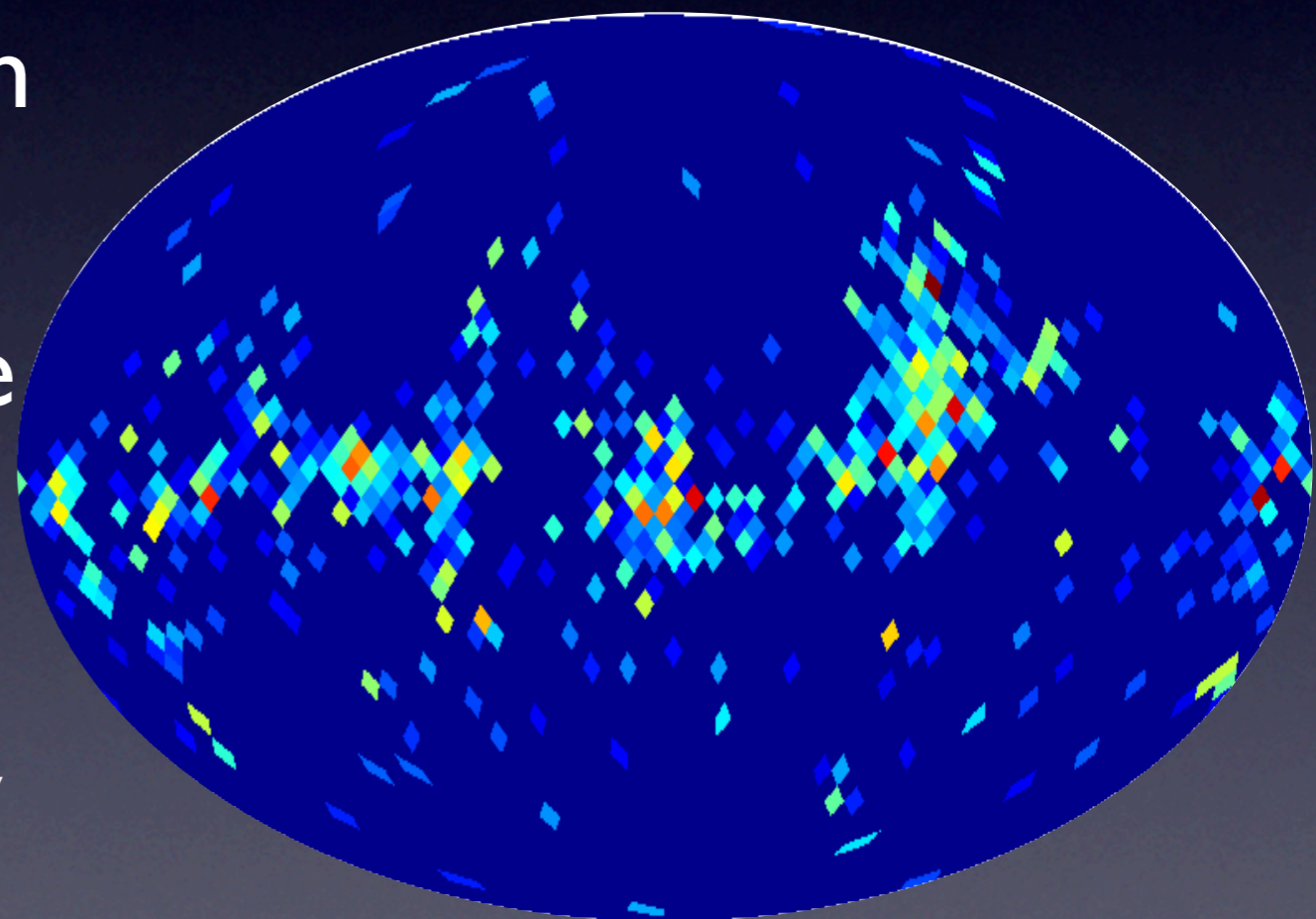
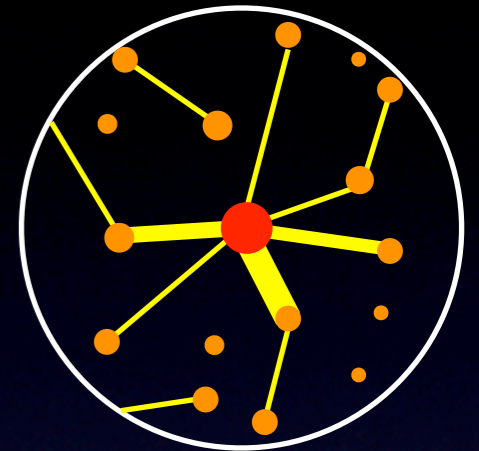
$$M_{\text{cluster}} \approx 2.7 \times 10^{14} M_{\odot}/h$$



- By eye, filament distribution tends to be **planar**

# Solid Angle Subtended by Filaments

- **Project** all the halos in all the filaments in  $10\text{Mpc}/h$  sphere
- Calculate the solid angle subtended by those halos in filaments
  - About 10-30% of the sky is covered



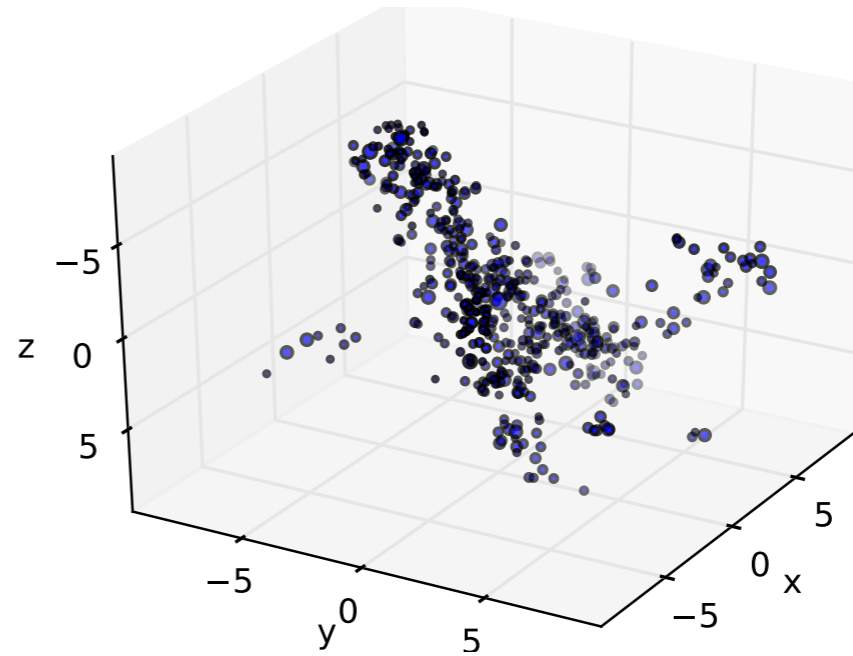
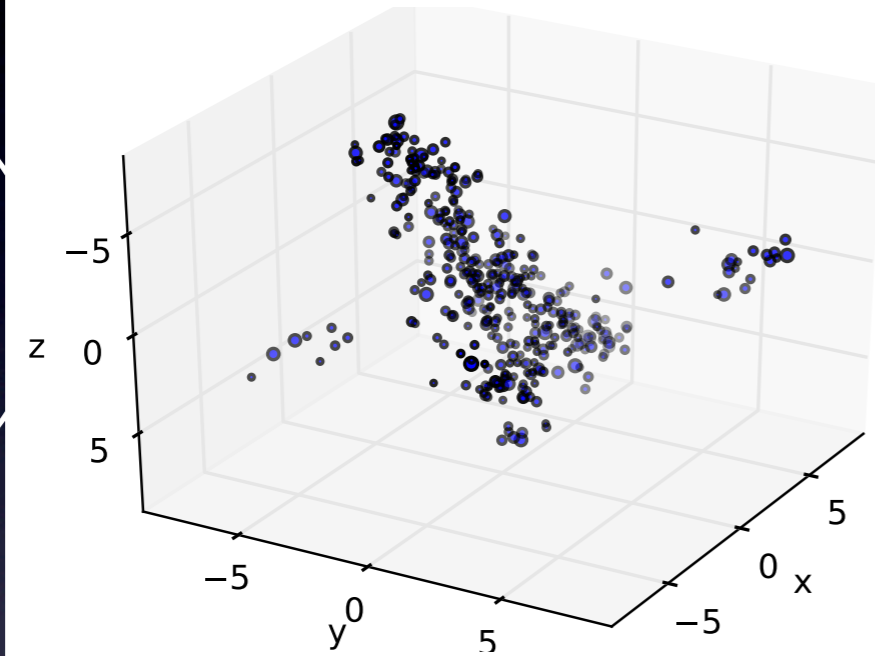

