

Spectroscopic Data for Neutral Francium (Fr I)

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Energy levels and hyperfine structure constants have been compiled for the sixteen longest lived isotopes of francium ($Z=87$). For most isotopes with atomic weights in the range $199 \leq A \leq 232$ the only measurements made are for the $7s\ ^2S_{1/2}$ and $7p\ ^2P_{1/2,3/2}^o$ levels. Additional energy-level data are available for ^{210}Fr , ^{212}Fr , and ^{221}Fr . Wavelengths with classifications and transition probabilities are tabulated for ^{212}Fr . In addition, the ionization energy is included for isotopes for which a sufficient number of levels have been measured, ^{212}Fr and ^{221}Fr . © 2007 by the U.S. Secretary of Commerce on behalf of the United States. All rights reserved. [DOI: 10.1063/1.2719251]

Key words: Francium; energy levels; atomic spectra; wavelengths; wave numbers; wavelength tables; hyperfine structure.

CONTENTS

| | |
|--------------------------------|-----|
| 1. Introduction. | 497 |
| 2. Spectroscopic Data. | 498 |
| 3. Acknowledgement. | 506 |
| 4. References. | 506 |

List of Tables

| | |
|---|-----|
| 1. Isotopes of francium. | 497 |
| 2. Isotopic spectral data for the $7s$ and $7p$ levels. | 498 |
| 3. Isotopic spectral data for the $8p$ levels. | 498 |
| 4. Spectral lines of ^{212}Fr I. | 499 |
| 5. Energy levels of ^{212}Fr I. | 502 |
| 6. Energy levels of ^{221}Fr I. | 505 |
| 7. Energy levels of ^{210}Fr I. | 506 |
| 8. Lifetimes of energy levels of ^{210}Fr I. | 506 |

1. Introduction

Although the existence of francium and some of its chemical properties were predicted as early as 1870 by Mendeleev, the element was not actually observed until 1939, when Marguerite Perey of the Curie Institute in Paris discovered a decay product of ^{227}Ac with the chemical properties of an alkali metal. Later she named the element Francium after her native country. The isotope she observed, $^{223}_{87}\text{Fr}$, is the longest-lived isotope, with a half-life of 21.8 min, and is the only one occurring naturally. However, according to the 86th Edition of the *CRC Handbook*,¹ 36 isotopes are recognized, with atomic weights in the range $199 \leq A \leq 232$. Most have half-lives of a few seconds or less; those with longer half-

lives include those in Table 1 (the magnetic moments are given as the ratio to the nuclear magneton, which is $5.050\ 783\ 43(43) \times 10^{-27}\ \text{J T}^{-1}$).

Francium is the most unstable of the first 101 elements and its short half-life has made it difficult to measure its physical properties. Like all alkalis it is very reactive and electropositive and also has a low ionization energy. It has an atomic number of 87 and a melting point just above room temperature ($27.2\ ^\circ\text{C}$). There are few practical uses for francium. However, it is of considerable spectroscopic interest because, as the heaviest alkali metal, it is an excellent candidate for parity non-conservation measurements. Theoretical investigation of the transition amplitude for the parity-non-conserving $7s-8s$ transition has been done by Dzuba *et*

TABLE 1. Isotopes of francium

| Isotope | Atomic weight ^a | Half-life ^a (min) | Spin ^a | Nuclear magnetic moment ^b (μ/μ_N) |
|-------------------|----------------------------|---------------------------------|-------------------|---|
| ^{207}Fr | 206.996 9 | 0.247 | 9/2 | +3.89(9) |
| ^{208}Fr | 207.997 13 | 0.985 | 7 | -4.75(10) |
| ^{209}Fr | 208.995 92 | 0.833 | 9/2 | +3.95(8) |
| ^{210}Fr | 209.996 40 | 3.2 | 6 | +4.40(9) |
| ^{211}Fr | 210.995 53 | 3.10 | 9/2 | +4.00(8) |
| ^{212}Fr | 211.996 18 | 20. | 5 | +4.62(9) |
| ^{213}Fr | 212.996 17 | 0.577 | 9/2 | +4.02(8) |
| ^{220}Fr | 220.012 313 | 0.457 | 1 | -0.67(1) |
| ^{221}Fr | 221.014 25 | 4.8 | 5/2 | +1.58(3) |
| ^{222}Fr | 222.017 54 | 14.3 | 2 | +0.63(1) |
| ^{223}Fr | 223.019 731 | 21.8 | 3/2 | +1.17(2) |
| ^{224}Fr | 224.023 23 | 3.0 | 1 | +0.40(1) |
| ^{225}Fr | 225.025 61 | 3.9 | 3/2 | +1.07(2) |
| ^{226}Fr | 226.029 3 | 0.82 | 1 | +0.071(2) |
| ^{227}Fr | 227.031 8 | 2.48 | 1/2 | +1.50(3) |
| ^{228}Fr | 228.035 7 | 0.65 | 2 | -0.76(2) |
| ^{229}Fr | 229.038 4 | 0.83 | | |

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^{a)} See the *CRC Handbook*.¹

^{b)} See Ekström *et al.*^{9,10}

TABLE 2. Isotopic spectral data for the 7s and 7p levels

| Atomic mass | $7s\ ^2S_{1/2}$ | $7p\ ^2P_{1/2}^\circ$ | | $7p\ ^2P_{3/2}^\circ$ | | |
|-------------|-----------------|--------------------------------------|----------------|--------------------------------------|----------------|----------------|
| | HFS A (MHz) | Isotopic frequency shift (MHz) | HFS A (MHz) | Isotopic frequency shift (MHz) | HFS A (MHz) | HFS B (MHz) |
| 207 | 8 484(1) | | | 5 239(4) | 90.7(6) | -42(13) |
| 208 | 6 650.7(8) | | 874.8(3) | 5 003(3) | 72.4(5) | 1(10) |
| 209 | 8 606.7(9) | | 1127.9(2) | 3 133(2) | 93.3(5) | -62(5) |
| 210 | 7 195.1(4) | | 946.3(2) | 2603(1) | 78.0(2) | 51(4) |
| 211 | 8 713.9(8) | | 1142.1(2) | 901(3) | 94.9(3) | -51(7) |
| 212 | 9 064.2(2) | 0 | 1187(7) | 0 | 97.2(1) | -26.0(2) |
| 213 | 8 757.4(19) | | 1150(8) | -1 641.0(2) | 95.3(3) | -36.0(5) |
| 220 | -6 549.2(12) | | | -20 806.8(5) | -73.2(5) | -126.8(5) |
| 221 | 6 209.9(10) | -22452(1) | 808(12) | -23 570.0(2) | 65.5(6) | -264.0(8) |
| 222 | 3 070(3) | | | -26 262(3) | 33(1) | 133(9) |
| 223 | 7 654(2) | | | -27 922(2) | 83.3(9) | 308(3) |
| 224 | 3 876(1) | | | -30 891(1) | 42.1(7) | 136(1) |
| 225 | 6 980(8) | | | -32 297(6) | 77(3) | 346(13) |
| 226 | 699(4) | | | -34 401(1) | 7(1) | -356(4) |
| 227 | 20 458(4) | | | -38 352(2) | 316(2) | |
| 228 | -3 731(4) | | | -40 077(5) | -41(2) | 627(12) |

*al.*² and the tie-in between isotope shifts and parity non-conservation analysis has been discussed by Dzuba *et al.*³

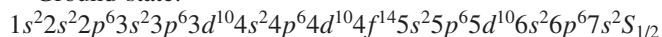
For this compilation of spectral data the literature has been reviewed and lists of the most accurate information have been assembled. The uncertainty for each value, as given by the original authors, is indicated in the tables; however, for some values the authors do not estimate the uncertainty, so we are unable to include that information. In the table of wavelengths, the wavelengths and their uncertainties are reported in units of ångströms. As all lines are between 2000 and 10 000 Å, air wavelengths are given, with the index of refraction determined by the three-term formula Peck and Reeder.⁴ The wave number of each transition is reported in reciprocal centimeters and its uncertainty can be determined from that of the wavelength. The calculated transition probabilities (A_{ki}) are given in units of inverse seconds. No estimate for their uncertainty was given by the authors. The lower level and upper level columns indicate the classification given for the transition.

