

Hard exclusive π^0 and η production

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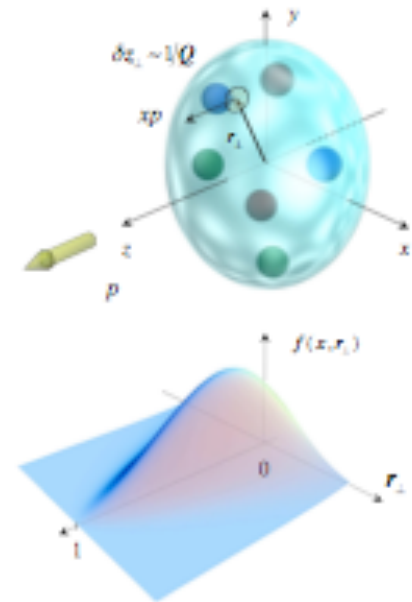
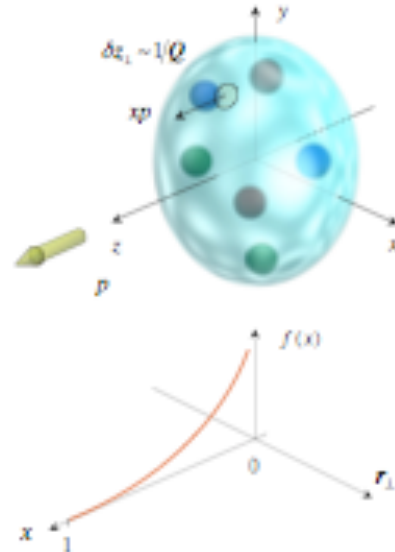
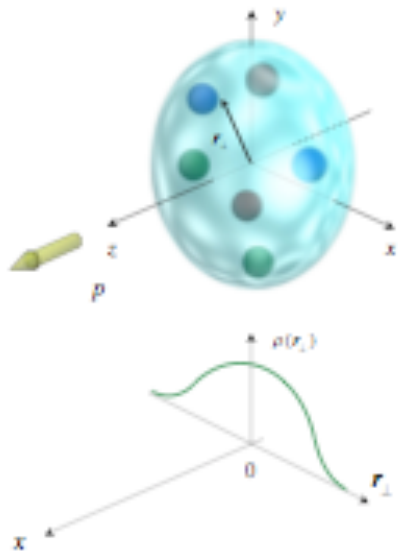
August 20, 2011

Hall-C Summer Workshop

Outline

- Physics motivation
- CLAS6 data on pseudoscalar meson electroproduction
- E12-06-108 Hard exclusive electroproduction of π^0 and η with CLAS12
- Conclusion

Description of hadron structure in terms of GPDs



Nucleon form factors

transverse charge & current densities

Nobel prize 1961- R. Hofstadter

Structure functions

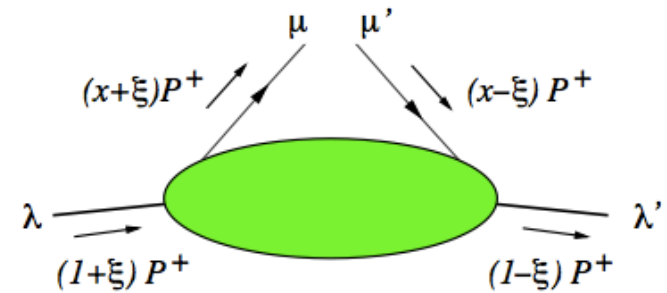
quark longitudinal momentum (polarized and unpolarized) distributions

Nobel prize 1990 –J.Friedman, H. Kendall, R. Taylor

GPDs

correlated quark momentum distributions (polarized and unpolarized) in transverse space

Generalized Parton Distributions



- There are 4 chiral even GPDs where partons do not transfer helicity \tilde{H}, H, E, E
- H and E are “unpolarized” and \tilde{H} and \tilde{E} are “polarized” GPD. This refers to the parton spins.
- 4 chiral odd GPDs flip the parton helicity $H_T, \tilde{H}_T, E_T, \tilde{E}_T$. H_T is connected with transversity

$$H_T^q(x, 0, 0) = h_1^q(x)$$

Basic GPD properties

- Forward limit

$$H^q(x, 0, 0) = q(x)$$

$$\tilde{H}^q(x, 0, 0) = \Delta q(x)$$

$$H_T^q(x, 0, 0) = h_1^q(x)$$

- Form factors

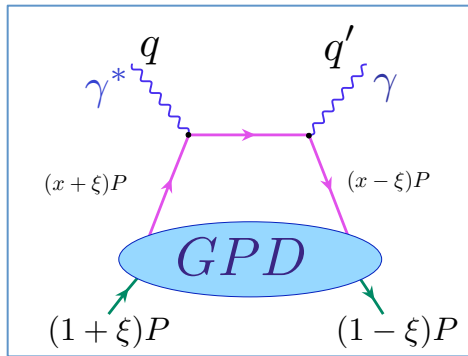
$$\int_{-1}^1 dx H^q(x, \xi, t) = F_1^q(t), \quad \int_{-1}^1 dx E^q(x, \xi, t) = F_2^q(t)$$

$$\int_{-1}^1 dx \tilde{H}^q(x, \xi, t) = g_A^q(t), \quad \int_{-1}^1 dx \tilde{E}^q(x, \xi, t) = g_P^q(t),$$

- Angular Momentum

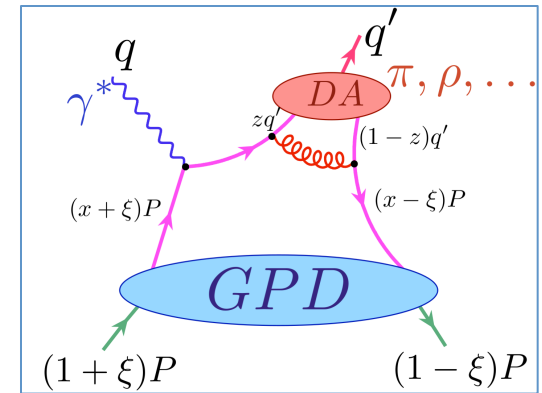
$$J^q(t) = \frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

(Ji's sum rule)



DVCS and DVMP

- Factorization theorem
- Access to fundamental degrees of freedom



DVCS:

- the clearest way to access the GPDs
- Only γ_T photons participate in DVCS
- Interference with BH process

DVMP:

- Factorization proven only for σ_L
 $\sigma_L \sim 1/Q^6$, $\sigma_T/\sigma_L \sim 1/Q^2$
- Meson distribution amplitude
- Gluon exchange required
- Vector and pseudoscalar meson production allows to separate flavor and separate the helicity-dependent and helicity independent GPDs.

\tilde{H}, \tilde{E}

H, E

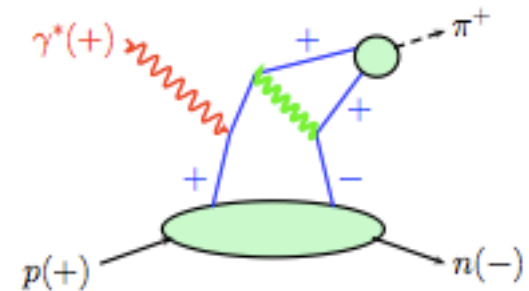
Meson	GPD flavor composition
π^+	$\Delta u - \Delta d$
π^0	$2\Delta u + \Delta d$
η	$2\Delta u - \Delta d$
ρ^0	$2u + d$
ρ^+	$u - d$
ω	$2u - d$

Transversity in hard exclusive electroproduction of pseudoscalar mesons

S. Goloskokov, P. Kroll, 2011, [arXiv:1106.4897v1](https://arxiv.org/abs/1106.4897v1)

- The data clearly show that a leading-twist calculation of DVMP within the handbag is insufficient. They demand higher-twist and/or power corrections.
- There is a large contribution from the helicity amplitude $M_{0-,++}$. Such contribution is generated by the the helicity-flip or transversity GPDs in combination with a twist-3 pion wave function.
- This explanation established an interesting connection to transversity parton distributions. The forward limit of H_T is the transversity.

$$M_{0-,++} \sim H_T$$



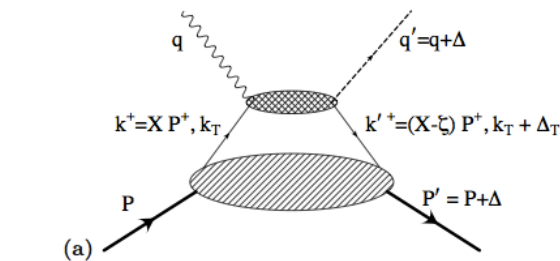
$$H_T^q(x, 0, 0) = h_1^q(x)$$

Nucleon Tensor Charge from Exclusive π^0 Electroproduction

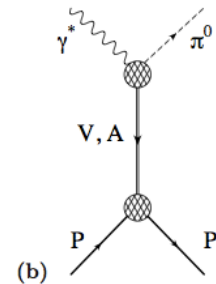
$$\gamma^* p \rightarrow p \pi^0$$

Ahmad, Goldstein, Luiti, Phys. Rev. D 79, 054014 (2009), arXiv:1104.5682v1

- The quantum numbers and Dirac structure of π^0 electroproduction restrict the possible contributions to the 4 chiral odd GPDs, one of which, H_T , is related to the transversity distribution and the tensor charge.
- This differs from DVCS and both vector and charge $\pi^{+/-}$ electroproduction, where the axial charge can enter the amplitudes.
- Contrary the tensor charge enters the π^0 process.