 $M_{\text{node}} \sim 5 \times 10^{14} M_{\text{sun}}$

# Spatial Distribution around Clusters

$$M_{\text{cluster}} \approx 2.7 \times 10^{14} M_{\odot}/h$$

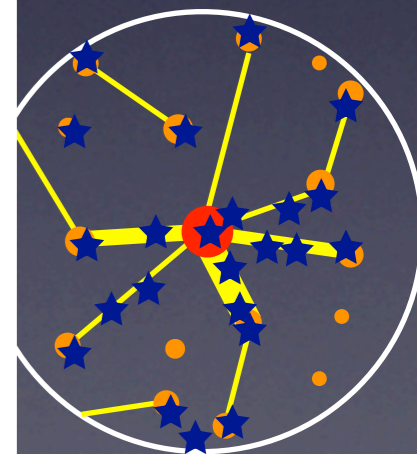
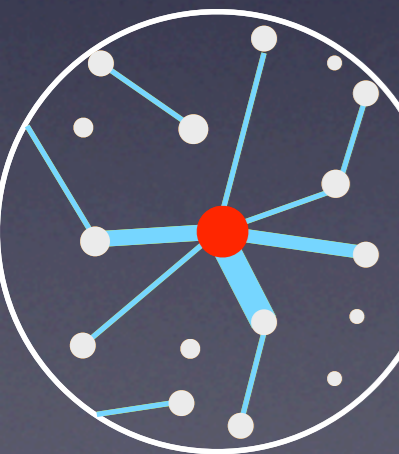
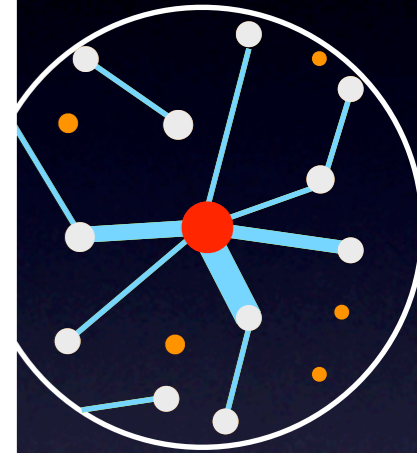
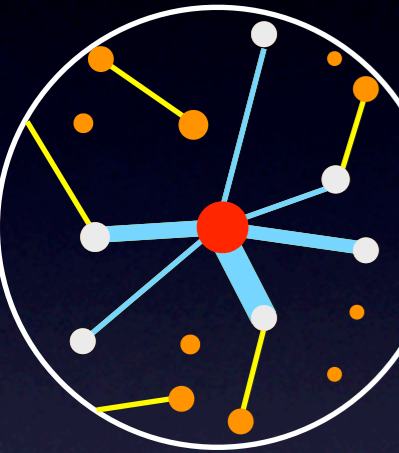
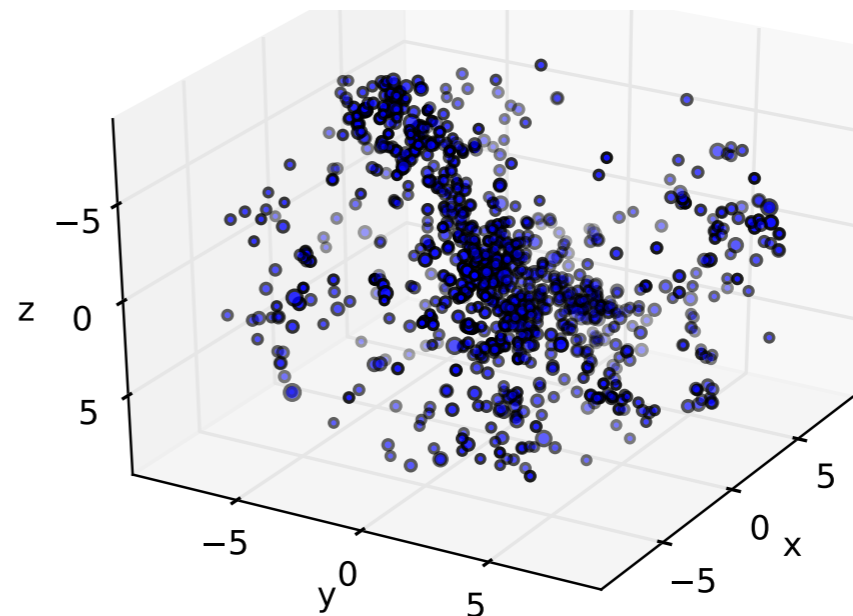
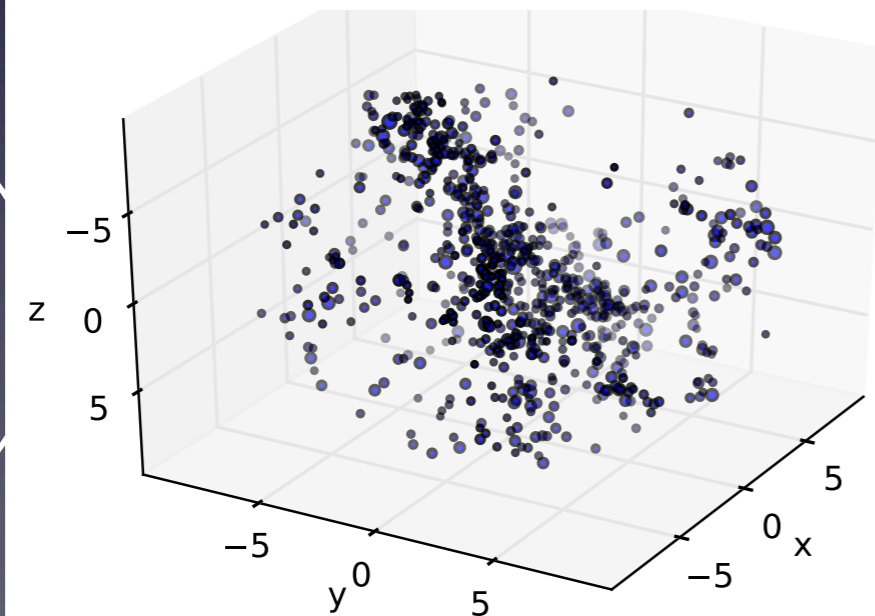
Cluster filaments

All filaments



Total Halo Mass

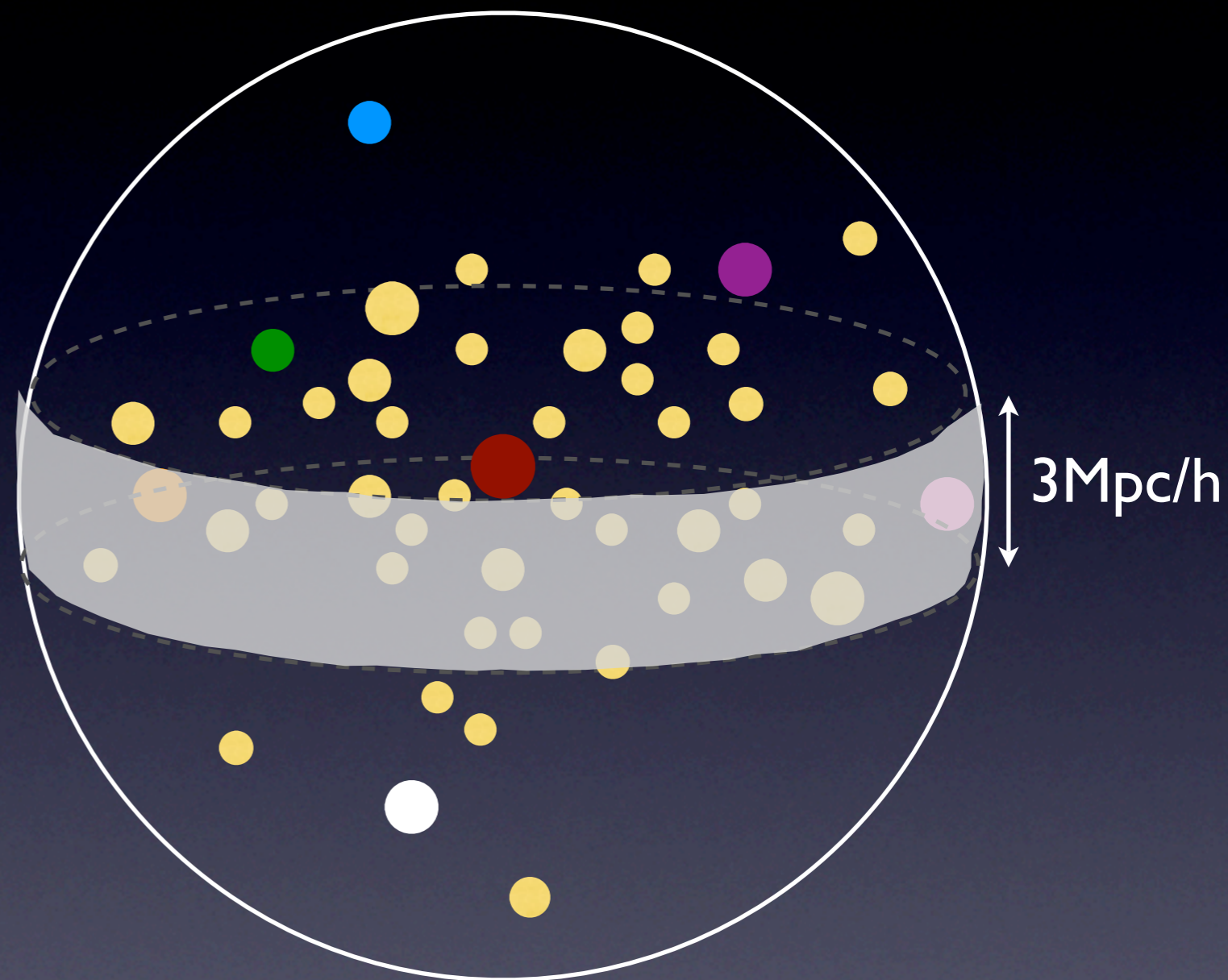
Galaxy Richness





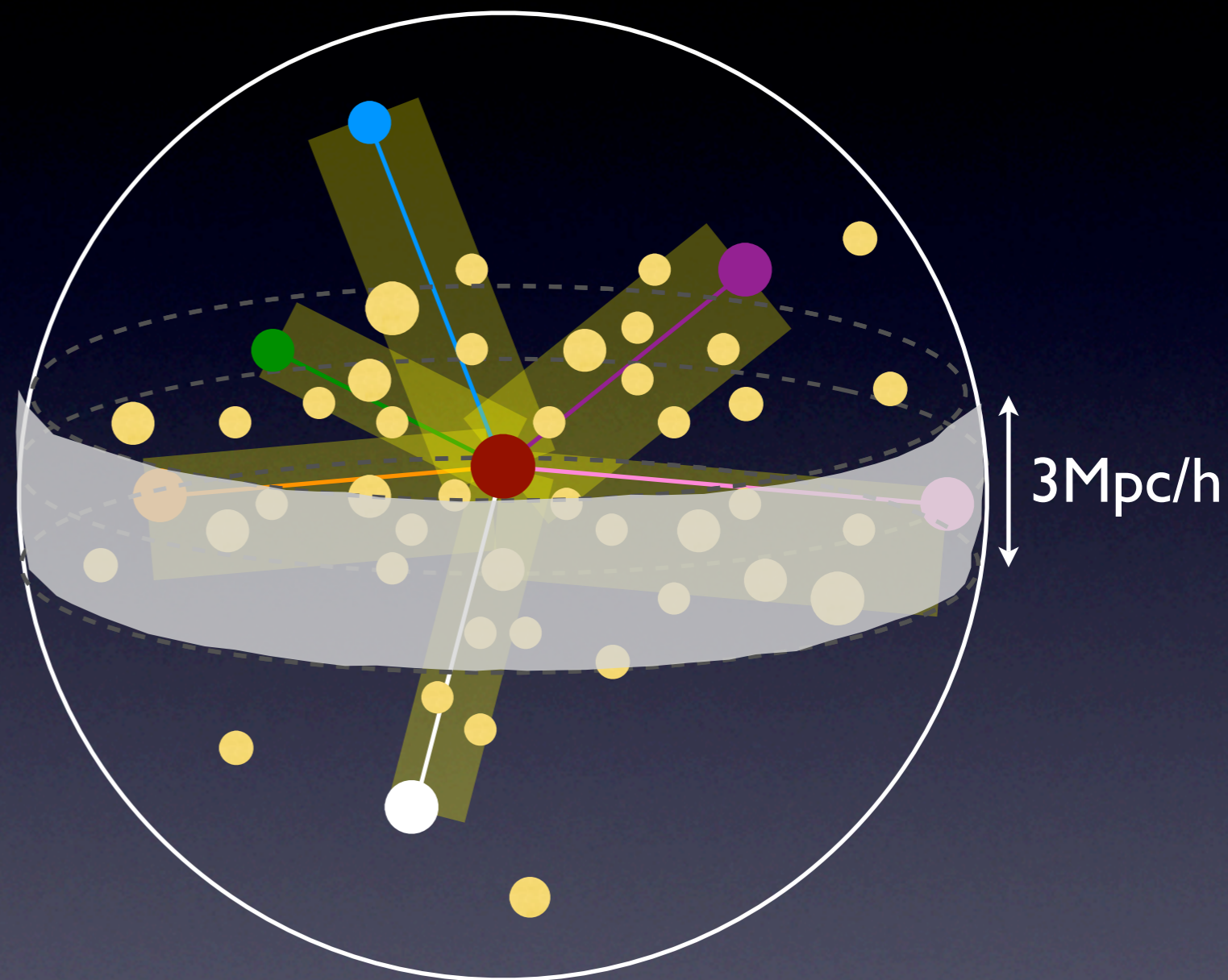
# Defining Planes

- “Plane”:
- Disk with 10 Mpc/h radius, 3 Mpc/h thick
- Orientation:
  - Contain max. mass
  - Cluster-Filaments
    - : Pairs of filaments
  - Other tracers
    - : Random directions



