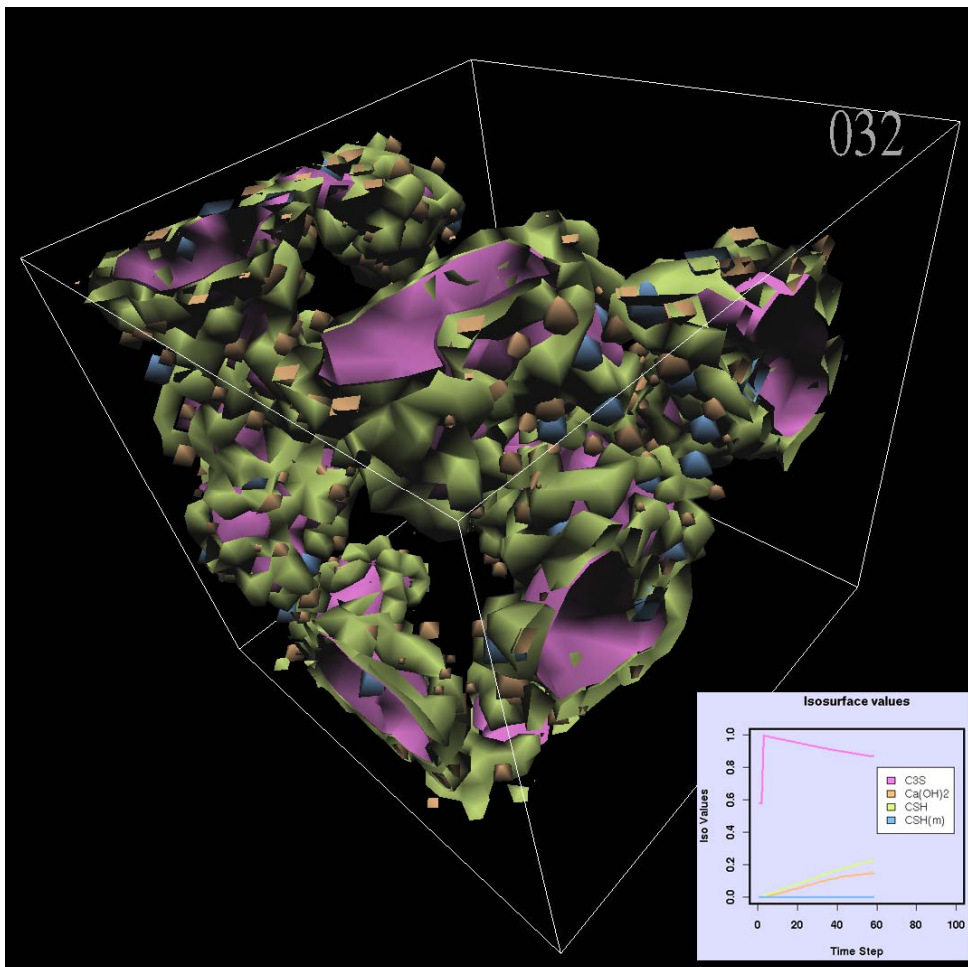


# Mathematical and Computational Sciences Division

Summary of Activities for Fiscal Year 2007



Information Technology Laboratory  
National Institute of Standards and Technology  
U.S. Department of Commerce

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## Abstract

This report summarizes the technical work of the Mathematical and Computational Sciences Division (MCSD) of NIST's Information Technology Laboratory. Part I (Overview) provides a high-level overview of the Division's activities, including highlights of technical accomplishments during the previous year. Part II (Features) provides further details on eight particular projects of particular note this year. This is followed in Part III (Project Summaries) by brief summaries of all technical projects active during the past year. Part IV (Activity Data) provides listings of publications, technical talks, and other professional activities in which Division staff members have participated. The reporting period covered by this document is October 2006 through December 2007.

*For further information, contact Ronald F. Boisvert, Mail Stop 8910, NIST, Gaithersburg, MD 20899-8910, phone 301-975-3812, email [boisvert@nist.gov](mailto:boisvert@nist.gov), or see the Division's web site at <http://math.nist.gov/mcsd/>.*

**Cover photo.** Visualization and analysis of the microstructure a computational model of cement hydration showing four distinct phases. This is the result of research performed by William George, Steve Satterfield, and Edith Enjolras of MCSD in collaboration with Jeffrey Bullard of the NIST Building and Fire Research Laboratory.

**Acknowledgement.** We are grateful to Robin Bickel for collecting the information and organizing the first draft of this report.

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**Part I**

# **Overview**



## **Introduction**

Applied mathematics and computation are critical to the advancement of science and engineering, which is, in turn, the principal fuel for industrial innovation. Indeed, a 2006 National Science Foundation report<sup>1</sup> states

*“Simulation-based engineering science ... is a discipline indispensable to the nation’s continued leadership in science and engineering. It is central to advances in biomedicine, nanomanufacturing, homeland security, microelectronics, energy and environmental sciences, advanced materials, and product development. There is ample evidence that developments in these new disciplines could significantly impact virtually every aspect of human experience.”*

A 2005 report<sup>2</sup> of the President’s Information Technology Advisory Committee (PITAC) concludes further that

*“Computational science is now indispensable to the solution of complex problems in every sector, from traditional science and engineering domains to such key areas as national security, public health, and economic innovation.”*

The connection to economic innovation has been emphasized by the Council on Competitiveness<sup>3</sup> which has stated that “high performance computing is not only a key tool to increasing competitiveness, it is also a tool that is essential to business survival.”

The disciplines of applied mathematics, statistics, and computer science are the foundation for computational science and engineering. Research in mathematical and statistical analysis, numerical algorithms, software tools, high performance computing, and visualization provide the basis for mathematical modeling, computational simulation, and data analysis in all fields. In this regard, close cooperation between mathematicians, computer scientists, and application scientists are critical. As the PITAC report states, “the 21st century’s most important problems ... are predominantly multidisciplinary, multi-agency, multisector, and collaborative.” Indeed, much of the most innovative research is now occurring at the intersection of mathematics, computer science, and applications, e.g., in areas like nanotechnology, bioinformatics, and quantum information.

**NIST.** The National Institute of Standards and Technology (NIST) plays a central role in the infrastructure for science and technology. Its mission is to promote U.S. innovation and industrial competitiveness by advancing measurement science, standards, and technology in ways that enhance economic security and improve our quality of life. In particular, the NIST Measurement and Standards Laboratories conduct research that advances the technology infrastructure needed by U.S. industry to continually improve products and services. Unveiled in 2006, the American Competitiveness Initiative underlines the importance of NIST in these efforts. Its report<sup>4</sup> identifies the following examples of critical roles for NIST in the coming years:

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<sup>1</sup> *Simulation-based Engineering Science: Revolutionizing Engineering Science Through Simulation*, Report of the National Science Foundation Blue-Ribbon Panel on Simulation-based Engineering Science, February 2006.

<sup>2</sup> *Computational Science: Ensuring America’s Competitiveness*, President’s Information Technology Advisory Committee, June 2005.

<sup>3</sup> *Study of US Industrial HPC Users*, Council on Competitiveness, 2004.

<sup>4</sup> *American Competitiveness Initiative: Leading the World in Innovation*, US Office of Science and Technology Policy, February 2006.

- *World-class capability and capacity in nanofabrication and nanomanufacturing that will help transform current laboratory science into a broad range of new industrial applications for virtually every sector of commerce, including telecommunications, computing, electronics, health care, and national security (NSF, DoE, NIST)*
- *Chemical, biological, optical, and electronic materials breakthroughs critical to cutting edge research in nanotechnology, biotechnology, alternative energy, and the hydrogen economy through essential infrastructure such as the National Synchrotron Light Source II and the NIST Center for Neutron Research (DoE, NIST)*
- *Overcoming technological barriers to the practical use of quantum information processing to revolutionize fields of secure communications, as well as quantum mechanics simulations used in physics, chemistry, biology, and materials science (DoE, NIST, NSF)*
- *Overcoming technological barriers to efficient and economic use of hydrogen, nuclear, and solar energy through new basic research approaches in materials science (DoE, NSF, NIST)*
- *Addressing gaps and needs in cyber security and information assurance to protect our IT-dependent economy from both deliberate and unintentional disruption, and to lead the world in intellectual property protection and control (NSF, NIST)*
- *Development of manufacturing standards for the supply chain to advance and accelerate the development and integration of more efficient production practices (NIST)*
- *Enhanced response to international standards challenges, which impact U.S. competitiveness and limit export opportunities for American businesses by acting as technical barriers to trade (NIST)*

## ITL Programs

### Begun FY 2007

#### Complex Systems

Complex Systems are composed of large interrelated, interacting entities which taken together, exhibit a macroscopic behavior which is not predictable by examination of the individual entities. The Complex Systems Program seeks to understand the fundamental science of these systems and develop rigorous descriptions (analytic, statistical, or semantic) that enable prediction and control of their behavior. Initially focused on the Internet and Grid Computing, this Program will facilitate predictability and reliability in these areas and other complex systems such as biotechnology, nanotechnology, semiconductors, and complex engineering.

#### Identity Management Systems

Identity management systems are responsible for the creation, use, and termination of electronic identities which are routinely used to access logical and physical resources, and have become a ubiquitous part of our national infrastructure. The Identity Management Systems Program is pursuing the development of common models and metrics for identity management, critical standards, and interoperability of electronic identities. These efforts will improve the quality, usability, and consistency of identity management systems while protecting privacy.

#### Information Discovery, Use, and Sharing

Society is awash in data - our ability to amass data has outpaced our ability to use it. Extracting knowledge, information, and relationships from this data is one of the greatest challenges faced by the scientists in the twenty-first century. The data can be as diverse as biological research data, medical images, automated newswire, speech, or video. The Information Discovery, Use, and Sharing Program fosters innovation throughout the information life cycle by developing the measurement infrastructure to enhance knowledge discovery, information exchange, and information usability. The Program enables novel computational approaches to data collection and analysis to be combined with improved interoperability techniques to effectively extract needed information from the wealth of available data.

### Planned Startups in FY 2008

#### Cybersecurity

Cybersecurity is focused on ensuring three security objectives of information technology systems: confidentiality, integrity, and availability. The Cybersecurity Program creates a balance between our statutory responsibilities and a basic and applied research program. The Program addresses long-term scientific issues in some of the building blocks of IT security - cryptography, security testing and evaluation, security metrics, and security properties - providing a more scientific foundation for cybersecurity, while maintaining a focus on near-term issues.

(continued)

**Enabling Scientific Discovery**

Modern scientific research has become more and more dependent on mathematical, statistical, and computational tools for enabling discovery. The Enabling Scientific Discovery Program promotes the use of these tools to dramatically advance our ability to predict the behavior of a broad range of complex scientific and engineering systems and enhance our ability to explore fundamental scientific processes. This Program focuses on interdisciplinary scientific projects that involve novel computational statistics and the development of simulation methods and software. These efforts will have a foundational impact on scientific discovery throughout U.S. industry, government, and academia.

**Pervasive Information Technologies**

Pervasive information technology is the trend towards increasingly ubiquitous connected computing sensors, devices, and networks that monitor and respond transparently to human needs. The Pervasive Information Technologies Program facilitates the creation of standards for sensor communication, networking interoperability, and sensor information security. The Program enables the use of pervasive information technologies to enhance personal and professional productivity and quality of life.

**Trustworthy Networking**

The Trustworthy Networking Program's research encompasses the security, reliability, scalability, robustness, adaptability, and performance of networking technologies. The Program includes long-term fundamental research that is vetted against existing networking protocols. These efforts provide commercially viable techniques to test, measure, and improve the trustworthiness of networking technologies at the earliest stages of development.

**Trustworthy Software**

Trustworthy software is software that performs as intended for a specific purpose, when needed, with operational resiliency and without unwanted side effects, behaviors, or exploitable vulnerabilities. The Trustworthy Software Program will improve the ability to model, produce, measure, and assess trustworthiness in software through new and innovative technologies, models, measurement methods, and software tools. The resulting technologies, models, methods, and tools will reduce the cost and time of building in or assessing software trustworthiness in applications and systems.

**Virtual Measurement Systems**

A virtual measurement is a quantitative result and its uncertainty, obtained primarily by a nontrivial computer simulation or computer-assisted measurements, for example, computational models of physical systems. The Virtual Measurement Systems Program introduces metrology constructs, standard references, uncertainty characterization, and traceability into scientific computation and computer-assisted measurements. Uncertainty characterization and traceability in modeling will result in predictive computing with quantified reliability.

*(This text is taken from the October 2007 ITL brochure edited by Elizabeth Lennon.)*

- *Accelerated work on advanced standards for new technologies (NIST)*
- *Advances in materials science and engineering to develop technologies and standards for improving structural performance during hazardous events such as earthquakes and hurricanes (NIST, NSF)*

**Information Technology at NIST.** As one of the major operating units at NIST, the Information Technology Laboratory (ITL) promotes US innovation and industrial competitiveness by advancing measurement science, standards, and technology through research and development in IT, mathematics, and statistics. The importance of applied mathematics and computational science to ITL's work is clear from the four core competencies that it has identified:

1. IT measurement and testing,
2. Mathematical and statistical analysis for measurement science,
3. Modeling and simulation for measurement science, and
4. IT standards development and deployment.

To respond to the needs of its customers in industry, academia, and government, ITL has developed a set of cross-cutting and interdisciplinary programs. See the sidebar for a brief description of each.

The other laboratories and research centers within NIST are also important customers of ITL. Indeed, NIST's measurement science research program has been transformed by the advent of computational science and engineering. Nearly every NIST project, both theoretical and experimental, typically now has critical computational components. An increasing number of NIST "products" are techniques, tools, and reference data to enable modeling, simulation, and data analysis in particular application domains. As a result, the expertise of applied mathematicians and computer scientists are in high demand within NIST.

**Mathematics and Computational Science at NIST.** The Mathematical and Computational Sciences Division (MCSD) is one of six technical Divisions within ITL. MCSD provides leadership within NIST in the solution to challenging mathematical and computational problems. In particular, we seek to ensure that the best mathematical and computational methods are applied to the most critical problems arising from the NIST measurement science program. In addition, we also engage in highly leveraged research and development efforts to improve the environment for computational science and engineering at large.

To accomplish these goals, MCSD staff members engage in the following types of activities: (a) peer-to-peer collaboration with NIST scientists and engineers in a wide variety of critical applications, (b) targeted outreach efforts with selected external communities to advance the state-of-the-art in their subfield, (c) development and dissemination of unique mathematical and computational tools, and (d) research in targeted areas of applied mathematics and computer science of high relevance to future NIST measurement programs.

In Part III of this document we provide descriptions of most ongoing technical projects of the Division. These are organized under the following broad topic areas:

#### Mathematical Research

- a. Mathematics of Metrology
- b. Quantum Information
- c. Fundamental Mathematical Software Development and Testing
- d. Mathematical Knowledge Management
- e. High Performance Computing
- f. High Performance Visualization

#### Mathematical Applications

- g. Mechanical Systems and Processes
- h. Electromagnetic Systems
- i. Chemistry and Biology
- j. Information Technology

We expect that expertise in these areas will have considerable bearing on many of the nascent ITL Programs. In Part III (Project Summaries) we identify specific projects which are part of the three programs started in FY 2007: Complex Systems; Information Discovery, Use and Sharing; and Identity Management. Startup of projects associated with the ITL programs forming in FY 2008 is currently in process.

## **Highlights**

In this section we identify some of the major accomplishments of the Division over the past year. We also provide news related to MCSD staff.

## **Technical Accomplishments**

MCSD has made significant technical progress in a wide variety of areas during the past year. Here we highlight a few examples. Further details are provided in Part II (Features) and Part III (Project Summaries) of this document.

This year MCSD undertook a significant new initiative with the title *Mathematical Foundations of Measurement Science for Information Systems*. This was enabled by \$1.3M in new funding from the 2007 NIST Cyber Security Initiative, part of the American Competitiveness

Initiative. Conceived as a long-term basic research program in mathematics, the goal of this effort is the understanding, and ultimately the measurement, of fundamental properties of information systems which relate to the reliability and security of our cyber infrastructure. A one-day invitational workshop for senior leaders in the field was held at NIST on May 29, 2007 to assess the potential for a mathematical research program in this area, to consider intermediate-level technical goals, and to identify external research programs with which collaboration would be appropriate. A panel of eight external experts was assembled for wide-ranging discussion with some 15 NIST staff. A workshop report has been issued.

An important goal of this program will be to identify and characterize fundamental measurable properties of complex information systems that are indicators of the inherent level of security (i.e., resilience to threats both known and unknown). The program will develop and analyze abstract mathematical models of information system structure and information flow. Initially, this fundamental work will be applied to the study of complex information systems, such as computer networks and distributed systems, i.e., the area of study which has come to be known as network science. Relevant models will be studied using the theory of discrete random processes, graph theory, queuing theory, and modern Monte Carlo based computational approaches. We will study emergent behavior in large-scale networks, network reliability theory, and the analysis and development of self-healing (homeostatic) systems. The projects started up as part of this effort are described in Part III (Project Summaries) in the subsection entitled Mathematical Applications: Information Technology.

Results of MCSD research on the flow of suspensions (mainly concrete), carried out with a 2006 NASA award of 1,000,000 CPU hours on the Columbia supercomputer at the NASA Ames Research Center, were demonstrated at the NASA and NIST booths at the SC 2007 conference held in Reno, NV on November 10-16, 2007. This is the main conference in the US showcasing research enabled by massively parallel computing (“supercomputing”). The computational models developed use dissipative particle dynamics (DPD) to simulate the flow and interaction of solid particles in a fluid matrix. State-of-the-art real-time visualization based on non-photorealistic rendering and graphical processing unit (GPU) programming facilitated exploration of the rheology simulation output. At the NASA booth, these visualizations were shown on a large 3x3 array of monitors. The results demonstrated advances in understanding the influence of finite size effects, stress transmission, time scales, and system equilibration for both spherical particles and real-shape particles of gravel and sand. This work was carried out by a team of researchers in the NIST Building and Fire Research Laboratory and MCSD, led by Nicos Martys and Edward Garboczi (BFRL), and William George and Judith Terrill (MCSD).

As follow-on to this effort, the team was awarded an additional 400,000 CPU hours on the NASA supercomputer for 2008 to work on the chemistry (hydration) of cement as well as the flow of suspensions. In January 2008 the team was also awarded 750,000 CPU hours on the Blue Gene/P system at Argonne National Laboratory. The allocation is one of 55 awards of supercomputer time given in a peer-reviewed competition known as the Innovative and Novel Computational Impact on Theory and Experiment (INCITE) program. The new CPU time will enable more detailed modeling of the rheological properties of suspensions, as well as new work on a model simulating the three-dimensional changes in structure and chemical composition of aqueous mineral systems, such as those found in environmental geochemistry, ceramic processing, and cement-based materials.

During FY 2007 William Mitchell of MCSD released Version 1.0 of his PHAML system for the solution of elliptic partial differential equations. Such problems are found in a wide variety of models of physical phenomena, from the diffusion of heat in metal to the energy levels of atoms, and hence their efficient solution is of high interest. The core of PHAML is designed to

solve linear self-adjoint elliptic problems on general two dimensional domains, but hooks are provided which enable the solution to a much wider class, including eigenvalue, nonlinear, and time-dependent problems. PHAML stands for Parallel Hierarchical Adaptive Multi-Level, which characterizes the methods upon which the software is based. The package is the culmination of a decade of research on advanced solution methods, including high order finite elements, adaptive mesh refinement, multigrid solution techniques, dynamic load balancing, and parallel computing. Earlier beta releases of the program have been used for a variety of purposes, including solution of scientific and engineering applications, a platform for the investigation of new numerical methods and approaches to programming parallel computers, and a classroom tool for studying numerical methods or parallel computing. At NIST, PHAML has been used, for example, for the solution of a very challenging instance of the Schrödinger equation related to a model of interacting atoms representing qubits in a neutral-atom-based quantum computer.

Researchers in academia and industry are now developing a variety of useful technologies that exploit quantum optics phenomena. Some examples include quantum computation, quantum key distribution, interferometry, and lithography. Creating and maintaining superpositions of states of many photons and entangling them are critical capabilities needed for many such applications. However, because of the extreme fragility of quantum systems, producing them is still very challenging. As part of a NIST Innovations in Measurement Science project, we are working with scientists in the NIST EEEL to develop strategies for optical state preparation, manipulation, and measurement. This year Scott Glancy, working with guest researcher H. M. Vasconcelos, completed a thorough analysis of schemes for making a class of optical states called “Schrödinger cat” states. These states contain an equal superposition of two coherent states of opposite phase. This work is providing critical guidance for EEEL researchers who are working to create such states in the laboratory.

Finally, completion is finally in sight for the Digital Library of Mathematical Functions, the online successor to the classic NBS *Handbook of Mathematical Functions* (M. Abramowitz and I. Stegun, 1964). All 36 chapters are in the final stages of validation, and the full DLMF is expected to be released this calendar year. Look for a pre-release sample of chapters on the DLMF web site, <http://dlmf.nist.gov/>.

## Technology Transfer and Professional Activities

The volume of technical output of MCS D remains high. During the last 18 months, Division staff members were (co-)authors of 31 articles appearing in peer-reviewed journals, including a paper published in *Nature*. Five other invited articles and 12 papers in conference proceedings were also published. Twenty-five additional papers have been accepted and are awaiting publication, while 18 others have been submitted for review. Division staff members gave 25 invited technical talks and presented 27 others to conferences and workshops.

MCS D continues to maintain an active Web site with a variety of information and services, including the Guide to Available Mathematical Software, the Matrix Market, and the SciMark Java benchmark. During calendar year 2007, the division web server satisfied nearly six million requests for pages, or more than 13,000 per day. More than 1.2 Gbytes of data were shipped each day. More than 500,000 distinct hosts were served. There have been more than 130 million “hits” on MCS D Web servers since they went online as NIST’s first web servers in 1994.

Among our most popular software downloads for calendar year 2007 were: Template Numerical Toolkit (linear algebra using C++ templates): 17,779 downloads, JAMA (linear algebra in Java): 16,422 downloads, LAPACK++ (dense linear algebra in C++) 6,975 downloads, and SparseLib++ (elementary sparse matrix manipulation in C++): 5,726 downloads. Another



indication of the successful transfer of our technology is references to our software in refereed journal articles. Our OOMMF software for modeling of micro- and nano-magnetic phenomena was cited in 103 such papers which were published in calendar 2007 alone.

Members of the Division are also active in professional circles. Staff members hold a total of 11 associate editorships of peer-reviewed journals. They are also active in conference organization, serving on four organizing/steering/program committees. Staff members organized three minisymposia for the International Congress on Industrial and Applied Mathematics (Zurich, 2007), as well as a Birds-of-a-Feather session at SIGGRAPH.

Service within professional societies is also prevalent. Ronald Boisvert serves as Co-Chair of the Publications Board of the Association for Computing Machinery (ACM) and is a member of the ACM Council, the association's board of directors. Fern Hunt serves on the Executive Committee of the Association for Women in Mathematics. Daniel Lozier serves as Vice-chair of the Society for Industrial and Applied Mathematics (SIAM) Activity Group on Orthogonal Polynomials and Special Functions. Staff members are also active in a variety of working groups. Ronald Boisvert serves as Chair of the International Federation for Information Processing (IFIP) Working Group 2.5 on Numerical Software, Donald Porter is a member of the Tcl Core Team, and Bruce Miller is a member of W3C's Math Working Group. Judith Terrill represents NIST on the High End Computing Interagency Working Group of the Federal Networking and Information Technology Research and Development (NITRD) Program.

For further details, see Part IV (Activity Data) of this document.

## Staff News

MCSD welcomed three new Postdoctoral Associates during this period. Brian Cloteaux joined MCSD in August 2007 from New Mexico State University, where he did research on analysis of abstract models of computation. At NIST he is working with Isabel Beichl on Monte Carlo methods for the estimation of properties of large-scale graphs. In September 2007 Bryan Eastin joined MCSD in Boulder from the University of New Mexico, where he did research on the relationship between error models and thresholds for fault-tolerant quantum computing. At NIST he will continue his investigations with Manny Knill. Finally, in January 2008, Valerie Coffman joined MCSD from Cornell University where she utilized finite element modeling to study the relationship between microscopic defects and the mechanical properties of polycrystals. At NIST she will be working with Stephen Langer on 3D image-based analysis of materials with complex microstructures.

During 2007 MCSD served as host to Grant Erdman, a research mathematician in the Information Operations and Special Programs Division of the Human Effectiveness Directorate of the Air Force Research Laboratory in San Antonio. As part of the Commerce Science Fellowship program, Erdman spent nine-months at NIST to learn of the organization and structure of the NIST measurement and science labs, while participating in technical projects related to his expertise in mathematical optimization.

Three guest researchers joined MCSD's Scientific Applications and Visualization Group this year to contribute to projects in high performance computing and scientific visualization. They are: Dr. Dong Yeon Cho of the School of Computer Science and Engineering of the Seoul National University (Korea), an expert in machine learning, genetic programming, and applications to bioinformatics, and Edith Enjolras and Cedric Houard, students at the College of Engineering in Computer Science, Modeling and Applications at the Blaise Pascal University in Clermont-Ferrand, France

During the summer of 2007 MCSD hosted 11 student interns working on a wide variety of projects, from image processing to quantum computer simulation; see the table for details.

<b>MCSD Student Interns - 2007</b>				
<b>Name</b>	<b>Institution</b>	<b>Program</b>	<b>Mentor</b>	<b>Project Title</b>
Liuyuan Chen	Montgomery Blair High School	Student Volunteer	B. Rust	Wrote Fortran subroutines & made calculations with Fortran and Matlab
Kevin Costello	Carnegie Mellon University	SURF	S. Glancy	Quantum computer simulation.
Kevin Dela Rosa	University of Texas-Arlington	SURF	R. Kacker	Integrate improved algorithm into Fire-Eye.
Michael Forbes	MIT	SURF	R. Kacker	Improving IPOG algorithm to yield smaller covering arrays.
Gillian Haemer	University of Southern California	Student Volunteer	A. O'Gallagher	Image processing in an immersive visualization environment.
Aaron Jones	Hampton College	SURF	J. Terrill	Visualizing nanostructures.
Olga Kuznetsova	University of Maryland	SURF	S. Langer	Object-oriented finite elements for analyzing material microstructure.
Adam Meier	University of Colorado	PREP	E. Knill	Simulating Fault Tolerant Architectures.
Omotunwase Olubayo	Hampton College	SURF	A. Peskin	Image processing and virtual reality.
Sathish Ragappan	Quince Orchard High School	Student Volunteer	J. Terrill	Curvature
Miguel Rios	University of Puerto Rico	SURF	J. Terrill	Physics Models for Transport in Compound Semiconductors.

SURF: NIST Student Undergraduate Student Fellowship Program. PREP: Professional Research Experience Program

## Recognition

Anthony Kearsley was selected as part of a four-person team to receive the Department of Commerce Bronze Medal for work on matrix assisted laser desorption/ionization-time of flight-mass spectroscopy (MALDI-TOF-MS). The team was cited for work which enabled the widespread use of MALDI as a quantitative measurement tool. In particular, they developed a comprehensive online resource that includes an automated, operator-independent data analysis tool (MassSpectator), a consolidated collection of sample preparation methods, and polymer mass spectroscopy workshop reports. The citation states "Because of their enormous value to industrial, academic, and government researchers, the database and the accompanying tools exemplify the highest level of service to those engaged in mass spectroscopy." The co-recipients of the award were William Wallace, Charles Guttman, and Kathleen Flynn of MSEL. The Bronze Medal is the highest honorary recognition presented at the annual NIST awards ceremony.

During FY 2007 two MCSD mathematicians were honored as Distinguished Scientists by the Association for Computing Machinery (ACM). Ronald Boisvert and Dianne O'Leary, a faculty appointee from the University of Maryland, were included in a group of 49 professionals in ACM's inaugural class of distinguished members. The ACM Distinguished Membership Program recognizes members with at least 15 years of professional experience who have significant accomplishments or who have achieved a significant impact on the computing field. Founded in 1947, ACM is the world's oldest and largest educational and scientific computing society.



Recipients of the 2007 Department of Commerce Bronze Medal (from left to right): Anthony Kearsley (MCSD), William Wallace (MSEL), Kathleen Flynn (MSEL), and Charles Guttman (MSEL).

Ronald Boisvert was co-author of a paper named as winner of the ITL Outstanding Conference Paper for 2007. The paper recognized was

Xiao Tang, Lijun Ma, Alan Mink, Anastase Nakassis, Hai Xu, Barry Hershman, Joshua Bienfang, David Su, Ronald F. Boisvert, Charles Clark, Carl Williams “Quantum key distribution system operating at sifted-key rate over 4 Mbit/s,” in *Proceedings of SPIE* **6244**, pp. 62440P-1-62440P-8 (April 2006).

The paper describes the design of the NIST high-speed quantum key distribution (QKD) system and the innovations in photonics, high-speed electronics, and information algorithms and protocols that were required to bring this system to fruition. With these techniques, the NIST QKD system significantly exceeded the world performance record for speed of key generation and exchange.

Also recognized with ITL Awards this year were Robin Bickel and David Gilsinn for their efforts in organizing the Division’s move from NIST North back to the NIST main campus during the summer of 2006.



*André Deprit*

Former NIST Senior Fellow and MCSD Guest Researcher André Deprit was inducted into the NIST Gallery of Distinguished Scientists, Engineers and Administrators in ceremonies held in Gaithersburg on October 19, 2007. He was cited for pioneering the use of symbolic computing to solve outstanding problems in celestial mechanics, including the theory of integrable dynamical systems with applications to the motion of artificial satellites. André passed away on November 7, 2006. He was represented at the ceremony by his son Etienne.

MCSD mathematician Bonita Saunders was selected to serve as a distinguished presenter at the 2007 Awards Gala of the Benjamin Banneker Institute for Science and Technology which was held in Washington, DC on November 7, 2007. The annual Awards Gala recognizes those making significant contributions to the Institute's mission, "to increase access to, and participation and performance in science and math related professions and academic pursuits by African Americans." Six awards were presented, recognizing excellence in grade school, high school, college, graduate school, PhD. pursuits, and life. Saunders presented the Grade School Award. Speakers at the event included NPR Journalist Juan Williams and TV personality Bill Cosby.

## Passings



**Joyce E. Conlon**, 50, a systems programmer for MCSD since 1999, died in Rockville, Md., on Nov. 14, 2007, after suffering a stroke. Born April 30, 1957, in Richmond, Va., Conlon grew up in suburban Baltimore and attended the University of Maryland-Baltimore County where she earned a Bachelor of Arts degree in mathematics in 1979. Conlon worked as a computer programmer for the Defense Mapping Agency from 1980 to 1985. She began her career at NIST in the fall of 1985 as a computer specialist in the Computer Services Division. Seeing her way through several division name changes, Conlon was reassigned to the ITL High Performance Systems and Services Division and finally to the MCSD in 1999. She retired in July 2005. While at the MCSD, she provided technical computing support to MCSD staff, served as MCSD Computer Security Officer, and was an integral member of the team working to develop the NIST Digital Library of Mathematical Functions (DLMF), the 21st century successor to the NBS Handbook of Mathematical Functions. She continued her work on the DLMF as a guest researcher and contractor until the time of her death. [This text was adapted from an article in *NIST Connections*.]

**Part II**

# **Features**



## Parallel Adaptive Multilevel Finite Elements

The numerical solution of partial differential equations is the most compute-intensive part of a wide range of scientific and engineering applications. As a result, the development of faster and more accurate methods for solving partial differential equations has received much attention in the past fifty years. Nevertheless, many applications at the cutting edge of research remain extraordinarily challenging. These problems necessitate the use of the most advanced numerical techniques and tools such as self-adaptive methods and parallel computers. This year we released the software package PHAML, which serves as a research platform to explore, improve, and apply advanced computational techniques of this type.

William F. Mitchell

The NIST-developed software package PHAML (Parallel Hierarchical Adaptive MultiLevel) can be used to solve a broad class of two-dimensional self-adjoint elliptic partial differential equations (PDEs), including systems of equations and eigenvalue problems, with a variety of boundary conditions. The spatial domain may be any connected region in the plane, including ones with curved boundaries and holes. Problems of this type are found in an extremely wide range of applications, from the study of heat diffusion to the modeling of fundamental properties of atoms.

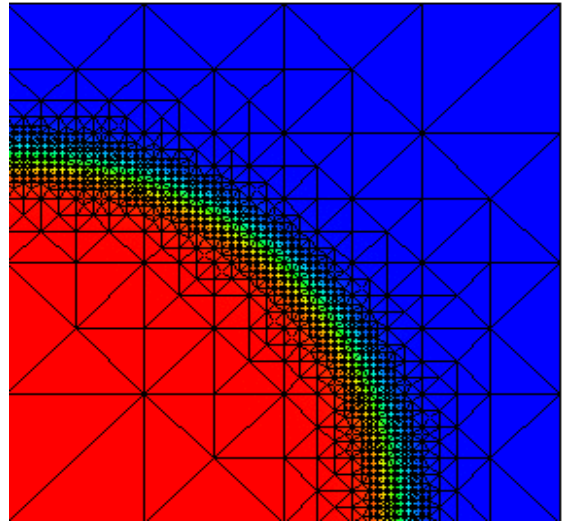
To enable computer solution, the PDE is discretized by the finite element method. We first partition the domain into a set of triangles (the grid or mesh). We then approximate the solution  $u$  by a function

$$\tilde{u} = \sum_i \alpha_i \varphi_i$$

where the  $\varphi_i$  form a set of  $N$  piecewise polynomial basis functions defined on the mesh. Inserting this function into a variational formulation of the PDE leads to a system of  $N$  linear equations (a matrix) that determines the  $N$  coefficients  $\alpha_i$ . Considerable skill is required in the selection of the mesh, the basis functions, and the linear solver to obtain a practical solution procedure.

Adaptive refinement is a critical extension of the finite element method when applied to complex simulations where most of the interesting activity is confined to a small part of the domain. For such problems a fine mesh is necessary to resolve rapidly varying portions of the solution. If such a mesh is applied uniformly over the domain the size of the linear system makes the problem intractable. An optimal grid is one in which

small triangles are used where the solution varies rapidly and larger ones where it is relatively smooth. With adaptive refinement, such an optimal grid is determined automatically through an iterative process in which, given an initial grid and approximate solution on the grid, those triangles with the largest estimated error are refined to create a new grid yielding a more accurate approximate solution. Fig. 1 shows an example of an adaptively generated grid.

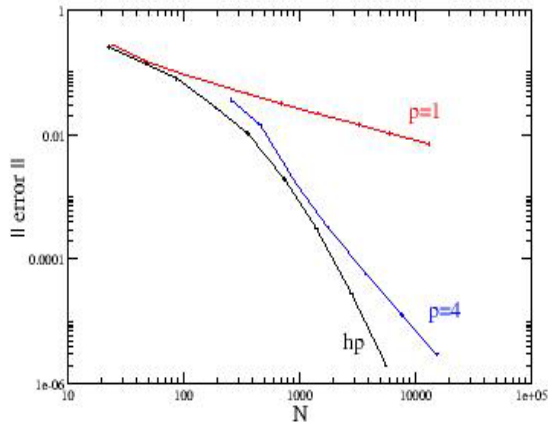


**Figure 1.** An adaptively refined grid for a solution that contains a sharp circular wave front.

The solution can be improved by not only reducing the size of the triangles but also by increasing the degree of the piecewise polynomials. PHAML allows the use of high order polynomials as well as the more common piecewise linear basis functions. Increasing the degree of the piecewise polynomial basis functions can be done locally, resulting in an approximate solution that is not uniform in polynomial degree over the grid.

When both the size of the triangles,  $h$ , and the polynomial degree,  $p$ , are determined adaptively, it is called  $hp$ -adaptive refinement.  $hp$ -adaptive methods are at the cutting edge of finite element research. The reduction of the error as a function of  $N$  can be much faster for an  $hp$ -adaptive method than for just  $h$  refinement, and even better than using a fixed high degree, as shown in Fig. 2. PHAML is currently being used to investigate various approaches to  $hp$ -adaptive refinement.

Even with using adaptive refinement to reduce  $N$ , it can still be very large for complex problems, perhaps in the millions. PHAML uses a multigrid solution technique for the linear system. Multigrid can solve the system in a number of operations proportional to  $N$ , which is optimal. PHAML is based on hierarchical bases, both in  $h$  and  $p$ , to give the different multigrid scales which



**Figure 2.** Behavior of the error as a function of  $N$  for adaptive refinement with linear elements, 4th degree elements, and hp-adaptive refinement.

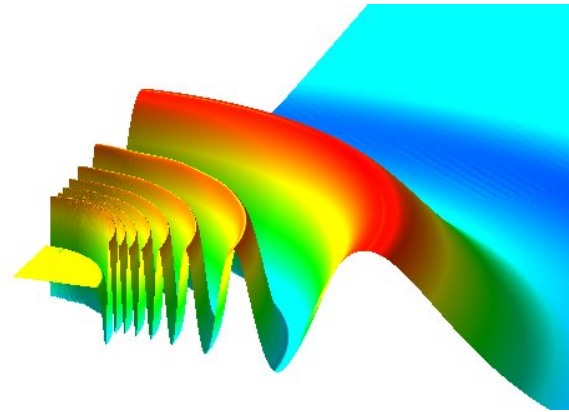
results in rapid convergence. The use of multiple levels in  $p$  is new and is still a topic of active research.

An additional tool for solving complex problems with large  $N$  is the use of parallel computers. PHAML was one of the first systems to use both adaptive refinement and multigrid on parallel computers. The research associated with PHAML brought about a new paradigm for parallel implementations called the full domain partition. New algorithms and implementations of multigrid and adaptive refinement, along with the necessary load balancing required to make it successful have been developed under this paradigm [1, 2]. PHAML uses message passing parallelism implemented through the Message Passing Interface (MPI). PHAML is written in Fortran 90 and designed as a collection of modules. Each module deals with one aspect of the program (grid refinement, error estimation, multigrid, etc.) and contains data types and associated operations. The details, including parallelism, are hidden from the user, who simply calls subroutines for operations such as solving the PDE or evaluating the computed solution. The interface to these subroutines contains a very large number of arguments which gives the user a great deal of control of the algorithms. Most arguments are optional, with reasonable default values, so the interface remains simple and clean for routine use. The specification of the problem to be solved (coefficients of the PDE, boundary conditions, domain) are defined by a few subroutines that the user writes. The PHAML User's Guide [3] provides all the information a user of PHAML needs.

