

Thermodynamic Properties of Steam in the Critical Region

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An analysis is presented of the experimental data on thermodynamic properties in the critical region of steam. The model used is that of revised and extended scaling, as given by the modern theory of critical phenomena. All thermodynamic properties are given in closed (parametric) form. The model has, in addition to three universal constants that are given by theory, sixteen adjustable parameters that were obtained by least-squares fit to *PVT* and speed-of-sound data. It is valid in the range 200–420 kg/m³ in density and 644–693 K in temperature. It accurately represents the experimental data for equation of state, vapor pressure, latent heat, specific heats C_p and C_v , and speed of sound. Our analysis permits new estimates of the critical parameters of steam, and has led to a number of conclusions regarding the mutual consistency of the experimental data. Tabulated values of the thermodynamic properties of steam are appended to the paper.

Key words: critical parameters; critical region; energy; equation of state; latent heat; scaling laws; specific heat; speed of sound; steam; thermodynamic function; thermodynamic tables; vapor pressure; water.

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1. Introduction

The modern theory of critical phenomena gives detailed predictions for the singular behavior of thermodynamic properties in fluids. In this paper we present the results of an analysis of the thermodynamic behavior of steam in the criti-

cal region in terms of a revised and extended scaled fundamental equation that incorporates these theoretical predictions. The use of this equation makes it possible to assess the consistency between the data for various thermodynamic properties of steam, such as the PVT properties, specific heats, and speed of sound. Detailed comparisons of these experimental data and the theoretical surface are presented. Tabulated values of the thermodynamic properties pressure, enthalpy, entropy, energy, specific heats at constant pressure and at constant volume, and speed of sound are given with temperature and density as entries. These tables will be helpful for testing global formulations of the thermodynamic behavior of steam for adequacy in the critical region, and for supplementing such formulations if they are found wanting.

In this paper, we introduce the concepts of critical anomalies and critical exponents in Sec. 2. The fundamental equation is developed in Sec. 3, while a complete listing of the equations for the thermodynamic properties is given in Appendix A, and the constants defining the equation are listed in Appendix B. In Sec. 4 the various data sources are discussed. Section 5 deals with the selection of critical constants for steam. Sections 6–10 are devoted to comparisons of experimental data for the equation of state, vapor pressure, latent heat, energy, specific heats C_v and C_p , and speed-of-sound with the predictions of our surface. Section 11 gives the values of the critical amplitude ratios, and compares them with the universal theoretical values. As mentioned in Sec. 12, tables of the thermodynamic properties of steam in the critical region have been prepared. These tables of the thermodynamic properties as a function of temperature along isochores, and also as a function of temperature and of pressure at saturation, are given in Appendix C. Appendix D lists the computer program used to generate the tables of thermodynamic properties. Appendix E gives units and conversion factors. Section 13 summarizes the principal conclusions of our work.

2. Critical Exponents

It is well known that thermodynamic properties show anomalous behavior when the critical point is approached. These critical anomalies are described by so-called power laws. If we denote by the symbol Δ the departure of a property from its critical value, and denote by an asterisk (*) a property value made dimensionless by appropriate combinations of the critical pressure, temperature, and density, then examples of these power laws are the following¹:

$$\begin{aligned}
 &\text{Compressibility along} & K_T^* &= \Gamma^\pm |\Delta T^*|^{-\gamma}, \\
 &\text{critical isochore:} & & \\
 &\text{Pressure along critical} & |\Delta P^*| &= D |\Delta \rho^*|^\delta, \\
 &\text{isotherm:} & & \\
 &\text{Density along coexistence} & |\Delta \rho^*| &= B |\Delta T^*|^\beta, \\
 &\text{curve:} & & \\
 &\text{Specific heat at constant} & C_v^* &= A^\pm |\Delta T^*|^{-\alpha}. \\
 &\text{volume along critical isochore:} & &
 \end{aligned} \tag{1}$$

Here ρ denotes the density, T the temperature, P the pressure. The superscript $+$ denotes an approach to the critical

temperature from higher, the superscript $-$ the same from lower temperatures. Only two of the critical exponents α , β , γ , and δ are independent. The others follow from them through scaling relations listed in Appendix A, (A.13) and (A.14). The constants Γ^\pm , D , B , A^\pm are called critical amplitudes.

The theory of critical phenomena asserts that the critical exponents of all fluids are the same, and to be identified with those calculated theoretically for three-dimensional Ising-like systems. This prediction has been verified by accurate experiments in a number of fluids. For reviews, we refer to Refs. 2–5. The available experimental material strongly supports the critical behavior of steam to be of the same type as that in other simpler fluids.⁶ In this work, we have therefore fixed the critical exponents at values predicted theoretically, namely,⁷

$$\beta = 0.325, \quad \delta = 4.82, \quad \Delta_1 = 0.50, \tag{2}$$

where Δ_1 is a "gap" exponent to be introduced in the next section. Values of the other exponents then follow from relations (A.13) and (A.14).

3. Fundamental Equation

Our fundamental equation is the one introduced by Ley-Koo and Green^{3,8}; these authors adapted, for use in representing fluid behavior, an expansion of the free energy around the critical point that had been proposed by Wegner⁹ for magnetic systems. The potential used in our work is $\tilde{P} = P^*/T^*$ as a function of $\tilde{\mu} = \mu^*/T^*$ and $\tilde{T} = -1/T^*$. Here P is the pressure, μ the chemical potential, and T the absolute temperature. Asterisks denote reduced properties: $P^* = P/P_c$, $T^* = T/T_c$, and $\mu^* = \mu\rho_c/P_c$, where P_c is the critical pressure, T_c the critical temperature, and ρ_c the critical density. This potential differs from those used in engineering applications in that both dependent and independent variables are intensive or "field" variables. As a consequence, the thermodynamic surface has a very simple structure, the vapor and liquid parts meeting with a discontinuous change in slope along a seam below T_c . This structure is consistent with the facts that intensive ("field") properties are identical in coexisting phases while their derivatives

$$(\partial \tilde{P} / \partial \tilde{\mu})_{\tilde{T}} = \tilde{\rho}, \quad (\partial \tilde{P} / \partial \tilde{T})_{\tilde{\mu}} = \tilde{U} \tag{3}$$

change discontinuously. Here $\tilde{U} = U/P_c V$, the reduced energy density, and $\tilde{\rho} = \rho/\rho_c$. In an approach to the critical point, the discontinuity in slope diminishes, to disappear at T_c . At the same time, however, the curvature of the surface at the phase boundary increases, and at the critical point the second derivatives

$$(\partial^2 \tilde{P} / \partial \tilde{\mu}^2)_{\tilde{T}} = \tilde{\chi}_T \tag{4}$$

as well as $(\partial^2 \tilde{P} / \partial \tilde{T}^2)_{\tilde{\mu}}$ and $(\partial^2 \tilde{P} / \partial \tilde{\mu} \partial \tilde{T})$ diverge strongly. Here $\tilde{\chi}_T$ denotes the reduced value of $\rho^2 TK_T$, K_T being the isothermal compressibility.

On the surface, there is only one direction singled out as special, namely, that of the seam, the vapor-liquid equilibrium curve. One can imagine this seam extrapolated into the one-phase region. We represent the seam by the relation between μ and T of its projection on the μ - T plane in terms

of an analytic representation

$$\tilde{\mu}_0(\tilde{T}) = \tilde{\mu}_c + \sum_{j=1}^3 \tilde{\mu}_j(\Delta\tilde{T})^j, \quad (5)$$

where

$$\Delta\tilde{T} = \tilde{T} + 1. \quad (6)$$

The assumption of analyticity of $\tilde{\mu}_0(\tilde{T})$ is essential; it is hard to prove experimentally, although some evidence has been accumulated, mainly from the behavior of the two-phase C_p .^{4,10} The analyticity is a feature not only of the Ising model and the lattice gas, but also of the decorated lattice models^{11,12} that closely represent the asymmetry between the liquid and the vapor observed in the laboratory and that is reflected, for instance, in the temperature variation of the average of coexisting liquid and vapor densities ("slope of the diameter").

In scaling, the physical variables $\tilde{\mu}$, \tilde{T} are transformed to a new coordinate system, one axis of which is the curve $\tilde{\mu}_0(\tilde{T})$. The other axis intersects the first at the critical point in a direction that is, in principle, arbitrary. Early scaling equations used the line $\tilde{T} = -1$, or $T = T_c$, as this axis. In the present work, we allow this axis to be in an arbitrary direction. This is achieved by writing the second variable as a linear combination of $\tilde{\mu} - \tilde{\mu}_0(\tilde{T}) = \Delta\tilde{\mu}$ and $\tilde{T} + 1 = \Delta\tilde{T}$. Thus, the independent scaling variables u_μ , u_t are constructed as follows, as analytic functions of $\tilde{\mu}$ and \tilde{T} :

$$au_\mu = \tilde{\mu} - \tilde{\mu}_0(\tilde{T}) = \Delta\tilde{\mu}, \quad (7)$$

$$u_t = \Delta\tilde{T} + c\Delta\tilde{\mu}.$$

Here a is an arbitrary scaling constant (see below) and c is the so-called mixing parameter.³ The potential \tilde{P} is now decomposed into two parts, one part \tilde{P}_{reg} , that is regular in the scaling variables and another part $\Delta\tilde{P}$, that contains the critical anomalies. One can think of the regular part as an analytic surface in $\tilde{P}(u_\mu, u_t)$ or $P(\mu, T)$ space, tangent to the thermodynamic surface at the critical point. It contains, therefore, the information on the critical-point values of the first derivatives ρ_c and U_c . The scaled part is to produce the infinities in second derivatives at the critical point. The asymptotic critical behavior is incorporated by postulating for this anomalous part the following generalized homogeneous form^{1,13}:

$$\Delta\tilde{P} = ak_0|u_t|^{2-\alpha}g_0\left(\frac{u_\mu}{|u_t|^{\beta\delta}}\right). \quad (8)$$

Here k_0 is a second arbitrary scaling constant; α , β , and δ are critical exponents defined in Eq. (1). Only two of these are independent; their values are universal, that is, the same for all fluids and other Ising-like systems. The function g_0 of the scaling fields is likewise universal, the argument in parentheses indicating functional dependence.

Apart from the implicit presence of the mixing parameter c , which disrupts symmetry in a nonuniversal manner, the scaled part of the potential contains only two arbitrary constants, a and k_0 , which one can think of as setting two scales, namely, for two of the three physical variables. The relation of generalized homogeneity (8) does not allow a free choice of more than two such factors.

Wegner⁹ showed that higher-order confluent singulari-

ties must be present at the critical point. In the present work, we will take one Wegner correction to scaling into account. Our potential thus has the form³:

$$\tilde{P}(u_t, u_\mu) = \tilde{P}_{\text{reg}}(u_t, u_\mu) + ak_0|u_t|^{2-\alpha}g_0\left(\frac{u_\mu}{|u_t|^{\beta\delta}}\right) + ak_1|u_t|^{2-\alpha+\Delta_1}g_1\left(\frac{u_\mu}{|u_t|^{\beta\delta}}\right). \quad (9)$$

The correction-to-scaling function g_1 is again a universal function of the same scaling variable $u_\mu/|u_t|^{\beta\delta}$. This function is multiplied by a different power of u_t than in the asymptotic term; a new critical exponent Δ_1 has been introduced, and, in addition, a new nonuniversal amplitude factor k_1 .

For the regular part of the potential, we have chosen the form:

$$\tilde{P}_{\text{reg}} = \tilde{P}_0(\tilde{T}) + \Delta\tilde{\mu} + \tilde{P}_{11}\Delta\tilde{\mu}\Delta\tilde{T}, \quad (10)$$

$$\tilde{P}_0(\tilde{T}) = 1 + \sum_{j=1}^3 \tilde{P}_j(\Delta\tilde{T})^j.$$

It may be worth pointing out that the term $\tilde{P}_{11}\Delta\tilde{\mu}\Delta\tilde{T}$ gives a contribution to the density linear in temperature and thus is responsible, in part, for introducing asymmetry in our model. It would be dangerous to identify this contribution with the temperature dependence of the coexistence curve diameter, since a second important, but anomalous, contribution to the slope of the diameter, proportional to $|\Delta\tilde{T}|^{1-\alpha}$, comes from the "mixing of variables."

Having thus completed the formal presentation of our potential, we proceed to the computational part. An important device for handling scaled equations is the transformation to Schofield's¹⁴ parametric variables r and θ , which denote, respectively, a distance from the critical point and a location on a contour of constant r . The scaling variables are transformed to parametric variables by the relations

$$\begin{aligned} u_\mu &= r^{\beta\delta}\theta(1-\theta^2), \\ u_t &= r(1-b^2\theta^2), \end{aligned} \quad (11)$$

in which the constant b^2 is universal. The variable θ reaches the values ± 1 on the coexistence curve. In asymptotic scaling, the assumption is made that the density $\Delta\tilde{\rho}$ varies linearly in θ :

$$\Delta\tilde{\rho} = k_0r^\beta\theta. \quad (12)$$

With this "linear-model" assumption, the potential and all its derivatives can be written in algebraically closed form, as simple polynomials in θ , with universal coefficients that are functions of the critical exponents β and δ .¹ We have made this assumption not only for the leading contribution to $\Delta\tilde{\rho}$, but also for that arising from the first Wegner correction. This choice leads to a similar set of polynomials in θ for the Wegner correction-to-scaling, with universal coefficients that are functions of the critical exponents β , δ , Δ_1 . The relevant expressions are all listed in Appendix A. We stress here that the seemingly complicating device of transformation to parametric variables has considerable advantages. Scaled algebraically closed forms that have been postulated for the equation of state^{10,15-17} are not integrable in closed form and other thermodynamic properties have to be de-

rived from them by numerical integration. These forms invariably suffer from the additional defect that they have a line of higher-order nonanalyticities stretching out from the critical point into the one-phase region. The linear-model parametric form possesses neither of these defects. Moreover, the use of the parametric form greatly simplifies the Legendre transformations that the thermodynamicist cannot escape.

Our fundamental equation contains the following constants:

| | | |
|---|---|---|
| 3 critical exponents (universal) | : | $\beta, \delta, \Delta_1,$ |
| 3 critical parameters | : | $P_c, \rho_c, T_c,$ |
| 5 parameters of the scaling function | : | $a, k_0, k_1, c, b^2,$ |
| 4 background parameters for the pressure | : | $\tilde{P}_1, \tilde{P}_2, \tilde{P}_3, \tilde{P}_{11},$ |
| 4 background parameters for caloric properties | : | $\tilde{\mu}_c, \tilde{\mu}_1, \tilde{\mu}_2, \tilde{\mu}_3.$ |

In what follows we will discuss how these parameters were determined. The values of the constants that we have used are listed in Appendix B. The equation is valid in a range of temperatures and densities as indicated in Fig. 1. All temperatures quoted are on the International Practical Temperature Scale of 1968, IPTS 1968,¹⁸ unless otherwise indicated. This potential was applied before by us to steam.¹⁹ The present results differ from those previously reported principally in a modified choice of the value of T_c .

Finally, a few remarks about the critical amplitudes introduced in Eq. (1). These amplitudes refer to limiting behavior and therefore contain no contributions from the correction-to-scaling term. Since the leading asymptotic term contains only two free constants, the six critical amplitudes introduced in Eq. (1) cannot be independent. Four relations between these amplitudes are listed in the Appendix, Eqs. (A38)–(A41). Theoretical predictions exist for these universal amplitude ratios.²⁰ In our fits of the potential to the properties of steam, we have left the constant b^2 adjustable, so

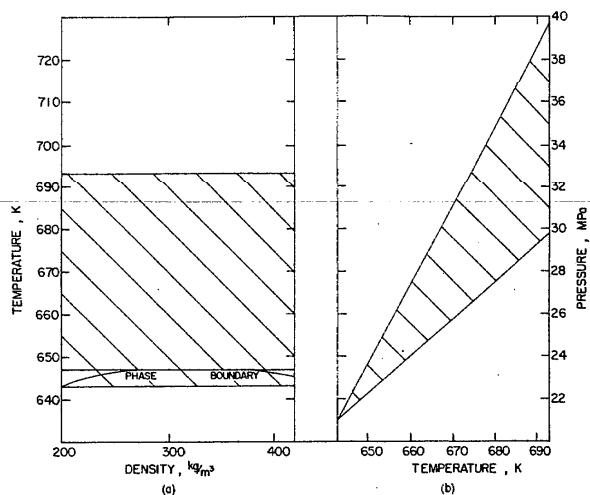


FIG. 1. Range of validity of the thermodynamic surface presented here in terms of (a) temperatures and densities, and (b) temperatures and pressures.

that a check on the universality of the amplitude ratios became possible.

4. Data Sources for Steam

In Table 1 we list the data sources relevant to this paper. The vapor pressure²¹ and latent heat²² data of Osborne and collaborators are, although almost 50 yr old, of unsurpassed quality and indispensable in the formulation of the thermodynamic behavior of steam. We have used these data to validate our surface below the critical point and to determine the critical parameters of steam. The *PVT* data of Rivkin *et al.*^{23,24} have formed the basis for determining most of the adjustable constants in our equation after we ascertained their consistency with the data of Osborne *et al.* The more recent high-quality *PVT* data of Kell *et al.*²⁵ are not in our range of interest, but we have ascertained the mutual consistency of the Kell and Osborne vapor pressure at 350 °C to be of the order of 5 mK. Caloric data of high quality are the C_p data of Sirota and Maltsev²⁶ and the speed-of-sound data of Erokhin and Kalyanov.²⁷ The latter were used to determine a few of the caloric "background" parameters in our equation. For both C_p and speed of sound, small adjustments of the temperature scales with respect to that of Rivkin *et al.* were required in order to obtain mutual consistency. The resulting thermodynamic surface, determined up to the integration constants for energy and entropy, was proven to be consistent with the energy and C_v data of Baehr and Schömäcker^{28,29} and with selected C_v data of Amir Khanov *et al.*³⁰

Table 1. Data sources

| Property | First author | Ref | Year |
|-----------------------------------|--------------|-------|---------|
| Vapor pressure | Osborne | 21 | 1933 |
| Latent heat | Osborne | 22 | 1937 |
| <i>PVT</i> | Rivkin | 23,24 | 1962-66 |
| Specific heat C_p | Sirota | 26 | 1962 |
| Specific heat C_v and energy | Baehr | 28,29 | 1974-75 |
| Specific heat C_v | Amir Khanov | 30 | 1974 |
| Speed of sound | Erokhin | 27 | 1980 |
| P_c, T_c | Blank | 31 | 1969 |
| P_c, T_c , vapor pressure | Scheffler | 32,33 | 1981 |

We have paid attention to the earlier³¹ and to the recent direct determination of the critical parameters P_c, T_c of steam by Scheffler *et al.*,^{32,33} and have found the latter marginally compatible with the surface presented here.