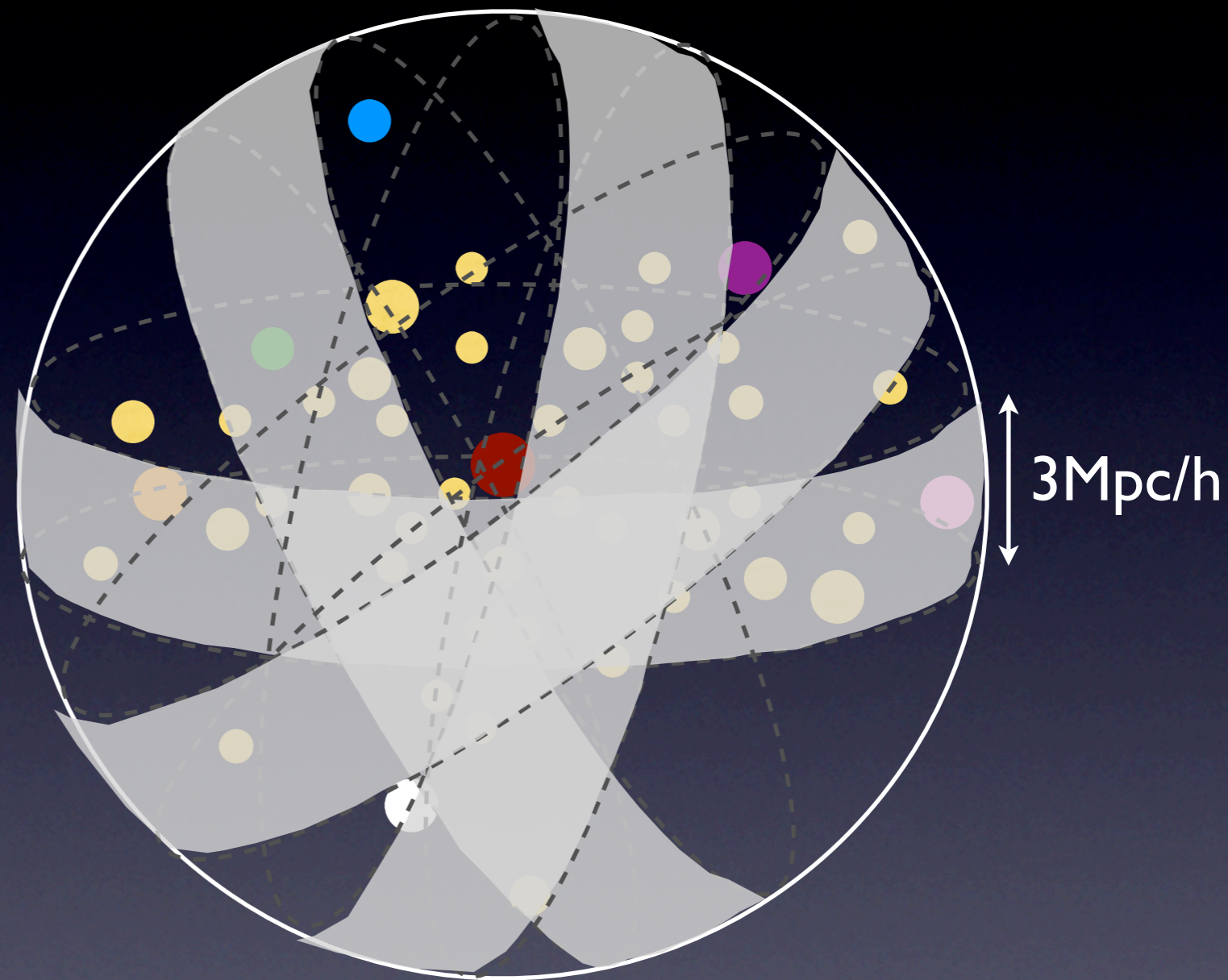
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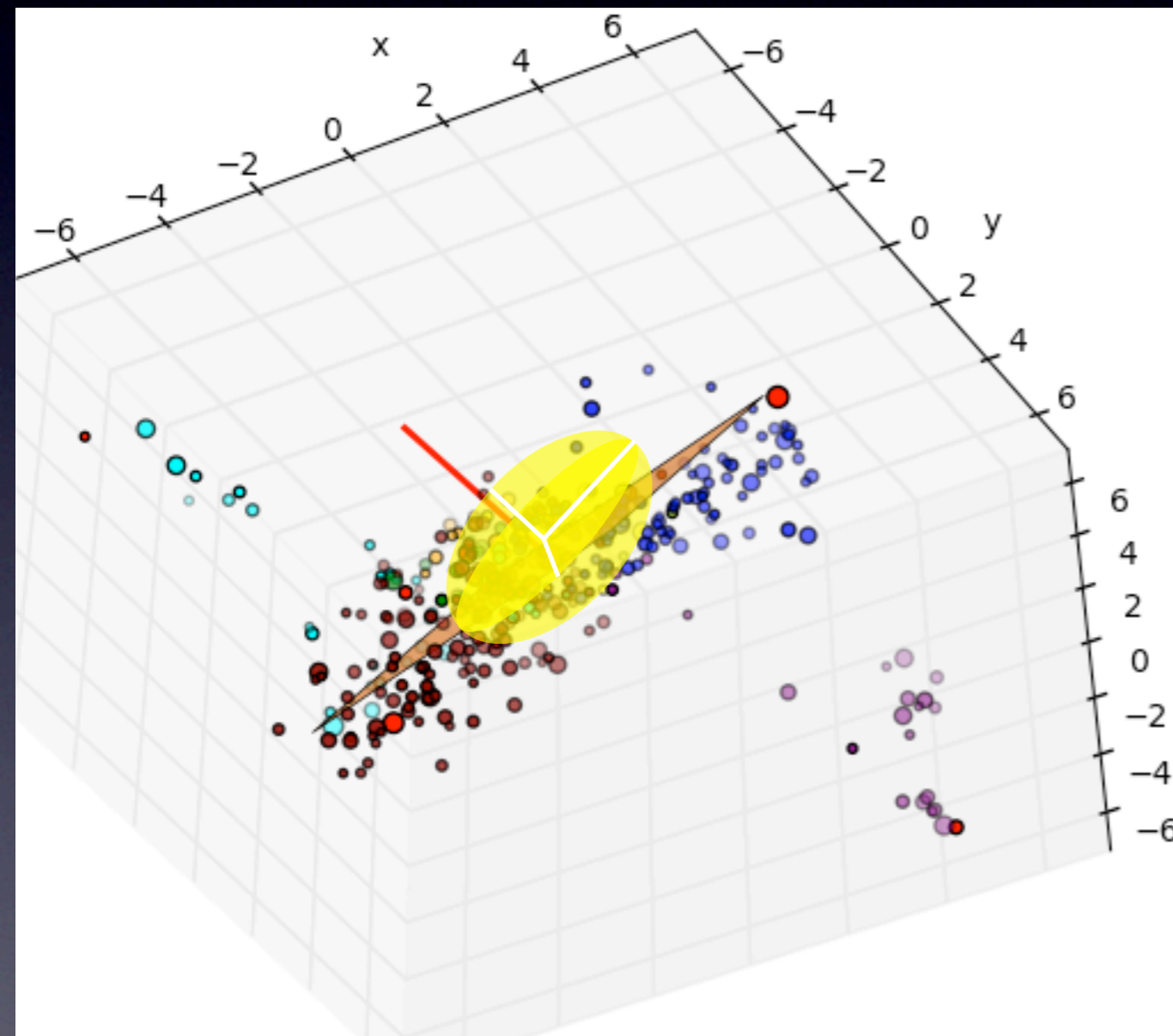


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# Planar Geometry around Clusters



- **~60-80%** of mass or richness in “planes”
- Planes from different tracers tend to be aligned
- Cluster major axis tends to lie in plane
- **Normal to the plane** is a special direction

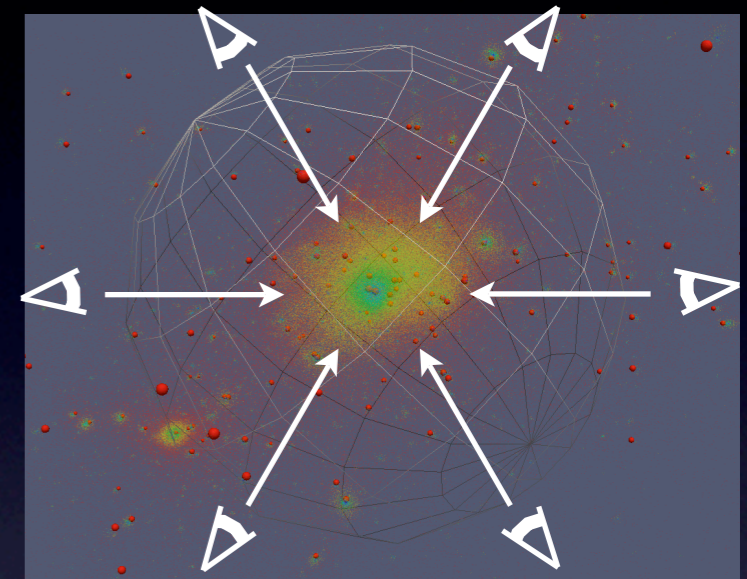
# Cluster Observables with Planar Environment

Are there correlations between the direction of the plane and the scatter in cluster mass measurements?

# Mass measurements in simulation

For more detail, see White, Cohn, & Smit 10

- Mass along 96 different lines of sight
- Mass measurements via
  - Richness
    - $N_{\text{red}}$ : Red galaxies, Max BCG, colors using Skibba & Sheth 09
    - $N_{\text{phase}}$ : All galaxies, cluster membership using Yang, Mo, & van den Bosch 08 (phase space)
  - Velocity dispersions ( $V_{3\sigma}$ ,  $V_{\text{phase}}$ ): dynamics of galaxies
  - SZ flux: based on the mass of halos, cylinder,  $r_{180b}$
  - Weak lensing: SIS or NFW profile, cylinder,  $r_{180b}$



