

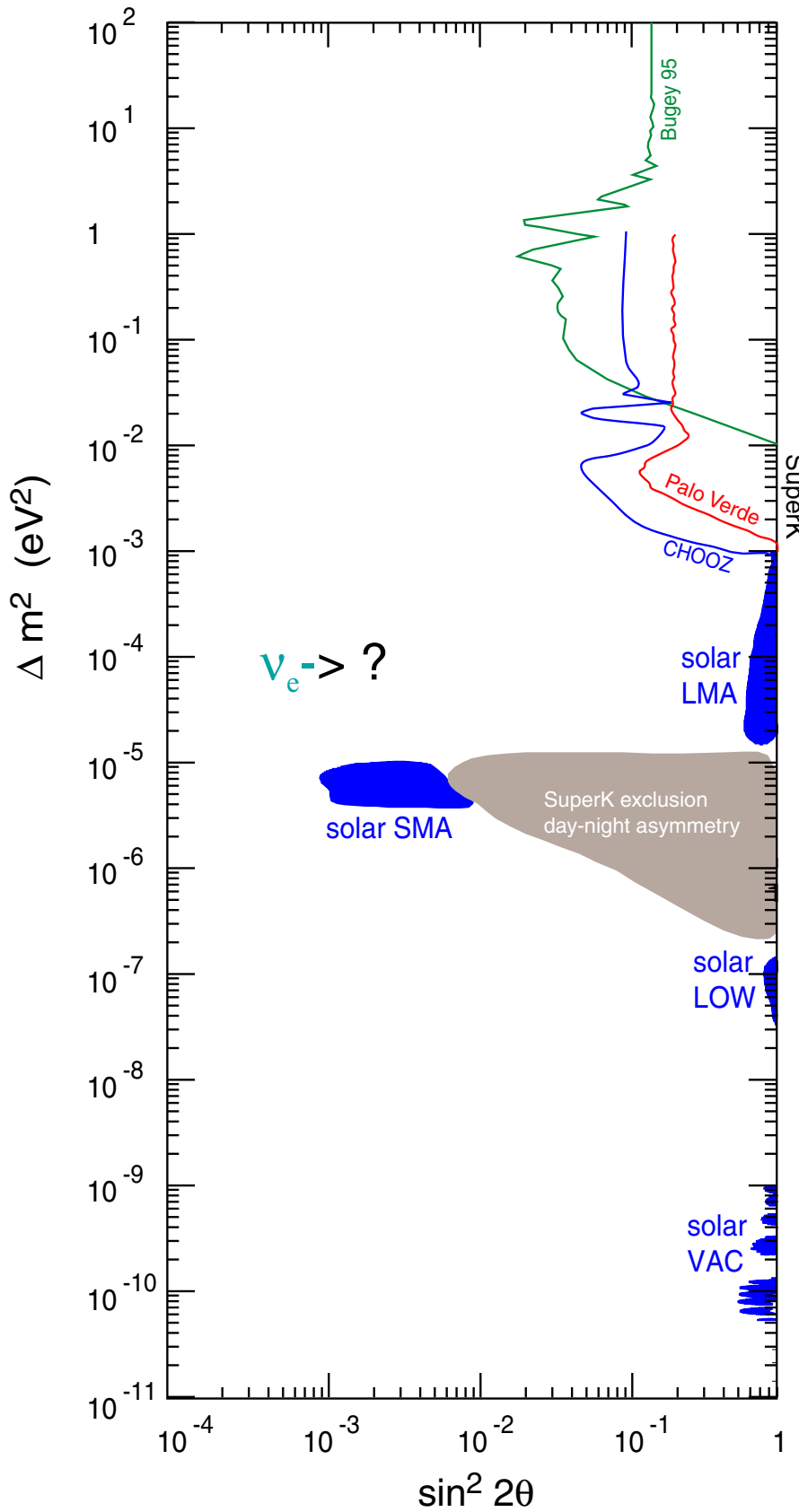
# Neutrino factories from muon storage rings

H. Schellman  
Northwestern University/FNAL

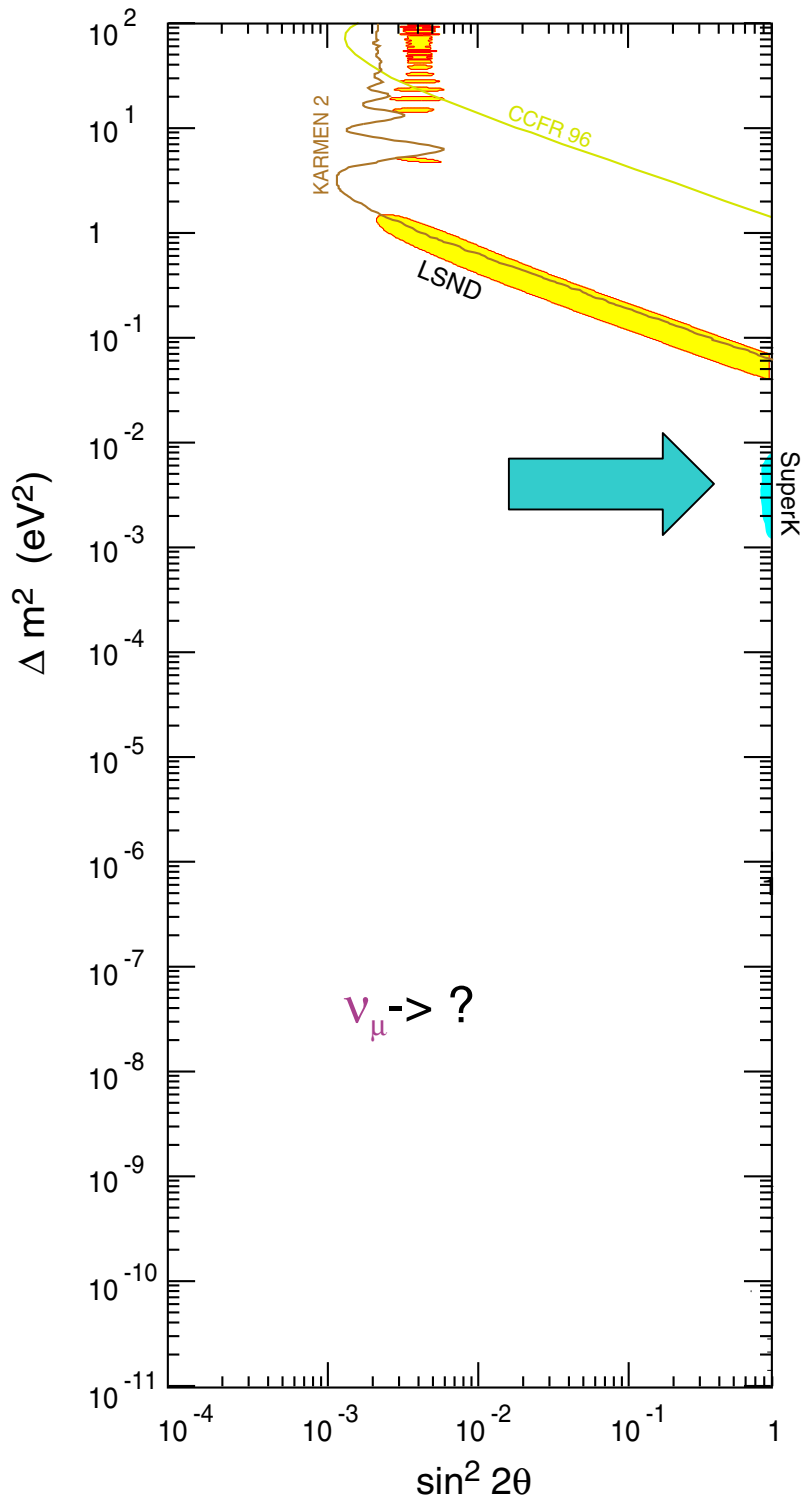
# Several studies of neutrino factory experiments

- **FNAL++ study**
  - 20-50 GeV
  - $10^{19}$ - $10^{20}$  muon decays
  - 732km, 3000 km, 7000km
- **CERN/Espana ...**
  - 50 GeV
  - $10^{20}$ - $10^{21}$  muon decays
  - 732km, 3500 km, 7000 km
- **Lots of new work shown at NUFACT00**
  - Bueno *et al.* hep-ph 0005007
  - Cervera *et al.* hep-ph 0002108
  - Albright *et al.* FNAL-FN 692
  - Barger *et al.*, hep-ph 9911524 + later

# What do we know about electron neutrino oscillations



- Solar neutrinos give low mass region
- Reactor experiments explore high  $\Delta m^2$  region



## What we know about muon neutrino oscillations

- From SuperK, Soudan, Macro ... know  $\sin^2 2\theta_{23} \sim 1$ .
- K2K, CGS, MINOS will tell us more.
- Muon neutrino expts require high energy, hence long baselines to be sensitive to low  $\Delta m^2$

# 3-flavor mixing

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

$$U = \begin{pmatrix} c_{13}c_{12} & c_{13}s_{12} & s_{13}e^{-i\delta} \\ -c_{23}s_{12} - s_{13}s_{23}c_{12}e^{i\delta} & c_{23}c_{12} - s_{13}s_{23}s_{12}e^{i\delta} & c_{13}s_{23} \\ s_{23}s_{12} - s_{13}c_{23}c_{12}e^{i\delta} & -s_{23}c_{12} - s_{13}c_{23}s_{12}e^{i\delta} & c_{13}c_{23} \end{pmatrix}$$

3 angles  $\theta_{12}$   $\theta_{13}$  and  $\theta_{23}$   
and complex phase  $\delta$

$$P(\nu_\alpha \rightarrow \nu_\beta) = \left| \langle \nu_\beta | e^{-iH_0L} | \nu_\alpha \rangle \right|^2 = \sum_{i,j} U_{\alpha i} U_{\beta i}^* U_{\alpha j}^* U_{\beta j} e^{-i\delta m_{ij}^2 L/2E}$$

3 masses  $\rightarrow$  only 2 mass differences

So far we know:

$\theta_{23}$  is large (atmospheric)

$\Delta m_{23}^2$  is  $> 10^{-3} \text{ eV}^2$  (atmospheric)

$\theta_{13}$  is small (reactor)

$$\begin{aligned}
P(\nu_\mu \rightarrow \nu_\mu) &\simeq 1 - 4|U_{\mu 3}|^2(1 - |U_{\mu 3}|^2) \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right) \\
&= 1 - 4 \sin^2(\theta_{23}) \cos^2(\theta_{13})(1 - \sin^2(\theta_{23}) \cos^2(\theta_{13})) \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right)
\end{aligned}$$

$$\begin{aligned}
P(\nu_\mu \rightarrow \nu_e) &\simeq 4|U_{e3}|^2|U_{\mu 3}|^2 \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right) \quad \text{LSND?} \\
&= \sin^2(2\theta_{13}) \sin^2(\theta_{23}) \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right)
\end{aligned}$$

$$\begin{aligned}
P(\nu_\mu \rightarrow \nu_\tau) &\simeq 4|U_{\mu 3}|^2|U_{\tau 3}|^2 \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right) \quad \Delta m_{23}^2, \theta_{23} \\
&= \sin^2(2\theta_{23}) \cos^4(\theta_{13}) \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right)
\end{aligned}$$

$$\begin{aligned}
P(\nu_e \rightarrow \nu_e) &\simeq 1 - 4|U_{e3}|^2(1 - |U_{e3}|^2) \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right) \\
&= 1 - \sin^2(2\theta_{13}) \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right),
\end{aligned}$$

$$\begin{aligned}
P(\nu_e \rightarrow \nu_\mu) &\simeq 4|U_{e3}|^2|U_{\mu 3}|^2 \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right) \quad \theta_{13} \\
&= \sin^2(2\theta_{13}) \sin^2(\theta_{23}) \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right),
\end{aligned}$$

$$\begin{aligned}
P(\nu_e \rightarrow \nu_\tau) &\simeq 4|U_{\tau 3}|^2|U_{e3}|^2 \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right) \\
&= \sin^2(2\theta_{13}) \cos^2(\theta_{23}) \sin^2\left(\frac{\delta m_{atm}^2 L}{4E}\right)
\end{aligned}$$

# What we are looking for in 10-15 years?

Assume  $\Delta m_{23}^2$  and  $\theta_{23}$  are well measured  
the next things to do are:

- Measure  $\sin^2\theta_{13}$  to  $\sim 0.001$
- See  $\nu_e \leftrightarrow \nu_\tau$
- Measure sign of  $\Delta M^2$
- Measure CP violation?
  
- All of these need a measurement of  $\nu_e \leftrightarrow \nu_X$
  
- A complete check of 3-flavor requires

$$\nu_e \leftrightarrow \nu_e$$

$$\nu_\mu \leftrightarrow \nu_e$$

$$\nu_e \leftrightarrow \nu_\mu$$

$$\nu_\mu \leftrightarrow \nu_\mu$$

and anti-particles

$$\nu_e \leftrightarrow \nu_\tau$$

$$\nu_\mu \leftrightarrow \nu_\tau$$

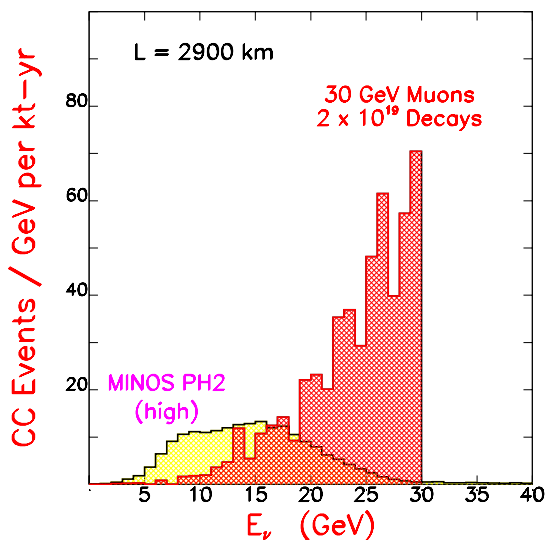
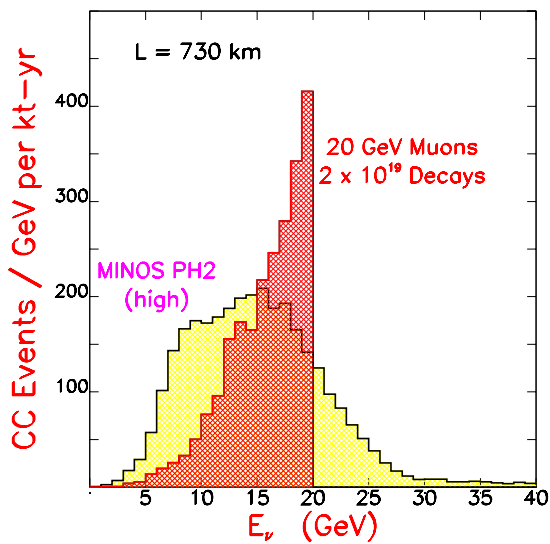
## 3 Flavor Scenarios

parameter	IA1	IA2	IA3	1B1	1C1
$\delta m_{32}^2$ (eV <sup>2</sup> )	$3.5 \times 10^{-3}$	$3.5 \times 10^{-3}$	$3.5 \times 10^{-3}$	$3.5 \times 10^{-3}$	0.3
$\delta m_{21}^2$ (eV <sup>2</sup> )	$5 \times 10^{-5}$	$6 \times 10^{-6}$	$1 \times 10^{-7}$	0.3	$7 \times 10^{-4}$
$\sin^2 2\theta_{23}$	1.0	1.0	1.0	1.0	0.53
$\sin^2 2\theta_{13}$	0.04	0.04	0.04	0.015	0.036
$\sin^2 2\theta_{12}$	0.8	0.006	0.9	0.015	0.89
$\delta$	$0, \pm\pi/2$	$0, \pm\pi/2$	$0, \pm\pi/2$	$0, \pm\pi/2$	$0, \pm\pi/2$
$\sin^2 2\theta_{atm}$	0.98	0.98	0.98	0.99	-
$\sin^2 2\theta_{reac}$	0.04	0.04	0.04	0.03	-
$\sin^2 2\theta_{solar}$	0.78	0.006	0.88	-	-
$\sin^2 2\theta_{LSND}$	-	-	-	0.03	0.036
$J$	0.02	0.002	0.02	0.002	0.015



