

# Triple-Axis Spectroscopy

Mark Lumsden



# References

G.L. Squires, “**Introduction to the Theory of Thermal Neutron Scattering**”

<http://www.amazon.com/Introduction-Theory-Thermal-Neutron-Scattering/dp/048669447X>

S.W. Lovesey, “**Theory of Neutron Scattering from Condensed Matter**”

G. Shirane, S.M. Shapiro, J.M. Tranquada, “**Neutron Scattering with a Triple-Axis Spectrometer: Basic Techniques**”

<http://www.amazon.com/Neutron-Scattering-Triple-Axis-Spectrometer-Techniques/dp/0521025893/>

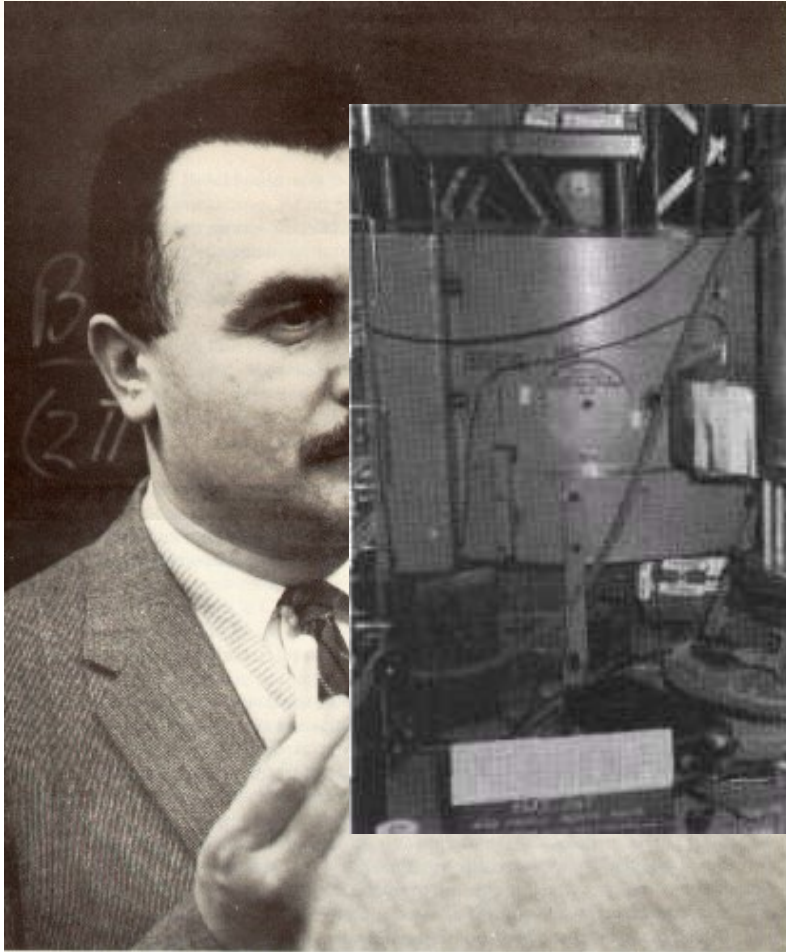


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# History

## 1994 Nobel Prize in Physics



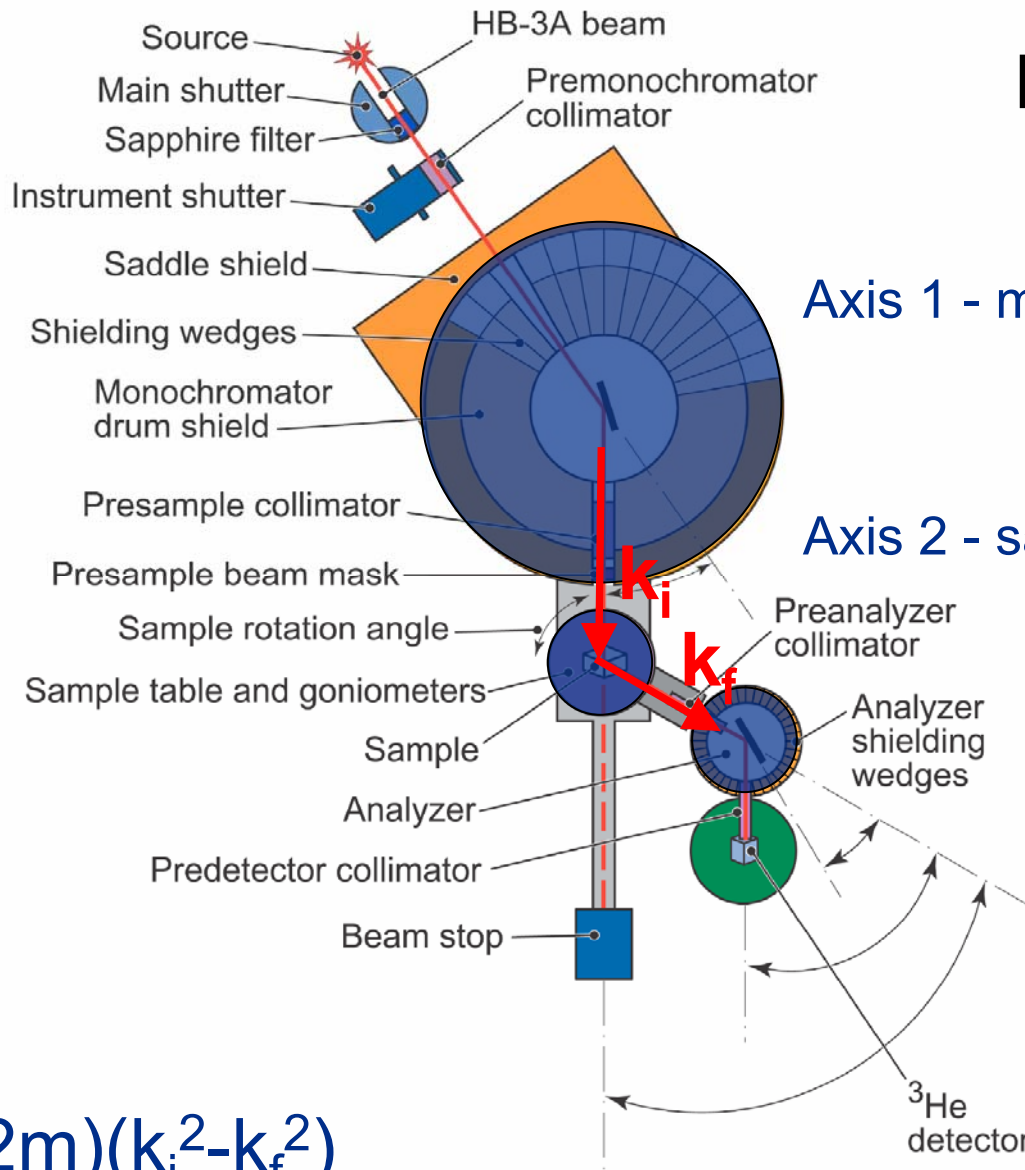
contributions to the  
study of the scattering  
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spectroscopy"

