11176-H508-R0-00

N7024300

TRW NOTE NO. 70-FMT-819

PROJECT APOLLO

TASK MSC/TRW A-50

APOLLO MISSION 11, TRAJECTORY RECONSTRUCTION AND POSTFLIGHT ANALYSIS VOLUME 1

16 MARCH 1970

Prepared for

MISSION PLANNING AND ANALYSIS DIVISION

NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

MANNED SPACECRAFT CENTER

HOUSTON, TEXAS

NAS 9-8166

11176-H508-R0-00

TRW NOTE NO. 70-FMT-819

PROJECT APOLLO

TASK MSC/TRW A-50

APOLLO MISSION 11, TRAJECTORY RECONSTRUCTION AND POSTFLIGHT ANALYSIS VOLUME 1

16 MARCH 1970

Prepared for
MISSION PLANNING AND ANALYSIS DIVISION
NATIONAL AERONAUTICS AND SPACE ADMINISTRATION
MANNED SPACECRAFT CENTER
NAS 9-8166

Approved by W. P. Girod
W. P. Girod, Manager
MSC/TRW Task A-50

Approved by J. E. Alexander
J. E. Alexander, Manager
Guidance and Control
Systems Department

Approved by H. L. Moore
H. L. Moore, Manager
MSC/TRW Task A-50

Approved by D. G. Saile
D. G. Saile, Assistant
Project Manager
Guidance and Performance
Mission Trajectory Control Program

Approved by R. K. Petersburg
R. K. Petersburg, Manager
Systems Evaluation
Department

Approved by R. P. Parten
R. P. Parten, Chief
Mission Planning Support
Office
NASA Manned Spacecraft
Center

TRW
SYSTEMS GROUP

FOREWORD

This report is submitted to the NASA Manned Spacecraft Center in accordance with MSC/TRW Task A-50 Contract NAS 9-8166. This report contains the postflight analysis performed in conjunction with the Apollo 11 mission and is issued as supplement one to the Apollo 11 Mission Report (NASA/MSC Report MSC-00171, Nov. 1969).

The report is issued in two volumes. Volume I contains details of the analysis and results obtained, including appendixes. Volume II contains a listing of the 45-day best estimated trajectory (BET) for the Apollo 11 mission in the NASA Apollo Trajectory (NAT) format. The listing is not generally distributed but is available from NASA/MSC upon request. Requests should be made to:

NASA/MSC Computations and Analysis Division
Central Metric Data File
Code ED-5, Building 12, Room 133
Houston, Texas 77058

Page Intentionally Left Blank

TABLE OF CONTENTS

Page Intentionally Left Blank

LIST OF TABLES

Page Intentionally Left Blank

LIST OF ILLUSTRATIONS

LIST OF TABLES

LIST OF ILLUSTRATIONS
(Cont)

7.0 APOLLO MISSION 11 TRAJECTORY RECONSTRUCTION AND POSTFLIGHT ANALYSIS

7.1 INTRODUCTION AND SUMMARY

7.1.1 Apollo 11 Mission

The Apollo 11 mission was launched from the Kennedy Space Center at 13:32:00 (hrs:min:sec) Greenwich Mean Time on 16 July 1969. Apollo 11 was the third manned lunar mission and the first to attempt and accomplish a landing on the lunar surface. A summary of the major events is presented in Table 7.1.

The descent phase of the mission was initiated during the thirteenth revolution of the moon at approximately $100^{h} 07^{m}$ Ground Elapsed Time (GET). The lunar module (LM) successfully landed on the lunar surface at approximately $102^{h}45^{m}$ GET.

The rendezvous phase began with ascent ignition during the 25^{th} CSM revolution and ended with docking at $128^{h}03^{m}$ GET. A summary of the CSM and LM maneuvers performed during descent and rendezvous is presented in Table 7.2 and a graphical representation of these phases of the mission which depicts the motion of the LM relative to the CSM is shown in Figures 7-1a and 7-1b.

7.1.2 Postflight Analysis

The objective of the postflight analysis task was, in general, to generate trajectory parameters and data for the command and service modules (CSM) and LM from S-IVB/CSM separation to the end of mission. As in the Apollo missions 9 and 10, a preliminary trajectory was generated from the best available RTCC vectors. The bulk of the postflight analysis effort was then concentrated on reconstruction of the two periods of flight from LM/CSM undocking to LM touchdown (descent phase) and from LM ascent to LM/CSM docking (rendezvous).

The RTCC vectors used to generate the preliminary NAT (NASA Apollo Trajectory) are summarized in Appendix A. Most of the lunar trajectories were generated using RTCC SS2 (inclination constrained) solution vectors rather than SS1 (no a priori) solution vectors. Unlike the Apollo 10

SS2 vectors which were constrained to the pre-LOI1, rev 18, and rev 29 planes, the Apollo 11 SS2 vectors were constrained on a rev to rev basis. Each SS2 vector contained two revs of data and was constrained to the SS1 solution plane of one of these two revs (exceptions existed at maneuvers). This technique prevented the accumulation of a large error in the out-of-plane component of position. The lunar potential model used in the generation of the preliminary NAT and for propagation of RTCC vectors was the Boeing R2 model defined in Appendix B.

The final NAT was produced by updating the preliminary NAT to include reconstructions of critical maneuvers for which telemetered acceleration data was available and to reflect the results of the trajectory reconstruction efforts performed on the descent and rendezvous periods of the mission. These reconstructions will be discussed in detail in the following sections.

In general, the postflight analysis was accomplished without difficulty. Coincident with the trajectory reconstruction activities, analyses were performed to determine the quality of the onboard tracking data (LM rendezvous radar, CSM sextant, CSM VHF ranging, and LM landing radar). The results of these analyses are also included in this report.

Table 7.1 Apollo 11 Sequence of Events

	CET h:m:s	GMT d:h:m:s
Range Zero	00:00:00	16:13:32:00
Insertion	00:11:49.3	16:13:43:49.3
Translunar Injection Ignition	02:44:16.2	16:16:16:16.2
S-IVB/CSM Separation	03:17:04.6	16:16:49:04.6
First Docking	03:24:03.1	16:16:56:03.1
Spacecraft Ejection	04:16:59.1	16:17:48:59.1
Midcourse Correction #1	26:44:58.7	17:16:16:58.7
Lunar Orbit Insertion #1	75:49:50.4	19:17:21:50.4
Lunar Orbit Insertion #2	80:11:36.8	19:21:43:36.8
Undocking	100:12:00	20:17:44:00
CSM Separation	100:39:52.9	20:18:11:52.9
Descent Orbit Insertion	101:36:14	20:19:08:14
Powered Descent Initiation	102:33:05.2	20:20:05:05.2
Touchdown	102:45:39.9	20:20:17:39.9
Liftoff	124:22:00.8	21:17:54:00.8
Coelliptic Sequence Initiation	125:19:36	21:18:51:36
Constant Differential Height	126:17:49.6	21:19:49:49.6
Terminal Phase Initiation	127:03:51.8	21:20:35:51.8
Terminal Phase Finalization	127:46:09.8	21:21:18:09.8
Second Docking	128:03:00	21:21:35:00
Final Separation	130:30:01	22:00:02:01
Transearth Injection	135:23:42.3	22:04:55:42.3
Midcourse Correction #2	150:29:57.4	22:20:01:57.4
CM/SM Separation	194:49:12.7	24:16:21:12.7
Entry Interface	195:03:05.7	25:02:35:05.7

Table 7.2 Descent and Rendezvous Maneuver Summary for Apollo 11

Maneuver	Type of Maneuver	Ignition Time (h:m:s) GET	Cutoff Time (h:m:s) GET	T/M Coverage	ΔV (FPS)
SEPARATION	CSM/RCS	100:39:52.9	100:40:01.9	Yes	2.6
DOI	LM/DPS	101:36:14.0	101:36:44.0	No	76.4
PDI	LM/DPS	102:33:05.0	102:45:42.2	Yes	6775.8
ASCENT	LM/APS	124:22:00.8	124:29:15.7	Yes	6070.1
CSI	LM/RCS	125:19:36	125:20:23	No	51.5
CDH	LM/RCS	126:17:49.6	126:18:07.4	Yes	19.9
TPI	LM/RCS	127:03:51.8	127:04:14.5	Yes	25.3
TPF	LM/RCS	127:46:09.8	127:46:38.1	No	31.4

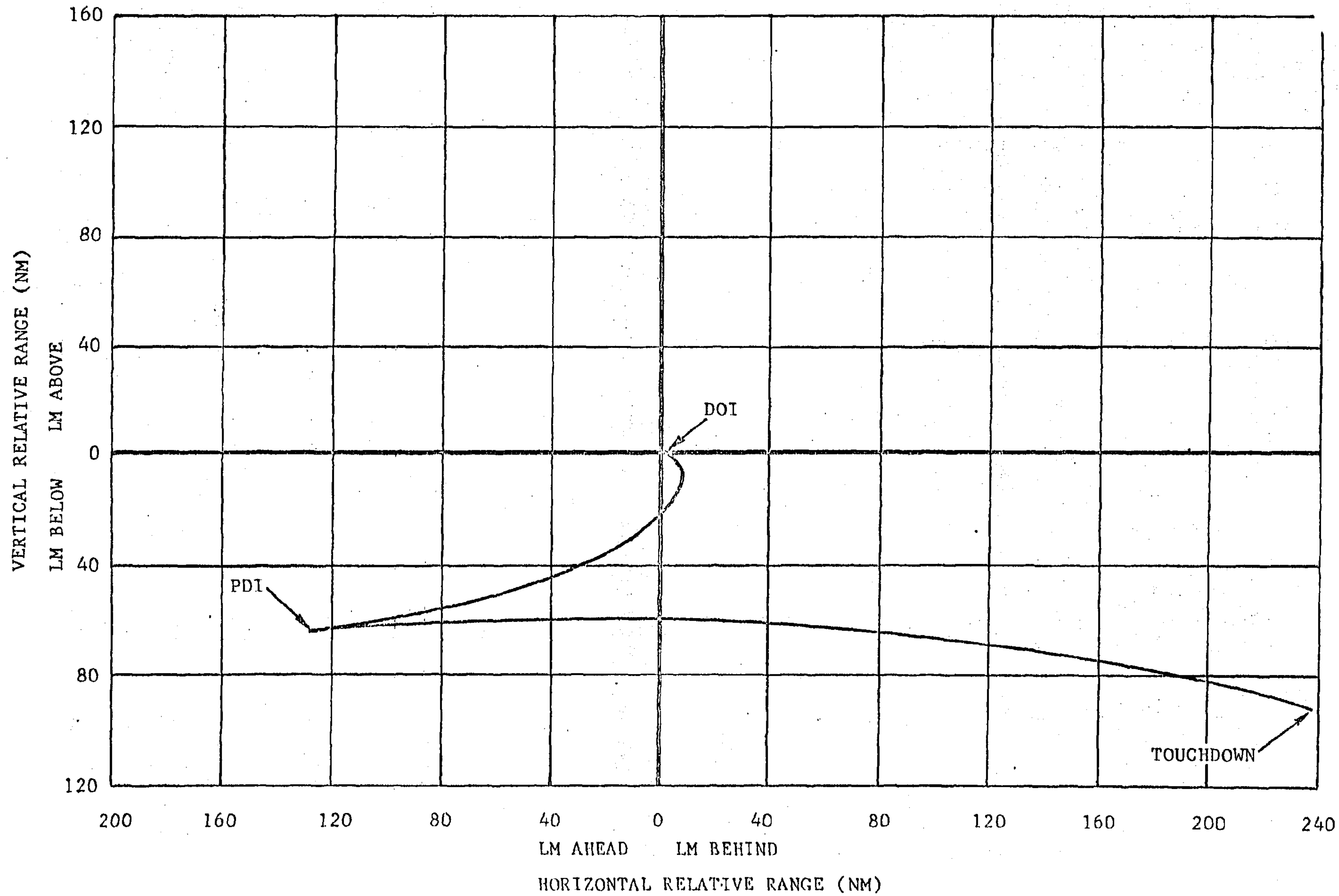


Figure 7-1a Relative Motion of the LM for Apollo 11 Descent - DOI to Landing (CSM Centered)

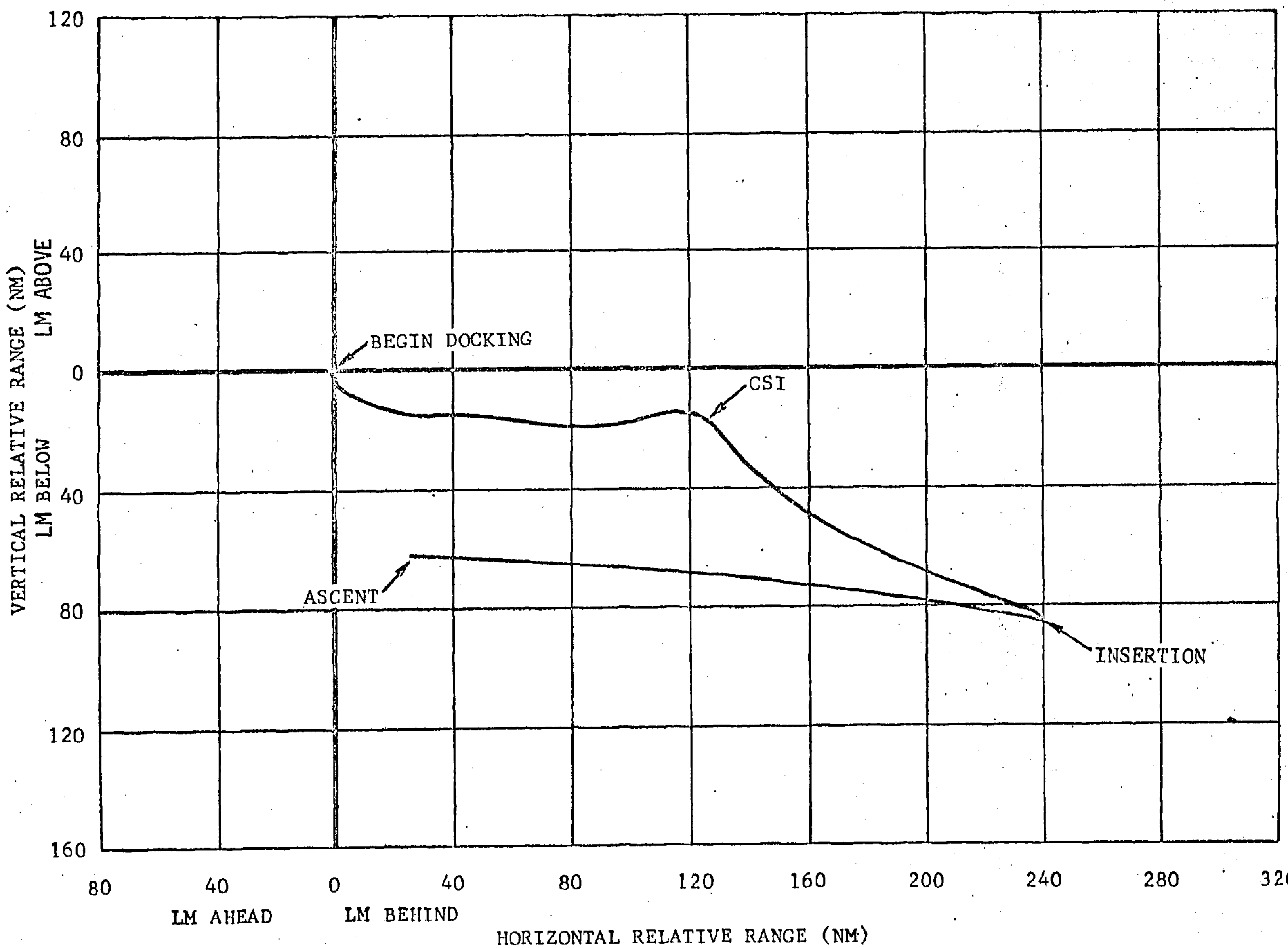


Figure 7-1b Relative Motion of the LM for Apollo 11 Rendezvous - Ascent to Docking (CSM Centered)

7.2 ORBIT ANALYSIS

7.2.1 Methods of Reconstruction

The HOPE Program was used as the basic orbit determination tool. The program utilizes a weighted least squares differential correction technique to regress on a large set of parameters. It is capable of handling two vehicles, and can use both ground based and onboard tracking data. An additional capability is the IGS (Inertial Guidance System) burn option which models the Apollo inertial measurement unit and uses telemetered acceleration data to reconstruct maneuvers.

The orbit determination was accomplished using four basic fit techniques. These techniques are described as follows:

a) MSFN free flight - regression on the state vector over free flight intervals as defined by spacecraft maneuvers using MSFN data.

b) MSFN IGS - regression on the state vector using, at maximum, one revolution of MSFN data and incorporating the spacecraft maneuvers which had telemetry coverage by means of the HOPE IGS burn model.

c) Onboard free flight - regression on the state vector over free flight intervals using available onboard tracking data to correct the LM trajectory with respect to a fixed CSM trajectory (MSFN fits).

d) Onboard IGS - regression on the state vector using available onboard data to correct the LM trajectory with respect to a fixed CSM trajectory and incorporation of the LM maneuver (which had telemetry coverage) by means of the HOPE IGS burn model.

More accurate trajectories are usually produced with techniques (b) and (d) since they take advantage of longer tracking data arcs. This factor is important in descent and rendezvous trajectory reconstruction since the tracking intervals between some maneuvers are too short to produce a representative trajectory over the whole segment.

As a result of the analysis of various lunar potential models contained in Reference 7, and on the basis of improved observation residuals and propagation characteristics, the L1 model (Langley Model 1) was used in the orbit analysis. This model is basically the Boeing R2 model augmented by a C33 term. Table 7.3 shows improvements in propagation characteristics of the L1 over the R2 model. Both models are defined in Appendix B.

The trajectories for both Apollo 11 vehicles during descent and rendezvous were reconstructed using the methods summarized above. The data used in these reconstruction activities primarily included low speed MSFN, high speed MSFN, rendezvous radar, VHF ranging, and sextant data. Telemetered acceleration data were used to reconstruct maneuvers where available and applicable. Table 7.2 lists the maneuvers performed during the descent and rendezvous periods. Figure 7-2 shows the tracking data arcs (which were available over the periods of interest) as a function of ground elapsed time. In Figure 7-2, the solid bars represent the transmitting (two-way) MSFN station and the numbers represent the number of observations upon which final fits were based. Note that some stations operated in the dual mode (simultaneous tracking of both the CSM and the LM).

The following paragraphs describe the trajectories which were used as the final BET for both vehicles.

7.2.2 CSM Best Estimate of Trajectory

The trajectories for the CSM lunar revolutions 13, 14, 25 and 26 were reconstructed from low speed MSFN tracking data compacted to a rate of two samples per minute or, in the case of stations operating in the dual mode, one sample every 36 seconds. The data used are summarized in Figure 7-2. The quantity of data obtained for revolutions 13 and 26 was good. Because of the partial data arcs from some stations on revolutions 14 and 25, the data quantity in these revs could only be rated as fair. Inclusion of data from a southern hemisphere station (Ascension) enhanced the geometry of the active tracking network configuration and contributed to the quality of all the fits.

Two reconstruction techniques were used to obtain the CSM BET's. The MSFN IGS fit technique was used on revolution 13 because of the presence of telemetered acceleration data from the CSM separation burn performed in the MSFN data arc. BET's for the remaining orbits of interest (14, 25 and 26) were obtained from MSFN free flight fits.

In general, the CSM BET's were of good quality. This is illustrated to some extent by the good position and velocity comparisons between revolutions (Table 7.4) and by the residual statistics listed for each fit in Appendix B. These statistics (standard deviation of .1 to .25 cycles per second) compare very well with Apollo 8 (standard deviations between .3 and .6 cycles per second) and Apollo 10 (standard deviations between .2 and .4 cycles per second). A portion of this improvement may be attributed to the better fit produced by the L1 lunar potential model.

Table 7.4 contains a summary of the final BET's giving fit type (technique), data interval, NAT trajectory interval, and position and velocity differences at matchpoints between segments.

7.2.3 LM Best Estimate of Trajectory

A major portion of the postflight analysis effort was directed towards reconstruction of the LM trajectories from undocking to landing and from liftoff through rendezvous. A discussion of the origin and quality of the final trajectories is included in the following paragraphs.

7.2.3.1 Descent Phase Trajectories

The descent phase was reconstructed in three segments; undocking to DOI, DOI to PDI, and PDI to Touchdown. The BET for undocking to DOI was obtained from a MSFN free flight fit based upon the entire data arc from revolution 13. The quantity of data was considerably better than for the CSM since five stations were tracking the LM. Residual statistics (summarized in Appendix B) compare well with the MSFN residual statistics obtained from the CSM fits. Note from Figure 7-2, which shows the tracking history, that the tracking station geometry was good.

The BET for the period from DOI to PDI was obtained from an onboard free flight fit based on CSM sextant and VHF ranging data taken prior to PDI. As can be seen in Figure 7-2 the data quantity was good, with 18 VHF ranging observations and 13 sextant sightings. Data quality is discussed more thoroughly in Section 7.3 The CSM trajectory which was used as the reference trajectory was the revolution 14 BET discussed in paragraph 7.2.2.

The BET for the powered descent segment of the flight was originally based on a fit obtained from low speed MSFN data taken from revolution 14 acquisition of signal to touchdown. The trajectory obtained from this fit was modified to force the landing point to coincide with the current best estimate of landing site location. Landing site parameters obtained from this descent trajectory (BET #3) were .6358° latitude, 23.4938° longitude, and -8557 feet altitude (referenced to the mean lunar radius). These figures compare well with the value published in Reference 10 as the best estimate (latitude .647° and longitude 23.505°, determined from postflight photo reduction).

Since the BET #3 was constrained to impact a desired landing site, the quality of the trajectory at PDI is not the best available. A subsequent reconstruction using a combination of onboard plus high speed MSFN data is discussed in Section 7.4 of this report. This combination of high speed data from acquisition of signal to landing and relative tracking data obtained prior to PDI produces a consistent and continuous representation of the LM trajectory from DOI to touchdown.

7.2.3.2 Rendezvous Trajectories

The BET for LM ascent was initialized with landing site coordinates of .6357° latitude, 23.4701° longitude, and a height of -8607 feet above the mean lunar radius. These initial conditions were then propagated to insertion using accelerometer data to model the ascent burn.

The LM BET for the period from insertion to TPF was reconstructed in two segments; insertion to CSI and CSI to TPF. The trajectory for the insertion to CSI segment was obtained from a MSFN free flight fit. The data arc and trajectory interval are described in Table 7.4. The MSFN data was good both quantitatively and qualitatively as can be seen in Figure 7-2. The residual statistics, summarized in Appendix B, show that the standard deviations of the doppler residuals are larger in this segment than in segments which have a less severe orbital geometry. This characteristic also existed in the Apollo 10 postflight results.

The second rendezvous segment covered the period from CSI to TPF. The BET chosen was obtained from an onboard data, IGS fit. The data used in the fit included LM rendezvous radar, CSM sextant, and CSM VHF ranging observations. In addition, telemetered acceleration data was used in the IGS burn option of HOPE to reconstruct the CDH and TPI burns. The data arcs are shown in Figure 7-2, and the residual statistics are summarized in Appendix B. Data quality was good, and the resulting BET produced an accurate relative trajectory. The CSM trajectory chosen as the reference for the relative observations was the revolution 26 trajectory described in paragraph 7.2.2. (The quality of the data and the reconstruction are discussed in more detail in Section 7.3 of this report.)

Table 7.3 Matchpoint Comparisons of Trajectories Produced with R2 and L1 Lunar Potential Models

Revolutions Compared	R2 POS RSS (ft)	R2 VEL RSS (ft/sec)	L1 POS RSS (ft)	L1 VEL RSS (ft/sec)
11-12	10,637	7.187	7544	5.756
12-13	9,936	8.178	4817	3.046
13-14	8,643	8.723	1555	2.53
25-26	9.595	9.139	2147	3.173

RSS = Square root of the sum of the squares of the differences between position (POS) or velocity (VEL) components.

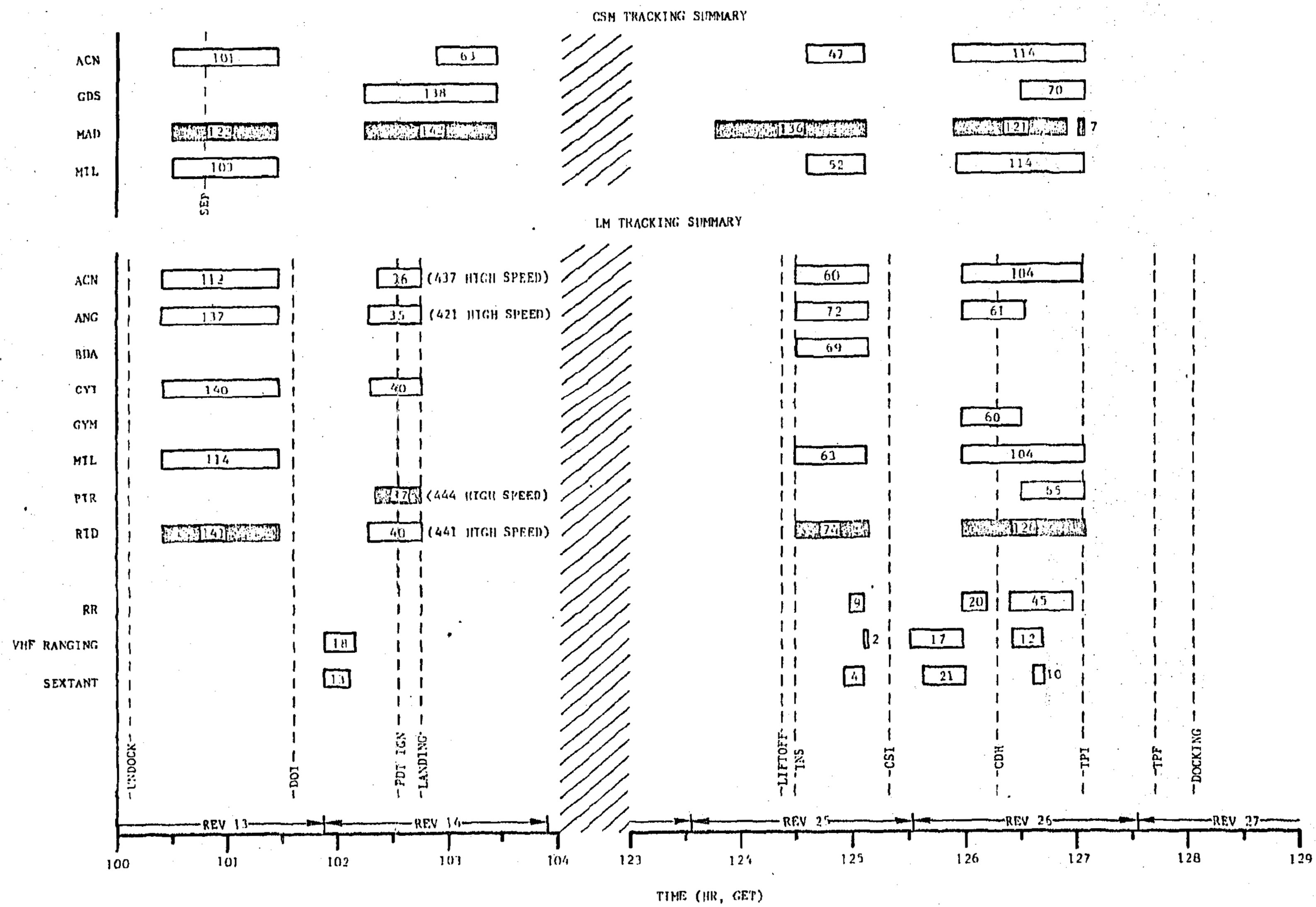


Figure 7-2 Tracking Data (Onboard and Ground Based) Timeline for Apollo 11 Descent and Rendezvous

Table 7.4 – Apollo Mission 11 BET Summary

Vehicle	Flight Segment	Fit Type	Data Interval (d:h:m:s) GMT	(d:h:m:s)	Trajectory Interval (d:h:m:s) GMT	(d:h:m:s)	ΔR ft	ΔV ft/sec
LM	Undock to DOI	MSFN F.F.	20:17:48:45	20:18:59:57	20:17:39:00	20:19:08:14.7	--	--
LM	DOI to PDI	O/B, F.F.	20:19:25:03	20:19:43:56	20:19:08:44.5	20:20:04:00	2007.	75.9*
LM	Powered Descent	Modified MSFN IGS	20:19:48:51	20:20:17:45	20:20:04:37.2	20:20:17:45.2	N/A	N/A
LM	Ascent	IMU only	---	---	21:17:53:58.9	21:18:03:08.9	--	--
LM	Insertion to CSI	MSFN F.F.	21:18:03:03	21:18:40:15	21:18:01:21	21:18:51:36	N/A	N/A
LM	CSI to POST TPI	O/B IGS	21:19:02:17	21:20:29:38	21:18:52:00	21:21:15:08	4253.	50.8**
CSM	Revolution 13	MSFN IGS	20:17:54:24	20:18:59:36	20:17:22:00	20:19:22:00	--	--
CSM	Revolution 14	MSFN F.F.	20:19:47:27	20:20:58:21	20:19:22:00	20:21:17:00	1555.	2.5
CSM	Revolution 25	MSFN F.F.	21:17:27:51	21:18:38:33	21:16:57:00	21:18:57:00	--	--
CSM	Revolution 25	MSFN F.F.	21:19:26:15	21:20:36:51	21:18:57:00	21:20:57:00	2147.	3.2

*DOI Burn ΔV = 76.4 ft/sec
**CSI Burn ΔV = 51.5 ft/sec

7.3 ONBOARD TRACKING DATA ANALYSIS

7.3.1 Introduction

Analysis of the LM rendezvous radar data from Apollo missions 9 and 10 and CSM VHF ranging data from Apollo 10 resulted in the conclusions that both data types were of high quality and, in general, produced trajectories consistent with those obtained from ground based tracking data (References 1 and 5).

A similar analysis of the onboard tracking data obtained during the Apollo 11 mission was performed with the following objectives:

a) Determine the consistency of the LM rendezvous radar data and the CSM VHF ranging data with similar data from Apollo missions 9 and 10.

b) Using these data as a standard of comparison, evaluate the LM sightings made with the CSM sextant.

c) Determine the consistency of all onboard data with the ground based data.

d) Use the onboard data to construct a more accurate LM rendezvous trajectory.

The onboard tracking data were obtained from the downlink telemetry tapes by a special purpose computer program designed to read the tape, and output the desired observations and associated information on punched cards. The format of the punched cards was the specified input to the HOPE Program. Editing of bad data was performed manually.

Onboard tracking data yields a measure of the position and velocity of one vehicle relative to another. It is necessary, therefore, to obtain a good, independent estimate of the trajectory of one vehicle and fix this as a reference trajectory. Since the LM trajectory is perturbed by several maneuvers during the descent and rendezvous mission periods, it is logical to fix the trajectory of the relatively quiescent CSM as the reference.

As discussed in Section 7.2, the CSM trajectory was reconstructed in four single revolution fits from MSFN tracking data. The three segments of interest here were MSFN free flight fits on revolutions 14, 25, and 26.

Trajectories for the LM free flight segments were also reconstructed from MSFN tracking data. The ground based MSFN tracking available for use during the periods of interest are summarized in timeline form in Figure 7-2.

The CSM trajectory was fixed as the reference, and the LM MSFN free flight trajectories were then used to initialize fits based on onboard data in the four segments where relative data were available. A priori confidence values of 10,000 feet were placed on each component of position and 10 feet per second on each component of velocity in the initial conditions.

The reconstruction activities will be discussed in more detail in the following sections. In addition, various tables and figures are included which serve to describe the operations performed and show the accuracy and validity of the data.

7.3.2 Onboard Measurements

Rendezvous radar data were obtained during three periods of the Apollo 11 mission; these were Insertion to CSI (9 observations), CSI to CDH (20 observations), and CDH to TPI (45 observations). As in previous missions, the amount of rendezvous radar data obtained was limited to those periods when telemetry coverage was available.

VHF ranging data were obtained from the CSM during four segments of the flight; these were DOI to PDI (18 observations), insertion to CSI (2 observations), CSI to CDH (17 observations), and CDH to TPI (12 observations). Since only two observations were obtained from Insertion to CSI, no meaningful statistics could be obtained.

Sextant data were obtained during the same periods of flight as were VHF ranging data; 13 observations between DOI and PDI, 4 observations from insertion to CSI, 21 observations from CSI to CDH, and 10 observations between CDH and TPI. Listings of all the data are included in Appendix D.

7.3.3 Evaluation of Onboard Tracking Data

Rendezvous Radar Data

In order to determine the quality of the rendezvous radar data, the residuals (differences between the actual measured value and a measurement value computed from given CSM and LM trajectories) were examined. The CSM trajectories used in obtaining these residuals were the BET's discussed in Section 7.2 of this report (one rev MSFN free flight fits). The LM trajectories were obtained by using technique (c) described in paragraph 7.2.1 (onboard free flight fits). All available onboard data were used in these fits.

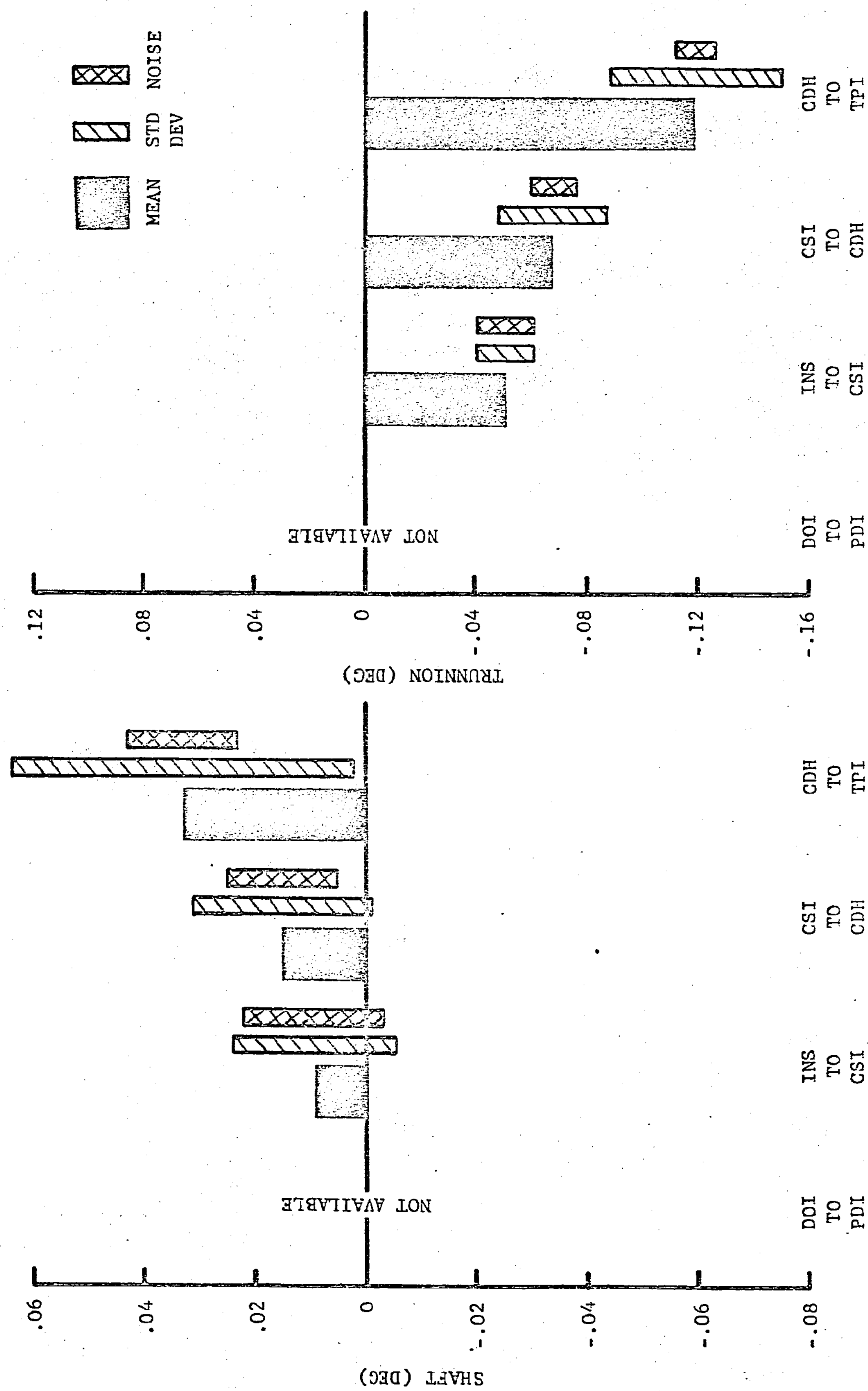
Table 7.5 lists residual statistics (mean, standard deviation, one-sigma noise estimate) computed from the onboard free flight fits of each segment and Figures 7-3a and 7-3b illustrate the results graphically. The data were generally well behaved as can be seen in the residual plots (Figures 7-4 through 7-6). The relatively large differences between the standard deviation and noise computed for shaft and trunnion in the CSI to CDH and CDH to TPI periods can partly be attributed to the fact that both rendezvous radar and sextant data were used in the fit. As the two data sets become more equal in size (weighted effect) or the sampling arcs more coincident, residual statistics deteriorate. This effect is demonstrated by the statistics listed in Table 7.6 which were obtained from fits made with only rendezvous radar data included. Note that when sextant data is eliminated, the RR shaft and trunnion means and deviations decrease in all segments. The shaft statistics are still relatively high (especially in the CDH and TPI period), indicating that a systematic error is still present in the shaft measurement. It should also be noted that the rendezvous radar residual statistics from Apollo 10 exhibited a similar characteristic (Reference 1). In Apollo 10, the standard deviations for both shaft and trunnion measurement are relatively large in the CDH to TPI period (no sextant data were included in Apollo 10 solutions). The large mean values seen in Table 7.5 are also a result of the inclusion of sextant data in the solution data sets. When only rendezvous radar data was included, the mean values decreased to near zero values.

The range residual statistics exhibited characteristics similar to the Apollo 10 data. When VHF ranging data is removed from the solution data set, standard deviations decrease and become, in two segments, almost equal to noise estimates. The mean values also approach zero, indicating that no bias is present.

Table 7.5 Summary of Rendezvous Radar Residual Statistics

	Insertion To CSI	CSI To CDH	CDH To TPI	
Shaft (deg)	.009	.015	.033	Mean
	.015	.016	.031	S. Dev.
	.013	.010	.010	Noise
Trunnion (deg)	-.051	-.068	-.119	Mean
	.010	.019	.031	S. Dev.
	.010	.008	.007	Noise
Range (feet)	79.	75.	55.	Mean
	144.	63.	92.	S. Dev.
	39.	37.	27.	Noise
Range Rate (fps)	.604	-.243	-.306	Mean
	.173	.339	.277	S. Dev.
	.6278	.6278	.6278	Q. E.*

* Quantization Error.


