

Energy Levels of Sodium, Na I through Na XI

W. C. Martin and Romuald Zalubas

Center for Radiation Research, National Measurement Laboratory, National Bureau of Standards, Washington, D.C. 20234

Energy level data are given for the atom and all positive ions of sodium ($Z=11$). These data have been critically compiled, mainly from published material on measurements and analyses of the optical spectra. We have derived or recalculated the levels for a number of the ions. In addition to the level value in cm^{-1} and the parity, the J value and the configuration and term assignments are listed if known. Leading percentages from the calculated eigenvectors are tabulated wherever available. Ionization energies are given for all spectra.

Key words: Atomic energy levels; atomic ions; atomic spectra; electron configurations; ionization potentials; sodium.

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I. Introduction

This compilation is one of a series being published by the NBS Atomic Energy Levels Data Center. The main program of this center is the critical compilation of energy level data, with emphasis at present on the first 30 elements. The more recent publications include compilations for Mg I-XII [Martin and Zalubas, 1980], Al I-XIII [Martin and Zalubas, 1979], K I-XIX [Corliss and Sugar, 1979b], Ca I-XX [Sugar and Corliss, 1979], Sc I-XXI [Sugar and Corliss, 1980], Ti I-XXII [Corliss and Sugar, 1979a], V I-XXIII [Sugar and Corliss, 1978], Cr I-XXIV [Sugar and Corliss, 1977], Mn I-XXV [Corliss and Sugar, 1977], Fe I-XXVI [Reader and Sugar, 1975], and Ni I-XXVIII [Corliss and Sugar, 1981]. Similar compilations for Si and Co are in progress.

Since the general methods used in these compilations were outlined previously [Martin and Zalubas, 1979, 1980], our explanation here is confined mainly to the tables and the material preceding them. The levels for the Na spectra have been compiled from data available to us through July, 1980.

The basic data listed after the main heading for each spectrum include the appropriate isoelectronic sequence (for ions), the configuration and term designation of the ground-state level, and the wavenumber corresponding to the principal ionization energy. The ionization energy is also given in

electron-volt (eV) units, an equivalence of 1 eV to $8065.479 \pm 0.021 \text{ cm}^{-1}$ being used for the conversion [Cohen and Taylor, 1973].

We have tried to describe our use of the data from the references for each spectrum in sufficient detail to make apparent the sources for at least all major groups of levels. More complete references, and references for several types of data not included here, are given in several bibliographic publications [Moore, 1968, Hagan and Martin, 1972, Hagan, 1977, Zalubas and Albright, 1980, Fuhr, Miller, and Martin, 1978, Miller, Fuhr, and Martin, 1980]. Our starting point in collecting the references was Moore's *Atomic Energy Levels*, Vol. I.

The symbols following the references indicate types of data or other content according to a code explained in the "Bibliography on Atomic Energy Levels and Spectra" publications [Hagan and Martin, 1972]. These symbols are especially useful for references otherwise listed without comment. We note that "EL," "CL," and "IP" refer to energy levels, classified lines, and ionization potentials, respectively, and "PT" and "AT" refer to theoretical results.

The spectroscopic notations used in energy-level compilations of the AEL Data Center are described fully in a recent publication [Martin, Zalubas, and Hagan, 1978]. This reference also describes the format of the tables in detail and includes material on coupling schemes, eigenvector percentages, allowed terms, and the Zeeman effect. In general we use the notation and conventions outlined there without comment.

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The levels are given in units of cm^{-1} with respect to the ground level at zero. Odd-parity levels are printed in italics. The assignment of a set of levels to a term is indicated by grouping the levels and by listing the configuration and term symbol for only the first (lowest) level of the group. Levels within terms are listed in order of position (*not J* value), and terms are listed in order of lowest levels, ungrouped levels being treated as terms.

The "Leading Percentages" column normally gives one or two percentages from a calculated eigenvector for the level. All percentages are rounded off to the nearest percent, and the % symbol is omitted. If the level has a name (under "Configuration" and "Term"), a first percentage not followed by a term symbol is for this name component. A first percentage followed by a term symbol normally represents the largest component in the eigenvector of a level for which no particular name is appropriate, the configuration and parentage for this component being shown under "Configuration." If two percentages are listed without comment, the second percentage is the largest of the remaining percentages from the same eigenvector as the first percentage. The configuration for the second-percentage term is omitted for a level having both percentages from the same configuration. If the levels of a term group also have second percentages from a common (second) term, this second-percentage term is usually printed only for the first level of the group.

Any variation from the above conventions for the Leading Percentages is made obvious by the notation and is mentioned in the comments.

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3. Tables of Energy Levels

Na I

Z=11

Ground state $1s^2 2s^2 2p^6 3s^2 S_{1/2}$ Ionization energy $41\,449.44 \pm 0.03 \text{ cm}^{-1}$ ($5.139117 \pm 0.000013 \text{ eV}$)**Experimentally Determined Levels, Series Formulae, Ionization Energy**

Meissner and Luft [1937] made interferometric measurements of this spectrum from 4664 to 8195 Å in one of the earliest spectroscopic applications of an atomic beam excited by electron impact. Except for the $4s^2 S$ level, all levels given here to three decimal places (without brackets) were derived from their wavelength measurements [Risberg, 1956]. The experimental uncertainty of $\pm 0.0005 \text{ Å}$ given by Meissner and Luft apparently does not allow for error of the Kr wavelength used as the standard, which was taken as 5570.2890 Å. Combining an accurate value of the 5570 Å line in $^{86}\text{Kr I}$ [Kaufman and Humphreys, 1969] with recent isotope-shift measurements for this line [Jackson, 1979], we obtain a wavelength of $5570.2894 \pm 0.0001 \text{ Å}$ for the natural Kr mixture used by Meissner and Luft. Correction for the corresponding systematic errors would lower the $3p^2 P^\circ$ and $4s^2 S$ levels by 0.001 cm^{-1} and the other levels by 0.002 to 0.003 cm^{-1} . We have not applied such corrections, but give the levels directly as derived by Risberg. The combined systematic and random errors are about $\pm 0.002 \text{ cm}^{-1}$ for the $3p^2 P^\circ$ levels and ± 0.004 to $\pm 0.006 \text{ cm}^{-1}$ for the other levels based on Meissner and Luft's measurements. The $3d$, $4d$, $5d$, and $6d^2 D$ fine-structure intervals from Meissner and Luft's measurements agree with the best current values (see below) to $\pm 0.001 \text{ cm}^{-1}$.

All except two of the two-place levels not in brackets are from Risberg, who measured the spectrum from a hollow-cathode source over the range 2852–11 404 Å. Johansson's [1961] measurements of several infrared wavelengths (12 679–23 379 Å) agreed with values predicted by Risberg's levels except for the $3d^2 D$ – $4f^2 F^\circ$ line; Johansson's redetermination of the $4f^2 F^\circ$ term is used here.

The $4s^2 S$ level (given to three places) and the $4p^2 P^\circ$ levels as confirmed by Johansson's measurements are probably accurate to $\pm 0.02 \text{ cm}^{-1}$. The other levels determined by Risberg agree with the predictions of series formulae (see below) to within $\pm 0.02 \text{ cm}^{-1}$, except for the $9d$ – $11d^2 D$ and $9f^2 F^\circ$ terms. Values of the $7d$ – $11d^2 D$ and $4f$ – $10f^2 F^\circ$ terms from series formulae are given below.

The $5g^2 G$ term was derived by Litzén [1970] from his measurement of the $4f$ – $5g$ wavelength (40 431.88 Å) with an uncertainty of $\pm 0.01 \text{ cm}^{-1}$ in the experimental wavenumber. An error of the $4f^2 F^\circ$ level and/or a Stark shift of the observed line would contribute to the error of the $5g^2 G$

position, however. Since Litzén deduced probable Stark shifts of $\sim 0.07 \text{ cm}^{-1}$ for the $5g$ levels in Li I and K I under similar experimental conditions, it seems appropriate to assume an uncertainty at least that large for the Na I $5g^2 G$ level. The quantum-defect formula used to calculate the higher $ng^2 G$ terms given here predicts the $5g^2 G$ level at $37\,059.50 \text{ cm}^{-1}$.

Risberg derived series formulae fitting the lowest few terms of each of the series $ns^2 S_{1/2}$, $np^2 P_{1/2}^\circ$, $np^2 P_{3/2}^\circ$, $nd^2 D$, and $nf^2 F^\circ$, and obtained the quoted ionization energy. The levels given here in brackets have been derived from series formulae with Risberg's value for the ionization limit. Except for the $np^2 P_{3/2}^\circ$ levels, the values were calculated with formulae given by Martin [1980]; the 2S , $^2P^\circ$, and 2D formulae are equivalent to the corresponding formulae of Risberg to within $< 0.01 \text{ cm}^{-1}$ in the predicted terms.

In general the uncertainty of the predicted levels with respect to the ground level is equal to the uncertainty of the limit, about $\pm 0.03 \text{ cm}^{-1}$. All levels below the ionization limit can be obtained to within this approximate uncertainty from the formulae, the termination of the calculated nl levels tabulated here being arbitrary. The calculated levels are given to three decimal places because the uncertainty of any nl – $n'l'$ separation obtained from the formulae is less than 0.01 cm^{-1} for sufficiently high n and n' .

A considerable part of the more recent spectroscopy of the alkali atoms has been devoted to observations of Stark and/or hyperfine structures. Data of these types are not included here, but we note that bibliographies covering both subjects through June 1979 are available [see the introduction].

 $ns^2 S$ and $np^2 P^\circ$ Terms: Higher Levels, $np^2 P^\circ$ Fine Structure

Calculated values are listed for the $ns^2 S$ and $np^2 P^\circ$ levels through $n=50$. The $ns^2 S$ levels for $n=13$ – 50 and the $np^2 P_{1/2}^\circ$ levels for $n=9$ – 40 were calculated with the $ns^2 S_{1/2}(1)$ and $np^2 P_{1/2}^\circ$ quantum-defect formulae given by Martin. The $np^2 P^\circ$ terms for $n=41$ – 50 are given at the baricenter of the $^2 P_{1/2}^\circ$ and $^2 P_{3/2}^\circ$ positions predicted by the respective formulae.

The $np^2 P_{3/2}^\circ$ levels for $n=9$ – 40 were obtained by adding fine-structure intervals $\Delta E(^2 P^\circ)$ to the $np^2 P_{1/2}^\circ$ levels, with

$$\Delta E(^2 P^\circ) = A(n^*)^{-3} - B(n^*)^{-5},$$

$$A = 179.7 \pm 0.4 \text{ cm}^{-1} \quad (5387 \pm 12 \text{ GHz}),$$

$$B = 73.8 \pm 2 \text{ cm}^{-1} \quad (2212 \pm 60 \text{ GHz}).$$

The constants A and B were derived by fitting the experimental $3p \ ^2P^\circ$ interval and the $np \ ^2P^\circ$ intervals as determined by microwave techniques for $n=16-19$ [Gallagher et al., 1977b] and for $n=23-25$ and $32-36$ [Fabre et al., 1980]. An approximate value for the quantum defect $n-n^* = 0.855$ can be used in evaluating this $\Delta E(^2P^\circ)$ expression for high values of n . In fitting the $3p \ ^2P^\circ$ interval, which mainly determines the value of B , we used the n^* values of the $2p_{3/2}^\circ$ level; sufficiently accurate values of $n^*(^2P_{3/2}^\circ)$ [Risberg, 1956, Martin, 1980] should be used in evaluating the expression at lower values of n . The predicted $4p$ and $5p \ ^2P^\circ$ intervals agree with the experimental values to within $<0.01 \text{ cm}^{-1}$, and the predicted intervals for $6p-8p$ may well be more accurate than the experimental values. The predicted $9p-15p$ intervals are more accurate than the corresponding differences of levels from the Ritz formulae.

The accuracy of the above $\Delta E(^2P^\circ)$ formula for high n is much greater than can be shown by the three-place intervals used for the table here, the accuracy of course deriving from the accuracy of the microwave data. For comparisons at the level of accuracy of the microwave data, it should be noted that the predicted intervals for $16p-19p \ ^2P^\circ$ are slightly less than the experimental values, whereas most of the more accurate experimental $^2P^\circ$ intervals in the $23p-36p$ range are slightly less than the formula values. For example, the formula gives intervals of 1067.4 MHz and 495.6 MHz for $18p$ and $23p \ ^2P^\circ$, respectively, whereas the experimental values are 1068.4 ± 1.5 MHz [Gallagher et al., 1977b] and 494.6 ± 1.2 MHz [Fabre et al., 1980]. The internal consistency of either the $16p-19p$ data or the $23p-36p$ data would correspond to errors of the constants A and B about half those given above.

Fabre et al. [1980] observed millimeter resonances due to $ns \ ^2S_{1/2} - n'p \ ^2P_{1/2}^\circ$ and $ns \ ^2S_{1/2} - n'p \ ^2P_{3/2}^\circ$ transitions ($n' = n$ or $n' = n + 1$) in the ranges $n'=23-25$ and $32-36$. The frequencies of the corresponding transitions obtained from the levels here agree with the accurate microwave data to the nearest 0.001 cm^{-1} . The levels here also give agreement with the $ns \ ^2S_{1/2} - (n+1)s \ ^2S_{1/2}$ separations obtained by Goy et al. [1980] from their observations of two-photon millimeter resonances (n ranging from 32 to 40). The microwave data are much more accurate than $\pm 0.001 \text{ cm}^{-1}$, and quantum-defect formulae fitting the results for these high states to within the experimental uncertainties are given by Fabre et al. [1980] and Goy et al. An earlier paper by Fabre et al. [1978] includes several experimental term separations (in the range $n=23-41$) not remeasured in the more recent work; the results have been compared with the predictions of the formulae [Martin, 1980].

Thackeray [1949] observed the $3s \ ^2S_{1/2} - np \ ^2P^\circ$ series to $n=73$, but most of his measurements deviate systematically by about 0.2 cm^{-1} from the wavenumbers predicted for these lines by Risberg's data [Risberg, 1956]. The $17p \ ^2P^\circ$ position determined by Ducas and Zimmerman [1977], $41\,028.43 \pm 0.04 \text{ cm}^{-1}$, agrees with the predicted value of

$41\,028.44 \pm 0.03 \text{ cm}^{-1}$ (for the baricenter of the $17p \ ^2P_{1/2}^\circ$ and $^2P_{3/2}^\circ$ levels).

$nd \ ^2D$ Terms and Fine Structure

The tabulation of these terms as obtained from the quantum-defect formula extends through $n=30$. Gallagher et al. [1976b] derived experimental quantum defects for nd , nf , and ng terms in the range $n=13-17$ from experimental microwave frequencies corresponding to separations of the types $nd-nf$, $nd-ng$, and $nd-nh$. The quantum defects predicted by the $nd \ ^2D$ formula we used agree with the accurate experimental defects in this range to within equivalent term errors smaller than 0.001 cm^{-1} [Martin, 1980]. This agreement implies that the uncertainty of the calculated $nd \ ^2D$ levels near and above $n=13$ is equal to the uncertainty of the limit, $\pm 0.03 \text{ cm}^{-1}$. Risberg's experimental values for the $7d-11d \ ^2D$ levels are lower than the calculated values by 0.02 to 0.08 cm^{-1} [Risberg, 1956, Martin, 1980]; although Risberg was unable to explain the larger discrepancies, the predicted values for these levels are probably more accurate than the experimental values given in the main table here. We thus list the following predicted $nd \ ^2D$ levels, the fine-structure intervals being taken to agree to the nearest 0.001 cm^{-1} with much more accurate values given in references cited below:

Term	J	Level (cm^{-1})
$7d \ ^2D$	5/2	[39200.944]
	3/2	[39200.953]
$8d \ ^2D$	5/2	[39728.713]
	3/2	[39728.719]
$9d \ ^2D$	5/2	[40090.350]
	3/2	[40090.354]
$10d \ ^2D$	5/2	[40348.908]
	3/2	[40348.911]
$11d \ ^2D$	5/2	[40540.137]
	3/2	[40540.139]

Among the more recent determinations of the inverted $nd \ ^2D$ fine-structure intervals are those by Salour [1976] ($n=3, 6, 7, 8$), Eckstein et al. [1978] ($n=4$), Fredriksson and Svanberg [1976] ($n=4-9$), Fabre et al. [1975] ($n=9-16$), Gallagher et al. [1976a] ($n=11-16$), Gallagher et al. [1977b] ($n=15-17$), and Leuchs and Walther [1979] ($n=21-31$). The measurements for the $4d-17d$ and $21d-31d$ terms have yielded the intervals with stated uncertainties of ± 1 to $\pm 0.1 \text{ MHz}$ (± 0.00003 to $\pm 0.000003 \text{ cm}^{-1}$). The data are too extensive for separate tabulation here, but we quote a two-term formula that predicts the intervals $\Delta E(^2D)$ for $n \geq 4$ with good accuracy [Leuchs and Walther, 1979]:

$$\Delta E(^2D) = -A(n^*)^{-3} + B(n^*)^{-5},$$

$$A = 97.8 \pm 1.1 \text{ GHz} \quad (3.262 \pm 0.037 \text{ cm}^{-1}),$$

$$B = 519 \pm 11 \text{ GHz} \quad (17.31 \pm 0.37 \text{ cm}^{-1}).$$

The approximation $n^* = n - 0.014$ should be used with these values of the constants, which Leuchs and Walther re-determined using the experimental $4d$ and $23d$ 2D intervals (-1028.4 ± 0.4 MHz [Eckstein et al., 1978] and -8.00 ± 0.10 MHz).

Theoretical calculations of the nd 2D fine structures have been made by Luc-Koenig [1976] ($n=3-16$), Holmgren et al. [1976] ($n=3-6$), and Sternheimer et al. [1978] ($n=3-6$), for example.

