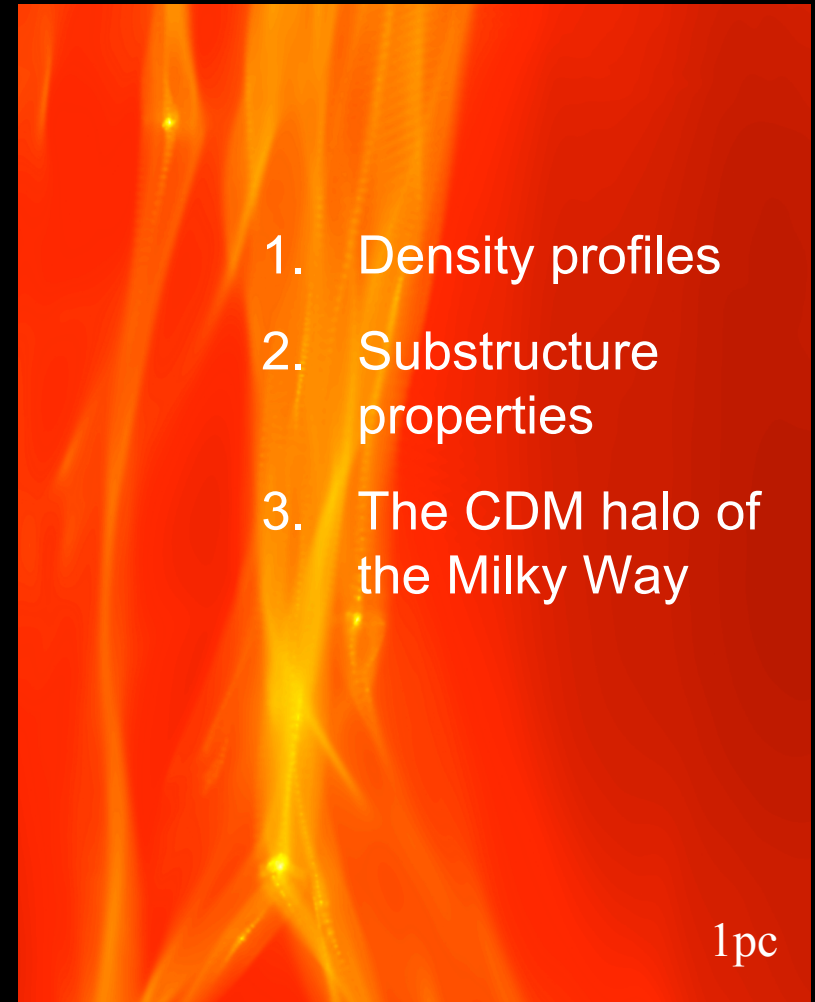
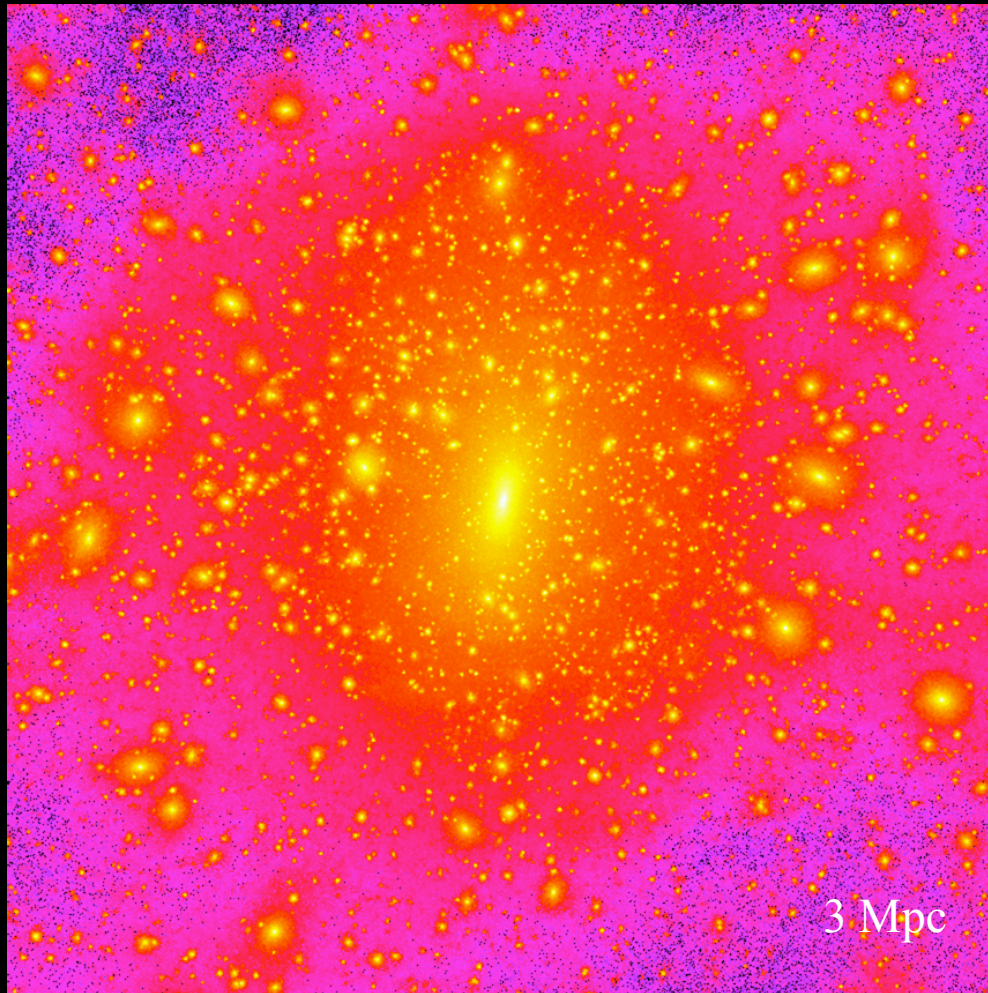


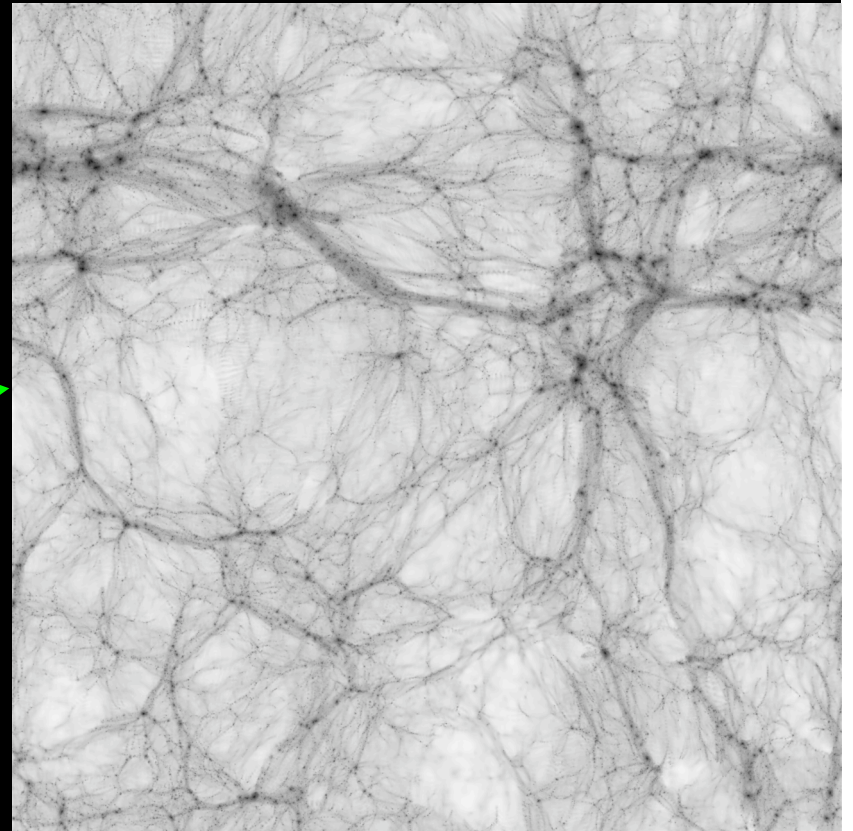
The distribution of cold dark matter in our Galaxy



Jürg Diemand, Piero Madau (UCSC) and
Ben Moore, Joachim Stadel (University of Zurich)

Why Cold Dark Matter ?

- Cluster dynamics (Zwicky ~1930), galaxy dynamics
- BBN, CMB, IaSNe + Cluster abundance
-> non-baryonic dark matter dominates structure formation
- The large scale dark matter distribution of the concordance Λ CDM model agrees well with galaxy surveys (SDSS, 2dF, ...) using plausible recipes to populate halos with galaxies
- ...
- Lyman-alpha forest observations and the early reionisation (1st year WMAP data) favour the concordance Λ CDM model over models with less small scale power (like WDM)
- There is a promising CDM candidate: The neutralino. It would form structures down to 10^{-6} solar mass scales

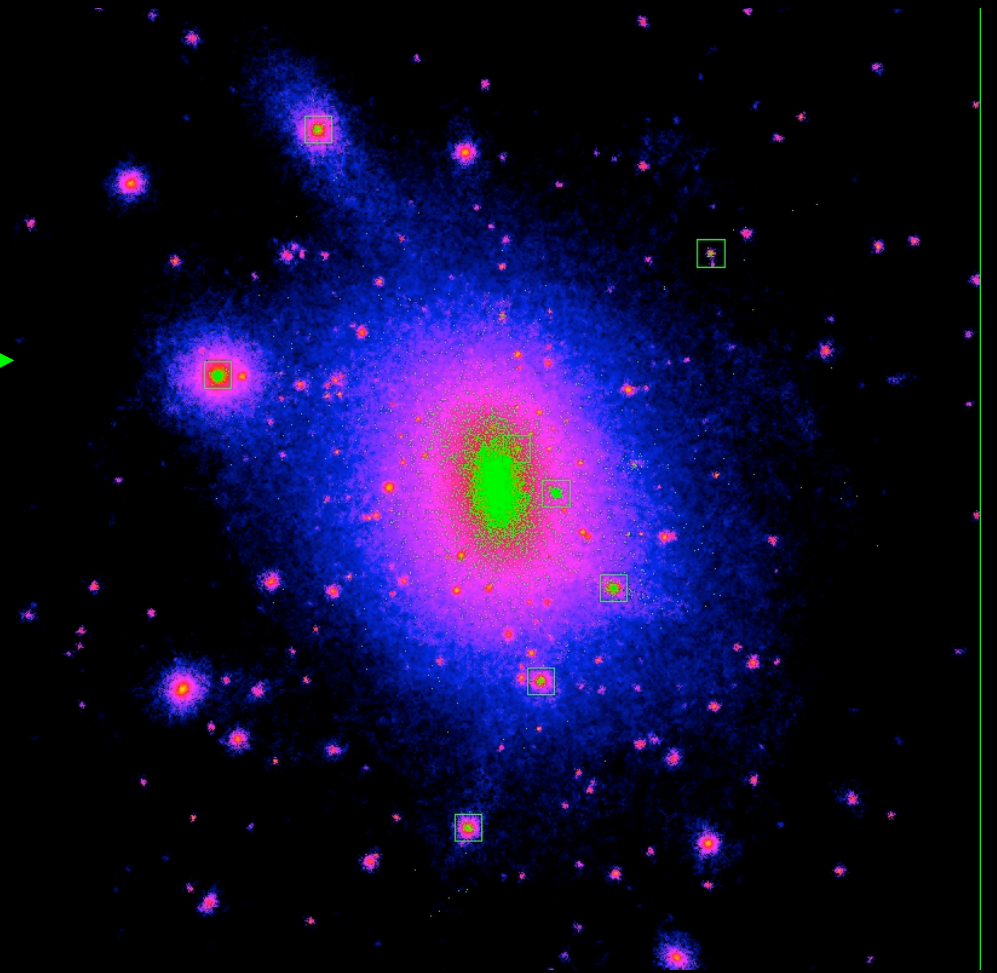


And why not CDM ...?

On smaller scales
(i.e. inside the halos)
there could be problems with
CDM:

- a) too much substructure →
- b) too steep density profiles
- c) angular momentum distribution

But all three points depend
enough on complicated, not well
understood and modelled gas-
physics to leave hope for
reconciliation.



This talk: Halo structure in a CDM only Universe

Well defined problem (no free parameters),
well suited for numerical simulation.

Simulations have revealed much about DM halo structure,
some open questions remain:

- Density profile within 1% of the virial radius:
Singular ('cuspy') or approaching a constant density core?
- Subhalo inner structure, abundance, spatial & velocity distribution?
- Local dark matter distribution in real- and phase-space?

CAUTION:

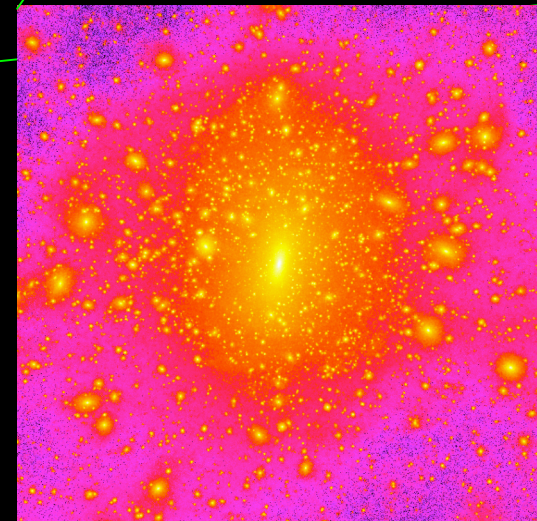
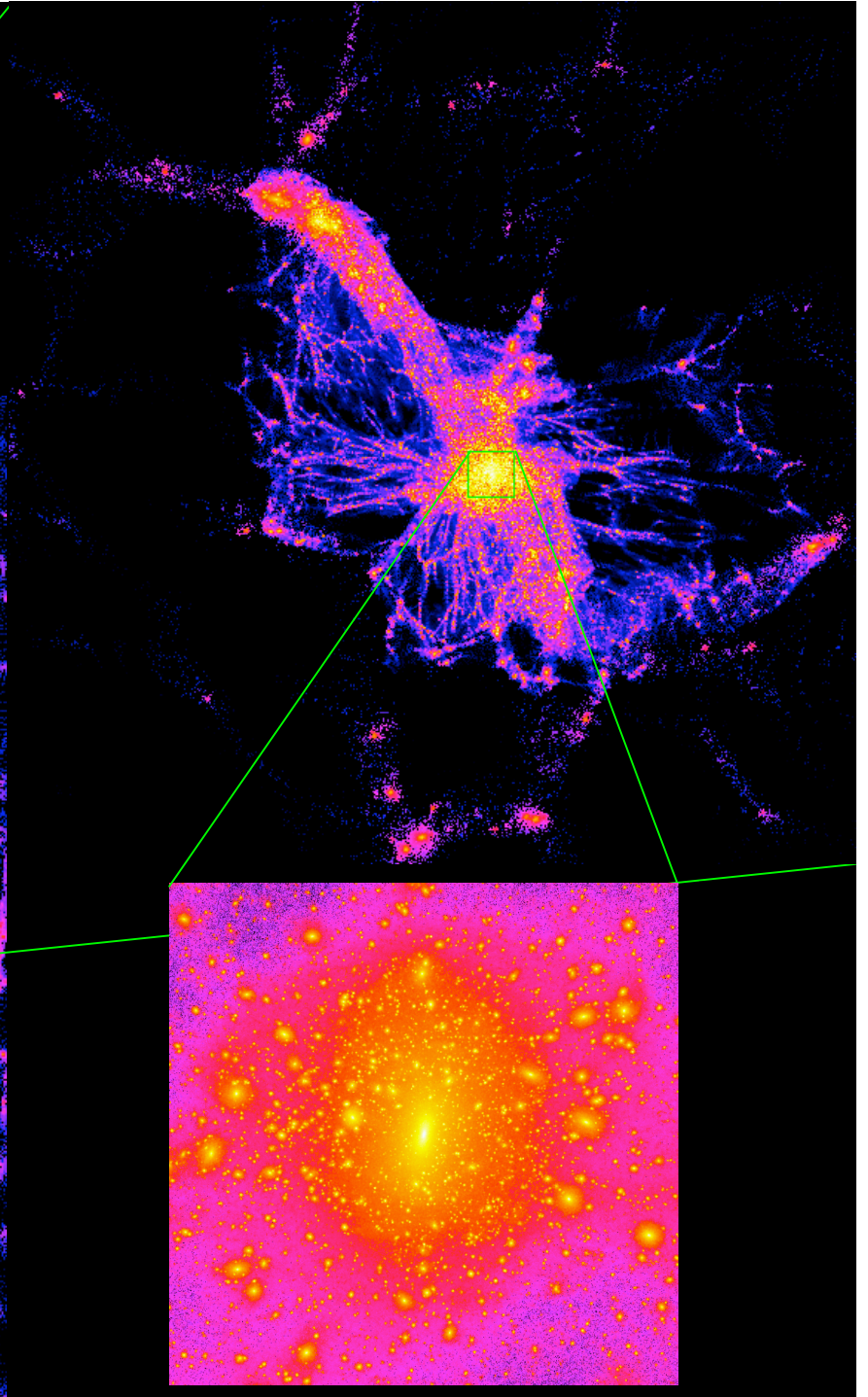
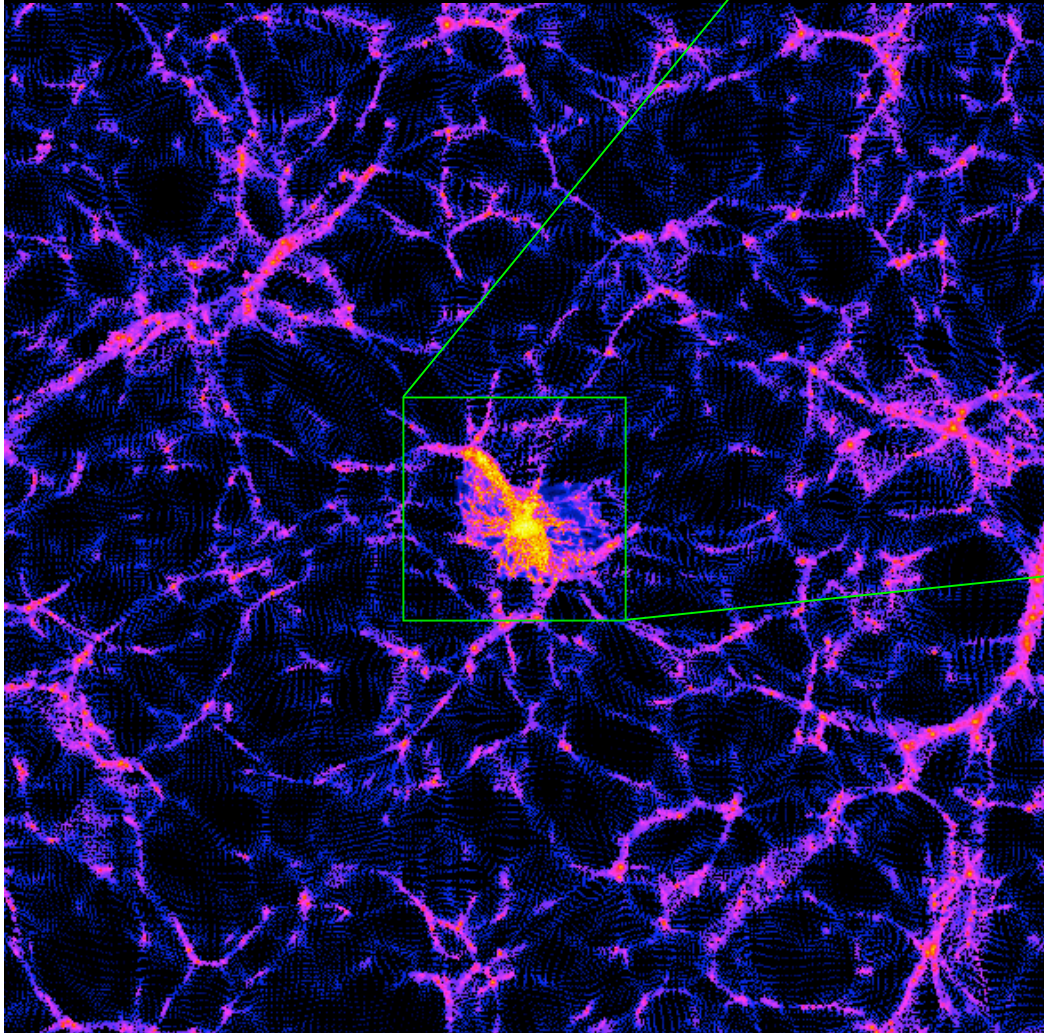
Only some of these results can be applied directly to the real Universe