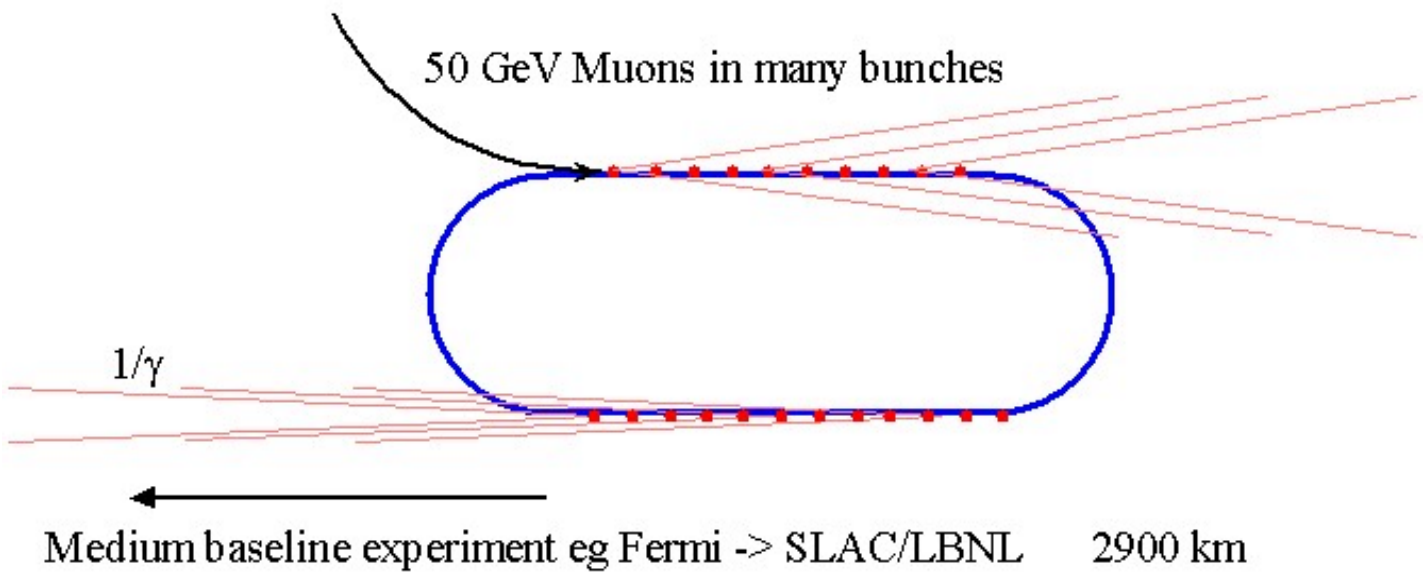
# Why not use conventional beam

- Conventional beam is great for measuring  $\nu_\mu$  related parameters to  $\sim 1\%$ .
- Limitations are electron detection in hadron showers limits  $\nu_\mu \rightarrow \nu_e$
- To go beyond 1% on  $\nu_\mu \leftrightarrow \nu_e$  or get mass effects and CP violation, need:
  - long baseline,
  - higher energy,
  - way to see  $\nu_\mu \leftrightarrow \nu_e$  transitions with better accuracy.



# The Neutrino Source

## Muon Storage Ring as a Neutrino Source

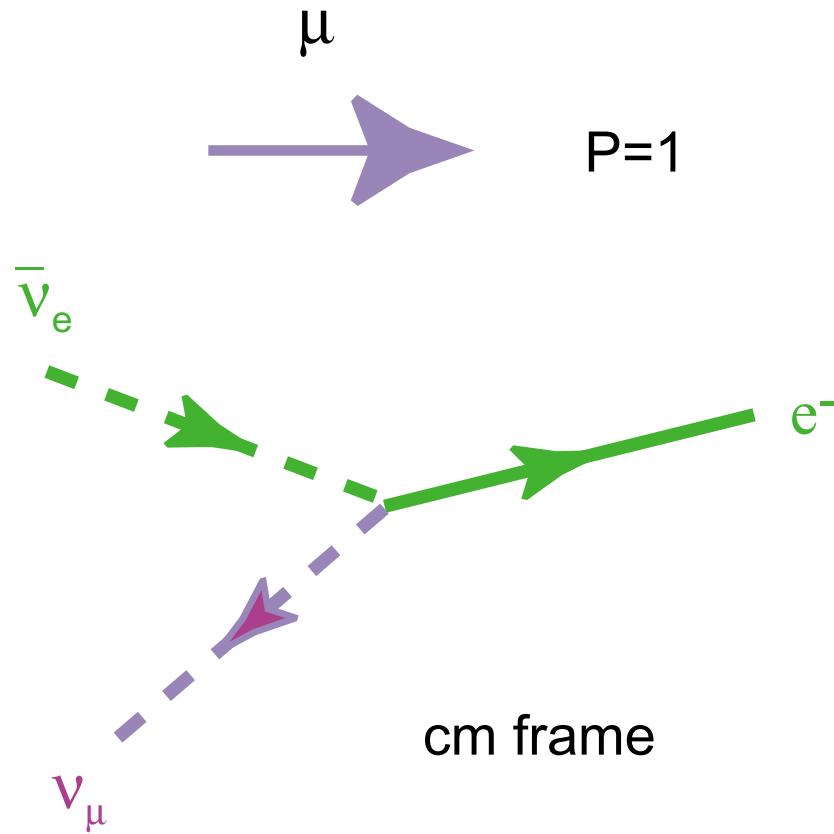


Parameters for the Muon Storage Ring		
Energy	GeV	50
decay ratio	%	>40
Designed for inv. Emittance	m*rad	<b>0.0032</b>
Cooling designed for inv. Emitt.	m*rad	<b>0.0016</b>
$\beta$ in straight	m	160
$N_\mu$ /pulse	$10^{12}$	6
typical decay angle of $\mu = 1/\gamma$	mrاد	2.0
Beam angle $(\sqrt{\epsilon/\beta_0}) = (\sqrt{\epsilon} \gamma)$	mrاد	0.2
Lifetime $c*\gamma*\tau$	m	$3 \times 10^5$

$\gamma = (1 - \alpha^2)^{-1/2} / \beta$

6/14/00

# Properties of neutrino beams from muon decay



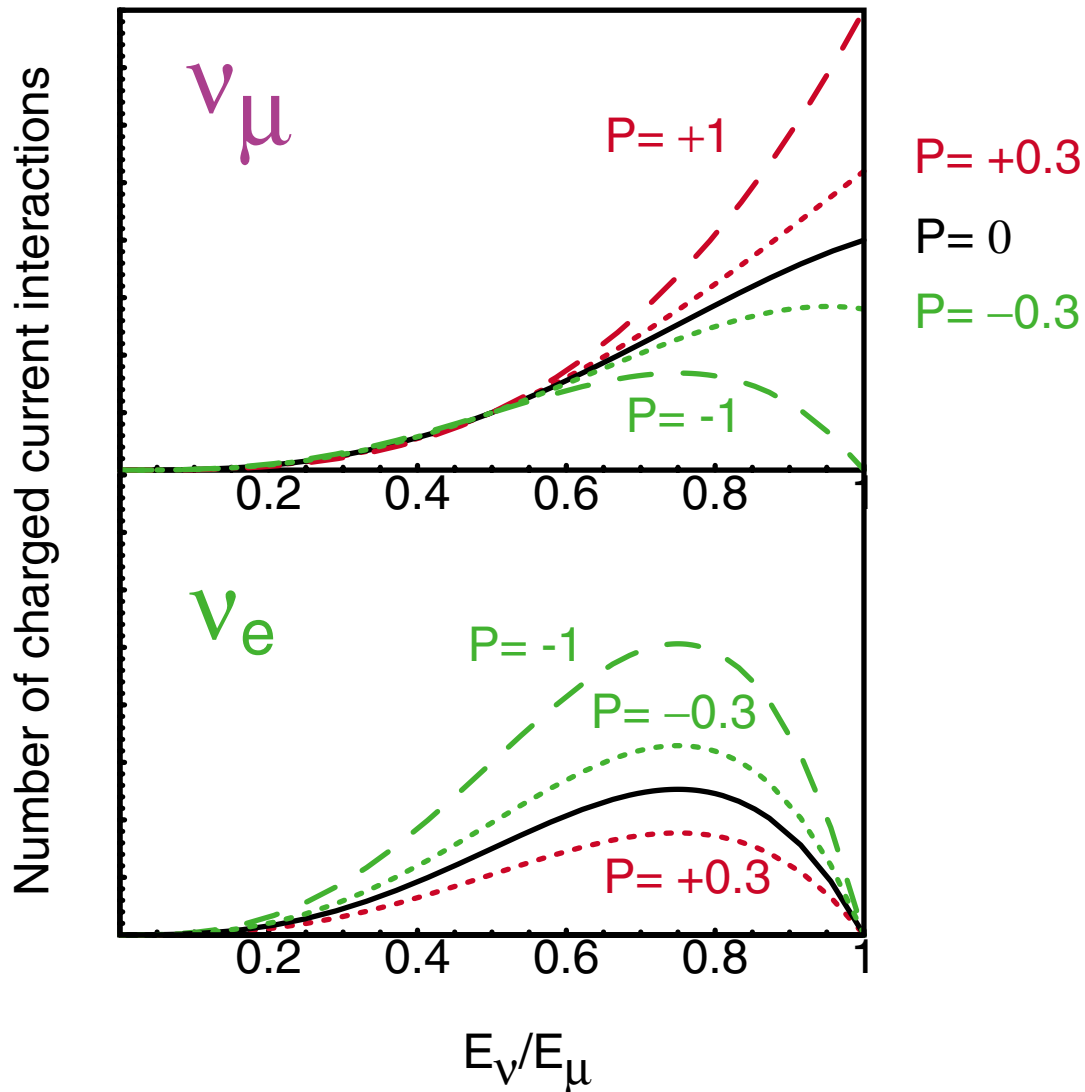
$$\frac{dN(\nu_\mu)}{dz d \cos \theta_{CM}} = 2z^2[(3 - 2z) \mp P(1 - 2z) \cos \theta]$$

$$\frac{dN(\nu_e)}{dz d \cos \theta_{CM}} = 6z^2[(1 - z) \mp P(1 - z) \cos \theta]$$

$$z = \frac{E_\nu}{E_{max}} \quad \text{where} \quad E_{max} = m_\mu/2$$

Single decay mode and well defined kinematics

# Neutrino interaction rates as a function of scaled neutrino energy



Beam is a mixture of  $\nu_\mu$  and anti- $\nu_e$  or  $\nu_e$  and anti- $\nu_\mu$ . Peaked towards high energies, Polarization is hard to get but can be used to remove backgrounds from the mixture.

# Why bother with muon decay?

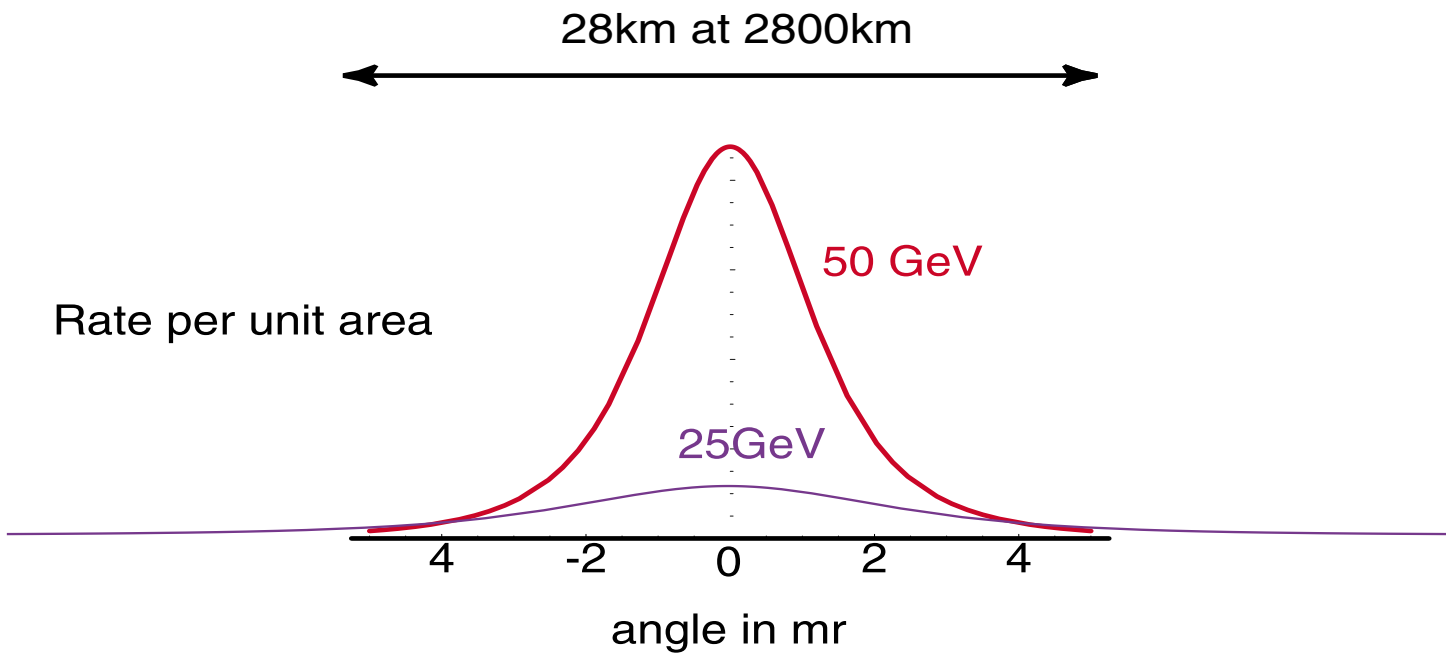
- Goal is maximum neutrino/proton
  - Decay pions/kaons at low energy
  - More decay in decay volume  
(~3% at FNAL high energy  $\nu$  beam)
  - Then accelerate
  - 40% of muons decay in the right direction
- Very well understood source
  - Only one decay process
  - Parent particles ~ monochromatic
  - Around long enough to monitor

See  $\nu_e \rightarrow \nu_\mu$  in the  $\nu_e \rightarrow \nu_\mu \rightarrow \mu^- + X$  channel 'Wrong sign muons'

$\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu \rightarrow \mu^+ + X$  is the conventional muon source

