

# Microstructure Effects of Thermoelectric Nanowire Composites

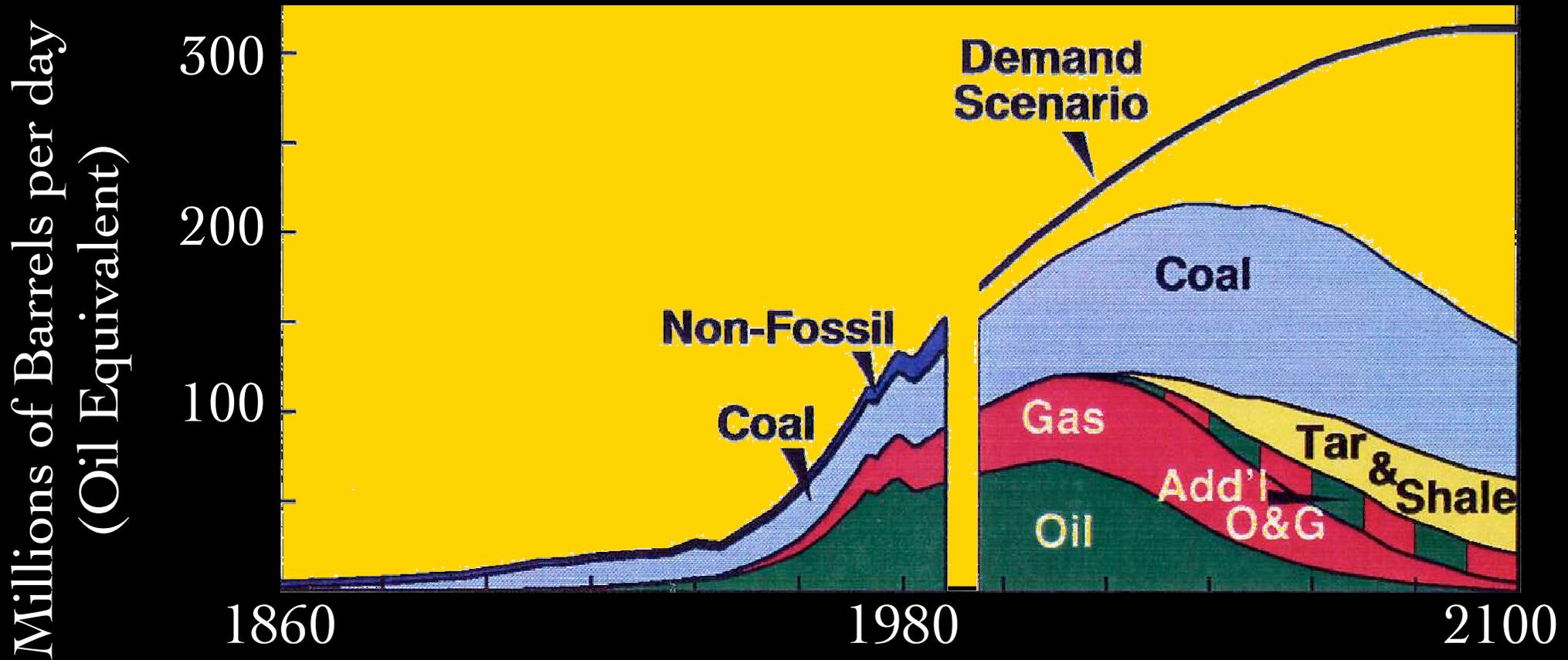
8/24/2006

Mara Howell

Prof. R. Edwin García

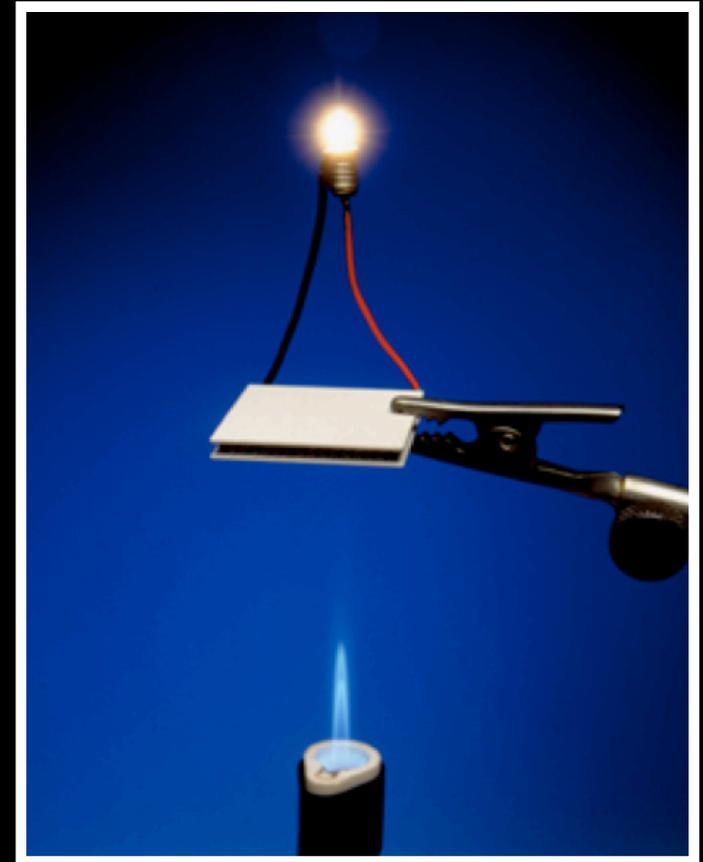
Prof. Tim Sands

# Motivation



*Bookout, John F. (President of Shell USA), "Two Centuries of Fossil Fuel Energy"  
International Geological Congress, Washington DC; July 10, 1985.*

$$ZT = \frac{S^2 \sigma}{\kappa_{el} + \kappa_{ph}} T$$

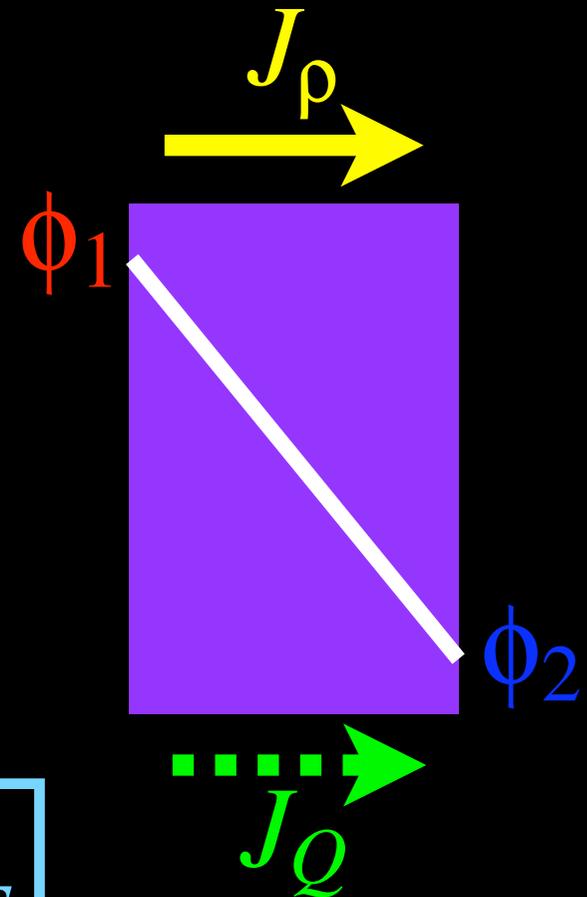
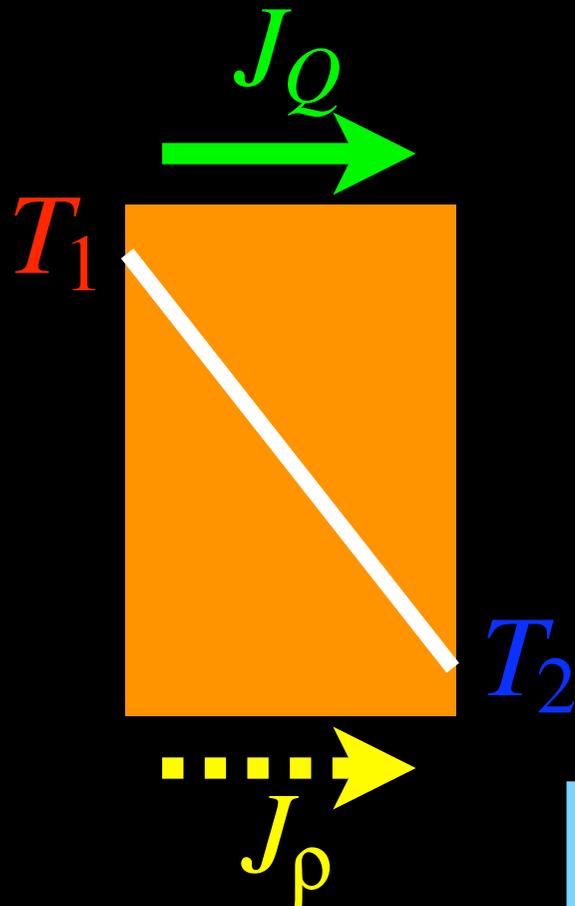