Interactive graphics provide another means of obtaining the results of PHAML's computations. The graphics engine is a separate parallel process which receives data from the computational processes by message passing. The user has interactive control of the graphics as PHAML is running. Control includes rotate, zoom and pan operations, and selection of what

is to be displayed (solution, error, grid, parallel partition, etc.). Figs. 1 and 3 provide two examples of the graphics that are available. PHAML makes use of the OpenGL graphics library, which is freely available on nearly every computer platform, supporting the goal of providing freely available and highly portable tools.

Version 1 of PHAML was released in May 2007; see <http://math.nist.gov/phaml>. It has been used by scientists for solving application problems [4, 5], researchers in scientific computing for comparing different methods, and instructors of classes on numerical solution of PDEs and parallel computing.



**Figure 3.** The computed solution of a model of two interacting atoms, as displayed by the PHAML graphics engine.

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## Participants

W. F. Mitchell, M. McClain (MCSD); E. Tiesinga (PL)

<http://math.nist.gov/phaml>



## Computable Error Bounds for Delay Differential Equations

A problem of increasing importance in many applications is how to assess the quality of computed results from models involving differential equations. Quite often the best error estimates provide only an order of magnitude assessment rather than rigorous numerical bounds. In the early 1970's A. P. Stokes developed a method of proving the existence of periodic solutions for nonlinear differential and functional differential equations in the neighborhood of approximate solutions which yields precise error bounds. He demonstrated several examples for ordinary differential equations, but gave no computed error bound in the case of functional differential equations. Recently D. E. Gilsinn [1] developed the numerical methods needed to prove the existence of periodic solutions for delay differential equations in the neighborhood of approximate periodic solutions and calculating exact error bounds. Here we provide some background on delay differential equations, outline the argument that leads to exact error bounds, and give an example of the application of the method to a classic Van der Pol equation with delay.

David E. Gilsinn

Systematic work with mathematical models in medicine and biology involving differential equations with delay terms began in the early 1900's with the studies of R. Ross [5] on problems in malaria epidemiology. This early work was extended during the period 1920-1940 for applications in areas such population ecology, business cycles, and control systems [3, 4, 7]. All of these studies pointed out the need to consider the "transmission time" between when an input is introduced into a system and when a response is expected, that is, the *delay* inherent in the system.

Such problems have also arisen in manufacturing. Machine tool chatter is a self-excited oscillation of a cutting tool against the surface being machined. It typically is heard as a high frequency noise in a machine shop. In the manufacturing literature it is referred to as regenerative chatter. In the 1950's Tobias and Fishwick [8] developed models to explain this self-excited oscillation using delay terms. In the process of a turning operation with a lathe, the surface being cut at a certain time is affected by the results from the cutting tool during the cut at the previous revolution on the same surface. Any slight imperfection in this previous cut affects the current cut and can start an oscillation that could generate chatter.

Early work in the studies of machine tool chatter led to linear delay differential equations of the form

$$m\ddot{x}(t) + \frac{h}{\omega}\dot{x}(t) + \lambda x(t) = -k(x(t) - x(t-T)), \quad (1)$$

where the coefficients are determined from experiments. A linear theory would predict, however, that the amplitude of vibration would increase indefinitely once the depth of cut exceeded some critical value. In the early 1970's Hanna and Tobias [2] introduced cubic nonlinearities in the model and modified the equation to the form

$$\begin{aligned} m\ddot{x}(t) + \frac{h}{\omega}\dot{x}(t) + \lambda(x(t) + b_1x(t)^2 + b_2x(t)^3) \\ = -k[(x(t) - x(t-T)) \\ + C_1(x(t) - x(t-T))^2 \\ + C_2(x(t) - x(t-T))^3]. \end{aligned} \quad (2)$$

With this modification some good qualitative correspondence between predictions and theoretical studies was obtained.

Many such problems in biology, population dynamics, and machining can be written in the vector form

$$\omega \dot{x}(t) = X(x(t), x(t-\omega)), \quad (3)$$

where we look for periodic solutions with a frequency of  $\omega$  on the interval  $[0, 2\pi]$ . Approximate periodic solution can be found by optimization methods using finite trigonometric series of the form

$$\hat{x}_m = a_2 \cos(t) + \sum_{n=2}^m [a_{2n} \cos(nt) + a_{2n-1} \sin(nt)] \quad (4)$$

The  $\sin(nt)$  term is often dropped so that one can estimate the frequency  $a_1 = \bar{\omega}$ . To shorten notation one usually uses  $x_h = x(t-h)$ . The problem then is to determine conditions for which equation (3) has an exact periodic solution with frequency  $\omega$  and determine numerically computable error bounds for the approximate periodic solution and frequency. There exist programs that allow you to compute numerical solutions to (3); however they usually can only give approximate estimates of error bounds based on grid size.

The fundamental argument that establishes the existence and bounds for the approximate periodic solution and frequency rests on generalizations of two results, one from linear algebra, and one from elementary optimization theory. The linear algebra result can be stated as follows. The algebraic system  $Ax=b$  has a solution if and only if  $b^T \bar{u} = 0$  for all solutions of  $A^*u = 0$ , where  $A^* = \bar{A}^T$  is the adjoint, and the overbar represents complex conjugates. This result states that the system  $Ax=b$  has a solution if and only if the right hand side,  $b$ , is orthogonal to all solutions of the adjoint system. The result is sometimes referred to as the solvability condition. Its extension into the space of

functions and operators is often referred to as the Fredholm alternative. The other result comes from optimization theory and is called the fixed point theorem. In effect, we are given a function,  $S(x)$ , defined on some space, and we look for a solution to the problem  $x = S(x)$ .

Assume that one has constructed an approximate  $2\pi$ -periodic solution as in (4) and an approximate frequency  $\hat{\omega}$ . If you substitute these into (3) you will get a system similar to (3) but with an error term

$$\hat{\omega} \dot{\hat{x}} = X(\hat{x}, \hat{x}_{\hat{\omega}}) + k, \quad (5)$$

where  $k(t)$  is  $2\pi$ -periodic and bounded by some constant  $r$  so that  $|k(t)| \leq r$ . In order to study any solutions to (3) in the neighborhood of  $(\hat{\omega}, \hat{x})$  one introduces the variational equation about  $(\hat{\omega}, \hat{x})$

$$\hat{\omega} \dot{z} = dX(\hat{x}, \hat{x}_{\hat{\omega}}; z, z_{\hat{\omega}}) = \hat{A}z + \hat{B}_{\hat{\omega}}, \quad (6)$$

where  $\hat{A} = X_1(\hat{x}, \hat{x}_{\hat{\omega}})$ ,  $\hat{B} = X_2(\hat{x}, \hat{x}_{\hat{\omega}})$ . The adjoint equation relative to (6) is given by

$$\hat{\omega} \dot{v} = -v\hat{A} - v_{-\hat{\omega}}\hat{B}. \quad (7)$$

An important relationship between the  $2\pi$ -periodic solutions of (6) and (7) is that they both have the same finite number of  $2\pi$ -periodic solutions.

In order to state a property that  $(\hat{\omega}, \hat{x})$  must satisfy we define a characteristic multiplier.  $\rho$  is a characteristic multiplier of the linear delay equation

$$y'(t) = A(t)y(t) + B(t)y(t-\omega) \quad (8)$$

where  $A(t)$ ,  $B(t)$  are  $2\pi$ -periodic, if there is non-trivial solution  $y(t)$  of (8) such that

$$y(t+2\pi) = \rho y(t) \quad (9)$$

Note:  $y(t)$  would be a  $2\pi$ -periodic solution of (8) if  $\rho=1$ .

There is a property that  $(\hat{\omega}, \hat{x})$  must satisfy that gives a condition that essentially guarantees that  $(\hat{\omega}, \hat{x})$  is in some sense isolated. In particular,  $(\hat{\omega}, \hat{x})$  is said to be non-critical if the variational equation (6) with respect to  $(\hat{\omega}, \hat{x})$  has a simple characteristic multiplier,  $\rho_0$ , that need not be unity, and all other characteristic multipliers are not unity. Next, if  $v_0$  is the single solution of the adjoint equation (7) associated with  $\rho_0$ , then

$$\int_0^{2\pi} v_0^T J(\hat{x}, \hat{\omega}) dt \neq 0, \quad (10)$$

where

$$J(\hat{x}, \hat{\omega}) = \dot{\hat{x}} + \hat{B}\dot{\hat{x}}_{\hat{\omega}}$$

The form of the Fredholm alternative that is relevant here is as follows. The nonhomogeneous system

$$\hat{\omega} \dot{x} = \hat{A}x + \hat{B}x_{\hat{\omega}} + f, \quad (11)$$

has a unique  $2\pi$ -periodic solution if and only if

$$\int_0^{2\pi} v_0^T f dt = 0 \quad (12)$$

for all independent solutions  $v_0$  of (7). Furthermore there exists a constant  $M>0$ , independent of  $f$ , such that

$$|x| \leq M|f|. \quad (13)$$

This is just an operator version of the linear algebra solvability condition.

One looks for an exact solution and frequency for (3) by perturbing the approximate solution and frequency. To do this one can introduce the perturbations

$$\omega = \hat{\omega} + \beta, \quad x = \hat{x} + \frac{\hat{\omega}}{\omega} z. \quad (14)$$

If these are substituted into (3), then a perturbed variational equation about the approximate solution can be written in the form

$$\hat{\omega} \dot{z} = dX(\hat{x}, \hat{x}_{\hat{\omega}}; z, z_{\hat{\omega}}) + R(z, \beta) - \beta J(\hat{x}, \hat{\omega}) - k, \quad (15)$$

where  $R(z, \beta)$  is a rather long error term, but is only a function of  $z$  and  $\beta$  defined in (14). Now consider an associated equation

$$\hat{\omega} \dot{z} = dX(\hat{x}, \hat{x}_{\hat{\omega}}; z, z_{\hat{\omega}}) + g - \beta J(\hat{x}, \hat{\omega}) - k. \quad (16)$$

and apply the Fredholm solvability result to (16). In particular, if  $(\hat{\omega}, \hat{x})$  is noncritical with respect to (3), then there exists a unique  $\beta$ , designated  $\beta(g)$ , such that

$$g - \beta(g) J(\hat{x}, \hat{\omega}) - k \perp v_0, \quad (17)$$

where  $v_0$  is the solution of the adjoint equation (7) corresponding to the characteristic multiplier  $\rho_0$  of equation (6). Furthermore there exists a  $2\pi$ -periodic solution of (16), designated by  $z(g)$ , that satisfies

$$|z(g)| \leq M |g - \beta(g) J(\hat{x}, \hat{\omega}) - k|, \quad (18)$$

for some  $M>0$ . Finally there exist computable constants,  $\lambda_0, \lambda_1$ , such that

$$\begin{aligned} |\beta(g)| &\leq \lambda_0 (|g| + r) \\ |z(g)| &\leq \lambda_1 (|g| + r) \end{aligned} \quad (19)$$

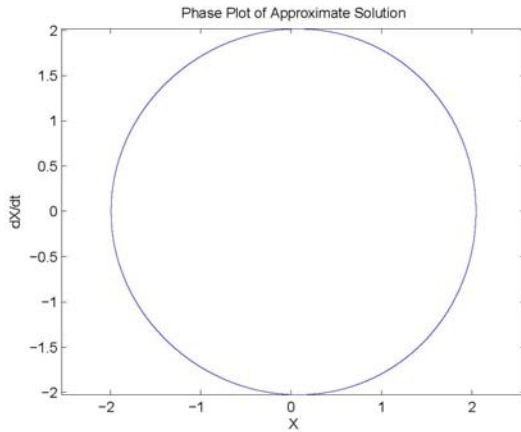
The fixed point property can now be used to obtain the final result. Define a map

$$S(g) = R(z(g), \beta(g)). \quad (20)$$

This map satisfies the following properties that provide sufficient conditions for a fixed point. There exist two functions  $E_1(\delta)$ ,  $E_2(\delta)$  and two positive constants  $F_1, F_2$  so that

$$\begin{aligned} |S(g)| &\leq E_1(g), \\ |S(g) - S(\tilde{g})| &\leq E_2(g) |g - \tilde{g}|, \end{aligned} \quad (21)$$

where



**Figure 2.** Phase plot of approximate solution for the Van der Pol equation

$$\begin{aligned} E_1(\delta) &\leq F_1 \delta^2, \\ E_2(\delta) &\leq F_2 \delta. \end{aligned} \quad (22)$$

The final result can then be stated as follows. If  $(\hat{\omega}, \hat{x})$  is noncritical with respect to (3) and  $\delta$  is selected so that

$$\delta \leq \min\{1/F_1, 1/2F_2, \hat{\omega}/4\lambda_0\} \quad (23)$$

With  $r \leq \delta$ , then there exists an exact frequency  $\omega$ , and solution of (3) such that

$$\begin{aligned} |x - \hat{x}| &\leq 4\lambda_1\delta, \\ |\omega - \hat{\omega}| &\leq 2\lambda_0\delta. \end{aligned} \quad (24)$$

Although there seems to be a large number of parameters to compute, they can all be estimated. Of all the parameters the one that tends to be the most critical is  $M$  in (18).

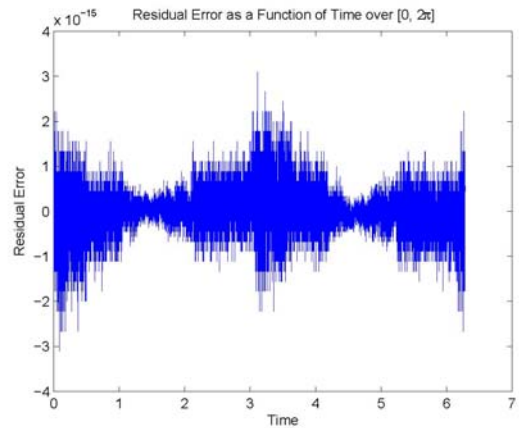
This result was applied to the classic Van der Pol equation with delay in the form

$$\omega^2 \ddot{x} + \omega\lambda(x(t-\omega)^2 - 1)\dot{x}(t-\omega) + x = 0 \quad (25)$$

For  $t \in [0, 2\pi]$ . An approximate solution and frequency were estimated by a Galerkin projection method as

$$\begin{aligned} \hat{x}(t) &= 2.0185 \cos(t) \\ &+ 2.5771 \times 10^{-3} \sin(2t) + 2.5655 \times 10^{-2} \cos(2t) \\ &+ 1.0667 \times 10^{-4} \sin(3t) - 5.2531 \times 10^{-4} \cos(3t) \\ &- 7.1780 \times 10^{-6} \sin(4t) - 2.2043 \times 10^{-6} \cos(4t), \\ \hat{\omega} &= 1.0012, \end{aligned} \quad (26)$$

where only the first few harmonics have been displayed. The residual was estimated by substituting (25) into (24) and computing the maximum value over the interval  $[0, 2\pi]$ . The result was  $r = 3.1086 \times 10^{-15}$ . The distribution of errors is shown in Fig. 1 and the approximate solution is shown in Fig. 2. Some lengthy estimates yield the following parameter values  $M =$



**Figure 1.** Residual error of approximate solution for the Van der Pol equation

$2.7618 \times 10^2$ ,  $\lambda_0 = 8.4091$ ,  $\lambda_1 = 6.6736 \times 10^3$ . One can then compute  $F_1 = 2.5941 \times 10^9$ ,  $F_2 = 1.0798 \times 10^{10}$ ,  $\delta = 4.6305 \times 10^{-11}$ . With these values (21) and (22) will produce a convergent fixed point iteration. One can then finally estimate the error between the approximate frequency and solution and the exact as

$$\begin{aligned} |x - \hat{x}| &\leq 1.2361 \times 10^{-6}, \\ |\omega - \hat{\omega}| &\leq 7.7877 \times 10^{-10}. \end{aligned} \quad (27)$$

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## Participants

David E. Gilsinn, Sita Ramamurti

## Making Optical “Schrödinger Cat” States

*We are developing technologies that exploit exotic quantum effects in optical systems for practical use. For example, photons may be useful for encoding information as quantum bits (qubits) for quantum computation and communication. Quantum entanglement between photons can also be used to enhance the sensitivity of interferometers. The ability to prepare and measure a particular class of photon states called “Schrödinger cat” states is a prerequisite to developing applications of this type. We have completed an analysis of many cat creation schemes, and are working with the NIST Electronic and Electrical Engineering Lab (EEEL) to build an experiment that will produce them.*

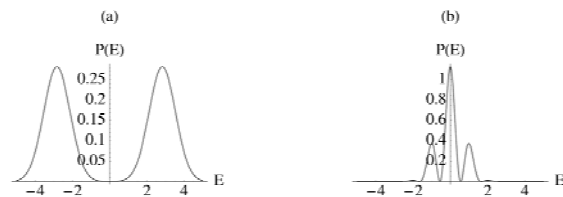
Scott Glancy

Quantum optics is a field rich with potential for developing new technologies and fundamental physics experiments. There is a strong history of optical experiments testing and verifying some of the foundations of quantum theory such as superpositions of states and entanglement. Researchers are now developing useful technologies that exploit these quantum phenomena. Some examples include quantum computation, communication, and cryptography, interferometry, and lithography. Because of the extreme fragility of the quantum systems, creating and maintaining superpositions of states of many photons and entangling them is still very challenging. We are developing strategies for optical state preparation, manipulation, and measurement, and we are building experiments to implement these strategies.

We have completed a thorough analysis of many schemes for making a class of optical states, which we call “Schrödinger cat” states [1]. These states contain an equal superposition of two coherent states of opposite phase. We have made significant progress toward making cat states in the laboratory.

A classical beam of light, produced for example by a laser, is composed of oscillating electric and magnetic fields. As a classical light wave travels through space its electric field vector oscillates up and down between two extreme positive and negative values. However, for light beams in “Schrödinger cat” states the electric field vector exists in a coherent superposition of pointing both up and down. At each of the wave’s anti-nodes one may measure a large positive or negative electric field, each with probability 1/2, as shown in Fig. 1. At the node, one expects to find zero electric field, but instead we see a probability distribution centered at zero with some interesting structure. This is

caused by quantum interference between the electric-field-up and the electric-field-down parts of the cat state. In Schrödinger’s thought experiment a diabolical device produces a cat which is in superposition of dead and live. Our cat states are analogous in that they exist in a superposition of two distinct electric field configurations. Of course they are quite different from Schrödinger’s original cat because they contain only a few photons and do not purr.



**Figure 1.** Part (a) shows the probability distribution for measuring electric field  $E$  at an anti-node of a light beam in a cat state. (b) shows the probability distribution at a node. The electric field units are arbitrary.

Cat states are extremely fragile, because the absorption of a single photon destroys the superposition, washing out the interference seen in Fig. 1(b). Cat states containing many photons are very sensitive to absorption, because the probability that zero photons are lost decreases exponentially with the number of photons.

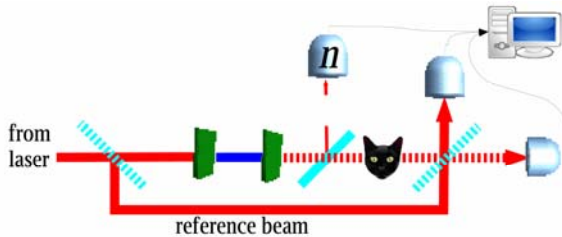
Cat states are necessary for several future technologies. One proposal for an optical quantum computer represents its quantum bits with beams of light whose electric fields are pointing up (logical 1) or down (logical 0). The cat state is an equal superposition of these states. This scheme also requires cat states as a resource for logic operations and teleportation of qubits.

Cat states may also be useful for precision measurements of small distances. When interferometry is performed with classical light, a laser beam is split in two; the two parts are then recombined and allowed to interfere with one another, creating a pattern of light and dark fringes spaced every  $\lambda/2$ , where  $\lambda$  is the light’s wavelength. If the difference in the path lengths traveled by the two beams changes, then the pattern of fringes will shift. The uncertainty in the measured distance is proportional to  $\lambda/\sqrt{N}$ , where  $N$  is the mean number of photons in the beam. If instead cat states are used in the interferometer, the distance between fringes (similar to that in Fig. 1(b)) is proportional to  $\lambda/\sqrt{N}$ , and the uncertainty of the distance measurement is  $\lambda/N$ . However, to take advantage of this enhanced interference in the cat state, one must ensure that none of the cat’s photons are absorbed. Furthermore, current experiments struggle to create cat states with  $N > 1.5$ , while conventional lasers can easily produce classical

beams with  $N > 10^{10}$ . The enhanced measurement precision is likely to be useful only in environments with low photon loss and limited laser power.

The creating of cat states remains an experimental challenge. The original proposal for transforming classical laser light into a cat requires a “Kerr” material that has both a strong nonlinear interaction and low photon absorption. Unfortunately our calculations show that the best currently available material (fused silica fibers) has a ratio of nonlinear strength to photon absorption that is nearly 300 times too small. Progress is being made in engineering Kerr materials, for example using photonic crystals and electromagnetically induced transparency.

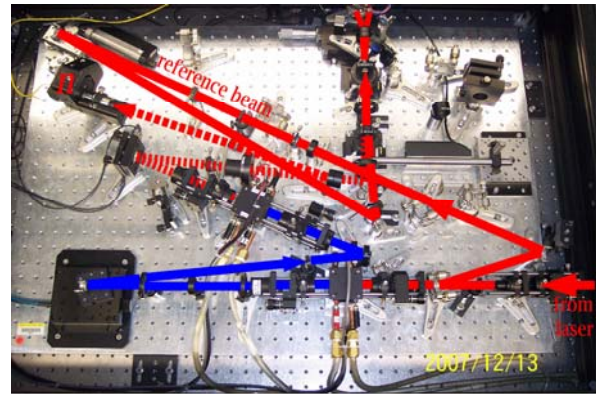
In the meantime, we require a more clever method to make cats. Several methods exist which exploit a general strategy of using an “easier” nonlinear interaction, splitting off part of the light, and making a measurement. Depending on the measurement result one may infer that a cat has been created in the remaining light beam. Each scheme exploits some trade-offs in the experimental requirements such as the type of nonlinearity used and the efficiency and noise level of photon detectors. These choices impact the degree to which the created state approximates an ideal cat, the number of photons the cat contains, the probability with which a cat is produced in each attempt, etc.



**Figure 2.** Diagram of photon subtraction scheme to make cat states. Red laser light enters from the left. The red light is converted to blue through frequency doubling in the green  $\text{KNbO}_3$  crystal. The blue light is then converted back to red during downconversion, creating the squeezed light. When the photon counter registers  $n$  photons, we know a cat has been created, which we verify in a final measurement.

The simplest of these schemes, “photon subtraction”, is shown in Fig 2. We first create a squeezed state of light through the lower order nonlinear process of frequency downconversion. During downconversion photons of frequency  $\omega$  are split into two photons with frequency  $\omega/2$ . We then use a mostly silvered mirror (with transmissivity 99%) to split off a small fraction of the squeezed beam, which is then sent to a photon detector. When the photon detector clicks, we know that a photon has been subtracted from the squeezed beam, which has now been transformed into a state that closely approximates a cat state.

In collaboration with members of the EEEL, we are implementing a photon subtraction experiment in the laboratory. The current optics arrangement appears in Fig. 3. Two crucial elements for the experiment’s success are the purity of the squeezed state created during downconversion and the efficiency of the photon detector. Our collaborators in EEEL have developed a high-efficiency, low noise photon detector which is capable of counting the number of photons. Our simulations show that subtracting multiple photons will significantly enhance the fidelity and size of the cat. We are also investigating innovative methods for high purity squeezing and algorithms for inferring what state our experiment has created from measured data.



**Figure 3.** Photograph of cat making laboratory experiment. Light enters at the lower right, and the final cat verification measurement occurs at the top, where the cat and reference beams are combined and then split.

This work is a component of the Quantum Optical Metrology Innovations in Measurement Science project, the goal of which is to create a “test-bed” of quantum optical state preparation (including cat state and others), manipulation, and measurement. Such a test-bed and the competence we have gained building it will allow us to explore and evaluate new technologies that exploit the quantum nature of light, including quantum information and measurement applications.

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## Participants

S. Glancy, E. Knill (MCSD); T. Gerrits, T. Clemment, S. W. Nam, R. Mirin (EEEL); H. M. Vasconcelos (Universidade Federal do Ceará, Brazil)

## Modeling the Rheological Properties of Suspensions

*Understanding the mechanisms of dispersion or agglomeration of particulate matter in complex fluids, such as suspensions, is of technological importance in many industries such as pharmaceuticals, coatings, and concrete. These fluids are disordered systems consisting of a variety of components with disparate properties that can interact in many different ways. Modeling and predicting the flow of such systems represents a great scientific and computational challenge requiring large-scale simulations.*

*Our goal in this project is to advance our understanding of the flow properties (rheology) of a specific suspension, fresh concrete, which is composed of cement, water, sand, and stones. Concrete rheology has a tremendous impact on the construction of concrete structures, an industry with a \$110B per year impact on the US economy. In collaboration with scientists in the NIST Building and Fire Research Laboratory (BFRL), we are developing a dissipative particle dynamics code, called QDPD, which is capable of performing large scale simulations of suspensions. QDPD is highly parallel and has been shown to efficiently scale up to at least 1,000 processors when running on the NASA supercomputer Columbia. .*

### William George

**Background.** Fluids can be characterized by properties known as yield stress and viscosity, each of which is a function of shear rate. Yield stress is the force applied per unit area to initiate the flow. Viscosity is the applied force per unit area needed to maintain a shear rate. Shear rate is the velocity gradient perpendicular to the flow direction. Many factors control viscosity and yield stress. In building materials like concrete (a combination of water, cement, sand, and stones) viscosity and yield stress depend on the ratio of water to cement, the volume of sand or stones used, as well as their shape and size distribution. In addition, there can be great variability in each of the component materials themselves. As a “concrete” example, rocks mined in quarries are usually angular because they are crushed when processed, while rocks taken from river beds are typically rounded due to erosion. It turns out that the more uniform the size of the rocks the harder it is to get a concrete suspension composed of those rocks to flow. In this case, the concrete fluid may actually jam when poured through a narrow opening thus causing delays in construction. Clearly, to optimize the flow properties of complex suspensions, one needs to understand the relationship between flow and properties of the fluid's constituents.

**QDPD.** Modeling and predicting the flow of complex disordered systems of this type represents a great scientific challenge. Simply accounting for the size and shape variation of the solid components of the suspension (cement particles, sand or rocks) presents difficult computational problems. Modeling a representative system may entail keeping track of up to 100,000 solids of varying shape and size. Further, many of the forces between rocks (aggregate) depend on the local surface curvature of the aggregate at points close to neighboring aggregates. This requires keeping track of the location, orientation and shortest distance between neighboring solids. Clearly, predicting the properties of such systems based upon modeling of such fundamental interactions necessitates large-scale simulations.

We have adopted and developed some novel modeling approaches originally based on cellular automata which can successfully take into account many of the complex features of a suspension. QDPD [1], which stands for Quaternion-based Dissipative Particle Dynamics (DPD), uses the recently developed DPD technique [2] to simulate the fluid and its interaction with the inclusions of the suspension. We have added other forces to this system to better account for the interaction between the large particles in the suspensions, the inclusions, e.g., lubrication forces that help keep the inclusions separated and van der Waals forces that introduce an attractive inter-particle force. Brownian forces are also added to maintain system temperature. Our original (serial) code was validated by both theory and experiments on idealized systems and has been extended to account for random-shaped objects with different inter-particle interactions.

We have recently enhanced QDPD to utilize the power of large parallel machines, regularly using 500+ processors, and sometimes using 1,000 or more processors, to simulate systems composed of over 32,000 inclusions and one million fluid particles. QDPD remains under constant development to improve its capabilities, such as ability to simulate non-Newtonian fluids, as well as to improve its parallel performance.

**NASA's Columbia supercomputer.** During the past year we were awarded 1 million CPU-hours of compute time on the NASA supercomputer Columbia to perform simulations with QDPD. Located at NASA's Ames Research Center in California, Columbia is a 10,240-CPU system based on SGI's NUMAflex architecture. Not only has this access enabled us to perform very large simulations, it has allowed us to analyze the effect of varying system parameters such as the density of inclusions in the suspensions, the applied shearing speed, and the distribution of inclusion sizes. With the added compute power we were also able to move from

spherical inclusions to realistically shaped inclusions for a more accurate simulation.

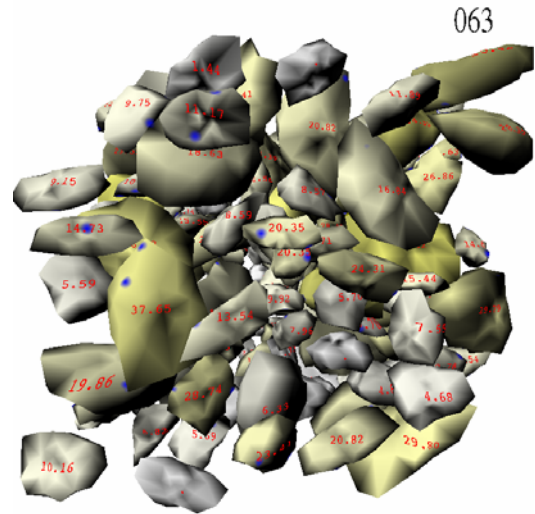
**Results.** We have developed a new scalable parallel algorithm that has enabled us to make advances in understanding the influence of finite size effects, stress transmission, time scales and system equilibration. Through numerical modeling and visualization, this research has provided greater insights into the physical mechanisms associated with the onset of flow. Aspects of yield stress and viscosity can be linked to spatio-geometric properties of suspensions including the number of neighboring rocks and their relative orientation. Further, by examining the very long time scale behavior of the rocks, we can link their motion to visco-elastic properties of the suspension.

**Hybrid Realistic / Non-Photorealistic Visualization.**

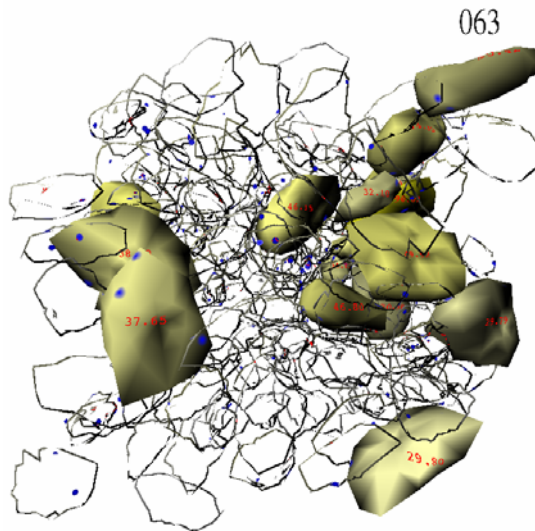
Visualization has proven to be critical to understanding the nature of the results generated from large-scale simulations of this type. We visualize the rocks directly, but augment the visualization with embedded data to provide additional information on interactions between rocks and the per-rock stress (see Fig. 1). The addition of these values allows quantitative observations and measurement, as opposed to the purely qualitative insight provided by most visualizations. In addition, blue dots show the points of interaction between rocks in the simulation. As the suspension becomes denser, it becomes increasingly difficult to find the high-stress particles in a visualization, much less chains of such particles. While a smaller system may be simple enough to understand without further visualization tools, the larger system in Fig. 1 and our biggest system to date, 2025 rocks, require extra tools, such as culling the less interesting rocks, in order to allow the scientist to find potential jamming.

In some cases the user would like to focus on the highest stress rocks, but still have some indication of the surrounding rocks. To achieve this, we turn to non-photorealistic rendering techniques to show these rocks in a sketchy style. The result, shown in Fig. 2, is quite effective, especially when seen in motion. The coherent motion of each low-stress rock's silhouette enhances the ability to recognize and distinguish individual rocks. Here we can clearly see a diagonal chain of rocks from the upper right, wrapping briefly to the opposite side (the simulation wraps toroidally).

In addition, it is useful to track the high-stress rocks from a single frame of through the entire simulation. That allows the scientist to see how those specific rocks move into gridlock, and how they escape, and continue on afterwards. For example, in some simulation runs, a small rock can be seen to move and twist to a new location while larger rocks remain locked in place. Then the larger rocks release, the stress goes down, and the aggregate motion continues.



**Figure 1.** Frame 63 in a simulation of the flow of rocks in a suspension. The per-rock stress is shown with a gray-yellow color scale, and also with a numeric value printed on the face for each rock.



**Figure 2.** Same frame 63 in a simulation of the flow of rocks in a suspension. Lower stress rocks are shown in sketch mode.

In addition, it is useful to track the high-stress rocks from a single frame of through the entire simulation. That allows the scientist to see how those specific rocks move into gridlock, and how they escape, and continue on afterwards. For example, in some simulation runs, a small rock can be seen to move and twist to a new location while larger rocks remain locked in place. Then the larger rocks release, the stress goes down, and the aggregate motion continues.

The sparse visualization of Fig. 2 makes it much easier to see and understand the per rock digital stress measurements. The stress value is centered on the face of the rock closest to the viewer, so as the system is rotated and manipulated, whether on the desktop or in the immersive visualization environment, the text always

remains at the correct orientation. Some interactive rotation is generally necessary to see the values on hidden rocks, but with many fewer rocks displayed as solid photo-realistic entities, it is straightforward to find a suitable view to read the data from each rock.

To assist the scientist in choosing a frame to display, we created an input analysis tool providing a graph of the total system stress per frame, with a slider to indicate a frame of interest (Fig. 3). For example, frames just before a steep drop-off in stress are of particular interest since they may indicate a time when the rocks in the aggregate were binding, but then moved suddenly to release the pressure. Other interactions with the GUI enable controlling other visual features.

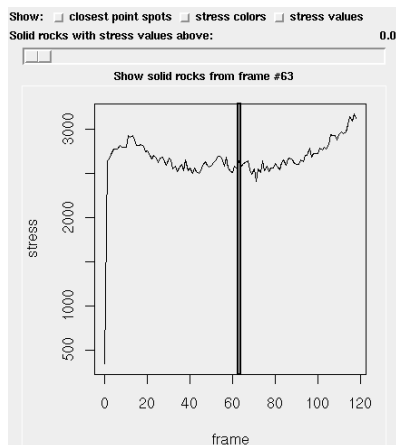


Figure 3. GUI for interactive exploration of the visualization.

**Shading-based visualization environment.** This set of visualizations was created with a procedural-shading-based add-on to our visualization environment. A shader is a procedure which determines the color (i.e. shading) and opacity of each point on a surface. Our shaders are written in the OpenGL Shading Language and run in the graphics hardware at each pixel on each rock. To determine the color and opacity of each pixel, the shader refers to the current rock and frame number, position of the pixel on the rock, and data packed into floating point texture variables. This procedure is responsible for creating the sketchy appearance for less important rocks, the stress color scale for solid rocks, placing the spots on the rock surface, and writing the numeric values on each rock.

This shading framework provides a very flexible mechanism for experimenting with new visualization ideas. The shading procedure can be modified and re-loaded while the application is running. It can use an arbitrary number of slider-controllable parameters for interactive manipulation of the shader's behavior. For example, we can interactively change the frame used to decide which rocks are solid, and the stress level at which we show a blue closest point and the level to show a solid rock rather than an outline.

Graphics hardware has a number of limitations that impact shaders. Some, like the maximum available texture memory, are hard limits (512 MB on our system), while others, like the number of texture accesses made by the shader, are soft limits affecting the frame rate and interactivity of the resulting visualization. For both reasons, we must process our sometimes multi-gigabyte raw data into a compact form to be stored in the limited texture memory for use by the shader. We keep the total stress for each rock on each frame, as well as the closest point location and stress for the highest-stress closest points for each rock on each frame. In each case, we need to turn a 3x3 stress tensor into a single scalar stress value for use and comparison, and combine these to produce a single stress value per rock. There are two principal choices, referred to as shear stress and normal stress, although in some cases we have performed visualization using distance or log stress. Rather than make a single choice, our software takes an arbitrary expression to guide texture creation.

These visualization methods provide insight by combining several quantitative methods to reveal spatial-temporal relationships. The user can find regions of interest rocks by visualizing lines of stress and embedded numerical values. They can graphically ask interactive questions and easily reduce their search for areas of interest. Our scientific collaborators report that the visualizations enable them to validate the physical correctness of the simulation, to detect problems, and to tune parameters of the model.

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## Participants

William L. George, Julien Lancien, Steve Satterfield, Marc Olano, Judith Terrill (MCS D); Nicos Martys, Edward Garboczi (NIST BFRL)

<http://math.nist.gov/mcsd/savg/vis/fluid/>



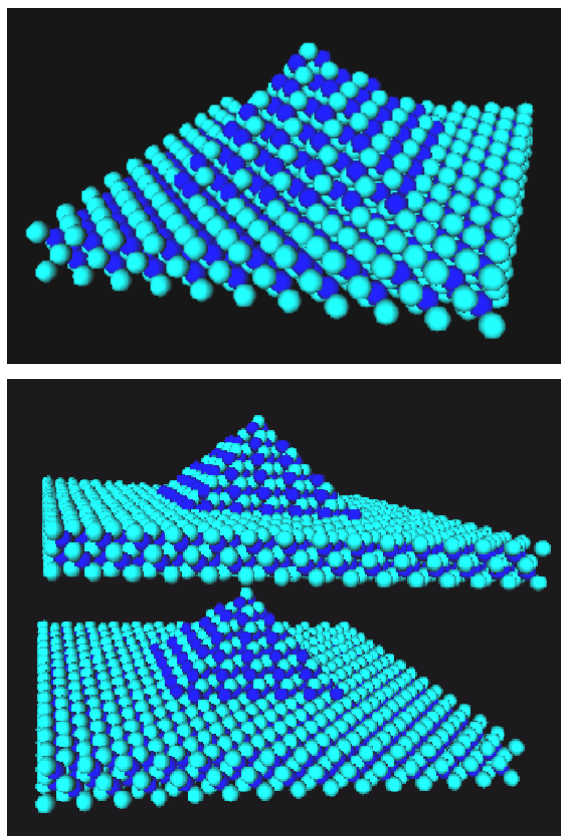
## Computation, Visualization of Nano-structures and Nano-optics

Research and development of nanotechnology, with applications ranging from smart materials to quantum computation to biolabs on a chip, has the highest national priority. Semiconductor nanoparticles, also known as nanocrystals and quantum dots, are one of the most intensely studied nanotechnology paradigms. Nanoparticles are typically 1 nm to 10 nm in size with a thousand to a million atoms. Precise control of particle size, shape and composition allows one to tailor charge distributions and control quantum effects to tailor properties completely different from the bulk and from small clusters. As a result of enhanced quantum confinement effects, nanoparticles act as artificial, man-made atoms with discrete electronic spectra that can be exploited as light sources for novel enhanced lasers, discrete components in nanoelectronics, qubits for quantum information processing, and enhanced ultrastable fluorescent labels for biosensors to detect, for example, cancers, malaria or other pathogens, and to do cell biology. We are working with the NIST Physics Laboratory to develop computationally efficient large scale simulations of such nanostructures. We are also working to develop immersive visualization techniques and tools to enable analysis of highly complex computational results of this type.