Method : Cosmological N-body simulations

- Cosmological initial conditions for a LambdaCDM Universe (0.27, 0.73) realised with particles displaced from cubic grid positions using GRAFICS by E. Bertschinger
- Solve (softened) gravitational interactions between these particles with PKDGRAV by J. Stadel & T. Quinn
- Limitation : Finite resolution leads to:
 - > flatter inner density profiles due to numerical relaxation
(JD et al. MNRAS, 348, 977, 2004)
 - > numerical overmerging (halos appear too smooth)
(Moore et al. ApJ, 457, 455, 1996)

High resolution clusters

Refinement (or 'Zoom'):
Resimulating halos with better
mass resolution

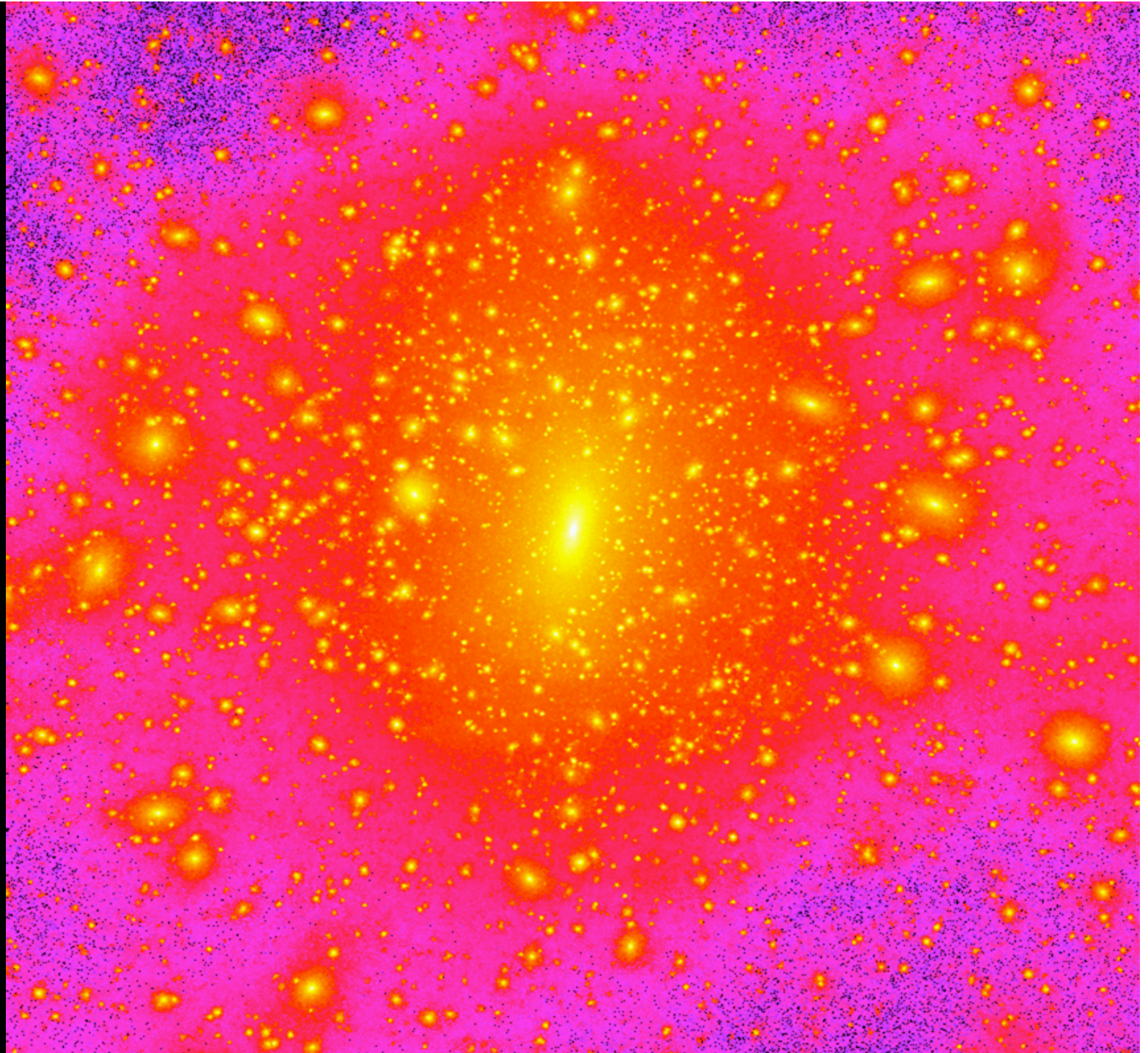


Highest
resolution
numerical
simulations
of the
structure of
dark matter
halos

10^5 steps

10^8 particles
(25 million
inside the
virial radius)

High mass
and force
resolution



Formation of a CDM cluster

movies are available at www.nbody.net

$R = 6.0 \text{ Mpc}$

$z = 10.155$



$a = 0.090$

diemand 2003

Now running:
A galaxy halo
with
 $N_{\text{vir}} = 130$ million

Here only half of
the virial radius at
 $z=0.5$ is shown

In total this run
will take about
300'000 CPU
hours
on NASA's
Columbia
Supercomputer



CDM density profiles: adiabatic contraction

The baryons cool and go into the inner region of the halo where the galaxy forms

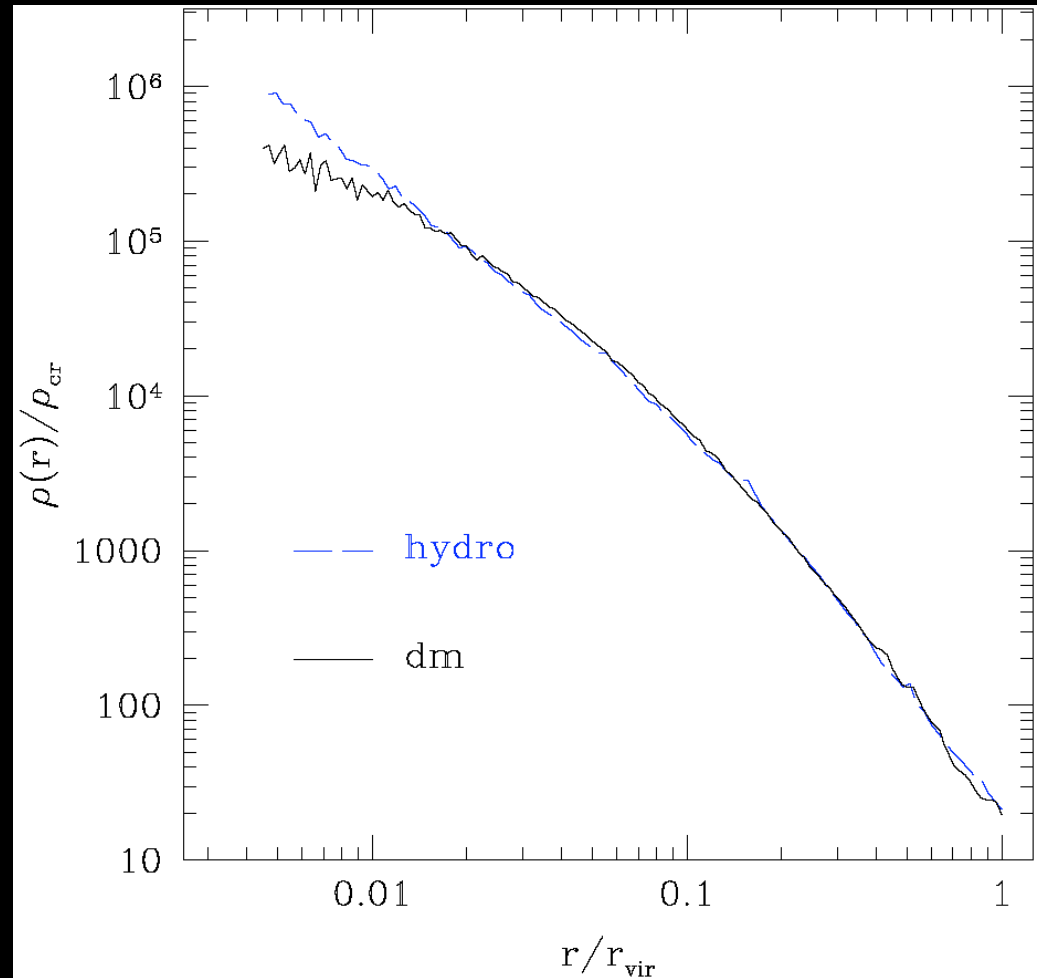
The dark matter contracts in response to the deepening potential well, the DM profile becomes steeper

This greatly increases the expected DM annihilation signal from the Galactic centre (Prada et al, PRL, 2005)

The slope of their final DM cusp (-1.4 to -1.9) depends on the assumed DM only profile (-1 to -1.5)



-> How steep are DM only inner density profiles?



Maccio et al. astro-ph/0506125

1) CDM density profiles: adiabatic contraction

The baryons cool and go into the inner region of the halo where the galaxy forms

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The slope of their final DM cusp (-1.4 to -1.9) depends on the assumed DM only profile (-1 to -1.5)



Substructure inner profiles resemble those of field halos (Kazantzidis et al., ApJ, 608,663,2004)

Most of them are dark matter dominated (dwarf galaxies, dark DM satellites)

-> little or no adiabatic contraction

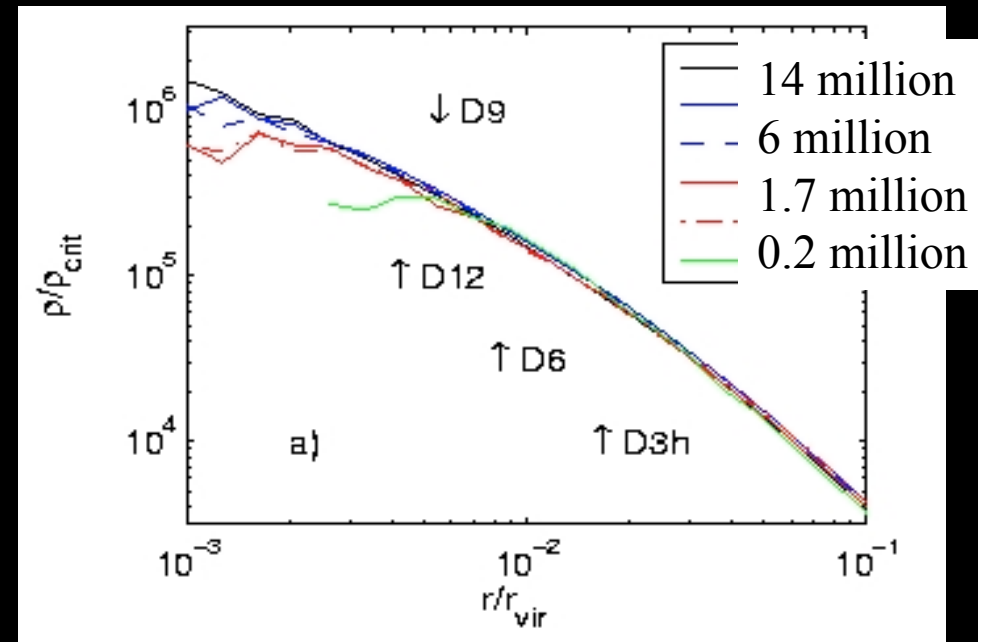
-> **How steep are DM only inner density profiles?**



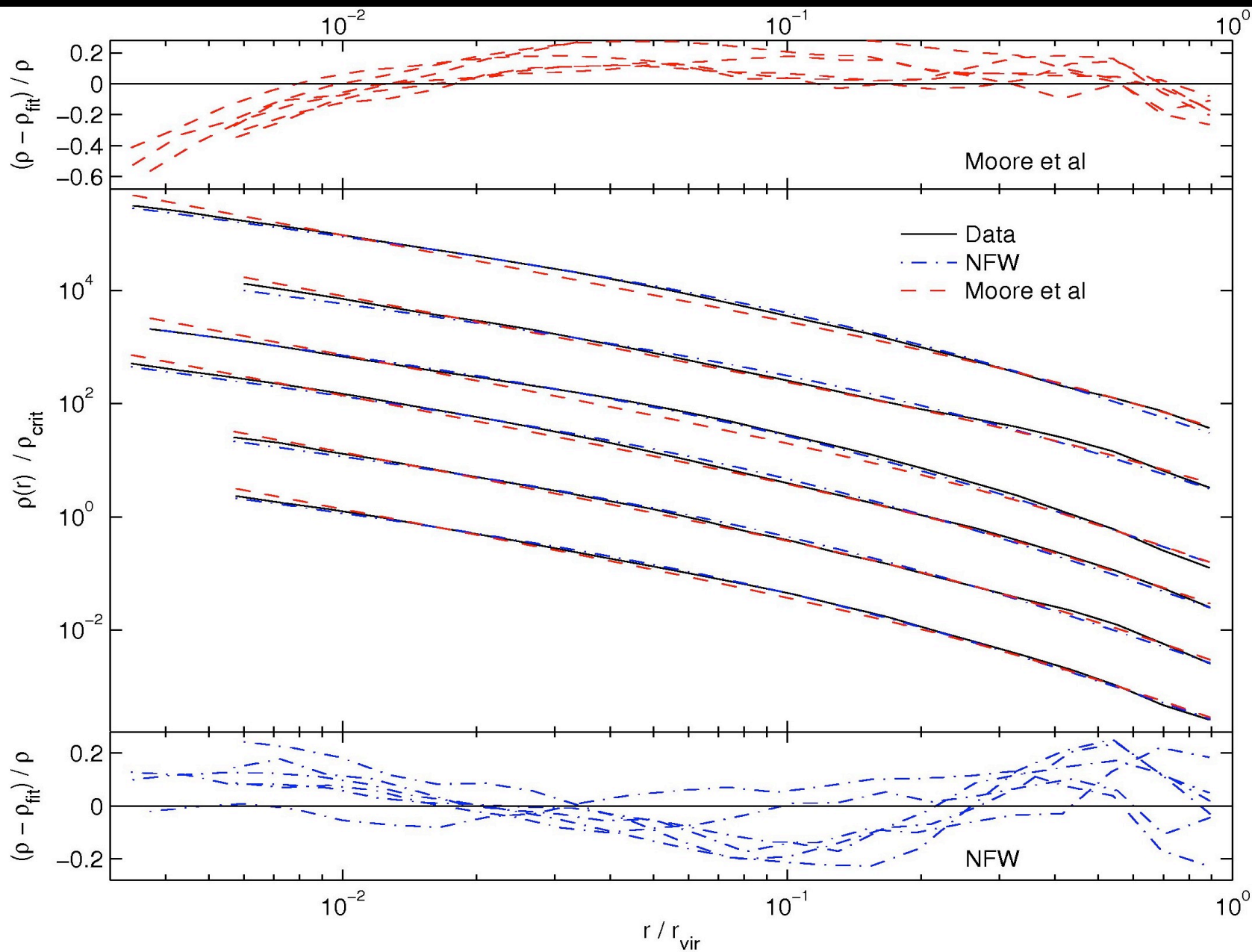
CDM density profiles: convergence tests

- Numerical flattening due to two body relaxation:
slow convergence, $r \sim N^{-1/3}$
1 million to resolve 1% of R_{virial} ,
1000 to resolve 10%