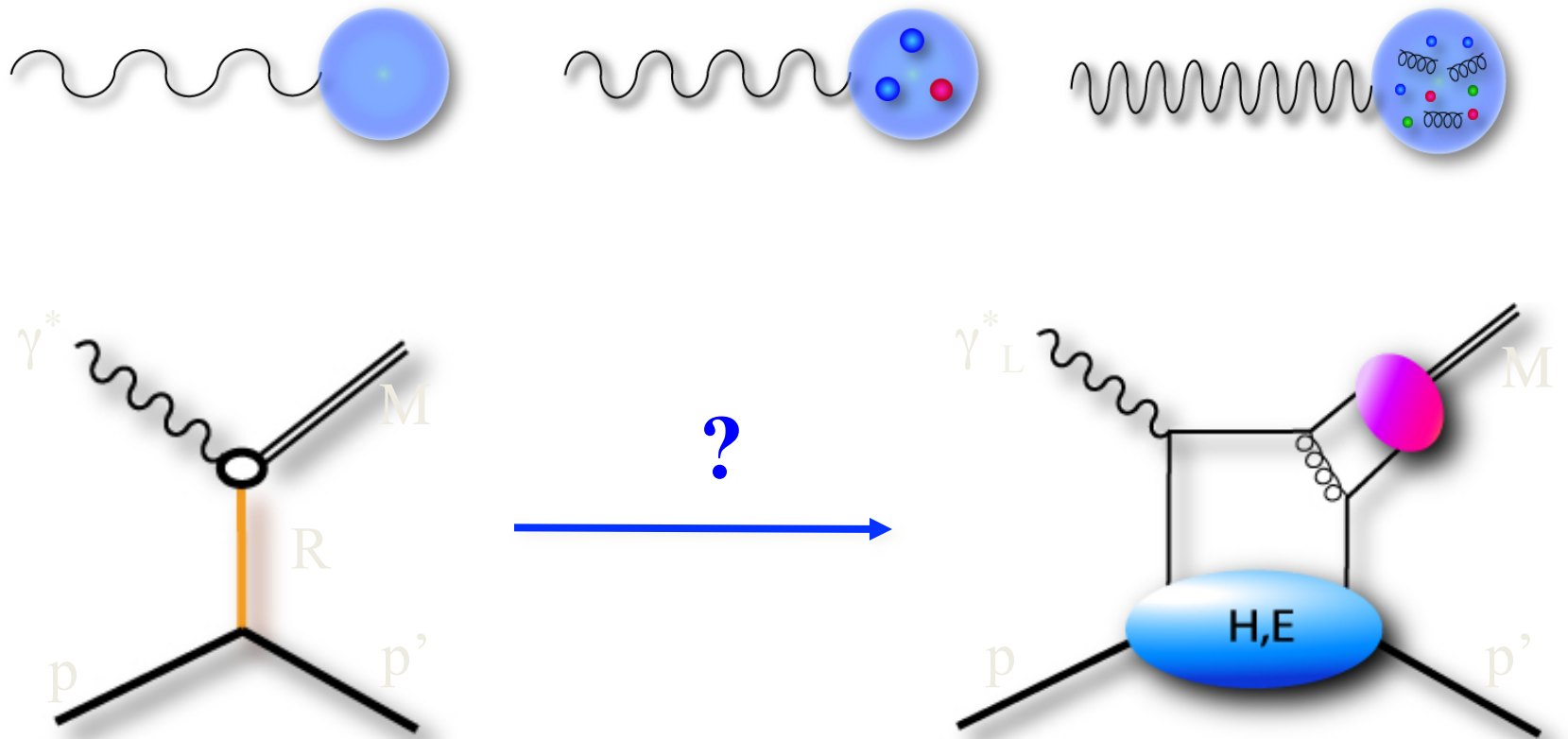


partonic degrees of freedom interpretation;



t-channel exchange diagram

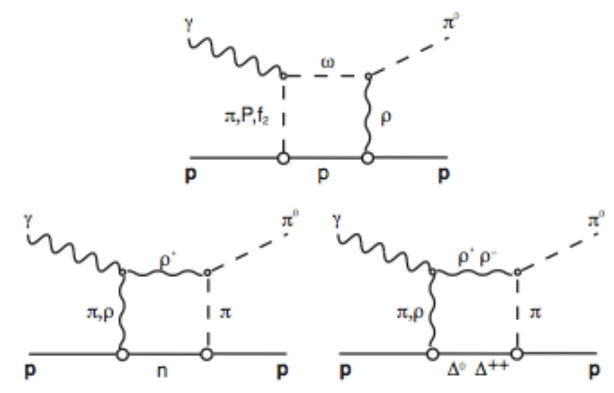
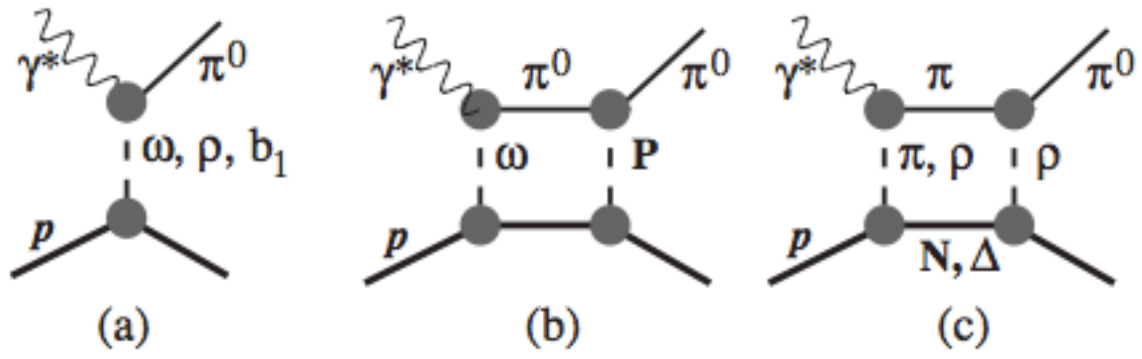
Transition from “hadronic” to the partonic degrees of freedom



$$\gamma^* p \rightarrow p \pi^0$$

Regge Model

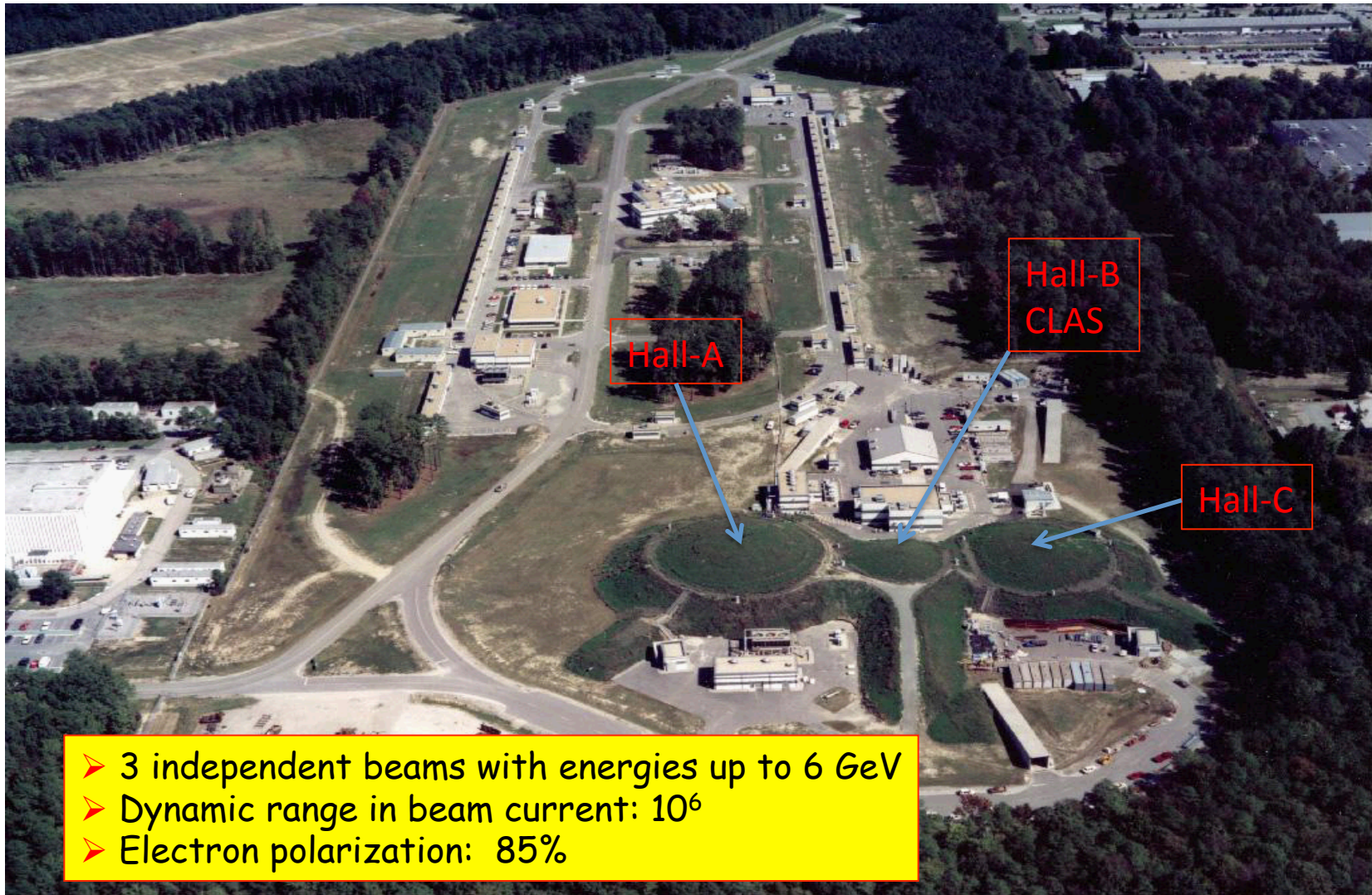
J.M. Laget 2010



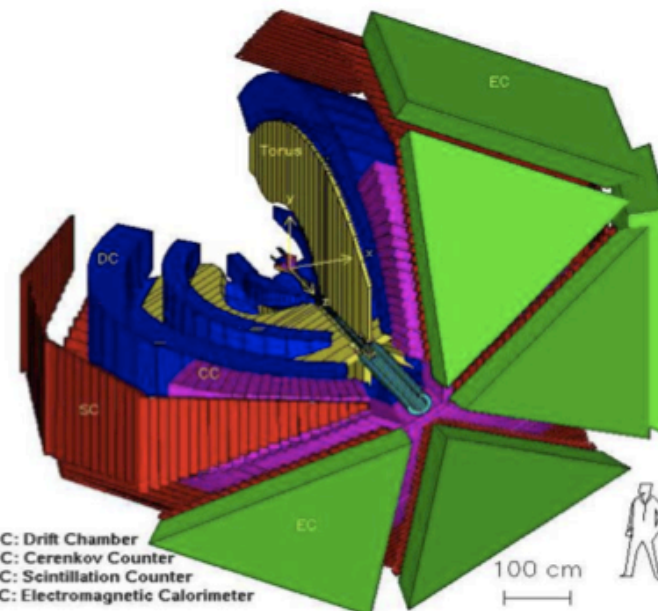
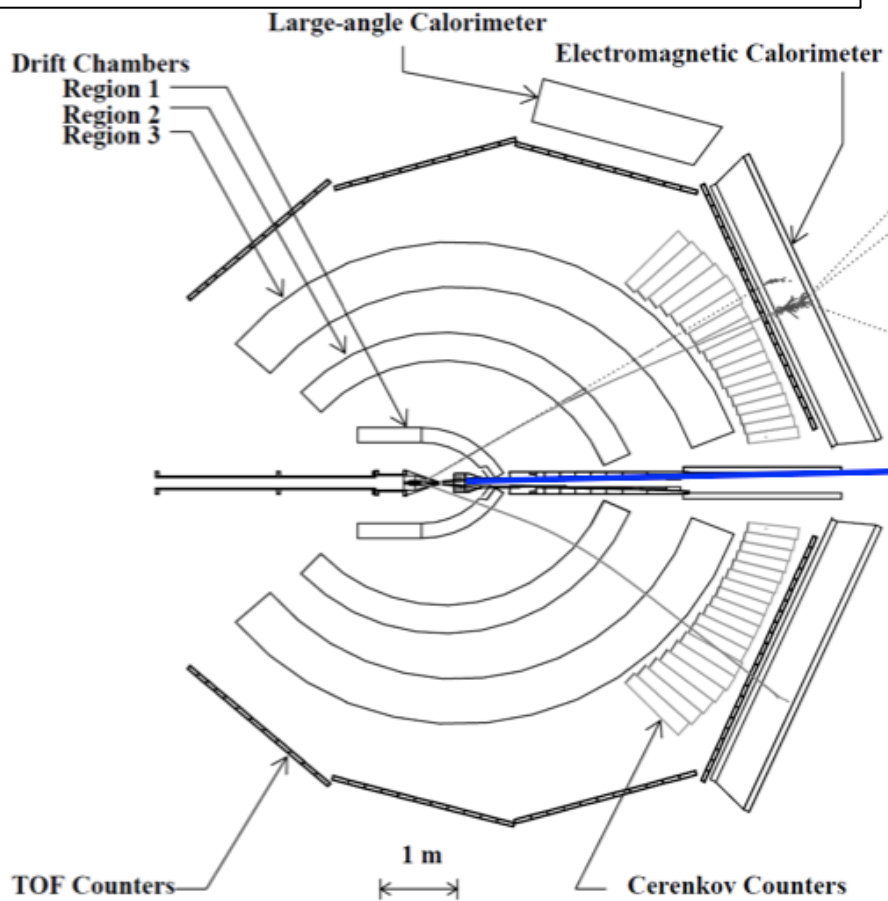
(a) Regge poles (vector and axial vector mesons)
 (b) and (c) pion cuts