The energy level tables contain the configuration, term, and J values of each energy level, using LS coupling to describe the configurations. For visual clarity, only the first member of the term has the configuration written out. The

level value and its uncertainty are given in the customary reciprocal centimeters. (As reported in Mohr and Taylor,⁵ the reciprocal centimeter is related to the SI unit for energy, the joule, by $1\text{ cm}^{-1} = 1.986\,445\,61(34) \times 10^{-23}\text{ J}$.) All hyperfine structure constants and isotope shifts are given in units of megahertz with the uncertainty in the last digit given in parentheses following the value. As is customary, the hyperfine splitting constant, A , is the magnetic dipole coefficient, whereas B is the electric quadrupole coefficient. The level reference and hyperfine reference refer to the source of the energy level value and hyperfine splitting constants, respectively.

2. Spectroscopic Data

Ground state:



Ionization energies:

$$^{212}\text{Fr} - 32\,848.872(9)\text{ cm}^{-1}; \quad 4.072\,740\,6(11)\text{ eV}$$

$$^{221}\text{Fr} - 32\,848.0(3)\text{ cm}^{-1}; \quad 4.072\,63(4)\text{ eV}$$

TABLE 3. Isotopic spectral data for the 8p levels

| Atomic mass | $8p\ ^2P_{1/2}^\circ$ | $8p\ ^2P_{3/2}^\circ$ | | |
|-------------|-----------------------|-----------------------------------|----------------|----------------|
| | HFS A (MHz) | Isotopic frequency shift (MHz) | HFS A (MHz) | HFS B (MHz) |
| 212 | 373.0(1) | 0 | 32.8(1) | -7.7(9) |
| 213 | | -1 615.0(3) | 31.6(1) | -7.0(25) |
| 220 | | -20 564.0(7) | -23.3(1) | 41.4(14) |
| 221 | | -23 298.0(8) | 22.4(1) | -85.7(8) |

Observing a sufficient quantity of francium to perform spectroscopic observations has been extremely difficult and the particular isotope produced depends on the technique utilized. The first spectral line reported was the D_2 resonance line observed at the European Organization of Nuclear Research (CERN) by Liberman *et al.*⁶ The francium produced at CERN, using bombardment of a uranium target by protons, is predominantly ^{212}Fr , but isotopes from $A=207$ to 228 have been observed by Coc *et al.*,^{7,8} Ekström *et al.*,^{9,10} and Liberman *et al.*¹¹ The hyperfine splitting constants for the $7s$ and $7p$ levels of these isotopes are summarized in Table 2 along with the isotopic shifts of the frequencies of the transition to the ground state. The shifts in frequency are measured with respect to the corresponding transitions in ^{212}Fr ($\delta\nu = \nu_{\text{isotope}} - \nu_{212}$). Thus a positive shift means that the level is farther from the ground state than the corresponding ^{212}Fr level.

Isotope shifts for the $7p\ ^2P_{3/2}^\circ$ levels and hyperfine splitting constant for them and the $7s\ ^2S_{1/2}$ levels are taken from Coc *et al.*^{7,8} and Duong *et al.*¹² The A values of the $7p\ ^2P_{1/2}^\circ$ levels of the isotopes from 208 to 212 were measured by Grossman *et al.*¹³ and the isotope shift for the $7p\ ^2P_{1/2}^\circ$ in

^{212}Fr was reported in Bauche *et al.*¹⁴ Duong *et al.*¹² measured the isotope shifts and hyperfine structure constants for the $8p\ ^2P^\circ$ levels listed in Table 3.

More extensive research using the ^{212}Fr produced by the CERN facilities has resulted in the measurement of the ns levels for $10 \leq n \leq 22$ and the nd levels for $8 \leq n \leq 20$ by Arnold *et al.*^{15,16} Values for the $7p$ and $8p$ levels have been determined by Bauche *et al.*¹⁴ and Duong *et al.*,¹² respectively. More recently, Biémont *et al.*¹⁷ augmented the experimental data by using the Ritz formula to predict all missing ns , np , and nd levels up to $n=30$. They also calculated the transition probabilities, which are listed in Table 4. The wavelengths given in Table 4 are calculated from the energy levels given in Table 5, as compiled in Biémont *et al.*;¹⁷ however, the $9s$ level value reported here is calculated from their Ritz formula because the value given in Table 2 of Biémont *et al.*¹⁷ is actually from a ^{210}Fr measurement. The ionization energy for ^{212}Fr and many of the hyperfine splitting constants were determined by Arnold *et al.*¹⁶ Splitting constants for the $7s$, $7p$, and $8p$ levels were determined by Duong *et al.*¹²