James Sims

We study the electrical and optical properties of semiconductor nanocrystals and quantum dots such as the pyramidal dot shown in Fig. 1. We also study more complex nanocrystal structures, with the nanocrystal coordinated with capping molecules and functionalized with linker molecules, and nanodevice architectures formed by linking together complex dot structures, also shown in Fig. 1. In the most complex structures this entails modeling on the order of a million atoms. Highly parallel computational and visualization platforms are critical for obtaining the computational speeds necessary for systematic, comprehensive study of such structures.

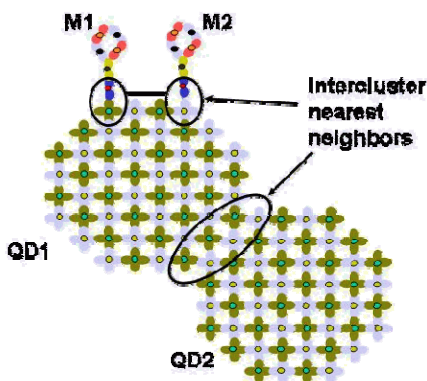
**Parallelization.** Often it is easy to define the simple nanosubsystems that make up a complex, heterogeneous nanosystem. However, it may be difficult to explicitly define the entire structure. A novel feature of our code is the ability to link together heterogeneous nanostructures (also referred to here as nanosubsystems). For example, when a nanoparticle nanostructure includes conjugating and linker molecules, these molecules can be assigned separately to different computational nodes to take advantage of the parallelization. If the nanosystem includes multiple smaller



**Figure 1.** A pyramid structure and a double pyramid structure of InAs quantum dots embedded in GaAs. The surrounding matrix of GaAs is not shown, but would be included in calculations. Coupling between InAs dots is done through the intervening GaAs matrix.

nanosubsystems linked together, then each smaller nanosubsystem can be parallelized on a different set of nodes with only minimal communication required between different nodes. Since we can do multiprocessor runs routinely, we have the basic building blocks for making larger structures by “stitching” together disparate subsystems into composite structures, each separate subsystem to be stitched together being a smaller multiprocessor run. The basic idea is to consider each smaller nanosubsystem as its own cluster, using the same input data as before, but at each iteration in the computation, information about atoms in the cluster that are intercluster neighbors (see Fig. 2) has to be distributed to the appropriate processors for the neighboring clusters, thereby “stitching” the calculations on the nanosubsystems in the heterogeneous structure together.

Now that we can routinely model nanosystems, our focus has shifted to modulating and controlling the optical properties of these self-assembled quantum dots using external strain which is modeled using an em-



**Figure 2.** Illustration of intercluster nearest neighbors in a nano-system with four subsystems: two quantum dots (QD1 and QD2) and two conjugating molecules (M1 and M2).

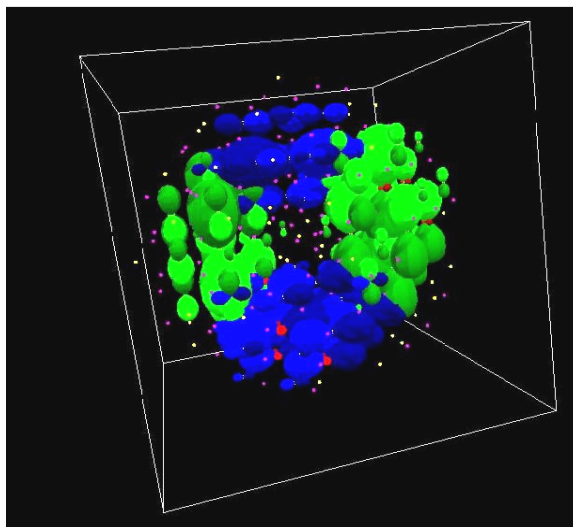
pirical valence force field. External strain leads to an internal lattice relaxation which manifests itself in a modification of the electron and hole states which are computed for the quantum dots. In this way the optical properties of the quantum dots are modified. A paper on this new development has been recently delivered at the Material Research Society meeting in Boston [3].

**Visualization.** Visual models of laboratory experiments and computational simulations to explore the nanoworld can be critical to comprehension. However, increasing amounts of data are being generated. For example, in one of our calculations, the region considered has nearly 700,000 atoms. Since each atom has 5 orbitals, there are 3.5 million pieces of data to describe one state. Both high performance computing and experiment must be augmented by high performance visualization. At NIST our visual analysis capabilities include both coarse grain capabilities and finer grain capabilities (which are more demanding of CPU and visualization resources), as well as static graphical representations and fully 3D immersive capabilities.

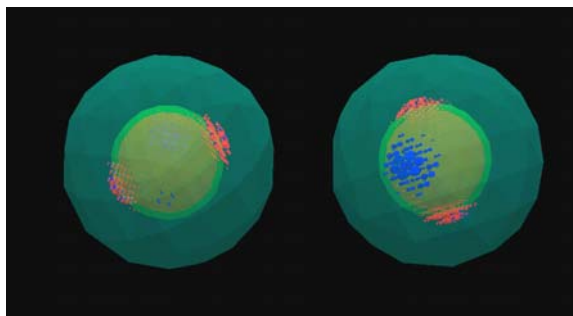
In our quantum dot simulations we visualize the atomic scale structure of the lattice and the charge density of the electrons and holes at both the fine grain and coarser grain levels. At the finer grained level, we visualize the charge density. For example, by displaying the contribution of  $s$  and  $p$  orbitals to the charge distribution of an eigenstate of a triple quantum dot structure, we are able to visualize when and how tunneling occurs between the structures and what orbitals are involved.

Finer detail can be represented in our visualizations. Fig. 3 shows the charge density of the lowest hole state in a CdS nanocrystal. In this case, much greater detail is apparent. The contributions from  $p_z$  orbitals (green) and  $p_x$  orbitals (blue) are shown. The contributions of

$p_y$  and  $s$  orbitals are not visible in this example. The orbitals are centered on the corresponding atom. The shape, size, and color represent the orbital type and the magnitude of its contribution. The different colors of the orbital lobes (for example, lighter and darker blue for  $p_x$ ) indicate the phase of the orbital. In this way, complete information about electron and hole states can be obtained. For example, state symmetries can be discerned immediately from these visualizations. Such symmetries are more difficult to discern otherwise.

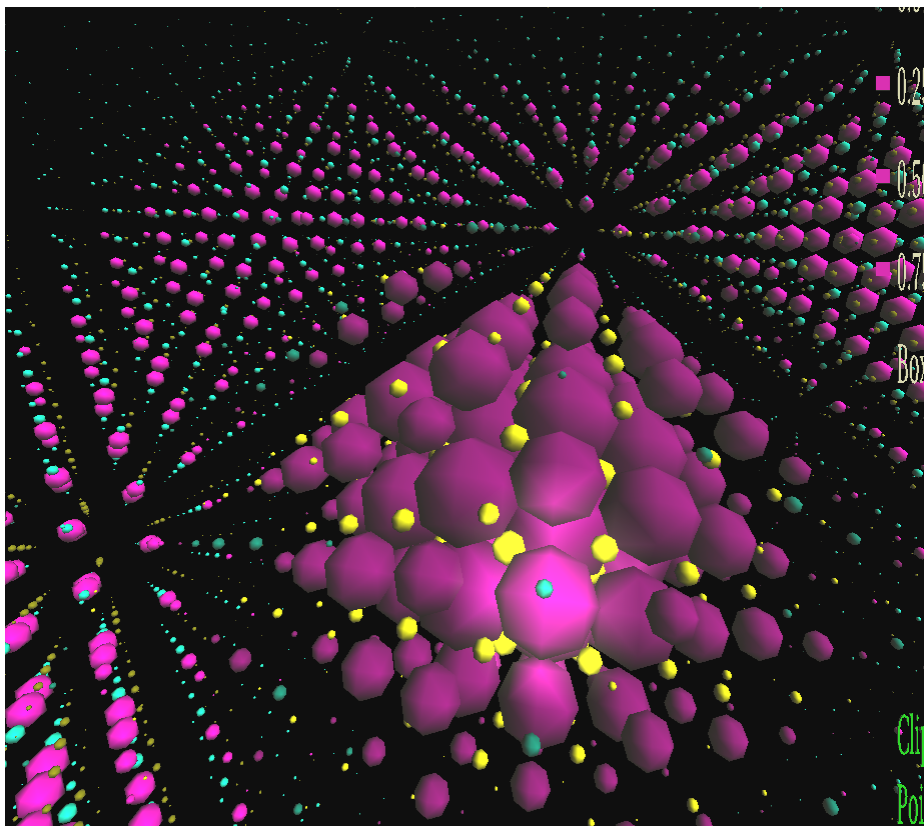


**Figure 3.** Charge density of the lowest hole state in a CdS nanocrystal.



**Figure 4.** Two different views of atomic state density of an electronic state trapped in the well region of a nanoheterostructured nanocrystal.

Even for these examples, the amount of data to be visualized can be prohibitive. Coarser grained visualizations can avoid that problem. Fig. 4 shows contours and transparent surfaces which illustrate charge densities in a coarser grained way. The figure shows the atomic scale charge density of an electronic state trapped in the well region of a CdS/HgS/CdS core/well/clad nanoheterostructured nanocrystal.



**Figure 5.** Snapshot from an immersive visualization of a quantum dot. The spheres represent  $s$  orbitals, which also are representative of the atoms in the structure.

We can do much more with the output of our nanostructure calculations. Our visual analysis capabilities include an immersive environment that allows scientists to interact with data by navigating through a three-dimensional virtual landscape of the data rather than by simply viewing pictures of the data. Our nanostructure calculations output detailed charge distributions which are transferred to the NIST immersive environment where they can be studied interactively. One can move through space, going inside the structure and moving around inside the structure. In this way one can visualize the structure looking in from the outside, or looking out from the inside. One can visualize both the nanostructure (see, for example, Fig. 5), and the atomic scale variation of calculated nanostructure properties from any orientation and position in space. This is not possible with any static graphical representation.

Such representations are tremendously helpful. They encapsulate the physics and allow one to easily see features that might be missed by just perusing the voluminous output from a supercomputer size calculation. Such insights are very helpful and greatly speedup the extraction of useful understanding and insights as we explore the properties of new and unfamiliar systems.

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James S. Sims, William L. George, Terrence J. Griffin, John G. Hagedorn, John T. Kelso, Marc Olano, Adele P. Peskin, Steven G. Satterfield, Judith Devaney Terrill (MCS D); Garnett Bryant (NIST PL)

<http://math.nist.gov/mcsd/savg/vis/nano/>

## Error Correction for Electromagnetic Motion Tracking Devices

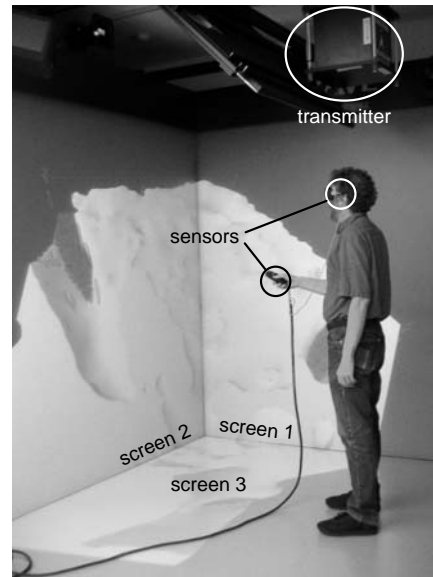
*MCSD researchers have developed algorithms for correcting both location and orientation errors in motion tracking devices. Such devices are used in a variety of fields such as immersive visualization, military, and medical applications. Positional errors in the data produced by these tracking devices compromise their utility. We present techniques for measuring and correcting these errors. In particular we use a method for interpolating orientation corrections that has not previously been used in this context. This method, unlike previous ones, is rooted in the geometry of the space of rotations. It is used in conjunction with a Delaunay tetrahedralization to enable both location and rotation correction based on scattered data samples. Our results show large improvements in both types of errors while imposing minimal computational burden.*

**John Hagedorn**

Motion tracking devices are used in a wide variety of applications. At NIST we use an electromagnetic motion tracking system as a critical part of our immersive visualization environment (Fig. 1). Motion tracking is essential because the location and orientation of the user's eyes must be tracked continuously so that the system can render images of a spatially stable virtual world, in stereo, and in real-time. In addition, motion tracking is also used on hand-held devices that operate as tools in the virtual world.

Fig. 1 illustrates several important components of the environment: three screens that provide the visual display, an electromagnetic motion tracker transmitter, and sensors. The screens are used to display a single three-dimensional scene. Motion trackers are very commonly used in such systems. Unfortunately, errors in motion tracking have substantial deleterious effects, such as: virtual objects move inappropriately as the user moves; straight lines appear bent when they cross screen boundaries; and virtual objects tied to the tracked hand-held device appear incorrectly positioned.

Fig. 2 illustrates one of these effects. Here, the grid lines should all be straight. To the user in the immersive environment, the lines appear bent at the points where they cross the boundaries between screens because the images are being drawn based on an incorrect tracked location for the eyes of the observer. This figure is based on actual errors observed in the motion tracking system at NIST. It is by no means the worst case that could have been provided. In informal observations made before initiating this project, we observed location errors in excess of 50 cm and orientation errors that appeared to be more than 15 degrees.

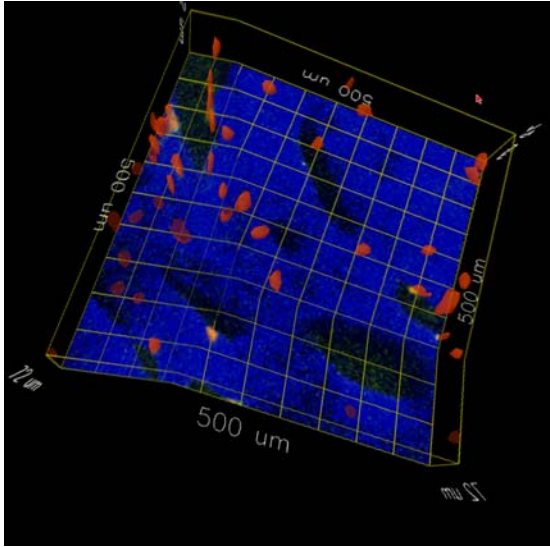


**Figure 1.** The NIST immersive visualization system. A single 3D scene is being displayed across the three screens. Note the tracker transmitter, a tracker sensor on the user's stereo glasses, and another sensor on a hand-held pointing device.

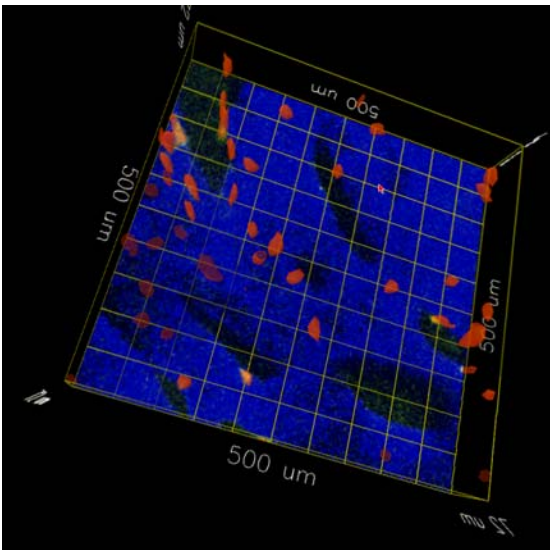
Our approach to correcting the tracker was to collect data at known locations and orientations and then to use these data to construct functions that represent the error [1]. This approach was simplified by verifying that errors were dependent on location, but not on orientation. This enabled us to construct correction functions based on measurements at a large number of locations using a fixed orientation at each location.

Our correction method is distinguished from prior work partly in our handling of the interpolation of orientation corrections. Our orientation interpolation method works entirely within the space of rotations and does not assume that the space of rotations is Euclidean. We use a quaternion representation of rotations, and we interpolate orientation corrections directly from measured orientation errors.

To correct the raw tracker data, we first record the tracker's measurements at a large set of known locations (and a fixed orientation) that encompass the volume that we need to accurately track. This enables us to calculate corrections at each of these points. We then perform a Delaunay tetrahedralization of the points based on the measured locations. Then, in real time, as the tracker reports each location and orientation, we find the tetrahedron that contains the measured location and generate barycentric coordinates for this location relative to the containing tetrahedron. The barycentric coordinates (which sum to 1 by construction) are used as weights for averaging the corrections at the vertices of the containing tetrahedron.



**Figure 2.** Distortions due to tracker miscalibration. The grid lines should be straight; they bend at the points where they cross the boundaries between screens in the immersive environment.



**Figure 3.** The scene shown in Fig. 2 with tracker data corrected by the methods described here.

For orientation averaging, we use these weights with a spherical weighted averaging technique [2] to average the correction rotations at each of the four vertices of the tetrahedron. This use of barycentric coordinates with spherical weighted averaging has a much clearer geometric rationale than previous methods.

In order to validate our methods, we collected raw tracker data at a second set of known locations and orientations; we refer to these as the *validation points*. We apply the correction algorithm to the validation points and compare the corrected data to the true locations and orientations. Table 1 reports the results. We see a 95.5% reduction in location errors and an 87.0% reduction in orientation errors. These improvements,

as best we can determine, equal or substantially surpass previous motion tracker correction methods.

	Location Errors		Orientation Errors	
	Ave	Std Dev	Ave	Std Dev
<b>Uncorrected</b>	37.51	19.30	19.57	8.96
<b>Corrected</b>	1.69	1.30	2.55	0.63

**Table 1.** Location errors (cm) and orientation errors (in degrees) for validation points before and after applying corrections.

When we apply this correction to the tracker data in our immersive visualization environment, the difference is clear to the user. Objects that should be stable appear to be stationary as the user moves through the virtual scene, the displayed pointer tracks the tracked hand-held device accurately, and there are no visual artifacts when objects cross the divisions between screens. The real-time correction causes no significant performance degradation of the interactive system. Fig. 3 shows the scene depicted in Fig. 2 after correction of the viewer's tracked position with our method.

Bringing together the use of spherical weighted averages with Delaunay tetrahedralization and barycentric coordinates provides a valuable approach to correcting tracker data based on samples at scattered points. The correction methods described here are in daily use in our immersive visualization environment and have yielded substantial improvement to the immersive experience. In addition to the qualitative benefits of this correction, this effort is an important step toward the assessment of uncertainty of virtual measurements of models and experimental data that are made in the interactive immersive visualization environment [3].

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## Participants

J. Hagedorn, S. Satterfield, J. Kelso, W. Austin<sup>5</sup>, J. Terrill, A. Peskin (MCSD)

<http://math.nist.gov/mcsd/savg/vis/tracker/>

<sup>5</sup> Student, Jackson State University

## Automated Combinatorial Testing for Software Systems

Most often, outages in modern business, industrial, medical, scientific, and transport systems are caused by unexpected faults in the underlying software, which is becoming increasingly complex. In complex software, failures are often the result of interaction bugs. An interaction bug is a fault that causes failure only when particular values of certain input parameters are specified in combination with particular values of other parameters. Interaction bugs may remain dormant until the unfortunate combination of parameter values is encountered in practice. Combinatorial testing is an approach to detect interaction bugs. Generally, combinatorial testing is used in functional or black-box testing where specifications of the functionality of the software system are given. It may also be useful in structural or white-box testing (i.e., when information about the software architecture and the internal structure is available). Much of the recent practice of combinatorial testing is focused on detecting interaction bugs involving two parameters. Many interaction bugs do involve two parameters only; however, a NIST investigation of actual faults suggests that up to six parameters do occur in practice. This NIST/ITL inter-divisional project has produced several algorithms and a combinatorial testing tool that advance the technology of combinatorial testing for complex software systems from detecting interaction bugs involving two parameters to six or more parameters.

### Raghu Kacker

Combinatorial testing is a relatively new approach, becoming popular beginning in the 1990s, for testing software systems. The initial focus was on pair-wise (2-way) testing in which all interaction bugs involving two parameters are sought. A NIST study [1] of actual faults in medical devices, browsers, servers, and a NASA application indicated that about 95 % of interaction bugs involved four or fewer parameters and no faults involved more than six parameters (Table 1). Thus, while interaction bugs typically involve a relatively small number of parameters, 2-way testing may not be adequate. On the other hand, a  $t$ -way testing strategy, for  $t$  from 2 to 6, may be adequate for many practical applications. The goal of this project is to advance the technology from pair-wise to multi-way testing and to demonstrate successful application to one or more applications.

The first step in combinatorial testing is to map the problem of detecting interaction bugs to a combinatorial framework. The parameters to be tested are defined. A finite subset of the (possibly infinite num-

ber) of input values is selected as test values. The number of test values for a parameter is its domain size. A test run can then be represented as a row consisting of one test value for each parameter. If there are  $k$  parameters with domain sizes  $v_1, v_2, \dots, v_k$ , respectively, then the test space consists of  $v_1 \times v_2 \times \dots \times v_k$  test runs (rows). Some knowledge of the functionality or of the structure of the software system is needed to specify the parameters and their test values such that the test space includes potential interaction bugs. Even for modest software the number  $v_1 \times v_2 \times \dots \times v_k$  (size of test space) could be very large to exercise all test runs in the test space. A combinatorial test suite is a subset of test runs selected from the test space such that all  $t$ -way combinations between the  $k$  parameters are exercised, for a chosen value of  $t$ .

Parameters	Cumulative percent of actual faults			
	M	B	S	N
1	66	29	42	68
1 - 2	97	76	70	93
1 - 3	99	95	89	98
1 - 4	100	97	96	100
1 - 5	100	99	96	100
1 - 6	100	100	100	100

**Table 1.** Cumulative distribution (expressed as percent) of the number of parameters involved in actual faults which occurred in software in medical devices (M), browsers (B), servers (S), and a NASA application (N)

**Covering arrays.** A covering array of strength  $t$  is a subset of  $N$  rows out of  $v_1 \times v_2 \times \dots \times v_k$  rows (test runs) that includes, at least once, each possible  $t$ -way combination of the test values of every possible subset of  $t$  parameters out of the  $k$  parameters. If  $t$  is less than  $k$  then the covering array size  $N$  is a fraction of the size of the test space. Table 2 shows a covering array of strength  $t = 3$  for  $k = 10$  where each parameter has  $v = 2$  test values (indicated by 0 and 1). The size of the test space is  $2^{10}$ , i.e., 1024 test runs would be necessary to exhaustively run all combinations of input parameters. Yet  $N = 13$  test runs include all 3-way combinations. (Note that there are 960 3-way combinations for ten 2-valued parameters). Thus, a test suite of 13 test runs based on this covering array will exercise all 3-way combinations among the values of  $k = 10$  parameter each having  $v = 2$  test values.

Construction of covering arrays of strength  $t$  (for  $t = 2, \dots, 6$  or more) with  $N$  as small as possible for practical number of parameters  $k$  and domain sizes  $v_1, v_2, \dots, v_k$  is a challenging problem. The state-of-the art in combinatorial mathematics deals with the special case in which each parameter takes on the same number of

values, i.e.,  $v_1 = v_2 = \dots = v_k = v$ , and even then yields covering arrays of minimum possible size  $N$  only for very few special values of  $k$ ,  $v$ , and  $t$ . In devising computational methods one must determine the entry in each cell such that the combinatorial property of the covering array is satisfied, but doing so with the smallest possible value of  $N$  is a difficult combinatorial optimization problem.

Collaboration between NIST/ITL and the University of Texas at Arlington has led to a tool, called FireEye, to generate covering arrays. FireEye [2] includes several algorithms. The basic algorithm, called IPOG, is described in [3]. The principle performance criteria for constructions of covering arrays are that the covering array size  $N$  should be as small as possible and the time taken for construction should also be as small as possible. On both criteria, FireEye using IPOG performs better than other publicly available tools. We are continually improving the algorithms. A faster version of IPOG, called IPOG-D, is described in reference [4]. Another algorithm, called Paintball, which can use a cluster of processors, is under development. A refinement of IPOG, called IPOG-F, is also under development. Using IPOG-F, a catalog of covering arrays of smaller covering array size  $N$  than indicated in the literature is being developed [5].

Combinatorial testing based on covering arrays generated using IPOG has also been shown to be useful for reachability testing in concurrent (parallel processing) programs [6]. We are investigating approaches to extend known covering arrays in various directions such as changes in domain sizes, increase in number of parameters, and increase in strength.

Rows	Parameters									
	1	2	3	4	5	6	7	8	9	10
1	0	0	0	0	0	0	0	0	0	0
2	1	1	1	1	1	1	1	1	1	1
3	1	1	1	0	1	0	0	0	0	1
4	1	0	1	1	0	1	0	1	0	0
5	1	0	0	0	1	1	1	0	0	0
6	0	1	1	0	0	1	0	0	1	0
7	0	0	1	0	1	0	1	1	1	0
8	1	1	0	1	0	0	1	0	1	0
9	0	0	0	1	1	1	0	0	1	1
10	0	0	1	1	0	0	1	0	0	1
11	0	1	0	1	1	0	0	1	0	0
12	1	0	0	0	0	0	0	1	1	1
13	0	1	0	0	0	1	1	1	0	1

**Table 2.** A covering array of 13 rows includes all eight triplets (000, 001, 010, 011, 100, 101, 110, and 111) between two possible values (0 and 1) for every three of the 10 parameters represented by columns (for example, see colored entries)

**Test oracles.** A covering array of strength  $t$  yields a combinatorial test suite for  $t$ -way testing. The next task is to determine the expected correct output of each test run against which the actual output may be compared. A test suite along with the correct output for each test run is the test oracle. We are investigating use of the model-checking tools, such as NuSMV (initially developed by Carnegie Mellon University and then improved by others), to create a test oracle. Determination of the expected correct outputs for test runs requires either complete specification of the functionality, a reference implementation of the software, or some model for the software.

We are investigating application of combinatorial testing for assurance of access control systems and for firewall policy testing. In these applications, functional specifications are available to construct test oracles. Other potential applications include communication protocol and process control systems. In these, specifications using finite state automata are common and could be used in constructing test oracles. We are also investigating the integration of our combinatorial test methods with modeling tools such as SIMULINK.

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## Participants

Raghu N. Kacker, Jeff Yu Lei, James F. Lawrence, Michael Forbes (MCSU); D. Richard Kuhn, Vincent Hu, Richard M. Ravello (NIST ITL); Tao Xie (NCSU); Renee Bryce (UNLV); Sreedevi Sampath (UMBC), Sagar Chaki, Arie Gurfinkel (CMU)

## Math Search

*As digital libraries of mathematical and scientific contents become widely available, it is essential to have search systems that empower users to search not only for text but also for equations and other mathematical constructs. To do this, the system must be math-aware, that is, it must recognize math symbols and structures in queries and contents, and it must present search results in a way that facilitates finding the desired information rapidly. We have developed a math-aware search system for the NIST Digital Library of Mathematical Functions (DLMF). This search system is general enough to be easily adapted to other math digital libraries.*

### Abdou Youssef

When it is released in 2008, the NIST Digital Library of Mathematical Functions (DLMF) will be a freely available, interactive, online resource providing reference information on the special functions of applied mathematics. As such, it is designed to be a modern successor to the *Handbook of Mathematical Functions* published by NBS in 1964 [1]. This classic handbook has become an indispensable resource for those doing research in the physical sciences and engineering. With nearly a million copies in print, the *Handbook* has become the most cited work in the mathematical literature. The DLMF is expected to become the new authoritative reference work on this subject. Updated to reflect developments in applied mathematics and computer science in the ensuing 40+ years, the DLMF will contain more than twice as much the technical material as the original *Handbook*.

As a mathematical reference work built on the same general model as the *Handbook*, the DLMF will contain some 36 chapters with mathematical definitions, identities, relations, information on computational methods and software, graphs, tables, and extensive references, but very little traditional text. To provide online support for users to locate the equations and expressions they need, the DLMF search system must be able to recognize mathematical symbols and structures, a requirement that is fundamentally different from Google-like text search. Field-based search systems have been built for math content providers, such as Zentralblatt [5] and MathSciNet [6], but they are based on text search and are unable to recognize mathematical notation. What is needed in all these cases is a math-aware, fine-grained, general-purpose search system. We have pioneered such a system for the DLMF [2, 3], which stands as the most advanced math search system to date. This tool is intended for

students, educators, researchers, and professionals in mathematics, physical sciences, and engineering. With minor adaptations, it is deployable by math/science publishers, professional societies, and other public and private math/science contents providers.

**Features of Math Search.** The following are essential components and features that we believe math search systems must have.

- *Math awareness.* This is the ability to recognize mathematical notation and structures, both in user queries and the digital library contents being searched. For example, the symbols “ $-$ ” and “ $/$ ” in “ $x-y/z$ ” are recognized as the subtraction and division operators (text search ignores such symbols), and the “ $2$ ” in “ $x^2$ ” is recognized as the power of  $x$ . (See Fig. 1.)
- *Query language and processing.* Users should be able to express their queries easily and intuitively, and the system must recognize the user’s intent, and process the query to satisfy that intent. In particular, the user’s query can be math fragments, where much information is implicit or expressed in wildcards. DLMF search analyzes the query and transforms it to a more explicit form that can be searched for effectively.
- *Ranking of search results.* To locate the needed information among hits, hits must be rank-ordered by relevance not only to the query but also to the general needs of math users. Math-specific factors unbeknown to text search ranking such as definitions, theorems, proofs, and names of certain mathematical concepts, carry more weight than other types of contents. Ranking of hits by the DLMF search engine takes such factors into account. (See Fig. 2.)
- *Hit description.* Each hit must be accompanied with a descriptive, query-relevant summary of the contents. The summary can be a combination of equations, graphs, portions of tables, or text. The DLMF search provides this important feature.

DLMF search has other features. These include specifying types of hits and highlighting math keywords (see Fig. 3). Also, we have enriched the math contents with metadata to enhance the ability of search systems to find relevant matches.

In the future, math search will be used in other applications and extended in different directions [4]. For example, it can be used for finding similarity of patterns and thus for scientific data mining (knowledge discovery). It can be synergistically combined with





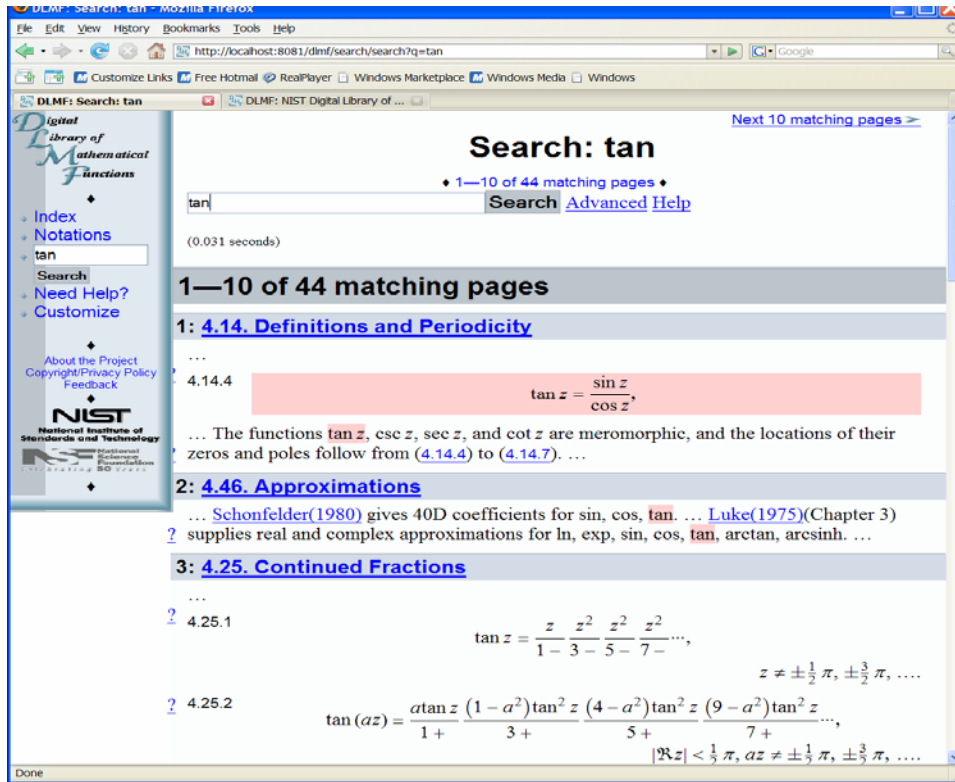


Figure 2. Search results of query “tan” (for the tangent function), showing good ranking and informative hit-description.

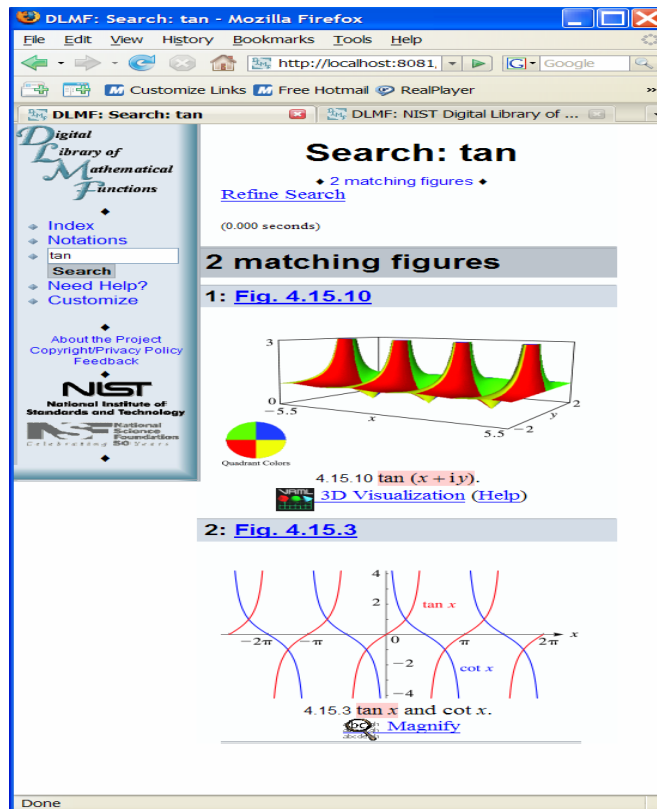


Figure 3. Limiting the search to graphs. It also illustrates highlighting of the search keyword “tan”.

**Part III**

# **Project Summaries**



## Mathematics of Metrology

### Computable Error Bounds for Delay Differential Equations

David Gilsinn  
Sita Ramamurthi

See feature article, page 25.

### The Lipschitz Exponent as an Image Metrology Tool

Alfred Carasso, MCSD  
Andras Vladar (NIST MEL)

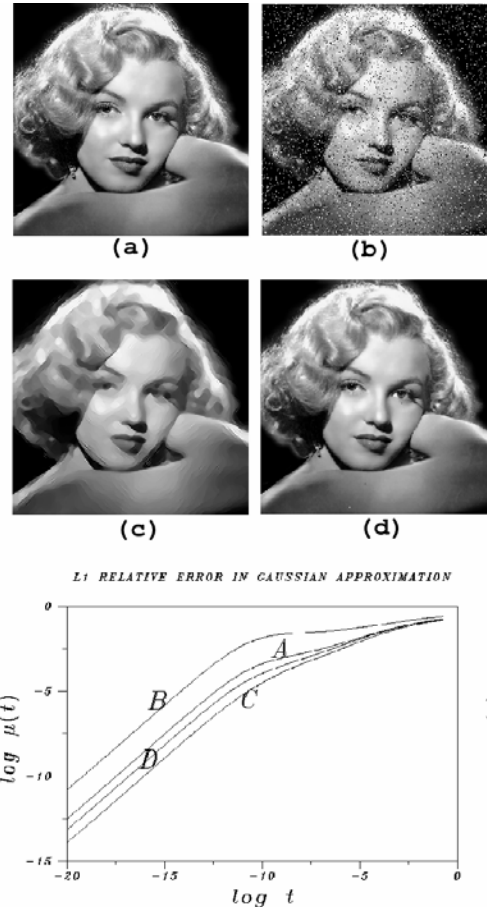
Recent work by A. Carasso and A. Vladar, to appear in *Optical Engineering*, further develops the notion of Lipschitz exponents by applying it to several areas of image analysis. This important MCSD image metrology tool can be helpful in both hardware and software applications. As a hardware tool, it can be used to quantify and monitor the performance of such imaging systems as electron microscopes, where the shape of the electron beam deteriorates over time. In recent years, digital image restoration has become pervasive in science and engineering. Lipschitz exponents can be used to evaluate and rank order the performance of competing image restoration algorithms.

The Lipschitz exponent  $\alpha$  of an image, where  $0 < \alpha < 1$ , measures the degree of fine structure and other non-differentiable features in an image. Images that are of bounded variation, or smoother, have  $\alpha = 1$ . The value of  $\alpha$  decreases systematically with increasing image roughness. Most natural images are not of bounded variation, and often have  $\alpha$  values less than 0.5. The value of  $\alpha$  changes when an image is degraded. The behavior of  $\alpha$  when that image is restored by various procedures is of prime interest, as it indicates the extent to which significant fine structure has been recovered.

The Lipschitz exponent can be found by convolving the given image,  $f(x,y)$ , with successively narrower Gaussians, to form the sequence of blurred images  $G_t f$ , as  $t$  tends to zero. Here  $t$  is a width parameter, and  $G_t f$  tends to  $f$  as  $t$  tends to zero. The slowness with which this happens is indicative of the non-smoothness of  $f(x,y)$ . Let  $\mu(t)$  denote the  $L_1$  relative error in approximating  $f$  by  $G_t f$ . The value of  $\alpha$  can be found by plotting  $\log(\mu(t))$  vs  $\log t$ , as  $t$  decreases from  $t=1$ , and evaluating the slope of that curve in the “slowly varying” region immediately to the left

of  $\log t=0$ . A NIST patent covering this methodology is currently being processed.