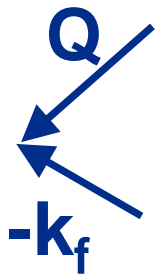
# Bragg's Law:

$$\lambda = 2d \sin\theta$$


Axis 1 - monochromator

Axis 2 - sample

Axis 3 - analyzer



$$Q = k_i - k_f$$

$$\Delta E = (\hbar^2/2m)(k_i^2 - k_f^2)$$

Neutron Sciences



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recip\_space\_2.avi

# TAS Instruments at HFIR: HB1A Ames Laboratory Fixed $E_i$ TAS



Fixed  $E_i=14.6$  meV

Good for elastic and lower energy inelastic measurements ( $< \sim 7$  meV).  
Very clean beam  
(very little  $\lambda/2$  contamination:  
 $\lambda/2 \sim 10^{-4} \lambda$ )

Instrument scientist: Jerel Zarestky

# TAS Instruments at HFIR: HB1 Polarized TAS



Instrument scientist: Andrey Zheludev

Currently, unpolarized with vertically focusing PG002 monochromator.

Polarized capabilities should be ready in late 2008.

Original instrument where Moon, Riste, and Koehler did initial polarized triple-axis measurements  
**Phys. Rev. 181 920 (1969).**

# TAS Instruments at HFIR: HB3 TAS



Instrument scientist: Mark Lumsden

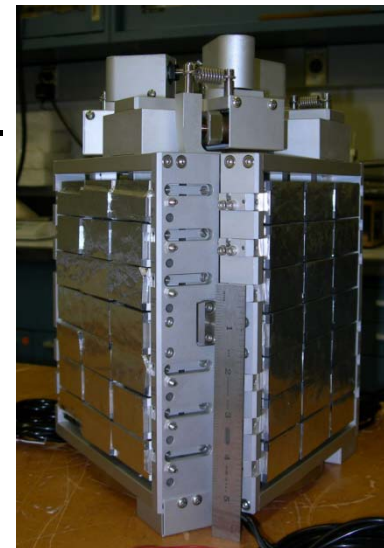
## Choice of 3 monochromators:

PG 002 – best intensity

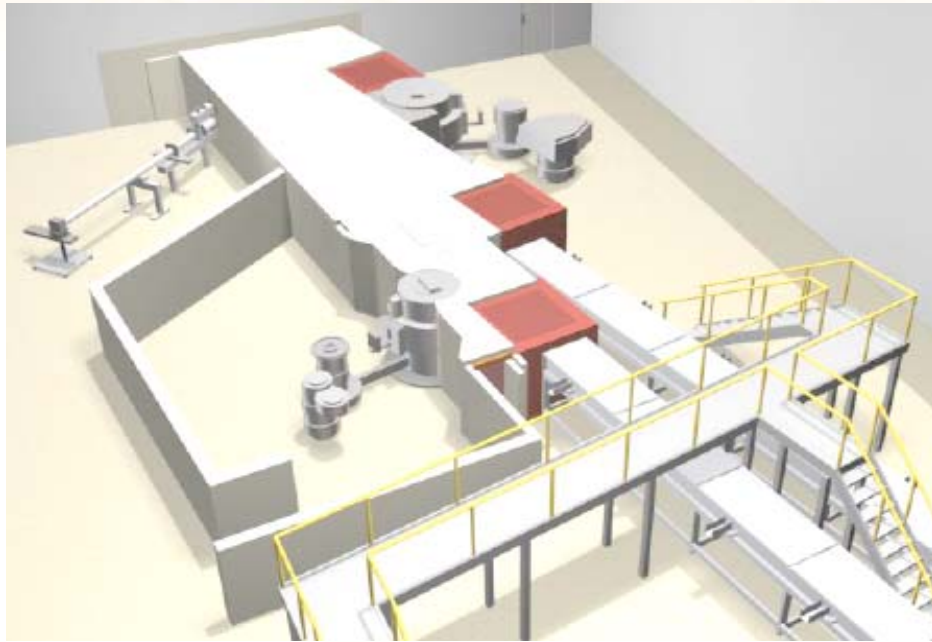
Si 111 – no  $\lambda/2$

Be 002 – good resolution at higher energies

All vertically focused.  
Approximate beam height at sample is about 1"



# TAS Instruments at HFIR: Future – cold TAS instruments



## US-Japan Cold TAS – CG4C:

$E_i$  2-20 meV

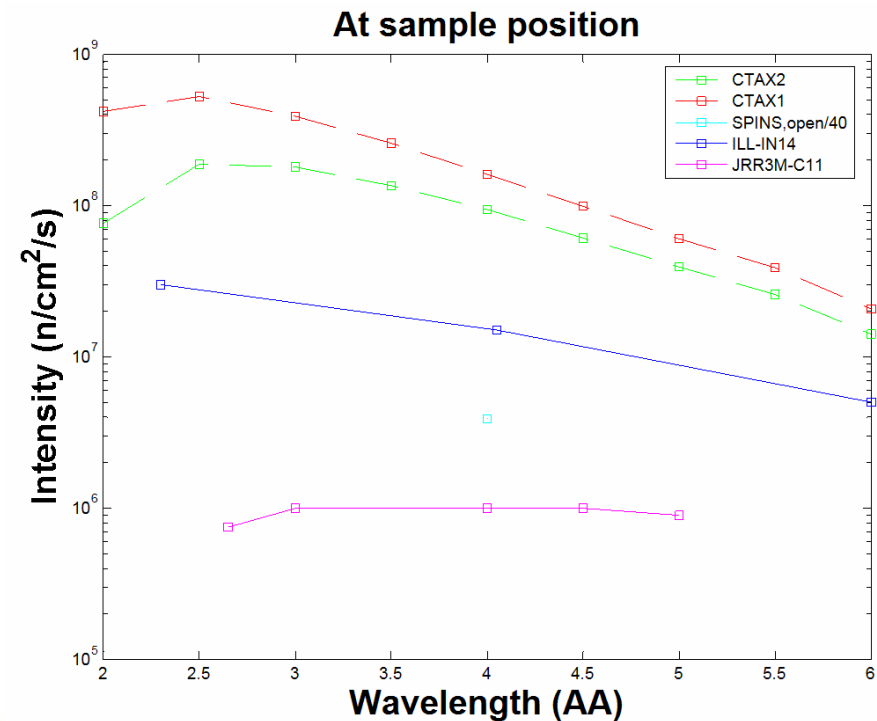
Flux  $\sim 10^8$  n/cm<sup>2</sup>/s

## CG1 TAS (VICTOR):

IDT Formed – guide in place

Highest flux cold TAS in world

Multi-blade analyzer





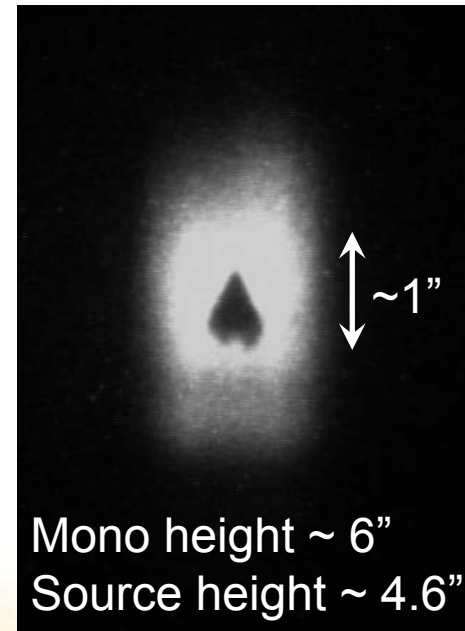
# Experimental Configuration - Monochromators

Monochromator	d-spacing	Comment
PG 002	3.35 Å	Very high reflectivity – best intensity
Si 111	3.135 Å	No $\lambda/2$ but lower intensity (good signal:noise)
Be 002	1.79 Å	Smaller d-spacing – good resolution at higher $\Delta E$
Heusler	3.437 Å	Polarizing monochromator

All vertically focusing:

$$\frac{1}{L_{Source-Mono}} + \frac{1}{L_{Mono-Sample}} = \frac{2 \sin(\theta_M)}{R}$$