MEAN
STD DEV
NOISE
TRUNNION (DEG)
.12
.08
.04
0
-.04
-.08
-.12
-.16
NOT AVAILABLE
DOI TO PDI
INS TO CSI
CSI TO CDH
CDH TO TPI
SHAFT (DEG)
.06
.04
.02
0
-.02
-.04
-.06
-.08
NOT AVAILABLE
DOI TO PDI
INS TO CSI
CSI TO CDH
CDH TO TPI

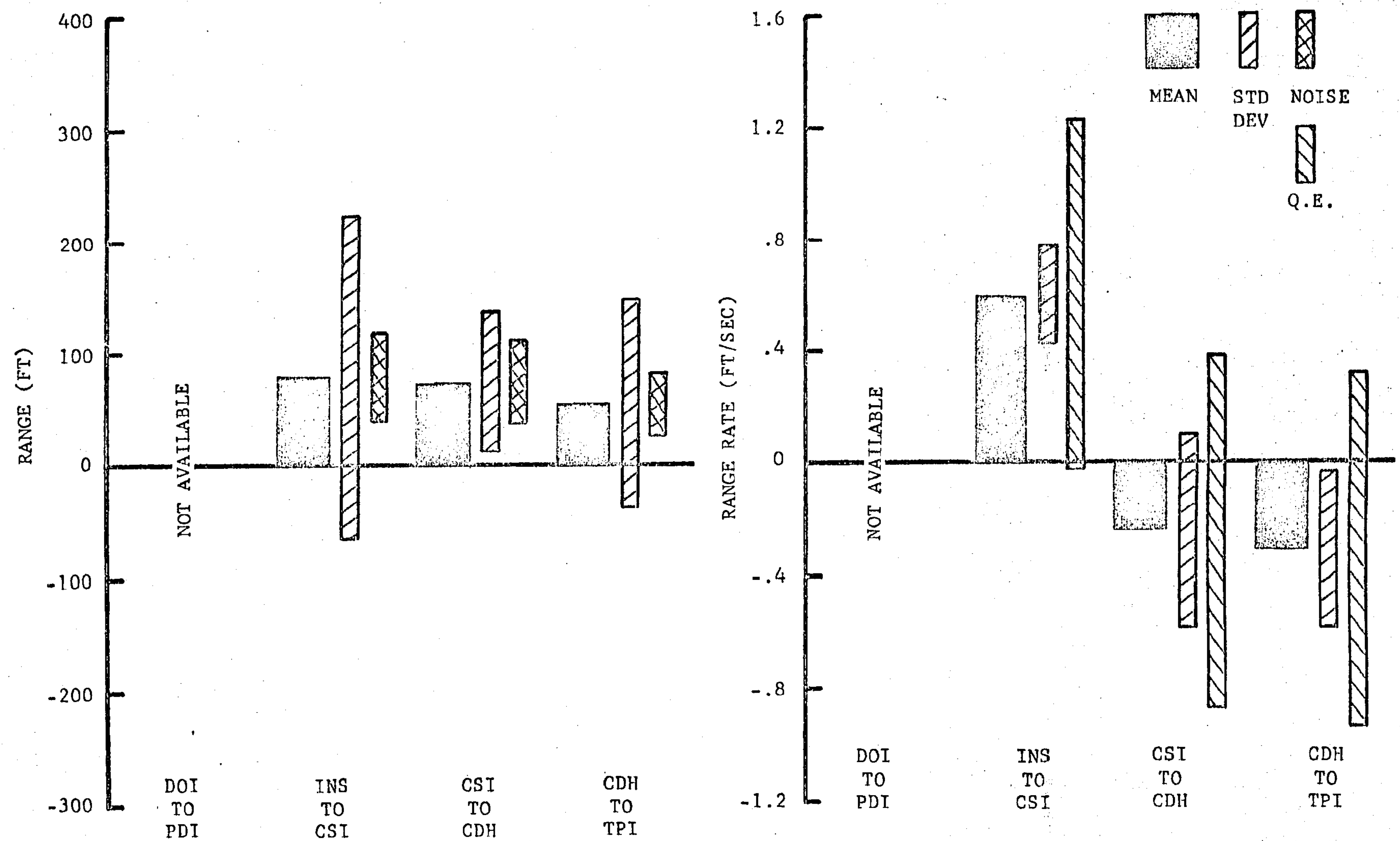
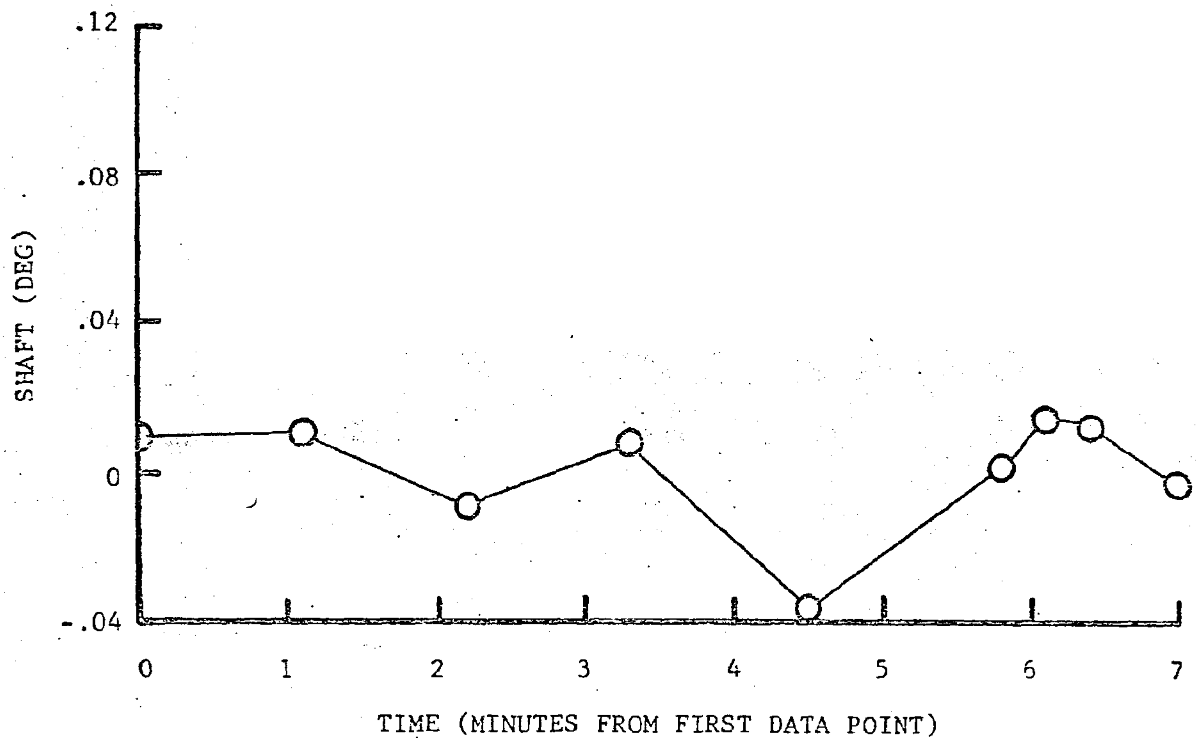


Figure 7-3b Rendezvous Radar Range and Range Rate Residual Statistics



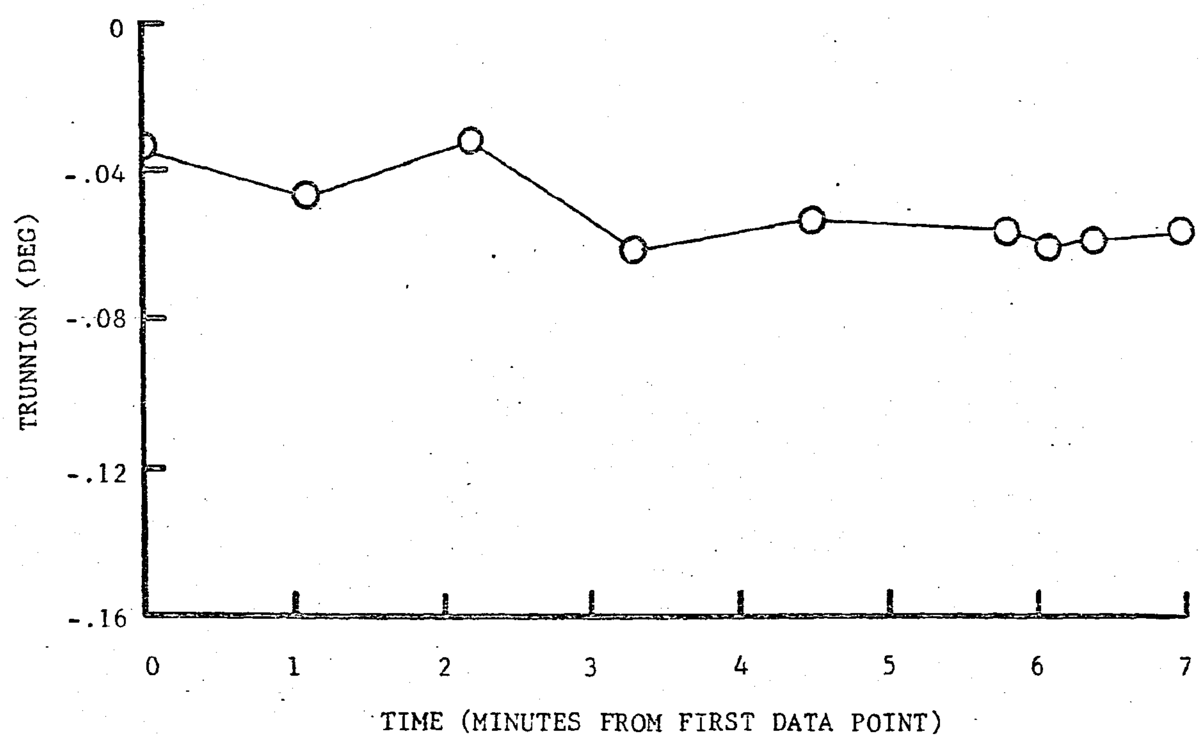
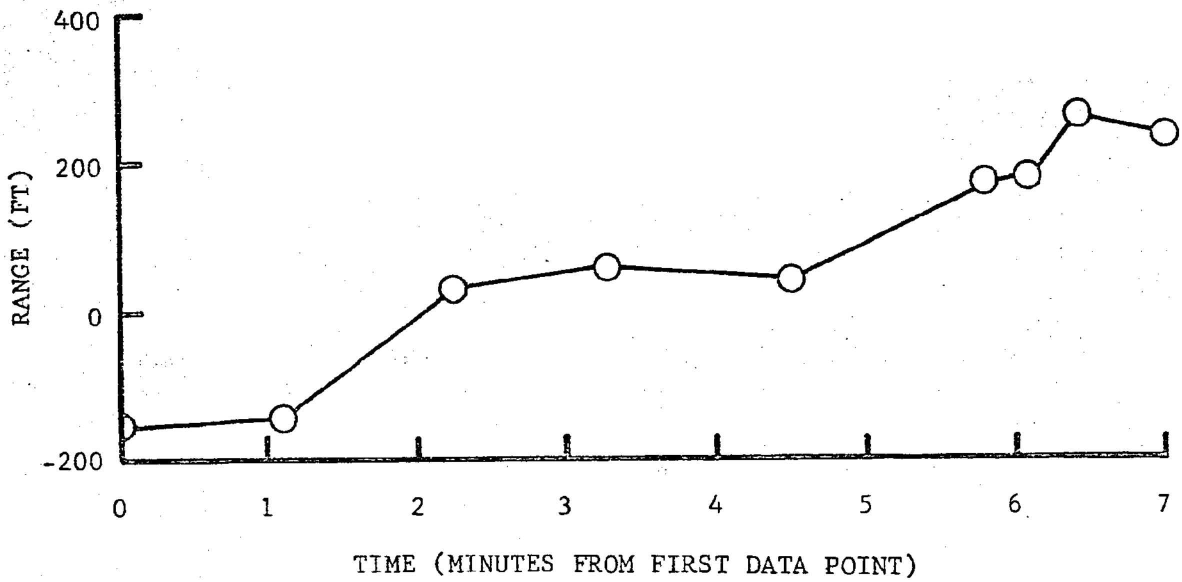


Figure 7-4 Rendezvous Radar Residuals (Insertion to CSI)



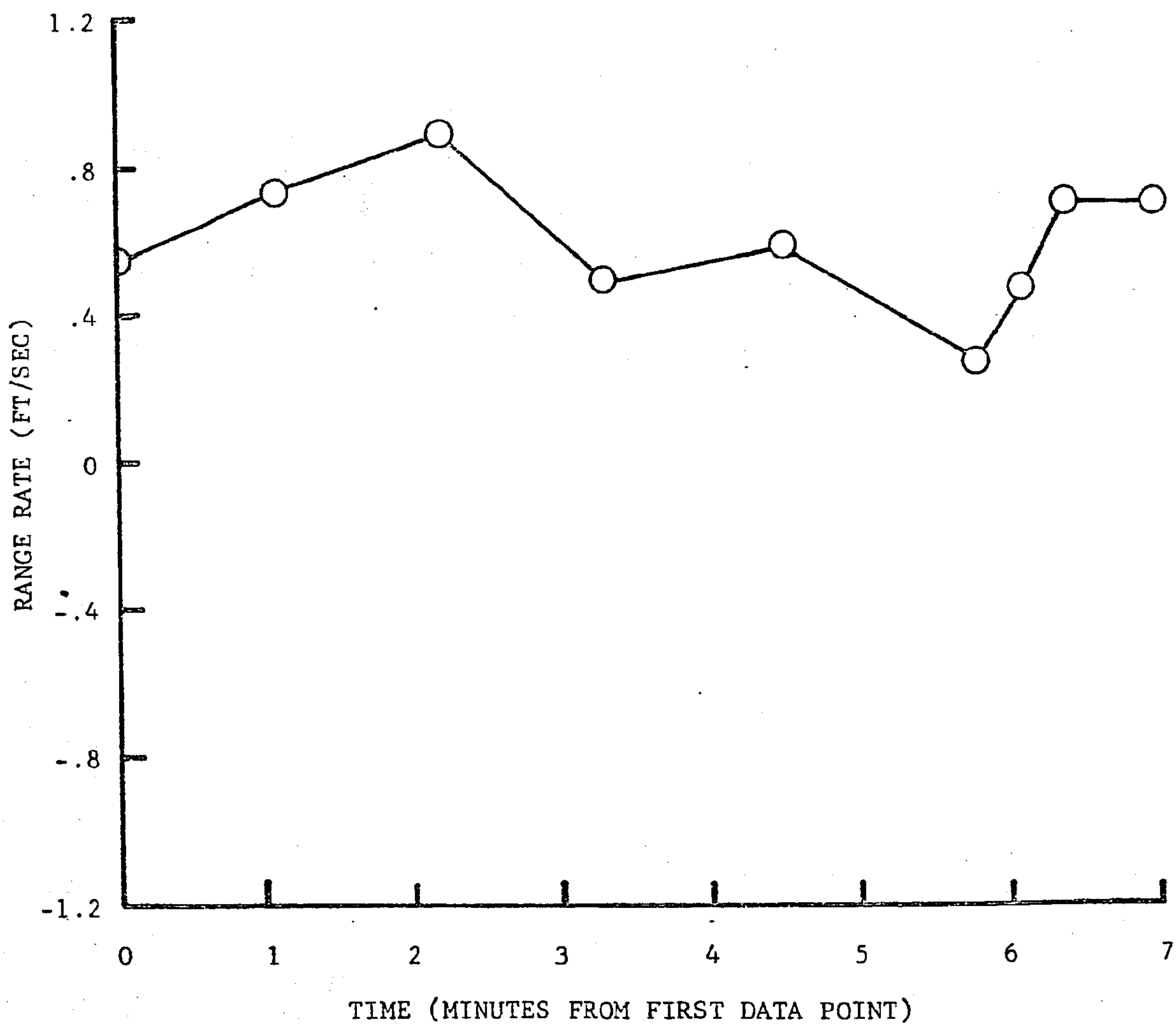


Figure 7-4 Concluded

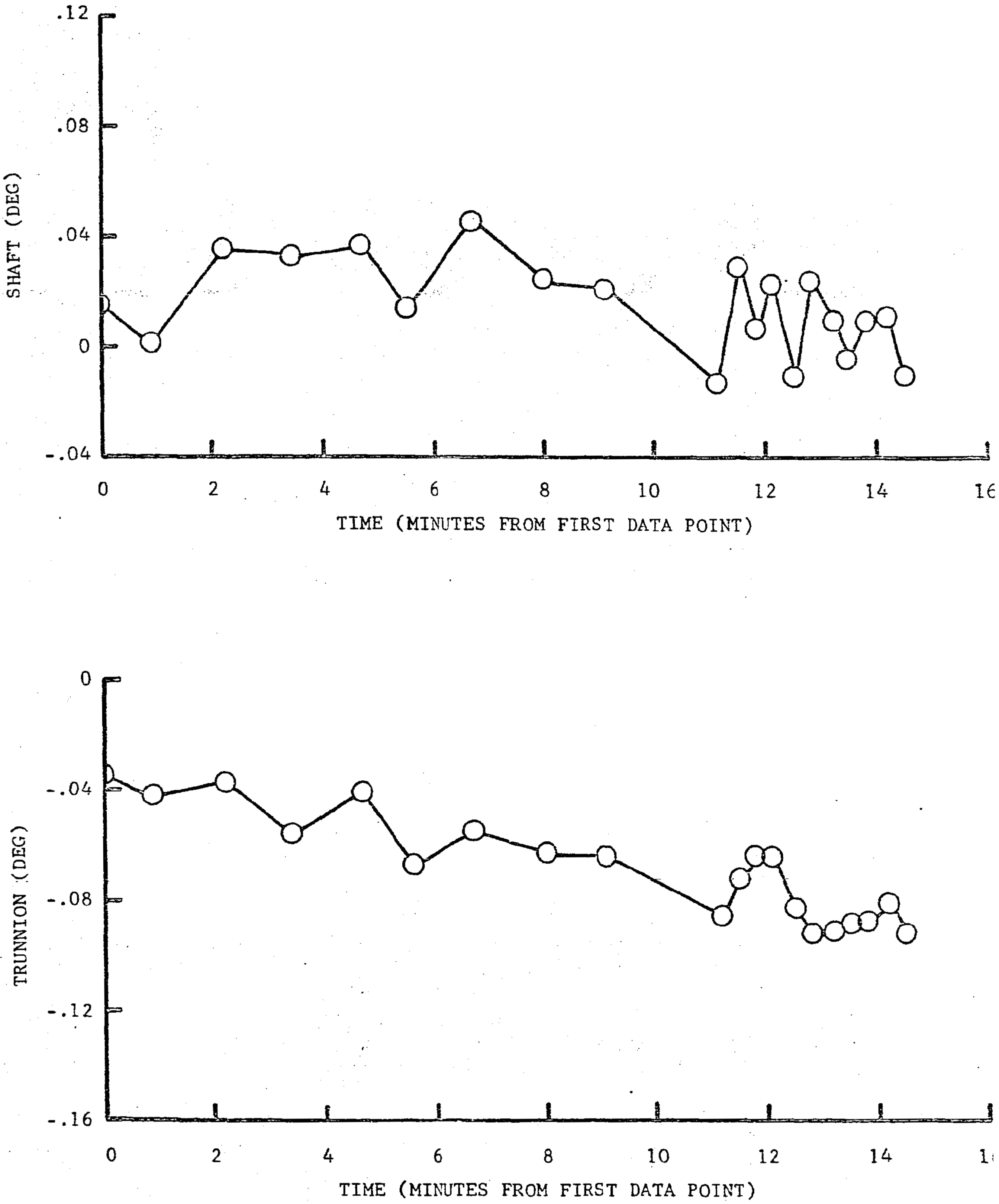


Figure 7-5 Rendezvous Radar Residuals (CSI to CDH)

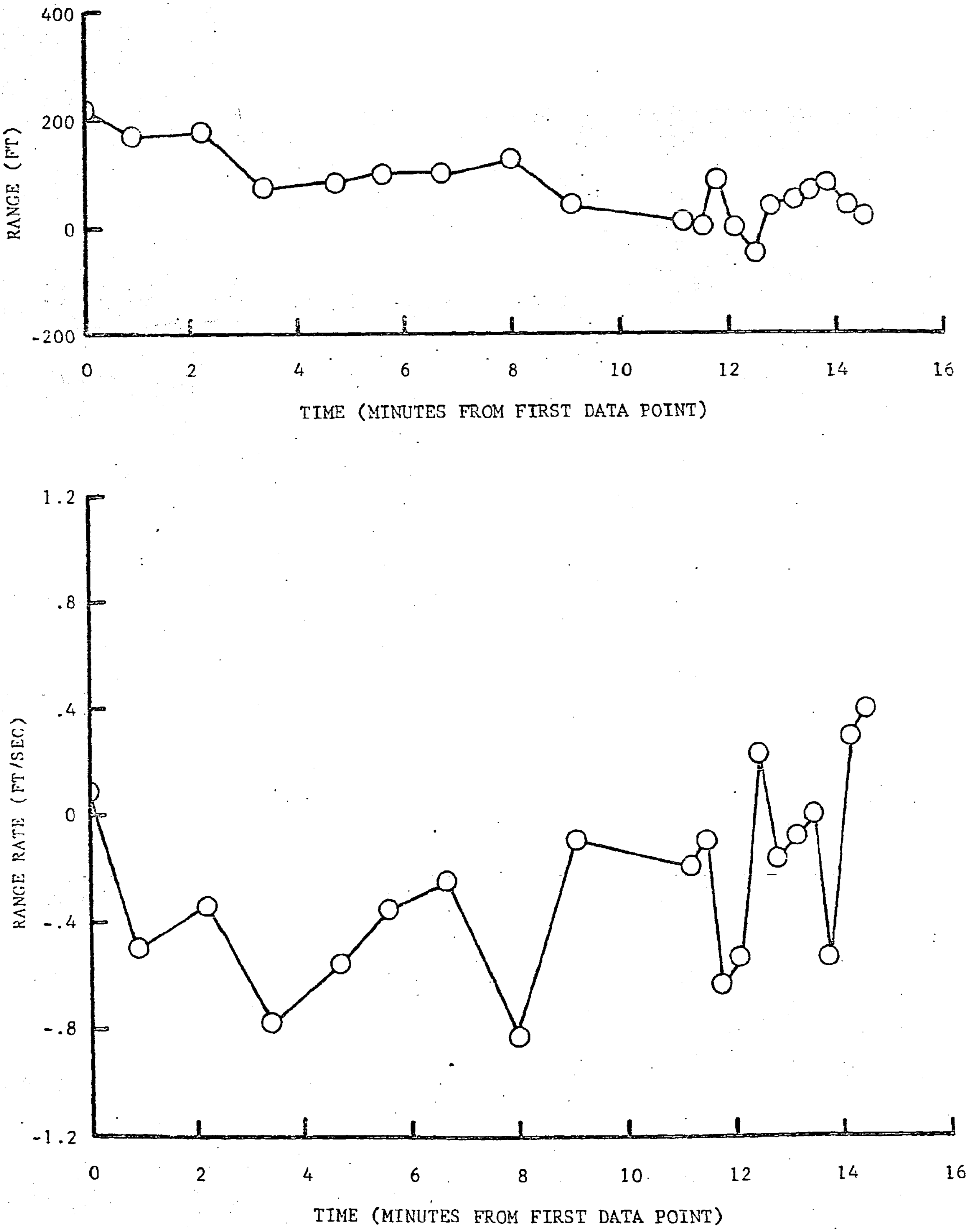


Figure 7-5 Concluded

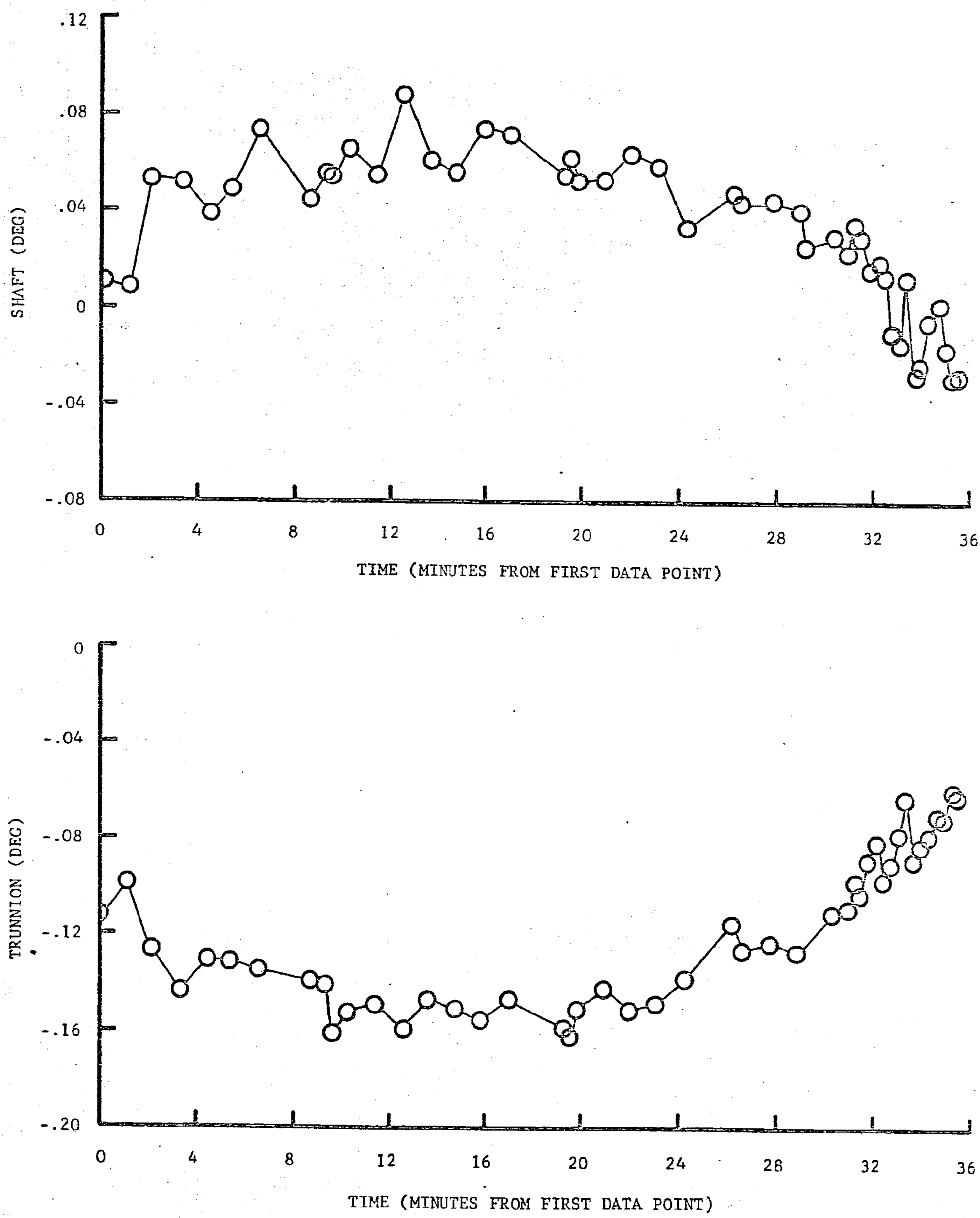


Figure 7-6 Rendezvous Radar Residuals (CDH to TPI)

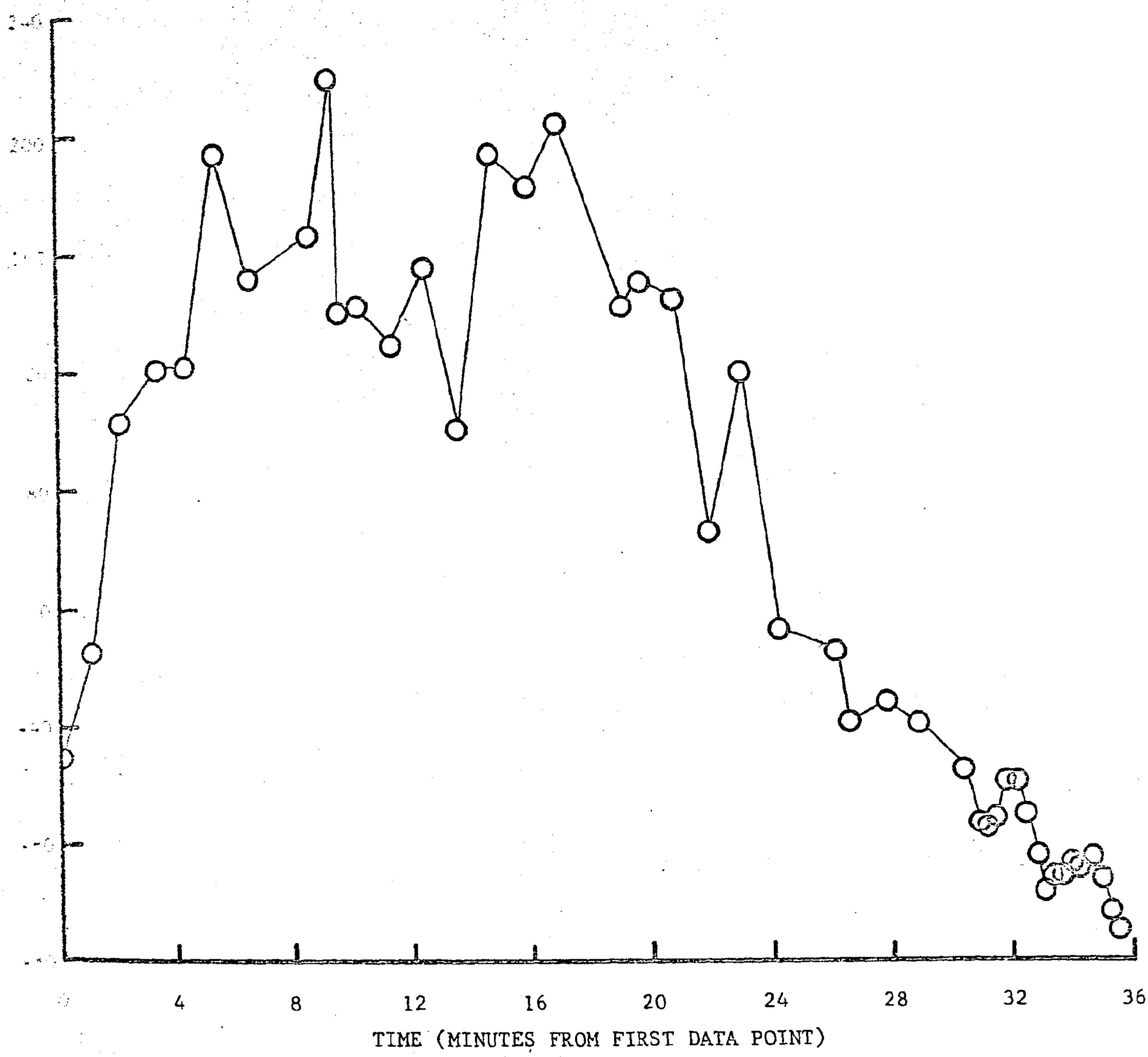


Figure 7-6 Continued

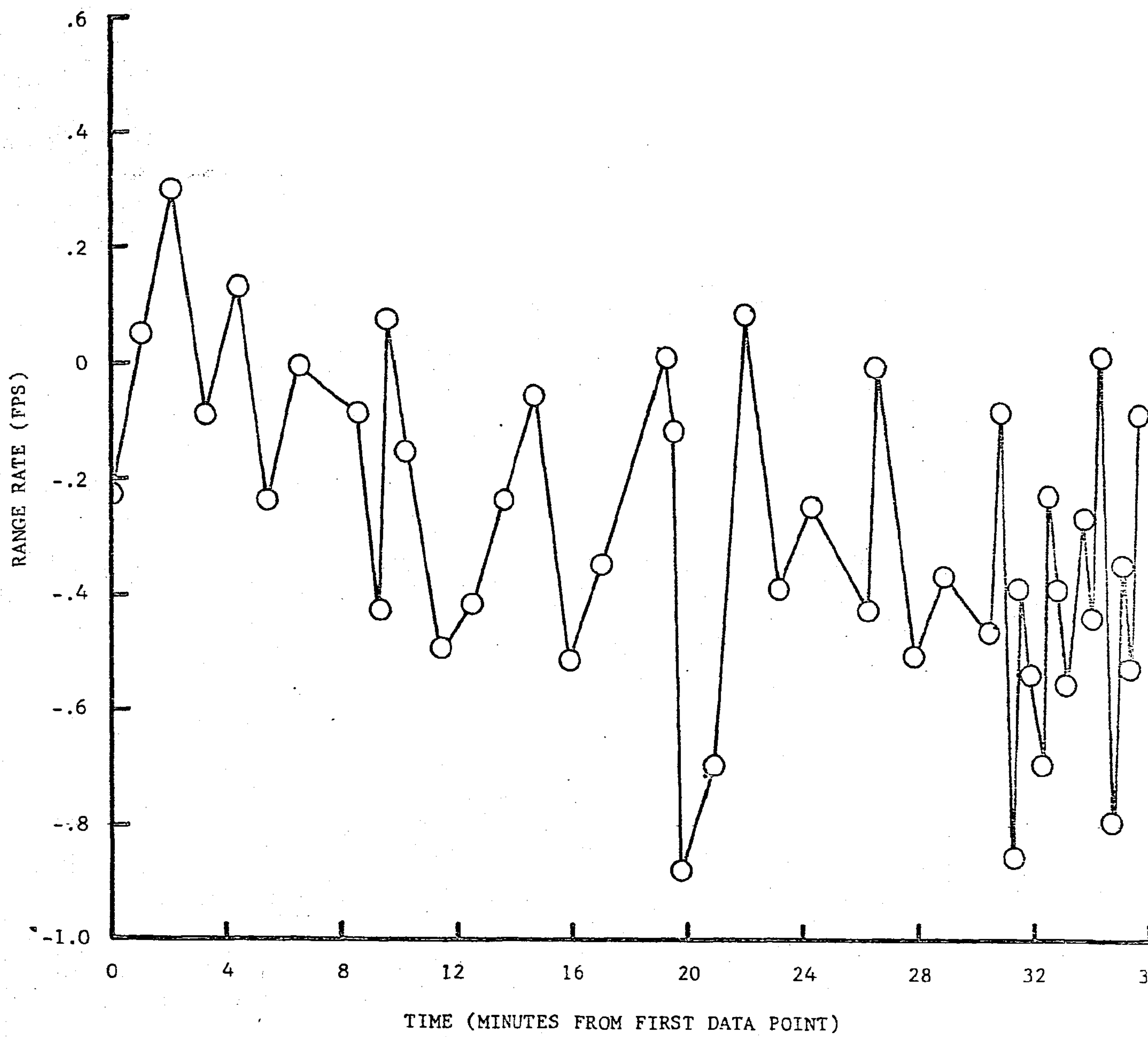


Figure 7-6 Concluded

Table 7.6 Rendezvous Radar Only Solution Residual Statistics

	INS-CSI	CSI-CDH	CDH-TPI	
Shaft	-.00007	.00028	.018	Mean
	.015	.014	.031	S. Dev.
Trunnion	-.00013	.00002	-.0005	Mean
	.0066	.0074	.0085	S. Dev.
Range	.55	.026	2.89	Mean
	39.	37.2	72.45	S. Dev.
Range Rate	-.343	-.105	-.196	Mean
	.187	.314	.304	S. Dev.

The range rate residuals were also of good quality. Mean values were all less than the downlink readout error (.6278 fps).

One sigma noise calculations for shaft, trunnion, and range rate from three missions are plotted as a function of average range in Figures 7-7 through 7-9. These figures show that the Apollo 11 noise estimates compare well with similar estimates from missions 9 and 10. Note that no definite trend is apparent in the angular noise as relative range varies. Figure 7-9 does seem to indicate, however, that the noise estimate for the range measurement does increase as average range increases. The Apollo 11 noise estimates for all three observables appear to be generally smaller than those obtained from previous missions.

VHF Ranging Data

Table 7.7 contains a summary of VHF ranging data residual statistics obtained from onboard free flight fits made over the three segments where adequate amounts of data were available. Figures 7-10, 7-11, and 7-12 contain plots of these residuals. Since only two observations were obtained from the insertion to CSI segment, only the DOI to PDI (18 observations), CSI to CDH (17 observations), and CDH to TPI (12 observations) segments are considered.

The VHF ranging data were generally of good quality. As expected, the smallest mean value was obtained during the DOI to PDI period when VHF ranging was the only range data type measuring the distance between vehicles. The mean values become increasingly large as more rendezvous radar data are included in the data set or as the data arcs become coincident in time. This can be seen in the large mean value for the CDH to TPI period. This large mean, however, is still within the bias specification limit of ±270 feet.

Figure 7-13 shows that the calculated noise values compare favorably with Apollo 10 results and are relatively constant when compared to those obtained from Apollo 10. The residual statistics listed in Table 7.7 are illustrated graphically in Figure 7-14.

Sextant

The residual statistics shown in Table 7.8 indicate that the CSM sextant is a very accurate instrument. Sextant observations were obtained

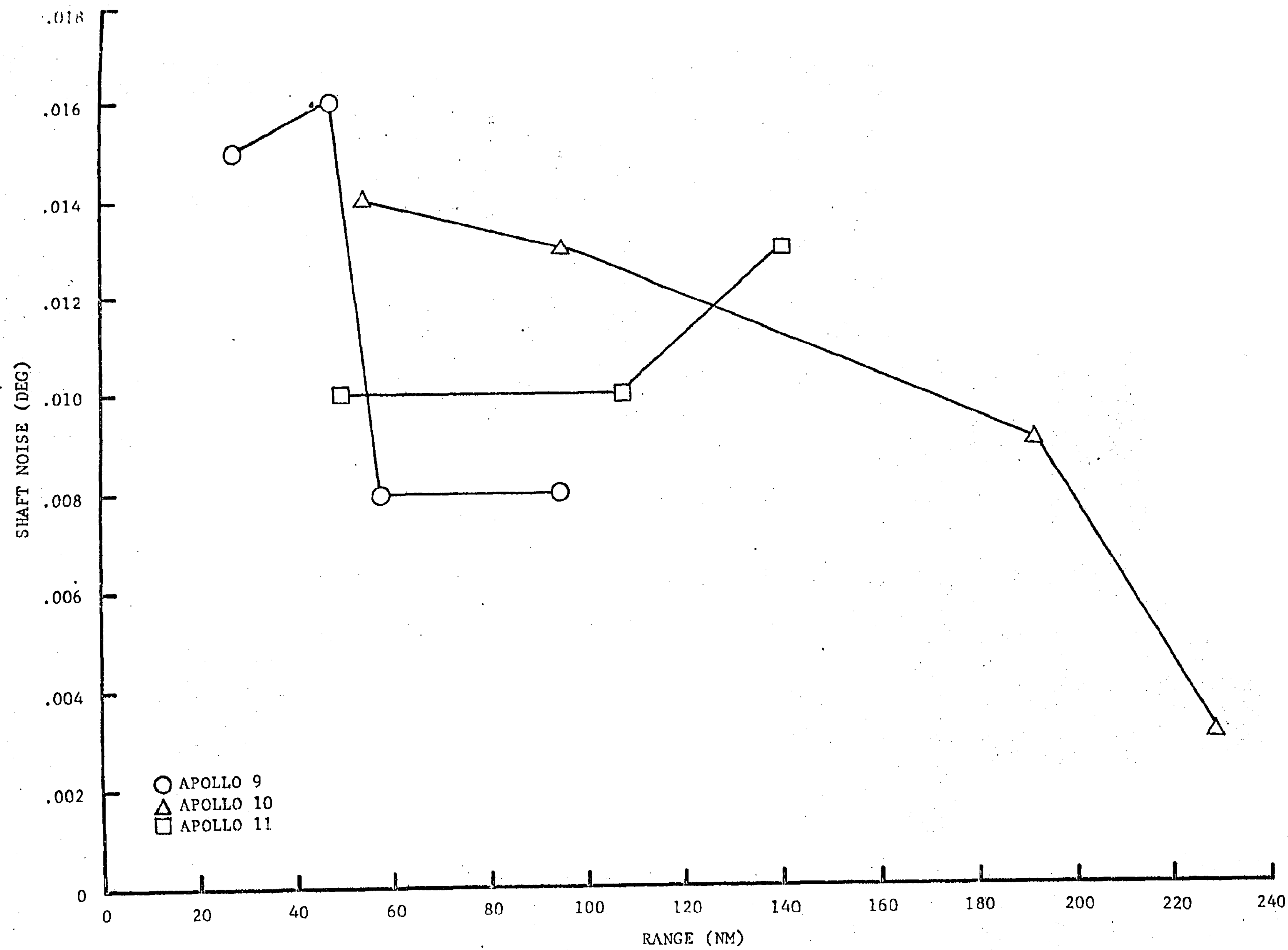


Figure 7-7 Rendezvous Radar Shaft Noise as a Function of Average Range

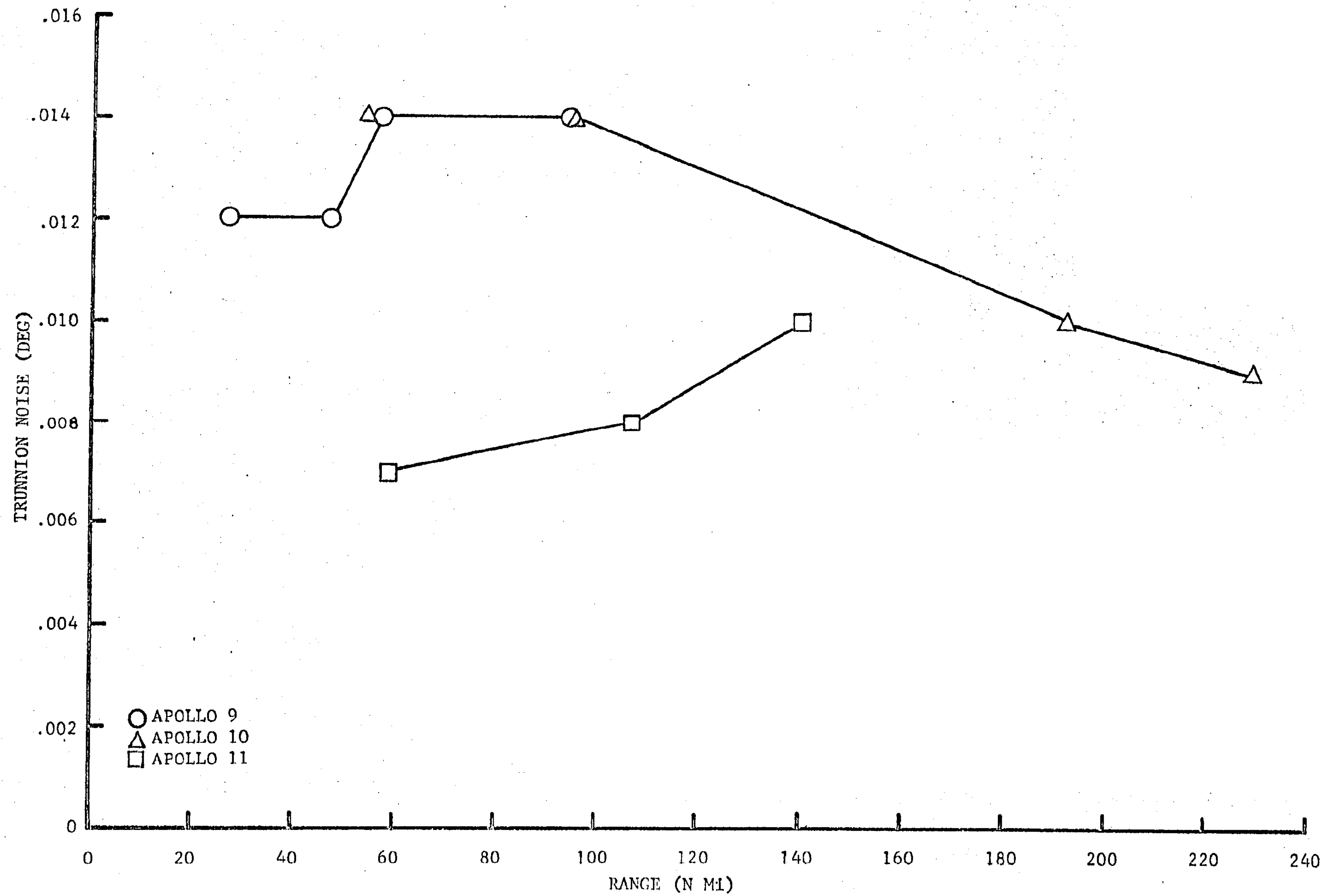


Figure 7-8 Rendezvous Radar Trunnion Noise as a Function of Average Range

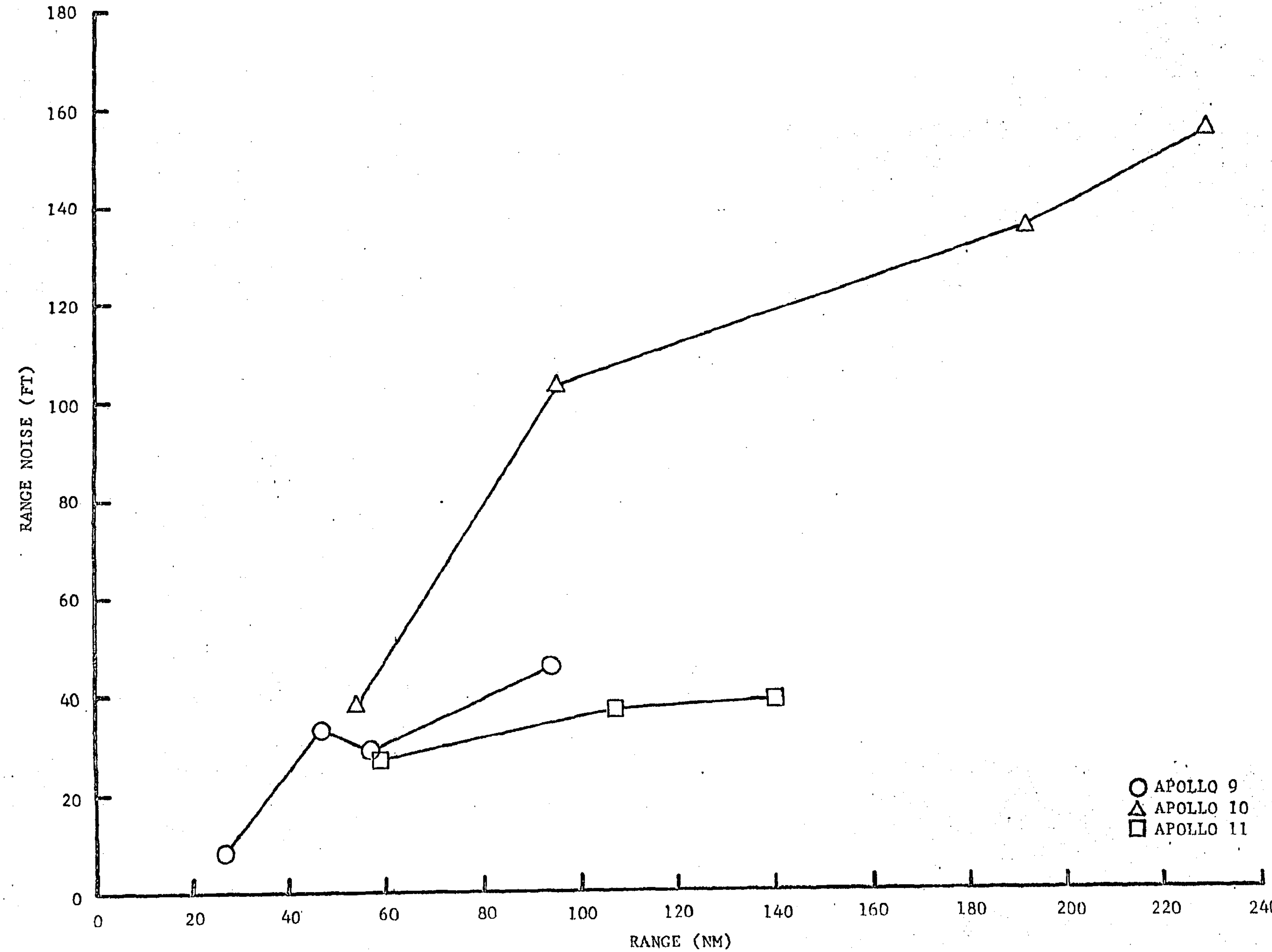


Figure 7-9 Rendezvous Radar Range Noise as a Function of Average Range

Table 7.7 Summary of VHF Ranging Residual Statistics

		DOI-PDI	CSI-CDH	CDH-TPI	
Range (feet)		-26.	-86.	-216.	Mean
		74.	104.	48.	S. Dev.
		23.	23.	19.	Noise