TABLE 4. Spectral lines of ^{212}Fr I

| λ_{air} (Å) | Uncertainty (Å) | σ (cm ⁻¹) | A_{ki} (s ⁻¹) | Lower level | Upper level |
|----------------------------|-----------------|------------------------------|-----------------------------|-----------------------|------------------------|
| 3086.287 | 0.005 | 32 391.99 | 8.00E+3 | $7s\ ^2S_{1/2}$ | $20p\ ^2P_{3/2}^\circ$ |
| 3086.843 | 0.005 | 32 386.15 | 8.01E+3 | $7s\ ^2S_{1/2}$ | $20p\ ^2P_{1/2}^\circ$ |
| 3092.514 | 0.005 | 32 326.77 | 1.00E+4 | $7s\ ^2S_{1/2}$ | $19p\ ^2P_{3/2}^\circ$ |
| 3093.197 | 0.005 | 32 319.63 | 9.82E+3 | $7s\ ^2S_{1/2}$ | $19p\ ^2P_{1/2}^\circ$ |
| 3100.211 | 0.005 | 32 246.51 | 1.23E+4 | $7s\ ^2S_{1/2}$ | $18p\ ^2P_{3/2}^\circ$ |
| 3101.063 | 0.005 | 32 237.65 | 1.23E+4 | $7s\ ^2S_{1/2}$ | $18p\ ^2P_{1/2}^\circ$ |
| 3109.885 | 0.005 | 32 146.20 | 1.57E+4 | $7s\ ^2S_{1/2}$ | $17p\ ^2P_{3/2}^\circ$ |
| 3110.966 | 0.005 | 32 135.03 | 1.57E+4 | $7s\ ^2S_{1/2}$ | $17p\ ^2P_{1/2}^\circ$ |
| 3122.284 | 0.005 | 32 018.55 | 2.10E+4 | $7s\ ^2S_{1/2}$ | $16p\ ^2P_{3/2}^\circ$ |
| 3123.684 | 0.005 | 32 004.20 | 2.11E+4 | $7s\ ^2S_{1/2}$ | $16p\ ^2P_{1/2}^\circ$ |
| 3138.547 | 0.005 | 31 852.65 | 2.81E+4 | $7s\ ^2S_{1/2}$ | $15p\ ^2P_{3/2}^\circ$ |
| 3140.409 | 0.005 | 31 833.76 | 2.81E+4 | $7s\ ^2S_{1/2}$ | $15p\ ^2P_{1/2}^\circ$ |
| 3160.492 | 0.005 | 31 631.49 | 4.00E+4 | $7s\ ^2S_{1/2}$ | $14p\ ^2P_{3/2}^\circ$ |
| 3163.046 | 0.005 | 31 605.95 | 3.91E+4 | $7s\ ^2S_{1/2}$ | $14p\ ^2P_{1/2}^\circ$ |
| 3191.165 | 0.005 | 31 327.46 | 5.81E+4 | $7s\ ^2S_{1/2}$ | $13p\ ^2P_{3/2}^\circ$ |
| 3194.810 | 0.005 | 31 291.72 | 5.81E+4 | $7s\ ^2S_{1/2}$ | $13p\ ^2P_{1/2}^\circ$ |
| 3236.029 | 0.005 | 30 893.16 | 9.16E+4 | $7s\ ^2S_{1/2}$ | $12p\ ^2P_{3/2}^\circ$ |
| 3241.504 | 0.005 | 30 840.98 | 9.15E+4 | $7s\ ^2S_{1/2}$ | $12p\ ^2P_{1/2}^\circ$ |
| 3305.752 | 0.005 | 30 241.60 | 1.56E+5 | $7s\ ^2S_{1/2}$ | $11p\ ^2P_{3/2}^\circ$ |
| 3314.578 | 0.006 | 30 161.07 | 1.56E+5 | $7s\ ^2S_{1/2}$ | $11p\ ^2P_{1/2}^\circ$ |
| 3423.900 | 0.006 | 29 198.09 | 3.04E+5 | $7s\ ^2S_{1/2}$ | $10p\ ^2P_{3/2}^\circ$ |
| 3439.675 | 0.006 | 29 064.18 | 3.02E+5 | $7s\ ^2S_{1/2}$ | $10p\ ^2P_{1/2}^\circ$ |
| 3653.102 | 0.007 | 27 366.20 | 7.52E+5 | $7s\ ^2S_{1/2}$ | $9p\ ^2P_{3/2}^\circ$ |
| 3686.510 | 0.007 | 27 118.21 | 7.24E+5 | $7s\ ^2S_{1/2}$ | $9p\ ^2P_{1/2}^\circ$ |
| 4225.655 | 0.009 | 23 658.31 | 2.82E+6 | $7s\ ^2S_{1/2}$ | $8p\ ^2P_{3/2}^\circ$ |
| 4325.361 | 0.009 | 23 112.96 | 2.64E+6 | $7s\ ^2S_{1/2}$ | $8p\ ^2P_{1/2}^\circ$ |
| 4946.157 | 0.002 | 20 212.074 | 1.67E+5 | $7p\ ^2P_{1/2}^\circ$ | $20d\ ^2D_{3/2}$ |
| 4959.144 | 0.002 | 20 159.143 | 2.00E+5 | $7p\ ^2P_{1/2}^\circ$ | $19d\ ^2D_{3/2}$ |
| 4969.031 | 0.002 | 20 119.035 | 4.57E+4 | $7p\ ^2P_{1/2}^\circ$ | $20s\ ^2S_{1/2}$ |
| 4974.988 | 0.002 | 20 094.945 | 2.39E+5 | $7p\ ^2P_{1/2}^\circ$ | $18d\ ^2D_{3/2}$ |
| 4987.192 | 0.002 | 20 045.771 | 5.59E+4 | $7p\ ^2P_{1/2}^\circ$ | $19s\ ^2S_{1/2}$ |
| 4994.600 | 0.002 | 20 016.040 | 2.98E+5 | $7p\ ^2P_{1/2}^\circ$ | $17d\ ^2D_{3/2}$ |
| 5009.918 | 0.002 | 19 954.842 | 6.97E+4 | $7p\ ^2P_{1/2}^\circ$ | $18s\ ^2S_{1/2}$ |