Cooke et al. [1977] measured the frequencies of nd $^2D_{3/2}-(n+1)p$ $^2P_{1/2}$ and nd $^2D_{3/2}-(n+1)p$ $^2P_{3/2}$ transitions for $n=30-32$. The corresponding frequencies predicted by quantum-defect formulae for the nd 2D (baricenter) and np $^2P_{1/2}$ positions [Martin, 1980], together with the formulae for the $\Delta E(^2D)$ and $\Delta E(^2P^\circ)$ intervals, agree with the observed frequencies to within the experimental errors of ± 4 MHz ($\pm 0.00013 \text{ cm}^{-1}$). Similarly predicted frequencies for the $29d$ $^2D-31p$ $^2P^\circ$ and $28d$ $^2D-29d$ 2D separations agree with the measurements of Fabre et al. [1978] to within their experimental errors.

nl ($l \geq 3$) Terms and Fine Structure

The nf $^2F^\circ$ terms are given through $n=30$, the ng 2G terms through $n=20$, and the nh $^2H^\circ$ and ni 2I terms through $n=10$. The derivations of the formulae used to calculate the bracketed levels have been described elsewhere [Martin, 1980]. Accurate experimental quantum defects for the $13f-17f$ $^2F^\circ$ terms [Gallagher et al., 1976b] were included in the evaluation of the nf $^2F^\circ$ -formula constants. The quantum defects from the ng 2G and nh $^2H^\circ$ formulae, also, agree with experimental values [Gallagher et al., 1976b] and theoretical values [Freeman and Kleppner, 1976] for $13g-15g$ 2G and $13h-15h$ $^2H^\circ$ to within equivalent term errors that are negligible compared with the $\pm 0.03 \text{ cm}^{-1}$ uncertainty of the limit. For comparison with the experimental values in the main table, the predicted values of the $4f-10f$ $^2F^\circ$ terms are:

Term	Level (cm^{-1})
$4f$ $^2F^\circ$	[34586.902]
$5f$ $^2F^\circ$	[37057.672]
$6f$ $^2F^\circ$	[38399.792]
$7f$ $^2F^\circ$	[39209.003]
$8f$ $^2F^\circ$	[39734.183]
$9f$ $^2F^\circ$	[40094.226]
$10f$ $^2F^\circ$	[40351.751]

There is some indication that the calculated nf $^2F^\circ$ levels in the region of $n=28$ are too high with respect to the nearby calculated nd 2D levels by ~ 100 MHz (0.003 to 0.004 cm^{-1}) [Martin, 1980].

Measurements of the fine-structure intervals for several nf $^2F^\circ$ terms have shown them to be close to hydrogenic values. Bjorkholm and Liao [1976] observed non-allowed two-photon $3s$ $^2S_{1/2}-4f$ $^2F^\circ$ transitions and determined the $4f$ $^2F^\circ$ interval as 229 ± 4 MHz; the value given by the hydrogenic formulae [Erickson, 1977] adjusted to the Na nuclear mass is 228.6 MHz (0.007626 cm^{-1}). Gallagher et al. [1977a] measured the intervals for the $11f$, $13f$, and $14f$ $^2F^\circ$ terms to about 2% uncertainties and obtained values about 5% less than the hydrogenic values. Less accurate values for the $11f-17f$ $^2F^\circ$ intervals were measured earlier by Gallagher et al. [1976a].

The results for the nf $^2F^\circ$ intervals lead to the expectation of near-hydrogenic fine structures for the terms of higher angular momentum ($l \geq 4$). The $13g-17g$ 2G and $13h-15h$ $^2H^\circ$ intervals measured by Gallagher et al. [1976b] are consistent with hydrogenic values, but the uncertainties are, respectively, comparable to and about three times larger than the hydrogenic intervals.

g_J Values

Accurate measurements of the relatively small deviations from Landé g_J values (corrected for the anomalous magnetic moment of the electron) are of interest in one-electron spectra. Beahn and Bedard [1977] determined the g_J value of the $3s$ $^2S_{1/2}$ ground state of ^{23}Na as $2.00229563 \pm 0.00000016$ using a spin-exchange optical pumping technique and known data for ^{87}Rb and for the electron. Hartmann [1970], by the optical double-resonance technique, obtained a value of 0.66581 ± 0.00012 for the g_J value of the $3p$ $^2P_{1/2}$ level.

Levels Above the Ionization Limit

Configurations involving excitations from the $2p$ or $2s$ shell have been identified in the interpretation of photoabsorption spectra below 410 \AA . Lines observed in absorption from the ground level were assumed to arise from transitions to odd-parity levels having $J = \frac{1}{2}$ or $\frac{3}{2}$. Connerade et al. [1971] measured such features in the region $180-410 \text{ \AA}$, their classifications including the outstanding doublet $2s^2 2p^6 3s^2 S_{1/2} - 2s^2 2p^6 3s^2 P_{3/2, 1/2}^\circ$ near 400 \AA . Wolff et al. [1972] also observed the ground-level absorption spectrum, including many (mostly weaker) lines not observed by Connerade et al. Most of the odd levels given here between the Na II $2s^2 2p^6$ 1S_0 and $2s^2 2p^6 3s$ $^1P_1^\circ$ limits are from lines measured by both of these groups, the two wavenumber determinations having been averaged. A few levels from lines measured only by Wolff et al. are included. Most of the levels are probably accurate to within $\pm 20 \text{ cm}^{-1}$. These levels must belong mainly to $2s^2 2p^6 3sns$ and $2s^2 2p^6 3snd$ ($n \geq 3$) configurations, but their detailed interpretation will in most cases probably require calculations including the significant configuration interactions [Wolff et al., 1972]. We

have followed Wolff et al. in listing a number of the levels below $306\,500\text{ cm}^{-1}$ without configuration assignments. Their suggested assignments for some of the other levels in this region are given tentatively. Connerade et al. suggested different assignments for most of these levels. The identifications of higher members of the overlapping series $2s^2 2p^5 3s(^1P^\circ)nd$ ($n=6-12$) and $2s^2 2p^5 3s(^1P^\circ)ns\ ^2P^\circ$ ($n=7-9$) were made by Connerade et al. These series were extended by Wolff et al. to $n=20$ and to $n=12$, respectively, the $(^1P^\circ)nd$ features being interpreted as arising from all three transitions (to the $J=\frac{1}{2}$, $\frac{3}{2}$, $\frac{5}{2}$ levels) allowed by the J selection rule. We have not listed these $(^1P^\circ)nd$ positions above $n=12$.

The levels of the $2s^2 2p^5 3s3p$ and $2s^2 2p^5 3s4p$ even configurations are from absorption lines ($356-398\text{ \AA}$) observed by Sugar et al. [1979] and classified as transitions from the excited $2s^2 2p^6 3p\ ^2P^\circ$ lower term. We have evaluated the upper levels directly from the experimental wavelengths; since the $3p\ ^2P_{3/2}^\circ-^2P_{1/2}^\circ$ separation of 17 cm^{-1} was not resolved, the upper levels having $J=\frac{1}{2}$ or $\frac{3}{2}$ were obtained with values for the lower $3p\ ^2P^\circ$ term adjusted to the theoretical (statistical) intensities of the two unresolved components of each line. The stated wavelength error of $\pm 0.02\text{ \AA}$ corresponds to a level error of about $\pm 15\text{ cm}^{-1}$.

Even-parity autoionizing levels of Na I have also been identified from ejected-electron spectra [see, e.g., Ross et al., 1976, and Pegg et al., 1975]. Sugar et al. reinterpreted several features in these spectra on the basis of their calculations of the above configurations (including interactions with additional configurations). The levels derived from electron data are not included here. Berry et al. [1974] suggested the classification $2s^2 2p^5(^2P^\circ)3s3p(^3P^\circ)\ ^4D_{7/2}-2s^2 2p^5(^2P^\circ)3s3d(^3D)\ ^4F_{9/2}$ for a line observed at 3882.8 \AA in beam-foil spectra. No other optical lines involving these levels have been classified, but the $^4D_{7/2}$ level can be estimated from the calculations of Sugar et al. as near $266\,500\text{ cm}^{-1}$.

Connerade et al. and Wolff et al. observed features in the absorption spectrum above the Na II $2s^2 2p^5 3s\ ^1P^\circ$ limit due to transitions of the type $2s^2 2p^6 3s\ ^2S_{1/2}-2s^2 2p^5 nln'l'$, with neither nl nor $n'l'$ (in the principal configuration of the upper odd-parity term) being a $3s$ electron. The positions and $2s^2 2p^5 3p^2$ configuration assignments of the lowest two such levels listed by Connerade et al. are tabulated here. Most of the observed features are asymmetric and very autoionization-broadened, and they include a number of window resonances. Several additional levels (up to $335\,200\text{ cm}^{-1}$) with assignments to $2s^2 2p^5 3pn p$ ($n=3-7$) configurations are given by Connerade et al.

The four $^2P^\circ$ terms assigned to configurations with a $2s$ vacancy ($535\,330-586\,200\text{ cm}^{-1}$) are from resonances observed in absorption from the ground level by LaVilla et al. [1981]. The positions correspond to the absorption maxima to within estimated uncertainties of 200 cm^{-1} (for the lowest of these terms) to 350 cm^{-1} . The three lower-energy features were classified earlier by Wolff et al.; their values for the energies, which are above the corresponding absorption maxima by about 1800 cm^{-1} , are less accurately determined out closer to the resonance centers. The strong

$2s(^2S)2p^6 3s3p(^3P^\circ)\ ^2P^\circ$ resonance, which was first observed by Connerade et al., has a striking Beutler-Fano profile with a width of about 2700 cm^{-1} [Codling et al., 1977]. LaVilla et al. give the energies and tentative classifications for several higher resonances (up to $636\,600\text{ cm}^{-1}$).

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ENERGY LEVELS OF SODIUM

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Na I

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Configuration	Term	<i>J</i>	Level (cm ⁻¹)
3s	² S	1/2	0.000	7h	² H°	9/2, 11/2	[39 209.877
3p	² P°	1/2 3/2	16 956.172 16 973.368	7i	² I	11/2, 13/2	[39 209.927
4s	² S	1/2	25 739.991	8p	² P°	1/2 3/2	39 298.35 39 298.84
3d	² D	5/2 3/2	29 172.839 29 172.889	9s	² S	1/2	39 574.85
4p	² P°	1/2 3/2	30 266.99 30 272.58	8d	² D	5/2, 3/2	39 728.70
5s	² S	1/2	33 200.675	8f	² F°	5/2, 7/2	39 734.16
4d	² D	5/2 3/2	34 548.731 34 548.766	8g	² G	7/2, 9/2	[39 734.669
4f	² F°	5/2, 7/2	34 586.92	8h	² H°	9/2, 11/2	[39 734.775
5p	² P°	1/2 3/2	35 040.38 35 042.85	8i	² I	11/2, 13/2	[39 734.814
6s	² S	1/2	36 372.620	9p	² P°	1/2 3/2	[39 794.486 [39 794.816
5d	² D	5/2 3/2	37 036.754 37 036.774	10s	² S	1/2	39 983.27
5f	² F°	5/2, 7/2	37 057.65	9d	² D	5/2, 3/2	40 090.31
5g	² G	7/2, 9/2	37 059.54	9f	² F°	5/2, 7/2	40 094.19
6p	² P°	1/2 3/2	37 296.32 37 297.61	9g	² G	7/2, 9/2	[40 094.571
7s	² S	1/2	38 012.044	9h	² H°	9/2, 11/2	[40 094.645
6d	² D	5/2 3/2	38 387.257 38 387.270	9i	² I	11/2, 13/2	[40 094.674
6f	² F°	5/2, 7/2	38 399.79	10p	² P°	1/2 3/2	[40 136.805 [40 137.035
6g	² G	7/2, 9/2	[38 400.896]	11s	² S	1/2	40 271.38
6h	² H°	9/2, 11/2	[38 401.140]	10d	² D	5/2, 3/2	40 348.83
7p	² P°	1/2 3/2	38 540.18 38 540.93	10f	² F°	5/2, 7/2	40 351.77
8s	² S	1/2	38 968.51	10g	² G	7/2, 9/2	[40 352.004
7d	² D	5/2, 3/2	39 200.93	10h	² H°	9/2, 11/2	[40 352.062
7f	² F°	5/2, 7/2	39 208.98	10i	² I	11/2, 13/2	[40 352.081
7g	² G	7/2, 9/2	[39 209.717]	11p	² P°	1/2 3/2	[40 382.926 [40 383.091
				12s	² S	1/2	40 482.22
				11d	² D	5/2, 3/2	40 540.07
				11f	² F°	5/2, 7/2	[40 542.282

Na I—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Configuration	Term	<i>J</i>	Level (cm ⁻¹)
11 <i>g</i>	² G	7/2, 9/2	[40 542.474]	17 <i>p</i>	² P°	1/2 3/2	[41 028.410] [41 028.453]
12 <i>p</i>	² P°	1/2 3/2	[40 565.777] [40 565.906]	18 <i>s</i>	² S	1/2	[41 053.690]
13 <i>s</i>	² S	1/2	[40 641.138]	17 <i>d</i>	² D	3/2, 5/2	[41 069.075]
12 <i>d</i>	² D	3/2, 5/2	[40 685.535]	17 <i>f</i>	² F°	5/2, 7/2	[41 069.663]
12 <i>f</i>	² F°	5/2, 7/2	[40 687.193]	17 <i>g</i>	² G	7/2, 9/2	[41 069.716]
12 <i>g</i>	² G	7/2, 9/2	[40 687.341]	18 <i>p</i>	² P°	1/2 3/2	[41 076.096] [41 076.132]
13 <i>p</i>	² P°	1/2 3/2	[40 705.337] [40 705.437]	19 <i>s</i>	² S	1/2	[41 097.261]
14 <i>s</i>	² S	1/2	[40 763.874]	18 <i>d</i>	² D	3/2, 5/2	[41 110.196]
13 <i>d</i>	² D	3/2, 5/2	[40 798.656]	18 <i>f</i>	² F°	5/2, 7/2	[41 110.692]
13 <i>f</i>	² F°	5/2, 7/2	[40 799.964]	18 <i>g</i>	² G	7/2, 9/2	[41 110.737]
13 <i>g</i>	² G	7/2, 9/2	[40 800.081]	19 <i>p</i>	² P°	1/2 3/2	[41 116.116] [41 116.146]
14 <i>p</i>	² P°	1/2 3/2	[40 814.265] [40 814.344]	20 <i>s</i>	² S	1/2	[41 134.012]
15 <i>s</i>	² S	1/2	[40 860.637]	19 <i>d</i>	² D	3/2, 5/2	[41 144.992]
14 <i>d</i>	² D	3/2, 5/2	[40 888.393]	19 <i>f</i>	² F°	5/2, 7/2	[41 145.414]
14 <i>f</i>	² F°	5/2, 7/2	[40 889.442]	19 <i>g</i>	² G	7/2, 9/2	[41 145.452]
14 <i>g</i>	² G	7/2, 9/2	[40 889.536]	20 <i>p</i>	² P°	1/2 3/2	[41 150.030] [41 150.056]
15 <i>p</i>	² P°	1/2 3/2	[40 900.913] [40 900.976]	21 <i>s</i>	² S	1/2	[41 165.298]
16 <i>s</i>	² S	1/2	[40 938.271]	20 <i>d</i>	² D	3/2, 5/2	[41 174.697]
15 <i>d</i>	² D	3/2, 5/2	[40 960.772]	20 <i>f</i>	² F°	5/2, 7/2	[41 175.059]
15 <i>f</i>	² F°	5/2, 7/2	[40 961.626]	20 <i>g</i>	² G	7/2, 9/2	[41 175.092]
15 <i>g</i>	² G	7/2, 9/2	[40 961.703]	21 <i>p</i>	² P°	1/2 3/2	[41 179.020] [41 179.042]
16 <i>p</i>	² P°	1/2 3/2	[40 970.967] [40 971.019]	22 <i>s</i>	² S	1/2	[41 192.149]
17 <i>s</i>	² S	1/2	[41 001.504]	21 <i>d</i>	² D	3/2, 5/2	[41 200.257]
16 <i>d</i>	² D	3/2, 5/2	[41 019.998]	21 <i>f</i>	² F°	5/2, 7/2	[41 200.570]
16 <i>f</i>	² F°	5/2, 7/2	[41 020.703]	22 <i>p</i>	² P°	1/2 3/2	[41 203.994] [41 204.013]
16 <i>g</i>	² G	7/2, 9/2	[41 020.766]	23 <i>s</i>	² S	1/2	[41 215.367]

ENERGY LEVELS OF SODIUM

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Na I - Continued

Configuration	Term	J	Level (cm^{-1})	Configuration	Term	J	Level (cm^{-1})
22d	2D	$\frac{3}{2}, \frac{5}{2}$	[41 222.410]	28f	$^2F^{\circ}$	$\frac{5}{2}, \frac{7}{2}$	[41 309.456]
22f	$^2F^{\circ}$	$\frac{5}{2}, \frac{7}{2}$	[41 222.632]	29p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 310.905] [41 310.913]
23p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 225.662] [41 225.679]	30s	2S	$\frac{1}{2}$	[41 315.770]
24s	2S	$\frac{1}{2}$	[41 235.578]	29d	2D	$\frac{3}{2}, \frac{5}{2}$	[41 318.825]
23d	2D	$\frac{3}{2}, \frac{5}{2}$	[41 241.734]	29f	$^2F^{\circ}$	$\frac{5}{2}, \frac{7}{2}$	[41 318.944]
23f	$^2F^{\circ}$	$\frac{5}{2}, \frac{7}{2}$	[41 241.973]	30p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 320.249] [41 320.256]
24p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 244.532] [41 244.596]	31s	2S	$\frac{1}{2}$	[41 324.634]
25s	2S	$\frac{1}{2}$	[41 253.280]	30d	2D	$\frac{3}{2}, \frac{5}{2}$	[41 327.392]
24d	2D	$\frac{3}{2}, \frac{5}{2}$	[41 258.693]	30f	$^2F^{\circ}$	$\frac{5}{2}, \frac{7}{2}$	[41 327.499]
24f	$^2F^{\circ}$	$\frac{5}{2}, \frac{7}{2}$	[41 258.903]	31p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 328.678] [41 328.685]
25p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 261.200] [41 261.213]	32s	2S	$\frac{1}{2}$	[41 332.644]
26s	2S	$\frac{1}{2}$	[41 268.872]	32p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 336.309] [41 336.315]
25d	2D	$\frac{3}{2}, \frac{5}{2}$	[41 273.656]	33s	2S	$\frac{1}{2}$	[41 339.908]
25f	$^2F^{\circ}$	$\frac{5}{2}, \frac{7}{2}$	[41 273.842]	33p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 343.238] [41 343.243]
26p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 275.875] [41 275.886]	34s	2S	$\frac{1}{2}$	[41 346.514]
27s	2S	$\frac{1}{2}$	[41 282.676]	34p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 349.550] [41 349.555]
26d	2D	$\frac{3}{2}, \frac{5}{2}$	[41 286.925]	35s	2S	$\frac{1}{2}$	[41 352.540]
26f	$^2F^{\circ}$	$\frac{5}{2}, \frac{7}{2}$	[41 287.090]	35p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 355.315] [41 355.320]
27p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 288.899] [41 288.909]	36s	2S	$\frac{1}{2}$	[41 358.052]
28s	2S	$\frac{1}{2}$	[41 294.955]	36p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 360.596] [41 360.600]
27d	2D	$\frac{3}{2}, \frac{5}{2}$	[41 298.747]	37s	2S	$\frac{1}{2}$	[41 363.107]
27f	$^2F^{\circ}$	$\frac{5}{2}, \frac{7}{2}$	[41 298.894]	37p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 365.444] [41 365.448]
28p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 300.510] [41 300.519]	38s	2S	$\frac{1}{2}$	[41 367.754]
29s	2S	$\frac{1}{2}$	[41 305.927]	38p	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	[41 369.906] [41 369.909]
28d	2D	$\frac{3}{2}, \frac{5}{2}$	[41 309.324]				