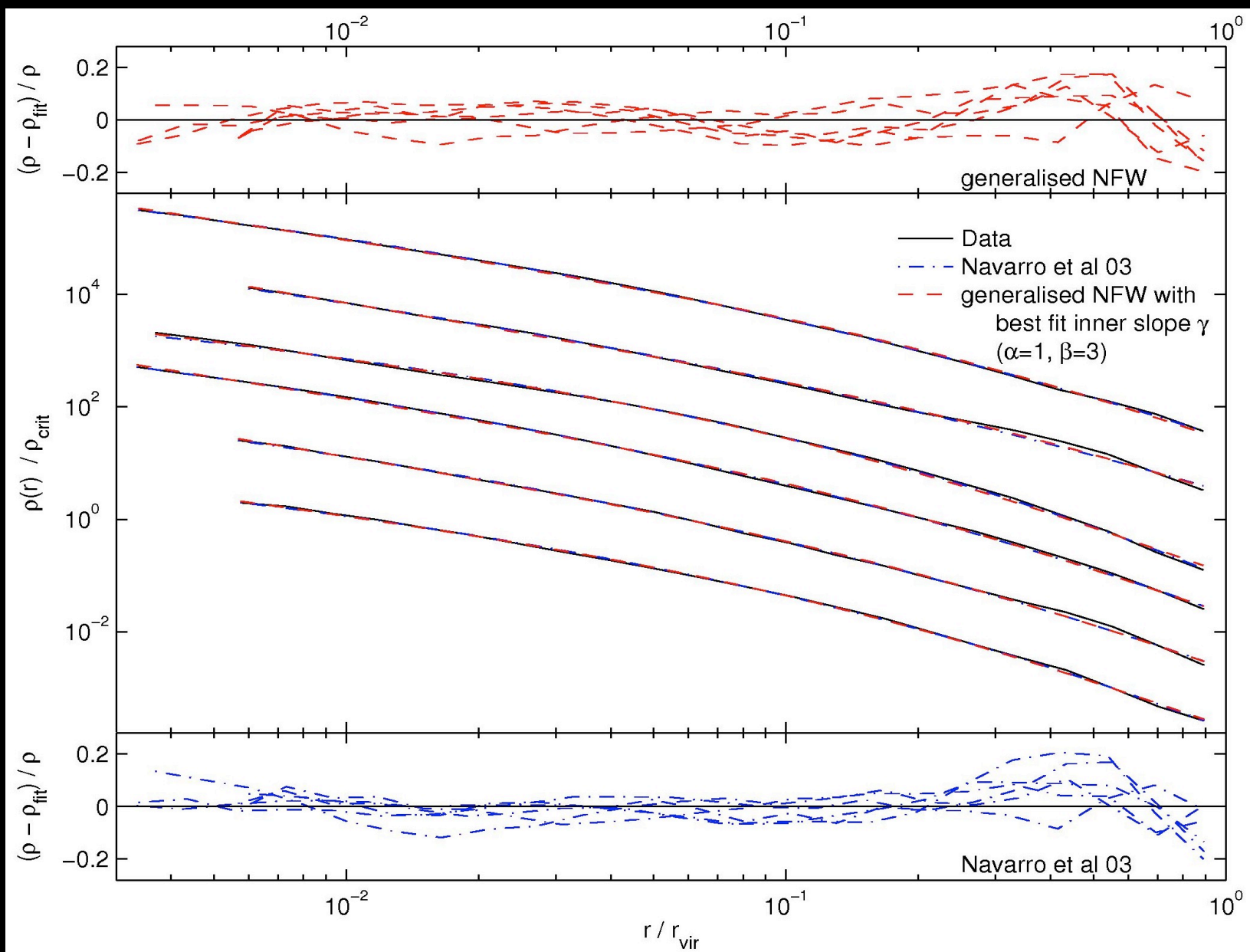
(JD et al. MNRAS, 353, 624, 2004)



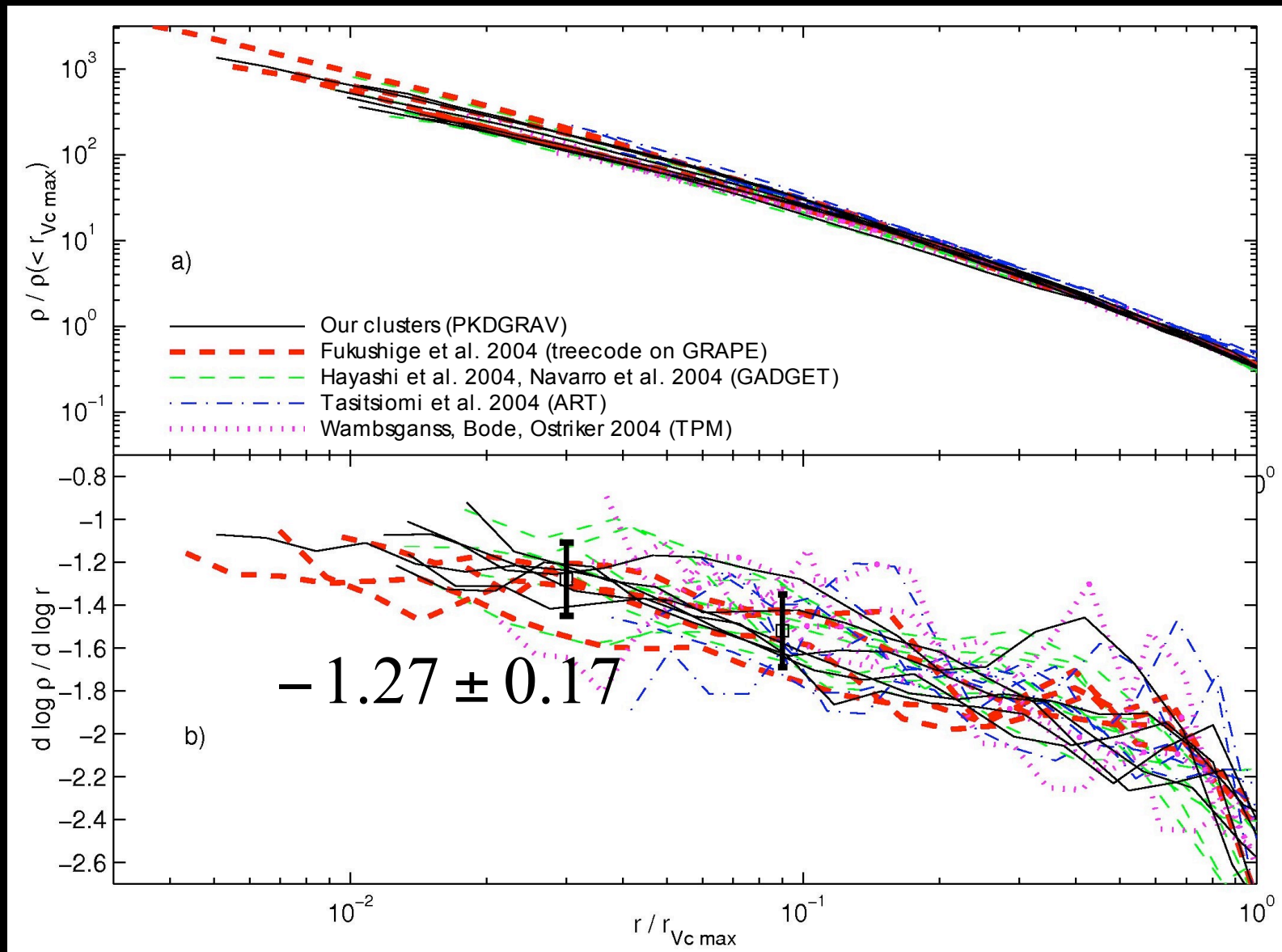
CDM cluster density profiles



CDM cluster density profiles



CDM cluster density profiles



CDM halo profiles

- Agreement among simulators. 5 different groups using different codes and initial conditions.
- Generalized NFW profiles with inner slopes of -1.2 ± 0.14 fit our 6 cluster profiles very well.
- Cored or cusped in the center? Still open at this resolution... (of up to 25 million inside R_{vir})

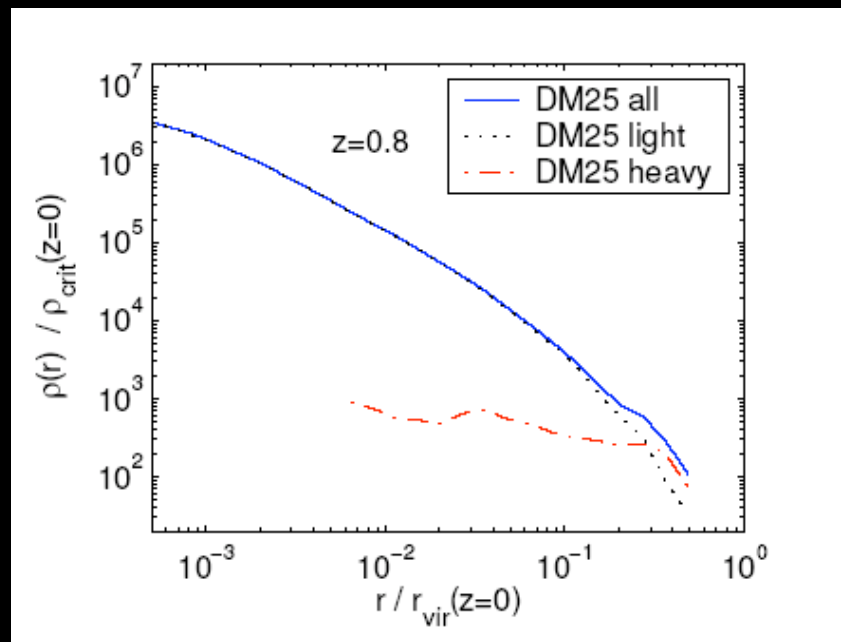
Resolving the inner halo with a multimass approach

Reducing the high resolution region to the core forming part can reduce the CPU time by more than a factor of 10 !

Now we have also heavier particles inside of the halo. They need to have large force softenings ($\sim 0.01 r_{\text{vir}}$) to avoid mass segregation.

Multimass approach reproduces the density profile for the 6 million particles cluster:

(JD, et al. astro-ph/0504215)



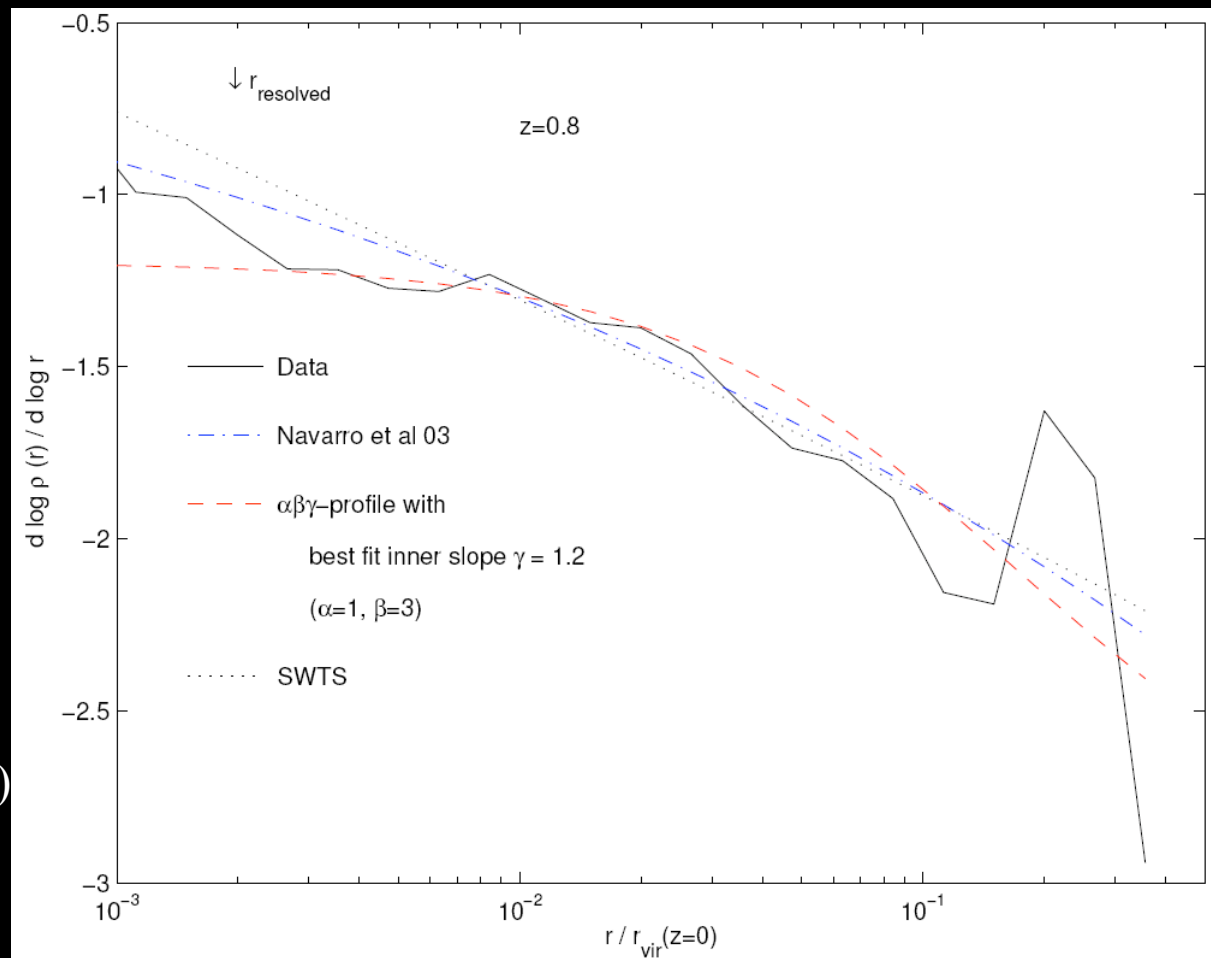
Resolving the inner halo with a multimass approach

Run DM25: effective resolution of 130 million particles in R_{vir} ,
run down to $z=0.8$

logarithmic slope:

-> indicates that
cuspy profiles
describe the
very inner part
better

(JD et al. astro-ph/0504215)



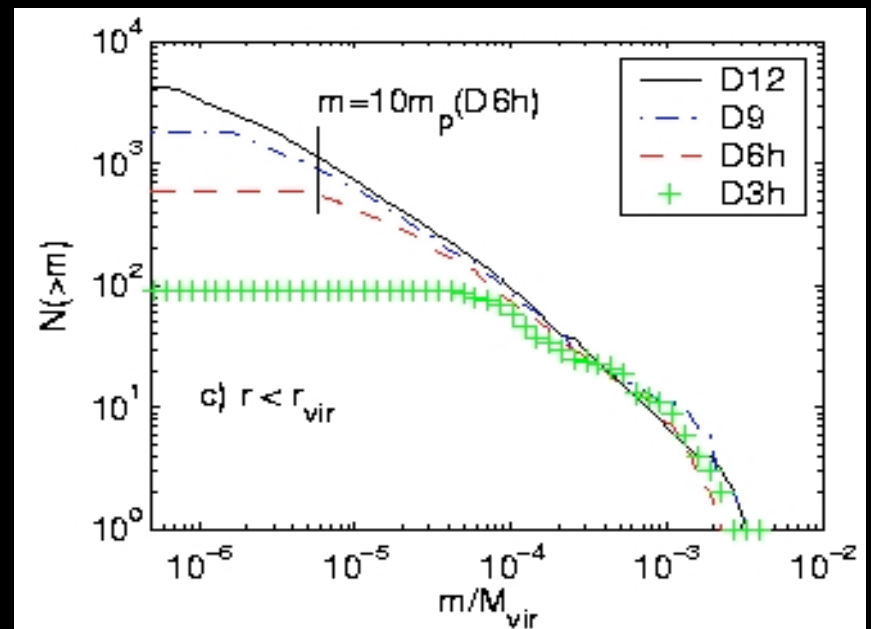
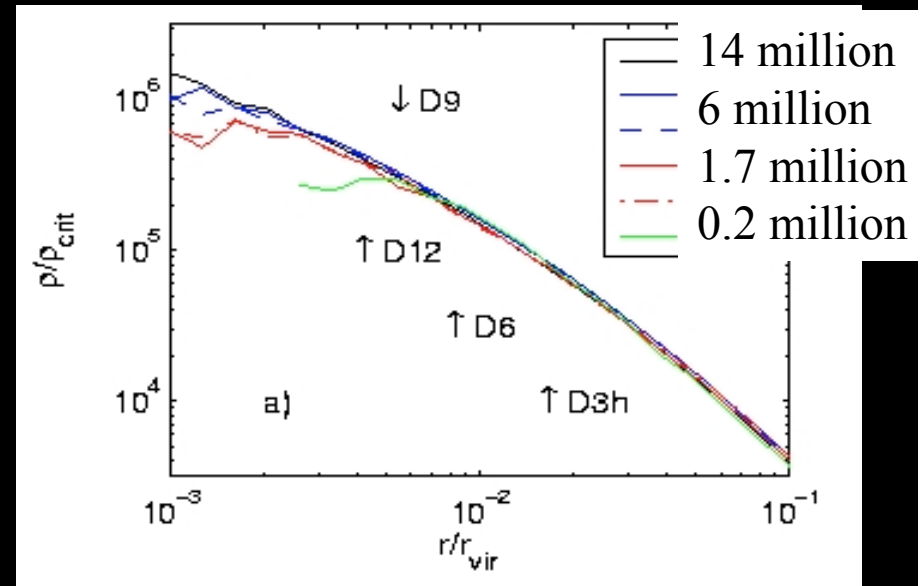
2) Substructure: Convergence tests