TABLE 4. Spectral lines of ^{212}Fr I—Continued

| λ_{air} (Å) | Uncertainty (Å) | σ (cm $^{-1}$) | A_{ki} (s $^{-1}$) | Lower level | Upper level |
|----------------------------|-----------------|------------------------|-----------------------|-------------------------------|--------------------------------|
| 5019.293 | 0.002 | 19 917.570 | 3.81E+5 | 7p $^2\text{P}_{1/2}^{\circ}$ | 16d $^2\text{D}_{3/2}$ |
| 5038.896 | 0.002 | 19 840.083 | 8.88E+4 | 7p $^2\text{P}_{1/2}^{\circ}$ | 17s $^2\text{S}_{1/2}$ |
| 5051.011 | 0.002 | 19 792.500 | 4.84E+5 | 7p $^2\text{P}_{1/2}^{\circ}$ | 15d $^2\text{D}_{3/2}$ |
| 5076.691 | 0.002 | 19 692.380 | 1.15E+5 | 7p $^2\text{P}_{1/2}^{\circ}$ | 16s $^2\text{S}_{1/2}$ |
| 5092.753 | 0.002 | 19 630.273 | 6.28E+5 | 7p $^2\text{P}_{1/2}^{\circ}$ | 14d $^2\text{D}_{3/2}$ |
| 5127.362 | 0.002 | 19 497.773 | 1.56E+5 | 7p $^2\text{P}_{1/2}^{\circ}$ | 15s $^2\text{S}_{1/2}$ |
| 5149.331 | 0.002 | 19 414.591 | 8.48E+5 | 7p $^2\text{P}_{1/2}^{\circ}$ | 13d $^2\text{D}_{3/2}$ |
| 5197.664 | 0.002 | 19 234.056 | 2.14E+5 | 7p $^2\text{P}_{1/2}^{\circ}$ | 14s $^2\text{S}_{1/2}$ |
| 5228.917 | 0.002 | 19 119.097 | 1.19E+6 | 7p $^2\text{P}_{1/2}^{\circ}$ | 12d $^2\text{D}_{3/2}$ |
| 5299.592 | 0.002 | 18 864.130 | 3.05E+5 | 7p $^2\text{P}_{1/2}^{\circ}$ | 13s $^2\text{S}_{1/2}$ |
| 5346.417 | 0.002 | 18 698.916 | 1.76E+6 | 7p $^2\text{P}_{1/2}^{\circ}$ | 11d $^2\text{D}_{3/2}$ |
| 5396.176 | 0.002 | 18 526.490 | 1.55E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 20d $^2\text{D}_{5/2}$ |
| 5396.469 | 0.002 | 18 525.485 | 2.62E+4 | 7p $^2\text{P}_{3/2}^{\circ}$ | 20d $^2\text{D}_{3/2}$ |
| 5411.578 | 0.002 | 18 473.763 | 1.86E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 19d $^2\text{D}_{5/2}$ |
| 5411.932 | 0.002 | 18 472.554 | 3.13E+4 | 7p $^2\text{P}_{3/2}^{\circ}$ | 19d $^2\text{D}_{3/2}$ |
| 5423.708 | 0.002 | 18 432.446 | 6.99E+4 | 7p $^2\text{P}_{3/2}^{\circ}$ | 20s $^2\text{S}_{1/2}$ |
| 5430.372 | 0.002 | 18 409.829 | 6.66E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 18d $^2\text{D}_{5/2}$ |
| 5430.806 | 0.002 | 18 408.356 | 3.73E+4 | 7p $^2\text{P}_{3/2}^{\circ}$ | 18d $^2\text{D}_{3/2}$ |
| 5445.352 | 0.002 | 18 359.182 | 8.73E+4 | 7p $^2\text{P}_{3/2}^{\circ}$ | 19s $^2\text{S}_{1/2}$ |
| 5453.642 | 0.002 | 18 331.277 | 2.77E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 17d $^2\text{D}_{5/2}$ |
| 5454.185 | 0.002 | 18 329.451 | 4.55E+4 | 7p $^2\text{P}_{3/2}^{\circ}$ | 17d $^2\text{D}_{3/2}$ |
| 5456.375 | 0.002 | 18 322.095 | 4.56E+5 | 7p $^2\text{P}_{1/2}^{\circ}$ | 12s $^2\text{S}_{1/2}$ |
| 5472.457 | 0.002 | 18 268.253 | 1.06E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 18s $^2\text{S}_{1/2}$ |
| 5482.954 | 0.002 | 18 233.276 | 3.45E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 16d $^2\text{D}_{5/2}$ |
| 5483.645 | 0.002 | 18 230.981 | 5.80E+4 | 7p $^2\text{P}_{3/2}^{\circ}$ | 16d $^2\text{D}_{3/2}$ |
| 5507.052 | 0.002 | 18 153.494 | 1.35E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 17s $^2\text{S}_{1/2}$ |
| 5520.637 | 0.002 | 18 108.823 | 4.48E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 15d $^2\text{D}_{5/2}$ |
| 5521.524 | 0.002 | 18 105.911 | 7.37E+4 | 7p $^2\text{P}_{3/2}^{\circ}$ | 15d $^2\text{D}_{3/2}$ |
| 5531.716 | 0.002 | 18 072.553 | 2.67E+6 | 7p $^2\text{P}_{1/2}^{\circ}$ | 10d $^2\text{D}_{3/2}$ |
| 5552.227 | 0.002 | 18 005.791 | 1.75E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 16s $^2\text{S}_{1/2}$ |
| 5570.255 | 0.002 | 17 947.516 | 1.74E+6 | 7p $^2\text{P}_{3/2}^{\circ}$ | 14d $^2\text{D}_{5/2}$ |
| 5571.444 | 0.002 | 17 943.684 | 9.77E+4 | 7p $^2\text{P}_{3/2}^{\circ}$ | 14d $^2\text{D}_{3/2}$ |
| 5612.892 | 0.002 | 17 811.184 | 2.37E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 15s $^2\text{S}_{1/2}$ |
| 5637.589 | 0.002 | 17 733.157 | 2.35E+6 | 7p $^2\text{P}_{3/2}^{\circ}$ | 13d $^2\text{D}_{5/2}$ |
| 5639.228 | 0.002 | 17 728.002 | 1.32E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 13d $^2\text{D}_{3/2}$ |
| 5697.247 | 0.002 | 17 547.467 | 3.25E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 14s $^2\text{S}_{1/2}$ |
| 5718.746 | 0.002 | 17 481.500 | 7.38E+5 | 7p $^2\text{P}_{1/2}^{\circ}$ | 11s $^2\text{S}_{1/2}$ |
| 5732.468 | 0.002 | 17 439.657 | 1.09E+6 | 7p $^2\text{P}_{3/2}^{\circ}$ | 12d $^2\text{D}_{5/2}$ |
| 5734.818 | 0.002 | 17 432.508 | 1.80E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 12d $^2\text{D}_{3/2}$ |
| 5819.941 | 0.002 | 17 177.541 | 4.60E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 13s $^2\text{S}_{1/2}$ |
| 5853.491 | 0.002 | 17 079.088 | 4.44E+6 | 7p $^2\text{P}_{1/2}^{\circ}$ | 9d $^2\text{D}_{3/2}$ |
| 5872.900 | 0.002 | 17 022.645 | 1.58E+6 | 7p $^2\text{P}_{3/2}^{\circ}$ | 11d $^2\text{D}_{5/2}$ |
| 5876.462 | 0.002 | 17 012.327 | 2.65E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 11d $^2\text{D}_{3/2}$ |
| 6009.574 | 0.002 | 16 635.506 | 6.84E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 13s $^2\text{S}_{1/2}$ |
| 6095.276 | 0.002 | 16 401.607 | 3.56E+6 | 7p $^2\text{P}_{3/2}^{\circ}$ | 10d $^2\text{D}_{5/2}$ |
| 6101.095 | 0.002 | 16 385.964 | 3.99E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 10d $^2\text{D}_{3/2}$ |
| 6185.60 | 0.02 | 16 162.12 | 7.93E+2 | 6d $^2\text{D}_{3/2}$ | 20p $^2\text{P}_{3/2}^{\circ}$ |
| 6187.83 | 0.02 | 16 156.28 | 7.94E+3 | 6d $^2\text{D}_{3/2}$ | 20p $^2\text{P}_{1/2}^{\circ}$ |
| 6210.66 | 0.02 | 16 096.90 | 9.90E+2 | 6d $^2\text{D}_{3/2}$ | 19p $^2\text{P}_{3/2}^{\circ}$ |
| 6213.41 | 0.02 | 16 089.76 | 9.91E+3 | 6d $^2\text{D}_{3/2}$ | 19p $^2\text{P}_{1/2}^{\circ}$ |
| 6219.813 | 0.002 | 16 073.208 | 1.33E+6 | 7p $^2\text{P}_{1/2}^{\circ}$ | 10s $^2\text{S}_{1/2}$ |
| 6241.78 | 0.02 | 16 016.64 | 1.23E+3 | 6d $^2\text{D}_{3/2}$ | 18p $^2\text{P}_{3/2}^{\circ}$ |
| 6245.24 | 0.02 | 16 007.78 | 1.21E+4 | 6d $^2\text{D}_{3/2}$ | 18p $^2\text{P}_{1/2}^{\circ}$ |
| 6263.01 | 0.02 | 15 962.35 | 6.89E+3 | 6d $^2\text{D}_{5/2}$ | 20p $^2\text{P}_{3/2}^{\circ}$ |
| 6281.12 | 0.02 | 15 916.33 | 1.53E+3 | 6d $^2\text{D}_{3/2}$ | 17p $^2\text{P}_{3/2}^{\circ}$ |
| 6285.53 | 0.02 | 15 905.16 | 1.54E+4 | 6d $^2\text{D}_{3/2}$ | 17p $^2\text{P}_{1/2}^{\circ}$ |
| 6288.70 | 0.02 | 15 897.13 | 8.60E+3 | 6d $^2\text{D}_{5/2}$ | 19p $^2\text{P}_{3/2}^{\circ}$ |
| 6320.62 | 0.02 | 15 816.87 | 1.05E+4 | 6d $^2\text{D}_{5/2}$ | 18p $^2\text{P}_{3/2}^{\circ}$ |