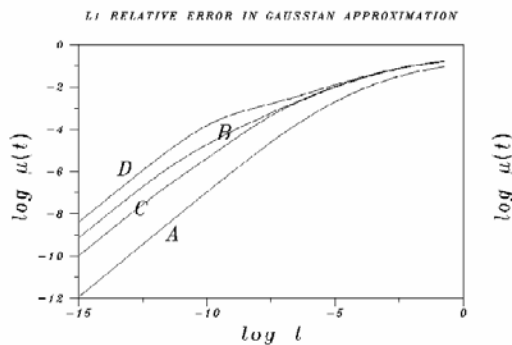
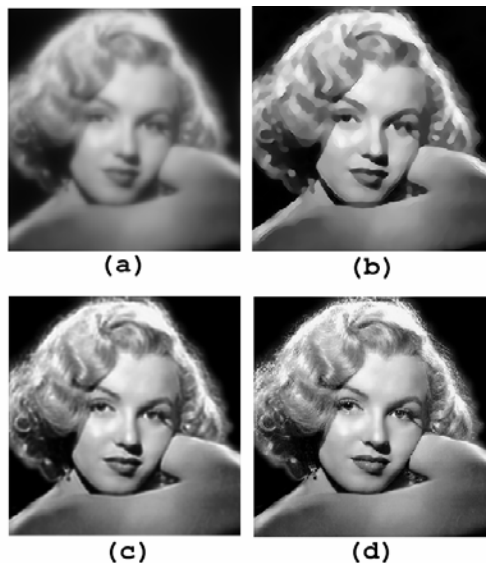
The experiments in Figs. 1 and 2 deal with synthetically degraded images, and the  $\mu(t)$  vs  $t$  traces A, B, C, D correspond to images (a), (b), (c), and (d) respectively. In both these figures, Lipschitz exponents were obtained by estimating trace slopes on the interval  $-7 \leq \log t < 0$ .



**Figure 1.** Image Denoising. Noise addition can artificially lower Lipschitz exponent  $\alpha$ , while some noise removal algorithms can eliminate texture and increase  $\alpha$ . Traces A, B, C, and D correspond to images (a), (b), (c), and (d) respectively. Exponents  $\alpha$  obtained by estimating trace slopes on  $-7 \leq \log t < 0$ .

Fig. 1 involves noising and denoising the 512 x 512 Marilyn Monroe image. The original image (a) has trace A with  $\alpha = 0.591$ . Salt and pepper noise was added to produce image (b) with trace B and  $\alpha = 0.302$ . Two distinct denoising methods were examined. The ‘total variation’ method produced image (c), where a good deal of texture has been eliminated along with the noise. This led to a substantially larger  $\alpha = 0.714$  in trace C. The second denoising method used

was 2D median filtering in image (d). This is a good approximation to the original, and trace  $D$ , with  $\alpha = 0.645$ , is closer to trace  $A$  than is trace  $C$ .



**Figure 2.** Image Deblurring. Not all deblurring algorithms are equally effective at recovering image texture

Our second example, summarized in Fig. 2, involves blurring and deblurring the Marilyn Monroe image. Fig. 2(a) with trace  $A$  and  $\alpha = 0.887$  results from synthetic blurring of Fig. 1(a) by convolution with a Lorentzian density. Blurring without adding noise increases  $\alpha$ , as blurring is generally a smoothing operation. Three mathematically distinct methods of deblurring image (a) are examined. The Marquina-Osher total variation method produces image (b) with trace  $B$  and  $\alpha = 0.695$ , higher than the original value of  $0.591$ . Image (c) with trace  $C$  and  $\alpha = 0.714$ , results from 200 Lucy-Richardson iterations. Both of these procedures smooth out the image and fail to recover fine structure. Image (d) with trace  $D$  and  $\alpha = 0.616$  is quite close to the original. It was produced using the “slow evolution from the continuation boundary” (SECB) procedure.

Use of Lipschitz exponents will play a significant role in ongoing NIST research. State of the art

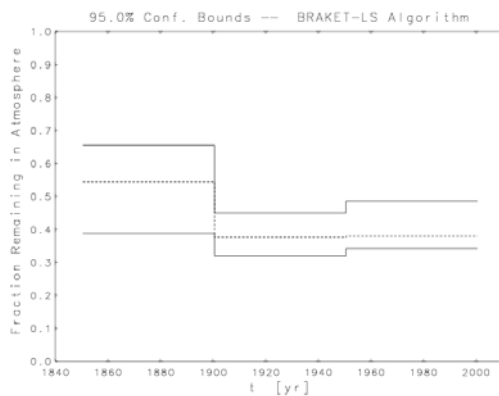
software tools, such as Caltech curvelet denoising, Mumford-Shah regularization, and Bremen minimum-norm blind deconvolution can be evaluated and applied to NIST problems.

## Systems Identification and Parameter Estimation

*Bert W. Rust*

Identifying a system of ordinary differential equations (ODEs) describing the dynamical relationships between (1) man-made carbon dioxide emissions  $P(t)$ , (2) atmospheric carbon dioxide concentrations  $c(t)$ , and (3) global temperatures  $T(t)$  would provide a useful tool for evaluating mitigation strategies for global warming. Last year I demonstrated that changes in  $T(t)$  vary linearly with changes in  $c(t)$  and that the warming is accelerating. That acceleration is driven by the ever increasing emissions  $P(t)$ . Attempts to model the  $c(t)$  measurements by assuming that a constant fraction of the emissions remain in the atmosphere failed because that fraction has apparently changed during the 151 year period for which measurements are available. The relationship between  $c(t)$  and  $P(t)$  can be modeled by an underdetermined linear system in which the annual  $P(t)$  measurements are used to form the matrix, the  $c(t)$  measurements are the elements of the right hand side vector, and the elements of the solution vector are the unknown annual values of the fraction remaining in the atmosphere. Unfortunately, the  $c(t)$  record has many gaps, so the matrix has dimensions  $83 \times 153$ . This problem would be hopelessly underdetermined were it not for two additional considerations: (1) the elements of the solution vector are constrained to lie between the values 0 and 1, and (2) it is not necessary to determine the fraction for each individual year, but rather is sufficient to determine average values over suitably chosen subintervals of time. O’Leary’s BRAKET-LS algorithm was used to compute these constrained averages and their confidence interval bounds. The results for three equally spaced subintervals of [1850, 2000] are shown in Fig. 1.

It is clear that a single value of about 0.377 will suffice for the whole twentieth century and that a statistically significantly higher value of about 0.545 is required for the earlier period. It is not clear that the jump from the higher to the lower value occurred exactly at epoch 1900.0, and future work will be directed toward a more accurate estimate of this threshold time. Future work on this project will also concentrate on refining the ODE for  $P(t)$  and on simultaneously fitting the solutions of all three equations to their respective time series.



**Figure 1.** The fraction of man-made carbon dioxide emissions that remains in the atmosphere. The dashed lines are the BRAKET-LS estimates of the average values on the subintervals  $[1850, 1900]$ ,  $[1900, 1950]$ , and  $[1950, 2000]$ . The corresponding solid lines define 95 % confidence intervals for the estimates. The interval bounds are not symmetrically spaced about the estimates because the elements of the solution vector were constrained by the calculation to lie in the interval  $[0, 1]$ .

## Sparse Representations in High Dimensional Geometry

Bradley Alpert  
Yu Chen (New York University)

Medical diagnostic systems often produce images that lack quantitative information or comparability across imaging systems, which can lead to difficulties in diagnosis and long-term management of disease that requires patient monitoring. Elaborate measurements are taken, digitally processed, then reported in essentially qualitative form. For MRI, functional MRI, and some other processes, formation of the images relies on filtering and Fourier transformation.

Although the computational recovery of functions from their Fourier representations is considered routine, aside from possible efficiency concerns arising from unequidistant data, standard approaches assume that the functions are smooth and can be recovered with the discrete Fourier transform (computed via the FFT). When this assumption fails, as is evident from Fourier data that are not small at the highest frequencies measured, some sort of attenuation, or bellring, scheme is typically used. This procedure tends to blur sharp features and, being more art than science, can lead to different functions (images) in different systems. Although this problem, and the Gibbs phenomenon, have received attention from mathematicians in recent years, recently developed methods tend to work well only in an asymptotic sense; they do not exploit available data efficiently.

Despite inherent limits on resolution that can be obtained from truncated Fourier data, a change of assumptions from *smooth* to *piecewise smooth* can lead to significantly improved recoveries. Procedures implementing this idea are not completely established even for functions (signals) in one dimension; they are yet more challenging in two and three dimensions, where discontinuities may be expected to occur along mostly smooth curves or surfaces. This constraint, which magnifies the advantage of the piecewise smoothness assumption, must be appropriately reflected in the methods used. Alpert and Yu Chen are conducting extensive numerical experiments to understand this environment and to develop reliable procedures for these problems.

A related, yet more general, challenge is parsimonious, or sparse, representation and recovery of functions under assumptions appropriate to an application. Although there is considerable current interest in the mathematical community in these problems ( $L^1$ -norm minimization, compressed sensing, sparse representation in high-dimensional geometry), and much recent progress (initiated in pivotal work by Candes, Romberg, and Tao) most of the methods being explored are limited to linear spaces. While linearity is a natural starting point, strong evidence suggests that image recovery cannot be done this way yet nevertheless is within reach.

The initial approach involves applying the sparse recovery methods, and experimenting with others, to Fourier data generated from numerical models of scatterers. The deficiencies of the resulting recoveries are characterized and point to ways that the representation space should be altered and the recovery procedures extended.

## Sequential Importance Sampling and the Markov Chain Monte Carlo Method

Isabel Beichl  
Francis Sullivan

The Markov Chain Monte Carlo Method (MCMC) has been studied by many researchers and an extensive theory has been developed. But getting quantitative answers to problems is still difficult because MCMC can be slow, and determining its rate of convergence is far from obvious. On the other hand, a less well-studied Monte Carlo method, sequential importance sampling (SIS), can sometimes be very fast but rigorous bounds on variance are lacking.

As one example, for the monomer/dimer problem Kenyon, Randall and Sinclair developed an MCMC method which has not been successfully used

for practical computation, while we have developed an SIS method and computed quantities of interest. So, the situation is: MCMC can be trusted but may be very, very difficult to use, whereas SIS gives a numerical answer, but it's hard to verify that the answer is correct. The research question is how to combine the best of both methods. We have recently developed the following.

1. A way to use our SIS method to reliably estimate optimal parameters such as fugacities (i.e., prob-

ability of accepting proposed moves) for MCMC, and so to avoid the trial and error aspect of deciding what fugacities to use.

2. A way to use the SIS method to calculate the mixing time for the MCMC method efficiently. The mixing time tells us the convergence rate and thus determines the number of steps that must be taken between samples.



## Quantum Information

### Making Optical “Schrödinger Cat” States

Scott Glancy  
 Emanuel Knill  
 T. Gerrits (NIST EEEL)  
 T. Clemment (NIST EEEL)  
 Sae Wo Nam (NIST EEEL)  
 Richard Mirin (NIST EEEL)  
 H. M. Vasconcelos (Universidade Federal do Ceará, Brazil)

**See feature article, page 28.**

**Funding:** NIST Innovations in Measurement Science program.

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### Quantum Computing with Ion Traps

E. Knill  
 D. Leibfried (NIST PL)  
 D. Wineland (NIST PL)  
 Ion Storage Group (NIST PL)

Quantum computers have the potential for significantly speeding up many useful algorithms. However, building quantum computers is challenging. Currently available quantum devices can realize computations with only a few quantum bits (qubits) and steps. Atomic qubits in ion traps are currently considered one of the leading candidates for realizing large quantum computers. We are collaborating with the Ion Storage Group on experiments to determine the suitability of ion traps for large scale information processing and to verify the basic principles of the needed quantum control. We are also participating in research on new approaches to realizing quantum information in ion traps.

To determine the quality of quantum control in the context of quantum information processing, we developed a randomized strategy for determining an effective error probability per quantum gate and implemented it with one-qubit gates in an ion trap. The basic idea is that it suffices to determine the increase in error probability of long sequences of gates as a function of the length of the sequence. Furthermore, because of what we know of fault-tolerant quantum architectures, it suffices to consider a special subset of gates for which the final answer can be efficiently predicted using classical computation. Using this strategy, we determined that the basic one-qubit gates in our test

configuration had an effective error probability of only 0.5%. Since the sources of the errors are well understood, we expect that this error probability can be greatly reduced by better stabilization of the needed lasers and other technological improvements. Once sufficiently high-quality two-qubit gates are available, we hope to repeat this experiment with two or more ion qubits.

One of the problems of the traditional scheme for manipulating the states of ion qubits is that it requires many independently and precisely controllable laser beams. We participated in an analysis of an alternative approach developed by D. Leibfried based on static laser beams where the manipulations are realized by moving ions. Since precise ion movement is required in any case, this has the potential for greatly reducing the complexity of ion trap quantum computers. The analysis shows that the necessary quantum gates can be implemented in parallel with sufficiently low error using static laser beams. Because the beams can be derived by multiple passes of a single beam, the power requirement is also reduced significantly.

One of the goals of our collaboration is to demonstrate so-called logical quantum information encoded in a quantum error-correcting code capable of correcting all one-qubit errors. Such a demonstration should include preparation of logical states, application of logical gates and measurement of logical information. The logical gates need to be performed with sufficiently low error. The technology needed for such a demonstration is currently being developed and tested.

- [1] E. Knill, D. Leibfried, R. Reichle, J. Britton, R. B. Blakestad, J. D. Jost, C. Langer, R. Ozeri, S. Seidelin, and D. J. Wineland, Randomized Benchmarking of Quantum Gates, arXiv:0707.1032, *Physical Review A*, to appear, 2007.
- [2] D. Leibfried, E. Knill, C. Ospelkaus, D. J. Wineland, Transport Quantum Logic Gates for Trapped Ions, *Physical Review A* **76** (2007), pp.032324/1—12.

**Funding:** Quantum Information ACI Initiative (2007).

## Quantum Computing Theory

Scott Glancy

Emanuel Knill

Adam Meier

Yanbao Zhang

R. Somma (LANL)

G. Ortiz (Univ. of Indiana)

The implementation of quantum computers is based on a substantial body of theoretical work showing the utility of quantum algorithms and providing techniques for protecting quantum devices from inevitable noise. Our contributions to quantum computing theory include work on better understanding the limitations as well as the power of quantum computers and better methods for measuring observables in quantum physics simulations on quantum computers.

One of the most promising applications of quantum computers is to the simulation of quantum physics. In most such simulations, the desired answer is the expectation of an observable. The simplest way to determine such an expectation with a given accuracy  $1/n$  is to run the simulation  $1/n^2$  times, make a von Neumann measurement of the observable each time and take the average of the answers. For sufficiently well understood observables, it was known that the resources needed could be reduced from  $1/n^2$  to  $1/n$  by taking advantage of quantum mechanical effects. We showed that essentially the same improvement is possible for any observable under mild assumptions. An important part of our algorithm for determining the expectation of an observable is to provide rigorous confidence intervals, where the efficiency of the algorithm is logarithmic in the inverse p-value associated with the confidence interval. This greatly improves the performance of the conventional measurement schemes based on phase estimation or the quantum Fourier transform, which require resources that grow linearly with the inverse p-value.

The applications of quantum information to communication include quantum cryptography and quantum secret sharing. Such applications make possible protocols that cannot be realized using only classical information processing. One reason for the power of quantum information in this setting is the presence of quantum non-locality, which are correlations with no classical analogue. Experiments that verify the presence of quantum non-locality have been performed, but are still subject to “loop holes”, that is, a reasonable but unverifiable assumption is required to ensure that there is no classical explanation for the data. Removal of the loop holes requires better detectors and/or better choices of experimental configurations. We are developing a computational framework based on information theory to compare and optimize experimental configurations. An impor-

tant part of the framework is a toolkit for statistical analysis of experimental data that can provide explicit p-values for rejecting all possible classical explanations for the data.

In previous years we have developed and simulated fault-tolerant quantum computing architectures that can tolerate surprisingly high error rates per quantum gate. This year, we have started to develop new simulation algorithms for fault-tolerant architectures. The goal of our effort is to greatly improve the efficiency of the simulations and to enable simulation of architectures based on quantum systems with more than two dimensions. So far we have implemented the C++ libraries for the basic operations of such quantum systems and for data structures needed to keep track of the necessary quantum gates and their errors. Once we have tested and refined the C++ libraries, we will use them to compare different architectures. Future research is aimed at simulations of universal gate sets and non-stochastic error models.

- [1] E. Knill, G. Ortiz, and R. D. Somma, Optimal Quantum Measurements of Expectation Values of Observables, *Physical Review A* **75** (2007), pp. 012328/1-13.

**Funding:** NIST Innovations in Measurement Science. Quantum Information ACI Initiative (2007).

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## Preparing Ancillary States for Quantum Computation

Bryan Eastin

The promise of quantum computing is unlikely to be realized without effective quantum error correction, but quantum error correction itself requires the application of quantum operations. To perform these in a robust manner it is necessary to utilize ancillary systems prepared in known quantum states. Below a certain threshold, the effective, that is, encoded, error rate decreases as the number of quantum systems in the encoding increases, but the difficulty of preparing the necessary ancillary states typically increases with the size of the encoding as well. Employing standard methods and codes, the direct implementation of even relatively small quantum encodings is impractical. In the literature on error thresholds for quantum computation, this problem is circumvented by employing a layered (or concatenated) approach to error correction and state construction. Codes and procedures that permit more direct state construction are intriguing, however, because they ought to require fewer quantum systems for their implementation.

In the coming year I plan to investigate new procedures and codes relevant to the construction of large ancillary states. With regards to new procedures,

I hope that the completion of my present work on inferring the location of propagated errors based on the measurement of complementary errors and knowledge of the preparation circuit will facilitate the construction of a broad class of quantum states. My coding research will focus primarily on low-density parity-check (LDPC) quantum codes, a class for which state preparation is dramatically simplified, but at the cost of less favorable code parameters. Both the development of new LDPC codes and more detailed error analyses of existing codes are included among my goals.

**Funding:** *NIST/NRC Postdoctoral Research Program.*

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## Adaptive Finite Element Modeling of Two Confined and Interacting Atoms

*William F. Mitchell*

*Marjorie A. McClain*

*Eite Tiesinga (NIST PL)*

We have applied the parallel adaptive refinement and multigrid finite element code PHAML (see feature article, page 23) to a two-dimensional Schrödinger equation in order to study the feasibility of a quantum computer based on extremely cold neutral alkali-metal atoms. Qubits are implemented as motional states of an atom trapped in a single well of an optical lattice. Quantum gates are constructed by bringing two atoms together in a single well leaving the interaction between them to cause entanglement. Quantifying the entanglement reduces to solving for selected eigenfunctions of a Schrödinger's equation that contains a Laplacian, a trapping potential and a short-ranged interaction potential. The behaviors of the eigenfunction due to the trapping potential and interaction potential

are on very different scales, which requires the use of adaptive refinement and high order finite elements.

A critical component of adaptive refinement algorithms is the a posteriori local error estimator, which is used to determine where the error is the largest, and hence which triangles should be refined to optimally reduce the error. Error estimators for elliptic boundary value problems were studied extensively in the 1980's and 1990's. The same error estimators are valid for elliptic eigenvalue problems like Schrödinger's equation. Moreover, a simple additional calculation gives an estimate of the error in the eigenvalue, too. We have added this capability to our code.

Use of high degree piecewise polynomials has proved to be crucial to get the high accuracy solutions required for correctly modeling the atom interactions. We are studying the use of a new technique, hp-adaptive refinement, to improve on this even further. With hp-adaptive refinement one adapts both the element size and polynomial degree locally. Properly done, this technique has a faster convergence rate than fixed-degree adaptive methods. Preliminary results with one strategy for hp-adaptivity look promising. We are continuing to study other strategies.

We have demonstrated the utility of our code for single-channel, time independent models through experiments in which we examined the effect of varying the scattering length, and of varying the trap aspect ratio. We have now extended the code to handle multi-channel problems. We solved a two-channel Feshbach model of potassium and performed experiments in which we varied the magnetic field surrounding the trapped atoms, and obtained results very close to a similar experiment of Paul Julienne (NIST PL). In the coming year we will further extend and examine the multi-channel capabilities, and begin studying time dependent models.

**Funding:** *Quantum Information ACI Initiative (2007).*

## **Fundamental Mathematical Software Development and Testing**

### **Parallel Adaptive Multilevel Finite Elements**

*William Mitchell  
Marjorie McClain  
Eite Tiesinga (NIST PL)*

See feature article, page 23.

### **OOF: Finite Element Analysis of Material Microstructures**

*Stephen A. Langer  
Andrew C.E. Reid  
Rhonald C. Lua (Penn State University)  
Valerie R. Coffman (Cornell University)  
R. Edwin Garcia (Purdue University)  
Olga Kuznetsova (University of Maryland)*

<http://www.ctcms.nist.gov/oof/>

The OOF Project, a collaboration between MCS and NIST Materials Science and Engineering Laboratory, is developing software tools for analyzing real material microstructure. The microstructure of a material is the (usually) complex ensemble of polycrystalline grains, second phases, cracks, pores, and other features occurring on length scales large compared to atomic sizes. The goal of OOF is to use data from a micrograph to compute the macroscopic behavior of the material via finite element analysis. OOF is intended to be a general tool, applicable to a wide variety of microstructures in a wide variety of physical situations.

This year the OOF team released six new versions of the OOF2 program: 2.0.1, 2.0.2, and 2.0.3, and three pre-release (alpha) versions of 2.0.4. These programs were downloaded 1,453 times from the OOF website. The final version of OOF1 accounted for an additional 675 downloads.

The OOF customer base continues to be broad. We received help requests from about 60 users in FY07, representing 17 domestic and 17 foreign academic institutions, 3 domestic and 3 foreign industrial laboratories, and 2 domestic and 1 foreign government laboratory. (Some users did not identify themselves and were not included in the statistics.)

New features introduced to OOF2 this year include the following.

**Subproblems.** A typical OOF2 problem is to solve for the value of one or more fields (temperature,

polarization, etc) at all points within a microstructure. OOF2 now can divide the job into subproblems, limiting the solution to a portion of the microstructure (just one material type, for example) or to a subset of the defined fields.

**Periodic Boundary Conditions.** Most real micrographs are not periodic, but simulated microstructures are often periodic. OOF2 can now generate a periodic mesh to perform calculations on periodic microstructures. Previous versions of OOF2 could use a periodic micrograph but could not guarantee that the finite element mesh or the computed fields would respect the periodicity.

**Automatic Mesh Generation.** The OOF2 user creates a finite element mesh and adapts it to fit the geometry of a microstructure by interactively applying a series of software tools. Version 2.0.3 introduced a method of doing this with very little user interaction. In the new method, the user specifies the length scales of the largest and smallest microstructural features of interest and a tolerance, and the program automatically applies a series of modification operations to generate a mesh that approximates the features. The method works well on a wide variety of microstructural geometries, as long as the features are distinctly delineated.

**Orientation Mapping.** Beginning with version 2.0.4, OOF2 has the ability to read orientation mapping data files. These files are created by electron backscatter diffraction (EBSD) experiments, and directly give the orientation of the crystal axes at points in a micrograph. Previously, OOF users had to invent orientations for the grains of a microstructure, or laboriously enter them by hand. Users can now start with the EBSD data instead of a conventional micrograph, and use actual orientations. OOF2 has built-in support for the orientation map file formats used by the two major suppliers of EBSD equipment, and can easily be extended to use other formats.

OOF2 is still under development. Current efforts are centered on solving for time-dependent and non-linear material properties. We have also begun work on OOF3D, which will compute three dimensional physical properties from three dimensional micrographs.

## Sparse BLAS Standardization

Roldan Pozo

Iain Duff (Rutherford Appleton Labs)

Michael Heroux (Sandia National Laboratory)

<http://math.nist.gov/spblas>  
<http://www.netlib.org/blas/blast-forum>

MCSD has played a leading role in the standardization effort for the Basic Linear Algebra Subprograms (BLAS) and continues to be a major contributor for the design and development of reference software and documentation. The BLAS are kernels for computational linear algebra subroutines comprising of fundamental matrix/vector operations common to most scientific computing applications. By standardizing such interfaces, computer manufacturers and software vendors can provide high-performance implementations especially suited to a specific hardware platform. By developing their applications in terms of BLAS, computational scientists can achieve high levels of performance and portability. The original BLAS, which were developed for dense vector and matrix operations from the late 1970s through the early 1990s, achieved this goal very well. To this, the BLAS Technical Forum (an international consortium of industry, academia, and government institutions, including Intel, IBM, Sun, HP/Compaq/Digital, SGI/Cray, Lucent, Visual Numerics, and NAG) formed an updated BLAS standard which addresses these extensions.

Among the most significant components of the updated BLAS standard is support for sparse matrix computations. R. Pozo of MCSD served as chair of the Sparse BLAS subcommittee during the standardization process, and NIST was first to develop and release a public domain reference implementation in ANSI C for early versions of the standard, which helped shape the final specification. After the standard was formally approved and accepted, the complete technical specification was published, and a special issue of the *ACM Transactions of the Mathematical Software* (TOMS) was devoted to the new BLAS standard, including a paper co-authored by R. Pozo and other subcommittee members providing an overview of the sparse matrix interface.

This year saw the development of a new C++ interface using abstract base classes, which define a specific interface and greatly simplifies the Sparse BLAS specification. The code interface is less than 600 lines of C++, yet captures the complexity vector and matrix operations with basic types (real and complex, single or double precision) and supports general types (e.g. intervals, multiprecision variables) beyond the original BLAST specification.

## TNT: Object Oriented Numerical Programming

Roldan Pozo

<http://math.nist.gov/tnt/>

NIST has a history of developing some of the most visible object-oriented linear algebra libraries, including Lapack++, Iterative Methods Library (IML++), Sparse Matrix Library (SparseLib++), Matrix/Vector Library (MV++), and most recently the Template Numerical Toolkit (TNT). This package has downloaded to several thousand developers and is currently in use in several industrial and commercial applications.

TNT incorporates many of the ideas we have explored with previous designs, and includes new techniques that were difficult to support before the availability of ANSI C++ compilers. The package includes support for both C and Fortran multidimensional arrays, vector, matrices, and application modules, such as linear algebra.

The design of TNT separates the interface specification from the actual implementation. This allows library developers to create specialized modules that take advantage of particular hardware platforms, utilize vendor-specific libraries, or implement different C++ strategies, such as expression templates, or instrumented versions for debugging sessions.

Developments in the latest design of TNT (v. 3.0.8) provide support for both multidimensional arrays and integrate a linear linear algebra module of fundamental algorithms (LU, Cholesky, SVD, QR, and eigenvalues), as well as sparse matrix support (with computational operations via the Sparse BLAS). Also developed this year were example codes to interface with LAPACK high performance linear algebra library.

The TNT web site provides a basic implementation for testing and development, as well as links to other library packages that utilize the TNT interface. Full documentation and source code for all TNT components are available on-line.

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## SciMark, a Web-based Benchmark for Numerical Computing in Java

Roldan Pozo

Bruce Miller

<http://math.nist.gov/scimark>

The NIST SciMark benchmark continues to be one of the most widely used Java scientific benchmarks and is in the process of being included in the new SPECjvm2007 benchmark. SciMark consists of computational kernels for FFTs, SOR, Monte Carlo

integration, sparse matrix multiply, and dense LU factorization, comprising a representative set of computational styles commonly found in numerical applications. SciMark can be run interactively from Web browsers, or can be downloaded and compiled for stand-alone Java platforms. Full source code is provided, in Java and C programming languages for comparison under different compilers and execution environments. The SciMark result is recorded as megaflop rates for the numerical kernels, as well as an aggregate score for the complete benchmark. The current results database lists submissions from more than 3,000 submissions from computational platforms ranging from palm devices to high-end servers, and contains reports from nearly every operating system

and virtual machine environment currently in use, including Solaris, FreeBSD, MacOS, Sun OS, IRIX, OSF1, Linux, OS/2, and Windows 95, 98, 2K, ME, NT, and XP.

SciMark and its kernel components have become a pseudo-standard in industry and academia. They were adopted by the Java Grande Benchmark Forum, Sun Microsystems used SciMark 2.0 to demonstrate the floating-point improvements to their JVM, and most recently are being included in in SPECjvm2007 benchmark.

As of January 2007, the record for SciMark is over 1 Gflops, with some of the kernel benchmarks (notably the LU factorization) running over 2 Gflops on a single-processor PC.

## Mathematical Knowledge Management

### Math Search

Abdou Youssef  
Bruce Miller  
Daniel Lozier  
Ronald Boisvert

See feature article, page 40.

**Associated ITL Program:** *Information Discovery, Use, and Sharing.*

**Funding:** *NIST Systems Integration for Manufacturing Applications (SIMA) program.*

### Digital Library of Mathematical Functions

Daniel Lozier  
Ronald Boisvert  
Joyce Conlon  
Peter Ketcham  
Marjorie McClain  
Bruce Miller  
Frank W. J. Olver  
Bonita Saunders  
Abdou Youssef  
Charles Clark (NIST PL)  
Gloria Wiersma (NIST PL)  
Qiming Wang (NIST ITL)  
Richard Askey (U. of Wisconsin, Madison)  
Michael Berry (U. Bristol, UK)  
Leonard Maximon (George Washington U.)  
Morris Newman (U. California, Santa Barbara)  
Ingram Olkin (Stanford)  
Peter Paule (J. Kepler U., Linz, Austria)  
William Reinhardt (U. Washington, Seattle)  
Nico Temme (CWI, Amsterdam)

30 authors under contract

25 validators under contract

<http://dlmf.nist.gov/>  
<http://dlmf-i.nist.gov/>

Mathematical functions, from the elementary ones like the trigonometric functions to the multitude of special functions, are an integral part of all modern developments in theoretical and applied science. They are used to model natural phenomena in fields from quantum theory to astrophysics, formulate problems and solutions in engineering applications, and support numerical computations. To make effective use of

mathematical functions, practitioners must have ready access to a reliable catalog of their properties.

Traditionally, in all fields of science, catalogs of relevant properties have existed in the form of massive published handbooks. These are still being produced and can be found on the desks of working scientists. An important example is the 1000-page Handbook of Mathematical Functions, edited by Abramowitz and Stegun, and published in 1964 by the National Bureau of Standards. Recently, however, the Web is showing great promise as a more advantageous method. A big potential advantage is that scientists can begin to integrate handbook data into documents and computer programs directly, bypassing the need for time-consuming and error-prone reentry of data, and by use of *metadata*, providing for much richness in Web interconnections, Web annotation, Web search, and so on. Another advantage is high-resolution graphics that users can rotate and view from any angle, giving them an unprecedented way of visualizing the complex behavior of mathematical special functions.

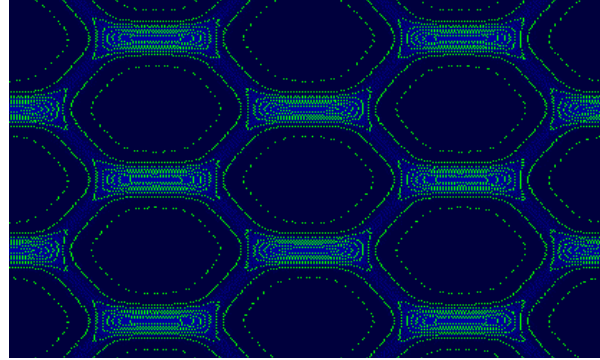
The Digital Library of Mathematical Functions has two main goals. First, we are reviewing the published literature on special functions, selecting the properties most relevant to current applications, and publishing an up-to-date handbook of the traditional sort. The handbook will consist of 33 chapters devoted to individual classes of special functions plus 4 chapters on algebraic and analytical methods, asymptotic approximations, numerical methods, and computer algebra. The most recent comprehensive handbook of special functions is the one by Abramowitz and Stegun, mentioned in the preceding paragraph. Still in print and in widespread use, it is badly out-of-date with respect to recent mathematical research, current scientific applications of special functions, and computational methods. Our second goal is to disseminate the same information, with significant augmentations, from a Web site at NIST. The augmentations include live links to available online software and references, a math-aware search capability, a facility for downloading formulas into word processors and computer software systems, and interactive visualizations.

The project is large, and the contributors fall into several categories. The *editorial board* consists of 4 principal and 8 associate editors. They are responsible for the selection and presentation of the technical information in book and Web formats. Since the beginning of the project, the principal editors have met frequently to review progress and to make midcourse corrections when necessary. *Authors* consist of expert individuals selected for their published research achievements and their ability to write for the intended

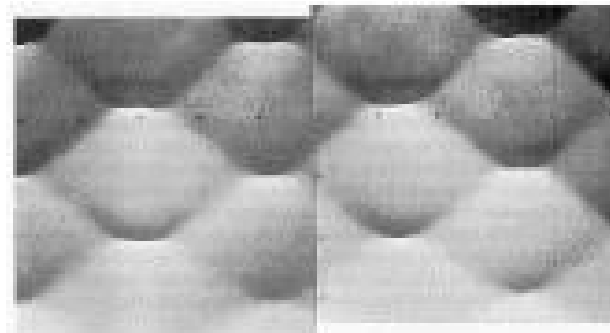
audience of scientists, engineers and mathematicians. Their contributions are being carefully edited and, in many cases, extensively revised by the principal editors to achieve uniformity of content and presentation across all chapters. *Validators*, like the authors, consist of expert individuals selected for their research accomplishments. Their responsibility is to check the work of the authors and editors, and to recommend corrections and improvements. This is a vital step to uphold the worldwide reputation of NIST as a reliable source of accurate, useful and timely scientific reference information. The *project staff* consists of highly qualified mathematicians and computer scientists whose responsibilities, broadly, are (i) construction of a mathematical database that encodes the entire technical content of the DLMF, (ii) application of advanced visualization methods and tools that enable users to display and manipulate complex functional surfaces, (iii) development of software tools to facilitate the production of the book and Web site, (iv) research into advanced techniques for the unambiguous translation of mathematical formulas and facts among different computer systems and application of these techniques into the DLMF when appropriate, (v) research into the frontiers of technical search methodology to enable effective queries involving fragments of technical mathematics and application of these techniques into the DLMF when appropriate. The *support staff* consists of individuals capable in the use of advanced mathematics document processors, symbolic and numerical computation packages, and bibliographic tools such as those provided by the American Mathematical Society.

By the end of calendar year 2007, all chapters but one (Computer Algebra) had been validated, and resolution of the validator's reports with the author's chapters had begun. Inclusion of Computer Algebra has been deferred until the other 36 chapters have been published. Validation confirms the mathematical correctness of the chapters. Resolution involves (i) integrating the validator's recommendations into the chapters, done at NIST, and (ii) obtaining approvals from the validators and authors that each chapter is ready for publication.

In July, 2007, the beta version of the DLMF Web site was placed behind the NIST firewall for internal usage and feedback. The announcement ran in the NIST Technicalendar for 6 weeks. A number of useful comments were received about the mathematical contents and, especially, the variety of rich Web interconnections we have been developing: (i) math-aware search, visualization, and cross-referencing within the DLMF, and (ii) links to external Web sites for bibliographic data, full texts of referenced articles, public-domain software, and available documentation for proprietary software.



**Figure 1.** The nonlinear Kadomtsev-Petviashvili differential equation (KP equation) is used to model the evolution of waves in shallow water. One family of such waves generates surface patterns that are two-dimensional, periodic, and hexagonal. These patterns are clearly visible, for example, when looking down into a swimming pool. They have been modeled with the KP equation. Shown above are level curves of an analytical solution derived in terms of Riemann theta functions. For properties of these functions see Chapter 21 of the DLMF. For a comparison of this analytical solution to experiment see Fig. 2 and the reference quoted there.



**Figure 2.** Two-dimensional periodic waves in a shallow water wave tank. Taken from Joe Hammack, Daryl McCallister, Norman Scheffner and Harvey Segur, "Two-dimensional periodic waves in shallow water. Part 2. Asymmetric waves," *J. Fluid Mech.* (1995), Vol. 285, pp. 95-122. The caption reads "Mosaic of two overhead photographs, showing surface patterns of waves in shallow water".

A number of innovative features will be present in the online DLMF. For example, in the DLMF, every symbol encountered in display equations is linked to its definition. To illustrate this, consider the equation

$$sn(x, k) = \sin(am(x, k)).$$

With just two clicks a Web user is able to "call up" the definitions of  $sn$  (a Jacobian elliptic function),  $x$  and  $k$  (real variables),  $\sin$  (the trigonometric function), and  $am$  (the Jacobian amplitude function). In contrast, a book user would have to scan the text for the definitions or consult the index. In the DLMF this equation can be located using the search tool with a simple query like "sn am". It appears high up on the hit list.

The remaining work for the public release of the DLMF is expected to be complete in 2008. The release schedule (subject to change) is



March 31	Partial public release of Web site
June 30	Selection of publisher
Sept. 30	Delivery of files to publisher
Dec. 31	Full public release of Web site Book in print

**Funding:** *National Science Foundation. NIST Systems Integration for Manufacturing Applications (SIMA) program.*

## Cultivating (Legacy) Mathematical Data

*Bruce Miller*

*Michael Kohlhase (Jacobs University, Bremen)*

*Heinrich Stamerjohanns (Jacobs University, Bremen)*

When the Digital Library of Mathematical Functions project was begun, a key issue was selecting the document format to use for preparing the material. The format had to support extensive and complex mathematical content, high-quality typesetting, and conversion to standard web formats. Above all, it had to be familiar to and convenient for the 40-50 authors, validators and editors who would be working on the project. One format so handily met all of these constraints but one, that LaTeX became the uncontroversial choice.

But, when no then-available system was sufficient to losslessly convert the DLMF source materials to XML and MathML, a parallel project was started to create one in-house, soon dubbed LaTeXXML. A fruitful period of quiet but intense development ensued where LaTeXXML and DLMF were able to leverage each other's strengths. Eventually, it became clear that this was a rather capable tool with broader application; the hammer thus set out in search of nails --- it didn't have to search for long.