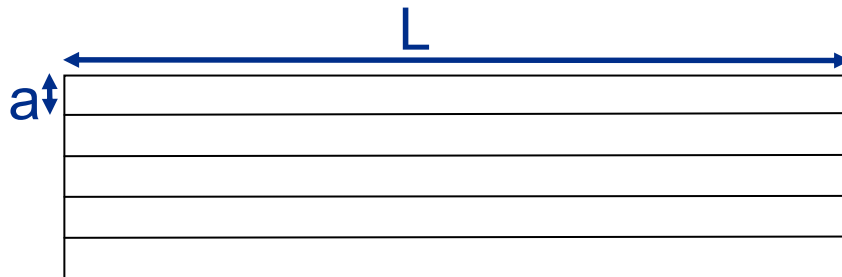
As lengths are fixed, need to adjust R for each  $\theta_M$  to maintain focus



# Experimental Configuration - collimators

## Collimations:

Source-Monochromator  
Monochromator-Sample  
Sample-Analyzer  
Analyzer-Detector



Collimation  $\alpha = a/L$

Helps define resolution – example (Rescal):

48'-40'-40'-120'  $E_f = 14.7\text{meV}$   $\Delta E = 0.92\text{meV}$   $I = 1$

48'-20'-20'-120'  $E_f = 14.7\text{meV}$   $\Delta E = 0.75\text{meV}$   $I \sim 0.44$

<http://www.ill.fr/Computing/resources/software/matlab/>

# Experimental Configuration - filters

## Role of filters

Reduce fast neutron background – significant source of background on all TAS instruments

Bragg's Law:  $\lambda = 2d \sin\theta$

If satisfy scattering condition for  $\lambda$  **you will also for  $\lambda/2$ ,  $\lambda/3$ , ... assuming reflections with  $d/2$ ,  $d/3$ , ... exist.**

Want a filter to transmit  $\lambda$  with high efficiency but reject  $\lambda/2$  and  $\lambda/3$  (higher orders aren't typically relevant due to reactor spectrum)



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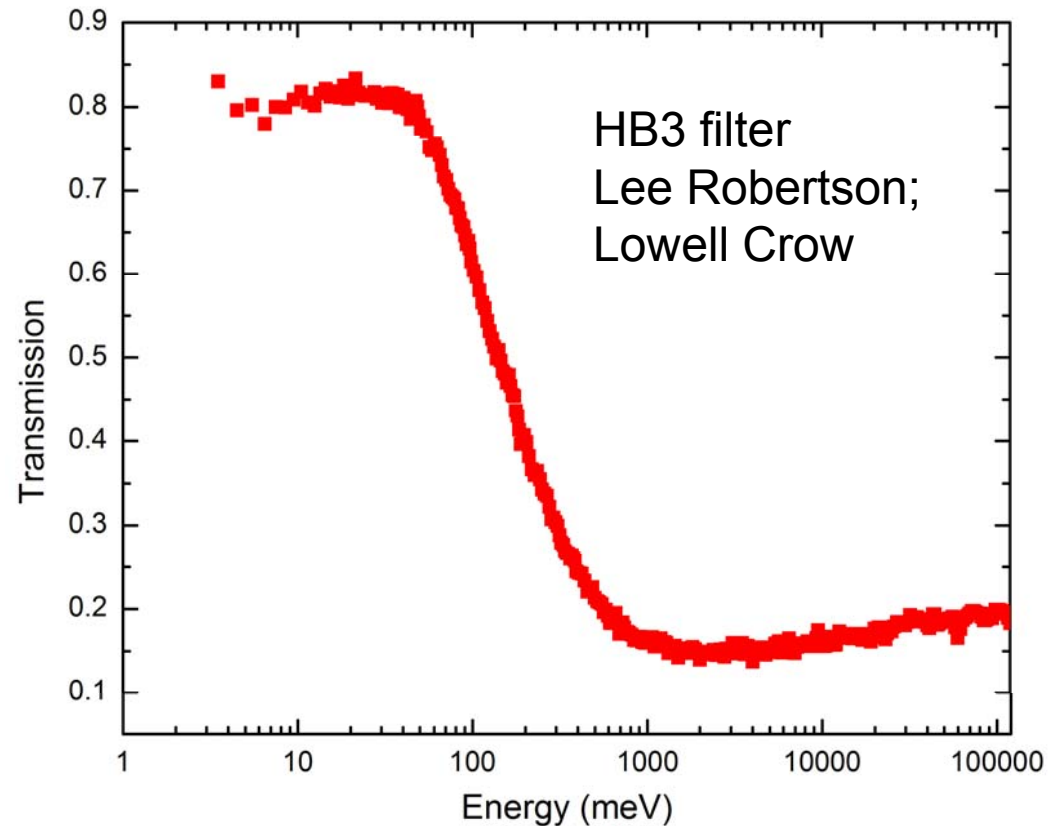
# Experimental Configuration - filters

## Sapphire fast neutron filter

Present on all instruments

Inelastic phonon and multiphonon processes dominate at high energies reducing transmission