Vector meson cuts

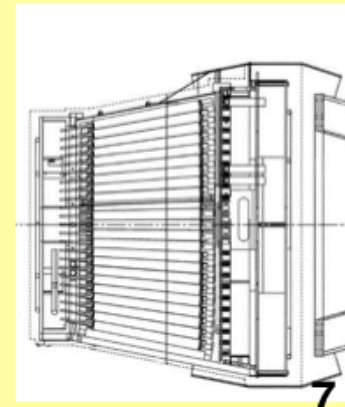
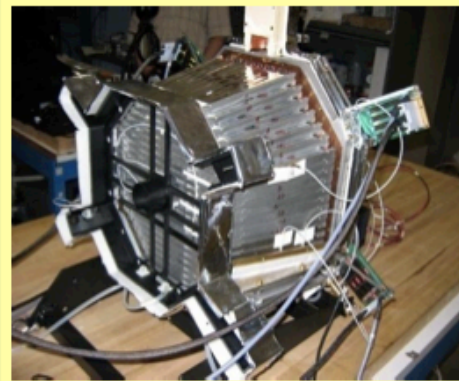
JLab Site: The 6 GeV Electron Accelerator



CEBAF Large Acceptance Spectrometer CLAS



Inner Calorimeter



CLAS Lead Tungstate Electromagnetic Calorimeter

424 crystals, 18 RL,
Pointing geometry,
APD readout

Pseudoscalar mesons

$$ep \rightarrow en\pi^+$$

$$ep \rightarrow ep\pi^0, \quad \pi^0 \rightarrow \gamma\gamma$$

$$ep \rightarrow ep\eta, \quad \eta \rightarrow \gamma\gamma$$

CLAS6: lots of data.
CLAS12: Exp. # E12-06-108

Vector mesons

$$ep \rightarrow en\rho^+, \quad \rho^+ \rightarrow \pi^+\pi^0$$

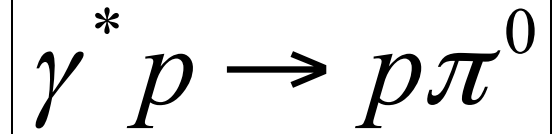
$$ep \rightarrow ep\rho^0, \quad \rho^0 \rightarrow \pi^+\pi^-$$

$$ep \rightarrow ep\omega, \quad \omega \rightarrow \pi^+\pi^-\pi^0$$

$$ep \rightarrow ep\phi, \quad \phi \rightarrow K^+K^-$$

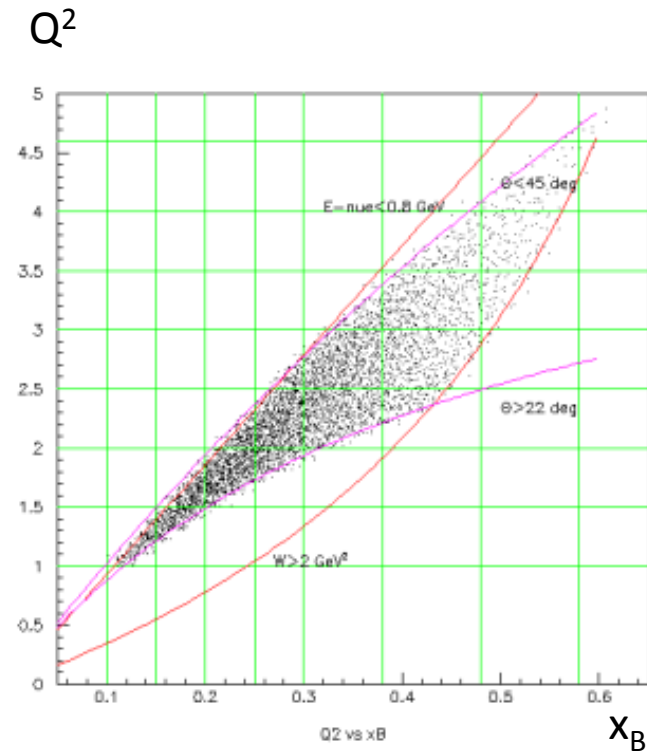
New proposal being prepared
for PAC 38

4 Dimensional Grid



Rectangular bins are used.

- Q^2 - 7 bins(1.-4.5 GeV^2)
- x_B - 7 bins(0.1-0.58)
- t - 8 bins(0.09-2.0 GeV)
- ϕ - 20 bins(0-360°)
- π^0 data ~2000 points
- η data ~1000 points



Monte Carlo

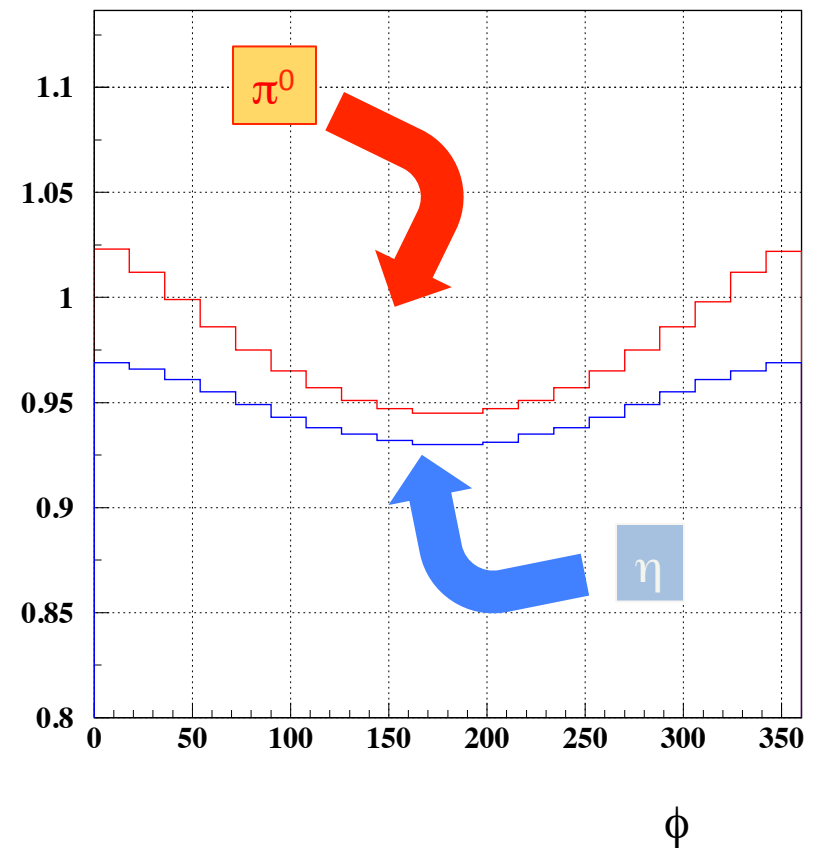
- Empirical model for the structure cross sections was used for the MC simulation and radiative corrections
- This model is based on CLAS data
- MC simulation included the radiative effects and used empirical model for the Born term.
- 100 M events were simulated with GSIM program.

Radiative Corrections

- Radiative Corrections were calculated using **Exclurad** package with structure cross sections described by our empirical cross section.

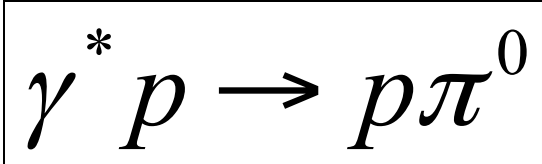
$$Q^2 = 1.15 \text{ GeV}^2 \quad x_B = 0.13 \quad -t = 0.1 \text{ GeV}^2$$

$$RadCor = \frac{\sigma_{Rad}}{\sigma_{Born}}$$

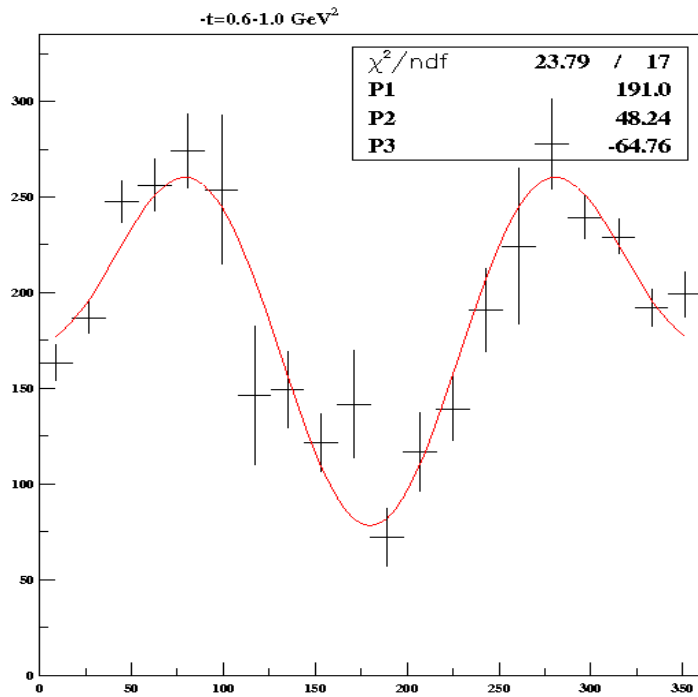


Structure Functions

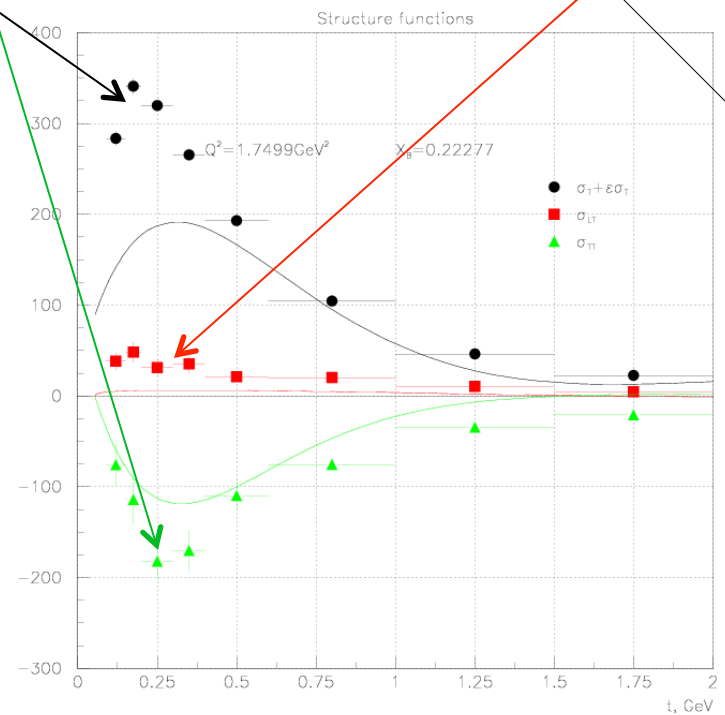
$\sigma_T + \epsilon \sigma_L$ σ_{TT} σ_{LT}



$$\frac{d\sigma}{dt d\phi}(Q^2, x, t, \phi) = \frac{1}{2\pi} \left(\frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi$$