[www.tellurex.com](http://www.tellurex.com)

# Thermoelectricity

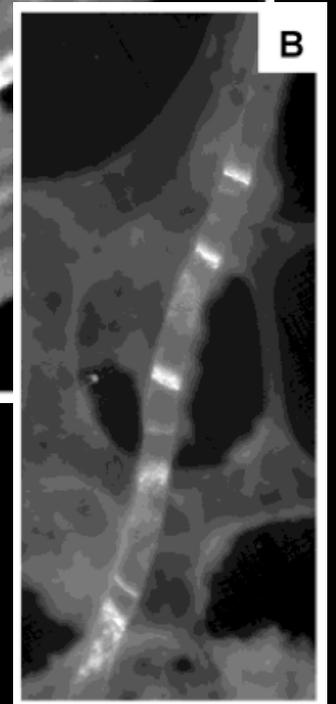
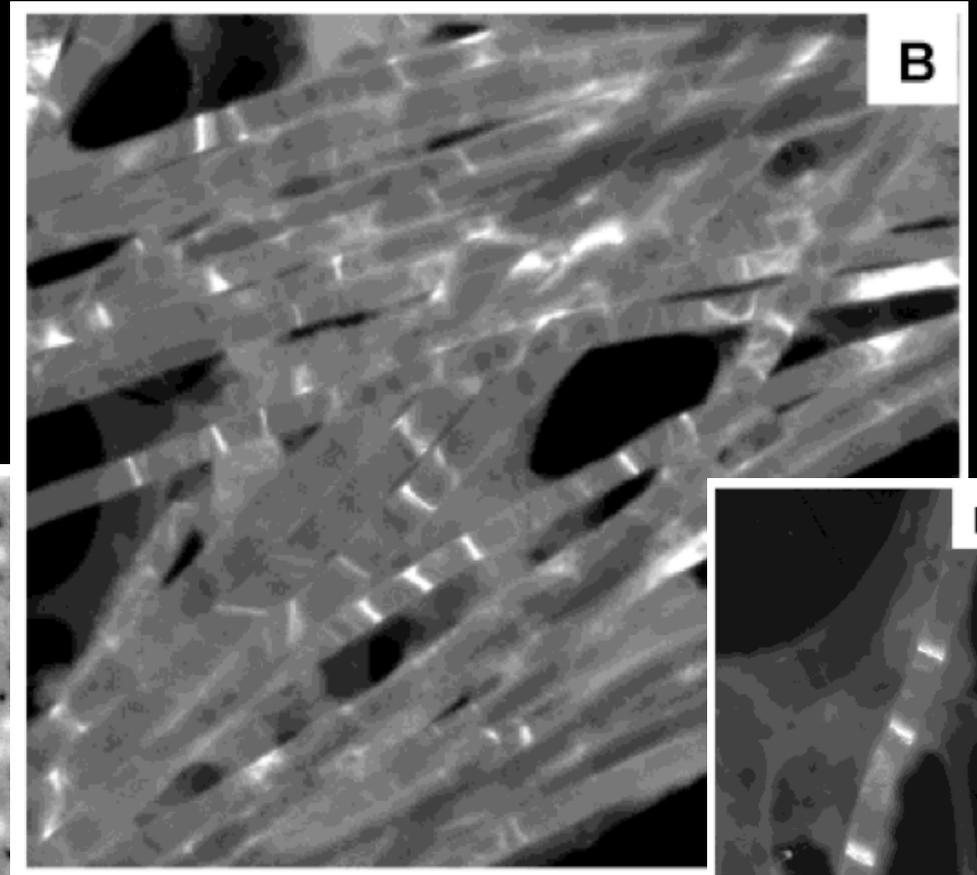
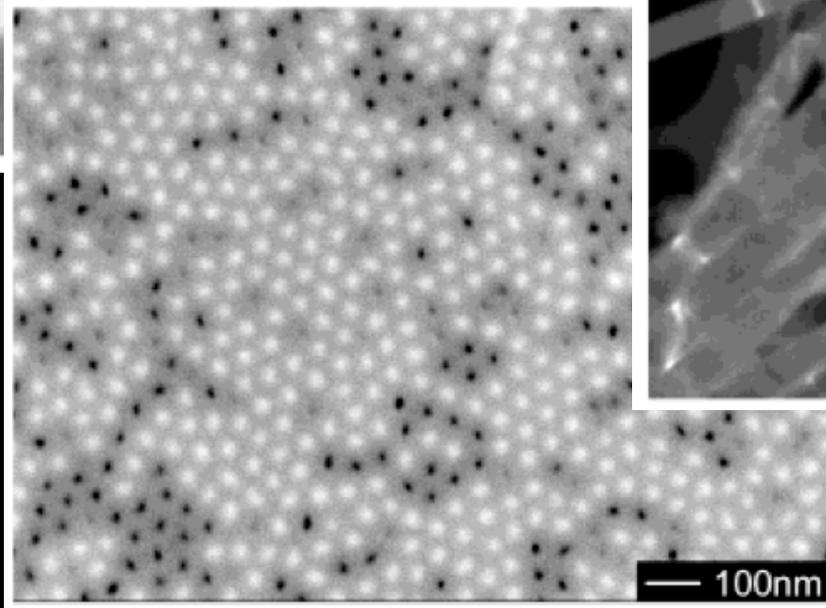
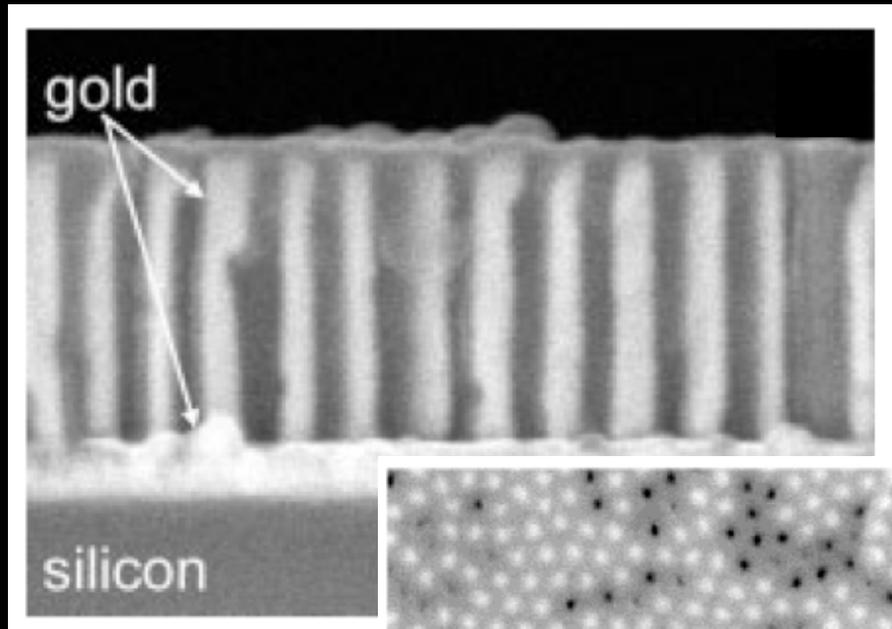
Seebeck ("Direct") Effect

