

**NIST Special Publication 260-137**  
**2005 Edition**

*Standard Reference Materials*<sup>®</sup>

**Hydrogen Cyanide H<sup>13</sup>C<sup>14</sup>N Absorption  
Reference for 1530 nm to 1565 nm  
Wavelength Calibration – SRM 2519a**

Sarah L. Gilbert  
William C. Swann  
Chih-Ming Wang

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**1565 nm Wavelength Calibration –**  
**SRM 2519a**

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## Abstract

Standard Reference Material (SRM) 2519a is an optical-fiber-coupled wavelength reference based on the fundamental absorption lines of hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$  in the 1530 nm to 1565 nm region. The main difference between SRM 2519a and its predecessor, SRM 2519, is the use of lower pressure in the hydrogen cyanide cell to produce narrower lines. Thus SRM 2519a extends the use to higher resolution and higher accuracy applications. The center wavelengths of 54 lines of the  $2\nu_3$  rotational-vibrational band of hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$  are certified with uncertainties ranging from 0.04 pm to 0.24 pm. This uncertainty is an improvement of more than an order of magnitude over SRM 2519. This document describes SRM 2519a and details the uncertainty analysis.

Keywords: absorption; hydrogen cyanide; HCN; molecular spectroscopy; optical fiber communications; pressure broadening; pressure shift; Standard Reference Material; wavelength calibration; wavelength division multiplexing; wavelength reference; wavelength standards; WDM

## 1. Introduction

Wavelength division multiplexing (WDM) in optical fiber communication systems increases bandwidth by using many wavelength channels. Current WDM systems typically employ 50 or 100 GHz channel spacing (0.4 or 0.8 nm, respectively) in the 1530–1565 nm WDM C-band and may expand into the 1565–1625 nm L-band. Wavelength references are needed in these regions to calibrate instruments that are used to characterize components and monitor the wavelengths of the channels. In addition, optical fiber sensors based on the wavelength shift of fiber Bragg grating reflection peaks require wavelength calibration; some of these systems need wavelength calibration references with better than 1 pm uncertainty. These sensor systems typically operate in the optical fiber communication regions, particularly the WDM C-band, where components and measurement equipment are readily available. Previously, we developed wavelength calibration Standard Reference Materials (SRMs) for these regions based on acetylene (SRM 2517a, 1510–1540 nm [1]), hydrogen cyanide (SRM 2519, 1530–1560 nm [2]), and carbon monoxide (SRMs 2514 and 2515, 1560–1630 nm [3]).

This document describes a new wavelength calibration standard, SRM 2519a. The main difference between SRM 2519a and its predecessor, SRM 2519, is the use of lower pressure in the hydrogen cyanide cell to produce narrower lines. Thus SRM 2519a can be used in higher resolution and higher accuracy applications.

Fundamental atomic or molecular absorption lines provide wavelength references that are very stable under changing environmental conditions, such as temperature and pressure variations or the presence of electromagnetic fields. The hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$   $2\nu_3$  rotational-vibrational combination band, shown in Fig. 1, contains more than 50 absorption lines in the 1530 to 1565 nm region.

The SRM contains a 15 cm long fused silica absorption cell filled to a pressure of 3.3 kPa (25 Torr) with  $\text{H}^{13}\text{C}^{14}\text{N}$  gas. The  $\text{H}^{13}\text{C}^{14}\text{N}$  gas was produced by reducing 99 % isotopically pure potassium cyanide with stearic acid under vacuum [4]. The gas is contained in the cell with all-glass seals at the windows and the fill port. To prevent interference fringes in the transmitted signal, the windows are mounted at an angle of  $11^\circ$  and are also wedged by about  $2^\circ$ . Light from a singlemode optical fiber is collimated into a free beam, passes through the cell, and is coupled into another singlemode fiber. The cell holder is packaged in a small instrument box (approximately 32 cm long  $\times$  12.5 cm wide  $\times$  9 cm high) with two FC/APC fiber connectors for the input and output of a user-supplied light source. When measured using a narrowband source, such as a tunable laser, the 15 cm path length provides lines with depths ranging from 6 % to 50 % and widths of 7 to 20 pm. When measured with an optical spectrum analyzer (OSA) set at 0.05 nm resolution bandwidth, the maximum line depth is reduced to about 25 %; this depth is further reduced to about 15 % when measured using an OSA set at 0.1 nm resolution bandwidth. The certificate for SRM 2519a is presented in Appendix A. It includes the certified wavelength values, spectra, and instructions for use.

For a wavelength reference, the stability of the wavelength of each absorption line is a critical characteristic. The largest potential source of line shift is energy level shifts caused by the interaction of the molecules during elastic collisions [5]. Commonly called the pressure shift, this shift depends linearly on the collision frequency. For wavelength calibration of instruments,

it is often desirable to use a moderate or high pressure sample in order to increase the apparent line depth when observed with moderate instrument resolution. This results in pressure broadening and a slight pressure shift of the line centers. Our measurement of the pressure-induced shift and broadening for 25 lines in the  $2\nu_3$  rotational-vibrational band of  $\text{H}^{13}\text{C}^{14}\text{N}$  is described in Ref. 4 (Appendix B of this document).

The dominant sources of uncertainty for SRM 2519a are the pressure shift uncertainty and the line center uncertainty due to the presence of small nearby lines. Section 2 gives the uncertainty analysis for the pressure shift adjustment and section 3 details the uncertainty analysis for the line center measurement. In section 4 we briefly describe the NIST certification procedure, and we summarize the results in section 5.

## 2. Pressure Shift Adjustment

SRM 2519a uses hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$  gas at a pressure of 3.3 kPa (25 Torr). We have accurately measured the line centers, pressure shift, and pressure broadening for 25 lines in the  $\text{H}^{13}\text{C}^{14}\text{N}$   $2\nu_3$  rotational-vibrational combination band and have calculated the molecular constants of the band [4]. The SRM's certified line center for each of the 25 lines measured at NIST is determined by adding the line's pressure shift at 3.3 kPa to the measured zero-pressure line center. We calculate the zero-pressure line centers of other lines in the band using the molecular constants, and add the appropriate pressure shift derived using interpolation and extrapolation (described below).

The uncertainties quoted in this document are specified as either *standard uncertainties* (i.e.,  $1\sigma$  values) or *expanded uncertainties* using a coverage factor of 2 (i.e.,  $2\sigma$  values). If no specification is given, the uncertainties quoted are expanded uncertainties.

Figure 2 shows the results of our pressure shift measurements [4]. The pressure shift varies considerably with line number, from about +0.09 pm/kPa to -0.15 pm/kPa (about -1.5 to +2.5 MHz/Torr). At the SRM pressure of 3.3 kPa, this corresponds to a pressure shift ranging from +0.3 pm (line P4) to -0.5 pm (line P20).

Linear interpolation and extrapolation were used to obtain the pressure shift coefficients for lines that we did not measure. The uncertainty of a predicted value of an individual observation in linear regression [6] was used as the uncertainty of the interpolated and extrapolated shift coefficients. Since we do not have a quantitative theoretical model for the pressure shift of hydrogen cyanide, we took a conservative approach of using the t-table value with only 1 degree of freedom to obtain the expanded uncertainty of the interpolated and extrapolated values.

There are two components of the pressure shift uncertainty for the SRMs: the component arising from the pressure shift coefficient uncertainty (described above) and the component arising from the uncertainty of the pressure within the absorption cell ( $P = 3.3 \pm 0.7$  kPa). We add these two components in quadrature to obtain the pressure shift uncertainty for each certified line. The pressure shift coefficient values, the pressure shift at the SRM pressure of  $3.3 \pm 0.7$  kPa, and the respective uncertainties are tabulated in Table 1.

Temperature changes affect the collision frequency of molecules in the cell, and therefore slightly modify the pressure shift. This effect would cause only a 0.2 % change of the pressure shift for a 1 °C temperature change [4]. Since the collisional cross section may also have a small temperature dependence (due to small changes of population in the rotational levels, for example), we measured the temperature dependence of line P16 and verified that the fractional change of the pressure shift and broadening is small ( $\leq 0.3 \text{ \%}/^\circ\text{C}$ ). We would not expect this temperature dependence to be significantly different for other lines of the spectrum. To avoid thermal stress of the optical packaging, we recommend that the SRM units be used and stored near ambient room temperature ( $22 \pm 5 \text{ }^\circ\text{C}$ ); in this small temperature range, temperature effects on the pressure shift are negligible compared to the other sources of uncertainty described in this document.

### 3. Line Center Measurement Uncertainty

Wings of nearby lines can skew the shape of the line being measured and shift its apparent center. In addition to the strong lines of the  $2\nu_3$  band, there are a number of weak lines throughout the spectrum that are due to hot bands (transitions that are not out of the ground vibrational state) [7]. These small hot band lines overlap some of the main ( $2\nu_3$ ) lines and have a significant potential to shift their apparent line center. We obtained the offsets of any weak lines relative to a particular main line from Ref. 7, which gives line centers for the hot band transitions as well as for the weaker  $\text{H}^{12}\text{C}^{14}\text{N}$  and  $\text{H}^{13}\text{C}^{15}\text{N}$  lines. From our high resolution scans using a tunable diode laser, we determined the strength and width of any smaller lines that are within 3 linewidths of any main  $\text{H}^{13}\text{C}^{14}\text{N}$   $2\nu_3$  lines. We found that only 11 main lines have nearby smaller lines that are strong enough to be of concern (relative strength of the small line  $> 0.2 \text{ \%}$  of the main line): R25, R8, R7, R5, R4, R1, R0, P2, P7, P13, and P20.

To estimate the effect of these weak nearby lines, we developed a model in which we could add a weak line to a simulation of a particular measured line. We then fit the modeled line, both with and without the adjacent simulated weak line, using both Voigt and Lorentzian fitting routines in commercial fitting software and a variety of fitting ranges about the line center. Using the largest shift obtained for each line as an upper bound on the uncertainty (rectangular distribution), we obtained standard uncertainty values according to Ref. [8] for the 11 lines listed above. These standard uncertainties are listed in Table 2 as the “nearby line” component of the standard uncertainty.

A slope or a variation in the background level can shift the apparent center of a line. Light source spectral power variation, interference fringes due to reflected laser light, and wavelength dependence of the optical components can all cause background variation. For high accuracy applications, the SRM user is advised to normalize the signal to the light source spectrum. In addition, polarization-dependent loss is present due to the angled cell windows. This can cause time-varying throughput if the polarization state into the SRM varies (due to optical fiber patchcord motion, for example). We have designed the SRM to reduce interference fringes and other sources of background variation, but these effects could not be eliminated. We estimate the standard uncertainty due background variations inherent in the SRM to be 0.02 pm. We list this in Table 2 as the “SRM repeatability” component of the standard uncertainty.



## 4. NIST Certification Procedure

The purpose of the SRM certification procedure is to verify that the unit (a) contains the correct pressure of the appropriate isotopic species of hydrogen cyanide gas, (b) has no significant contaminants, and (c) shows no evidence of cell leakage. Measurements of the spectral band, similar to that shown in Figure 1 of the certificate in Appendix A, are made using a broadband source and an optical spectrum analyzer. Higher resolution measurements are made using a tunable diode laser (~1 MHz linewidth) and a calibrated wavelength meter; spectra similar to those shown in Figure 2 of the certificate in Appendix A are taken of each SRM unit, and one or more lines are accurately fit to verify the line's center and width using the procedure described in Ref. [4]. To test for cell leakage, the higher resolution measurements described above are repeated after a minimum waiting period of one month, and the results are compared to the earlier data. Any differences between the two data sets, particularly the linewidth values, may indicate cell leakage. This test is repeated on any suspicious unit, and the unit is rejected if it continues to change or does not meet the line center specifications.

## 5. Summary

The uncertainty components for each certified line are given in Table 2. The zero-pressure line center uncertainty is our uncertainty in determining the line centers (from Ref. [4]). The pressure shift uncertainty, described in section 2, is from the last column of Table 1; it includes contributions from the pressure shift coefficient uncertainty and the cell pressure uncertainty. The nearby line uncertainty and the SRM repeatability uncertainty are described in section 3.

Table 3 gives certified wavelengths and uncertainties for 54 lines of the  $2\nu_3$  rotational-vibrational band of  $\text{H}^{13}\text{C}^{14}\text{N}$ . The lines are certified with expanded uncertainties ( $2\sigma$ ) ranging from 0.04 pm to 0.24 pm.