5. Critical Parameters for Steam

The values of the critical parameters P_c, T_c have been repeatedly determined in an apparatus first designed and built by Blank, an optical high-pressure cell in which the difference in refractive index of coexisting phases could be observed to disappear. In the course of the years, several

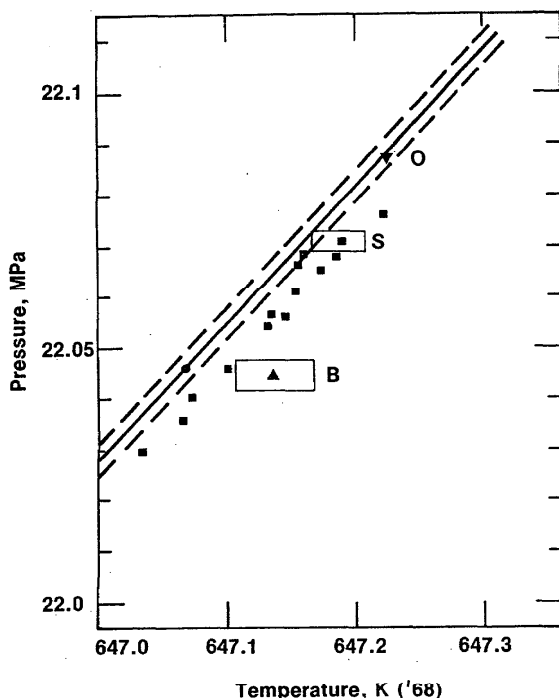


FIG. 2. The full curve is the vapor pressure curve and critical isochore according to our surface based on the *PVT* data of Rivkin *et al.* (Refs. 23 and 24). The dashed curves are confidence limits based on Rivkin's error estimates. The predicted vapor pressure curve agrees closely with the vapor pressures of Osborne *et al.* (Ref. 21). (Osborne's highest point, \blacktriangledown , we believe to be slightly supercritical). The direct determinations of P_c , T_c are those of Blank, \blacktriangle , (Ref. 31) and of Scheffler *et al.*, \blacksquare , (Refs. 32 and 33). Their respective error estimates are indicated by rectangles. Vapor pressure measurements of Scheffler *et al.* \blacksquare , are also shown, as far as they are in the range of this plot. Our indirect determination of T_c based on the latent heats of Osborne *et al.* (Ref. 22) is indicated by \bullet ; it is 0.12 K below the T_c value of Scheffler.

values of T_c were reported that ranged from 647.14 K³¹ to 647.19 K in the most recent experiment by Scheffler *et al.*^{32,33} The value of P_c reported by Blank falls about 0.01 MPa below the surface determined by Rivkin's data (Fig. 2). Scheffler *et al.* made considerable improvement in the pressure measurements; they reported $T_c = (647.19 \pm 0.02)$ K, $P_c = (22.071 \pm 0.002)$ MPa.

Although this point lies about 0.006 MPa below Rivkin's *PVT* surface (Fig. 2), this pressure difference is within the combined estimated uncertainty. We have determined critical-point parameters in a different way, namely, by analysis of appropriate fluid property data in the critical region. The analysis tools are the scaling laws, and the analysis proceeds in two steps. First, from experimental values of extensive properties in coexisting phases, such as densities, refractive indices, or latent heats, the temperature at which these properties become equal, i.e., the critical temperature T_c , can be estimated with a reliability depending on the accuracy and distribution of the property data considered. We were fortunate to have the latent heat data of Osborne *et al.* available for this purpose. Secondly, from a scaled analysis of vapor pressure and *PVT* data the vapor pressure curve and its extension, the critical isochore, can be established with

good precision, but the actual value of T_c is usually poorly defined. Once, however, the value of T_c is established by other means, that of P_c follows immediately. This is the path we have followed in an indirect determination of the critical parameters of steam. The vapor pressure and latent heat data of Osborne *et al.*^{21,22} have documented traceability and accuracy of pressure and temperature scales, and are consistent with Rivkin's *PVT* data to a better degree than with the (P_c, T_c) value of Scheffler *et al.* Therefore we have refrained from using the latter.

Osborne *et al.* measured the latent heats g , b , accompanying isothermal extraction of unit mass of vapor, resp. liquid, from their calorimeter. These quantities are related to the densities ρ_L, ρ_V of the phases and the vapor pressure by

$$b = (T/\rho_L)(dP/dT)_{\text{vap}}, \quad (13)$$

$$g = (T/\rho_V)(dP/dT)_{\text{vap}}.$$

The known scaled expressions for ρ_L, ρ_V , and dP/dT (A32, A33) imply those for b and g . To leading order, $g - b$ behaves as $\rho_L - \rho_V$, that is, as $\Delta\tilde{T}^\beta$.

In a previous publication, a simple power-law expression $B|\Delta T^*|^\beta$ with free exponent β was fitted in the range 350–374 °C to the quantity $(g - b)/(g + b)$, after it was corrected for the slope of the coexistence-curve diameter.⁶ We obtained $T_c = (373.85 \pm 0.01)$ °C (IPTS 1948), the error indicating a doubling of χ^2 . The highest point 374 °C, was inconsistent with the other data and, consequently, excluded from the fit. The equations in Appendix A, however, can be used to represent the latent-heat data in a theoretically more satisfying manner, but in a smaller range. We used a preliminary fit of our potential to the *PVT* data to calculate all terms except the leading one. After subtracting the correction terms from the latent heat data (the largest correction, at the lowest temperature, being 1.5%), we fitted the corrected values of $(g - b)/(g + b)$ in the range 370–374 °C again to the asymptotic power law $B|\Delta T^*|^\beta$ with free exponent β . Again, the highest point seemed inconsistent and was excluded. The results for the dependence of the chi-square of the fit on the choice of T_c are given in Table 2. The optimum value of T_c was 373.84 °C (IPTS 1948), within 0.01° from the one published before,⁶ while the value 0.324 ± 0.002 obtained for the exponent β is in excellent agreement with the theory.⁷ A larger change, of 0.07 °C, is now required for doubling χ^2 , which reflects increased uncertainty because of the smallness of the range. Thus, we have assumed for T_c in this paper

$$T_c = 373.84 \text{ °C (IPTS 1948)} = 647.067 \text{ K (IPTS 1968)}, \quad (14)$$

given a difference of 0.077 K between readings on IPTS 1948 and IPTS 1968 near the critical point of steam.¹⁸ The corresponding value of P_c is unequivocally defined by the vapor pressure and *PVT* data. We obtained

$$P_c = 22.046 \text{ MPa} \quad (15)$$

with an intrinsic uncertainty of 0.003 MPa and one propagated from the temperature uncertainty δT_c , so that $\delta P_c = (0.267\delta T_c \pm 0.003)$ MPa. The value of ρ_c can be inferred from a scaled fit to *PVT* data or from further analysis of the latent heat data.

Table 2. Analysis of the latent heat of steam [22] with varying T_c

| T_c , °C (IPTS 1948) | Fit to uncorrected data in the range 330-373.5°C [6] | | Fit to corrected data in the range 370-373.5°C [this work] | |
|---------------------------|---|---------|---|---------|
| | χ^2 | β | χ^2 | β |
| 373.82 | | | 1.98 | 0.320 |
| 373.85 | 2.19 | 0.3357 | 1.84 | 0.322 |
| 373.84 | 1.06 | 0.3359 | 1.84 | 0.324 |
| 373.85 | 0.55 | 0.3361 | 1.96 | 0.326 |
| 373.86 | 0.66 | 0.3365 | 2.19 | 0.527 |
| 373.87 | 1.35 | 0.3365 | 2.53 | 0.329 |

Table 3. Critical parameters of steam

| | Used here | Estimated uncertainty | Direct determination | |
|------------------------------|-----------|---------------------------|----------------------|--------------------|
| | | | [31] | [33] |
| P_c , MPa | 22.0460 | (0.2676 $T_c \pm 0.003$) | 22.045 ± 0.003 | 22.071 ± 0.002 |
| T_c , K | 647.067 | ± 0.1 | 647.14 ± 0.03 | 647.19 ± 0.03 |
| ρ_c , kg/m ³ | 322.778 | ± 2.2 | | |

Our fit to the PVT data yields

$$\rho_c = 322.8 \text{ kg/m}^3, \quad (16)$$

while a latent-heat analysis gives $\rho_c = (321.2 \pm 3.1) \text{ kg/m}^3$. The values we have obtained for ρ_c from scaled fits of a variety of complexity give optimum ρ_c values no more than 2.2 kg/m^3 removed from the one given. Table 3 summarizes our results for the critical parameters of steam.

The value of T_c determined indirectly is substantially, 0.12 K, below that of the most recent direct determination.^{32,33} Against our choice weighs the fact that we have rejected the 374 °C latent heat values, but Osborne himself mentions considerable experimental difficulties at this point.²² In favor of our choice weighs the extraordinary consistency of latent heat, vapor pressure, and PVT data that is obtained as a result (cf. Sec. 7). We hesitate, however, to assign to our current knowledge of T_c an absolute accuracy of better than 0.1 °C.

6. Equation of State

The scaling function parameters a , k_0 , k_1 , c , b^2 , and the pressure background parameters \tilde{P}_1 , \tilde{P}_2 , \tilde{P}_3 , together with ρ_c , were determined by fitting the equation of state to the PVT data of Rivkin and co-workers.^{23,24} The parameter \tilde{P}_{11} was derived from the known slope of the coexistence curve diameter. The experimental data were assigned absolute weights by propagation of error on the basis of the following error estimates^{23,24} and private communication (S. L. Rivkin, 1977):

$$\sigma_P = 0.001 \text{ MPa}, \quad \sigma_T = 0.02 \text{ K}, \quad \sigma_\rho = 0.05\%. \quad (17)$$

The equation fits the experimental PVT data with statistic

chi-square of 0.58 in the range bounded by

$$200 \text{ kg/m}^3 \leq \rho \leq 420 \text{ kg/m}^3, \quad (18)$$

$$644 \text{ K} \leq T \leq 693 \text{ K}.$$

A comparison between the experimental PVT data and the values calculated from our equation is presented in Figs. 3-5, in the form of pressure deviations as function of density along various isotherms. The equation reproduces the data within the estimated experimental errors. Some systematic

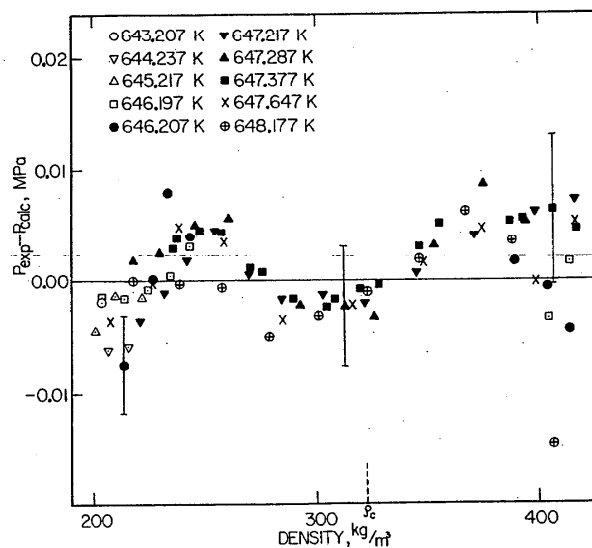


Fig. 3. Deviations of the experimental pressure data of Rivkin *et al.* from the calculated values in the temperature range $643.207 \text{ K} \leq T \leq 648.177 \text{ K}$.

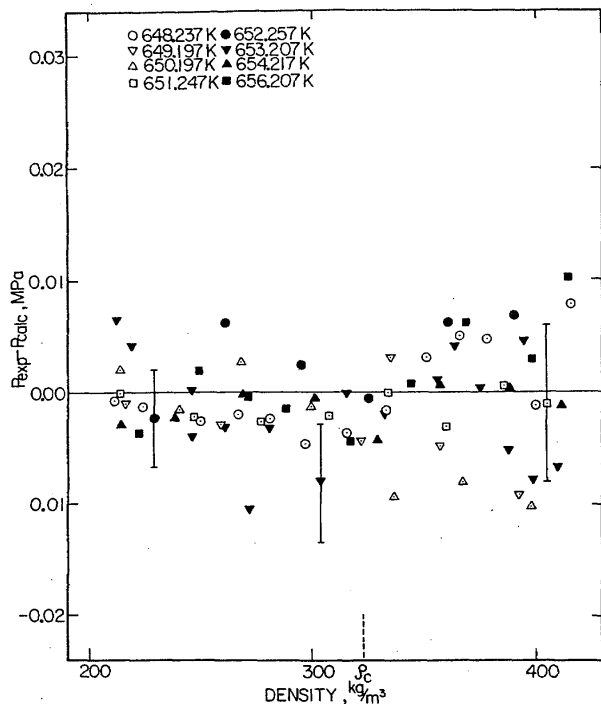


FIG. 4. Deviations of the experimental pressure data of Rivkin *et al.* from the calculated values in the temperature range 648.237 K < T < 656.207 K.

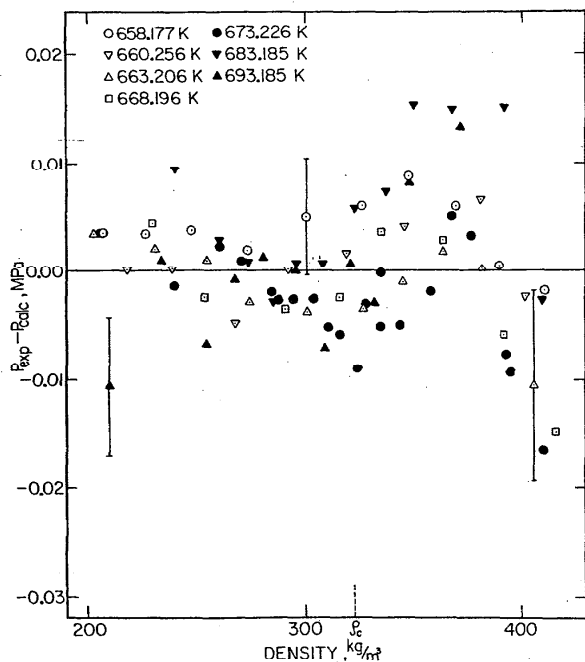


FIG. 5. Deviations of the experimental pressure data of Rivkin *et al.* from the calculated values in the temperature range 658.177 K < T < 693.185 K.

trends, albeit within the estimated error, are visible in the data within a few degrees from the critical point.

7. Vapor Pressure and Latent Heat

The equation of state fitted to the *PVT* data of Rivkin *et al.* can be used to predict the vapor pressure. A comparison

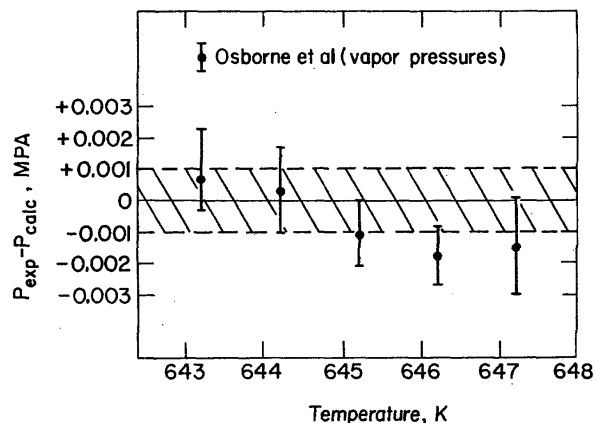


FIG. 6. Comparison between the vapor pressure data of Osborne *et al.* (Ref. 21) and the vapor pressures calculated from the equation of state deduced from the *PVT* data of Rivkin *et al.* (Refs. 23 and 24). The error bars denote the spread of the repeated measurements of (Ref. 21) and the error band corresponds to the direct pressure error of Rivkin's measurements, ± 0.001 MPa.

with the vapor pressures of Osborne *et al.*²¹ is presented in Fig. 6. Although a small systematic trend is present, the data agree with the predicted curve to better than 0.002 MPa. This is very good agreement in view of the fact that the spread by Osborne *et al.* of repeat determinations of the vapor pressure is about ± 0.001 MPa, and the uncertainty of the pressures of Rivkin *et al.* is given as ± 0.001 MPa, with no allowance made for a possible error in temperature.

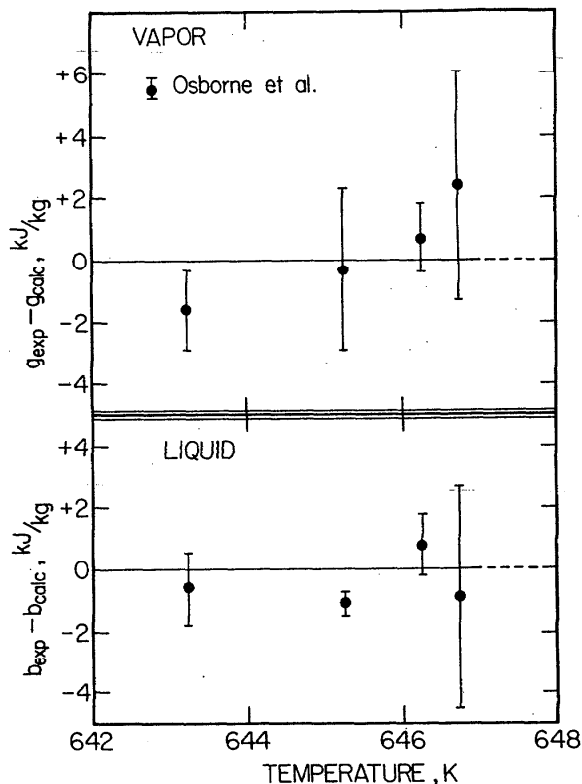


FIG. 7. Comparison between the latent heat data of Osborne *et al.* (Ref. 22) and the values calculated from our surface. The error bars indicate the standard deviations of the repeatedly measured data.

Table 4. Coexistence properties according to our equation, and the data of Osborne et al. [21,22]

| T, °C (IPTS 1948) | T, K (IPTS 1968) | P _{vap} (exp) MPa | P _{vap} (calc) MPa | g(exp) kJ/kg | g(calc) kJ/kg | b(exp) kJ/kg | b(calc) kJ/kg |
|----------------------|---------------------|-------------------------------|--------------------------------|-----------------|------------------|-----------------|------------------|
| 370 | 643.227 | 21.0524 | 21.0517 | 800.44 | 802.07 | 359.35 | 359.94 |
| 371 | 644.227 | 21.3056 | 21.3053 | | 771.25 | 374.29 | 376.11 |
| 372 | 645.227 | 21.5615 | 21.5625 | 733.65 | 733.93 | 395.48 | 396.57 |
| 373 | 646.227 | 21.8217 | 21.8235 | 683.05 | 682.34 | 427.56 | 426.72 |
| 373.5 | 646.727 | | 21.9555 | 642.98 | 640.54 | 452.35 | 453.23 |
| (374.0) | 647.227 | 22.0873 | 22.0888 | (586.62) | | (504.3) | |

The measured latent heats g , b ,²² can also be compared with our surface. The comparison is presented in Fig. 7. The highest point has been excluded, as discussed in Sec. 5. The experimental data agree to within the spread of repeat measurements with the prediction. The worst departure is 2 kJ/kg. The experimental and predicted values of vapor pressure and latent heats are shown in Table 4.

8. Sources of Error and Measures of Experimental Discrepancies

In the comparison of our surface with data other than those of Rivkin and Osborne, small discrepancies will usually be found that could be due to a number of factors that are usually not known. A major source of error will be the uncertainty in temperature. The critical temperature of steam is quite high, and it is hard to reproduce the temperature scale and eliminate the temperature gradients to better than a few hundredths of a degree unless special metrological precautions are taken. A similar problem arises with the pressure scale which, at 20 MPa, cannot be absolutely reproduced to much better than 1 part in 10^4 . Near the critical point, because of the near linearity of the isochores, 1 part in 10^4 in pressure corresponds with approximately 0.01 K, and a discrepancy found between data sets can be quantified either as a difference in temperature scale or in pressure scale, even though the actual cause of the discrepancy may be a different one. For reasons of convenience, we express discrepancies in terms of a difference in temperature scale from that defined by the Osborne-Rivkin data, which we consider as correct in view of their consistency and of the traceability of Osborne's scales.

Because of the strong divergences of the compressibility and the expansion coefficient near a critical point, uncertainties in pressures and temperature, and sample variability due to differences in impurity content, all cause greatly-enlarged errors in the density. Consequently, in those experiments where a property is reported as a function of pressure rather than density, the *location* of the maximum in a diverging quantity such as the isobaric C_p , or in the minimum of a quantity like the isothermal speed of sound, will appear *shifted in density* with respect to the predicted curve. As stated earlier, we will quantify the shift by stating the change in temperature scale required, with respect to that of the Osborne-Rivkin data, in order to eliminate the offset in the location of the extremum.