While LaTeX may not be the universal document format, it certainly is the most broadly used within most of the scientific world, particularly where mathematics is involved. In fact it is actively used in those communities and a vast amount of so-called legacy material exists in that format. For example, the arXiv (<http://arxiv.org/>) contains almost a half million e-prints virtually all coming from LaTeX sources. Thus, beyond its obvious application to authors who wish to convert and present articles on the web, LaTeXXML might serve to convert the arXiv to a more broadly usable XML form. Yet another DLMF spin-off, then, was the mass conversion of the arXiv to the generation of a large test suite to support the development of math-aware search engines and similar research in Mathematical Knowledge Management. The long-term goal of such work is that eventually scientists and engineers will be able to enter mathematics in search engines and find relevant articles as easily

as they search for text terms today. Eventually, mathematical software, computer algebra systems, and similar may execute such searches automatically, behind the scenes, to accomplish their work.

During this year, the group at NIST, in collaboration with a group at Jacobs University in Bremen (formerly International University Bremen), began a project to apply LaTeXXML to the arXiv corpus. A flexible mass-conversion and reporting system was developed at Jacobs and was applied to the task. A particular strength of the system is that it collects and summarizes conversion problems. This led to several iterations of refinement of the LaTeXXML program --- it should be noted that LaTeX is both a powerful system and a quirky one that seemingly invites peculiar authoring idioms. At this point, the conversion of almost 300 thousand documents has been attempted, with over half being converted without error to intermediate XML form, and with almost 200 thousand converted to XHTML and MathML. The resulting improvements have, of course, come back to benefit the DLMF project.

Future work will focus on refining and improving the conversion rate, and getting broader coverage of the document styles used by various journals and publishers. Of course, we will also begin exploring the opportunities provided by the large data set.

The emphasis to this point has been on the presentational aspects of the mathematics. Future efforts will also be directed at developing methods and heuristics to synthesis a more semantic view of the mathematical material. This will greatly open the horizons for research into search methods and knowledge management.

Related to this work, Bruce Miller gave presentations at the Mathematical Knowledge Management Conference at Linz in June and at the International Congress on Industrial and Applied Mathematics at Zurich in July. Finally, Bruce Miller and Michael Kohlhase have been active participants in the W3C Math Working Group developing the third version of the MathML standard.

**Associated ITL Program:** *Information Discovery, Use and Sharing.*

**Funding:** *NIST Systems Integration for Manufacturing Applications (SIMA) program.*

## Visualization of Complex Function Data

Bonita Saunders

Qiming Wang (NIST ITL)

Sandy Ressler (NIST ITL)

Daniel Lozier

Frank Olver

Effective visualizations can aid a researcher's understanding of high level functions that arise as solutions to problems in the mathematical and physical sciences. Consequently, a considerable effort has been devoted to developing state-of-the-art interactive 3D visualizations for the NIST Digital Library of Mathematical Functions. Using techniques from numerical grid generation and web-based visualization technologies such as the Virtual Reality Modeling Language (VRML) and X3D, we have completed over 200 3D visualizations for the digital library. A sample chapter on the gamma function is available externally at <http://dlmf.nist.gov/Contents>; internally, see <http://dlmf-i.nist.gov/>.

With preliminary visualizations completed for all chapters, we are now focusing on improving presentation quality while maintaining plot and data accuracy. Plot accuracy concerns the visual display of the data. We have used numerical grid generation techniques to create computational grids that successfully capture key surface features such as zeros, poles, and branch cuts, but we continue to work on adaptive enhancements to improve the rendering of surfaces with steep gradients. While primarily using VRML and X3D, we have also developed prototypes using alternative technologies such as embedded 3D and video capture to make the visualizations more accessible to users on platforms where no suitable VRML/X3D plugin is currently available.

To validate data accuracy we are computing the function values using codes from at least two independent sources, including standard computer algebra packages such as Mathematica and Maple, routines from repositories such as the NIST Guide to Available Mathematical Software (GAMS, <http://gams.nist.gov/>), and personal FORTRAN and C codes from the chapter authors themselves. Validation of static 2D image data is almost complete, and validation of data files for 3D visualizations has begun.

As the visualization work for the current phase of the NIST DLMF winds down, we will concentrate more on extending our work to on-demand generation of mathematical graphs and tables. This may be a stand-alone capability or ultimately be incorporated as part of the DLMF. We are searching the web for sites that may offer some of these capabilities and

looking at the possibility of extending work on the live generation of tables completed by former NIST post-doctoral associate and faculty appointee Bruce Fabijonas.

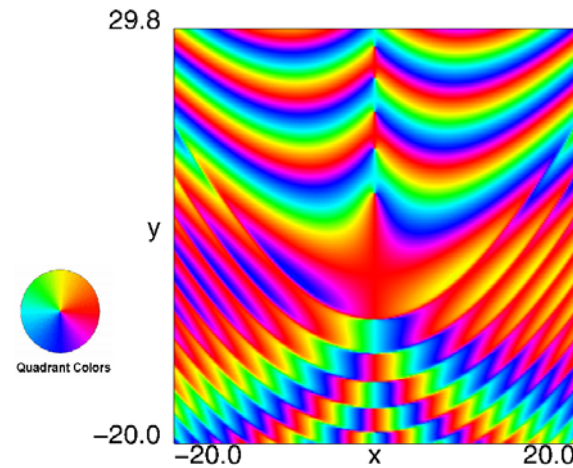


Figure 1. Density plot of phase of swallowtail canonical integral function  $\Psi_3(x,y,3)$ .

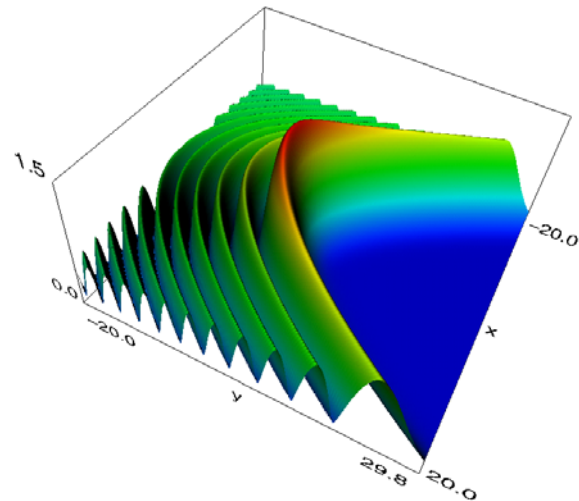


Figure 2. Modulus of swallowtail canonical integral function  $|\Psi_3(x,y,3)|$ .

- [1] Q. Wang, B. Saunders, and S. Ressler, "Dissemination of 3D Visualizations of Complex Function Data for the NIST Digital Library of Mathematical Functions," *CODATA Data Science Journal* **6** (2007) (Supplement on the *Proceedings of the 20<sup>th</sup> International CODATA Conference*, Beijing, China, October 2006), pp. S146, S154.
- [2] B. Saunders and Q. Wang, "From B-Spline Mesh Generation to Effective Visualizations for the NIST Digital Library of Mathematical Functions," *Curve and Surface Design: Avignon 2006, Proceedings of the Sixth International Conference on Curves and Surfaces*, Avignon, France, pp. 235-243.

## High Performance Computing

### Modeling the Rheological Properties of Suspensions

William George  
Julien Lancien  
Steve Satterfield  
Marc Olano  
Nicos Matrys (NIST BFRL)

See feature article, page 30.

**Funding:** Virtual Cement and Concrete Testing Laboratory (VCCTL) Consortium.

### Computation, Visualization of Nanostructure and Nano-optics

James Sims  
William George  
Terrence Griffin  
John Hagedorn  
John Kelso  
Marc Olano  
Adele Peskin  
Steve Satterfield  
Judith Terrill  
Garnett Bryant (NIST PL)

See feature article, page 33

### High Precision Hy-CI Variational Calculations on Small Atomic Systems

James S Sims  
Stanley A Hagstrom (Indiana University)

The ultimate goal of this work is to produce wave functions and energy levels of few electron atoms and ions with a precision that goes well beyond what can be achieved experimentally. In the past two decades, there have been breathtaking improvements in computer hardware and innovations in mathematical formulations and algorithms, opening up the real possibility that theoretical successes for the two electron atomic problem (He) and the two electron molecular problem (H<sub>2</sub>) can be extended to atoms (and molecules) with more than two electrons.

There are formidable bottlenecks to accomplishing this goal, as evidenced by the fact that in going from He (two electrons) to Li (three electrons) to Be (four electrons), the situation vis a vis high precision calculations degrades to the point that there are no calculations of the ground or excited states with an error of less than present day experimental uncertainty. This project attempts to remove the bottlenecks with a combination of mathematical formulations and algorithms revolving around a mathematical technique pioneered by Sims and Hagstrom many years ago (the Hylleraas-Configuration Interaction (Hy-CI) technique), and the use of extended precision, parallel computing, and efficient techniques for integral calculation and storage.

A notable accomplishment this year has been the completion of the second of three studies undertaken on math and computational science issues in Hy-CI calculations. "Math and computational science issues in high-precision Hylleraas-configuration interaction variational calculations II. Kinetic energy and Nuclear attraction integrals" has been published in *J. Phys. B. At. Mol. Opt. Phys.* A third (and final) study in the series, dealing with the requisite four-electron integrals, is nearly completed. This study has entailed the development of a new technique for the rapid evaluation of four-electron integrals utilizing recursion relations. Techniques for storing and retrieving the integrals as part of the matrix element assembly, the hardest part of the problem, are being developed. A hashing scheme has been worked out for this which, in combination with the recursion relations, resulted in 238,052 four electron integrals being calculated in 4.99 seconds in a 300 term Hy-CI calculation. These numbers are a validation that the recursion techniques are the only viable way to handle these integrals in a high-precision calculation.

The combination of these achievements this year and previous efforts culminating in an extended-precision parallel dense matrix generalized eigenvalue solver, should lead to a benchmark calculation on the Beryllium atom (the prototype for high precision atomic calculations for atoms with four or more electrons), resulting in theoretical predictions as accurate (or better) than modern experiments.

- [1] James S Sims and Stanley A. Hagstrom, "Combined Configuration-Interaction-Hylleraas-Type Wave-Function Study of the Ground State of the Beryllium Atom," *Physical Review A* **4**, 1971, pp. 908-916.
- [2] James S. Sims and Stanley A. Hagstrom, "High Precision Hy-CI Variational Calculations for the Ground State of Neutral Helium and Heliumlike Ions," *International Journal of Quantum Chemistry* **90** (6), 2002, pp. 1600-1609.
- [3] James S. Sims and Stanley A. Hagstrom, "High Precision Variational Born-Oppenheimer Energies of the

Ground State of the Hydrogen Molecule,” *Journal of Chemical Physics* **124**, 2006, 094101.

- [4] James S. Sims and Stanley A. Hagstrom, “Math and Computational Science Issues in High-precision Hy-CI calculations II. Kinetic Energy and Electron-nucleus Interaction Integrals,” *Journal of Physics B: Atomic, Molecular, and Optical Physics* **40**, 2007, pp. 1575-1587.

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## Screen Saver Science

*William L. George  
Julien Lancien*

<http://math.nist.gov/mcsd/savg/parallel/screen>

The Screen Saver Science (SSS) project aims to develop a computing resource composed of a heterogeneous set of PCs, scientific workstations, and other available computers, that can be easily used by scientists to execute large highly distributed, compute intensive applications. Each individual computer makes itself available for participating in a computation only when it would otherwise be idle, such as when its screen saver is running. SSS is based on Jini, an open software architecture built on Java and intended for the development of robust network services. There are several goals to this project. First, we hope to utilize the idle processing power of the many PCs, workstations, and cluster nodes we have available here at NIST to execute production scientific codes. The compute power of personal PCs and workstations continues to increase and they have become increasingly capable of executing large compute intensive applications due to faster processors and larger main memories. Second, the SSS computing environment will allow us to develop and experiment with new highly parallel and distributed algorithms more suitable for emerging grid environments. Finally, the use of Java for scientific applications is of interest in general, and so the development of applications for SSS will give us the opportunity to explore this topic on actual production quality applications. Up until recently, this type of project would have required a large investment in software development just to become minimally functional and so was not practical, especially for a small team of programmers. However, with the introduction of Jini, and more specifically the Jini based network service called Javaspaces, the most difficult parts of this project have now become straightforward. Javaspaces is a portable, machine independent, shared memory system that expands upon the tuple-space concepts developed in the 1980s by David Gelernter of Yale University.

Over the past year we have developed a system of scripts to manage SSS workers on the compute

nodes of the ITL/PL Linux cluster Raritan, thus enabling us to utilize every free cycle. We have also enhanced SSS in several basic ways. The user interface, specifically for submission of SSS computations to the Raritan cluster, and the retrieval of results has been simplified. The SSS infrastructure has been improved to simplify its building, packaging, and distribution, and to better support application development by multiple researchers

A user interface to SSS, to be used by those submitting computations to the SSS system as well as those simply allowing SSS tasks to run on their machine, has been completed. The interface is web-based, built on the ‘Ruby-on-Rails’ framework and uses jruby, a Java implementation of the Ruby scripting language. Using jruby, instead of the standard C-based Ruby implementation, allows us to more easily interact with both the Rails framework and the SSS system.

The OS specific parts of SSS have been reduced to a minimum. For example, we now use the Java Installer Builder, IzPack (<http://izpack.org>), to create a simple cross-platform (Linux, Mac, MS Windows) installer for SSS.

W. George and Guest Researcher J. Lancien have completed the initial draft of the SSS Users Manual and Administrators Guide.

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## Computational Modeling of Cement Paste Hydration and Microstructure Development

*William George  
Edith Enjolras  
Jeffrey Bullard (NIST BFRL)*

<http://math.nist.gov/mcsd/savg/parallel/hydration/>

Understanding the complex chemical changes that occur when cement powder is mixed with water is a long-standing but extremely challenging technological goal. Fundamental computational modeling of the hydration of cement is difficult because it involves a large number of coupled nonlinear rate equations that must be solved on a random three-dimensional spatial domain.

To address these challenges, we are applying a new computational model called HydratiCA which has several advantages over previous attempts to model cement paste hydration. HydratiCA is based on concepts of transition state theory and uses stochastic cellular automaton algorithms to simultaneously model 3-D reaction and transport phenomena. This allows us to track the detailed kinetics and equilibria that occur in a diverse range of cementitious systems. At the length scales required to finely resolve the reaction mechanisms and microstructure changes in cement paste,

HydratiCA must take small time steps (approximately  $10^{-5}$  seconds) to remain numerically stable. In other words, tens of millions of time steps are required to simulate the behavior of cement paste for just one hour. Therefore, parallelization of the model is important for modeling systems that are large enough to be realistic, avoiding finite size effects, and still be able to complete the simulations in a reasonable amount of time.

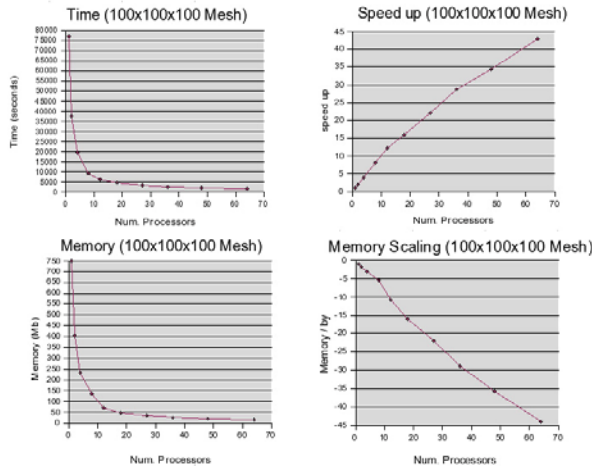


Figure 1. Performance of the parallel HydratiCA code for a 100x100x100 mesh

This year we parallelized the HydratiCA code using a spatial decomposition. This code has been tested on the Raritan linux cluster and shown to scale well. Performance of the parallel code can be seen in the figure below. NASA has granted us 200,000 hours of CPU time on its Columbia supercomputer at NASA Ames research Laboratory this year to study the scalability of the code, and to perform validation tests.

[1] E. Enjolras, W. George, J. Bullard, and J. Terrill, "Parallelization of HydratiCA," presented at the VCCTL semi-annual consortium meeting, Nov. 2007, NIST Gaithersburg.

[2] J. Terrill, W. George, T. Griffin, J. Hagedorn, J. Kelso, M. Olano, A. Peskin, S. Satterfield, J. Sims, J. Bullard, J. Dunkers, N. Marty, A. O'Gallagher, and G. Haemer, "Extending Measurement Science to Interactive Visualization Environments", Chapter in *Trends in Interactive Visualization: A-State-of-the-Art Survey*, edited by Elena Zudilova-Seinstra, Tony Adriaansen and Robert van Liere, to be published by Springer, UK.

**Funding:** Virtual Cement and Concrete Testing Laboratory (VCCTL) Consortium.

## Physics Models for Transport in Compound Semiconductors

Miguel Rios  
 Adele Peskin  
 Terence Griffin  
 Judith Terrill  
 Herbert S. Bennett (NIST EEEL)

Physics models for carrier transport in semiconductors are essential inputs of computer programs that simulate the behavior of nanoelectronic and optoelectronic devices. Such simulations increase understanding, reduce times-to market, and assist in making selections from among competing or alternative technologies. As devices shrink in size to nanometers, performing experimental measurements becomes more costly and time-consuming. This means that computer simulations will become more essential for advances in future nanotechnologies.

Unlike many physics models that are based on using variations in parameters to fit experimental data, the NIST physics models developed in this project are based on quantum mechanical calculations with no fitting parameters to account for dopant ion effects and many-body physics effects. The calculations include many-body quantum effects and bandgap narrowing due to dopant ion carrier interactions. The many-body quantum effects treat both electron-electron and electron-hole interactions. The results are unique because other reported treatments for the electric susceptibility

- (1) Do not treat these effects self-consistently,
- (2) Are Taylor series expansions in either the ratio  $R = Q^2/A$  or the inverse of  $R$ , where  $Q$  is the magnitude of the normalized wave vector and  $A$  is the normalized frequency used in the measurements, and
- (3) Do not give the structure shown in the Fig. 1.

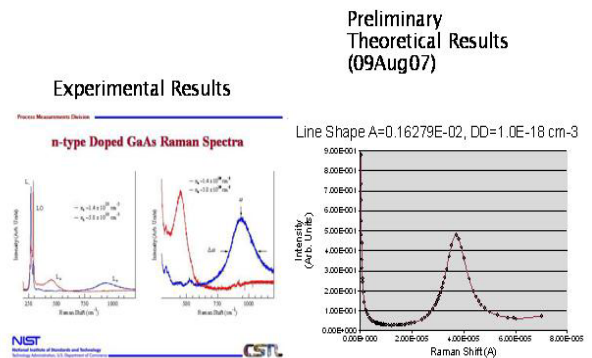


Figure 1. Comparison of theoretical and experimental results.

These results will change the way researchers and process engineers interpret non-destructive measurements to extract the carrier concentrations of GaAs

wafers. The wafer carrier concentration is a key figure of merit associated with a go/no-go decision for determining whether a wafer meets specifications and should undergo further processing.

This year the code was made completely open source. Also, a “first time ever” visualization of the theoretical complex electric susceptibility and Raman's line shape was computed and visualized. The visualization helps scientists to reduce the range of their data, reducing the time and cost of the experiments. This could lead to major improvements in the electronics and semiconductors fields; especially, for compound semiconductor nano-layers on silicon wafers. The comparison with experiment is shown in Fig. 1.

## High Performance Visualization

### **Error Correction for Electromagnetic Motion Tracking Devices**

*John Hagedorn  
Steve Satterfield  
John Kelso  
Whitney Austin  
Judith Terrill  
Adele Peskin*

See feature article, page 36.

### **Computation, Visualization of Nanostructure and Nano-optics**

*James Sims  
William George  
Terrence Griffin  
John Hagedorn  
John Kelso  
Marc Olano  
Adele Peskin  
Steve Satterfield  
Judith Terrill  
Garnett Bryant (NIST PL)*

See feature article, page 33

### **Virtual Cement and Concrete Testing Laboratory**

*William George  
Terence Griffin  
John Hagedorn  
John Kelso  
Julien Lancien  
Adele Peskin  
Steve Satterfield  
James Sims  
Judith Terrill  
Clarissa Ferraris (NIST BFRL)  
Edward Garboczi (NIST BFRL)  
Nicos Martys (NIST BFRL)*

The NIST Building and Fire Research Laboratory (BFRL) does experimental and computational research in cement and concrete. MCSD has an ongoing collaboration with them to develop highly efficient

parallel implementations of their modeling codes and in creating visualizations of their data. This work is done in the context of the Virtual Cement and Concrete Testing Laboratory (VCCTL) Consortium which we helped form in 2001. The NIST-led consortium consists of eight industrial members: BASF Admixtures (MBT), Ready Mixed Concrete (RMC) Foundation, Association Technique l'Industrie des Liant Hydrauliques (ATILH), National Stone Sand and Gravel Association (NSSGA), W.R. Grace, Sika Technology AG, Verein Deutscher Zementwerke eV (VDZ), and the Portland Cement Association. The overall goals of the consortium are to develop a virtual testing system to reduce the amount of physical concrete testing and to expedite the overall research and development process. It is expected that this will result in substantial time and cost savings to the concrete construction industry as a whole. MCSD continues as an active participant in the VCCTL.

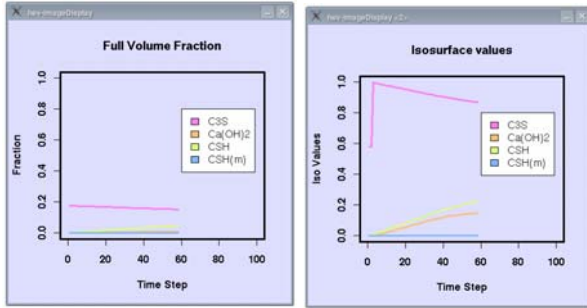
**Funding:** *Virtual Cement and Concrete Testing Laboratory (VCCTL) Consortium.*

### **Visualization of Cement Paste Hydration and Microstructure Development**

*Steve Satterfield  
William George  
Edith Enjolras  
Jeffrey Bullard (NIST BFRL)*

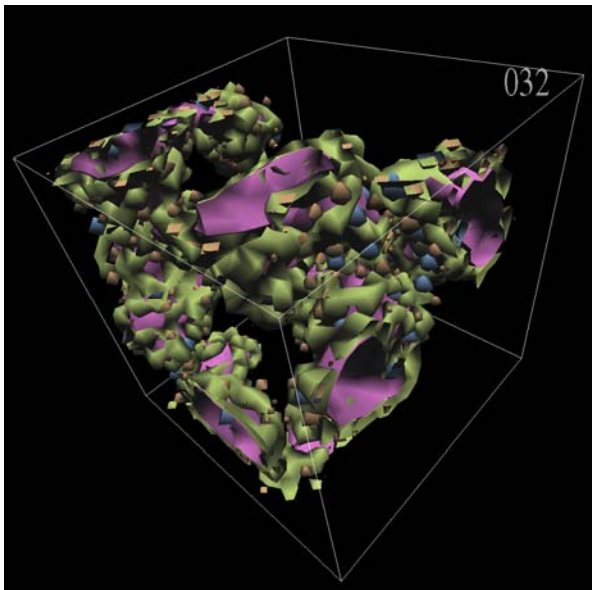
<http://math.nist.gov/mcsd/savg/vis/hydration/>

When cement powder is mixed with water, complex chemical and microstructure changes occur. This is termed hydration. The NIST BFRL is developing a new a new computational model called HydratiCA. Visualization of the output of this model is important first for validation as model development proceeds. It is also important to facilitate understanding the distribution of phases in 3D. The output of the hydration numerical simulation is a 3D volume of data with percentage values for each of multiple material phases at each voxel location. Over the course of the simulation time, a series of data volumes is produced at the time intervals of interest. For each data set, an over all volume fraction is computed for each phase and plotted as a 2D graph. From the volume fraction values, a series of isosurface values is computed and also displayed as a 2D graph. See Fig. 1)



**Figure 1.** Full Volume Fraction Plot (left) and Isosurface Values Plot (right)

For each material phase a series of isosurfaces is generated. These time series of isosurfaces are combined (Fig. 2) into a 3D animation utilizing DIVERSE ([diverse.sourceforge.net](http://diverse.sourceforge.net)) and in-house developed software. These components (3D animation, 2D plots, interactions) are combined into a complete application for interactive exploration and analysis in the immersive visualization environment by the domain scientists.



**Figure 2.** Four combined phases (components of cement paste) at timestep 32.

Future work in the area will evolve this application into a *Virtual Cement Analysis Probe (VCAP)*. The immersive visualization environment will be used to interactively probe the data and create application specific analysis and measurements. Additional software enhancements will allow alternate data representations such as volume rendering to augment the current isosurface representation.

**Funding:** *Virtual Cement and Concrete Testing Laboratory (VCCTL) Consortium.*

## Three-D Desktop

John Kelso  
Terence Griffin  
John Hagedorn  
Marc Olano  
Adele Peskin  
Steven Satterfield  
Judith Terrill

<http://math.nist.gov/mcsd/savg/vis/desktop>

Immersive visualization systems have many advantages, but not all users have ready access to these systems. Additionally sometimes it's easier to look at new data on a desktop in the office rather than go down the hall to use the immersive system, and sometimes the immersive system is not available at all due to distance, time or other constraints.

To this end, SAVG is developing the “3D-desktop”, a set of tools to help users more effectively use our immersive software in a desktop environment. These tools can not completely bridge the gap between desktop and immersive systems, but can help ameliorate the situation. Some of the tools will be general and can be used in any application, and some will be geared towards a specific application or type of application.

Our immersive software development API, DIVERSE, automatically allows applications to be used in both immersive and desktop systems. But, the API does not address user interface questions that are raised due to the differences between the two types of systems. Therefore our tools do not need to modify the underlying immersive application, but merely replace the immersive interaction techniques with ones more suitable for desktop use, and augment these techniques with additional tools to make up for the lack of intuitive presence necessitated by the desktop system.

Our progress so far on this project consists of the following general purpose tools:

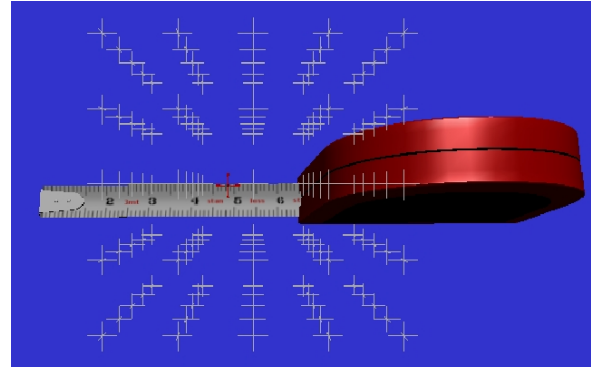
1. **Display Control Panel.** The display control panel allows users to:
  - Choose the type of frustum projection; parallel or perspective. A perspective view helps the user get a sense of depth, and a parallel view lets the user more easily determine the geometry of their data.
  - Modify the field of view of the perspective view, or width of the parallel view. The field of view can reduce or exaggerate the distortion of the geometry due to the perspective transformation.
  - Specify the distance to the near and far clipping planes. The near clipping plane discards all geometry in front of the plane, and the far clipping plane discards all geometry behind the plane.



Specifying their distance can help the desktop user get a sense of the relative depths of objects in the application.

2. **3-View Displays.** The 3-view display tool creates three additional windows, each sighting along each of the three major axes. Each of the X, Y and Z displays has its own control panel, a superset of the general display control panel, additionally allowing the user to specify the distance from the origin and position in the plane orthogonal to the line of sight. A center button will automatically center the geometry in the window.
3. **Grids.** The grid tool enhances the sense of depth by creating grids of markers in the virtual environment indicating the position of the wand, or any other positional object in the virtual environment. In addition, a roller can be used to specify the scale of the grid, making it finer or coarser as needed for the application. Four types of grids can be independently selected.
  - *exact*, which displays the exact position of the wand with a red cross hair
  - *nearest*, which displays a bright cross-hair when the wand is close to a grid point
  - *proximity*, which displays a 5x5x5 grid of cross-hairs around the grid point nearest to the wand
  - *background*, which displays a static field of small cross-hairs, which can be used to determine the position of objects in the virtual environment by use of geometric occlusion.
  - *unit cube*, which displays a set of nested cubes centered around the nearest grid point
  - *axes*, which displays a set of five axis objects—the objects are centered and equally spaced along the +Y axis (going into the screen)
4. **hev-pickerRollers.** This tool allows the user to manipulate a generic picker object such as used by the grid tool. The tool is a GUI control panel containing:
  - rollers for each of the picker's six degrees of freedom, and a numerical display for each roller. The displays give the screen or data coordinates of the picker, as specified below
  - radio buttons to select whether the picker moves in the screen's coordinate space, or the data's coordinate space.
  - a button to indicate if the picker should move with navigations in the virtual environment (i.e., move with the model) or remain stationary.

Fig. 1 shows a tape measure in a proximity grid with the exact position of the wand shown as a red crosshair.



**Figure 1.** A tape measure in a proximity grid with the exact position of the wand shown as a red cross hair.

We have also developed application specific slider tools for the lung cancer project. The lung tumor sliders position a virtual lung tumor in an isosurface representing a lung. In the immersive system the user merely grabs and moves the tumor to the desired location by use of the tracked wand. Our desktop tool uses a set of sliders which move the tumor in any axis. A radio button allows the user to choose whether the tumor moves in the screen's coordinate space or in the data's coordinate space.

The 3D desktop project will continue to explore new user interface and tools to help enhance the immersive capabilities of desktop users.

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## Visualization of Network Dynamics

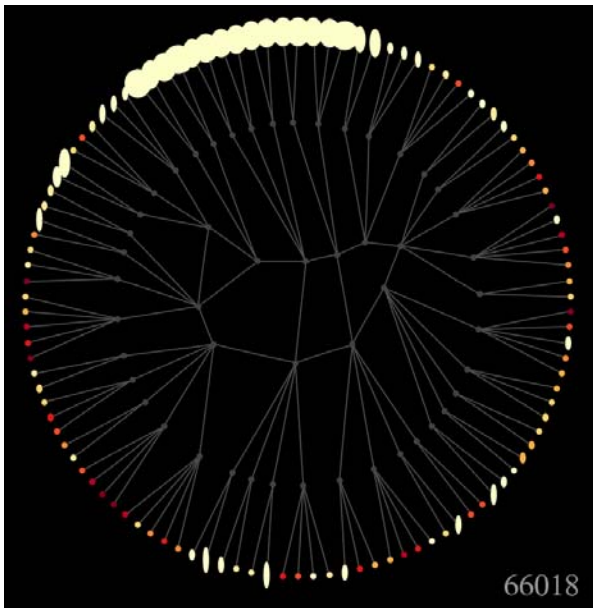
*John Hagedorn  
Cedric Houard  
Dong Yeon Cho  
Judith Terrill  
Fern Hunt  
Kevin Mills (NIST ITL)  
E. Schwartz (NIST ITL)*

<http://math.nist.gov/mcsd/savg/vis/network/index.html>

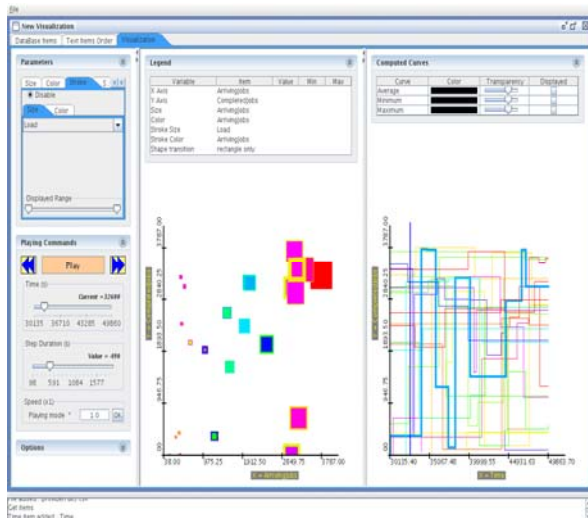
As part of the ITL Complex Systems program, we are creating visualizations and developing a software system that enables researchers to data visualizations from their model output. The purpose of these visualizations is to provide better understanding of the grid computing and network models. We have created a series of static and animated visualizations of network simulation data (Fig. 1). We have developed a data visualization tool that handles data from the grid computing models (Fig. 2). This tool is flexible and adaptable to a wide variety of types of data. We have also been using machine learning tools to explore the network simulation data. Fig. 3 is an example of using a hierarchical clustering tool on this data. Future work

will include the enhancement of the grid model visualization tool to provide additional modes of visualization, interactions, and data derivations. We will also be developing a similar flexible tool for visualizing time-dependent network model data. Machine learning tools will continue to be used to explore the data.

**Associated ITL Program:** *Complex Systems.*



**Figure 1.** Visualizations of network simulation data



**Figure 2.** Data visualization tool that handles data from the grid computing models



**Figure 3.** An example of using a hierarchical clustering tool on network simulation data.

## Monitoring Change in Lung Tumors

Adele Peskin  
John Kelso  
Terence Griffin  
Judith Terrill  
Alden Dima (NIST ITL)  
Karen Kafadar (CU Denver)

<http://math.nist.gov/mcsd/savv/vis/imaging/index.html>

Detection of lung tumors by computerized tomographic (CT) imaging presents a number of challenges. There are currently a large number of different methods in use for measuring tumor growth by comparing CT scans taken at different points in time. A scarcity of useful data in the medical imaging community has led to variable results for tumor growth measurements. The work in our group for this project is two-fold: we are developing a common database of medical images containing tumors of known size on which to test measurement techniques, and we are working on a new method of measuring tumor growth using this data.

Our new tumor data is being created by embedding phantom tumors of known size into existing lung data. The starting data is a set of CT slices from the Cornell University lung database. A sample slice of this data is pictured in Fig. 1. We have developed a set of tools to visualize this lung data in our visualization system, both in the immersive environment and on the desktop. A 3D version of 40 slices of this data is shown in Fig. 2, a visualization of an isosurface created from the pixel values of the images.



Figure 1. Original Cornell lung data

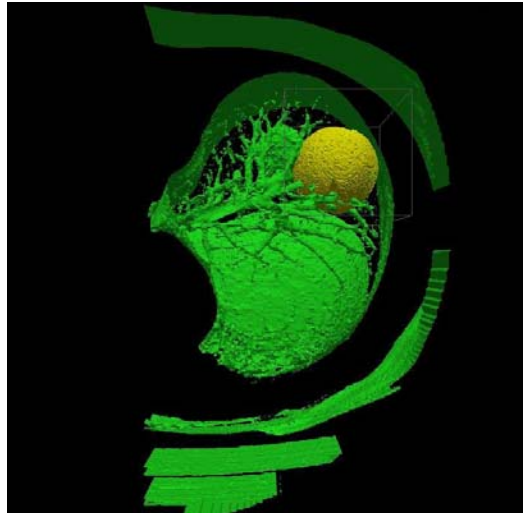


Figure 4. Insertion

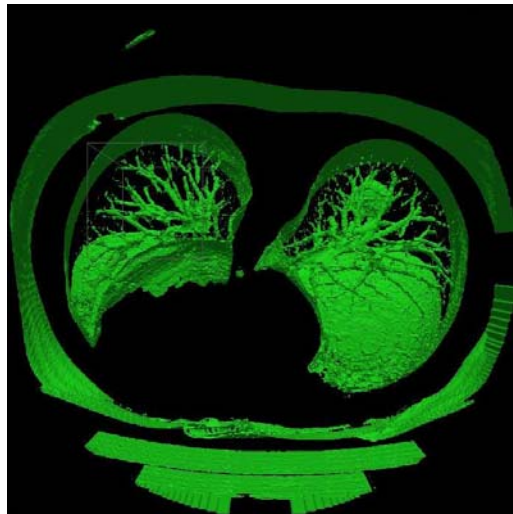


Figure 2. Isosurface of 40 slices of this data

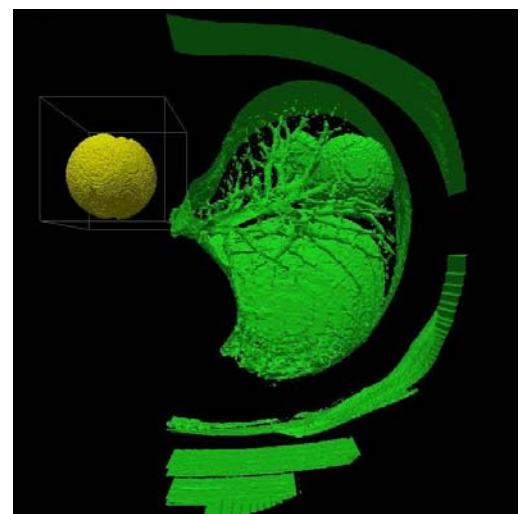


Figure 5. Isosurface of the new lung data

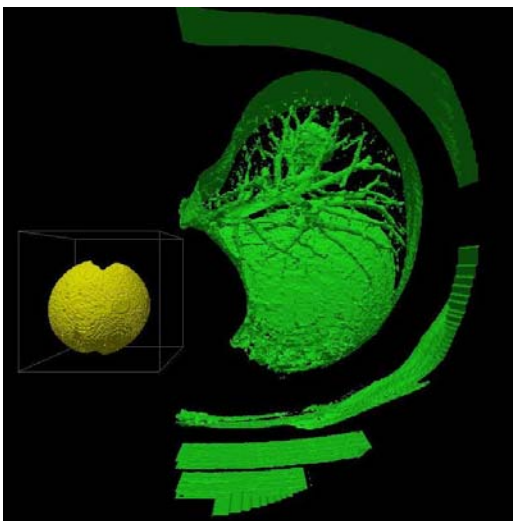


Figure 3. Cornell lung data and the FDA phantom tumor.

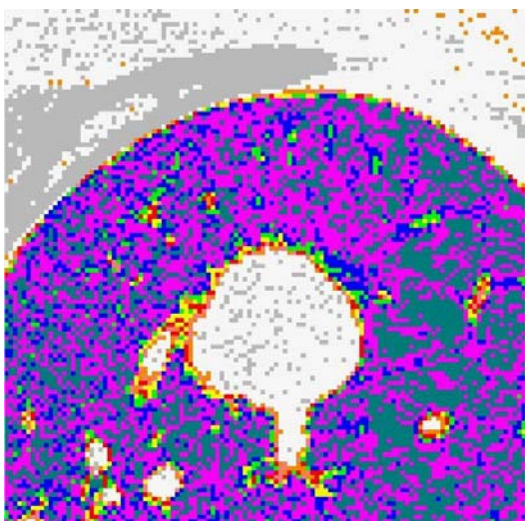


Figure 6. Pixel distribution color-coded in one slice of the Cornell data set

We have developed the tools to embed phantom tumors into this data, and output the modified slices in the same format (DICOM) in which we received them. An example of a modified image is shown in Figs. 3, 4, and 5, in which an isosurface from a phantom tumor from the FDA is shown, the phantom tumor is inserted into the data, and the data is then updated.