# Planar Environment vs. Observables

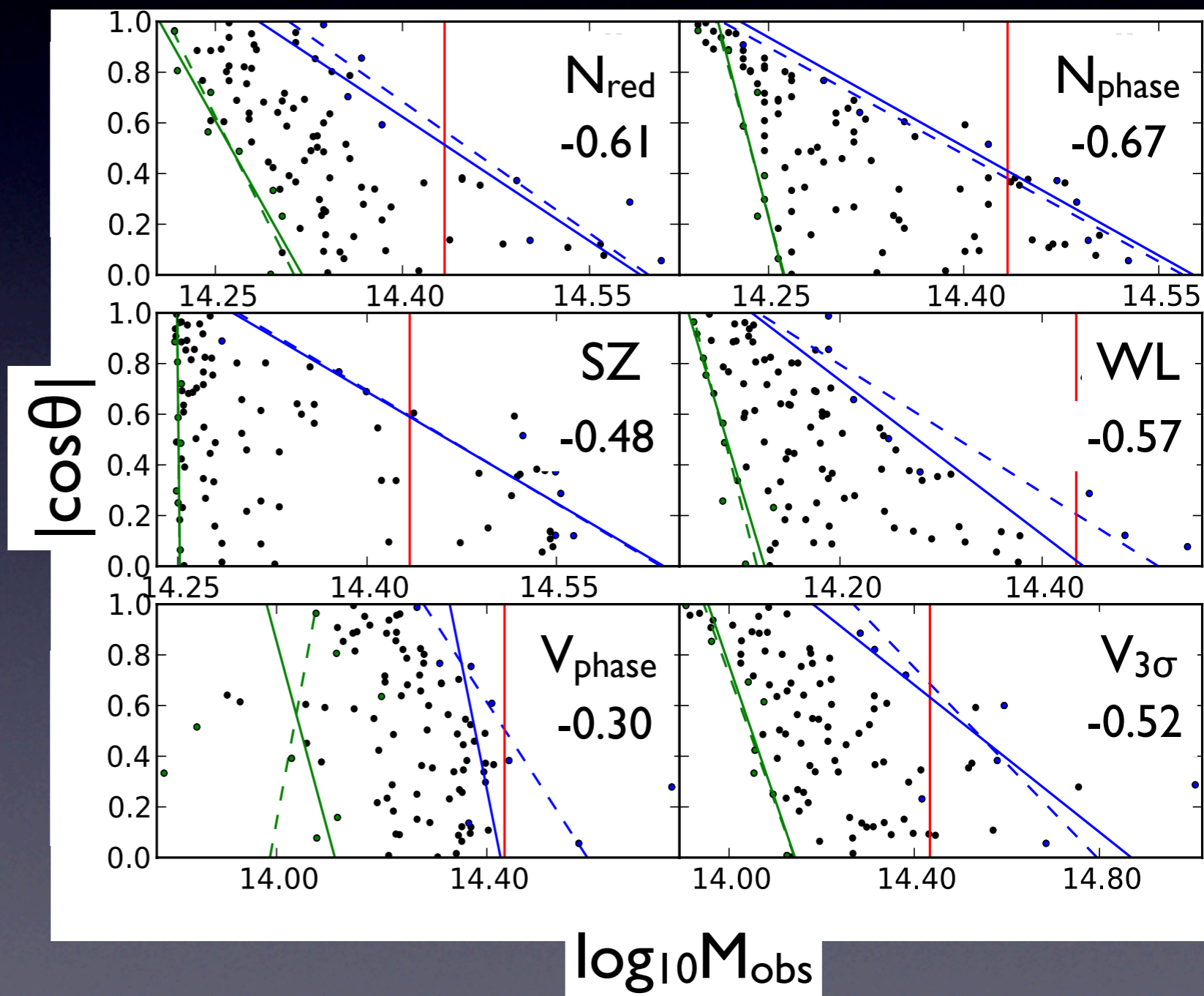
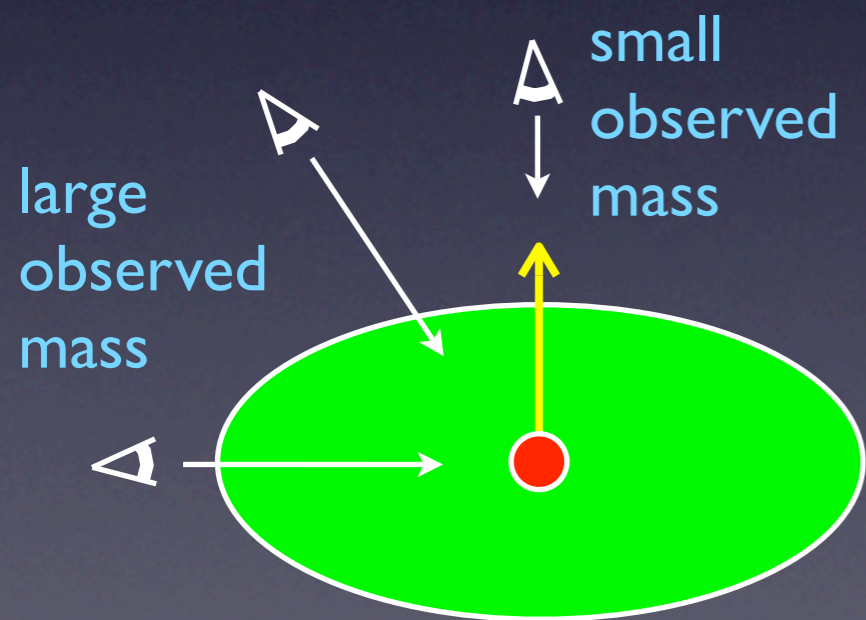
- Consider the angle of normal to plane with the line of sight for cluster observation



# Example of correlation around one cluster

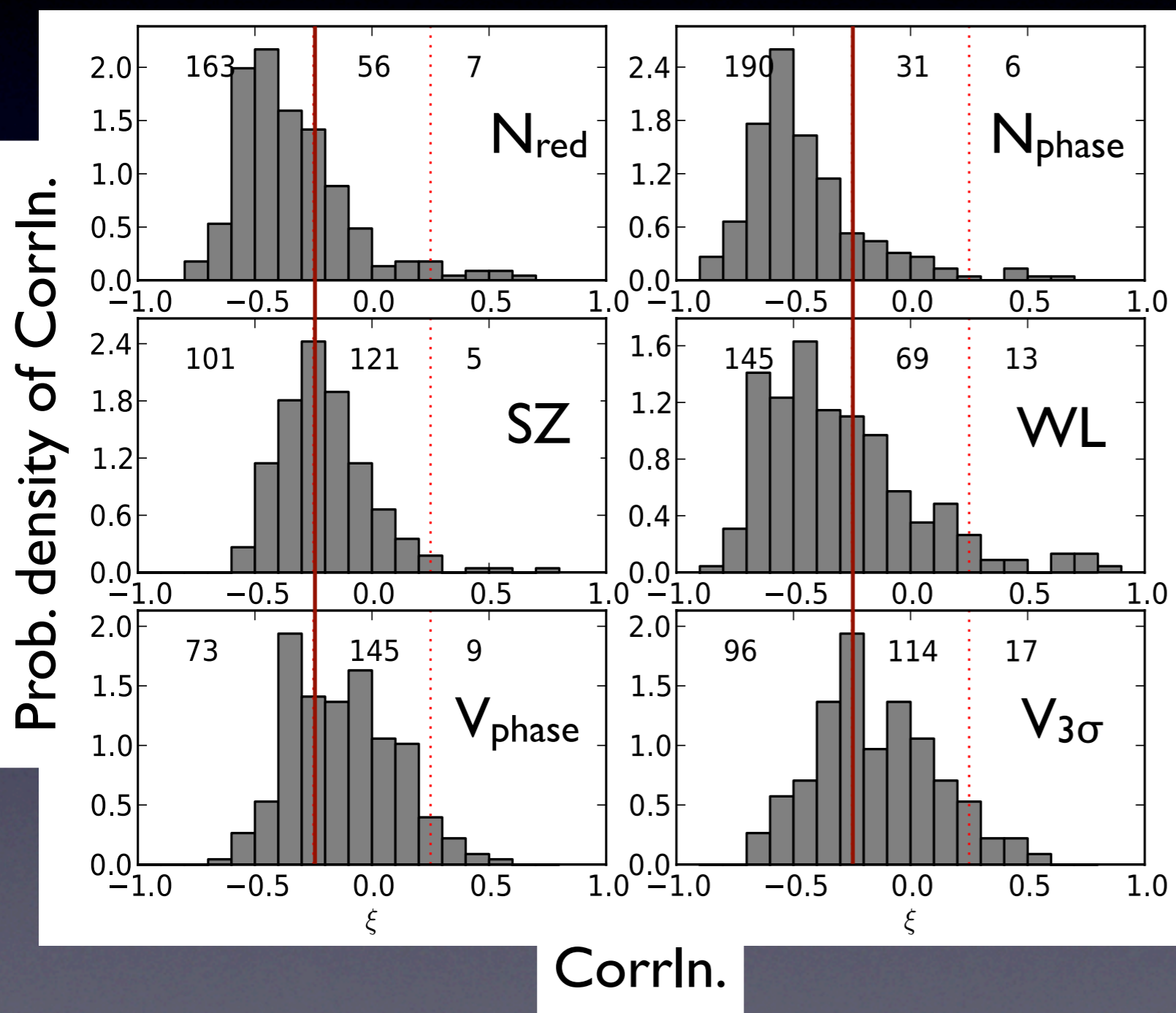
$$M_{\text{cluster}} = 2.7 \times 10^{14} M_{\odot}/h$$

Correlation between  
angle with plane and  
observational scatter



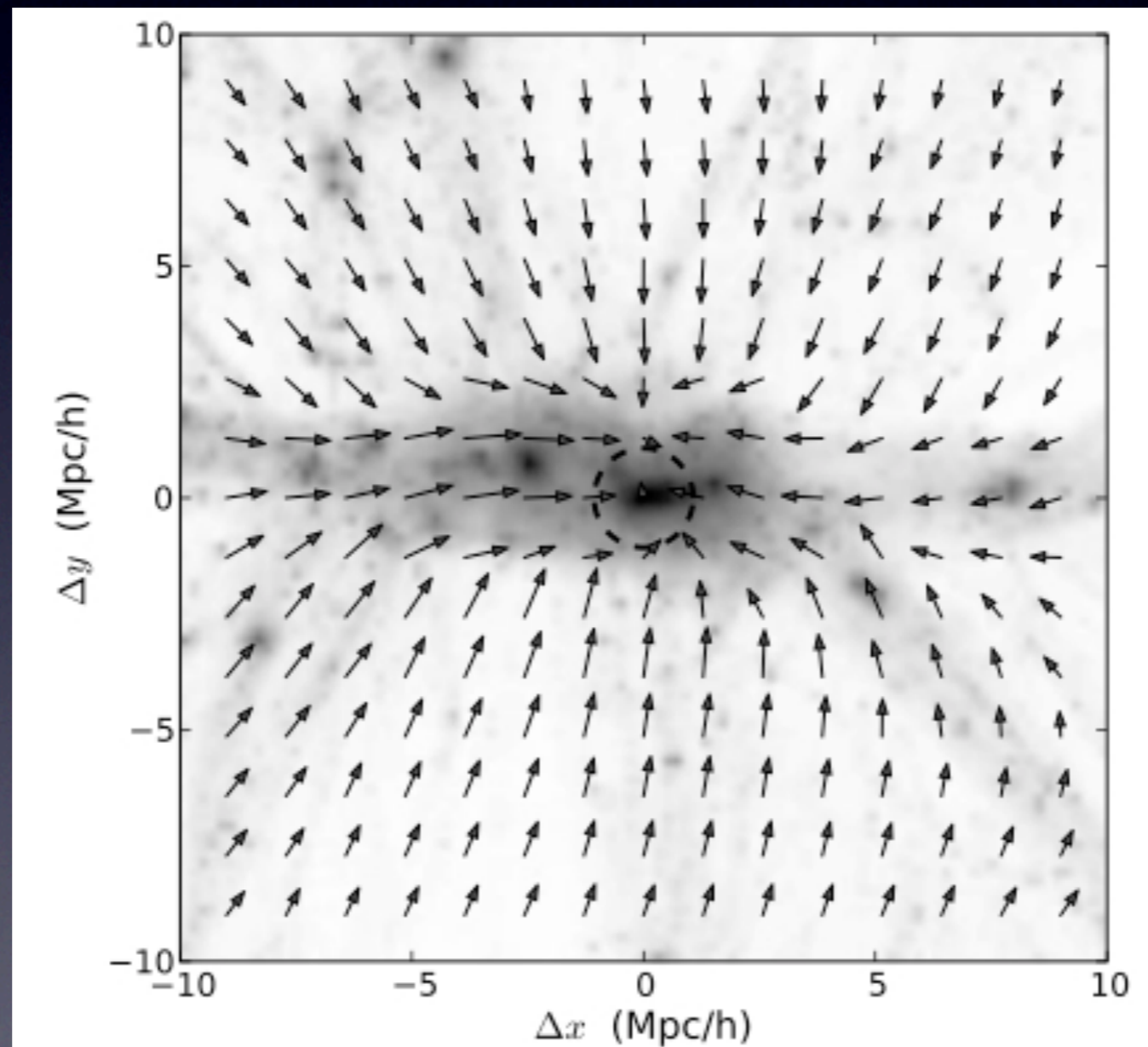


# Correlation coefficient distribution for all clusters



- Significant correlation ( $< -0.25$ ) for many clusters
- Corrn. depends on the type of measurement