Quantification of a discrepancy between predicted and measured property data by means of an adjustment of the temperature scale is to be carefully distinguished from the uncertainty in the assignment of a value of T_c to the Rivkin *PVT* data (Sec. 5). The *PVT* data themselves are not sensitive to the choice of T_c . Derived properties, however, are, for instance, the main effect of a change in choice of T_c for the Rivkin data is a change in the predicted value of the peak *height* of a divergent quantity such as C_p , while the *location* of the peak is not affected. An offset in peak height will be quantified by giving the amount by which the T_c assignment to Rivkin's data is to be changed in order to eliminate the offset. In general, we will find that the shifts required to eliminate discrepancies are within reasonable expectations of experimental uncertainty. We have found no convincing reasons to doubt the accuracy of the model.

Finally, a source of error in near critical data that is not to be overlooked is that of gravity-induced density gradients in regions where the compressibility is high. As a consequence, the average bulk density in a *PVT* experiment departs from the density at the level at which the pressure is measured, while the theoretical infinity in C_v is suppressed. Moldover *et al.*³⁴ estimated the range from T_c within which gravity produces errors larger than 1% in the property in question on the critical isochore. These estimates were made for xenon in a cell 1 cm high. In steam, in a 10 cm high cell, these ranges would be 0.15 K for more than 1% error in C_v , and 0.3 K for more than 1% error in density. In the Rivkin *PVT* data, however, the intrinsic pressure error of 0.001 MPa is five times larger than the hydrostatic head in the cell, and therefore gives the dominant uncertainty in the density near the critical point. The C_v data of Baehr *et al.* were not taken within a range of 0.15 K from the critical temperature. Of the C_v data points of Amirchanov *et al.*, the one or two closest to the peak value occasionally are within the gravity-affected range.

9. Caloric Background, Energy, and Speed of Sound

The constants $\tilde{\mu}_i$ in the fundamental equation have to be determined from caloric properties. Of these constants, $\tilde{\mu}_c$ and $\tilde{\mu}_1$ are related to the zeropoints of entropy and energy; they enter into the first derivatives U , H , and S , but not into the second derivatives, specific heats, and speed of sound.

In previous work,¹⁹ the coefficients, $\bar{\mu}_1$ and $\bar{\mu}_2$ were determined by fitting the energy equation to the internal energy data of Baehr and co-workers²⁸ while the coefficient $\bar{\mu}_3$ was set equal to zero. Recently, however, Erokhin and Kalyanov have reported sound velocity data for steam in an extended region around the critical point.²⁷ The speed-of-sound data are more sensitive to the choice of the $\bar{\mu}_i$ ($i > 1$) so that these constants can be determined more accurately. The speed-of-sound data also indicate that the coefficient $\bar{\mu}_3$ in the expansion (A6a) for $\bar{\mu}_0(T)$ cannot be neglected in the temperature and density range under consideration.

If we determine the coefficients $\bar{\mu}_1$, $\bar{\mu}_2$, and $\bar{\mu}_3$ from the energy data of Baehr and co-workers^{28,29} in the way described before,¹⁹ we obtain

$$\begin{aligned}\bar{\mu}_1 &= -22.657 \pm 0.007, \\ \bar{\mu}_2 &= -17.750 \pm 0.345, \\ \bar{\mu}_3 &= -5.455 \pm 0.407.\end{aligned}\quad (19)$$

It should be noted that Baehr's energy values are anchored to those of the surface of Keenan *et al.* at 350 °C. On the other hand, if we determine $\bar{\mu}_2$ and $\bar{\mu}_3$ from the speed-of-sound data of Erokhin and Kalyanov²⁷ we obtain

$$\bar{\mu}_2 = -17.888 \pm 0.010, \quad \bar{\mu}_3 = -4.933 \pm 0.061. \quad (20)$$

The two sets of values are in excellent agreement, but the values deduced for $\bar{\mu}_2$ and $\bar{\mu}_3$ from speed-of-sound data evidently have a higher accuracy. These values, Eq. (20), have been adopted in this work.

This leaves the zeropoint constants $\bar{\mu}_c$ and $\bar{\mu}_1$ to be determined. This was done by identifying the energy and entropy of our surface at $T = 648.15$ K, $\rho = 230$ kg/m³, with those of the global surface proposed by Haar, Gallagher, and Kell.³⁵ The results are

$$\bar{\mu}_c = -11.233, \quad \bar{\mu}_1 = -22.655. \quad (21)$$

The value for $\bar{\mu}_1$ is in excellent agreement with that¹⁹ obtained from a direct fit to the energy data of Baehr *et al.*^{28,29}

After all constants in the equation have thus been deter-

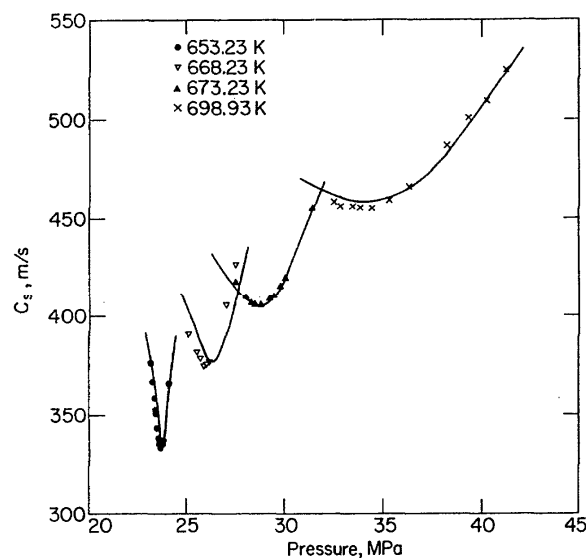


FIG. 9. The speed of sound as a function of pressure in the temperature range 653.23 K $< T < 698.93$ K. The data are those of Erokhin and Kalyanov (Ref. 27). The curves represent values predicted by our equation.

mined (Appendix B), comparisons will be made with experimental data for speed-of-sound, energy, and specific heat at constant volume.

A comparison of the speed-of-sound data of Erokhin and Kalyanov and the values calculated from our equation is presented in Figs. 8 and 9. The equation reproduces correctly the magnitude of the speed-of-sound minima at all temperatures indicating agreement with the value of T_c ascribed to Rivkin's data (cf. Sec. 8). In Fig. 10 we show how much the fit to the speed-of-sound data closest to the critical point improves by lowering their temperature values by 0.06 K; the location of the minima improves while the good agreement of the minimum values is retained.

In our opinion, a combined uncertainty in realization of

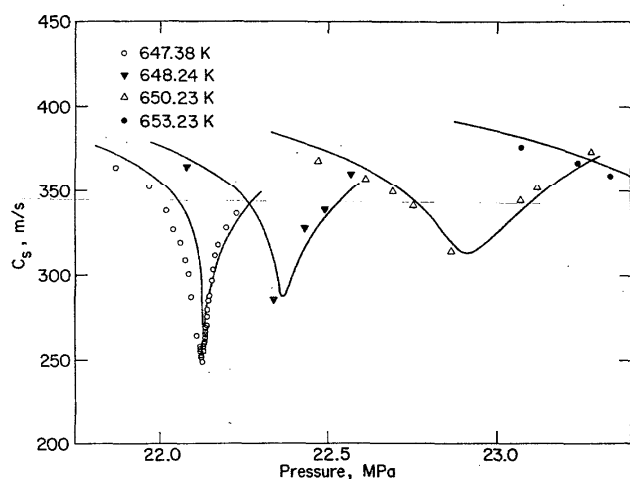


FIG. 8. The speed of sound as a function of pressure in the temperature range 647.38 K $< T < 653.23$ K. The data points are those of Erokhin and Kalyanov (Ref. 27). The curves represent values predicted by our equation.

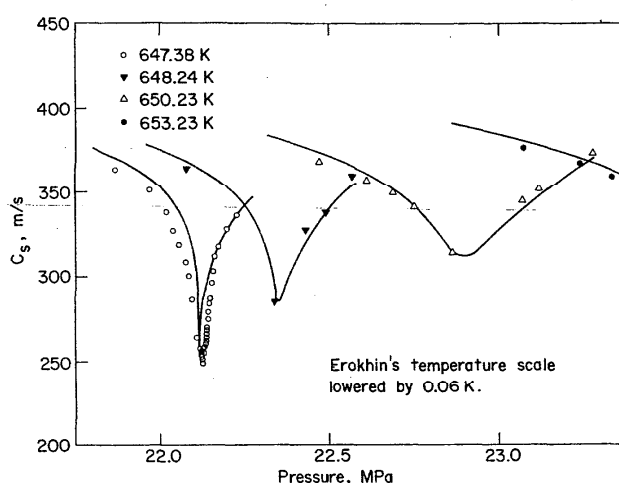


FIG. 10. Another comparison of the speed of sound in the same range as that of Fig. 8, but after subtracting 0.06 K from the temperature values of (Ref. 27). This temperature adjustment eliminates most of the systematic difference between data and prediction.

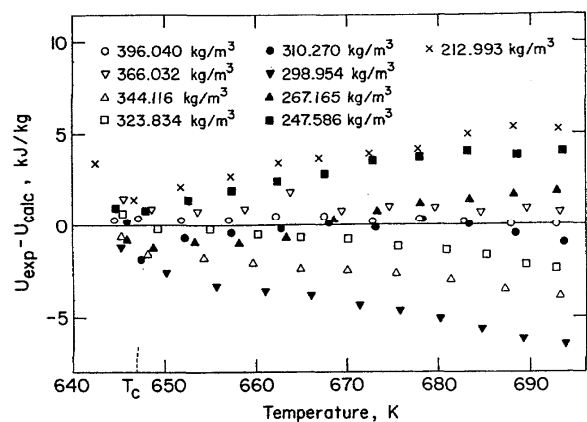


FIG. 11. Deviations of the experimental energy data of Baehr *et al.* (Ref. 28) from the calculated values.

pressure and temperature measurement and in sample composition, as expressed by 0.06 K in temperature, is not unreasonable.

The comparison with the energy data of Baehr *et al.*²⁸ is shown in Fig. 11. Although the deviations along each isochore have a systematic character, the departures from the surface are well within the claimed accuracy of the data. In Fig. 12 we compare with the C_v data reported by Baehr and Schomäcker.²⁹ The data were obtained as the ratio of energy increments ΔU over temperature increments ΔT , with ΔT of the order of degrees; the predicted curves in Fig. 12 represent the quantity $\Delta U/\Delta T$, with ΔT the experimental temperature increments. In general, the data are accurately consistent with the weakly diverging specific heat C_v predicted by the scaling laws. An exception is formed by some of the two-phase data on the 310.27 kg/m³ isochore that do not rise steeply enough. No adjustment of the temperature scale was required.

Amirkhanov, Kerimov, and co-workers have, at various occasions, published detailed measurements of the specific heat C_v near the phase boundary. A previous analysis indicated that not all these data appeared to be mutually consistent.⁶

In a book published since by Amirkhanov *et al.*,³⁰ the

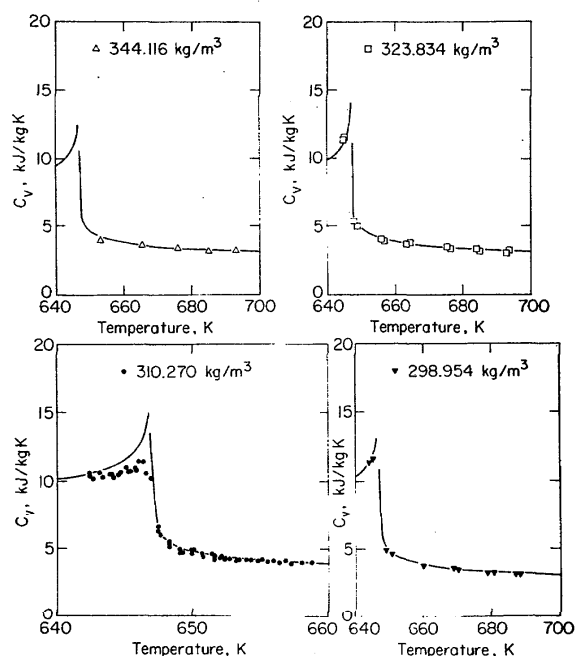


FIG. 12. The specific heat $\bar{C}_v = \Delta U/\Delta T$ as a function of temperature. The symbols represent the data reported by Baehr and Schomäcker (Ref. 29). The curves represent values predicted by our equation.

older measurements are scrutinized; several sets being discarded because of the presence of air. This book, however, also contains new C_v data not hitherto published. Those are the ones we compare with here. A problem we encountered is that the jump in C_v , from a 2-phase to a 1-phase value, occurs between 374.10 and 374.18 °C (IPTS 1948), which is 0.31 °C above our choice of T_c . After all of Amirkhanov's temperatures were lowered by this amount, (a much larger adjustment than for any of the other data, and one for which we have no satisfactory explanation), our surface gives a very close representation of this anomalous region of C_v (Fig. 13). Note especially how well the steep rise in C_v is represented on the 315.457 kg/m³ isochore where the two-phase C_v doubles in a span of a few K. As mentioned, Baehr's nearby isochore did not show this predicted rise in the two-phase region (Fig. 12).

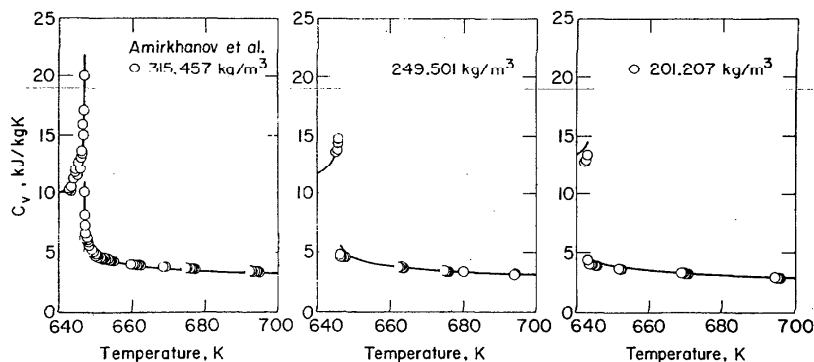


FIG. 13. The specific heat C_v as a function of temperature. The circles represent the data of Amirkhanov *et al.* (Ref. 30) after 0.31 K was subtracted from all experimental temperatures.

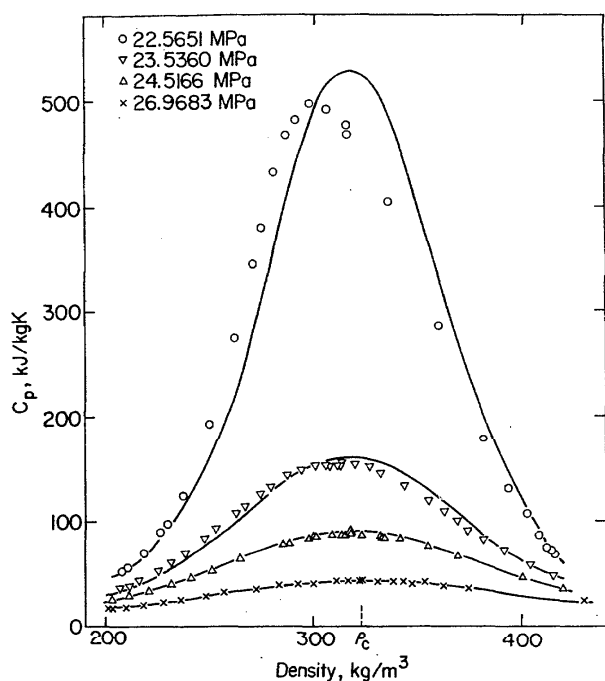


FIG. 14. The data of Sirota and Maltsev (Ref. 26) for the specific heat C_p along isobars, and as a function of density, are compared with the curves generated by our surface. The peak heights are well predicted but there is a small shift in density between the experimental and predicted values.

10. Specific Heat C_p

A comparison between the values calculated for the specific heat C_p and the experimental data of Sirota and Maltsev²⁶ is presented in Fig. 14. The data were taken as enthalpy increments in given finite temperature intervals

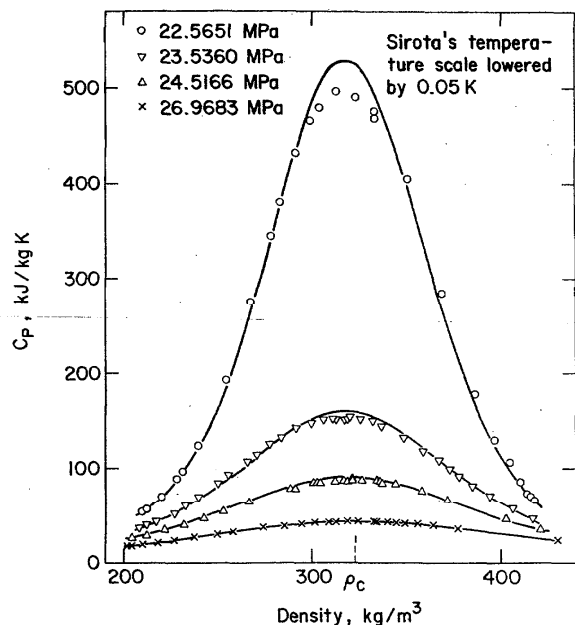


FIG. 15. A lowering of the experimental temperatures by 0.05 K eliminates the offset between C_p experiment and prediction observed in Fig. 14.

and the points shown in the plot represent values of $\Delta H / \Delta T$. Our predicted values are, likewise, values of $\Delta H / \Delta T$ over the experimental temperature intervals. Since the temperature intervals ΔT were small and smoothly varying, and the points closely spaced, smooth curves could be drawn through the predicted points. The equation reproduces the experimental maxima in C_p at all temperatures; the maximum difference in the peak values is about 5% to 6% at the 22.5651 MPa isobar.

This difference of peak heights could be further reduced by ascribing a lower value of T_c to the PVT data, as we did before¹⁹; cf. also Sec. 8. Values for T_c substantially lower than the one used here, however, although reconcilable with the PVT data, are less compatible with Osborne's latent heats. In Fig. 14 the comparison is made with the C_p data plotted as function of density, rather than temperature. The scaled equation was used to transform the experimental pressures to densities. The plot reveals a small offset in peak location between the experimental data and the predicted curve, as noted earlier.¹⁹ The effect can be eliminated by lowering Sirota's temperature values by 0.05 K, as demonstrated in Fig. 15. We conclude that the C_p data of Sirota and Maltsev and the PVT data of Rivkin *et al.* are consistent at an acceptable level.

11. Critical Amplitude Ratios

The scaling function parameter b^2 , although predicted to be universal, was actually determined by us from the fit. Universality of b^2 implies universality of the critical amplitude ratios [see Eqs. (A38)–(A41) in Appendix A]. The amplitude ratios we obtain in our fit are indeed in agreement with the values predicted theoretically, as shown in Table 5.

Table 5. Critical amplitude ratios

| | Theory [20] | Theory [20] | Our results |
|---------------------------|----------------|-----------------|-------------|
| A^+ / A^- | 0.51 | 0.55 | 0.532 |
| r^+ / r^- | 5.07 | 4.80 | 4.886 |
| $\Gamma^+ D B^{\delta-1}$ | 1.75 | 1.6 | 1.693 |
| $A^+ r^+ / B^2$ | 0.059 | 0.066 | 0.0568 |
| series | | t -expansion | |
| expansion | | renormalization | |
| 1sing | | group | |

12. Thermodynamic Tables

Tables of the thermodynamic properties pressure, enthalpy, entropy, energy, specific heats, and speed of sound have been prepared along closely spaced isochores, and as a function of temperature.

In addition, a table of saturation properties has been constructed. The tables are given in Appendix C.