TABLE 4. Spectral lines of ^{212}Fr I—Continued

| λ_{air} (Å) | Uncertainty (Å) | σ (cm $^{-1}$) | A_{ki} (s $^{-1}$) | Lower level | Upper level |
|----------------------------|-----------------|------------------------|-----------------------|-------------------------------|--------------------------------|
| 6329.403 | 0.003 | 15 794.911 | 1.10E+6 | 7p $^2\text{P}_{3/2}^{\circ}$ | 11s $^2\text{S}_{1/2}$ |
| 6331.90 | 0.02 | 15 788.68 | 1.99E+3 | 6d $^2\text{D}_{3/2}$ | 16p $^2\text{P}_{3/2}^{\circ}$ |
| 6337.66 | 0.02 | 15 774.33 | 1.99E+4 | 6d $^2\text{D}_{3/2}$ | 16p $^2\text{P}_{1/2}^{\circ}$ |
| 6360.96 | 0.02 | 15 716.56 | 1.33E+4 | 6d $^2\text{D}_{5/2}$ | 17p $^2\text{P}_{3/2}^{\circ}$ |
| 6399.14 | 0.02 | 15 622.78 | 2.63E+3 | 6d $^2\text{D}_{3/2}$ | 15p $^2\text{P}_{3/2}^{\circ}$ |
| 6406.89 | 0.02 | 15 603.89 | 2.63E+4 | 6d $^2\text{D}_{3/2}$ | 15p $^2\text{P}_{1/2}^{\circ}$ |
| 6413.04 | 0.02 | 15 588.91 | 1.73E+4 | 6d $^2\text{D}_{5/2}$ | 16p $^2\text{P}_{3/2}^{\circ}$ |
| 6482.03 | 0.02 | 15 423.01 | 2.28E+4 | 6d $^2\text{D}_{5/2}$ | 15p $^2\text{P}_{3/2}^{\circ}$ |
| 6484.210 | 0.003 | 15 417.819 | 3.91E+6 | 7p $^2\text{P}_{3/2}^{\circ}$ | 9d $^2\text{D}_{5/2}$ |
| 6491.03 | 0.02 | 15 401.62 | 3.61E+3 | 6d $^2\text{D}_{3/2}$ | 14p $^2\text{P}_{3/2}^{\circ}$ |
| 6494.876 | 0.003 | 15 392.499 | 6.41E+5 | 7p $^2\text{P}_{3/2}^{\circ}$ | 9d $^2\text{D}_{3/2}$ |
| 6501.81 | 0.02 | 15 376.08 | 3.52E+4 | 6d $^2\text{D}_{3/2}$ | 14p $^2\text{P}_{1/2}^{\circ}$ |
| 6507.242 | 0.003 | 15 363.248 | 8.04E+6 | 7p $^2\text{P}_{1/2}^{\circ}$ | 8d $^2\text{D}_{3/2}$ |
| 6576.33 | 0.02 | 15 201.85 | 3.06E+4 | 6d $^2\text{D}_{5/2}$ | 14p $^2\text{P}_{3/2}^{\circ}$ |
| 6621.74 | 0.03 | 15 097.59 | 5.01E+3 | 6d $^2\text{D}_{3/2}$ | 13p $^2\text{P}_{3/2}^{\circ}$ |
| 6637.46 | 0.03 | 15 061.85 | 5.00E+4 | 6d $^2\text{D}_{3/2}$ | 13p $^2\text{P}_{1/2}^{\circ}$ |
| 6710.54 | 0.03 | 14 897.82 | 4.35E+4 | 6d $^2\text{D}_{5/2}$ | 13p $^2\text{P}_{3/2}^{\circ}$ |
| 6817.87 | 0.03 | 14 663.29 | 7.49E+3 | 6d $^2\text{D}_{3/2}$ | 12p $^2\text{P}_{3/2}^{\circ}$ |
| 6842.22 | 0.03 | 14 611.11 | 7.46E+4 | 6d $^2\text{D}_{3/2}$ | 12p $^2\text{P}_{1/2}^{\circ}$ |
| 6912.04 | 0.03 | 14 463.52 | 6.50E+4 | 6d $^2\text{D}_{5/2}$ | 12p $^2\text{P}_{3/2}^{\circ}$ |
| 6948.987 | 0.003 | 14 386.619 | 1.90E+6 | 7p $^2\text{P}_{3/2}^{\circ}$ | 10s $^2\text{S}_{1/2}$ |
| 7134.91 | 0.03 | 14 011.73 | 1.16E+4 | 6d $^2\text{D}_{3/2}$ | 11p $^2\text{P}_{3/2}^{\circ}$ |
| 7176.16 | 0.03 | 13 931.20 | 1.15E+5 | 6d $^2\text{D}_{3/2}$ | 11p $^2\text{P}_{1/2}^{\circ}$ |
| 7179.866 | 0.001 | 13 923.998 | 4.78E+7 | 7s $^2\text{S}_{1/2}$ | 7p $^2\text{P}_{3/2}^{\circ}$ |
| 7238.11 | 0.03 | 13 811.96 | 1.01E+5 | 6d $^2\text{D}_{5/2}$ | 11p $^2\text{P}_{3/2}^{\circ}$ |
| 7285.892 | 0.004 | 13 721.375 | 6.93E+6 | 7p $^2\text{P}_{3/2}^{\circ}$ | 8d $^2\text{D}_{5/2}$ |
| 7309.713 | 0.004 | 13 676.659 | 1.13E+6 | 7p $^2\text{P}_{3/2}^{\circ}$ | 8d $^2\text{D}_{3/2}$ |
| 7441.98 | 0.04 | 13 433.59 | 2.75E+6 | 7p $^2\text{P}_{1/2}^{\circ}$ | 9s $^2\text{S}_{1/2}$ |
| 7709.04 | 0.04 | 12 968.22 | 1.99E+4 | 6d $^2\text{D}_{3/2}$ | 10p $^2\text{P}_{3/2}^{\circ}$ |
| 7789.47 | 0.04 | 12 834.31 | 1.95E+5 | 6d $^2\text{D}_{3/2}$ | 10p $^2\text{P}_{1/2}^{\circ}$ |
| 7829.65 | 0.04 | 12 768.45 | 1.72E+5 | 6d $^2\text{D}_{5/2}$ | 10p $^2\text{P}_{3/2}^{\circ}$ |
| 7901.71 | 0.04 | 12 652.01 | 6.55E+3 | 8s $^2\text{S}_{1/2}$ | 20p $^2\text{P}_{3/2}^{\circ}$ |
| 7905.36 | 0.04 | 12 646.17 | 6.56E+3 | 8s $^2\text{S}_{1/2}$ | 20p $^2\text{P}_{1/2}^{\circ}$ |
| 7942.65 | 0.04 | 12 586.79 | 7.98E+3 | 8s $^2\text{S}_{1/2}$ | 19p $^2\text{P}_{3/2}^{\circ}$ |
| 7947.16 | 0.04 | 12 579.65 | 7.99E+3 | 8s $^2\text{S}_{1/2}$ | 19p $^2\text{P}_{1/2}^{\circ}$ |
| 7993.62 | 0.04 | 12 506.53 | 9.92E+3 | 8s $^2\text{S}_{1/2}$ | 18p $^2\text{P}_{3/2}^{\circ}$ |
| 7999.29 | 0.04 | 12 497.67 | 9.93E+3 | 8s $^2\text{S}_{1/2}$ | 18p $^2\text{P}_{1/2}^{\circ}$ |
| 8058.26 | 0.04 | 12 406.22 | 1.29E+4 | 8s $^2\text{S}_{1/2}$ | 17p $^2\text{P}_{3/2}^{\circ}$ |
| 8065.52 | 0.04 | 12 395.05 | 1.29E+4 | 8s $^2\text{S}_{1/2}$ | 17p $^2\text{P}_{1/2}^{\circ}$ |
| 8142.03 | 0.04 | 12 278.57 | 1.70E+4 | 8s $^2\text{S}_{1/2}$ | 16p $^2\text{P}_{3/2}^{\circ}$ |
| 8151.56 | 0.04 | 12 264.22 | 1.66E+4 | 8s $^2\text{S}_{1/2}$ | 16p $^2\text{P}_{1/2}^{\circ}$ |
| 8169.418 | 0.002 | 12 237.409 | 3.22E+7 | 7s $^2\text{S}_{1/2}$ | 7p $^2\text{P}_{1/2}^{\circ}$ |
| 8253.55 | 0.04 | 12 112.67 | 2.28E+4 | 8s $^2\text{S}_{1/2}$ | 15p $^2\text{P}_{3/2}^{\circ}$ |
| 8266.44 | 0.04 | 12 093.78 | 2.28E+4 | 8s $^2\text{S}_{1/2}$ | 15p $^2\text{P}_{1/2}^{\circ}$ |
| 8326.45 | 0.02 | 12 006.62 | 1.66E+7 | 7p $^2\text{P}_{1/2}^{\circ}$ | 7d $^2\text{D}_{3/2}$ |
| 8407.05 | 0.04 | 11 891.51 | 3.18E+4 | 8s $^2\text{S}_{1/2}$ | 14p $^2\text{P}_{3/2}^{\circ}$ |
| 8425.15 | 0.04 | 11 865.97 | 3.17E+4 | 8s $^2\text{S}_{1/2}$ | 14p $^2\text{P}_{1/2}^{\circ}$ |
| 8510.47 | 0.04 | 11 747.00 | 3.66E+6 | 7p $^2\text{P}_{3/2}^{\circ}$ | 9s $^2\text{S}_{1/2}$ |
| 8627.63 | 0.04 | 11 587.48 | 4.68E+4 | 8s $^2\text{S}_{1/2}$ | 13p $^2\text{P}_{3/2}^{\circ}$ |
| 8654.33 | 0.04 | 11 551.74 | 4.66E+4 | 8s $^2\text{S}_{1/2}$ | 13p $^2\text{P}_{1/2}^{\circ}$ |
| 8963.59 | 0.05 | 11 153.18 | 7.53E+4 | 8s $^2\text{S}_{1/2}$ | 12p $^2\text{P}_{3/2}^{\circ}$ |
| 8977.15 | 0.05 | 11 136.33 | 3.85E+4 | 6d $^2\text{D}_{3/2}$ | 9p $^2\text{P}_{3/2}^{\circ}$ |
| 9005.72 | 0.05 | 11 101.00 | 7.31E+4 | 8s $^2\text{S}_{1/2}$ | 12p $^2\text{P}_{1/2}^{\circ}$ |
| 9141.13 | 0.05 | 10 936.56 | 3.31E+5 | 6d $^2\text{D}_{5/2}$ | 9p $^2\text{P}_{3/2}^{\circ}$ |
| 9181.62 | 0.05 | 10 888.34 | 3.61E+5 | 6d $^2\text{D}_{3/2}$ | 9p $^2\text{P}_{1/2}^{\circ}$ |
| 9519.73 | 0.05 | 10 501.62 | 1.30E+5 | 8s $^2\text{S}_{1/2}$ | 11p $^2\text{P}_{3/2}^{\circ}$ |
| 9593.29 | 0.05 | 10 421.09 | 1.29E+5 | 8s $^2\text{S}_{1/2}$ | 11p $^2\text{P}_{1/2}^{\circ}$ |
| 9604.50 | 0.03 | 10 408.93 | 1.29E+7 | 7p $^2\text{P}_{3/2}^{\circ}$ | 7d $^2\text{D}_{5/2}$ |