Na I—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Configuration	Term	<i>J</i>	Level (cm ⁻¹)
39s	² S	1/2	[41 372.035]	2s ² 2p ⁵ (² P°)3s3p(² P°)	⁴ P	5/2	268 533
39p	² P°	1/2	[41 374.021]			3/2	268 933
		3/2	[41 374.024]				
40s	² S	1/2	[41 375.989]	2s ² 2p ⁵ (² P°)3s3p(² P°)	² D	3/2	269 727
40p	² P°	1/2	[41 377.825]			5/2	270 196
		3/2	[41 377.828]				
41s	² S	1/2	[41 379.647]	2s ² 2p ⁵ (² P°)3s3p(² P°)	² S	1/2	273 240
41p	² P°	1/2, 3/2	[41 381.351]			5/2	280 596
						3/2	282 063
42s	² S	1/2	[41 383.038]	2s ² 2p ⁵ (² P°)3s3p(¹ P°)	² S	1/2	280 785
42p	² P°	1/2, 3/2	[41 384.620]			3/2	281 032
						1/2	282 334
43s	² S	1/2	[41 386.188]	2s ² 2p ⁵ (² P°)3s3p(¹ P°)	² P	3/2	281 032
43p	² P°	1/2, 3/2	[41 387.660]			1/2	282 334
						3/2	288 470
44s	² S	1/2	[41 389.119]	2s ² 2p ⁵ 3s(³ P°)4s	² P°?	1/2	288 666
44p	² P°	1/2, 3/2	[41 390.490]			1/2, 3/2	290 232
						1/2, 3/2	290 488
45s	² S	1/2	[41 391.852]	2s ² 2p ⁵ 3s(³ P°)3d?		1/2, 3/2	290 806
45p	² P°	1/2, 3/2	[41 393.131]			1/2, 3/2	291 404
						1/2, 3/2	292 103
46s	² S	1/2	[41 394.402]	2s ² 2p ⁵ 3s(³ P°)4p	² D	5/2	295 054
46p	² P°	1/2, 3/2	[41 395.598]			3/2	295 317
						1/2, 3/2	296 576
47s	² S	1/2	[41 396.787]	2s ² 2p ⁵ 3s(¹ P°)4p	² D	5/2	297 048
47p	² P°	1/2, 3/2	[41 397.906]			3/2	296 618
						1/2	296 808
48s	² S	1/2	[41 399.020]	2s ² 2p ⁵ 3s(¹ P°)4p	² S	1/2	297 121
48p	² P°	1/2, 3/2	[41 400.069]			3/2	296 808
						1/2	297 121
49s	² S	1/2	[41 401.114]	2s ² 2p ⁵ 3s(¹ P°)4p	² P	3/2	296 808
49p	² P°	1/2, 3/2	[41 402.099]			1/2	297 121
						1/2, 3/2	297 660
50s	² S	1/2	[41 403.080]	2s ² 2p ⁵ 3s(³ P°)4d?		1/2, 3/2	297 856
50p	² P°	1/2, 3/2	[41 404.006]			1/2, 3/2	297 856
						1/2, 3/2	298 989
.....				2s ² 2p ⁵ 3s(³ P°)4d?		1/2, 3/2	298 989
Na II 2s ² 2p ⁶ (¹ S ₀)	<i>Limit</i>		41 449.44	2s ² 2p ⁵ 3s(³ P°)5d?		1/2, 3/2	300 614
2s ² 2p ⁵ 3s ²	² P°	3/2	248 159			1/2, 3/2	300 614
		1/2	249 508			1/2, 3/2	300 786

Na I—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Configuration	Term	<i>J</i>	Level (cm ⁻¹)
$2s^2 2p^5 3s(^3P^o)5d?$		$1/2, 3/2$	301 974	$2s^2 2p^5 3s(^1P^o)9d$		$1/2, 3/2$	308 745
		$1/2, 3/2$	302 430	$2s^2 2p^5 3s(^1P^o)11s$	$^2P^o$	$3/2$ $1/2$	308 890 308 938
		$1/2, 3/2$	304 056	$2s^2 2p^5 3s(^1P^o)10d$		$1/2, 3/2$	309 029
		$1/2, 3/2$	304 528	$2s^2 2p^5 3s(^1P^o)12s$	$^2P^o$	$1/2, 3/2$	309 157
		$1/2, 3/2$	304 894	$2s^2 2p^5 3s(^1P^o)11d$		$1/2, 3/2$	309 219
		$1/2, 3/2$	305 192	$2s^2 2p^5 3s(^1P^o)12d$		$1/2, 3/2$	309 369
		$1/2, 3/2$	305 671	Na II $2s^2 2p^5 3s(^1P_1^o)$	Limit		310 212
	Na II $2s^2 2p^5 3s(^3P_2^o)$	Limit		$2s^2 2p^5 3p^2$		$1/2, 3/2$	310 977
		$1/2, 3/2$	306 374	$2s^2 2p^5 3p^2$		$1/2, 3/2$	312 188
$2s^2 2p^5 3s(^1P^o)6d$		$1/2, 3/2$	306 890				
Na II $2s^2 2p^5 3s(^3P_1^o)$	Limit		307 139	$2s(^2S)2p^6 3s3p(^3P^o)$	$^2P^o$	$1/2, 3/2$	535 330
$2s^2 2p^5 3s(^1P^o)8s$	$^2P^o$	$1/2, 3/2$	307 502	$2s(^2S)2p^6 3s3p(^1P^o)$	$^2P^o$	$1/2, 3/2$	546 600
Na II $2s^2 2p^5 3s(^3P_0^o)$	Limit		307 731	$2s2p^6 3s(^3S)4p$	$^2P^o$	$1/2, 3/2$	559 600
$2s^2 2p^5 3s(^1P^o)7d$		$1/2, 3/2$	307 786	Na II $2s2p^6 3s(^3S_1)$	Limit		573 300
$2s^2 2p^5 3s(^1P^o)9s$	$^2P^o$	$1/2, 3/2$	308 146	Na II $2s2p^6 3s(^1S_0)$	Limit		577 300
$2s^2 2p^5 3s(^1P^o)8d$		$1/2, 3/2$	308 368	$2s2p^6 3p(^3P^o)4s$	$^2P^o$	$1/2, 3/2$	586 200
$2s^2 2p^5 3s(^1P^o)10s$	$^2P^o$	$3/2$	308 566				
		$1/2$	308 623				

Na II

 $Z=11$

Ne I isoelectronic sequence

Ground state $1s^2 2s^2 2p^6 \ ^1S_0$ Ionization energy $381\,390.2 \pm 2 \text{ cm}^{-1}$ ($47.2867 \pm 0.0003 \text{ eV}$)

Wu [1971] reobserved this spectrum and extended the analysis to include the classification of more than 500 lines from 270 to 6566 Å. His line list has not been published, but the wavelengths and classifications listed by Kelly and Palumbo [1973] for the region below 2000 Å are from his results. The tables of Bowen [1928] and Frisch [1931] give most of the lines classified in the earlier analyses, the original LS term designations for the $2p^5 3d$ and $4s$ levels being due to Söderqvist [1934]. Tsui et al. [1965] list 18 lines due to $3d-4f$ transitions (4293–4533 Å).

Most of the levels below the ionization limit are from Wu's thesis. All the excited levels have a standard-deviation error of 2 cm^{-1} with respect to the $2p^6 \ ^1S_0$ ground level. The standard-deviation error of differences between the excited levels varies from perhaps 0.5 cm^{-1} or less for levels given to one decimal place to less than 0.1 cm^{-1} for most of the two-place levels.

The levels are arranged into terms of the most appropriate coupling scheme, LS or $J_1 l$, for each configuration. The leading percentages are from Hansen's calculations [1980]. The first percentages listed for the $2p^5 3s$ and $2p^5 3p$ levels apply to the LS -coupling designations, the leading percentages in $J_1 l$ coupling being given after the word "or". The first percentages for the $2p^5 3d$, $2p^5 4s$, and $2p^5 4p$ levels are for the $J_1 l$ -coupling designations, with the leading LS percentages following. Hansen's calculation of the $2p^5 3p$ levels included a 3S correction discussed in his 1973 paper. The calculation for $2p^5 3d$ and $2p^5 4s$ included the interaction between these configurations; the largest configuration mixing occurs between the $2p^5(^2P_{3/2})3d \ ^2[^3/2]^\circ$ and $2p^5(^2P_{3/2})4s \ ^2[^3/2]^\circ$ pairs, the eigenvectors for each of these terms including a large (21–31%) component from the other term.

Several of Wu's $2p^5 4p$ levels have unexpectedly large deviations from the relative positions predicted by Hansen's calculations. Pending further results on the analysis, we have omitted four of these levels and tentatively changed one J value. The reality of Wu's $2p^5(^2P_{1/2})4p \ ^2[^1/2]_0$ level has been previously questioned [Artru and Kaufman, 1975, A. M. Crooker, private communication, 1975]. We have replaced his $(^2P_{3/2})4p \ ^2[^5/2]_3$ level with a new value based on two previously unclassified lines. One of the $2p^5 4d$ levels is shown as tentative, and one $2p^5 5f$ level was omitted. Two $2p^5 6f$ levels are listed as questionable, and we have also made minor revisions in the values of a few higher $2p^5 nf$ and ng levels.

Wu determined the energy of the Na III $2p^5 \ ^2P^\circ$ term baricenter with respect to the Na II ground level by fitting a core-polarization formula to the Na II $2p^5 4f$, $5f$, and $6f$ config-

urations. Since the resulting values of the Na III $2p^5 \ ^2P^\circ$ levels are probably accurate to within a few tenths of one cm^{-1} with respect to the excited Na II levels, these $^2P^\circ$ limits should have about the same accuracy as the excited levels with respect to the Na II ground level ($\pm 2 \text{ cm}^{-1}$). The baricenter of any Na II $2p^5 nl$ ($l \geq 3$) configuration can be predicted from the Na III $2p^5 \ ^2P^\circ$ baricenter and the polarization parameters; Wu gives predicted values for the $2p^5 nf$, ng , and nh configurations through $n=10$.

The three lowest terms above the Na III $2s^2 2p^5 \ ^2P^\circ$ limits, i.e., the $2s2p^6 3s \ ^3S$ and 1S and $2s2p^6 3p \ ^3P^\circ$ terms, are from measurements of ejected-electron spectra by Breuckmann et al. [1977]. The autoionization width of each of the $2s2p^6 3s$ levels ($\sim 2100 \text{ cm}^{-1}$) is about half their separation and is larger than the separation of the Na III $2s^2 2p^5 \ ^2P_{3/2}^\circ$ and $^2P_{1/2}^\circ$ final states. We have taken the $2s2p^6 3s \ ^3S_1$ level as 18.65 eV above the Na III $^2P_{3/2}^\circ$ limit [Fig. 7 of Breuckmann et al.], and used the $2s2p^6 3s \ ^1S_0-^3S_1$ separation of 0.50 eV derived by Breuckmann et al. from their analysis of the overlapping resonances. The $2s2p^6 3s$ levels are probably accurate to within $\pm 350 \text{ cm}^{-1}$ and the $2s2p^6 3p \ ^3P^\circ$ term to within $\pm 250 \text{ cm}^{-1}$. Other Na II terms above the principal ionization energy have been determined from such spectra by Breuckmann et al. and by Ross et al. [1976], for example. Eissner et al. [1980] have calculated positions and autoionization widths for a number of the $2s2p^6 ns$ and $2s2p^6 np$ terms.

Lucatoro and McIlrath [1976] observed the $2s^2 2p^6 \ ^1S_0-2s2p^6 np \ ^1P_1^\circ$ series ($n=3-8$) in absorption in the 157–177 Å region. The autoionizing $2s2p^6 np \ ^1P^\circ$ levels obtained from their measurements are probably accurate to $\pm 200 \text{ cm}^{-1}$. Lucatoro and McIlrath also extended observations of the $2s^2 2p^6-2s^2 2p^5 ns$ and nd ($J=1$) series to higher members than are tabulated here (to $n=13$ or 14), the lines being classified as blends of transitions to $2p^5 nd$ and $(n+1)s$ levels.

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Na II

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Leading percentages			
2p ⁶	¹ S	0	0.0				
2p ⁵ 3s	³ P°	2	264 921.32	100	or	100	(² P _{3/2} ^o) ² [³ / ₂] ^o
		1	265 689.62	96	or	55	(² P _{3/2} ^o) ² [³ / ₂] ^o
		0	266 281.62	100	or	100	(² P _{1/2} ^o) ² [¹ / ₂] ^o
2p ⁵ 3s	¹ P°	1	268 762.96	96	or	55	(² P _{1/2} ^o) ² [¹ / ₂] ^o
2p ⁵ 3p	³ S	1	293 220.33	99	or	75	(² P _{3/2} ^o) ² [¹ / ₂]
2p ⁵ 3p	³ D	3	297 248.82	100	or	100	(² P _{3/2} ^o) ² [⁵ / ₂]
		2	297 635.61	88	or	70	(² P _{3/2} ^o) ² [⁵ / ₂]
		1	298 165.44	91	or	56	(² P _{1/2} ^o) ² [³ / ₂]
2p ⁵ 3p	¹ D	2	299 189.96	65	or	61	(² P _{3/2} ^o) ² [³ / ₂]
2p ⁵ 3p	¹ P	1	299 885.37	60	or	56	(² P _{3/2} ^o) ² [³ / ₂]
2p ⁵ 3p	³ P	2	300 103.92	67	or	68	(² P _{1/2} ^o) ² [³ / ₂]
		0	300 387.82	100	or	60	(² P _{1/2} ^o) ² [¹ / ₂]
		1	300 507.11	66	or	75	(² P _{1/2} ^o) ² [¹ / ₂]
2p ⁵ 3p	¹ S	0	308 860.80	100	or	60	(² P _{3/2} ^o) ² [¹ / ₂]
2p ⁵ (² P _{3/2} ^o)3d	² [¹ / ₂] ^o	0	330 549.35	97	or	97	³ P°
		1	330 636.75	74	or	89	
2p ⁵ (² P _{3/2} ^o)3d	² [³ / ₂] ^o	2	330 789.05	56	or	61	³ P°
		1	331 745.06	52	or	59	¹ P°
2p ⁵ (² P _{3/2} ^o)3d	² [⁷ / ₂] ^o	4	331 123.04	100	or	100	³ F°
		3	331 186.70	99	or	53	
2p ⁵ (² P _{3/2} ^o)4s	² [³ / ₂] ^o	2	331 496.51	68	or	68	³ P°
		1	331 873.93	63	or	48	
2p ⁵ (² P _{3/2} ^o)3d	² [⁵ / ₂] ^o	2	331 665.59	88	or	57	³ F°
		3	331 707.90	89	or	46	³ D°
2p ⁵ (² P _{1/2} ^o)4s	² [¹ / ₂] ^o	0	332 710.11	97	or	97	³ P°
		1	333 162.94	79	or	58	¹ P°
2p ⁵ (² P _{1/2} ^o)3d	² [⁵ / ₂] ^o	2	332 802.21	88	or	43	³ F°
		3	332 841.93	89	or	54	³ D°
2p ⁵ (² P _{1/2} ^o)3d	² [³ / ₂] ^o	2	332 962.57	85	or	51	³ D°
		1	333 107.74	83	or	61	
2p ⁵ (² P _{3/2} ^o)4p	² [¹ / ₂]	1	340 239.8	87	or	94	³ S
		0		96	or	53	³ P

Na II—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Leading percentages			
$2p^5(^2P_{3/2}^{\circ})4p$	$2[{}^5_2]$	3	341 255.6	100	or	100	3D
		2	341 457.7	81	or	70	
$2p^5(^2P_{3/2}^{\circ})4p$	$2[{}^3_2]$	1		94	or	41	1P
		2?	341 907.0	83	or	67	3P
$2p^5(^2P_{1/2}^{\circ})4p$	$2[{}^3_2]$	1	342 738.6	94	or	62	3D
		2		96	or	44	1D
$2p^5(^2P_{1/2}^{\circ})4p$	$2[{}^1_2]$	1	342 971.0	87	or	64	3P
		0		96	or	53	1S
$2p^5(^2P_{3/2}^{\circ})4d$	$2[{}^1_2]^{\circ}$	0	<i>352 969.8</i>				
		1	<i>353 032.9</i>				
$2p^5(^2P_{3/2}^{\circ})4d$	$2[{}^3_2]^{\circ}$	2	<i>353 151.8</i>				
		1	<i>353 600.6</i>				
$2p^5(^2P_{3/2}^{\circ})4d$	$2[{}^7_2]^{\circ}$	4	<i>353 202.6</i>				
		3	<i>353 240.4</i>				
$2p^5(^2P_{3/2}^{\circ})4d$	$2[{}^5_2]^{\circ}$	2	<i>353 463.2</i>				
		3	<i>353 483.8</i>				
$2p^5(^2P_{3/2}^{\circ})5s$	$2[{}^3_2]^{\circ}$	2	<i>353 536.7</i>				
		1	<i>353 719.3</i>				
$2p^5(^2P_{3/2}^{\circ})4f$	$2[{}^3_2]$	1	353 837.23				
		2	353 838.44				
$2p^5(^2P_{3/2}^{\circ})4f$	$2[{}^9_2]$	5	353 881.13				
		4	353 881.16				
$2p^5(^2P_{3/2}^{\circ})4f$	$2[{}^5_2]$	3	353 925.81				
		2	353 926.69				
$2p^5(^2P_{3/2}^{\circ})4f$	$2[{}^7_2]$	3	353 972.42				
		4	353 972.63				
$2p^5(^2P_{1/2}^{\circ})4d$	$2[{}^5_2]^{\circ}$	2	<i>354 526.3</i>				
		3	<i>354 559.2?</i>				
$2p^5(^2P_{1/2}^{\circ})4d$	$2[{}^3_2]^{\circ}$	2	<i>354 707.0</i>				
		1	<i>354 876.5</i>				
$2p^5(^2P_{1/2}^{\circ})5s$	$2[{}^1_2]^{\circ}$	0	<i>354 859.8</i>				
		1	<i>354 997.8</i>				
$2p^5(^2P_{1/2}^{\circ})4f$	$2[{}^7_2]$	3	355 280.89				
		4	355 281.16				
$2p^5(^2P_{1/2}^{\circ})4f$	$2[{}^5_2]$	3	355 283.70				
		2	355 284.53				
$2p^5(^2P_{3/2}^{\circ})5d$	$2[{}^1_2]^{\circ}$	0	<i>363 332.2</i>				
		1	<i>363 347.4</i>				