13. Discussion

We have presented a description of the thermodynamic behavior of steam in the range 200–420 kg/m³, 643–693 K,

including the critical point. The fundamental equation is of the form predicted by the modern theory of critical phenomena, and includes a correction-to-scaling term and a device for introducing gas-liquid asymmetry. In total, 16 adjustable parameters were used.

The *PVT* data of Rivkin *et al.* were found to be consistent with the vapor pressure and latent-heat data of Osborne *et al.* to a high degree of accuracy.

The speed-of-sound data of Erokhin and Kalyanov and C_p data of Sirota and Maltsev are consistent with the *PVT* of Rivkin after small adjustments of the respective temperature scales, of the order of a few hundredths of a degree. The energy and C_v data of Baehr *et al.* are also consistent with the *PVT* data, but the tolerances of these data are somewhat larger than those of C_p and speed of sound.

The C_v data of Amirkhanov *et al.* which include values very near the critical point, are represented in fine detail by our surface. A large adjustment of the temperature scale, -0.31 K, however, was needed.

There exists an internationally recognized formulation for the thermodynamic surface of steam recommended for scientific and industrial use.³⁶ We do not present a comparison here with the predictions from this international formulation or other global formulations. The reason is that the International Association for the Properties of Steam is in the process of adopting a new formulation which will be more accurate and valid in a much larger range.^{35,37} In this paper the quality of our fundamental equation for the critical region has been judged solely on the basis of a comparison with the experimental data.

Acknowledgments

This work was supported in part by the Office of Standard Reference Data. Computer time for this project was provided by the Computer Science Center at the University of Maryland. We have profited from discussions with, and access to unpublished work of A. A. Aleksandrov, L. Haar, S. L. Rivkin, A. M. Sirota, J. Straub, and K. Scheffler.

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Appendix A. Revised and Extended Scaling Equations for the Thermodynamic Properties of Fluids

A.1. Reduced thermodynamic quantities

$$\begin{aligned} \tilde{T} &= -\frac{T_c}{T}, & \tilde{\mu} &= \frac{\mu}{T} \cdot \frac{\rho_c T_c}{P_c}, & \tilde{P} &= \frac{P}{T} \cdot \frac{T_c}{P_c}, \\ \tilde{\rho} &= \frac{\rho}{\rho_c}, & \tilde{U} &= \frac{U}{V} \cdot \frac{1}{P_c}, & \tilde{S} &= \frac{S}{V} \cdot \frac{T_c}{P_c}, \end{aligned} \quad (\text{A1})$$

$$\tilde{A} = \frac{A}{VT} \cdot \frac{T_c}{P_c}, \quad \tilde{H} = \frac{H}{VT} \cdot \frac{T_c}{P_c}, \quad \tilde{\chi}_T = \left(\frac{\partial \tilde{p}}{\partial \tilde{\mu}} \right)_T,$$

$$\tilde{C}_v = \frac{C_v}{V} \cdot \frac{T_c}{P_c}, \quad \tilde{C}_p = \frac{C_p}{V} \cdot \frac{T_c}{P_c}.$$

(T is temperature, μ is chemical potential, P is pressure, ρ is density, U is energy, S is entropy, A is helmholtz free energy, H is enthalpy, V is volume, C_v is heat capacity at constant V , C_p is heat capacity at constant P).

A 2. Thermodynamic relations

$$\begin{aligned} d\tilde{P} &= \tilde{U} d\tilde{T} + \tilde{\rho} d\tilde{\mu}, \\ d\tilde{A} &= -\tilde{U} d\tilde{T} + \tilde{\mu} d\tilde{\rho}, \\ d\tilde{H} &= -\tilde{T} d\tilde{U} + \tilde{\rho} d\tilde{\mu}, \\ d\tilde{S} &= -\tilde{T} d\tilde{U} - \tilde{\mu} d\tilde{\rho}, \end{aligned} \quad (\text{A2})$$

with

$$\begin{aligned} \tilde{A} &= \tilde{\rho}\tilde{\mu} - \tilde{P}, \\ \tilde{H} &= \tilde{P} - \tilde{T}\tilde{U}, \\ \tilde{S} &= \tilde{H} - \tilde{\rho}\tilde{\mu} = -\tilde{T}\tilde{U} - \tilde{A}. \end{aligned} \quad (\text{A3})$$

A 3. Fundamental equations

$$\Delta\tilde{T} = \tilde{T} + 1, \quad (\text{A4a})$$

$$\Delta\tilde{\mu} = \tilde{\mu} - \tilde{\mu}_0(\tilde{T}), \quad (\text{A4b})$$

$$\tilde{P} = \tilde{P}_0(\tilde{T}) + \Delta\tilde{\mu} + \tilde{P}_{11}\Delta\tilde{\mu}\Delta\tilde{T} + \Delta\tilde{P}, \quad (\text{A5})$$

with

$$\tilde{\mu}_0(\tilde{T}) = \tilde{\mu}_c + \sum_{j=1}^3 \tilde{\mu}_j (\Delta\tilde{T})^j, \quad (\text{A6a})$$

$$\tilde{P}_0(\tilde{T}) = 1 + \sum_{j=1}^3 \tilde{P}_j (\Delta\tilde{T})^j. \quad (\text{A6b})$$

A 4. Derived thermodynamic quantities

$$\tilde{\rho} = 1 + \tilde{P}_{11}\Delta\tilde{T} + \left(\frac{\partial\Delta\tilde{P}}{\partial\Delta\tilde{\mu}} \right)_{\Delta\tilde{T}}, \quad (\text{A7})$$

$$\tilde{U} = \frac{d\tilde{P}_0}{d\tilde{T}} - \tilde{\rho} \frac{d\tilde{\mu}_0}{d\tilde{T}} + \tilde{P}_{11}\Delta\tilde{\mu} + \left(\frac{\partial\Delta\tilde{P}}{\partial\Delta\tilde{T}} \right)_{\Delta\tilde{\mu}}, \quad (\text{A8})$$

$$\tilde{\chi}_T = \left(\frac{\partial^2\Delta\tilde{P}}{\partial\Delta\tilde{\mu}^2} \right)_{\Delta\tilde{T}}, \quad (\text{A9})$$

$$\begin{aligned} \left(\frac{\partial\tilde{P}}{\partial\tilde{T}} \right)_{\tilde{\rho}} &= \frac{d\tilde{P}_0}{d\tilde{T}} + \tilde{P}_{11} \left[\Delta\tilde{\mu} - \frac{\tilde{\rho}}{\tilde{\chi}_T} \right] \\ &+ \left(\frac{\partial\Delta\tilde{P}}{\partial\Delta\tilde{T}} \right)_{\Delta\tilde{\mu}} - \frac{\tilde{\rho}}{\tilde{\chi}_T} \frac{\partial^2\Delta\tilde{P}}{\partial\Delta\tilde{\mu}\partial\Delta\tilde{T}}, \end{aligned} \quad (\text{A10})$$

$$\begin{aligned} \frac{\tilde{C}_v}{\tilde{T}^2} &= \frac{d^2\tilde{P}_0}{d\tilde{T}^2} - \tilde{\rho} \frac{d^2\tilde{\mu}_0}{d\tilde{T}^2} - \frac{\tilde{P}_{11}^2}{\tilde{\chi}_T} \\ &+ \left(\frac{\partial^2\Delta\tilde{P}}{\partial\Delta\tilde{T}^2} \right)_{\Delta\tilde{\mu}} - \frac{2\tilde{P}_{11}}{\tilde{\chi}_T} \frac{\partial^2\Delta\tilde{P}}{\partial\Delta\tilde{\mu}\partial\Delta\tilde{T}} \\ &- \frac{1}{\tilde{\chi}_T} \left(\frac{\partial^2\Delta\tilde{P}}{\partial\Delta\tilde{\mu}\partial\Delta\tilde{T}} \right)^2, \end{aligned} \quad (\text{A11})$$

$$\tilde{C}_p = \tilde{C}_v + \frac{\tilde{\chi}_T}{\tilde{\rho}^2} \left[\tilde{P} - \tilde{T} \left(\frac{\partial\tilde{P}}{\partial\tilde{T}} \right)_{\tilde{\rho}} \right]^2. \quad (\text{A12})$$

A 5. Critical exponents

$$\alpha_0 = \alpha, \quad \alpha_1 = \alpha - \Delta_1, \quad (\text{A13})$$

$$\beta_0 = \beta, \quad \beta_1 = \beta + \Delta_1, \quad (\text{A13})$$

$$\gamma_0 = \gamma, \quad \gamma_1 = \gamma - \Delta_1,$$

with

$$2 - \alpha = \beta(\delta + 1), \quad \gamma = \beta(\delta - 1). \quad (\text{A14})$$

A 6. Parametric equations for singular terms

$$\Delta\tilde{\mu} = r^{\beta\delta} a \theta (1 - \theta^2), \quad (\text{A15})$$

$$\Delta\tilde{T} = r(1 - b^2\theta^2) - c\Delta\tilde{\mu}, \quad (\text{A16})$$

$$\Delta\tilde{P} = \sum_{i=0}^1 r^{2-\alpha_i} a k_i p_i(\theta), \quad (\text{A17})$$

$$\left(\frac{\partial\Delta\tilde{P}}{\partial\Delta\tilde{\mu}} \right)_{\Delta\tilde{T}} = \sum_{i=0}^1 [r^{\beta_i} k_i \theta + c r^{1-\alpha_i} a k_i s_i(\theta)], \quad (\text{A18})$$

$$\left(\frac{\partial\Delta\tilde{P}}{\partial\Delta\tilde{T}} \right)_{\Delta\tilde{\mu}} = \sum_{i=0}^1 r^{1-\alpha_i} a k_i s_i(\theta), \quad (\text{A19})$$

$$\begin{aligned} \left(\frac{\partial^2\Delta\tilde{P}}{\partial\Delta\tilde{\mu}^2} \right)_{\Delta\tilde{T}} &= \sum_{i=0}^1 \left[r^{-\gamma_i} \frac{k_i}{a} u_i(\theta) + 2c r^{\beta_i-1} k_i v_i(\theta) \right. \\ &\left. + c^2 r^{-\alpha_i} a k_i w_i(\theta) \right], \end{aligned} \quad (\text{A20})$$

$$\frac{\partial^2\Delta\tilde{P}}{\partial\Delta\tilde{\mu}\partial\Delta\tilde{T}} = \sum_{i=0}^1 [r^{\beta_i-1} k_i v_i(\theta) + c r^{-\alpha_i} a k_i w_i(\theta)], \quad (\text{A21})$$

$$\left(\frac{\partial^2\Delta\tilde{P}}{\partial\Delta\tilde{T}^2} \right)_{\Delta\tilde{\mu}} = \sum_{i=0}^1 r^{-\alpha_i} a k_i w_i(\theta). \quad (\text{A22})$$

A 7. Auxiliary functions

$$p_i(\theta) = p_{0i} + p_{2i}\theta^2 + p_{4i}\theta^4, \quad (\text{A23})$$

$$s_i(\theta) = s_{0i} + s_{2i}\theta^2, \quad s'_i(\theta) = 2s_{2i}\theta, \quad (\text{A24})$$

$$q(\theta) = 1 + \{b^2(2\beta\delta - 1) - 3\}\theta^2 - b^2(2\beta\delta - 3)\theta^4, \quad (\text{A25})$$

$$u_i(\theta) = [1 - b^2(1 - 2\beta_i)\theta^2]/q(\theta), \quad (\text{A26})$$

$$v_i(\theta) = [\beta_i(1 - 3\theta^2)\theta - \beta\delta(1 - \theta^2)\theta]/q(\theta), \quad (\text{A27})$$

$$\begin{aligned} w_i(\theta) &= [(1 - \alpha_i)(1 - 3\theta^2)s_i(\theta) \\ &- \beta\delta(1 - \theta^2)\theta s'_i(\theta)]/q(\theta), \end{aligned} \quad (\text{A28})$$

with

$$p_{0i} = + \frac{\beta\delta - 3\beta_i - b^2\alpha_i\gamma_i}{2b^4(2 - \alpha_i)(1 - \alpha_i)\alpha_i},$$

$$p_{2i} = - \frac{\beta\delta - 3\beta_i - b^2\alpha_i(2\beta\delta - 1)}{2b^2(1 - \alpha_i)\alpha_i}, \quad (\text{A29})$$

$$p_{4i} = + \frac{2\beta\delta - 3}{2\alpha_i},$$

$$s_{0i} = (2 - \alpha_i)p_{0i},$$

$$s_{2i} = - \frac{\beta\delta - 3\beta_i}{2b^2\alpha_i}. \quad (\text{A30})$$

A 8. Two-phase properties

Variables:

$$\theta = \pm 1,$$

$$\Delta\tilde{\mu} = 0,$$

$$\Delta\tilde{T} = r(1 - b^2). \quad (\text{A31})$$

Vapor pressure:

$$\tilde{P}_{\text{vap}} = \tilde{P}_0(\tilde{T}) + \sum_{i=0}^1 r^{2-\alpha_i} a k_i p_i(1), \quad (\text{A32})$$

Coeexisting densities:

$$\frac{\tilde{\rho}_L + \tilde{\rho}_V}{2} = 1 + \tilde{P}_{11} \Delta \tilde{T} + \sum_{i=0}^1 cr^{1-\alpha_i} ak_{i,s_i}(1),$$

$$\frac{\tilde{\rho}_L - \tilde{\rho}_V}{2} = \sum_{i=0}^1 r^{\beta_i} k_i. \quad (\text{A33})$$

Helmholtz free energy:

$$\tilde{A} = \tilde{\rho} \tilde{\mu}_0(\tilde{T}) - \tilde{P}_0(\tilde{T}) - \sum_{i=0}^1 r^{2-\alpha_i} ak_{i,p_i}(1). \quad (\text{A34})$$

Energy:

$$\tilde{U} = \frac{d\tilde{P}_0}{d\tilde{T}} - \tilde{\rho} \frac{d\tilde{\mu}_0(\tilde{T})}{d\tilde{T}} + \frac{1}{1-b^2}$$

$$\times \sum_{i=0}^1 (2-\alpha_i) r^{1-\alpha_i} ak_{i,p_i}(1). \quad (\text{A35})$$

Entropy:

$$\tilde{S} = -\tilde{\rho} \tilde{\mu}_0(\tilde{T}) + \tilde{P}_0(\tilde{T}) - \tilde{T} \left[\frac{d\tilde{P}_0}{d\tilde{T}} - \tilde{\rho} \frac{d\tilde{\mu}_0}{d\tilde{T}} \right]$$

$$+ \sum_{i=0}^1 r^{2-\alpha_i} ak_{i,p_i}(1)$$

$$- \frac{\tilde{T}}{1-b^2} \sum_{i=0}^1 (2-\alpha_i) r^{1-\alpha_i} ak_{i,p_i}(1). \quad (\text{A36})$$

Specific heat C_v :

$$\frac{\tilde{C}_v}{\tilde{T}^2} = \frac{d^2\tilde{P}_0}{d\tilde{T}^2} - \tilde{\rho} \frac{d^2\tilde{\mu}_0}{d\tilde{T}^2}$$

$$+ \left(\frac{1}{1-b^2} \right)^2 \sum_{i=0}^1 (2-\alpha_i)(1-\alpha_i) r^{-\alpha_i} ak_{i,p_i}(1). \quad (\text{A37})$$

A 9. Critical amplitude ratios

$$\frac{A^+}{A^-} = \frac{(b^2-1)^{2-\alpha} p_{00}}{p_{00} + p_{20} + p_{40}}, \quad (\text{A38})$$

$$\frac{\Gamma^+}{\Gamma^-} = \frac{2}{(b^2-1)^{\gamma-1} \{1-b^2(1-2\beta)\}}, \quad (\text{A39})$$

$$\Gamma^+ DB^{\delta-1} = \frac{b^{\delta-3}}{(b^2-1)^{\gamma-1}}, \quad (\text{A40})$$

$$\frac{A^+ \Gamma^+}{B^2} = (2-\alpha)(1-\alpha)\alpha(b^2-1)^{2\beta} p_{00}. \quad (\text{A41})$$

Appendix B. Parameter Values for the Thermodynamic Surface of Steam in the Critical Region

TABLE B1. Parameter values^a

| | |
|----------------------------------|---|
| Critical exponents: | $\beta = 0.325^b$ $\delta = 4.82^b$ $\Delta_1 = 0.50^b$ |
| Critical parameters: | $T_c = 647.067 \text{ K}^c$ $\rho_c = 322.778 \text{ kg/m}^3^d$ $P_c = 22.0460 \text{ MPa}^c$ |
| Parameters in scaling functions: | $a = +23.667^d$ $k_0 = +1.4403^d$ $k_1 = +0.2942^d$ $c = -0.01776^d$ $b^2 = +1.3757^d$ |
| Pressure background parameters: | $\tilde{P}_1 = +6.8445^d$ $\tilde{P}_2 = -25.4915^d$ $\tilde{P}_3 = +5.238^d$ $\tilde{P}_{11} = +0.4918^f$ |
| Caloric background parameters: | $\tilde{\mu}_c = -11.233^g$ $\tilde{\mu}_1 = -22.655^g$ $\tilde{\mu}_2 = -17.888^h$ $\tilde{\mu}_3 = -4.933^h$ |

^a The number of decimals given exceeds the number of significant decimals so as to retain precision in complex calculations.

^b Fixed from theory.

^c From latent heat data of Osborne *et al.*

^d From fit to *PVT* data of Rivkin *et al.*

^e Derived from vapor pressure curve.

^f From known coexistence curve diameter.

^g From identification of our surface with that of Haar *et al.* at $T = 648.15 \text{ K}$ and $\rho = 230 \text{ kg/m}^3$.

^h From fit to speed of sound data of Erokhin and Kalyanov.

Appendix C. Tables of Thermodynamic Properties of Steam in the Critical Region

The uncertainty of the tabulated values is generally a few units in the last decimal given. However, in special cases, such as for the densities near ρ_c and T_c and the specific heats in the region where they vary rapidly, the uncertainty will be much larger.