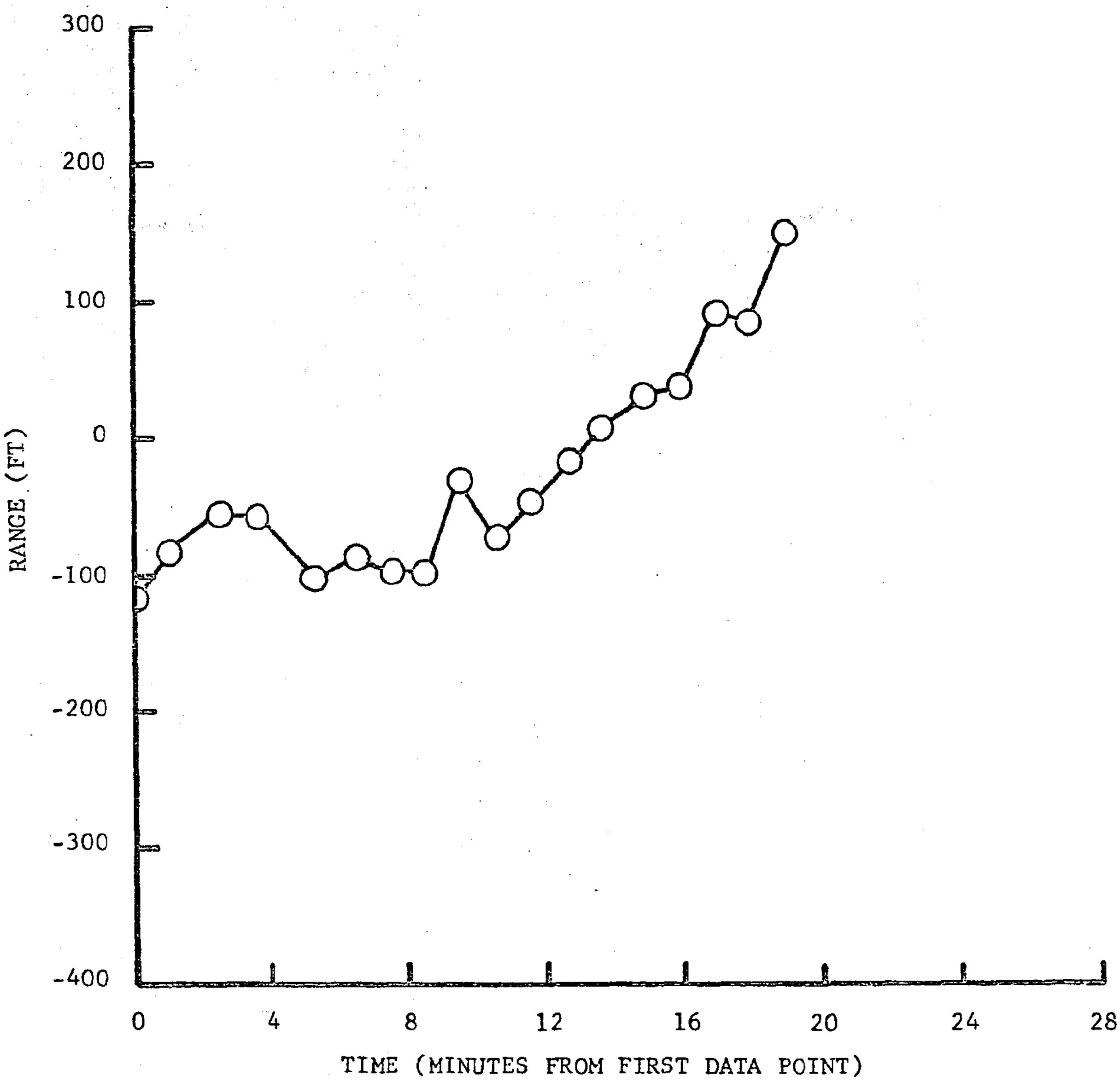


Figure 7-10 VHF Ranging Residuals (DOI to PDI)

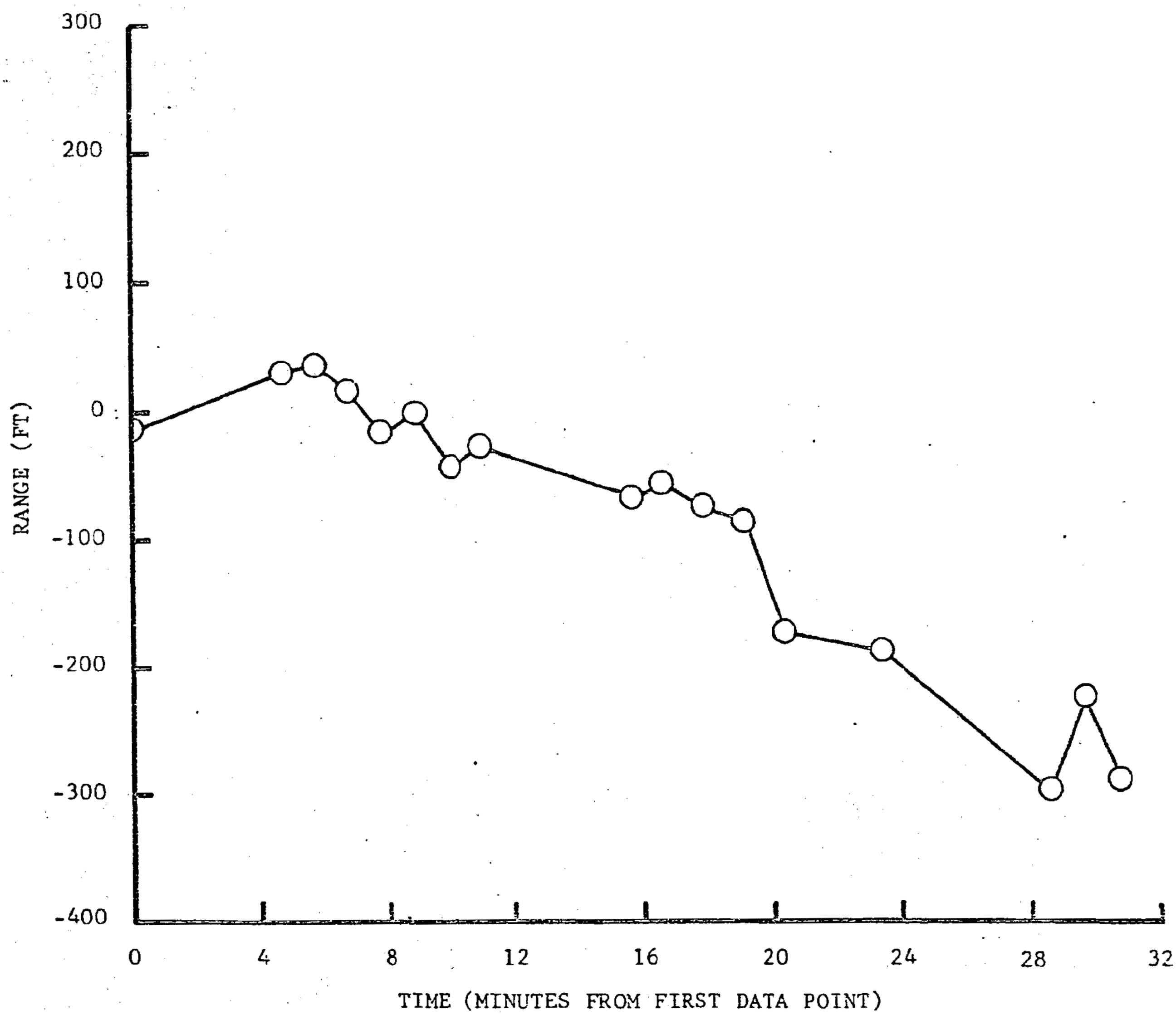


Figure 7-11 VHF Ranging Residuals (CSI to CDH)

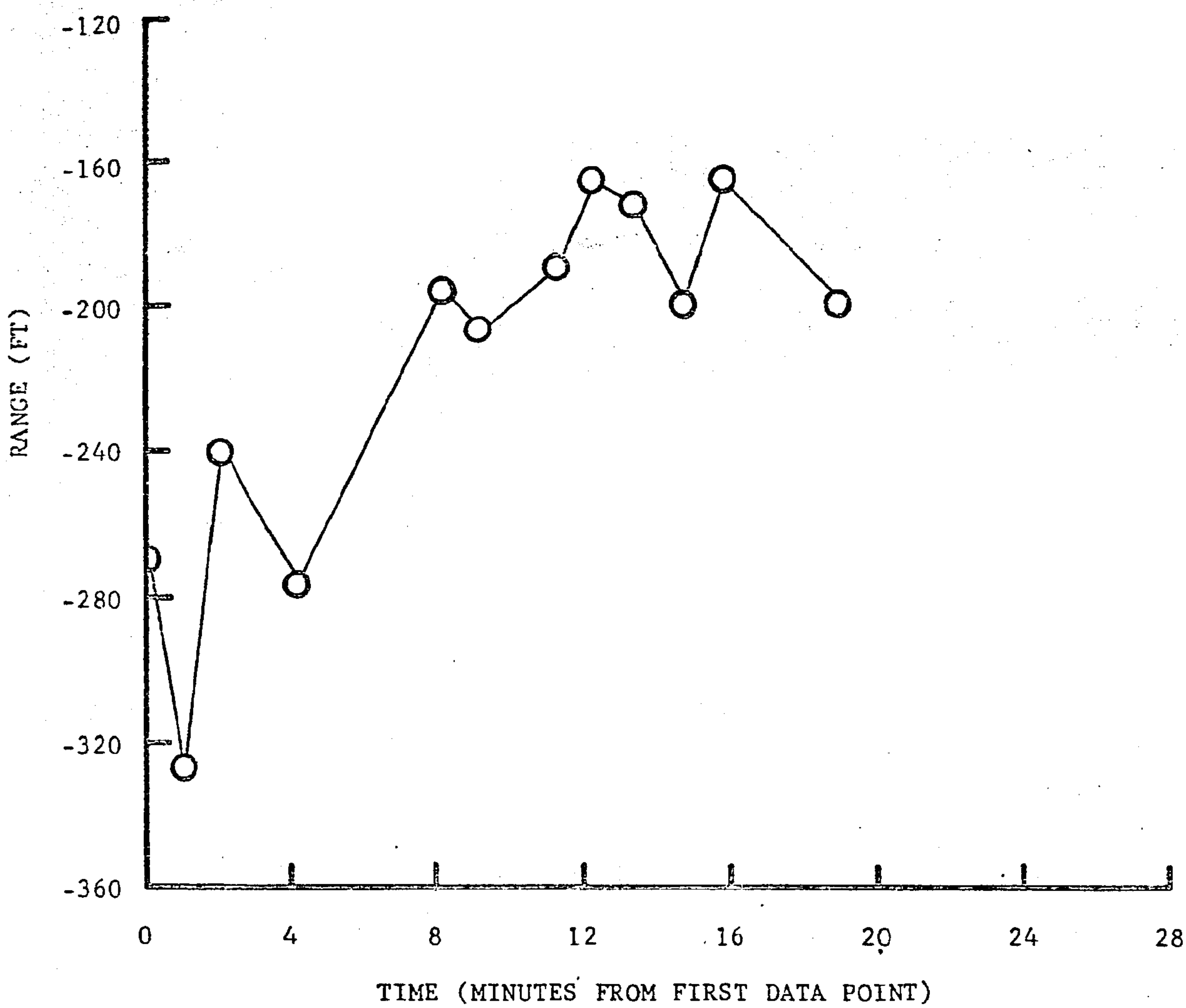


Figure 7-12 VHF Ranging Residuals (CDH to TPI)

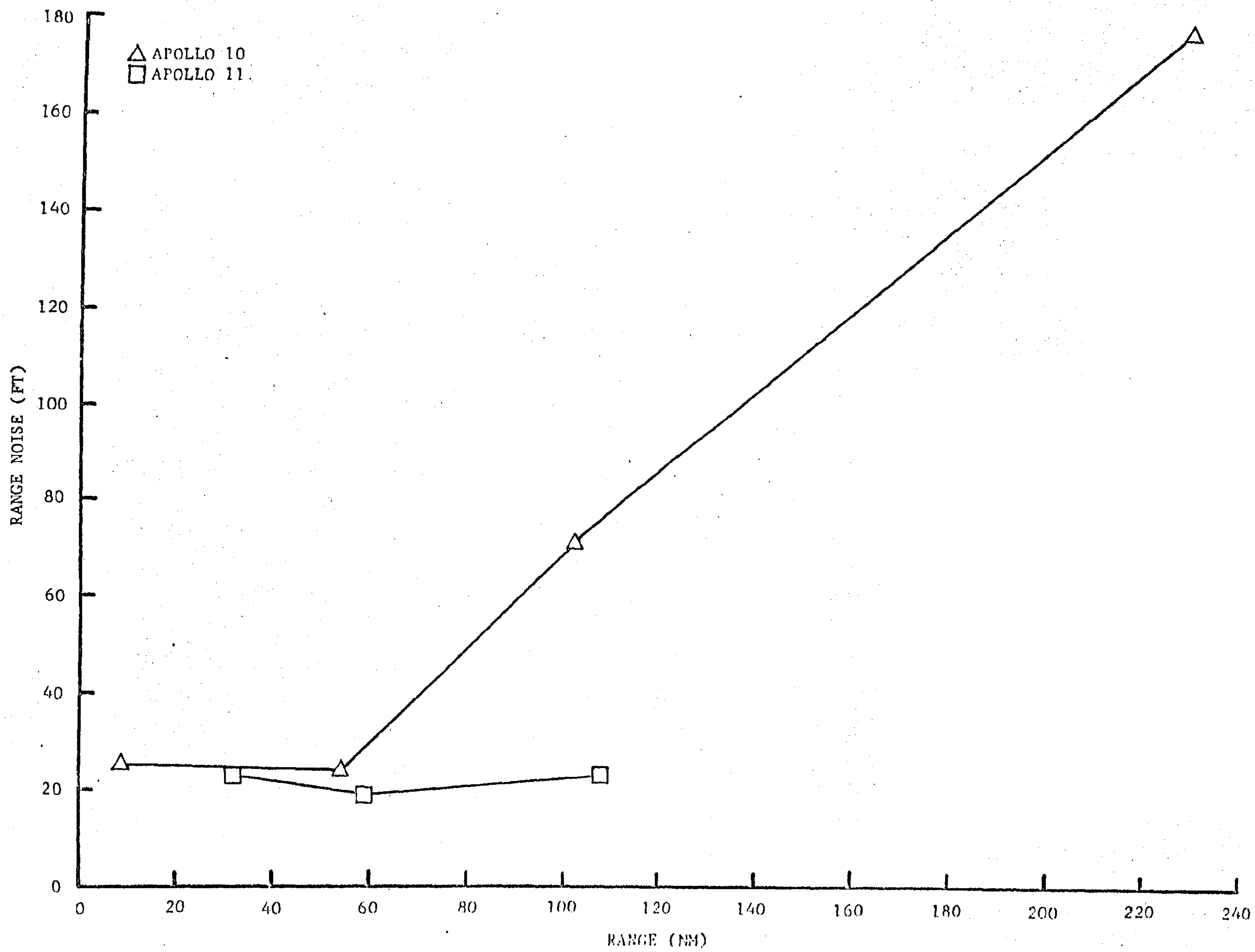


Figure 7-13 VHF Ranging Noise as a Function of Average Range

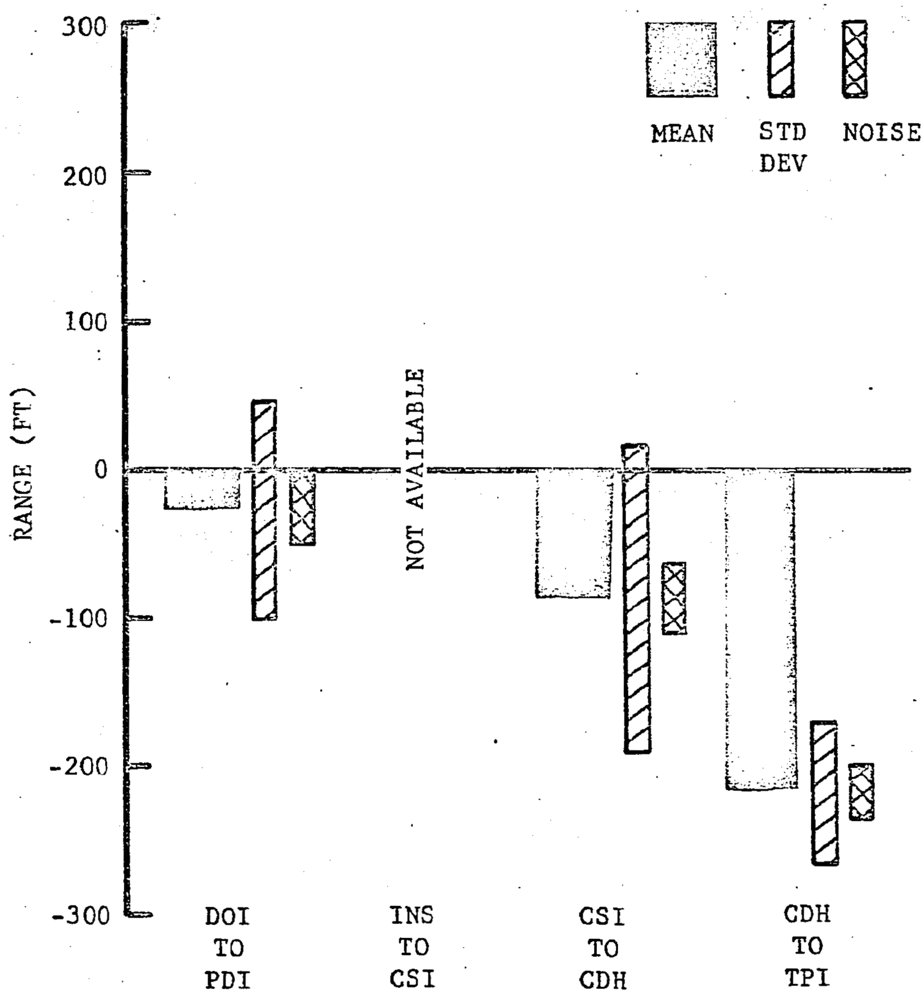


Figure 7-14 VHF Ranging Residual Statistics

Table 7.8 Summary of Sextant Residual Statistics

	DOI To PDI	Insertion To CSI	CSI To CDH	CDH To TPI	
Shaft (deg)	-.001	.0005	.0002	.0017	Mean
	.015	.005	.011	.013	S. Dev.
	.014	Insufficient Data	.010	.011	Noise
Trunnion (deg)	-.0004	-.000009	.0004	-.001	Mean
	.004	.003	.006	.008	S. Dev.
	.003	Insufficient Data	.006	.011	Noise

in four of the free flight segments; DOI to PDI (13 sightings), insertion to CSI (4 sightings), CSI to CDH (21 sightings), CDH to TPI (10 sightings).

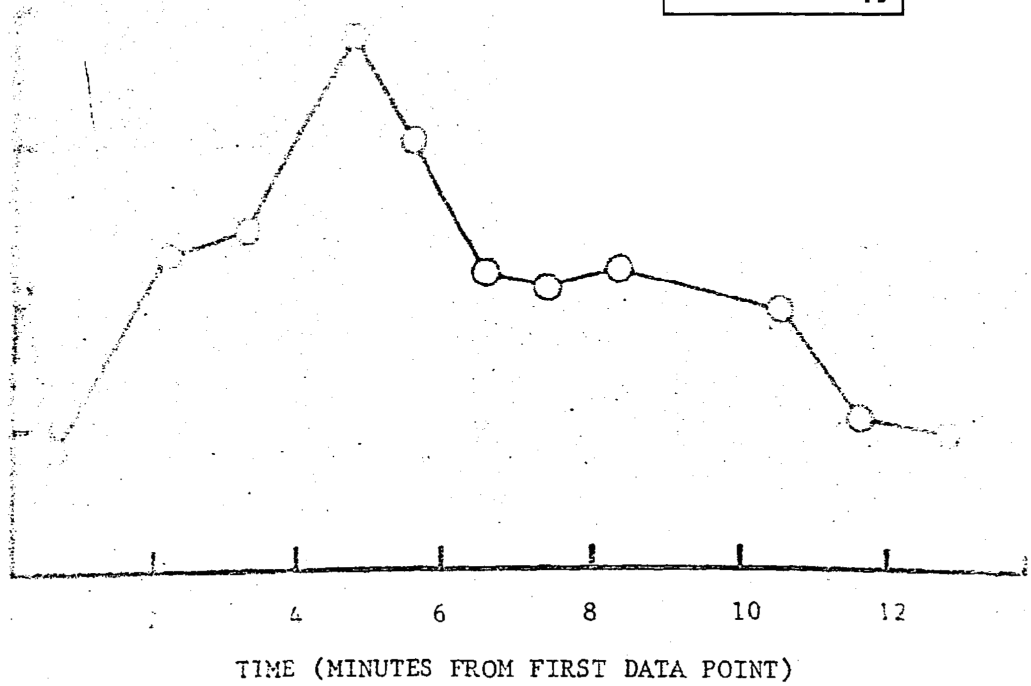
The close agreement of the standard deviations with the noise estimates and the very small means listed indicate that there are essentially no biases in either angle.

The residual patterns (Figures 7-15 through 7-18) are very well behaved. The random noise estimates (Figure 7-19) compare well with rendezvous radar angular noise estimates and no trend can be identified with respect to average range. Note the good agreement with the Apollo 9 noise estimates plotted in Figure 7-19.

Onboard Tracking Data Consistency

In order to determine the consistency of trajectories reconstructed from onboard tracking data with those obtained from MSFN tracking data, state vector comparisons were made over the propagation intervals. These comparisons were made in a UVW-type coordinate system and the results are presented in graphic form. In the figures presented, RZ is the negative of the U or radial component, RX is the V or downrange component, and RY is the negative of the W or crossrange component of a system centered at the CSM. RXD, RYD and RZD are the respective velocities.

Three LM trajectories were obtained for the period from DOI to PDI. Figure 7-21 plots (as a function of time) the out-of-plane component of LM position relative to the CSM for a MSFN free flight trajectory, an onboard data free flight trajectory, and the final BET (combined high speed MSFN and onboard tracking data). It can be seen that the addition of onboard tracking data drastically improves this component of position. Figures 7-22 and 7-23 show the differences between relative trajectories obtained from the MSFN and from the onboard tracking free flight fits. There are large differences in the trajectories which are primarily due to the poor quality of the MSFN free flight fit, but the comparisons do show that the downrange and radial components compare fairly well inside the MSFN data arc.



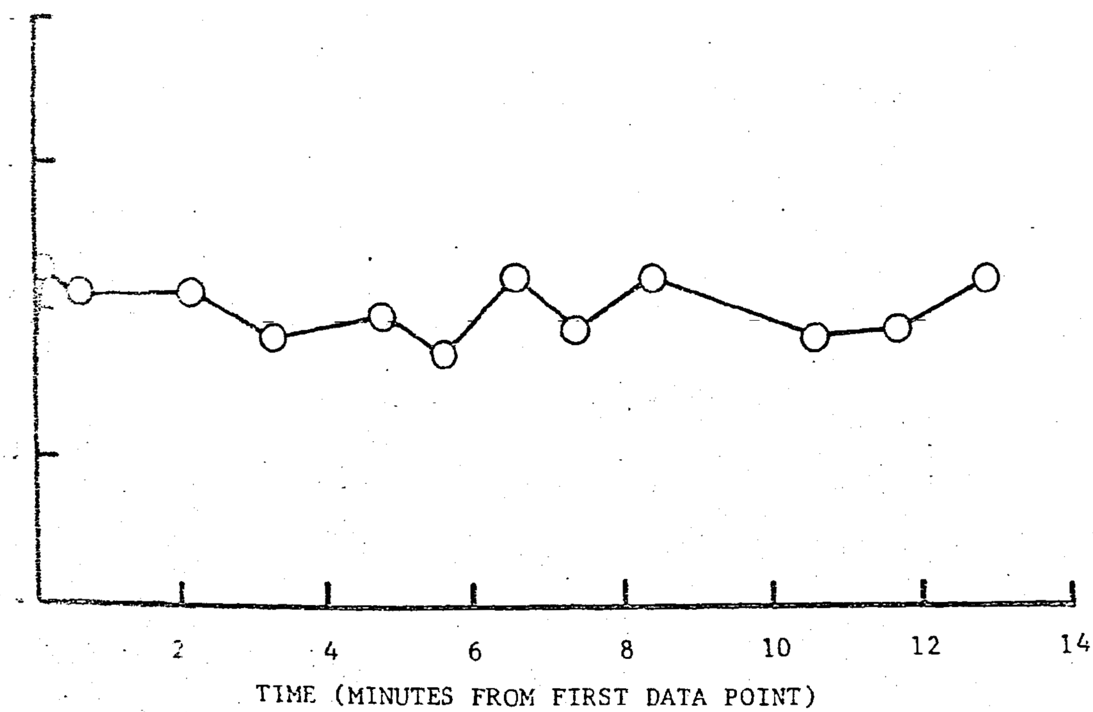


Figure 7-15 Sextant Residuals (DOI to PDI)

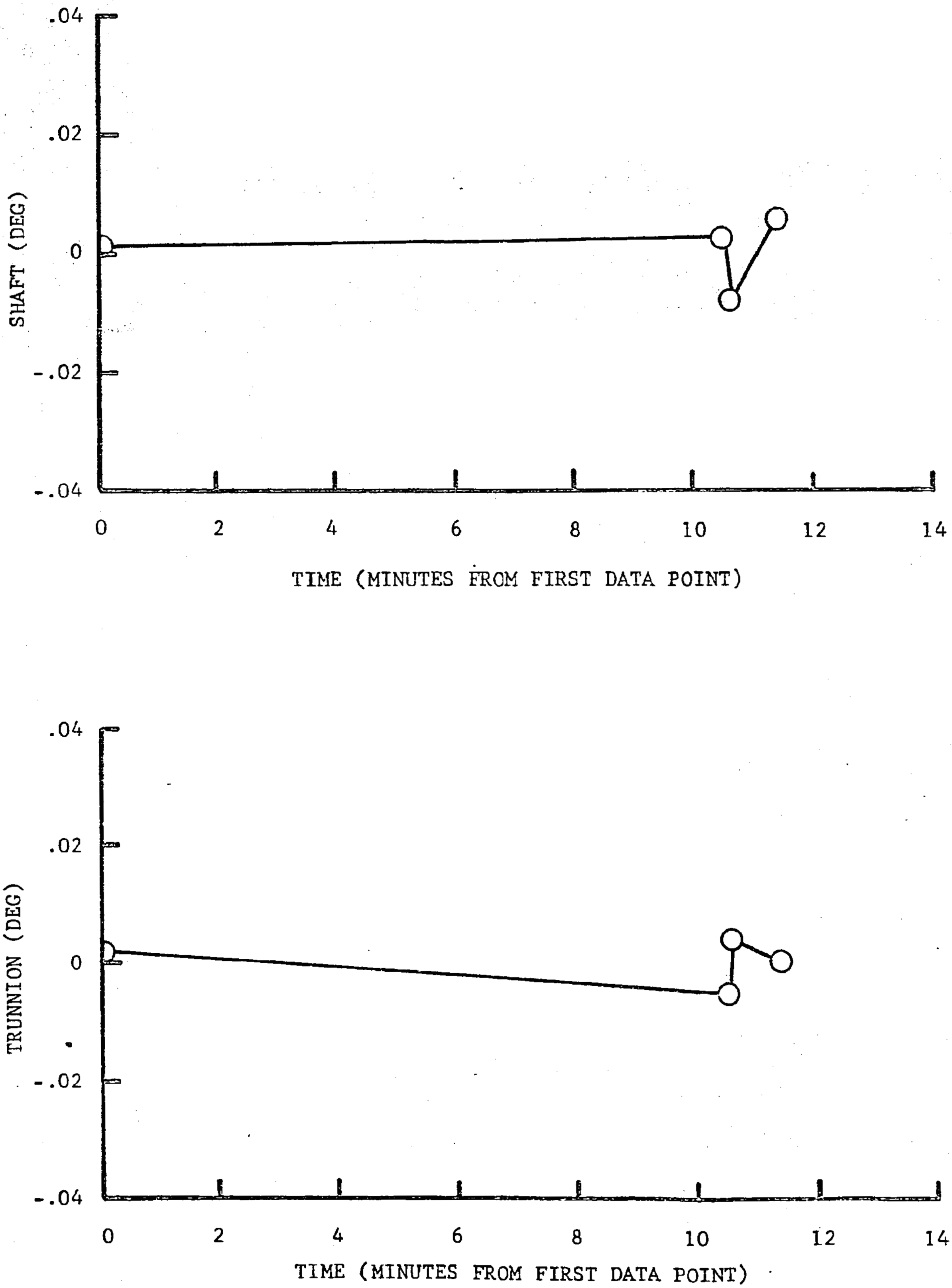


Figure 7-16 Sextant Residuals (Insertion to CSI)

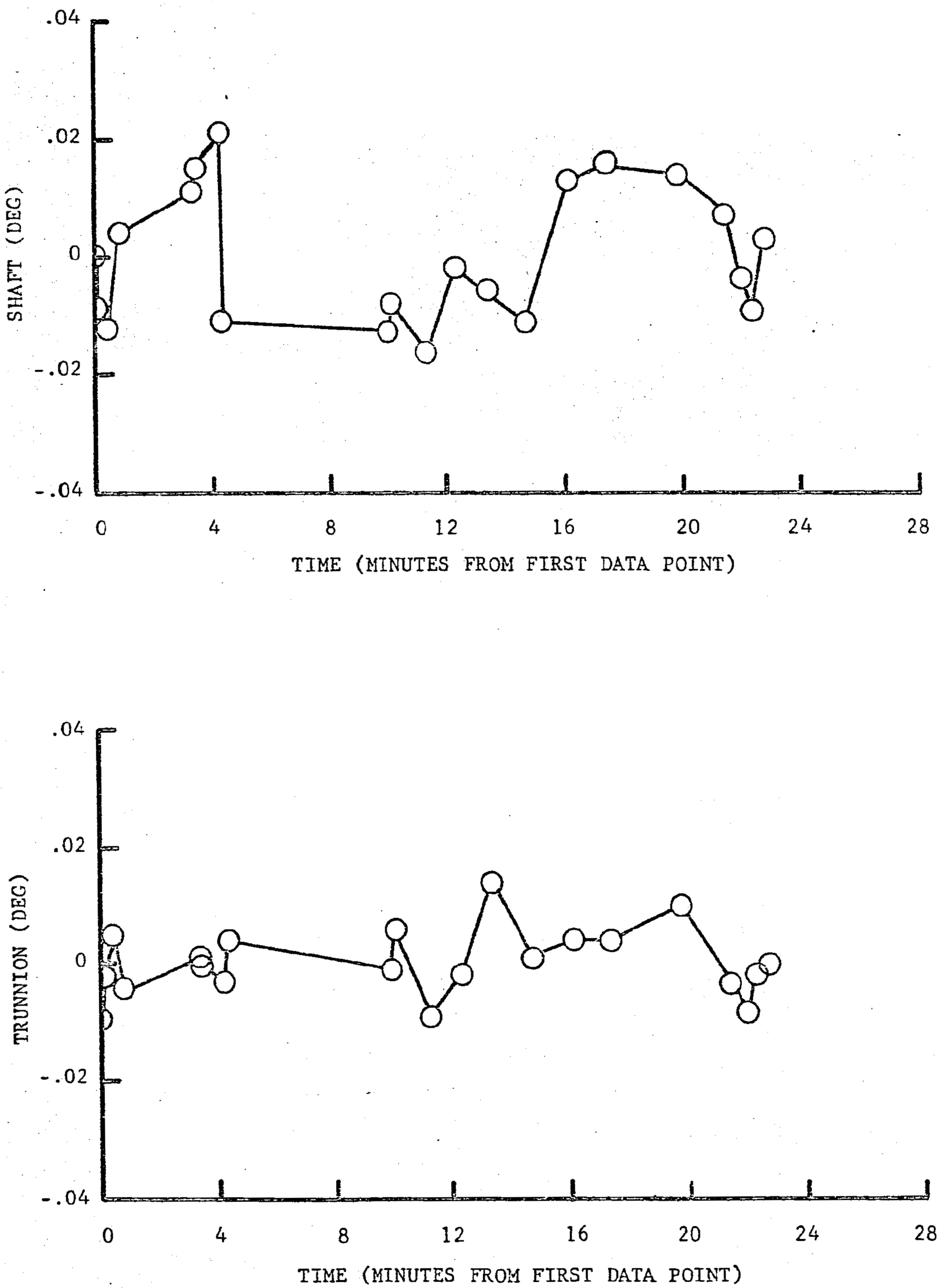


Figure 7-17 Sextant Residuals (CSI to CDH)

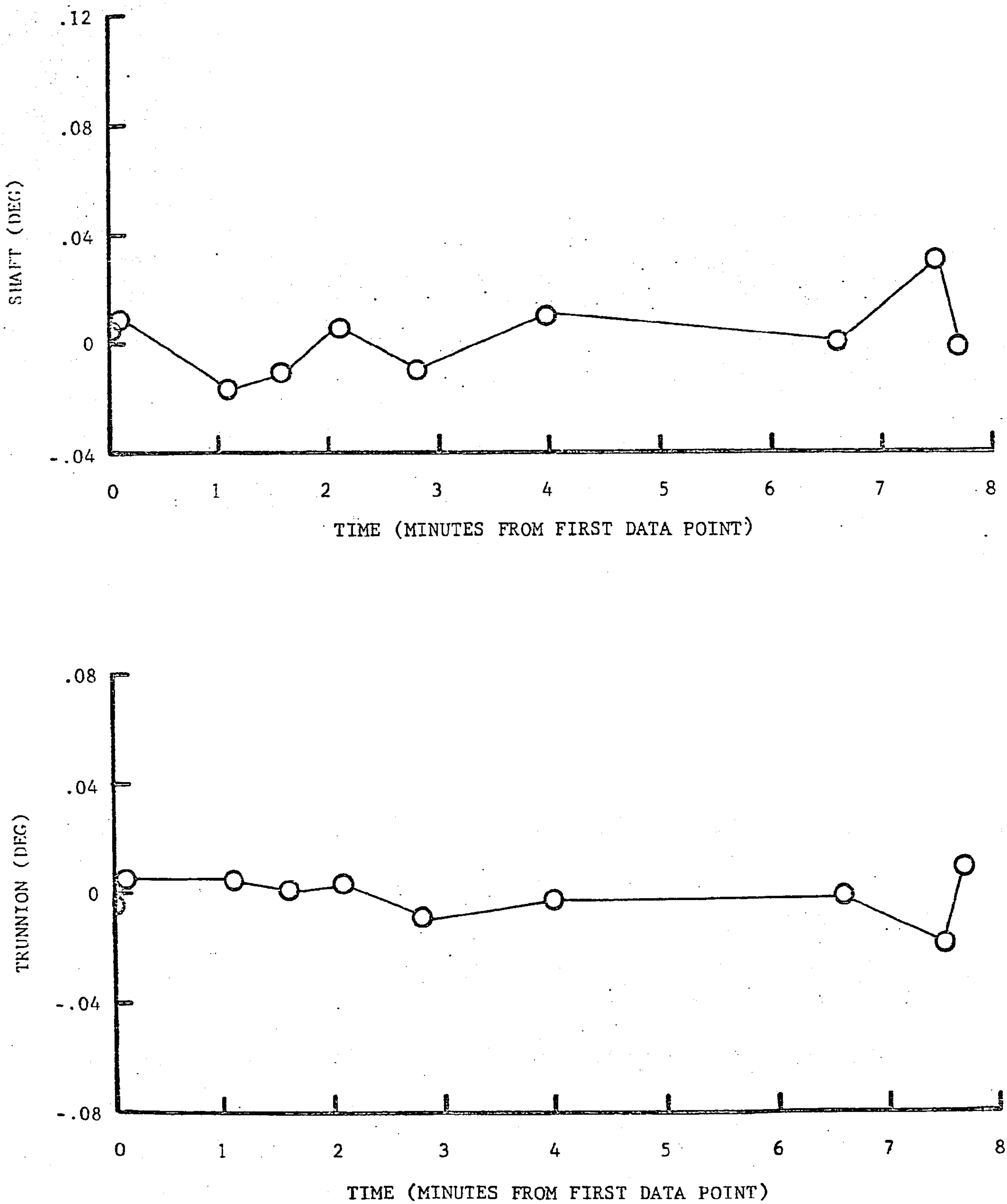


Figure 7-18 Sextant Residuals (CDH to TPI)