A sample certificate for SRM 2519a is presented in Appendix A. The certificate includes the certified wavelength values, spectra, and instructions for use. Appendix B gives details of our line center, pressure shift, and pressure broadening measurements.

## 6. References

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**Table 1. Pressure Shift of H<sup>13</sup>C<sup>14</sup>N Lines:** Pressure shift coefficients and pressure shifts at SRM 2519a pressure of  $3.3 \pm 0.7$  kPa for lines in the  $2\nu_3$  band of H<sup>13</sup>C<sup>14</sup>N. The lines measured at NIST [4] are indicated in bold. The other line values are interpolated and extrapolated from the measured values. The pressure shift uncertainty is the quadrature combination of the contribution from the pressure shift coefficient uncertainty and the contribution from the cell pressure uncertainty.

line	pressure shift coefficient pm/kPa	coefficient standard uncertainty ( $1\sigma$ ) pm/kPa	pressure shift at 3.3 kPa pm	shift standard uncertainty ( $1\sigma$ ) pm
R26	0.043	0.016	0.143	0.056
R25	0.048	0.013	0.161	0.046
R24	0.054	0.010	0.180	0.038
<b>R23</b>	<b>0.060</b>	<b>0.001</b>	<b>0.198</b>	<b>0.020</b>
R22	0.065	0.006	0.217	0.031
<b>R21</b>	<b>0.071</b>	<b>0.001</b>	<b>0.236</b>	<b>0.024</b>
R20	0.076	0.007	0.252	0.034
R19	0.080	0.007	0.268	0.035
<b>R18</b>	<b>0.085</b>	<b>0.001</b>	<b>0.284</b>	<b>0.029</b>
R17	0.085	0.006	0.284	0.035
R16	0.085	0.006	0.283	0.035
<b>R15</b>	<b>0.085</b>	<b>0.001</b>	<b>0.283</b>	<b>0.028</b>
R14	0.076	0.006	0.253	0.032
R13	0.067	0.006	0.223	0.030
<b>R12</b>	<b>0.058</b>	<b>0.001</b>	<b>0.193</b>	<b>0.019</b>
R11	0.042	0.006	0.140	0.025
<b>R10</b>	<b>0.026</b>	<b>0.001</b>	<b>0.088</b>	<b>0.009</b>
<b>R9</b>	<b>0.005</b>	<b>0.001</b>	<b>0.018</b>	<b>0.003</b>
<b>R8</b>	<b>-0.021</b>	<b>0.003</b>	<b>-0.069</b>	<b>0.012</b>
<b>R7</b>	<b>-0.034</b>	<b>0.003</b>	<b>-0.114</b>	<b>0.016</b>
R6	-0.058	0.017	-0.195	0.061
<b>R5</b>	<b>-0.083</b>	<b>0.001</b>	<b>-0.275</b>	<b>0.028</b>
R4	-0.097	0.008	-0.323	0.043
<b>R3</b>	<b>-0.111</b>	<b>0.001</b>	<b>-0.371</b>	<b>0.037</b>
R2	-0.102	0.008	-0.339	0.043
<b>R1</b>	<b>-0.092</b>	<b>0.001</b>	<b>-0.308</b>	<b>0.031</b>
<b>R0</b>	<b>-0.066</b>	<b>0.001</b>	<b>-0.222</b>	<b>0.022</b>
<b>P1</b>	<b>0.043</b>	<b>0.001</b>	<b>0.143</b>	<b>0.015</b>
P2	0.059	0.007	0.196	0.029
P3	0.075	0.007	0.249	0.033
<b>P4</b>	<b>0.091</b>	<b>0.001</b>	<b>0.303</b>	<b>0.030</b>
<b>P5</b>	<b>0.084</b>	<b>0.001</b>	<b>0.280</b>	<b>0.028</b>
P6	0.063	0.007	0.211	0.032
P7	0.043	0.007	0.142	0.027
P8	0.022	0.007	0.073	0.025
<b>P9</b>	<b>0.001</b>	<b>0.001</b>	<b>0.004</b>	<b>0.003</b>
<b>P10</b>	<b>-0.024</b>	<b>0.001</b>	<b>-0.080</b>	<b>0.008</b>
<b>P11</b>	<b>-0.050</b>	<b>0.001</b>	<b>-0.165</b>	<b>0.017</b>
P12	-0.071	0.009	-0.235	0.038
P13	-0.091	0.009	-0.305	0.043
<b>P14</b>	<b>-0.112</b>	<b>0.001</b>	<b>-0.375</b>	<b>0.038</b>
P15	-0.126	0.012	-0.419	0.058
<b>P16</b>	<b>-0.139</b>	<b>0.002</b>	<b>-0.463</b>	<b>0.047</b>
<b>P17</b>	<b>-0.146</b>	<b>0.001</b>	<b>-0.485</b>	<b>0.049</b>
P18	-0.147	0.015	-0.491	0.069
P19	-0.149	0.015	-0.498	0.070
<b>P20</b>	<b>-0.151</b>	<b>0.003</b>	<b>-0.504</b>	<b>0.051</b>
P21	-0.145	0.014	-0.484	0.068
P22	-0.139	0.014	-0.465	0.067
<b>P23</b>	<b>-0.134</b>	<b>0.001</b>	<b>-0.445</b>	<b>0.045</b>
<b>P24</b>	<b>-0.126</b>	<b>0.001</b>	<b>-0.419</b>	<b>0.042</b>
P25	-0.118	0.014	-0.393	0.061
P26	-0.110	0.021	-0.367	0.080
P27	-0.102	0.029	-0.341	0.102

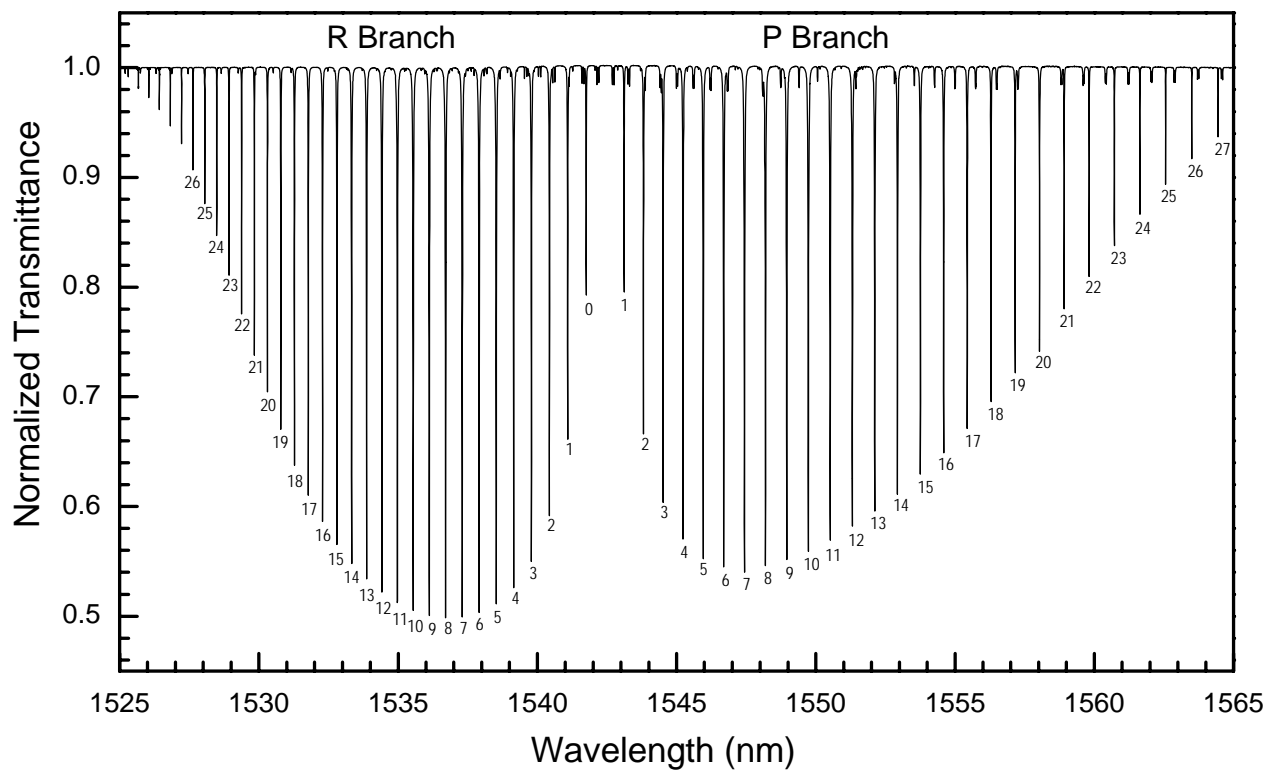
**Table 2. SRM Line Center Uncertainty:** Components of uncertainty and the combined expanded uncertainty for lines in the  $2\nu_3$  band of  $\text{H}^{13}\text{C}^{14}\text{N}$  at SRM 2519a conditions (pressure of  $3.3 \pm 0.7$  kPa and SRM packaging). The lines measured at NIST [4] are indicated in bold.

line	Standard Uncertainty Components ( $1\sigma$ ) – pm			SRM repeatability	Combined Expanded Uncertainty ( $2\sigma$ ) pm
	zero-pressure line center [4]	pressure shift (from Table 1)	nearby line		
R26	0.010	0.056		0.02	0.12
R25	0.007	0.046	0.058	0.02	0.15
R24	0.006	0.038		0.02	0.09
<b>R23</b>	<b>0.005</b>	<b>0.020</b>		<b>0.02</b>	<b>0.06</b>
R22	0.005	0.031		0.02	0.07
<b>R21</b>	<b>0.005</b>	<b>0.024</b>		<b>0.02</b>	<b>0.06</b>
R20	0.005	0.034		0.02	0.08
R19	0.005	0.035		0.02	0.08
<b>R18</b>	<b>0.005</b>	<b>0.029</b>		<b>0.02</b>	<b>0.07</b>
R17	0.005	0.035		0.02	0.08
R16	0.005	0.035		0.02	0.08
<b>R15</b>	<b>0.005</b>	<b>0.028</b>		<b>0.02</b>	<b>0.07</b>
R14	0.005	0.032		0.02	0.08
R13	0.005	0.030		0.02	0.07
<b>R12</b>	<b>0.005</b>	<b>0.019</b>		<b>0.02</b>	<b>0.06</b>
R11	0.005	0.025		0.02	0.06
<b>R10</b>	<b>0.005</b>	<b>0.009</b>		<b>0.02</b>	<b>0.05</b>
<b>R9</b>	<b>0.005</b>	<b>0.003</b>		<b>0.02</b>	<b>0.04</b>
<b>R8</b>	<b>0.011</b>	<b>0.012</b>	<b>0.003</b>	<b>0.02</b>	<b>0.05</b>
<b>R7</b>	<b>0.014</b>	<b>0.016</b>	<b>0.012</b>	<b>0.02</b>	<b>0.06</b>
R6	0.014	0.061		0.02	0.13
<b>R5</b>	<b>0.005</b>	<b>0.028</b>	<b>0.006</b>	<b>0.02</b>	<b>0.07</b>
R4	0.006	0.043	0.035	0.02	0.12
<b>R3</b>	<b>0.006</b>	<b>0.037</b>		<b>0.02</b>	<b>0.09</b>
R2	0.006	0.043		0.02	0.10
<b>R1</b>	<b>0.005</b>	<b>0.031</b>	<b>0.035</b>	<b>0.02</b>	<b>0.10</b>
<b>R0</b>	<b>0.006</b>	<b>0.022</b>	<b>0.006</b>	<b>0.02</b>	<b>0.06</b>
<b>P1</b>	<b>0.005</b>	<b>0.015</b>		<b>0.02</b>	<b>0.05</b>
P2	0.005	0.029	0.081	0.02	0.18
P3	0.005	0.033		0.02	0.08
<b>P4</b>	<b>0.005</b>	<b>0.030</b>		<b>0.02</b>	<b>0.07</b>
<b>P5</b>	<b>0.005</b>	<b>0.028</b>		<b>0.02</b>	<b>0.07</b>
P6	0.006	0.032		0.02	0.08
P7	0.006	0.027	0.115	0.02	0.24
P8	0.006	0.025		0.02	0.07
<b>P9</b>	<b>0.006</b>	<b>0.003</b>		<b>0.02</b>	<b>0.04</b>
<b>P10</b>	<b>0.005</b>	<b>0.008</b>		<b>0.02</b>	<b>0.04</b>
<b>P11</b>	<b>0.005</b>	<b>0.017</b>		<b>0.02</b>	<b>0.05</b>
P12	0.007	0.038		0.02	0.09
P13	0.007	0.043	0.006	0.02	0.10
<b>P14</b>	<b>0.007</b>	<b>0.038</b>		<b>0.02</b>	<b>0.09</b>
P15	0.008	0.058		0.02	0.12
<b>P16</b>	<b>0.008</b>	<b>0.047</b>		<b>0.02</b>	<b>0.10</b>
<b>P17</b>	<b>0.006</b>	<b>0.049</b>		<b>0.02</b>	<b>0.11</b>
P18	0.011	0.069		0.02	0.15
P19	0.011	0.070		0.02	0.15
<b>P20</b>	<b>0.011</b>	<b>0.051</b>	<b>0.052</b>	<b>0.02</b>	<b>0.15</b>
P21	0.011	0.068		0.02	0.14
P22	0.011	0.067		0.02	0.14
<b>P23</b>	<b>0.006</b>	<b>0.045</b>		<b>0.02</b>	<b>0.10</b>
<b>P24</b>	<b>0.005</b>	<b>0.042</b>		<b>0.02</b>	<b>0.09</b>
P25	0.006	0.061		0.02	0.13
P26	0.008	0.080		0.02	0.16
P27	0.010	0.102		0.02	0.21