Table C1. Thermodynamic properties along isochores at regular temperature increments.

| Temp. | Pressure | Density | Internal Energy | Enthalpy | Entropy | C_p | C_v | Velocity of Sound | Phase Region |
|-------|----------|-------------------|-----------------|----------|---------|---------|-------|-------------------|--------------|
| K | MPa | kg/m ³ | kJ/kg | kJ/kg | kJ/kg.K | kJ/kg.K | | m/s | |
| 643.0 | 20.995 | 200.0 | 2234.5 | 2339.5 | 4.8090 | | 14.46 | | 2 |
| 644.0 | 21.184 | 200.0 | 2239.3 | 2345.2 | 4.8165 | 81.4 | 4.50 | 364.9 | 1 |
| 645.0 | 21.371 | 200.0 | 2243.8 | 2350.6 | 4.8234 | 71.0 | 4.39 | 368.5 | 1 |
| 646.0 | 21.557 | 200.0 | 2248.1 | 2355.9 | 4.8301 | 63.1 | 4.29 | 371.8 | 1 |
| 647.0 | 21.741 | 200.0 | 2252.4 | 2361.1 | 4.8367 | 57.0 | 4.21 | 374.8 | 1 |
| 648.0 | 21.925 | 200.0 | 2256.5 | 2366.2 | 4.8431 | 52.1 | 4.14 | 377.7 | 1 |
| 650.0 | 22.290 | 200.0 | 2264.7 | 2376.1 | 4.8557 | 44.6 | 4.02 | 383.0 | 1 |
| 655.0 | 23.191 | 200.0 | 2284.2 | 2400.2 | 4.8856 | 33.2 | 3.80 | 394.9 | 1 |
| 660.0 | 24.081 | 200.0 | 2302.8 | 2423.2 | 4.9139 | 26.7 | 3.64 | 405.4 | 1 |
| 665.0 | 24.962 | 200.0 | 2320.7 | 2445.5 | 4.9409 | 22.6 | 3.52 | 415.0 | 1 |
| 670.0 | 25.836 | 200.0 | 2338.1 | 2467.2 | 4.9669 | 19.6 | 3.43 | 424.0 | 1 |
| 675.0 | 26.705 | 200.0 | 2355.0 | 2488.5 | 4.9921 | 17.4 | 3.35 | 432.6 | 1 |
| 680.0 | 27.568 | 200.0 | 2371.5 | 2509.4 | 5.0165 | 15.8 | 3.28 | 440.8 | 1 |
| 685.0 | 28.427 | 200.0 | 2387.8 | 2529.9 | 5.0403 | 14.4 | 3.22 | 448.7 | 1 |
| 690.0 | 29.283 | 200.0 | 2403.7 | 2550.1 | 5.0635 | 13.3 | 3.17 | 456.4 | 1 |
| 695.0 | 30.135 | 200.0 | 2419.4 | 2570.1 | 5.0862 | 12.4 | 3.12 | 463.9 | 1 |
| 643.0 | 20.995 | 220.0 | 2170.7 | 2266.1 | 4.6948 | | 13.49 | | 2 |
| 644.0 | 21.247 | 220.0 | 2184.4 | 2280.9 | 4.7161 | | 13.95 | | 2 |
| 645.0 | 21.490 | 220.0 | 2196.0 | 2293.7 | 4.7342 | 155.6 | 4.88 | 346.9 | 1 |
| 646.0 | 21.694 | 220.0 | 2200.8 | 2299.4 | 4.7416 | 121.7 | 4.69 | 352.3 | 1 |
| 647.0 | 21.899 | 220.0 | 2205.4 | 2305.0 | 4.7488 | 100.9 | 4.54 | 356.7 | 1 |
| 648.0 | 22.102 | 220.0 | 2209.9 | 2310.3 | 4.7557 | 86.6 | 4.42 | 360.7 | 1 |
| 650.0 | 22.504 | 220.0 | 2218.5 | 2320.8 | 4.7690 | 67.9 | 4.24 | 367.6 | 1 |
| 655.0 | 23.495 | 220.0 | 2238.9 | 2345.7 | 4.8003 | 44.9 | 3.94 | 381.9 | 1 |
| 660.0 | 24.474 | 220.0 | 2258.1 | 2369.4 | 4.8295 | 33.9 | 3.75 | 394.0 | 1 |
| 665.0 | 25.444 | 220.0 | 2276.5 | 2392.1 | 4.8572 | 27.4 | 3.61 | 404.9 | 1 |
| 670.0 | 26.408 | 220.0 | 2294.2 | 2414.3 | 4.8838 | 23.2 | 3.49 | 414.9 | 1 |
| 675.0 | 27.366 | 220.0 | 2311.5 | 2435.9 | 4.9094 | 20.2 | 3.40 | 424.3 | 1 |
| 680.0 | 28.319 | 220.0 | 2328.3 | 2457.0 | 4.9342 | 17.9 | 3.33 | 433.3 | 1 |
| 685.0 | 29.269 | 220.0 | 2344.8 | 2477.8 | 4.9584 | 16.2 | 3.26 | 441.9 | 1 |
| 690.0 | 30.215 | 220.0 | 2360.9 | 2498.3 | 4.9819 | 14.8 | 3.21 | 450.2 | 1 |
| 695.0 | 31.158 | 220.0 | 2376.8 | 2518.5 | 5.0048 | 13.7 | 3.16 | 458.3 | 1 |
| 643.0 | 20.995 | 240.0 | 2117.4 | 2204.9 | 4.5997 | | 12.69 | | 2 |
| 644.0 | 21.247 | 240.0 | 2130.3 | 2218.8 | 4.6197 | | 13.10 | | 2 |
| 645.0 | 21.504 | 240.0 | 2143.7 | 2233.3 | 4.6405 | | 13.73 | | 2 |
| 646.0 | 21.759 | 240.0 | 2156.7 | 2247.3 | 4.6606 | 319.4 | 5.28 | 328.9 | 1 |
| 647.0 | 21.981 | 240.0 | 2161.8 | 2253.4 | 4.6685 | 208.9 | 4.95 | 332.2 | 1 |
| 648.0 | 22.201 | 240.0 | 2166.6 | 2259.1 | 4.6759 | 157.7 | 4.74 | 343.3 | 1 |
| 650.0 | 22.638 | 240.0 | 2175.8 | 2270.1 | 4.6901 | 107.1 | 4.46 | 352.8 | 1 |
| 655.0 | 23.714 | 240.0 | 2197.0 | 2295.8 | 4.7226 | 60.3 | 4.06 | 370.3 | 1 |
| 660.0 | 24.778 | 240.0 | 2216.7 | 2319.9 | 4.7525 | 42.3 | 3.83 | 384.2 | 1 |
| 665.0 | 25.833 | 240.0 | 2235.4 | 2343.0 | 4.7808 | 32.8 | 3.67 | 396.4 | 1 |
| 670.0 | 26.884 | 240.0 | 2253.4 | 2365.4 | 4.8078 | 26.9 | 3.54 | 407.5 | 1 |
| 675.0 | 27.930 | 240.0 | 2270.9 | 2387.2 | 4.8337 | 22.9 | 3.44 | 417.8 | 1 |
| 680.0 | 28.972 | 240.0 | 2287.9 | 2408.6 | 4.8589 | 20.1 | 3.36 | 427.5 | 1 |
| 685.0 | 30.012 | 240.0 | 2304.5 | 2429.6 | 4.8832 | 17.9 | 3.29 | 436.8 | 1 |
| 690.0 | 31.049 | 240.0 | 2320.8 | 2450.2 | 4.9069 | 16.2 | 3.23 | 445.8 | 1 |
| 695.0 | 32.083 | 240.0 | 2336.9 | 2470.5 | 4.9301 | 14.8 | 3.18 | 454.4 | 1 |
| 643.0 | 20.995 | 260.0 | 2072.4 | 2153.1 | 4.5192 | | 12.00 | | 2 |
| 644.0 | 21.247 | 260.0 | 2084.6 | 2166.3 | 4.5381 | | 12.39 | | 2 |
| 645.0 | 21.504 | 260.0 | 2097.2 | 2179.9 | 4.5577 | | 12.96 | | 2 |
| 646.0 | 21.764 | 260.0 | 2110.7 | 2194.4 | 4.5786 | | 14.02 | | 2 |
| 647.0 | 22.016 | 260.0 | 2121.3 | 2206.0 | 4.5950 | 554.6 | 5.52 | 314.4 | 1 |
| 648.0 | 22.252 | 260.0 | 2126.5 | 2212.1 | 4.6031 | 312.6 | 5.08 | 325.3 | 1 |
| 650.0 | 22.719 | 260.0 | 2136.2 | 2223.6 | 4.6181 | 169.1 | 4.65 | 338.8 | 1 |
| 655.0 | 23.873 | 260.0 | 2158.1 | 2249.9 | 4.6515 | 78.5 | 4.15 | 360.3 | 1 |
| 660.0 | 25.017 | 260.0 | 2178.1 | 2274.4 | 4.6820 | 51.1 | 3.89 | 376.2 | 1 |
| 665.0 | 26.156 | 260.0 | 2197.1 | 2297.7 | 4.7107 | 38.0 | 3.71 | 389.8 | 1 |
| 670.0 | 27.291 | 260.0 | 2215.3 | 2320.3 | 4.7379 | 30.4 | 3.57 | 401.9 | 1 |
| 675.0 | 28.423 | 260.0 | 2232.9 | 2342.2 | 4.7641 | 25.4 | 3.47 | 413.1 | 1 |
| 680.0 | 29.553 | 260.0 | 2250.0 | 2363.7 | 4.7894 | 21.9 | 3.38 | 423.6 | 1 |
| 685.0 | 30.682 | 260.0 | 2266.7 | 2384.7 | 4.8139 | 19.4 | 3.31 | 433.6 | 1 |
| 690.0 | 31.810 | 260.0 | 2283.1 | 2405.5 | 4.8377 | 17.4 | 3.25 | 443.1 | 1 |
| 695.0 | 32.936 | 260.0 | 2299.2 | 2425.9 | 4.8610 | 15.8 | 3.19 | 452.3 | 1 |

Table C1. Thermodynamic properties along isochores at regular temperature increments (continued).

| Temp. | Pressure | Density | Internal Energy | Enthalpy | Entropy | C _p | C _v | Velocity of Sound | Phase Region |
|-------|----------|-------------------|-----------------|----------|---------|----------------|----------------|-------------------|--------------|
| K | MPa | kg/m ³ | kJ/kg | kJ/kg | kJ/kg.K | kJ/kg.K | | m/s | |
| 643.0 | 20.995 | 280.0 | 2033.8 | 2108.8 | 4.4502 | | 11.42 | | 2 |
| 644.0 | 21.247 | 280.0 | 2045.4 | 2121.3 | 4.4682 | | 11.77 | | 2 |
| 645.0 | 21.504 | 280.0 | 2057.4 | 2134.2 | 4.4868 | | 12.31 | | 2 |
| 646.0 | 21.764 | 280.0 | 2070.1 | 2147.9 | 4.5066 | | 13.29 | | 2 |
| 647.0 | 22.027 | 280.0 | 2083.8 | 2162.5 | 4.5278 | 2431.8 | 6.46 | 284.7 | 1 |
| 648.0 | 22.276 | 280.0 | 2089.7 | 2169.2 | 4.5368 | 635.3 | 5.42 | 307.6 | 1 |
| 650.0 | 22.770 | 280.0 | 2099.8 | 2181.1 | 4.5524 | 251.7 | 4.80 | 326.4 | 1 |
| 655.0 | 23.995 | 280.0 | 2122.0 | 2207.7 | 4.5865 | 96.1 | 4.20 | 352.2 | 1 |
| 660.0 | 25.215 | 280.0 | 2142.3 | 2232.3 | 4.6172 | 58.6 | 3.91 | 370.2 | 1 |
| 665.0 | 26.433 | 280.0 | 2161.3 | 2255.7 | 4.6460 | 42.1 | 3.72 | 385.2 | 1 |
| 670.0 | 27.651 | 280.0 | 2179.6 | 2278.3 | 4.6734 | 33.0 | 3.58 | 398.4 | 1 |
| 675.0 | 28.869 | 280.0 | 2197.2 | 2300.3 | 4.6996 | 27.2 | 3.48 | 410.5 | 1 |
| 680.0 | 30.088 | 280.0 | 2214.4 | 2321.8 | 4.7249 | 23.3 | 3.39 | 421.8 | 1 |
| 685.0 | 31.306 | 280.0 | 2231.1 | 2342.9 | 4.7495 | 20.4 | 3.31 | 432.4 | 1 |
| 690.0 | 32.525 | 280.0 | 2247.5 | 2363.7 | 4.7733 | 18.2 | 3.25 | 442.6 | 1 |
| 695.0 | 33.744 | 280.0 | 2263.7 | 2384.2 | 4.7966 | 16.5 | 3.19 | 452.3 | 1 |
| 643.0 | 20.995 | 300.0 | 2000.3 | 2070.3 | 4.3904 | | 10.91 | | 2 |
| 644.0 | 21.247 | 300.0 | 2011.4 | 2082.2 | 4.4076 | | 11.24 | | 2 |
| 645.0 | 21.504 | 300.0 | 2022.9 | 2094.5 | 4.4254 | | 11.74 | | 2 |
| 646.0 | 21.764 | 300.0 | 2035.0 | 2107.6 | 4.4442 | | 12.66 | | 2 |
| 647.0 | 22.028 | 300.0 | 2049.0 | 2122.4 | 4.4658 | | 17.55 | | 2 |
| 648.0 | 22.288 | 300.0 | 2055.9 | 2130.1 | 4.4764 | 1126.5 | 5.66 | 292.6 | 1 |
| 650.0 | 22.804 | 300.0 | 2066.2 | 2142.2 | 4.4924 | 326.8 | 4.86 | 316.9 | 1 |
| 655.0 | 24.095 | 300.0 | 2088.6 | 2168.9 | 4.5267 | 107.4 | 4.21 | 346.8 | 1 |
| 660.0 | 25.389 | 300.0 | 2108.8 | 2193.4 | 4.5574 | 62.7 | 3.91 | 366.7 | 1 |
| 665.0 | 26.686 | 300.0 | 2127.8 | 2216.8 | 4.5861 | 44.2 | 3.71 | 383.0 | 1 |
| 670.0 | 27.987 | 300.0 | 2146.0 | 2239.3 | 4.6134 | 34.2 | 3.58 | 397.2 | 1 |
| 675.0 | 29.291 | 300.0 | 2163.6 | 2261.3 | 4.6396 | 28.0 | 3.47 | 410.2 | 1 |
| 680.0 | 30.598 | 300.0 | 2180.7 | 2282.7 | 4.6648 | 23.8 | 3.38 | 422.2 | 1 |
| 685.0 | 31.907 | 300.0 | 2197.5 | 2303.8 | 4.6893 | 20.8 | 3.31 | 433.5 | 1 |
| 690.0 | 33.218 | 300.0 | 2213.8 | 2324.6 | 4.7131 | 18.5 | 3.24 | 444.2 | 1 |
| 695.0 | 34.531 | 300.0 | 2229.9 | 2345.0 | 4.7364 | 16.7 | 3.19 | 454.5 | 1 |
| 643.0 | 20.995 | 320.0 | 1971.1 | 2036.7 | 4.3380 | | 10.47 | | 2 |
| 644.0 | 21.247 | 320.0 | 1981.7 | 2048.1 | 4.3545 | | 10.78 | | 2 |
| 645.0 | 21.504 | 320.0 | 1992.7 | 2059.9 | 4.3716 | | 11.24 | | 2 |
| 646.0 | 21.764 | 320.0 | 2004.3 | 2072.3 | 4.3896 | | 12.10 | | 2 |
| 647.0 | 22.028 | 320.0 | 2017.6 | 2086.4 | 4.4102 | | 16.69 | | 2 |
| 648.0 | 22.295 | 320.0 | 2025.0 | 2094.7 | 4.4216 | 1380.9 | 5.66 | 283.5 | 1 |
| 650.0 | 22.832 | 320.0 | 2035.3 | 2106.6 | 4.4375 | 345.1 | 4.82 | 311.4 | 1 |
| 655.0 | 24.187 | 320.0 | 2057.4 | 2133.0 | 4.4714 | 107.5 | 4.16 | 344.4 | 1 |
| 660.0 | 25.555 | 320.0 | 2077.4 | 2157.3 | 4.5019 | 62.1 | 3.87 | 366.0 | 1 |
| 665.0 | 26.932 | 320.0 | 2096.3 | 2180.5 | 4.5303 | 43.7 | 3.68 | 383.5 | 1 |
| 670.0 | 28.318 | 320.0 | 2114.4 | 2202.9 | 4.5574 | 33.8 | 3.55 | 398.7 | 1 |
| 675.0 | 29.709 | 320.0 | 2131.8 | 2224.7 | 4.5834 | 27.7 | 3.45 | 412.4 | 1 |
| 680.0 | 31.107 | 320.0 | 2148.8 | 2246.1 | 4.6085 | 23.5 | 3.36 | 425.1 | 1 |
| 685.0 | 32.509 | 320.0 | 2165.5 | 2267.1 | 4.6328 | 20.6 | 3.29 | 437.0 | 1 |
| 690.0 | 33.915 | 320.0 | 2181.8 | 2287.7 | 4.6565 | 18.3 | 3.23 | 448.3 | 1 |
| 695.0 | 35.325 | 320.0 | 2197.8 | 2308.2 | 4.6796 | 16.6 | 3.17 | 459.0 | 1 |
| 643.0 | 20.995 | 340.0 | 1945.2 | 2007.0 | 4.2919 | | 10.07 | | 2 |
| 644.0 | 21.247 | 340.0 | 1955.4 | 2017.9 | 4.3077 | | 10.37 | | 2 |
| 645.0 | 21.504 | 340.0 | 1966.0 | 2029.2 | 4.3241 | | 10.81 | | 2 |
| 646.0 | 21.764 | 340.0 | 1977.2 | 2041.2 | 4.3414 | | 11.61 | | 2 |
| 647.0 | 22.028 | 340.0 | 1989.9 | 2054.7 | 4.3612 | | 15.93 | | 2 |
| 648.0 | 22.302 | 340.0 | 1996.7 | 2062.3 | 4.3716 | 1026.2 | 5.42 | 282.2 | 1 |
| 650.0 | 22.861 | 340.0 | 2006.6 | 2073.9 | 4.3869 | 289.0 | 4.67 | 310.8 | 1 |
| 655.0 | 24.283 | 340.0 | 2028.2 | 2099.7 | 4.4200 | 96.1 | 4.08 | 345.7 | 1 |
| 660.0 | 25.727 | 340.0 | 2047.9 | 2123.6 | 4.4499 | 57.0 | 3.81 | 368.6 | 1 |
| 665.0 | 27.189 | 340.0 | 2066.5 | 2146.4 | 4.4780 | 40.6 | 3.63 | 387.1 | 1 |
| 670.0 | 28.662 | 340.0 | 2084.3 | 2168.6 | 4.5047 | 31.8 | 3.51 | 403.1 | 1 |
| 675.0 | 30.146 | 340.0 | 2101.6 | 2190.3 | 4.5304 | 26.2 | 3.41 | 417.5 | 1 |
| 680.0 | 31.638 | 340.0 | 2118.4 | 2211.5 | 4.5553 | 22.5 | 3.33 | 430.8 | 1 |
| 685.0 | 33.137 | 340.0 | 2134.9 | 2232.4 | 4.5794 | 19.7 | 3.26 | 443.3 | 1 |
| 690.0 | 34.643 | 340.0 | 2151.1 | 2253.0 | 4.6030 | 17.6 | 3.21 | 455.0 | 1 |
| 695.0 | 36.154 | 340.0 | 2167.0 | 2273.3 | 4.6259 | 16.0 | 3.15 | 466.2 | 1 |

THERMODYNAMIC PROPERTIES OF STEAM IN THE CRITICAL REGION

Table C1. Thermodynamic properties along isochores at regular temperature increments (continued).