TABLE 4. Spectral lines of ^{212}Fr I—Continued

| λ_{air} (Å) | Uncertainty (Å) | σ (cm $^{-1}$) | A_{ki} (s $^{-1}$) | Lower level | Upper level |
|----------------------------|-----------------|------------------------|-----------------------|--------------------------|------------------|
| 9687.24 | 0.03 | 10 320.03 | 2.09E+6 | $7p \ ^2P_{3/2}^{\circ}$ | $7d \ ^2D_{3/2}$ |

TABLE 5. Energy levels of ^{212}Fr I

| Configuration | Term | J | Level (cm $^{-1}$) | Uncertainty (cm $^{-1}$) | Level reference | Hyperfine constants | | Hyperfine reference |
|---------------|---------------|-----|---------------------|---------------------------|-----------------|---------------------|----------|---------------------|
| | | | | | | A (MHz) | B (MHz) | |
| $7s$ | 2S | 1/2 | 0.000 | 0.002 | 16 | 9064.4(15) | | 12 |
| $7p$ | $^2P^{\circ}$ | 1/2 | 12 237.409 | 0.002 | 14 | 1187(7) | | 12 |
| | | 3/2 | 13 923.998 | 0.002 | 14 | 97.2(1) | -26.0(2) | 12 |
| $6d$ | 2D | 3/2 | 16 229.87 | 0.03 | 17 | | | |
| | | 5/2 | 16 429.64 | 0.03 | 17 | | | |
| $8s$ | 2S | 1/2 | 19 739.98 | 0.03 | 17 | | | |
| $8p$ | $^2P^{\circ}$ | 1/2 | 23 112.960 | 0.005 | 12 | 373.0(1) | | 12 |
| | | 3/2 | 23 658.306 | 0.004 | 12 | 32.8(1) | -7.7(9) | 12 |
| $7d$ | 2D | 3/2 | 24 244.03 | 0.03 | 17 | | | |
| | | 5/2 | 24 332.93 | 0.03 | 17 | | | |
| $9s$ | 2S | 1/2 | 25 671.00 | 0.04 | 17 | | | |
| $9p$ | $^2P^{\circ}$ | 1/2 | 27 118.21 | 0.05 | 17 | | | |
| | | 3/2 | 27 366.20 | 0.05 | 17 | | | |
| $8d$ | 2D | 3/2 | 27 600.657 | 0.007 | 16 | 13.0(6) | | 16 |
| | | 5/2 | 27 645.373 | 0.007 | 16 | -7.2(6) | | 16 |
| $10s$ | 2S | 1/2 | 28 310.617 | 0.006 | 16 | 401(5) | | 16 |
| $10p$ | $^2P^{\circ}$ | 1/2 | 29 064.18 | 0.05 | 17 | | | |
| | | 3/2 | 29 198.09 | 0.05 | 17 | | | |
| $9d$ | 2D | 3/2 | 29 316.497 | 0.007 | 16 | 7.1(7) | | 16 |
| | | 5/2 | 29 341.817 | 0.007 | 16 | -3.6(4) | | 16 |
| $11s$ | 2S | 1/2 | 29 718.909 | 0.006 | 16 | 225(3) | | 16 |
| $11p$ | $^2P^{\circ}$ | 1/2 | 30 161.07 | 0.05 | 17 | | | |
| | | 3/2 | 30 241.60 | 0.05 | 17 | | | |
| $10d$ | 2D | 3/2 | 30 309.962 | 0.006 | 15 | | | |
| | | 5/2 | 30 325.605 | 0.006 | 15 | | | |
| $12s$ | 2S | 1/2 | 30 559.504 | 0.006 | 15 | | | |
| $12p$ | $^2P^{\circ}$ | 1/2 | 30 840.98 | 0.05 | 17 | | | |
| | | 3/2 | 30 893.16 | 0.05 | 17 | | | |
| $11d$ | 2D | 3/2 | 30 936.325 | 0.006 | 15 | | | |
| | | 5/2 | 30 946.643 | 0.006 | 15 | | | |
| $13s$ | 2S | 1/2 | 31 101.539 | 0.006 | 15 | | | |
| $13p$ | $^2P^{\circ}$ | 1/2 | 31 291.72 | 0.05 | 17 | | | |
| | | 3/2 | 31 327.46 | 0.05 | 17 | | | |
| $12d$ | 2D | 3/2 | 31 356.506 | 0.006 | 15 | | | |
| | | 5/2 | 31 363.655 | 0.006 | 15 | | | |
| $14s$ | 2S | 1/2 | 31 471.465 | 0.006 | 15 | | | |