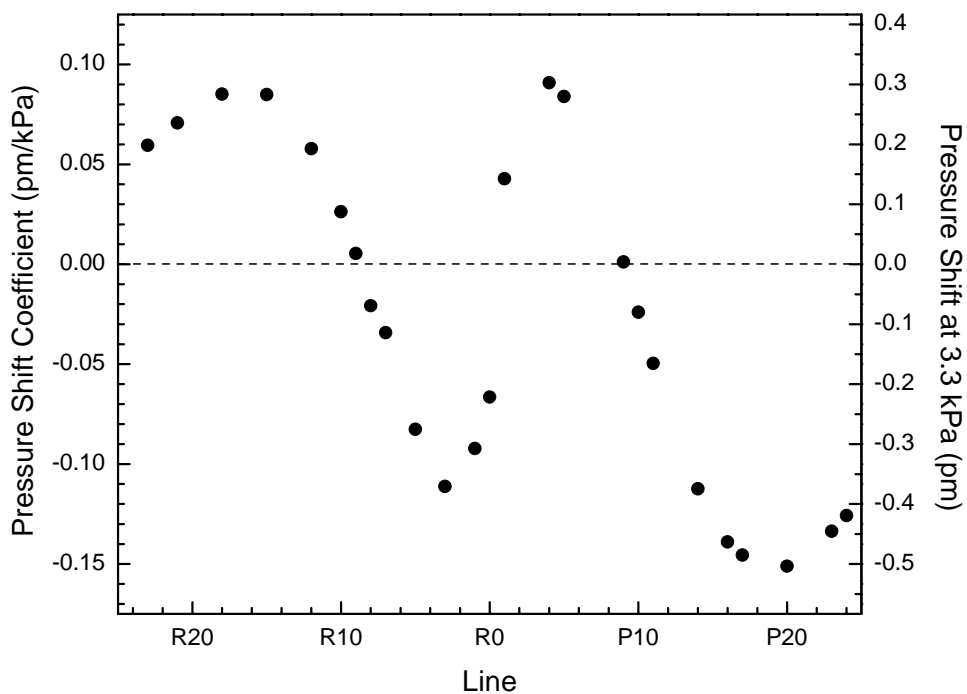
**Table 3. Certified Wavelengths for SRM 2519a**

Values from Ref. [4] adjusted for the pressure shift listed in Table 1 due to the 3.3 kPa (25 Torr) cell pressure. These vacuum wavelengths of the  $2\nu_3$  band of  $\text{H}^{13}\text{C}^{14}\text{N}$  are certified with the uncertainty indicated in parentheses for the last digits. The uncertainties quoted are the expanded uncertainty using a coverage factor  $k = 2$  (i.e., our quoted uncertainty is  $\pm 2\sigma$ ).

R Branch	Wavelength (nm)	P Branch	Wavelength (nm)
26	1527.63342(12)	1	1543.11423(5)
25	1528.05474(15)	2	1543.80967(18)
24	1528.48574(9)	3	1544.51503(8)
23	1528.92643(6)	4	1545.23033(7)
22	1529.37681(7)	5	1545.95549(7)
21	1529.83688(6)	6	1546.69055(8)
20	1530.30666(8)	7	1547.43558(24)
19	1530.78615(8)	8	1548.19057(7)
18	1531.27537(7)	9	1548.95555(4)
17	1531.77430(8)	10	1549.73051(4)
16	1532.28298(8)	11	1550.51546(5)
15	1532.80139(7)	12	1551.31045(9)
14	1533.32954(8)	13	1552.11546(10)
13	1533.86745(7)	14	1552.93051(9)
12	1534.41514(6)	15	1553.75562(12)
11	1534.97258(6)	16	1554.59079(10)
10	1535.53981(5)	17	1555.43605(11)
9	1536.11683(4)	18	1556.29141(15)
8	1536.70364(5)	19	1557.15686(15)
7	1537.30029(6)	20	1558.03240(15)
6	1537.90675(13)	21	1558.91808(14)
5	1538.52305(7)	22	1559.81389(14)
4	1539.14921(12)	23	1560.71983(10)
3	1539.78523(9)	24	1561.63593(9)
2	1540.43120(10)	25	1562.56218(13)
1	1541.08703(10)	26	1563.49859(16)
0	1541.75280(6)	27	1564.44519(21)



**Figure 1.** Spectrum of the hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$   $2\nu_3$  rotational-vibrational band obtained by scanning a tunable diode laser and measuring the laser power transmitted through a 15 cm long absorption cell filled to a pressure of 3.3 kPa (25 Torr).



**Figure 2.**  $\text{H}^{13}\text{C}^{14}\text{N}$  pressure shift measurements (Ref. [4]): Plot of the pressure shift coefficient and pressure shift at the SRM pressure of 3.3 kPa versus line number for the measured lines of the  $2\nu_3$  band.

## **Appendix A**

SRM 2519a Certificate

## **Appendix B**

Journal Article:

W.C. Swann and S.L. Gilbert, "Line centers, pressure shift, and pressure broadening of 1530–1560 nm hydrogen cyanide wavelength calibration lines," *J. Opt. Soc. Am. B* **22**, 1749-1756 (2005).



National Institute of Standards & Technology

# Certificate of Analysis

## Standard Reference Material<sup>®</sup> 2519a

High Resolution Wavelength Calibration Reference for 1530 nm – 1565 nm  
Hydrogen Cyanide H<sup>13</sup>C<sup>14</sup>N

Serial No.:

This Standard Reference Material (SRM) is intended for wavelength calibration in the spectral region from 1530 nm to 1565 nm; the center wavelengths of 54 lines of the 2v<sub>3</sub> rotational-vibrational band of hydrogen cyanide H<sup>13</sup>C<sup>14</sup>N are certified. This SRM can be used for calibrating a variety of wavelength-measuring instruments such as optical spectrum analyzers, tunable lasers, and wavelength meters. SRM 2519a is a single-mode optical-fiber-coupled absorption cell containing hydrogen cyanide H<sup>13</sup>C<sup>14</sup>N gas at a pressure of 3.3 kPa (25 Torr). The absorption path length is 15 cm and the absorption lines are about 15 pm wide. The cell is packaged in a small instrument box (approximately 32 cm long x 12.5 cm wide x 9 cm high) with two FC/APC fiber connectors for the input and output of a user-supplied light source. The main difference between SRM 2519a and its predecessor, SRM 2519, is the use of lower pressure in the hydrogen cyanide cell to produce narrower lines. Thus, SRM 2519a extends the use to higher resolution and higher accuracy applications.

**Certified Wavelength Values:** The line centers, pressure shift, and pressure broadening for 25 lines in the H<sup>13</sup>C<sup>14</sup>N 2v<sub>3</sub> rotational-vibrational combination band have been accurately measured at NIST, and the molecular constants of the band have been determined [1]. The certified line center for each of the 25 lines measured at NIST was determined by adding the line's pressure shift (due to collisions between HCN molecules at the 3.3 kPa pressure within the SRM cell) to the measured zero-pressure line center. The zero-pressure line centers of other lines in the band were calculated from the molecular constants of the band, and the appropriate pressure shift was derived using interpolation and extrapolation [2]. Details of the measurement procedure, data analysis, and uncertainty analysis can be found in references 1 and 2. A spectrum of the absorption band is shown in Figure 1, and certified wavelength values are given in Table 1. Figures 2 through 4 show scans near lines P10, P11, and P16. The center wavelengths of the lines listed in Table 1 are certified with uncertainties ranging from 0.04 pm to 0.24 pm. These uncertainties are the expanded uncertainties using a coverage factor  $k = 2$  (i.e., our quoted uncertainty is  $\pm 2\sigma$ ).

**Expiration of Certification:** The certification of this SRM is indefinite within the measurement uncertainties specified, provided the SRM is handled, stored, and used in accordance with the instructions given in this certificate (see "Storage and Handling").

The coordination of the development of the SRM and supporting measurements were performed by W.C. Swann and S.L. Gilbert of the NIST Optoelectronics Division.

Statistical consultation was provided by C.M. Wang of the NIST Statistical Engineering Division.

The support aspects involved in the issuance of this SRM were coordinated through the NIST Standard Reference Materials Program by C.S. Davis of the NIST Measurement Services Division.

Kent B. Rochford, Chief  
Optoelectronics Division

Robert L. Watters, Jr., Chief  
Measurement Services Division

Gaithersburg, MD 20899  
Certificate Issue Date: 13 May 2005  
*See Certificate Revision History on Last Page*



Table 1. Certified Wavelengths for SRM 2519a

R Branch	Wavelength (nm)	P Branch	Wavelength (nm)
26	1527.63342(12)	1	1543.11423(5)
25	1528.05474(15)	2	1543.80967(18)
24	1528.48574(9)	3	1544.51503(8)
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1	1541.08703(10)	26	1563.49859(16)
0	1541.75280(6)	27	1564.44519(21)

Certified vacuum wavelengths of line centers in the  $\text{H}^{13}\text{C}^{14}\text{N } 2\nu_3$  rotational-vibrational band at the SRM pressure of 3.3 kPa (25 Torr). Line centers are certified with the uncertainty indicated in parenthesis for the last digits. The uncertainties quoted are the expanded uncertainty using a coverage factor  $k = 2$  (i.e., our quoted uncertainty is  $\pm 2\sigma$ ).