Peltier ("Converse") Effect



$$ZT = \frac{S^2 \sigma}{\kappa_{el} + \kappa_{ph}} T$$

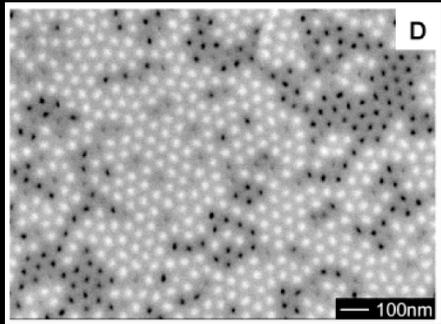
# Nanowire Composites



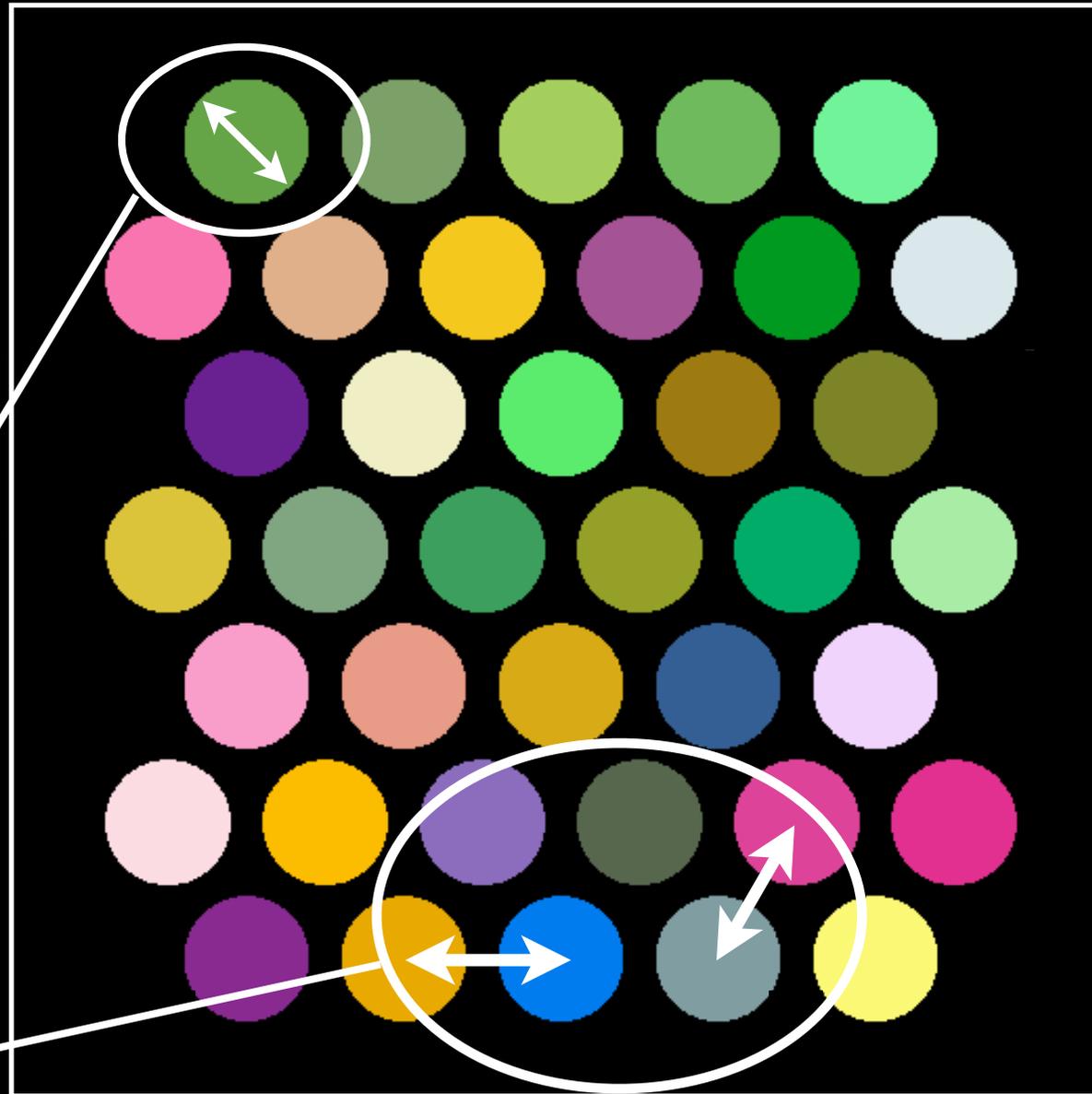
*Sander et al., Chem. Mat., V. 15, 2002*