ENERGY LEVELS OF SODIUM

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Na II—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Leading percentages
$2p^5(^2P_{3/2}^{\circ})5d$	$2[{}^3/2]_{\circ}$	2	363 441.7	
		1	363 631.9	
$2p^5(^2P_{3/2}^{\circ})6s$	$2[{}^3/2]_{\circ}$	2	363 610.2	
		1	363 725.8	
$2p^5(^2P_{3/2}^{\circ})5f$	$2[{}^3/2]$	1	363 767.98	
		2	363 769.03	
$2p^5(^2P_{3/2}^{\circ})5f$	$2[{}^3/2]$	5	363 790.60	
		4	363 790.64	
$2p^5(^2P_{3/2}^{\circ})5f$	$2[{}^5/2]$	3	363 814.78	
		2	363 815.38	
$2p^5(^2P_{3/2}^{\circ})5f$	$2[{}^7/2]$	3	363 837.82	
		4	363 837.94	
$2p^5(^2P_{1/2}^{\circ})5d$	$2[{}^3/2]_{\circ}$	2	364 744.1	
		1	364 931.1	
$2p^5(^2P_{1/2}^{\circ})6s$	$2[{}^1/2]_{\circ}$	0	365 009.9	
		1	365 043.5	
$2p^5(^2P_{1/2}^{\circ})5f$	$2[{}^7/2]$	3	365 173.42	
		4	365 173.7	
$2p^5(^2P_{1/2}^{\circ})5f$	$2[{}^5/2]$	3	365 174.10	
		2		
$2p^5(^2P_{3/2}^{\circ})6d$	$2[{}^1/2]_{\circ}$	0		
		1	368 494.1	
$2p^5(^2P_{3/2}^{\circ})7s$	$2[{}^3/2]_{\circ}$	2		
		1	369 070.5	
$2p^5(^2P_{3/2}^{\circ})6f$	$2[{}^3/2]$	1	369 158.71	
		2	369 159.46	
$2p^5(^2P_{3/2}^{\circ})6f$	$2[{}^9/2]$	5	369 171.93	
		4	369 172.01	
$2p^5(^2P_{3/2}^{\circ})6g$	$2[{}^5/2]_{\circ}$	3,2	369 184.02	
$2p^5(^2P_{3/2}^{\circ})6f$	$2[{}^5/2]$	3	369 186.50	
		2	369 186.73	
$2p^5(^2P_{3/2}^{\circ})6g$	$2[{}^{11/2}]_{\circ}$	6,5	369 189.22	
$2p^5(^2P_{3/2}^{\circ})6g$	$2[{}^7/2]_{\circ}$	4,3	369 198.7	
$2p^5(^2P_{3/2}^{\circ})6f$	$2[{}^7/2]$	3,4	369 199.6	
$2p^5(^2P_{3/2}^{\circ})6g$	$2[{}^9/2]_{\circ}$	5,4	369 203.4	
$2p^5(^2P_{1/2}^{\circ})6d$	$2[{}^3/2]_{\circ}$	2		
		1	370 035.6	

Na II—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Leading percentages
$2p^5(^2P_{1/2}^{\circ})7s$	$2[1/2]^{\circ}$	0	370 378.6	
		1		
$2p^5(^2P_{1/2}^{\circ})6f$	$2[7/2]$	3,4	370 547.8	
$2p^5(^2P_{1/2}^{\circ})6f$	$2[5/2]$	3	370 548.06?	
		2	370 548.50?	
$2p^5(^2P_{1/2}^{\circ})6g$	$\left\{ \begin{array}{l} 2[9/2]^{\circ} \\ 2[7/2]^{\circ} \end{array} \right.$	5,4	370 560.6	
		4,3		
$2p^5(^2P_{3/2}^{\circ})7f$	$2[3/2]$	1	372 407.6	
		2	372 407.9	
$2p^5(^2P_{3/2}^{\circ})7f$	$2[9/2]$	5,4	372 415.9	
$2p^5(^2P_{3/2}^{\circ})7g$	$2[5/2]^{\circ}$	3,2	372 423.4	
$2p^5(^2P_{3/2}^{\circ})7f$	$2[5/2]$	3,2	372 425.4	
$2p^5(^2P_{3/2}^{\circ})7g$	$2[11/2]^{\circ}$	6,5	372 426.7	
$2p^5(^2P_{3/2}^{\circ})7g$	$2[7/2]^{\circ}$	4,3	372 432.3	
$2p^5(^2P_{3/2}^{\circ})7f$	$2[7/2]$	4,3	372 433.3	
$2p^5(^2P_{3/2}^{\circ})7g$	$2[9/2]^{\circ}$	5,4	372 436.2	
$2p^5(^2P_{1/2}^{\circ})7f$	$2[7/2]$	4,3	373 787.8	
$2p^5(^2P_{1/2}^{\circ})7f$	$2[5/2]$	3,2	373 788.1	
$2p^5(^2P_{1/2}^{\circ})7g$	$\left\{ \begin{array}{l} 2[9/2]^{\circ} \\ 2[7/2]^{\circ} \end{array} \right.$	5,4	373 796.4	
		4,3		
$2p^5(^2P_{3/2}^{\circ})8f$	$2[3/2]$	2,1	374 514.9	
$2p^5(^2P_{3/2}^{\circ})8f$	$2[9/2]$	5,4	374 520.3	
$2p^5(^2P_{3/2}^{\circ})8f$	$2[7/2]$	4,3	374 532.1	
$2p^5(^2P_{1/2}^{\circ})8f$	$\left\{ \begin{array}{l} 2[7/2] \\ 2[5/2] \end{array} \right.$	4,3	375 890.0	
		3,2		
Na III ($^2P_{3/2}^{\circ}$)	<i>Limit</i>		381 390.2	
Na III ($^2P_{1/2}^{\circ}$)	<i>Limit</i>		382 756.5	
$2s2p^6 3s$	3S	1	531 810	
$2s2p^6 3s$	1S	0	535 840	
$2s2p^6 3p$	$^3P^{\circ}$	0-2	562 780	

ENERGY LEVELS OF SODIUM

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Na II—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Leading percentages
$2s2p^6 3p$	$^1P^\circ$	1	564 210	
$2s2p^6 4p$	$^1P^\circ$	1	606 350	
$2s2p^6 5p$	$^1P^\circ$	1	622 430	
$2s2p^6 6p$	$^1P^\circ$	1	630 240	
$2s2p^6 7p$	$^1P^\circ$	1	634 720	
$2s2p^6 8p$	$^1P^\circ$	1	637 430	
Na III $2s2p^6(^2S_{1/2})$	<i>Limit</i>		645 845	

Na III

Z = 11

F I isoelectronic sequence

Ground state $1s^2 2s^2 2p^5 \ ^2P^{\circ}_{3/2}$ Ionization energy $577\,654\text{ cm}^{-1}$ (71.6205 eV)

The levels are from new observations and analysis of the spectrum by Lundström and Minnhagen [1972], Minnhagen and Nietsche [1972], and Minnhagen [1975]. Lundström and Minnhagen give wavelengths for 90 Na III lines in the 181–380 Å range and for the $2s2p^6 \ ^2S_{1/2} - 2s^2 2p^4(^3P)3p \ ^2P^{\circ}_{3/2}$ line at 649.5 Å. Their measurements allowed determination of the $2s^2 2p^5 \ ^2P^{\circ}$ interval to better than $\pm 1\text{ cm}^{-1}$, the $2s2p^6 \ ^2S_{1/2}$ level and the $2s^2 2p^4(^3P)3s$, $3p$, $3d$, and $4s$ levels being determined to about ± 1.5 to $\pm 2.5\text{ cm}^{-1}$ with respect to the ground level. The $2s^2 2p^4(^1D)3s$, $3p$, $3d$, and $4s$ levels should be accurate to about $\pm 3\text{ cm}^{-1}$ relative to the ground level, the $(^1S)3s$, $3p$, $3d$, and $4s$ levels to about $\pm 4\text{ cm}^{-1}$, and the $2s^2 2p^4 4d$ and $5s$ levels to about $\pm 6\text{ cm}^{-1}$. Most of the levels are from Minnhagen and Nietsche, who also list the wavelengths and classifications of 177 lines in the 1325–2638 Å region. They established the relative positions of the $(^3P)3s$, $3p$, $3d$, and $4s$ levels to ± 0.1 to $\pm 0.2\text{ cm}^{-1}$, and the relative positions within the $(^1D)3s$, $3p$, $3d$, $4s$ group to about the same uncertainties; the uncertainties of differences between these two groups are about $\pm 0.5\text{ cm}^{-1}$. The $(^1S)3s$, $3p$, and $3d$ levels are internally consistent to about 0.15 cm^{-1} , and the $(^1S)4s \ ^2S$ level should be accurate to about $\pm 0.5\text{ cm}^{-1}$ with respect to this group. These levels having 1S parentage are connected to the groups based on 3P and 1D only through ground-term combinations.

Minnhagen classified about 80 lines (1755–2010 Å) as $2p^4 3d-4f$ transitions. Most of the $2p^4 4f$ levels are accurate to about ± 0.1 to $\pm 0.3\text{ cm}^{-1}$ with respect to the $2p^4 3d$ levels, which means an uncertainty of about $\pm 3\text{ cm}^{-1}$ relative to the ground level.

A significant feature of the level determinations by Minnhagen and Nietsche is that the quartet-doublet level differences, within and between the different configuration groups as discussed above, have the same accuracies as corresponding differences within the multiplicity systems. Minnhagen and Nietsche give details of their extension and revision of the term system. Most of the previously known levels retained by them were first located by Söderqvist

[1934], whose monograph includes references to earlier work on Na III.

The leading percentages for the $2p^4 3p$ and $2p^4 3d$ levels are from Minnhagen and Nietsche, who list all percentages $\geq 3\%$. The LS -coupling purities of the $2p^4 3p$ levels are mostly high, but two of the $2p^4 3d$ levels ($J=5/2$) have the same $2p^4(^3P)3d \ ^2D$ leading component. The designations here are those of Minnhagen and Nietsche, except that we omit any name for one of these levels, $465\,398\text{ cm}^{-1}$. Minnhagen and Nietsche also calculated the $2p^4 3s$ and $2p^4 4s$ levels. The LS purities are high, the largest mixing being between $2p^4(^3P)4s \ ^4P_{3/2}$ and $^2P_{3/2}$ (a 6% mixture in each of the two eigenvectors).

Minnhagen notes that the $2p^4 4f$ levels fall into five groups, according to the $2p^4$ parent levels, and are further grouped into close pairs. The leading percentages in the $J_1 l$ coupling scheme, from Minnhagen's paper, verify the high purity of these levels in this scheme. The missing $2p^4(^1S_0)4f \ ^2[3]^{\circ}$ level pair is calculated to lie near $582\,270\text{ cm}^{-1}$, i.e., above the Na IV $2p^4 \ ^3P$ limits, and Minnhagen notes matrix elements allowing autoionization from these levels.

Johannesson and Lundström derived the ionization energy by careful isoelectronic interpolation. No estimate of the error was given, but it may be comparable to the error of $\pm 10\text{ cm}^{-1}$ estimated for their Mg IV limit determination.

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ENERGY LEVELS OF SODIUM

Na III

Configuration	Term	J	Level (cm ⁻¹)	Leading percentages
2s ² 2p ⁵	2P°	3/2	0.0	
		1/2	1 366.3	
2s2p ⁶	2S	1/2	264 455.0	
2s ² 2p ⁴ (3P)3s	4P	5/2	366 154.41	
		3/2	367 040.66	
		1/2	367 550.17	
2s ² 2p ⁴ (3P)3s	2P	3/2	373 632.32	
		1/2	374 679.91	
2s ² 2p ⁴ (1D)3s	2D	5/2	399 174.71	
		3/2	399 182.31	
2s ² 2p ⁴ (3P)3p	4P°	5/2	406 190.15	99
		3/2	406 550.63	99
		1/2	406 865.11	100
2s ² 2p ⁴ (3P)3p	4D°	7/2	410 976.94	100
		5/2	411 536.38	97
		3/2	411 951.78	98
		1/2	412 189.46	100
2s ² 2p ⁴ (3P)3p	2D°	5/2	414 281.85	98
		3/2	415 172.28	98
2s ² 2p ⁴ (3P)3p	2S°	1/2	416 909.31	80 16 3P°
2s ² 2p ⁴ (3P)3p	4S°	3/2	417 403.98	99
2s ² 2p ⁴ (3P)3p	2P°	3/2	418 417.50	85 13 (1D) 3P°
		1/2	418 556.54	69 20 3S°
2s ² 2p ⁴ (1S)3s	2S	1/2	435 028.00	
2s ² 2p ⁴ (1D)3p	2F°	5/2	440 940.20	100
		7/2	441 055.67	100
2s ² 2p ⁴ (1D)3p	2D°	3/2	445 797.52	99
		5/2	445 873.20	100
2s ² 2p ⁴ (1D)3p	2P°	3/2	447 547.96	86
		1/2	448 107.31	86
2s ² 2p ⁴ (3P)3d	4D	7/2	460 257.21	98
		5/2	460 409.70	99
		3/2	460 593.62	99
		1/2	460 746.98	99
2s ² 2p ⁴ (3P)3d	4F	9/2	462 891.04	99
		7/2	463 245.76	99
		5/2	463 691.90	99
		3/2	464 077.16	99
2s ² 2p ⁴ (3P)3d	2F	7/2	463 970.91	99

Na III—Continued

Configuration	Term	J	Level (cm ⁻¹)	Leading percentages		
$2s^2 2p^4(^3P)3d$	2D	$\frac{5}{2}$	464 390.17	44	32	2F
		$\frac{3}{2}$	465 017.83	76	14	4P
$2s^2 2p^4(^3P)3d$	4P	$\frac{1}{2}$	464 411.94	99		
		$\frac{3}{2}$	464 631.29	82	10	2D
		$\frac{5}{2}$	464 945.37	56	37	2F
$2s^2 2p^4(^3P)3d$		$\frac{5}{2}$	465 398.59	42	2D	35 4P
$2s^2 2p^4(^3P)3d$	2P	$\frac{1}{2}$	466 011.91	98		
		$\frac{3}{2}$	466 788.03	93	6	2D
$2s^2 2p^4(^1S)3p$	$^2P^\circ$	$\frac{1}{2}$	478 842.99	99		
		$\frac{3}{2}$	478 884.07	99		
$2s^2 2p^4(^3P)4s$	4P	$\frac{5}{2}$	479 975.34			
		$\frac{3}{2}$	480 779.21			
		$\frac{1}{2}$	481 358.65			
$2s^2 2p^4(^3P)4s$	2P	$\frac{3}{2}$	482 402.20			
		$\frac{1}{2}$	483 388.55			
$2s^2 2p^4(^1D)3d$	2G	$\frac{9}{2}$	492 313.91	100		
		$\frac{7}{2}$	492 316.41	100		
$2s^2 2p^4(^1D)3d$	2P	$\frac{3}{2}$	493 192.06	99		
		$\frac{1}{2}$	493 293.98	99		
$2s^2 2p^4(^1D)3d$	2S	$\frac{1}{2}$	493 849.24	100		
$2s^2 2p^4(^1D)3d$	2D	$\frac{5}{2}$	494 602.73	99		
		$\frac{3}{2}$	494 685.86	99		
$2s^2 2p^4(^1D)3d$	2F	$\frac{5}{2}$	495 429.75	100		
		$\frac{7}{2}$	495 435.20	100		
$2s^2 2p^4(^1D)4s$	2D	$\frac{3}{2}$	511 433.8			
		$\frac{5}{2}$	511 434.3			
$2s^2 2p^4(^3P)4d$	4F	$\frac{5}{2}$	514 007			
		$\frac{3}{2}$	514 241			
$2s^2 2p^4(^3P)4d$	4P	$\frac{3}{2}$	514 069			
		$\frac{5}{2}$	514 608?			
$2s^2 2p^4(^3P)4d$	2F	$\frac{5}{2}$	514 688			
$2s^2 2p^4(^3P)4d$	2D	$\frac{3}{2}$	515 017			
		$\frac{5}{2}$	515 365			
$2s^2 2p^4(^3P)4d$	2P	$\frac{1}{2}$	515 140			
		$\frac{3}{2}$	515 984			
$2s^2 2p^4(^3P_2)4f$	$^2[4]^\circ$	$\frac{9}{2}$	515 595.6	98		
		$\frac{7}{2}$	515 607.27	93	5	$^2[3]^\circ$
$2s^2 2p^4(^3P_2)4f$	$^2[3]^\circ$	$\frac{5}{2}$	515 635.09	98		
		$\frac{7}{2}$	515 635.4	93	5	$^2[4]^\circ$