- Numerical flattening due to two body relaxation:
slow convergence, $r \sim N^{-1/3}$
1 million to resolve 1% of R_{virial} ,
1000 to resolve 10%

(Moore et al. ApJ 1998; JD et al. MNRAS 2004)

- Numerical Overmerging:
=> incomplete subhalo sample for $N < 100$

(JD et al. MNRAS, 352, 535, 2004)

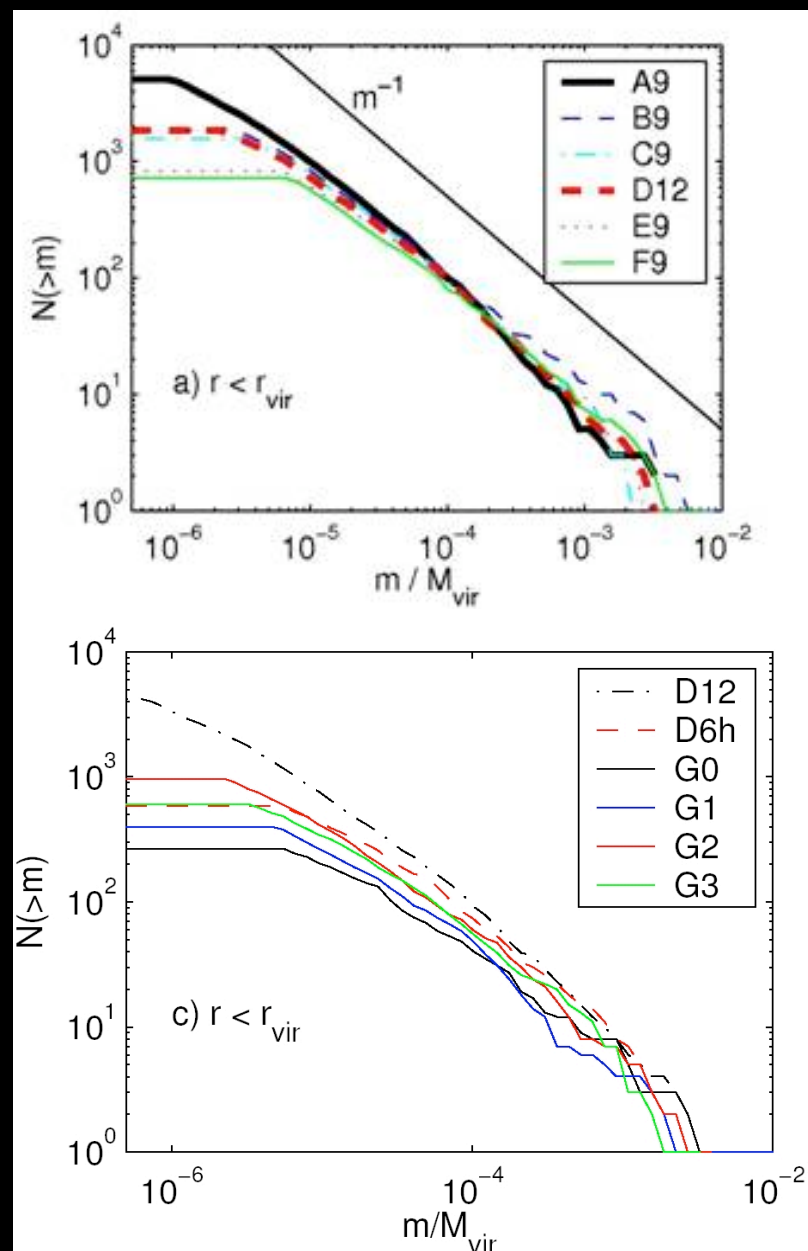


Substructure abundance

Steep cumulative mass functions,
close to $N(>m) \sim m^{-1}$

The absolute $z=0$ abundance depends
on the host mass, galaxies have about
a factor of 2 less substructure.
(Gao et al. 2004)

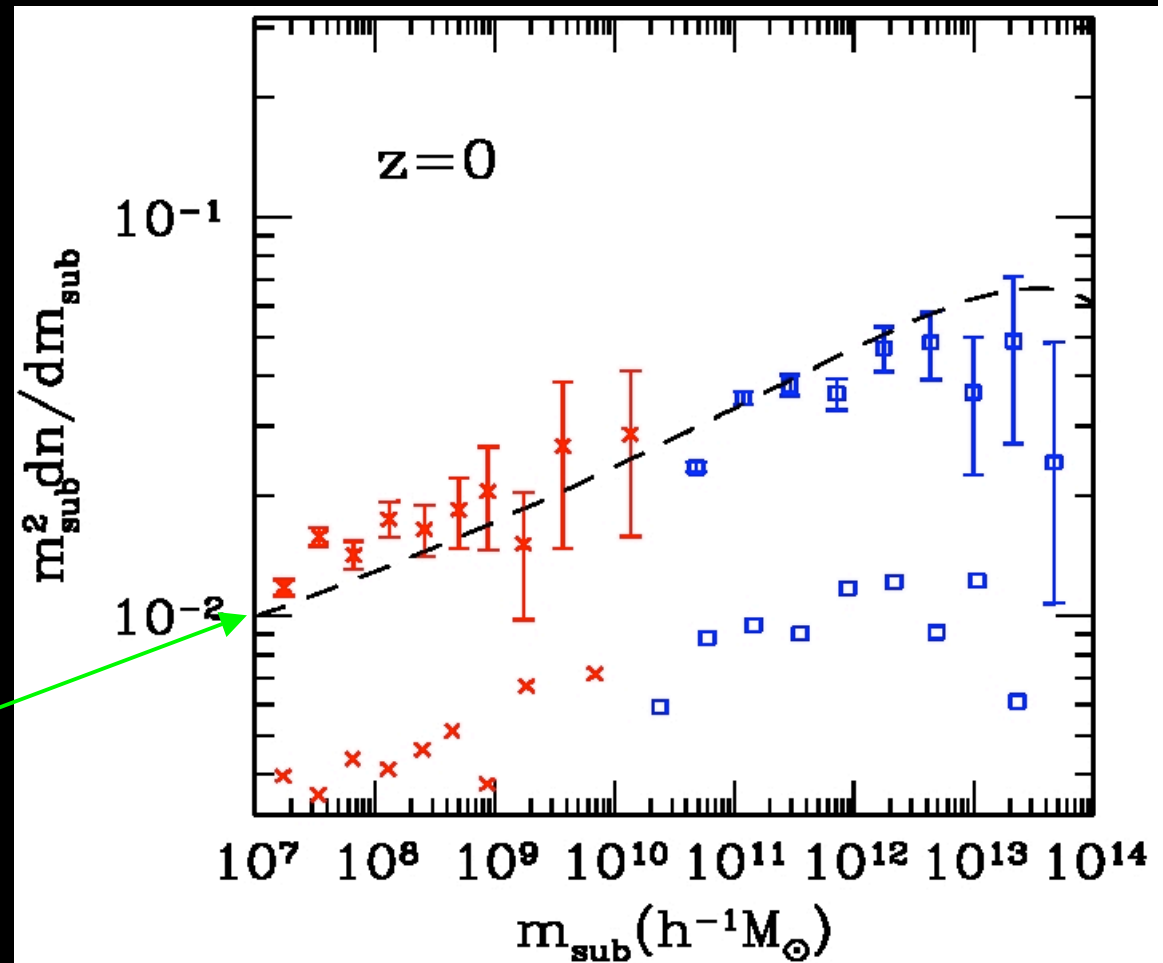
Hosts of equal similar age and
concentration are expected to have
similar subhalo abundances.



Substructure abundance

Abundance per unit host mass is independent of the host mass
(Kravtsov et al 2004;
Gao et al. 2004)

And similar to field halo mass function



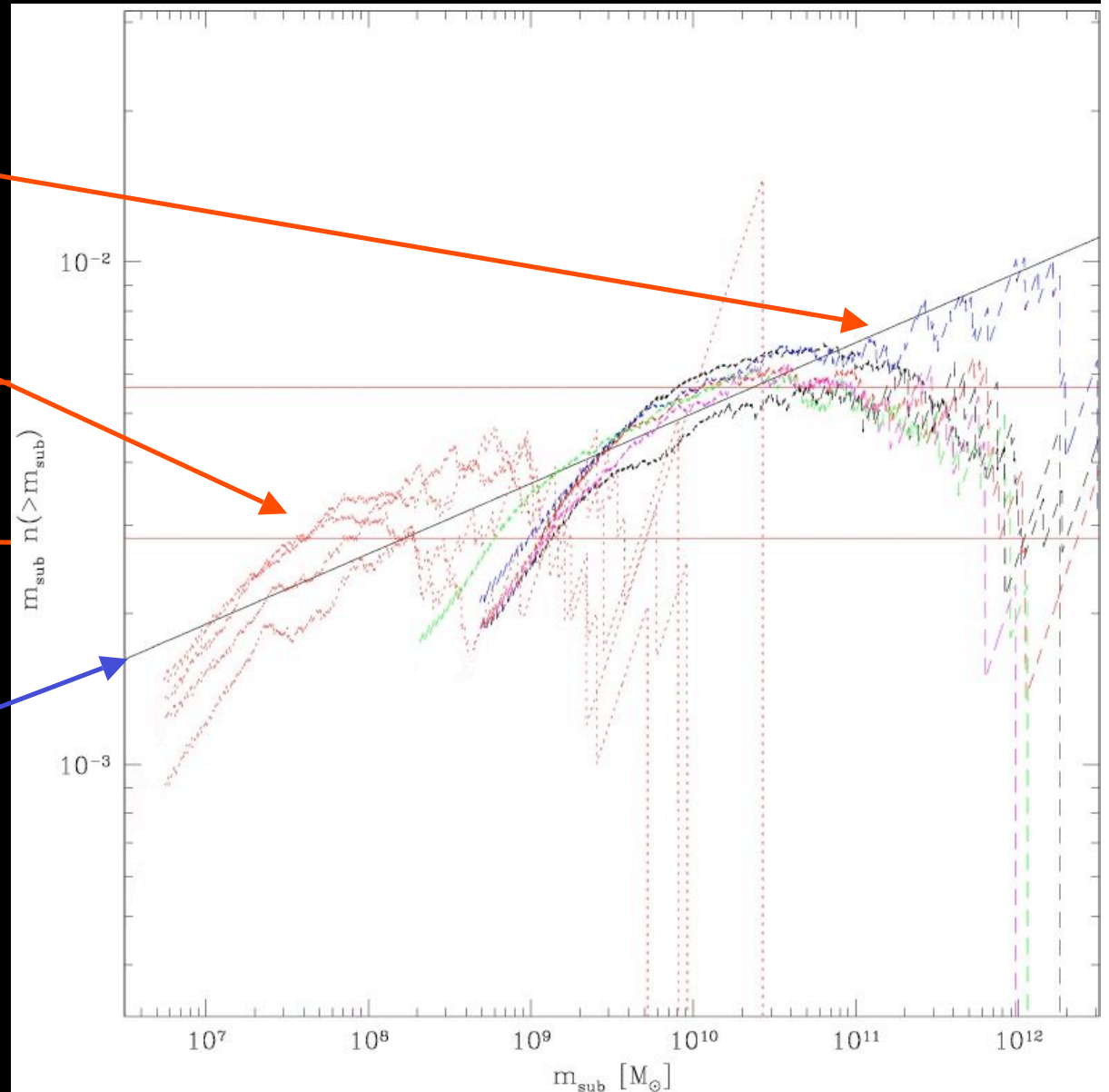
From Gao et al., MNRAS, 2004

Substructure abundance

Same result from our
six clusters
and
four galaxies

factor of two between
galaxies and clusters

$$dn/dm \sim m^{-1.86}$$



Substructure abundance

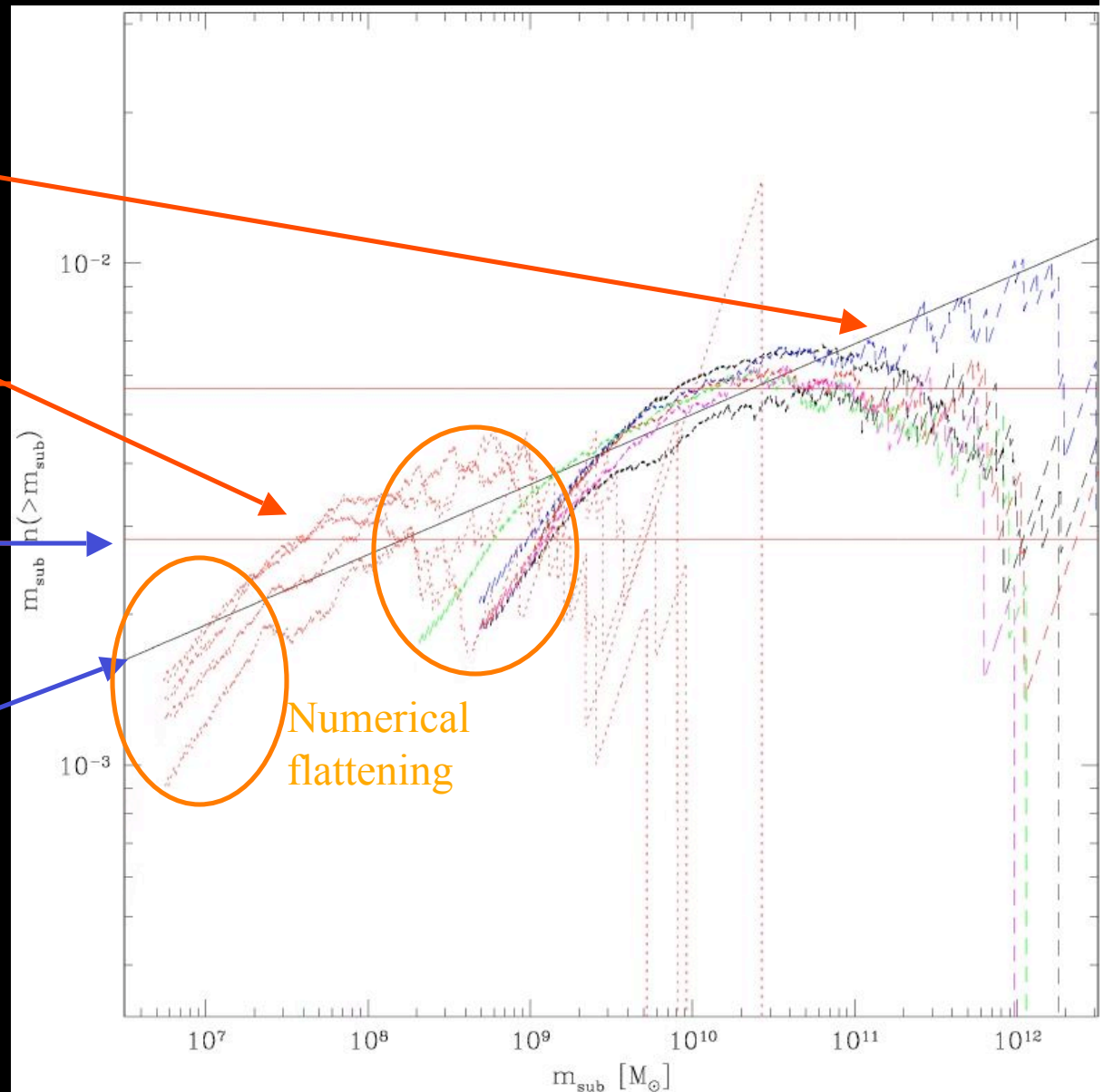
Same result from our
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factor of two between
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$$dn/dm \sim m^{-2}$$