*Sander, M.S., Tan, L.-S., Advanced Functional Materials 13 (2003) p. 393.*

# Microstructural Effects



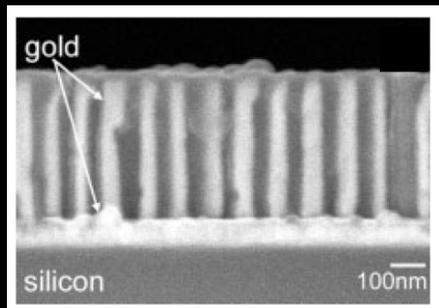
Wire  
diameter



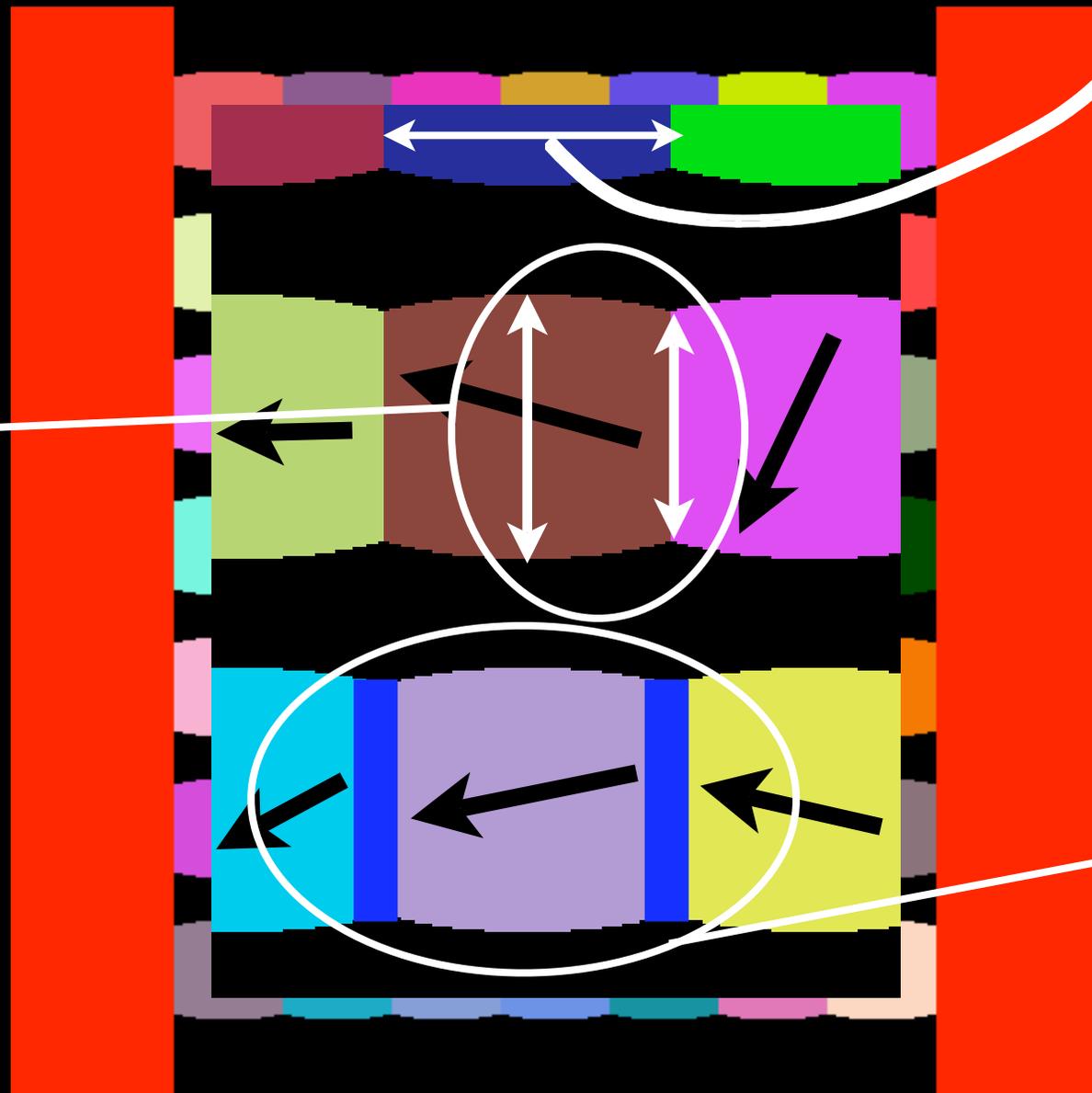
Spacing  
between  
wires

Volume  
fraction of  
nanowire

# Microstructural Effects



Wire diameter



Length of grains

Grain boundaries

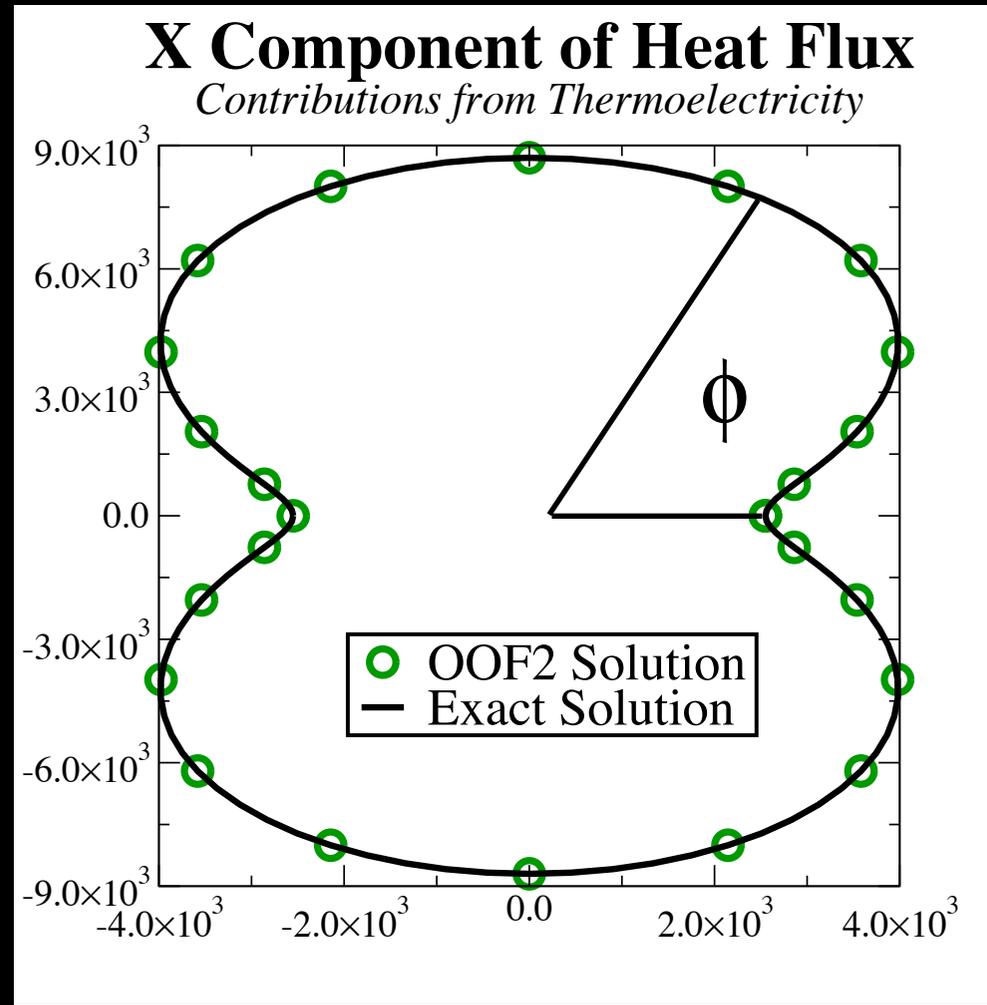
# Extending OOF2

$$C_p \frac{\partial T}{\partial t} = -\nabla \cdot \vec{J}_Q$$

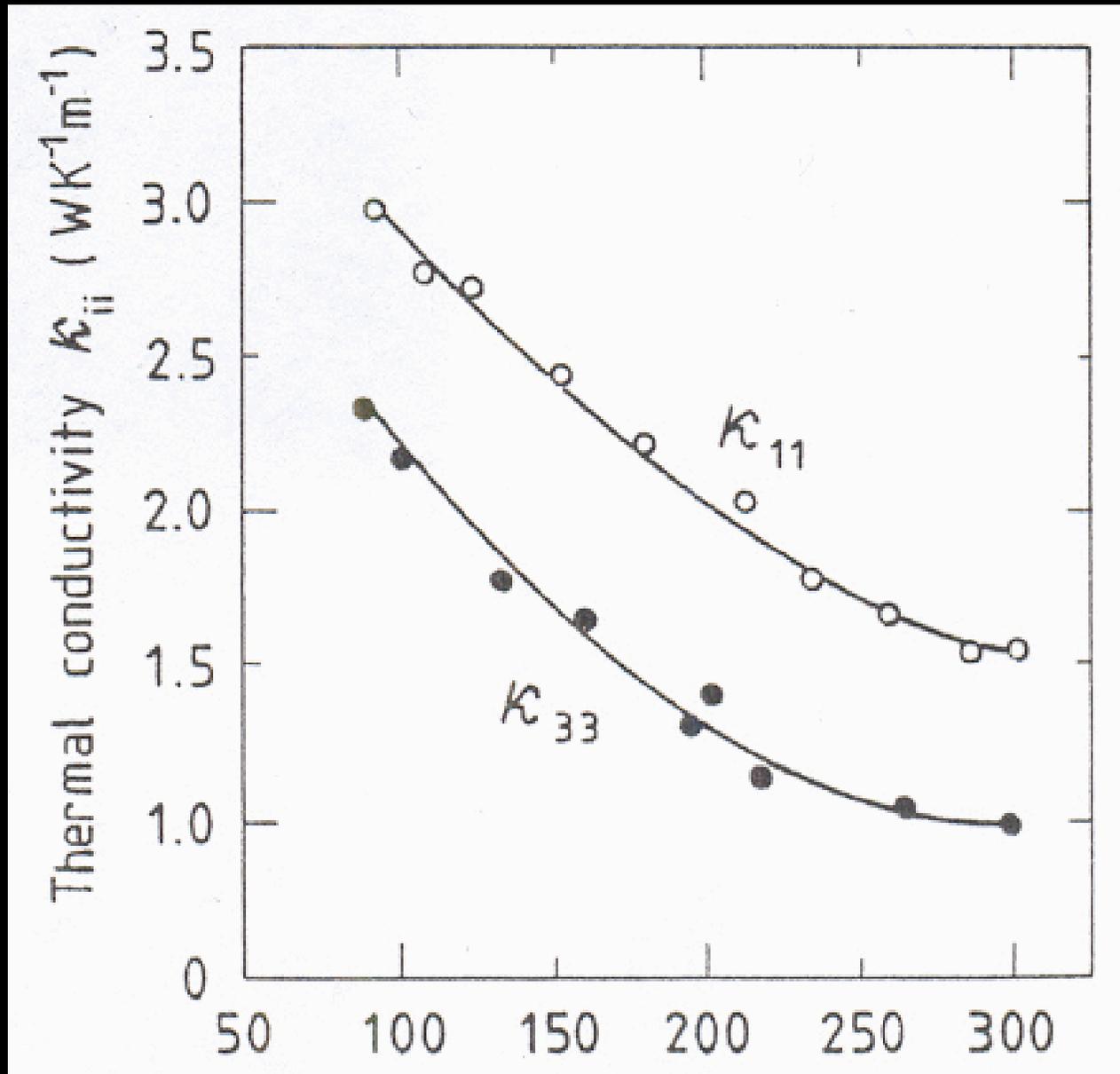
$$\frac{\partial \rho}{\partial t} = -\nabla \cdot \vec{J}_\rho$$

$$\vec{J}_Q = -\overset{\leftrightarrow}{\kappa} \nabla T - T \overset{\leftrightarrow}{L} \nabla \phi$$

$$\vec{J}_\rho = -\overset{\leftrightarrow}{\sigma} \nabla \phi - \overset{\leftrightarrow}{L} \nabla T$$