## Neutrino Event rates vs angle

$\theta$  typical is  $\sim 1/\gamma$



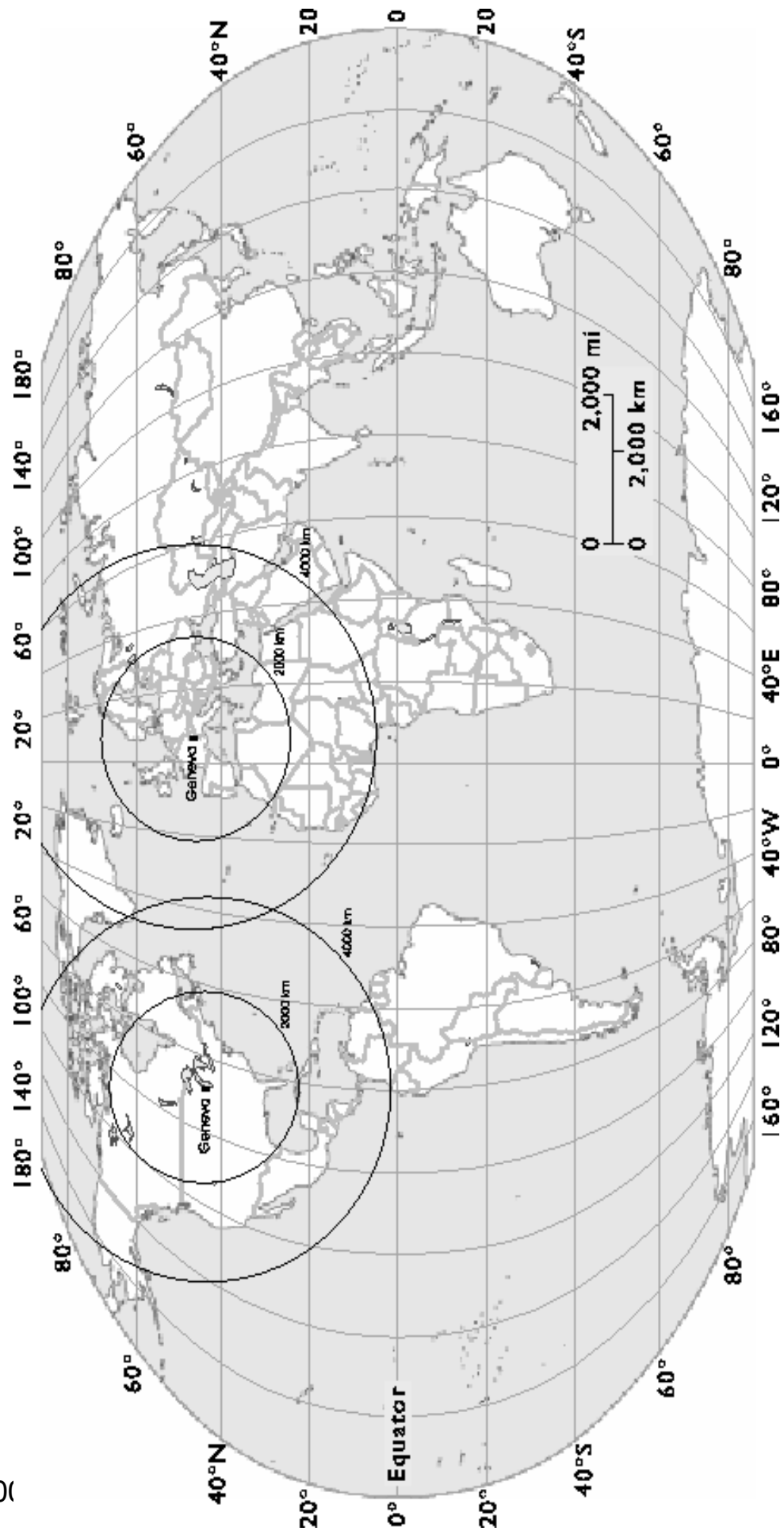
Spread of beam scales as  $1/E^2$

Event rate/neutrino scales as  $E$

For same  $L$  event rate/unit area scales as  $E^3$

Spread of beam scales as  $L^2$

For fixed  $E/L$ , event rate/unit area scales as  $E$



# Event rates for a 10 kton detector

Rates				
		L=732 km	L=2900 km	L=7400 km
$\mu^-$ 10 <sup>20</sup> decays	$\nu_\mu$ CC	226000	14400	2270
	$\nu_\mu$ NC	67300	4120	680
	$\bar{\nu}_e$ CC	87100	5530	875
	$\bar{\nu}_e$ NC	30200	1990	300
$\mu^+$ 10 <sup>20</sup> decays	$\bar{\nu}_\mu$ CC	101000	6380	1000
	$\bar{\nu}_\mu$ NC	35300	2240	350
	$\nu_e$ CC	197000	12900	1980
	$\nu_e$ NC	57900	3670	580

$E_\mu = 30 \text{ GeV}$

No oscillations

No polarization

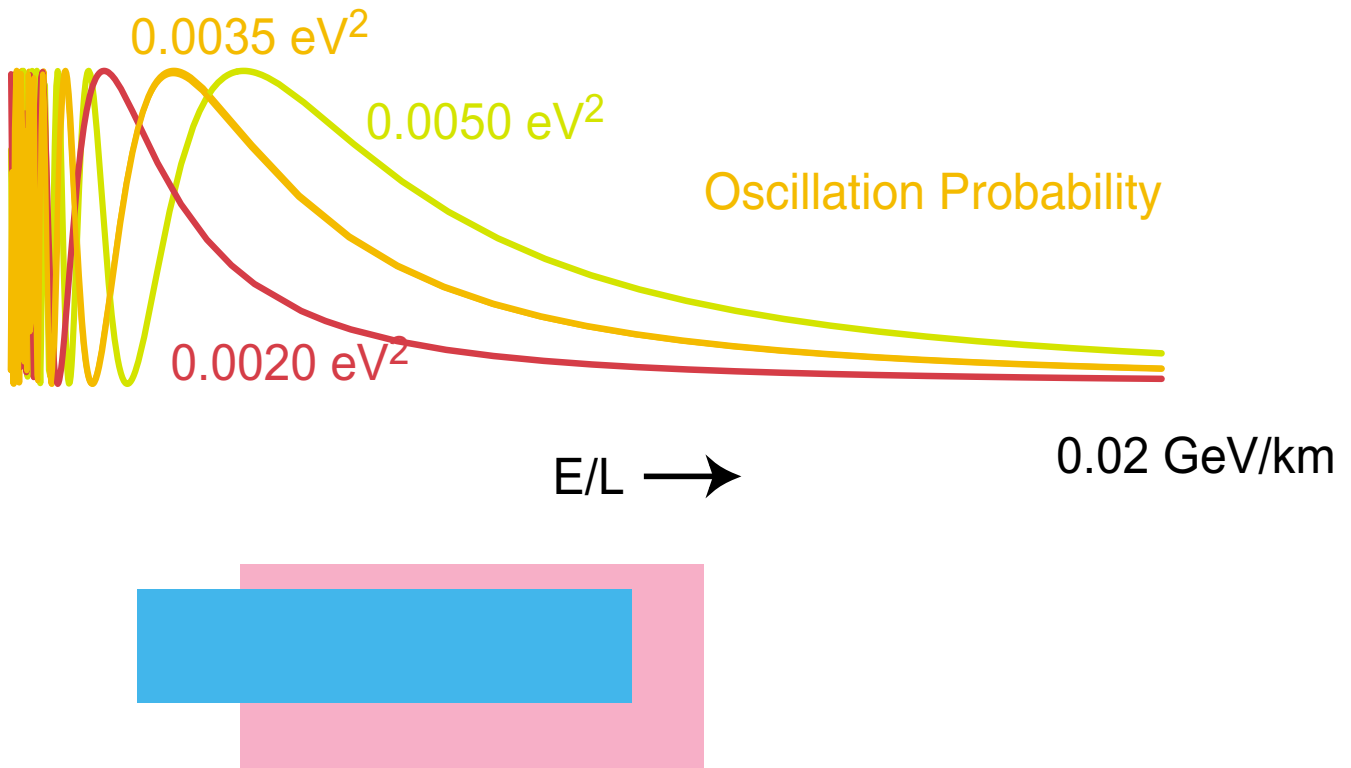
No beam divergence



Experiments can be described by their E/L coverage

$$\bullet P(\nu_\alpha \rightarrow \nu_\beta) \sim \sin^2 2\theta \sin^2[1.27 \Delta m^2 L/E]$$

$\bullet m$  in eV,  $L$  in km,  $E$  in GeV



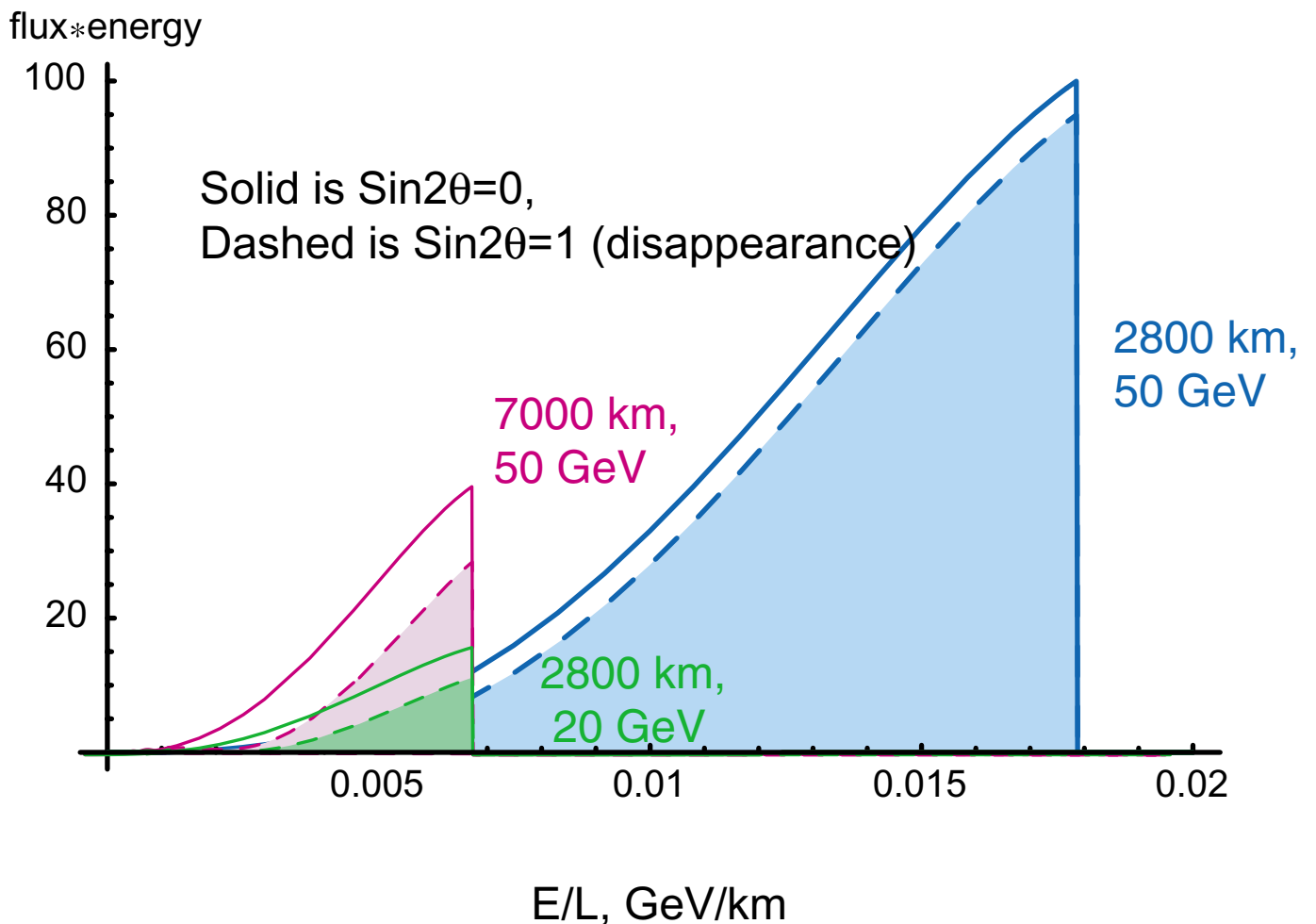
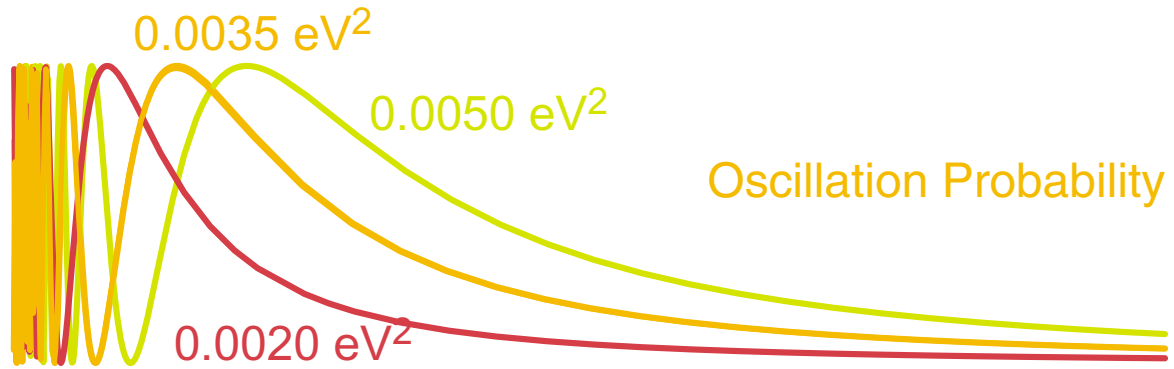
If  $E/L \ll \Delta m^2$ ,  $P(\nu_\alpha \rightarrow \nu_\beta) \sim \frac{1}{2} \sin^2 2\theta$

If  $E/L \gg \Delta m^2$ ,  $P(\nu_\alpha \rightarrow \nu_\beta) \sim 0$

If  $E/L \sim \Delta m^2$ , can measure both  $\Delta m^2$  and  $\sin^2 2\theta$