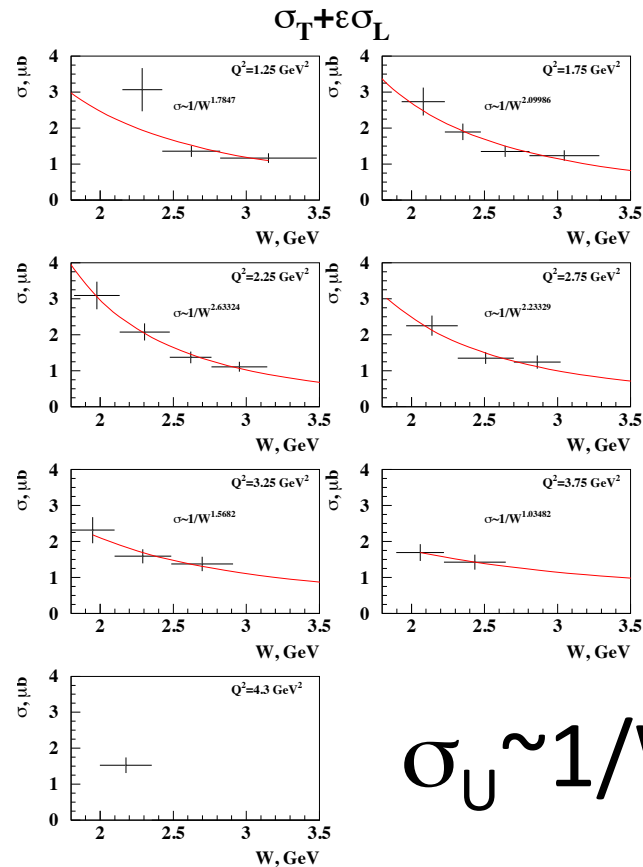
ϕ distribution



GM Laget Regge model

$\sigma_U = \sigma_T + \varepsilon \sigma_L$ W dependence

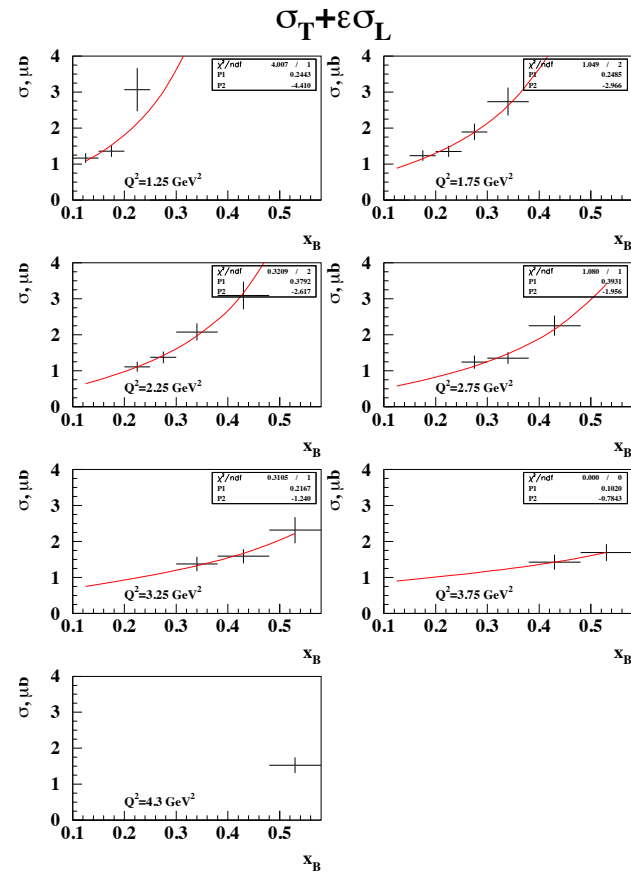
- σ_U decreases with W at Jlab kinematics
- This behavior is typical for Regge model
- Difficult to get such dependence with conventional GPD models



$$\sigma_U \sim 1/W^{1.5-2}$$

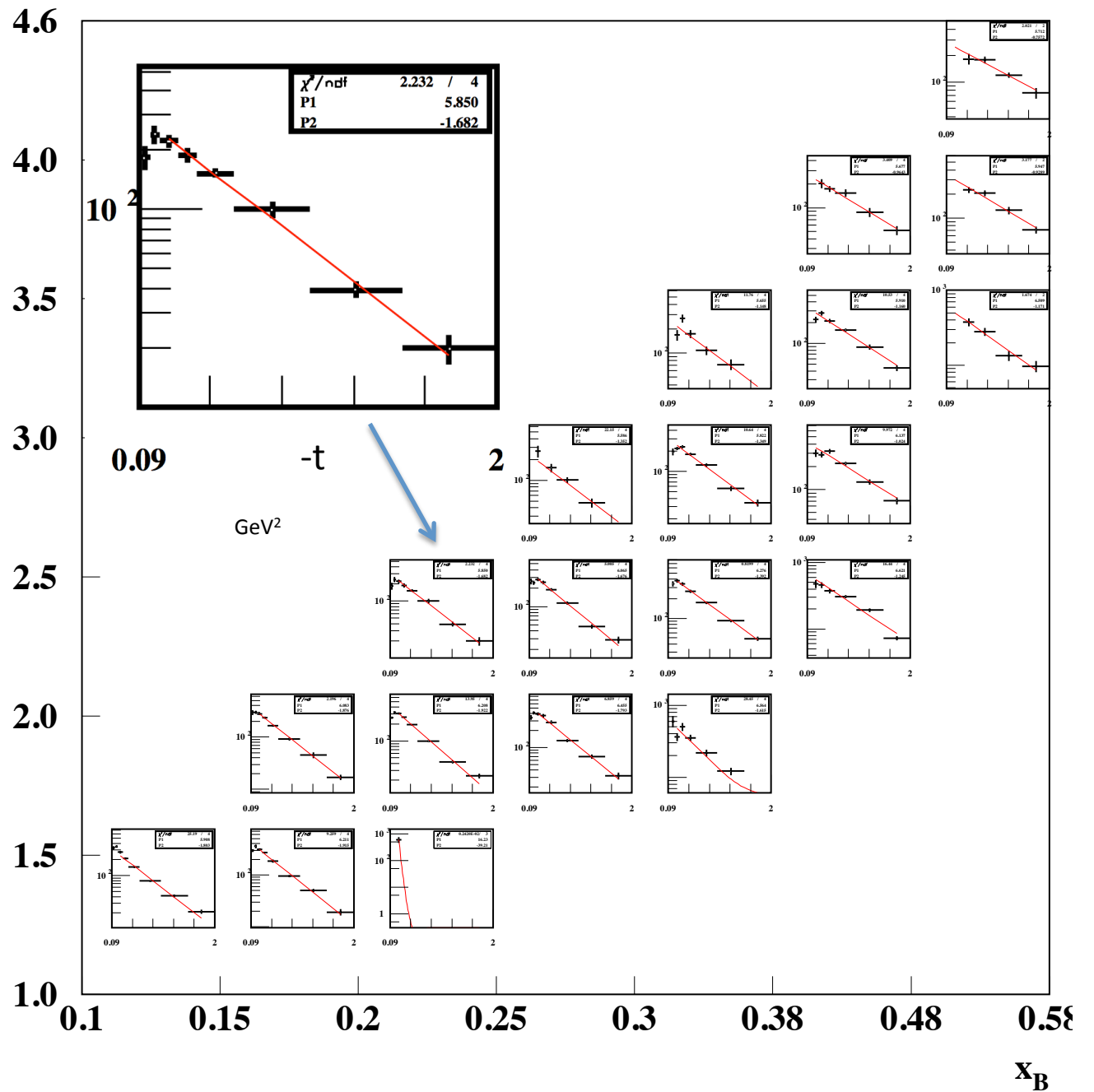
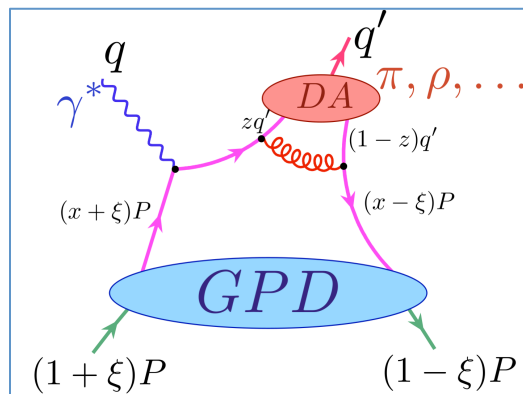
$\sigma_U = \sigma_T + \epsilon \sigma_L$ x_B dependence

- Another way to view the cross section as a function of x_B
- σ_U increases with x_B
- $W = Q^2(1/x - 1)$