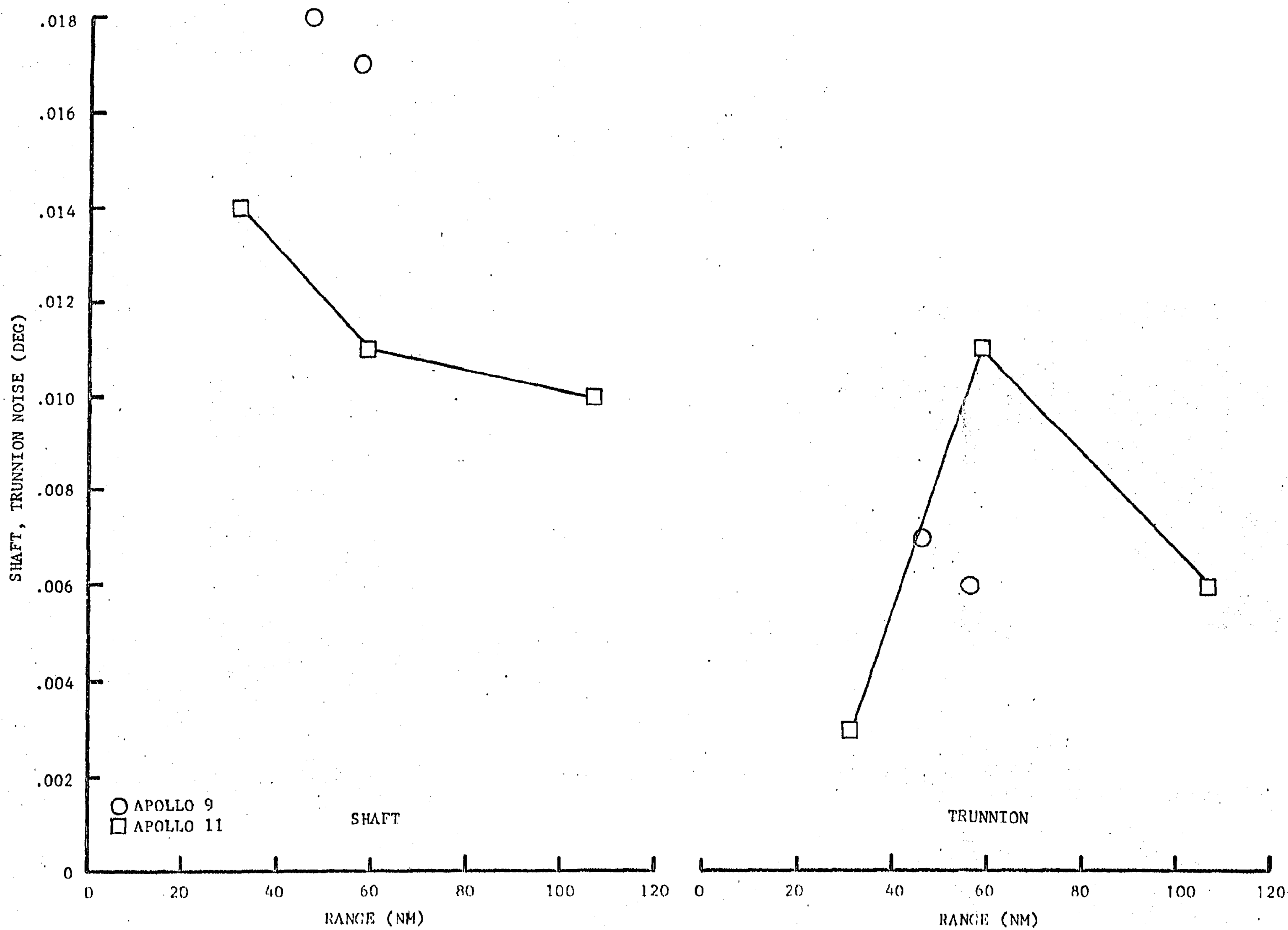


Figure 7-10 Sextant Angular Random Noise as a Function of

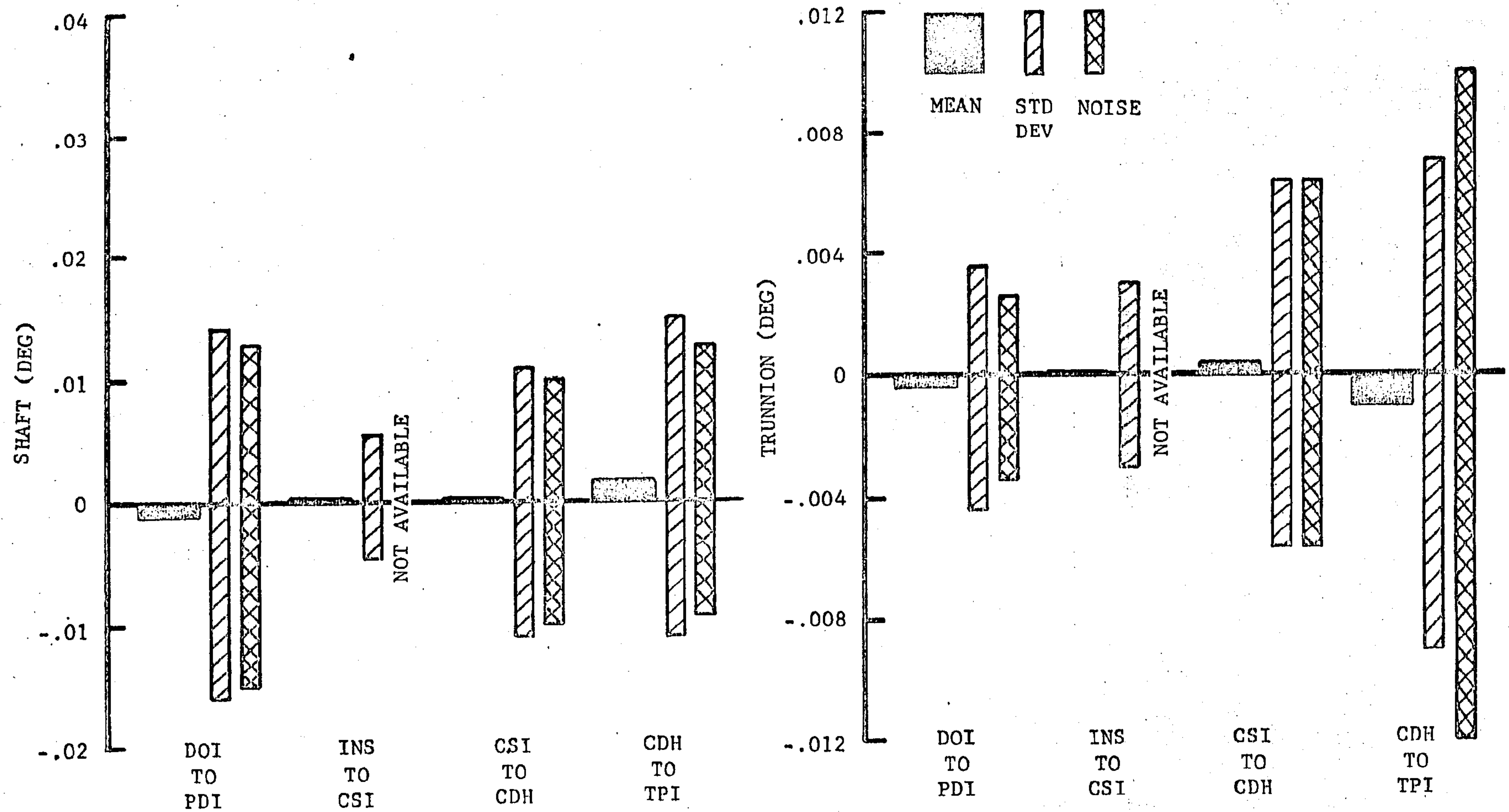


Figure 7-20 Sextant Residual Statistics

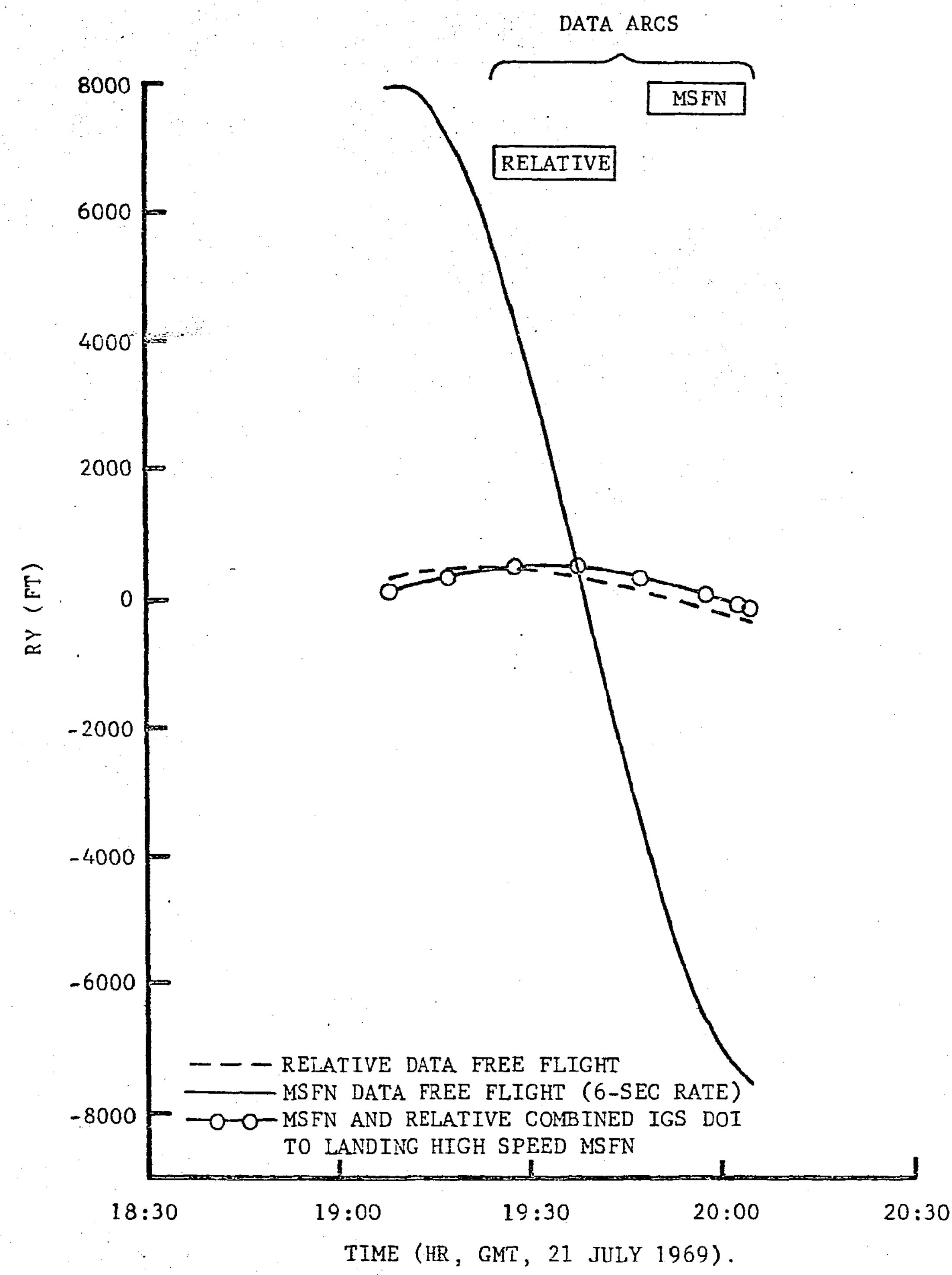


Figure 7-21 Out-of-Plane Component of LM Position Relative to CSM (DOI to PDI)

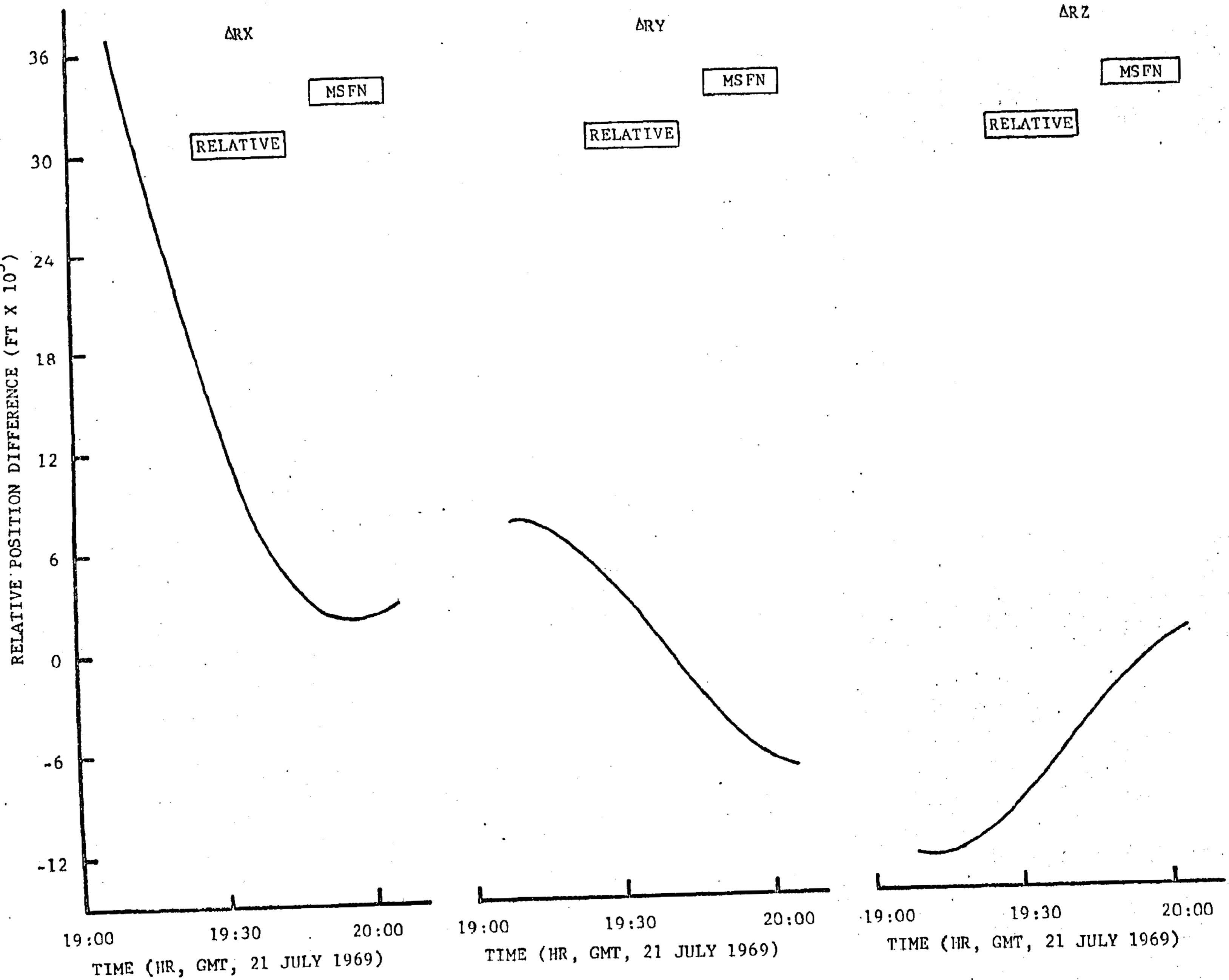
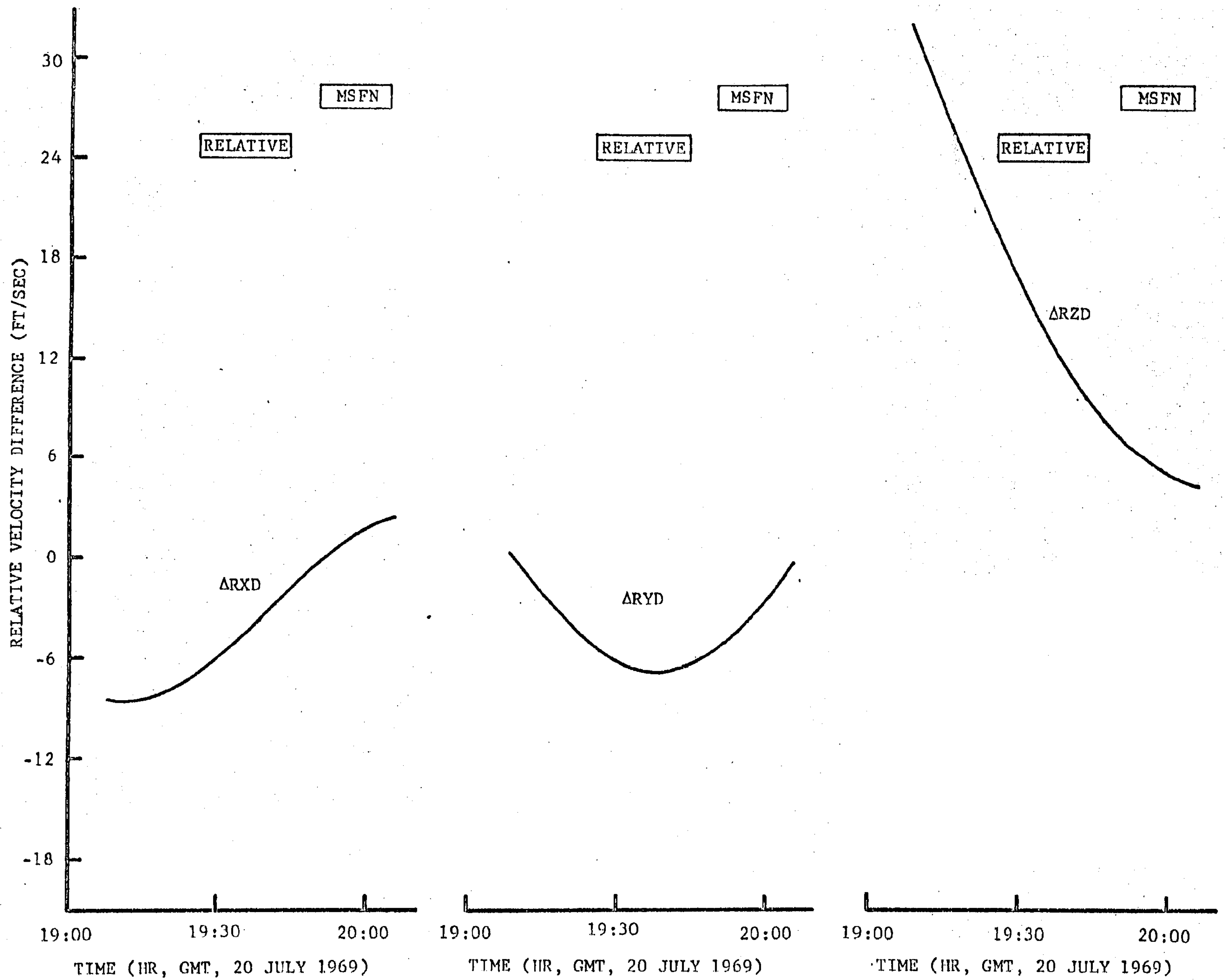


Figure 7-22 Differences Between Position Components of Relative Trajectories (DOI to PDI)


30
24
18
12
6
0
-6
-12
-18
RELATIVE VELOCITY DIFFERENCE (FT/SEC)
RELATIVE
MSFN
ΔRXD
19:00
19:30
20:00
TIME (HR, GMT, 20 JULY 1969)
RELATIVE
MSFN
ΔRYD
19:00
19:30
20:00
TIME (HR, GMT, 20 JULY 1969)
RELATIVE
MSFN
ΔRZD
19:00
19:30
20:00
TIME (HR, GMT, 20 JULY 1969)

Figures 7-24 and 7-25 show the differences between position and velocity components of the two relative trajectories obtained for the Insertion to CSI period. These trajectories were obtained from a MSFN (low speed) data free flight fit and an onboard data free flight fit. Note that the differences between the RX and RZ components are nominal whereas the RY component (crossrange) is large. This characteristic is expected since onboard data fits produce a much better relative trajectory in the out-of-plane sense. Figure 7-26 illustrates the better crossrange position obtained from onboard data fits.

Figure 7-27 illustrates that the trajectory obtained from onboard tracking data eliminates three to four thousand feet of relative crossrange error which the MSFN data could not. The phase differences evident in Figures 7-26 and 7-27 result primarily from differences in the determination of the right ascension of the ascending node of the orbits. The results of this phase difference are very evident in the plot of the differences between out-of-plane position components of trajectories derived from MSFN and from onboard data (Figure 7-28 (ΔRY)).

The important feature to note in these figures is that the trajectories based on onboard tracking data eliminate a large portion of the crossrange error present in independent MSFN fits for both vehicles. It is also interesting to note that in the out-of-plane position curves shown in Figures 7-26 and 7-27, that the trajectories produced from relative data match across the CSI burn much more closely than the fits produced from MSFN data. While this agreement does depend, to some extent, on a good match between the CSM trajectories, the relative data did produce a more continuous trajectory in the out-of-plane sense from one independent fit to another.

Despite the large out-of-plane differences, it can be seen that trajectories produced from onboard tracking data are generally consistent with MSFN based fits, especially in overlaping data arcs (Figures 7-24 and 7-28). Therefore, because of better characteristics in the relative sense, trajectories produced from relative tracking data are more suitable for detailed rendezvous analysis purposes.

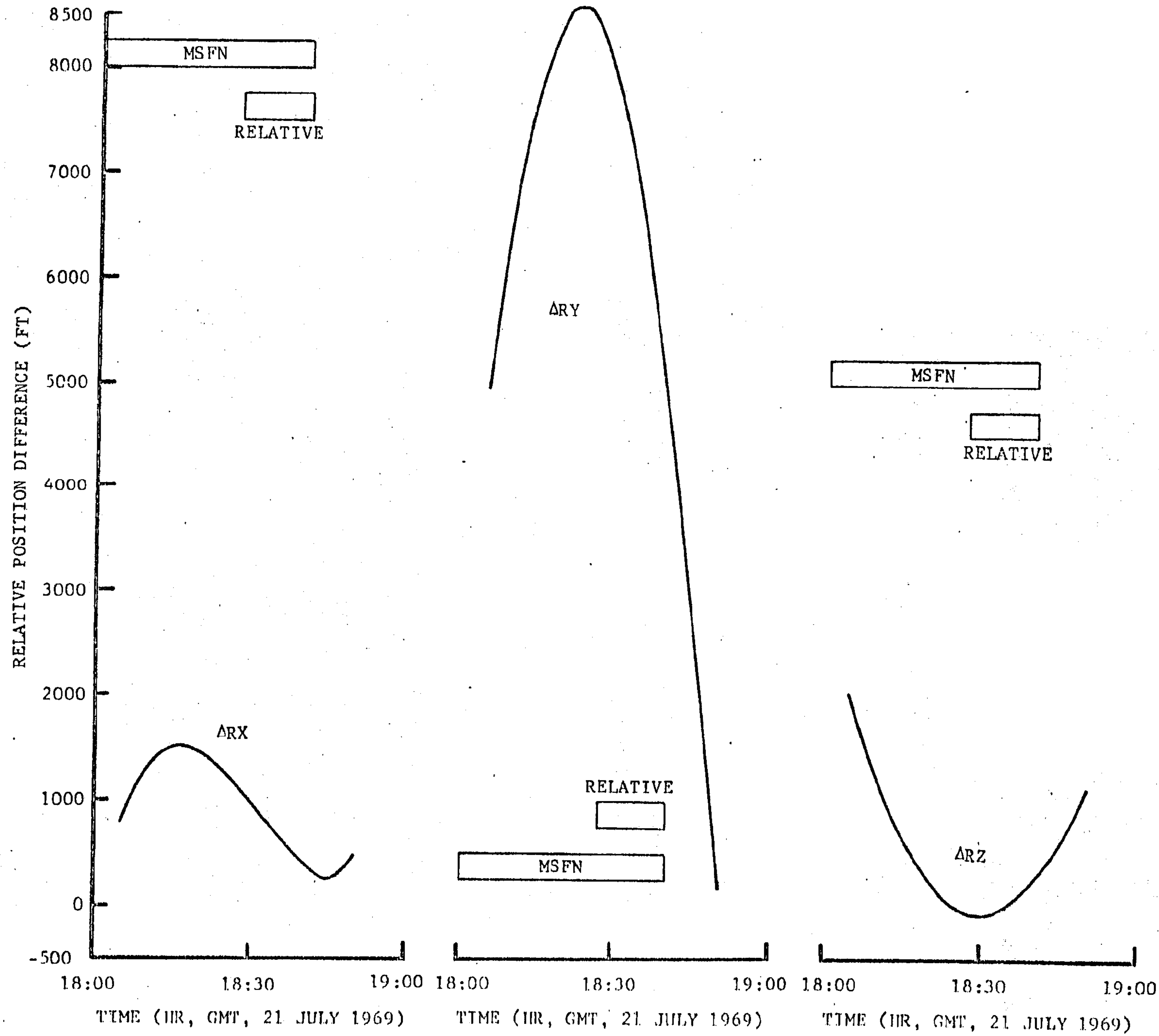


Figure 7-24 Differences Between Position Components of Relative Trajectories (Insertion to CSI)

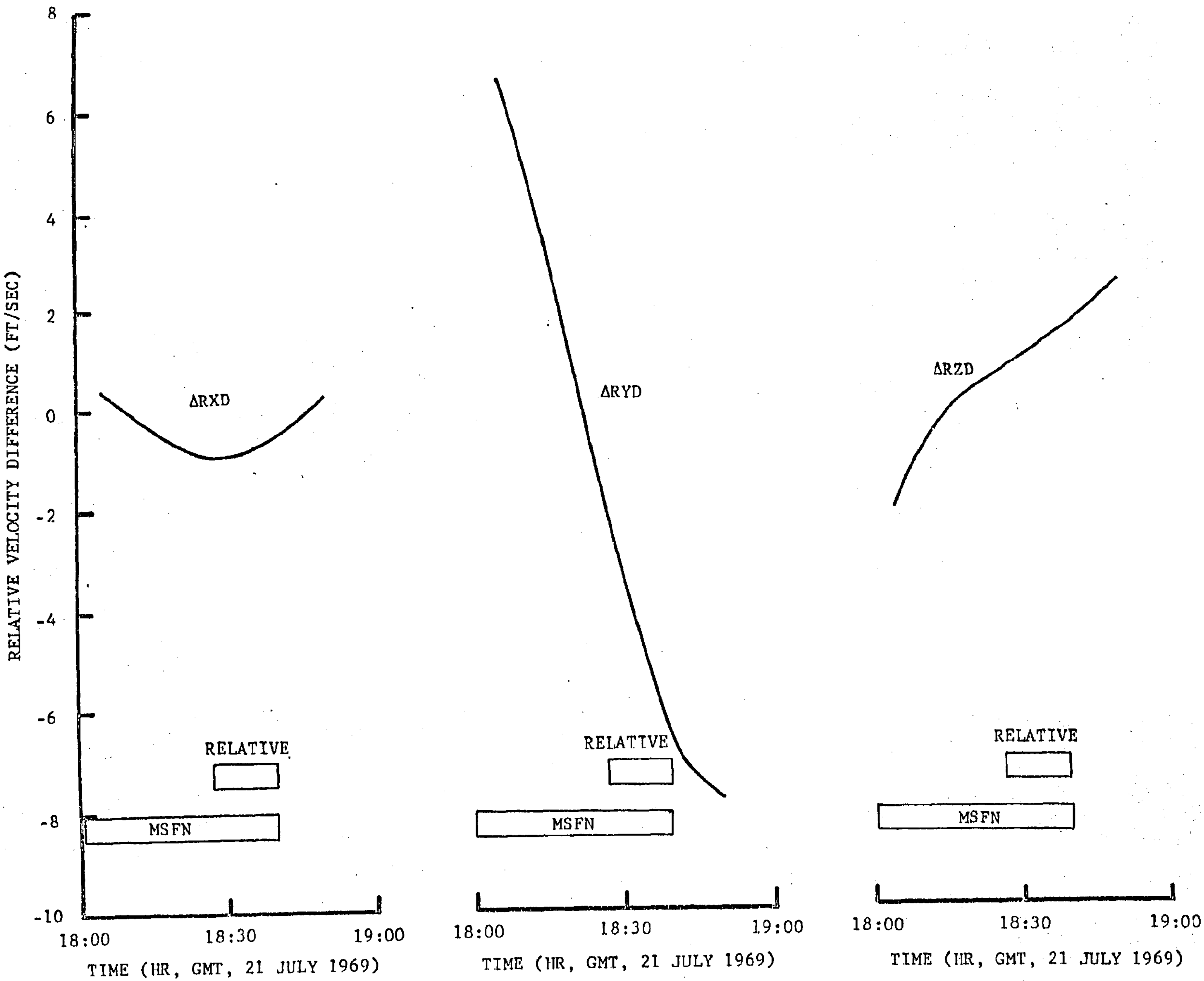


Figure 7-25 Differences Between Velocity Components of Relative Trajectories (Insertion to CSI)

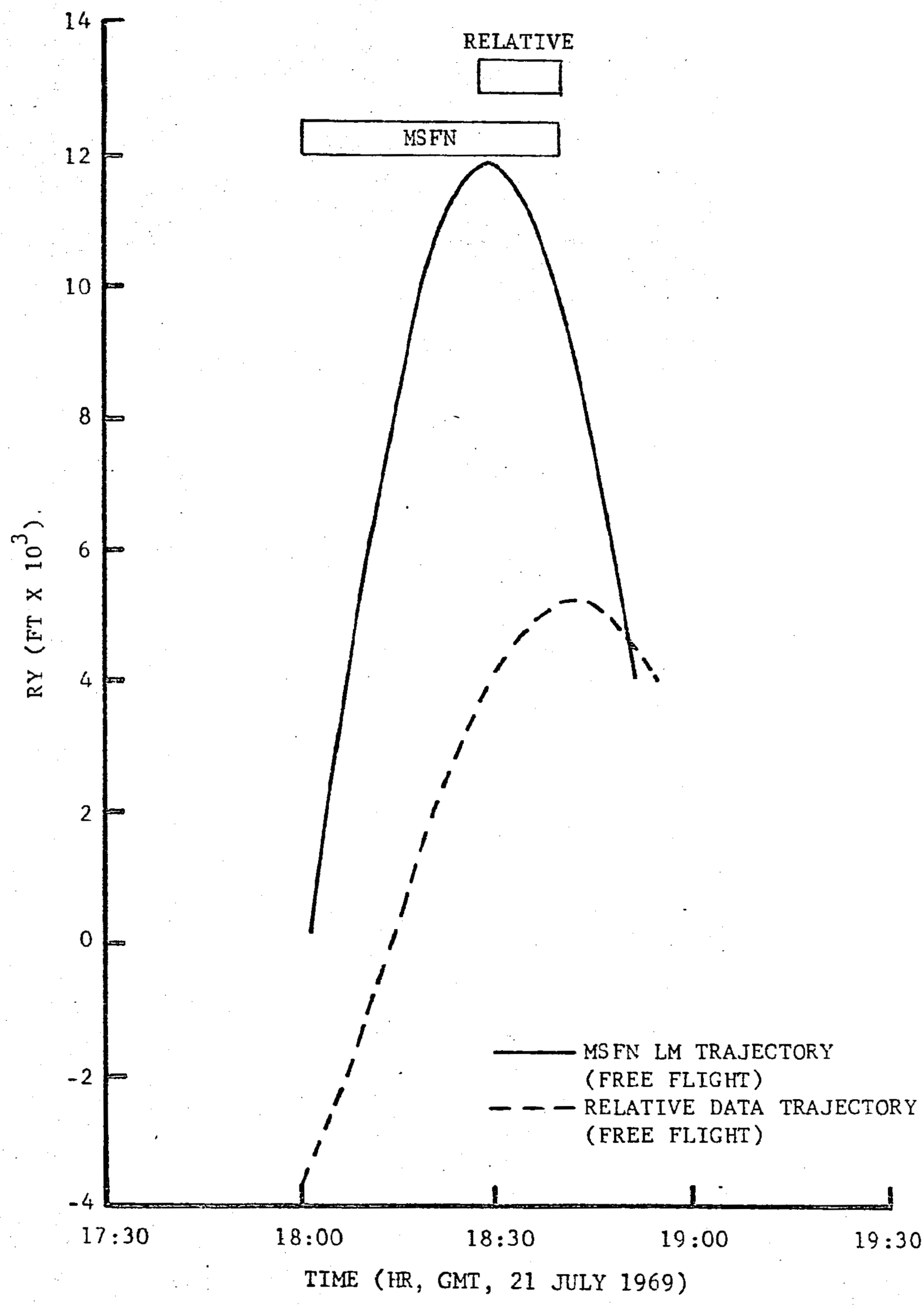


Figure 7-26 Out-of-Plane Component of LM Position Relative to CSM (Insertion to CSI)

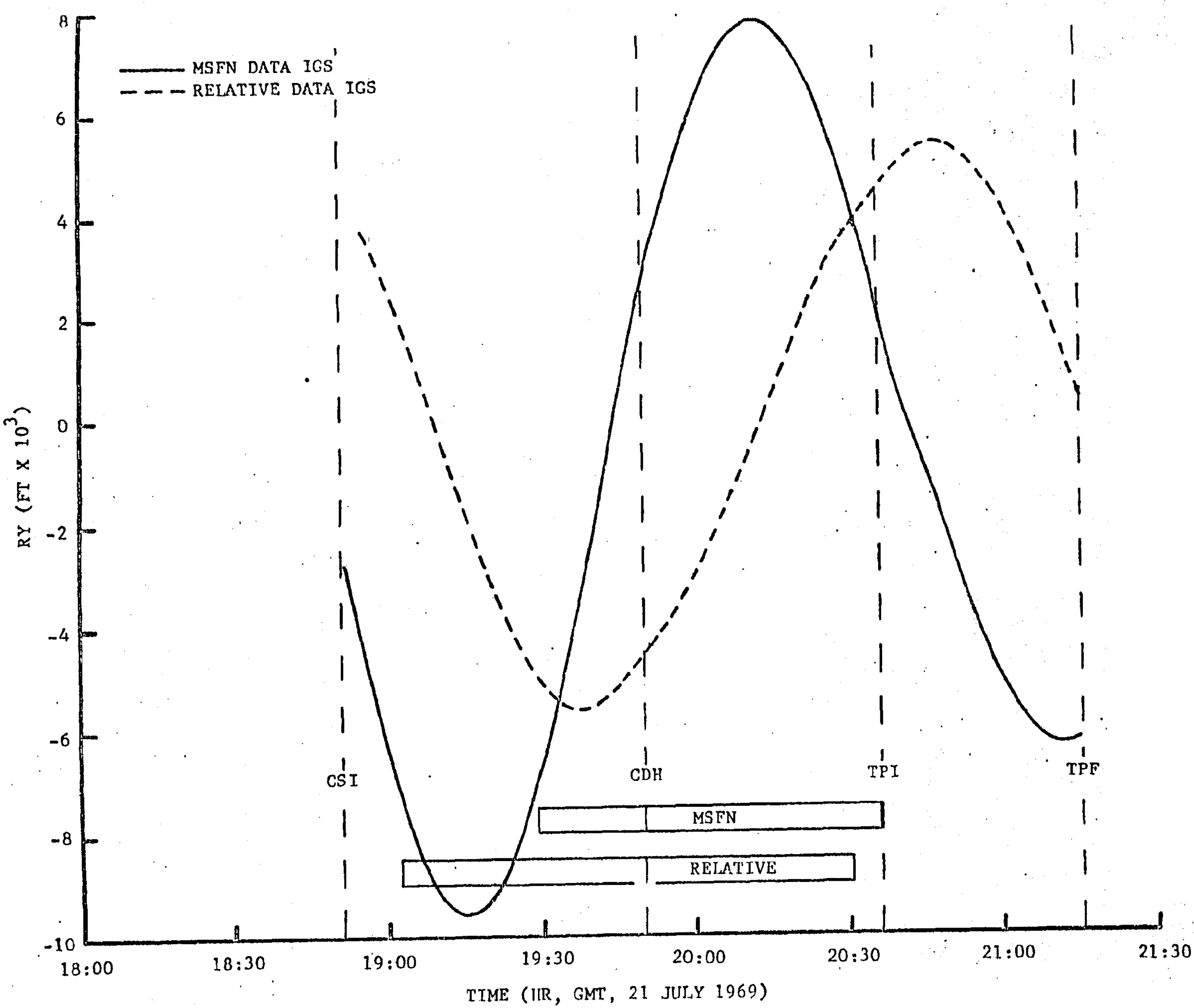


Figure 7-27 Out-of-Plane Component of LM Position Relative to CSM (CSI to TPF)

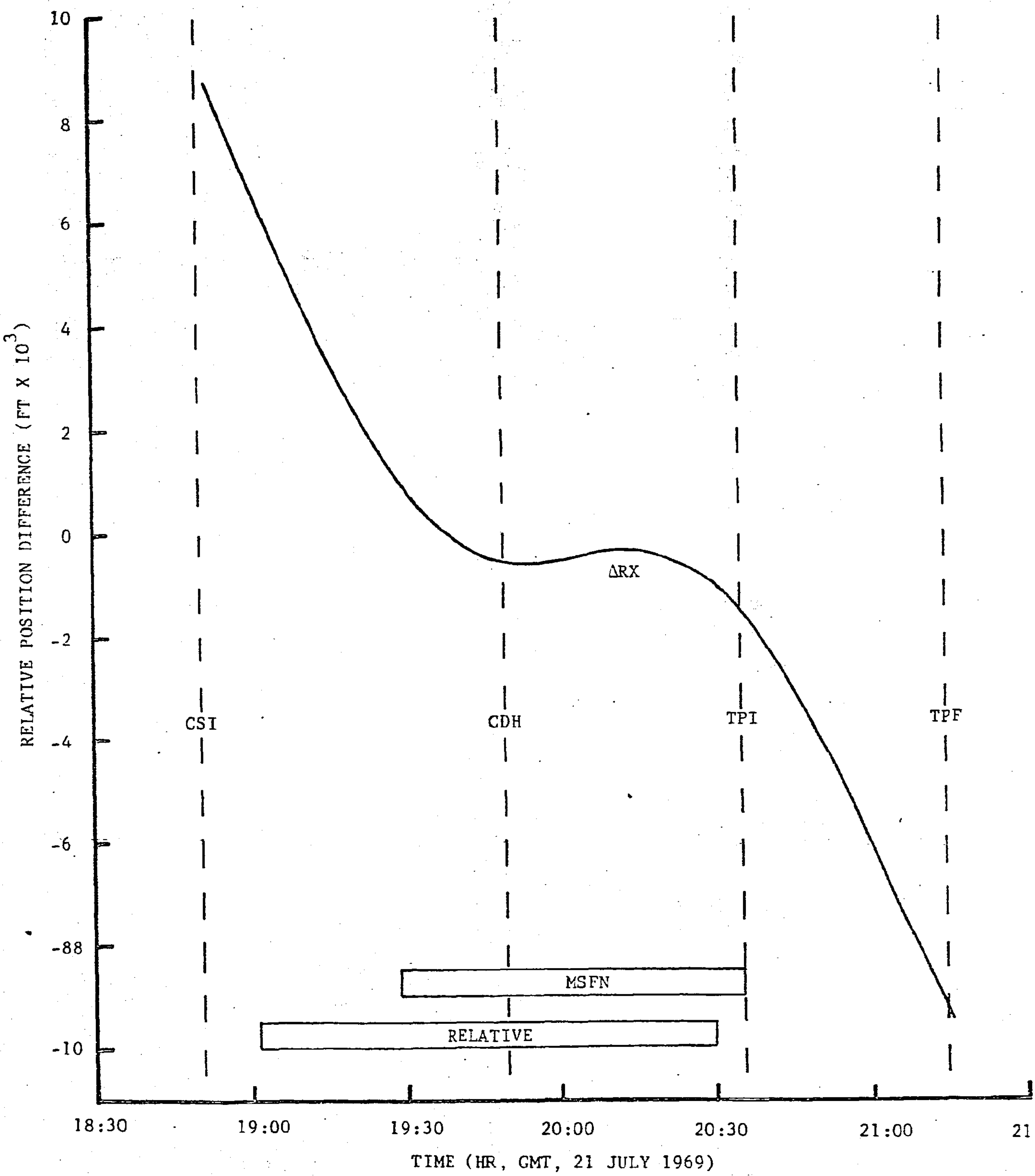


Figure 7-28 Differences Between Position Components of Relative Trajectories (CSI to TPF)

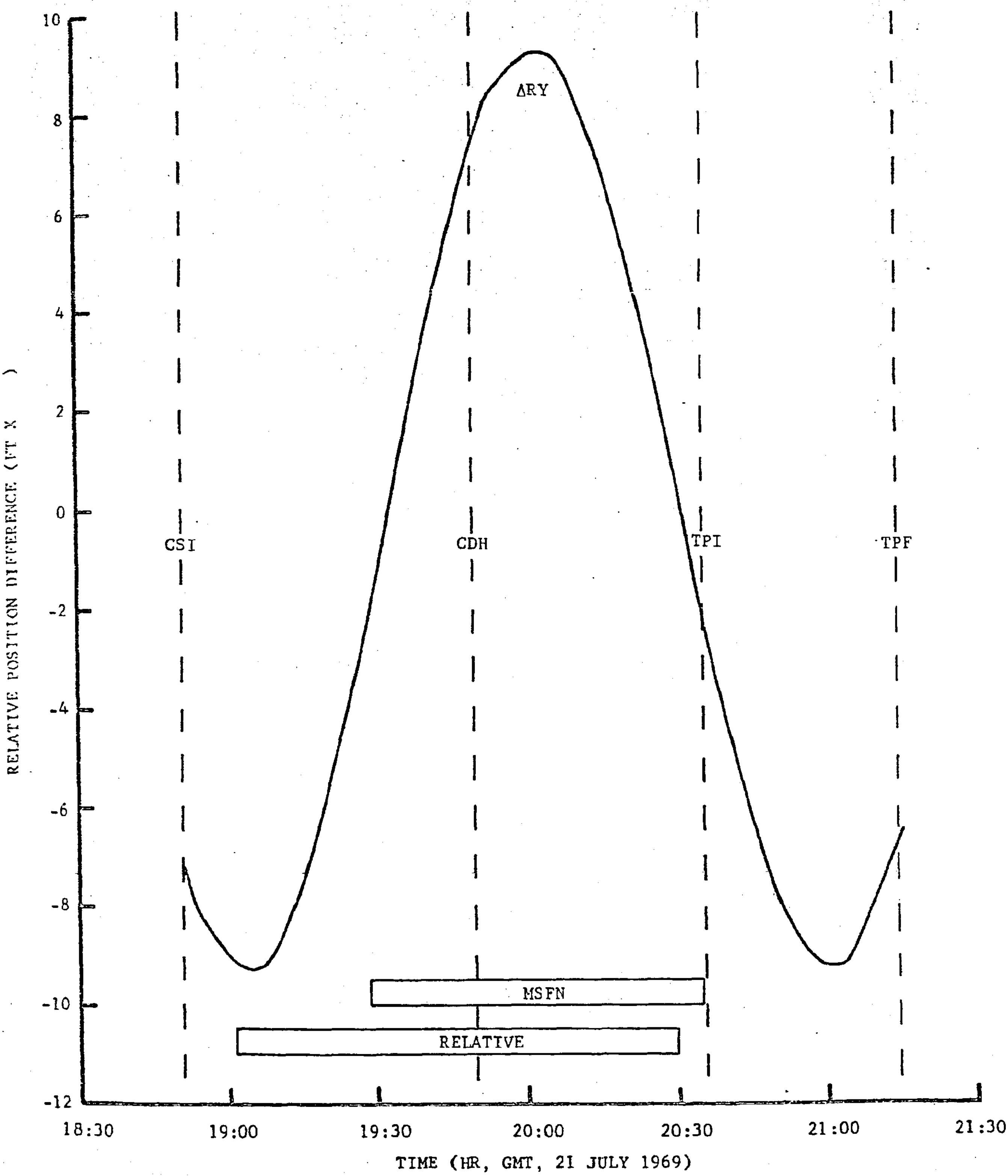


Figure 7-28 (Continued)