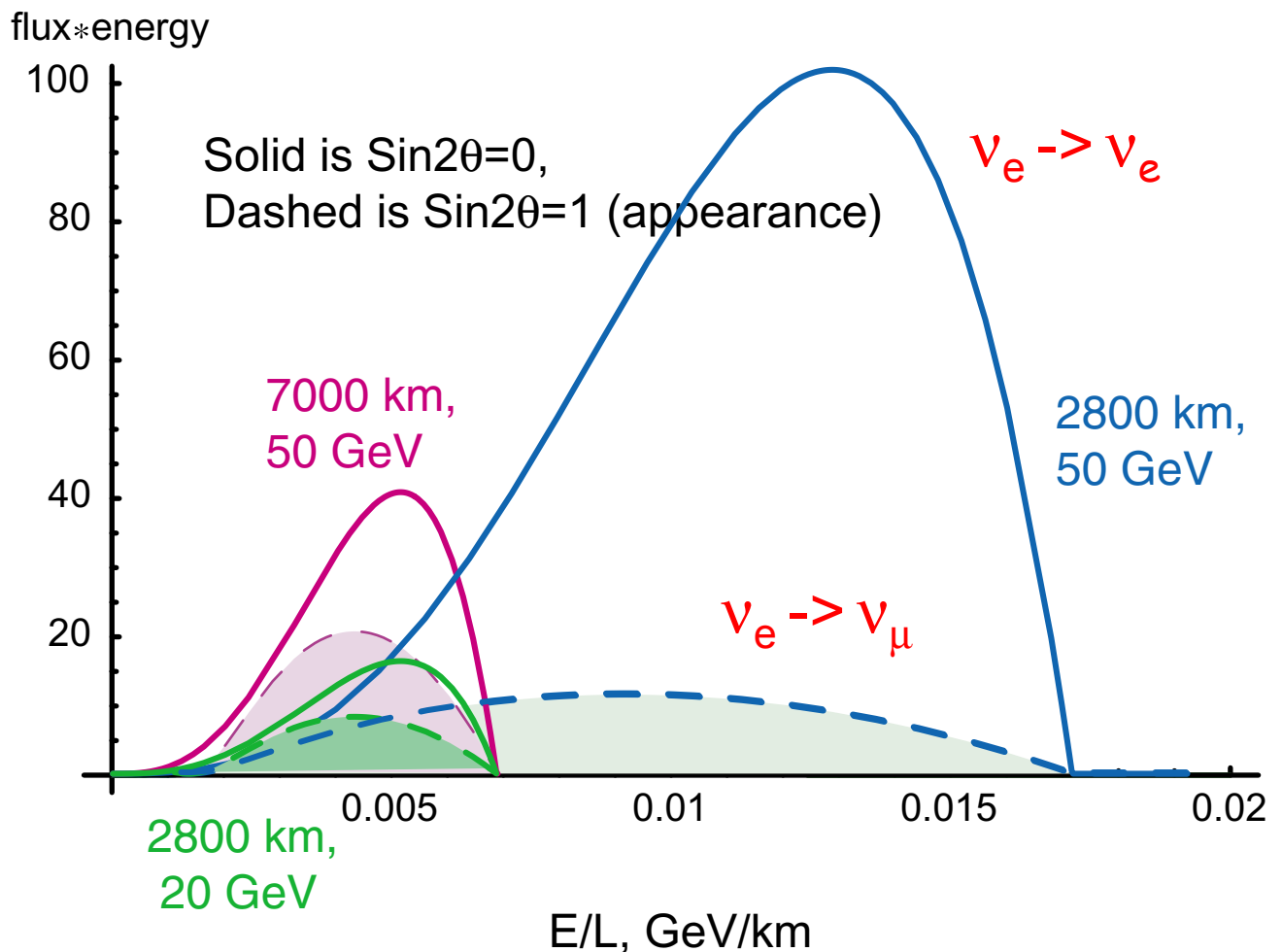
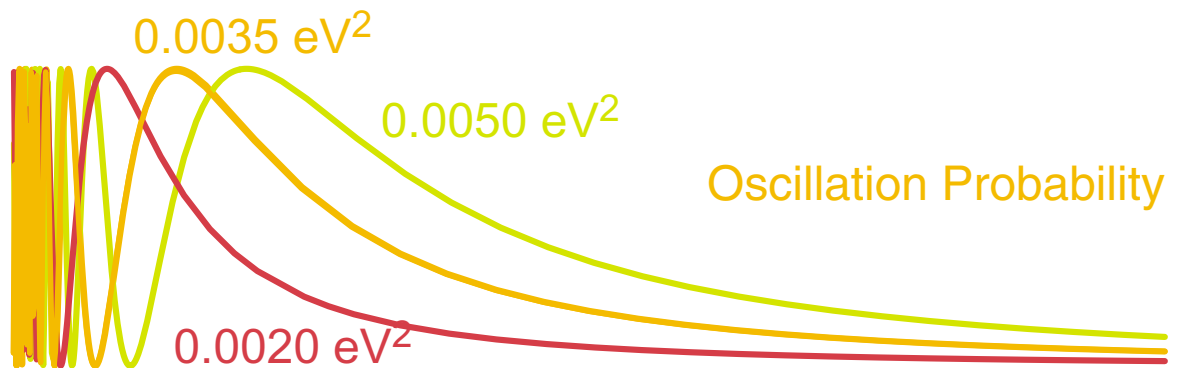
# Numbers of muon neutrino interactions for fixed number of muon decays

$\Delta m^2 = 0.0035 \text{ eV}^2$



# Numbers of electron neutrino interactions for fixed number of muon decays

$\Delta m^2 = 0.0035 \text{ eV}^2$

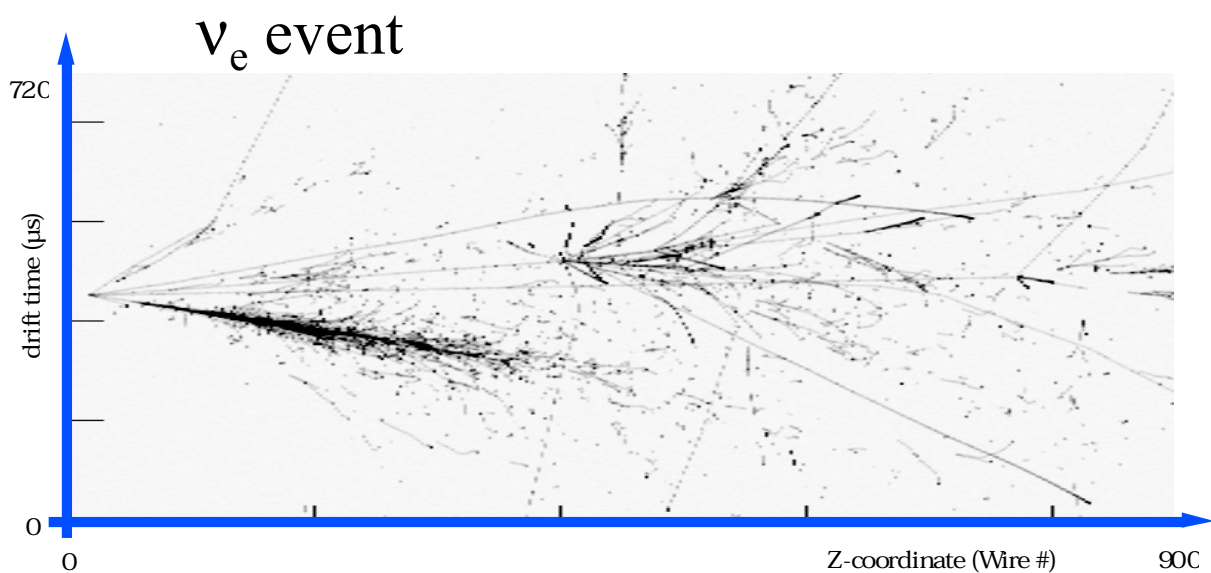
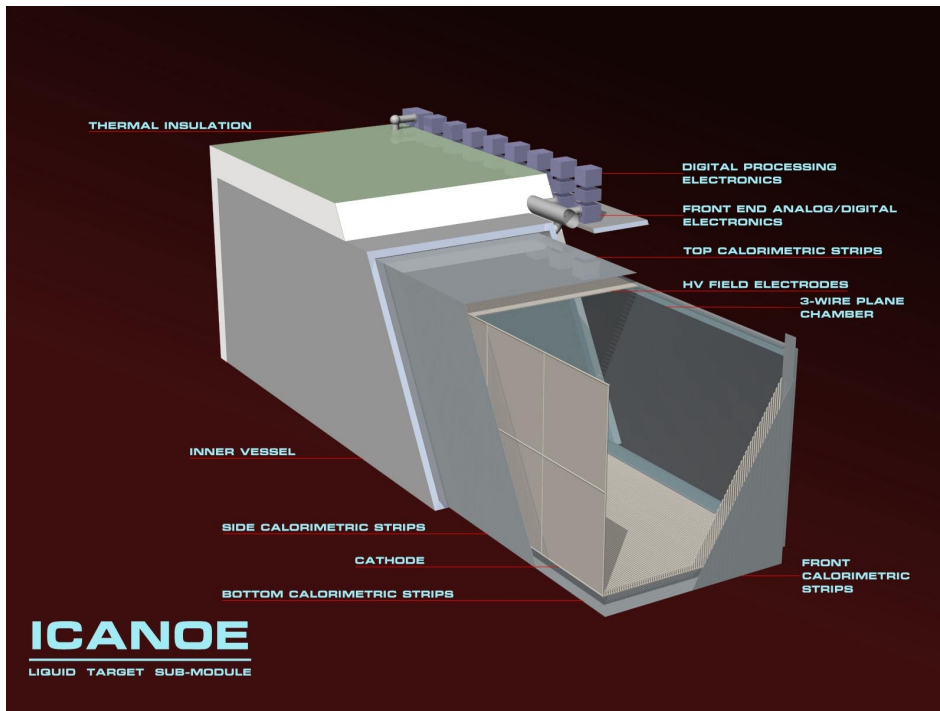


# Detectors

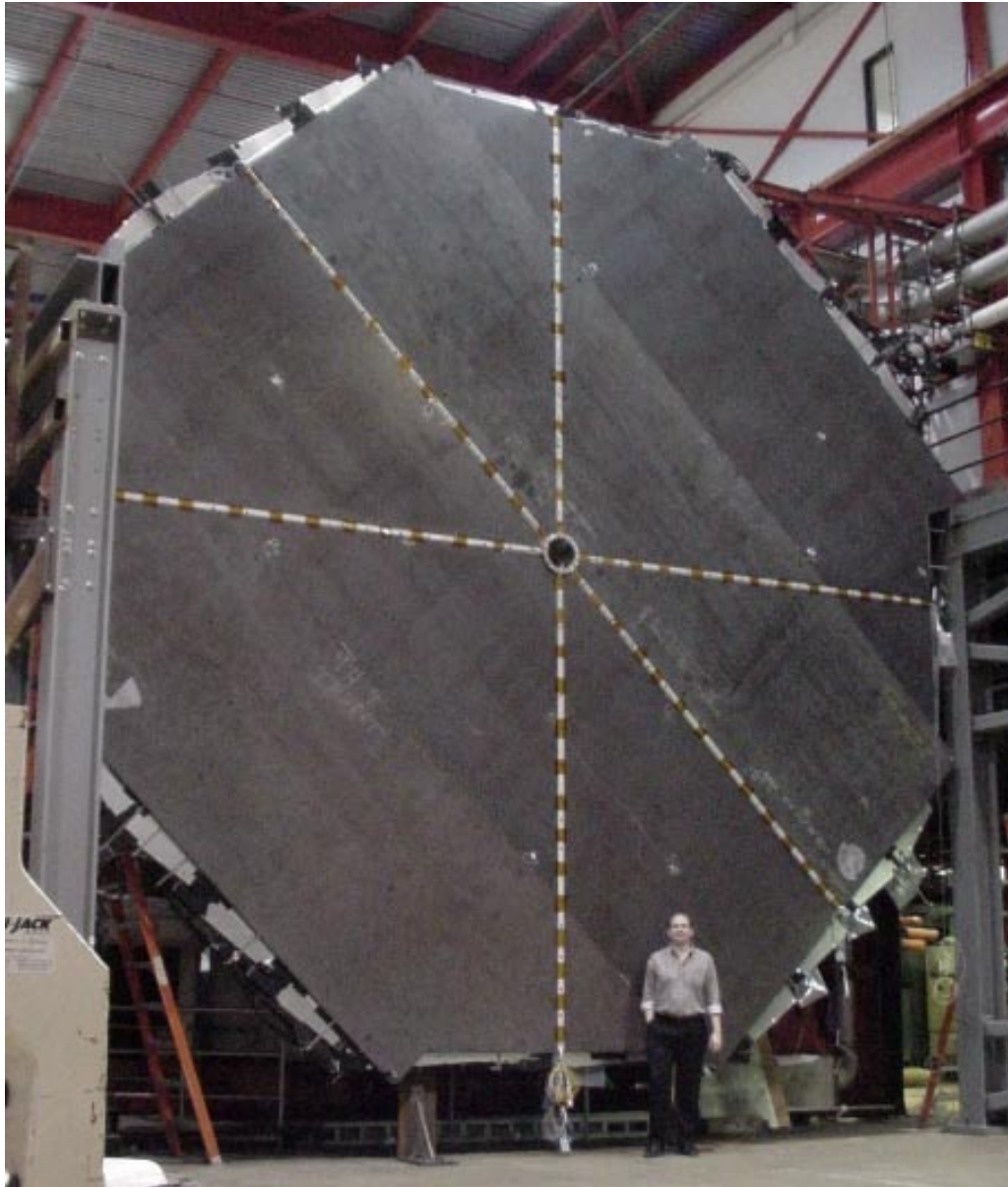
'Protons are cheaper than muons'

- Tau detection
  - Emulsion/msgc ~ 1-20 kTons
  - Tau id, electron id
- Liquid argon drift
  - 10-20 kTons
  - Electron id!
- Magnetized Iron Scintillator
  - 20-100 kTons
  - Good muon id!
- Water Cerenkov with magnet tail
  - 50-500 kTons
  - Electron id, limited muon charge

# Liquid Argon with drift readout



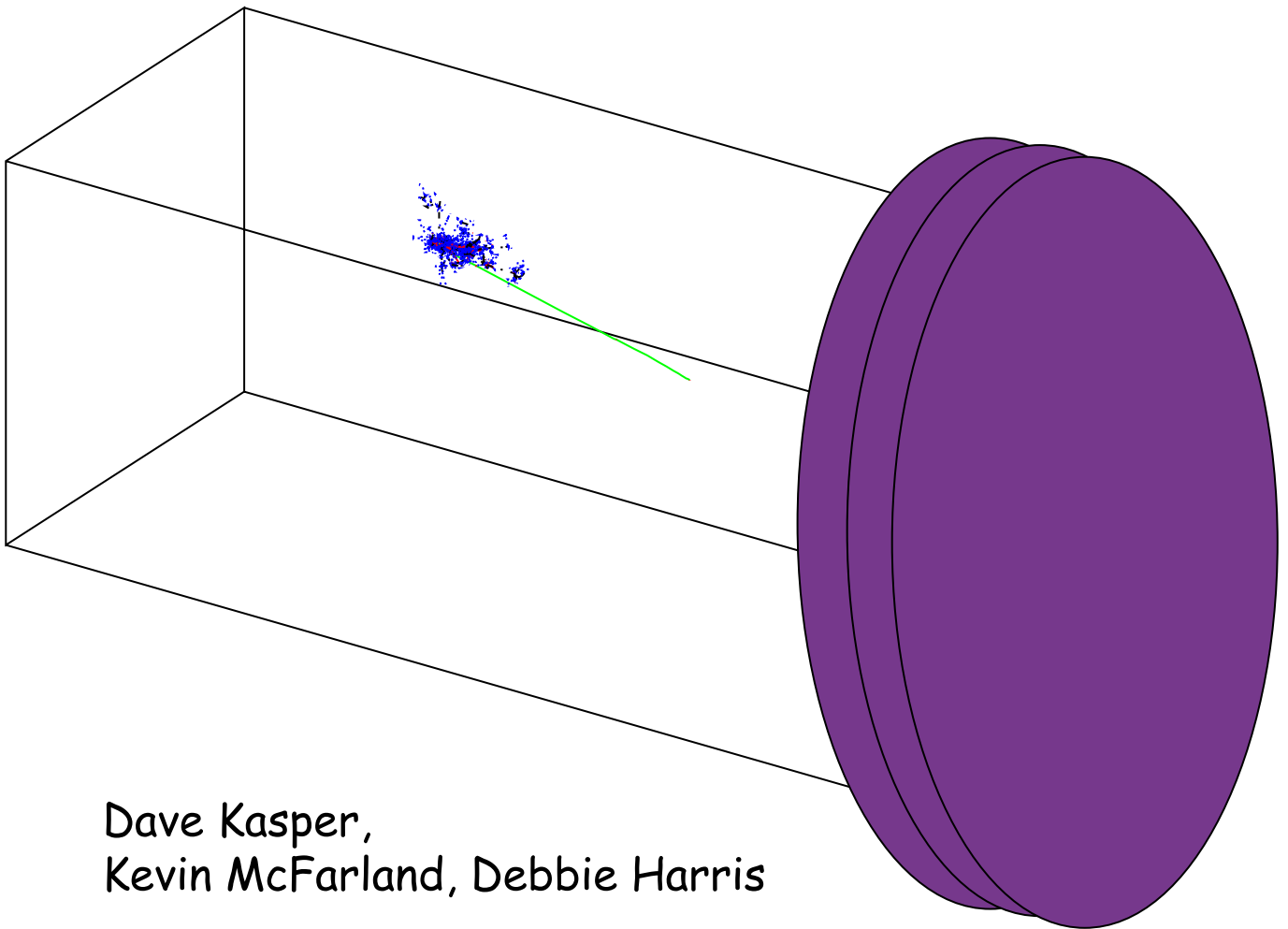
# Steel-Scintillator MINOS/MONOLITH/anon.