ENERGY LEVELS OF SODIUM

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Na III—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Leading percentages		
$2s^2 2p^4 ({}^3P_2) 4f$	$2[2]^\circ$	$\frac{3}{2}$	515 764.23	94	6	$({}^3P_1) 2[2]^\circ$
		$\frac{5}{2}$	515 773.67	94	5	
$2s^2 2p^4 ({}^3P_2) 4f$	$2[5]^\circ$	$\frac{11}{2}$	515 871.96	100		
		$\frac{9}{2}$	515 872.81	100		
$2s^2 2p^4 ({}^3P_2) 4f$	$2[1]^\circ$	$\frac{1}{2}$	515 994.5	100		
		$\frac{3}{2}$	516 000.6	100		
$2s^2 2p^4 ({}^3P_1) 4f$	$2[2]^\circ$	$\frac{3}{2}$	516 817.76	94	6	$({}^3P_2) 2[2]^\circ$
		$\frac{5}{2}$	516 823.62	95	5	
$2s^2 2p^4 ({}^3P_1) 4f$	$2[4]^\circ$	$\frac{9}{2}$	516 859.91	98		
		$\frac{7}{2}$	516 864.62	98		
$2s^2 2p^4 ({}^3P_1) 4f$	$2[3]^\circ$	$\frac{7}{2}$	517 029.6	99		
		$\frac{5}{2}$	517 033.0	99		
$2s^2 2p^4 ({}^3P_0) 4f$	$2[3]^\circ$	$\frac{7}{2}$	517 374.54	98		
		$\frac{5}{2}$	517 377.58	98		
$2s^2 2p^4 ({}^3P) 5s$	$2P$	$\frac{3}{2}$	522 720			
		$\frac{1}{2}$	523 527			
$2s^2 2p^4 ({}^1S) 3d$	$2D$	$\frac{5}{2}$	529 461.64	100		
		$\frac{3}{2}$	529 497.70	99		
$2s^2 2p^4 ({}^1D) 4d$	$2S$	$\frac{1}{2}$	543 640			
$2s^2 2p^4 ({}^1D) 4d$	$2P$	$\frac{3}{2}$	544 226			
		$\frac{1}{2}$	544 278			
$2s^2 2p^4 ({}^1D) 4d$	$2D$	$\frac{5}{2}$	544 749			
		$\frac{3}{2}$	544 788			
$2s^2 2p^4 ({}^1D) 4d$	$2F$	$\frac{5}{2}$	544 915			
$2s^2 2p^4 ({}^1D_2) 4f$	$2[1]^\circ$	$\frac{3}{2}$	546 187.1?	100		
		$\frac{1}{2}$		100		
$2s^2 2p^4 ({}^1D_2) 4f$	$2[5]^\circ$	$\frac{11}{2}$	546 440.3	100		
		$\frac{9}{2}$	546 441.0	100		
$2s^2 2p^4 ({}^1D_2) 4f$	$2[2]^\circ$	$\frac{3}{2}$	546 509.3	100		
		$\frac{5}{2}$	546 510.55?	100		
$2s^2 2p^4 ({}^1D_2) 4f$	$2[3]^\circ$	$\frac{7}{2}$	546 810.1	100		
		$\frac{5}{2}$	546 811	100		
$2s^2 2p^4 ({}^1D_2) 4f$	$2[4]^\circ$	$\frac{7}{2}$	546 887.36	100		
		$\frac{9}{2}$	546 888.34	100		
$2s^2 2p^4 ({}^1S) 4s$	$2S$	$\frac{1}{2}$	547 910.7			

Na III—Continued

Configuration	Term	J	Level (cm ⁻¹)	Leading percentages
$2s^2 2p^4 ({}^1D) 5s$	2D	$\frac{3}{2}$	552 404	
		$\frac{5}{2}$	552 416?	
<hr/>				
Na IV (3P_2)	<i>Limit</i>		577 654	
Na IV (3P_1)	<i>Limit</i>		578 760	
Na IV (3P_0)	<i>Limit</i>		579 230	
Na IV (1D_2)	<i>Limit</i>		608 494	
Na IV (1S_0)	<i>Limit</i>		644 150	

Na IV

Z=11

O I isoelectronic sequence

Ground state $1s^2 2s^2 2p^4 \ ^3P_2$ Ionization energy 797 800 cm^{-1} (98.92 eV)

Söderqvist's analysis of this spectrum included classification of 73 lines in the 129–412 Å region as transitions to the $2s^2 2p^4$ ground-configuration levels from upper $2s2p^5$ and $2s^2 2p^3 ns, nd$ singlet and triplet levels [Söderqvist, 1934]. A few $2s^2 2p^3 3s-3p$ and $3p-3d$ transitions as observed in beam-foil spectra were classified by Gaillard et al. and by Dufay et al. Minnhagen [1976] has used new observations of the 136–412 Å and 1456–2156 Å regions to make a major extension of the analysis and to improve the values of most of the previously known levels. A total of about 150 lines are classified.

The triplet and singlet terms are from Minnhagen's paper, except for the $2p^6 \ ^1S$ level, which is from Edlén [1980]. Minnhagen determined the $2s^2 2p^4 \ ^3P$ and $2s2p^5 \ ^3P^\circ$ levels to about $\pm 1 \text{ cm}^{-1}$. We list the $2s^2 2p^4 \ ^1D_2$ level to the nearest 0.1 cm^{-1} , since its determination from the $2s^2 2p^4 \ ^3P-^1D$ nebular lines [Bowen, 1960] should be accurate to about $\pm 1 \text{ cm}^{-1}$. The $2s^2 2p^4 \ ^1S$, $2s2p^5 \ ^1P^\circ$, and $2p^6 \ ^1S$ levels are probably accurate to about $\pm 2 \text{ cm}^{-1}$. The uncertainties of the higher triplet and singlet levels with respect to the ground term are generally larger, increasing to about $\pm 10 \text{ cm}^{-1}$ for some of the highest levels. The relative positions of those higher levels given to the nearest 0.1 cm^{-1} , however, should be accurate to about ± 0.2 to $\pm 0.4 \text{ cm}^{-1}$.

Minnhagen also established the levels of the three quintet terms with good relative accuracy, but no lines connecting them with the triplet and singlet systems have been classified. An unknown common correction "x" is thus added to each quintet level. The position of the quintet system for $x=0$ is a prediction based on the values of the $2s^2 2p^3 (^4S) 3s \ ^5S^\circ$ and $(^4S) 3d \ ^5D^\circ$ terms calculated by Kaufman and Wyart [1980] and the experimental separation of these two terms. This prediction differs by only 80 cm^{-1} from the connection predicted by Minnhagen, and the standard error is about 300 cm^{-1} .

Söderqvist [1946] and Minnhagen have located one term belonging to a configuration of the type $2s2p^4 nl$ ($n \geq 3$), the $2s2p^4 (^4P) 3d \ ^3D$ term lying above the ionization limit. Buchet and Buchet-Poulizac classified a line at 220 Å as the unresolved Na IV multiplet $2s2p^5 \ ^3P^\circ - 2s2p^4 (^4P) 3s \ ^3P$. The resulting $2s2p^4 (^4P) 3s \ ^3P$ position near $699\,000 \text{ cm}^{-1}$ appears consistent with the data for Mg V and Al VI, but we have not included the term here pending more accurate wavelength measurements and resolution of the fine structure.

Minnhagen's paper includes the results of theoretical calculations of the $2s^2 2p^3 3s$, $3p$ and $3d$ configurations. The leading eigenvector percentages given here for the $2s^2 2p^3 3p$

levels are from these calculations, some of the percentages close to 100% and some smaller second percentages being from a private communication [Minnhagen, 1980]. Minnhagen [1976] notes a few doubtful points in the analysis and includes comparisons of several configurations along the isoelectronic sequence.

The leading percentages for the $2s2p^5$, $2s^2 2p^3 3s$, and $2s^2 2p^3 3d$ levels are from a recent calculation that included the interactions of these three odd-parity configurations [Kaufman and Wyart, 1980; see Artru and Kaufman, 1980]. Although the configuration mixing in the eigenvectors is at most a few percent, Artru and Kaufman found inclusion of the configuration interactions important to account for rather large displacements of several terms from their predicted single-configuration positions.

The ground-configuration $2s^2 2p^4$ levels are very pure in LS coupling, but the small mixing of the two $J=2$ states and of the two $J=0$ states is important for calculation of forbidden-line transition probabilities. Garstang gives expansion formulae for the mixing coefficients for the p^2 and p^4 configurations. These formulae and his values for the spin interaction parameters give 0.057% mixing of the Na IV $2s^2 2p^4 \ ^3P_2$ and 1D_2 states and 0.18% mixing of the 3P_0 and 1S_0 states (these being the squares of Garstang's coefficients b and d , respectively, expressed as percentages).

The ionization energy was derived by Edlén [1964] from formulae adjusted to give a best fit for the isoelectronic data. His value agrees well with the value given by Söderqvist, $797\,741 \text{ cm}^{-1}$. No uncertainty was stated, but an error greater than a few hundred cm^{-1} is unlikely.

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Na IV

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Leading percentages	
$2s^2 2p^4$	3P	2	0.0		
		1	1 106.3		
		0	1 576.0		
$2s^2 2p^4$	1D	2	30 839.8		
$2s^2 2p^4$	1S	0	66 496		
$2s 2p^5$	$^3P^\circ$	2	243 681.9	99	
		1	244 687.6	99	
		0	245 238.8	99	
$2s 2p^5$	$^1P^\circ$	1	343 688	99	1 $2p^3(^2D^\circ)3d \ ^1P^\circ$
$2s^2 2p^3(^4S^\circ)3s$	$^5S^\circ$	2	473 950.0+x	100	
$2s^2 2p^3(^4S^\circ)3s$	$^3S^\circ$	1	486 650.2	100	
$2s^2 2p^3(^4S^\circ)3p$	5P	1	524 773.3+x	100	
		2	524 838.6+x	100	
		3	524 950.6+x	100	
$2s^2 2p^3(^2D^\circ)3s$	$^3D^\circ$	3	525 085	100	
		2	525 117	100	
		1	525 139	100	
$2s^2 2p^3(^2D^\circ)3s$	$^1D^\circ$	2	531 410	99	
$2s^2 2p^3(^4S^\circ)3p$	3P	1	536 159.1	94	5 $(^2D^\circ) \ ^3P$
		2	536 178.8	94	5
		0	536 184.9	94	5
$2s^2 2p^3(^2P^\circ)3s$	$^3P^\circ$	1	550 157	99	1 $2p^3(^2D^\circ)3d \ ^3P^\circ$
		0	550 158?	99	1
		2	550 186	99	1
$2s^2 2p^3(^2P^\circ)3s$	$^1P^\circ$	1	556 796	99	1 $2p^3(^2D^\circ)3d \ ^1P^\circ$
$2p^6$	1S	0	570 823		
$2s^2 2p^3(^2D^\circ)3p$	3D	1	572 379.5	92	6 $(^2P^\circ) \ ^3D$
		2	572 393.8	94	5
		3	572 546.0	95	5
$2s^2 2p^3(^2D^\circ)3p$	3F	2	575 768.1	99	1 $(^2D^\circ) \ ^3D$
		3	575 821.0	99	1
		4	575 886.6	100	
$2s^2 2p^3(^2D^\circ)3p$	1F	3	577 782.7	100	

ENERGY LEVELS OF SODIUM

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Na IV—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Leading percentages	
2s ² 2p ³ (⁴ S°)3d	⁵ D°	4	587 960.7+x	100	
		3	587 964.3+x	100	
		2	587 971.2+x	100	
		1	587 977.2+x	100	
		0	587 979.6+x	100	
2s ² 2p ³ (⁴ S°)3d	³ D°	1	594 888.1	99	1 (² D°) ³ D°
		2	594 899.2	99	1
		3	594 934	99	1
2s ² 2p ³ (² D°)3p	¹ D	2	596 578.9	96	2 (² P°) ¹ D
2s ² 2p ³ (² P°)3p	³ D	3	600 509.6	95	4 (² D°) ³ D
		2	600 534.1	94	5
		1	600 567.7	94	6
2s ² 2p ³ (² P°)3p	¹ P	1	606 831?	75	14 (² D°) ¹ P
2s ² 2p ³ (² P°)3p	¹ D	2	612 611?	98	2 (² D°) ¹ D
2s ² 2p ³ (² D°)3d	³ F°	2	635 566.0	97	2 (² P°) ³ F°
		3	635 675.6	97	2
		4	635 817.2	98	1
2s ² 2p ³ (² D°)3d	³ G°	5	637 669.6	100	
		4	637 705.1	99	1 (² D°) ³ F°
		3	637 728.0	99	1
2s ² 2p ³ (² D°)3d	¹ G°	4	638 188.6	99	
2s ² 2p ³ (² D°)3d	³ D°	3	638 825	98	1 (⁴ S°) ³ D°
		2	638 943	99	1
		1	639 007	99	1
2s ² 2p ³ (² D°)3d	¹ P°	1	641 193	95	2 (² P°) ¹ P°
2s ² 2p ³ (² D°)3d	³ P°	2	643 052	97	2 (² P°) ³ P°
		1	643 311	95	2 (² D°) ³ S°
		0	643 420?	98	1 2p ³ (² P°)3s ³ P°
2s ² 2p ³ (² D°)3d	¹ D°	2	643 625.6	94	6 (² P°) ¹ D°
2s ² 2p ³ (² D°)3d	³ S°	1	644 166	97	2 (² D°) ³ P°
2s ² 2p ³ (⁴ S°)4s	³ S°	1	644 819		
2s ² 2p ³ (² D°)3d	¹ F°	3	646 419.6	100	
2s ² 2p ³ (² P°)3d	³ P°	0	663 137?	99	
		1	663 509	99	1 (¹) (¹)
		2	663 623	98	?
2s ² 2p ³ (² P°)3d	³ F°	4	663 150.5	98	1 (¹) (¹)
		3	663 176.3	98	
		2	663 212.4	96	
2s ² 2p ³ (² P°)3d	¹ D°	2	664 637	91	2 (¹) (¹)

Na IV—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Leading percentages		
2s ² 2p ³ (² P°)3d	³ D°	3	665 344	98	1	(² D°) ³ D°
		2	665 370	91	6	(² P°) ¹ D°
		1	665 400	99		
2s ² 2p ³ (² P°)3d	¹ F°	3	667 442	100		
2s ² 2p ³ (² P°)3d	¹ P°	1	673 140	98	2	(² D°) ¹ P°
2s ² 2p ³ (⁴ S°)4d	³ D°	2	684 626			
		3	684 630			
		1	684 640			
2s ² 2p ³ (² D°)4s	³ D°	3	689 753			
		2	689 789			
		1	689 808			
2s ² 2p ³ (² D°)4s	¹ D°	2	691 781			
2s ² 2p ³ (² P°)4s	³ P°	0	714 468?			
		1	714 468			
		2	714 483			
2s ² 2p ³ (² P°)4s	¹ P°	1	716 509			
2s ² 2p ³ (² D°)4d	³ D°	3	730 702			
		2	730 728			
		1	730 742			
2s ² 2p ³ (² D°)4d	¹ P°	1	731 684			
2s ² 2p ³ (² D°)4d	³ P°	2	732 325			
		1	732 346			
		0				
2s ² 2p ³ (² D°)4d	³ S°	1	732 979			
2s ² 2p ³ (² D°)4d	¹ D°	2	733 288			
2s ² 2p ³ (² D°)4d	¹ F°	3	733 919			
2s ² 2p ³ (² P°)4d	¹ D°	2	755 785			
2s ² 2p ³ (² P°)4d	¹ F°	3	756 995			
Na v (⁴ S _{3/2})	<i>Limit</i>		797 800			
2s2p ⁴ (⁴ P)3d	³ D	3	813 494			
		2	813 527			
		1	813 648?			

Na V

Z=11

N I isoelectronic sequence

Ground state $1s^2 2s^2 2p^3 \ ^4S_{3/2}$ Ionization energy $1\ 116\ 300\ \text{cm}^{-1}$ (138.40 eV)

Söderqvist observed and analyzed this spectrum, his 1946 paper giving 103 lines classified as Na V transitions in the region 100–515 Å. The line list of Goto, Gautam, and Joshi includes a few additional lines classified as transitions between Na V levels from Söderqvist's analysis (163–1806 Å).

We have reevaluated the doublet levels, based on the quartet-doublet intersystem connection discovered by Edlén [1964] and consideration of the entire combination array. A value of $-36\ \text{cm}^{-1}$ is adopted for both intervals $2s^2 2p^3 \ ^2D_{3/2}^{\circ} - ^2D_{3/2}^{\circ}$ and $2s2p^4 \ ^2D_{5/2} - ^2D_{3/2}$, this value for the former interval agreeing somewhat better with the observations and with Edlén's [1972] predicted value of $-46\ \text{cm}^{-1}$ than does Söderqvist's value of $-25\ \text{cm}^{-1}$. The $2s2p^4 \ ^4P$ levels are probably accurate to within ± 10 to $\pm 15\ \text{cm}^{-1}$, and the doublet levels up to the $2p^5 \ ^2P^{\circ}$ term should have about this accuracy within the doublet system; the errors of intersystem differences may be several times larger, but the experimental system connection differs from Edlén's [1972] predicted value by only $23\ \text{cm}^{-1}$. Beginning a little below $900\ 000\ \text{cm}^{-1}$ we have rounded most of the levels to the nearest $10\ \text{cm}^{-1}$, since some of the levels in this region may have errors up to $\pm 100\ \text{cm}^{-1}$ or more.

A number of the upper levels appear questionable in that they are derived from single weak lines or lines also assigned to other ionization stages. Most such levels are assigned to $2s^2 2p^2 4s$, $4d$, or $5d$ terms. We have specifically indicated some of the more questionable doublet levels as tentative. Söderqvist's $2s^2 2p^2(^3P)4d \ ^2F_{5/2}$ and $2s^2 2p^2(^3P)4s \ ^4P_{3/2}$ levels are omitted, the former having two inconsistent combinations and the latter no combinations in the line list.

Söderqvist's [1946] value for the ionization energy as derived from series data is quoted above, to the nearest $100\ \text{cm}^{-1}$. Edlén's [1964] fit of semiempirical formulae to the isoelectronic sequence yielded a value $100\ \text{cm}^{-1}$ lower. No estimate of the uncertainty was given.