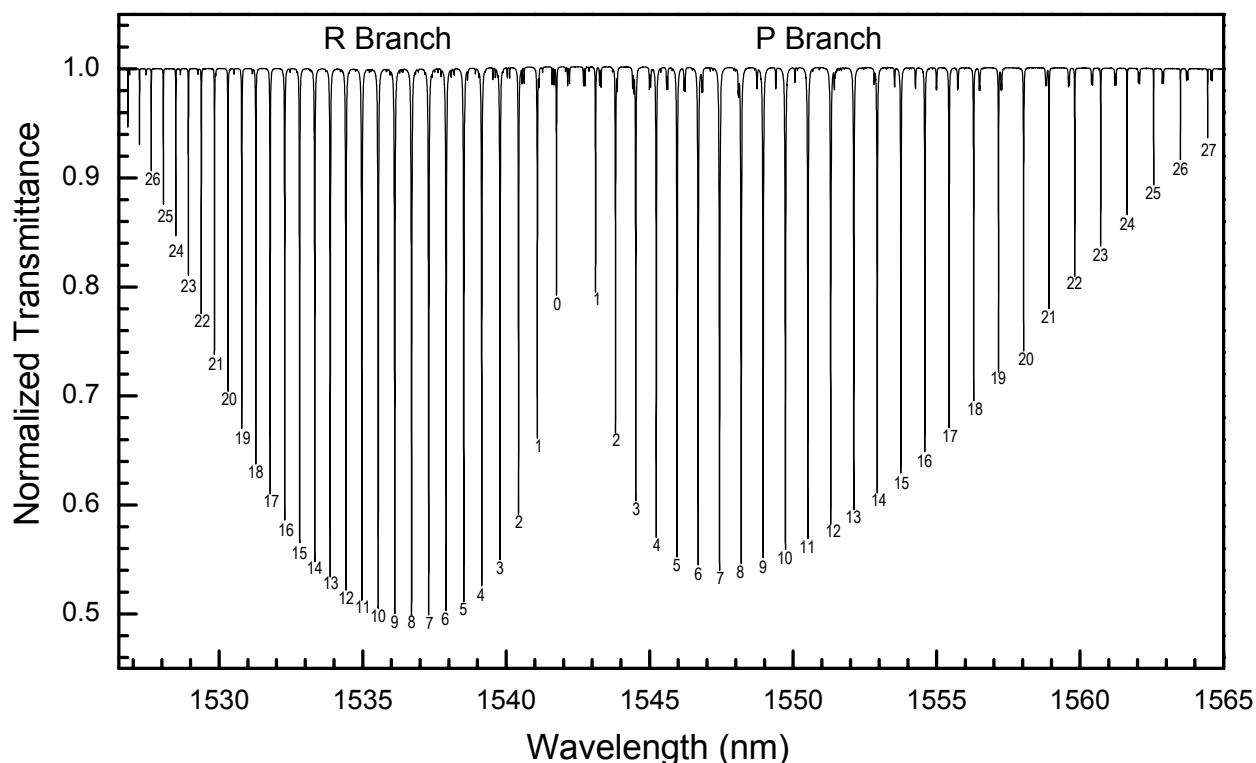


Figure 1. Normalized spectrum of the hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N } 2\nu_3$  band obtained by scanning a tunable diode laser ( $\sim 1$  MHz linewidth) and measuring the laser power transmitted through a SRM unit. The SRM contains a 15 cm long absorption cell filled with  $\text{H}^{13}\text{C}^{14}\text{N}$  to a pressure of 3.3 kPa (25 Torr). A file containing these data can be downloaded from the data file link on this web page: <http://ts.nist.gov/srmcertificate/?srm=2519a>.

**Storage and Handling:** The protective caps provided for the FC/APC fiber connectors should be replaced when the SRM is not in use. This SRM is intended to be used in a laboratory environment near ambient room temperature ( $22\text{ }^\circ\text{C} \pm 5\text{ }^\circ\text{C}$ ). The user should avoid exposing the unit to large temperature variations, temperature cycling, or mechanical shock, as these may cause the optical alignment to degrade. Such optical misalignment affects the throughput of the SRM but will not shift the centers of the absorption lines.

**Maintenance of SRM Certification:** The gas is contained in a glass cell with all-glass seals at the windows and the fill port. In the unlikely event of cell leakage, the linewidths and the small pressure shift of the line centers will change. Contact NIST if the linewidths or depths differ significantly from those shown in Figures 1–3, when measured with comparable resolution (see specific criteria in the section Suggested Procedure for High-Accuracy Requirements). If substantive changes occur that affect the certification, NIST will notify the purchaser. Registration (see attached sheet) will facilitate notification.

**Certification Measurement Conditions and Procedure:** The long term stability of hydrogen cyanide and the use of fundamental molecular absorption lines render the SRM insensitive to changes in environmental conditions. The purpose of the certification procedure is to verify that the unit contains the correct pressure of  $\text{H}^{13}\text{C}^{14}\text{N}$  gas, has no significant contaminants, and shows no evidence of cell leakage. Measurements of the spectral band, similar to that shown in Figure 1, are made using a broadband source and an optical spectrum analyzer. Higher resolution measurements are made using a tunable diode laser ( $\sim 1$  MHz linewidth) and a calibrated wavelength meter; spectra similar to that shown in Figure 2 are taken of each SRM unit and one or more lines are accurately fit to verify the line's center and width using the procedure described in reference [1]. To test for cell leakage, the higher resolution measurements are repeated after a minimum waiting period of one month.

## INSTRUCTIONS FOR USE

**General Considerations:** The SRM can be used to calibrate a laser or wavelength-measuring instrument in the 1530 nm to 1565 nm region. The values in Table 1 are vacuum wavelengths; if the user requires the wavelength in air, the appropriate correction for the index of refraction of air must be applied [3]. Depending on what type of instrument is being calibrated, a user-supplied broadband source or a tunable narrowband source may be used. Typical optical connections are shown in Figure 5. The unit is bi-directional (has no preferred input/output port); connections to the unit should be made using single-mode optical fibers terminated with clean FC/APC connectors.

**Use With a Broadband Source:** A broadband source in the 1530 nm to 1565 nm region (such as a light emitting diode, white light, or amplified spontaneous emission source) is useful when calibrating an instrument such as a diffraction grating based optical spectrum analyzer. A schematic for this type of calibration is shown in Figure 5(a). Light from the broadband source is coupled into the SRM, and the output (transmission through the SRM) is connected to the instrument that is being calibrated. The absorption lines of hydrogen cyanide appear as dips in the spectrum of the light source.

**Use With a Tunable Source:** The SRM can be used to calibrate the wavelength scale of a tunable source in this region (such as a diode laser, a fiber laser, or a source filtered by a tunable filter). A schematic for this type of calibration is shown in Figure 5(b). The laser is tuned over one or more of the hydrogen cyanide absorption lines. The transmission through the SRM is monitored by a detector; the transmitted power passes through a minimum at the center of an absorption line. Alternatively, a tunable laser source and the SRM can be used to check the calibration of a wavelength meter by measuring the wavelength of the laser (using the wavelength meter) as the laser is tuned through an absorption line.

**Suggested Procedure for Low-Accuracy Requirements – Calibration Uncertainty > 30 pm:** If calibrating an instrument using a broadband source, use an instrument resolution of  $\leq 0.1$  nm. If using a tunable source, use a data point density of at least one point every 0.005 nm (5 pm). After identifying a particular absorption line by comparing to the spectrum in Figure 1, find the center or minimum point of the line. Calibrate the instrument to the center wavelength of this line (from Table 1) using the calibration procedure specified by the instrument manufacturer. The instrument's linearity can be checked by repeating the procedure for a different absorption line and comparing it to the value listed in Table 1.

**Suggested Procedure for Moderate-Accuracy Requirements – Calibration Uncertainty in the Approximate Range of 3 pm to 30 pm:** If the source power varies significantly with wavelength, divide the SRM transmission spectrum by the source spectrum to obtain a normalized trace. After identifying a particular absorption line by comparing to the spectrum in Figure 1, make a high resolution scan of the line. If calibrating an instrument using a broadband source, use an instrument resolution of  $\leq 0.05$  nm. If using a tunable source, use a data point density of at least one point every 0.002 nm (2 pm). Find the wavelength readings on both sides of the line where the absorption is 50 % of the maximum; the line center is half way between these two wavelength readings. For higher accuracy results, repeat this procedure five times and take the average of the measurements. Calibrate the instrument to the center wavelength of this line (from Table 1) using the calibration procedure specified by the instrument manufacturer. The instrument's linearity can be checked by repeating the procedure for a different absorption line and comparing it to the value listed in Table 1.

**NOTE:** Highly reproducible *relative* wavelength measurements can be made using the procedure described for moderate-accuracy requirements. However, the procedure described in the following section is recommended to achieve high-accuracy *absolute* wavelength calibration.

**Suggested Procedure for High-Accuracy Requirements – Calibration Uncertainty < 3 pm:** Connect a narrowband tunable light source (source bandwidth  $\leq 1$  pm) to one of the fiber connectors on the SRM unit. After identifying a particular absorption line by comparing to the spectrum in Figure 1, make a high resolution scan of the line. To minimize polarization-dependent transmittance changes, avoid movement of the connecting fiber patchcords during the measurement. Use a data point density of at least one point every 1 pm and divide the SRM transmission spectrum by the source spectrum to obtain a normalized trace. Using a fitting technique such as the least squares technique, fit the absorption data to a Lorentzian or Voigt lineshape. Details of a line fitting procedure and potential errors sources can be found in reference 1, which is also included as an appendix in reference 2. Calibrate the instrument to the center wavelength of this line (from Table 1) using the calibration procedure specified by the instrument manufacturer. The instrument's linearity can be checked by repeating the procedure for a different absorption line and comparing it to the value listed in Table 1. Contact NIST if the width of line P16 differs by more than 25 % from the width shown in Figure 2, when measured using comparable resolution. A large change in linewidth could indicate cell leakage.

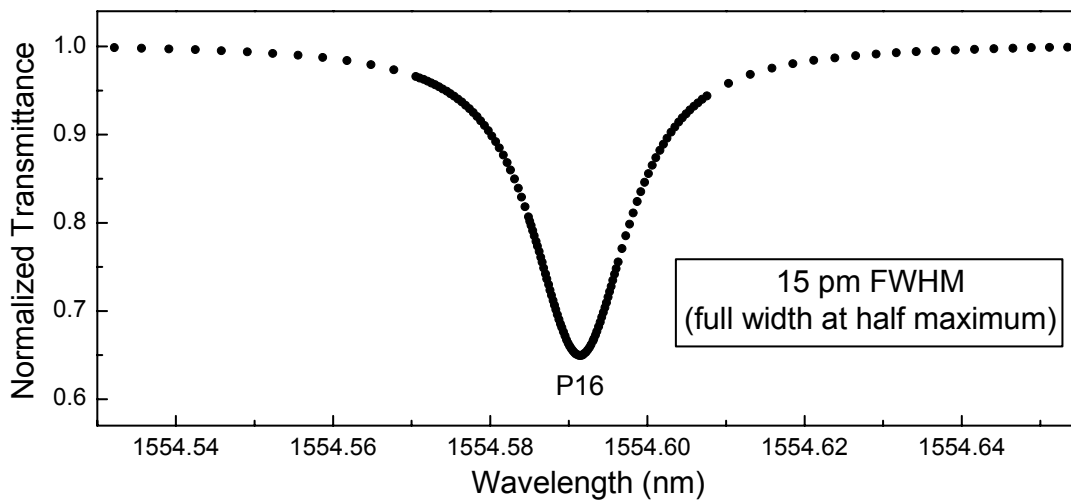


Figure 2. Spectrum of line P16 from Figure 1 obtained by scanning a tunable diode laser (laser linewidth  $\sim 1$  MHz).

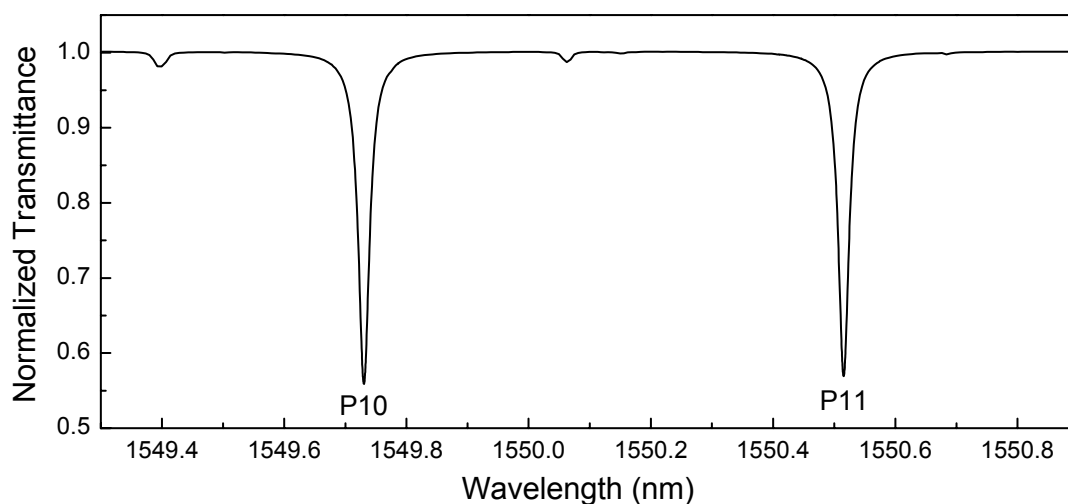


Figure 3. Spectrum of lines P10 and P11 from Figure 1 obtained by scanning a tunable diode laser.