Scatter in a given mass measurement is correlated with the filamentary environment (via projection effects)

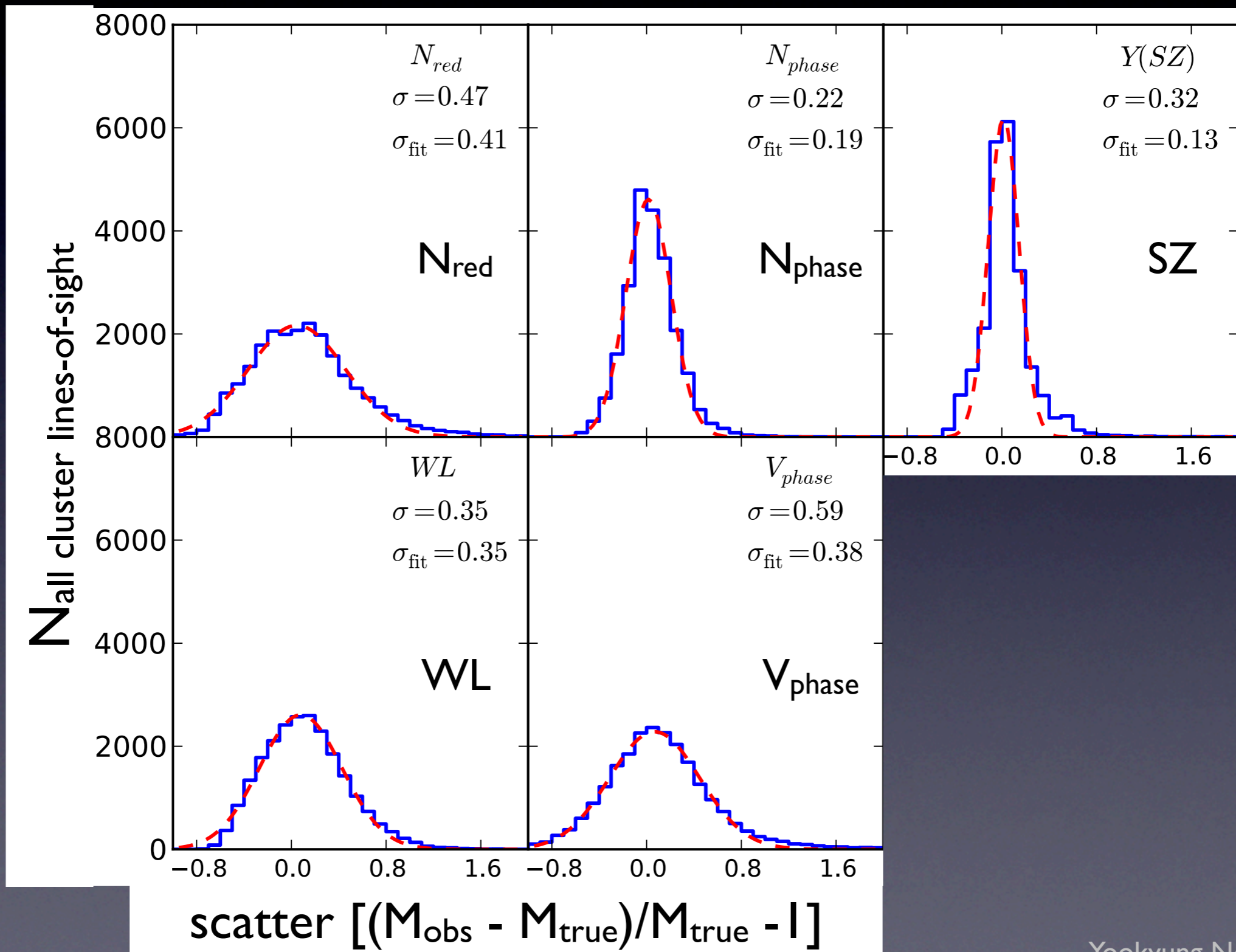


White, Cohn & Smit I I

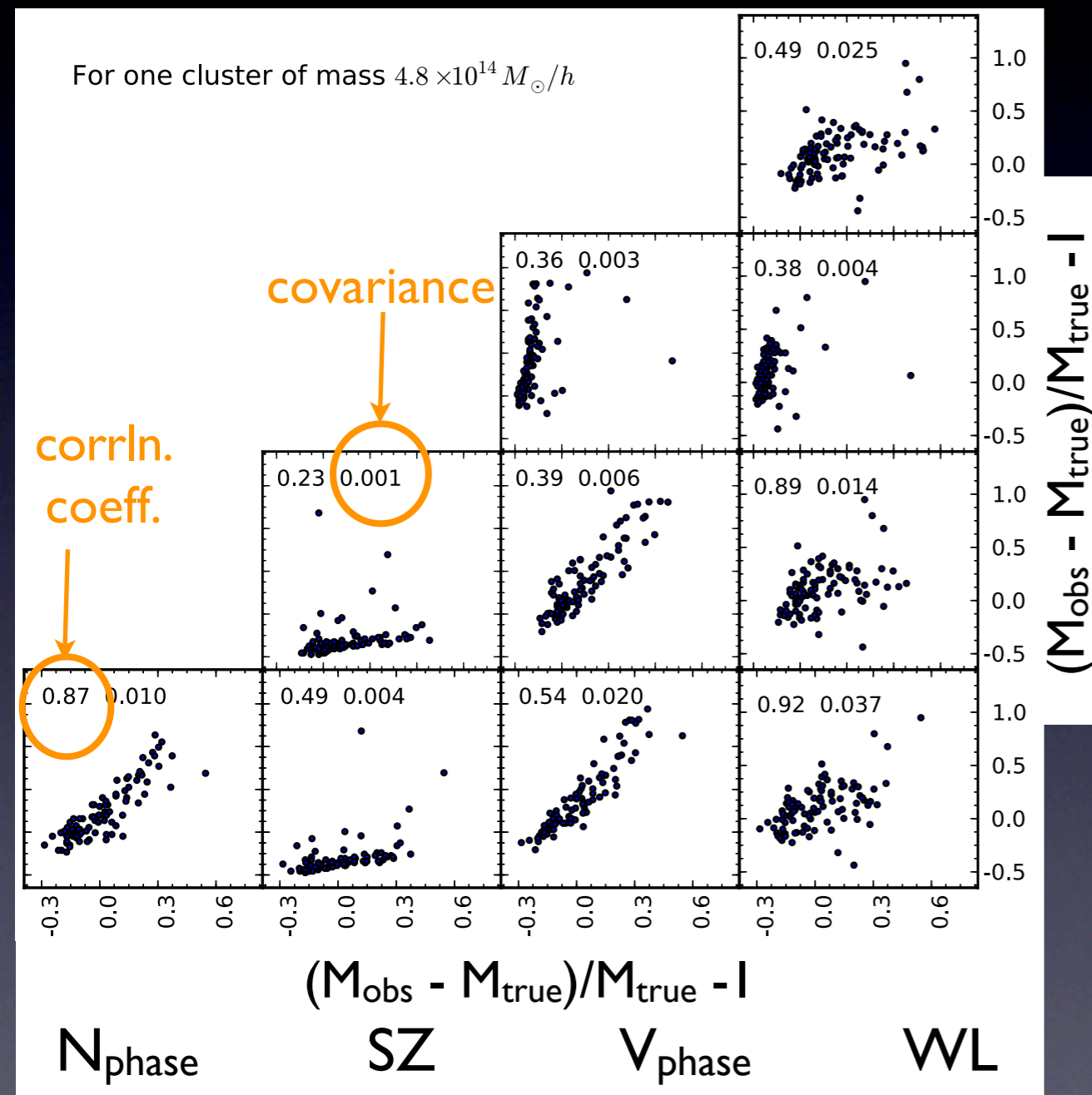
Yookyung Noh (UC Berkeley)

- Are the scatters in different cluster mass measurements correlated with each other?
- What are physical origins of the scatters of cluster mass measurements?

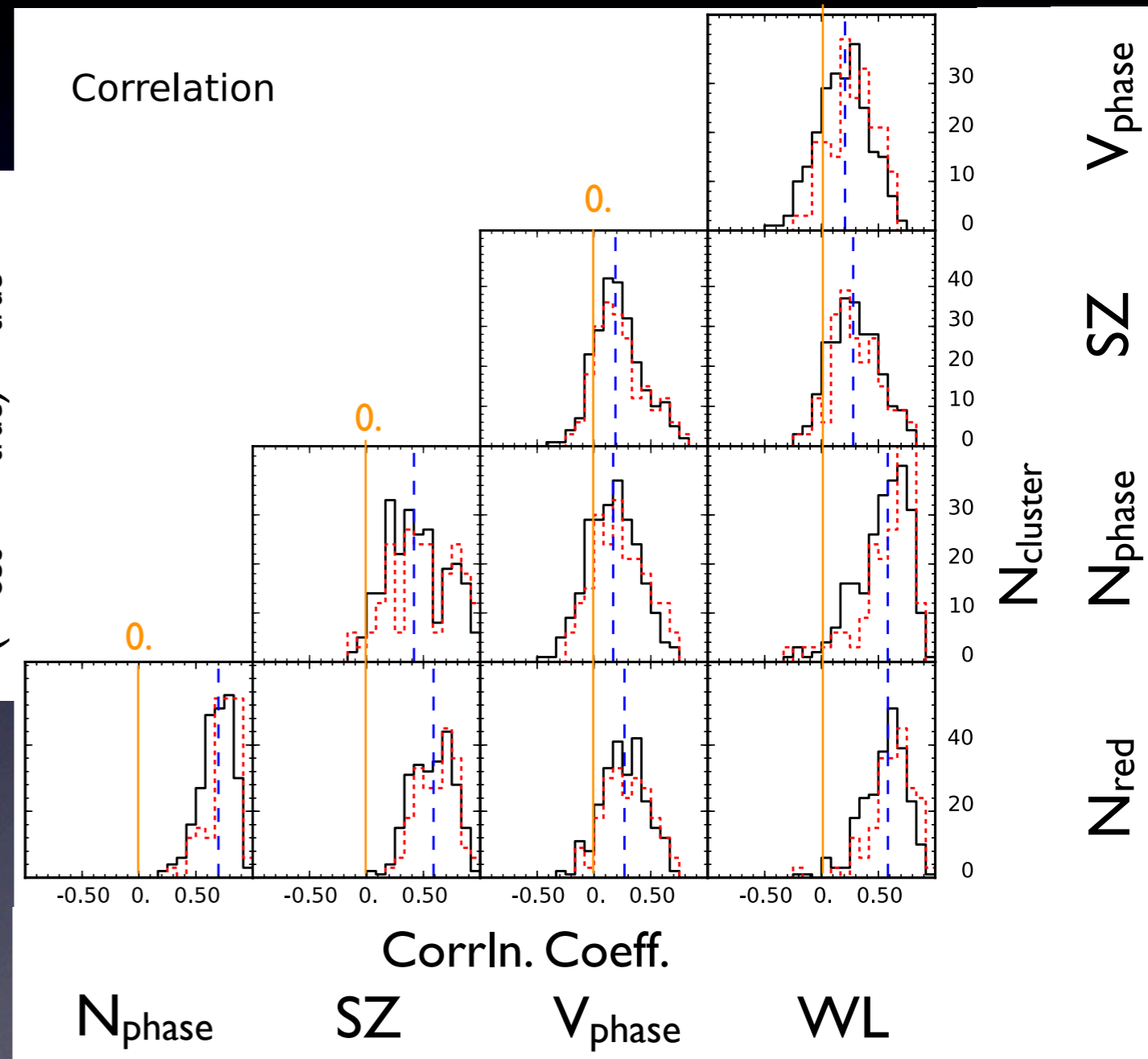
# Scatter in Cluster Mass Measurements



# Correlated Scatter



A single cluster



Ensemble of clusters

# Correlated Mass Scatter

- **Why is this important?** Rykoff++08, Stanek++10, White, Cohn, & Smit10, etc.
  - Stacking of ensemble of clusters can result in a bias
  - Error estimates can be incorrect for the joint measurement of one cluster

Analyses are beginning to include: Rozo ++09, Mantz++10, Benson++11, etc.  
A recent application to an observational cluster sample: Angulo++12 etc.