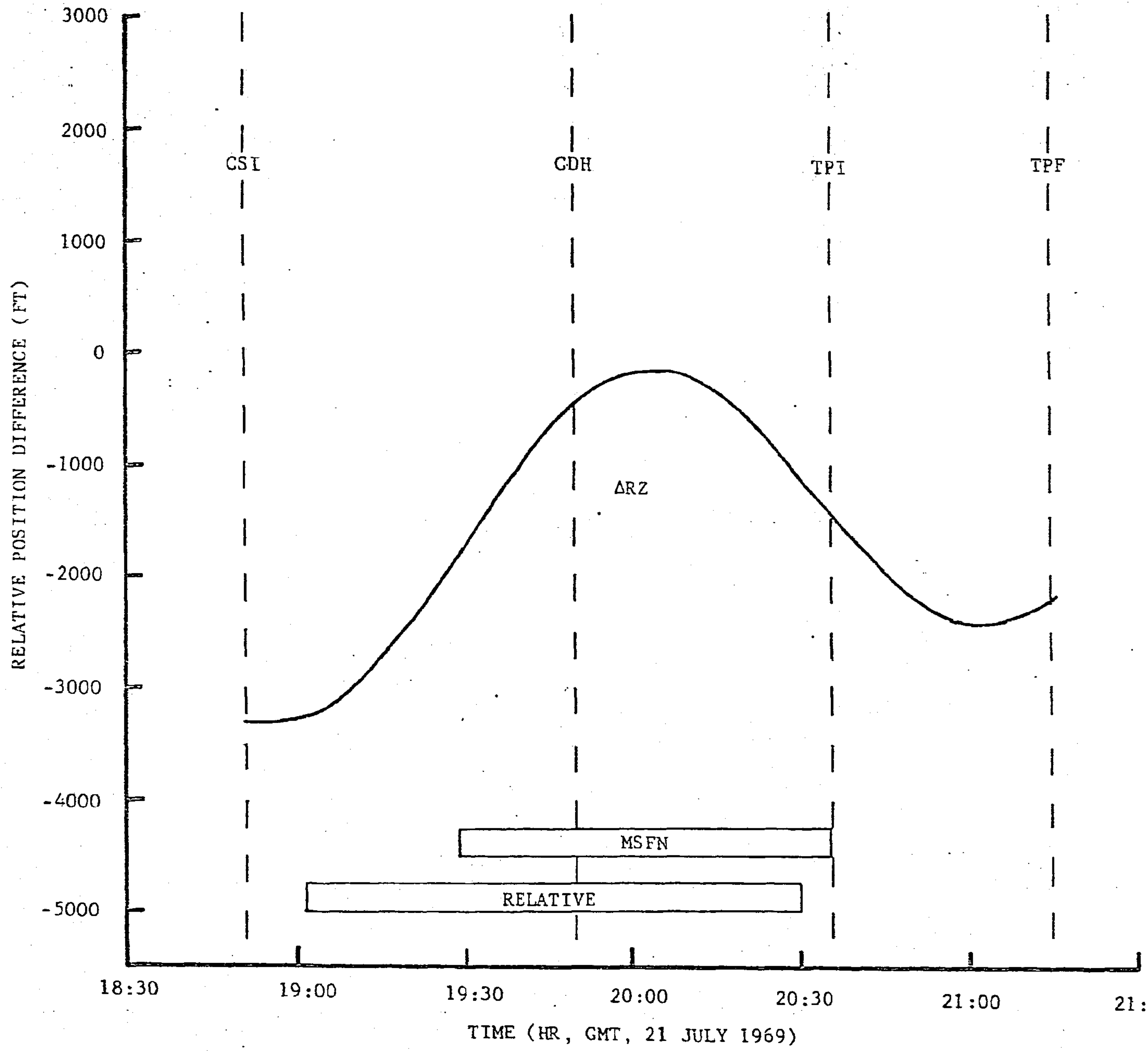


Figure 7-28 (Concluded)

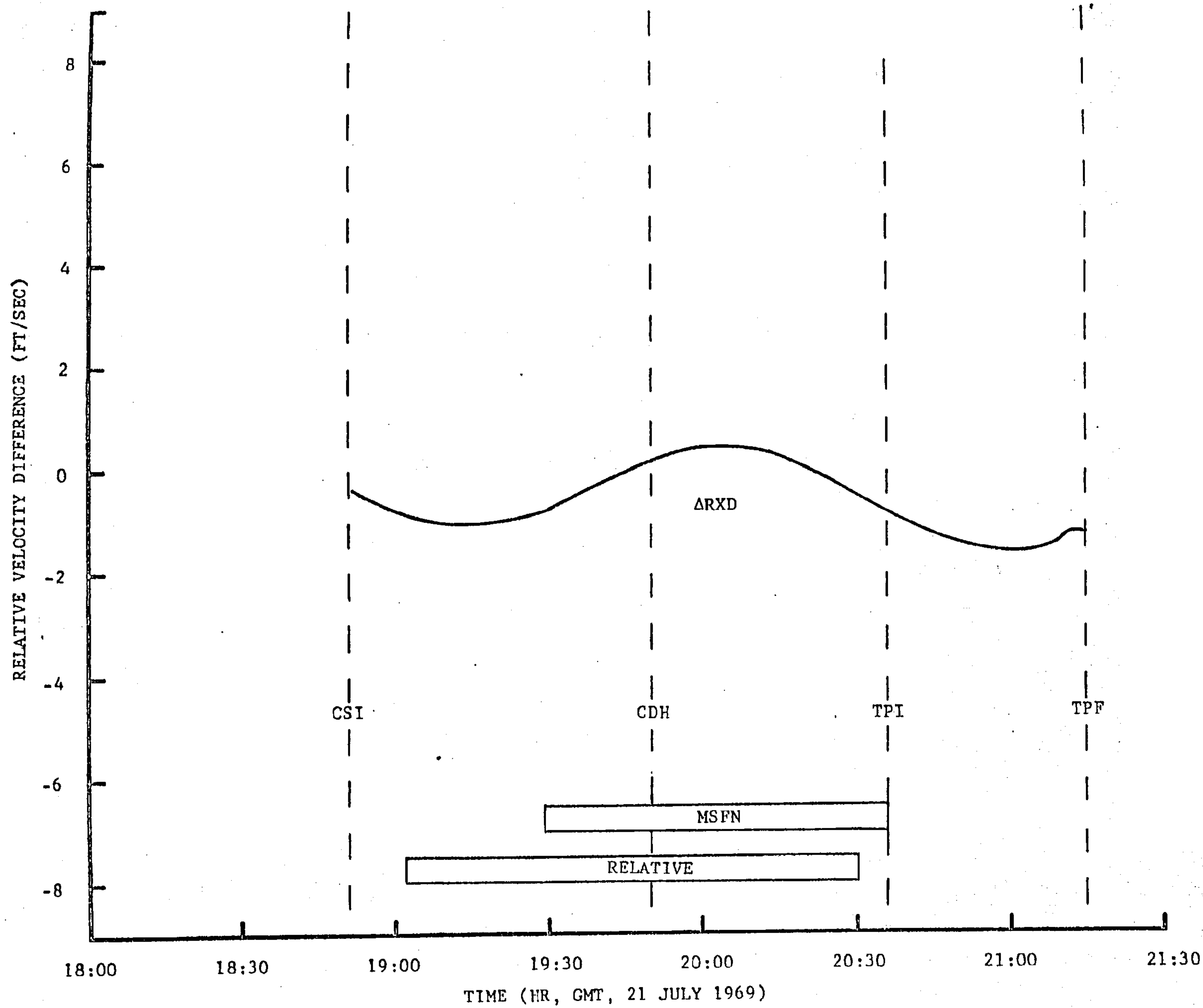
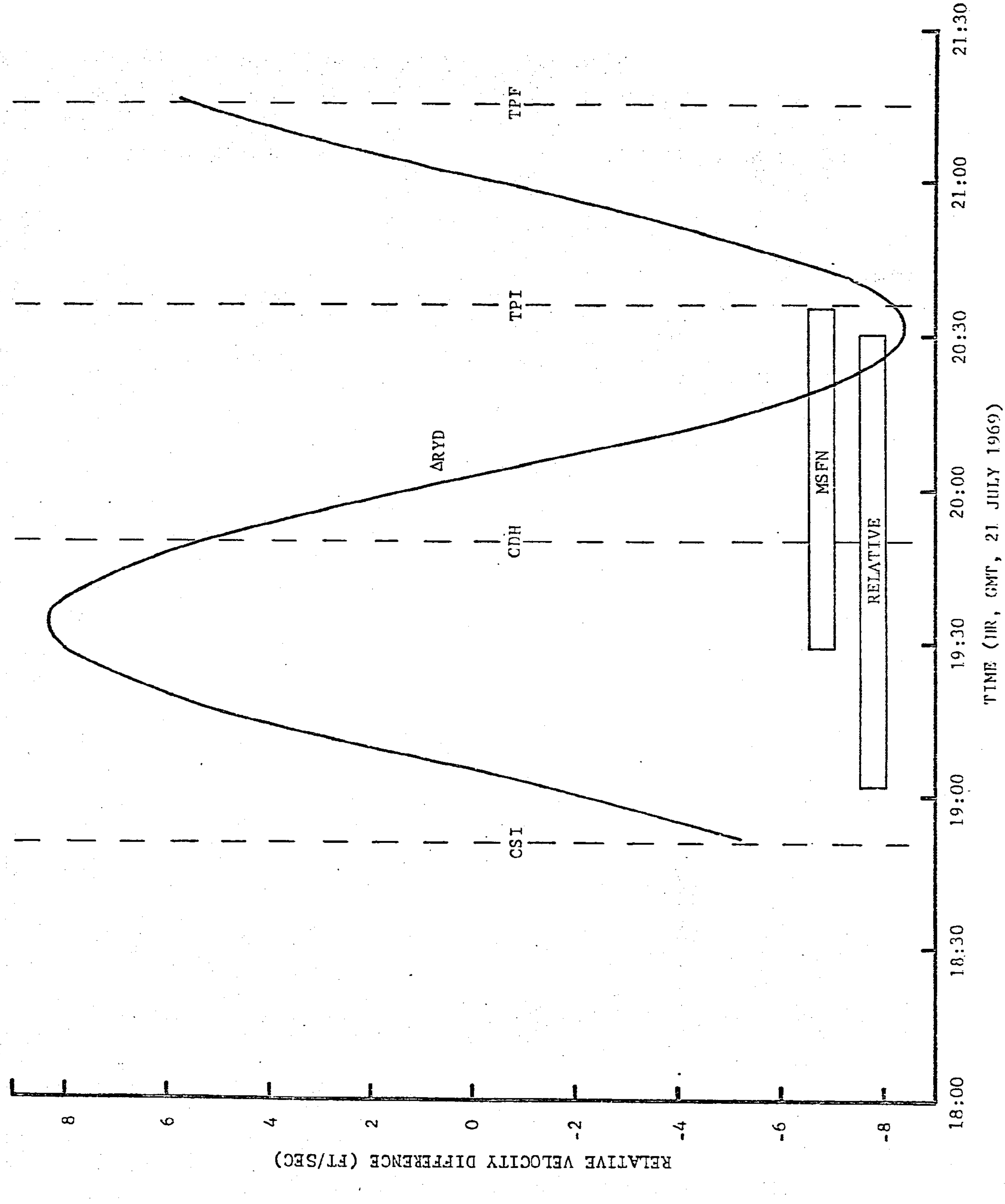


Figure 7-29 Differences Between Velocity Components of Relative Trajectories (CSI to TPF)


RELATIVE VELOCITY DIFFERENCE (FT/SEC)
8
6
4
2
0
-2
-4
-6
-8
TIME (HR, GMT, 21 JULY 1969)
18:00
18:30
19:00
19:30
20:00
20:30
21:00
21:30
CSI
CDH
TPI
TPF
ΔRYD
MSFN
RELATIVE

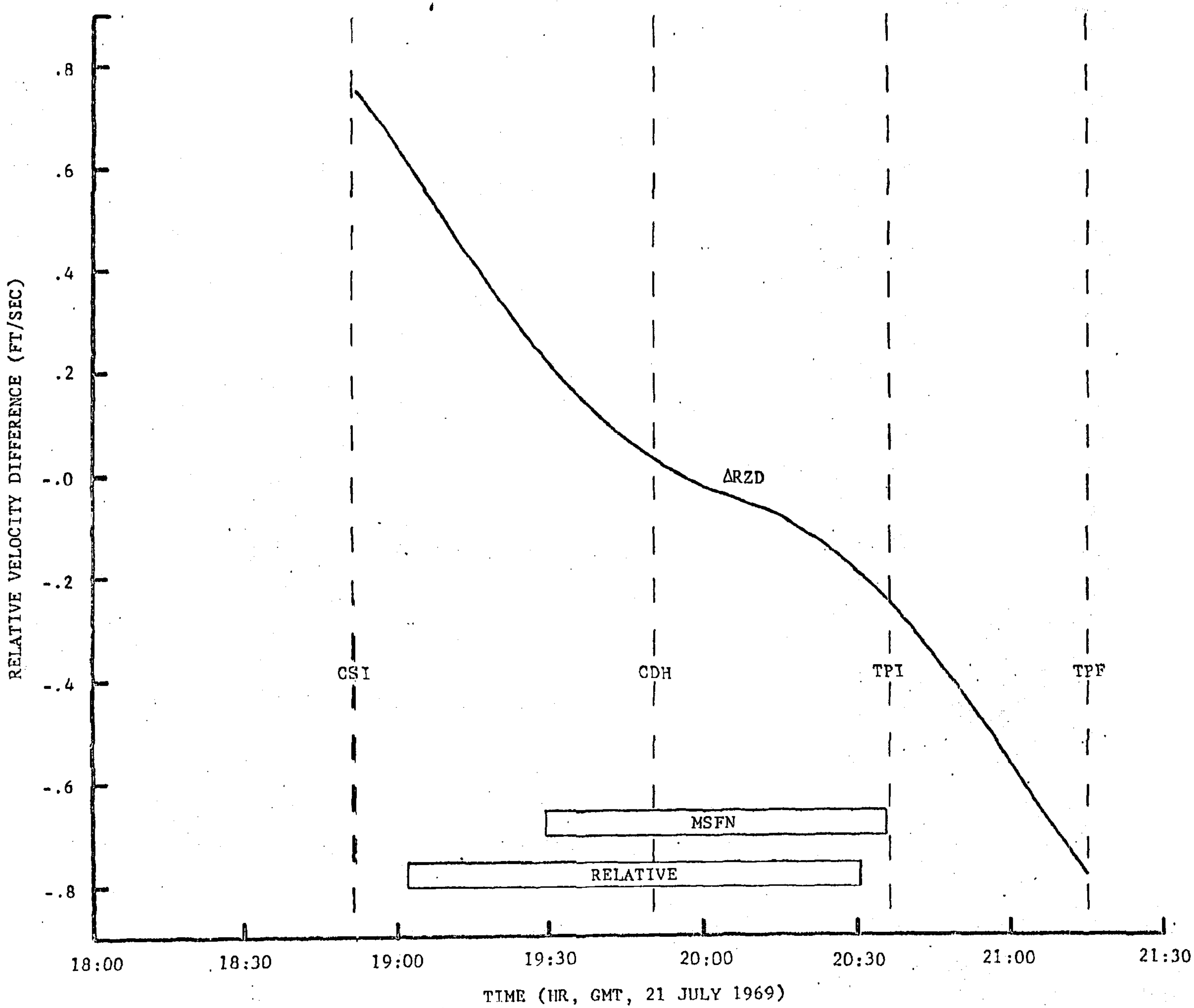


Figure 7-29 Concluded

Table 7.9 Comparison of Rendezvous Radar Noise Estimates with Specification Requirements

Free Flight Segment	Average Range (n. mi.)	Angular Noise 3σ (deg) Est.	Angular Noise 3σ (deg) Spec.	Range Noise 3σ (feet) Est.	Range Noise 3σ (feet) Spec.
INS to CSI	140	.049	.1146	117.	2126.
CSI to CDH	107	.038	.1146	111.	1627.
CDH to TPI	59	.037	.1146	81.	890.

Table 7.10 Comparison of VHF Ranging and Sextant Noise Estimates with Specification Requirements

Free Flight Segment	Average Range (n. mi.)	Sextant Angular Noise 3σ (deg) Est.	Sextant Angular Noise 3σ (deg) Spec(1)	VHF Ranging Range Noise 3σ (feet) Est.	VHF Ranging Range Noise 3σ (feet) Spec.
DOI to PDI	32	.043	-	69.	180.
INS to CSI	140	NA		NA	
CSI to CDH	107	.035	-	69.	180.
CDH to TPI	59	.047	-	57.	180.

(1) No specification value was available.

Specification Comparisons

Table 7.9 compares the 3σ values of noise estimated from the rendezvous radar residuals with specification requirements. It can be seen that the estimates were all well within specification limits. Noise estimates for the sextant and VHF ranging data are listed in Table 7.10. Although no specification value was found for the sextant, the values obtained (RSS of individual angle noise estimates) were all within acceptable limits. The VHF ranging noise estimates also compare well with specifications.

Conclusions

The following conclusions were drawn from the analysis.

1. The onboard data was generally of good quality. The sextant data, examined for the first time, appeared to be as accurate as the rendezvous radar angular measurements.

2. Estimates of data random noise were all within specification and expected values.

3. Trajectories produced from onboard tracking data proved to be generally consistent with those produced from MSFN data. It was found that a method used in the past to demonstrate trajectory consistency was inadequate. On Apollo 10, trajectories were compared only at selected times. Because of the significantly large phase differences found to be present in relative trajectories, the values for out-of-plane position differences obtained at selected times may be misleading. The out-of-plane position components must be plotted as a function of time in order to see the total differences in the trajectories.

7.4 LANDING RADAR DATA ANALYSIS

The landing radar data analysis consisted of generating and evaluating landing radar residuals (difference between observed measurement and computed measurement) and mapping of the lunar surface profile and groundtrack with the slant range measurement.

The landing radar data were obtained by processing the downlink telemetry data with a special purpose computer program which outputs onboard observations on punched cards in a HOPE-compatible format.

The HOPE Program was used to compute simulated landing radar observables from selected LM trajectories and from auxiliary information such as REFSMAT, gimbal angles, and radar operating mode. The LM trajectories were generated by the HOPE Program utilizing telemetered acceleration data in the IGS burn option to model the descent burn. Residuals were then formed by subtracting the computed from the actual observable value. Paragraph 7.4.2 presents statistics and selected plots of residuals obtained from various LM state vectors.

Terrain mapping data were obtained from a small, special pupose computer program designed to compute terrain altitude above a mean lunar radius as a function of latitude and longitude. The results of an attempt to correlate this terrain data with lunar contour maps are presented in Paragraph 7.4.3.

7.4.1 Descent Trajectories

Six different descent trajectories were examined in the landing radar data analysis. The origins of these trajectories are summarized as follows:

(a) RTCC - This vector was obtained in the RTCC in real time.

(b) MSFN (LS) - This vector was obtained from an IGS fit using low speed MSFN data obtained from acquisition of signal to LM touchdown (revolution 14). The doppler data were compacted to two observations per minute.

(c) Onboard - This vector was obtained from a free flight fit using CSM sextant and VHF ranging observations. The technique required fixing the CSM trajectory as a reference and updating the LM state from onboard observations and the CSM reference trajectory.

(d) BET #3 - The MSFN state vector described in item (b) above, was used as the basis for this trajectory. The BET #3 was obtained by correcting the MSFN low speed state with a linear error analysis program so that the resultant powered descent trajectory would impact a desired landing site with a relative velocity of zero. The landing coordinates used as reference were the MPB photographic estimate.

(e) Lear - High speed MSFN data (ten samples per second) obtained over a 232 second data arc just prior to PDI were fit by the Lear Powered Flight Processor producing this state vector.

(f) Onboard/MSFN (H-S) - This trajectory was obtained with the HOPE Program and used high speed MSFN doppler data which had been compacted to 30 observations/minute and from CSM sextant and VHF ranging data using the HOPE orbit determination program. The descent burn was modeled by the HOPE IGS burn option. The HOPE weighted least squares solution vector included position and velocity at epoch (which was prior to PDI), and Y platform misalignment. The tracking data interval was from DOI to LM touchdown. Figure 7-2 shows the tracking data timeline.

In order to gauge the quality of the landing radar data, it was necessary to determine that the above trajectories did accurately represent the actual descent trajectory. This quality judgement was based largely on the landing point conditions obtained from each trajectory. These landing sites obtained from each trajectory are summarized graphically in Figure 7-30. Note that both the BET #3 and the Onboard/MSFN H-S estimates are very close to the 16mm photographic estimate (accepted as the best estimate).

Since the data type being examined is a velocity measurement, it is most important that the reference trajectory be virtually free of velocity errors in the data arc. The onboard/MSFN H-S trajectory contains a large velocity error at landing where the BET #3 was constructed in such a manner that the velocities are zero at landing. Therefore, the BET #3 was chosen as the basic reference upon which to base the analysis of landing radar velocity residuals.

7.4.2 Landing Radar Velocity Residuals

Table 7.12 lists the velocity residual statistics obtained from all the trajectories considered in the analysis. Note the small mean values obtained from the reference trajectory (BET #3). In the absence of a real standard of comparison, the mean values obtained from BET #3 were reasonably small. Standard deviations indicate that V_{YA} and V_{ZA} are somewhat more erratic than V_{XA}. However, these values are still of reasonably good quality as shown by Figures 7-31 through 7-33. These figures show the BET #3 velocity residuals plotted versus time. In addition, specification limits have been plotted. Note that a few points fall outside specification.

It is difficult to isolate measurement errors from trajectory errors in this particular case. The descent trajectory is a particularly difficult one to reconstruct, and the landing radar velocity data are particularly sensitive to trajectory errors. Notice that the velocity residuals in Figures 7-31 through 7-33 tend toward zero at landing where the BET #3 velocities were constrained to zero. In contrast, the trajectory obtained from the Onboard/MSFN H-S fit is known to contain velocity errors at landing. The resultant total velocity at landing as 8.02 fps, with the primary contribution in the Z direction (North). The residual statistics show a mean value for V_{YA} of 6.966 fps. Since V_{YA} was directed roughly North, the large mean value reflects the -7.96 fps in the Z component of velocity at landing. The residuals obtained from the Onboard/MSFN H-S fit are plotted in Figures 7-34 through 7-36.

The residual statistics listed in Table 7.12 also indicate that the best trajectories do produce the best landing radar velocity residual statistics, that is, the BET #3 and the Onboard/MSFN H-S trajectories produce the smallest residual mean values. This fact, together with the sensitivity which the data has exhibited to trajectory velocities indicate that descent trajectory reconstruction activities will be aided considerably by the landing radar velocity data.*

---

* Subsequent reconstructions using landing radar data have produced a a trajectory landing at acceptable coordinates (Lat. = .649 deg, Long. = 23.490 deg) with a total relative velocity of .96 fps. A report of this reconstruction will be forthcoming under a separate cover.

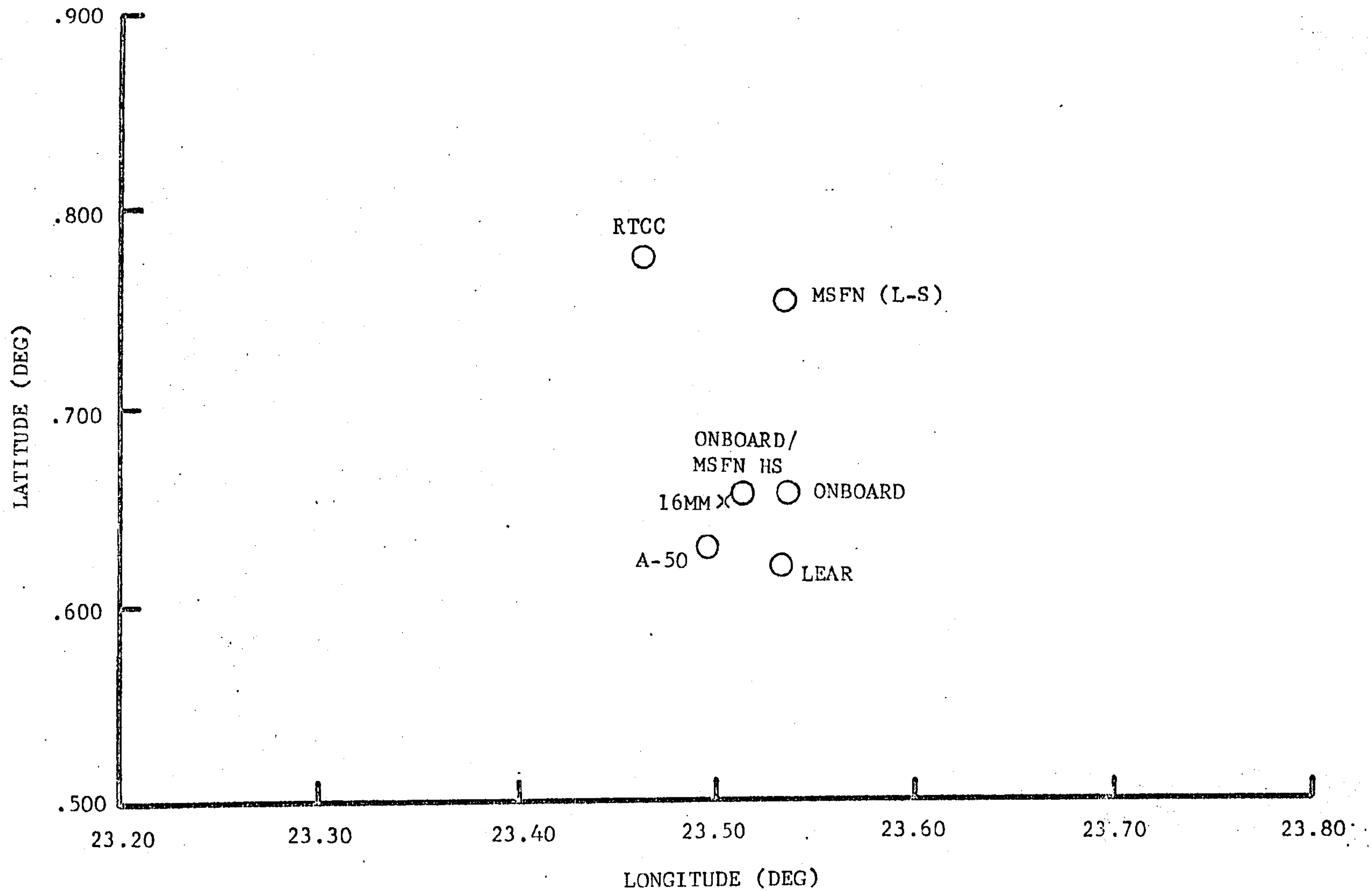


Figure 7-30 LM Landing Site Coordinates

Table 7.11 LM Landing Site Coordinates

VECTOR SOURCE	LATITUDE (deg)	LONGITUDE (deg)	RADIUS (n.mi.)
RTCC	0.777	23.461	936.59
MSFN (L-S)	0.756	23.537	937.93
ONBOARD (VHF, SXT)	0.656	23.538	936.90
BET #3	0.630	23.497	937.15
LEAR	0.620	23.532	936.66
16MM	0.647	23.505	N/A
ONBOARD/MSFN H-S	0.655	23.515	937.04

Table 7.12 Landing Radar Velocity Residual Statistics

Vector Source	V_{XA}	V_{YA}	V_{ZA}
RTCC			
Mean	9.543	3.909	3.022
S.Dev.	1.532	5.455	3.918
Noise	1.172	3.891	3.446
MSFN (LS)			
Mean	-1.997	6.501	4.533
S.Dev.	1.758	4.081	3.486
Noise	1.120	3.281	3.661
ONBOARD			
Mean	2.681	6.724	4.640
S.Dev.	1.475	4.209	3.430
Noise	1.316	3.948	2.203
BET #3			
Mean	.857	.893	-.173
S.Dev.	1.829	4.306	3.689
Noise	1.142	4.565	2.361
LEAR			
Mean	4.733	5.625	4.287
S.Dev.	1.018	4.189	3.723
Noise	.718	3.932	2.340
ONBOARD/MSFN (H-S)			
Mean	.234	6.966	1.729
S.Dev.	1.183	3.866	2.978
Noise	.575	3.336	2.349

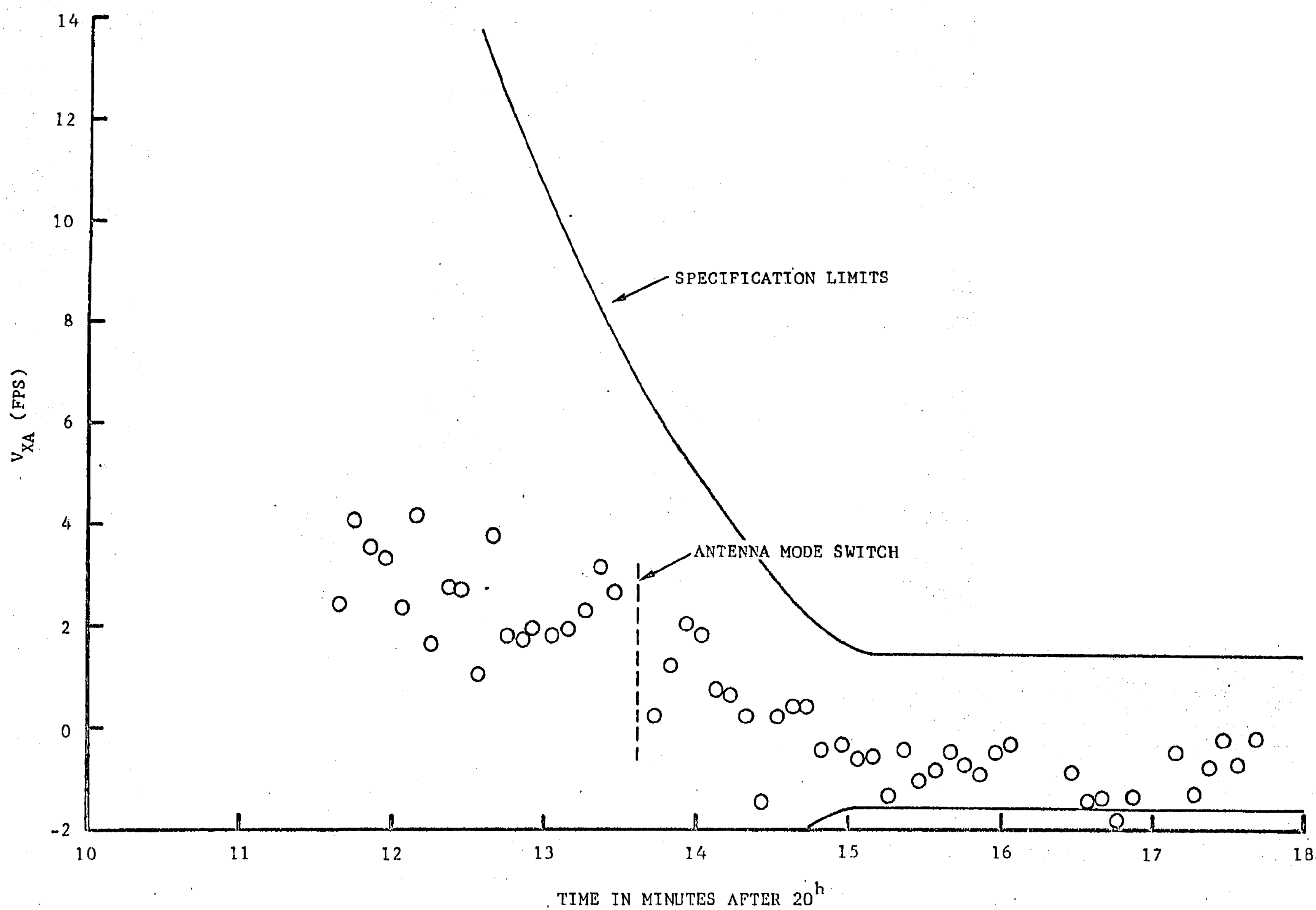


Figure 7-31. Landing Radar X-Antenna Velocity Residuals (BET#3)

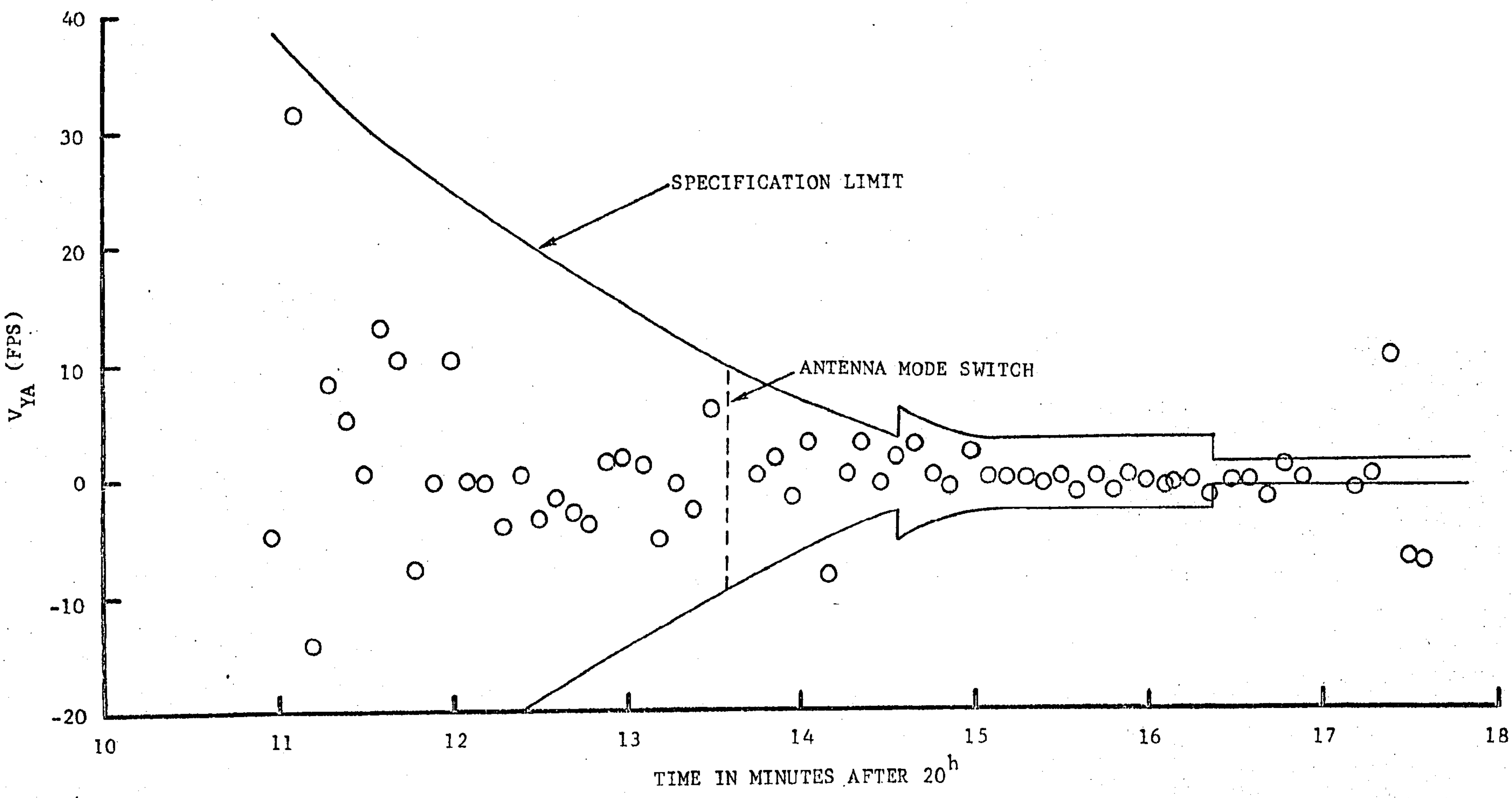


Figure 7-32 . Landing Radar Y-Antenna Velocity Residuals (BET#3)

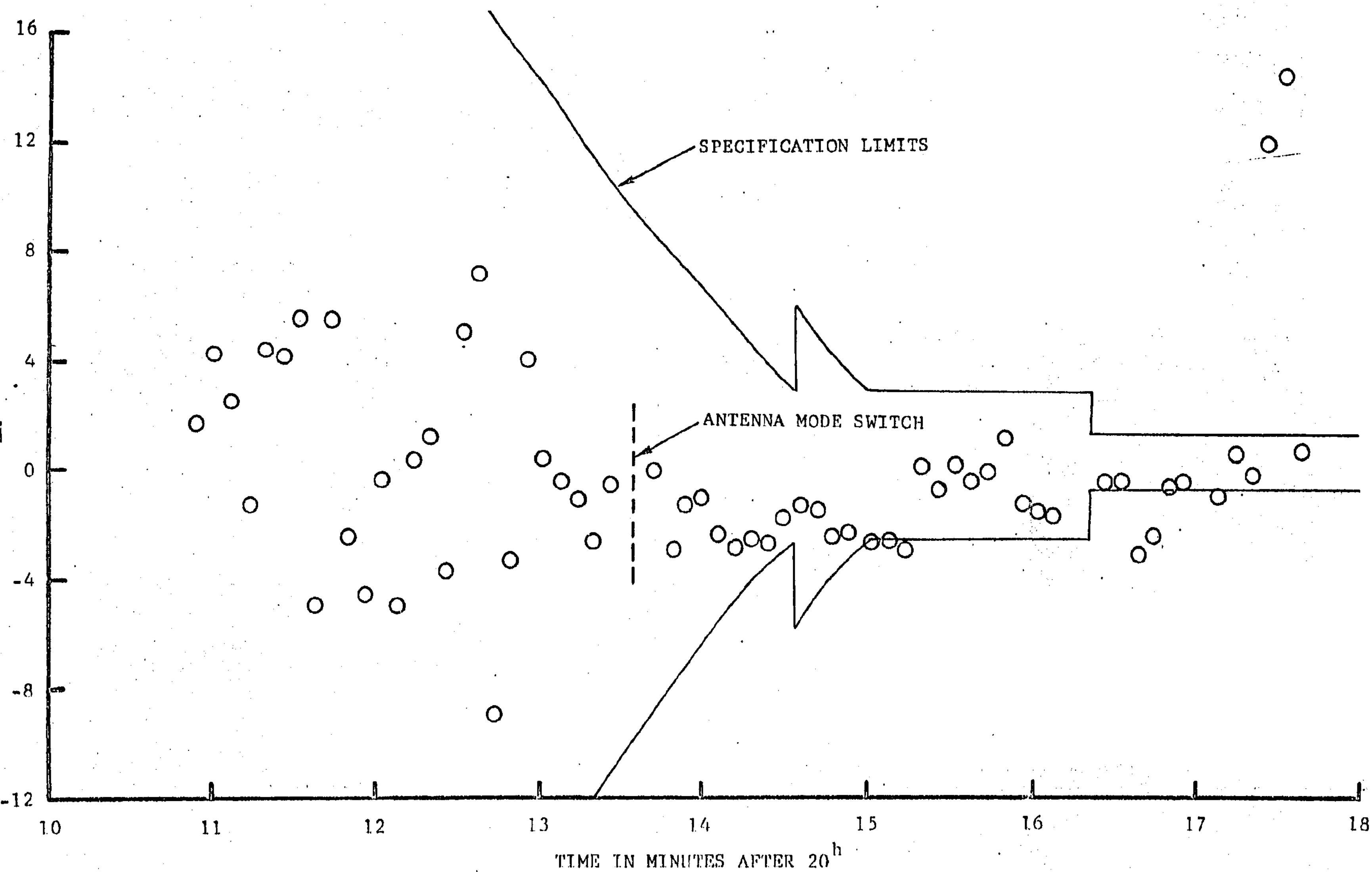


Figure 7-23. Landing Radar Z-Antenna Velocity Residuals (RET#2)

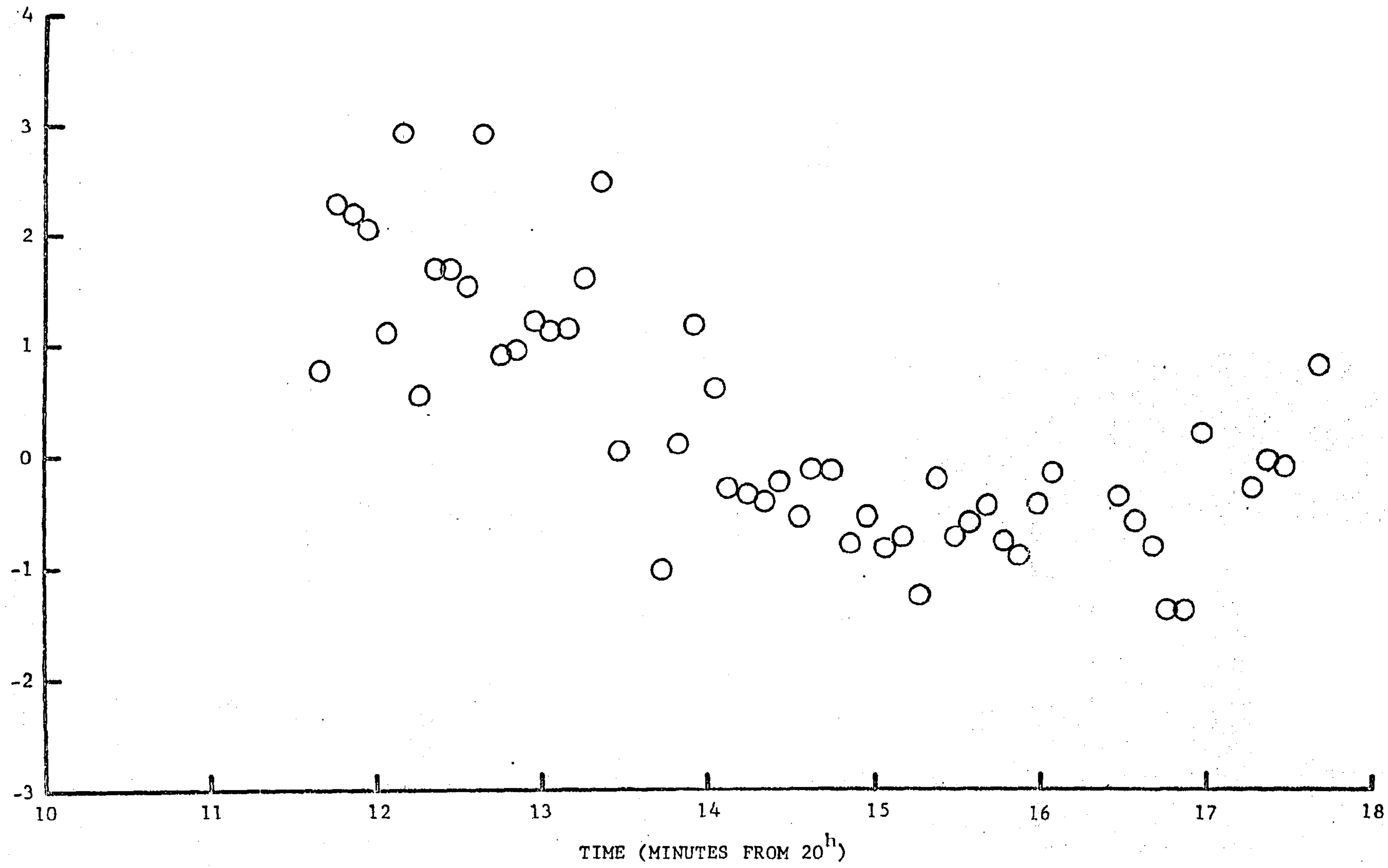


Figure 7-34 . Landing Radar X-Antenna Velocity Residuals (Onboard/MSFN H-S)