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Na v

Configuration	Term	J	Level (cm ⁻¹)	Configuration	Term	J	Level (cm ⁻¹)
$2s^2 2p^3$	$^4S^{\circ}$	$\frac{3}{2}$	0	$2p^5$	$^2P^{\circ}$	$\frac{3}{2}$ $\frac{1}{2}$	568 348 569 977
$2s^2 2p^3$	$^2D^{\circ}$	$\frac{5}{2}$ $\frac{3}{2}$	48 330 48 366	$2s^2 2p^2(^3P)3s$	4P	$\frac{1}{2}$ $\frac{3}{2}$ $\frac{5}{2}$	671 136 671 790 672 757
$2s^2 2p^3$	$^2P^{\circ}$	$\frac{1}{2}$ $\frac{3}{2}$	73 218 73 255	$2s^2 2p^2(^3P)3s$	2P	$\frac{1}{2}$ $\frac{3}{2}$	683 238 684 434
$2s2p^4$	4P	$\frac{5}{2}$ $\frac{3}{2}$ $\frac{1}{2}$	215 860 216 896 217 440	$2s^2 2p^2(^1D)3s$	2D	$\frac{3}{2}, \frac{1}{2}$	710 039
$2s2p^4$	2D	$\frac{5}{2}$ $\frac{3}{2}$	297 880 297 916	$2s^2 2p^2(^1S)3s$	2S	$\frac{1}{2}$	749 402
$2s2p^4$	2S	$\frac{1}{2}$	350 747	$2s^2 2p^2(^3P)3d$	2P	$\frac{3}{2}$ $\frac{1}{2}$	793 194 793 617
$2s2p^4$	2P	$\frac{3}{2}$ $\frac{1}{2}$	372 731 373 932	$2s^2 2p^2(^3P)3d$	4D	$\frac{7}{2}$ $\frac{5}{2}, \frac{3}{2}$ $\frac{1}{2}$	797 060 797 270

Na v—Continued

Configuration	Term	J	Level (cm^{-1})	Configuration	Term	J	Level (cm^{-1})
$2s^2 2p^2(^3P)3d$	2F	$5/2$	798 059	$2s^2 2p^2(^1D)4s$	2D	$5/2, 3/2$	928 830?
		$7/2$	799 295			$2s^2 2p^2(^3P)4d$	2P
$2s^2 2p^2(^3P)3d$	4P	$5/2$	798 174	$2s^2 2p^2(^3P)4d$	4D		
		$3/2$	798 620			$5/2, 3/2$	
		$1/2$	798 862			$1/2$	939 860
$2s2p^3(^5S^{\circ})3s$	$^4S^{\circ}$	$3/2$	801 950	$2s^2 2p^2(^3P)4d$	4P	$5/2$	940 720
$2s^2 2p^2(^3P)3d$	2D	$3/2$	809 314			$3/2$	940 930
		$5/2$	809 682			$1/2$	
$2s^2 2p^2(^1D)3d$	2F	$7/2$	829 269	$2s^2 2p^2(^3P)4d$	2F	$7/2$	942 150?
		$5/2$	829 463			$2s^2 2p^2(^3P)4d$	2D
$2s^2 2p^2(^1D)3d$	2D	$3/2$	832 846	$5/2$	945 100		
		$5/2$	832 988	$2s2p^3(^3D^{\circ})3p$	2F	$7/2$	950 220
$2s^2 2p^2(^1D)3d$	2P	$1/2$	838 200			$5/2$	950 760?
		$3/2$	838 485	$2s^2 2p^2(^1D)4d$	2F	$7/2, 5/2$	974 110?
$2s^2 2p^2(^1D)3d$	2S	$1/2$	842 829			$2s^2 2p^2(^1D)4d?$	$^2D?$
		$1/2-5/2$	847 539	$2s2p^3(^3D^{\circ})3d$	$^4P^{\circ}$		
$2s^2 2p^2(^1S)3d$	2D	$3/2, 5/2$	867 530?			$3/2$	1 004 620
		$1/2$				$1/2$	1 004 790
$2s2p^3(^3D^{\circ})3s$	$^4D^{\circ}$	$1/2-7/2$	878 320	$2s2p^3(^3D^{\circ})3d$	$^4D^{\circ}$	$1/2-7/2$	1 008 210
$2s^2 2p^2(^3P)4s$	4P	$1/2$	892 240			$2s2p^3(^3D^{\circ})3d$	$^4S^{\circ}$
		$3/2$		$2s2p^3(^3D^{\circ})3d$	$^2F^{\circ}$		
		$5/2$	893 820			$5/2$	1 011 330
$2s2p^3(^3D^{\circ})3s$	$^2D^{\circ}$	$3/2, 5/2$	894 860	$2s^2 2p^2(^1D)5d$	2F	$7/2, 5/2$	1 038 970?
$2s^2 2p^2(^3P)4s$	2P	$1/2$	896 715?			$2s^2 2p^2(^1D)5d$	2D
		$3/2$	897 910?				
$2s2p^3(^5S^{\circ})3d$	$^4D^{\circ}$	$1/2-7/2$	908 710				
$2s2p^3(^3P^{\circ})3s$	$^4P^{\circ}$	$1/2-5/2$	919 070				
				Na VI (3P_0)	<i>Limit</i>		1 116 300

ENERGY LEVELS OF SODIUM

Na VI

Z=11

CI isoelectronic sequence

Ground state $1s^2 2s^2 2p^2 \ ^3P_0$

Ionization energy $1\ 388\ 750 \pm 400\ \text{cm}^{-1}$ ($172.18 \pm 0.05\ \text{eV}$)

The levels are based mainly on the observations and analysis by Söderqvist, whose 1946 paper gives 134 lines assigned to Na VI in the range 80–638 Å. Fawcett measured and classified the three $2s2p^3-2p^4$ lines arising from the $2p^4 \ ^1D_2$ and $\ ^1S_0$ levels; the isoelectronic data showed that Söderqvist's value for the former level was incorrect [Fawcett, 1971, Anno and Teruya, 1971]. Goto, Gautam, and Joshi gave a number of new lines in the 119–2205 Å range as belonging to this spectrum.

We have redetermined or confirmed the level values. Most of the $2s^2 2p^2$, $2s2p^3$, and $2p^4$ triplet levels are probably accurate to about $\pm 15\ \text{cm}^{-1}$. The singlet-triplet inter-combinations classified by Söderqvist occur at shorter wavelengths, and the lowest singlet levels may thus have an additional systematic error with respect to the ground and other low triplet levels; the $2s^2 2p^2 \ ^1D_2-\ ^3P_2$ separation adopted here, however, is only $12\ \text{cm}^{-1}$ less than that given by Edlén's semi-empirical formulae. Beginning with the $2s^2 2p3s$ configuration we have rounded off the higher levels to the nearest $10\ \text{cm}^{-1}$, since the uncertainty increases and may be $\pm 100\ \text{cm}^{-1}$ or larger for the highest levels.

The quintet system of levels was established by Söderqvist, but he found no intercombination lines connecting this system with the triplets. Goto et al. classified two lines as transitions from the $2s2p^3 \ ^5S_2^o$ level to the $2s^2 2p^2 \ ^3P_1$ and $\ ^3P_2$ levels (974 and 985 Å, relative intensities 10 and 5, respectively). These classifications may be questioned, however, since the transition to the $\ ^3P_2$ level is calculated to be the stronger of the two lines in the isoelectronic sequence up to about Cr XIX [Kastner et al., 1977], and this expectation has been confirmed by observations through Ne V. We have thus taken the Na VI triplet-quintet con-

nection given by the above classifications as tentative and listed the quintet levels with "+x" to indicate a possible systematic correction. The most probable value of x estimated solely from isoelectronic extrapolation procedures [Edlén et al., 1969] would appear to be about -200 to $-400\ \text{cm}^{-1}$.

Several levels based on single weak (usually doubly classified) lines are given here as tentative and three of the more doubtful high levels were omitted; these are Söderqvist's $2s^2 2p5d \ ^3P_2^o$, $2s2p^2(^2D)4d \ ^3D$, and $2s2p^2(^2D)5d \ ^3F$ levels.

The $2s^2 2pnd \ ^1F_3^o$ levels ($n=3$ through 6) appear to constitute the best series for determination of the ionization energy. We have redetermined the limit of this series, which is the Na VII $2s^2 2p \ ^2P_{3/2}^o$ level, using the $2pnd \ ^1F_3^o$ positions given here. The resulting value for the Na VII $2s^2 2p \ ^2P_{1/2}^o$ principal limit is given above.

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Na VI

Configuration	Term	J	Level (cm ⁻¹)	Configuration	Term	J	Level (cm ⁻¹)
$2s^2 2p^2$	$\ ^3P$	0	0	$2s2p^3$	$\ ^3D^o$	3	204 132
		1	698			2	204 223
		2	1 859			1	204 261
$2s^2 2p^2$	$\ ^1D$	2	35 498	$2s2p^3$	$\ ^3P^o$	2,1,0	241 341
$2s^2 2p^2$	$\ ^1S$	0	74 414	$2s2p^3$	$\ ^1D^o$	2	312 315
$2s2p^3$	$\ ^5S^o$	2	103 362+x	$2s2p^3$	$\ ^3S^o$	1	320 589
				$2s2p^3$	$\ ^1P^o$	1	350 319

Na VI—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Configuration	Term	<i>J</i>	Level (cm ⁻¹)		
$2p^4$	3P	2	477 277	$2s2p^2(^4P)3d$	5D	2,3	1 041 630 + <i>x</i> ?		
		1	478 597						
		0	479 157	$2s2p^2(^4P)3d$	5P	3	1 045 650 + <i>x</i>		
$2p^4$	1D	2	506 114			1	1 046 070 + <i>x</i>		
							1 046 400 + <i>x</i>		
$2p^4$	1S	0	579 173	$2s2p^2(^4P)3d$	3P	2	1 047 410		
$2s^2 2p3s$	$^3P^\circ$	0				0	1 048 100		
							1	807 320	
							2	808 800	
$2s^2 2p3s$	$^1P^\circ$	1	817 740	$2s2p^2(^4P)3d$	3F	2	1 053 880		
$2s^2 2p3p$	3P	0		$2s2p^2(^4P)3d$	3D	1	1 067 760		
							1	872 580	
							2	873 290	
$2s^2 2p3d$	$^3F^\circ$	2	919 480	$2s2p^2(^2D)3p$	$^1F^\circ$	3	1 072 040		
							$^1D^\circ$	2	1 077 890
							$2s2p^2(^4P)3s$	5P	1
2	923 620 + <i>x</i>								
3	924 560 + <i>x</i>								
$2s^2 2p3d$	$^3D^\circ$	1	929 774	$2s2p^2(^2D)3d$	3F	2,3,4	1 125 320		
							2	930 000	
							3	930 510	
$2s^2 2p3d$	$^3P^\circ$	2	933 920	$2s^2 2p4d$	$^3F^\circ$	2	1 128 690		
							1	934 460	
							0	934 740?	
$2s^2 2p3d$	$^1F^\circ$	3	945 450	$2s2p^2(^2D)3d$	3P	0,1,2	1 130 630		
							$^1D^\circ$	2	1 131 170
							$^3D^\circ$	1	1 133 490
$2s^2 2p3d$	$^1P^\circ$	1	946 530	$2s^2 2p4d$	$^1D^\circ$	2	1 131 170		
							2	1 133 870	
							3	1 134 750	
$2s2p^2(^4P)3s$	3P	0	949 780	$2s2p^2(^2D)3d$	3D	1,2,3	1 134 090		
							1	950 370	
							2	951 390	
$2s2p^2(^4P)3p$	$^3S^\circ$	1	970 840	$2s^2 2p4d$	$^3P^\circ$	2	1 136 380		
$2s2p^2(^4P)3p$	$^3D^\circ$	1		$2s^2 2p4d$	$^1F^\circ$	3	1 140 860		
							2	996 010	
							3	996 740	
$2s2p^2(^4P)3p$	$^3D^\circ$	1		$2s2p^2(^2D)3d$	3S	1	1 144 280		
							2	996 010	
							3	996 740	
$2s2p^2(^4P)3p$	$^3P^\circ$	0		$2s2p^2(^2D)3d$	1D	2	1 147 860		
							1	1 005 070?	
							2	1 005 710	
$2s2p^2(^2D)3s$	3D	1,2,3	1 016 270	$2s2p^2(^4P)4s$	1P	1	1 151 280		
							5P	3	1 205 340 + <i>x</i>
							3P	2	1 214 190?
$2s2p^2(^2D)3s$	1D	2	1 033 360	$2s^2 2p5d$	$^3D^\circ$	3	1 228 210?		
$2s2p^2(^2D)3p$	$^3D^\circ$	1,2,3	1 040 220	$2s^2 2p5d$	$^1F^\circ$	3	1 231 110		

Na VI—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Configuration	Term	<i>J</i>	Level (cm ⁻¹)		
$2s2p^2(^4P)4d$	5P	3	1 250 010 + <i>x</i> ?	$2s^2 2p6d$	$^1F^{\circ}$	3	1 280 130		
		2	1 250 930 + <i>x</i> ?			$2s2p^2(^2D)4d$	3F	2,3,4	1 334 585
		1		$2s2p^2(^2D)4d$	3P			0,1,2	1 335 520
$2s2p^2(^4P)4d$	3F	2	1 253 370			$2s2p^2(^4P)5d$	5P	3	1 343 360 + <i>x</i> ?
		3	1 253 950						
		4	1 254 750						
$2s2p^2(^4P)4d$	3D	1,2,3	1 258 610					
$2p^3(^4S^{\circ})3p$	3P	0,1,2	1 265 580	Na VII ($^2P^{\circ}_{1/2}$)	<i>Limit</i>		1 388 750		

Na VII

Z = 11

B I isoelectronic sequence

Ground state $1s^2 2s^2 2p^2 P^{\circ}_{1/2}$ Ionization energy $1\ 681\ 700 \pm 250\ \text{cm}^{-1}$ ($208.51 \pm 0.03\ \text{eV}$)

The levels are based on the observations and analysis by Söderqvist, whose 1944 paper gives 158 lines classified as Na VII transitions in the range 62–492 Å. The positions of the $2s^2 4d\ ^2D_{5/2}$ and $2p^2(^1D)3p\ ^2D^{\circ}$ levels have been changed to agree better with the experimental wavenumbers of their transitions. The values of most of the other doublet levels are as given by Söderqvist, adjusted to a value of zero for the ground level, except that beginning with the $2s^2 3s\ ^2S_{1/2}$ level at $951\ 350\ \text{cm}^{-1}$ all levels are rounded to the nearest $10\ \text{cm}^{-1}$. The errors of some of the higher levels may be $\pm 100\ \text{cm}^{-1}$ or more, whereas the probable errors of most of the lower doublets (given to the nearest cm^{-1}) should be of the order of $\pm 10\ \text{cm}^{-1}$. Fawcett's observations of this spectrum included the $2s2p^2\ ^2P-2p^3\ ^2D^{\circ}$ doublet near 780 Å, but the measured wavelengths of the two (diagonal) lines were less accurate than predictions from Söderqvist's levels.

The quartet system of levels is listed with an unknown added quantity "x" because no quartet-doublet transitions have been definitely identified. The position of the quartets relative to the doublets is from Edlén's estimate of the $2s2p^2\ ^4P$ position (by graphic methods applied to the isoelectronic sequence). The uncertainty of this connection should be much smaller than the $209\ \text{cm}^{-1}$ by which it differs from the previous estimate by Söderqvist. The differences between Söderqvist's values for the $2s2p^2\ ^4P$ and $2p^3\ ^4S^{\circ}_{3/2}$ levels are $18\ \text{cm}^{-1}$ less than his experimental wave-

numbers for the corresponding three lines connecting these terms. We have thus raised the $2p^3\ ^4S^{\circ}$ level, and consequently the higher even-parity quartet levels, by this amount relative to the $2s2p^2\ ^4P$ levels. Three other quartet levels have been changed by varying amounts, again to give better agreement with experimental wavenumbers.

Söderqvist gave the $2p^2(^3P)3d\ ^2F, ^2D$, and $2s2p(^1P^{\circ})4d\ ^2F^{\circ}$ levels as tentative. We list as questionable several additional levels based entirely on lines classified as belonging partly to other Na spectra or on single weak lines. Interactions of the configurations based on the different cores ($2s^2, 2s2p, 2p^2$) can be expected, and the interpretation of some of the higher levels should probably be regarded as tentative.

The limit given above is the value given by Söderqvist ($1\ 681\ 679\ \text{cm}^{-1}$) rounded to the nearest $100\ \text{cm}^{-1}$. We obtained a limit of $1\ 681\ 750\ \text{cm}^{-1}$ by optimizing a quantum-defect plot of the longest series, $3s^2 nd\ ^2D_{5/2}$ ($n=3-8$). Our estimate of the probable error is based on this series.