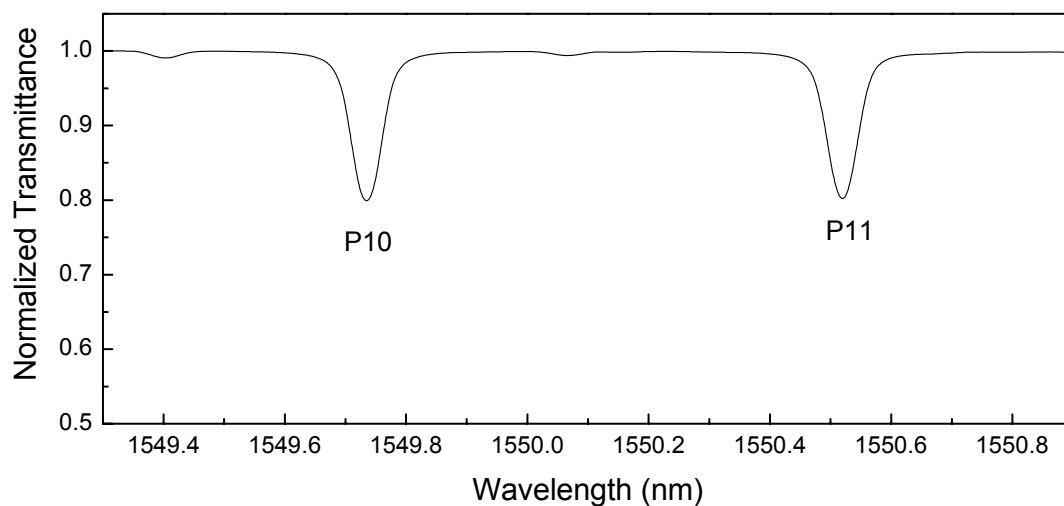
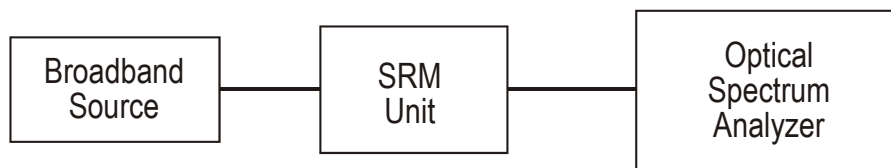


Figure 4. Spectrum of lines P10 and P11 obtained using a broadband source and an optical spectrum analyzer set to 0.05 nm resolution.



(a)



(b)

Figure 5. (a) Schematic of technique when using the SRM and a broadband source to calibrate an optical spectrum analyzer. (b) Schematic of technique when using the SRM to calibrate a tunable source. A wavelength meter can be calibrated by using a tunable laser in the configuration shown in (b) and measuring its wavelength using the wavelength meter.

#### REFERENCES

- [1] Swann, W.C.; Gilbert, S.L.; *Line Centers, Pressure Shift, and Pressure Broadening of 1530–1560 nm Hydrogen Cyanide Wavelength Calibration Lines*; J. Opt. Soc. Am. B. (2005) in press. Note: This paper is included as an appendix in reference [2] (below).
- [2] Gilbert, S.L.; Swann, W.C.; *Hydrogen Cyanide  $H^{13}C^{14}N$  Absorption Reference for 1530 nm to 1565 nm Wavelength Calibration – SRM 2519a*; NIST Special Publication 260-137 2005 ed, in press.
- [3] Edlen, B.; *The Refractive Index of Air*; Metrologia, Vol. 2, p. 12 (1966); CRC Handbook of Chemistry and Physics 77th ed., pp. 10–266, (1996); Stone, J.A.; Zimmerman, J.H.; *Index of Refraction of Air*; <http://patapsco.nist.gov/mel/div821/Wavelength/Documentation.asp#IndexofRefractionofAir>.

**Certificate Revision History:** 13 May 2005 (This editorial revision reflects adding an “a” to the URL address listed in Figure 1); 11 April 2005 (Original certificate date).

*Users of this SRM should ensure that the certificate in their possession is current. This can be accomplished by contacting the SRM Program at: telephone (301) 975-6776; fax (301) 926-4751; e-mail [srminfo@nist.gov](mailto:srminfo@nist.gov); or via the Internet at <http://www.nist.gov/srm>.*

# Line centers, pressure shift, and pressure broadening of 1530–1560 nm hydrogen cyanide wavelength calibration lines

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We have measured the line centers and pressure-induced shift and broadening of 25 lines in the  $2\nu_3$  rotational–vibrational band of hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$ . These lines can be used as wavelength references in the optical fiber communication wavelength division multiplexing C-band (approximately 1530–1565 nm). We find that the pressure shift varies with line number from +0.09 pm/kPa to –0.15 pm/kPa (approximately –1.5 to +2.5 MHz/Torr). The pressure broadening also varies with line number and is typically between 1 and 5.4 pm/kPa (17–90 MHz/Torr). We determined the line centers of 21 lines with an expanded uncertainty ( $2\sigma$ ) of 0.01 pm ( $\approx 1$  MHz), an improvement of more than 1 order of magnitude over previous line center measurements of this band. We also calculate the molecular constants for the band, yielding improved determination of the band origin frequency and the excited-state molecular constants. © 2005 Optical Society of America

OCIS codes: 020.3690, 060.2330, 120.3940, 120.4800, 300.1030, 300.6390.

## 1. INTRODUCTION

Wavelength division multiplexing (WDM) in optical fiber communication systems increases bandwidth by use of many wavelength channels. Current WDM systems typically employ 50 or 100 GHz channel spacing (0.4 or 0.8 nm, respectively) in the 1530–1565 nm WDM C-band. WDM will likely expand into the L-band region (approximately 1565–1625 nm), and WDM may be implemented in shorter-wavelength regions as well. Wavelength references are needed in these regions to calibrate instruments that are used to characterize components and monitor the wavelengths of the channels. In addition, optical fiber sensors based on the wavelength shift of fiber Bragg grating reflection peaks require wavelength calibration; some of these systems need wavelength calibration references with better than 1 pm uncertainty. These sensor systems typically operate in the optical fiber communication regions, particularly the WDM C-band, where components and measurement equipment are readily available.

Fundamental atomic or molecular absorptions provide wavelength references that are stable under changing environmental conditions such as temperature and pressure variations or the presence of electromagnetic fields. The National Institute of Standards and Technology (NIST) has developed wavelength calibration transfer standards in the 1510–1630 nm region based on acetylene,<sup>1,2</sup> hydrogen cyanide,<sup>3</sup> and carbon monoxide.<sup>4,5</sup> The hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$  spectrum, shown in Fig. 1, is particularly well matched to the WDM C-band, with more than 50 strong absorption lines in the 1530–1565 nm region. We decided to upgrade the hydrogen cyanide NIST Standard Reference Material (SRM) transfer standard to higher accuracy. The vacuum wavelengths of lines in the hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$   $2\nu_3$  rotational–vibrational band have been determined at very low pressure with an uncer-

tainty of 0.12 pm (about 15 MHz).<sup>6</sup> Since we would like to certify our SRM to comparable or higher accuracy than this, we require improved accuracy on the line center values.

For a wavelength reference, the stability of the wavelength of each absorption line is a critical characteristic. The largest potential source of line shift is the energy-level shift caused by the interaction of the molecules during elastic collisions.<sup>7</sup> Commonly called the pressure shift, this shift depends linearly on the collision frequency. It is often desirable to use an intermediate or high-pressure sample for wavelength calibration of instruments, to pressure broaden the lines, and to match the reference bandwidth to the instrument resolution. This results in the strongest signals for a given resolution bandwidth. The hydrogen cyanide SRM will be at a pressure of 3.3 kPa (25 Torr). Thus we also need accurate measurements of the pressure shift of each line to determine the SRM wavelengths.

We measured the line centers, pressure shifts, and pressure broadening of 25 lines in the  $2\nu_3$  rotational–vibrational band of hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$ . We also extrapolated these line centers to zero pressure and compared those values with the literature values. Finally, we determined the molecular constants for the band. We describe our measurement procedure in Section 2 and summarize the results in Section 3. Conclusions are presented in Section 4.

## 2. MEASUREMENT DESCRIPTION AND DATA ANALYSIS

A schematic diagram of our measurement apparatus is shown in Fig. 2. Light from a tunable diode laser is filtered using a fiber Fabry–Perot filter and is typically sent through two absorption cells simultaneously; the trans-

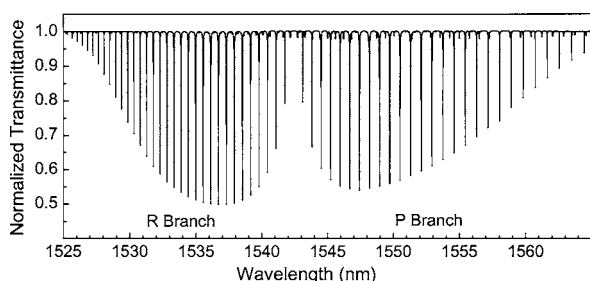


Fig. 1. Hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$   $2\nu_3$  rotational-vibrational band spectrum obtained by scanning a tunable diode laser and measuring the laser power transmitted through a 15 cm long cell filled to a pressure of 3.3 kPa (25 Torr).

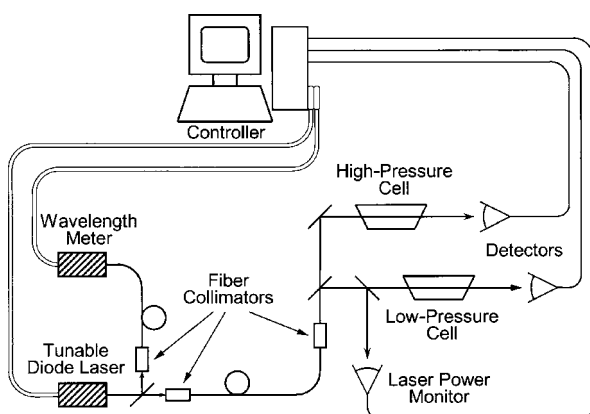


Fig. 2. Diagram of the pressure shift measurement apparatus.

mission through each cell is monitored by detectors. One cell contained  $\text{H}^{13}\text{C}^{14}\text{N}$  gas at a relatively low pressure of  $\approx 0.13$  kPa (1 Torr), and the other contained a higher pressure of either 3.3 kPa (25 Torr) or 6.0 kPa (45 Torr). A third detector monitored the laser power, and a wavelength meter measured the laser's vacuum wavelength with a standard uncertainty ( $1\sigma$ ) of  $\approx 2.5$  parts in  $10^9$  (0.5 MHz or 0.004 pm at 1560 nm). A computer controlled the laser wavelength scan and recorded the readings of the three detectors and wavelength meter.

The fused-silica absorption cells are 15 cm long, with windows attached to the cells by a glass frit method. To prevent interference fringes in the transmitted signal, the windows are mounted at an angle of  $11^\circ$  and are also wedged by  $\approx 2^\circ$ . The cells were first evacuated and leak checked and were then filled with isotopically pure gas. The  $\text{H}^{13}\text{C}^{14}\text{N}$  gas was produced by reducing 99% isotopically pure potassium cyanide with stearic acid under vacuum and mild heat (approximately  $80^\circ\text{C}$ ). The reaction generates  $\text{H}^{13}\text{C}^{14}\text{N}$  gas, a small amount of other isotopic species of hydrogen cyanide (HCN), traces of  $\text{H}_2\text{O}$  and  $\text{CO}_2$  from decomposition of the stearic acid, and other reaction products that remain solid under vacuum. The gas sample was transferred from the reaction flask into a separate, previously evacuated flask. The trace of  $\text{CO}_2$  gas was removed by freezing this flask in a dry ice bath, then opening the flask to a vacuum pump that pumps the  $\text{CO}_2$  away from the frozen HCN. The HCN sample was then transferred to a flask containing phosphorous pentoxide desiccant that removes the trace of  $\text{H}_2\text{O}$ . The HCN sample is stored in this flask until ready for use; any

traces of air that migrate into the flask through the valve are removed immediately prior to use by freezing the flask in liquid nitrogen and pumping away any remaining gases. During the fill process the pressure in the fill manifold (and hence the cell) was monitored with a capacitance manometer. The higher-pressure cells were prepared under our direction by an outside vendor; these were tipped off at the stem using a torch, forming an all-glass seal. The low-pressure cell was prepared in-house to allow further control of the gas sample purity; this cell was sealed using a glass valve with O-ring seals.