- **How can we take care of it?**
  - Calibrate with simulations
  - Understand what it is physically related to

# Correlated Mass Scatter

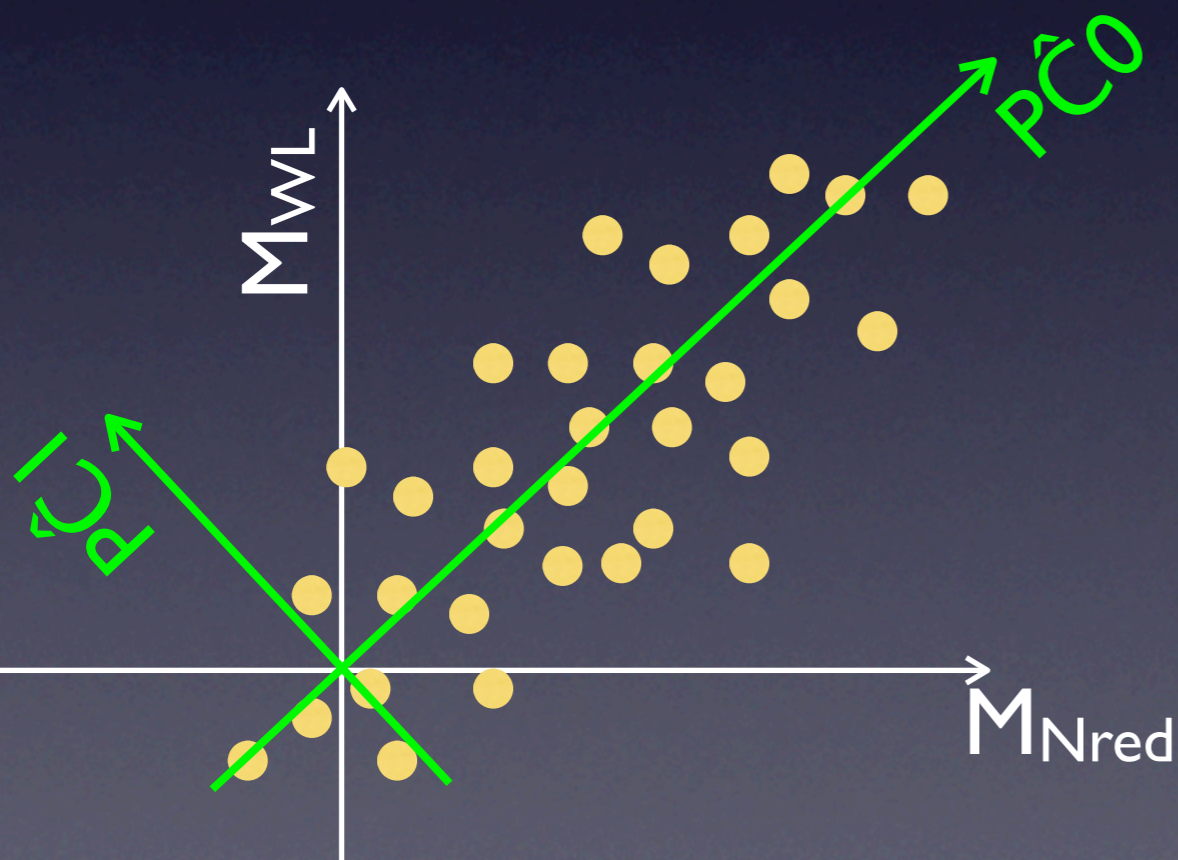
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# Principal Component Analysis(PCA)

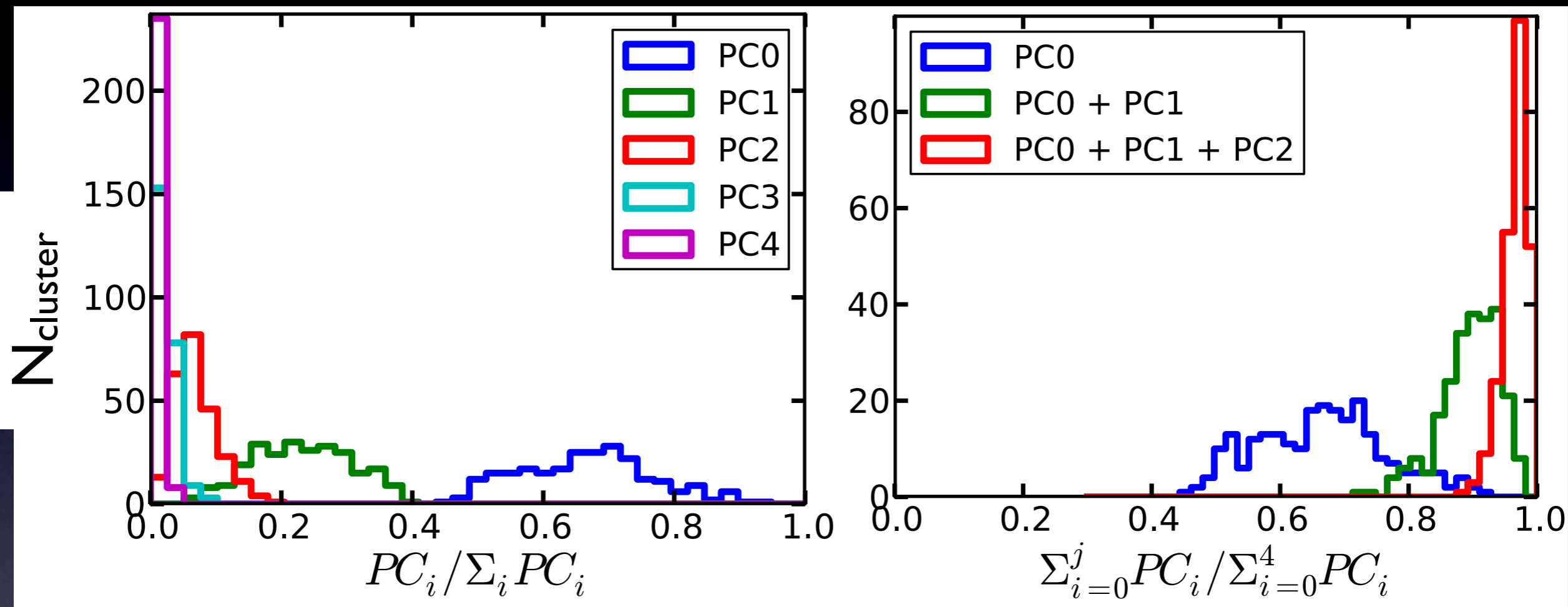
- Convert a set of correlated variables into a set of independent variables



- $\hat{PC}$ s are eigenvectors of covariance/correlation matrix
- Corresponding eigenvalues indicate the importance of  $\hat{PC}$ s
- $\hat{PC}_0$  gives the direction of the largest variance



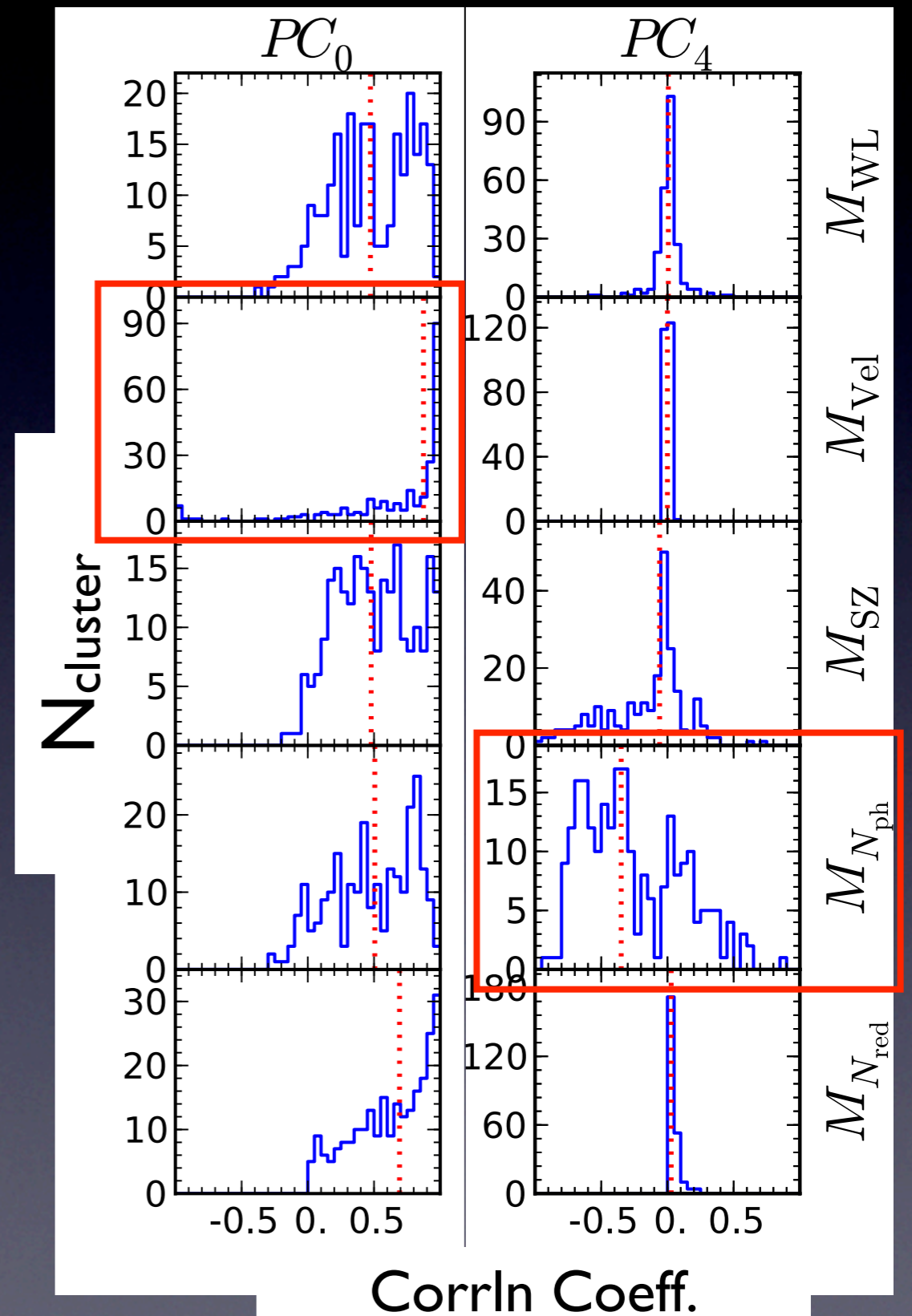
# PCA for Cluster Observables



- **PC0 accounts for 70% of total variance on average**
  - $\hat{PC}_0 \sim 0.42M_{\text{red}} + 0.14M_{\text{ph}} + 0.19M_{\text{sz}} + 0.83M_{\text{vel}} + 0.29M_{\text{wl}}$
- Including PC0 and PC1 accounts for 95% of total variance on average