# Validation of Model

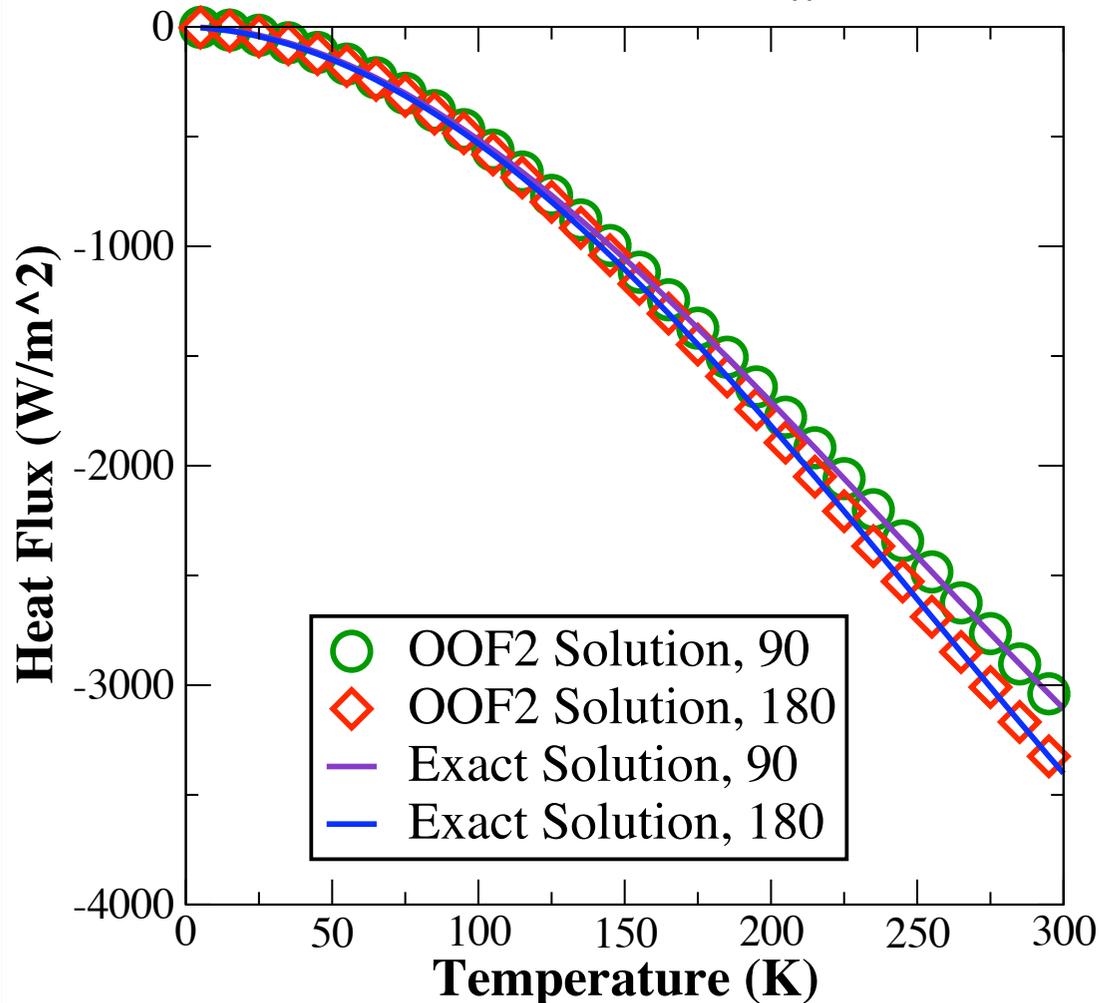


Non-Linear  
Properties for  
Bismuth Telluride

# Validation of Model

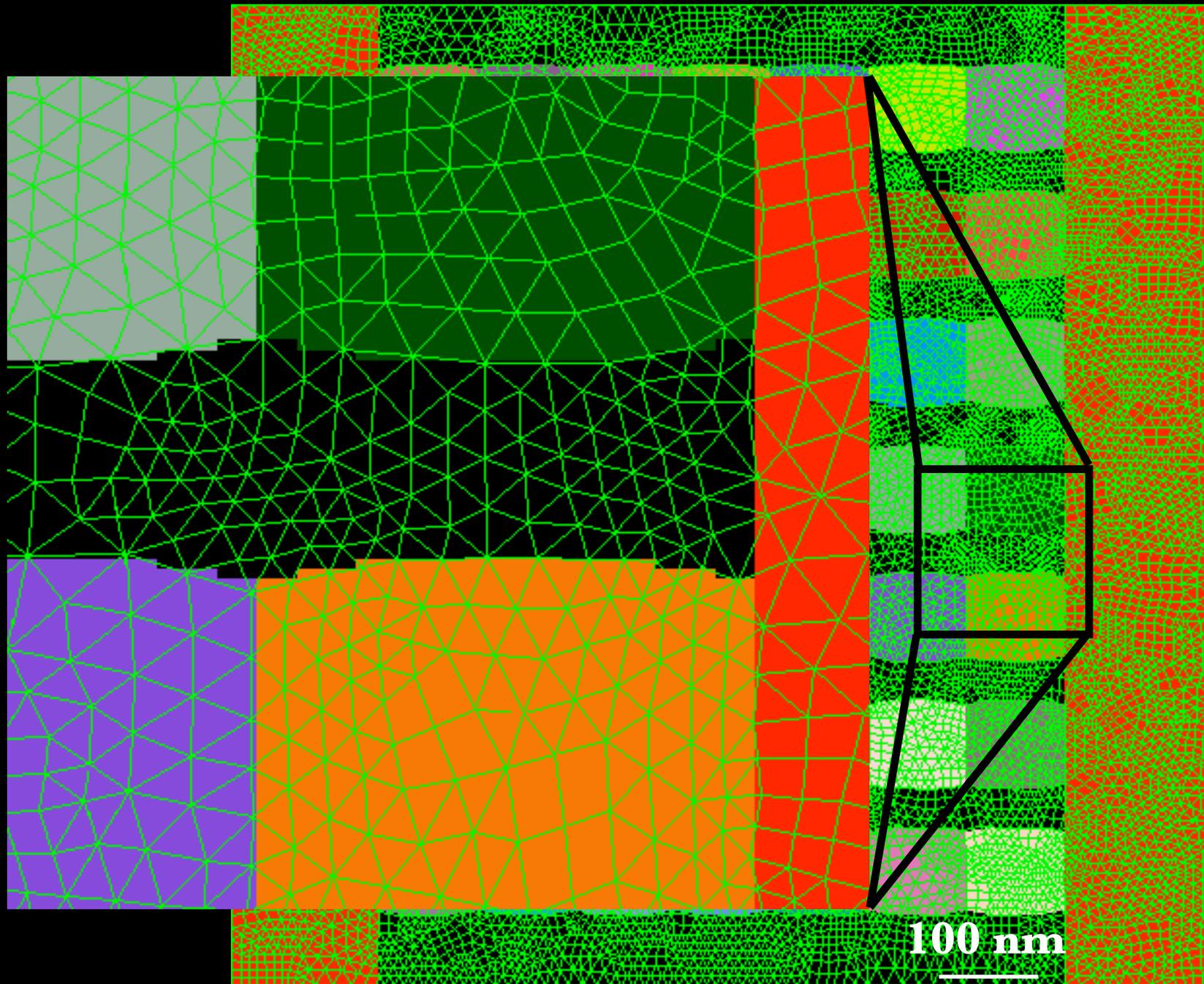
## Heat Flux as a Function of Temperature