Figure 3 shows spectra of line *P*16 obtained at 0.9 and 3.3 kPa HCN pressure. The pressure broadening in the higher-pressure spectrum is obvious, and a small shift in the center wavelength is apparent. The measured quantity, the transmitted laser power  $I_T$ , is related to the absorption coefficient  $\alpha$  and the absorption path length  $L$  by

$$I_T = I_0 \exp(-\alpha L), \quad (1)$$

where  $I_0$  is the incident laser power. We first divided the cell transmission curves by the laser power monitor signal to remove common-mode intensity variations and normalized the data. We then took the natural logarithm to obtain the absorbance  $\alpha L$ .

Individual lines were then fitted to Voigt profiles<sup>7</sup> using an orthogonal distance regression algorithm.<sup>8</sup> With the orthogonal distance regression, called either error-in-variables or total-least-squares regression, we obtain the model parameters by minimizing the sum of squares of the orthogonal distances from the model to the data points. The fitting program was able to account for a background slope and uncertainties in both  $x$  (wavelength) and  $y$  (transmitted laser power). A Voigt profile is a convolution of Lorentzian and Gaussian profiles; it results when there is a combination of Gaussian broadening (resulting from Doppler broadening, for example) and Lorentzian line shape (resulting from the natural linewidth or pressure broadening, for example). In our situation, the natural linewidth is small (typically  $< 2$  MHz for molecular absorption lines in this region<sup>9</sup>) compared with the Gaussian Doppler broadening ( $\approx 450$  MHz) and the Lorentzian pressure broadening. The pressure-broadened

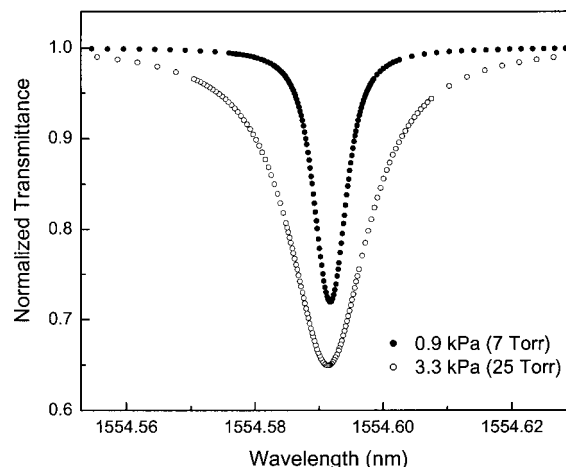


Fig. 3. Tunable diode laser scan of  $\text{H}^{13}\text{C}^{14}\text{N}$  line *P*16 showing the transmittance through a low-pressure cell (0.9 kPa) and a higher-pressure (3.3 kPa) cell.



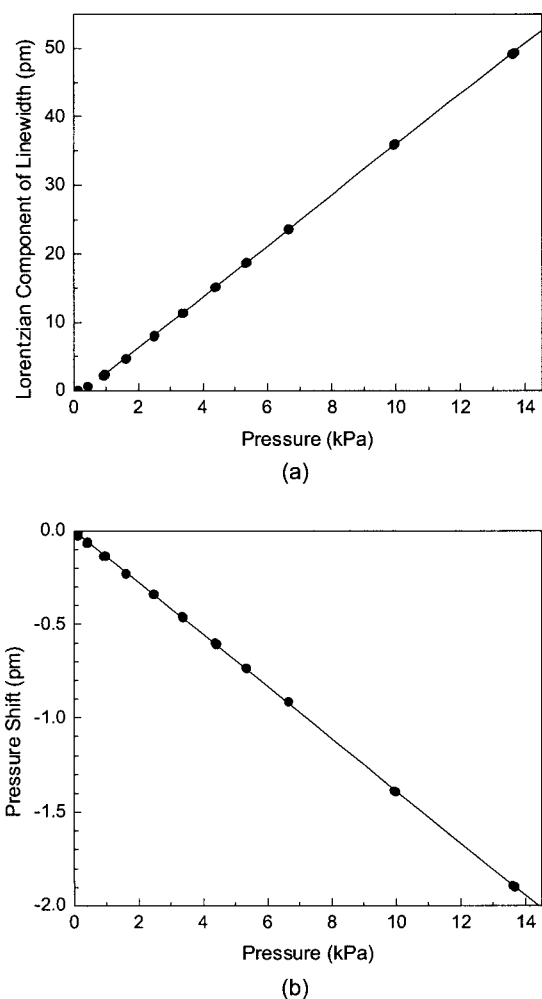


Fig. 4. (a) FWHM of the Lorentzian component of  $\text{H}^{13}\text{C}^{14}\text{N}$  line  $P16$  versus pressure and the corresponding linear least-squares fit to the higher-pressure data ( $>0.9$  kPa). (b) Line  $P16$  center wavelength shift from the zero-pressure value versus pressure and the corresponding linear least-squares fit to the data. For both plots, the error bars are smaller than the points.

component of the linewidths ranged from  $0.04\times$  to  $9\times$  the Doppler-broadened component. We used the calculated Doppler linewidth for each line, ranging from 3.57 to 3.62 pm (Ref. 7) and allowed the other fitting parameters to vary.

Short-term statistical variation of the wavelength meter reading and the laser power transmitted through the absorption cells added noise to the data scans. To determine this statistical variation of the wavelength measurement, we repeatedly measured the laser's wavelength while it was stabilized to a  $^{87}\text{Rb}$  transition (see Subsection 2.A). The statistical variation of repeated measurements yielded a Gaussian distribution with a standard deviation of 0.004 pm. We determined the experimental uncertainty in the normalized transmitted laser power (transmittance) by measuring the statistical variation of the data within a region of a line wing. The standard deviation of these fluctuations was typically between  $5\times 10^{-5}$  and  $1\times 10^{-4}$ . To account for the short-term statistical variation, each data point of a scan was assigned a standard uncertainty of 0.004 pm for the wavelength and

a fractional uncertainty of  $1\times 10^{-4}$  for the transmittance. The fitting program determined the line centers and the Lorentzian component of the linewidths and the corresponding uncertainties. The resultant line-center-fit standard uncertainties were typically 0.003 pm.

To accurately determine the cells' pressures and monitor them over the course of the measurements, we generated a plot of the Lorentzian component of the linewidth (derived from the Voigt line fit) versus pressure for line  $P16$ . This allowed us to later determine a cell's pressure at any time by measuring the width of line  $P16$  and comparing it with the plot. We mounted a cell in our pressure shift measurement apparatus and attached it to our fill manifold with a copper tube, which allowed us to monitor the cell pressure using the capacitance manometer while we measured the linewidth and line center. We conducted these measurements on line  $P16$  for several pressures between 0.13 kPa (1 Torr) and 13 kPa (100 Torr). Figure 4(a) is a plot of the full width at half-maximum (FWHM) of the Lorentzian component of line  $P16$  versus pressure. As can be seen, the Lorentzian component of the width (pressure broadening) has a linear dependence on pressure for pressures higher than  $\approx 0.5$  kPa. The deviation from this linear dependence at low pressure is likely due to collisional narrowing arising from velocity averaging. This effect is negligible at higher pressures, where pressure broadening dominates, but can cause the line shape to deviate from the expected Voigt profile at low pressures.<sup>10</sup> A linear least-squares fit to the higher-pressure data is also shown on the plot. Figure 4(b) shows the line center wavelength shift versus pressure for the same line and the corresponding linear least-squares fit; as can be seen from this plot, the pressure shift is linearly dependent on pressure. On the basis of our calibration of linewidth versus pressure for line  $P16$ , the pressures for the medium- and high-pressure cells used in the subsequent shift measurements were  $3.36\pm 0.02$  kPa ( $25.22\pm 0.13$  Torr) and  $5.91\pm 0.03$  kPa ( $44.34\pm 0.22$  Torr), respectively. The low-pressure cell, which was filled immediately prior to the measurements, showed an exponential decay in pressure from  $0.133\pm 0.008$  kPa ( $1.00\pm 0.06$  Torr) to  $0.106\pm 0.008$  kPa ( $0.80\pm 0.06$  Torr) over the nine-day duration of the measurements. This pressure change was likely due to adsorption of HCN on the cell surface; the pressure appeared to be approaching a steady-state value near 0.10 kPa. We did not observe any pressure change of the higher-pressure cells during the measurements. The pressure uncertainty quoted here is the expanded uncertainty obtained by applying a coverage factor of  $k=2$  (i.e., our quoted uncertainty is  $\pm 2\sigma$ ).<sup>11</sup>

In Subsections 2.A and 2.B we discuss the aspects that contributed to our measurement uncertainty for the line center, pressure shift, and pressure-broadening measurements.

#### A. Wavelength Meter Uncertainty

We used a NIST-built wavelength meter that has a wavelength measurement standard deviation of 2.5 parts in  $10^9$  (equivalently, 0.004 pm, or 0.5 MHz at 1560 nm). We set up a high-accuracy wavelength reference to test the wavelength meter accuracy and statistical variation.<sup>3</sup> Diode laser light at 1560.5 nm is amplified with an erbium-



doped fiber amplifier and is frequency doubled in a periodically poled lithium niobate crystal. The resultant 780 nm light is then used to conduct saturated absorption spectroscopy on the  $5S_{1/2} \rightarrow 5P_{3/2}$  transitions of rubidium ( $^{85}\text{Rb}$  and  $^{87}\text{Rb}$ ), and the laser is actively stabilized to one of the hyperfine components. The line centers of these transitions were measured with an uncertainty of  $\pm 0.4$  MHz (Ref. 12), and the  $^{87}\text{Rb}$  d/f crossover transition was measured with an uncertainty of 5.5 kHz.<sup>13</sup> We verified the accuracy of our stabilized laser by measuring its frequency with a stabilized frequency comb referenced simultaneously to the NIST calcium optical frequency standard and a hydrogen maser that was calibrated by the Cs clock.<sup>14</sup> Our measurement of the 1560 nm frequency with the laser stabilized to the  $^{87}\text{Rb}$  d/f crossover transition is 192 113 990.7 MHz, with an expanded uncertainty ( $2\sigma$ ) of  $\pm 0.7$  MHz. This corresponds to the 780 nm frequency of 384 227 981.3  $\pm$  1.4 MHz, which differs by only 0.6 MHz from the much more accurate determination of the  $^{87}\text{Rb}$  d/f transition. We used this rubidium-stabilized reference to calibrate our wavelength meter between scans of the hydrogen cyanide lines; by averaging multiple measurements, we obtained a wavelength calibration standard uncertainty ( $1\sigma$ ) of 0.35 MHz. We combined this wavelength calibration standard uncertainty with the uncertainty due to the wavelength meter drift between calibrations to obtain a wavelength measurement standard uncertainty of 0.004 pm ( $\approx 0.5$  MHz) at 1560 nm. We verified the linearity of the wavelength meter by measuring a series of  $^{12}\text{C}_2\text{H}_2$  lines between 1528 and 1538 nm. These measurements were performed much like our HCN line center measurements; the line centers for cells at two different pressures were measured, and the extrapolated zero-pressure line centers were compared with those reported in Ref. 9. We performed this measurement twice: once just before the HCN measurements and once near the completion of the HCN measurements. The average of our measured  $^{12}\text{C}_2\text{H}_2$  line centers was within 0.002 pm of the values reported in Ref. 9, which have a standard uncertainty of 0.001 pm.

### B. Background Variation

A slope or a variation in the background level can shift the apparent center of a line, particularly for the wide lines of the high-pressure cells. Interference fringes due to reflected laser light, wavelength dependence of the optical components, beam-pointing stability, and variations in the laser power can cause background variation. As mentioned above, we removed common-mode laser power variations by dividing the cell transmittance data by the power monitor data. To avoid effects due to the wavelength dependence of optical fiber couplers (splitters), we used free-space beam splitters to send the laser light to the cells and the power monitor. We minimized interference effects by using wedged cell windows and beam splitters, windowless detectors, and two optical isolators. These precautions reduced the background variation from these sources to a negligible level.