| Temp. | Pressure | Density | Internal Energy | Enthalpy | Entropy | C _p | C _v | Velocity of Sound | Phase Region |
|-------|----------|-------------------|-----------------|----------|---------|----------------|----------------|-------------------|--------------|
| K | MPa | kg/m ³ | kJ/kg | kJ/kg | kJ/kg.K | kJ/kg.K | | m/s | |
| 643.0 | 20.995 | 360.0 | 1922.3 | 1980.6 | 4.2508 | | 9.73 | | 2 |
| 644.0 | 21.247 | 360.0 | 1932.1 | 1991.1 | 4.2661 | | 10.00 | | 2 |
| 645.0 | 21.504 | 360.0 | 1942.3 | 2002.0 | 4.2819 | | 10.42 | | 2 |
| 646.0 | 21.764 | 360.0 | 1953.1 | 2013.5 | 4.2986 | | 11.18 | | 2 |
| 647.0 | 22.029 | 360.0 | 1965.0 | 2026.2 | 4.3171 | 2889.7 | 6.16 | 253.2 | 1 |
| 648.0 | 22.314 | 360.0 | 1970.4 | 2032.4 | 4.3255 | 520.9 | 5.01 | 289.5 | 1 |
| 650.0 | 22.898 | 360.0 | 1979.8 | 2043.4 | 4.3399 | 199.5 | 4.46 | 316.1 | 1 |
| 655.0 | 24.395 | 360.0 | 2000.7 | 2068.4 | 4.3719 | 78.1 | 3.96 | 351.3 | 1 |
| 660.0 | 25.924 | 360.0 | 2019.8 | 2091.9 | 4.4010 | 48.9 | 3.73 | 375.0 | 1 |
| 665.0 | 27.475 | 360.0 | 2038.1 | 2114.4 | 4.4285 | 36.0 | 3.57 | 394.2 | 1 |
| 670.0 | 29.043 | 360.0 | 2055.6 | 2136.3 | 4.4548 | 28.7 | 3.46 | 410.8 | 1 |
| 675.0 | 30.625 | 360.0 | 2072.7 | 2157.7 | 4.4802 | 24.0 | 3.37 | 425.8 | 1 |
| 680.0 | 32.217 | 360.0 | 2089.3 | 2178.8 | 4.5048 | 20.8 | 3.29 | 439.6 | 1 |
| 685.0 | 33.820 | 360.0 | 2105.6 | 2199.6 | 4.5287 | 18.4 | 3.23 | 452.5 | 1 |
| 690.0 | 35.430 | 360.0 | 2121.7 | 2220.1 | 4.5520 | 16.6 | 3.18 | 464.7 | 1 |
| 695.0 | 37.047 | 360.0 | 2137.4 | 2240.3 | 4.5748 | 15.2 | 3.13 | 476.3 | 1 |
| 643.0 | 20.995 | 380.0 | 1901.7 | 1957.0 | 4.2141 | | 9.41 | | 2 |
| 644.0 | 21.247 | 380.0 | 1911.3 | 1967.2 | 4.2289 | | 9.68 | | 2 |
| 645.0 | 21.504 | 380.0 | 1921.1 | 1977.7 | 4.2442 | | 10.07 | | 2 |
| 646.0 | 21.764 | 380.0 | 1931.5 | 1988.8 | 4.2603 | | 10.79 | | 2 |
| 647.0 | 22.037 | 380.0 | 1940.9 | 1998.9 | 4.2749 | 455.4 | 4.97 | 284.6 | 1 |
| 648.0 | 22.339 | 380.0 | 1945.7 | 2004.5 | 4.2822 | 232.8 | 4.57 | 304.7 | 1 |
| 650.0 | 22.955 | 380.0 | 1954.4 | 2014.8 | 4.2957 | 123.6 | 4.21 | 327.5 | 1 |
| 655.0 | 24.540 | 380.0 | 1974.4 | 2039.0 | 4.3263 | 59.3 | 3.83 | 361.6 | 1 |
| 660.0 | 26.163 | 380.0 | 1993.0 | 2061.9 | 4.3546 | 40.0 | 3.63 | 385.5 | 1 |
| 665.0 | 27.814 | 380.0 | 2010.8 | 2084.0 | 4.3815 | 30.6 | 3.50 | 405.1 | 1 |
| 670.0 | 29.485 | 380.0 | 2028.0 | 2105.6 | 4.4073 | 25.1 | 3.40 | 422.2 | 1 |
| 675.0 | 31.173 | 380.0 | 2044.8 | 2126.9 | 4.4323 | 21.4 | 3.32 | 437.6 | 1 |
| 680.0 | 32.874 | 380.0 | 2061.3 | 2147.8 | 4.4565 | 18.8 | 3.25 | 451.7 | 1 |
| 685.0 | 34.586 | 380.0 | 2077.4 | 2168.4 | 4.4801 | 16.8 | 3.20 | 465.0 | 1 |
| 690.0 | 36.309 | 380.0 | 2093.2 | 2188.8 | 4.5032 | 15.3 | 3.15 | 477.4 | 1 |
| 695.0 | 38.040 | 380.0 | 2108.9 | 2209.0 | 4.5258 | 14.1 | 3.10 | 489.3 | 1 |
| 643.0 | 20.995 | 400.0 | 1883.2 | 1935.7 | 4.1810 | | 9.13 | | 2 |
| 644.0 | 21.247 | 400.0 | 1892.5 | 1945.6 | 4.1954 | | 9.38 | | 2 |
| 645.0 | 21.504 | 400.0 | 1902.0 | 1955.8 | 4.2102 | | 9.75 | | 2 |
| 646.0 | 21.764 | 400.0 | 1912.1 | 1966.5 | 4.2258 | | 10.44 | | 2 |
| 647.0 | 22.072 | 400.0 | 1917.6 | 1972.8 | 4.2343 | 150.3 | 4.35 | 313.1 | 1 |
| 648.0 | 22.395 | 400.0 | 1921.8 | 1977.8 | 4.2409 | 110.4 | 4.18 | 326.2 | 1 |
| 650.0 | 23.052 | 400.0 | 1930.0 | 1987.6 | 4.2534 | 74.8 | 3.97 | 345.1 | 1 |
| 655.0 | 24.741 | 400.0 | 1949.0 | 2010.9 | 4.2827 | 43.7 | 3.69 | 377.1 | 1 |
| 660.0 | 26.473 | 400.0 | 1967.1 | 2033.3 | 4.3101 | 31.9 | 3.53 | 400.6 | 1 |
| 665.0 | 28.235 | 400.0 | 1984.5 | 2055.1 | 4.3363 | 25.5 | 3.42 | 420.2 | 1 |
| 670.0 | 30.020 | 400.0 | 2001.4 | 2076.4 | 4.3616 | 21.5 | 3.34 | 437.5 | 1 |
| 675.0 | 31.824 | 400.0 | 2017.9 | 2097.4 | 4.3862 | 18.8 | 3.27 | 453.0 | 1 |
| 680.0 | 33.642 | 400.0 | 2034.1 | 2118.2 | 4.4101 | 16.7 | 3.21 | 467.4 | 1 |
| 685.0 | 35.474 | 400.0 | 2050.0 | 2138.7 | 4.4334 | 15.2 | 3.16 | 480.8 | 1 |
| 690.0 | 37.317 | 400.0 | 2065.7 | 2158.9 | 4.4562 | 14.0 | 3.11 | 493.5 | 1 |
| 695.0 | 39.169 | 400.0 | 2081.1 | 2179.0 | 4.4785 | 12.9 | 3.07 | 505.5 | 1 |
| 643.0 | 20.995 | 420.0 | 1866.5 | 1916.5 | 4.1511 | | 8.88 | | 2 |
| 644.0 | 21.247 | 420.0 | 1875.5 | 1926.1 | 4.1651 | | 9.12 | | 2 |
| 645.0 | 21.504 | 420.0 | 1884.8 | 1936.0 | 4.1795 | | 9.47 | | 2 |
| 646.0 | 21.819 | 420.0 | 1890.5 | 1942.5 | 4.1884 | 85.9 | 4.08 | 331.9 | 1 |
| 647.0 | 22.164 | 420.0 | 1894.6 | 1947.3 | 4.1947 | 69.7 | 3.97 | 343.4 | 1 |
| 648.0 | 22.513 | 420.0 | 1898.5 | 1952.1 | 4.2007 | 59.5 | 3.88 | 352.9 | 1 |
| 650.0 | 23.220 | 420.0 | 1906.1 | 1961.4 | 4.2125 | 47.0 | 3.76 | 368.5 | 1 |
| 655.0 | 25.033 | 420.0 | 1924.4 | 1984.0 | 4.2405 | 32.2 | 3.56 | 397.7 | 1 |
| 660.0 | 26.889 | 420.0 | 1941.8 | 2005.9 | 4.2670 | 25.2 | 3.44 | 420.4 | 1 |
| 665.0 | 28.776 | 420.0 | 1958.8 | 2027.3 | 4.2926 | 21.1 | 3.35 | 439.6 | 1 |
| 670.0 | 30.687 | 420.0 | 1975.4 | 2048.4 | 4.3174 | 18.3 | 3.28 | 456.7 | 1 |
| 675.0 | 32.617 | 420.0 | 1991.6 | 2069.2 | 4.3416 | 16.3 | 3.22 | 472.2 | 1 |
| 680.0 | 34.565 | 420.0 | 2007.5 | 2089.8 | 4.3651 | 14.8 | 3.17 | 486.6 | 1 |
| 685.0 | 36.526 | 420.0 | 2023.3 | 2110.2 | 4.3882 | 13.6 | 3.12 | 500.1 | 1 |
| 690.0 | 38.499 | 420.0 | 2038.8 | 2130.4 | 4.4107 | 12.6 | 3.08 | 512.8 | 1 |
| 695.0 | 40.482 | 420.0 | 2054.1 | 2150.5 | 4.4328 | 11.8 | 3.04 | 525.0 | 1 |

Table C2. Properties of coexisting phases at regular temperature increments.

| vapor | | | | | | | | | |
|---------|----------|-------------------|-------------|-----------------|----------|---------|----------------|----------------|-------------------|
| Temp. | Pressure | Density | Latent Heat | Internal Energy | Enthalpy | Entropy | C _p | C _v | Velocity of Sound |
| K | MPa | kg/m ³ | kJ/kg | kJ/kg | kJ/kg | kJ/kg.K | kJ/kg.K | | m/s |
| 643.00 | 20.995 | 199.78 | 451.8 | 2235.3 | 2340.4 | 4.8104 | 95.4 | 4.64 | 361.1 |
| 643.20 | 21.045 | 201.78 | 443.3 | 2231.2 | 2335.5 | 4.8024 | 100.4 | 4.67 | 359.6 |
| 643.40 | 21.095 | 203.84 | 434.5 | 2227.0 | 2330.5 | 4.7943 | 106.0 | 4.70 | 358.0 |
| 643.60 | 21.146 | 205.99 | 425.5 | 2222.7 | 2325.3 | 4.7858 | 112.2 | 4.73 | 356.4 |
| 643.80 | 21.197 | 208.22 | 416.2 | 2218.2 | 2320.0 | 4.7771 | 119.3 | 4.76 | 354.7 |
| 644.00 | 21.247 | 210.55 | 406.5 | 2213.5 | 2314.4 | 4.7681 | 127.3 | 4.80 | 352.9 |
| 644.20 | 21.298 | 212.97 | 396.5 | 2208.6 | 2308.6 | 4.7588 | 136.6 | 4.83 | 350.9 |
| 644.40 | 21.350 | 215.52 | 386.1 | 2203.6 | 2302.6 | 4.7491 | 147.3 | 4.88 | 348.9 |
| 644.60 | 21.401 | 218.20 | 375.2 | 2198.2 | 2296.3 | 4.7389 | 159.8 | 4.92 | 346.7 |
| 644.80 | 21.452 | 221.03 | 363.8 | 2192.7 | 2289.7 | 4.7283 | 174.7 | 4.97 | 344.4 |
| 645.00 | 21.504 | 224.04 | 351.8 | 2186.8 | 2282.7 | 4.7171 | 192.7 | 5.02 | 341.8 |
| 645.20 | 21.555 | 227.25 | 339.1 | 2180.5 | 2275.3 | 4.7053 | 214.7 | 5.08 | 339.1 |
| 645.40 | 21.607 | 230.70 | 325.6 | 2173.8 | 2267.5 | 4.6927 | 242.5 | 5.15 | 336.0 |
| 645.60 | 21.659 | 234.44 | 311.1 | 2166.6 | 2259.0 | 4.6792 | 278.3 | 5.23 | 332.7 |
| 645.80 | 21.712 | 238.55 | 295.3 | 2158.7 | 2249.7 | 4.6646 | 326.2 | 5.32 | 328.8 |
| 646.00 | 21.764 | 243.12 | 277.9 | 2150.1 | 2239.6 | 4.6485 | 393.6 | 5.42 | 324.4 |
| 646.20 | 21.816 | 248.31 | 258.5 | 2140.3 | 2228.2 | 4.6305 | 494.6 | 5.55 | 319.1 |
| 646.40 | 21.869 | 254.39 | 236.0 | 2129.0 | 2215.0 | 4.6098 | 661.6 | 5.72 | 312.6 |
| 646.60 | 21.922 | 261.87 | 208.7 | 2115.3 | 2199.1 | 4.5849 | 986.2 | 5.96 | 304.0 |
| 646.80 | 21.975 | 271.99 | 172.6 | 2097.2 | 2178.0 | 4.5521 | 1858.6 | 6.36 | 291.0 |
| 647.00 | 22.028 | 290.37 | 108.7 | 2065.6 | 2141.5 | 4.4953 | 9198.8 | 7.47 | 261.7 |
| 647.067 | 22.0460 | 322.778 | .0 | 2014.8 | 2083.1 | 4.4050 | | | .0 |
| liquid | | | | | | | | | |
| Temp. | Pressure | Density | Latent Heat | Internal Energy | Enthalpy | Entropy | C _p | C _v | Velocity of Sound |
| K | MPa | kg/m ³ | kJ/kg | kJ/kg | kJ/kg | kJ/kg.K | kJ/kg.K | | m/s |
| 645.00 | 21.504 | 425.44 | 351.8 | 1880.4 | 1930.9 | 4.1716 | 88.2 | 4.11 | 328.6 |
| 645.20 | 21.555 | 421.90 | 339.1 | 1885.1 | 1936.2 | 4.1797 | 98.7 | 4.17 | 324.0 |
| 645.40 | 21.607 | 418.11 | 325.6 | 1890.2 | 1941.8 | 4.1882 | 112.1 | 4.23 | 319.2 |
| 645.60 | 21.659 | 414.02 | 311.1 | 1895.6 | 1947.9 | 4.1974 | 129.7 | 4.30 | 314.0 |
| 645.80 | 21.712 | 409.57 | 295.3 | 1901.4 | 1954.4 | 4.2074 | 153.6 | 4.39 | 308.5 |
| 646.00 | 21.764 | 404.64 | 277.9 | 1907.9 | 1961.6 | 4.2183 | 187.8 | 4.50 | 302.6 |
| 646.20 | 21.816 | 399.08 | 258.5 | 1915.0 | 1969.7 | 4.2306 | 240.3 | 4.63 | 295.9 |
| 646.40 | 21.869 | 392.63 | 236.0 | 1923.3 | 1979.0 | 4.2448 | 329.7 | 4.80 | 288.4 |
| 646.60 | 21.922 | 384.76 | 208.7 | 1933.4 | 1990.3 | 4.2621 | 510.2 | 5.06 | 279.2 |
| 646.80 | 21.975 | 374.23 | 172.6 | 1946.7 | 2005.5 | 4.2852 | 1024.2 | 5.48 | 267.0 |
| 647.00 | 22.028 | 355.38 | 108.7 | 1970.8 | 2032.8 | 4.3272 | 5920.7 | 6.69 | 243.0 |
| 647.067 | 22.0460 | 322.778 | .0 | 2014.8 | 2083.1 | 4.4050 | | | .0 |

Table C3. Properties of coexisting phases at regular pressure intervals.

| vapor | | | | | | | | | |
|---------|----------|-------------------|-------------|-----------------|----------|---------|----------------|----------------|-------------------|
| Temp. | Pressure | Density | Latent Heat | Internal Energy | Enthalpy | Entropy | C _p | C _v | Velocity of Sound |
| K | MPa | kg/m ³ | kJ/kg | kJ/kg | kJ/kg | kJ/kg.K | kJ/kg.K | | m/s |
| 643.02 | 21.000 | 199.99 | 450.9 | 2234.9 | 2339.9 | 4.8096 | 95.9 | 4.64 | 361.0 |
| 643.22 | 21.050 | 201.98 | 442.4 | 2230.8 | 2335.0 | 4.8016 | 101.0 | 4.67 | 359.5 |
| 643.42 | 21.100 | 204.04 | 433.7 | 2226.6 | 2330.0 | 4.7935 | 106.5 | 4.70 | 357.9 |
| 643.62 | 21.150 | 206.17 | 424.8 | 2222.3 | 2324.9 | 4.7851 | 112.8 | 4.73 | 356.3 |
| 643.81 | 21.200 | 208.37 | 415.6 | 2217.9 | 2319.6 | 4.7765 | 119.8 | 4.76 | 354.6 |
| 644.01 | 21.250 | 210.66 | 406.0 | 2213.3 | 2314.1 | 4.7677 | 127.8 | 4.80 | 352.8 |
| 644.21 | 21.300 | 213.05 | 396.2 | 2208.5 | 2308.5 | 4.7585 | 136.9 | 4.84 | 350.9 |
| 644.40 | 21.350 | 215.54 | 386.0 | 2203.5 | 2302.6 | 4.7490 | 147.4 | 4.88 | 348.9 |
| 644.60 | 21.400 | 218.16 | 375.4 | 2198.3 | 2296.4 | 4.7391 | 159.6 | 4.92 | 346.7 |
| 644.79 | 21.450 | 220.91 | 364.3 | 2192.9 | 2290.0 | 4.7288 | 174.0 | 4.97 | 344.5 |
| 644.99 | 21.500 | 223.81 | 352.7 | 2187.2 | 2283.3 | 4.7180 | 191.2 | 5.02 | 342.0 |
| 645.18 | 21.550 | 226.90 | 340.5 | 2181.2 | 2276.1 | 4.7066 | 212.1 | 5.08 | 339.4 |
| 645.37 | 21.600 | 230.19 | 327.6 | 2174.8 | 2268.6 | 4.6946 | 238.1 | 5.14 | 336.5 |
| 645.56 | 21.650 | 233.74 | 313.8 | 2167.9 | 2260.5 | 4.6817 | 271.1 | 5.21 | 333.3 |
| 645.76 | 21.700 | 237.60 | 298.9 | 2160.5 | 2251.9 | 4.6680 | 314.3 | 5.29 | 329.7 |
| 645.95 | 21.750 | 241.86 | 282.7 | 2152.4 | 2242.4 | 4.6530 | 373.3 | 5.39 | 325.6 |
| 646.14 | 21.800 | 246.62 | 264.8 | 2143.5 | 2231.9 | 4.6364 | 458.2 | 5.51 | 320.9 |
| 646.33 | 21.850 | 252.07 | 244.5 | 2133.3 | 2220.0 | 4.6177 | 590.2 | 5.65 | 315.2 |
| 646.52 | 21.900 | 258.56 | 220.7 | 2121.4 | 2206.1 | 4.5959 | 821.4 | 5.85 | 307.9 |
| 646.71 | 21.950 | 266.77 | 191.1 | 2106.5 | 2188.8 | 4.5689 | 1320.1 | 6.14 | 297.9 |
| 646.89 | 22.000 | 278.71 | 149.0 | 2085.5 | 2164.4 | 4.5309 | 3066.8 | 6.69 | 281.3 |
| 647.067 | 22.0460 | 322.778 | .0 | 2014.8 | 2083.1 | 4.4050 | | | .0 |
| liquid | | | | | | | | | |
| Temp. | Pressure | Density | Latent Heat | Internal Energy | Enthalpy | Entropy | C _p | C _v | Velocity of Sound |
| K | MPa | kg/m ³ | kJ/kg | kJ/kg | kJ/kg | kJ/kg.K | kJ/kg.K | | m/s |
| 644.99 | 21.500 | 425.69 | 352.7 | 1880.0 | 1930.5 | 4.1711 | 87.5 | 4.11 | 328.9 |
| 645.18 | 21.550 | 422.28 | 340.5 | 1884.6 | 1935.6 | 4.1788 | 97.5 | 4.16 | 324.5 |
| 645.37 | 21.600 | 418.66 | 327.6 | 1889.4 | 1941.0 | 4.1870 | 110.0 | 4.22 | 319.9 |
| 645.56 | 21.650 | 414.78 | 313.8 | 1894.6 | 1946.8 | 4.1957 | 126.1 | 4.29 | 315.0 |
| 645.76 | 21.700 | 410.59 | 298.9 | 1900.1 | 1952.9 | 4.2051 | 147.6 | 4.37 | 309.8 |
| 645.95 | 21.750 | 406.00 | 282.7 | 1906.1 | 1959.7 | 4.2153 | 177.4 | 4.47 | 304.2 |
| 646.14 | 21.800 | 400.89 | 264.8 | 1912.7 | 1967.1 | 4.2266 | 221.3 | 4.58 | 298.1 |
| 646.33 | 21.850 | 395.08 | 244.5 | 1920.2 | 1975.5 | 4.2394 | 291.2 | 4.74 | 291.2 |
| 646.52 | 21.900 | 388.23 | 220.7 | 1928.9 | 1985.4 | 4.2545 | 417.6 | 4.94 | 283.3 |
| 646.71 | 21.950 | 379.64 | 191.1 | 1939.9 | 1997.7 | 4.2733 | 702.9 | 5.25 | 273.3 |
| 646.89 | 22.000 | 367.29 | 149.0 | 1955.5 | 2015.4 | 4.3006 | 1777.1 | 5.84 | 258.6 |
| 647.067 | 22.0460 | 322.778 | .0 | 2014.8 | 2083.1 | 4.4050 | | | .0 |

Appendix D. Computer Program for Table Generation

In this Appendix the FORTRAN program is listed that yields the thermodynamic properties of steam in the region shown in Fig. 1 and specified by Eq. (18).