Greatly reduces fast neutron background of instruments



# Experimental Configuration - filters

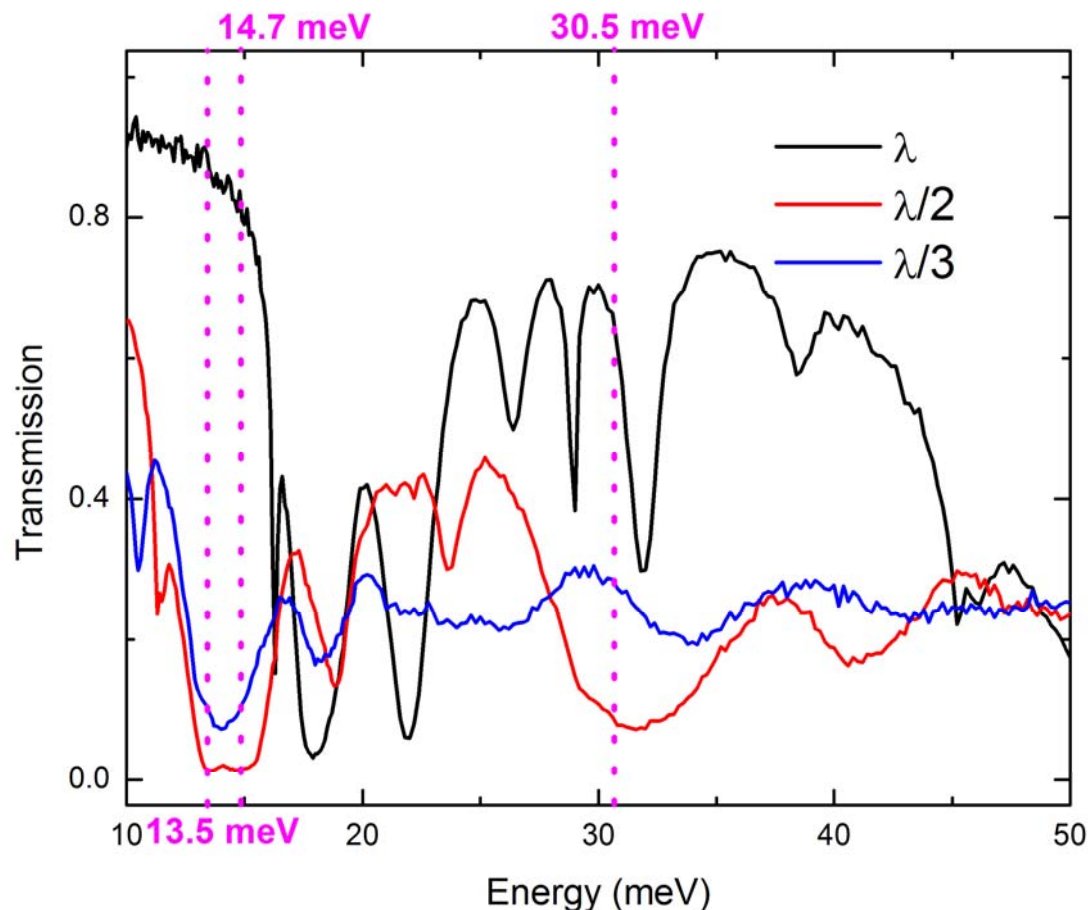
## PG Filter:

PG with c-axis along beam direction.

Bragg scattering occurs for  $k$  values where

$$2k \sin(90 - \phi_{hkl}) = \mathbf{G}_{hkl}$$

Where  $\phi_{hkl}$  is angle between reciprocal lattice vector  $\mathbf{G}_{hkl}$  and c-axis.



# Experimental Configuration - filters

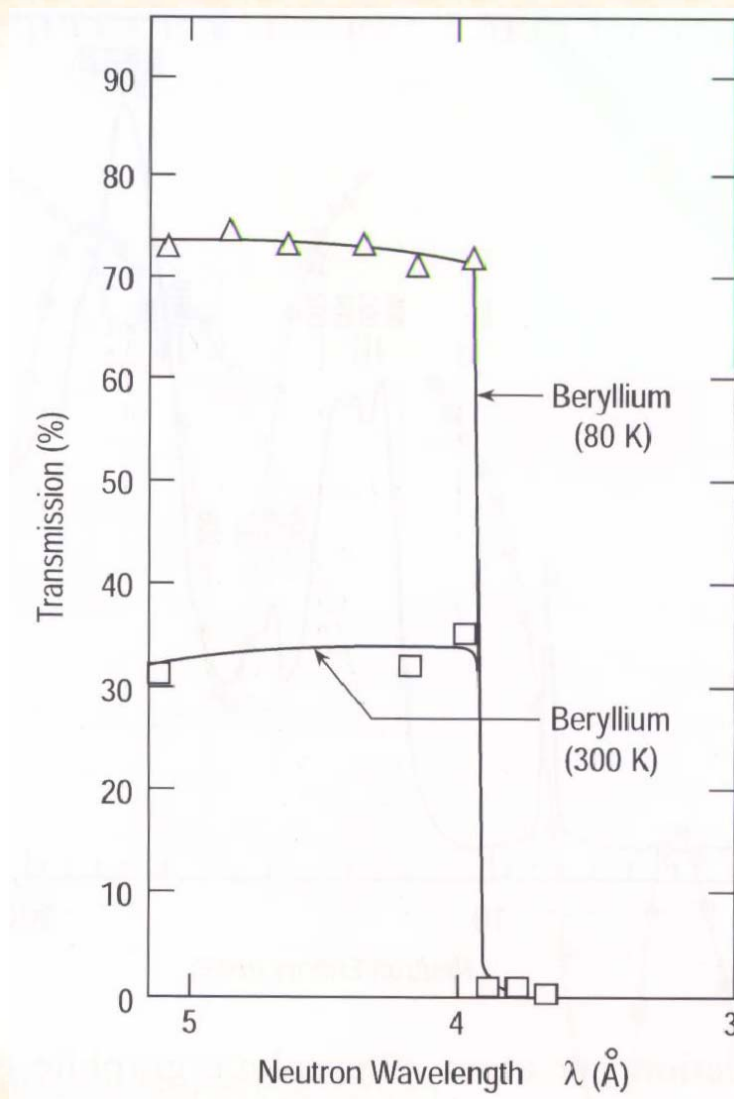
## Be/BeO filter:

Bragg scattering filters

Max wavelength for which Bragg scattering can occur is:

$$\lambda_{\text{cutoff}} = 2d_{\text{max}}$$

$\lambda/2d < 1$ : for  $\lambda > \lambda_{\text{cutoff}}$ , can have no Bragg scattering and beam gets transmitted.



# TAS Experiment – before arriving

## Sample size:

Powder – typically 10-50g

Single crystal: > 300 mg  
(preferred > 1g)

Often need to coalign several  
crystals to attain enough mass.



## TAS Experiment – before arriving

Characterize sample before arriving – at least, examine with x-rays. NOTE: x-rays examine near-surface while neutrons examine bulk.

Know what scattering plane you want to explore – TAS measures in a plane

Know structure and come with a list of Bragg reflection intensities



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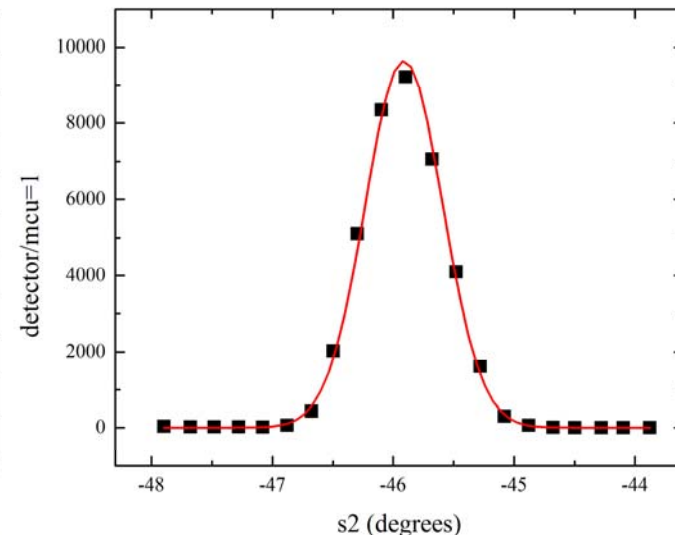
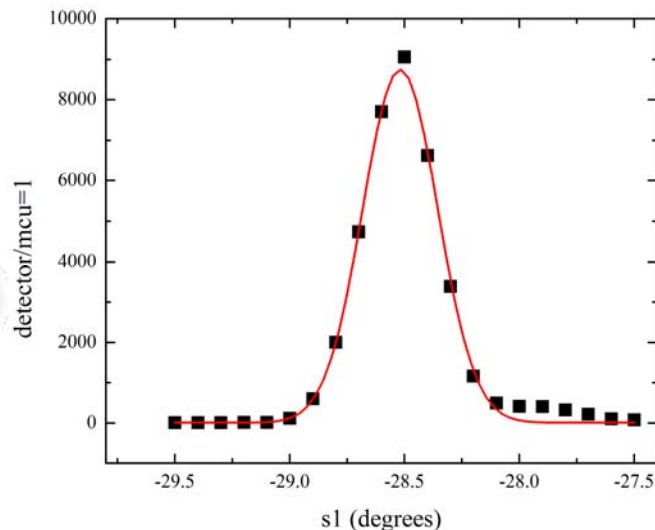
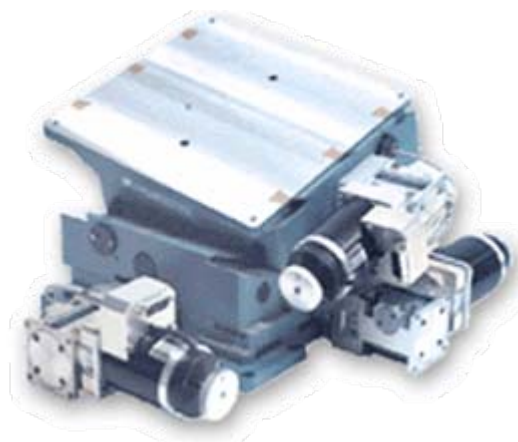


# TAS Experiment - align sample

Software at ORNL uses UB matrix to define orientation.