*Nonlinear Seebeck Coefficient*



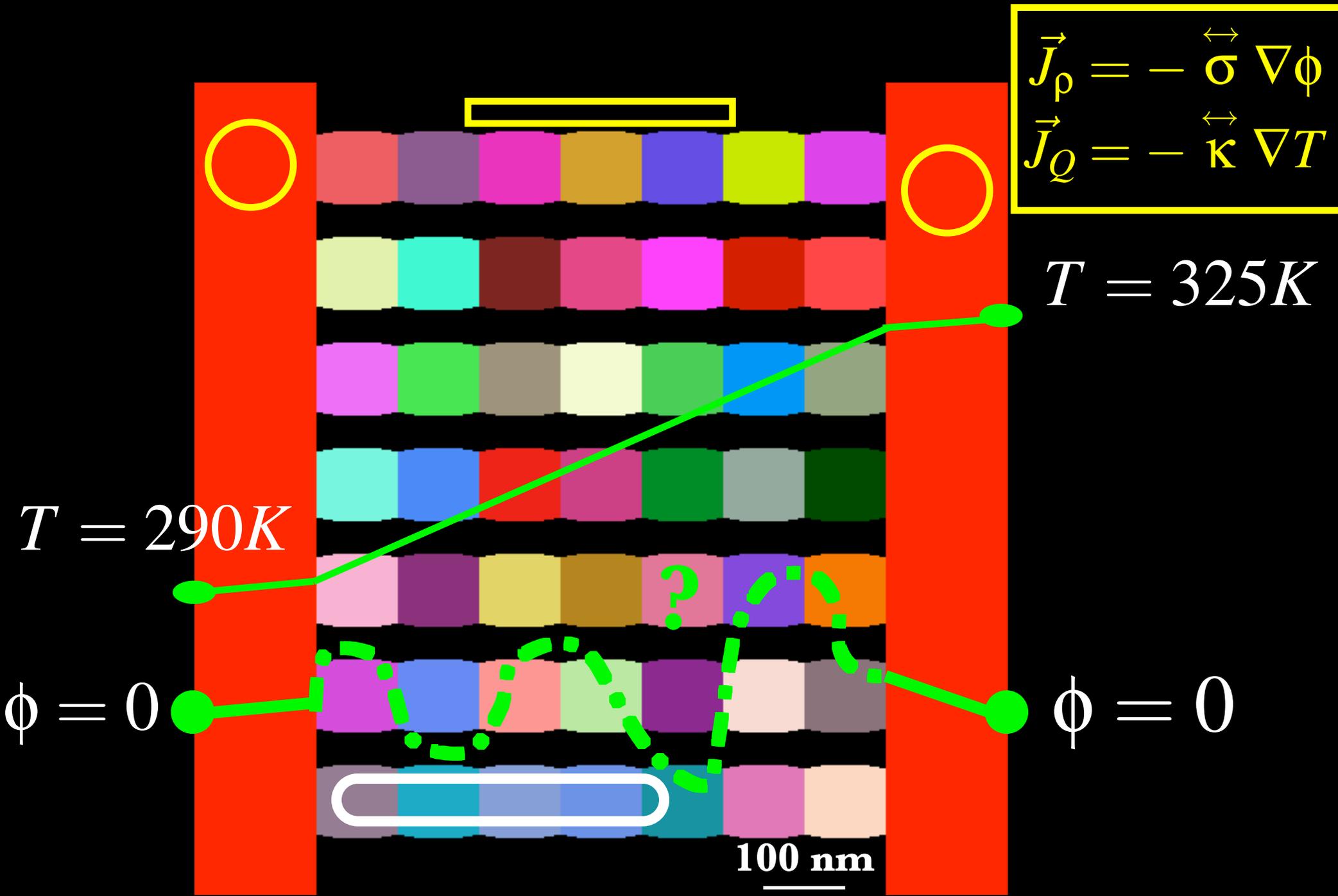
$$J_Q = -\kappa \nabla T - T \cdot L \nabla V$$

Analytical and  
numerical  
solutions differ  
by 1 part per 10  
million



$$\vec{J}_\rho = -\overleftrightarrow{\sigma} \nabla\phi$$

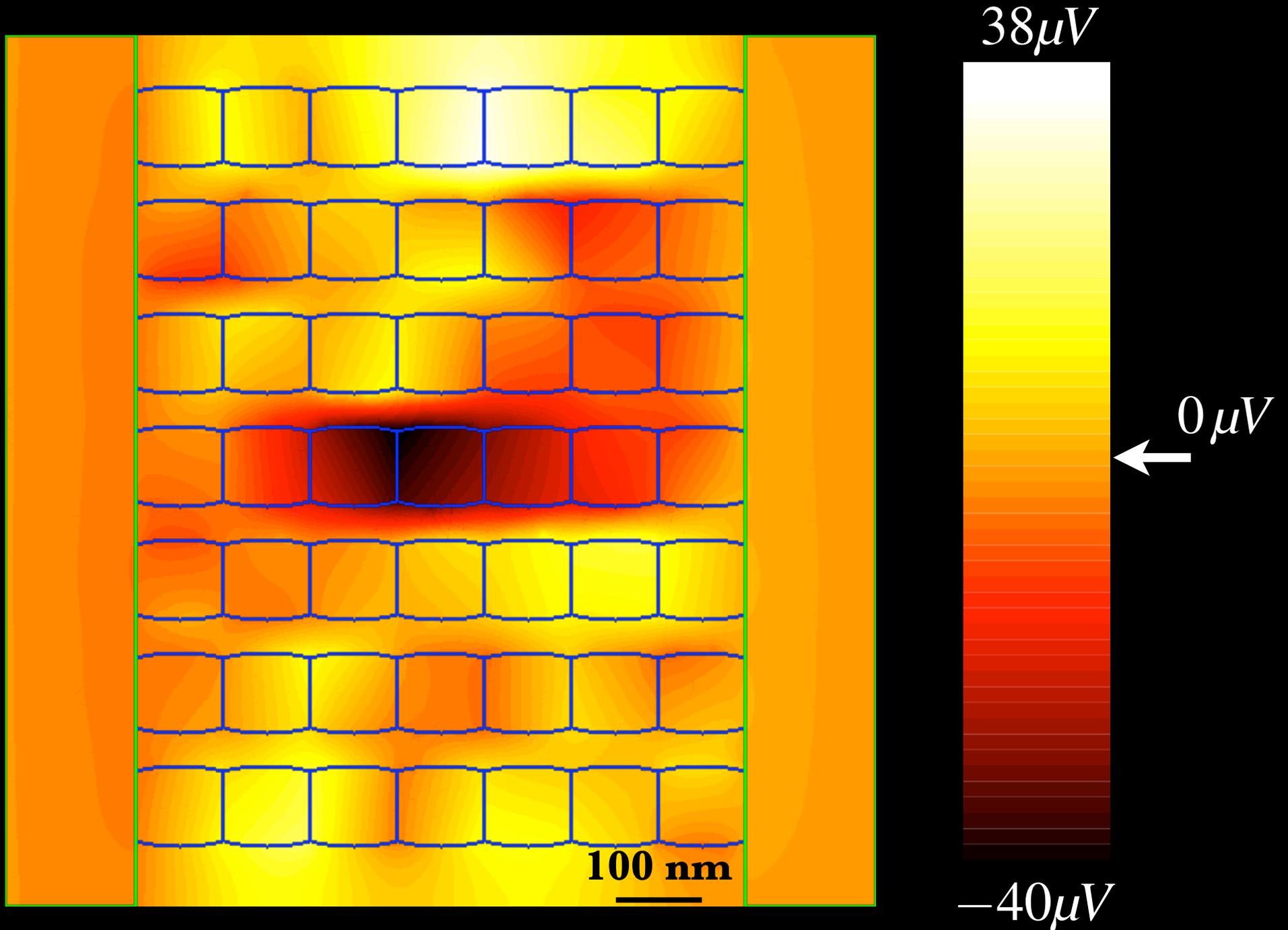
$$\vec{J}_Q = -\overleftrightarrow{\kappa} \nabla T$$