# PCs vs. Observables

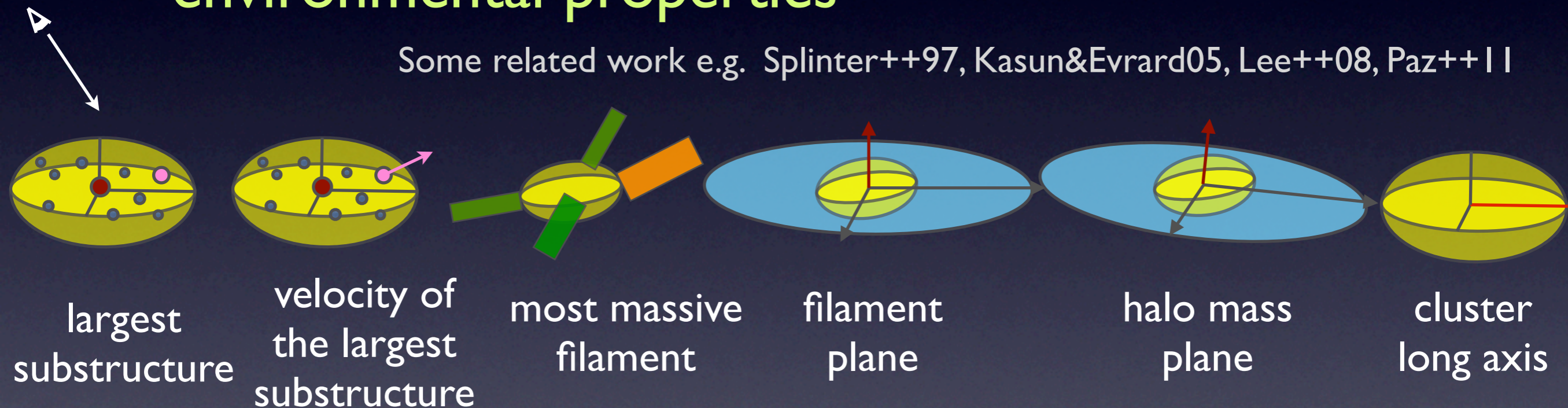
- Velocity dispersion mass measurements show the largest correlation with PC0
- $N_{\text{phase}}$  mass measurements show the largest correlation with PC4



# Cluster Properties depending on line-of-sight

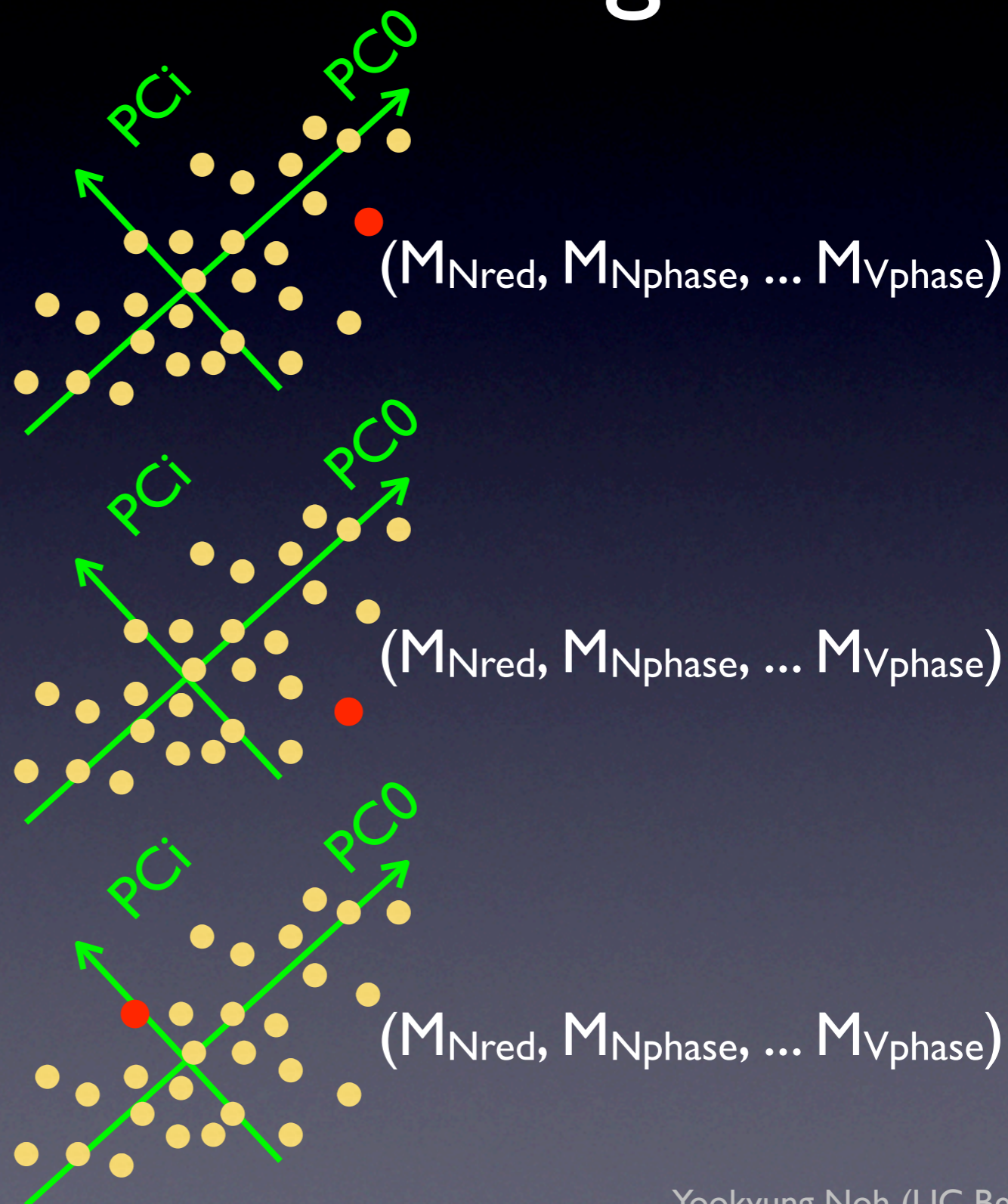
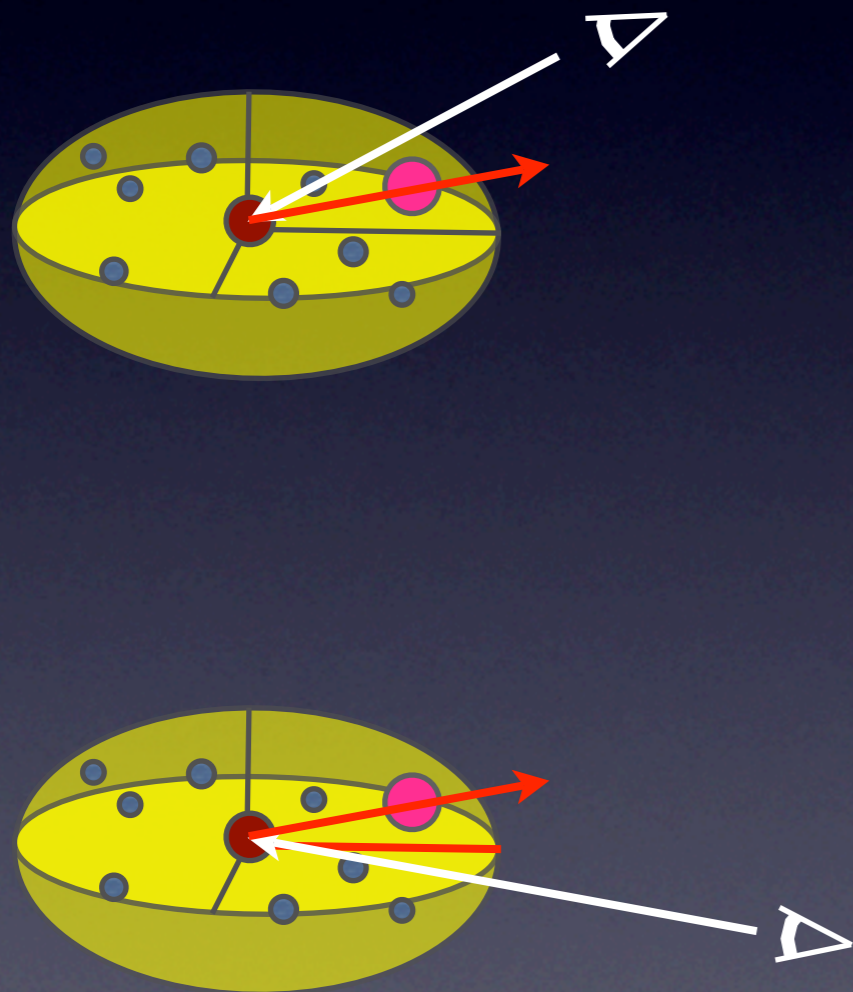
- Consider directional dependent intrinsic and environmental properties

Some related work e.g. Splinter++97, Kasun&Evrard05, Lee++08, Paz++11



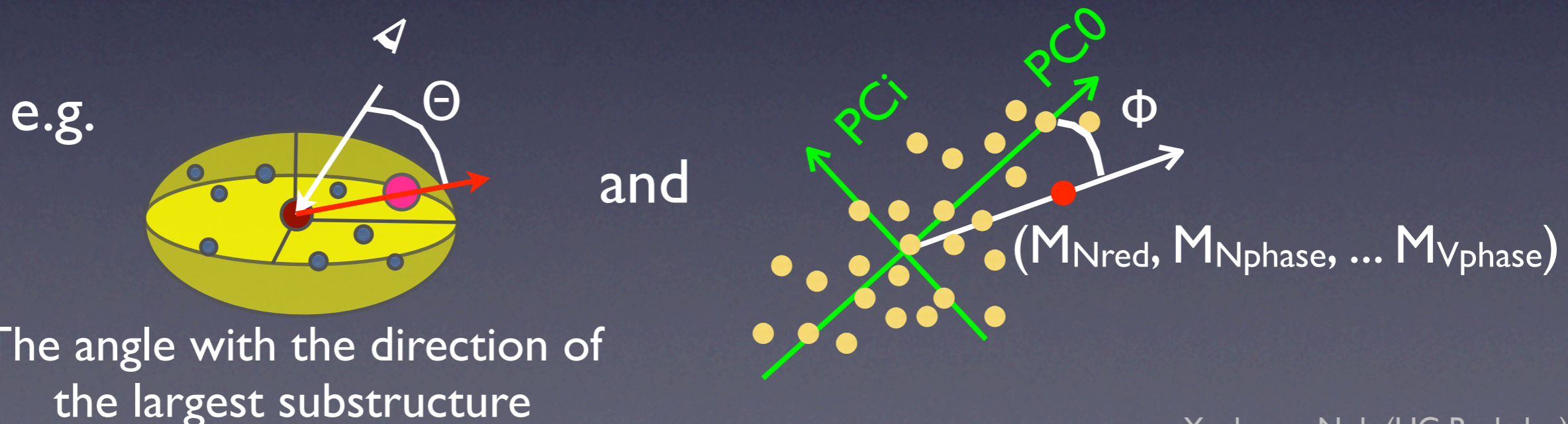
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e.g.