$$dn/dm \sim m^{-1.86}$$

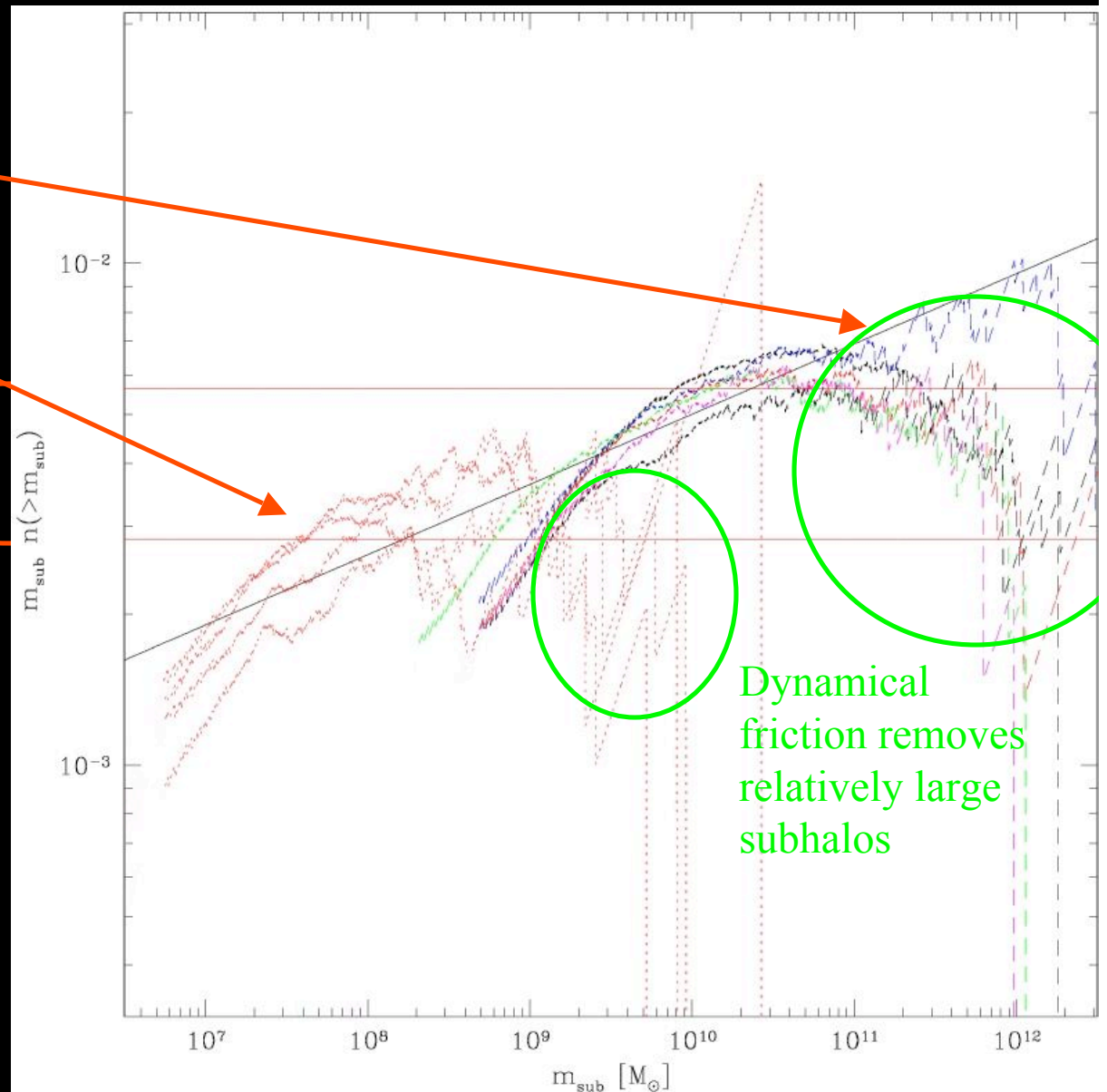
-> similar to field halo mass
function $n(M, z=0)$
steeper due to sub-
substructure? $\max_z n(M, z)$?



Substructure abundance

Same result from our
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and
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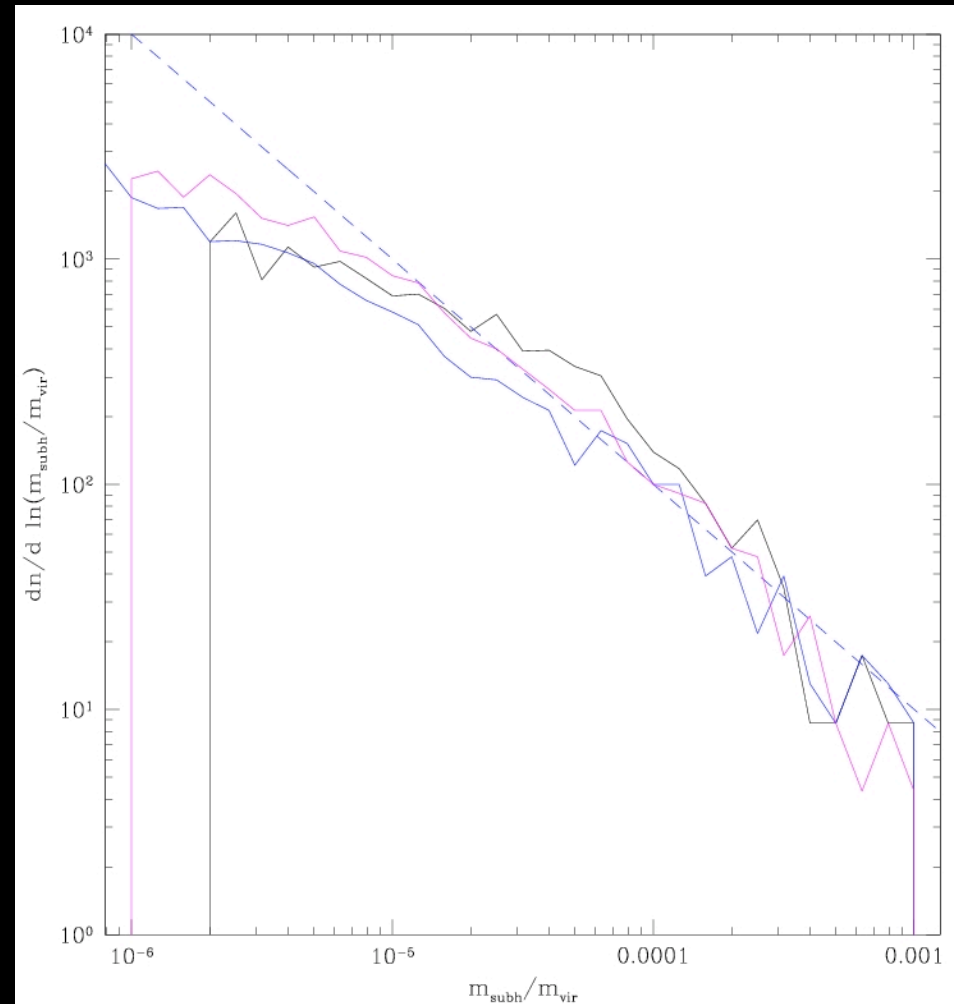
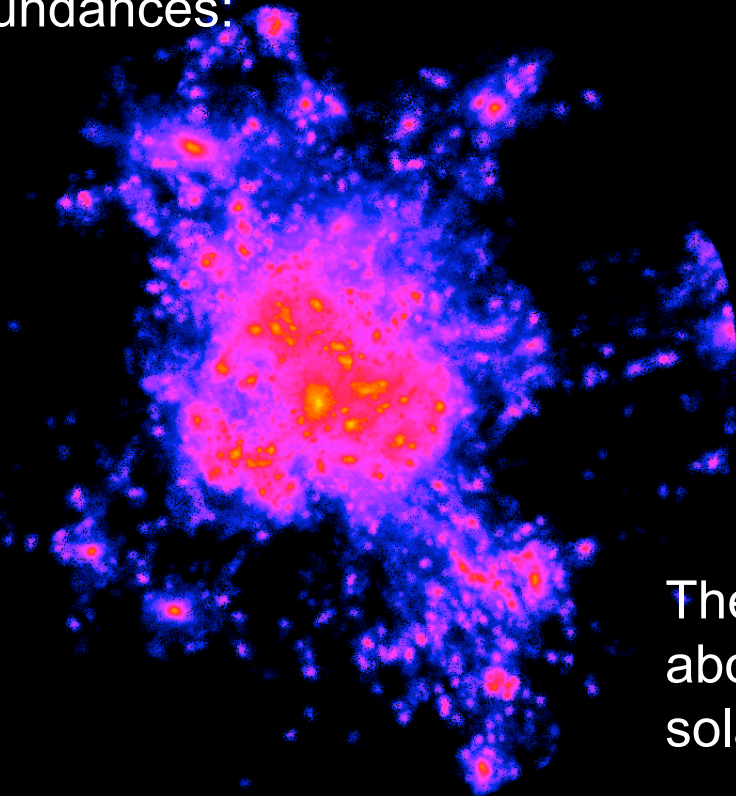
factor of two between
galaxies and clusters



Substructure abundance

Here we compare $z=0$ clusters with a 0.005 solar mass halo at $z=76$, mass resolution 10^{-9} solar masses; black line

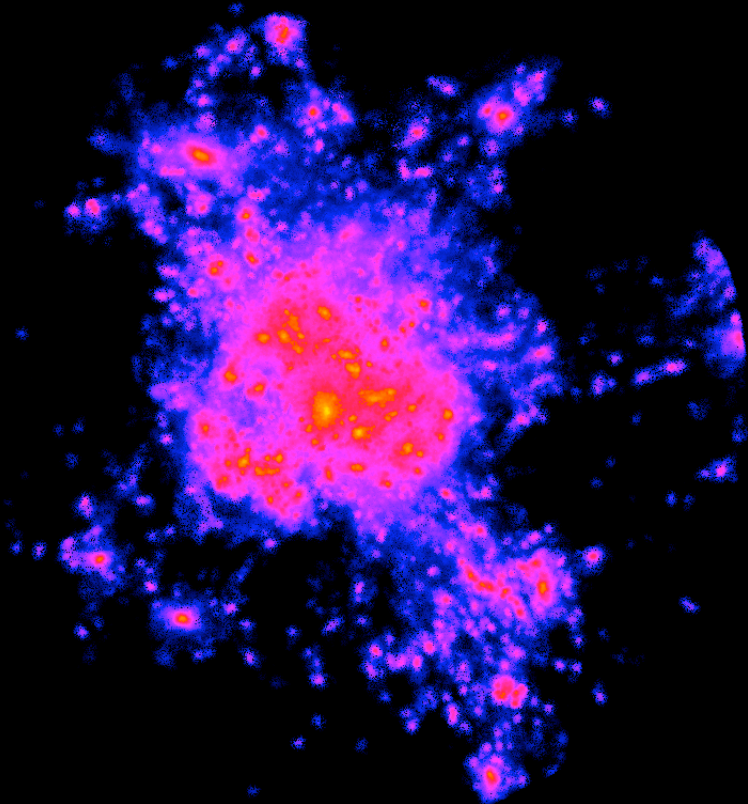
These are young, low c (~ 4) systems and we find similar subhalo abundances:



The Milk Way halo has about 5×10^{15} subhalos above the SUSY free streaming scale of 10^{-6} solar masses. (JD, Moore, Stadel, 2005)

Substructure abundance

The Milk Way halo has about 5×10^{15} subhalos above the SUSY free streaming scale of 10^{-6} solar masses. (JD, Moore, Stadel, 2005)



Impulsive heating approximation suggests that some micro-halos are disrupted by stars.

But this approximation is inadequate to decide disruption:

In simulated “disruptive” encounters with stars the minihalo only loses some of its mass in the outer part where tides are most effective and the cusp survives.

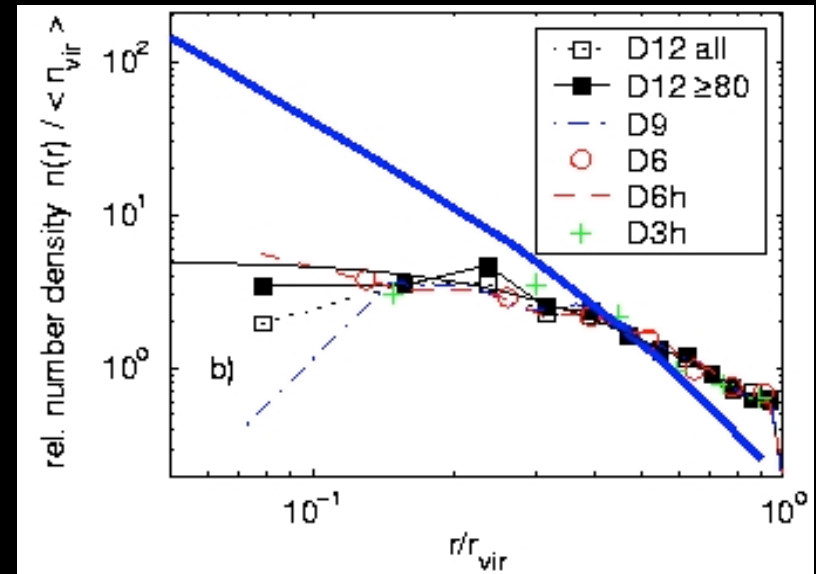
Substructure number density profiles

Number density profile selected by bound mass (or circular velocity) today is shallower than the DM profile.

Profile is independent of subhalo mass.

$$n(r) \sim 1 / (1 + (r/r_H)^2) , r_H = 1.3 r_{s\text{NFW}}$$

(JD et al. MNRAS, 352, 535, 2004)

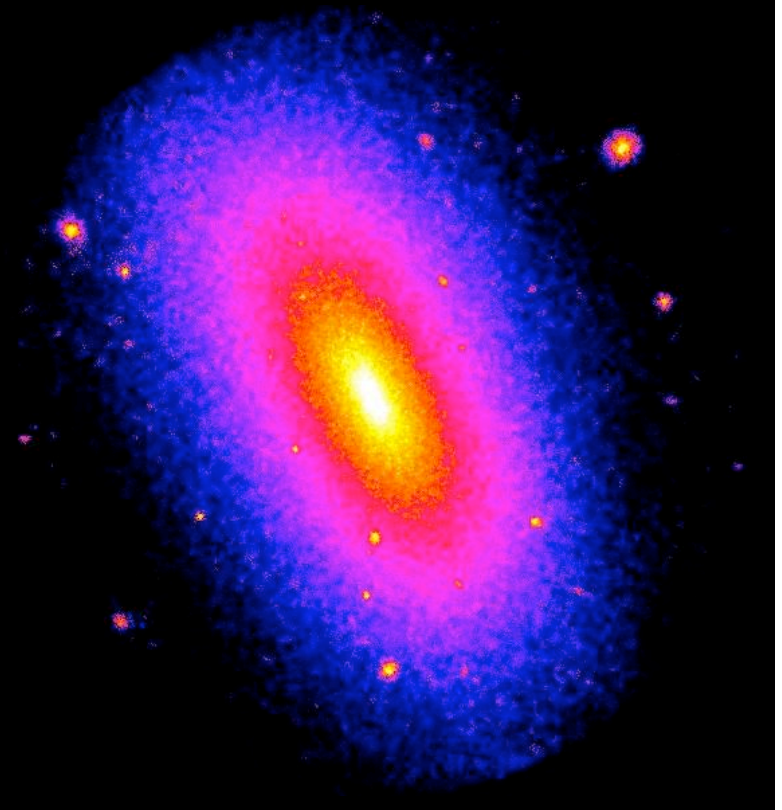
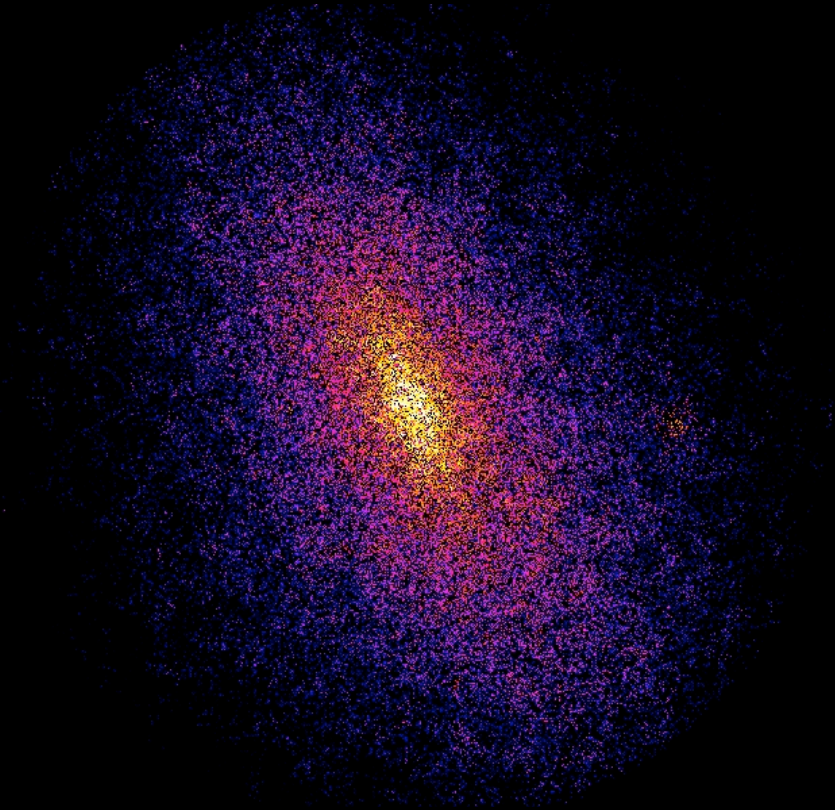


Substructure number density profiles

Subhalos in the inner part of CDM halos have usually lost most of their mass due to tidal stripping (Kravtsov et al. 2004; Gao et al. 2004). They only survive in high resolution simulations:

The inner 10% of a galaxy halo resolved with 1 million particles in R_{vir}

Same region and object resolved with 27 million p.