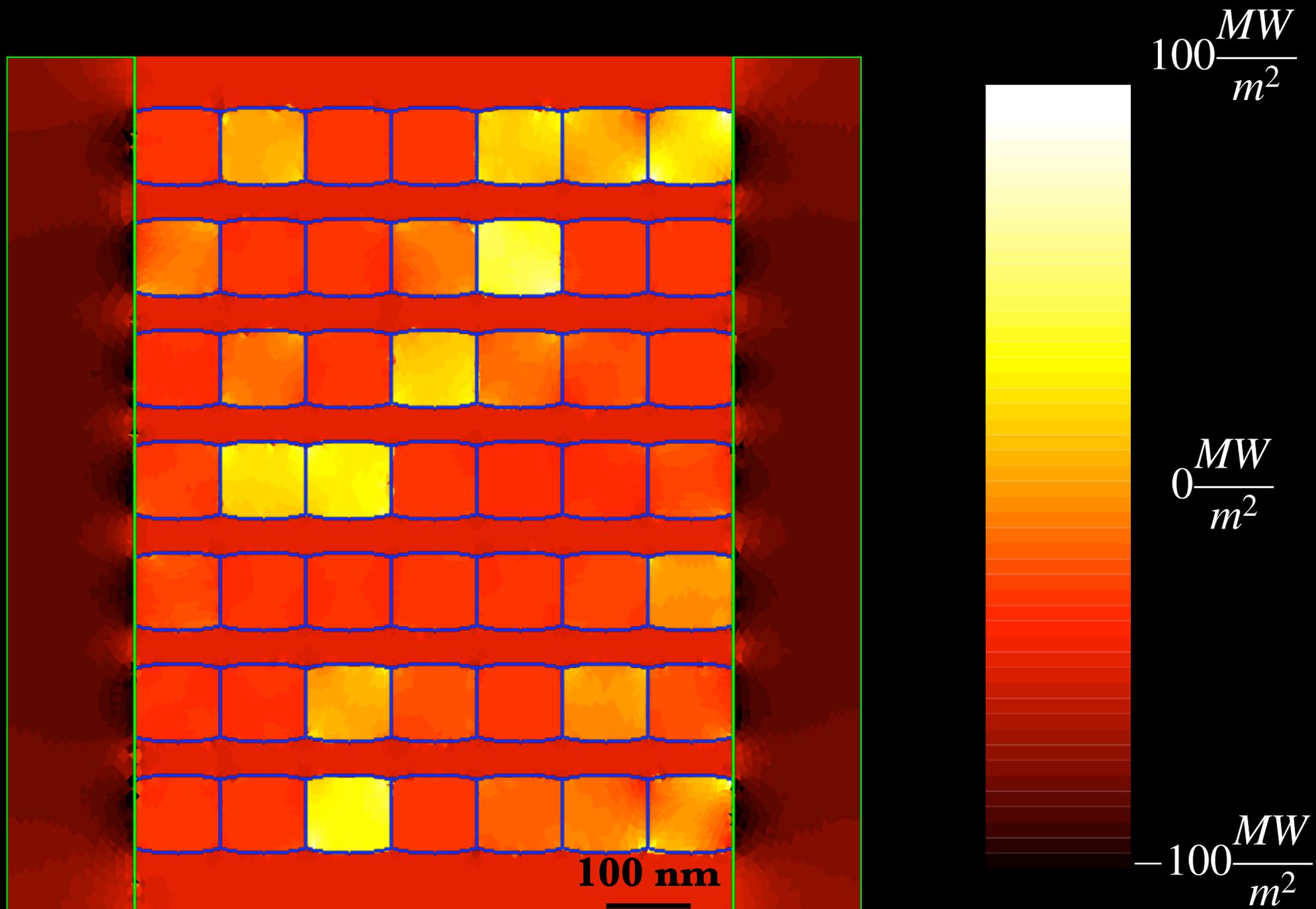
$$\vec{J}_Q = -\overleftrightarrow{\kappa} \nabla T - T \overleftrightarrow{L} \nabla\phi$$

$$\vec{J}_\rho = -\overleftrightarrow{\sigma} \nabla\phi - \overleftrightarrow{L} \nabla T$$