In order to make accurate measurements of tumors in this lung data, we are studying the pixel distributions in and around the tumors in the CT data, to understand which pixels can be said to be statistically inside the tumor and which pixels outside. Again, we

use our visualization tools to help locate areas of specified pixels values, designated by a series of different colors in the image shown in Fig. 6 of the tumor located in Fig. 1. By understanding where areas of noise are located and the range of pixels values at tumor surfaces, we can characterize the shapes of these objects. The goal is to develop a method to measure tumor properties without requiring input from people reading the CT data, which often varies significantly from person to person.

**Associated ITL Program:** *Information Discovery, Use and Sharing.*

## Mathematical Applications: Mechanical Systems and Processes

### Application of Optimization Techniques to Design for Multi-Hazard Conditions

Florian Potra

Emil Simiu (NIST BFRL)

Traditionally, structures subjected to more than one potential hazard (e.g., wind and earthquake) have been designed independently for each individual hazard. This assures their safety under any of the potential hazards. However, techniques are currently being developed allowing designs to exhibit synergies, in the sense that design features that assure safety under any one of the hazards are utilized to improve performance under all hazards for which the structure must be designed. These techniques do not typically result in optimal designs with respect to cost or reliability.



**Figure:** This solar energy collection array illustrates the type of structure being considered in this study.

This project, which has just gotten underway, is aimed at developing an approach to design for multi-hazard conditions that assures optimality of the design for each individual hazard, as well as assuring optimality across the multiple hazards. To our knowledge this type of integrative optimization approach has never before been used in a structural engineering context. To test and illustrate the potential of our approach the example of a structural assembly developed as part of a novel renewable energy system is being considered. The assembly includes columns supporting water-filled pipes, heated by sun rays reflected onto the pipes by large arrays of computer-guided mirrors. Under constraints guaranteeing that the column design assures

safety against buckling under the vertical loads transmitted by the pipes, modern mathematical optimization techniques are being applied to obtain optimal designs under (1) wind forces dependent upon the angle between the wind direction and the axis of the pipes, (2) direction-independent seismic forces, and (3) wind forces or seismic forces characterized by specified probabilities of exceedance.

**Funding:** NIST Innovations in Measurement Science.

### Instability in Pipe Flow

G. B. McFadden

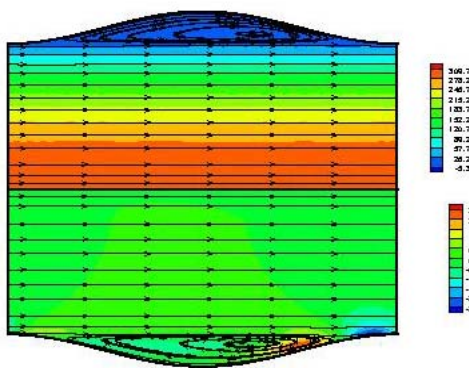
D. L. Cotrell (Lawrence Livermore National Lab)

B. J. Alder (Lawrence Livermore National Lab)

This study explores a classical problem in the stability of the flow of fluid through a cylindrical pipe. This type of flow is relevant to a number of important applications, ranging from material transport in pipelines to blood flow in veins and arteries. The flow is driven by pressure gradients along the direction of the pipe, and is retarded by the effects of friction on the walls of the pipe. In general the nature of the flow depends on the ratio of inertial forces to viscous forces in the fluid, as measured by the dimensionless Reynolds number. For small Reynolds numbers (high relative viscosity) the flow is laminar. For large enough Reynolds numbers, however, the laminar flow is observed to become unstable, leading to more complicated (“secondary”) flows. The resulting turbulence in the flow field gives rise to additional phenomena such as enhanced mixing and an increase in the pressure gradient required to drive the flow. The prediction of the onset of instability is often possible by employing linear stability theory to determine critical modes that grow temporally or spatially; such studies have been successful for a number of flow geometries, but not for the case of pipe flow.

For an idealized pipe of infinite length and circular cross-section a simple one-dimensional flow can be found from the underlying equations of motion whose stability can be examined through numerical means. There is a long known contradiction between the resulting linear stability results and the experimental observation that such flows become unstable at a Reynolds number of about 2000 for ordinary pipes. A hint that wall roughness may be important can be gathered from experiments which show that for smoothed pipes the onset of the instability can greatly exceed 2000. In this work we investigate the possibility that

the use of stick (or no-slip) boundary conditions in modeling the flow is responsible for the discrepancy between theory and experiment, because such models ignore the amplitude variations associated with the roughness of the wall. Once that length scale is introduced (here, crudely, through a corrugated pipe), linear stability analyses leads to stable vortex formation at low Reynolds number above a finite amplitude of the corrugation, and unsteady flow at a higher Reynolds number, where indications are that the vortex dislodges. Remarkably, extrapolation to infinite Reynolds number of both of these transitions leads to a finite and nearly identical value of the amplitude, implying that below this amplitude, the vortex cannot form because the wall is too smooth and, hence, stick boundary results prevail. The current work should serve as a general warning that stick boundary conditions, for example, in narrow biological channels where the surface roughness of the wall can be a significant fraction of the channel width, or, as another example, in the drag reduction problem, may be inappropriate. For the smooth walled case there exists a rigorous proof of stability for axisymmetric disturbances, with strong evidence that all linear perturbations decay for all values of the Reynolds number. Thus, there remains much interest in the cause of this transition and how one may affect the Reynolds number at which transition occurs.



**Figure 1.** Base flow velocity contours. The upper portion of the figure shows axial velocity shading and streamlines, while the lower portion of the figure shows radial velocity shading and streamlines.

To investigate the linear stability of the base flow, a standard normal mode analysis is used which results in a system of homogeneous linear differential equations in the radial and axial coordinate for the velocity and pressure eigenfunctions. The disturbance velocity boundary conditions are zero on the pipe. Since the coefficients of this system are periodic in the axial direction, Floquet theory is used to consider disturbances whose structure is possibly incommensurate with corrugation wavelength. Discretization of the disturbance equations using finite-element methods leads to a sparse generalized algebraic eigenvalue problem, a minimum Reynolds number is sought for which

at least one temporal eigenvalue is neutrally stable. Results show that for fixed corrugation amplitude and small Reynolds numbers the base flow is primarily unidirectional with significant streamline curvature seen only near the bulge and no vortex present in the domain. For sufficiently large Reynolds number the onset of vortex formation is observed in the bulge region (see Fig. 1); however, the flow is stable according to linear stability analysis both above and below this Reynolds number. If the Reynolds number is increased beyond this first transition, a value is reached at which the steady and axisymmetric bulge vortex flow transitions to an unsteady flow.

This work has been accepted for publication in the *Proceeding of the National Academy of Sciences*.

## Materials Data and Metrology for Applications to Machining Processes, Frangible Ammunition, and Body Armor

*Timothy Burns*

*Steven Mates (NIST MSEL)*

*Richard Rhorer (NIST MEL)*

*Eric Whitenton (NIST MEL)*

*Debasis Basak (Orbital Sciences Corporation)*

The split-Hopkinson pressure bar (SHPB) is an instrument that is used in laboratories throughout the world to obtain material response data for the purposes of modeling and simulation of phenomena that involve rapid, permanent material deformation. Applications of SHPB data include weapons effects modeling such as armor penetration, safety studies such as simulation of crash-tests, measurement of the strength of ceramic materials, and the simulation of material forming operations in manufacturing.

Development of the NIST SHPB, also called the NIST Kolsky Bar after the man who made significant advancements in Hopkinson's original design, was initiated several years ago for the purpose of obtaining improved material response data for the modeling and simulation of high-speed machining operations. An SHPB test involves placing a thin, disk-shaped sample of the test material between two long, hardened cylindrical steel rods. Using precision alignment, the centerline of the sample disk is made to coincide with the centerlines of the two long bars. By means of propulsion by a compressed air gun, a shorter striker rod of the same material is launched so that it collides normally with the outside end of the incident bar, which conducts a compressive stress wave into the sample. The two long steel rods remain elastic in their response to the impact loading.

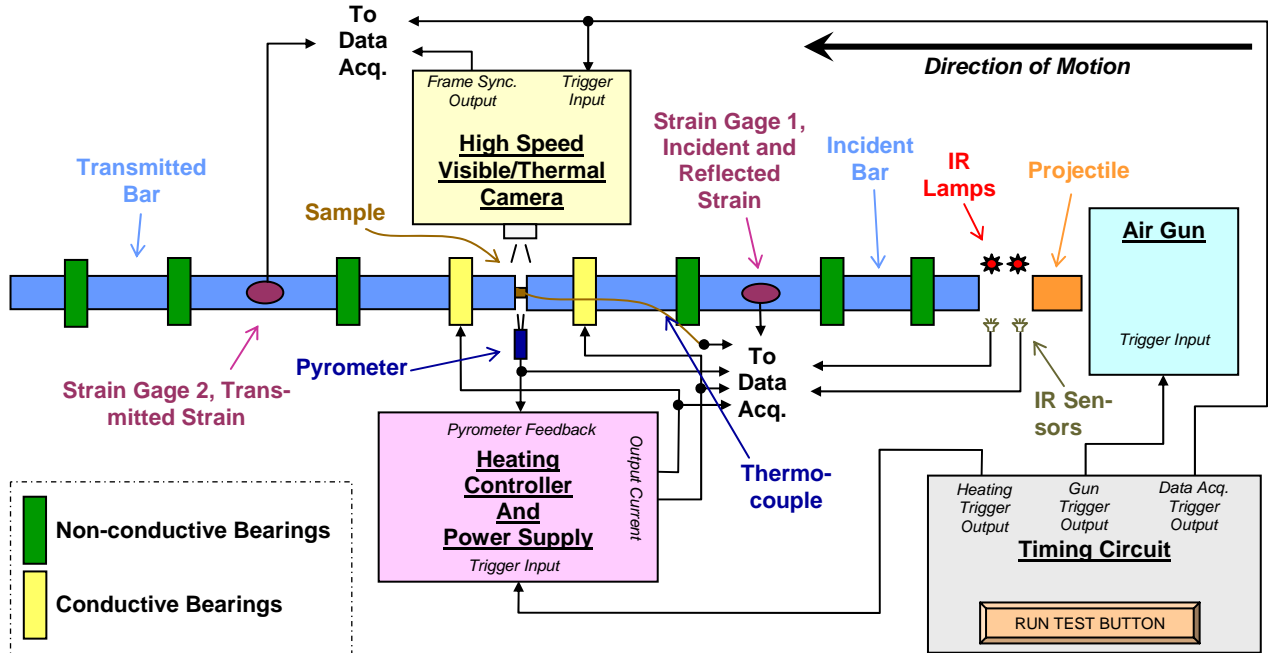


Figure: The NIST pulse-heated split-Hopkinson (Kolsky) pressure bar.

By ignoring radial effects, the experiment can be modeled using one-dimensional elastic wave theory. Due to an impedance mismatch at the bar-sample boundary, the input stress pulse splits into a tensile wave that is reflected back into the input bar, and a lower-amplitude compressive wave that travels through the sample and continues to propagate into the transmitted bar. When the compression wave enters the sample, it causes a permanent deformation of the material, known as plastic strain, at a rapid rate of deformation, or strain rate.

Unique features of the NIST Kolsky Bar facility are a capability for pulse-heating a test specimen from room temperature to a significant percentage of its melting temperature in tens of milliseconds prior to impact loading, and sophisticated instrumentation for measuring and controlling the sample temperature. These thermal capabilities, which are still being improved upon, have provided a means of simulating experimentally the extremely rapid heating that occurs in thin cutting regions during high-speed machining operations.

The development of the NIST SHPB was initially funded in large part by the Intramural ATP Program. Development of improved instrumentation for this work continues to be supported by MEL,

MSEL, and ITL. The National Institute of Justice (DOJ), through OLES, the NIST Office of Law Enforcement Research, has also supported development of the NIST Kolsky Bar in its room-temperature configuration for the study of the dynamic response of frangible bullets.

During the present fiscal year, it was demonstrated that, for a carbon steel of interest in manufacturing, the pulse-heated material response is considerably stiffer than had previously been measured in tests in other laboratories, in which samples had been pre-heated slowly prior to impact. Post-test metallographic studies on the pulse-heated samples support the hypothesis that certain thermally-activated transformations in the material's microstructure have insufficient time to run to completion under the rapid heating conditions that are present in high-speed machining operations, with the result that higher cutting forces are required for these processes. This work has significant implications for the modeling and simulation of manufacturing operations that involve material removal by rapid machining.

**Funding:** NIST Advanced Technology Program. National Institute of Justice (US DOJ via NIST Office of Law Enforcement Standards).

## **Mathematical Applications: Electromagnetic Systems**

### **Micromagnetic Modeling**

Michael Donahue

Donald Porter

Robert McMichael (NIST MSEL)

<http://math.nist.gov/oommf/>

Advances in magnetic devices such as recording heads, field sensors, magnetic nonvolatile memory (MRAM), and magnetic logic devices are dependent on an understanding of magnetization processes in magnetic materials at the nanometer level. Micromagnetics, a mathematical model used to simulate magnetic behavior, is needed to interpret measurements at this scale. MCS D is working with industrial and academic partners, as well as with colleagues in the NIST MSEL, PL, and EEEL, to improve the state-of-the-art in micromagnetic modeling.

Michael Donahue and Donald Porter in MCS D have developed a widely used public domain computer code for doing computational micromagnetics, the Object-Oriented Micromagnetic Modeling Framework (OOMMF). OOMMF serves as an open, well-documented environment in which algorithms can be evaluated on benchmark problems. OOMMF has a modular structure that allows independent developers to contribute extensions that add to the basic functionality of OOMMF. The past year has seen two such contributions. The first, produced primarily at the Polish Academy of Sciences but in collaboration with researchers in ITL, adds support for periodic boundary conditions to OOMMF. The second is a spin momentum transfer module developed at the IBM Zurich Research Laboratory. OOMMF also provides a fully functional micromagnetic modeling system, handling both two and three-dimensional problems, with sophisticated extensible input and output mechanisms. OOMMF has become an invaluable tool in the magnetics research community. During fiscal year 2007 alone, the software was downloaded more than 3400 times, and use of OOMMF was acknowledged in 82 peer-reviewed journal articles.

OOMMF is part of a larger activity, the Micromagnetic Modeling Activity Group (muMAG), formed to address fundamental issues in micromagnetic modeling through two activities: the development of public domain reference software, and the definition and dissemination of standard problems for testing modeling software. MCS D staff members are involved in development of the standard problem suite as well. There are currently four standard problems in the suite, testing both static and dynamic magnetization proper-

ties. The fourth standard problem, which tests magnetization dynamics, received a new submission this year, and new results and comparisons on this problem also figured prominently in a book chapter co-authored by one of ITL staff. Efforts have recently begun to draft a new standard problem to compare models and techniques for simulating the effects of spin momentum transfer.

In addition to the continuing development of OOMMF, the project also involves collaborative research using OOMMF. The project has provided modeling support for a four-laboratory NIST Innovations in Measurement Science (IMS) project (EEEL, MSEL, PL and ITL) on high sensitivity magnetic sensors, and for an ATP project on "Spin Momentum Transfer Oscillators for High-Frequency Nanoelectronic Applications." The project has also been instrumental in the 2007 IMS proposal (with MSEL and EEEL), "Magnetic nanostructures for post-CMOS electronics," which has been approved by the NIST Leadership Board for funding, pending budget availability. The MCS D micromagnetic project produced three journal papers, three conference presentations and two invited talks this past year.

Progress on computational issues has been a recent focus. A commonly used technique for computing the self-magnetostatic interaction tensor from analytic formulae has been determined to produce significant errors. Corrections of the worst of the errors, which occur in the far-field, have been developed employing asymptotic approximations. Techniques to minimize or control for errors introduced when the spatial resolution of the computation grid does not exactly represent the boundaries of the simulated material are in development. Also being pursued are code revisions to exploit the concurrency opportunities made possible by the increasing availability of multi-core hardware platforms.

Another focus area is the modeling of spin momentum transfer to magnetic domain walls arising from electric current flow. This spintronic effect is expected to play an important role in the near-term development of magnetic memory and logic devices. A project starting within ITL's Virtual Measurement Systems program is expected to produce a standard problem suitable to establish confidence in our ability to simulate this phenomenon.

**Funding:** *NIST Innovations in Measurement Science.*



## Time-Domain Algorithms for Computational Electromagnetics

Bradley Alpert  
Andrew Dienstfrey

<http://math.nist.gov/AlgoCEM>

Acoustic and electromagnetic waves, including radiation and scattering phenomena, are increasingly modeled using time-domain computational methods, due to their flexibility in handling wide-band signals, material inhomogeneities, and nonlinearities. For many applications, particularly those arising at NIST, the accuracy of the computed models is essential. Existing methods, however, typically permit only limited control over accuracy; high accuracy generally cannot be achieved for reasonable computational cost.

Applications that require modeling of electromagnetic (and acoustic) wave propagation are extremely broad, ranging over device design, for antennas and waveguides, microcircuits and transducers, and low-observable aircraft; nondestructive testing, for turbines, jet engines, and railroad wheels; and imaging, in geophysics, medicine, and target identification. At NIST, applications include the modeling of antennas (including those on integrated circuits), waveguides (microwave, photonic, and at intermediate terahertz frequencies), transducers, and in nondestructive testing.

The objective of this project is to advance the state of the art in electromagnetic computations by eliminating three existing weaknesses with time domain algorithms for computational electromagnetics to yield: (1) accurate nonreflecting boundary conditions (that reduce an infinite physical domain to a finite computational domain), (2) suitable geometric representation of scattering objects, and (3) high-order convergent, stable spatial and temporal discretizations for realistic scatterer geometries. The project is developing software to verify the accuracy of new algorithms and reporting these developments in publications and at professional conferences.

Recently Alpert and Dienstfrey have collaborated to attack the problem of fast eigenfunction transforms that arises in some time-domain electromagnetics computations (as well as elsewhere). In particular, representations of functions as expansions of eigenfunctions from Sturm-Liouville differential equations, which enable efficient application of certain naturally-occurring operators, must themselves be obtained typically by transforming from pointwise function values. Recent progress in fast algorithms for these transformations, from many researchers and resulting in methods analogous to the fast Fourier transform (FFT) to compute the discrete Fourier transform, has not yet achieved the efficiency to enable widespread acceptance of these new methods. Many of

the methods rely on a divide-and-conquer approach that requires repeated interpolation of functions having a prescribed form and it is this operation that consumes the majority of the computation time in a transformation. Alpert and Dienstfrey have discovered, from an identity satisfied by the Green's function of a Sturm-Liouville equation, a new fast algorithm for these interpolations. This algorithm is expected to outperform significantly the fastest existing method for interpolation, which is based on the fast multipole method.

Although these eigenfunction expansions are more specialized than Fourier expansions, they are essential for efficient computation in certain special settings, which include spherical or elliptical geometry, plane-polar representations, bandlimited signals, and a number of more unusual problems. The recent work is expected to result in faster transforms, as well as fast applications of certain related operators, that arise in these problems.

Earlier work of this project has been recognized by researchers developing methods for computational electromagnetics and has influenced work on these problems at Boeing and HRL (formerly Hughes Research Laboratories). It has also been cited widely, including by researchers at Brown University, Caltech, University of Colorado, University of Illinois, Michigan State University, University of Texas, Yale University, University of Basel, and Tsing Hua University.

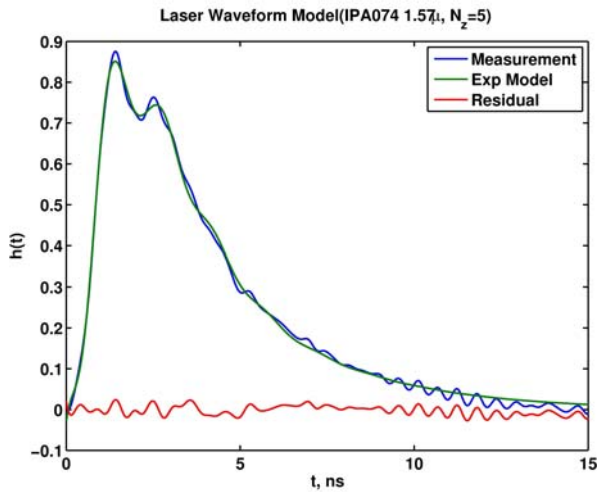
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## Laser Pulse Shape Measurement for Laser Guidance and Range Finding

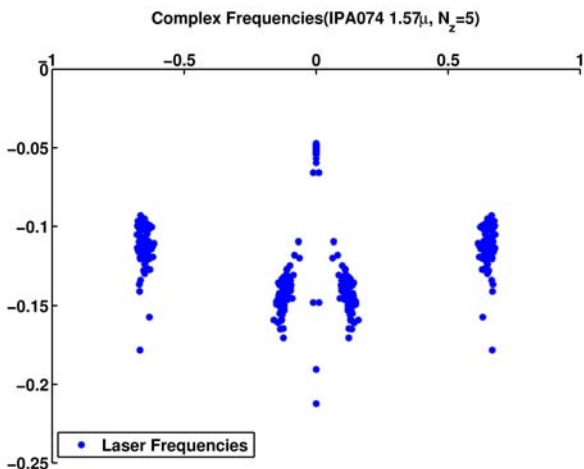
Andrew Dienstfrey  
Jack Wang (NIST ITL)  
Paul Hale (NIST EEEL)  
Rodney Leonhardt (NIST EEEL)

Laser target designators are used in a variety of military applications including range-finding and guidance technologies. As these technologies rely on measuring the reflectance of a far-away object in a battlefield environment with significant optical clutter, it is essential that the armed services have the capability to calibrate extremely sensitive *radiometers* (devices used for measurement of low-power optical signals). This capability is maintained through a coordinated effort involving private defense contractors, and measurement services provided by NIST. The current solution is predicated on the ability to model the relevant laser waveforms as having a *sufficiently broad, Gaussian shape*. In saying this, two fundamental constraints are in effect. One is that the laser waveform is symmetric about its peak. The other is that the ratio of the characteristic time of the laser waveform (e.g., the full-width-

half-max time) to the response time of the radiometer is much greater than one, i.e., the radiometer is fast relative to the optical signal it measures. These two assumptions allow one to model the waveform measurement process as a relatively simple rescaling operation.



**Figure 1.** Example of laser measurement, exponential model, and the residual error. The combination of the prominent secondary lobe and fast laser pulse ( $\approx 5$  ns) results in a non-trivial convolution between waveform and the radiometer response function.



**Figure 2.** Complex frequencies resulting from non-linear fit of measured waveform data for  $1.57 \mu\text{m}$  laser.

Recent changes in Department of Defense (DoD) policy require that next-generation laser target designators operate in the “eye-safe” wavelength region,  $\lambda \approx 1.5 \mu\text{m}$ . To meet this requirement, based on proprietary design considerations, the contractors that manufacture the test sets for verifying operation of these target designators now generate laser waveforms that deviate substantially from a Gaussian shape. Furthermore, the characteristic times of the lasers have

been measured to be on the order of 6 ns. By contrast, the next generation radiometers designed and built by NIST to meet the extreme sensitivity requirements of this application have impulse response times between 3 to 5 ns. Thus, both of the previous assumptions, symmetric laser pulse shape and relatively fast instrument response, are violated.

In the spring of 2007, the DoD Coordinated Calibration Group (CCG) contracted the NIST Waveform Metrology Team to perform a detailed study of options available to calibrate this next generation of laser target designators. As a first step, hundreds of representative laser waveforms were measured using a variety of techniques. One of these measurements involved running the laser in a high-power mode in which case the optical output could be measured with a “fast” photo-detector (as opposed to the radiometer which is extremely sensitive but slow.) After deconvolution of the detector response function from the measured waveform, we are confident that we have an accurate measurement of the laser waveform shape. Based on this shape, and subsequent analyzes, NIST is currently reviewing a hierarchy of calibration strategies for the CCG. These strategies entail different levels of complexity with corresponding cost-accuracy trade-offs. NIST is considering performing extensive simulations to better quantify these trade-offs. Of fundamental importance for this effort is sufficiently accurate description of the laser waveform shape.

In the fall of 2007 Andrew Dienstfrey explored the possibility of modeling the waveforms as a sum of damped exponential modes,

$$h(t) = \sum_1^N \hat{h}_n \exp(i2\pi f_n t),$$

where the order  $N$ , expansion coefficients  $\hat{h}_n$ , and complex frequencies  $f_n$  are unknowns. Models of this form are suggested by physical motivations. Estimation of the parameters entails a nonlinear step which solves for the unknown frequencies, followed by a linear least-squares solve for the expansion coefficients. One such routine was implemented which accomplishes the nonlinear solve by eigenvalue analysis of a suitable matrix. A typical measured laser waveform, a five term exponential fit, and the residual are shown in Fig. 1. Anticipating that this degree of approximation error is acceptable for the present application, several hundred waveforms were analyzed. The resulting distribution of complex frequencies for a particular class of lasers is shown in Fig. 2. From this plot it appears the frequencies exhibit natural groupings in regions of the complex plane. This would suggest the possibility to model a “typical” laser waveform as a sum of damped exponentials with frequencies drawn from of an empirically determined multivariate, complex distribution.

In 2008 we will pursue developing and validating an exponential model for laser waveforms as described above. Pending success, the model will be used to validate and quantify the accuracy of calibration strategies that NIST will propose to the CCG. This research is partially sponsored by the 2004 competence proposal, “New Paradigms in High-Speed Waveform Metrology” and the 2007 Coordinated Calibration Group proposal, “Proposal for laser pulse shape measurement system to support 1.5 micron low-level pulsed-laser metrology”.

**Funding:** *NIST Innovations in Measurement Science. US Department of Defense Coordinated Calibration Group.*

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## Modeling of Optical Spectra

*Peter Ketcham  
Eric Shirley (NIST PL)*

Among the materials exploited by optical technology are crystalline materials with useful properties in the ultraviolet spectral range. These materials are incorporated into ultraviolet optical systems and optoelectronic devices that have relevance to photolithography and the

semiconductor manufacturing industry. However, these materials are not fully understood and significant experimental uncertainties exist in their ultraviolet optical properties. In conjunction with the NIST Physics Lab, MCSD is performing first-principle calculations of the optical properties of these materials. Advanced theoretical models of the optical properties are based upon the absorption of a photon and the production of an electron-hole pair. Simpler models, which do not take electronic excitations into account, may fail to give quantitatively accurate results. The inclusion of electron-hole interactions in the theoretical model involves extensive computations which in turn demand high-performance computing systems.

P. Ketcham is currently collaborating with E. Shirley (NIST PL) to realize these theoretical models on multicore, multiprocessor, large-memory, high-performance computing systems. A message-passing approach has been chosen and the LAM implementation of the message-passing interface (MPI) provides the parallel programming software platform. Progress has been made in developing prototype parallel codes that call the MPI libraries from the C programming language under the Linux operating system.

## Mathematical Applications: Chemistry and Biology

### Modeling of Photochemical Reactions in a Focused Laser Beam

Fern Y. Hunt

A.K. Gaigalas (NIST CSTL)

Fluorescent techniques are widely used to measure and detect phenomena in the chemical, biomedical and material sciences. However the accuracy and sensitivity of these materials is severely limited by photodegradation — the photochemical reactions that transform excited fluorophores into a non-fluorescent species. Photodegradation is the result of a combination of processes that occur on multiple time scales. Therefore, experimental investigation and determination of the photodegradation rate has been quite difficult. For the past two years Fern Hunt has collaborated with A. Gaigalas and co-workers of CSTL to develop mathematical analyses that facilitate an experimental frequency domain based photodegradation measurement technique developed by Gaigalas *et al.*

Starting with a coupled pair of partial differential equations that model the dynamics of fluorescent decay in the course of the frequency domain experiment, we were able to obtain a dramatic simplification of the model using singular perturbation techniques and averaging. Our model incorporates the continuous entry of fluorescent fluid into the measurement apparatus at its base as well as the excitation of the fluorescent particles by a periodically fluctuating laser light located at the apparatus center. Previous work by others neglected the boundary conditions and assumed uniform illumination of the region.

Our simplifications can (in large part) be justified rigorously and as a result we derived a functional form that can be used to fit phase shift measurements as a function of laser frequency. A description of this analysis was finalized and appeared in [1]. This past year, we showed that the fit parameters are related to characteristics of the apparatus and physical constants of the experiment. This enabled us to obtain good quantitative as well as qualitative agreement with experimental results including known photodegradation rates [2].

- [1] A.K. Gaigalas, F.Y. Hunt, and L. Wang, Modeling of Photochemical Reactions in a Focused Laser Beam, *Journal of Research of NIST* **4** (2007), pp. 191-208.
- [2] A.K. Gaigalas, F.Y. Hunt, and L. Wang, Interpretation of Measurements of Photochemical Reactions in Focused Laser Beams—Part 2, in preparation.

### Optical Coherence Tomography for Biomedical Imaging

Andrew Dienstfrey

Tasshi Dennis (NIST EEEL)

Shelle Dyer (NIST EEEL)

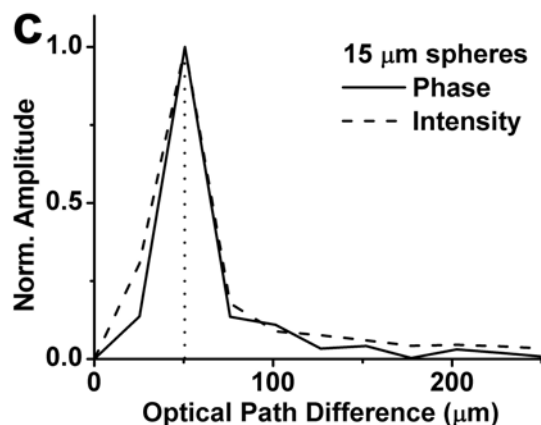
Paul Williams (NIST EEEL)

Biomedical imaging techniques are increasingly being developed for diagnosis and monitoring of a wide range disease models. Well-known modalities include: MRI, PET scans, and quantitative x-ray tomography (qCT). Recently, optical coherence tomography (OCT) has been added to this list as it has been demonstrated to give quantitative structural information pertaining to biological scatterers. One proposed application has been to use OCT as a diagnostic tool for cancer.

Over a range of optical frequencies and electromagnetic constitutive parameters, it has been shown that cell nuclei are the dominant contributors to the back-scattered radiation. Thus, measurements of this scattering can be inverted for nuclei features, for example the characteristic size. As many epithelial cell cancers (e.g., cervical, esophageal, colon, skin, oral) exhibit enlarged cell nuclei as a precancerous condition, it is hoped that a fiber-based OCT technique could serve as an early diagnostic tool for these disease models. Additional biomedical uses of OCT currently being investigated include: imaging of cellular substructures, assessment of the efficacy of chemopreventative agents, and measurement of characteristics of large-scale intracellular organization.



**Figure 1.** A micrograph of a sphere-nanotube phantom created by NIST. The polystyrene sphere has a diameter of approximately 8  $\mu\text{m}$  and is attached to a tungsten probe tip by a 100 nm double-wall carbon nanotube. This structure was used to compare measured scattering data with analytic results from Mie theory.



**Figure 2.** Sizing distribution for 15  $\mu\text{m}$  diameter (as stated by manufacturer) polystyrene spheres measured by NIST swept-source OCT. The optical path difference is the product of the sphere diameter and the refractive index. The peak corresponds to a sphere diameter of 15.5  $\mu\text{m}$  1.4  $\mu\text{m}$ .

This past year A. Dienstfrey continued collaboration with S. Dyer, T. Dennis, and P. Williams in NIST's Optoelectronics Division to investigate the quantitative potential of this technology. A phantom consisting of a single sphere scatterer was created and measured using the NIST-developed swept-source OCT system. The polystyrene sphere was approximately 8.5  $\mu\text{m}$  in diameter and was attached to a tungsten probe tip by a multi-wall carbon nano-tube with a 100 nm diameter. (See Fig. 1). To our knowledge this is the first nanoscale spherical phantom to be developed and measured. This research could serve as a prototype for sensitive optical scattering measurements based on single sphere geometries at scales and optical parameters of biological significance. Returning to the spherical imaging measurements of last year, the data was analyzed more completely taking into account several sources of uncertainty. This analysis revealed that the current NIST OCT system is capable of measuring diameters of polystyrene spheres as small as 15.5  $\mu\text{m}$  with an uncertainty of  $\pm 1.4 \mu\text{m}$  or 9%; see Fig. 2). The results of this research were accepted for publication [1].

- [1] T. Dennis, S. D. Dyer, A. Dienstfrey, S. Gurpreet, and P. Rice, Analyzing Quantitative Light Scattering Spectra of Phantoms Measured with Optical Coherence Tomography, *Journal of Biomedical Optics*, to appear.

## Accuracy and Standards for X-ray Measurements of Bone Mineral Density

Andrew Dienstfrey

Tammy Oreskovic (NIST MSEL)

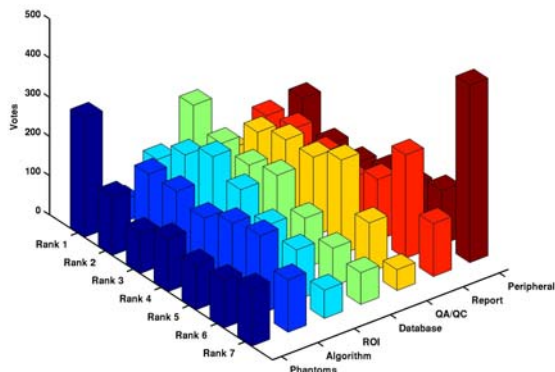
Lawrence Hudson (NIST PL)

Herbert Bennett (NIST EEEL)

Bone mineral density (BMD), as measured by dual-energy x-ray absorptiometry (DXA), is the principle biomarker used for assessing bone health and fracture risk, and for diagnosis and treatment monitoring of bone-related diseases such as osteoporosis. Currently no national, cross-manufacturer standards exist for assessment of the accuracy of DXA measurement of BMD. Fundamental problems include the questionable absolute accuracy of, and lack of cross-calibration among, DXA systems; cross-vendor studies of the same subject show that BMD results can vary by up to 18%. Bone-mineral densities reported for patients in  $\text{g}/\text{cm}^2$  have no traceability to the international system of weights and measures. This lack of comparability stifles commercial competition—clinics are hesitant to switch to new hardware because it introduces an unknown connection to previous results. It also inhibits the free flow of patients and their histories. This situation threatens the credibility of a growing industry, and has implications for patient care, regulation, Medicare and insurance reimbursement, and drug discovery.

Improvements in DXA BMD measurement accuracy would have significant economic and societal impact. As stated by the National Osteoporosis Foundation, osteoporosis threatens an estimated 44 million Americans, 10 million of whom may already have the disease. Almost 34 million more are estimated to have low bone mass, placing them at increased risk for osteoporosis. The annual direct care costs for osteoporotic fractures range from \$12 to \$18 B per year. Indirect costs (e.g., lost productivity for patients and caregivers) likely add billions of dollars more. These costs may double or triple in the coming decades as the average age of the US population increases.

The Surgeon General's *Report on Osteoporosis and Bone Health* (2004) cites DXA variability as a fundamental limitation in BMD measurements. The NIST Bone Health Team was formed in 2005 as a United States Measurement Services (USMS) team to assess DXA technology. The problem is difficult technically due to: (1) an incomplete understanding of the X-ray physics of the soft and hard tissues responsible for bone-health and its structural and mechanical properties, and (2) proprietary algorithms used by manufacturers to analyze the radiograph scans, isolate regions of interest, and determine the areas of the defined regions.



**Figure 1.** More than 1000 persons from North America and Europe responded to the NIST-ISCD survey. Respondents were asked to rank seven items in order of importance: phantoms, image-analysis algorithms, region of interest selection, database, quality assurance and control, DXA report quantities, and peripheral DXA technology.

It is important for NIST to develop a thorough understanding of the technology and its shortcomings prior to embarking upon and reaching any technical, measurement-based conclusions. In 2007, as a follow-on to the report documenting the 2006 USMS Workshop on Bone Health [1], NIST and the International Society of Clinical Densitometry (ISCD) designed and issued a web-based survey to further define the problems and potential NIST role in this technology. Over 1000 respondents ranked sources of error in order of importance. Preliminary results of the survey are shown in Fig. 1. In parallel, correspondences were established with world experts in DXA and bone health including researchers from: University of California at San Francisco, Johns Hopkins, Case Western University, and the Institute of Medical Physics at the University Erlangen-Nuernberg.

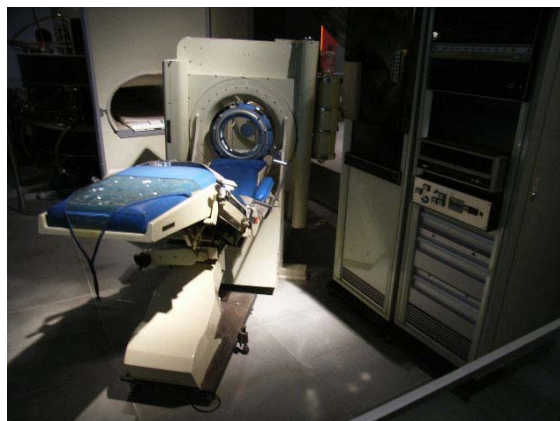
In 2008 we will complete the analysis of the survey, and work to achieve a consensus between those results and expert opinions. A proposed budget initiative is currently being developed by NIST's Physics Lab to provide support for this work in the future.

- [1] H. S. Bennett, A. Dienstfrey, L. T. Hudson, T. Fuerst, and J. Shepherd, Standards and Measurements for Assessing Bone Health – Workshop Report Co-sponsored by the International Society for Clinical Densitometry (ISCD) and the National Institute of Standards and Technology (NIST), *Journal of Clinical Densitometry* 9(4) (Oct. 2006), pp. 399-405.