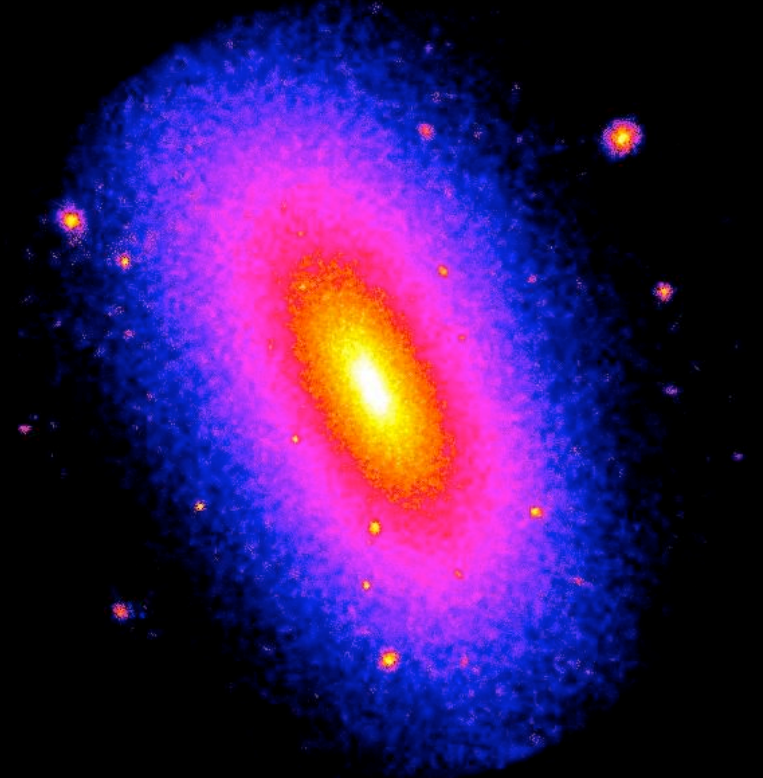
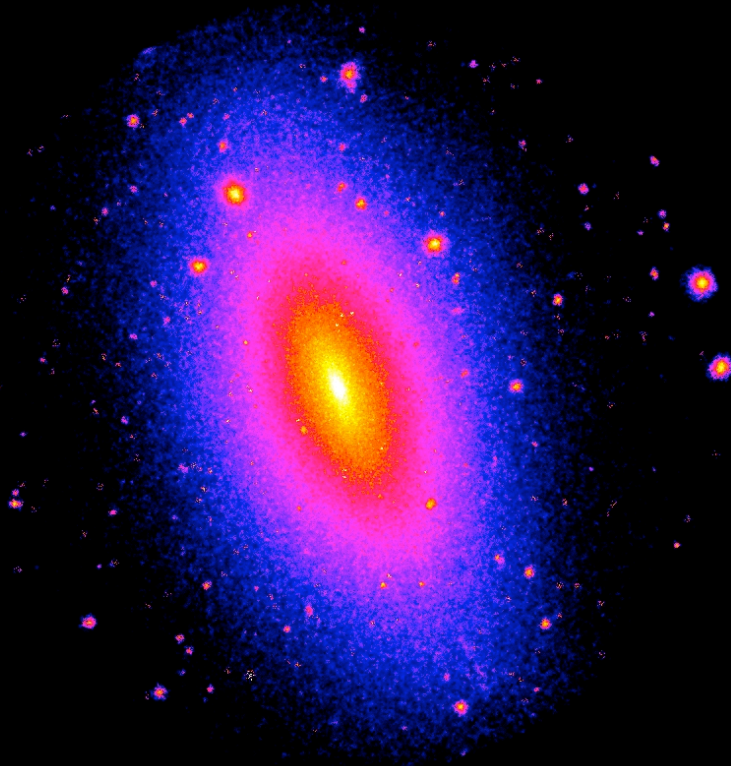


Substructure number density profiles

Subhalos in the inner part of CDM halos have usually lost most of their mass due to tidal stripping (Kravtsov et al. 2004; Gao et al. 2004). They only survive in high resolution simulations:

The inner 10% of a galaxy halo resolved with **130 million** particles in Rvir

Same region and object resolved with 27 million p.



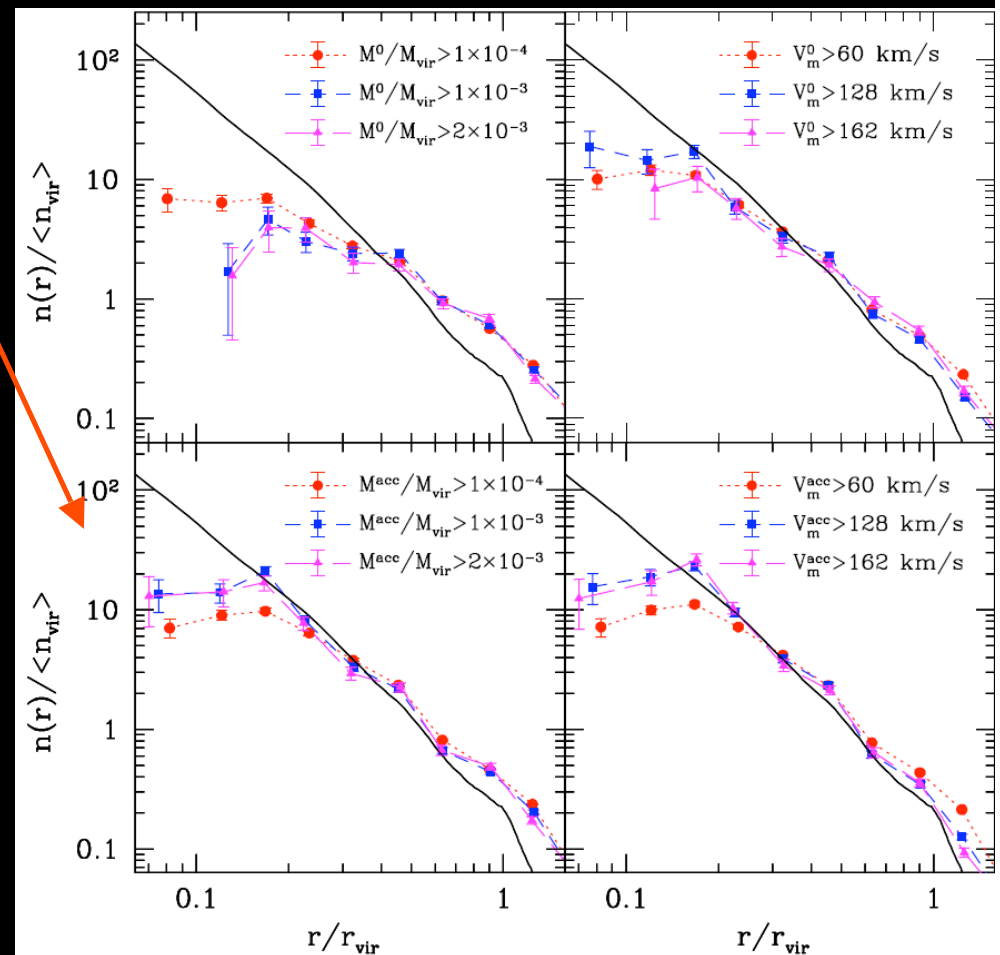
Subhalos destruction is rare, mass loss is common: 83% of the well resolved (over 100 particles) halos in a cluster forming region at $z=2$ survive as subhalos (with at least 10 bound particles) until $z=0$. (Ghigna et al. 2000, JD et al. 2004)

Substructure number density profiles

The number density of galaxies in groups and clusters roughly trace the mass and not the $z=0$ selected subhalos. Three related ways to obtain a realistic galaxy distribution in CDM subhalos:

1) Simply select halos by mass or circular velocity before accretion

from Nagai & Kravtsov, ApJ 2004



Substructure number density profiles

The number density of galaxies in groups and clusters roughly traces the mass and not the $z=0$ selected subhalos. Three related ways to obtain a realistic galaxy distribution in CDM subhalos:

- 1) Simply select halos by mass or circular velocity before accretion (Nagai & Kravtsov, ApJ 2004)
- 2) Use a semi analytic model to populate N-body halos (Springel et al. MNRAS 2001, Gao et al. MNRAS 2004, Kravtsov et al. ApJ 2004)

Substructure number density profiles

The number density of galaxies in groups and clusters roughly traces the mass and not the $z=0$ selected subhalos. Three related ways to obtain a realistic galaxy distribution in CDM subhalos:

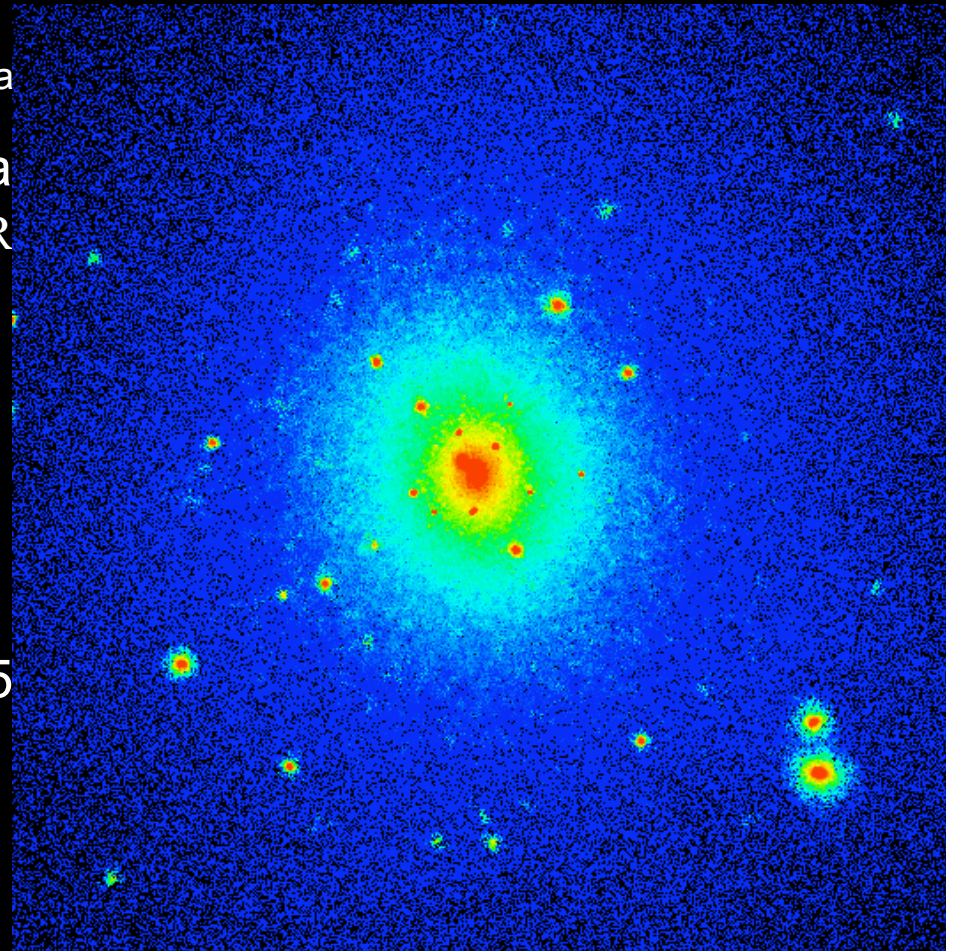
1) Simply select halos by mass or circular velocity before accretion (Naga

2) Use a semi analytic model to popula (Springel et al. MNRAS 2001, Gao et al. MNR

3) High resolution hydro simulations:

$n_{\text{SUB}}(r)$ now follows the dark matter density profile down to 5% of the virial radius

from A. Maccio et al. astro-ph/0506125



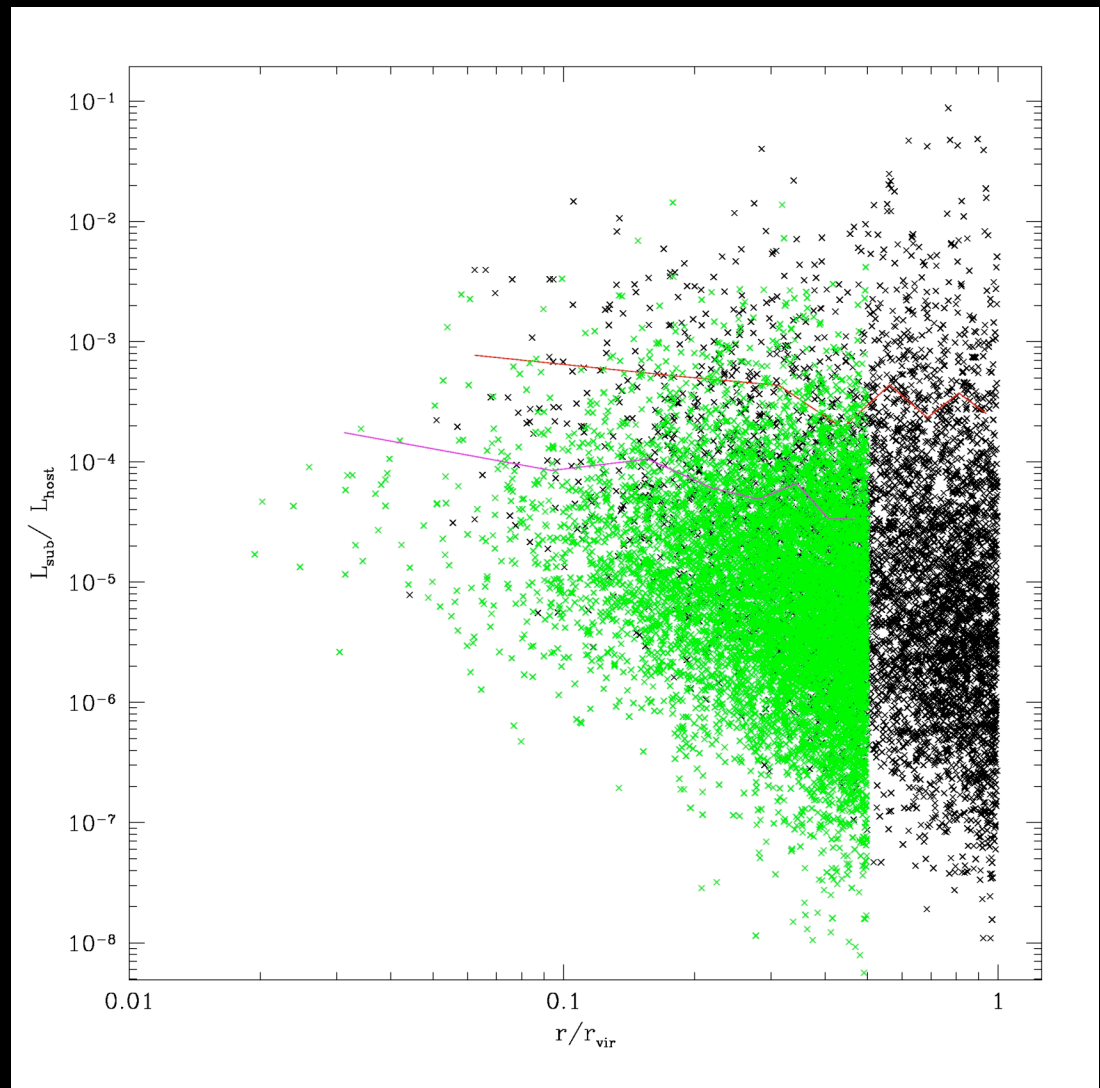
Substructure number density profiles

Assuming NFW density profiles the DM annihilation luminosity of a halo is
 $L \sim \rho_s^2 r_s^3$

The luminosity of the resolved subhalos is about twice the one of the host halo, this gives a lower limit for the boost factor of about 3.

It could be > 100
(Calcaneo-Roldan & Moore, PRD, 2000)

Inner subhalos are more luminous ...