50 kT version of MINOS

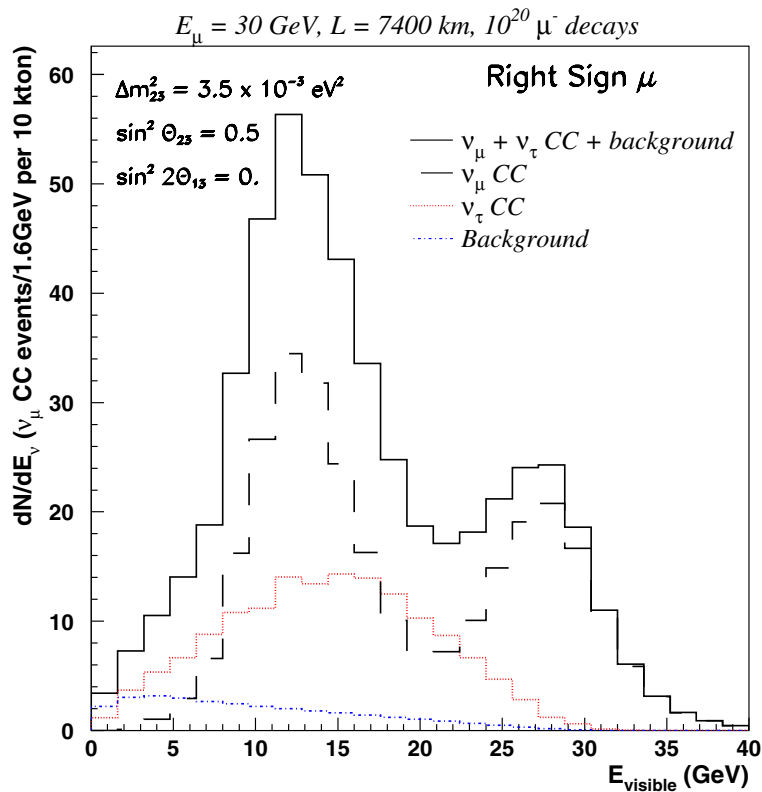
# 10xSuperK?

Water detector followed by analyzing magnet

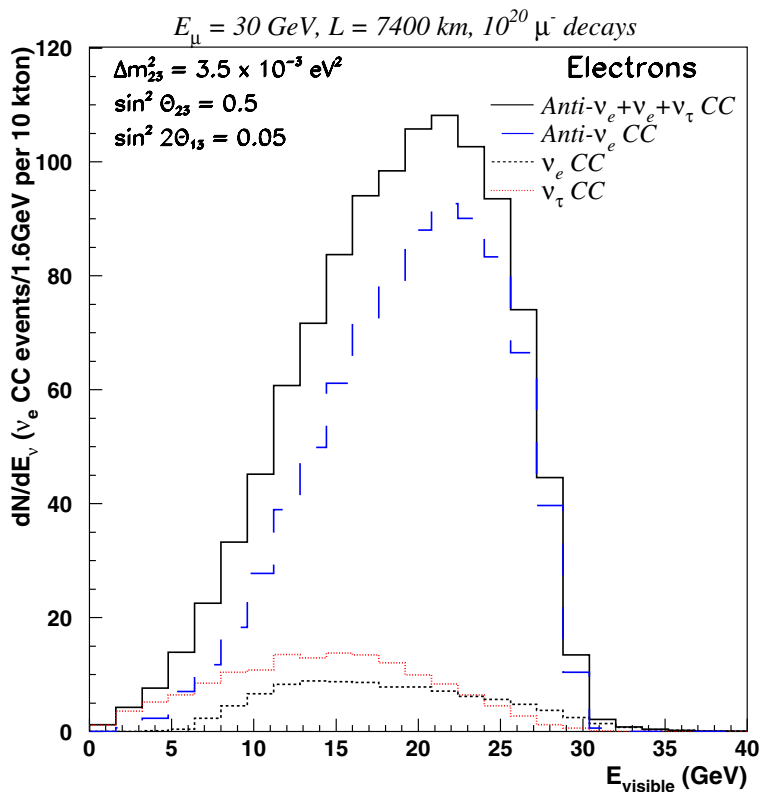


Dave Kasper,  
Kevin McFarland, Debbie Harris

# 10<sup>20</sup> muon decays



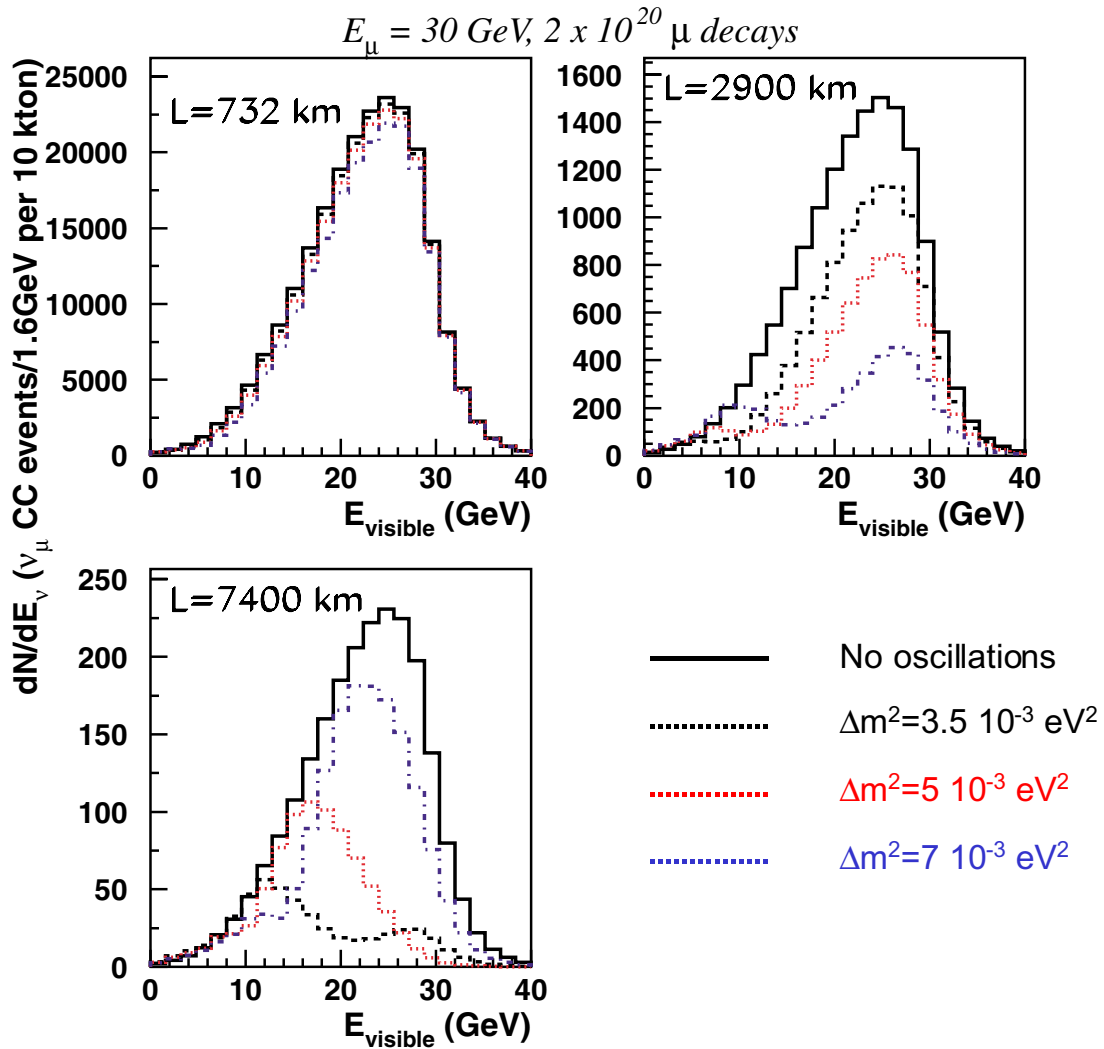
- Right sign muons
  - Dip due to oscillation
- Tau's contribute
  - Signal?
  - Background?



Bueno et al.



# Disappearance Experiment $\nu_\mu \rightarrow \nu_\tau$



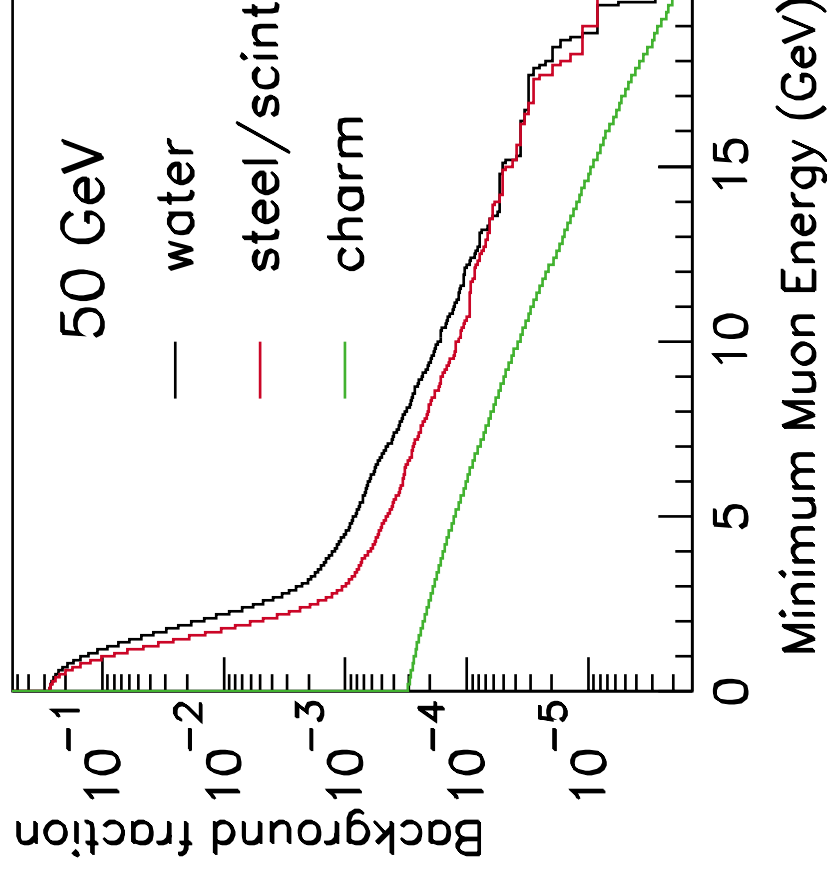
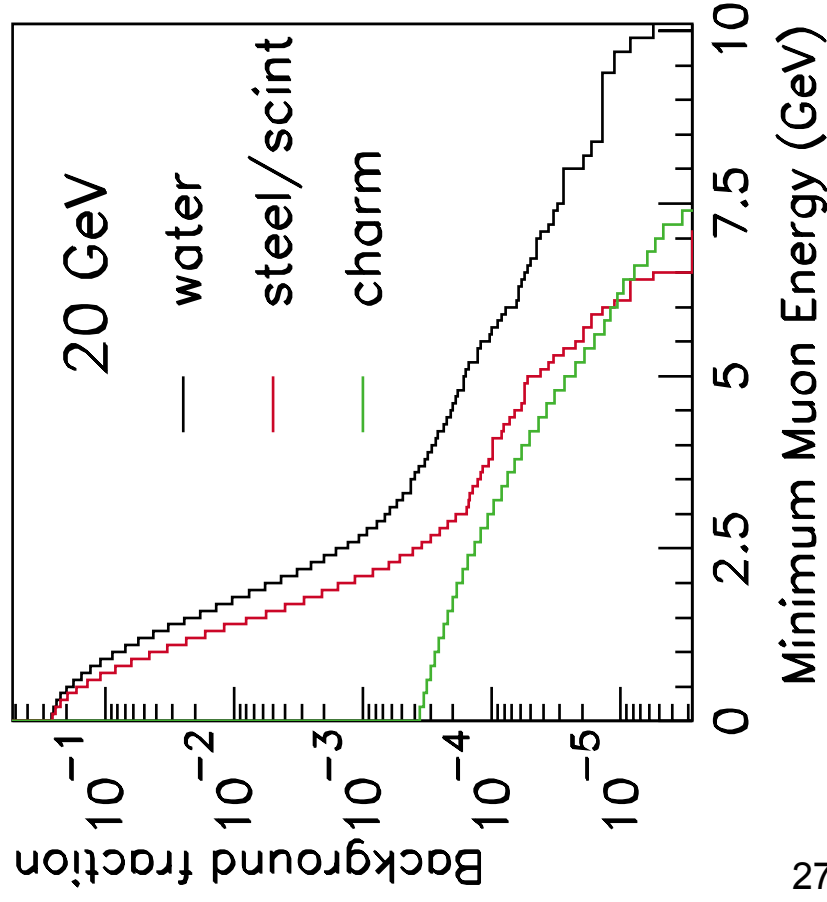
Mario Campanelli, ETH Zurich

# What determines the machine energy?

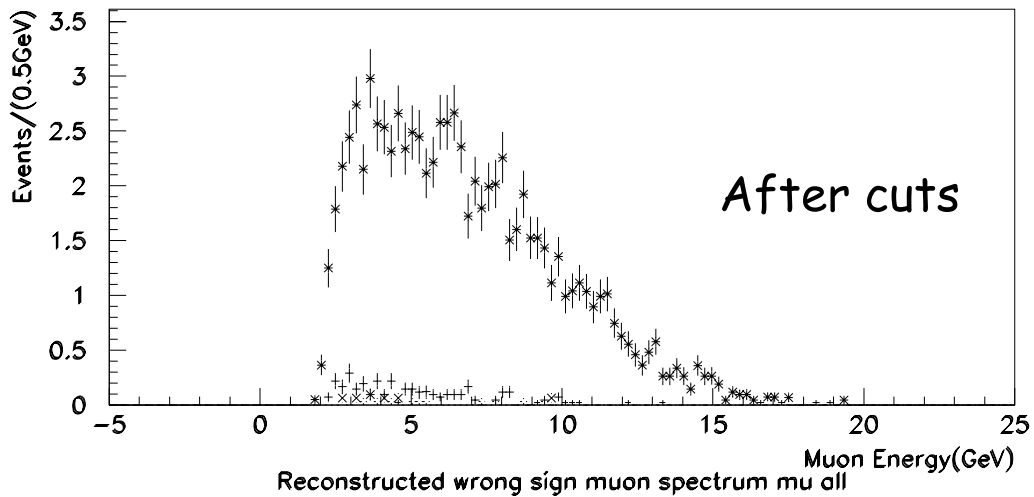
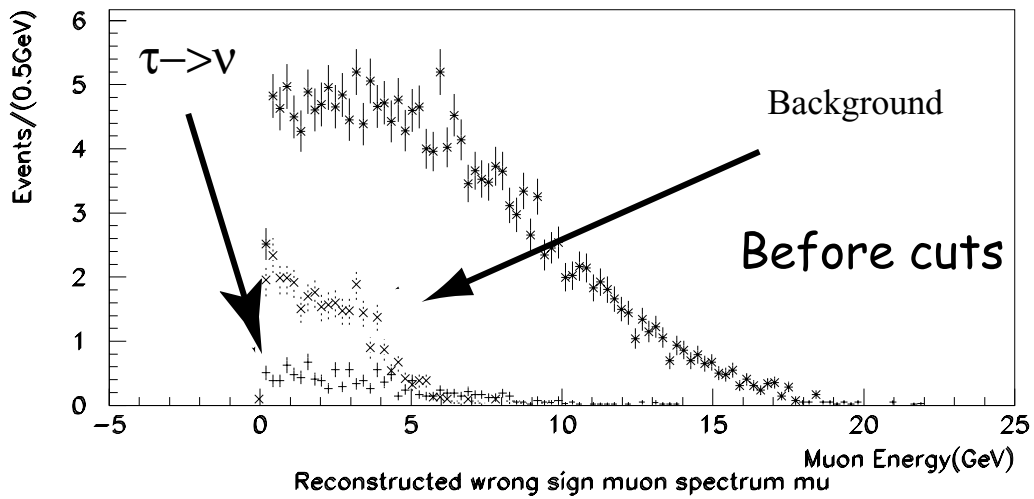
- We're interested in  $\nu_e \rightarrow \nu_\mu$
- Need to tag wrong sign muons with very low backgrounds
- there are also anti- $\nu_\mu$  in the beam
- Wrong sign muons from
  - Hadron decay
  - Charm decay
  - Non-interacting hadrons
  - Charge confusion
- How do you tell a 2 GeV pion from a 2 GeV muon at the 0.01% level?