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 EL CL W IP
 Söderqvist, J. [1944], *Ark. Mat., Astron. Fys.* **30**, 1–20. EL CL W IP

Na VII

Configuration	Term	<i>J</i>	Level (cm^{-1})	Configuration	Term	<i>J</i>	Level (cm^{-1})
$2s^2 2p$	$^2P^{\circ}$	$1/2$	0	$2p^3$	$^2D^{\circ}$	$5/2$	412 311
		$3/2$	2 139			$3/2$	412 395
$2s2p^2$	4P	$1/2$	114 978+x	$2p^3$	$^2P^{\circ}$	$1/2$	465 017
		$3/2$	115 711+x			$3/2$	465 111
		$5/2$	116 778+x				
$2s2p^2$	2D	$5/2$	205 412	$2s^2 3s$	2S	$1/2$	951 350
		$3/2$	205 448	$2s^2 3p$	$^2P^{\circ}$	$1/2$	1 008 420
					$3/2$		
$2s2p^2$	2S	$1/2$	264 400	$2s^2 3d$	2D	$3/2$	1 060 580
$2s2p^2$	2P	$1/2$	283 869			$5/2$	1 060 700
		$3/2$	285 189				
$2p^3$	$^4S^{\circ}$	$3/2$	367 290+x				

ENERGY LEVELS OF SODIUM

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Na VII—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Configuration	Term	<i>J</i>	Level (cm ⁻¹)
2s2p(³ P°)3s	⁴ P°	1/2	1 077 250+x	2p ² (¹ D)3s	² D	3/2	1 331 140
		3/2	1 077 980+x			5/2	1 331 970
		5/2	1 079 310+x				
2s2p(³ P°)3s	² P°	1/2	1 103 220	2s ² 4d	² D	3/2	1 335 810
		3/2	1 104 620			5/2	1 335 830
2s2p(³ P°)3p	² P	1/2	1 126 810	2p ² (³ P)3p	⁴ D°	7/2	1 338 450+x
		3/2	1 127 430			⁴ P°	5/2
2s2p(³ P°)3p	² D	3/2	1 154 780	2p ² (³ P)3p	² D°	3/2, 5/2	1 348 720
		5/2	1 156 180			⁴ S°	3/2
2s2p(³ P°)3p	² S	1/2	1 172 340	2p ² (¹ D)3p	² F°	5/2	1 377 820
2s2p(³ P°)3d	⁴ D°	1/2				7/2	7/2
		3/2	1 185 720+x	2p ² (³ P)3d	² F	5/2	1 388 500?
		5/2	1 185 980+x			7/2	1 388 970?
7/2	1 186 460+x						
2s2p(³ P°)3d	² D°	3/2	1 186 630	2p ² (³ P)3d	² D	3/2, 5/2	1 390 450?
		5/2	1 187 890			² D°	3/2, 5/2
2s2p(³ P°)3d	⁴ P°	5/2	1 192 330+x	2p ² (³ P)3d	⁴ P	5/2	1 399 050+x
		3/2	1 192 850+x			3/2	1 399 580+x
		1/2	1 193 190+x			1/2	1 399 870+x
2s2p(¹ P°)3s	² P°	1/2, 3/2	1 198 290	2p ² (¹ D)3d	² D	3/2, 5/2	1 415 630
2s2p(³ P°)3d	² F°	5/2	1 209 910			2s2p(³ P°)4s	⁴ P°
		7/2	1 211 240				
2s2p(³ P°)3d	² P°	3/2	1 217 190	2p ² (¹ D)3d	² F	5/2	1 428 720
		1/2	1 217 950			7/2	1 428 800
2s2p(¹ P°)3p	² D	3/2	1 251 670	2p ² (¹ D)3d	² P	1/2	1 432 140
		5/2	1 252 010			3/2	1 432 610
2s2p(¹ P°)3p	² P	1/2	1 253 350	2s2p(³ P°)4s	² P°	1/2	
		3/2	1 253 780			3/2	1 432 600?
2s2p(¹ P°)3p	² S	1/2	1 258 880	2s2p(³ P°)4p	² P	1/2	1 442 710
						3/2	1 443 170
2p ² (³ P)3s	⁴ P	1/2		2s2p(³ P°)4p	² D	3/2	1 452 100
		3/2	1 290 030+x			5/2	1 453 350
		5/2	1 291 560+x				
2s2p(¹ P°)3d	² F°	5/2, 7/2	1 292 330	2s ² 5d	² D	3/2	1 461 520
						5/2	1 461 590
2s ² 4s	² S	1/2	1 294 910	2s2p(³ P°)4d	⁴ D°	1/2	
2s2p(¹ P°)3d	² D°	3/2	1 303 450?			3/2	1 462 380+x
		5/2	1 303 610			5/2	1 462 420+x
		7/2		7/2	1 463 250+x		
2s2p(¹ P°)3d	² P°	1/2, 3/2	1 306 470	2s2p(³ P°)4d	² D°	3/2	
						5/2	1 464 050

Na VII—Continued

Configuration	Term	J	Level (cm^{-1})	Configuration	Term	J	Level (cm^{-1})
$2s2p(^3P^{\circ})4d$	$^4P^{\circ}$	$\frac{5}{2}$	$1\ 464\ 850+x$	$2s2p(^3P^{\circ})5d$	$^4D^{\circ}$	$\frac{1}{2}-\frac{7}{2}$	$1\ 589\ 270+x$
$2s2p(^3P^{\circ})4d$	$^2F^{\circ}$	$\frac{5}{2}$ $\frac{7}{2}$	$1\ 471\ 560$ $1\ 472\ 730$	$2s2p(^3P^{\circ})5d$	$^4P^{\circ}$	$\frac{1}{2}-\frac{5}{2}$	$1\ 590\ 050+x$
$2s2p(^3P^{\circ})4d$	$^2P^{\circ}$	$\frac{3}{2}$ $\frac{1}{2}$	$1\ 473\ 810?$ $1\ 474\ 530?$	$2s2p(^3P^{\circ})5d$	$^2F^{\circ}$	$\frac{5}{2}$ $\frac{7}{2}$	$1\ 592\ 820$ $1\ 593\ 920$
$2s^2\ 6d$	2D	$\frac{3}{2}, \frac{5}{2}$	$1\ 529\ 460$	$2s^2\ 8d$	2D	$\frac{3}{2}, \frac{5}{2}$	$1\ 596\ 400$
$2s2p(^1P^{\circ})4s$	$^2P^{\circ}$	$\frac{1}{2}, \frac{3}{2}$	$1\ 538\ 950?$	$2p^2(^3P)4p$	$^4D^{\circ}$	$\frac{3}{2}-\frac{7}{2}$	$1\ 646\ 110+x$
$2s2p(^1P^{\circ})4p$	2D	$\frac{3}{2}, \frac{5}{2}$	$1\ 561\ 890?$	$2s2p(^3P^{\circ})6d$	$^4D^{\circ}$	$\frac{1}{2}-\frac{7}{2}$	$1\ 657\ 520+x$
$2s^2\ 7d$	2D	$\frac{3}{2}, \frac{5}{2}$	$1\ 570\ 080$	$2p^2(^3P)4d$	4P	$\frac{5}{2}$ $\frac{3}{2}$ $\frac{1}{2}$	$1\ 668\ 320+x?$ $1\ 668\ 920+x?$
$2s2p(^1P^{\circ})4d$	$^2F^{\circ}$	$\frac{5}{2}, \frac{7}{2}$	$1\ 577\ 810?$				
$2s2p(^3P^{\circ})5p$	2P	$\frac{1}{2}, \frac{3}{2}$	$1\ 578\ 350$				
$2s2p(^3P^{\circ})5p$	2D	$\frac{3}{2}, \frac{5}{2}$	$1\ 583\ 740$	Na VIII (1S_0)	<i>Limit</i>		1 681 700

Na VIII

 $Z=11$

Be I isoelectronic sequence

Ground state $1s^2 2s^2 \ ^1S_0$ Ionization energy $2\ 131\ 300 \pm 250\ \text{cm}^{-1}$ ($264.25 \pm 0.03\ \text{eV}$)

Levels Below the Principal Ionization Limit

Söderqvist analyzed this spectrum as obtained with a vacuum-spark source. The classified lines occurred in two regions, with three longer-wavelength transitions comprising the $2s^2 \ ^1S_0 - 2s2p \ ^1P_1^\circ$ resonance line (411 Å) and two $2s2p \ ^3P^\circ - 2p^2 \ ^3P$ lines. Fawcett's measurements of the $2s2p - 2p^2$ lines (492–500 Å) include the complete $^3P^\circ - ^3P$ multiplet and the $^1P_1^\circ - ^1S_0$ line. The $2s2p$ and $2p^2$ levels given here are from Edlén, who has evaluated the levels of these configurations for Be I-like spectra by combining the experimental data with requirements of isoelectronic regularity. It appears that the probable errors for these Na VIII levels are not greater than a few cm^{-1} . The values of the $2s2p \ ^3P^\circ$ and $2p^2 \ ^3P$ levels with respect to the $2s^2 \ ^1S_0$ ground level as determined by Edlén may be as accurate as the intrasystem separations (singlet-singlet or triplet-triplet); we have, however, listed the triplet levels with a quantity "+x" to indicate the lack of an experimental determination of the intersystem connection for Na VIII.

Söderqvist's 1944 paper has 83 lines in the range 51–118 Å classified as transitions from $2snl$ and $2pnl$ ($n \geq 3$) levels of Na VIII. We have redetermined these higher levels by combining Söderqvist's wavenumbers with the low levels from Edlén. Most of the higher levels are rounded to the nearest $10\ \text{cm}^{-1}$, the probable errors varying from perhaps 20 or $30\ \text{cm}^{-1}$ to more than $100\ \text{cm}^{-1}$. (The quantity "x" is probably negligible compared to the experimental uncertainties of these levels.)

A number of the higher levels are given here as tentative, each being derived from a single line not normally

expected to be the strongest combination or otherwise questionably classified. The classification of the weaker lines is complicated by interactions between the two series types ($2snl$ and $2pnl'$) known to occur in this isoelectronic sequence. The lowest missing term, $2s3p \ ^3P^\circ$, is predicted to lie about $3000\ \text{cm}^{-1}$ above the $2s3p \ ^1P^\circ$ term [Odabasi, 1969]. Odabasi's configuration-interaction eigenvectors for the $2s3p$ terms in this sequence indicate that depression of the $2s3p \ ^1P^\circ$ term by interaction with $2p3s \ ^1P^\circ$ is mainly responsible for this anomaly; in Na VIII the percentage composition of the $2s3p \ ^1P^\circ$ term includes 9.6% $2p3s \ ^1P^\circ$, whereas the mixing of the $^3P^\circ$ terms from these two configurations is only 0.7%. Odabasi's eigenvectors include contributions from nine configurations.

We derived the quoted ionization limit by minimizing irregularities in a quantum-defect plot for the $2snd \ ^1D_2$ series, which appears to be the least perturbed of the four-member series. This value for the limit agrees with the value given by Söderqvist ($2\ 131\ 140\ \text{cm}^{-1}$) to within our estimate of the probable error. The designations of several levels assigned to other series are given as questionable because of intensity and quantum-defect irregularities.

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Na VIII

Configuration	Term	J	Level (cm^{-1})	Configuration	Term	J	Level (cm^{-1})		
$2s^2$	1S	0	0	$2p^3$	1D	2	361 145		
$2s2p$	$^3P^\circ$	0	125 880+x	$2p^2$	1S	0	446 136		
		1	126 612+x			$2s3s$	3S	1	1 239 974+x
		2	128 218+x						
$2s2p$	$^1P^\circ$	1	243 208	$2s3s$	1S	0	1 262 780		
$2p^2$	3P	0	327 476+x	$2s3p$	$^1P^\circ$	1	1 294 230		
		1	328 310+x						
		2	329 729+x						

Na VIII—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Configuration	Term	<i>J</i>	Level (cm ⁻¹)
2s3d	³ D	1	1 327 226+x	2p4p	³ D	1	
		2	1 327 265+x			2	1 816 010+x?
		3	1 327 388+x			3	1 817 290+x
2s3d	¹ D	2	1 347 740	2p4p	³ P	2	1 822 880+x
2p3s	³ P°	0	1 399 670+x	2p4d	¹ D°	2	1 827 570
		1	1 400 470+x	2p4p	¹ D	2	1 827 640
		2	1 402 200+x				
2p3s	¹ P°	1	1 426 125	2p4d	³ D°	3	1 833 530+x
2p3p	¹ P	1	1 432 980	2p4d	³ P°	2	1 835 010+x
2p3p	³ D	1	1 439 410+x?			1	1 835 290+x?
		2	1 440 260+x?			0	
		3	1 441 880+x			3	1 838 860
2p3p	³ S	1	1 452 400+x	2s5p	¹ P°	1	1 838 910
2p3p	³ P	0		2p4d	¹ P°	1	1 843 110
		1	1 459 850+x	2s5d?	³ D?	1,2,3	1 848 670+x?
		2	1 460 770+x				
2p3d	¹ D°	2	1 469 150	2s5d	¹ D	2	1 848 960
2p3p	¹ D	2	1 474 580	2s6p	¹ P°	1	1 930 910
2p3p	¹ S	0	1 481 510	2s6d?	³ D?	1,2,3	1 933 430+x
2p3d	³ D°	1	1 485 140+x	2s6d	¹ D	2	1 935 230
		2	1 485 340+x	2p5p	³ P	2	1 988 680+x
		3	1 486 080+x				
2p3d	³ P°	2	1 491 980+x	2p5p	¹ D	2	1 990 540
		1	1 492 630+x	2p5d	¹ D°	2	1 991 220
		0	1 492 980+x				
2p3d	¹ F°	3	1 507 790	2p5d	³ D°	3	1 994 370+x
2p3d	¹ P°	1	1 513 730	2p5d	³ P°	2	1 994 930+x
2s4s	³ S	1	1 649 480+x			1	1 995 200+x?
2s4s	¹ S	0	1 656 820			0	
2s4p	¹ P°	1	1 673 390			2p5d	¹ F°
2s4d	³ D	1,2,3	1 683 370+x	2p6p?	³ D?	1,2,3	2 076 930+x?
2s4d	¹ D	2	1 689 970	2p6d	³ D°	1,2,3	2 080 460+x
2p4p	¹ P	1	1 813 190	2p6d	³ P°	2,1,0	2 081 170+x
				2p6d	¹ F°	3	2 083 210
				Na IX (² S _{1/2})	Limit		2 131 300

Na IX

 $Z=11$

Li I isoelectronic sequence

Ground state $1s^2 2s^2 2S_{1/2}$ Ionization energy $2\,418\,570\text{ cm}^{-1}$ (299.867 eV)

Söderqvist observed the $1s^2 2s-1s^2 np$ and $1s^2 2p-1s^2 ns$, nd ($n \geq 3$) series in the 44–81 Å region. Most of the $1s^2 nl$ levels are from these measurements, and the $2p^2 P_{3/2}^{\circ}$ level is from his measurement of the $2s^2 S_{1/2}-2p^2 P_{3/2}^{\circ}$ line at 681.72 Å. The $2p^2 P_{3/2}^{\circ}-2p^2 P_{1/2}^{\circ}$ interval is from one of several semi-empirical formulae for energies in this isoelectronic sequence derived by Edlén. The resulting value of the $2p^2 P_{1/2}^{\circ}$ level agrees with Fawcett's [1970] measurement of the $2s^2 S_{1/2}-2p^2 P_{1/2}^{\circ}$ wavelength (694.17 ± 0.04 Å) to within the experimental uncertainty. The agreement of Edlén's values with experimental values along the sequence makes an error greater than ~5 cm⁻¹ for the Na IX $2p^2 P^{\circ}$ levels appear unlikely. We have reevaluated Söderqvist's ns ($n \geq 3$) and nd levels based wholly or in part on combinations with the $2p^2 P_{1/2}^{\circ}$ level, since the new value of this level is 24 cm⁻¹ above his determination. The values of all the $1s^2 nl$ ($n \geq 3$) levels are rounded to the nearest 10 cm⁻¹, the estimated errors varying from perhaps ±50 cm⁻¹ to about ±200 cm⁻¹.

The Ritz formulae for $1s^2 ns$ and $1s^2 np$ and the polarization formula for $1s^2 nl$ ($l \geq 2$) given by Edlén predict the entire spectrum for levels below the $1s^2 1S_0$ limit. Levels calculated from the formulae are of course free of series irregularities arising from experimental error, and the absolute accuracy of the formulae appears to be at least comparable to the experimental accuracy. Kastner gives predicted intervals for the $np^2 P^{\circ}$, $nd^2 D$, and $nf^2 F^{\circ}$ terms through $n=10$ and notes the relatively large irregularities of the experimental Na IX $nd^2 D$ splittings for $n=4$ and 6 (almost certainly due to experimental errors).

In addition to the $2p^2 P^{\circ}$ interval, we have used Edlén's results for the ionization energy, the $4f^2 F^{\circ}$ and $5s^2 S$ terms, and the $4p^2 P^{\circ}$ interval (not resolved by Söderqvist). Edlén's isoelectronic-formula value for the ionization energy, which is given here rounded to the nearest 10 cm⁻¹, is 50 cm⁻¹ above Söderqvist's value and 25 cm⁻¹ below the (average) value obtained by Edlén using another method. The $4f^2 F^{\circ}$ and $5s^2 S$ levels are taken at Edlén's values with respect to the limit (not with respect to lower levels, for which the values given here differ somewhat from those used by Edlén). The quantum defect of Söderqvist's $5s^2 S_{1/2}$ level is very irregular in the $ns^2 S_{1/2}$ series, the indicated error of his measurement of the weak $2p^2 P_{3/2}^{\circ}-5s^2 S_{1/2}$ line being about 400 cm⁻¹. Edlén rejected an experimental identification of the $3d^2 D-4f^2 F^{\circ}$ line [Fawcett, 1971] as being too far from the predicted wavelength.

The wavenumber given by Söderqvist for the $2s^2 S_{1/2}-7p^2 P^{\circ}$ line gives a more regular behavior of the $np^2 P^{\circ}$ series

than would the value $2\,235\,986\text{ cm}^{-1}$ corresponding to the tabulated wavelength (44.723 Å); the latter is thus assumed to be a misprint for 44.725 Å.

The terms of the $1s2s^2$, $1s2s2p$, and $1s2p^2$ configurations are included in the table. Spectral features due to such K-shell excitations, which of course lie far above the $1s^2 1S_0$ ionization limit, have been observed near or blended with the Na X $1s^2 1S_0-1snp^1 P^{\circ}$, $3P^{\circ}$ resonance lines in the 11 Å region. Transitions from the $1s2s2p$ and $1s2p^2$ doublet terms are among the strongest contributors to such features in the spectra of laser-produced plasmas [see, e.g., Aglitskii et al.]. Since the available wavelength measurements for these lines in Na refer to unresolved blends, we have given the levels as obtained from energy separations calculated by Vainshtein and Safronova [1975; see also their 1978 publication]. The $1s2s^2$ and $1s2p^2$ levels were derived by combining Vainshtein and Safronova's results with the $1s^2 2p^2 P^{\circ}$ levels given here, and all the K-excitation levels were rounded to the nearest 100 cm⁻¹. Comparisons of theoretical and experimental values of such terms in higher spectra of this isoelectronic sequence suggest that errors greater than about ±2000 cm⁻¹ are unlikely for the Na IX calculated levels. (The errors of the calculated fine-structure splittings should be much smaller.) The paper of Boiko et al. and references cited therein give wavelengths for transitions from $1s2l2l'$ terms and also $1s2l3l'$ terms. Feldman et al., for example, have assigned a feature observed by them at 11.029 Å (near the Na X $1s^2 1S_0-1s2p^1 P_1^{\circ}$ resonance line) as arising from a blend of transitions of the type $1s^2 3l'-1s2p3l'$.