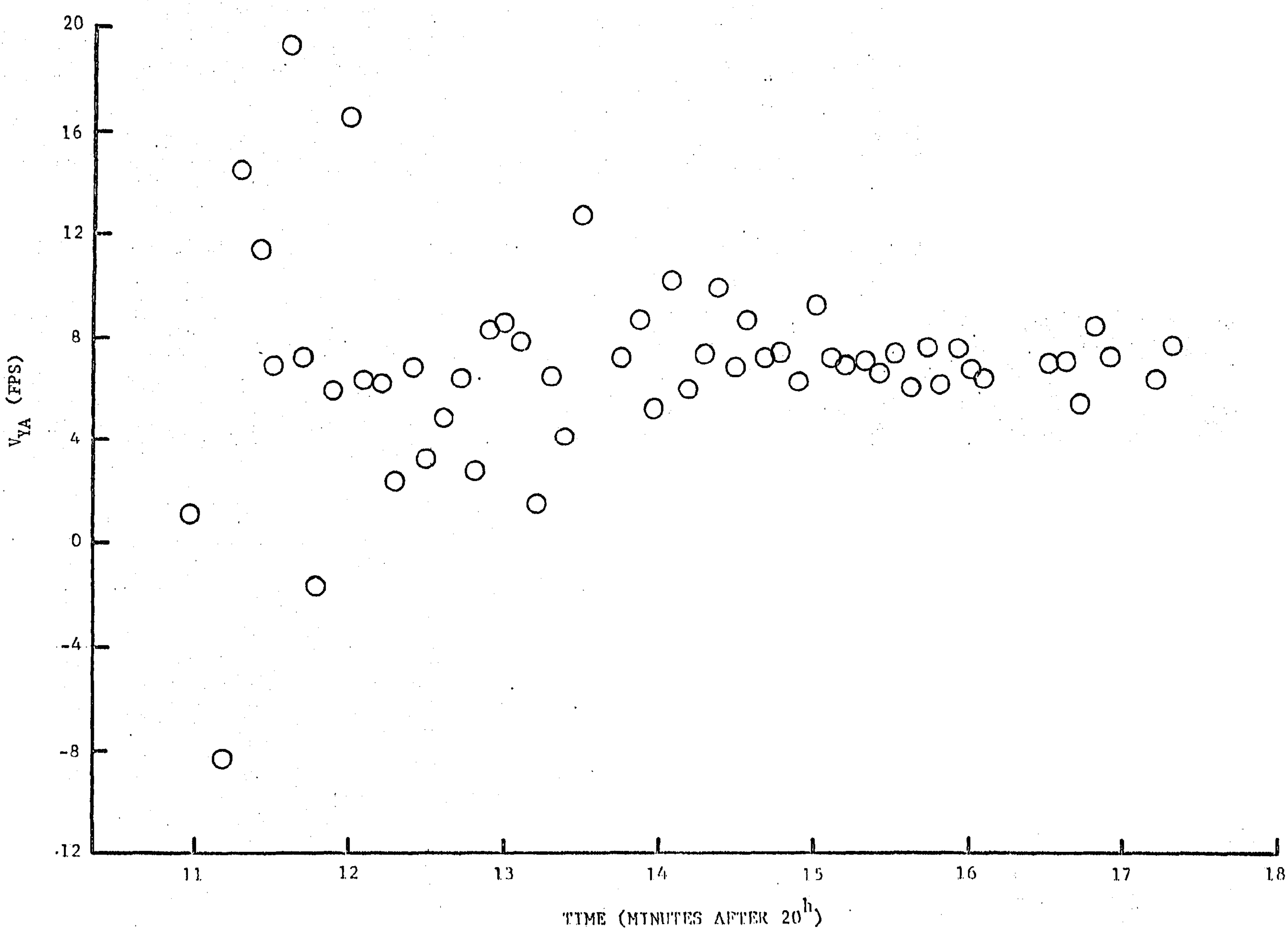


Figure 7-35. Landing Radar Y-Antenna Velocity Residuals (Onboard/MSFN H-S)

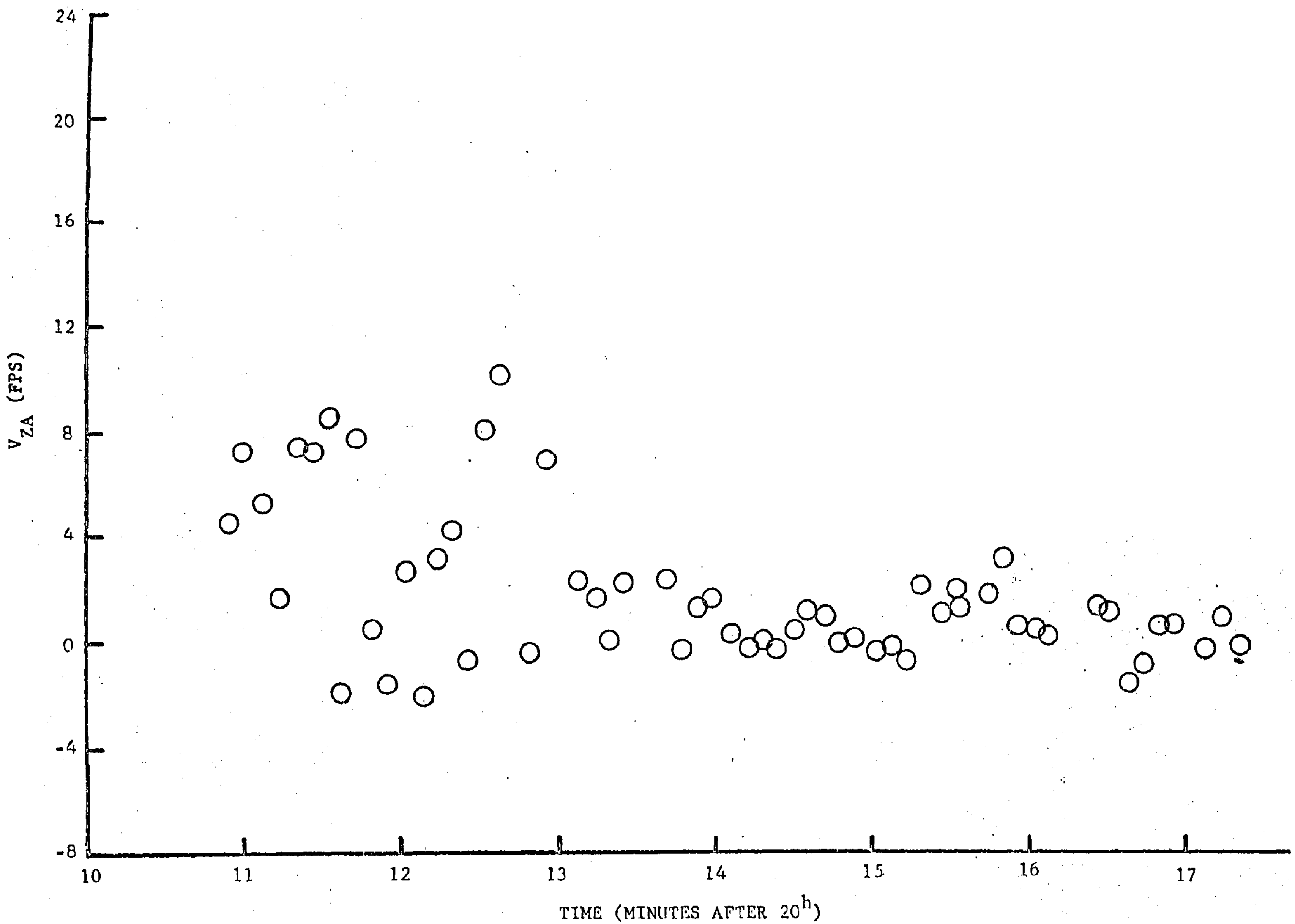


Figure 7-36. Landing Radar Z-Antenna Velocity Residuals (Onboard/MSFN H-S)

7.4.3 Lunar Surface Altitude Along Groundtrack

Landing Radar range residuals are used to compute an estimate of the relative altitude of the surface along the groundtrack of the piercepoint.

Surface altitude relative to the landing site is plotted versus angular range in Figure 7-37. Time ticks are indicated at the LR range read times (2-second intervals).

The ground track of the range beam piercepoint is shown in Figure 7-38. The plot is made on Lunar Maps ORB-II-6 and ORB-I-3 (scale 1: 100,000)*. The latitude does not agree with postflight estimates of Tranquility Base coordinates. Time ticks are at LR range read times and correspond to those on the surface altitude plot. The size of the range beam on the surface is indicated by the small ellipses drawn periodically along the groundtrack.

Little quantitative information can be obtained from Figure 7-38.1 except to note that the gentle upward slope of the terrain on the approach to the landing site is in general agreement with the surface altitude plot.

On Figure 7-38.2, surface altitude variations can be correlated to several prominent features:

The 170 ft drop in altitude between the readings at 102:39:37.19 and 102:39:39.19 correspond to range beam centers at the top and bottom of a cliff.

The point at 102:39:51.19 is centered in a fairly large crater. A depression of approximately 300 ft is clearly outlined in the surface altitude plot.

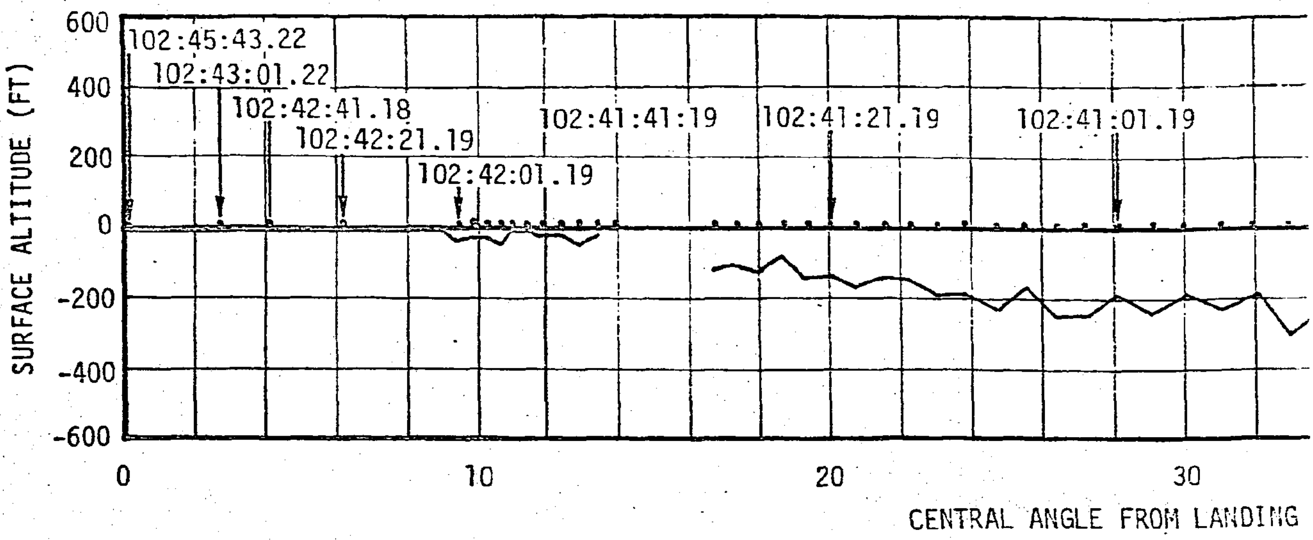
* Map legend: Contour lines (at 50 meter intervals) are indexed by an estimate of the radius in meters with the first three digits omitted. Crater markings such as 45R (110) indicate - Height of rim above terrain = 45 meters, Crater depth (floor to rim) = 110 meters.

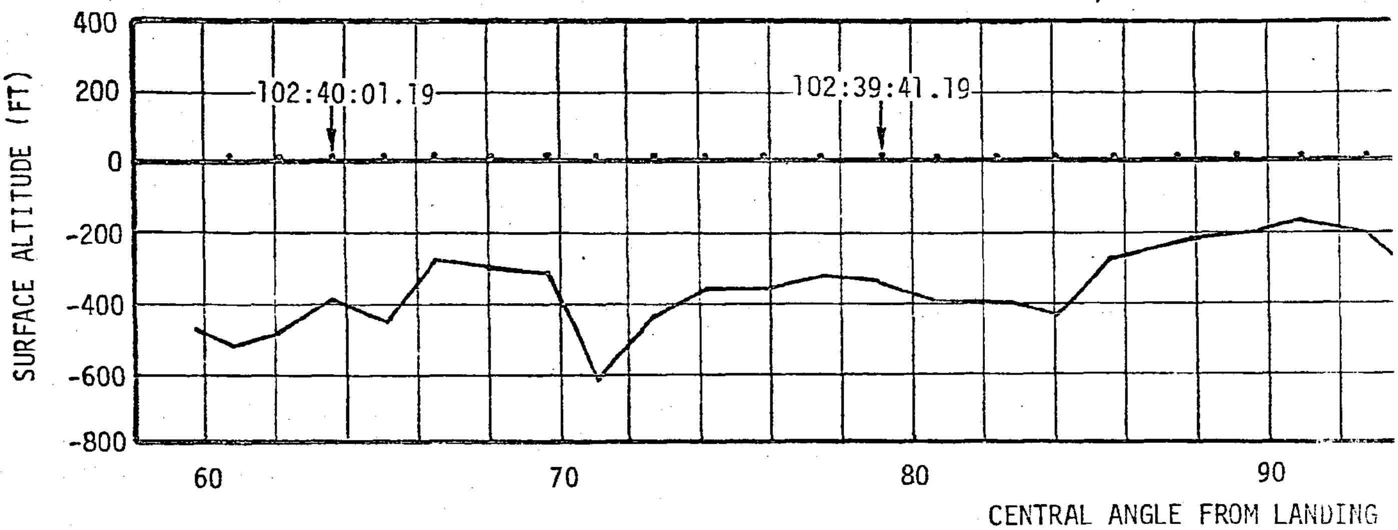
The point at 102:39:23.19 falls inside a crater, and a depression of approximately 200 ft is indicated.

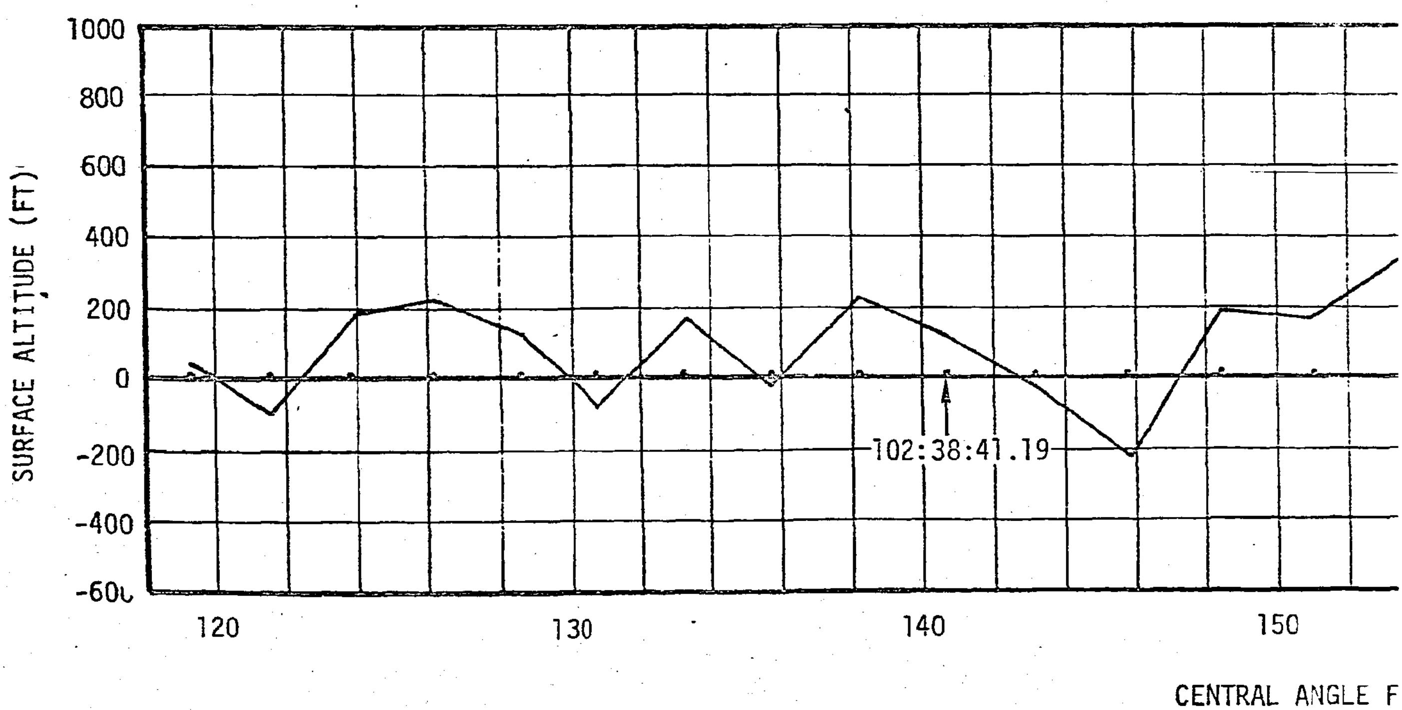
As the range beam intersection grows in size with increasing LM altitude, surface details become increasingly difficult to resolve. The overall downward terrain slope along the groundtrack in Figure 7-38.3 is in general agreement with the surface altitude plot.

The altitude of the LM above the LLS radius during LR range data coverage is shown in Figure 7-39.

The data presented in this section results from a HOPE program orbit determination which includes LR velocity in the DC fit. This option has only recently become available and the results presented here are among the first obtained using Apollo 11 data. The principal effect of including LR velocity in the fit is to produce a more accurate relative velocity profile. Surface altitude plots, derived from earlier versions of the descent trajectory, show unrealistic terrain slopes due to small inplane velocity errors.







FOLDOUT FRAME

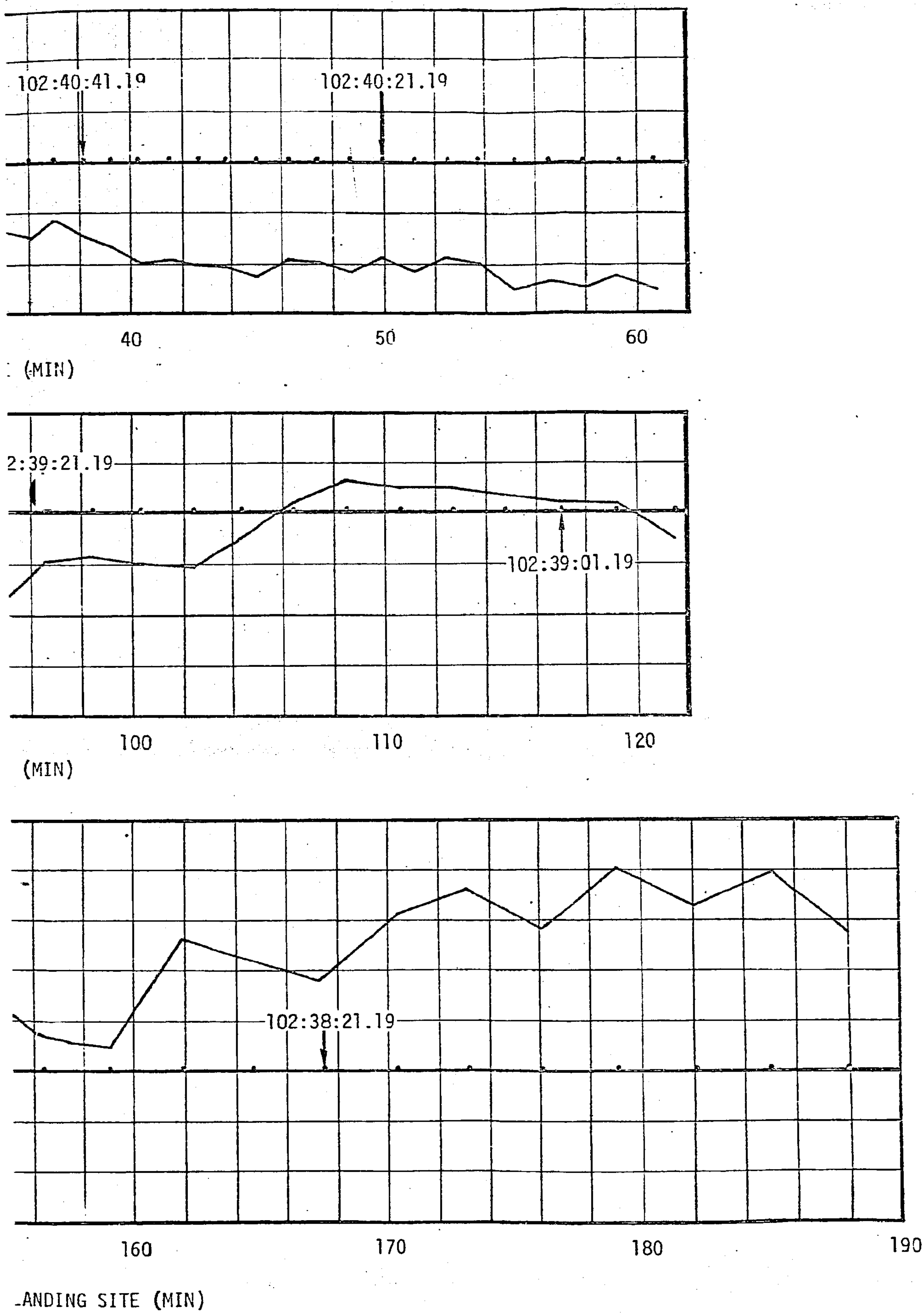
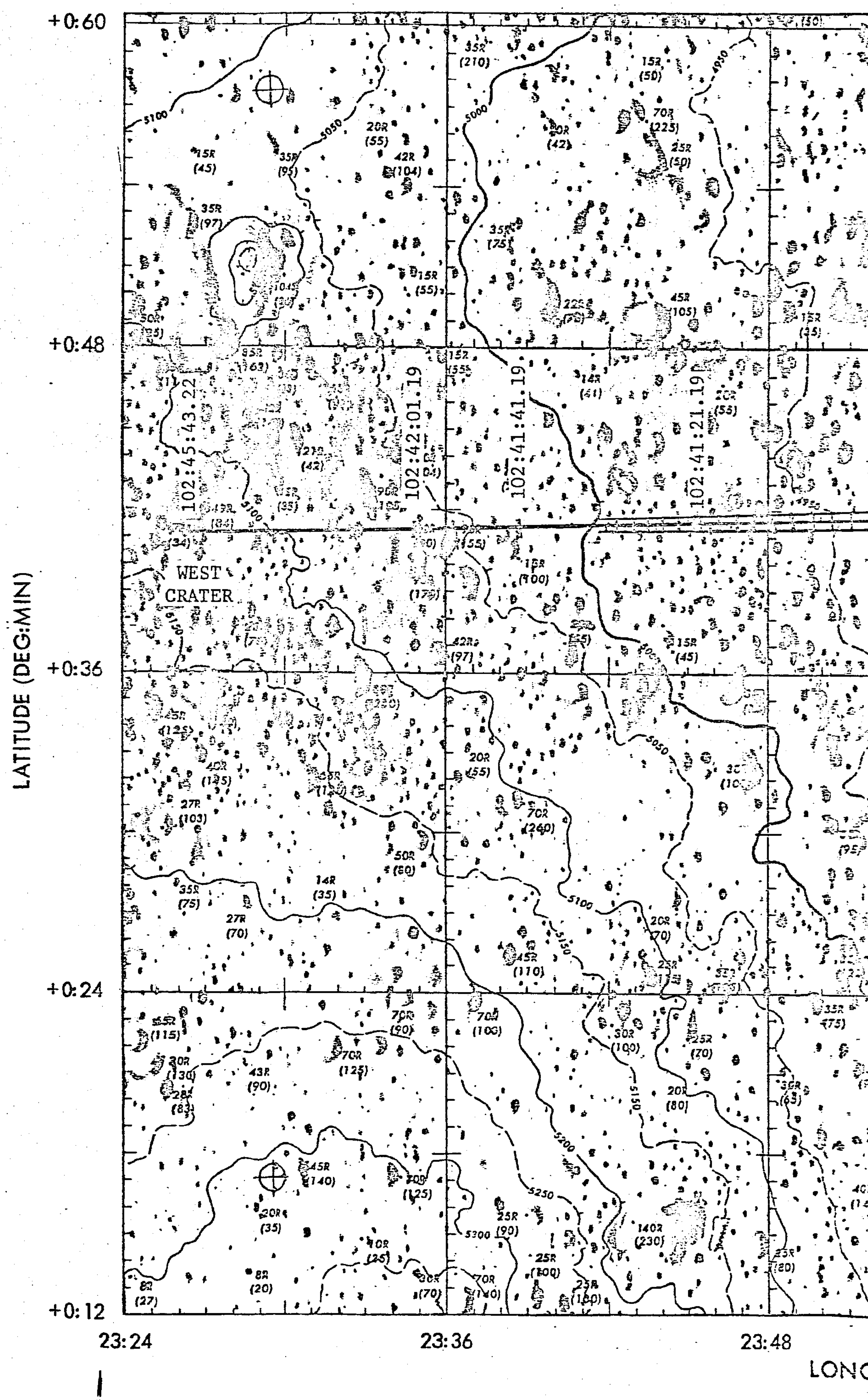


Figure 7-37 Surface Altitude Along Groundtrack

FOLDOUT FRAME 2



FOLDOUT FRAME

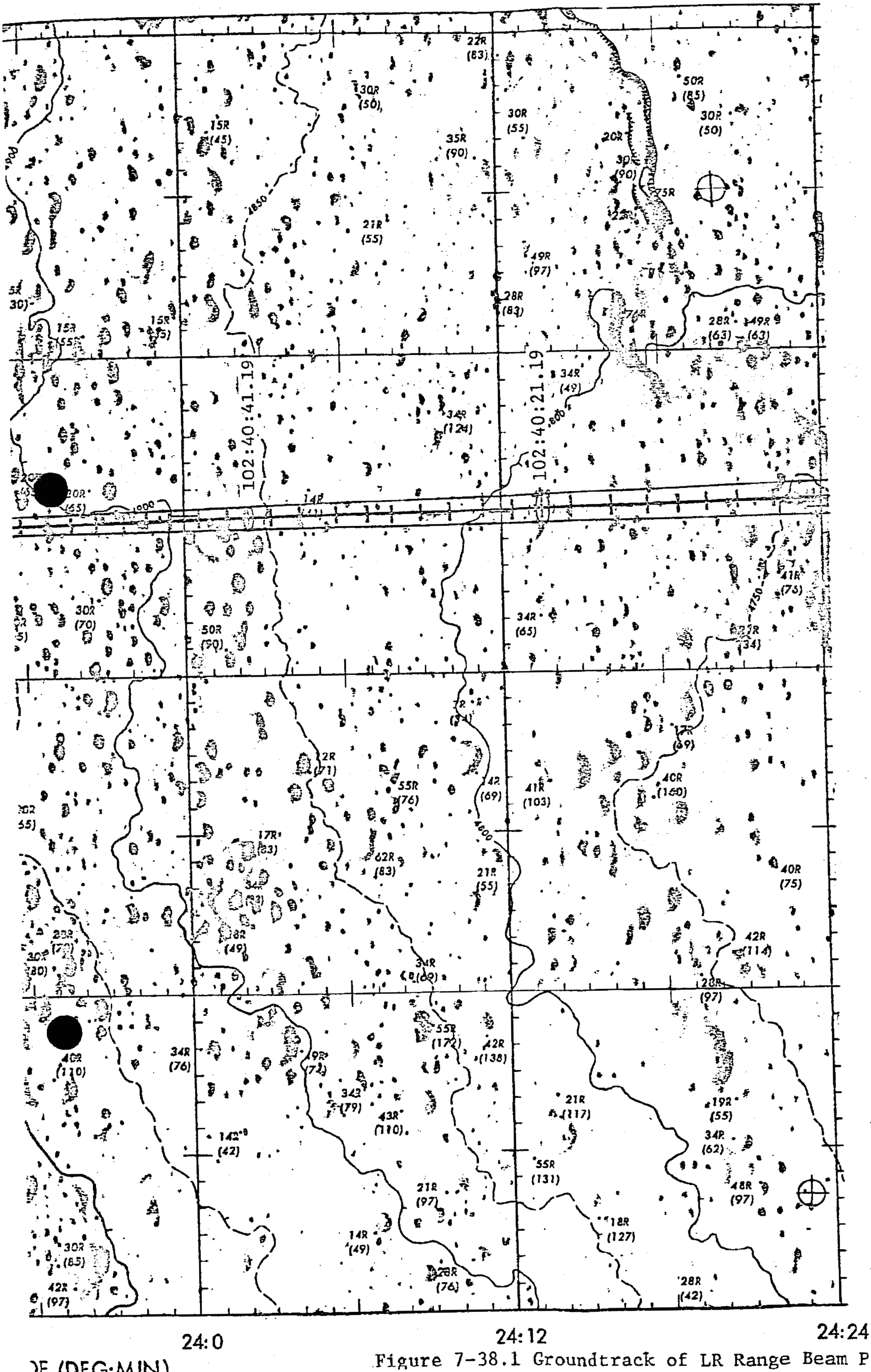
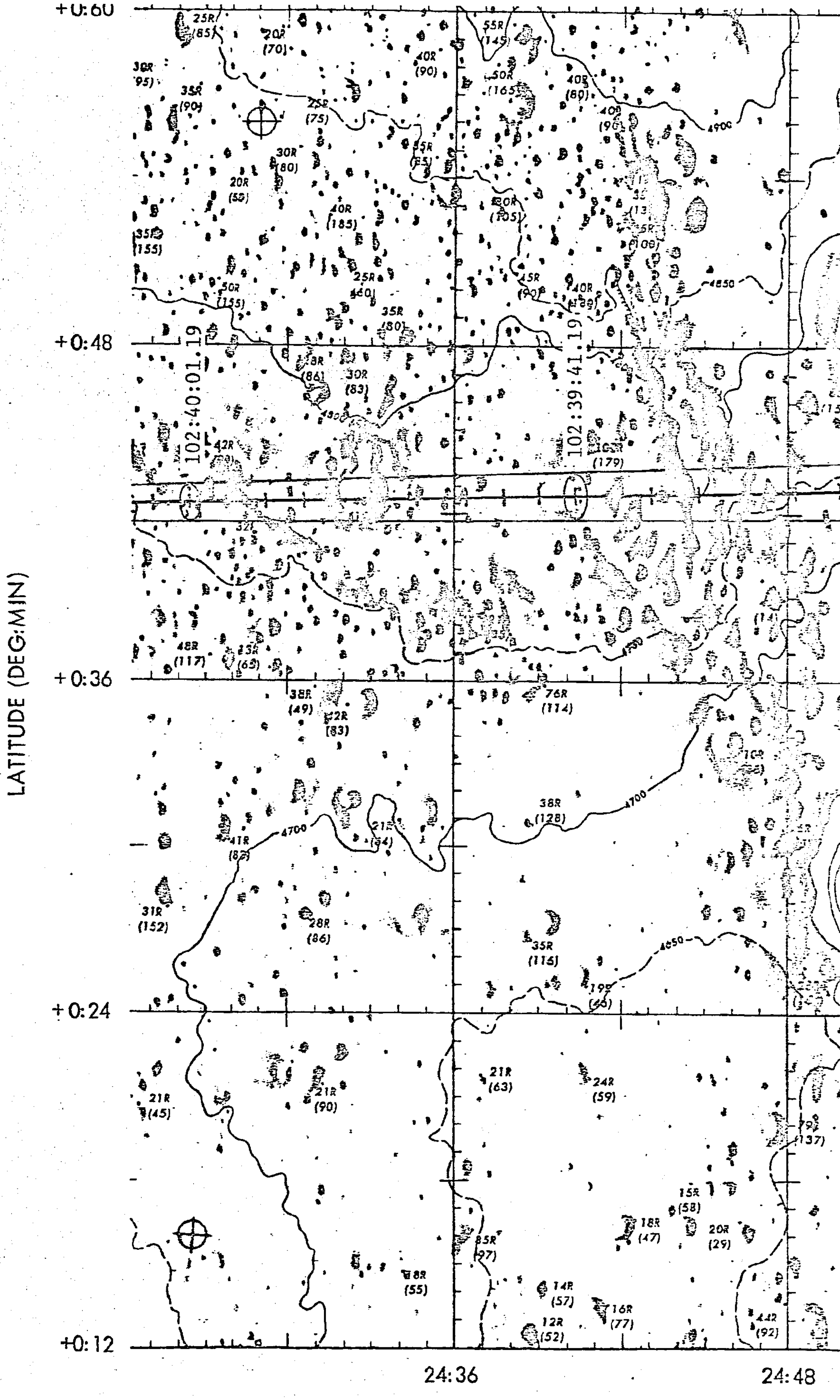


Figure 7-38.1 Groundtrack of LR Range Beam Piercepoint

FOLDOUT FRAME α



FOLDOUT FRAME

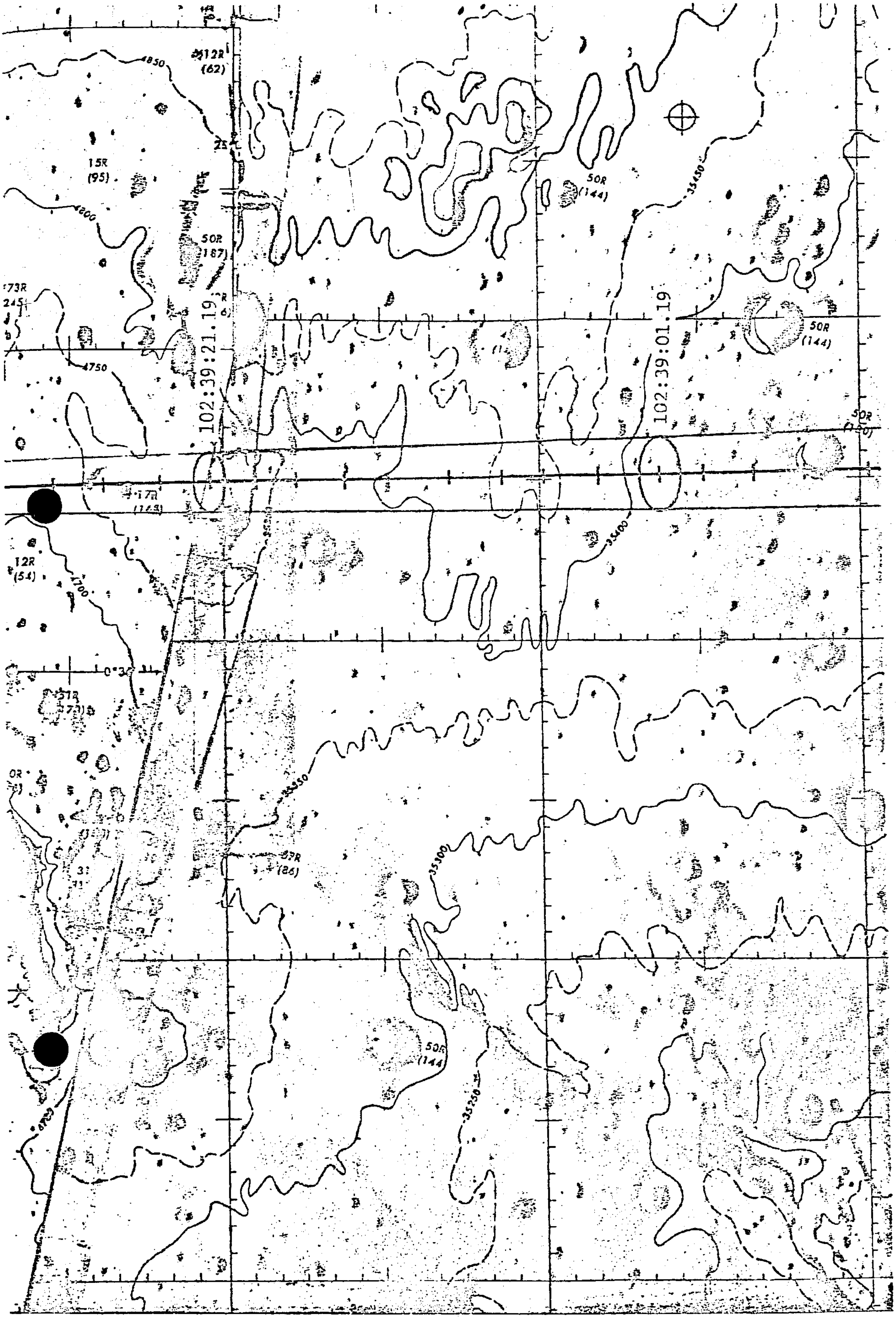
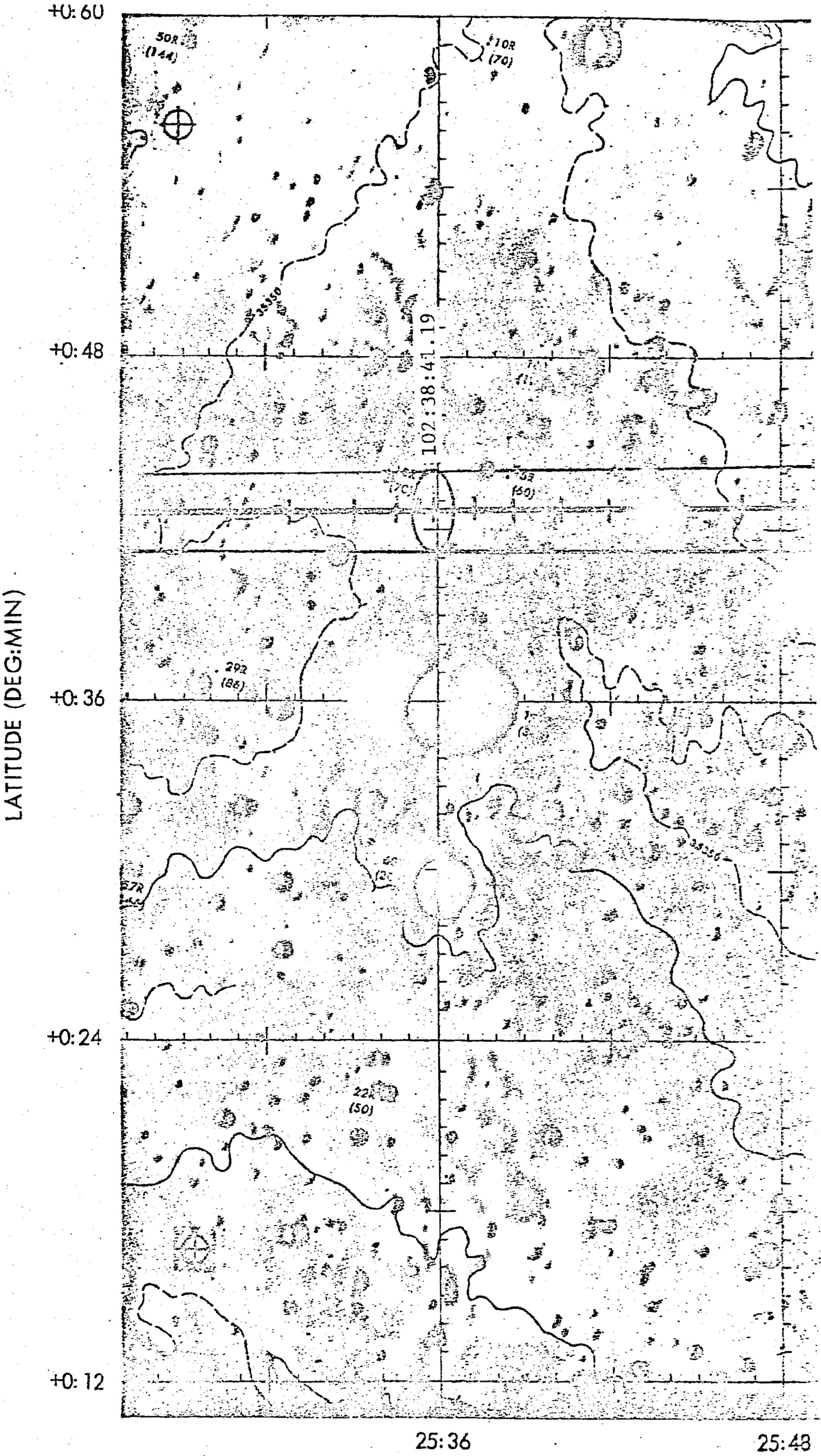