# Backgrounds to $\bar{\nu}_e \rightarrow \bar{\nu}_\mu \rightarrow \mu^+$

Pions which do not interact!



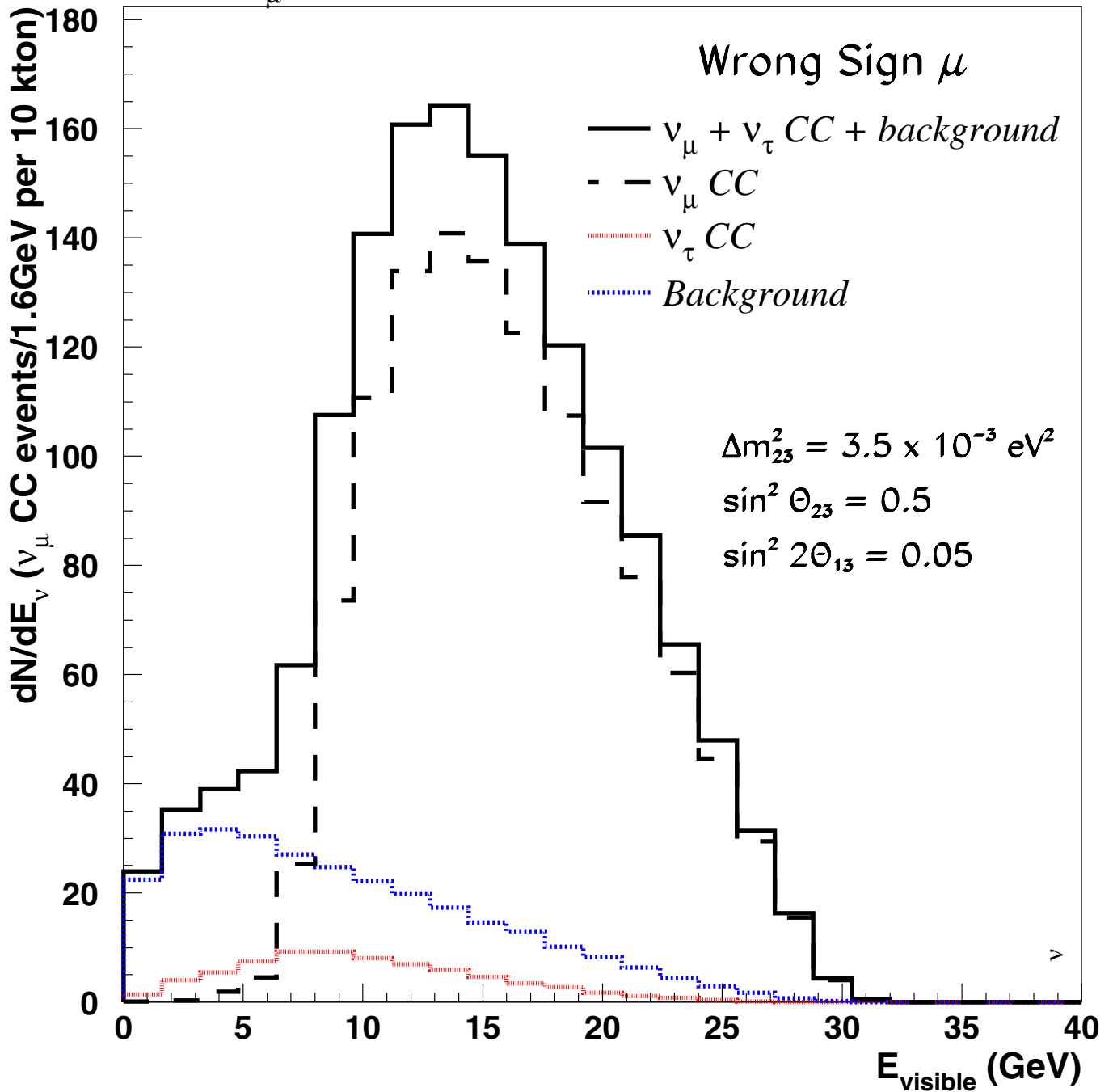
Wrong sign muon signal  
10 kt Iron-scintillator detector  
20 GeV muon decay  
 $10^{20}$  decays

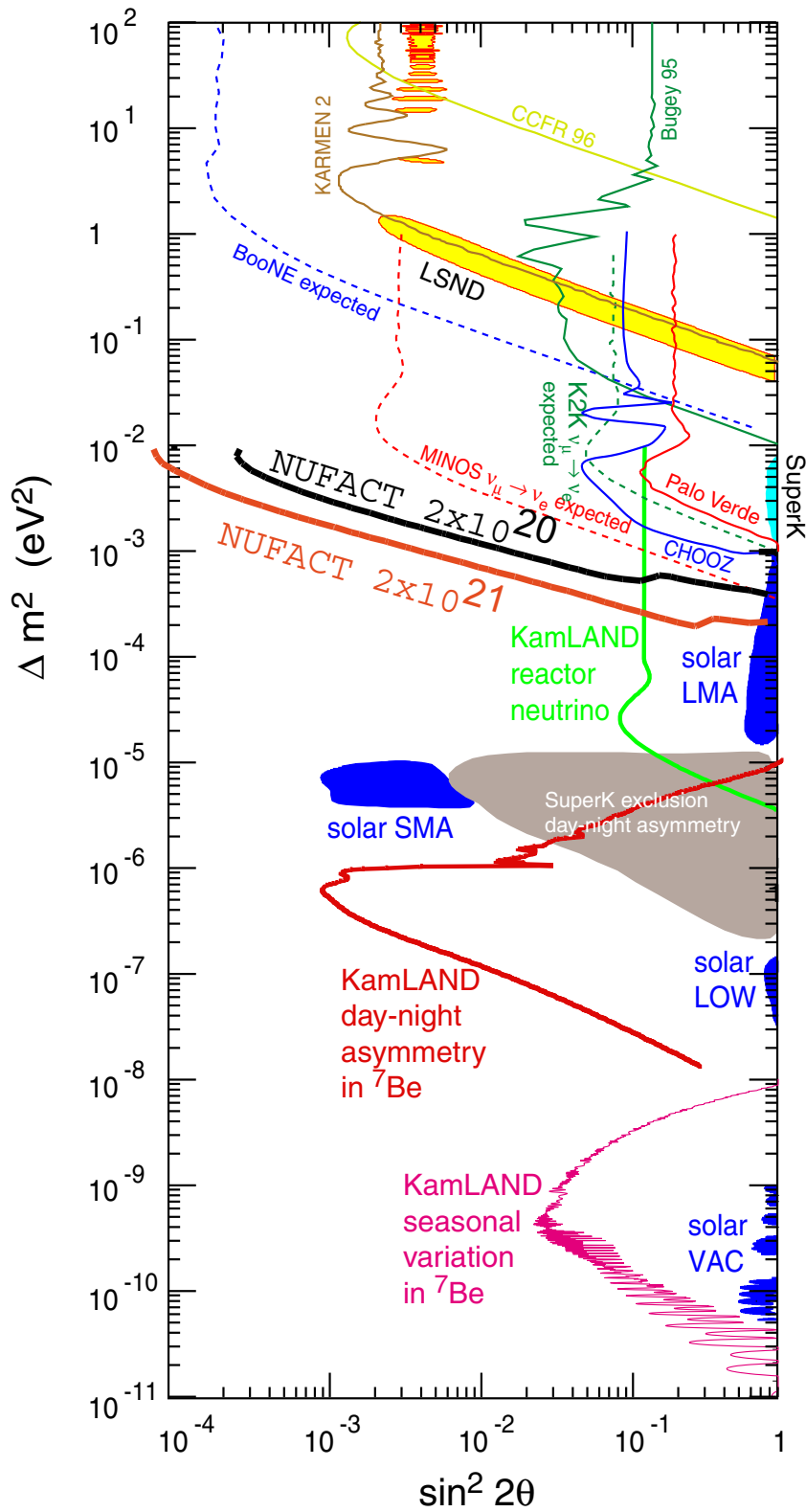


Bernstein, Harris, McFarland, Spentzouris

# $10^{21}$ muon decays

$E_\mu = 30 \text{ GeV}$ ,  $L = 7400 \text{ km}$ ,  $10^{21} \mu^+$  decays





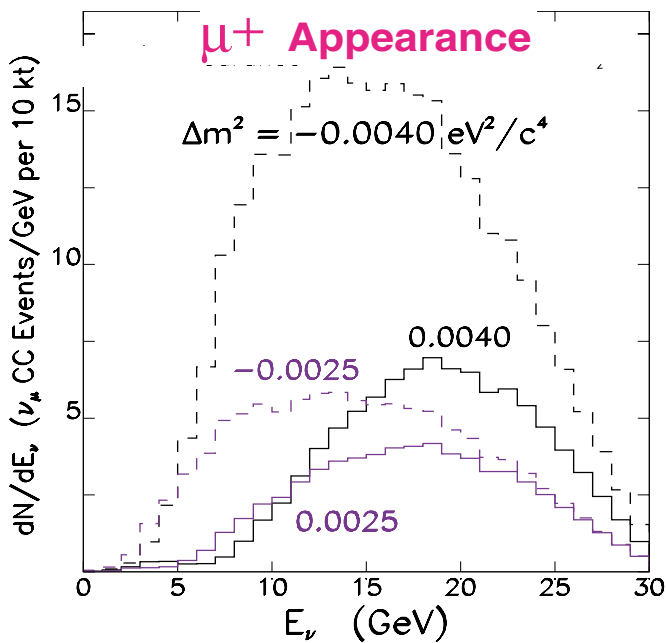
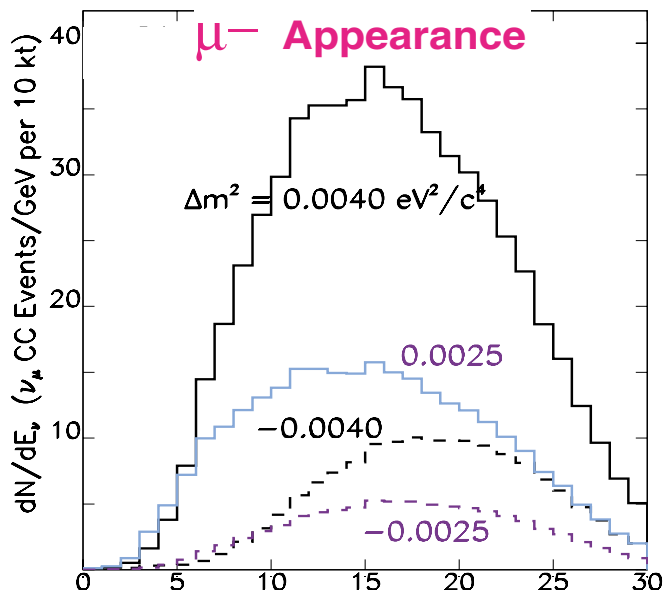
Limits on  $\sin^2 2\theta_{13}$  for a 10kt detector 7400 km away.

Bueno *et al.*

# $\nu_e > \nu_\mu$ Appearance

**FNAL > SLAC/LBNL**  
**(L = 2800 km) 10kT**       **$E_\mu = 30$  GeV**  
 **$2 \times 10^{20}$  Decays**

**Three Flavor Mixing**  
 $\Delta m^2_{21} = 5 \times 10^5 \text{ eV}^2/\text{c}^4$   
 $\sin^2 2\theta_{23} = 1 \quad \delta = 0$   
 $\sin^2 2\theta_{12} = 0.8$   
 $\sin^2 2\theta_{31} = 0.04$



*Sign of  $\Delta m^2$  can be determined thanks to matter effects*

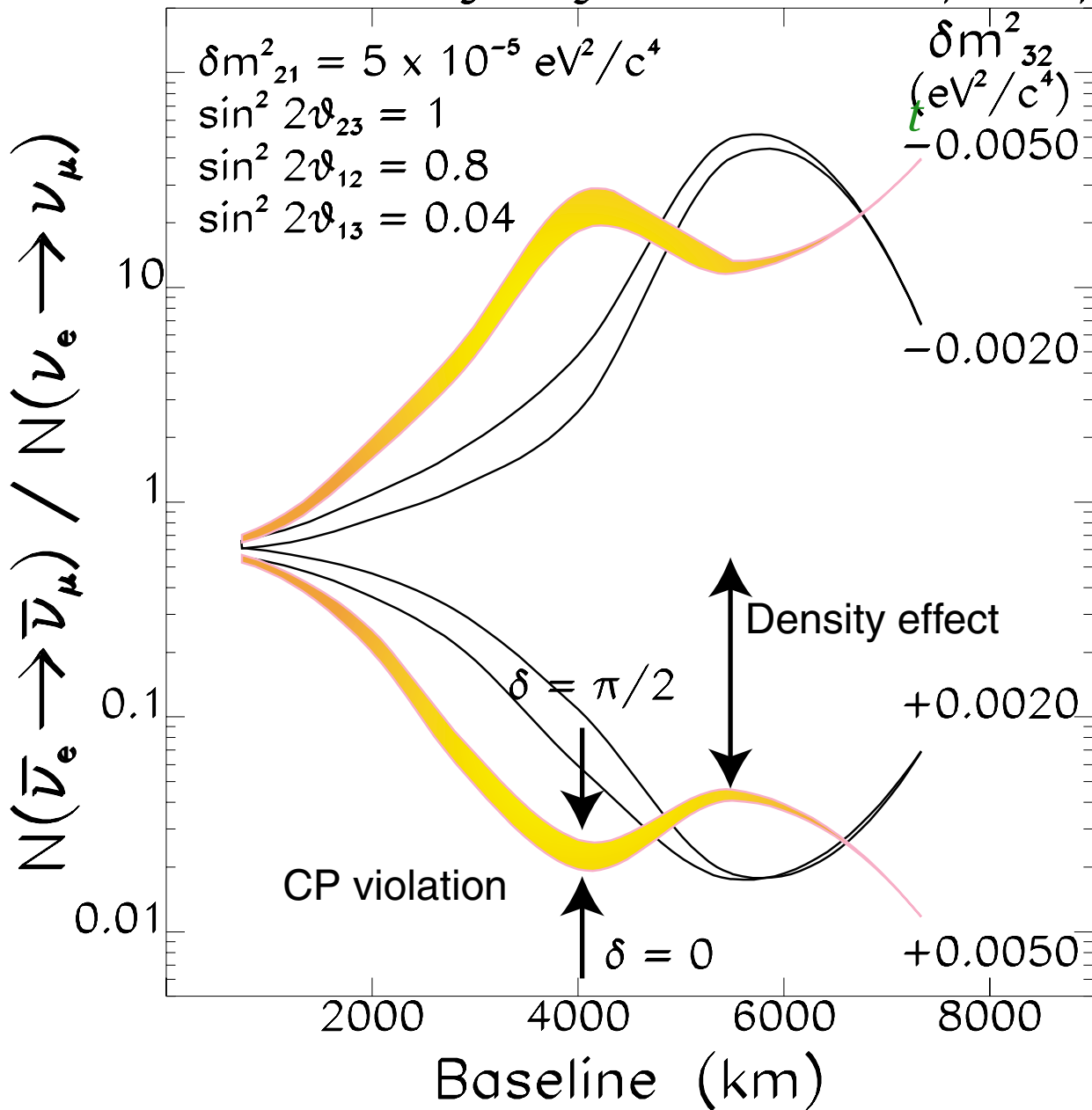
*Barger Geer Raja Whisnant  
 FermilabPub 99341*