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Na ix

Configuration	Term	J	Level (cm^{-1})	Configuration	Term	J	Level (cm^{-1})
$1s^2(1S)2s$	2S	$1/2$	0	$1s^2(1S)7p$	$^2P^\circ$	$1/2, 3/2$	2 235 890
$1s^2(1S)2p$	$^2P^\circ$	$1/2$ $3/2$	144 062 146 688	$1s^2(1S)7d$	2D	$3/2$ $5/2$	2 237 160 2 237 170
$1s^2(1S)3s$	2S	$1/2$	1 375 950				
$1s^2(1S)3p$	$^2P^\circ$	$1/2$ $3/2$	1 415 370 1 416 130	Na x ($1S_0$)	Limit		2 418 570
$1s^2(1S)3d$	2D	$3/2$ $5/2$	1 430 000 1 430 200	$1s2s^2$	2S	$1/2$	[8 815 600]
$1s^2(1S)4s$	2S	$1/2$	1 840 350	$1s(2S)2s2p(^3P^\circ)$	$^4P^\circ$	$1/2$ $3/2$ $5/2$	[8 854 500] [8 855 100] [8 857 000]
$1s^2(1S)4p$	$^2P^\circ$	$1/2$ $3/2$	[1 856 440] [1 856 770]	$1s(2S)2s2p(^3P^\circ)$	$^2P^\circ$	$1/2$ $3/2$	[8 963 700] [8 965 200]
$1s^2(1S)4d$	2D	$3/2$ $5/2$	1 862 250 1 862 570	$1s2p^2$	4P	$1/2$ $3/2$ $5/2$	[9 008 000] [9 009 200] [9 010 500]
$1s^2(1S)4f$	$^2F^\circ$	$5/2$ $7/2$	[1 862 930] [1 862 980]	$1s(2S)2s2p(^1P^\circ)$	$^2P^\circ$	$1/2$ $3/2$	[9 016 900] [9 017 500]
$1s^2(1S)5s$	2S	$1/2$	[2 051 520]	$1s2p^2$	2D	$5/2$ $3/2$	[9 075 600] [9 076 400]
$1s^2(1S)5p$	$^2P^\circ$	$1/2, 3/2$	2 059 600	$1s2p^2$	2P	$1/2$ $3/2$	[9 095 100] [9 097 700]
$1s^2(1S)5d$	2D	$3/2$ $5/2$	2 062 860 2 062 910	$1s2p^2$	2S	$1/2$	[9 178 900]
$1s^2(1S)6p$	$^2P^\circ$	$1/2, 3/2$	2 169 670	Na x $1s2s(^3S_1)$	Limit		[11 353 910]
$1s^2(1S)6d$	2D	$3/2$ $5/2$	2 171 390 2 171 550				

Na X

Z=11

He I isoelectronic sequence

Ground state $1s^2\ ^1S_0$ Ionization energy $11\ 816\ 996 \pm 100\ \text{cm}^{-1}$ ($1465.133 \pm 0.012\ \text{eV}$)***1sns* and *1snp* Terms, Ionization Energy**

Aglitskii et al. have observed the first two members of the $1s^2\ ^1S_0$ — $1snp\ ^1P_1^o$ resonance series beginning near $11\ \text{\AA}$ ($n=2$). Their wavelength measurements agree with theoretical calculations, but the experimental uncertainty corresponds to $\pm 2500\ \text{cm}^{-1}$ in the $1s2p\ ^1P_1^o$ position. The calculated values for the $1snl$ levels given here should be much more accurate. The $1sns$ and $1snp$ levels for $n=2-5$, as well as the ionization energy, are from calculations by Ermolaev and Jones [unpublished supplement to their paper]. Most of the uncertainty in the ionization energy is due to the Lamb-shift contribution, the $\pm 100\ \text{cm}^{-1}$ given with the value above being only an order-of-magnitude estimate of the probable error based on Ermolaev and Jones' discussion. Approximately the same error would apply to all the $1sns$ and $1snp$ excited levels with respect to the ground level. The errors of the excited levels with respect to the limit are expected to be smaller, decreasing with n from perhaps about $20\ \text{cm}^{-1}$ for $n=2$. There is at present some uncertainty about the accuracies of various theoretical energy calculations for higher ions in the He I sequence; accurate wavelength measurements for a number of transitions along the sequence will be useful in this regard (see, for example, the comparisons by Berry et al. of theoretical $1s2s\ ^3S$ — $1s2p\ ^3P^o$ separations with available experimental values for the sequence). We give Ermolaev and Jones' values and the other $1snl$ levels to the nearest cm^{-1} for convenience in comparing with other calculations or future experimental results.¹

The mixtures of the $1snp\ ^3P_1^o$ and $^1P_1^o$ states obtained from Ermolaev and Jones' supplementary table are not given as leading percentages below, since the eigenvector purities are $>99\%$; their tabulated coefficients give singlet-triplet percentage mixtures of 0.10% for $1s2p$ to 0.14% for $1s5p$.

The theoretical values for the lower levels of the series can be extended to obtain values for arbitrarily high members. The $1sns$ and $1snp$ levels given for $n=6-10$ were obtained from Ritz formulae with constants derived by fitting Ermolaev and Jones' lower terms ($n=2-5$) to within maximum deviations of 1 to $3\ \text{cm}^{-1}$:

¹The estimated errors for the ionization energies and the $1sns$ and $1snp$ levels given in our compilations for Mg XI and Al XII [see references in the Introduction] were based on the accuracies of the ionization energies stated by Ermolaev and Jones in their summary Table 1. A closer reading of Sec. 3 of their paper indicates that the estimated errors of the ionization energies given in the above compilations should be increased by about an order of magnitude; these increased errors apply to all the excited levels with respect to the ground states.

$$\text{Level}/\text{cm}^{-1} = 11\ 816\ 995.5 - 10\ 973\ 469(n^*)^{-2}$$

$$n - n^* = a + bn^{-2} + cn^{-1}$$

	<i>a</i>	<i>b</i>	<i>c</i>
3S_1	0.0456129	0.0064034	0.021862
1S_0	0.0184800	-0.0105071	0.009298
$^3P^o$	0.0175534	-0.0007314	0.006847
$^1P_1^o$	-0.0029084	-0.0116177	0.004739

The $^3P^o$ values are for the term baricenters.

***1snd* and *1snf* Terms**

Theoretical values are also given for the $1snd$ and $1snf$ terms through $n=6$. The values are based on variational calculations for $1s3d$ [Brown, 1968] and higher $1snd$ terms [Brown and Cortez, 1971] and for the $1snf$ terms [Brown, 1969]. These calculations did not include relativistic and radiative corrections, but combination of the $1snl$ term values (obtained from the total energies) with the $1s\ ^2S_{1/2}$ ionization limit of Ermolaev and Jones yields $1snl$ levels effectively including these corrections for the $1s$ electron. The error in Ermolaev and Jones' value for the ionization energy obviously must be included in the errors of the resulting $1snl$ positions with respect to the ground level. As an approximation for the largest of the remaining corrections, the relativistic shift associated with the nl electron, we assumed the Sommerfeld-Dirac correction for the baricenter of the hydrogenic nl term for core charge $Z_c=10$ [Edlén, 1964]. This smaller relativistic lowering of the levels varies from $325\ \text{cm}^{-1}$ for the $1s3d$ terms to $43\ \text{cm}^{-1}$ for the $1s6f$ terms.

The fine-structure separations of the $1s3d\ ^3D$ levels are from Vainshtein and Safronova's calculations [1976]. Their values for the $1s3l$ levels, which include relativistic and radiative contributions, give the $1s3d\ ^3D$ and 1D terms lower by 83 and $153\ \text{cm}^{-1}$, respectively, relative to the $1s3s$ singlet-triplet mean position than is obtained with the levels given here. The $1s3l$ positions with respect to the $1s^2\ ^1S_0$ ground level as calculated by Vainshtein and Safronova, however, are higher than the values here by $453\ \text{cm}^{-1}$ ($1s3d\ ^1D_2$) to $680\ \text{cm}^{-1}$ (the $1s3p\ ^3P^o$ levels).

It is of interest to compare the $1snd$ and $1snf$ energies with predictions of the core-polarization theory of term

defects in two-electron ions. For this purpose the energies are taken with respect to the $1s^2S_{1/2}$ limit, and the appropriate quantities from Brown, or Brown and Cortez, are the differences between the calculated (non-relativistic) $1snl$ singlet-triplet mean energies and the corresponding Bohr hydrogenic energies ($100R_N/n^2$). These differences, which are the calculated non-relativistic term defects, range from 268 cm^{-1} for $1s3d$ to 2 cm^{-1} for $1s6f$. They are smaller than the core-polarization defects predicted in the dipole plus quadrupole-polarizability approximation [Martin, 1970, and references therein] by 19 to 31 cm^{-1} for the $1snd$ terms and by 2 to 3 cm^{-1} for the $1snf$ terms. These results and similar comparisons for other two-electron ions indicate that, in this region of the isoelectronic sequence, the polarization formulae yield relatively accurate values for all the $1snl$ ($l \geq 2$) non-relativistic singlet-triplet mean energies. Levels of the higher $1snd$ and $1snf$ configurations in Na X can be derived from Ritz formulae fitted to the lower members of these series as given here.

Hyperfine Structure

The magnetic moment of the Na^{23} nucleus ($2.218u_N$, spin $3/2$) gives a hyperfine-structure factor $a_s = 16.7\text{ cm}^{-1}$ for the Na XI $1s$ electron [Kastner, 1972]. We call attention to the resulting hyperfine structures of the Na X $1snl$ triplet levels [Kopfermann, 1958], which are thus comparable to or larger than some of the calculated fine-structure and term separations given here. It will be necessary to take the hyperfine splittings into account if sufficiently accurate observations are made.

Doubly Excited Configurations

Transitions of the type $1snl-2l'nl''$ ($n \geq 2$) from doubly excited upper configurations in Na X can give rise to "satellite" features near the Na XI $1s^2S-2p^2P^o$ resonance doublet at 10.02 \AA . Feldman et al., for example, have observed such Na X features in the spectra of laser-produced plasmas. The main transitions involved were identified by Feldman et al., but most such features may be unresolved blends [see, for example, the more recent interpretation of the analogous Mg XI features in Table 6 of Boiko et al.]. Several of the stronger features are from $2s2p$ and $2p^2$ upper

terms [Feldman et al.]. The $2s^2^1S$ level, the $2s2p^3P^o$ and $1P^o$ levels, and the $2p^2^1D$ and $1S$ levels are given here as calculated relative to the ground level by Vainshtein and Safronova [1976]; the $2p^2^3P$ levels from this reference were lowered by 400 cm^{-1} for inclusion here, to improve the overall agreement with values from the calculated $1s2p^3P^o-2p^2^3P$ wavelengths [Vainshtein and Safronova, 1978] combined with the $1s2p^3P^o$ levels given here. All the doubly excited levels are rounded to the nearest 100 cm^{-1} . Such theoretical values have proved accurate to within the experimental errors of the available measurements in this region of the isoelectronic sequence [Boiko et al.], which would correspond to about $\pm 2000\text{ cm}^{-1}$ for Na X.

Transitions from upper terms belonging to configurations of the type $2l'3l''$ have also been identified as contributing to satellite features of the hydrogenic-ion $1s^2S-2p^2P^o$ resonance doublet in the spectra of nearby elements. We have not included such terms here, but theoretical values are given by Vainshtein and Safronova [1976], for example.

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Na X

Configuration	Term	J	Level (cm^{-1})	Configuration	Term	J	Level (cm^{-1})
$1s^2$	$1S$	0	0	$1s2p$	$1P^o$	1	[9 088 700]
$1s2s$	$3S$	1	[8 935 337]	$1s3s$	$3S$	1	[10 558 946]
$1s2p$	$3P^o$	0	[9 022 345]	$1s3p$	$3P^o$	0	[10 582 781]
		1	[9 022 867]			1	[10 582 947]
		2	[9 025 264]			2	[10 583 658]
$1s2s$	$1S$	0	[9 027 981]	$1s3s$	$1S$	0	[10 583 431]

Na x—Continued

Configuration	Term	<i>J</i>	Level (cm ⁻¹)	Configuration	Term	<i>J</i>	Level (cm ⁻¹)				
1s3d	³ D	1	[10 596 647]	1s6d	¹ D	2	[11 512 137]				
		2	[10 596 667]			1s6p	¹ P°	1	[11 512 505]		
		3	[10 596 925]					1s7s	³ S	1	[11 590 091]
1s3d	¹ D	2	[10 597 475]	1s7s	¹ S					0	[11 591 874]
1s3p	¹ P°	1	[10 601 080]			1s7p	³ P°			0,1,2	[11 591 920]
1s4s	³ S	1	[11 115 065]					1s7p	¹ P°	1	[11 593 248]
		1s4p	³ P°	0	[11 124 873]					1s8s	³ S
		1		[11 124 944]	1s8s	¹ S	0				
2	[11 125 244]	1s8p		³ P°			0,1,2	[11 644 781]			
1s4s	¹ S		0				[11 124 986]	1s8p	¹ P°	1	[11 645 667]
			1s4d		³ D	1,2,3	[11 130 639]			1s9s	³ S
		1s4d	¹ D	2		[11 131 017]	1s9s				
1s4f	³ F°	2,3,4	[11 131 051]	1s9p		³ P°		0,1,2	[11 680 991]		
1s4f		¹ F°	3		[11 131 056]			1s9p	¹ P°	1	[11 681 612]
1s4p		¹ P°	1		[11 132 393]		1s10s			³ S	1
1s5s	³ S		1	[11 369 887]	1s10s	¹ S					0
1s5p			³ P°	0				[11 374 842]	1s10p		³ P°
1		[11 374 879]		1s10p			¹ P°	1		[11 707 327]	
2	[11 375 032]	1s10p			¹ P°	1		[11 707 327]			
1s5s	¹ S		0			[11 374 868]					
1s5d			³ D	1,2,3		[11 377 767]	Na XI (² S _{1/2})	<i>Limit</i>	[11 816 996]		
1s5d		¹ D		2	[11 377 984]	2s ²	¹ S	0	[18 757 400]		
1s5f	³ F°	2,3,4		[11 377 987]	2s2p	³ P°	0	[18 780 000]			
1s5f		¹ F°	3	[11 377 991]	1		[18 781 500]				
1s5p		¹ P°	1	[11 378 646]	2		[18 784 900]				
1s6s	³ S		1	[11 507 469]	2p ²	³ P	0	[18 856 100]			
1s6s			¹ S	0	[11 510 320]		1	[18 857 800]			
1s6p		³ P°	0,1,2	[11 510 337]	2		[18 860 700]				
1s6d	³ D		1,2,3	[11 512 003]	2p ²	¹ D	2	[18 900 900]			
1s6f			³ F°	2,3,4	[11 512 130]		2s2p	¹ P°	1	[18 909 900]	
1s6f		¹ F°		3	[11 512 133]		2p ²		¹ S	0	[19 034 800]
				Na XI 2p(² P _{1/2})	<i>Limit</i>	[21 788 480]					

Na XI

Z=11

H I isoelectronic sequence

Ground state $1s^2S_{1/2}$ Ionization energy $13\,297\,672 \pm 2 \text{ cm}^{-1}$ ($1648.714 \pm 0.004 \text{ eV}$)

The levels and ionization energy are based on theoretical values calculated by Erickson using the nuclear mass for the naturally occurring Na^{23} isotope. The values here are adjusted to the Rydberg constant determined by Goldsmith, Weber, and Hänsch ($R_\infty = 109\,737.31476 \pm 0.00032 \text{ cm}^{-1}$). The standard-deviation error of $\pm 2 \text{ cm}^{-1}$ in the ionization energy also applies to all the excited levels with respect to the ground level. The errors for the separations of excited levels are smaller; Erickson gives each level to the number of decimal places appropriate for a stated quantum-electrodynamics error. His table is complete through $n=11$ and has the ns , np , and nl ($l=n-1$) levels through $n=20$. We give all levels through $n=5$ and list the ns and np levels through $n=10$.

The uncertainty of the ionization energy in eV units arises from the conversion factor (see the introduction).

The experimental uncertainties of wavelength measurements in the region of the Na XI $1s$ - np resonance series are very large in comparison with any expected errors in the corresponding theoretical wavelengths. Aglitskii et al., for example, have measured the wavelengths of the $1s^2S$ - $2p^2P^\circ$ and $1s^2S$ - $3p^2P^\circ$ unresolved doublet lines from laser-produced plasmas as $10.026 \pm 0.003 \text{ \AA}$ and $8.461 \pm 0.004 \text{ \AA}$.

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Na XI

Configuration	Term	J	Level (cm^{-1})	Configuration	Term	J	Level (cm^{-1})
1s	2S	$1/2$	0	4f	$^2F^\circ$	$5/2$ $7/2$	[12 467 607.8] [12 467 719.6]
2p	$^2P^\circ$	$1/2$ $3/2$	[9 971 484.8] [9 976 865.6]	5p	$^2P^\circ$	$1/2$ $3/2$	[12 765 972.1] [12 766 316.4]
2s	2S	$1/2$	[9 971 713.7]	5s	2S	$1/2$	[12 765 987.0]
3p	$^2P^\circ$	$1/2$ $3/2$	[11 819 964.3] [11 821 558.8]	5d	2D	$3/2$ $5/2$	[12 766 315.8] [12 766 430.3]
3s	2S	$1/2$	[11 820 032.8]	5f	$^2F^\circ$	$5/2$ $7/2$	[12 766 430.1] [12 766 487.3]
3d	2D	$3/2$ $5/2$	[11 821 556.1] [11 822 086.1]	5g	2G	$7/2$ $9/2$	[12 766 487.2] [12 766 521.5]
4p	$^2P^\circ$	$1/2$ $3/2$	[12 466 713.2] [12 467 385.8]	6p	$^2P^\circ$	$1/2$ $3/2$	[12 928 493.5] [12 928 692.8]
4s	2S	$1/2$	[12 466 742.2]	6s	2S	$1/2$	[12 928 502.2]
4d	2D	$3/2$ $5/2$	[12 467 384.7] [12 467 608.2]				

Na XI—Continued

Configuration	Term	J	Level (cm^{-1})	Configuration	Term	J	Level (cm^{-1})
$7p$	$^2P^\circ$	$\frac{1}{2}$ $\frac{3}{2}$	[13 026 470.8] [13 026 596.2]	$9s$	2S	$\frac{1}{2}$	[13 193 641.7]
$7s$	2S	$\frac{1}{2}$	[13 026 476.2]	$10p$	$^2P^\circ$	$\frac{1}{2}$ $\frac{3}{2}$	[13 164 813.3] [13 164 856.3]
$8p$	$^2P^\circ$	$\frac{1}{2}$ $\frac{3}{2}$	[13 090 052.6] [13 090 136.7]	$10s$	2S	$\frac{1}{2}$	[13 164 815.2]
$8s$	2S	$\frac{1}{2}$	[13 090 056.3]		Limit		[13 297 671.6]
$9p$	$^2P^\circ$	$\frac{1}{2}$ $\frac{3}{2}$	[13 133 639.1] [13 133 698.1]				