Wings of nearby absorption lines can also skew the shape of the line being measured and shift its apparent center. In addition to the strong lines of the  $2\nu_3$  band, there are a number of weak lines throughout the spec-

trum that are due to hot bands (transitions that are not out of the ground vibrational state).<sup>6</sup> We also observed a number of weak  $\text{H}^{12}\text{C}^{14}\text{N}$  and  $\text{H}^{13}\text{C}^{15}\text{N}$  lines in our spectra; presumably these arise from incomplete separation of  $^{12}\text{C}$  and a biasing toward the heavy isotope  $^{15}\text{N}$  during the isotopic enrichment of the original potassium cyanide sample. To minimize the effect of weak neighboring lines on our line center and pressure shift measurements, we avoided measuring lines in the spectrum that had weak lines close to the primary line. To estimate the effect of weak nearby lines on the lines that we did measure, we developed a model in which we could add a weak line to a simulation of a particular measured line. The width and area of any weak lines within the flanks of a measured line were estimated by observing similar weak lines that were not adjacent to any strong lines. We obtained the off-sets of any weak lines relative to a particular measured line from Ref. 6, which gives line centers for the hot-band transitions, as well as for the  $\text{H}^{12}\text{C}^{14}\text{N}$  and  $\text{H}^{13}\text{C}^{15}\text{N}$  lines. We then fitted the modeled line, both with and without the adjacent simulated weak line, using the same fitting routine we used to fit the measured lines. In both the data fitting and the simulation we limited the range of data being fit to the central portion of the line, clipping away any data with amplitude less than 35% of a line's maximum amplitude. Any weak lines outside of this data range were found to have a negligible effect on the simulated line centers; slopes in the fitted data caused by the wings of adjacent weak lines were accounted for by our fitting routine. Of all the lines we measured, only lines *R7*, *R8*, and *P20* had adjacent weak lines with line centers within the fitted data; therefore we conclude that we can limit our detailed investigation to these lines. The line center difference given by the simulation's results with and without the weak line gives us an estimate of the line center shift caused by the adjacent weak line. The model showed negligible effects (shifts of less than 0.001 pm) of adjacent weak lines on the 0.13 kPa (1 Torr) line centers. Observation of the spectra verified this; the weak lines were clearly separated from the measured lines. The model revealed shifts of up to 0.005 pm for the 3.3 kPa (25 Torr) cell and up to 0.012 pm for the 6 kPa (45 Torr) cell. Extrapolating the modeled line centers to zero pressure revealed shifts as large as 0.004 pm for these lines.

### 3. PRESSURE SHIFT, LINE CENTER, AND PRESSURE-BROADENING RESULTS

The line center fit standard uncertainties for the 25 lines at three pressures were typically 0.003 pm. To obtain the unperturbed line center values, we extrapolated the line centers to zero pressure using a linear least-squares fitting procedure. We also derived the pressure shift coefficient (change in line center wavelength versus pressure) from this fit. The pressure-broadening coefficient for each line was determined by a linear least-squares fit to the Lorentzian component of the linewidth. We determined the uncertainties in these fit parameters using a Monte Carlo procedure whereby multiple least-squares fits to the data were performed within the boundaries of the data point uncertainties. The uncertainty in the respective fit parameters dominated the uncertainty of our pres-

**Table 1. Line Center, Pressure Shift, and Pressure-Broadening Results for  $\text{H}^{13}\text{C}^{14}\text{N}^a$** 

Line	Line Center Extrapolated to Zero Pressure (vacuum wavelength, nm)	Shift Coefficient		Broadening Coefficient	
		(pm/kPa)	(MHz/Torr)	(pm/kPa)	(MHz/Torr)
R23	1528.926232(10)	0.060(2)	-1.02(3)	1.0(3)	17(5)
R21	1529.836643(10)	0.071(2)	-1.21(3)	1.4(3)	24(5)
R18	1531.275090(10)	0.085(2)	-1.45(3)	2.2(3)	38(4)
R15	1532.801111(10)	0.085(2)	-1.44(3)	3.2(2)	55(4)
R12	1534.414943(10)	0.058(2)	-0.98(3)	4.3(2)	73(3)
R10	1535.539723(10)	0.026(2)	-0.45(3)	4.9(2)	83(3)
R9	1536.116809(10)	0.005(1)	-0.09(2)	5.0(2)	85(3)
R8	1536.703707(22)	-0.021(6)	0.35(9)	5.1(1)	87(2)
R7	1537.300409(27)	-0.034(7)	0.58(12)	5.1(1)	86(2)
R5	1538.523322(11)	-0.083(2)	1.39(3)	4.8(2)	81(3)
R3	1539.785605(12)	-0.111(2)	1.87(4)	4.0(2)	67(3)
R1	1541.087342(10)	-0.092(2)	1.55(3)	3.0(2)	50(3)
R0	1541.753026(11)	-0.066(2)	1.12(3)	2.6(2)	44(4)
P1	1543.114083(10)	0.043(2)	-0.72(3)	2.6(3)	44(4)
P4	1545.230028(10)	0.091(2)	-1.52(3)	4.0(2)	68(3)
P5	1545.955208(10)	0.084(2)	-1.40(3)	4.5(1)	76(2)
P9	1548.955546(11)	0.001(2)	-0.02(3)	5.4(1)	90(2)
P10	1549.730587(10)	-0.024(1)	0.40(2)	5.3(1)	89(2)
P11	1550.515630(11)	-0.050(2)	0.82(3)	5.2(1)	86(2)
P14	1552.930882(14)	-0.112(3)	1.86(4)	4.3(2)	71(3)
P16	1554.591255(16)	-0.139(3)	2.30(6)	3.5(2)	59(3)
P17	1555.436539(12)	-0.146(2)	2.41(3)	3.2(2)	52(3)
P20	1558.032905(22)	-0.151(5)	2.49(9)	2.2(3)	36(5)
P23	1560.720279(11)	-0.134(2)	2.19(3)	1.4(3)	23(4)
P24	1561.636345(10)	-0.126(2)	2.06(3)	1.2(2)	19(4)

<sup>a</sup>Results are for the measured lines of the  $2\nu_3$  band of hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$  at a temperature of  $22^\circ \pm 2^\circ \text{C}$ . The line center vacuum wavelength results are for low-pressure conditions; our measurements (column 2) are values obtained by extrapolating the line center to zero pressure. The broadening coefficient is the pressure dependence of the FWHM of the Lorentzian component of the Voigt line profile. The uncertainties in the final digits of the values are indicated in parentheses. The uncertainties quoted are the expanded uncertainties obtained by applying a coverage factor  $k=2$  (i.e., our quoted uncertainty is  $\pm 2\sigma$ ).

sure shift and pressure-broadening determinations. Our zero-pressure line center uncertainty had an additional component due to the wavelength measurement standard uncertainty of 0.004 pm. We combined the wavelength measurement uncertainty with the fit uncertainty using the root-sum-of-squares method to obtain the total uncertainty for the line centers. This analysis resulted in larger uncertainty for the lines identified in Section 2 as having adjacent weak lines (*R7*, *R8*, and *P20*); since the resultant uncertainty for these lines is consistent with our modeling results, we did not add any additional uncertainty due to adjacent lines. Temperature changes affect the collision frequency of molecules in the cell and therefore slightly modify the pressure shift.<sup>1,7</sup> This effect would cause only a 0.2% change of the pressure shift for a 1 °C temperature change.<sup>1</sup> Since the collisional cross section may also have a small temperature dependence (due to small changes of population in the rotational levels, for example), we measured the temperature dependence of line *P16* and verified that the fractional change of the pressure shift and broadening is small ( $\leq 0.3\% / ^\circ\text{C}$ ). We would not expect this temperature dependence to be significantly different for other lines of the spectrum. For the measurements reported here, the temperature was  $22^\circ \pm 2^\circ \text{C}$ . This temperature range would have a negligible effect on our pres-

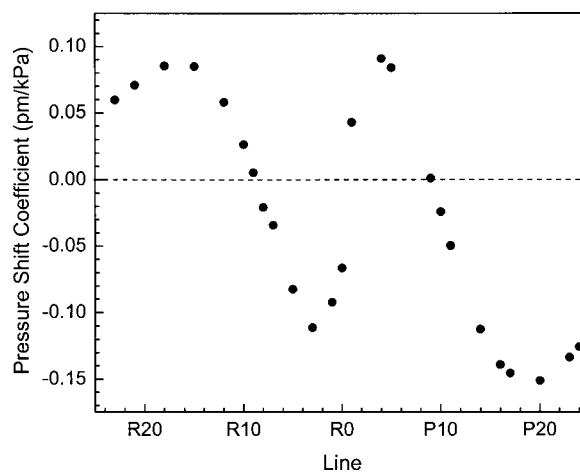


Fig. 5. Measured pressure shift coefficient versus line number for the  $\text{H}^{13}\text{C}^{14}\text{N}$   $2\nu_3$  rotational-vibrational band. The error bars are smaller than the data points.

sure shift, broadening, and zero-pressure line center determinations compared with the other sources of uncertainty. Table 1 summarizes our line center, pressure shift, and pressure-broadening results.

Figure 5 shows the pressure shift versus line number. We find that the pressure shift varies considerably with

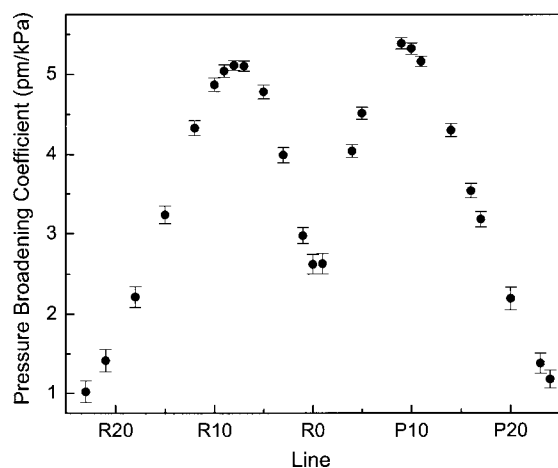


Fig. 6. Measured pressure dependence of the Lorentzian component (FWHM) of the linewidth derived from a Voigt fit versus line number for the  $\text{H}^{13}\text{C}^{14}\text{N } 2\nu_3$  rotational-vibrational band. Error bars are one standard uncertainty ( $1\sigma$ ).

**Table 2. Line Center Vacuum Wavelength Measurement Comparison<sup>a</sup>**

Line	This Paper Line Center Extrapolated to Zero Pressure (nm)	Ref. 6 (nm)	Difference (pm)
R23	1528.92623(1)	1528.92582(24)	0.42(24)
R21	1529.83664(1)	1529.83632(24)	0.32(24)
R18	1531.27509(1)	1531.27487(24)	0.22(24)
R15	1532.80111(1)	1532.80095(24)	0.16(24)
R12	1534.41494(1)	1534.41481(24)	0.13(24)
R10	1535.53972(1)	1535.53962(24)	0.10(24)
R9	1536.11681(1)	1536.11669(24)	0.12(24)
R8	1536.70371(2)	1536.70360(24)	0.11(24)
R7	1537.30041(3)	1537.30031(24)	0.10(24)
R5	1538.52332(1)	1538.52322(24)	0.10(24)
R3	1539.78561(1)	1539.78552(24)	0.09(24)
R1	1541.08734(1)	1541.08724(24)	0.10(24)
R0	1541.75303(1)	1541.75292(24)	0.11(24)
P1	1543.11408(1)	1543.11398(24)	0.10(24)
P4	1545.23003(1)	1545.22993(24)	0.10(24)
P5	1545.95521(1)	1545.95512(24)	0.09(24)
P9	1548.95555(1)	1548.95547(24)	0.07(24)
P10	1549.73059(1)	1549.73051(24)	0.08(24)
P11	1550.51563(1)	1550.51556(24)	0.07(24)
P14	1552.93088(1)	1552.93082(24)	0.07(24)
P16	1554.59126(2)	1554.59121(24)	0.04(24)
P17	1555.43654(1)	1555.43650(24)	0.04(24)
P20	1558.03291(2)	1558.03288(24)	0.03(24)
P23	1560.72028(1)	1560.72024(24)	0.04(24)
P24	1561.63635(1)	1561.63632(24)	0.03(24)

<sup>a</sup>Line center vacuum wavelength results for this measurement compared with those from Ref. 6 for low-pressure conditions; our measurements (column 2) are values obtained by extrapolating the line center to zero pressure. The expanded uncertainties ( $2\sigma$ ) in the final digits of the values are indicated in parentheses. We assumed that the uncertainties given in Ref. 6 are one standard uncertainty and we multiplied them by 2.

line number, from approximately +0.09 pm/kPa to -0.15 pm/kPa (approximately -1.5 to +2.5 MHz/Torr). We found that the pressure broadening also varied with line number (Fig. 6). The pressure broadening was largest

for the stronger lines in each branch (R7, R8, P9, and P10) and is significantly smaller for lines far from the band center (transitions between states with high rotational quantum numbers).