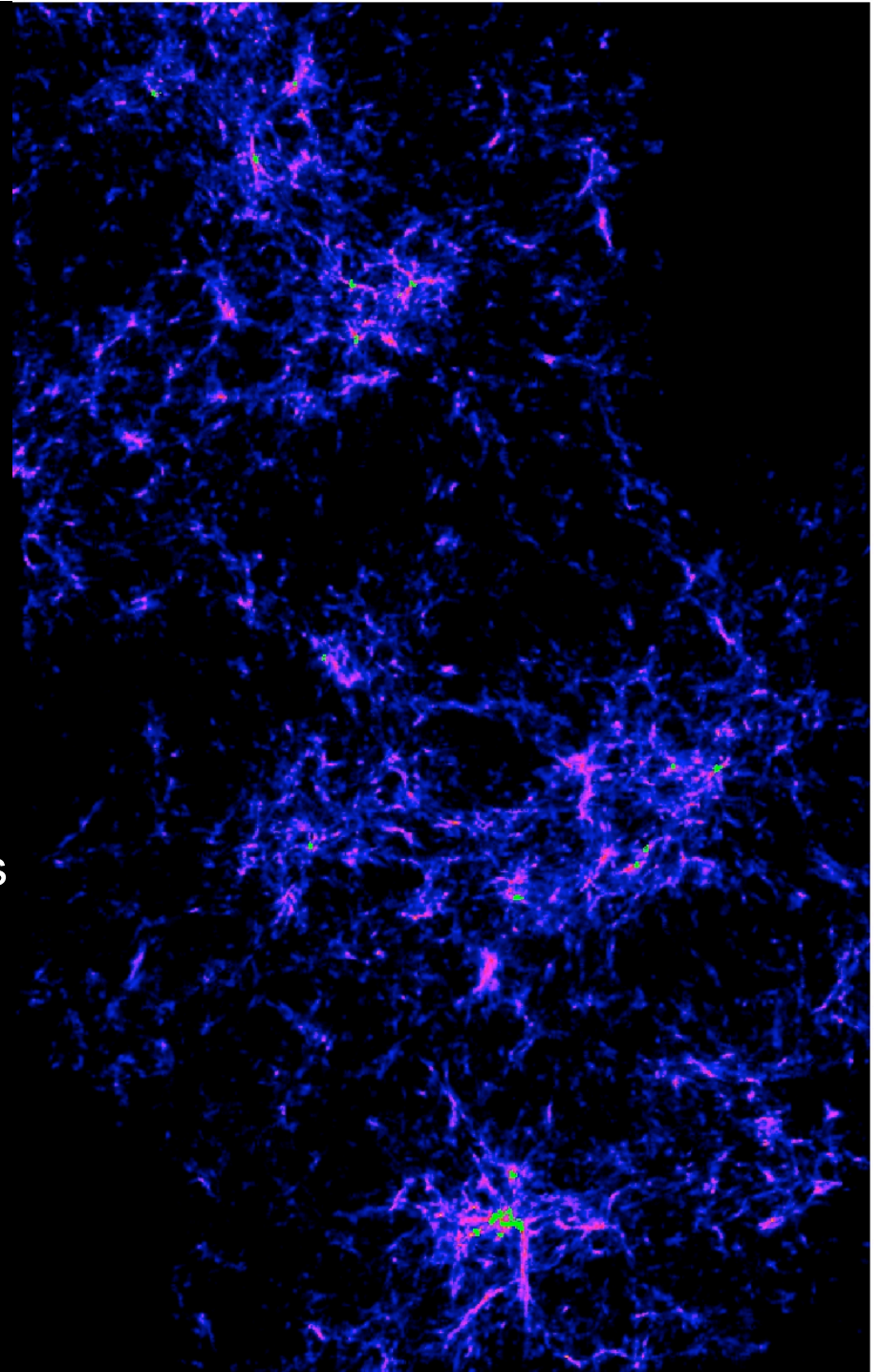
Substructure number density profiles

Inner subhalos are more luminous ... because they formed earlier and are denser:

Early forming halos are strongly clustered around the centers of larger scale fluctuations.

In this example halos more massive than $5e7 M_{\text{sun}}$ at redshift 18 are marked (green). These are rare ($>3.5 \sigma$) fluctuations

(JD et al. astro-ph/0506615)



Substructure number density profiles

Inner subhalos are more luminous ... because they formed earlier and are denser:

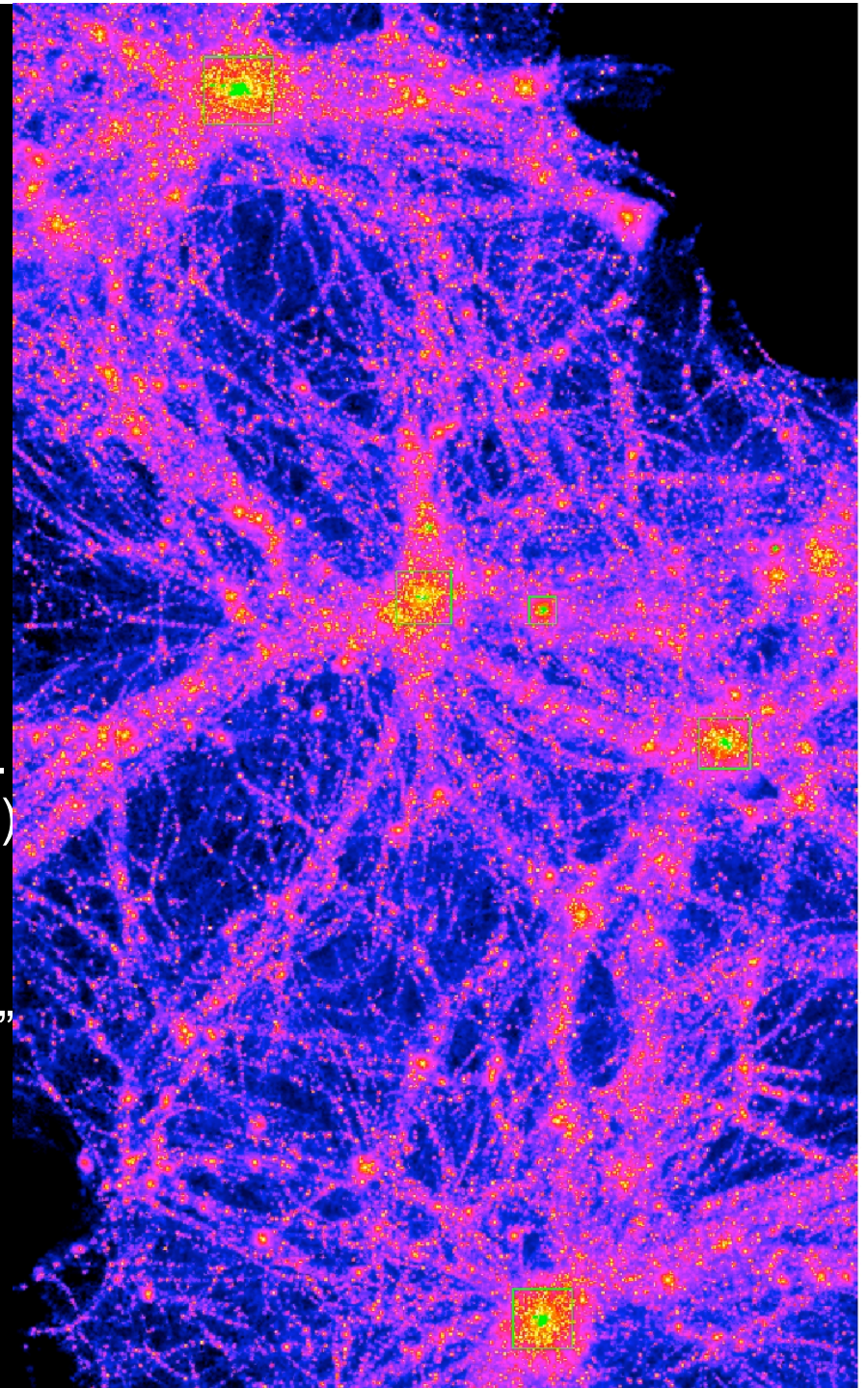
Early forming halos are strongly clustered around the centers of larger scale fluctuations.

Most of the marked material ends up near the centers of the largest $z=0$ halos.
(\rightarrow massive BHs from PopIII near the GC)

(JD et al. astro-ph/0506615)

Also “Age dependence of halo clustering”
(Gao, Springel & White, astro-ph/0506510)

This important property of hierarchical structure formation is missing in current semi-analytic models.



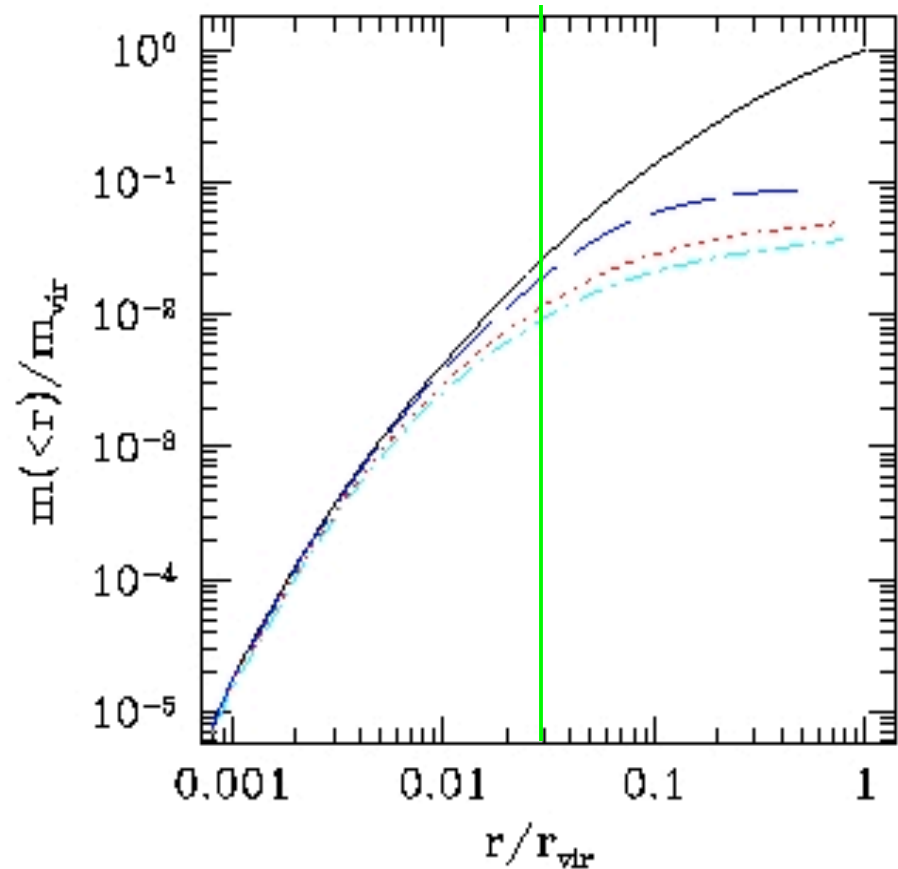
Substructure number density profiles

Inner subhalos are more
luminous ...

For DM around us the halo
formation times were typically
 $(z+1) = 2 (z_f + 1)$

i.e. local subhalos are twice as
concentrated and eight times
more luminous than an average
subhalo

> 2 sigma material

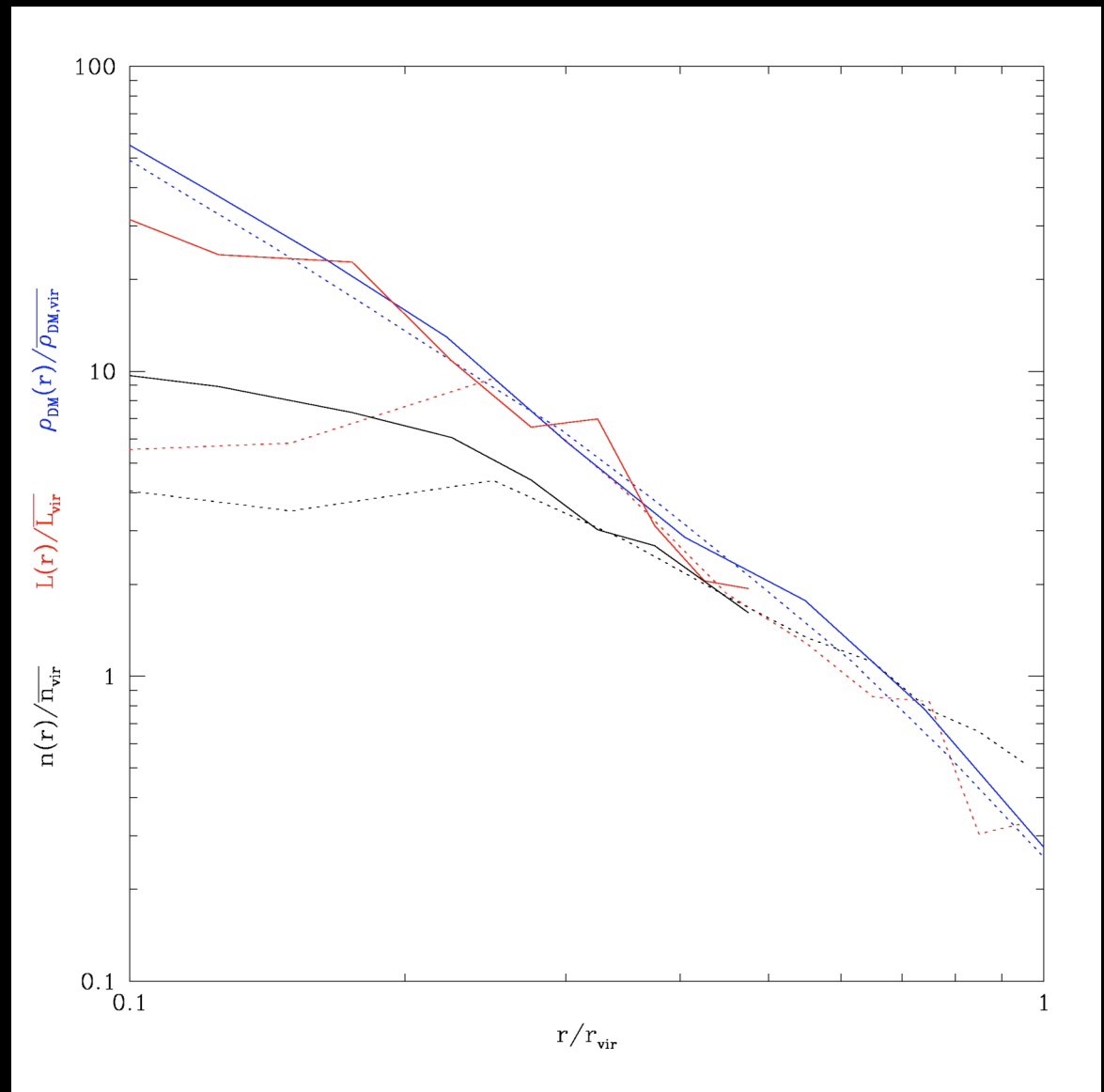


JD et al. astro-ph/0506615

Substructure number density profiles

DM annihilation
luminosity of subhalos
 $L \sim \rho_s^2 r_s^3$
traces the mass:

-> substructure increases
the global sky brightness
in any given direction

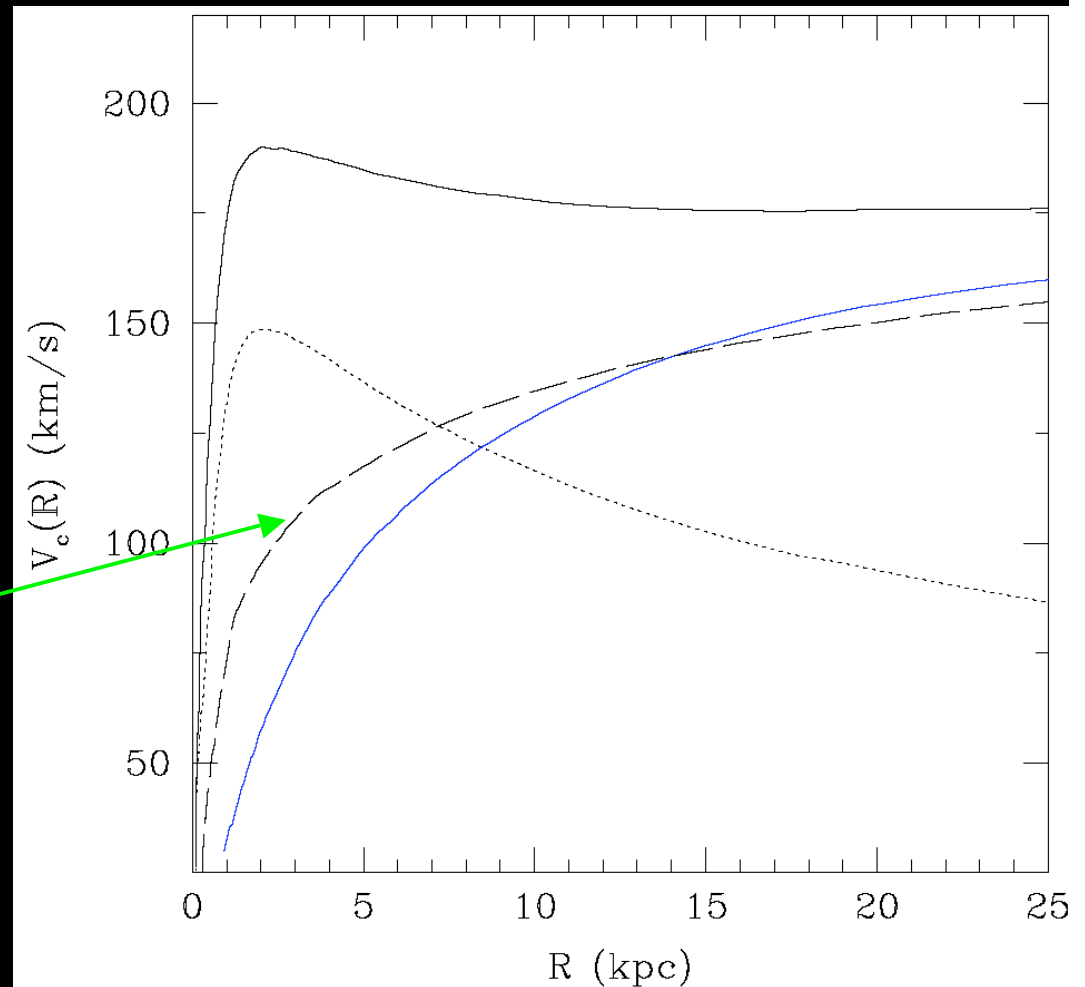


3) DM in the Milky Way

To reproduce the local circular velocity of 220 km/s after adiabatic contraction, the Milky Way could have formed in a dark halo with a maximum circular velocity of 190 km/s before contraction

The inner DM cusp gets steeper

(Maccio et al. astro-ph/0506125)



Such LCDM halos have 300+-100 subhalos with $v_{\text{max}} > 10$ km/s, but around the Milky Way there are only about 10 satellite galaxies: “Missing satellites problem”...