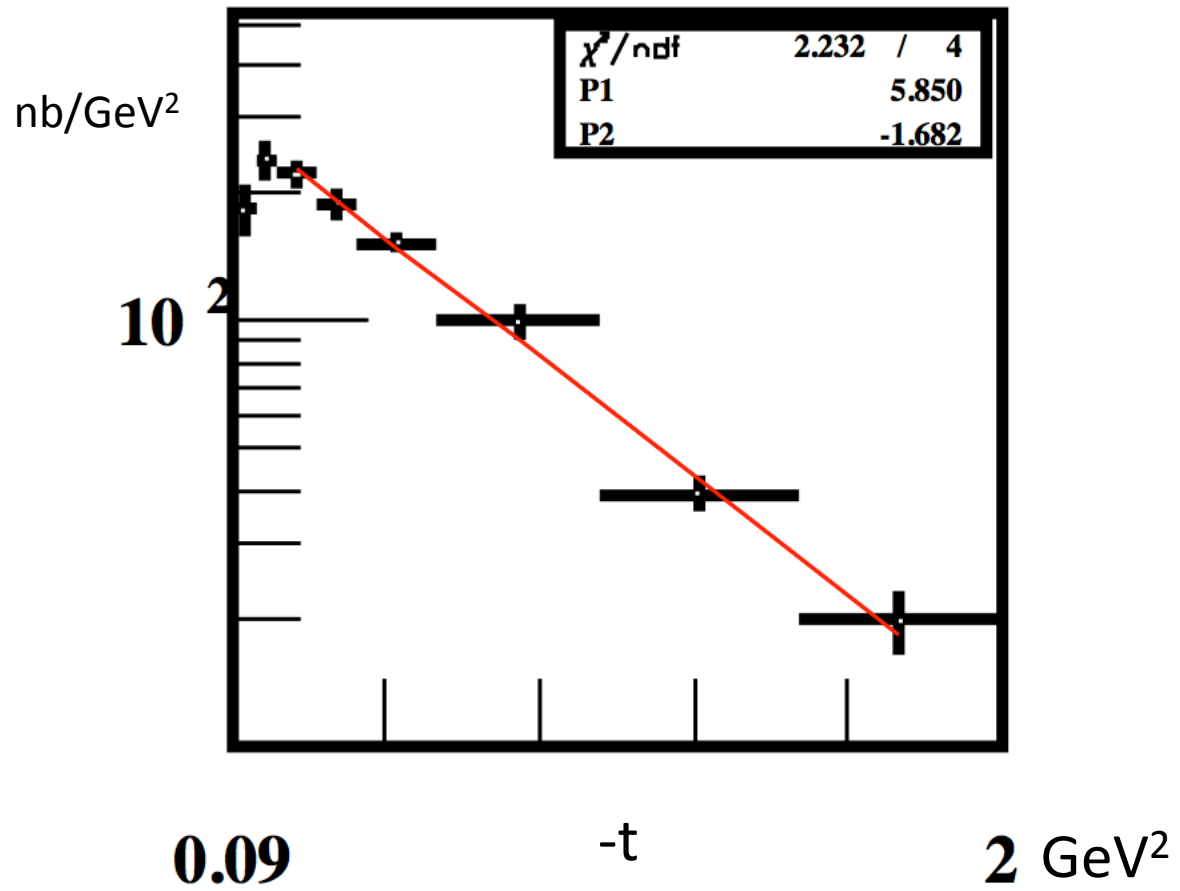


$$d\sigma_U/dt \propto Q^2$$

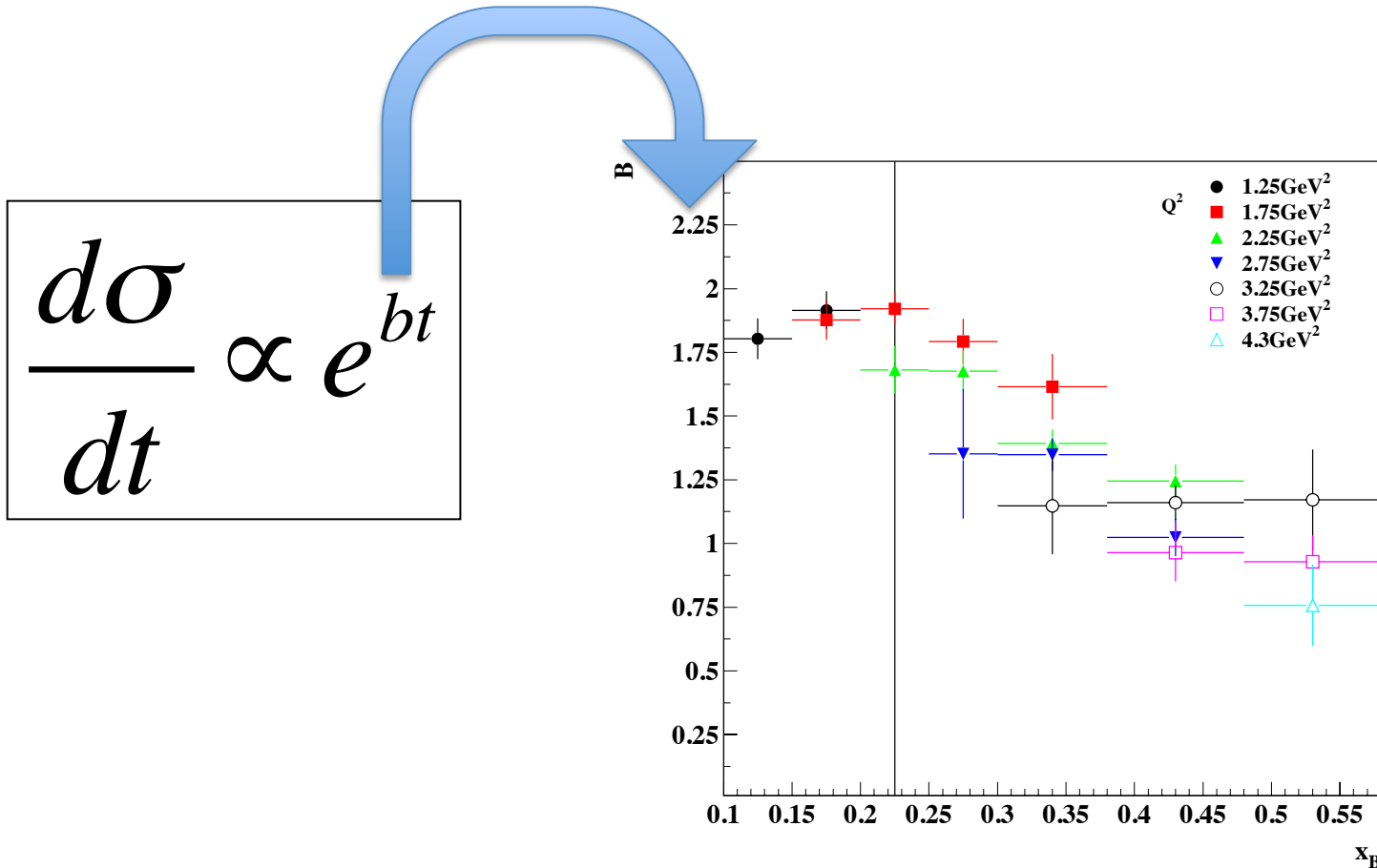
$$\frac{d\sigma}{dt}(\gamma^* p \rightarrow ep\pi^0) \propto e^{bt}$$



$$d\sigma_U/dt$$



t-slope parameter: x_B dependence

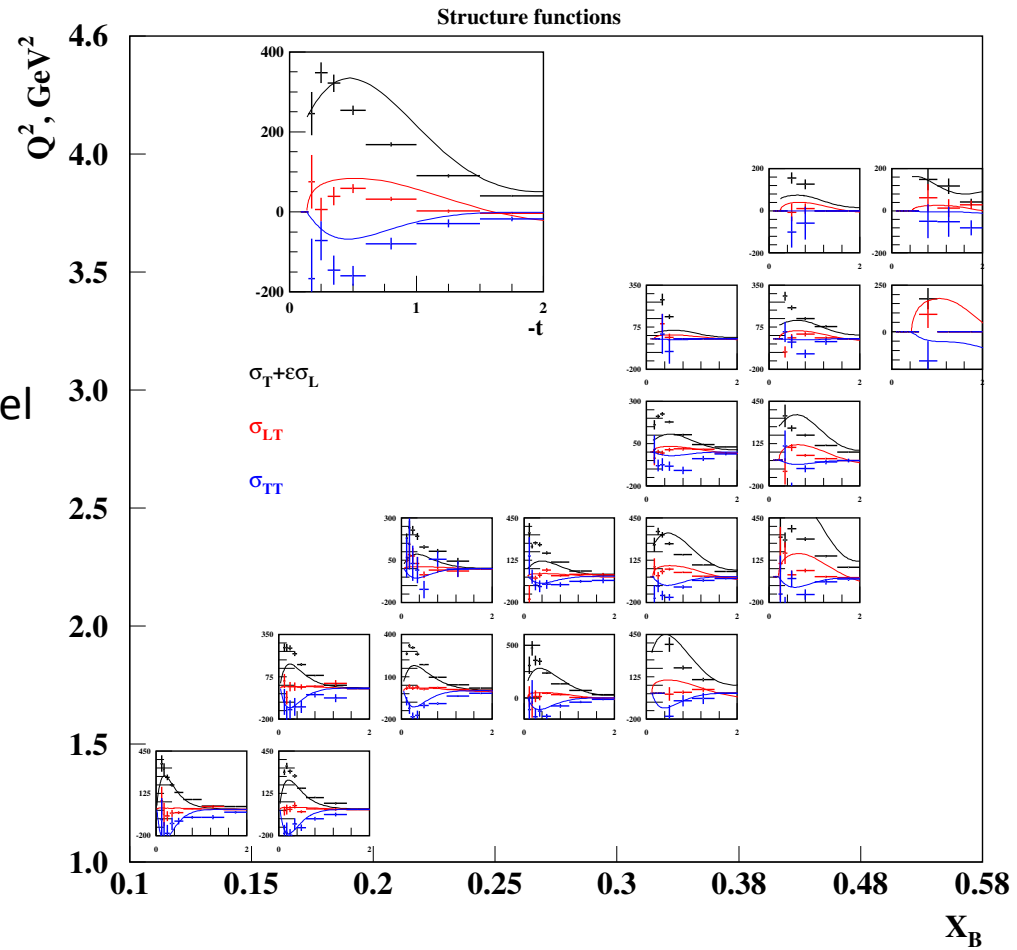


The dependence on Q^2 is very weak. The slope parameter is decreasing with increasing x_B . Looking to this picture we can say that the perp width of the partons with $x \rightarrow 1$ goes to zero.

Structure Functions

$$\sigma_U = \sigma_T + \varepsilon\sigma_L \quad \sigma_{TT} \quad \sigma_{LT}$$

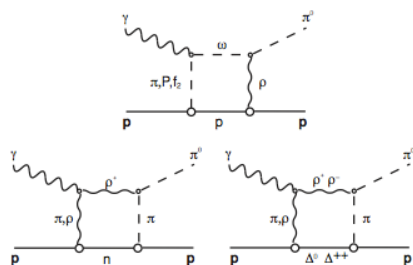
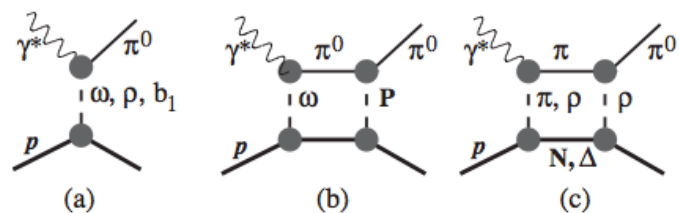
Lines – Regge model