The independent variables are temperature T in K and density D in kg/m^3 . The program computes the following properties: pressure P in MPa, energy U in kJ/kg, enthalpy H in kJ/kg, entropy S in kJ/kg.K, specific heat at constant volume CV in kJ/kg.K, specific heat at constant pressure CP in kJ/kg.K, velocity of sound CS in m/s, compressibility $COMP$ in 1/MPa.

The transformation from temperature and density to the parametric variables r and θ of the extended and revised scaled equations is performed iteratively in the subroutine CONVER. Initial guesses for r and θ to be used in CONVER are provided by the subroutine RTHETA of Moldover³⁸ which solves simple scaled equations with $c = 0$ and $k_1 = 0$. The pressure and other thermodynamic properties are calculated in the subroutine THERMO.

As a second option the temperature and pressure can be used as input variables. In this case, first the density is found from the equation of state by Newton iteration in the subroutine DFIND, after which the computations proceed as described above.

If saturation properties are desired, the independent variable is temperature; in this case $\theta = -1(+1)$ for the vapor (liquid) side and $r = \Delta\tilde{T}/(1 - b^2)$. All properties, including density and latent heat, are then calculated in THERMO. As a second option the pressure can be used as the input variable. The temperature is then found from the vapor pressure equation in the subroutine TFIND after which the calculation proceeds as described above.

The subroutine RANGE checks whether the desired point lies within the range of the validity of the equation of state.

An example of the usage of these subroutines is given by the main program shown and a sample of the output is presented.

This code has been developed and tested on a Univac 1180/1108 computer.

```

-----
BLOCKDATA
C
C THIS SUBROUTINE SUPPLIES THE PARAMETERS USED IN THE EQUATION
C OF STATE.
C
DOUBLE PRECISION A,Q
COMMON /COEFS/A(20),Q(20),ANAMES(20),QNAAMES(20)
DATA A/-.017762D0,5.2380D0,0.0D0,-25.4915D0,6.8445D0,.325D0,1.4403
1D0,0.0D0,1.3757D0,23.6666D0,4.82D0,.2942D0,-11.2326D0,-22.6547D0
2,-17.8876D0,-4.9332D0,4*0.0D0/
DATA Q/-.006D0,-.003D0,0.0D0,647.067D0,322.778D0,22.0460D0
1,.267D0,-1.6D0,12*0.0D0/
DATA ANAMES/6HC ,6HP3 ,6HDELROC,6HP2 ,6HP1 ,6HBETA
1,6HK0 ,6HDELTC ,6HB*B ,6HA ,6HDELTA ,6HK1 ,6HMUC
2,6HMU1 ,6HMU2 ,6HMU3 ,6HS00 ,6HS20 ,6HS01 ,6HS21 /
DATA QNAAMES/6HPOINTA,6HPOINTB,6HDELPC ,6HTC ,6HRHOC ,6HPC
1,6HDFC DTC,6HSLOPDI,6HP11 ,6HALPHA ,6HF00 ,6HP20 ,6HP40
2,6HDELTAI,6HALPHAI,6HBETA I,6HGAMMAI,6HP01 ,6HP21 ,6HP41 /
END
-----
SUBROUTINE CONST
C
C THIS SUBROUTINE CALCULATES ALL QUANTITIES NOT DEPENDENT ON R OR THETA.
C
IMPLICIT DOUBLE PRECISION (A-H,O-Z)
COMMON /COEFS/ A(20),Q(20)
COMMON /CRITS/TC,RHOC,PC,PCON,UCON,SCON,DPCON
EQUIVALENCE (DELI,Q(14)),(BETA,A(6)),(DELTA,A(11)),(BESQ,A(9))
1,(CC,A(1)),(AA,A(10)),(XKO,A(7)),(ALPHA,Q(10))
2,(ALHI,Q(15)),(BETI,Q(16)),(GAMI,Q(17)),(P01,Q(18)),(P21,Q(19))
3,(P00,Q(11)),(P20,Q(12)),(P40,Q(13)),(P41,Q(20))
4,(S00,A(17)),(S20,A(18)),(S01,A(19)),(S21,A(20))
C
ALPHA = 2.0D0 - A(6)*(A(11) + 1.0D0)
GAMMA = BETA*(DELTA - 1.0D0)
DELI = 0.50D0
ALHI = ALPHA - DELI
BETI = BETA + DELI
GAMI = GAMMA - DELI
ERR = 2.0D0*BETA*DELTA - 1.0D0
P00 = (BETA*(DELTA-3.0D0)-BESQ*ALPHA*GAMMA)/(2.0D0*
1 BESQ*BESQ*(2.0D0-ALPHA)*(1.0D0-ALPHA)*ALPHA)
P20=-((BETA*(DELTA-3.)-BESQ*ALPHA*ERR)/(2.*BESQ*(1.-ALPHA)*(ALPHA))
P40=(ERR-2.)/2./ALPHA
S00 = (2.-ALPHA)*P00
S20 = -BETA*(DELTA-3.)/2./BESQ/ALPHA
P01 = (BETA*(DELTA-3.0D0)-3.0D0*DELI-A(9)*ALHI*GAMI)
1 /((2.0D0*A(9)*A(9)*(2.0D0-ALHI)*(1.0D0-ALHI)*ALHI)
P21 = -((BETA*(DELTA-3.0D0)-3.0D0*DELI-A(9)*ALHI*ERR)
1 (2.0D0*A(9)*(1.0D0-ALHI)*ALHI))
P41 = (.5*ERR - 1.)/ALHI
S01 = (2.-ALHI)*P01
S21 = -(BETA*DELTA-3.*BETI)/2./BESQ/ALHI
C
C CALCULATE P11 FROM THE DIAMETER OF THE COEXISTENCE CURVE.
DA=Q(1)
DB=Q(2)
RA = DA/(1.0D0 - BESQ)
RB = DB/(1.0D0 - BESQ)
SW0 = S00+S20
DRO=SW0*(RA**(1.-ALPHA)-RB**(1.-ALPHA))
PTW = P01 + P21 + P41
SW1 = S01+S21
DR1=SW1*(RA**(1.-ALHI)-RB**(1.-ALHI))
D1=CC*AA*XKO*DRO
D2=CC*AA*A(12)*DR1
Q(9) = (Q(8)*(1./(1.-DB)-1./(1.-DA))+D1+D2)/(DB-DA)
C
Q(3)=A(8)*Q(7)
TC=Q(4)+A(8)
RHOC=Q(5)+A(3)
PC=Q(6)+Q(3)
PCON=PC/TC
UCON=1.D3*PC
SCON=UCON/TC
DPCON=PCON/RHOC/RHOC
RETURN
END
-----
SUBROUTINE RANGE(IRANGE,IOPT,T,D,P)
C
C THIS ROUTINE DETERMINES WHETHER THE ENTRY POINT IS WITHIN THE RANGE
C OF VALIDITY OF THE EQUATION OF STATE (IRANGE=1), OR NOT (IRANGE=0).
C
IMPLICIT REAL*8(A-H,O-Z)
COMMON/SATUR/ISAT

```

```

COMMON/CRITS/TC,RHOC,PC
DATA TMIN,TMAX/643.D0,695.D0/,DMIN,DMAX/200.D0,420.D0/
C
IRANGE=1
IF(ISAT.NE.0) GO TO 10
IF(T.LT.TMIN .OR. T.GT.TMAX) GO TO 99
IF(IOPT.EQ.2) GO TO 20
IF(D.LT.DMIN .OR. D.GT.DMAX) GO TO 99
RETURN
20 CALL THERMO(1,T,DMIN,PHIN,R,THETA)
CALL THERMO(1,T,DMAX,PHAX,R,THETA)
IF(P.LT.PMIN .OR. P.GT.PMAX) GO TO 99
RETURN
10 IF(IOPT.EQ.2) GO TO 30
IF(T.GE.TC) GO TO 99
IF(ISAT.EQ.-1 .AND. T.LT.TMIN) GO TO 99
IF(ISAT.EQ. 1 .AND. T.LT.645.D0) GO TO 99
RETURN
30 IF(P.GE.PC) GO TO 99
IF(ISAT.EQ.-1 .AND. P.LT.21.0D0) GO TO 99
IF(ISAT.EQ. 1 .AND. P.LT.21.5D0) GO TO 99
RETURN
99 IRANGE=0
WRITE(6,2)
2 FORMAT(2X,'THIS POINT IS OUTSIDE THE RANGE!'/)
RETURN
END
-----
SUBROUTINE THERMO(IDFIND,T,D,P,R1,TH1)
C
C 1. NOT ON THE SATURATION CURVE (ISAT=0) :
C GIVEN THE TEMPERATURE T(K) AND DENSITY D(KG/M3), THIS ROUTINE
C CALCULATES PRESSURE P(MPA) AND ITS DERIVATIVES W.R.T D AT
C CONSTANT T DPDD(MPA/(KG/M3)) AND W.R.T T AT CONSTANT D
C DPDT(MPA/K), ENERGY U AND ENTHALPY H(KJ/KG), ENTROPY AND
C SPECIFIC HEATS CP AND CV(KJ/KGK), VELOCITY OF SOUND CS(M/S),
C AND COMPRESSIBILITY COMP(1/MPA).
C IF THE ENTRY POINT IS IN THE 2-PHASE REGION (IPHASE=2) IT
C RETURNS CP=COMP=CS=0.
C IF IDFIND=1 IT CALCULATES ONLY P AND DPDD.
C 2. ON THE SATURATION CURVE (ISAT.NE.0) :
C GIVEN THE TEMPERATURE T, IT CALCULATES THE DENSITY D, LATENT HEAT
C AND ALL THE ABOVE PROPERTIES ON THE VAPOR SIDE (ISAT=-1), OR THE
C LIQUID SIDE (ISAT=1).
C
IMPLICIT DOUBLE PRECISION (A-H,O-Z)
COMMON/THERM/IPHASE,DPDD,DPDT,U,H,ENTROP,CP,CV,CS,COMP
COMMON/SATUR/ISAT,HEAT,DLIQ,DVAP
COMMON/COEFS/A(20),Q(20)
COMMON/CRITS/TC,RHOC,PC,PCON,UCON,SCON,DPCON
DIMENSION S(2),XK(2),SD(2)
EQUIVALENCE (PW1,A(5)),(PW2,A(4)),(PW3,A(2)),
1 (AMC,A(13)),(AM1,A(14)),(AM2,A(15)),(AM3,A(16)),
2 (P00,Q(11)),(P20,Q(12)),(P40,Q(13)),
3 (P01,Q(18)),(P21,Q(19)),(P41,Q(20)),
4 (AA,A(10)),(XK0,A(7)),(XK1,A(12)),(PW11,Q(9)),
5 (ALPHA,Q(10)),(ALHI,Q(15)),(BESQ,A(9))
C
XK(1)=XK0
XK(2)=XK1
TEE=(T-TC)/TC
TW=-TC/T
DTW=1.D0+TW
IF(ISAT.NE.0) GO TO 10
RHO=D/RHOC
CALL CONVER(RHO,TEE,AMU,TH1,R1,RHO1,S,RHODI,ERR)
GO TO 12
10 TH1=1.D0
IF(ISAT.EQ.-1) TH1=-0.9999999999999999D0
IF(ISAT.EQ. 1) TH1= 0.9999999999999999D0
R1=DTW/(1.D0-BESQ)
CALL SS(R1,TH1,S,SD)
RHO=TH1*(XK0*R1**A(6)+XK1*R1**Q(16))+A(1)*(S(1)+S(2))
RHO=1.D0+PW11*DTW*RHO
D=RHO*RHOC
AMU=0.D0
12 TT1=TH1*TH1
TT2=TT1*TT1
PW0=1.D0+DTW*(PW1+DTW*(PW2+DTW*PW3))
PMMU=AMU*RHODI
POTH=P00+P20*TT1+P40*TT2
P1TH=P01+P21*TT1+P41*TT2
DPW0=XK0*POTH*R1**(2.-ALPHA)
DPW1=XK1*P1TH*R1**(2.-ALHI)
DPW=AA*(DPW0+DPW1)
PW=PW0+PMMU+DPW
IF(IDFIND.EQ.1) GO TO 11

```

```

DPODT=PW1+DTW*(2.D0*PW2+3.D0*PW3*DTW)
DMODT=AM1+DTW*(2.D0*AM2+3.D0*AM3*DTW)
UW=DP0DT-RHO*DMODT+PW1*AMU+S(1)+S(2)
HW=PW-TW*UW
AMW=AMU+AMC+DTW*(AM1+DTW*(AM2+DTW*AM3))
SW=HW-RHO*AMW
C
D2P0DT=2.D0*PW2+6.D0*PW3*DTW
D2M0DT=2.D0*AM2+6.D0*AM3*DTW
11 IF(DABS(TH1).GE.1.D0) GO TO 13
    IPHASE=1
    CALL AUX(R1,TH1,D2PDT2,D2PDHT,D2PDM2,AA,XK,SD,CVCOEX)
    DPDD=DPCON*D*T/D2PDM2
    IF(IDFIND.EQ.1) GO TO 15
    DPDTCD=DP0DT+PW1*(AMU-RHO/D2PDM2)+S(1)+S(2)-D2PDHT*RHO/D2PDM2
    DPWDTW=PW-TW*DPDTCD
    CVITW2=D2P0DT-RHO*D2M0DT+D2PDT2-(PW1+D2PDHT)**2/D2PDM2
    CVW=CVITW2*T*TW
    CPW=CVW+D2PDM2*DPWDTW*DPWDTW/(RHO*RHO)
    COMP=1.D0/(D*DPDD)
    CS=1.D3*DSQRT(CPW/CVW*DPDD)
    IF(ISAT.EQ.0) GO TO 14
    RHO1=1.D0+PW1*DTW+A(1)*(S(1)+S(2))
    RHO2=XK0*R1**A(6)+XK1*R1**Q(16)
    DLIQ=RHOC*(RHO1+RHO2)
    DVAP=RHOC*(RHO1-RHO2)
    BPD2=PW-TW*(UW+RHO*DMODT)
    HEAT=1.D3*T*(PCON*DPDT2)*(1.D0/DVAP-1.D0/DLIQ)
    GO TO 14
13 IPHASE=2
    DPDD=0.
    IF(IDFIND.EQ.1) GO TO 15
    DPDTCD=UW+RHO*DMODT
    DPWDTW=PW-TW*DPDTCD
    CVI0=(2.-ALPHA)*(1.-ALPHA)*R1**(-ALPHA)*XK0*POTH
    CVI1=(2.-ALHI)*(1.-ALHI)*R1**(-ALHI)*XK1*P1IH
    CVITW2=D2P0DT-RHO*D2M0DT+AA*(1./(1.-BESQ))**2*(CVI0+CVI1)
    CVW=CVITW2*T*TW
    CPW=0.
    COMP=0.
    CS=0.
C
14 DPDT=PCON*DPWDTW
    SCOND=SCON/D
    U=UW*UCON/D
    H=HW*SCOND*T
    ENTROP=SW*SCOND
    CV=CVW*SCOND
    CP=CPW*SCOND
15 P=PW*PCON*T
    RETURN
    END

```

SUBROUTINE DFIND(T,P,D,DGUESS,DMIN,DMAX)

```

C
C GIVEN THE TEMPERATURE T(K), PRESSURE P(MPA), AND AN INITIAL
C GUESS DENSITY DGUESS(KG/M3), THIS ROUTINE FINDS THE
C CORRESPONDING DENSITY D(KG/M3) IN THE RANGE (DMIN,DMAX).
C IF T IS BELOW THE CRITICAL ISOTHERM, DGUESS MUST BE SET
C EQUAL TO THE CRITICAL DENSITY, OTHERWISE IT MAY YIELD
C ERRONEOUS RESULTS. IF THE ENTRY POINT IS IN THE 2-PHASE
C REGION CRITICAL DENSITY IS RETURNED FOR D.
C

```

```

    IMPLICIT REAL*8(A-H,O-Z)
    COMMON/THERM/IPHASE,DPDD
C

```

```

C
D=DGUESS
DO 10 I=1,20
CALL THERMO(1,T,D,PP,R,THETA)
PDIF=PP-P
IF(IPHASE.EQ.2) GO TO 18
DELD=-PDIF/DPDD
D=D+DELD
IF(D.LT.DMIN) D=DMIN
IF(D.GT.DMAX) D=DMAX
IF(DABS(DELD/D).LT.1.D-6) GO TO 19
GO TO 10
18 IF(DABS(PDIF).LE.0.D0) GO TO 19
IF(PDIF.LT.0.D0) D=DMAX
IF(PDIF.GT.0.D0) D=DMIN
10 CONTINUE
WRITE(6,21) T,P,PP,D
21 FORMAT(5X,'DFIND DOES NOT CONVERGE :',4F12.4)
21 RETURN
19 RETURN
END