# CP violation?

$$E_\mu = 20 \text{ GeV}$$

$$E_{\text{min}} = 4 \text{ GeV}$$

Relative wrong-sign muon rates  $\mu^+$  cf  $\mu^-$



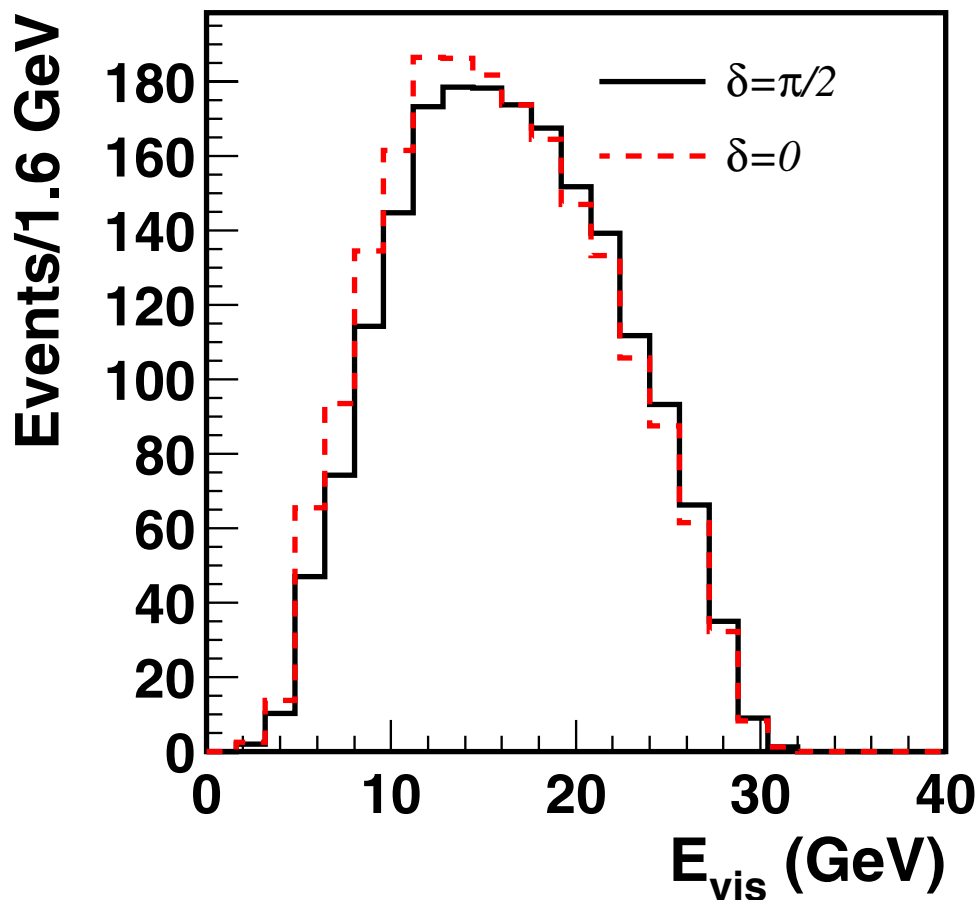
*V. Barger, S. Geer, R. Raja, K. Whisnant*



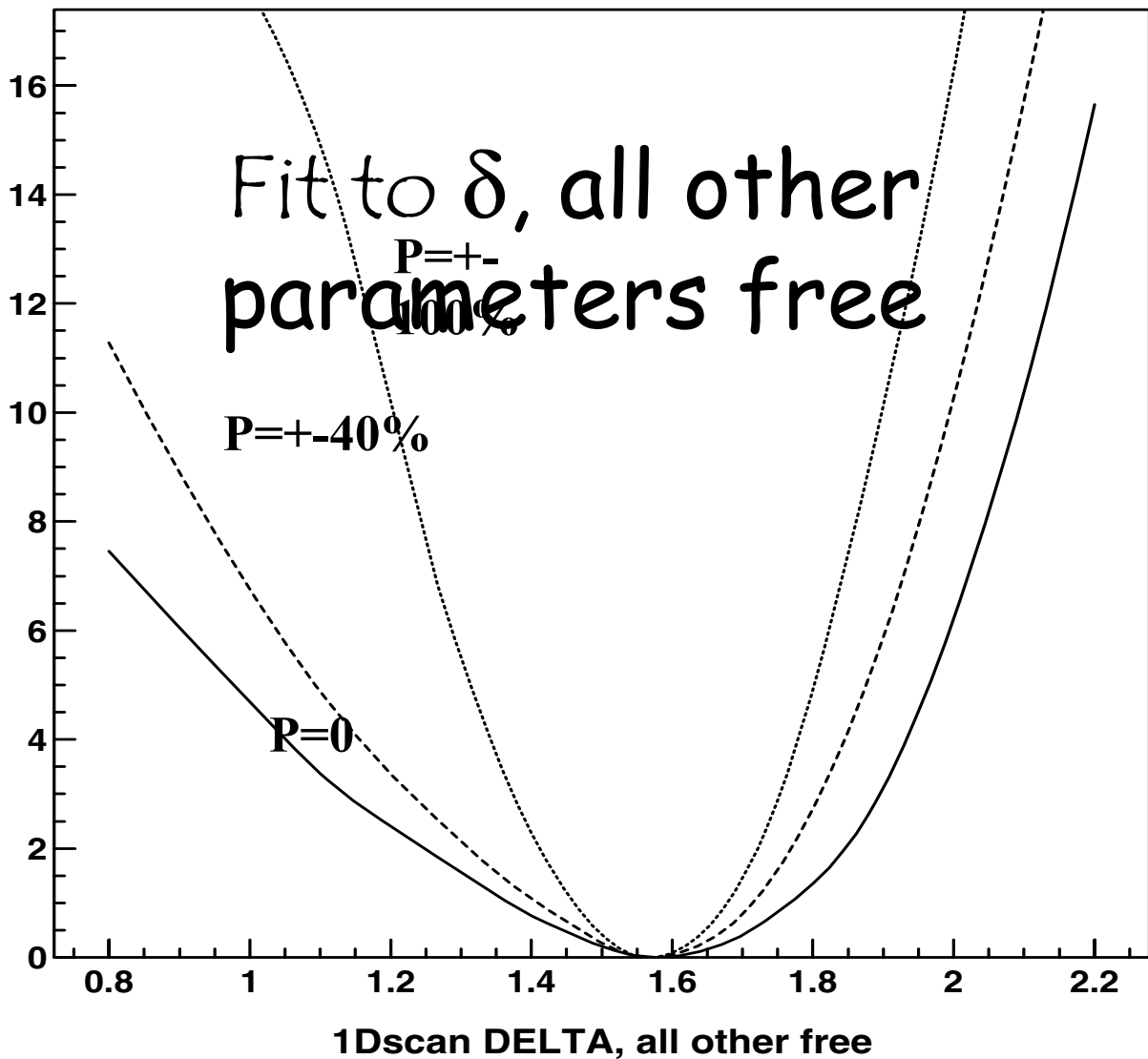
# What optimal CP violation looks like

Assume Solar LMA solution, large  $\theta_{12}$ ,  $\theta_{13}$

## Wrong-sign muons



$10^{21} \mu$ , 3500 km

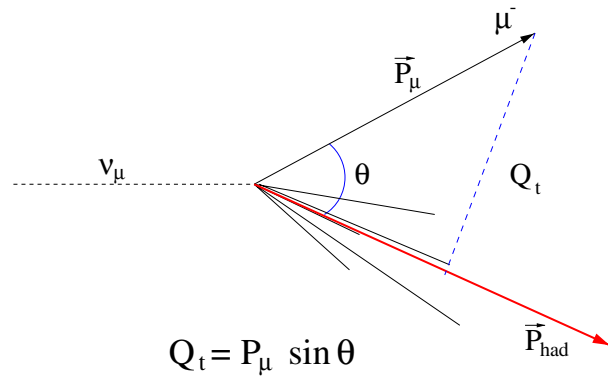


$P = 0 :$	$\delta = 1.57 \pm 0.20$
$P = \pm 40\%$	$\delta = 1.57 \pm 0.15$
$P = \pm 100\%$	$\delta = 1.57 \pm 0.10$

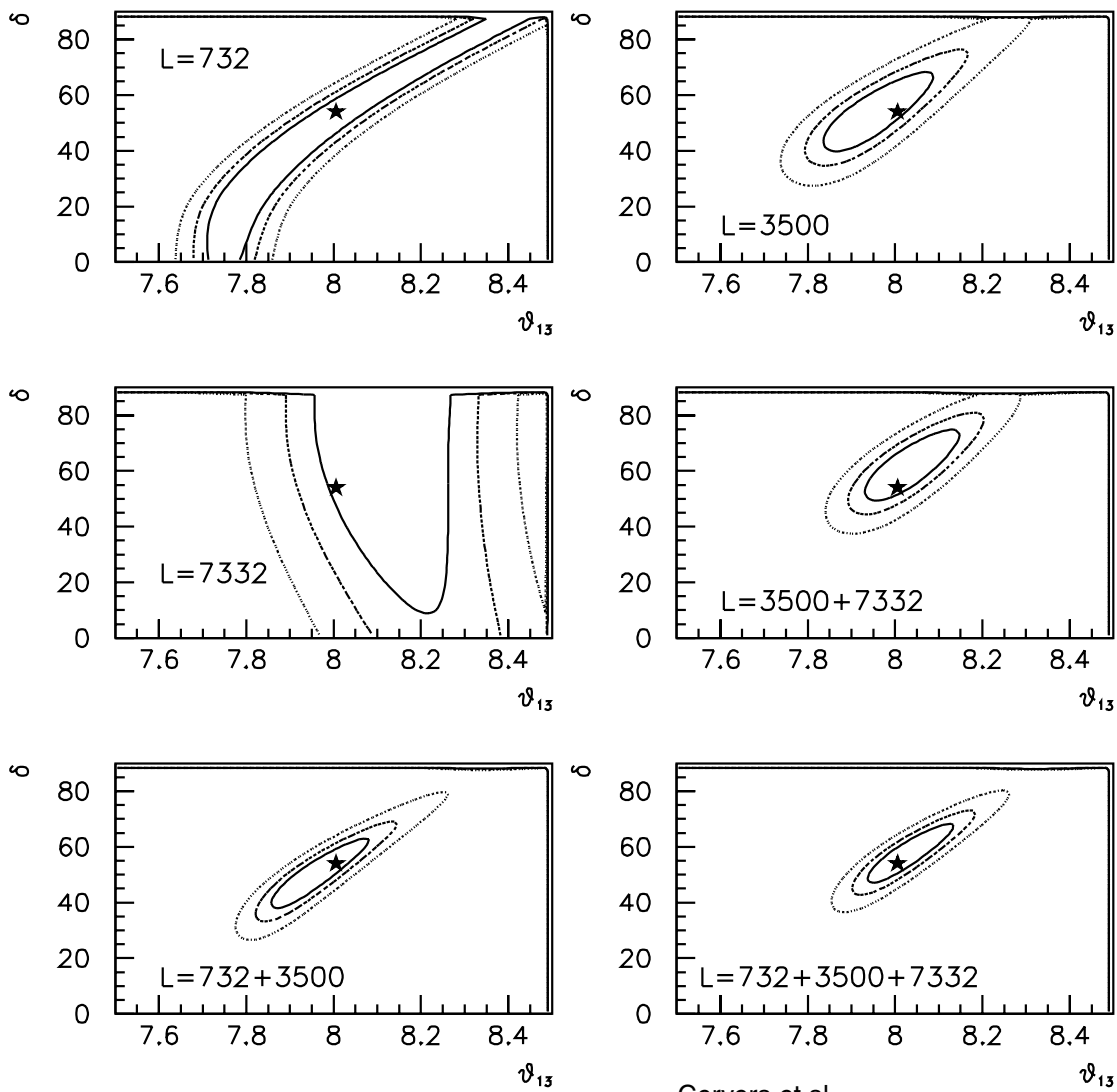
**Blondel NUFACT00 - CP/polarization**

Kinematic cuts can increase sensitivity at high event rates.

Cervera et al.



68, 90 and 99% confidence levels

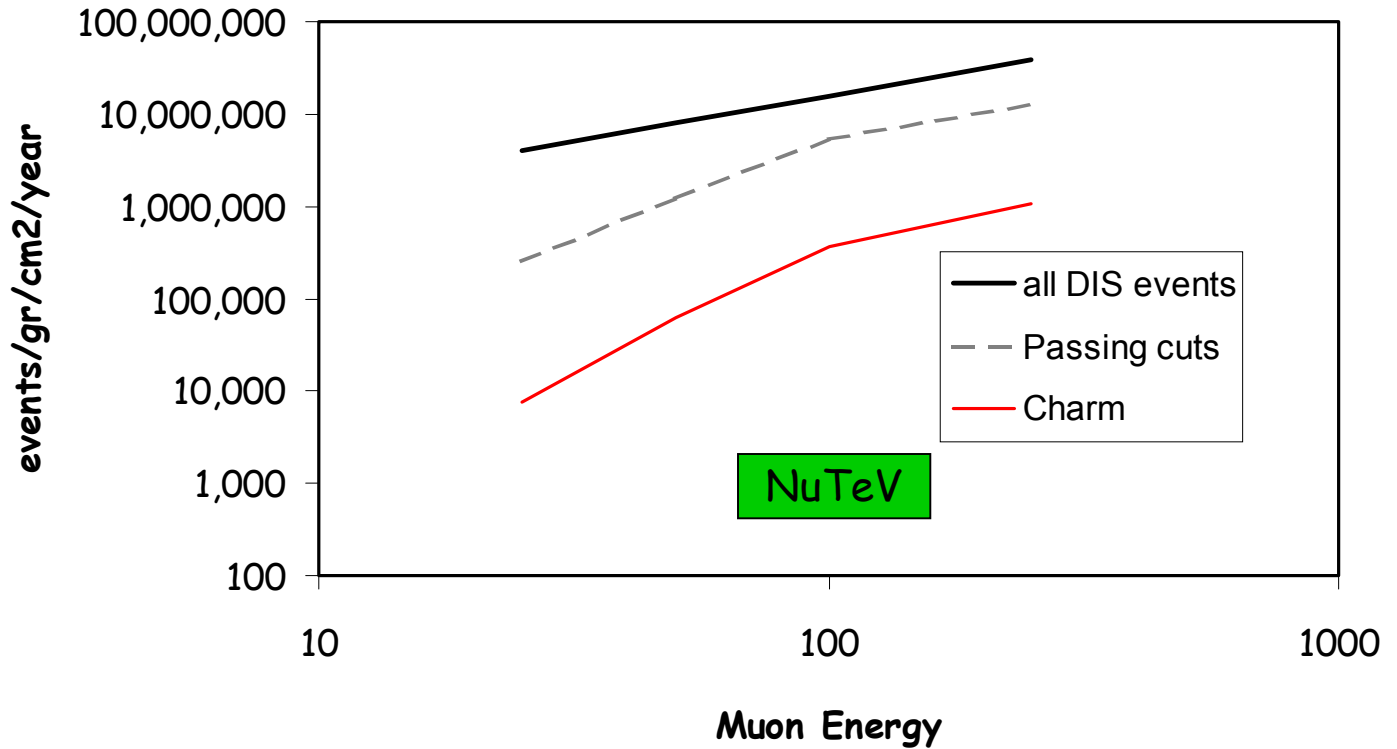


Cervera et al.