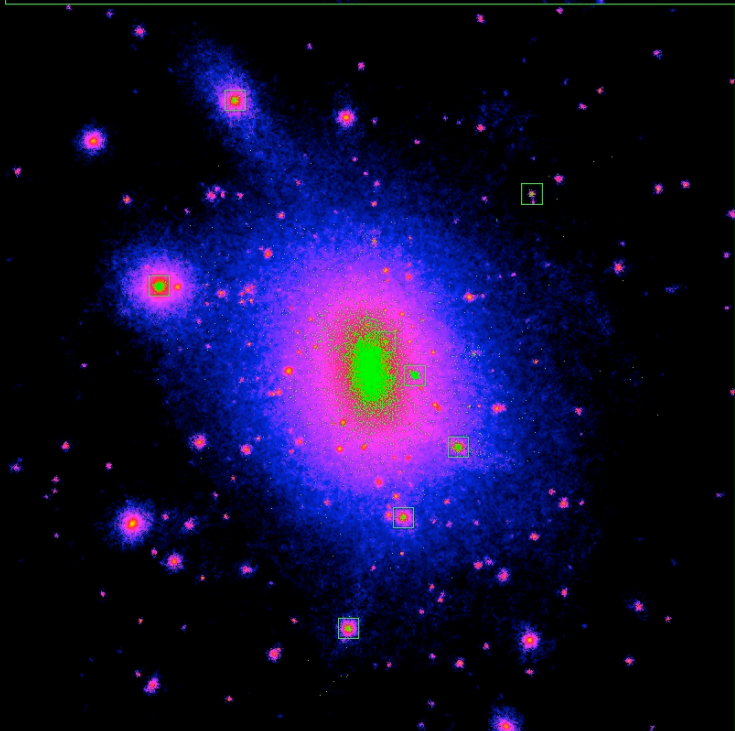
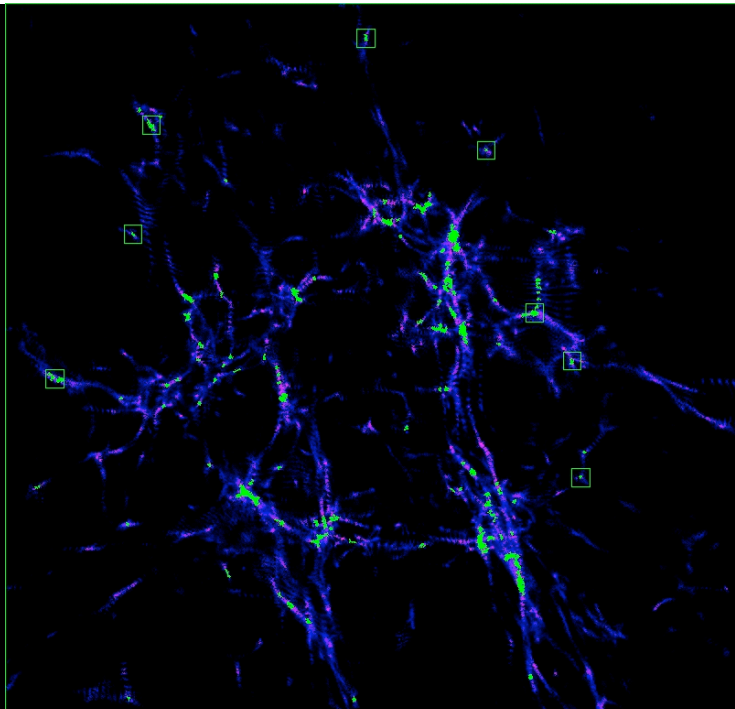
Milky Way stellar halo and dwarf satellites:

Assume proto-galaxies formed in halos above 10^8 solar masses ($T_{\text{vir}} > 10^4$ K) which formed before reionisation.

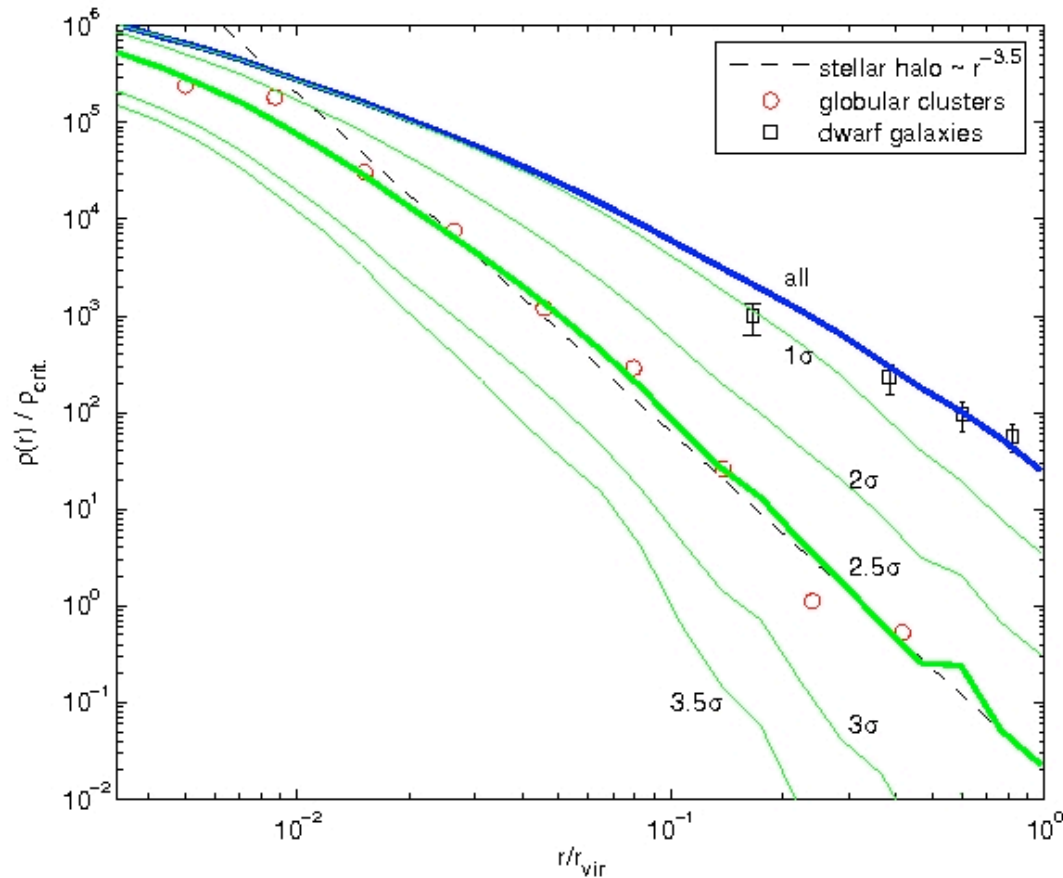
After reionisation gas accretion into small halos is suppressed (Bullock et al. ApJ 2000)

A few ($\sim 5\%$), most remote proto-galaxies survive as dwarfs satellites with radial profile, velocity function and total number like observed around the Milky Way.

Most join the MW early (bias!) and are disrupted producing a realistic, concentrated halo of old, metal poor stars (Moore et al 2005, submitted)



Building blocks of the Milky Way halo

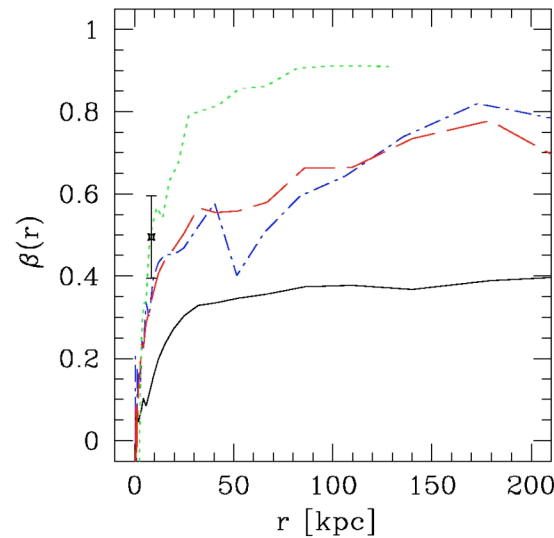
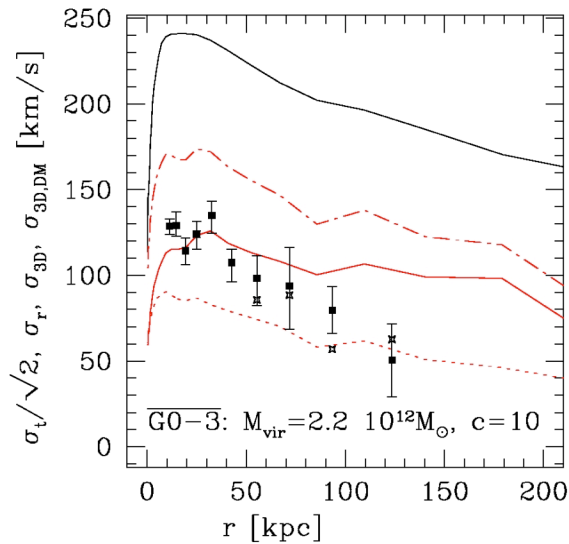
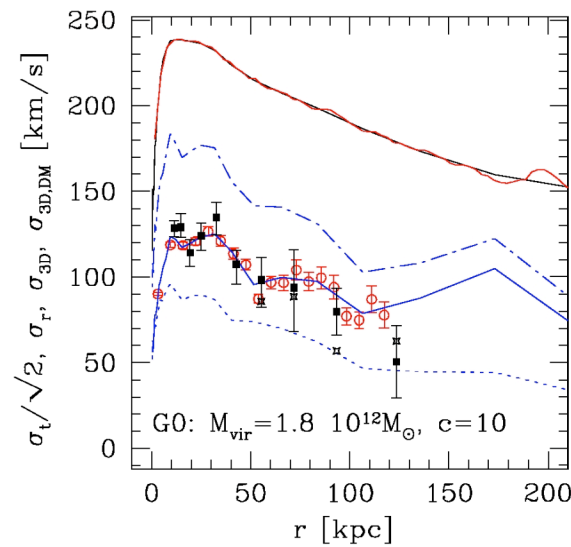
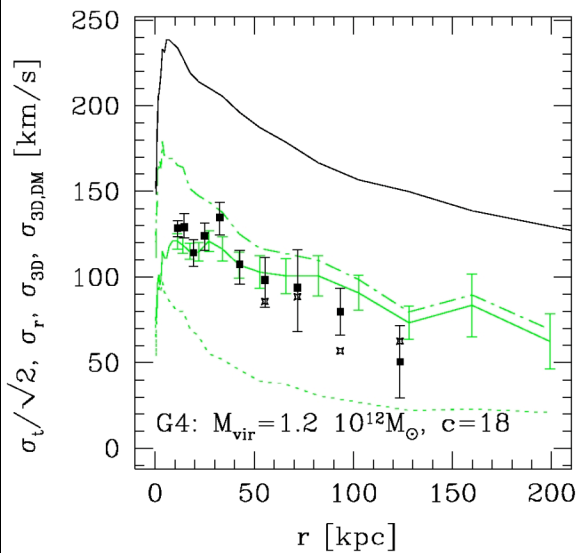


If reionisation is at $z=12$ our proto-galaxies are rare peaks above 2.5σ . They are strongly clustered towards the galaxy center and produce a concentrated stellar halo.

(Moore et al 2005, submitted)

Data from W. E. Harris (physun.physics.mcmaster.ca/Globular.html)

Milky Way stellar halo



Our model stellar halo also has similar kinematics as observed.

The outer halo and therefore the virial mass are not well constrained yet, but better data will be available soon (RAVE, GAIA)

JD et al. astro-ph/0506615

Summary

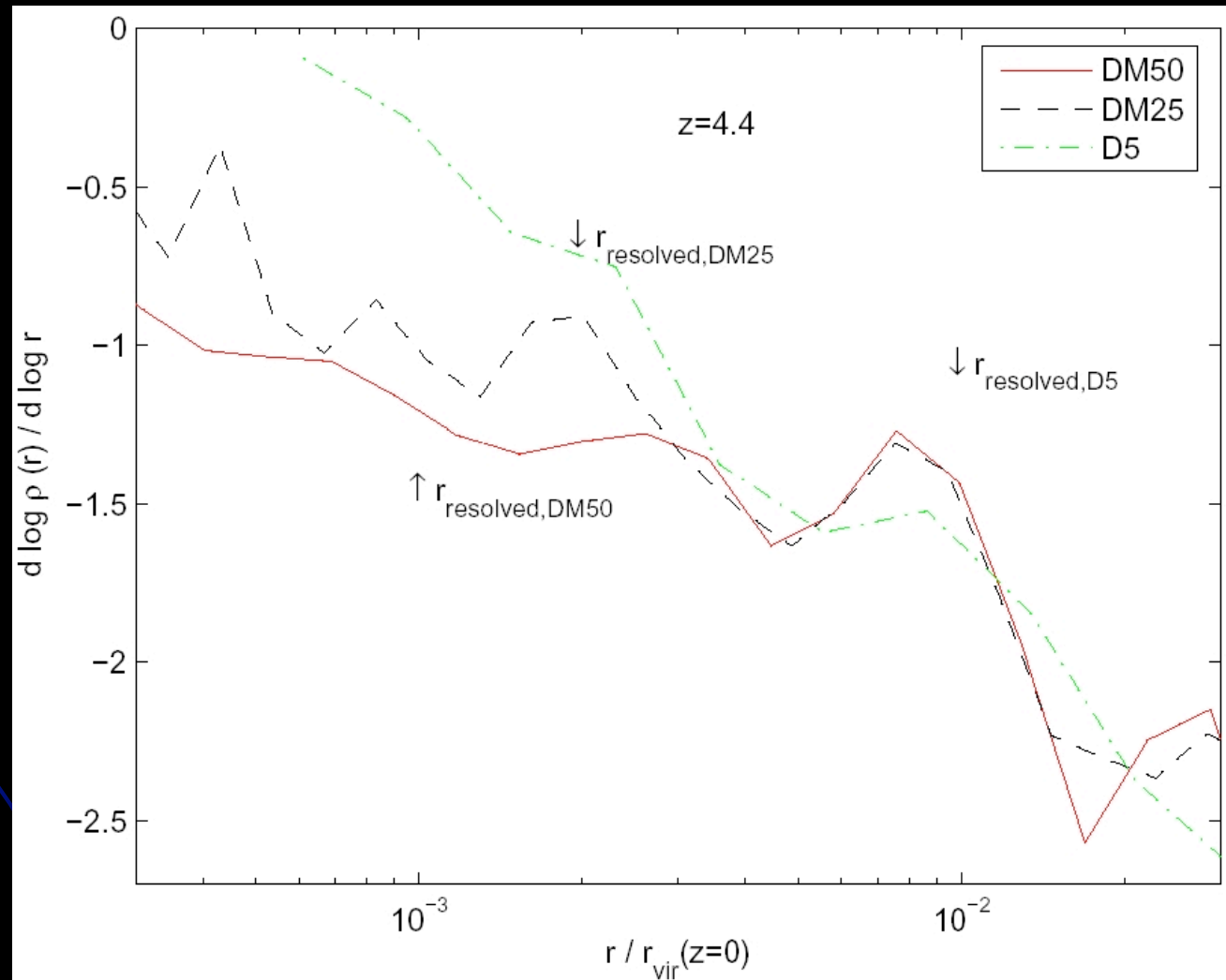
- inner density profiles seem to have steep cusps, on average $\sim r^{-1.2}$. They are very difficult to resolve due to numerical relaxation.
- large abundance of subhalos and steep mass functions similar to field halo mass functions.
- same age halos have self similar substructure properties, from cluster to sub-solar mass scales.
- resolved subhalos are more extended than the dark matter but their annihilation luminosity follows the mass.
- if proto-galaxies formed only in those small halos which reach $10^8 M_{\text{sun}}$ before $z=12$, they will build up a realistic stellar halo and satellite galaxy population.

Resolving the inner halo with a multimass approach

Run DM50: effective resolution of one billion particles in R_{vir} , stopped at $z=4.4$

logarithmic slope:

-> indicates that cuspy profiles describe the very inner part better



Resolving the inner halo with a multimass approach

Combining run DM50 with lower resolution runs of the same system one can estimate the profile of a billion particle cluster at $z=0$:

logarithmic slope:

-> indicates that cuspy profiles describe the very inner part better

(JD, et al. astro-ph/0504215)