$$\gamma^* p \rightarrow p \pi^0$$

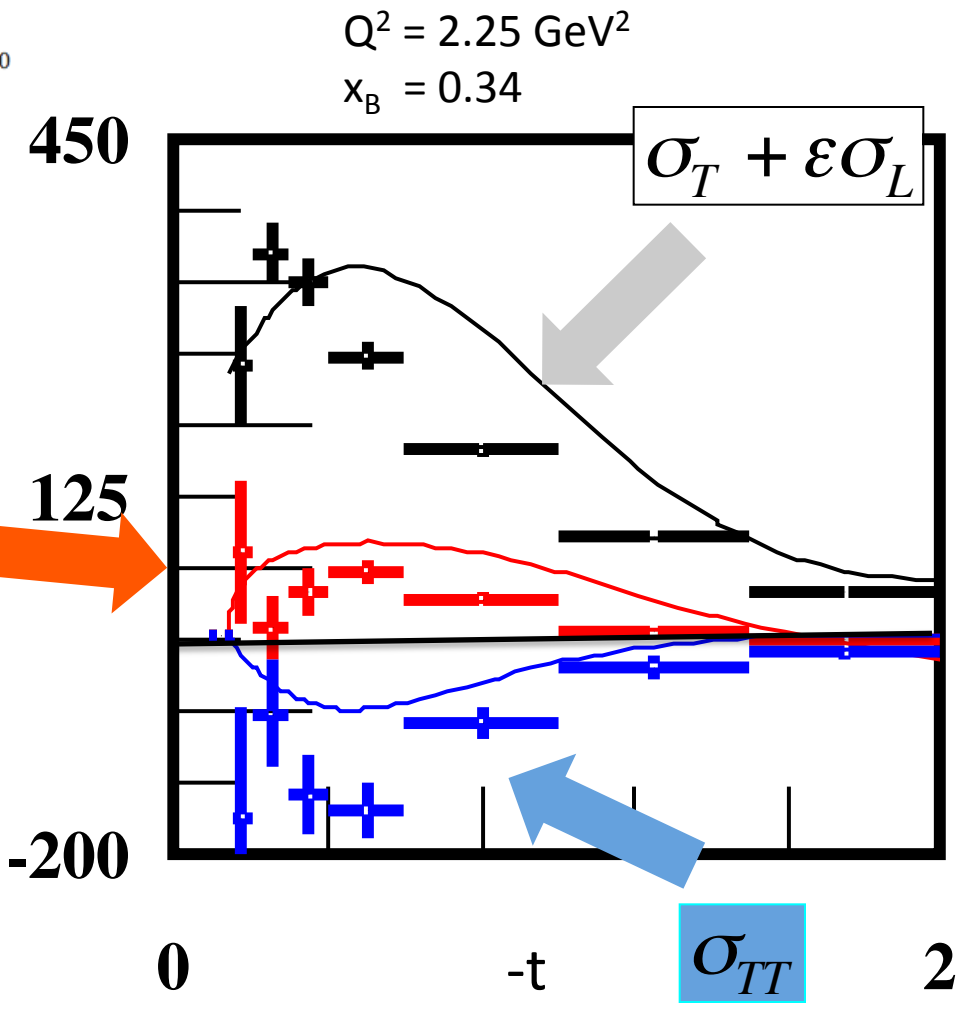
JML Regge model

$$\sigma_U = \sigma_T + \epsilon \sigma_L \quad \sigma_{TT} \quad \sigma_{LT}$$

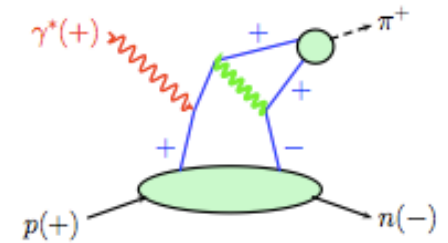


σ_{LT}

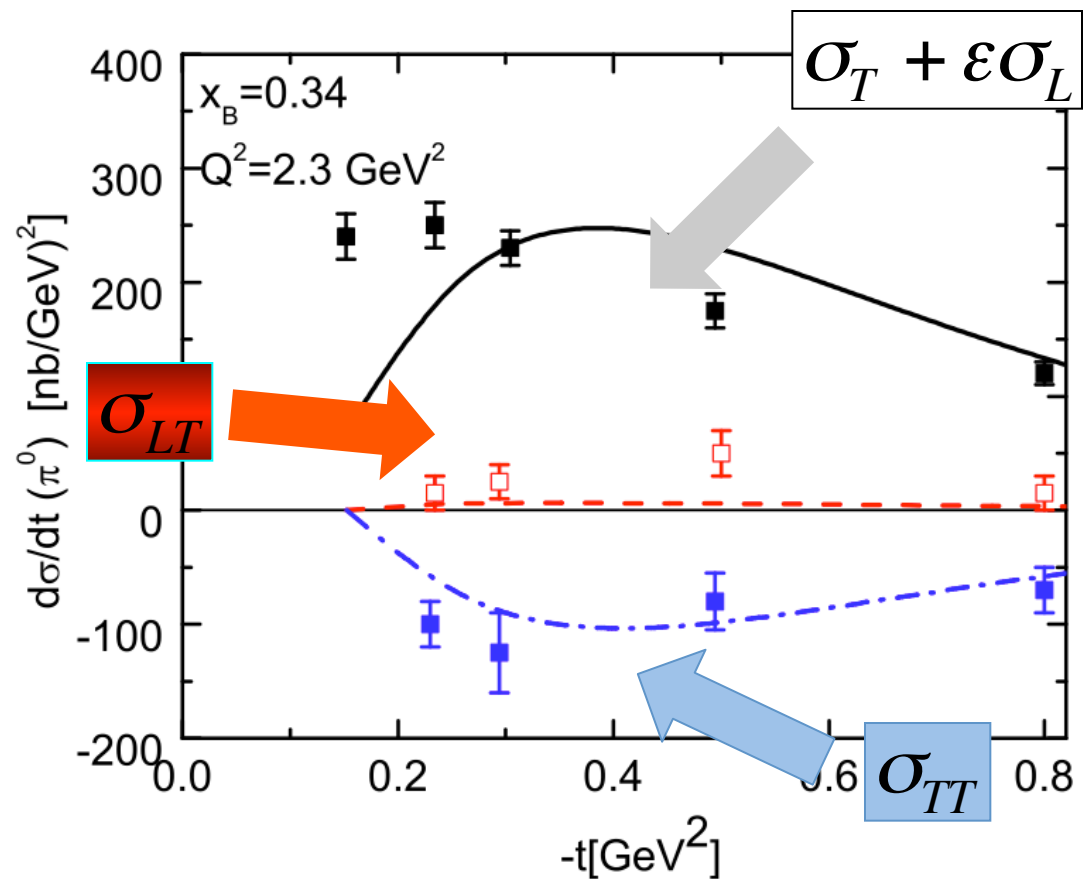
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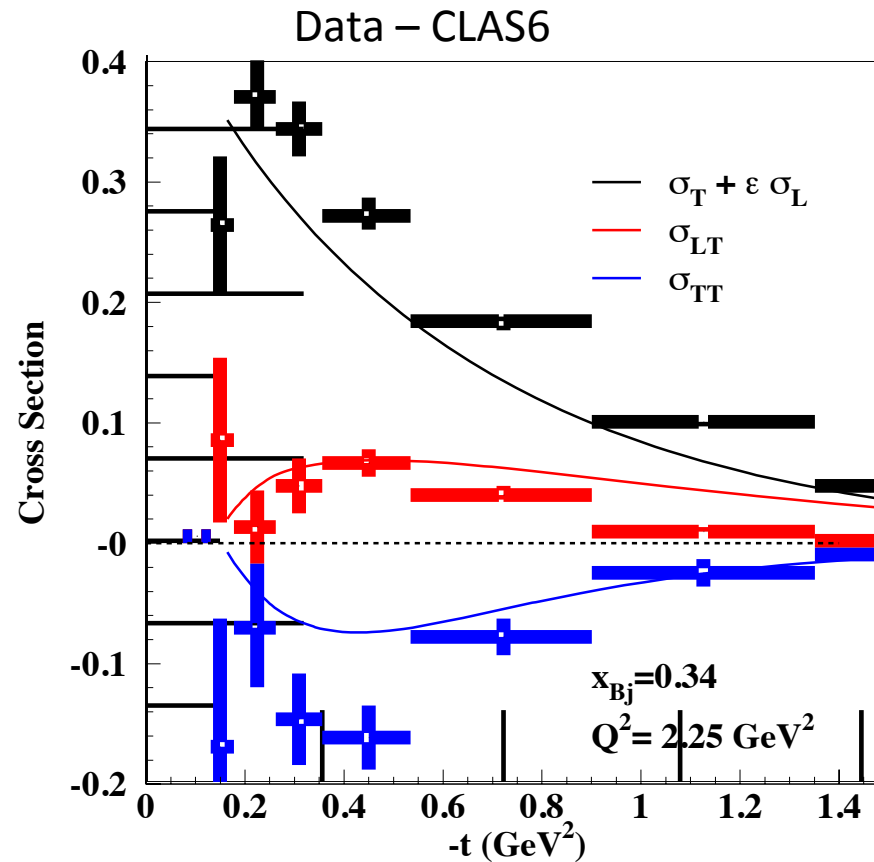
Goloskokov & Kroll GPD Model



- Include **transversity GPDs**
 H_T and $\bar{E}_T = 2\tilde{H}_T + E_T$ Dominate in CLAS kinematics.
 Successfully described data.
- Pseudoscalar meson production provides unique possibility to access the transversity GPDs.



Goldstein and Liuti GPD_T model

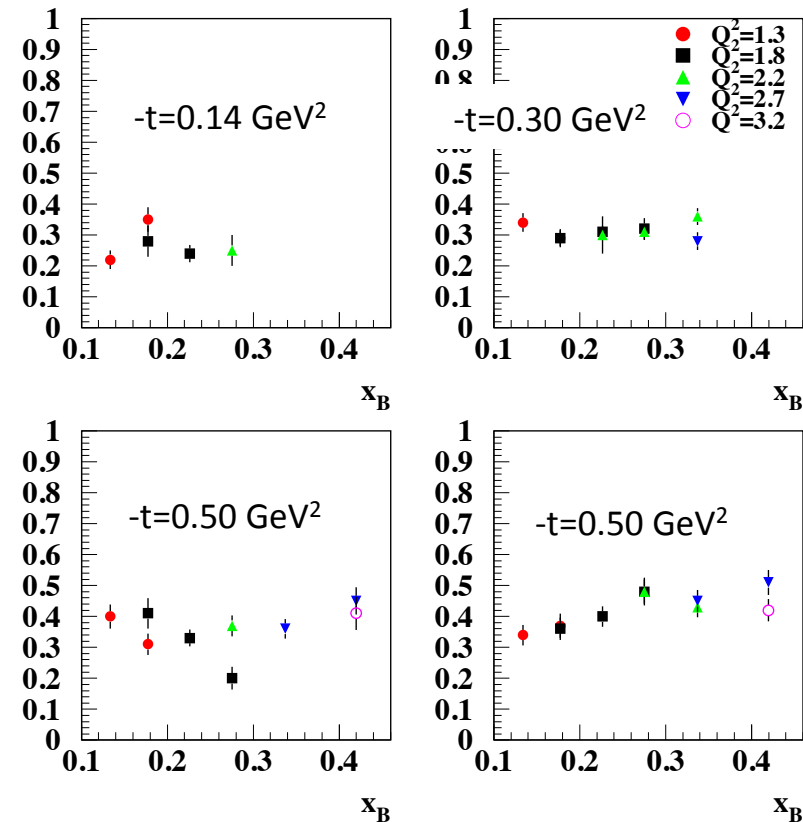
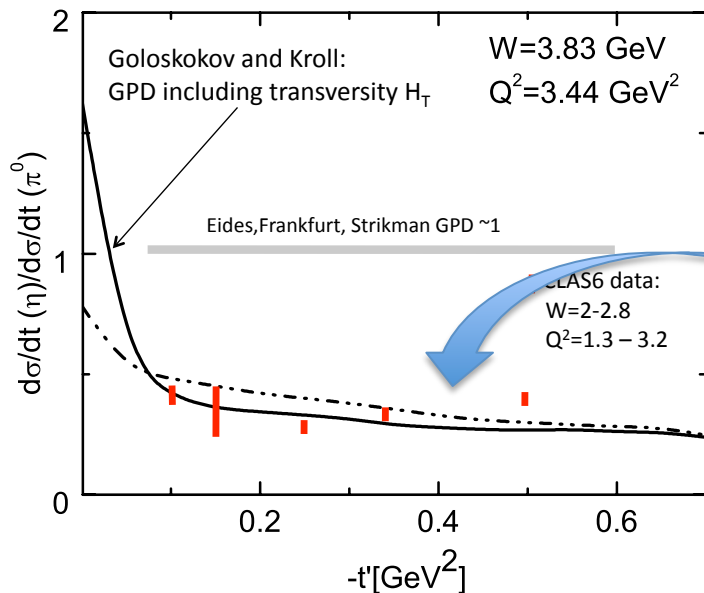