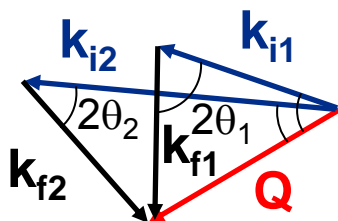
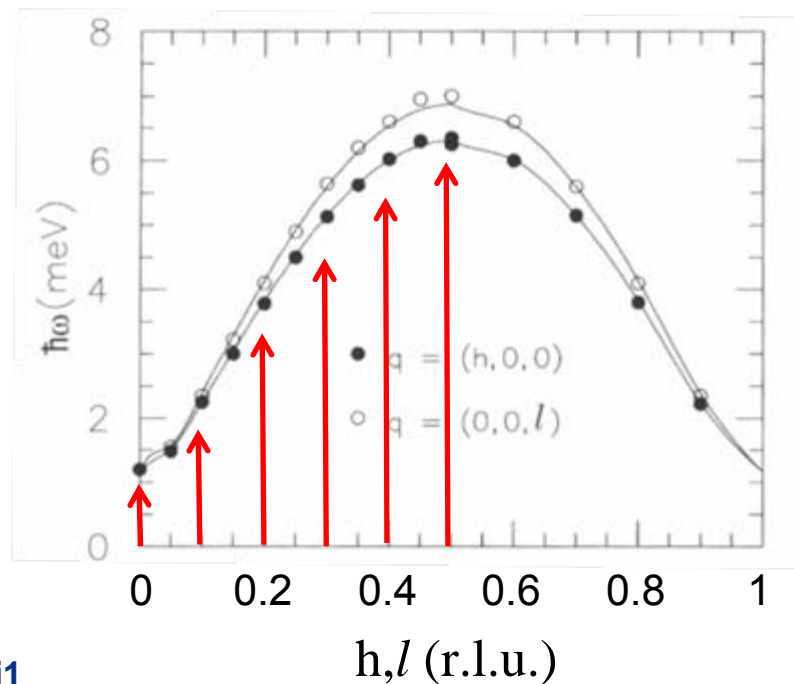
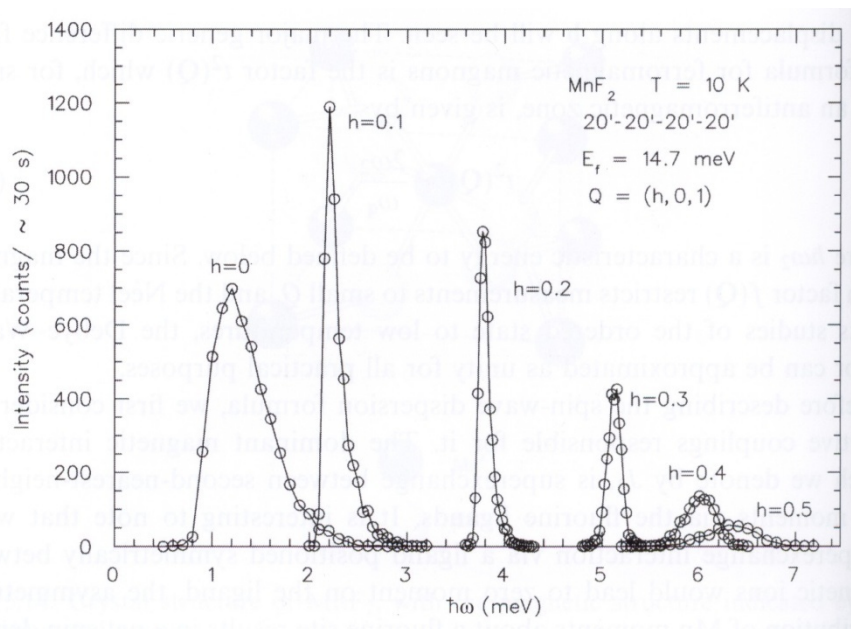
M.D. Lumsden, J.L. Robertson, and M. Yethiraj, *J. Appl. Cryst.* 38 (2005) 405.

Perform transverse and longitudinal scans through 2 or more reflections. Also scan arcs at each reflection. Input the lattice constants. Tell the computer what the reflections are (for instance, the current spectrometer angles give me the (200) Bragg peak).



# TAS Experiment - scans

## Constant-Q scan - concept developed by Brockhouse



# TAS Experiment – resolution

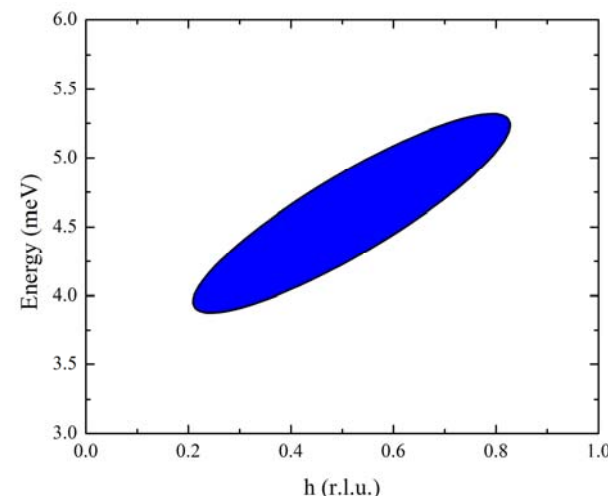
The resolution of the TAS is dependent on:

1. Monochromator/analyzer d-spacing
2. Monochromator/analyzer mosaic spreads
3. Sample mosaic spread
4. Collimations (S-M; M-S; S-A; A-D)
5. Distances (not in simplest approximation)

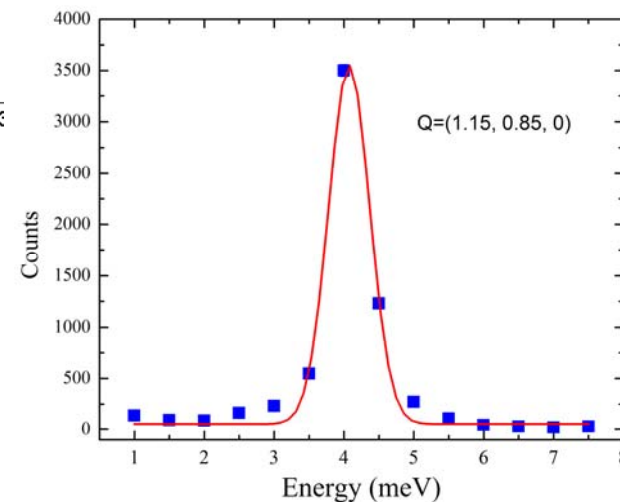
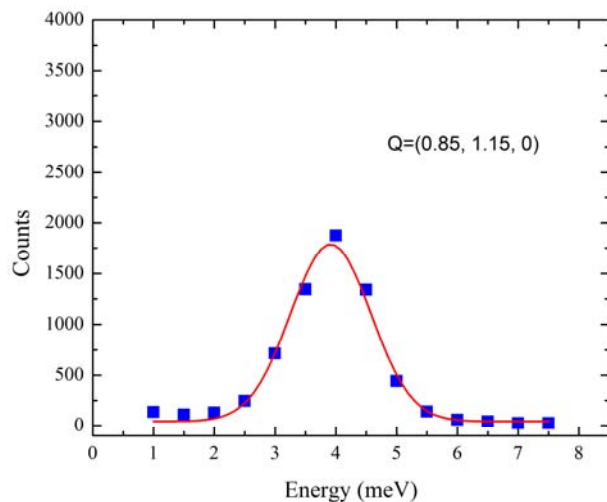
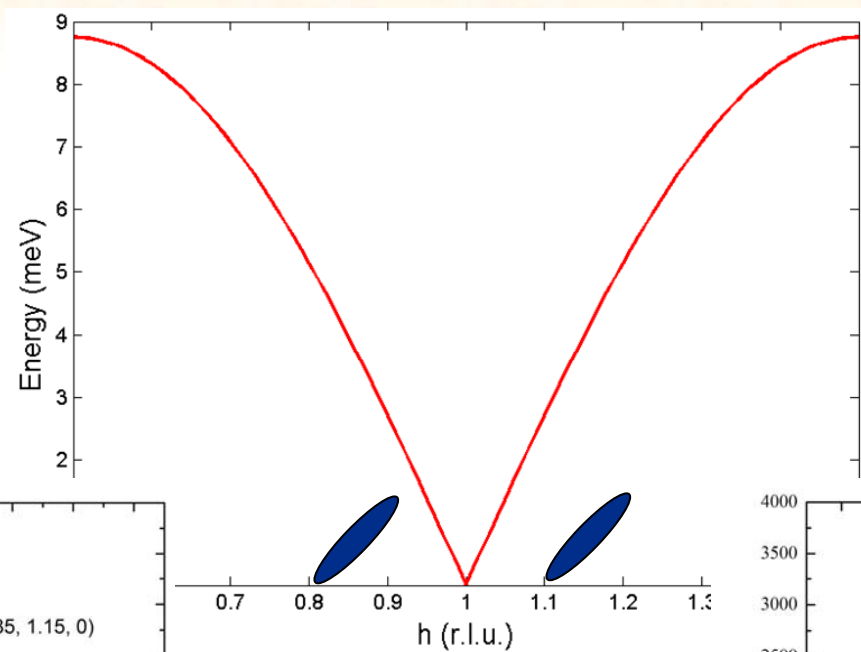
Shape: cigar-like ellipsoid

What we measure:

$$I(\vec{Q}_0, \omega_0) \propto \iint R(\vec{Q} - \vec{Q}_0, \omega - \omega_0) S(\vec{Q}, \omega) d\vec{Q} d\omega$$



# TAS Experiment - resolution - focusing



# TAS Experiment – resolution

Proper way to analyze data is to convolute expected  $S(\mathbf{Q},\omega)$  with instrumental resolution.

Reslib - A. Zheludev (MATLAB)

<http://neutron.ornl.gov/~zhelud/reslib/index.html>

## References:

M. J. Cooper and R. Nathans, *Acta Cryst.* (1967) **23**, 357-367.

N. J. Chesser and J. D. Axe, *Acta Cryst.* (1973) **A29**, 160-169.

M. Popovici, *Acta Cryst.* (1975) **A31**, 507-513.