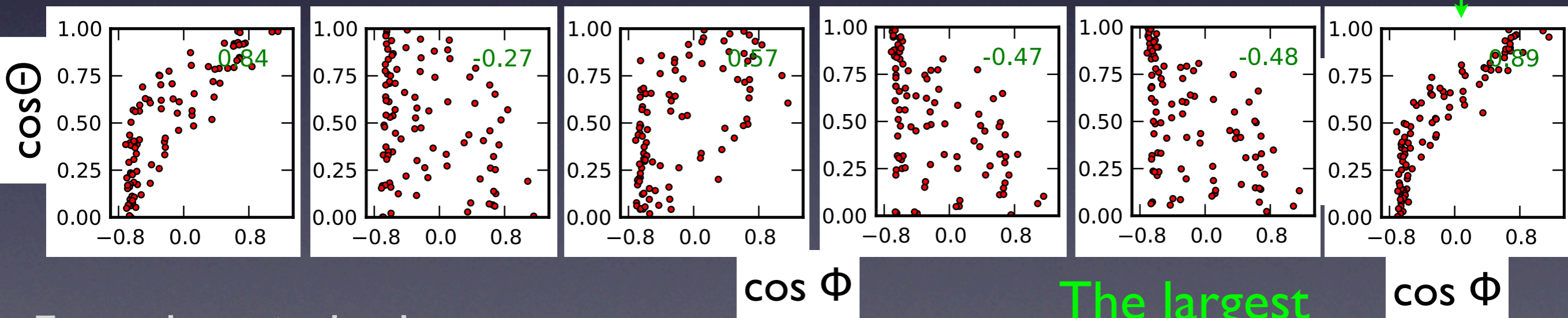
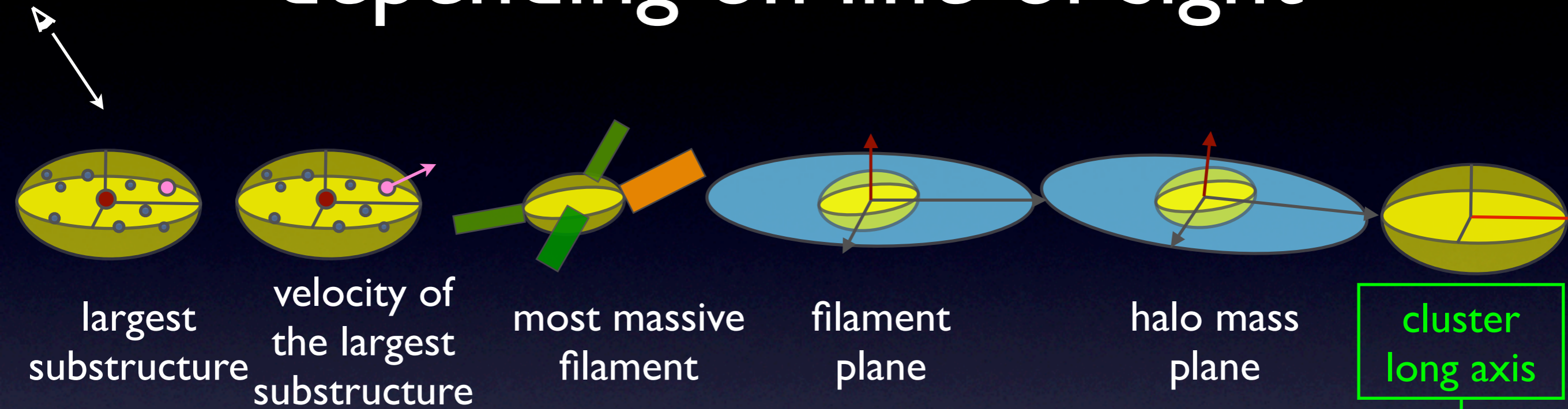


# Correlation with line-of-sight dependent Properties

- Calculate the correlations between
  - $|\cos\Theta|$  between line-of-sight direction and each of directional properties
  - $\cos\phi$  of the mass scatter along each line-of-sight to PC0 direction



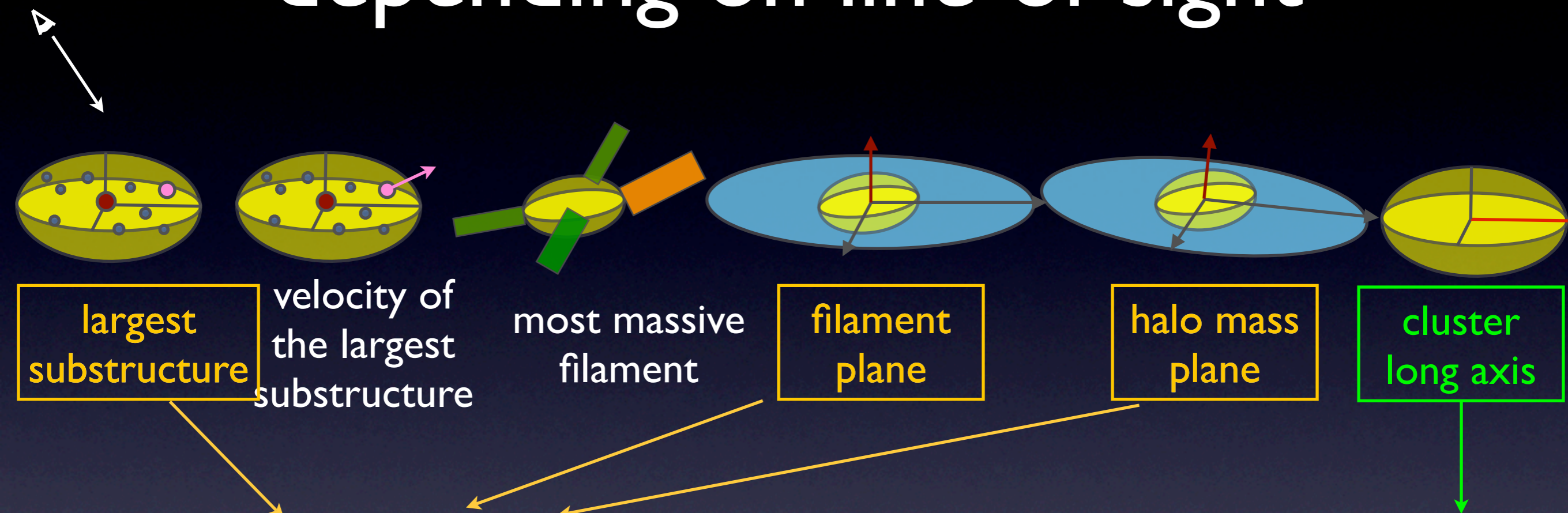
# Cluster Properties depending on line-of-sight



Example: a single cluster

The largest correlation/covariance

# Cluster Properties depending on line-of-sight



Next largest correlation/covariance

Many of these axes are close to each other in direction

The largest correlation/covariance → observing along long axis has largest contribution from PC0

Correlations with the long axis and mass scatters have been discussed in e.g. Becker & Kravtsov 11, Feroz & Hobson 12

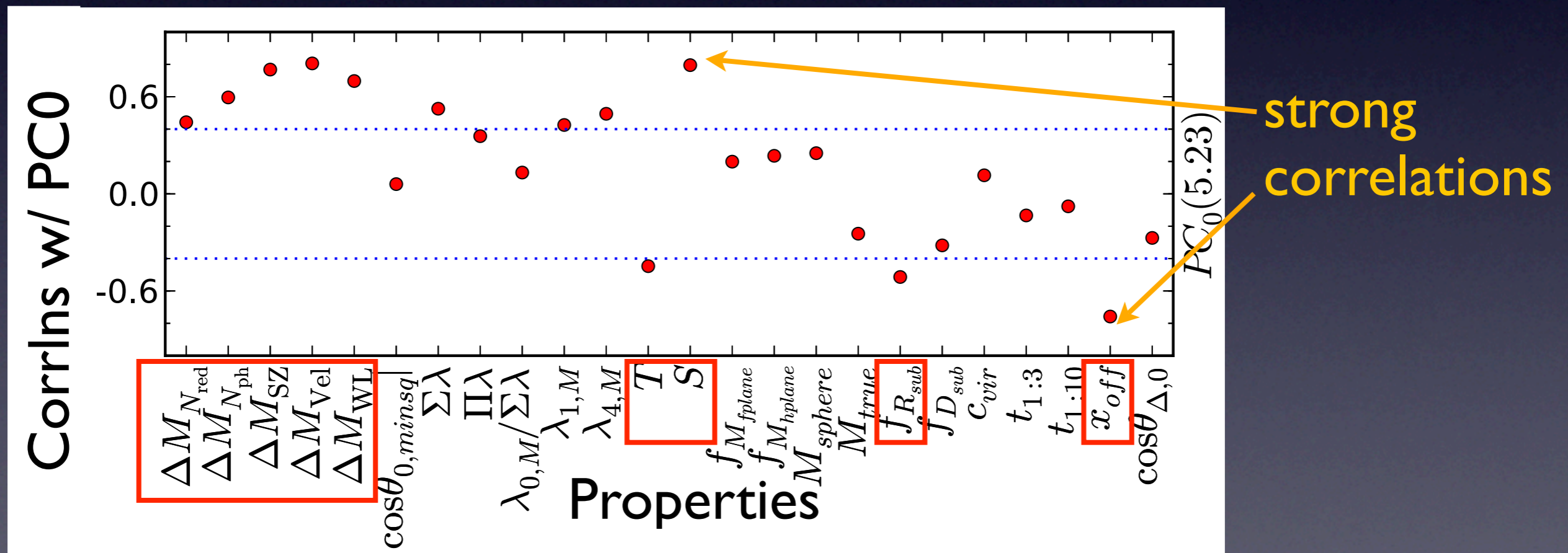
# PCA for Ensemble of Clusters

- Calculate PC's for scalar properties  
Earlier related work: Jeason-Daniel++, Einasto++, Skibba&Maccio(11)
- **Mass scatter properties:** average scatter (i.e.  $[\langle M_{\text{obs}} \rangle - M_{\text{true}}]/M_{\text{true}}$ ), PC's from mass scatter PCA, etc.
- **Physical properties:** mass fraction in filament plane, richness fraction in biggest sub halos, triaxiality, etc.
- PC0 accounts for  $\sim 20\%$  of total variance
  - Including up to PC4 accounts for  $\sim 50\%$  of total variance



# PCA for Ensemble of Clusters

- PC0 is strongly correlated with the average offsets in mass measurements and shape parameters



# Summary

- Filament distributions around clusters are planar
  - A source of scatter in mass measurements
- Scatters in different mass measurements are often correlated with each other
  - can cause biases, error, underestimates, etc. if not taken into account
  - Due to the shared physical origins of scatter:  
Cluster long axis is most correlated with PC0
  - Analyzed using PCA: which combinations of scatter tend to occur together?

# Summary

- Calibrating the scatters and their correlations requires simulations which faithfully reproduce observables, systematics and selection function