We are looking forward to extend the comparison with GPD-based model in the full kinematic domain of CLAS6

η/π^0 Ratio

$$\frac{\sigma(ep \rightarrow e\eta)}{\sigma(ep \rightarrow e\pi^0)}$$

- The dependence on the x_B and Q^2 is very weak.
- The ratio in the photoproduction is near 0.2-0.3 (very close to what we have at our smallest Q^2).
- Conventional GPD models predict this ratio to be around 1 (at low $-t$).
- **KG model** predicts this ratio to be $\sim 1/3$ at CLAS values of t



$$\bar{E}_T = 2\tilde{H}_T + E_T$$

Indication of large contributions from the GPD \bar{E}_T with the same same sign for u and d-quark parts

CLAS12

Luminosity $10^{35} \text{ cm}^2 \text{ s}^{-1}$

Forward Detector

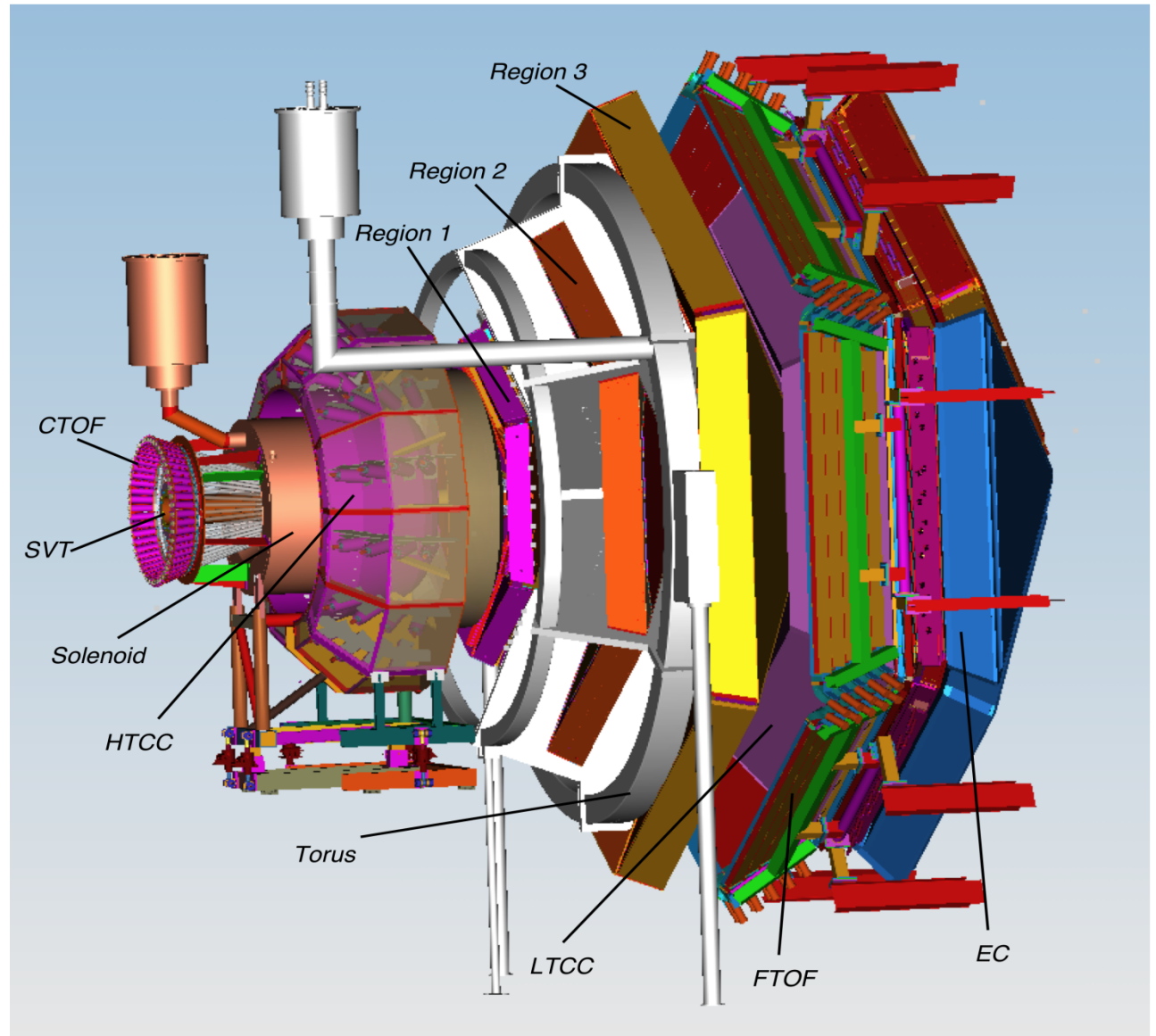
- TORUS magnet
- Forward SVT tracker
- HT Cherenkov Counter
- Drift chamber system
- LT Cherenkov Counter
- Forward ToF System
- Preshower calorimeter
- E.M. calorimeter

Central Detector

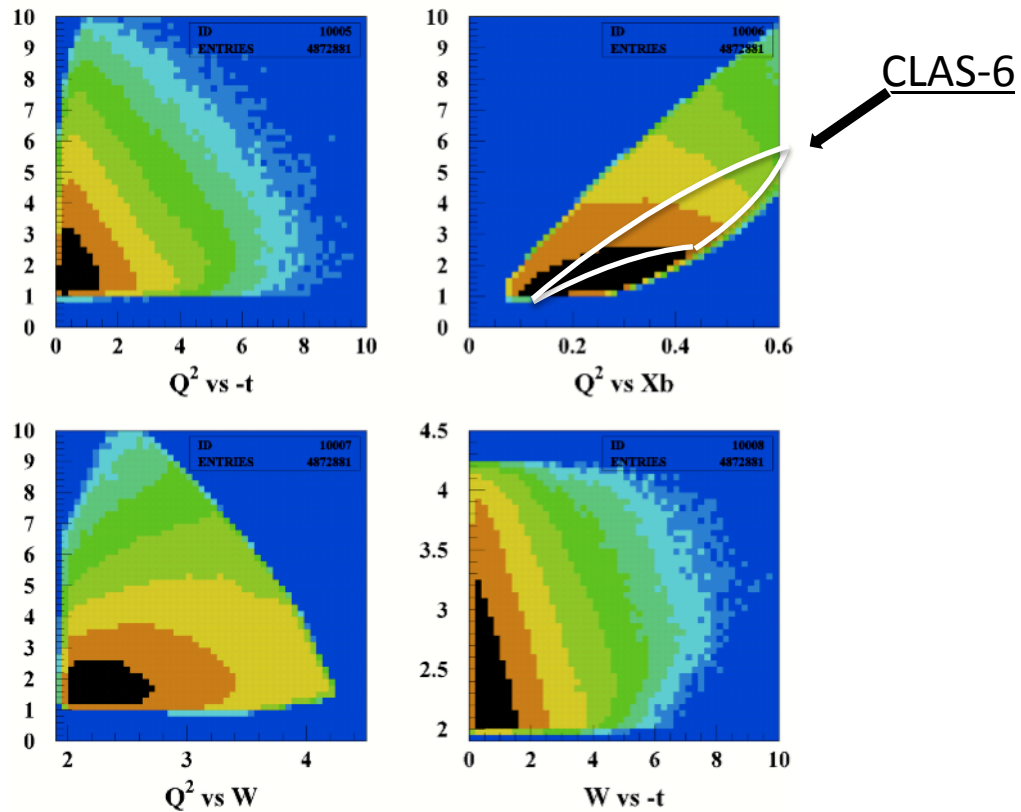
- SOLENOID magnet
- Barrel Silicon Tracker
- Central Time-of-Flight
- Polarized target (NSF)

Proposed upgrades

- Micromegas (CD)
- Neutron detector (CD)
- RICH detector (FD)
- Forward Tagger (FD)



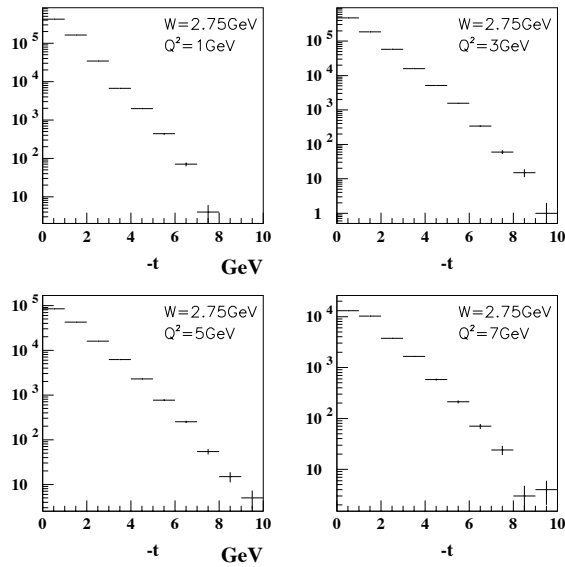
CLAS12 Kinematic Coverage



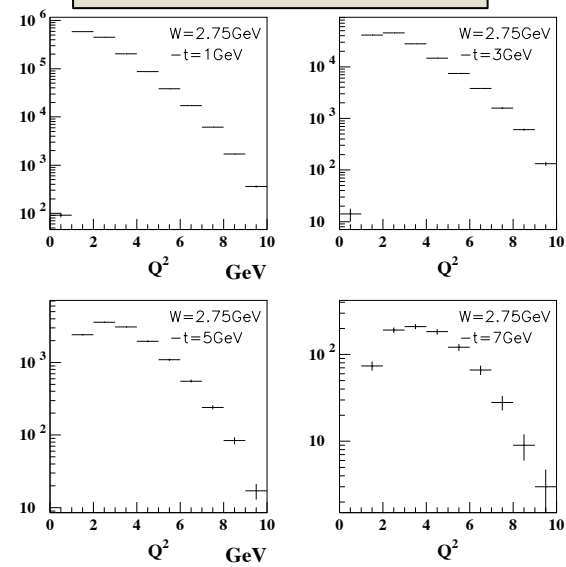
Statistics

$W=2.75 \pm 0.75 \text{ GeV}$

t-distribution
 $\Delta Q^2 = 2 \text{ GeV}^2$



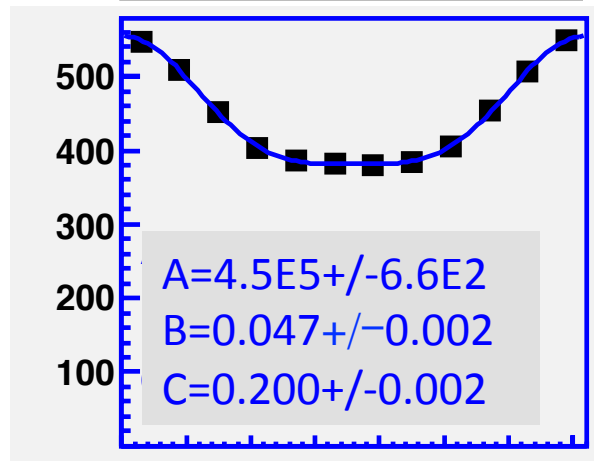
Q^2 -distribution
 $\Delta t = 2 \text{ GeV}^2$