# Near Experiments

- Place detectors 50 m from end of straight section
- Get 1000 times current statistics!
  - Hydrogen targets
  - Polarized targets
  - Charm
  - Beauty? (not at 50 GeV)
  - Rare phenomena

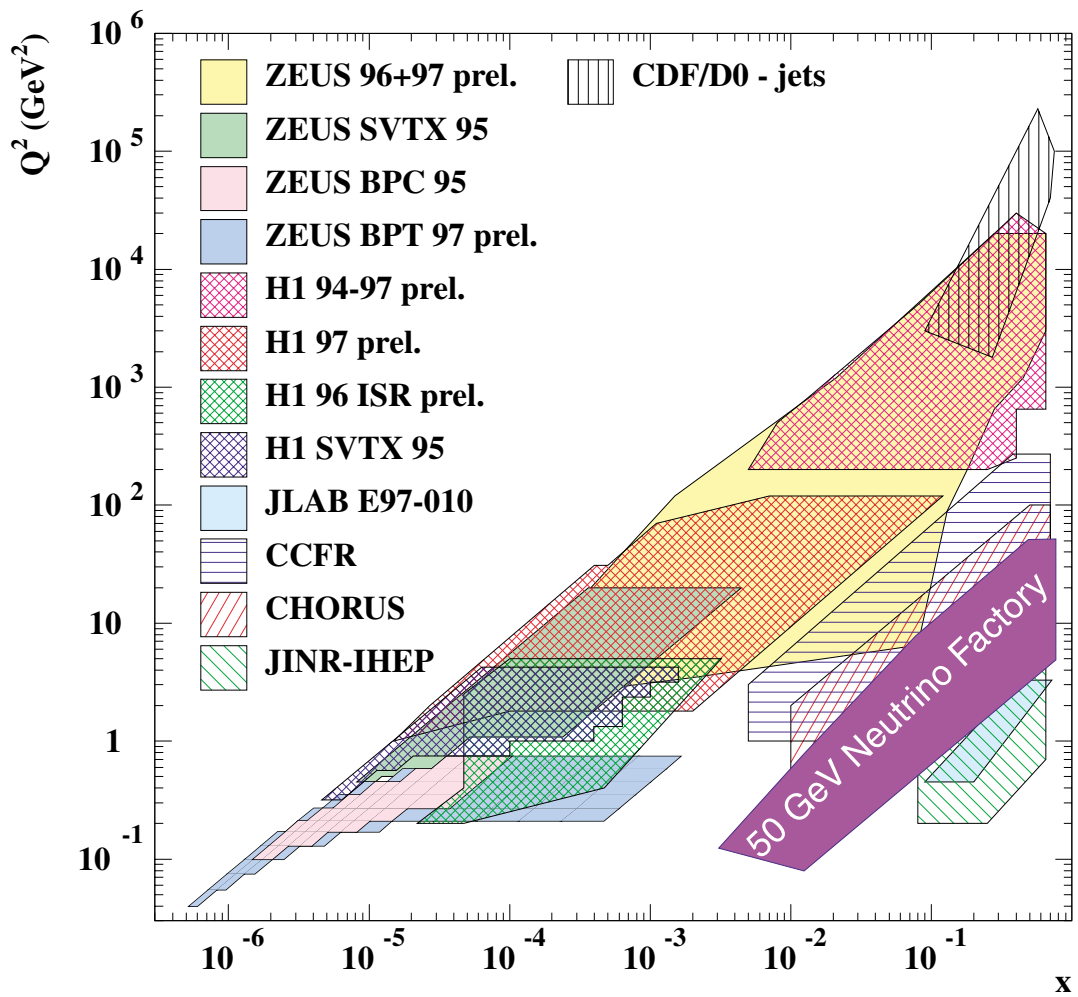
## Charged current event rates at near detectors



At 50 GeV, 7.9M events/gr/cm<sup>2</sup>/year  
But only 22% are within 20 cm radius  
(82% pass loose kinematic cuts)

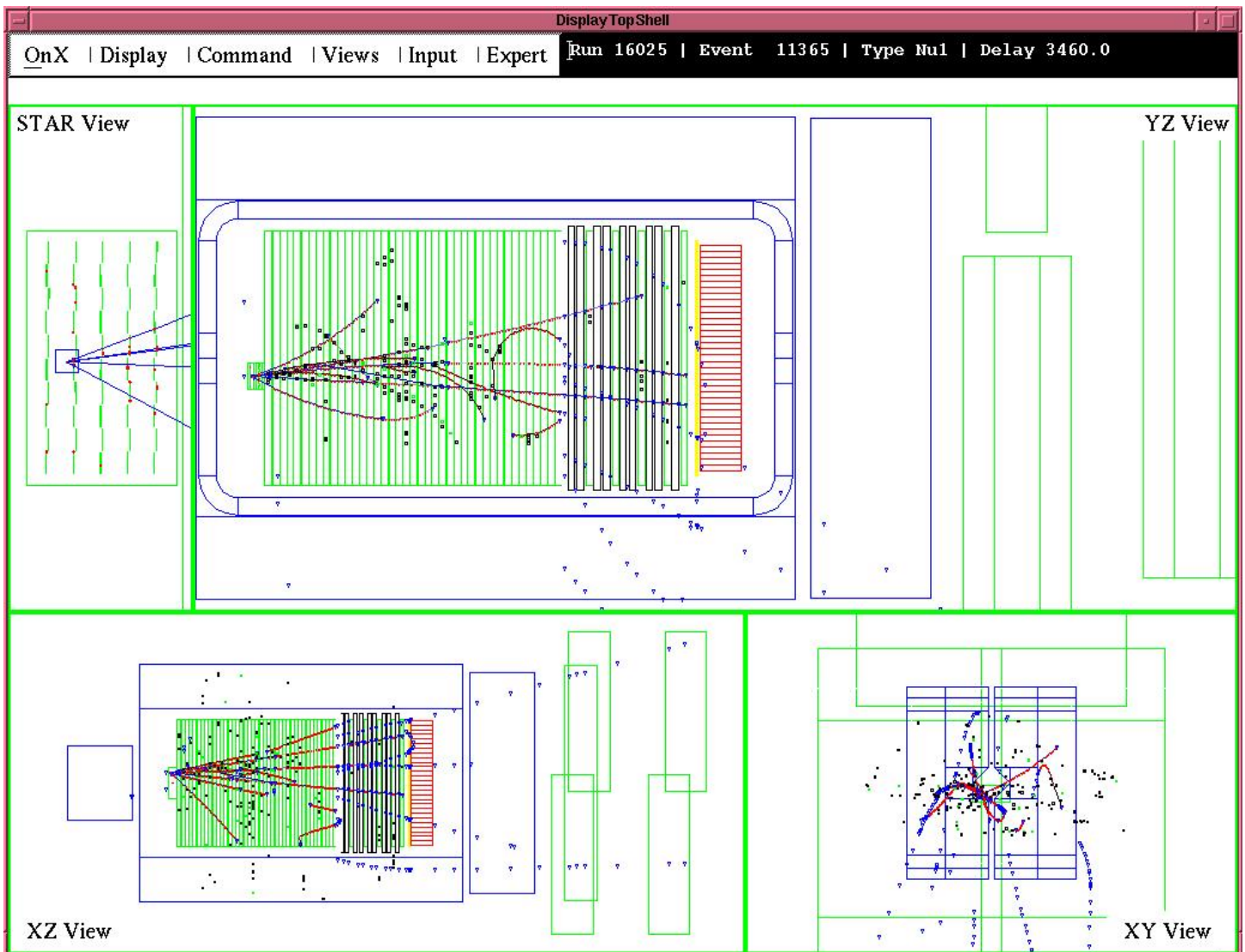
1000 times current experiments!

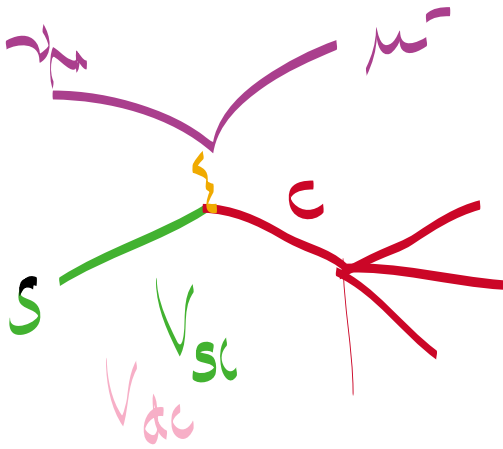
# Deep Inelastic Scattering Experiments



# Detector like NOMAD

10 kg targets in front of tracking/calorimetry

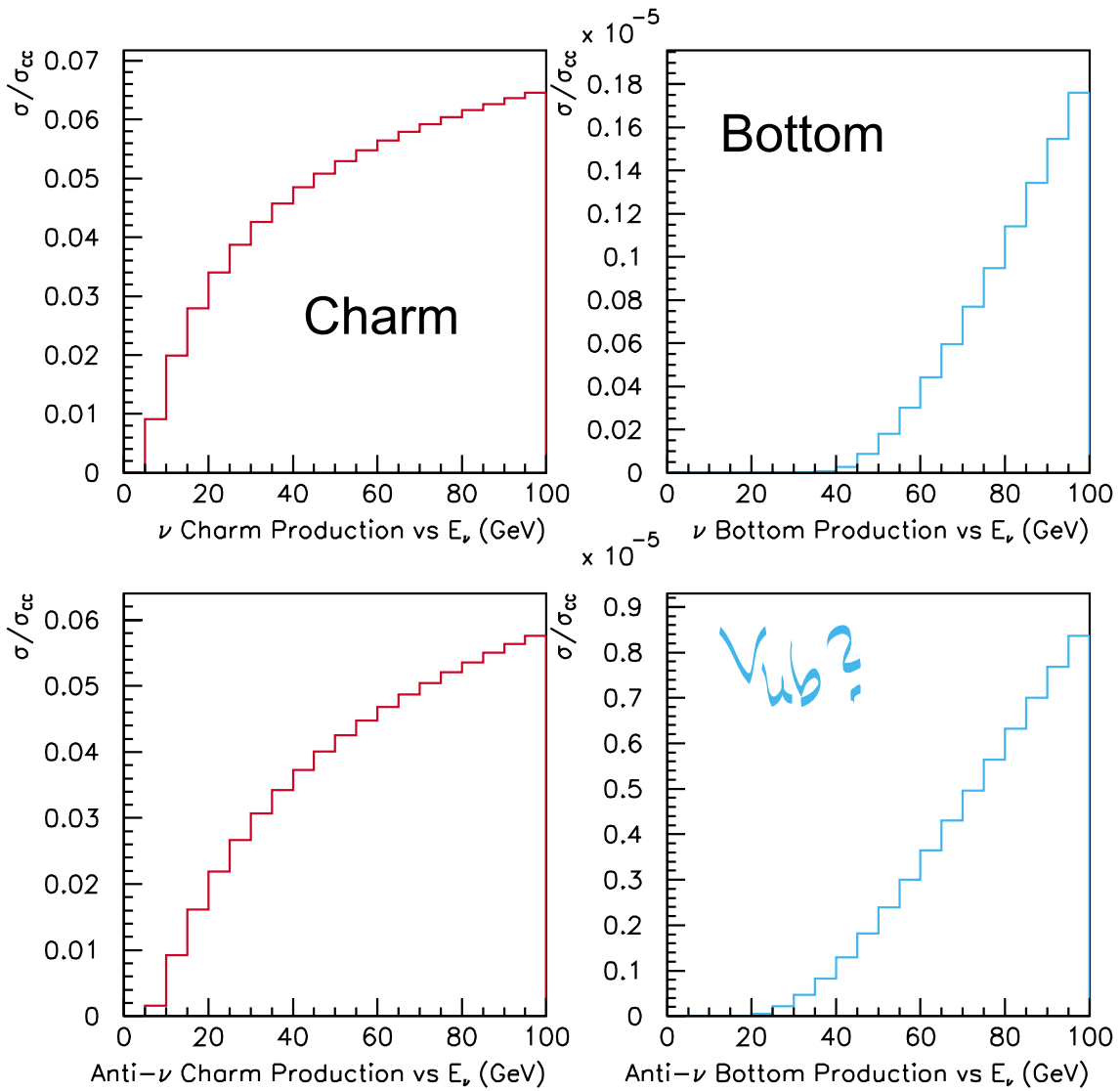




140 Si wafer target  
 17 M CC events  
 -> .5-1M charm

1 ton target  
 120 M charm

Heavy Flavor Production vs  $E_\nu$

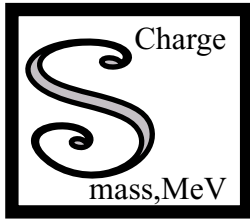




# Conclusions

- Baselines of  $\sim 3000-7000$  are very interesting
- Large detectors are needed (and the cheap way to go)
- Intensities  $> \sim 10^{20}$ /year open allow
  - very accurate measure of  $\Delta m_{23}^2$  and  $\theta_{23}$
  - Measure  $\sin^2 2\theta_{13}$  and sign of  $\Delta m_{23}^2$
- May be sensitive to CP violation if  $\sin^2 2\theta_{13}$ ,  $\sin^2 2\theta_{12}$  and  $\Delta m_{12}^2$  are large (lucky LMA solution)

Near detector physics factor of 1000 better than present or foreseen expts.



# Standard Model of Elementary Particles

		3 Generations of Fermions			Force Carriers	
Q u a r k s		$\frac{2}{3}$ <b>u</b> $\sim 5$	$\frac{2}{3}$ <b>c</b> $\sim 1350$	$\frac{2}{3}$ <b>t</b> 175000	<b>g</b> $0$ $0$ Strong Interactions	
		$-\frac{1}{3}$ <b>d</b> $\sim 9$	$-\frac{1}{3}$ <b>s</b> $\sim 175$	$-\frac{1}{3}$ <b>b</b> $\sim 4500$		$0$ $0$ <b><math>\gamma</math></b> Electro-magnetism
L e p t o n s		$0?$ <b><math>\nu_1</math></b> $0?$	$0?$ <b><math>\nu_2</math></b> $0?$	$0?$ <b><math>\nu_3</math></b> $0?$	$0$ $91187$ <b><math>Z^0</math></b> Weak Interactions	
		<b>e</b> 0.511	<b><math>\mu</math></b> 105.66	<b><math>\tau</math></b> 1777.2		$\pm 1$ <b><math>W^\pm</math></b> 81400

Masses are in MeV

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