TABLE 5. Energy levels of ^{212}Fr I—Continued

| Configuration | Term | J | Level (cm^{-1}) | Uncertainty (cm^{-1}) | Level reference | Hyperfine constants | | Hyperfine reference |
|---------------|--------------------|-----|-------------------------------|-------------------------------------|--------------------|---------------------|---------|------------------------|
| | | | | | | A (MHz) | B (MHz) | |
| 14p | $^2\text{P}^\circ$ | 1/2 | 31 605.95 | 0.05 | 17 | | | |
| | | 3/2 | 31 631.49 | 0.05 | 17 | | | |
| 13d | ^2D | 3/2 | 31 652.000 | 0.006 | 15 | | | |
| | | 5/2 | 31 657.155 | 0.006 | 15 | | | |
| 15s | ^2S | 1/2 | 31 735.182 | 0.006 | 15 | | | |
| 15p | $^2\text{P}^\circ$ | 1/2 | 31 833.76 | 0.05 | 17 | | | |
| | | 3/2 | 31 852.65 | 0.05 | 17 | | | |
| 14d | ^2D | 3/2 | 31 867.682 | 0.006 | 15 | | | |
| | | 5/2 | 31 871.514 | 0.006 | 15 | | | |
| 16s | ^2S | 1/2 | 31 929.789 | 0.006 | 15 | | | |
| 16p | $^2\text{P}^\circ$ | 1/2 | 32 004.20 | 0.05 | 17 | | | |
| | | 3/2 | 32 018.55 | 0.05 | 17 | | | |
| 15d | ^2D | 3/2 | 32 029.909 | 0.006 | 15 | | | |
| | | 5/2 | 32 032.821 | 0.006 | 15 | | | |
| 17s | ^2S | 1/2 | 32 077.492 | 0.006 | 15 | | | |
| 17p | $^2\text{P}^\circ$ | 1/2 | 32 135.03 | 0.05 | 17 | | | |
| | | 3/2 | 32 146.20 | 0.05 | 17 | | | |
| 16d | ^2D | 3/2 | 32 154.979 | 0.006 | 15 | | | |
| | | 5/2 | 32 157.274 | 0.006 | 15 | | | |
| 18s | ^2S | 1/2 | 32 192.251 | 0.006 | 15 | | | |
| 18p | $^2\text{P}^\circ$ | 1/2 | 32 237.65 | 0.05 | 17 | | | |
| | | 3/2 | 32 246.51 | 0.05 | 17 | | | |
| 17d | ^2D | 3/2 | 32 253.449 | 0.006 | 15 | | | |
| | | 5/2 | 32 255.275 | 0.006 | 15 | | | |
| 19s | ^2S | 1/2 | 32 283.180 | 0.006 | 15 | | | |
| 19p | $^2\text{P}^\circ$ | 1/2 | 32 319.63 | 0.05 | 17 | | | |
| | | 3/2 | 32 326.77 | 0.05 | 17 | | | |
| 18d | ^2D | 3/2 | 32 332.354 | 0.006 | 15 | | | |
| | | 5/2 | 32 333.827 | 0.006 | 15 | | | |
| 20s | ^2S | 1/2 | 32 356.444 | 0.006 | 15 | | | |
| 20p | $^2\text{P}^\circ$ | 1/2 | 32 386.15 | 0.05 | 17 | | | |
| | | 3/2 | 32 391.99 | 0.05 | 17 | | | |
| 19d | ^2D | 3/2 | 32 396.552 | 0.006 | 15 | | | |
| | | 5/2 | 32 397.761 | 0.006 | 15 | | | |
| 21s | ^2S | 1/2 | 32 416.340 | 0.006 | 15 | | | |
| 21p | $^2\text{P}^\circ$ | 1/2 | 32 440.87 | 0.05 | 17 | | | |
| | | 3/2 | 32 445.71 | 0.05 | 17 | | | |
| 20d | ^2D | 3/2 | 32 449.483 | 0.006 | 15 | | | |
| | | 5/2 | 32 450.488 | 0.006 | 15 | | | |
| 22s | ^2S | 1/2 | 32 465.937 | 0.006 | 15 | | | |

TABLE 5. Energy levels of ^{212}Fr I—Continued

| Configuration | Term | J | Level (cm^{-1}) | Uncertainty (cm^{-1}) | Level reference | Hyperfine constants | | Hyperfine reference |
|---------------|--------------------|-----|-------------------------------|-------------------------------------|--------------------|---------------------|---------|------------------------|
| | | | | | | A (MHz) | B (MHz) | |
| 22p | $^2\text{P}^\circ$ | 1/2 | 32 486.43 | 0.05 | 17 | | | |
| | | 3/2 | 32 490.48 | 0.05 | 17 | | | |
| 21d | ^2D | 3/2 | 32 493.64 | 0.03 | 17 | | | |
| | | 5/2 | 32 494.48 | 0.03 | 17 | | | |
| 23s | ^2S | 1/2 | 32 507.47 | 0.03 | 17 | | | |
| 23p | $^2\text{P}^\circ$ | 1/2 | 32 524.76 | 0.05 | 17 | | | |
| | | 3/2 | 32 528.19 | 0.05 | 17 | | | |
| 22d | ^2D | 3/2 | 32 530.86 | 0.03 | 17 | | | |
| | | 5/2 | 32 431.57 | 0.03 | 17 | | | |
| 24s | ^2S | 1/2 | 32 542.59 | 0.03 | 17 | | | |
| 24p | $^2\text{P}^\circ$ | 1/2 | 32 557.32 | 0.05 | 17 | | | |
| | | 3/2 | 32 560.25 | 0.05 | 17 | | | |
| 23d | ^2D | 3/2 | 32 562.52 | 0.03 | 17 | | | |
| | | 5/2 | 32 563.13 | 0.03 | 17 | | | |
| 25s | ^2S | 1/2 | 32 572.56 | 0.03 | 17 | | | |
| 25p | $^2\text{P}^\circ$ | 1/2 | 32 585.20 | 0.05 | 17 | | | |
| | | 3/2 | 32 587.72 | 0.05 | 17 | | | |
| 24d | ^2D | 3/2 | 32 589.68 | 0.03 | 17 | | | |
| | | 5/2 | 32 590.20 | 0.03 | 17 | | | |
| 26s | ^2S | 1/2 | 32 598.34 | 0.03 | 17 | | | |
| 26p | $^2\text{P}^\circ$ | 1/2 | 32 609.27 | 0.05 | 17 | | | |
| | | 3/2 | 32 611.45 | 0.05 | 17 | | | |
| 25d | ^2D | 3/2 | 32 613.15 | 0.03 | 17 | | | |
| | | 5/2 | 32 613.60 | 0.03 | 17 | | | |
| 27s | ^2S | 1/2 | 32 620.67 | 0.03 | 17 | | | |
| 27p | $^2\text{P}^\circ$ | 1/2 | 32 630.19 | 0.05 | 17 | | | |
| | | 3/2 | 32 632.09 | 0.05 | 17 | | | |
| 26d | ^2D | 3/2 | 32 633.57 | 0.03 | 17 | | | |
| | | 5/2 | 32 633.97 | 0.03 | 17 | | | |
| 28s | ^2S | 1/2 | 32 640.14 | 0.03 | 17 | | | |
| 28p | $^2\text{P}^\circ$ | 1/2 | 32 648.48 | 0.05 | 17 | | | |
| | | 3/2 | 32 650.15 | 0.05 | 17 | | | |
| 27d | ^2D | 3/2 | 32 651.44 | 0.03 | 17 | | | |
| | | 5/2 | 32 651.79 | 0.03 | 17 | | | |
| 29s | ^2S | 1/2 | 32 657.22 | 0.03 | 17 | | | |
| 29p | $^2\text{P}^\circ$ | 1/2 | 32 664.57 | 0.05 | 17 | | | |
| | | 3/2 | 32 666.04 | 0.05 | 17 | | | |
| 28d | ^2D | 3/2 | 32 667.18 | 0.03 | 17 | | | |
| | | 5/2 | 32 667.49 | 0.03 | 17 | | | |
| 30s | ^2S | 1/2 | 32 672.29 | 0.03 | 17 | | | |