## Monitoring and Modeling Change in Lung Tumors

Adele Peskin  
 Javier Bernal  
 David Gilsinn  
 Terence Griffin  
 John Kelso  
 Judith Terrill  
 Alden Dima (NIST ITL)  
 Charles Fenimore (NIST ITL)  
 Karen Kafadar (CU Denver)

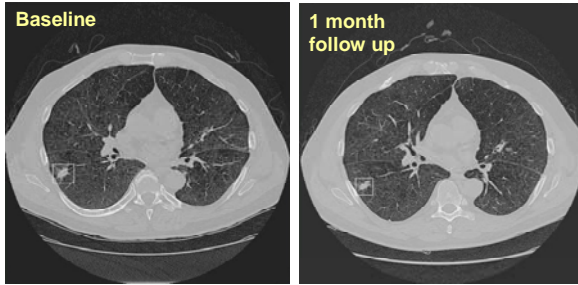
Lung cancer is a disease of uncontrolled cell growth in tissues of the lung. It is the most common cause of cancer related deaths in men and second most in women and is responsible for 1.3 million deaths worldwide annually. Tumors may be seen in chest X-ray and computed tomography (CT); see Fig. 1. The latter provides a sequence of 2D images by section (Fig 2). A diagnosis is usually confirmed by biopsy. Treatments include surgery, chemotherapy, and radiotherapy. With treatment, the five-year survival rate is 14%.



**Figure 1.** A typical CT scanner.

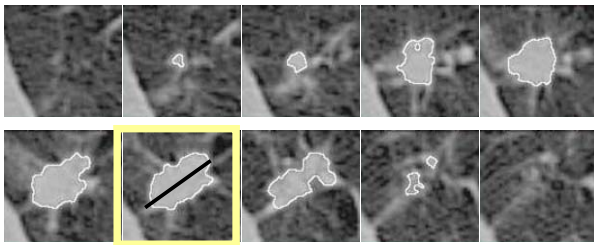


**Figure 2.** CT scan of a lung section

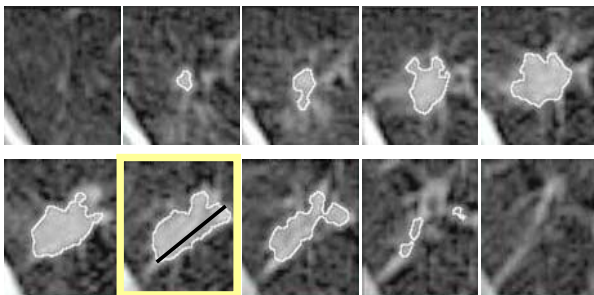


**Figure 3.** Preliminary CT scan (left) with tumor identified by a box outline at lower left, and scan of the same patient one month later (right).

Detection of lung tumors by computerized tomographic (CT) imaging presents a number of different challenges. There are currently a large number of different methods in use for measuring tumor growth by comparing CT scans taken at different points in time. A scarcity of useful data in the medical imaging community has led to variable results for tumor growth measurements. The work in our group for this project is two-fold: we are developing a common database of medical images containing tumors of known size on which to test measurement techniques, and we are working on a new method of measuring tumor growth using this data.



**Figure 4.** A diameter measurement of the tumor from the baseline scans, one of which shown in Fig. 3 (left). Estimated diameter was 17.7 mm.



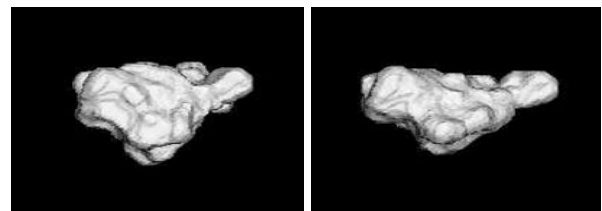
**Figure 5.** A linear measurement of the same tumor one month later showing a slight decrease in the linear size. In this case the measurement was 17.1 mm, a decrease in size of about 3%.

Trained medical radiologists examine the individual CT scans from a patient over several scan sessions and determine abnormal tissue. They assist drug companies in clinical test of new drugs. They determine the effect of drug treatments on patients.

Radiologists currently estimate change by measuring linear distance across scans. Volume change is now considered a better measure of drug effect. The need for this change in tactics is illustrated in the following figures where linear measurements and volume measurements of an actual tumor are compared.

Figs. 4 and 5 show a small cancer tumor outlined in a box in the lower left of the images. These two images were taken a month apart. Radiologist performed linear measurements of the two tumors. These are shown as lines across small portions of ten scans covering the volume of the tumor identified above. These linear measurements are made across the CT scan section with what the radiologist considered the largest diameter portion of the tumor.

Solid models of the tumors from the preliminary scan and the one month follow up (Fig 6) show a much larger estimate of a decrease in the size of the tumor. In the case of these two scans the estimate of tumor reduction is nearly 40% by using volumes as opposed to 3% using linear measurements.



**Figure 6.** Preliminary volume estimated as 886 mm<sup>3</sup> (left), and volume estimate one month later is 525 mm<sup>3</sup> (right)

The Food and Drug Administration (FDA) is currently involved with the study of lung cancer and has developed simulated human torsos and simulated lung cancer tumors of known dimensions and volumes, called phantom nodules. Reference phantom nodules, with or without noise, such as spheres, ellipsoids, etc will be placed in these simulated torsos and CT scans made to determine whether accurate volumes can be estimated from CT scan slices.

This year we have begun an effort to study the measurement of lung cancer tumors. We are approaching this on two fronts. To be able to compare methods for estimating volumes a reliable source of realistic CT data with tumors of known volume is needed. To obtain this, we are embedding known, simulated or phantom tumors into existing CT scan data obtained from Cornell University. This work is currently going on in the MCS D Scientific Applications and Visualization Group.; see page 49. We are also studying methods to estimate tumor volumes from existing data.

**Modeling Lung Tumors.** Estimating volumes from 2-D scans is a challenging problem. For many of the CT scanners in use the spacing between scans can run 3 mm thus providing voids in between scans. The approach used in many CT software packages is to count

up the small volumes, or voxels, associated with pixels within the regions of interest. Depending on the size of these small volumes they may overlap non-tumor volumes at the boundaries and give a possibly erroneous volume estimate. As a result, we are investigating other methods of volume estimation. Two approaches based on extracting  $(x, y, z)$  data representing points on the boundary of the object are being considered.

Scans using fine resolution CT's, called micro CT's, will be used to scan reference objects and a segmentation algorithm will be applied to these scans to identify the objects. Looking at CT scans as density objects, a technique will be developed to identify boundary of an embedded object. From this, a series of  $(x, y, z)$  data points on the edge will be obtained. From this, estimates of the volumes of the embedded objects will then be computed in several ways in order to determine an optimal approach to volume estimation.

Two of the FDA phantom nodules have been given to NIST to have researchers in MEL use coordinate measuring machines (CMM's) to measure points on the surface and estimate volumes from the probed points. Since the phantom nodules were near spherical, MEL attempted to fit spheres to the data, but experienced relatively large residual errors. MEL sent their measured data to us to determine whether other methods could be used to model the data more accurately. We are currently considering using multi-dimensional B-splines to model the near spherical phantom nodules. Work is continuing along this line.

An early, although crude method, to estimate volumes directly from scan images relied on the idea of computing the volume of cylinders of different sizes stacked one on top of the other. The volume of a simple cylinder is just the area of a base times the height. If a radiologist outlines a tumor on each scan in a session by designating the boundary points then the area of an outlined scan can be computed by methods of either multivariate calculus or computational geometry as

$$A = \frac{1}{2} \sum_{i=1}^{n-1} (y_{i+1}x_i - x_{i+1}y_i),$$

where the summation is taken over boundary points taken in order. Each of these areas can be multiplied by the distance between scans and those volumes summed to generate an estimate of the volume.

The two outlined tumor scans in Figs. 7 and 8 indicate how crude an estimate this can be however. There is clearly a large discontinuity between the two outlined tumors that requires some form of a continuation or smooth mapping in between. Some current work is concentrated on developing functional form models using B-splines for each of the outlines and then using a mapping technique called a homotopy to map one boundary function to the other and thus gen-

erating a reasonable transition model of the volume of the tumor between the two scans.

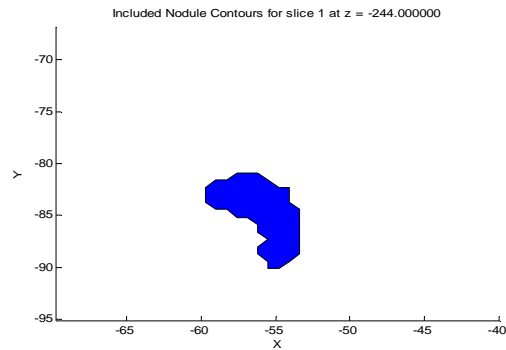


Figure 7. An outline of a tumor on one scan

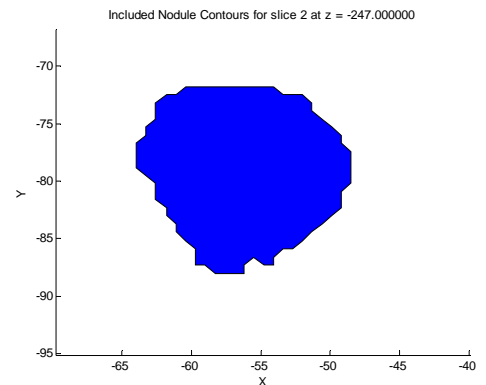


Figure 8. Outline of the same tumor in a scan 3 mm below the previous.

For a sufficiently dense set of points on the surface methods of computational geometry based on tetrahedralization can be used to estimate volume. The so-called Power Crust method is under study. One of these modeled data sets is shown below.

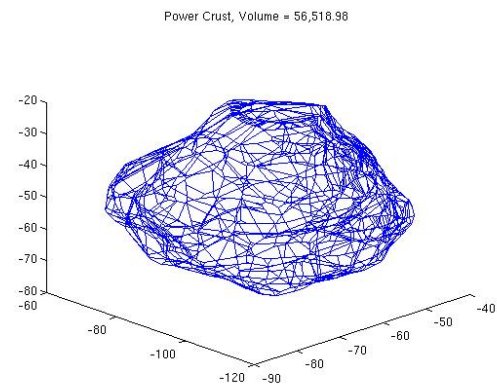


Figure 9. A triangulated surface of a lung cancer tumor data set.

**Associated ITL Program:** *Information Discovery, Use and Sharing.*

**Funding:** *Biomedical Imaging ACI Initiative (2007).*



## Computational Biology and Cell Imaging

*Adele Peskin*

*Javier Bernal*

*David Gilsinn*

*Alden Dima (NIST ITL)*

*John Lu (NIST ITL)*

*Jim Filliben (NIST ITL)*

*Anne Plant (NIST CSTL)*

*John Elliot (NIST CSTL)*

*Michael Halter (NIST CSTL)*

Cell images are obtained by phase-contrast microscopy over extended periods of time. The resulting database of image frames can typically produce gigabytes of data and tens of thousands of images. This makes some form of automated image tracking and analysis critical. There are two parallel efforts within this recently initiated project.

The first effort involves identifying precise boundaries of static images of cells that have been made to fluoresce with a red intensity with one treatment and can then be treated subsequently in order to identify specific cell nuclei. This work primarily will involve development and application of image segmentation algorithms.

In a separate effort, there is work involved to identify the distribution of cell image intensities as the cells begin to split. This involves identifying cell motions throughout many images taken over hours. Not only does this effort involve time series analysis of intensity data, but it involves studying diffusion models of cell motion. There has been recent work in the literature using level set methods to model cell motion. At the moment a review of the current state of cell motion modeling is underway.

**Associated ITL Program:** *Information Discovery, Use and Sharing.*

## **Mathematical Applications: Information Technology**

### **Automated Combinatorial Testing for Software Systems**

*Raghu Kacker*

*Jeff Yu Lei*

*James Lawrence*

*Michael Forbes*

*Richard Kuhn (NIST ITL)*

*Vincent Hu (NIST ITL)*

*Richard Rivello (NIST ITL)*

*Tao Xie (North Carolina State University)*

*Renee Bryce (University of Nevada Las Vegas)*

*Sreedevi Sampath (UMBC)*

*Sagar Chaki (Carnegie Mellon University)*

*Arie Gurfinkle (Carnegie Mellon University)*

**See feature article, page 38.**

**Funding:** *Cyber Security ACI Initiative (2007).*

### **Foundations of Measurement Science for Information Systems**

*Ronald F. Boisvert*

*Isabel Beichl*

*Brian Cloteaux*

*John Hagedorn*

*Fern Y. Hunt*

*Raghu Kacker*

*James Lawrence*

*Roldan Pozo*

*Judith Terrill*

*Vladimir Marbukh (NIST ITL)*

*Anoop Singhal (NIST ITL)*

Modern information systems are astounding in their complexity. Software applications are built from thousands of interacting components. Computer networks interconnect millions of independently operating nodes. Large-scale network-based applications provide the basis for critical services of national scope, such as financial transactions and electrical power distribution. In spite of our increasing reliance on such systems, our ability to build far outpaces our ability to secure. As a result, much of our cyber infrastructure is in peril. Communication protocols controlling the behavior of individual nodes lead to unexpected macroscopic behavior, such as waves of network congestion. Local anomalies in power grids propagate in unexpected ways leading to large-scale outages. Vulnerabilities in individual computer systems are exploited in viral at-

tacks resulting in widespread loss of data and system availability. The cost of such events has already led to loss of productivity in the billions of dollars. The long term stability of our critical infrastructure and its resilience to attack is simply unknown.

The critical nature of this problem is widely recognized, and much research is being devoted to the hardening of existing computer infrastructure. However, most of this work is focused on the near-term, providing much needed tools to prevent malicious exploitation of vulnerabilities discovered in current systems. We will continue to remain vulnerable to cyber attack until we can develop a fundamental understanding of the nature of the information systems which we construct. We know, for example, that there are limits to what computers can do: there are functions that are simply not computable. What are the fundamental limits of security? What are the inherent properties of large-scale computing systems? How do these influence security and reliability? How can these be measured? Can such measurements be exploited to ensure the stability of our cyber infrastructure? In short, we are badly in need of an underlying measurement science for complex information systems.

Measurement science has long provided a basis for the understanding and control of physical systems. For example, the Carnot cycle relates elementary measurable properties of gas molecules to a fundamental limit of the efficiency of heat engines independent of their complexity. Similar types of deep understanding and insight are simply lacking for complex information systems. We have no way to relate macro-scale phenomena to measurable properties of the components from which large-scale information systems are built. How do information systems grow? What macro-scale phenomena can they give rise to? Under what circumstances are they stable? When and how do they exhibit phase transitions? The basis for such understanding is beginning to emerge from the study of abstract models of information system structure and dynamics. If such study can lead to the identification of fundamental measurement quantities, then improved methods of design, monitoring, and, ultimately, control can be considered.

In this program, initiated this year, we will begin to develop the theoretical foundations needed for the emergence of a true measurement science for complex information systems. The basis for such work will be found in the fields of discrete mathematics, theoretical computer science, as well as in models and approaches utilized in the physical and biological sciences. We will develop and analyze abstract mathematical models of information system structure

and information flow. In this regard, the study of combinatorial structures (e.g., abstract networks and graphs), probability, information theory, dynamical systems, and control theory will be central. Relevant models will be studied using the emerging theory of discrete random processes, graph theory, queuing theory, and modern Monte Carlo based computational approaches. Such fundamental work will be applied to the study of complex information systems, such as computer networks and distributed systems. An important goal of this work will be to identify and characterize fundamental measurable properties of complex information systems that are indicators of the inherent level of security (i.e., resilience to threats both known and unknown). In this regard, we will study emergent behavior in large-scale networks, network reliability theory, theories of trust, and the analysis and development of self-healing (homeostatic) systems.

To help frame the possibilities for this new research program, a one-day invitational workshop for senior leaders in the field was held on May 29, 2007. The purpose of the workshop was to assess the potential for a mathematical research program in this area, to suggest intermediate-level technical goals, and to identify external research programs with which collaboration would be appropriate. A panel of eight external experts was assembled to participate in a wide-ranging discussion with some 15 NIST staff members who also participated. A workshop report has been issued as a NIST Internal Report [1].

Several projects within MCSD were developed for the initial year of the program. These include the following.

- Methods for Characterizing Massive Networks  
*I. Beichl and B. Cloteaux*  
See description below.
- Analysis of a Distributed Protocol for Network Control  
*F. Hunt and V. Marbukh*  
See description below.
- Standard Reference Data for Complex Network research  
*R. Pozo*  
See description below.
- Visualization of Network Dynamics  
*J. Hagedorn and J. Terrill*  
See description page 65.
- Automated Combinatorial Testing for Software Systems  
*R. Kacker and J. Lawrence*  
See description above.

In addition, a project in the ITL Computer Security Division was also supported under this program:

- Modeling Network Vulnerabilities Using Attack Graphs  
*Anoop Singhal*

Today's computer systems face sophisticated attackers who combine multiple vulnerabilities to penetrate networks with devastating impact. The overall security of a network cannot be determined by simply counting the number of vulnerabilities. To accurately assess the security of networked systems, one must understand how vulnerabilities can be *combined* to stage an attack. We model such composition of vulnerabilities through *attack graphs*. By simulating incremental network penetration, and propagating attack likelihoods, we measure the overall security of a networked system. From this, we score risk mitigation options in terms of maximizing security and minimizing cost. We populate our attack graph models from live network scans and databases that have knowledge about properties such as vulnerability likelihood, impact, severity, and ease of exploitation. Our flexible model can be used to quantify overall security of networked systems, and to study cost/benefit tradeoffs for analyzing return on security investment [2].

- [1] I. Beichl and R. Boisvert, "Mathematical Foundations of Measurement Science for Information Systems: Report of a Planning Workshop," NISTIR 7465, October 24, 2007.
- [2] S. Noel, L. Wang, A. Singhal, and S. Jajodia, Measuring Security Risk of Networks Using Attack Graphs, submitted.

**Associated ITL Program:** *Complex Systems.*

**Funding:** *Cyber Security ACI Initiative (2007).*

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## Methods for Characterizing Massive Networks

*Isabel Beichl*  
*Brian Cloteaux*  
*Francis Sullivan*

A type of data of increasing importance in information technology is one that is based not on floating point values but rather on connections between objects which can be modeled as graphs or networks. Such complex systems arise in many areas such as the power grid, the Internet, communications, and transportation networks. In all these cases, resources are delivered through restricted channels and reliability is critical. We have begun an effort to develop measurement techniques and tools for characterizing such objects based on sound mathematical methods. In most cases, the size of these objects makes exact measurement impossible.

We are in the process of building novel computational tools to generate meaningful statistics about real networks to yield fundamental measures of reliability.

We have developed Monte Carlo methods based on sequential importance sampling to count the number of spanning trees of a graph along with all subforests with  $k$  edges for each  $k$ . There already exists a method to count all spanning trees of a graph, which uses the determinant of a particular matrix. This is impractical for the size of network we are measuring. However, it has allowed us to test our methods on smaller data. We have also tested our method on real-world examples for which the determinant method cannot be used, e.g., representations of the Internet at the autonomous systems level. This is a graph with 24,566 nodes and 102,946 edges obtained from a database at UCLA.

In the process of this investigation, methods to compute with numbers whose size is such that they can only be represented in practice by their exponent have been developed.

We have used this information to compare the results with a random graph having the same degree sequence as the original data. The random graph with a given degree sequence was generated by a program we developed based on the Blitzstein-Diaconis method, enhanced to include the requirement that the resulting graph be connected. The object was to determine the validity of results obtained by generating random graphs that are “similar” to actual data. The random graph approach to modeling real data is widely used by some research groups. Our preliminary conclusion is the unsurprising but important one—random graphs don’t capture important details contained in real data.

**Associated ITL Program:** *Complex Systems.*

**Funding:** *Cyber Security ACI Initiative (2007).*

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## Analysis of a Distributed Protocol for Network Control

*Fern Y. Hunt*

*Vladimir. Marbukh (NIST ITL)*

Congestion control is critical to the (smooth) functioning of modern communication networks in particular and the Internet in general. The goal of congestion protocols is to allow many users to share network resources without causing congestion collapse. In addition it is desirable to use as much of the available network capacity as possible and ensure some fairness among users. In was shown by Frank Kelly and later many others that achievement of these objectives can be represented as a global optimization problem of system utility where some notion of fairness could be expressed by a choice of utility function.

Congestion control can then be seen as a distributed iterative solution to this problem (Lin and Shroff). Recently Vladimir Marbukh considered the problem of appropriately routing traffic networks within the TCP/AQM protocol and he proposed the introduction of controls that randomly assign routes to traffic in a way that minimizes the mean link load. Simulations of his ideas show that by adjusting the degree of randomness one can optimize network performance and avoid the “route flapping” phenomenon where traffic switches between one or more links with the minimum load at a given point in time. A straightforward representation of the corresponding optimization problem is not convex. This year we reformulated it as a convex optimization problem and we are now in the process of examining the stability of the optimal points as a function of the randomness parameter. We hope to be able to extend the analysis to the dynamics of the protocol examining its behavior when the number of users is large. We also hope to formulate an appropriate fluid limit description in this setting.

- [1] V. Marbukh, “Decentralized Control of Large-Scale Networks as a Game with Local Interactions: Cross-layer TCP/IP Optimization (preprint 2007).

**Associated ITL Program:** *Complex Systems.*

**Funding:** *NIST Innovations in Measurement Science. Cyber Security ACI Initiative (2007).*

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## Standard Reference Data for Complex Network Research

*Roldan Pozo*

The study of complex or “self-organizing” networks is a relatively young, yet active research area. Much of the focus is to determine how graphs from “real” phenomena (such as protein interactions, social networks, structure of the World Wide Web, etc.) differ from synthetic or “engineered” graphs that are constructed by design. Clearly they are different, but how? Three key metrics (clustering coefficient, graph diameter, and degree distribution) are commonly used in the literature, and these techniques have served as encouraging first steps, but further research is needed to yield more meaningful distinctions and truly understand the nature of these complex networks.

One fundamental question to ask, however, is what are the precise “real” graphs that are being used to drive these theories? Clearly, the conclusions being reached can be only as good as the quality and availability of the original data. Most papers provide little information about this, making any kind of comparison or verification of approaches difficult.

For example, a commonly studied collaboration network in the literature is the Movie Actor graph, where two movie actors are connected if they have worked together on the same movie. This information is usually culled from the Internet Movie Database (imdb.com). However, there is no single Movie Actor graph because this database is changing snapshot of the entertainment industry at any given time. Furthermore, what one chooses to count in their particular search (foreign films, documentaries, TV movies, specific epochs or genres) will generate different graphs. In fact, there are several of these Movie Actor graphs floating around in the literature, so a citation is not really meaningful unless it contains a timestamp and documentation of the specific queries used in its generation. A similar argument can be made for other association networks, such as co-author or citation graphs.

Another example is networks based on the structure of the World Wide Web. In this case, each web page is a node and two pages are connected if there a hypertext link from one to the other. These are typically generated by web crawlers and can vary greatly depending on where they crawl and what decisions they make about what constitutes a "link." For example: Do different anchors to the same page count as separate links? How are non-static pages handled? What file types are processed? How robust it is with broken links and sloppy HTML pages? This list can be quite long, and each decision path will yield a different graph. On top of this, the Web is, of course, not a static entity. Many of the Web graphs out there provide little of these details and usually present only the topological structure (i.e., URLs removed) so it is difficult to confirm or validate them independently.

Similar concerns exist for graphs taken from other application domains. Often the data is incomplete, poorly documented, or missing pieces crucial to its description. There are ongoing debates about whether particular networks are really scale-free or not, or whether the conclusions of some papers are actually valid. Usually these concerns lie at the heart of how data was collected and analyzed.

Our motivation for developing a standard reference data set for complex networks is to provide a collection of public and well-documented "real-world" graphs that serve as a test bed of reasonably validated data which researchers can utilize to (1) verify and compare the algorithms and analysis of various approaches in the literature, (2) to ensure that everyone is using the same reference data in their studies, (3) to have one convenient location where one can browse and search for network graphs of various characteristics, (4) to provide a focal point for the research community to contribute and exchange network graphs from various application domains, and (5) to provide a testbed for development of software analysis tools

(e.g., graphical viewers, graph partitioners, clustering algorithms) that will aid in the further development and research of complex networks. This effort was begun in mid FY 2007.

**Associated ITL Program:** *Complex Systems.*

**Funding:** *NIST Innovations in Measurement Science. Cyber Security ACI Initiative (2007).*



**Part IV**

**Activity Data**





## Publications

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30. R. Somma, H. Barnum, G. Ortiz, and E. Knill, "Efficient Solvability of Hamiltonians and Limits on the Power of Some Quantum Computational Models," *Physical Review Letters* **92** (Nov. 10 2006), Art. No. 190501.
31. Q. Wang, B. Saunders, and S. Ressler, "Dissemination of 3D Visualizations of Complex Function Data for the NIST Digital Library of Mathematical Functions," *CODATA Data Science Journal* **6** (2007), pp. S146-S154.

## Journal of Research of NIST

1. A. Gaigalas, F. Hunt, and L. Wang, "Modeling of Photochemical Reactions in a Focused Laser Beam," *NIST Journal of Research* **112** (4) (July-August 2007), pp. 191-208.
2. J. Hagedorn, J. Dunkers, S. Satterfield, A. Peskin, J. Kelso, and J. Terrill, "Measurement Tools for the Immersive Visualization Environment: Steps Toward the Virtual Laboratory," *NIST Journal of Research* **112** (5) (Sept.-Oct. 2007), pp. 257-270.
3. A. Kearsley and D. Cotrell, "Flow Control Through the Use of Topography," *NIST Journal of Research* **112** (3) (2007), pp. 1-9.
4. Z. Levine, A. Kearsley, and J. Hagedorn, "Bayesian Tomography for Projections with an Arbitrary Transmission Function with an Application to Electron Tomography," *Journal of Research of NIST* **111** (6) (Nov.-Dec. 2006), pp. 411-417.
5. G.B. McFadden, S.R. Coriell, K. F. Gurski, and D. L. Cotrell, "Convective Instabilities in Two Liquid Layers," *NIST Journal of Research* **112** (5) (Sept.-Oct. 2007), pp. 271-281.

## Other Invited Publications

1. I. Beichl, D.P. O'Leary, and F. Sullivan, "Your Homework Assignment: Monte Carlo Minimization," *IEEE Computing in Science and Engineering* **9** (1) (2007), pp 72-80.
2. I. Beichl, D.P. O'Leary and F. Sullivan, "Answers to Your Homework Assignment," *IEEE Computing in Science and Engineering* **9** (2) (2007), pp. 99-103.
3. J. Hagedorn, J. Dunkers, A. Peskin, J. Kelso, and J. Devaney Terrill, "Quantitative, Interactive Measurement of Tissue Engineering Scaffold Structure in an Immersive Visualization Environment," *Biomaterials Forum* **28** (4) (2006), pp. 6-9.
4. W. F. Mitchell, Review of "Understanding and Implementing the Finite Element Method," by Mark S. Gockenbach, *SIAM Review*, **49** (3) (2007), pp. 532-533.
5. J. Miltat and M. Donahue, "Numerical Micromagnetics: Finite Difference Methods," in *Handbook of Magnetism and Advanced Magnetic Materials*, Volume 2: Micromagnetism, (H. Kronmüller and S. Parkin, eds.), Wiley 2007.

## Conference Proceedings

1. T. J. Burns, S. P. Mates, R. L. Rhorer, E. P. Whitenon, and D. Basak, "Recent Results from the NIST Pulse-Heated Kolsky Bar, in *Proceedings of the 2007 Society for Experimental Mechanics Annual Conference*, Springfield, MA, June 3-6, 2007.
2. T. Dennis, S. D. Dyer, and A. Dienstfrey, "Phase-Dispersion Light Scattering for Quantitative Size-Imaging of Spherical Scatterers," in *Proceedings of SPIE Photonics West 2007* **6446** (Feb. 2007), San Jose, CA, January 20-25, 2007.
3. S. D. Dyer, L. K. Street, S. M. Etzel, T. Dennis, A. Dienstfrey, V. Tsvankin, and W. Tan, "Characterization of Cell Samples from Measurements of Spectroscopic Scattering Phase-Dispersion," in *Proceedings of SPIE Photonics West 2007* **6446** (Feb. 2007), San Jose, CA, January 20-25, 2007.
4. J. T. Fong, J. J. Filliben, and R. J. Fields, "An Uncertainty & Risk-based Approach toward a Cost-Effective High-Temperature Material Property Database," in *Proceedings National Nuclear Security Administration (NNSA) Future Technologies Conference II, Track Three (Materials Technology Trends for Defense & National Security)*, Oct. 11-12, 2006, Washington, DC.
5. J. T. Fong, J. J. Filliben, W. F. Ranson, and P. V. Marcal, "A Real-Time Non-Contact and Direct-Measurement-based Fatigue Life Prediction Methodology with Uncertainty & Risk Analyses," in *Proceedings National Nuclear Security Administration (NNSA) Future Technologies Conference II, Track Four (Future Trends in Analysis and Characterization)*, Oct. 11-12, 2006, Washington, DC.
6. J. T. Fong, J. J. Filliben, and R. J. Fields, "Uncertainty Quantification of Material Properties of Two Types of Steels at Elevated Temperatures for Stochastic Modeling of Structures on Fire," in *Proceedings of a Three Metals Society (TMS) Symposium on Innovations in Measurement Science to Assess the Performance of New Materials in the Real-World*, Orlando, FL, Feb. 25-Mar. 1, 2007.
7. A. Gaigalas, F. Hunt, K. Cole, and L. Wang, "Interpretation of Photochemical Reactions in Focused Laser Beams," in *Proceedings of the 8th WSEAS Conference on Mathematics and Computers in Biology and Chemistry* (2007), pp. 85-89.
8. Y. Lei, R. Kacker, D. R. Kuhn, V. Okun, and J. Lawrence, "IPOG: A General Strategy for T-Way Software Testing," in *14<sup>th</sup> Annual IEEE International Conference on Engineering of Computer-Based Systems*, Tucson, AZ, 2007, pp. 549 – 556.
9. N. S. Martys, C. F. Ferraris, V. Gupta, J.H. Cheung, J. G. Hagedorn, A. P. Peskin, E. J. Garboczi, "Computational Model Predictions of Suspension Rheology: Comparison to Experiment," in *Proceedings of the 12th International Conference on the Chemistry of Cement*, Montreal, Canada, July 8-13, 2007.
10. R. Radebaugh and A. O'Gallagher, "Modeling a Fast Cooldown Technique for Pulse Tube Cryocoolers," in *Proceedings of the Beijing International Congress of Refrigeration* (Aug. 2007), paper no. ICR07-A1-1319.
11. B. Rust and B. Thijsse, "Data-Based Models for Global Temperature Variations," in *Proceedings of the 2007 International Conference on Scientific Computing* (2007), Las Vegas, NV, June 25-28, 2007, pp. 10-16.
12. B. Saunders and Q. Wang, "From B-Spline Mesh Generation to Effective Visualizations for the NIST Digital Library of Mathematical Functions," in *Curve and Surface Design, Proceedings of the Sixth International Conference on Curves and Surfaces*, Avignon, France, June 29 – July 5, 2006, pp. 235-243.

## Technical Reports

1. I. Beichl and R. Boisvert, "Mathematical Foundations of Measurement Science for Information Systems: Report of a Planning Workshop," NISTIR 7465, October 24, 2007.
2. D. E. Gilsinn, "Approximating Periodic Solutions of Autonomous Delay Differential Equations," NISTIR 7375, November, 2006.
3. W. F. Mitchell, "PHAML User's Guide," NISTIR 7374, October, 2006.

## Accepted

1. J. B. Bowles, J. T. Fong, R. deWit, and J. J. Filliben, "Verification of a Finite Element Cantilever Beam Vibration model of a Micro- and Nano-Measurement Problem using a Metrology-based Approach," *Proceedings of ASME Pressure Vessels & Piping Conference*, San Antonio, TX, July 22-26, 2007.
2. A. S. Carasso and A. E. Vladar, "Calibrating Image Roughness by Estimating Lipschitz Exponents, with Applications to Image Restoration," *Optical Engineering*.

3. Y. Chao, J. T. Fong, P. S. Lam, and R. deWit, "Uncertainties in Transferring Fracture Toughness from Laboratory to Large Scale Structures," *Proceedings of ASME Pressure Vessels & Piping Conference*, San Antonio, TX, July 22-26, 2007.
4. D. L. Cotrell, G. B. McFadden, and B. J. Alder, "Effect of an Axially-periodic Radius on the Linear Stability of Pipe Flow," *Proceedings of the National Academy of Sciences*.
5. T. Dennis, S. D. Dyer, A. Dienstfrey, S. Gurpreet, and P. Rice, "Analyzing Quantitative Light Scattering Spectra of Phantoms Measured with Optical Coherence Tomography," *Journal of Biomedical Optics*.
6. D. G. Edwards, J. T. Fong, R. deWit, and J. J. Filiben, "Verification of a Stochastic Finite Element Cylinder-Impact Model of a Crashworthiness Problem using Response Surface Methodology and Fractional Factorial Design," *Proceedings of ASME Pressure Vessels & Piping Conference*, San Antonio, TX, July 22-26, 2007.
7. J. T. Fong, W. F. Ranson, III, R. I. Vachon, and P. V. Marcal, "A Non-Contact NDE Methodology for Prediction of Fatigue Failure," *Proceedings of ASME Pressure Vessels & Piping Conference*, San Antonio, TX, July 22-26, 2007.
8. J. T. Fong, R. deWit, G. B. Sinclair, and J. J. Filiben, "Verification of a Stochastic Finite Element Frictionless Contact/Rigid Indentor Model using a Metrological Approach and two Finite Element Codes, ANSYS and ABAQUS," *Proceedings ASME Pressure Vessels & Piping Conference*, San Antonio, TX, July 22-26, 2007.
9. J. T. Fong, and O. F. Hedden, eds., "Engineering Safety, Applied Mechanics, and Nondestructive Evaluation (NDE)," *Proceedings of an ASME Symposium on NDE in honor of Dr. Spencer H. Bush (1920-2005)*, *ASME 2007 Pressure Vessels & Piping Conference*, San Antonio, TX, July 25-26, 2007.
10. S. Glancy and H. M. Vasconcelos, Methods for Producing Optical Coherent State Superpositions, <http://arxiv.org/abs/0705.2045>, *Journal of the Optical Society of America B*.
11. N.K. Gupta, E.P. Shine, R.C. Tuckerfield, and J.T. Fong, "Validation of Computer Models for Nuclear Material Shipping Packages," *Proceedings ASME 2007 Pressure Vessels & Piping Conference*, San Antonio, TX, July 23-26, 2007, Paper No. PVP2007-26751.
12. F. Hunt, A. Gaigalas, and L. Wang, "Mathematical Derivation of a Model of the Frequency Domain Measurement Technique," *NIST Journal of Research*.
13. R. Kacker, "Comments on 'Bayesian Evaluations of Comparison Data' by Ignacio Lira," *Metrologia*.
14. R. Kacker, K.-D. Sommer, and R. Kessel, "Evolution of Modern Approaches to Express Uncertainty in Measurement," *Metrologia*.
15. A. Kearsley and W. Wallace, "New Approaches to Data Reduction in Mass Spectrometry," *MALDI and ESI Mass Spectrometry of Synthetic Polymers*, Liang Li (ed.), Wiley Interscience, 2007.
16. Y. Lei, R. Carver, R. Kacker, and D. Kung, "A Combinatorial Testing Strategy for Concurrent Programs," *Software Testing, Verification and Reliability*.
17. Y. Lei, R. Kacker, D. Kuhn, V. Okun, and J. Lawrence, "IPOG/IPOG-D: Efficient Test Generation for Multi-way Combinatorial Testing," *Software Testing, Verification and Reliability*.
18. L. A. Melara, A. J. Kearsley, and R. A. Tapia, "A Homotopy Method in the Regularization of Total Variation Denoising Problems," *Journal of Optimization Theory and Applications*.
19. B.R. Miller, "Creating Webs of Math Using LaTeX," *Proceedings 6th International Congress on Industrial and Applied Mathematics*, Zurich, Switzerland, July 17, 2007.
20. D. G. Porter and M. J. Donahue, "Precession Axis Modification to a Semi-analytical Landau-Lifshitz Solution Technique," *Journal of Applied Physics*.
21. A. C. E. Reid, R. C. Lua, R. E. Garcia, V. R. Coffman, and S. A. Langer, "Modeling Microstructures with OOF2," *International Journal of Materials and Product Technology*.
22. B. Rust and D. O'Leary, "Residual Periodograms for Choosing Regularization Parameters for Ill-Posed Problems," *Inverse Problems*.
23. B. Thijsse and B. Rust, "Freestyle Data Fitting and Global Temperatures," *Computing in Science and Engineering*.
24. J. Terrill, W. George, T. Griffin, J. Hagedorn, J. Kelso, M. Olano, A. Peskin, S. Satterfield, J. Sims, J. Bullard, J. Dunkers, N. Martys, A. O'Gallagher, and G. Haemer, "Extending Measurement Science to Interactive Visualization Environments," Chapter in *Trends in Interactive Visualisation: A State-of-the-Art Survey*, edited by Elena Zudilova-Seinstra, Tony Adriaansen and Robert van Liere, to be published by Springer, UK.

25. A. Youssef, "Methods of Relevance Ranking and Hit-content Generation in Math Search," *Proceedings of Mathematical Knowledge Management (MKM 2007)*, RISC, Hagenberg, Austria, June 27-30, 2007.

## Submitted

1. P. Barker, Y. Xiao, F. Hunt, and N. Glenn, "Whole Genome Amplification Improves FISH Hybridization with Bacterial Artificial Chromosome Cancer Biomarker Probes."
2. I. Beichl, S. Bullock, and D. Song, "A Quantum Algorithm Detecting Concentrated Maps."
3. T. J. Burns, S. P. Mates, R. L. Rhorer, E. P. Whinton, and D. Basak, "Recent Results from the NIST Pulse-Heated Kolsky Bar."
4. R. J. Epstein, S. Sedelin, D. Leibfried, J. H. Wensberg, J. J. Bollinger, J. M. Amini, R. B. Blakestad, J. Britton, J. P. Home, W. M. Itano, J. D. Jost, E. Knill, C. Langer, R. Ozeri, N. Shiga, and D. J. Wineland, "Simplified Motional Heating Rate Measurements of Trapped Ions."
5. D. E. Gilsinn, "On Algorithms for Estimating Computable Error Bounds for Approximate Periodic Solutions of an Autonomous Delay Differential Equation."
6. D. E. Gilsinn, "A Pseudospectral Approximation to the Fundamental Matrix of a Linear Delay Differential Equation with Periodic Coefficients."
7. C. M. Guttman, K. M. Flynn, and A. J. Kearsley, "Numerical Optimization of Matrix-Assisted Laser Desorption/Ionization Time of Flight Mass Spectrometry: Application to Synthetic Polymer Molecular Mass Distribution Measurement".
8. F. Y. Hunt, A. K. Gaigalas, and L. Wang, "Mathematical Derivation of a Model of the Frequency Domain Measurement Technique"
9. R. Kacker, "Classical and Bayesian Interpretation of the Birge Test of Consistency and Its Generalized Version in Interlaboratory Evaluations."
10. S. Kim, M. I. Aladjem, G. B. McFadden, and K.W. Kohn, "Fine Tuning of p53-Mdm2-MdmX Network by MdmX during DNA Damage Response."
11. E. Knill, D. Leibfried, R. Reichle, J. Britton, B. Blakestad, D. Jost, C. Langer, R. Ozeri, S. Seidelin, D. J. Wineland, "Randomized Benchmarking of Quantum Gates."