Figure 7-38.2

FOLDOUT FRAME 2



FOLDOUT FRAME

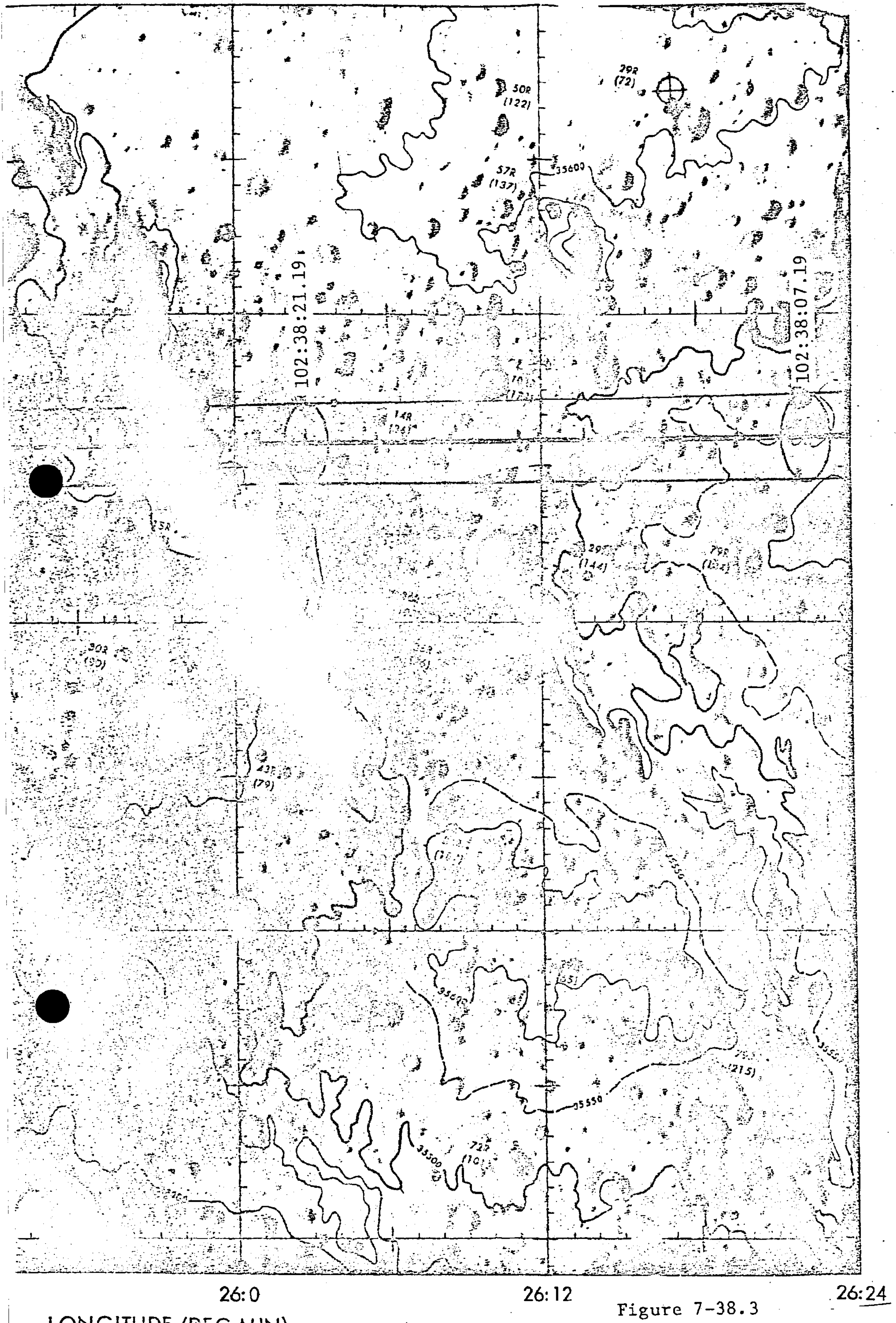


Figure 7-38.3

FOLDOUT FRAME 2

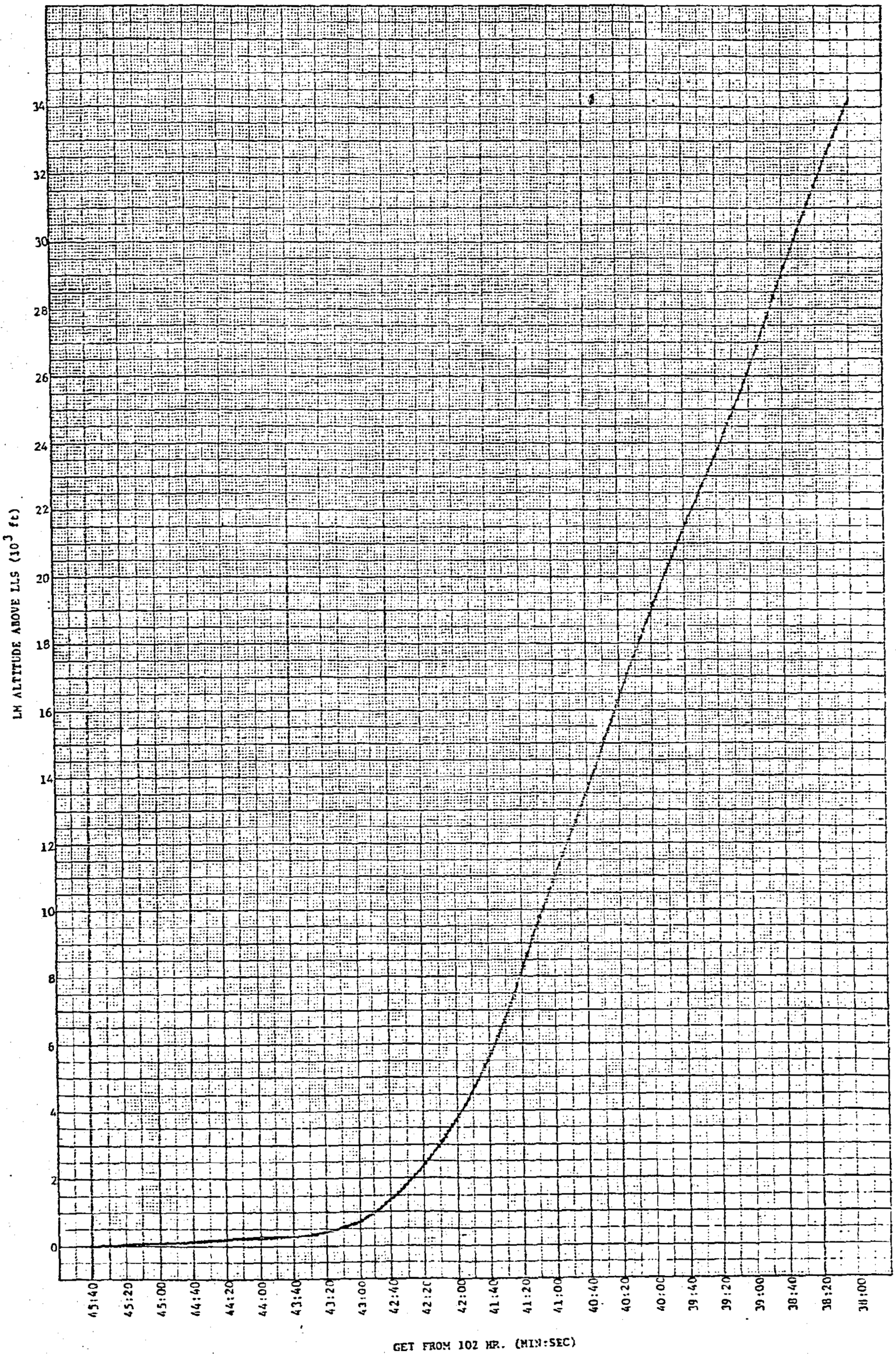


Figure 7-39 Altitude of LM During LR Range Sampling

Page Intentionally Left Blank

REFERENCES

1. Barnett, E. L. and Moore, H. L., "Analysis of Apollo 10 LM Rendezvous Radar Data and CSM VHF Ranging Data", TRW IOC 5522.8-67, 25 July 1969.

2. Barnett, E. L., "Method to Estimate Radar Data Noise", TRW IOC 3422.6-110, 17 May 1967.

3. Barnett, E. L., "Postflight Reconstruction of the Apollo 11 Descent Trajectory Using the HOP[illegible] Program", TRW IOC 5522.8-106, 5 November 1969.

4. "CSM/LM Spacecraft Operational Data Book - Part I", North American Rockwell Corporation, SNA-8-D-027, 1 November 1968.

5. Friedlander, M. M., "Analysis of LM Rendezvous Radar Data for Apollo 9", TRW IOC 5522.[illegible]2, 9 May 1969.

6. Friedlander, M. M., "Preliminary Analysis of Apollo 11 Landing Radar Data", TRW IOC 5522.8-76, 15 August 1969.

7. Hinely, A. O. and Norris, [illegible]., "Lunar Model Analysis For Apollo 12", TRW IOC 5522.8-84, 31 August 1969.

8. Jankowski, S. C., "Summary of the CSM, LM Vectors Used to Generate the Preliminary NAT for Apollo 11", TRW IOC 5522.8-77, 19 August 1969.

9. "Master End Item Spec for Lunar Module", Grumman AED, LSP-470-2D.

10. Schiesser, E. L., "Apollo 11 Landing Site and LM Landing Position Determination", NASA/MSC memorandum 69-FM41-349, 30 October 1969.

Page Intentionally Left Blank

APPENDIX A

Summary of CSM, LM Vectors Used to Generate the Preliminary NAT for Apollo 11

Appendix A documents the vectors used to generate the NAT trajectory in order that the user may know the quality of the trajectory. Since most of the vectors were not based on postflight fits but rather on RTCC vectors which were then propagated, propagation errors arise which can degrade the trajectory.

In order to reduce the error, the lunar orbit propagation times were kept to a minimum. Also, the total difference in position and velocity (which is a measure of the quality of the trajectory) were calculated at a common time point for adjacent trajectory intervals and tabulated in Table A.1 (CSM)and Table A.2 (LM) for user convenience. Whenever two intervals were separated by a maneuver, the ΔV as exhibited in Tables A.1 and A.2 represents the difference between the total velocity difference and the measured velocity of the maneuver.

Each table lists the vector ID and RTCC batch number, the source of the vector, the initial time of the vector, the propagation interval, the total differences in position and velocity of adjacent intervals, and comments relevent to a particular propagation interval. Maneuvers are listed between the appropriate free flight intervals for easy reference.

Most lunar trajectories were generated using RTCC SS2 (inclination constrained) solution vectors as opposed to SS1 (no a priori) solution vectors. Unlike the Apollo 10 SS2 vectors which were constrained to the pre-LOI1, rev 18, and rev 29 planes, the Apollo 11 SS2 vectors were constrained on a rev-to-rev basis. Each SS2 vector contained two revs of data and was constrained to the SS1 solution plane of one of these two revs (exceptions existed at maneuvers).

By using the new SS2 scheme, the Apollo 11 out-of-plane error was not allowed to accumulate as it did during the Apollo 10 mission.

It should be noted that the vectors used to generate the trajectory from insertion to TPI were based on free flight solutions utilizing MSFN data and not RTCC vectors. The quality of the vector from DOI to PDI was questionable, but was included because no better vector was available at that time.

In general, the quality of the CSM trajectory was better than the quality of the LM trajectory during the rendezvous period.

Table A.1 Apollo 11 CSM NAT Trajectories

Vector ID	Source	Vector Time (d:h:m:s) GMT	Trajectory Interval (GMT) (d:h:m:s)	(d:h:m:s)	ΔR (ft)	ΔV (fps)	Comment
GDSS081	RTCC*	16:17:33:48	16:16:22:03	16:17:49:13	346	0.6	TLI to extraction
MILX103	RTCC	16:17:49:24	16:17:49:13	16:18:12:01	6066	0.8	Extraction to evasive
HSKS153	RTCC	17:03:33:18	16:18:12:04.39	17:16:16:57.92	---	0.2	Evasive to MCC2
PIRX034	RTCC	17:16:21:06	17:16:17:01.47	19:04:00:00	15438	0.6	MCC2 to $19^d04^h00^m$
ANGX389	RTCC	19:07:45:24	19:04:00:00	19:17:27:52.38	---	---	$19^d04^h00^m$ to LOI1
PIRX407	RTCC	19:17:47:36	19:17:27:52.38	19:19:28:00	2338	8.91	Rev 1
RIDX420	RTCC	19:17:47:36	19:19:28:00	19:21:43:36	6201	3.8	Rev 2 to LOI2
GWMX455	RTCC	19:22:07:24	19:21:43:53	20:01:37:00	16789	5.76	Revs 3 and 4
GWMX472	RTCC	20:02:02:12	20:01:37:00	20:03:37:00	5438	3.50	Rev 5
HAWX479	RTCC	20:04:02:48	20:03:37:00	20:05:37:00	5092	3.56	Rev 6
HAWX485	RTCC	20:05:58:48	20:05:37:00	20:07:37:00	3963	3.17	Rev 7
CROX490	RTCC	20:07:57:18	20:07:37:00	20:09:32:00	4629	6.03	Rev 8
CROX496	RTCC	20:10:01:42	20:09:32:00	20:11:32:00	4093	2.10	Rev 9
CROX501	RTCC	20:11:53:36	20:11:32:00	20:13:27:00	10114	8.10	Rev 10
MILX507	RTCC	20:13:52:00	20:13:27:00	20:17:22:00	7597	6.39	Revs 11 and 12
ANGX067	RTCC	20:15:50:18	20:17:22:00	20:18:11:58.24	5166	6.36	Rev 13 pre sep
ACNX527	RTCC	20:18:12:36	20:18:11:58.24	20:21:17:00	3666	2.36	Post sep and rev 14
HAWX535	RTCC	20:19:46:54	20:21:17:00	20:23:17:00	5126	3.48	Rev 15
GDSX522	RTCC	20:21:47:06	20:23:17:00	21:01:17:00	8472	5.12	Rev 16
GWMX550	RTCC	20:23:43:12	21:01:17:00	21:03:17:00	3921	3.15	Rev 17
GWMX555	RTCC	21:01:41:42	21:03:17:00	21:05:12:00	4023	3.07	Rev 18
CROX564	RTCC	21:03:40:48	21:05:12:00	21:07:12:00	3915	3.47	Rev 19
HAWX569	RTCC	21:05:38:06	21:17:12:00	21:09:12:00	3754	3.44	Rev 20
NBEX573	RTCC	21:07:36:18	21:09:12:00	21:11:07:00	4342	4.21	Rev 21
MADX579	RTCC	21:09:34:36	21:11:07:00	21:13:07:00	3814	3.05	Rev 22
CROX584	RTCC	21:11:33:06	21:13:07:00	21:15:02:00	6678	5.94	Rev 23
ACNX595	RTCC	21:15:29:12	21:15:02:00	21:18:57:00	5070	3.38	Revs 24 and 25
CDSX600	RTCC	21:17:27:30	21:18:57:00	21:20:57:00	5813	2.99	Rev 26
HAWX625	RTCC	21:21:30:00	21:20:57:00	22:00:02:07.1	4052	4.46	Docking and sep revs 27 and 28
HSKX651	RTCC	22:00:03:06	22:00:02:07.1	22:02:57:00	3065	2.85	Post sep and rev 29
CDSX657	RTCC	22:01:20:12	22:02:57:00	22:04:58:12	7604	5.00	Rev 30
ANGX695	RTCC	22:07:37:36	22:04:58:12	22:14:00:00	---	---	TEI
PAO**	RTACF**	22:20:01:54.53	22:14:00:00	22:20:02:05.29	---	0.1	MCC5
PAO	RTACF	23:05:31:59.99	22:20:02:05.29	23:15:30:00	19159	0.3	
PAO	RTACF	23:15:31:59.99	23:15:30:00	24:01:30:00	20419	0.4	CSM/LM sep
PAO	RTACF	24:01:32:00	24:01:30:00	24:16:21:18	21098	4.7	Entry interface
PAO	RTACF	24:16:35:06	25:16:21:18	24:16:35:06	---	---	

*Real Time computer center (RTCC) on-line listing.
**Real Time auxiliary computer facility (RTACF) checkout monitor for the Postflight Analysis Office (PAO).

Table A.2 Apollo 11 LM NAT Trajectories

Vector	Source	Vector Time (d:h:m:s) GMT	Trajectory Interval (d:h:m:s)	Trajectory Interval (d:h:m:s) GMT	ΔR (ft)	ΔV (fps)	Comment
MSFN FIT	TRW	20:19:08:06.6	20:17:45:38.	20:19:08:14.1	---	---	Undock to DOI
REAL TIME	MPAD	20:20:04:35.17	20:19:08:43.9	20:20:05:04.4	---	---	DOI to PDI
MSFN FIT	TRW	21:18:01:14.88	21:18:01:14.88	21:18:51:34.7	8400	0.7	INS to CSI
MSFN FIT	TRW	21:19:49:46	21:18:52:21.7	21:19:49:46	8558	1.4	CSI to CDH
MSFN FIT	TRW	21:19:50:04.08	21:19:50:04.08	21:20:36:30.8	---	---	CDH to TPI

APPENDIX B

Supplementary Data

Appendix B contains supplementary information which is too detailed for the main body of the report. This information includes a summary of the radar data used in each BET fit segment, a summary of ground and on-board data weights used in HOPE, a summary of the USBS station locations, and a summary of the components used in the R2 and L1 lunar potential models.

Tables B.1 and B.2 list by vehicle statistics computed from the data used in each BET fit, the type and number of observables, and the mean and standard deviations obtained from the residuals calculated in the final iteration of the fit. The range statistics are in feet, doppler units are cycles per second, range rate units are in feet per second, and angular units are degrees.

Table B.3 lists the data weights used in the HOPE Program for ground based radar data and Table B.4 lists the data weights used in the HOPE Program for onboard data by type of observable.

Table B.5 lists the terms of the R2 lunar potential model.

Table B.6 lists the terms of the Langley 1 lunar potential mode, a modification of the R2 model.

Table B.7 lists the S-band tracking stations and their locations as used in the Apollo 11 postflight analysis. All locations are referenced to the Fischer Ellipsoid of 1960. The mean surface refractivity numbers for each station for the month of July are also listed.

Table B.1 CSM BET Ground Based Tracking Data Statistics

Station	Data Type	Number of OBS	Mean	σ
		Rev 13 Segment		
MAD	2-way doppler	122	-.013	.236
MIL	3-way doppler	103	-.009	.246
ACN	3-way doppler	101	-.018	.235
		Rev 14 Segment		
MAD	2-way doppler	142	.002	.186
GDS	3-way doppler	138	.009	.182
ACN	3-way doppler	63	-.004	.171
		Rev 25 Segment		
MAD	2-way doppler	136	.002	.160
MIL	3-way doppler	52	.001	.165
ACN	3-way doppler	47	.007	.157
		Rev 26 Segment		
MAD	2-way doppler	128	.001	.223
MIL	3-way doppler	114	.0005	.199
ACN	3-way doppler	114	.005	.188
GDS	3-way doppler	70	.006	.182

Table B.2 LM BET Ground Based and Onboard Tracking Data Statistics

Station	Data Type	Number of OBS	Mean	σ
	Undock to DOI Segment			
RID	2-way doppler	141	-.023	.193
CYI	3-way doppler	140	-.049	.202
ACN	3-way doppler	112	-.014	.193
ANG	3-way doppler	137	.030	.219
MIL	3-way doppler	114	-.012	.189
	DOI to PDI Segment			
	Sextant shaft	13	-.0097	.015
	Sextant trunnion	13	-.0004	.004
	VHF ranging	18	-26.000	74.000
	Insertion to CSI Segment			
RID	2-way doppler	74	-.022	.315
BDA	3-way doppler	69	-.019	.319
ANG	3-way doppler	72	.059	.315
ACN	3-way doppler	60	.011	.320
MIL	3-way doppler	63	.014	.316
	CDH to Post-TPI Segment			
	Sextant shaft	31	.030	.026
	Sextant trunnion	31	.011	.023
	VHF ranging	29	-394.000	222.000
	Rend. radar shaft	65	-.012	.107
	Rend. radar trunnion	65	-.084	.056
	Rend. radar range	65	142.000	271.000
	Rend. radar range rate	65	-.115	.543

Table B.3 Ground Based Radar Data Weighting

Data Type	Radar	Weighting
Range	USB: 30-ft. antenna 85-ft. antenna	600 ft.
Doppler (2-way)	USB: 30-ft. antenna 85-ft. antenna	0.1 cycle/sec.
Doppler (3-way)	USB: 30-ft. antenna 85-ft. antenna	0.1 cycle/sec.

Table B.4 Onboard Data Weighting

Data Type	Shaft	Trunnion	Range	Range Rate
Rendezvous radar	.01	.01	30.	1.
Sextant	.001	.001		
VHF ranging			30.	

Table B.5 R2 Lunar Potential Model

Term	Value
J2	2.07108×10^{-4}
J3	-2.1×10^{-5}
C22	2.0716×10^{-5}
C31	3.4×10^{-5}
	All other harmonics are zero

Table B.6 L1 Lunar Potential Model

Term	Value
J2	2.07180×10^{-4}
J3	-2.1×10^{-5}
C22	2.0716×10^{-5}
C31	3.4×10^{-5}
C33	2.583×10^{-6}
	All other harmonics are zero

Table B.7 USBS Station Locations

Station	Antenna	Identification	Latitude* (deg)	Longitude* (deg)	Altitude* (ft)	Surface Refractivity
Antigua	30'	ANG	17.01692	298.24715	141.08	378
Ascension	30'	ACN	-7.95510	345.67330	1843.83	353
Bermuda	30'	BDA	32.35195	295.34287	68.90	377
Canary Island	30'	CYI	27.76454	344.36519	567.69	343
Honeysuckle Creek	85'	HSK	-35.58361	148.97805	3757.55	296
Carnarvon	30'	CRO	-24.90705	133.72620	82.00	325
Goldstone	85'	GDS	35.34154	243.12655	2975.066	279
Grand Bahama	30'	GMB	26.63286	281.76234	16.40	386
Guam	30'	GWM	13.31062	144.73747	416.67	373
Guaymas	30'	GYM	27.96382	249.27943	62.34	368
Hawaii	30'	HAW	22.12666	200.33528	3772.97	308
Madrid	85'	MAD	40.45514	355.83183	2551.18	299
Merritt Island	30'	MIL	28.50866	279.30738	32.81	385
Texas	30'	TEX	27.65428	262.62220	32.81	395
Honeysuckle Creek Wing	85'	NBE	-35.40111	148.98153	2199.15	296
Goldstone Wing	85'	PIR	35.38952	243.14078	3186.02	279
Madrid Wing	85'	RID	40.42843	355.75128	2524.93	299

*All quantities are referenced to the Fischer Ellipsoid of 1960.

APPENDIX C

LM Rendezvous Radar Data, CSM VHF Ranging Data and CSM Sextant (Apollo 11)

The LM rendezvous radar data that was used in the analysis are listed in the two card format of the HOPE orbit determination program. The first card specifies the vehicle taking the observation, the vehicle that is being observed, the time of the observation (year (mod 1900), month, day, hour, minute, and second (GMT)), three code numbers, shaft observable, trunnion observable, range observable, and range rate observable. The second card specifies the inner, middle, and outer gimbal angles. The units are feet, degrees, and seconds.

The CSM VHF ranging data are also listed in the same format. The card format differences are the following: 1) vehicle ID's are reversed, 2) code numbers are different, 3) range is the only observable, and 4) gimbal angles are not needed to process the ranging data.

The CSM sextant data are also listed. The card format is also similar to the rendezvous radar cards.

DOI TO PDI

VEH1	VEH2		YYMMDDHHMMSS.SSS	XF	SHAFT(DEG) / INNER(DEG)	TRUN(DEG) / MIDDLE(DEG)	RANGE(FT) / OUTER(DEG)	RRATE(FPS)	
CSM	LEM	69	720184617.695	62	88.2641602	29.1824434			1
					54.6350098	4.6472168	338.5437012		2
CSM	LEM	69	7201925 3.547114				84093.437		1
									2
CSM	LEM	69	720192534.824	62	.5163574	23.3789155			1
					327.7551270	1.8347168	2.5158691		2
CSM	LEM	69	720192540.676	62	.6372070	23.3349702			1
					327.9528809	1.8457031	2.6037598		2
CSM	LEM	69	7201926 3.816114				89136.613		1
									2
CSM	LEM	69	720192729.605114				97035.563		1
									2
CSM	LEM	69	720192610.746	62	1.2524414	22.9257295			1
					329.1064453	1.8676758	3.0322266		2
CSM	LEM	69	720192839.305114				104205.380		1
									2
CSM	LEM	69	720192746.867	62	.4174805	22.0852754			1
					332.3254395	2.0214844	2.5927734		2
CSM	LEM	69	720193019.016114				115871.521		1
									2
CSM	LEM	69	720192856.437	62	359.9121094	22.3022554			1
					333.7866211	2.1643066	2.5048828		2
CSM	LEM	69	720193026.348	62	359.7253418	22.1319673			1
					336.0058594	2.2631836	2.5158691		2
CSM	LEM	69	720193133.504114				125897.112		1
									2
CSM	LEM	69	720193112.766	62	359.5056152	22.1786592			1
					336.9177246	2.3510742	2.5268555		2
CSM	LEM	69	720193234.348114				134950.523		1
									2
CSM	LEM	69	720193212.098	62	.5493164	22.4670503			1
					337.7526855	2.5158691	3.5156250		2

CSM	LEM	69	720193335.516114			144915.354	1
							2
CSM	LEM	69	7201933 1.707 62	359.3627930	23.0026338		1
				338.0273437	2.6696777	3.0212402	2
CSM	LEM	69	720193436.426114			155791.600	1
							2
CSM	LEM	69	720193538.477114			167700.785	1
							2
CSM	LEM	69	7201934 1.316 62	.2197266	22.7362154		1
				339.1369629	2.8125000	3.8012695	2
CSM	LEM	69	720193638.824114			180278.346	1
							2
CSM	LEM	69	720193612.625 62	1.1206055	22.1814058		1
				340.9167480	3.1311035	4.8120117	2
CSM	LEM	69	720193741.965114			194435.693	1
							2
CSM	LEM	69	720193718.957 62	.2307129	22.0221040		1
				341.3562012	3.2958984	4.4714355	2
CSM	LEM	69	720193850.777114			211023.488	1
							2
CSM	LEM	69	720193829.965 62	.1098633	22.7060030		1
				340.7299805	3.5156250	4.8559570	2
CSM	LEM	69	720193953.195114			227125.195	1
							2
CSM	LEM	69	720194053.867114			243712.990	1
							2
CSM	LEM	69	720194154.324114			261212.203	1
							2
CSM	LEM	69	720194254.785114			279562.070	1
							2
CSM	LEM	69	720194356.004114			299127.164	1
							2

INS TO CSI

VEH1	VEH2	YYMMDDHHMMSS.SSS		XFSHAFT(DEG) INNER(DEG)	TRUN(DEG) MIDDLE(DEG)	RANGE(FT) OUTER(DEG)	RRATE(FPS)	
CSM	LEM	69 721182722.246	62	359.3078613	22.7444551			1
				36.1230469	1.6699219	1.5380859		2
LEM	CSM	69 721183052.766	11	359.9890137	.1208496	888923.836	-193.9901	
				259.4860840	1.0437012	.1098633		2
LEM	CSM	69 721183158.105	11	359.5605469	.0769043	876692.312	-179.5511	
				256.1901855	1.0437012	.1428223		2
LEM	CSM	69 7211833 7.746	11	359.9670410	.0439453	864835.992	-164.4841	
				251.7846680	1.1096191	.2087402		2
LEM	CSM	69 721183415.707	11	357.8906250	359.3188477	854105.273	-150.6721	
				249.9938965	.9448242	.8789063		2
LEM	CSM	69 721183523.215	11	354.1003418	355.5175781	844350.078	-136.8601	
				249.8620605	4.0539551	4.3395996		2
LEM	CSM	69 721183641.754	11	354.1113281	2.9113770	834294.719	-121.7931	
				245.4125977	1.8786621	357.1325684		2
LEM	CSM	69 7211837 .504	11	356.2646484	4.5483398	832043.516	-118.0261	
				242.1936035	3.3398438	355.4736328		2
LEM	CSM	69 721183719.246	11	358.7145996	2.5708008	829942.398	-114.2601	
				238.6779785	3.8562012	357.5939941		2
CSM	LEM	69 721183749.316	62	.8459473	21.9534395			1
				.8569336	5.7238770	8.0639648		2
LEM	CSM	69 721183753.215	11	.9667969	358.7475586	826115.359	-107.9821	
				234.4592285	5.5480957	1.6040039		2
CSM	LEM	69 721183753.574	62	.8789063	21.9479463			1
				.6262207	5.7458496	8.1188965		2
CSM	LEM	69 721183842.324	62	358.9782715	21.8518159			1
				357.9016113	6.0974121	7.3608398		2
CSM	LEM	69 7211839 4.004114				818270.469		1
								2
CSM	LEM	69 721184012.098114				812133.586		1

CSI TO CDH

VEH1	VEH2	YYMMDDHHMMSS.SS XF	SHAFT(DEG) INNER(DEG)	TRUN(DEG) MIDDLE(DEG)	RANGE(FT) OUTER(DEG)	RRATE(FPS)	
CSM	LEM	69 72119 217.414114			746693.828		1
							2
CSM	LEM	69 72119 7 2.098114			731503.539		1
							2
CSM	LEM	69 72119 8 2.566114			728283.195		1
							2
CSM	LEM	69 72119 9 4.617114			724941.336		1
							2
CSM	LEM	69 72119 943.887 62	1.1096191	22.5576875			1
			259.3762207	1.5930176	3.2080078		2
CSM	LEM	69 72119 946.906 62	1.0656738	22.6428316			1
			259.1455078	1.5930176	3.1970215		2
CSM	LEM	69 7211910 5.555 62	.8898926	22.8378389			1
			258.0139160	1.6259766	3.1640625		2
CSM	LEM	69 7211910 9.316114			721417.187		1
							2
CSM	LEM	69 721191029.414 62	1.4282227	21.2393281			1
			258.4094238	1.6040039	3.2629395		2
CSM	LEM	69 721191113.117114			717953.797		1
							2
CSM	LEM	69 721191215.125114			714490.414		1
							2
CSM	LEM	69 721191258.777 62	.2856445	22.6373384			1
			249.4555664	2.5158691	4.0979004		2
CSM	LEM	69 7211913 .547 62	.2416992	22.6675508			1
			249.3347168	2.5268555	4.0869141		2
CSM	LEM	69 721191320.387114			710844.742		1
							2
CSM	LEM	69 721191352.465 62	359.3298340	22.5933931			1
			246.7749023	3.0102539	4.1857910		2
CSM	LEM	69 721191357.098 62	359.3847656	22.7691743			1
			246.3684082	3.0651855	4.3505859		2

CSM	LEM	69	121191752.375114			694743.03?		
CSM	LEM	69	721191853.535114			690915.086		
CSM	LEM	69	721191941.215 62	.6152344	22.2473238			1
				229.9328613	.9997559	2.3291016		2
CSM	LEM	69	721191948.887 62	.4724121	22.4121187			1
				229.3945312	1.0327148	2.2961426		2
CSM	LEM	69	7211920 8.625114			686054.195		1
								2
CSM	LEM	69	7211921 3.785 62	359.3957520	21.9946382			1
				226.1096191	1.1645508	1.7907715		2
CSM	LEM	69	721192125.965114			680889.492		1
								2
CSM	LEM	69	7211922 3.438 62	358.4948730	22.1621797			1
				223.0224609	1.3842773	1.5380859		2
CSM	LEM	69	721192226.598114			676636.211		1
								2
CSM	LEM	69	7211923 7.707 62	.7910156	22.8625581			1
				219.1992187	1.0217285	2.6257324		2
CSM	LEM	69	721192424.516 62	359.6594238	22.0660493			1
				216.2438965	.6481934	1.3183594		2
CSM	LEM	69	721192545.574114			662114.297		1
								2
CSM	LEM	69	721192548.605 62	358.6157227	22.0687959			1
				212.1679687	.3845215	.2856445		2
CSM	LEM	69	7211926 9.484 62	359.0002441	21.8655488			1
				211.3549805	.3186035	.4504395		2
CSM	LEM	69	721192933.285 62	358.7145996	21.8902681			1
				201.4892578	.1538086	.0988770		2
LEM	CSM	69	721192935.656 11	359.8461914	356.1877441	643993.273	-84.7531	
				76.0144043	9.2724609	3.3288574		2
LEM	CSM	69	721193041.336 11	354.1113281	2.3400879	638290.234	-87.8921	
				78.5083008	.8789063	357.0886230		2
CSM	LEM	69	721193052.586114			636837.656		1
								2
CSM	LEM	69	7211931 7.395 62	359.1979980	22.0193574			1
				196.8200684	.0329590	.2636719		2
CSM	LEM	69	721193142.527 62	358.8684082	22.0578096			1
				195.0952148	.0109863	.0329590		

LEM	CSM	69 721193149.117 11	359.0551758	359.9011230	632287.039	-90.4031
			70.4113770	7.6574707	359.4946289	2
CSM	LEM	69 7211932 1.266 62	358.6816406	22.0578096		1
			194.2053223	.0219727	359.9340820	2
CSM	LEM	69 7211932 2.215114			630700.781	1
						2
CSM	LEM	69 721193224.527 62	358.4619141	22.0468233		1
			193.1066895	.0549316	359.8352051	2
LEM	CSM	69 721193256.945 11	358.5717773	357.1875000	625983.672	-93.5421
			67.5878906	1.3293457	2.2851563	2
CSM	LEM	69 7211933 5.035114			624867.711	1
						2
LEM	CSM	69 7211934 4.824 11	1.0986328	359.3518066	619605.273	-96.0531
			61.8640137	7.3498535	.2966309	2
LEM	CSM	69 721193512.375 11	357.2753906	2.5378418	613076.797	-98.5651
			62.3693848	355.5834961	357.1545410	2
LEM	CSM	69 721193617.215 11	355.4956055	4.6252441	606623.359	-101.0761
			61.1718750	5.3063965	354.4299316	2
LEM	CSM	69 721193736.617 11	356.5393066	354.8803711	598519.039	-104.8431
			56.3269043	4.1308594	4.3615723	2
LEM	CSM	69 721193842.035 11	.2307129	354.8474121	591540.312	-106.7261
			49.5922852	10.7226562	4.6691895	2
LEM	CSM	69 721194047.637 11	353.4411621	357.3193359	577807.992	-111.7481
			50.3833008	3.9111328	1.7138672	2
LEM	CSM	69 7211941 6.355 11	1.7578125	356.2536621	575706.875	-112.3761
			41.2426758	9.5581055	3.5156250	2
LEM	CSM	69 721194125.125 11	.4284668	.2526855	573680.797	-113.6321
			41.6491699	4.9438477	359.2749023	2
LEM	CSM	69 721194144.145 11	358.5278320	4.3505859	571429.594	-114.2601
			42.6379395	.7910156	355.1220703	2
LEM	CSM	69 7211942 4.105 11	356.6601562	4.6472168	569103.359	-114.2601
			43.5168457	359.3627930	354.8583984	2
LEM	CSM	69 721194227.074 11	355.2209473	3.7792969	566551.992	-115.5151
			43.9343262	1.7578125	355.5285645	2
LEM	CSM	69 721194246.027 11	354.0454102	3.2409668	564375.836	-116.1431
			44.2199707	2.8564453	355.9130859	2
LEM	CSM	69 7211943 5.457 11	353.3203125	2.4938965	562124.633	-116.7711
			44.0222168	2.5927734	356.6601562	2
LEM	CSM	69 721194324.848 11	357.0336914	1.5380859	559873.437	-118.0261
			39.4189453	2.8454590	357.7917480	2

LEM	CSM	69	721194347.367	11	2.8564453	.4614258	557171.992	-118.0261
					32.5195313	.0988770	359.0332031	2
LEM	CSM	69	7211944 7.426	11	2.4279785	359.2199707	554770.719	-118.6541
					32.0141602	4.4384766	.4504395	2

CDH TO TPI

VEH1	VEH2	YYMMDDHHMMSS.SSS	XF	SHAFT(DEG) INNER(DEG)	TRUN(DEG) MIDDLE(DEG)	RANGE(FT) OUTER(DEG)	RRATE(FPS)
LEM	CSM	69 721195358.598	11	358.5058594	353.4082031	481156.477	-124.3041
				7.8552246	353.7487793	6.3281250	2
LEM	CSM	69 7211955 3.687	11	1.5380859	3.2629395	473127.199	-123.6771
				1.6259766	348.9807129	356.0339355	2
CSM	LEM	69 721195535.055	114			468954.590	1
							2
LEM	CSM	69 7211956 9.316	11	355.4626465	355.8471680	465097.918	-123.0491
				4.6472168	356.1328125	4.0649414	2
CSM	LEM	69 721195635.664	114			461420.207	1
							2
LEM	CSM	69 721195717.098	11	359.6923828	355.6384277	456768.477	-123.0491
				357.1545410	356.3635254	3.9770508	2
CSM	LEM	69 721195738.605	114			453764.301	1
							2
LEM	CSM	69 721195824.957	11	354.8254395	3.9111328	448439.039	-122.4211
				358.7475586	358.4838867	355.8361816	2
LEM	CSM	69 721195926.266	11	.3076172	.5932617	441010.078	-122.4211
				350.3430176	357.9345703	359.0441895	2
CSM	LEM	69 721195945.348	114			438209.445	1
							2
LEM	CSM	69 72120 031.117	11	359.9121094		433055.836	-121.7931
				347.7282715	15.1281738	359.6154785	2
LEM	CSM	69 72120 236.715	11	357.7368164	357.8356934	417822.719	-121.1651
				343.8171387	357.7807617	1.9665527	2
LEM	CSM	69 72120 318.117	11	359.7143555	.0329590	412870.078	-121.1651
				339.9060059	7.4157715	359.6484375	2
LEM	CSM	69 72120 336.746	11	1.6589355	358.7915039	410543.836	-120.5381
				337.0605469	5.4272461	1.0766602	2
CSM	LEM	69 72120 348.926	114			408740.285	1
							2
LEM	CSM	69 72120 412.254	11	1.7138672	355.8691406	406266.559	-120.5381
				335.3356934	4.0209961	3.9880371	2

CSM	LEM	69	72120	450.437114				401327.426		1
										2
LEM	CSM	69	72120	520.215	11	355.5834961	2.8564453	398087.199	-120.5381	
						338.2470703	5.0207520	356.5173340		2
LEM	CSM	69	72120	628.125	11	357.2424316	358.3850098	389982.879	-119.9101	
						333.4460449	9.8327637	.9228516		2
CSM	LEM	69	72120	655.426114				386380.180		1
										2
CSM	LEM	69	72120	7 6.906	62	359.4506836	22.5467012			1
						93.6364746	1.0876465	1.2304688		2
CSM	LEM	69	72120	713.957	62	359.3408203	22.5851533			1
						93.2739258	1.1755371	1.2744141		2
LEM	CSM	69	72120	735.625	11	.0659180	359.3737793	381878.559	-119.2821	
						327.3706055	.7690430	.4724121		2
CSM	LEM	69	72120	756.324114				379149.602		1
										2
CSM	LEM	69	72120	813.984	62	359.7692871	22.8350923			1
						90.1977539	1.3732910	1.8237305		2
LEM	CSM	69	72120	842.707	11	358.5498047	2.4499512	373999.359	-118.6541	
						325.7336426	.7800293	357.4072266		2
CSM	LEM	69	72120	844.977	62	359.2858887	22.3791597			1
						89.1979980	1.4721680	1.5820313		2
CSM	LEM	69	72120	9 6.414114				370825.324		1
										2
CSM	LEM	69	72120	917.125	62	358.7145996	21.8023775			1
						88.2751465	1.5930176	1.3183594		2
LEM	CSM	69	72120	951.086	11	355.8581543	3.9550781	365895.039	-118.6541	
						325.2392578	1.0546875	355.8691406		2
CSM	LEM	69	72120	954.586	62	358.5607910	22.0330904			1
						86.2866211	1.5930176	1.1975098		2
CSM	LEM	69	721201017.637114					362379.523		1
										2
LEM	CSM	69	721201059.355		11	358.5827637	4.0759277	357865.758	-118.0261	
						319.3395996	1.4392090	355.8471680		2
CSM	LEM	69	7212011	5.098	62	.1318359	22.8433321			1
						82.2106934	1.0546875	1.4172363		2
CSM	LEM	69	721201128.637114					354055.246		1
										2
LEM	CSM	69	721201310.047		11	357.1655273	358.9453125	342482.559	-116.7711	
						314.7033691	359.3627930	1.1206055		2

LEM	CSM	69	721201328.746	11	353.8366699	357.7258301	340306.398	-116.7711
					317.1752930	359.6923828	2.3620605	2
CSM	LEM	69	721201339.566	62	359.7802734	22.7746675		1
					75.1464844	1.1425781	1.1425781	2
LEM	CSM	69	721201347.437	11	354.5178223	356.2097168	338130.238	-117.3991
					315.6152344	.3845215	3.8342285	2
CSM	LEM	69	721201434.098	62	.1318359	22.5192354		1
					72.8723145	1.6149902	1.9555664	2
CSM	LEM	69	721201436.617114				332059.707	1
								2
CSM	LEM	69	721201447.098	62	359.6594238	22.7499483		1
					72.0703125	1.7687988	1.8786621	2
LEM	CSM	69	721201452.555	11	357.4951172	2.7136230	330551.199	-116.7711
					309.6826172	357.1325684	357.5280762	2
LEM	CSM	69	7212016 .547	11	356.8249512	358.4838867	322596.957	-115.5151
					307.2436523	1.9885254	1.5600586	2
LEM	CSM	69	7212017 8.656	11	2.0764160	359.4177246	314792.797	-115.5151
					298.8830566	3.8122559	.9228516	2
LEM	CSM	69	721201816.816	11	354.5068359	3.9770508	306876.078	-114.8871
					303.3984375	357.4401855	356.5173340	2
LEM	CSM	69	7212020 9.406	11	.3186035	358.9892578	294006.719	-114.2601
					292.5878906	358.3410645	1.3732910	2
LEM	CSM	69	721202038.305	11	356.2426758	.5383301	290695.578	-113.6321
					295.4223633	355.3527832	.1538086	2
LEM	CSM	69	721202145.957	11	358.0554199	.1867676	283032.117	-113.6321
					290.5883789	359.6154785	.2636719	2
LEM	CSM	69	721202251.035	11	357.6928711	359.9670410	275678.199	-113.0041
					288.0944824	1.6259766	.4504395	2
LEM	CSM	69	721202424.887	11	359.3078613	.0549316	265125.699	-112.3761
					282.3706055	6.7016602	.4394531	2
LEM	CSM	69	721202454.926	11	359.8681641	359.7692871	261748.898	-111.7481
					280.5578613	3.4167480	.8239746	2
LEM	CSM	69	721202513.324	11	359.7473145	359.5056152	259694.680	-112.3761
					279.9755859	358.0883789	1.1315918	2
LEM	CSM	69	721202532.207	11	358.6486816	358.7255859	257593.559	-111.7481
					280.2832031	357.3303223	1.9775391	2
LEM	CSM	69	721202550.605	11	356.8029785	357.6379395	255558.100	-111.7481
					281.3049316	359.8242187	3.0432129	2
LEM	CSM	69	7212026 9.004	11	354.1333008	356.2536621	253513.260	-111.7481
					283.1616211	2.8674316	4.1638184	2

LEM	CSM	69	721202627.586	11	350.5078125	354.3969727	251440.279	-111.1211
					285.9741211	6.4270020	5.3063965	2
LEM	CSM	69	721202646.504	11	346.2451172	351.9360352	249329.779	-111.1211
					289.4567871	10.7666016	6.4050293	2
LEM	CSM	69	7212027 5.555	11	343.1799316	354.0563965	247209.898	-111.1211
					291.6979980	6.6467285	4.9768066	2
LEM	CSM	69	721202724.695	11	350.3430176	.4724121	245099.398	-111.1211
					283.8208008	1.8237305	359.9890137	2
LEM	CSM	69	721202743.746	11	359.8352051	.0109863	242998.279	-110.4931
					273.5266113	359.9890137	.7470703	2
LEM	CSM	69	7212028 2.785	11	.3186035	357.4731445	240906.539	-110.4931
					272.2961426	358.0773926	3.2958984	2
LEM	CSM	69	721202821.785	11	359.7912598	354.8913574	238814.799	-109.8651
					272.0874023	356.7041016	5.9216309	2
LEM	CSM	69	721202840.785	11	359.3188477	356.2316895	236732.439	-110.4931
					271.7578125	359.0332031	4.6032715	2
LEM	CSM	69	721202859.797	11	358.8574219	357.6818848	234640.699	-109.8651
					271.4172363	.1757813	3.1530762	2
LEM	CSM	69	721202918.816	11	.1428223	358.9892578	232548.959	-109.8651
					269.3408203	1.0546875	1.8786621	2
LEM	CSM	69	721202937.816	11	358.6816406	.2526855	230466.600	-109.2371
					270.0439453	.9777832	.6042480	2

APPENDIX D

Apollo 11 Landing Radar Data

The LM landing radar data that was used in the analysis is listed in the two card format of the HOPE orbit determination program. The first card specifies the vehicle, the time of the observation (year (mod 1900), month, day, hour, minute, and second), three code numbers, V_{XA} measurement, V_{YA} measurement, V_{ZA} measurement, and the slant range measurement (ρ). The second card specifies the inner, middle, and the outer gimbal angles. The units are feet and feet per second.