TABLE 5. Energy levels of ^{212}Fr I—Continued

| Configuration | Term | J | Level (cm^{-1}) | Uncertainty (cm^{-1}) | Level reference | Hyperfine constants | | Hyperfine reference |
|--------------------------|--------------------|-------|-------------------------------|-------------------------------------|--------------------|---------------------|---------|------------------------|
| | | | | | | A (MHz) | B (MHz) | |
| 30p | $^2\text{P}^\circ$ | 1/2 | 32 678.80 | 0.05 | 17 | | | |
| | | 3/2 | 32 680.10 | 0.05 | 17 | | | |
| 29d | ^2D | 3/2 | 32 681.11 | 0.03 | 17 | | | |
| | | 5/2 | 32 681.39 | 0.03 | 17 | | | |
| 30d | ^2D | 3/2 | 32 693.50 | 0.03 | 17 | | | |
| | | 5/2 | 32 693.75 | 0.03 | 17 | | | |
| Fr II ($^1\text{S}_0$) | | Limit | 32 848.872 | 0.009 | 16 | | | |

A second approach to producing francium atoms was used by Andreev *et al.*^{18,19} at the Institute of Spectroscopy of the USSR Academy of Sciences. They produced atoms of ^{221}Fr by decay of ^{229}Th , then used two-photon laser spectroscopy to measure Rydberg levels for ns ($23 \leq n \leq 31$) and nd (22

$\leq n \leq 33$). The series was combined with the measurement of the $7p\ ^2\text{P}_{3/2}^\circ$ level by Duong *et al.*¹² to give the ionization limit given in the ^{221}Fr energy level table. Hyperfine splitting constants were determined by Coc *et al.*⁸ and Duong *et al.*¹² (See Table 6).

TABLE 6. Energy levels of ^{221}Fr I

| Configuration | Term | J | Level (cm^{-1}) | Uncertainty (cm^{-1}) | Level reference | Hyperfine constants | | Hyperfine reference |
|---------------|--------------------|---------|-------------------------------|-------------------------------------|--------------------|---------------------|-----------|------------------------|
| | | | | | | A (MHz) | B (MHz) | |
| 7s | ^2S | 1/2 | 0.000 | 0.002 | 14 | 6209.9(10) | | 12 |
| 7p | $^2\text{P}^\circ$ | 1/2 | 12 236.660 | 0.002 | 14 | 808(12) | | 8 |
| | | 3/2 | 13 923.212 | 0.002 | 12 | 65.5(6) | -264.0(3) | 12 |
| 8p | $^2\text{P}^\circ$ | 3/2 | 23 657.529 | 0.002 | 12 | 22.4(1) | -85.7(8) | 12 |
| 22d | ^2D | 3/2,5/2 | 32 530.34 | 0.18 | 19 | | | |
| 23s | ^2S | 1/2 | 32 506.57 | 0.23 | 19 | | | |
| 23d | ^2D | 3/2,5/2 | 32 562.08 | 0.19 | 19 | | | |
| 24d | ^2D | 3/2,5/2 | 32 589.16 | 0.12 | 19 | | | |
| 25s | ^2S | 1/2 | 32 571.5 | 0.3 | 19 | | | |
| 25d | ^2D | 3/2,5/2 | 32 612.49 | 0.08 | 19 | | | |
| 26s | ^2S | 1/2 | 32 597.5 | 0.2 | 19 | | | |
| 26d | ^2D | 3/2,5/2 | 32 632.93 | 0.09 | 19 | | | |
| 27s | ^2S | 1/2 | 32 619.68 | 0.13 | 19 | | | |
| 27d | ^2D | 3/2,5/2 | 32 650.87 | 0.09 | 19 | | | |
| 28d | ^2D | 3/2,5/2 | 32 666.57 | 0.10 | 19 | | | |
| 29s | ^2S | 1/2 | 32 656.28 | 0.10 | 19 | | | |
| 29d | ^2D | 3/2,5/2 | 32 680.53 | 0.13 | 19 | | | |
| 30s | ^2S | 1/2 | 32 671.26 | 0.13 | 19 | | | |
| 30d | ^2D | 3/2,5/2 | 32 692.84 | 0.16 | 19 | | | |
| 31s | ^2S | 1/2 | 32 684.95 | 0.18 | 19 | | | |
| 31d | ^2D | 3/2,5/2 | 32 703.83 | 0.15 | 19 | | | |

TABLE 6. Energy levels of ^{221}Fr I—Continued

| Configuration | Term | J | Level (cm $^{-1}$) | Uncertainty (cm $^{-1}$) | Level reference | Hyperfine constants | | Hyperfine reference |
|--------------------------|--------------|---------|---------------------|---------------------------|-----------------|---------------------|---------|---------------------|
| | | | | | | A (MHz) | B (MHz) | |
| 32d | ^2D | 3/2,5/2 | 32 713.8 | 0.3 | 19 | | | |
| 33d | ^2D | 3/2,5/2 | 32 722.71 | 0.18 | 19 | | | |
| Fr II ($^1\text{S}_0$) | | Limit | 32 848.0 | 0.3 | 19 | | | |

TABLE 7. Energy levels of ^{210}Fr I

| Configuration | Term | J | Level (cm $^{-1}$) | Uncertainty (cm $^{-1}$) | Level reference | Hyperfine constants | | Hyperfine reference |
|---------------|--------------------|-----|---------------------|---------------------------|-----------------|---------------------|---------|---------------------|
| | | | | | | A (MHz) | B (MHz) | |
| 7s | ^2S | 1/2 | 0.000 | 0.004 | 20 | 7195.1(4) | | 7 |
| 7p | $^2\text{P}^\circ$ | 1/2 | | | | 946.3(2) | | 23 |
| | | 3/2 | 13 924.085 | 0.002 | 7 | 78.0(2) | 51(4) | 7 |
| 8s | ^2S | 1/2 | 19 732.523 | 0.004 | 27 | 1577.8(11) | | 27 |
| 7d | ^2D | 3/2 | 24 244.831 | 0.003 | 24 | 22.3(5) | | 24 |
| | | 5/2 | 24 333.298 | 0.003 | 24 | -17.8(8) | 64(17) | 24 |
| 9s | ^2S | 1/2 | 25 671.021 | 0.006 | 20 | | | |

TABLE 8. Lifetimes of energy levels of ^{210}Fr I

| Level | $7p\ ^2\text{P}_{1/2}^\circ$ | $7p\ ^2\text{P}_{3/2}^\circ$ | $7d\ ^2\text{D}_{3/2}$ | $7d\ ^2\text{D}_{5/2}$ | $8s\ ^2\text{S}_{1/2}$ | $8p\ ^2\text{P}_{1/2}^\circ$ | $8p\ ^2\text{P}_{3/2}^\circ$ | $9s\ ^2\text{S}_{1/2}$ |
|--------------|------------------------------|------------------------------|------------------------|------------------------|------------------------|------------------------------|------------------------------|------------------------|
| Lifetime(ns) | 29.45(11) | 21.02(11) | 73.6(3) | 68(3) | 53.3(4) | 149(4) | 83.5(15) | 107.5(9) |
| Reference | 21 | 21 | 23 | 23 | 26 | 25 | 25 | 25 |

Scientists at the State University of New York at Stony Brook create the isotope ^{210}Fr by bombarding gold targets with highly accelerated ions of ^{18}O from a superconducting linear accelerator (Simsarian *et al.*,^{20–22} Grossman *et al.*,^{23,24} Aubin *et al.*,²⁵ and Gomez *et al.*²⁶). This technique produces 10^6 Fr ions/s, but the 3.2 min half-life of this isotope necessitates rapid transport to an optical trap where the measurement takes place. Using two-photon spectroscopy, they have been able to directly observe the 8s and 9s levels, as listed in Table 7. In addition to the spectroscopic data for ^{210}Fr summarized in Table 7, the lifetimes of several levels have been measured and are presented in Table 8.

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