12. D. R. Kuhn, Y. Lei, R. Kacker, V. Okun, and J. Lawrence, "An Algorithm for Covering Arrays with Strength Larger than Three."
13. Y. Lei, R. Kacker, D. R. Kuhn, V. Okun, and J. Lawrence, "Two-deterministic Strategies for Multi-way Software Testing."
14. N. S. Martys, D. Lootens, W. George, S. Satterfield, J. Kelso, and P. Hebraud, "Spatial-Temporal Correlations in Concentrated Suspensions."
15. N. S. Martys, D. Lootens, W. George, S. Satterfield, J. Kelso, and P. Hebraud, "Stress Chains Formation Under Shear of Concentrated Suspensions."
16. S. P. Mates, R. L. Rhorer, E. P. Whinton, T. J. Burns, and D. Basak, "A Pulse-Heated Kolsky Bar Technique for Measuring Flow Stress of Metals Subjected to High Loading and Heating Rates."
17. R. Radebaugh, Y. Huang, A. O'Gallagher, and J. Gary, "Calculated Regenerator Performance at 4 K with Helium-4 and Helium-3."
18. J. Sims, W. George, T. Griffin, J. Hagedorn, H. Hung, J. Kelso, M. Olano, A. Peskin, S. Satterfield, J. Terrill, G. Bryant, and J. Diaz, "Advancing Scientific Discovery through Parallelization and Visualization III. Tightbinding Calculations on Quantum Dots."

## Presentations

### Invited Talks

1. I. Beichl, "Using SIS to Speed Up MCMC," DIMACS Workshop on Markov Chain Monte Carlo: Synthesizing Theory and Practice, Trenton, NJ, June 5, 2007.
2. T. Burns, "Bifurcation in Material Flow During High-Speed Machining," Sixth International Congress on Industrial and Applied Mathematics, Zurich, Switzerland, July 16-20, 2007.
3. T. Burns, "Measurement and Modeling of Rapid Shear in High-Speed Machining," SHEAR 07, International Symposium on Shear Behavior and Mechanisms in Materials Plasticity, Nancy, France, September 4-7, 2007.
4. M. J. Donahue, "Overview and Outlook of the OOMMF Micromagnetic Modeling Package," IEEE Magnetism in Nanotechnology and Electronics Conference, Gaithersburg, MD, June 25, 2007.
5. J. Fong, "Verification and Validation of a Life-Prediction Model for Safety Assessment of Critical

- Structures,” Department of Mechanical Engineering Seminar, University of South Carolina, Columbia, SC, Oct. 4, 2006.
6. J. Fong, “An Uncertainty & Risk-based Approach toward a Cost-Effective High-Temperature Material Property Database,” National Nuclear Security Admin (NNSA) Future Technologies Conference II, Track Three (Materials Technology Trends for Defense & National Security), Washington, DC, Oct. 11, 2006.
  7. J. Fong, “A Real-Time Non-Contact and Direct-Measurement-based Fatigue Life Prediction Methodology with Uncertainty & Risk Analyses,” National Nuclear Security Admin (NNSA) Future Technologies Conference II, Track Four (Future Trends in Analysis and Characterization), Washington, DC, Oct. 12, 2006.
  8. J. Fong, “Verification of Finite Element Simulations of Progressive Failure of Structures on Fire,” Department of Civil Engineering Seminar, Tufts University, Medford, MA, Oct. 27, 2006.
  9. J. Fong, “On the Feasibility of Verification, Standardization, and Certification of a Library of Computational Models,” 2007 High Level Simulation Languages and Application Conference of the Western MultiConference on Modeling and Simulation (WMC '07), San Diego, CA, Jan. 15, 2007.
  10. J. Fong, “Verification of a Stochastic Finite Element Cylinder-Impact Model of a Crashworthiness Problem using Response Surface Methodology and Fractional Factorial Design,” Department of Statistics Seminar, University of South Carolina, Columbia, SC, Jan. 29, 2007.
  11. J. Fong, “Uncertainty Quantification of Material Properties of Two Types of Steels at Elevated Temperatures for Stochastic Modeling of Structures on Fire,” Symposium on Innovations in Measurement Science to Assess the Performance of New Materials in the Real-World, during the 2007 Annual Meeting of the Minerals, Metals, and Materials Society (TMS), Orlando, FL, Feb. 27, 2007.
  12. J. Fong, “A Layered Software Approach using TrueGrid, Ls-Dyna, and Ls-Opt to Computational Modeling with Applications in Pressure Vessels and Piping Technology for Nuclear Waste Packaging and Transportation,” DoD Savannah River National Laboratory, Aiken, SC, April 12, 2007.
  13. J. Fong, “A Non-Contact NDE Methodology for Prediction of Fatigue Failure,” ASME Symposium on Engineering Safety, Applied Mechanics, and Nondestructive Evaluation (NDE), 2007 Pressure Vessels and Piping Technology Conference, San Antonio, TX, July 25, 2007.
  14. F. Hunt, “A Sample Path Result for a Class of Markov Decision Processes,” Stochastic Control and Dynamics Workshop, Mathematical Sciences Research Institute, Univ. California, Berkeley, CA, Mar. 27, 2007.
  15. F. Hunt, “A Markov Decision Process Result Motivated by a Multiple Sequence Alignment,” Stochastic Dynamical Systems and Control Workshop, Berkeley, CA, April 5, 2007.
  16. R. Kacker, “A Review of the Guide to the Expression of Uncertainty in Measurement,” New Brunswick Laboratory, Argonne, IL Mar. 5-9, 2007.
  17. R. Kacker, “Frequentist and Bayesian Statistics in the Context of Evaluating Uncertainty,” New Brunswick Laboratory, Argonne, IL, Mar. 5-9, 2007.
  18. E. Knill, “Randomization Hypothesis,” When Matter Meets Information Workshop, Perimeter Institute, Waterloo Canada, June 25-29, 2007.
  19. S. Langer, “OOF: Analyzing Material Microstructure,” SIAM Conference on Computational Science and Engineering, Costa Mesa, CA, Feb. 19-23, 2007.
  20. D.W. Lozier, “MKM and the DLMF,” Mathematical Knowledge Management Workshop on Sustainability, Interoperability and Scalability, Dalhousie Distributed Research Institute and Virtual Environment (D-DRIVE), Dalhousie University, Halifax, Canada. April 26 - 29, 2007.
  21. B. R. Miller, “DLMF, LaTeXML and some Lessons Learned,” The Evolution of Mathematical Communications in the Age of Digital Libraries, IMA Workshop, Minneapolis, MN, Dec. 8-9, 2006.
  22. D.P. O’Leary, “Parallel Matrix Computation: From the ILLIAC to Quantum Computing,” Stanford 50: State of the Art and Future Directions of Computational Mathematics and Numerical Computing, Stanford University, Stanford, CA, March 30, 2007.
  23. D. Porter (panelist), “Open Discussion with the Tcl/Tk Core Team,” Fourteenth Annual Tcl/Tk Conference, New Orleans, LA, September 26, 2007.
  24. R. Radebaugh and A. O’Gallagher, “Modeling a Fast Cooledown Technique for Pulse Tube Cryocoolers,” 22<sup>nd</sup> International Congress of Refrigeration, Beijing, China, Aug. 22-25, 2007.

## Conference Presentations

1. R. Boisvert, "Special Functions, Reference Data and Mathematical Software," International Congress on Industrial and Applied Mathematics, Zurich, Switzerland, July 16, 2007.
2. G.W. Bryant, M. Zielinski, W. Jaskolski, J. Aizpuru, and J.S. Sims, "Controlling the Optical Properties of Self-Assembled Quantum Dots Using External Strain," Material Research Society Fall Meeting, Boston, MA., November 26-30, 2007.
3. A. Dienstfrey, R. Wittmann, and B. Rider, "Statistics of Electromagnetic Fields and Random Matrix Theory," (poster), Second CU-NIST Symposium, University of Colorado at Boulder, Mar. 22, 2007.
4. M. J. Donahue and R. D. McMichael, "Micromagnetics on Curved Geometries Using Rectangular Cells: Error Correction and Analysis," 10th Joint MMM/Intermag Conference, Baltimore, MD, Jan. 11, 2007.
5. M. J. Donahue, "Accurate Computation of the Demagnetization Tensor," 6th International Symposium on Hysteresis Modeling and Micromagnetics HMM-2007, Naples, Italy, 4-Jun-2007.
6. E. Enjolras, W. George, J. Bullard, and J. Terrill, "Parallelization of HydraticCA," VCCTL Bi-Annual Meeting, Gaithersburg MD, Nov. 13-14, 2007.
7. W. George, J. Lancien, N. Martys, J. Terrill, and E. Garboczi, "Large Scale Simulations of Suspensions," NASA Booth, Supercomputing 2007, Reno, NV, November 10-16, 2007.
8. S. Glancy, E. Knill, and H. Vasconcelos, "Entanglement Purification of Any Stabilizer State," Quantum Information Processing Workshop, Brisbane, Australia, Jan. 30, 2007.
9. S. Glancy, E. Knill, and H. Vasconcelos, "Entanglement Purification of Any Stabilizer State," American Physical Society March Meeting, Denver, CO, Mar. 5, 2007.
10. S. Glancy, "Entanglement Purification of Any Stabilizer State," Asian Conference on Quantum Information Science, Kyoto University, Kyoto, Japan, September 2-6, 2007.
11. F. Hunt, "Visualizing the Frequency Patterns in DNA," Pi Mu Epsilon ceremony at Mount St. Mary's University, Emmitsburg, MD, Nov. 19, 2006.
12. R. Kacker and J. Lawrence, "Trapezoidal and triangular distributions for Type B evaluation of standard uncertainty" PTB-BIPM Workshop on the Impact of Information Technology in Metrology, Berlin, Germany, June 5, 2007.
13. R. Kacker, R. Datla, and A. Parr, "Comments on the Evaluation of Key Comparison Data by Cox et al," (poster), PTB-BIPM Workshop on the Impact of Information Technology in Metrology, Berlin, Germany June 5-7, 2007.
14. E. Knill, "Randomized Benchmarking of Quantum Gates," American Physical Society March Meeting, Denver, CO, Mar. 14, 2007.
15. D.W. Lozier, "Utilizing the DLMF in Scientific Research," 6th International Congress on Industrial and Applied Mathematics, Zurich, Switzerland, July 16, 2007.
16. N.S. Martys, C.F. Ferraris, V. Gupta, J.H. Cheung, J.G. Hagedorn, A.P. Peskin, E.J. Garboczi, "Computational Model Predictions of Suspension Rheology: Comparison to Experiment," 12th International Conference on the Chemistry of Cement, Montreal, Canada, July 11, 2007.
17. N.S. Martys, C.F. Ferraris, W. George, J. Lancien, J. Terrill, E. Garboczi, A.P. Peskin, J. Hagedorn, M. Olano, J. Kelso, S. Satterfield, H. Zhu, J.H. Cheung, B.-W. Chun, V. Gupta, D. Lootens, R. Flatt, and B. Descheneaux, "Computational Modeling of Suspensions: Recent Advances and Future Research Directions," VCCTL Bi-Annual Meeting, Gaithersburg, MD, Nov. 13-14, 2007.
18. B. R. Miller, "Creating Webs of Math Using LaTeX," 6th International Congress on Industrial and Applied Mathematics, Zurich, Switzerland, July 17, 2007.
19. B.R. Miller, "Why TeX and LaTeXML?," Joint Joining Educational Mathematics and OpenMath Meeting, Linz, Austria, June 26, 2007.
20. W. F. Mitchell and E. Tiesinga, "An h-p Adaptive Strategy with Limited p," SIAM Conference on Computational Science and Engineering, Costa Mesa, CA, Feb. 18-23, 2007.
21. M. O'Hara and D.P. O'Leary, "Adiabatic Quantum Computing and the Adiabatic Theorem in The Presence of Noise," GRID (Graduate Research Interaction Day), University of Maryland, College Park, MD April 12, 2007.
22. M. O'Hara and D.P. O'Leary, "Adiabatic Quantum Computing and the Adiabatic Theorem in The Presence of Noise," Gordon Research Conference on Quantum Information Science, Il Ciocco, Lucca (Barga), Italy, April 15-20, 2007.

23. M. Olano and S. Satterfield, "Non-photorealistic Visualization of Cement," OSG BOF at ACM SIGGRAPH, San Diego, August 8, 2007.
24. F. Potra, "Interior Point Methods for Linear Complementarity Problems," International Congress on Industrial and Applied Mathematics, Zurich, Switzerland, July 18, 2007.
25. B. Rust, "Data-Based Models for Global Temperature Variations," CSC'07 - The 2007 International Conference on Scientific Computing, Las Vegas, NV, June 26, 2007.
26. S. Satterfield, J. Kelso, and M. Olano, "Diverse-Flexible Source VE API, Diverse BOF," ACM SIGGRAPH, San Diego, CA, August 8, 2007.
27. A. Youssef, "Recent Advances in Math Search," 6th International Congress on Industrial and Applied Mathematics, Zurich, Switzerland, July 17, 2007.

## **Software Released**

1. S. Langer, OOF2: analysis of materials with complex microstructure, version 2.0.2 (Feb. 16, 2007), Alpha versions 2.0.4a1 through 2.0.4a3 (May-June 2007), Beta versions 2.0.4b1 and 2.0.4b2 (July-August, 2007).  
See <http://www.ctcms.nist.gov/oof/oof2>
2. S. Langer, gtklogger: creation and execution of regression tests for programs that use a graphical user interface, version 1.0 (August 2007), version 1.1 (September 2007).  
See <http://www.ctcms.nist.gov/oof/gtklogger>
3. W.F. Mitchell, PHAML: parallel hierarchical adaptive multi-level solver for partial differential equations, version 1.0 (May 4, 2007), version 1.1.0 (July 3, 2007).  
See <http://math.nist.gov/phaml/>
4. D. Porter, Tcl/Tk: tool control language and toolkit, version 8.4.14 (October 19, 2006), version 8.5a6 (October 20, 2006), version 8.4.15 (May 25, 2007), version 8.4.16 (September 24, 2007), version 8.5b1 (September 26, 2007).
5. R. Pozo, TNT: Template Numerical Toolkit, version 3.0.4, version 3.0.5, version 3.0.6, version 3.0.7, version 3.0.8.  
See <http://math.nist.gov/tnt>

## **Conferences, Minisymposia, Lecture Series, Shortcourses**

### **MCS D Seminar Series**

1. B. Shneiderman (University of Maryland), "The Thrill of Discovery: Information Visualization for High-Dimensional Spaces," Oct. 3, 2006.
2. M. Mascagni (Florida State University), "Using Simple Stochastic Differential Equations to Solve Complicated Partial Differential Equations", Oct. 18, 2006.
3. S. Bullock (MCS D), "Projecting onto Qubit Irreps of Young Diagrams," Nov. 21, 2006.
4. B. Alpert (MCS D), "Sparse Representations and High-Dimensional Geometry: What's the Excitement?," Dec. 5, 2006.
5. T. Gill (Howard University), "Sufficiency Class for Global (in Time) Solutions to the Three-Dimensional Navier-Stokes Equations," Feb. 6, 2007.
6. E. Fried (Washington University, St. Louis), "Sharp-Interface Theory for Transitions Between the Isotropic and Uniaxial Nematic Phases of a Liquid Crystal," May 3, 2007.
7. J. Nakagawa (Nippon Steel Corp.), "Mathematics in Industry: How is a Hidden Rule Found from Operation Data?," May 25, 2007
8. L. Chen (University of Maryland), "Multigrid Analysis of  $H_1$ ,  $H(\text{curl})$  and  $H(\text{div})$  Systems for Locally Adapted Grids," June 5, 2007.
9. D. Mijuca (University of Belgrade, Serbia), "On the Use of Fully Three Dimensional Multifield Mixed Finite Element Scheme in Multiscale Structural and Building Energy Efficiency Simulations," June 28, 2007.
10. A Youssef (MCS D), "Advances in Math Search: Summarization and Relevance Ranking of Math Hits," Sept. 21, 2007.
11. B. Miller (MCS D), "LaTeXML: Converting LaTeX to XML and MathML," Sept. 28, 2007.
12. P.A. Lott (University of Maryland), "Efficient Numerical Simulation of Advection Diffusion Systems, Dec. 19, 2007.



## Local Events Organized

1. T. Burns, Program Committee, International Conference on Smart Machining Systems, NIST, Gaithersburg, MD, March 13-15, 2007.
2. D. Gilsinn, Shortcourse, Numerical Analysis with Matlab, NIST, Gaithersburg, MD, Oct. 3, 4, Nov. 7, 8, and Dec. 4, 6, 2007.
3. S. Glancy, Quantum Information Journal Club, NIST, Boulder, weekly event.

## External Events Organization

1. R. Boisvert and B. Ford (Oxford), Organizers, Minisymposium "Recent Advances in Software Tools for Scientific Computing," 6th International Congress on Industrial and Applied Mathematics (ICIAM), Zurich, Switzerland, July 16, 2007.
2. M. Donahue, International Steering Committee, Hysteresis Modeling and Micromagnetics Symposium.
3. J. Fong, Organizer, Symposium on Nondestructive Evaluation (NDE), ASME 2007 Pressure Vessels and Piping Conference, San Antonio, Texas, July 25-26, 2007.
4. D. W. Lozier, B. Miller, and A. Youssef, Organizers, Minisymposium "Math on the Web: Content Development and Implementation," 6th International Congress on Industrial and Applied Mathematics, Zurich, Switzerland, July 16-17, 2007.
5. W. F. Mitchell, Scientific Committee, International Conference of Numerical Analysis and Applied Mathematics (ICNAAM 2007), Corfu, Greece, Sept. 16-20, 2007.
6. W. F. Mitchell, Program Committee, International Conference on High Performance Computing, Networking and Communication Systems, Orlando, FL, July 9-12, 2007.
7. S. Satterfield, J. Kelso, and M. Olano, "DIVERSE Birds-of-a-Feather," ACM SIGGRAPH, San Diego, August 8, 2007.

## Other Professional Activities

### Internal

1. I. Beich, Director, ITL Student Undergraduate Research Fellowship (SURF) Program.
2. R. Boisvert, NIST Scientific Computing Steering Group.
3. B. Rust, ITL Awards Committee.
4. B. Rust, MCSD Seminar Chair.
5. Staff members regularly review manuscripts for the Washington Editorial Review Board (WERB) and the Boulder Editorial Review Board (BERB), as well as proposals for the NIST ATP and SBIR programs.

### External

#### Editorial

1. B. Alpert, Associate Editor, *SIAM Journal on Scientific Computing*.
2. I. Beichl, Editor, *IEEE Computing in Science and Engineering*.
3. R. Boisvert, Associate Editor, *ACM Transactions on Mathematical Software*.
4. R. Boisvert, Area Editor, (Numerical Analysis, Mathematical Software, and Computational Engineering, Finance, and Science), Computing Research Repository (CoRR), [www.arXiv.org](http://www.arXiv.org).
5. D. Gilsinn, Associate Editor, *ASME Journal of Computational and Nonlinear Dynamics*.
6. D. Gilsinn and Balakumar Balachandran (University of Maryland), and Tamas Kalmar-Nagy (Texas A&M), eds., *Delay Differential Equations: Recent Advances and New Directions*, Springer, to appear.
7. D. Lozier, Associate Editor, *Mathematics of Computation*.
8. G. McFadden, Associate Editor, *Journal of Crystal Growth and Interfaces and Free Boundaries*.
9. W. Mitchell, Associate Editor, *International Journal of Applied Mathematics and Computational Science*, *Journal of Numerical Analysis*, *Industrial and Applied Mathematics*, and *Applied Numerical Analysis and Computational Mathematics*.
10. R. Pozo, Associate Editor, *ACM Transactions on Mathematical Software*.

11. J. Terrill, Editor, *Journal of Information Visualization, Special Issue on Visual Analysis of Human Dynamics*.

### Boards and Committees

1. R. Boisvert, Co-chair, Publication Board of the Association for Computing Machinery (ACM).
2. R. Boisvert, Member, ACM Awards Committee.
3. R. Boisvert, Chair, International Federation for Information Processing's Working Group 2.5 (Numerical Software).
4. R. Boisvert, Member, Review Panel, U.S. Army's basic (6.1) research program in Mathematics, Modeling, Communications, Networks, and Information Sciences.
5. F. Hunt, Member, Executive Committee of the Association for Women in Mathematics.
6. D. Lozier, Vice Chair, SIAM Activity Group on Orthogonal Polynomials and Special Functions.
7. B. Miller, Member, Math Working Group, W3C (the World Wide Web Consortium).
8. D. Porter, Member, Tcl Core Team.
9. B. Saunders, Member, Selection Committee, Etta Z. Falconer Lecture.
10. J. Terrill, Member, Federal High End Computing Implementation Task Force.
11. J. Terrill, Member, Federal High End Computing Research and Development, and Infrastructure Interagency Working Group.

### Reviewing

1. Division staff members referee manuscripts for a wide variety of journals including *ACM Transactions on Mathematical Software*, *Applied Physics Letters*, *Engineering with Computers*, *High Performance Computing*, *Networking and Communication Systems*, *IEEE International Symposium on Information Theory*, *IEEE Transactions on Information Theory*, *IEEE Transactions on Microwave Theory and Techniques*, *International Journal of Computational Science and Engineering*, *International Journal of Computer Mathematics*, *Journal of Manufacturing Science and Engineering*, *Journal of Mathematical Analysis and Applications*, *Letters in Mathematical Physics*, *Nature*, *Nature Physics*, *Nonlinear Dynamics*, *Numerische Mathematik*, *Optics Communications*, *Optics Express*, *Physica B*, *Physics Letters A*, *Physical Review A*, *Physical*

*Review A: Atomic, Molecular, and Optical Physics*, *Physical Review B*, *Physical Review Letters*, *Quantum Information and Computation*, *SIAM Journal of Scientific Computing*, *Transactions of the American Mathematical Society*.

2. Staff members review proposals for the following research programs: ACEnet Research Fellowships (Atomic Canada). ATP, Department of Energy, NIH, NIST Innovations in Measurement Science (IMS) Program, NSF

### External Contacts

MCSD staff members make contact with a wide variety of organizations in the course of their work. Examples of these follow.

#### Industrial Labs

ActiveState  
 Agilent Technologies  
 Bergen Scientific (Norway)  
 Chemical Abstracts Service  
 CWI Amsterdam (The Netherlands)  
 Design Science Inc.  
 Etnus  
 Fox TV  
 Gamma Logic  
 GE Research  
 Hewlett Packard  
 Hospira  
 IBM  
 Johnson Scientific  
 Mathworks, Inc.  
 Nippon Steel Corp.  
 Orbital Sciences Corp.  
 Plastic Technologies  
 Politecnico di Torino  
 Portland Cement Association  
 Proctor & Gamble Corp.  
 Raytheon  
 Rowan Williams Davies & Irwin Inc.  
 Simula Research Laboratory (Norway)  
 Simulistics  
 Stillwater Supercomputing Solutions  
 STMicroelectronics  
 Tech-EDV  
 UGS Corp.  
 Victoria Interrante  
 Viewray Inc.  
 Visual Numerics, Inc.

#### Government/Non-profit Organizations

AT&T Labs  
 Air Force Research Laboratory

Argonne National Laboratory  
 Army Intelligence Evaluation Center  
 Army Research Office  
 Council on Competitiveness  
 CWI (Amsterdam)  
 IDA Center for Computing Sciences  
 Institute for Systems Biology (Seattle)  
 Institut Laue Langevin (France)  
 International Federation for Information Processing  
 Jet Propulsion Laboratory  
 KTH Royal Institute of Technology (Sweden)  
 Lawrence Berkeley Laboratory  
 Lawrence Livermore National Laboratory  
 Los Alamos National Laboratory  
 NAG Ltd.  
 National Aeronautics and Space Administration  
 NASA Ames Research Center  
 National Center for Atmospheric Research  
 National Reconnaissance Office  
 National Science Foundation  
 National Security Agency  
 Naval Research Laboratory  
 Ohio Supercomputer Center  
 Sandia National Laboratories  
 Savannah River National Laboratory  
 U.S. Air Force Phillips Laboratory  
 World Wide Web Consortium

### Universities

American University  
 California Institute of Technology  
 Carnegie Mellon University  
 Case Western Reserve University  
 Catholic University of Leuven (Belgium)  
 Cornell University  
 Dartmouth College  
 Dnipropetrovsk University (Ukraine)  
 Drexel University  
 George Mason University  
 Georgetown University  
 George Washington University  
 Georgia Tech  
 Howard University  
 Illinois Institute of Technology  
 Indiana University  
 Iowa State University  
 Jacobs University (Bremen, Germany)  
 Johannes Kepler University (Linz, Austria)  
 Louisiana State University  
 MIT  
 New York University  
 North Carolina State University  
 Oregon State University  
 Penn State University  
 Purdue University  
 Rensselaer Polytechnic Institute

Russian Academy of Sciences (Russia)  
 Shaw University  
 Southeast University  
 Southern Methodist University  
 Stanford University  
 Technical University of Munich (Germany)  
 Texas A&M  
 Texas Tech  
 Trinity University  
 Tufts University  
 UCLA  
 Universidade Federal do Ceará, Brazil  
 Université Henri Poincare (France)  
 University of Aachen (Germany)  
 University of British Columbia  
 University of Bristol (UK)  
 University of California Davis  
 University of California San Diego  
 University of California Santa Barbara  
 University of Catolica de Valparaiso (Chile)  
 University of Colorado  
 University of Florida  
 University of Hanover  
 University of Helsinki (Finland)  
 University of Henri Poincare (France)  
 University of Karlsruhe (Germany)  
 University of Kent (UK)  
 University of Illinois Medical Center  
 University of Indiana  
 University of Linkoping (Sweden)  
 University of Magdeburg (Germany)  
 University of Maryland Baltimore County  
 University of Maryland College Park  
 University of Michigan  
 University of Minnesota  
 University of Natural Science (Vietnam)  
 University of Nevada Las Vegas  
 University of New Mexico  
 University of Nottingham (England)  
 University of Oxford (UK)  
 University of Patras (Greece)  
 University of Rovira I Virgili (Spain)  
 University of Saarland (Germany)  
 University of South Carolina  
 University of South Florida  
 University of Tennessee  
 University of Texas at Arlington  
 University of Texas at Austin  
 University of Toronto (Canada)  
 University of Utah  
 University of Vienna (Austria)  
 University of Washington  
 University of Western Ontario (Canada)  
 University of Wisconsin  
 Uppsala University (Sweden)  
 Utsunomiya University (Japan)  
 Virginia Tech

Yale University  
Williams College

**Part V**

# **Appendices**



## **Staff**

MCS D consists of full time permanent staff located at NIST laboratories in Gaithersburg, MD and Boulder, CO. This is supplemented with a variety of faculty appointments, guest researchers, postdoctoral appointments, and student appointments. The following list reflects all appointments held during any portion of FY 2007.

### **Division Staff**

Ronald Boisvert, *Chief*, Ph.D. (Computer Science), Purdue University, 1979

Robin Bickel, *Secretary*

Jeffrey Fong, Ph.D. (Applied Mechanics and Mathematics), Stanford University, 1966

Roldan Pozo, Ph.D. (Computer Science), University of Colorado at Boulder, 1991

Christopher Schanzle, B.S. (Computer Science), University of Maryland – Baltimore County, 1989

#### *Guest Researchers*

Barry Bernstein / Illinois Institute of Technology

Grant Erdmann, Commerce Science Fellow / Air Force Research Laboratory

### **Mathematical Modeling Group**

Geoffrey McFadden, *Leader*, Ph.D. (Mathematics), New York University, 1979

Bradley Alpert (Boulder), Ph.D. (Computer Science), Yale University, 1990

Timothy Burns, Ph.D. (Mathematics), University of New Mexico, 1977

Alfred Carasso, Ph.D. (Mathematics), University of Wisconsin, 1968

Andrew Dienstfrey (Boulder), Ph.D. (Mathematics), New York University, 1998

Michael Donahue, Ph.D. (Mathematics), The Ohio State University, 1991

Fern Hunt, Ph.D. (Mathematics), New York University,

Raghu Kacker, Ph.D. (Statistics), Iowa State University, 1979

Anthony Kearsley, Ph.D. (Computational and Applied Mathematics), Rice University, 1996

Peter Ketcham, M.S. (Mathematics), University of Minnesota, 1997

Stephen Langer, Ph.D. (Physics), Cornell University, 1989

Agnes O’Gallagher (Boulder), M.S. (Applied Math), University of Colorado at Boulder, 1991

Donald Porter, Ph.D. (Electrical Engineering), Washington University, 1996

#### *NRC Postdoctoral Associates*

Valerie Coffman, Ph.D. (Physics), Cornell University, 2006

#### *Contractors*

Andrew C.E. Reid, Ph.D. (Physics), Queen’s University, Kingston, Ontario, 1994

#### *Faculty Appointees*

Daniel Anderson / George Mason University

Dianne O’Leary / University of Maryland College Park

Florian Potra / University of Maryland Baltimore County

#### *Guest Researchers*

Mirit Aladjem / National Institutes of Health

Richard Braun / University of Delaware

David Cotrell / Lawrence Livermore National Laboratory

John Gary (Boulder)

Katharine Gurski / George Washington University

Seung-Ill Haan / University of Maryland Baltimore County  
 Sohyoung Kim / National Institutes of Health  
 Yu (Jeff) Lei / University of Texas at Arlington

*Students*

Kevin Dela Rosa / University of Texas at Arlington  
 Michael Forbes / MIT  
 Gillian Haemer / University of Southern California  
 Olga Kuznetsova / University of Maryland College Park

## Mathematical Software Group

Daniel Lozier, *Leader*, Ph.D. (Applied Mathematics), University of Maryland, 1979  
 Marjorie McClain, M.S. (Mathematics), University of Maryland College Park, 1984  
 Bruce Miller, Ph.D. (Physics), University of Texas at Austin, 1983  
 William Mitchell, Ph.D. (Computer Science), University of Illinois at Urbana-Champaign, 1988  
 Bert Rust, Ph.D. (Astronomy), University of Illinois at Urbana-Champaign, 1974  
 Bonita Saunders, PhD (Mathematics), Old Dominion University, 1985

*Contractors*

Joyce Conlon, B.A. (Mathematics), University of Maryland Baltimore County, 1979

*Faculty Appointees*

Frank Olver / University of Maryland College Park  
 G.W. Stewart / University of Maryland College Park  
 Abdou Youssef / George Washington University

*Guest Researchers*

Leonard Maximon / George Washington University

*Students*

Liuyuan Chen (Montgomery Blair High School, Maryland)

## Optimization and Computational Geometry Group

Ronald Boisvert, *Acting Leader*

Isabel Beichl, Ph.D. (Mathematics), Cornell University, 1981  
 Javier Bernal, Ph.D. (Mathematics), Catholic University, 1980  
 Brian Cloteaux, Ph.D. (Computer Science), New Mexico State University, 2007  
 David Gilsinn, Ph.D. (Mathematics), Georgetown University, 1969  
 Scott Glancy (Boulder), Ph.D. (Physics), University of Notre Dame, 2003  
 Emanuel (Manny) Knill (Boulder), Ph.D., (Mathematics), University of Colorado at Boulder, 1991

*NRC Postdoctoral Associates*

Bryan Eastin, Ph.D. (Physics), University of New Mexico, 2007

*Faculty Appointees*

Saul Gass / University of Maryland College Park  
 James Lawrence / George Mason University

*Guest Researchers*

Stephen Bullock / IDA Center for Computing Sciences  
 Sita Ramamurti / Trinity University, DC  
 David Song / Korea Institute for Advanced Study  
 Francis Sullivan / IDA Center for Computing Sciences  
 Christoph Witzgall, NIST Scientist Emeritus



*Students*

Kevin Costello / Carnegie Mellon University  
Adam Meier / University of Colorado  
Yanbao Zhang / University of Colorado

**Scientific Applications and Visualization Group**

Judith Devaney, *Leader*, Ph.D. (Information Technology), George Mason University, 1998  
Yolanda Parker, *Office Manager*  
Robert Bohn, Ph.D. (Physical Chemistry), University of Virginia, 1991  
William George, Ph.D. (Computer/Computational Science), Clemson University, 1995  
Terence Griffin, B.S. (Mathematics), St. Mary's College of Maryland, 1987  
John Hagedorn, M.S. (Mathematics), Rutgers University, 1980  
John Kelso, M.S. (Computer Science), George Washington University, 1984  
Adele Peskin (Boulder), Ph.D. (Chemical Engineering), University of Colorado at Boulder, 1985  
Steven Satterfield, M.S. (Computer Science), North Carolina State University, 1975  
James Sims, Ph.D. (Chemical Physics), Indiana University, 1969

*Faculty Appointees*

Marc Olano (University of Maryland Baltimore County)

*Guest Researchers*

Dong Yeon Cho / Seoul National University, Korea  
Edith Enjolra / Université Blaise Pascal, France  
Cedric Houard / Université Blaise Pascal, France  
Julien Lancien / France

*Students*

Aaron Jones / Hampton College  
Omotunwase Olubayo / Hampton College  
Sathish Ragappan / Quince Orchard High School, Maryland  
Miguel Rois / University of Puerto Rico

## **Glossary of Acronyms**

ACM	Association for Computing Machinery
ANSI	American National Standards Institute
API	application programmer's interface
ASME	American Society of Mechanical Engineers
ATP	NIST Advanced Technology Program
BFRL	NIST Building and Fire Research Laboratory
BLAS	Basic Linear Algebra Subprograms
BMD	bone mineral density
CCG	DoD Coordinated Calibration Group
CMM	coordinate measuring machine
CMU	Carnegie Mellon University
CODATA	Committee on Data for Science and technology
CPU	central processing unit
CSTL	NIST Chemical Science and Technology Laboratory
CT	computed tomography
CWI	Centrum voor Wiskunde en Informatica (Amsterdam)
DARPA	DOD Defense Advanced Research Projects Agency
DIVERSE	Device Independent Virtual Environments — Reconfigurable, Scalable, Extensible (visualization software)
DLMF	Digital Library of Mathematical Functions (MCS D project)
DOD	U.S. Department of Defense
DOE	U.S. Department of Energy
DOJ	U.S. Department of Justice
DPD	dissipative particle dynamics
DXA	dual-energy x-ray absorptiometry
EEEL	NIST Electronics and Electrical Engineering Laboratory
FDA	Food and Drug Administration
FFT	fast Fourier transform
FY	fiscal year
GAMS	Guide to Available Mathematical Software
GPU	Graphics processing unit
HPC	high performance computing
HTML	hypertext markup language
Hy-CI	Hylleraas-Configuration Interaction technique
ICIAM	International Congress on Industrial and Applied Mathematics
IDA	Institute for Defense Analysis
IEEE	Institute of Electronics and Electrical Engineers
IML++	Iterative Methods Library
ISCD	International Society of Clinical Densitometry
IT	information technology
ITL	NIST Information Technology Laboratory
IFIP	International Federation for Information Processing
JAMA	Java Matrix package
MALDI-TOF	matrix-assisted laser desorption/ionization time-of-flight
MCMC	Markov chain Monte Carlo
MCS D	ITL Mathematical and Computational Sciences Division
MEL	NIST Manufacturing Engineering Laboratory
MIT	Massachusetts Institute of Technology
MKM	mathematical knowledge management
MMM	magnetism and magnetic materials
MPI	Message Passing Interface
MRI	magnetic resonance imaging
MSEL	NIST Materials Science and Engineering Laboratory
MV++	Matrix/Vector Library

μmag	Micromagnetics Activity Group
NASA	National Aeronautics and Space Administration
NCSU	North Carolina State University
NIH	National Institutes of Health
NIST	National Institute of Standards and Technology
NISTIR	NIST Internal Report
NITRD	Networking and Information Technology Research and Development
NNSA	National Nuclear Security Administration
NRC	National Research Council
NSF	National Science Foundation
OCT	optical coherence tomography
ODE	ordinary differential equation
OLES	NIST Office of Law Enforcement Standards
OOF	Object-Oriented Finite Elements (software package)
OOMMF	Object-Oriented Micromagnetic Modeling Framework (software package)
PDE	partial differential equation
PET	positron emission tomography
PHAML	Parallel Hierarchical Adaptive Multi Level (software)
PITAC	President's Information Technology Advisory Committee
PL	NIST Physics Laboratory
PREP	Professional research Experience Program
QDPD	quaternion-based dissipative particle dynamics
QKD	quantum key distribution
RAVE	Reconfigurable Automatic Virtual Environment
SAVG	MCSA Scientific Applications and Visualization Group
SECB	slow evolution from the continuation boundary
SHPB	split-Hopkinson pressure bar
SIAM	Society for Industrial and Applied Mathematics
SIGGRAPH	ACM Special Interest Group on Graphics
SIMA	NIST Systems Integration for Manufacturing Applications Program
SIS	sequential importance sampling
SOR	successive overrelaxation
SPIE	International Society for Optical Engineering
SRM	standard reference material
SSS	Screen Saver Science
SURF	Student Undergraduate Research Fellowship
SVD	singular value decomposition
TNT	Template Numerical Toolkit
UMBC	University of Maryland Baltimore County
UNLV	University of Nevada Las Vegas
URL	universal resource locator
VCCTL	Virtual Cement and Concrete Testing Laboratory
VRML	virtual reality modeling language
W3C	World Wide Web Consortium
XML	Extensible Markup Language