Example of the Simulated cross section and asymmetry

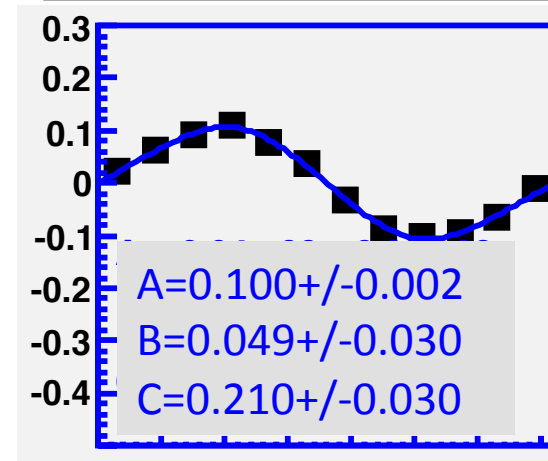
Simulated cross section

$$\sigma = A(1 + B \cos 2\varphi + C \cos \varphi)$$



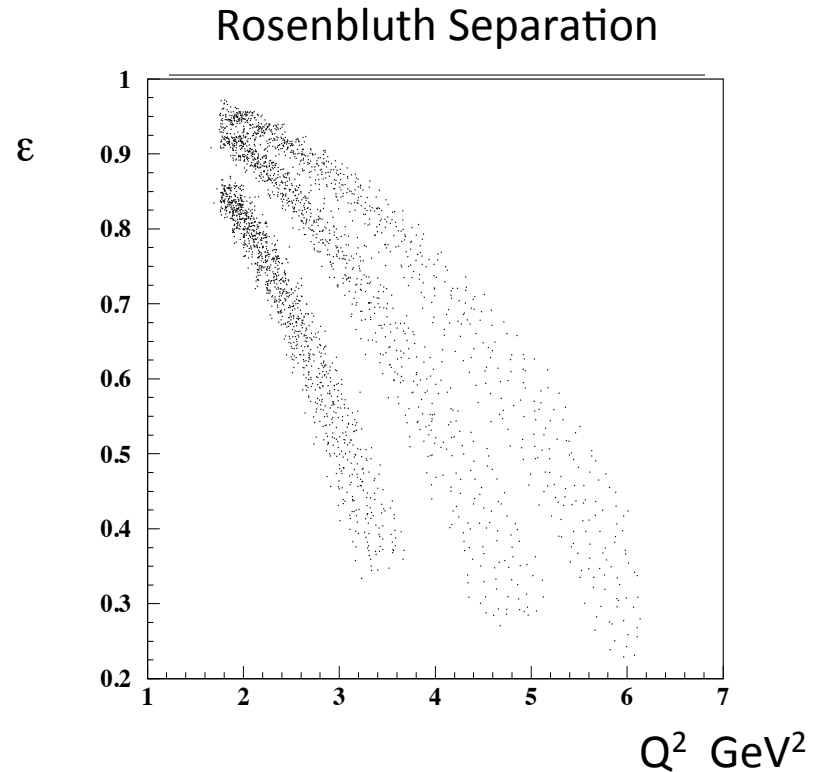
Simulated beam-spin asymmetry

$$\alpha = A \sin \varphi / (1 + B \cos 2\varphi + C \cos \varphi)$$



Anticipated systematic errors

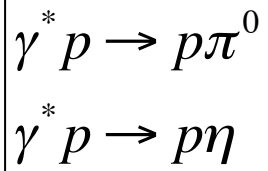
Source	Error
Acceptance	2.5 %
Beam Charge	0.2 %
Particle ID	1.0 %
Radiative Corrections	1.0 %
$\sigma_U = \sigma_T + \epsilon \sigma_L$	4.0 %
σ_L, σ_T	10-30 %



$R=0.4$
 $x_B=035\pm 0.5$



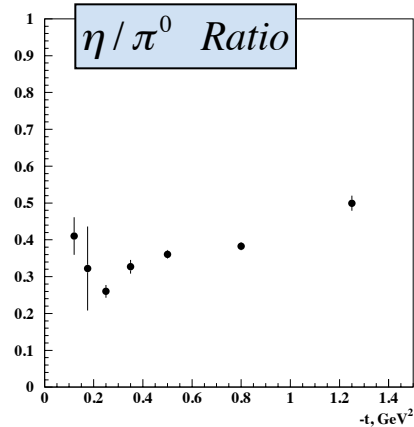
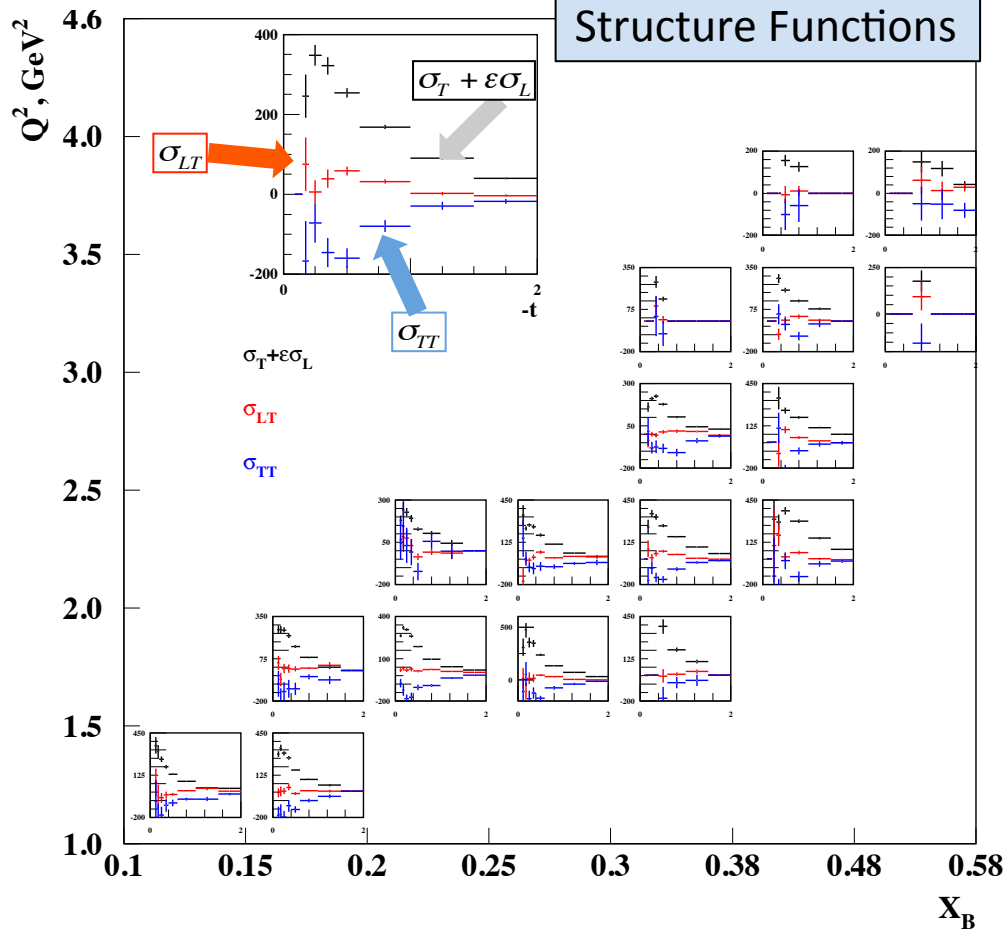
Q^2 GeV ²	3	3.5	4.5	5
$\Delta\sigma_T/\sigma_T$ %	33	16	28	18
$\Delta\sigma_L/\sigma_L$ %	20	13	23	19



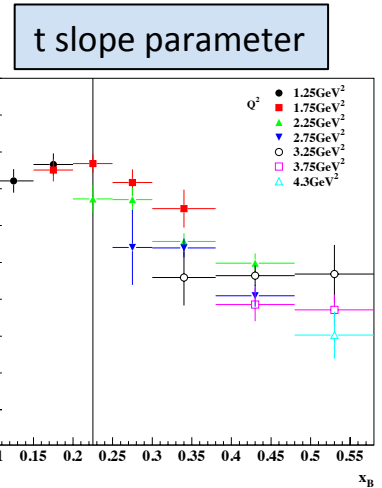
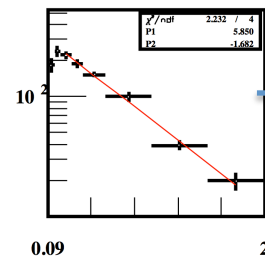
Going from 6 to 11 GeV

Reliable extraction of the structure functions for π^0 and η was demonstrated with CLAS6 experimental setup. These data and the new theoretical developments make the CLAS-12 experiment even more compelling

- Higher Q^2 – map the Q^2 evolution of structure functions
- Higher t range – backward pion production
- σ_T/σ_L separation



$$\frac{d\sigma}{dt}(\gamma^* p \rightarrow e p \pi^0) \propto e^{bt}$$



Summary

- The discovery of Generalized Parton Distributions has opened up a new and exciting avenue of hadron physics that needs exploration in dedicated experiments.
- Moderate to high energy, high luminosity, and large acceptance spectrometers are needed to measure GPDs in deeply virtual exclusive processes.
- The JLab 12 GeV Upgrade provides the tools to do this well and explore the nucleon at a much deeper level.

The Fin

$$\gamma^* p \rightarrow p\pi^0$$

$\sigma_U = \sigma_T + \epsilon\sigma_L$: Q^2 dependence

$$\sigma_U \sim 1/Q^3$$

- Factorization theorem states that in the limit $Q^2 \rightarrow \infty$ exclusive electroproduction of mesons is described by hard rescattering amplitude, generalized parton distributions (GPDs), and the distribution amplitude $\Phi(z)$ of the outgoing meson.
- The prove applies only to the case when the virtual photon has *longitudinal polarization*
- $Q^2 \rightarrow \infty$ $\sigma_L \sim 1/Q^6$, $\sigma_T/\sigma_L \sim 1/Q^2$
- We are not there yet!