Table 2 compares our determinations of the zero-pressure line center values with the values reported in Ref. 6. Our standard uncertainty ( $1\sigma$ ) is typically near 0.005 pm, whereas the estimated uncertainty given in Ref. 6 is  $5 \times 10^{-4} \text{ cm}^{-1}$  (0.12 pm). With the exception of a deviation in the short-wavelength region (particularly lines R21 and R23), the results are in good agreement.

We were able to obtain molecular constants for the ground and excited states and determine zero-pressure line center values for other lines in the band by fitting our line center data (converted to  $\text{cm}^{-1}$ ) with the following function:

$$\Delta T_m = \Delta T + B'(m^2 + m) - D'(m^2 + m)^2 + H'(m^2 + m)^3 - B''(m^2 - m) + D''(m^2 - m)^2 - H''(m^2 - m)^3. \quad (2)$$

The index  $m = J + 1$  for the R branch, and  $m = -J$  for the P branch, where  $J$  is the ground-state rotational quantum number;  $\Delta T_m$  is the  $m$ th line center wavenumber and  $\Delta T$  is the wavenumber of the pure vibrational transition (band origin). The molecular constants  $B'$  and  $B''$  are the excited- and ground-state rotational constants, respectively; and  $D'$ ,  $D''$ ,  $H'$ , and  $H''$  are the corresponding centrifugal distortion constants.<sup>9,15</sup> Figure 7 shows the fit to the data and the residuals. The reduced residual-sum-of-squares ( $\chi^2$ ) value for the fit is 0.5, which suggests that we overestimated our uncertainties. Table 3 shows the molecular constants returned by the fit, as well as a comparison of our results with those of Refs. 6 and 16. The line centers of lines R0–R27 and P1–P28, calculated from the molecular constants, are listed in Table 4.

Comparison of our results with those of Ref. 16 shows agreement to within our  $1\sigma$  uncertainties for the ground-state constants ( $B''$ ,  $D''$ , and  $H''$ ). Our results also agree well with those reported in Ref. 6 for  $B'$  and  $B''$ , but have poor agreement for  $\Delta T$ ,  $D'$ , and  $D''$ . The value of  $D''$  in Ref. 6 also disagrees with that determined in Ref. 16 by approximately the same amount. The line center results in Ref. 6 are lower than ours by 0.1 pm on average, which led to the  $4 \times 10^{-4} \text{ cm}^{-1}$  (0.1 pm) discrepancy between

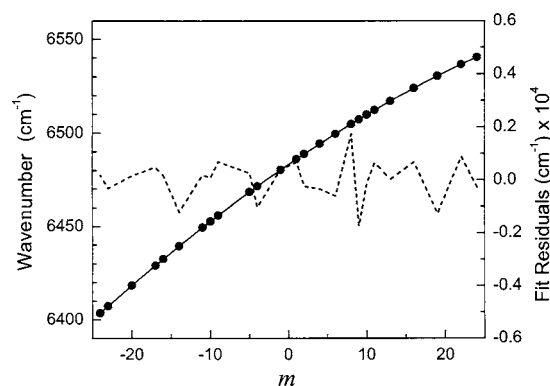


Fig. 7. Zero-pressure line centers (data points), results of fit to Eq. (2) (solid line), and residuals of the fit (dashed curve). The index  $m = J + 1$  for the R branch, and  $m = -J$  for the P branch. The molecular constants determined by this fit are given in Table 3.

their value for  $\Delta T$  and ours. The authors in Ref. 6 conducted only high-accuracy measurements ( $0.0005\text{ cm}^{-1}$  or  $0.12\text{ }\mu\text{m}$  uncertainty) of lines  $P23$ – $P30$  of the  $2\nu_3$  band of  $\text{H}^{13}\text{C}^{14}\text{N}$  and used lower-accuracy measurements for the remainder of the band in their determination of the molecular constants. As can be seen in Table 2, our line center values are in excellent agreement with those of Ref. 6 for lines with high  $J$  values in the  $P$  branch, but the agreement progressively deteriorates for lines that are further away from this region.

#### 4. DISCUSSION

We have measured the line centers, pressure shift coefficients, and pressure-broadening coefficients for 25 lines of the  $2\nu_3$  rotational–vibrational band of hydrogen cyanide  $\text{H}^{13}\text{C}^{14}\text{N}$ . We find that the pressure shift varies considerably with line number, from approximately  $+0.09\text{ pm/kPa}$  to  $-0.15\text{ pm/kPa}$  (approximately  $-1.5$  to  $+2.5\text{ MHz/Torr}$ ). The pressure broadening also varies with line

**Table 3. Molecular Constants for  $\text{H}^{13}\text{C}^{14}\text{N}^a$**

Constant	This Work ( $\text{cm}^{-1}$ )	Ref. 16	Difference	Ref. 6	Difference
$\Delta T$	6483.28225(2)	—	—	6483.28267(18)	$-0.00042(18)$
$B'$	1.42045356(27)	—	—	1.42045300(46)	$5.6(53) \times 10^{-7}$
$D'$	$2.7225(9) \times 10^{-6}$	—	—	$2.7039(26) \times 10^{-6}$	$1.9(3) \times 10^{-8}$
$H'$	$3.3(9) \times 10^{-12}$	—	—	—	—
$B''$	1.44000029(27)	1.44000046(4)	$-1.7(27) \times 10^{-7}$	1.44000020(22)	$0.9(35) \times 10^{-7}$
$D''$	$2.7684(9) \times 10^{-6}$	$2.7682(3) \times 10^{-6}$	$2(10) \times 10^{-10}$	$2.7525(26) \times 10^{-6}$	$1.6(3) \times 10^{-8}$
$H''$	$2.63(90) \times 10^{-12}$	$2.66(35) \times 10^{-12}$	$-0.03(96) \times 10^{-12}$	—	—

<sup>a</sup>Constants were obtained from a fit of our extrapolated zero-pressure line center values to Eq. (2).  $\Delta T$  is the wavenumber of the pure vibrational transition (band origin).  $B'$ ,  $D'$ , and  $H'$  are the excited-state molecular constants; and  $B''$ ,  $D''$ , and  $H''$  are the ground-state molecular constants. Comparisons with constants reported in Refs. 6 and 16 (converted to  $\text{cm}^{-1}$ ) are also shown. The standard uncertainties ( $1\sigma$ ) in the final digits of the values are indicated in parentheses; we assumed that the uncertainties quoted in Ref. 16 are  $1\sigma$ . Our standard uncertainty for the band origin  $\Delta T$  includes a  $4 \times 10^{-6}\text{ cm}^{-1}$  fit uncertainty and a  $1.7 \times 10^{-5}\text{ cm}^{-1}$  wavelength measurement uncertainty.

**Table 4. Calculated Wavenumbers and Vacuum Wavelengths of Line Centers<sup>a</sup>**

$R$ Branch	Wavenumber ( $\text{cm}^{-1}$ )	Wavelength (nm)	$P$ Branch	Wavenumber ( $\text{cm}^{-1}$ )	Wavelength (nm)
$R27$	6547.83810(10)	1527.221633(25)	$P1$	6480.40226(3)	1543.114084(8)
$R26$	6546.07370(8)	1527.633273(18)	$P2$	6477.48325(3)	1543.809474(8)
$R25$	6544.26885(6)	1528.054581(13)	$P3$	6474.52527(3)	1544.514784(8)
$R24$	6542.42358(4)	1528.485564(10)	$P4$	6471.52840(3)	1545.230025(8)
$R23$	6540.53793(4)	1528.926231(9)	$P5$	6468.49272(3)	1545.955208(8)
$R22$	6538.61193(4)	1529.376588(8)	$P6$	6465.41828(3)	1546.690341(8)
$R21$	6536.64562(4)	1529.836645(8)	$P7$	6462.30516(3)	1547.435435(8)
$R20$	6534.63904(4)	1530.306408(8)	$P8$	6459.15344(3)	1548.190500(8)
$R19$	6532.59224(4)	1530.785886(8)	$P9$	6455.96319(3)	1548.955548(8)
$R18$	6530.50525(4)	1531.275088(8)	$P10$	6452.73448(3)	1549.730587(8)
$R17$	6528.37812(4)	1531.774020(8)	$P11$	6449.46740(3)	1550.515629(8)
$R16$	6526.21089(4)	1532.282693(8)	$P12$	6446.16201(3)	1551.310685(8)
$R15$	6524.00362(4)	1532.801112(8)	$P13$	6442.81840(3)	1552.115765(8)
$R14$	6521.75633(3)	1533.329289(8)	$P14$	6439.43664(3)	1552.930879(8)
$R13$	6519.46910(3)	1533.867229(8)	$P15$	6436.01682(3)	1553.756039(8)
$R12$	6517.14195(3)	1534.414943(8)	$P16$	6432.55902(3)	1554.591255(8)
$R11$	6514.77496(3)	1534.972439(8)	$P17$	6429.06332(3)	1555.436539(8)
$R10$	6512.36815(3)	1535.539724(8)	$P18$	6425.52981(3)	1556.291901(8)
$R9$	6509.92160(3)	1536.116810(8)	$P19$	6421.95857(4)	1557.157353(8)
$R8$	6507.43535(3)	1536.703703(8)	$P20$	6418.34968(4)	1558.032905(8)
$R7$	6504.90946(3)	1537.300413(8)	$P21$	6414.70324(4)	1558.918569(8)
$R6$	6502.34398(3)	1537.906949(8)	$P22$	6411.01934(3)	1559.814356(8)
$R5$	6499.73898(3)	1538.523321(8)	$P23$	6407.29806(3)	1560.720278(8)
$R4$	6497.09451(3)	1539.149536(8)	$P24$	6403.53949(4)	1561.636345(9)
$R3$	6494.41063(3)	1539.785605(8)	$P25$	6399.74373(4)	1562.562569(10)
$R2$	6491.68740(3)	1540.431537(8)	$P26$	6395.91087(5)	1563.498962(13)
$R1$	6488.92489(3)	1541.087341(8)	$P27$	6392.04100(7)	1564.445534(18)
$R0$	6486.12315(3)	1541.753028(8)	$P28$	6388.13423(10)	1565.402298(25)

<sup>a</sup>Line centers between  $R27$  and  $P28$  are calculated from the molecular constants returned by the fit to Eq (2). The uncertainties in the final digit of the values are indicated in parentheses. The uncertainties are combined expanded uncertainties ( $2\sigma$ ) that include our wavelength uncertainty ( $8 \times 10^{-6}\text{ nm}$ ) and the molecular constants fit uncertainty (typically  $2 \times 10^{-6}\text{ nm}$ ).



number and is typically between 1 and 5.4 pm/kPa (17–90 MHz/Torr); the broadening was largest on the stronger lines of each branch. We determined the line centers of the majority of these lines with an expanded uncertainty ( $2\sigma$ ) of 0.01 pm ( $\approx 1$  MHz), an improvement by more than an order of magnitude over previous line center measurements of this band. We also determined the ground- and excited-state molecular constants for the band, yielding improved results for the band origin and excited-state molecular constants.

Our pressure shift and broadening measurements of  $\text{H}^{13}\text{C}^{14}\text{N}$  show significantly different trends compared with our results for acetylene<sup>1</sup> and carbon monoxide.<sup>4</sup> This is not surprising since HCN is a strongly polar molecule and hence long-range dipole–dipole interactions dominate the collisional process. The Boltzmann-like distribution of the broadening coefficients has been noted in previous work.<sup>17</sup> The authors in Ref. 17 conclude that rotationally resonant dipole collisions, where one molecule goes from  $J$  to  $J+1$  and the other from  $J+1$  to  $J$ , have large cross sections in HCN and dominate the pressure broadening. The strong asymmetry of the pressure shift between the  $R$  and  $P$  branches and changes in sign that we observe here have also been observed in hydrogen fluoride and are analyzed in Ref. 18 in the framework of the impact approximation with an expansion of the  $S$  matrix to second order with respect to the intermolecular potential energy. The authors conclude that the sign of the shift depends on whether the first- or second-order term dominates.

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