LANDING RADAR OBSERVATIONS

VEHI	YYMMDDHHMMSS.SSS	XFVX(FPS) INNER(DEG)	VY(FPS) MIDDLE(DEG)	VZ(FPS) OUTER(DEG)	RANGE(FT)
LEM	69 72020 953.164125				43753.4501
		79.1564941	.2746582	28.0261233	2
LEM	69 72020 955.164125				41897.5701
		78.9147949	359.7583008	20.3796387	2
LEM	69 72020 957.164125				41144.1951
		78.3654785	359.9450684	12.7001953	2
LEM	69 72020 959.164125				39329.5501
		77.9589844	.6701660	4.9328613	2
LEM	69 7202010 1.164125				39005.8501
		77.8491211	1.2744141	1.2524414	2
LEM	69 7202010 3.164125				38671.3601
		78.0468750	1.1865234	3.0541992	2
LEM	69 7202010 5.164125				38520.3001
		78.1457520	.1867676	3.6694336	2
LEM	69 7202010 7.164125				38444.7701
		77.9919434	358.9782715	3.9221191	2
LEM	69 7202010 9.164125				37781.1851
		77.7502441	353.8793945	4.5593262	2
LEM	69 720201011.164125				37473.6691
		77.2558594	359.9352051	5.2294922	2
LEM	69 720201013.164125				37295.6351
		77.9340527	.3569336	4.7680664	2
LEM	69 720201015.164125				37284.8451
		77.8491211	1.2634277	3.8891602	2
LEM	69 720201017.164125				36594.2851
		77.2448730	.6921387	4.2187500	2
LEM	69 720201019.164125				36480.9901
		77.4645996	.5603027	5.0207520	2
LEM	69 720201021.164125				36480.9901
		77.3657227	1.3732910	4.9987793	2
LEM	69 720201025.164125				35666.3451
		77.1789551	358.5058594	3.1201172	2
LEM	69 720201027.164125				35785.0351

```
                                          76.8933105 359.34.8203   2.9663086           2
LEM         69 720201029.164125                                                35191.5841
                                          76.1682129    .8789063   3.186 352           2
LEM         69 720201031.164125                                                34862.4901
                                          76.7724609    .7910156   3.2849121           2
LEM         69 720201033.164125                                                34867.8851
                                          77.1130371 359.9890137   3.2629395           2
LEM         69 720201035.164125                                                34511.9141
                                          77.0031738 359.9340820   3.1081309           2
LEM         69 720201037.164125                                                34290.6201
                                          75.8056641    .5493164   3.0212402           2
LEM         69 720201039.164125                                                33195.4351
                                          74.2895508    .6811523   2.9223633           2
LEM         69 720201041.164125                                                33119.9151
                                          75.3222656    .2307129   2.8894043           2
LEM         69 720201043.164125                                                33087.5351
                                          76.5197754    .0878906   2.9443359           2
LEM         69 720201045.164125                                                32245.9151
                                          74.0039062 359.6484375   2.9553223           2
LEM         69 720201047.164125                                                31733.3901
                                          73.9160156   1.4721680   2.9553223           2
LEM         69 720201049.164125                                                31560.7501
                                          73.4436035    .7031250   2.8344727           2
LEM         69 720201051.164125                                                30890.0551
                                          72.6635742 359.6704102   2.7355957           2
LEM         69 720201053.164125                                                30514.1201
                                          72.9492188 359.8022461   1.1206055           2
LEM         69 720201054.086125                         1204.332                       1
                                          72.9931641 359.8352051 359.2968750           2
LEM         69 720201055.164125                                                30449.3801
                                          73.2128906 359.8022461 358.6596680           2
LEM         69 720201057.164125                                                30109.4951
                                          72.0373535 359.6044922 359.0551758           2
LEM         69 720201058.176125         -94.0511999                                    1
                                          71.7077637    .1318359 359.3408203           2
LEM         69 720201059.164125                                                29311.0351
                                          70.6640625    .5273438 359.4726562           2
LEM         69 7202011   .246125                        1232.243                       1
                                          69.8510742    .9008789 359.6813965           2
LEM         69 7202011 1.164125                                                28884.8301
                                          70.1636777   1.1206055 359.8352051           2
```

LEM	69 7202011 3.164125					27573.8451
		71.1584473	.8349609	.1098633		2
LEM	69 7202011 5.164125					28388.4901
		70.9277344	.3076172	.2746582		2
LEM	69 7202011 6.277125		-46.0559998			1
		70.0048828	.2416992	.3186035		2
LEM	69 7202011 7.164125					27676.3501
		69.0270996	359.9450684	.3735352		2
LEM	69 7202011 7.934125			1176.941		1
		68.9941406	.3076172	.3955078		2
LEM	69 7202011 9.164125					27325.6751
		68.7963867	.5712891	.4394531		2
LEM	69 720201111.164125					27309.4901
		69.5324707	.9997559	.4394531		2
LEM	69 720201111.957125		-94.7783995			1
		68.8293457	.1208496	.4394531		2
LEM	69 720201113.164125					26921.0501
		68.3459473	359.4177246	.3186035		2
LEM	69 720201113.957125			1138.975		1
		67.9174805	359.4836426	.3295898		2
LEM	69 720201115.164125					26726.8301
		67.9284668	.4284668	.2526855		2
LEM	69 720201117.164125					26273.6501
		66.8627930	.9008789	.1318359		2
LEM	69 720201117.957125		-59.6303992			1
		66.4562988	.8569336	.0549316		2
LEM	69 720201119.164125					25836.6551
		65.9729004	.6811523	359.9340820		2
LEM	69 720201119.957125			1136.895		1
		65.6872559	.5383301	359.7692871		2
LEM	69 720201121.164125					25797.1751
		66.4233398	1.0107422	359.6374512		2
LEM	69 720201123.164125					25798.8901
		67.1044922	.8239746	359.2419434		2
LEM	69 720201124.086125		-81.4463987			1
		67.1923828	.2966309	358.9892578		2
LEM	69 720201125.164125					25397.9451
		66.7639160	359.5275879	358.9123535		2
LEM	69 720201126.086125			1038.426		1
		67.7636719	.2526855	358.9782715		2
LEM	69 720201127.164125					25361.8951

```
                                 68.4228516    .9887695 358.9672852           2
LEM         69 720201129.164125                                     25016.6151
                                 67.5439453    .4064941 358.9233398           2
LEM         69 720201130.055125            -95.5056000                        1
                                 66.6870117 359.8022461 358.9892578           2
LEM         69 720201131.164125                                     24628.1751
                                 66.5441895 359.7253418 358.9782715           2
LEM         69 720201131.926125                            1014.676           1
                                 66.1816406 359.5275879 359.0332031           2
LEM         69 720201133.164125                                     24487.9051
                                 66.7089844 359.6594238 359.0002441           2
LEM         69 720201135.164125                                     24547.2501
                                 67.3022461 359.9670410 359.0112305           2
LEM         69 720201135.887125            -73.6896000                        1
                                 66.9177246    .0439453 358.9782715           2
LEM         69 720201137.164125                                     24282.8951
                                 67.2363281    .7250977 359.0112305           2
LEM         69 720201137.895125                             960.068           1
                                 66.4562988    .2526855 358.9343262           2
LEM         69 720201139.164125                                     23856.6901
                                 66.1486816 359.9340820 359.0441895           2
LEM         69 720201139.887125-978.4935837                                   1
                                 65.6652832 359.5605469 359.0332031           2
LEM         69 720201141.164125                                     23479.0401
                                 65.7202148 359.9340820 359.1101074           2
LEM         69 720201141.887125            -74.4167995                        1
                                 65.5554199    .4943848 359.1540527           2
LEM         69 720201143.164125                                     23203.8951
                                 65.3796387   1.3513184 359.1870117           2
LEM         69 720201143.965125                             960.588           1
                                 64.7534180   1.3732910 359.2529297           2
LEM         69 720201145.164125                                     22723.7401
                                 63.5888672    .6591797 359.1979980           2
LEM         69 720201145.895125-912.5479889                                   1
                                 63.2702637    .5053711 359.2309570           2
LEM         69 720201147.164125                                     22383.8551
                                 62.9077148    .1428223 359.1760254           2
LEM         69 720201147.895125            -80.2343988                        1
                                 63.5559082    .7141113 359.1760254           2
LEM         69 720201149.164125                                     22383.8551
                                 64.0283203   1.1755371 359.1650391           2
```

LEM	69	720201149.926125				920.542		1
			64.3469238	1.4282227	359.0991211			2
LEM	69	720201151.164125					22254.375	1
			63.5019766	.6811523	359.0771484			2
LEM	69	720201151.895125	-891.4247894					1
			63.3471680	.4064941	359.0441895			2
LEM	69	720201153.164125					21542.235	1
			62.5451660	359.7473145	359.2529297			2
LEM	69	720201153.887125		-93.3239994				1
			62.4572754	359.5935059	359.3627930			2
LEM	69	720201155.164125					21202.350	1
			62.1057129	359.7692871	359.5715332			2
LEM	69	720201155.887125				911.180		1
			62.0617676	359.9121094	359.7143555			2
LEM	69	720201157.164125					20921.81	1
			62.0537812	.6262207	359.9711230			2
LEM	69	720201157.895125	-845.0567856					1
			61.9519043	.8459473	.0549316			2
LEM	69	720201159.164125					20835.490	1
			61.9628906	1.5930176	.1757813			2
LEM	69	720201159.895125		-40.7231994				1
			61.2817383	1.2854004	.2856445			2
LEM	69	7202012 1.164125					20376.915	1
			60.8312988	1.3842773	.3845215			2
LEM	69	7202012 1.887125				905.633		1
			60.2050781	.9997559	.4284668			2
LEM	69	7202012 3.164125					20139.535	1
			60.2929687	.9997559	.5383301			2
LEM	69	7202012 3.895125	-791.4759903					1
			59.9633789	.6701660	.5383301			2
LEM	69	7202012 5.164125					19923.735	1
			60.5346680	.6152344	.6262207			2
LEM	69	7202012 5.887125		-62.5391994				1
			60.5017090	.4614258	.6262207			2
LEM	69	7202012 7.164125					19643.195	1
			61.2268066	.3735352	.6481934			2
LEM	69	7202012 7.887125				846.517		1
			61.2597656	.4724121	.6591797			2
LEM	69	7202012 9.164125					19448.975	1
			61.4355469	.4284668	.6152344			2
LEM	69	7202012 9.887125	-787.2255859					1

			61.3476562	.8239746	.6481934		2
LEM	69	720201211.164125				19058.300	1
			60.9982031	.8789063	.5932617		2
LEM	69	720201211.895125		-49.9655995			1
			60.7653809	1.4941406	.5822754		2
LEM	69	720201213.164125				18774.600	1
			59.8205566	1.7468262	.5493164		2
LEM	69	720201213.895125			835.422		1
			59.7436523	2.3510742	.4943848		2
LEM	69	720201215.164125				18365.235	1
			58.9196777	1.3073730	.4284668		2
LEM	69	720201215.957125	-734.4175873				1
			59.1833496	1.0217285	.2856445		2
LEM	69	720201217.164125				17981.535	1
			58.7878418	.0549316	.1538086		2
LEM	69	720201217.937125		-68.5991993			1
			59.6118164	.3405762	.0219727		2
LEM	69	720201219.164125				17857.450	1
			59.9743652	.8020020	359.8681641		2
LEM	69	720201219.895125			783.587		1
			60.6445313	1.2634277	359.7473145		2
LEM	69	720201221.164125				17522.960	1
			59.6777344	1.0107422	359.4946289		2
LEM	69	720201221.895125	-713.8095856				1
			59.4140625	.5822754	359.4067383		2
LEM	69	720201223.164125				17193.865	1
			58.5681152	.3625488	359.3078613		2
LEM	69	720201223.895125		-74.1743994			1
			58.4033203	359.9670410	359.3847656		2
LEM	69	720201225.164125				16859.375	1
			58.2495117	.3405762	359.4396973		2
LEM	69	720201225.926125			766.945		1
			58.2385254	.2197266	359.4726562		2
LEM	69	720201227.164125				16600.415	1
			58.6560059	1.0766602	359.5385742		2
LEM	69	720201227.895125	-679.8063812				1
			58.7219238	1.1425781	359.5385742		2
LEM	69	720201229.164125				16422.380	1
			59.1833496	1.8896484	359.5605469		2
LEM	69	720201229.895125		-48.9647999			1
			58.4912109	1.4611816	359.5495605		2

```
LEM      69 720201231.164125                                           16023.1501
                               58.1945801   1.1755371 359.5166016              2
LEM      69 720201231.895125                                746.662            1
                               57.4914551    .9118652 359.4726562              2
LEM      69 720201233.164125                                           15683.2651
                               57.5463867    .7800293 359.3957520              2
LEM      69 720201233.887125-636.2719879                                       1
                               57.0849609    .9228516 359.4506836              2
LEM      69 720201235.164125                                           15381.1451
                               57.5024414   1.0327148 359.5166016              2
LEM      69 720201235.887125             -46.5407996                           1
                               57.2827148   1.4501953 359.5825195              2
LEM      69 720201237.164125                                           15122.1851
                               57.7990723   1.5161133 359.6264648              2
LEM      69 720201237.895125                                707.135            1
                               57.8979492   1.9445801 359.6264648              2
LEM      69 720201239.164125                                           14825.4601
                               58.6120605   1.6040039 359.6594238              2
LEM      69 720201239.937125-628.5439911                                       1
                               58.7438965   1.6149902 359.6154785              2
LEM      69 720201241.164125                                           14474.7851
                               58.5351562    .4064941 359.6154785              2
LEM      69 720201242.055125             -51.8736000                           1
                               57.9748535    .6591797 359.5495605              2
LEM      69 720201243.164125                                           14145.6901
                               56.9860840    .5603027 359.5605469              2
LEM      69 720201243.895125                                661.022            1
                               56.8762207    .9887695 359.5385742              2
LEM      69 720201245.164125                                           13816.5951
                               56.6674805    .8459473 359.4616699              2
LEM      69 720201245.957125-591.8359909                                       1
                               57.5573730    .7141113 359.4177246              2
LEM      69 720201247.164125                                           13563.0301
                               57.9199219    .2746582 359.4067383              2
LEM      69 720201247.895125             -56.4791994                           1
                               58.3593750    .3295898 359.5275879              2
LEM      69 720201249.164125                                           13190.7751
                               56.9531250   1.2963867 359.7253418              2
LEM      69 720201249.895125                                632.071            1
                               56.5026855   1.5930176 359.8681641              2
LEM      69 720201251.164125                                           12910.2351
```

```
                                    55.6457520   1.7248535    .0000000            2
LEM        69 720201251.895125-543.9455948                                        1
                                    55.9643555   1.0107422    .0769043            2
LEM        69 720201253.164125                                          12516.4001
                                    56.0961914    .5053711    .1428223            2
LEM        69 720201253.937125              -48.9647999                           1
                                    56.6674805    .0988770    .2087402            2
LEM        69 720201255.164125                                          12322.1801
                                    56.7553711   1.4062500    .3186035            2
LEM        69 720201255.887125                             599.306                1
                                    56.6784668   1.7358398    .3845215            2
LEM        69 720201257.164125                                          11998.4801
                                    56.4477539   2.6916504    .4943848            2
LEM        69 720201257.895125-526.9277916                                        1
                                    56.3598633   1.7578125    .5053711            2
LEM        69 720201259.164125                                          11734.1251
                                    56.5686035    .7360840    .5163574            2
LEM        69 720201259.895125              -45.3287997                           1
                                    56.5026855 359.9459684    .5053711            2
LEM        69 7202013 1.164125                                          11437.4001
                                    56.9750977    .6701660    .5383301            2
LEM        69 7202013 1.887125                             555.272                1
                                    56.7224121   1.1096191    .5712891            2
LEM        69 7202013 3.164125                                          11226.9951
                                    56.8212891   2.0324707    .5932617            2
LEM        69 7202013 3.895125-501.8047905                                        1
                                    56.4697266   2.2631836    .6042480            2
LEM        69 7202013 5.164125                                          10957.2451
                                    57.1179199   1.7138672    .5493164            2
LEM        69 7202013 5.895125              -25.4519999                           1
                                    57.0959473   1.3073730    .5053711            2
LEM        69 7202013 7.164125                                          10601.1751
                                    57.3815918    .4174805    .4284668            2
LEM        69 7202013 7.895125                             513.666                1
                                    56.7663574    .5603027    .3845215            2
LEM        69 7202013 9.164125                                          10342.2151
                                    56.2280273    .1977539    .3295898            2
LEM        69 7202013 9.926125-469.6047897                                        1
                                    55.7446289    .4064941    .2526855            2
LEM        69 720201311.164125                                           9996.9351
                                    55.6677246    .0109863    .1647949            2
```

LEM	69	720201311.895125		-44.8439999			1
			55.7446289	.2526855	.0769043		2
LEM	69	720201313.164125				9743.370	1
			56.1071777	359.9450684	359.9670410		2
LEM	69	720201314.055125			473.793		1
			56.5466309	.2307129	359.8242187		2
LEM	69	720201315.164125				9473.620	1
			56.9421387	.1757813	359.7253418		2
LEM	69	720201315.926125	-454.4063911				1
			57.1728516	.7690430	359.6154785		2
LEM	69	720201317.164125				9171.500	1
			56.6125488	1.9116211	359.7253418		2
LEM	69	720201317.957125		-12.8471999			1
			56.6125488	2.5708008	359.9681641		2
LEM	69	720201319.164125				8928.725	1
			55.8984375	2.5598145	.0878906		2
LEM	69	720201319.895125			438.427		1
			56.1730957	2.0104980	.1977539		2
LEM	69	720201321.164125				8610.420	1
			55.9753418	1.5490723	.2966309		2
LEM	69	720201321.895125	-418.7287903				1
			56.2390137	1.0437012	.4174805		2
LEM	69	720201323.164125				8351.460	1
			56.0522461	1.0986328	.4833984		2
LEM	69	720201323.895125		-26.6639998			1
			56.1950684	.8569336	.5932617		2
LEM	69	720201325.164125				8022.365	1
			55.9863281	1.1315918	.6701660		2
LEM	69	720201325.895125			402.369		1
			55.8544922	.9777832	.7250977		2
LEM	69	720201327.164125				7795.775	1
			55.6347656	1.1315918	.8239746		2
LEM	69	720201327.895125	-386.7863922				1
			55.2502441	1.0656738	.8349609		2
LEM	69	720201329.164125				7504.445	1
			55.0964355	.9448242	.9118652		2
LEM	69	720201329.895125		-15.0287999			1
			54.6240234	.9338379	.9118652		2
LEM	69	720201331.164125				7250.880	1
			55.0305176	.5493164	.9448242		2
LEM	69	720201341.164125				6538.740	1

```
                                 46.3623047   1.7028809    .8898926          2
LEM         69 720201341.754125                            217.567           1
                                 46.3952637   2.2302246    .8569336          2
LEM         69 720201343.164125                                      6177.2751
                                 45.3955078   2.0544434    .7910156          2
LEM         69 720201343.895125-375.5807915                                  1
                                 45.7690430   1.5270996    .7141113          2
LEM         69 720201345.164125                                      5956.0801
                                 45.3186035    .7360840    .5383301          2
LEM         69 720201345.937125             -25.9368000                      1
                                 45.6481934    .3515625    .4614258          2
LEM         69 720201347.164125                                      5653.9601
                                 44.3957520   1.1975098    .3186035          2
LEM         69 720201347.965125                            206.992           1
                                 44.0112305   1.5930176    .2746582          2
LEM         69 720201349.164125                                      5395.0001
                                 43.3959961   2.4389648    .1538086          2
LEM         69 720201349.937125-332.3039932                                  1
                                 43.4399414   2.0874023    .0219727          2
LEM         69 720201351.164125                                      5184.5951
                                 44.1101074   1.8566895 359.7912598          2
LEM         69 720201351.926125             -18.6647999                      1
                                 43.9782715   1.4062500 359.7692871          2
LEM         69 720201353.164125                                      4979.5851
                                 44.3078613   1.1096191 359.8681641          2
LEM         69 720201353.887125                            190.869           1
                                 43.3959961   1.1865234 359.9560547          2
LEM         69 720201355.164125                                      4758.3901
                                 42.6269531   1.7797852    .0988770          2
LEM         69 720201355.957125-296.6263962                                  1
                                 42.4291992   3.2629395    .2526855          2
LEM         69 720201357.164125                                      4564.1701
                                 43.2531738   3.3618164    .3076172          2
LEM         69 720201357.957125             -15.5136000                      1
                                 43.0773926   1.8676758    .2636719          2
LEM         69 720201359.164125                                      4342.9751
                                 42.7697754 359.7692871    .2856445          2
LEM         69 720201359.945125                            173.013           1
                                 42.7697754 359.3518066    .2856445          2
LEM         69 7202014 1.164125                                      4084.0151
                                 39.7595215 359.8352051    .3625488          2
```

```
LEM        69 7202014 2.327125-259.2743950
                               39.6057123 359.5495605    .4594395                 1
                                                                                  2
LEM        69 7202014 3.164125                                           3857.0301
                               38.8245605 359.7253418    .4394531                 2
LEM        69 7202014 4.026125            -21.0888000                             1
                               39.0563965 359.4946289    .5603027                 2
LEM        69 7202014 5.164125                                           3696.1801
                               38.5621117 359.3298340    .5163574                 2
LEM        69 7202014 6.137125                            172.493                 1
                               38.2963398 359.4177246    .5493164                 2
LEM        69 7202014 7.164125                                           3544.5151
                               37.8369141 359.3408203    .6262207                 2
LEM        69 7202014 7.984125-226.0430968                                        1
                               36.7712402 359.9670410    .5603027                 2
LEM        69 7202014 9.164125                                           3269.3701
                               36.1010742    .3845215    .6921387                 2
LEM        69 720201410.145125            -19.6343999                             1
                               35.1123047    .8129883    .6811523                 2
LEM        69 720201411.164125                                           3145.2851
                               35.4099355    .7690430    .6481934                 2
LEM        69 720201412.027125                            164.519                 1
                               35.8044434    .3295898    .6921387                 2
LEM        69 720201413.164125                                           3048.1751
                               36.0900879    .3295898    .5603027                 2
LEM        69 720201414.164125-202.4735985                                        1
                               36.8811035    .0549316    .5712891                 2
LEM        69 720201415.164125                                           2864.7451
                               36.2548828    .6042480    .5712891                 2
LEM        69 720201416.047125            -14.7864000                             1
                               36.0131836   1.3293457    .5053711                 2
LEM        69 720201417.164125                                           2719.0801
                               35.4968262   1.6699219    .6701660                 2
LEM        69 720201418.055125                            150.823                 1
                               34.7937012   2.1423340    .7250977                 2
LEM        69 720201419.164125                                           2594.9951
                               34.5300293   2.0764160    .7580566                 2
LEM        69 720201420.066125-173.6223965                                        1
                               33.7609863   1.9017578    .8459473                 2
LEM        69 720201421.875125            -12.1199999                             1
                               33.3984375    .5493164    .9008789                 2
LEM        69 720201423.164125                                           2316.6131
```

			32.5085449	359.3188477	1.5051270		2
LEM	69	720201423.984125			140.248		1
			32.5085449	358.5058594	1.8566895		2
LEM	69	720201425.164125				2177.4221	
			32.2998047	358.6706543	2.5158691		2
LEM	69	720201426.164125	-152.8855972				1
			32.4865723	359.5385742	3.0102539		2
LEM	69	720201427.164125				2085.7071	
			32.8820801	359.9230957	3.2299805		2
LEM	69	720201428.027125		-9.9383998			1
			32.4316406	.1208496	3.3618164		2
LEM	69	720201429.164125				1960.5431	
			32.1020508	.1428223	3.4606934		2
LEM	69	720201430.176125			128.806		1
			30.9045410	359.4726562	3.2189941		2
LEM	69	720201431.164125				1853.7221	
			29.4104004	359.2529297	3.0432129		2
LEM	69	720201432.277125	-125.5799980				1
			28.9940430	359.3298340	2.7905273		2
LEM	69	720201433.164125				1749.0591	
			28.0371094	359.4836426	2.5598145		2
LEM	69	720201433.965125		-10.1807998			1
			27.7954102	.0439453	2.4609375		2
LEM	69	720201435.164125				1664.8971	
			27.8723145	.3295898	2.1862793		2
LEM	69	720201435.957125			122.739		1
			27.4328613	.4174805	1.9775391		2
LEM	69	720201437.176125				1573.1821	
			27.6416016	.7470703	1.7578125		2
LEM	69	720201437.957125	-108.5783987				1
			27.7075195	.5932617	1.5380859		2
LEM	69	720201439.176125				1469.5981	
			27.4548340	.6921387	1.1645508		2
LEM	69	720201440.055125		-11.3927999			1
			27.9272461	.8020020	1.2084961		2
LEM	69	720201441.176125				1401.6211	
			28.8171387	359.9890137	1.1975098		2
LEM	69	720201442.156125			101.589		1
			30.7177734	.2307129	1.1975098		2
LEM	69	720201444.387125	-93.2511978				1
			27.0153809	.2307129	1.3403320		2

LEM	69 720201445.207125				1228.9811
		25.4013906	.2856445	1.3623047	2
LEM	69 720201446.437125		-10.9979999		1
		24.5214844	.1098633	1.5380859	2
LEM	69 720201447.207125				1162.0831
		24.6972656	.3955078	1.4831543	2
LEM	69 720201448.047125			96.562	1
		25.1477051	.8459473	1.4721680	2
LEM	69 720201449.207125				1093.0271
		25.8947754	1.0217285	1.6479492	2
LEM	69 720201450.066125	-81.4015989			1
		26.2353516	1.1535645	1.5930176	2
LEM	69 720201451.215125				1027.2081
		26.0925293	.8459473	1.5161133	2
LEM	69 720201452.098125		-9.9383998		1
		25.5981445	.4833984	1.6259766	2
LEM	69 720201453.215125				978.6531
		24.7302246	.7250977	1.5380859	2
LEM	69 720201453.977125			85.120	1
		24.2248535	.9777832	1.4611816	2
LEM	69 720201455.215125				930.0981
		23.1811523	.9997559	1.5710449	2
LEM	69 720201453.977125			85.120	1
		24.2248535	.9777832	1.4611816	2
LEM	69 720201457.215125				590.2131
		21.8078613	1.2084961	1.3952637	2
LEM	69 720201457.824125	-60.5359993			1
		21.4892578	1.0217285	1.4282227	2
LEM	69 720201459.215125				801.6971
		21.0278320	.8789063	1.3183594	2
LEM	69 720201459.977125		-6.0599999		1
		20.8630371	.5712891	1.1975098	2
LEM	69 7202015 1.215125				758.5371
		20.2038574	.1208496	1.1865234	2
LEM	69 7202015 1.977125			74.545	1
		19.8083496	.2197266	1.1206055	2
LEM	69 7202015 3.215125				705.6661
		19.3139648	.2197266	.9228516	2
LEM	69 7202015 3.977125	-48.0423994			1
		18.9624023	.0878906	1.0986328	2
LEM	69 7202015 5.215125				662.5061

			18.6987305	.0549316	1.3293457	2
LEM	69	7202015 5.977125		-7.7568000		1
			18.5668945	359.9121094	1.3952637	2
LEM	69	7202015 7.215125				625.8201
			18.1054687	359.6484375	1.6918945	2
LEM	69	7202015 7.977125			66.570	1
			17.9626465	359.8022461	1.8237305	2
LEM	69	7202015 9.215125				581.5811
			17.6110842	359.3791504	1.9555664	2
LEM	69	7202015 9.906125	-38.6399994			1
			17.3144531	359.8461914	2.0654297	2
LEM	69	720201511.215125				551.3691
			17.1606445	.3515625	2.3291016	2
LEM	69	720201511.945125		-5.8176000		1
			17.0507812	.5603027	2.3840332	2
LEM	69	720201513.215125				512.5251
			16.6223145	.7250977	2.5598145	2
LEM	69	720201514.016125			58.596	1
			16.5344238	.9667969	2.6916504	2
LEM	69	720201515.215125				486.6291
			15.4687500	.9997559	2.8125000	2
LEM	69	720201515.984125	-27.9495997			1
			12.0739746	.6811523	2.9333496	2
LEM	69	720201517.215125				461.8121
			9.3383789	.7031250	3.2080078	2
LEM	69	720201518.004125		-4.3631999		1
			6.3061523	.4394531	3.3398438	2
LEM	69	720201519.215125				448.8641
			4.9768066	.1647949	3.5156250	2
LEM	69	720201519.937125			61.369	1
			5.1196289	.2087402	3.6804199	2
LEM	69	720201521.215125				429.4421
			5.1086426	.1647949	3.8671875	2
LEM	69	720201521.937125	-15.3271998			1
			5.5590820	.0219727	3.9990234	2
LEM	69	720201523.215125				405.7041
			5.9436035	.4504395	4.2187500	2
LEM	69	720201524.277125		-3.6360000		1
			5.4931641	.3955078	4.4165039	2
LEM	69	720201525.215125				389.5191
			5.7238770	.3295898	4.5493398	2

LEM	69	720201526.437125			57.729		1
			5.7348633	.4284668	4.7460938		2
LEM	69	720201527.215125				367.9391	1
			5.5371094	.3845215	4.8669434		2
LEM	69	720201528.445125	-12.1071998				1
			5.9545898	.2856445	5.0207520		2
LEM	69	720201529.215125				364.7921	1
			6.0424805	.3405762	5.1196289		2
LEM	69	720201530.437125		-1.9392000			1
			5.7897949	.2856445	5.2075195		2
LEM	69	720201531.215125				343.1221	1
			6.1083984	.2087402	5.1745605		2
LEM	69	720201532.437125			55.822		1
			6.3391113	.1867676	5.0537109		2
LEM	69	720201533.215125				335.5691	1
			6.1523438	.1098633	5.0097656		2
LEM	69	720201534.437125	-9.2735999				1
			6.4819336	359.8791504	4.9108887		2
LEM	69	720201535.215125				332.3321	1
			6.8334961	359.7912598	4.8229980		2
LEM	69	720201536.437125		-3.8784000			1
			6.8334961	359.5275879	4.6911621		2
LEM	69	720201537.215125				321.5421	1
			7.0642090	359.2639160	4.6362305		2
LEM	69	720201538.437125			51.661		1
			7.8222656	358.8903809	4.5043945		2
LEM	69	720201539.215125				321.5421	1
			7.6464844	358.6816406	4.3835449		2
LEM	69	720201540.496125	-9.1447998				1
			7.2619629	358.5278320	4.2626953		2
LEM	69	720201541.215125				316.1471	1
			7.2839355	358.3520508	4.1967773		2
LEM	69	720201542.445125		-3.6360000			1
			6.9104004	358.4399414	4.0100098		2
LEM	69	720201543.215125				312.9101	1
			8.3935547	358.6047363	3.9660645		2
LEM	69	720201544.477125			47.154		1
			11.0632324	358.7585449	3.9660645		2
LEM	69	720201545.215125				302.1201	1
			11.3488770	358.8244629	3.8891602		2
LEM	69	720201546.477125	-11.9783998				1

		11.7333984	359.0112305	3.7573242	2
LEM	69 720201547.215125				290.2511
		12.3266602	359.0332031	3.7243652	2
LEM	69 720201548.477125		-5.8176000		1
		13.6669922	359.2419434	3.6254883	2
LEM	69 720201549.215125				290.2511
		14.8425293	359.4726562	3.5705566	2
LEM	69 720201550.437125			41.433	1
		14.9374199	359.5605469	3.4826660	2
LEM	69 720201551.215125				282.6981
		15.1611328	359.6813965	3.4387207	2
LEM	69 720201552.445125	-11.3343998			1
		15.3588867	359.9780273	3.2958984	2
LEM	69 720201553.215125				268.6711
		15.3698730	.0659180	3.2080078	2
LEM	69 720201554.426125		-4.3631999		1
		15.7104492	.2526855	3.1091309	2
LEM	69 720201555.215125				267.5921
		15.7983398	.3515625	2.9882813	2
LEM	69 720201556.437125			30.858	1
		15.6225586	.3735352	2.8125000	2
LEM	69 720201557.215125				260.0391
		15.6005859	.3625488	2.7136230	2
LEM	69 720201558.437125	-9.1447998			1
		15.6555176	.4394531	2.5488281	2
LEM	69 720201559.215125				255.7231
		15.5236816	.5273438	2.4060059	2
LEM	69 7202016 .438125		-4.8480000		1
		15.4138184	.5822754	2.2192383	2
LEM	69 7202016 1.215125				256.8021
		15.4907227	.6591797	2.1093750	2
LEM	69 7202016 2.437125			22.537	1
		15.4907227	.8129883	1.9006348	2
LEM	69 7202016 3.215125				254.6441
		15.4687500	.8789063	1.7468262	2
LEM	69 7202016 4.437125	-7.2127999			1
		15.6774902	1.0107422	1.5380859	2
LEM	69 7202016 5.215125				246.0121
		15.7653809	1.1425781	1.3952637	2
LEM	69 7202016 6.496125		-4.3631999		1
		15.7653809	1.3623047	1.1865234	2

LEM	69	7202016 7.215125				244.9331
			15.4797363	1.4062500	1.1755371	2
LEM	69	7202016 8.496125			15.429	1
			10.5468750	1.2414551	1.2524414	2
LEM	69	7202016 9.215125				241.6961
			9.3493652	1.2414551	1.2963867	2
LEM	69	720201626.195125			8.321	1
			5.6689453	1.0546875	2.2412109	2
LEM	69	720201627.215125				169.4031
			5.5480957	.9558105	2.2521973	2
LEM	69	720201628.484125	-6.1823999			1
			.9777832	.5932617	2.3291016	2
LEM	69	720201629.215125				167.2451
			.9008789	.6042480	2.3620605	2
LEM	69	720201630.477125		-.7272000		1
			359.2749023	.5932617	2.4499512	2
LEM	69	720201631.215125				152.1391
			359.2309570	.8459473	2.4829102	2
LEM	69	720201632.516125			8.668	1
			359.7583008	2.1203613	2.6916504	2
LEM	69	720201633.215125				143.5071
			359.4726562	2.9003906	2.7905273	2
LEM	69	720201634.477125	-4.6367999			1
			358.6047363	2.9333496	2.9223633	2
LEM	69	720201635.215125				130.5591
			359.7583008	3.1311035	2.9333496	2
LEM	69	720201636.477125		.7272000		1
			.0329590	3.1970215	3.0541992	2
LEM	69	720201637.215125				115.4531
			359.7143555	2.9882813	3.1091309	2
LEM	69	720201638.445125			6.761	1
			359.5605469	1.9665527	3.1420898	2
LEM	69	720201639.215125				124.0851
			.0219727	.8898926	3.1530762	2
LEM	69	720201640.445125	-3.7352000			1
			359.7912598	.6042480	3.2739258	2
LEM	69	720201641.215125				117.6111
			.4614258	.4943848	3.3178711	2
LEM	69	720201642.484125		.0000000		1
			3.9990234	.8020020	3.4606934	2
LEM	69	720201643.215125				111.1371

		3.3178711	.7690430	3.5705566	2
LEM	69 720201644.477125			6.934	1
		2.6477051	.5163574	3.7133789	2
LEM	69 720201645.215125				98.1891
		2.6696777	.3845215	3.8122559	2
LEM	69 720201646.484125	-3.9927999			1
		3.0322266	.1538086	3.9770508	2
LEM	69 720201647.215125				84.1621
		2.9663086	359.5495605	4.0539551	2
LEM	69 720201648.484125		2.6664000		1
		3.4497070	358.2861328	4.1748047	2
LEM	69 720201649.215125				80.9251
		2.9223633	356.7810059	4.1748047	2
LEM	69 720201650.477125			7.281	1
		3.0871582	356.7810059	4.3835449	2
LEM	69 720201651.215125				78.7671
		5.3173828	356.8798828	4.6582031	2
LEM	69 720201652.445125	-1.2880000			1
		5.0756836	356.7919922	4.8339844	2
LEM	69 720201653.215125				78.7671
		4.7680664	356.8359375	4.9548340	2
LEM	69 720201654.316125		.0000000		1
		4.6142578	356.7150879	5.1525879	2
LEM	69 720201655.215125				76.6091
		4.4934082	356.4843750	5.2954102	2
LEM	69 720201656.387125			5.548	1
		4.1748047	356.3635254	5.4162598	2
LEM	69 720201657.215125				77.6881
		4.5373535	356.4074707	5.5920410	2
LEM	69 7202017 7.215125				55.0291
		6.0534668	2.0983887	8.0310059	2
LEM	69 7202017 7.848125			.000	1
		6.0314941	2.2631836	8.1848145	2
LEM	69 7202017 9.215125				57.1871
		4.1528320	1.8017578	8.6132813	2
LEM	69 7202017 9.996125	-1.5456000			1
		1.4831543	1.5490723	8.8330078	2
LEM	69 720201711.215125				56.1081
		354.9902344	.3405762	9.2504883	2
LEM	69 720201712.176125		-1.9392000		1
		355.5944824	.5493164	9.6130371	2

LEM	69	720201713.215125				45.3181
			355.7592773	1.5490723	9.9865723	2
LEM	69	720201714.437125			2.600	1
			356.1437988	2.6257324	10.3710937	2
LEM	69	720201715.215125				42.0811
			356.8469238	2.9003906	10.6567383	2
LEM	69	720201716.477125	-2.4472000			1
			357.4291992	3.3068848	11.0632324	2
LEM	69	720201717.215125				34.5281
			357.4951172	3.5375977	11.2719727	2
LEM	69	720201718.484125		.9696000		1
			358.2971191	3.7243652	11.6125488	2
LEM	69	720201719.215125				34.5281
			358.8354492	2.9663086	11.8103027	2
LEM	69	720201720.324125			3.467	1
			358.7915039	1.1535645	12.0849609	2
LEM	69	720201721.215125				28.0541
			358.6926270	1.1315918	12.3706055	2
LEM	69	720201722.324125	-1.4168000			1
			1.1535645	1.4721680	12.7770996	2
LEM	69	720201723.215125				28.0541
			1.7138672	.7141113	13.1066895	2
LEM	69	720201724.395125		11.8775998		1
			2.1093750	.1428223	13.4912109	2
LEM	69	720201725.215125				22.6591
			2.6586914	358.8024902	13.7988281	2
LEM	69	720201726.324125			15.429	1
			3.1420898	357.2863770	14.1613770	2
LEM	69	720201727.215125				22.6591
			3.0651855	357.3413086	14.2163086	2
LEM	69	720201728.316125	.9016000			1
			2.9333496	357.0886230	14.2712402	2
LEM	69	720201729.215125				11.8691
			3.5815430	355.5285645	14.3481445	2
LEM	69	720201730.336125		-7.2720000		1
			4.6472168	355.9240723	14.5019531	2
LEM	69	720201731.215125				24.8171
			4.8999023	356.0339355	14.5788574	2
LEM	69	720201732.324125			16.296	1
			5.3833008	356.1437988	14.7216797	2
LEM	69	720201733.215125				29.1331

		5.5151367	356.2866211	14.8205566	2
LEM	69 720201734.316125	7.5991999			1
		5.2075195	356.4514160	14.8205566	2
LEM	69 720201735.215125				21.5801
		4.7680664	356.5502930	14.8095703	2
LEM	69 720201736.324125		-9.6960000		1
		4.3615723	358.1323242	14.9084473	2
LEM	69 720201737.215125				18.3431
		3.5046387	359.9230957	15.0952148	2
LEM	69 720201738.348125			1.043	1
		1.5710449	.4504395	15.6225586	2
LEM	69 720201739.215125				10.7901
		.3515625	2.6037598	15.6555176	2
LEM	69 720201740.387125	.5152000			1
		4.5483398	.5953711	14.0185547	2