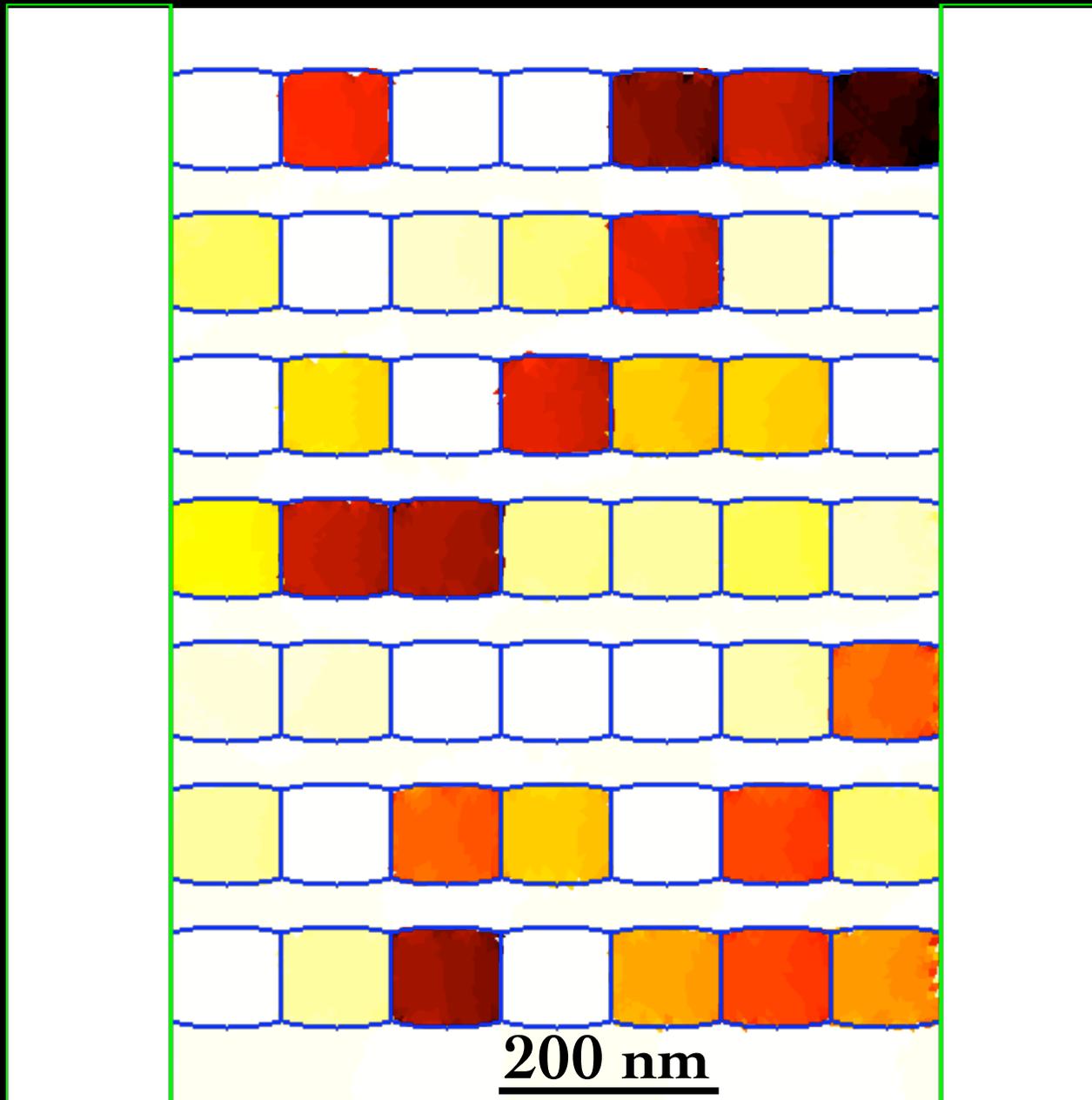
# Voltage Field



# Heat flux in the x direction



# Charge flux in the x direction



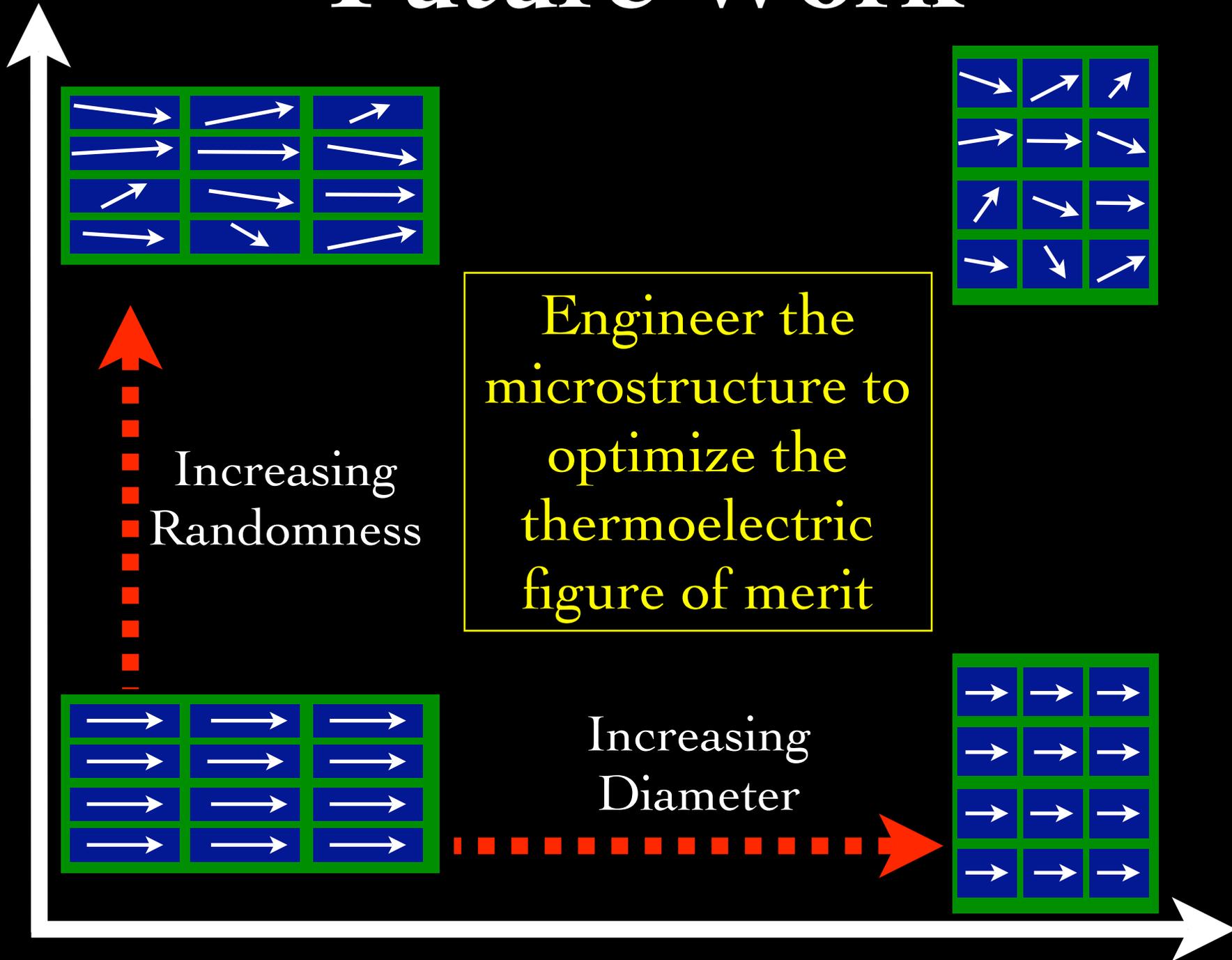
$$0.0 \frac{A}{m^2}$$

$$-1.0 \times 10^{11} \frac{A}{m^2}$$

# Conclusions

- Thermoelectricity induces internal voltages in the composite
- Misorientations at grain boundaries act as sources and sinks of charge carriers
- Grains not perfectly aligned with the fiber axis induce flux in the  $y$  and  $z$  directions
- OOF2 was successfully extended to study the effect of microstructure on thermoelectric nanowire composites

# Future Work

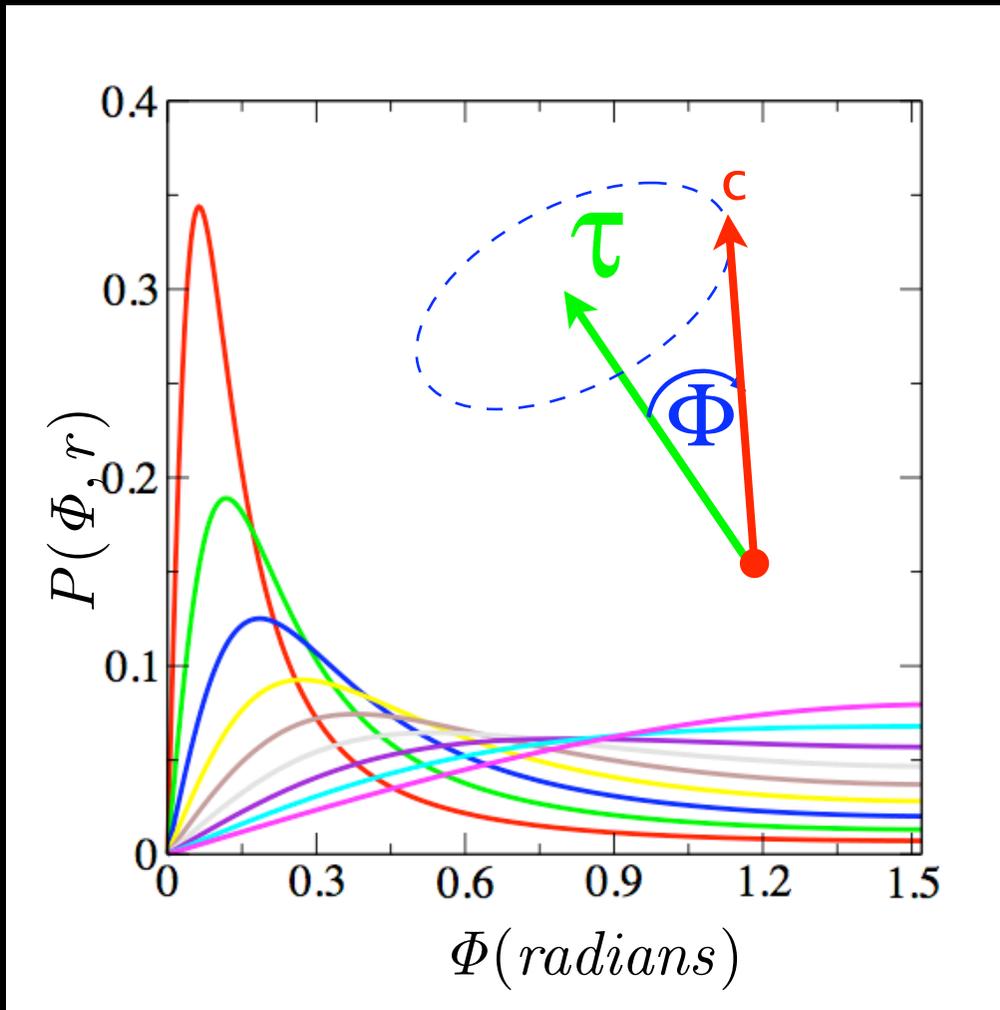
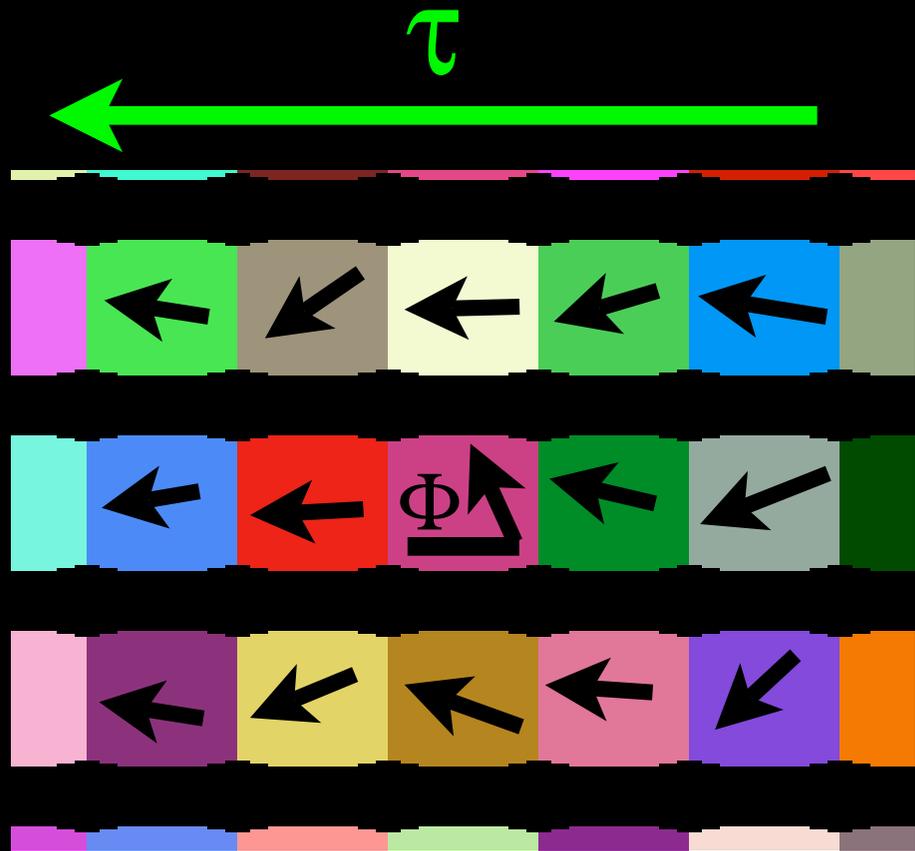


# Questions??

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# Texture Analysis



March Dollase Texture  
Probability Distribution

$$P(r, \Phi) = (r^2 \cos^2 \Phi + r^{-1} \sin^2 \Phi)^{\frac{-3}{2}}$$