```

```

SUBROUTINE TFIND(P,T)
C
C GIVEN A PRESSURE P(MPA) BELOW THE CRITICAL ISOBAR, IT FINDS THE
C CORRESPONDING TEMPERATURE T(K) ON THE SATURATION CURVE.
C
C IMPLICIT DOUBLE PRECISION (A-H,O-Z)
COMMON/THERM/IPHASE,DPDD,DPDT,U,H,ENTROP,CP,CV,CS,COMP
COMMON/SATUR/ISAT,HEAT,RHOL,RHOG
COMMON/CRITS/TC,RHOC,PC,PCON,UCON,SCON,DPCON
C
T=TC-1.D0
D=RHOC
ISAVE=ISAT
ISAT=2
DO 10 I=1,20
CALL THERMO(O,T,D,PP,R1,TH1)
DT=(PP-P)/DPDT
T=T-DT
IF(T.GT.TC) GO TO 12
IF(DABS(DT/T).LT.1.D-8) GO TO 20
GO TO 10
12 T=TC-0.001D0
10 CONTINUE
WRITE(6,11) P,PP,T
11 FORMAT(1X/1X'TFIND DOES NOT CONVERGE :',3F12.6/)
20 ISAT=ISAVE
RETURN
END
-----
SUBROUTINE CONVER(RHO,TEE,AMU,TH1,R1,RHO1S,S1,RHODI,ERROR1)
C
C THIS ROUTINE TRANSFORMS TEMPERATURE AND DENSITY TO THE PARAMETRIC VARIABLES
C R AND THETA ACCORDING TO THE REVISED AND EXTENDED SCALED EQUATIONS.
C
C IMPLICIT REAL*8 (A-H,O-Z)
COMMON /COEFS/ A(20),Q(20)
DIMENSION S1(2),SD(2)
EQUIVALENCE(BETA,A(6)),(DELTA,A(11)),(XK1,A(12)),(CC,A(1))
1 ,(ALH1,Q(15)),(ALPHA,Q(10)),(BESQ,A(9)),(P11,Q(9))
2 ,(DELI,Q(14)),(P1W,Q(18)),(P2W,Q(19)),(P4W,Q(20))
3 ,(AA,A(10)),(XK0,A(7)),(S00,A(17)),(S20,A(18)),(BETAI,Q(16))
C
TSTAR = TEE+1.D0
DTSTIN = 1.D0 - (1.D0/TSTAR)
R1=DTSTIN
IF(DTSTIN.LT.0.) R1=DTSTIN/(1.-BESQ)
TH1=0.
IF(DTSTIN.LT.0.) TH1=1.
CALL SS(R1,TH1,S1,SD)
RHODI = 1.D0 + P11*DTSTIN
RHODIT = RHODI + CC*S1(1) + CC*S1(2)
DRHO = RHO - RHODIT
AMU = 0.D0
IF(DTSTIN.GT.0.D0) GO TO 1
RHO1CO = XK0*R1**BETA + XK1*R1**BETAI
TWOFAZ = RHO1CO
IF (DABS(DRHO).GT.TWOFAZ) GO TO 1
RHO1S = DSIGN(RHO1CO,DRHO) + CC*S1(1)
TH1 = DSIGN(1.D0,DRHO)
ERROR1 = 1.D0
GO TO 999
1 CONTINUE
IF(DRHO.NE.0.D0) GO TO 2
TH1 = 0.D0
R1 = DTSTIN
RHO1S = CC*S1(1)
2 CONTINUE
C RULE FOR FIRST PASS
Y1 = DTSTIN
DEN1 = RHO - RHODIT
CALL RTHETA(R1,TH1,DEN1,Y1)
TT=TH1*TH1
AMU = AA* R1** (BETA*DELTA)*TH1*(1.D0-TT)
Y1 = DTSTIN + CC*AMU
CALL SS(R1,TH1,S1,SD)
RHOWEG = XK1*(R1**BETAI)*TH1 + CC*S1(2)
RHO1S = DEN1 + CC*S1(1) + RHOWEG
ERROR1 = RHO - RHODI - RHO1S
IF( DABS(ERROR1).LT.1.D-5 ) GO TO 999
C RULE FOR SECOND PASS
DEN12 = RHO - RHODI - CC*S1(1) + RHOWEG
IF (DEN12.EQ.DEN1) DEN12 = DEN1 - 1.D-06
CALL RTHETA(R1,TH1,DEN12,Y1)
TT = TH1*TH1
AMU = AA* R1** (BETA*DELTA)*TH1*(1.D0-TT)
Y1 = DTSTIN + CC*AMU
CALL SS(R1,TH1,S1,SD)
RHOWEG = XK1*R1**BETAI*TH1 + CC*S1(2)

```



```

RHO1S2 = DEN12 + CC*S1(1) + RHOWEG
ERROR2 = RHO - RHODI - RHO1S2
IF( DABS(ERROR2).GT.1.D-5 ) GO TO 998
ERROR1 = ERROR2
RHO1S = RHO1S2
GO TO 999
998 CONTINUE
C RULE FOR NTH PASS
DEN2 = DEN12
DO 44 ISIG = 1,10
SLOPE = (ERROR2-ERROR1)/(DEN2 -DEN1)
HOLD = DEN2
DEN2 = DEN1 - (ERROR1/SLOPE)
CALL RTHETA(R1,TH1,DEN2,Y1)
TT = TH1*TH1
AMU = AA* R1**(BETA*DELTA)*TH1*(1.D0-TT)
Y1 = DTSTIN + CC*AMU
CALL SS(R1,TH1,S1,SD)
RHOWEG = XK1*R1**BETA1*TH1 + CC*S1(2)
RHO1S = DEN2 + CC*S1(1) + RHOWEG
ERROR1 = ERROR2
ERROR2 = RHO - RHODI - RHO1S
IF( DABS(ERROR2).LT.1.D-6 ) GO TO 999
DEN1 = HOLD
44 CONTINUE
IF(DABS(ERROR2).GT.1.D-6) WRITE (6,66) ERROR2,RHO,DTSTIN,DEN2,CC
66 FORMAT(1X,'CONVER DOES NOT CONVERGE ',5E12.6)
999 CONTINUE
RETURN
END

```

```

-----
SUBROUTINE RTHETA(R,THETA, RHO,TEE )
C
CC THIS VERSION WILL FIT DATA FOR THETA GT 1.0 AND LT 1.000001
CC SOLVES RHO = EM*THETA*(R**BETA)
CC AND TEE = R*(1.D0 DESQ*THETA*THETA)
C
IMPLICIT REAL*8 (A-H,O-Z)
COMMON /COEFS/ A(20),Q(20)
EQUIVALENCE (BETA,A(6)),(EM,A(7)),(BESQ,A(9))
C
IF(EM.LE.0.D0 .OR. BESQ.LE.1.D0) GO TO 600
ABSRHO = DABS( RHO )
IF(ABSRHO .LT. 1.D-12 ) GO TO 600
BEE = DSQRT(BESQ)
IF(DABS(TEE) .LT. 1.D-12) GO TO 495
IF( TEE .LT. 0.D0 ) Z = 1.D0-(1.D0-BEE)*TEE/(1.D0-BESQ)
1 *(EM/ABSRHO)**(1.D0/BETA)
IF(TEE.GT.0.D0) Z = (1.D0+TEE*(EM/BEE/ABSRHO)**(1.D0/BETA))**(-BETA)
IF(-Z.GT.1.00234D0*BEE) GO TO 496
C = -RHO*BEE/EM/DABS(TEE)**BETA
Z = DSIGN(Z,RHO)
DO 500 N = 1, 16
Z2 = Z*Z
Z3 = 1.D0 - Z2
DZ = Z3*(Z+C*DABS(Z3)**BETA)/(Z3+2.D0*BETA*Z2)
Z = Z - DZ
IF(DABS(DZ/Z) .LT. 1.D-12) GO TO 498
500 CONTINUE
601 WRITE(6,450) R,THETA, RHO,TEE,BETA,EM,BESQ
IF(DABS(THETA).GT.1.0001) THETA=THETA/DABS(THETA)
RETURN
498 THETA = Z/BEE
R = TEE/(1.D0-Z*Z)
R = DABS(R)
RETURN
495 THETA = DSIGN(1.D0,RHO)/BEE
R = (RHO/(EM*THETA))**(1.D0/BETA)
RETURN
496 THETA = DSIGN(1.,RHO)
R = TEE / ( 1.000 - BESQ )
R = DABS(R)
RETURN
600 IF(DABS(TEE) .LT. 1.D-12) GO TO 601
IF(TEE.LT.0.D0) GO TO 496
THETA = 1.D-12
R = TEE
450 FORMAT(2X,'RTHETA DOES NOT CONVERGE' , 7(1X, E12.6) )
RETURN
END

```

```

-----
SUBROUTINE SS(R,TH,S,SD)
C
IMPLICIT DOUBLE PRECISION(A-H,O-Z)
DIMENSION S(2),SD(2)
COMMON /COEFS/ A(20),Q(20)
EQUIVALENCE (ALPHA,Q(10)),(BETA,A(6)),(BESQ,A(9)),(DELTA,A(11))
1,(DELI,Q(14)),(ALHI,Q(15)),(BETI,Q(16)),(GAMI,Q(17)),(POO,Q(11))

```

```

2,(P01,Q(18)),(S00,A(17)),(S20,A(18)),(S01,A(19)),(S21,A(20))
C
TT = TH*TH
S(1)= S00 + S20*TT
SD(1) = 2.*S20*TH
S(2) = S01 + S21*TT
SD(2) = 2.*S21*TH
S(1)=S(1)*A(10)*A(7)*R**(1.-ALPHA)
S(2)=S(2)*A(10)*A(12)*R**(1.-ALHI)
RETURN
END
-----
SUBROUTINE AUX(R1,TH1,D2PDT2,D2PDMT,D2PDM2,AA,XK,SD,CVCOEX)
C
C THIS SUBROUTINE CALCULATES SOME OF THE SECOND DERIVATIVES OF
C THE ANOMALOUS PART OF THE EQUATION OF STATE.
C
IMPLICIT REAL*8 (A-H,O-Z)
COMMON /COEFS/ A(20),Q(20)
DIMENSION XK(2),S(2), SD(2),W(2),Y(2),Z(2),COEX(2)
EQUIVALENCE (CC,A(1)),(BETA,A(6)),(BESQ,A(9)),(DELTA,A(11))
1,(ALPHA,Q(10)),(S00,A(17)),(S20,A(18)),(S01,A(19)),(S21,A(20))
C
DELI = 0.DO
S(1)=S00+S20*TH1*TH1
S(2)=S01+S21*TH1*TH1
SD(1) = 2.*TH1*S20
SD(2) = 2.*TH1*S21
WW = 0.DO
YY = 0.DO
ZZ = 0.DO
GAMMA = BETA*(DELTA - 1.DO)
TT1 = TH1*TH1
TER = 2.DO*BETA*DELTA - 1.DO
G = (1.+(BESQ*TER-3.)*TT1 - BESQ*(TER-2.)*TT1*TT1)
CVCOEX = 0.DO
DO 30 I = 1,2
ALHI = ALPHA - DELI
BETI = BETA + DELI
GAMI = GAMMA - DELI
W(I)=(1.-ALHI)*(1.-3.*TT1)*S(I)-BETA*DELTA*(1.-TT1)*TH1*SD(I)
W(I) = (W(I) *(R1**(-ALHI)))/G
W(I) = W(I)*XK(I)
WW = WW + W(I)
Y(I) = BETI*(1.DO-3.DO*TT1)*TH1 - BETA*DELTA*(1.DO-TT1)*TH1
Y(I) = (Y(I) *(R1**(-BETI - 1.DO)))*XK(I)/G
YY = YY + Y(I)
Z(I) = 1.DO - BESQ*(1.DO - (2.DO*BETI))*TT1
Z(I) = (Z(I) *(R1**(-GAMI)))*XK(I)/G
ZZ = ZZ + Z(I)
A1 = ((BETA*(DELTA-3.DO)-3.DO*DELI-BESQ*ALHI*GAMI)
1/(2.DO*BESQ*BESQ*(2.DO-ALHI)*(1.DO-ALHI)*ALHI)
A2 = 1+((BETA*(DELTA-3.DO)-3.DO*DELI-BESQ*ALHI*TER)/
1(2.DO*BESQ*(1.DO-ALHI)*ALHI))
A2 = - A2
A4 = 1.DO+((TER-2.DO)/(2.DO*ALHI))
F1 = A1 + A2 + A4
COEX(I) = ((2.DO - ALHI)*ALHI*(1.DO - ALHI)*(R1**(-ALHI))*F1*XK(I))
CVCOEX = CVCOEX + COEX(I)
DELI = 0.5DO
30 CONTINUE
D2PDT2 = AA*WW
D2PDMT = YY + AA*CC*WW
D2PDM2 = ZZ/AA + 2.DO*CC*YY + (CC**2)*AA*WW
RETURN
END
-----
SAMPLE MAIN PROGRAM
C
C ISAT=-1 CALCULATES PROPERTIES ON THE VAPOR SIDE OF THE SATURATION CURVE.
C ISAT=1 CALCULATES PROPERTIES ON THE LIQUID SIDE OF THE SATURATION CURVE.
C ISAT=0 CALCULATES PROPERTIES AT ANY POINT ON THE THERMODYNAMIC SURFACE
C NOT ON THE SATURATION CURVE.
C IOPT=1 TAKES AS INPUT VARIABLES TEMPERATURE AND DENSITY (WHEN ISAT=0),
C OR TEMPERATURE ONLY (WHEN ISAT.NE.0).
C IOPT=2 TAKES AS INPUT VARIABLES TEMPERATURE AND PRESSURE (WHEN ISAT=0),
C OR PRESSURE ONLY (WHEN ISAT.NE.0).
C UNITS ARE AS FOLLOWS: TEMPERATURE IN (K), DENSITY IN (KG/M3), PRESSURE
C IN (MPA), ENERGY IN (KJ/KG), SPECIFIC HEAT IN (KJ/KG.K), VELOCITY OF
C SOUND IN (M/S), COMPRESSIBILITY IN (1/MPA), ETC.
C
IMPLICIT REAL*8 (A-H,O-Z)
REAL ANAMES,QNAMES
COMMON/COEFS/A(20),Q(20),ANAMES(20),QNAMES(20)
COMMON/THERM/IPHASE,DPDD,DPDT,U,H,S,CP,CV,CS,COMP
COMMON/SATUR/ISAT,HEAT,DLIQ,DVAP
COMMON/CRITS/TC,RHOC,PC,PCON,UCON,SCON,DPCON

```

```

DATA DMIN,DMAX/200.00,420.00/
C
CALL CONST
WRITE(6,122)
WRITE(6,159) (I,A(I),ANAMES(I),I,Q(I),QNAMES(I),I=1,20)
WRITE(6,123)
C
100 READ(S,1,END=999) ISAT,IOPT,T,D,P
CALL RANGE(IRANGE,IOPT,T,D,P)
IF(IRANGE.EQ.0) GO TO 100
IF(IOPT.EQ.1) GO TO 200
IF(ISAT.EQ.0) CALL DFIND(T,P,D,RHOC,DMIN,DMAX)
IF(ISAT.NE.0) CALL TFIND(P,T)
200 CALL THERMO(0,T,D,P,R,THETA)
IF(ISAT.EQ.-1) WRITE(6,124) HEAT
IF(ISAT.EQ. 1) WRITE(6,125) HEAT
WRITE(6,121) IPHASE,T,D,P,U,H,S,CV,CP,CS,COMP
GO TO 100
999 STOP
C
1 FORMAT ( )
159 FORMAT(5X,2HA(,I2,2H)=,F12.6,5X,A6,5X,2HQ(,I2,2H)=,F12.6,
1 5X,A6)
124 FORMAT(5X,'VAPOR SIDE OF SATURATION CURVE: LATENT HEAT=',
1 F7.2)
125 FORMAT(5X,'LIQUID SIDE OF SATURATION CURVE: LATENT HEAT=',
1 F7.2)
121 FORMAT(5X,'IN',I2,'-PHASE REGION :',3X,'T=',F8.3,3X,'D=',
1 F8.3,3X,'P=',F8.4/5X,'U=',F7.1,3X,'H=',F7.1,3X,'S=',
1 F7.4,3X,'CV=',F7.3/5X,'CP=',E10.5,3X,'CS=',F7.2,3X,
3 'COMP=',E10.5/)
122 FORMAT(1X,'PARAMETERS OF THE SCALED EQUATIONS ARE :'/)
123 FORMAT('/' ENTER ISAT, IOPT, TEMPERATURE(K), DENSITY(KG/M3), ',
1 'PRESSURE(MPA)'/ (ENTRY FOR DEPENDENT VARIABLE(S) WILL
2 'BE IGNORED)'/)
END

```

@XQT,F

PARAMETERS OF THE SCALED EQUATIONS ARE :

| | | | | | |
|--------|------------|---------|--------|------------|--------|
| A(1)= | -.017762 | C | Q(1)= | -.006000 | POINTA |
| A(2)= | 5.238000 | P3 | Q(2)= | -.003000 | POINTB |
| A(3)= | .000000 | DELROCC | Q(3)= | .000000 | DELPC |
| A(4)= | -25.491500 | P2 | Q(4)= | 647.067000 | TC |
| A(5)= | 6.844500 | P1 | Q(5)= | 322.778000 | RHOC |
| A(6)= | .325000 | BETA | Q(6)= | 22.046000 | PC |
| A(7)= | 1.440300 | K0 | Q(7)= | .267000 | DPCBTC |
| A(8)= | .000000 | DELTC | Q(8)= | -1.600000 | SLOPDI |
| A(9)= | 1.375700 | B*RB | Q(9)= | .491776 | P11 |
| A(10)= | 23.666600 | A | Q(10)= | .108500 | ALPHA |
| A(11)= | 4.820000 | DELTA | Q(11)= | .586535 | P00 |
| A(12)= | .294200 | K1 | Q(12)= | -1.026243 | P20 |
| A(13)= | -11.232600 | MUC | Q(13)= | .612903 | P40 |
| A(14)= | -22.654700 | MU1 | Q(14)= | .500000 | DELTAI |
| A(15)= | -17.887600 | MU2 | Q(15)= | -.391500 | ALPHA1 |
| A(16)= | -4.933200 | MU3 | Q(16)= | .825000 | BETA I |
| A(17)= | 1.109430 | S00 | Q(17)= | .741500 | GAMMAI |
| A(18)= | -1.981396 | S20 | Q(18)= | .103246 | P01 |
| A(19)= | .246913 | S01 | Q(19)= | .160322 | P21 |
| A(20)= | -.843411 | S21 | Q(20)= | -.169860 | P41 |

ENTER ISAT, IOPT, TEMPERATURE(K), DENSITY(KG/M3), PRESSURE(MPA)
(ENTRY FOR DEPENDENT VARIABLE(S) WILL BE IGNORED)

```

> 0 1 680. 350. 0.
IN 1-PHASE REGION : T= 680.000 D= 350.000 P= 31.9201
U= 2103.7 H= 2194.9 S= 4.5297 CV= 3.313
CP= .21679+02 CS= 434.83 COMP= .98868-01

> 0 1 645. 240. 0.
IN 2-PHASE REGION : T= 645.000 D= 240.000 P= 21.5038
U= 2143.7 H= 2233.3 S= 4.6405 CV= 13.729
CP= .000000 CS= .00 COMP= .000000

> 0 2 650. 0. 23.
THIS POINT IS OUTSIDE THE RANGE!

> 0 2 650. 0. 23.
IN 1-PHASE REGION : T= 650.000 D= 390.593 P= 23.0000
U= 1941.4 H= 2000.3 S= 4.2731 CV= 4.083
CP= .94553+02 CS= 336.03 COMP= .52503+00

> -1 1 646. 0. 0.
VAPOR SIDE OF SATURATION CURVE: LATENT HEAT= 277.94
IN 1-PHASE REGION : T= 646.000 D= 243.117 P= 21.7639
U= 2150.1 H= 2239.6 S= 4.6485 CV= 5.421
CP= .39360+03 CS= 324.40 COMP= .28377+01

> 1 2 0. 0. 21.8
LIQUID SIDE OF SATURATION CURVE: LATENT HEAT= 264.78
IN 1-PHASE REGION : T= 646.138 D= 400.891 P= 21.8000
U= 1912.7 H= 1967.1 S= 4.2266 CV= 4.585
CP= .22126+03 CS= 298.08 COMP= .13549+01

```

Appendix E. Units and Conversion Factors*Units used in the tables*

| | |
|-------------------------------|-------------------|
| Pressure | MPa |
| Temperature | K |
| Density | kg/m ³ |
| Energy, enthalpy, latent heat | kJ/kg |
| Entropy, specific heats | kJ/kg.K |
| Sound velocity | m/s |

*Conversion factors*Pressure

| | |
|---------------------|--------------------------|
| MPa to | multiply table values by |
| Pa | 10 ⁶ |
| bar | 10 |
| atmosphere | 9.869233 |
| lbf/in ² | 145.037738 |

Density

| | |
|----------------------|--------------------------|
| kg/m ³ to | multiply table values by |
| mol/dm ³ | 0.0555083 |
| lbm/ft ³ | 0.0624280 |

Energy, enthalpy

| | |
|----------|--------------------------|
| kJ/kg to | multiply table values by |
| J/mol | 18.01534 |
| BTU/lbm | 0.4299226 |

Entropy, specific heats

| | |
|------------|--------------------------|
| kJ/kg.K to | multiply table values by |
| J/mol.K | 18.01534 |
| BTU/lbm.R | 0.2388459 |

Sound velocity

| | |
|--------|-------------------------|
| m/s to | multiply table value by |
| ft/s | 3.28083 |

Temperature

| | |
|------|---|
| K to | transform table value by |
| °C | $(T,^{\circ}\text{C}) = (T, \text{K}) - 273.15$ |
| °F | $(T,^{\circ}\text{F}) = 1.8[(T, \text{K}) - 273.15] + 32$ |
| R | $(T, \text{R}) = 1.8(T, \text{K})$ |