

# New Mechanism for Neutrino Mass Generation and Triply Charged Higgs Boson at the LHC

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# Goals

- To provide a new mechanism for light neutrino mass generation with new mass scale at the TeV.
- To connect the neutrino physics with the physics that can be explored at the LHC, even possibly at the Tevatron.
- Explore new signals for Higgs bosons

# Outline of Talk

- Introduction
- Model and the Formalism
- Phenomenological Implications
- Conclusions and Outlook

# Introduction

- The existence of neutrino masses are now firmly established.  
 $m_\nu \sim 10^{-2}$  eV  $\Rightarrow$  1st and only indication for physics beyond the SM
- $m_\nu$  is about a billion times smaller the quark and charged lepton masses
- What is the mechanism for such a tiny neutrino mass generation?

- Neutrino oscillation data gives

$$\Delta m_{21}^2 = 0.759 \pm 0.020 \times 10^{-4} eV^2,$$
$$|\Delta m_{32}^2| = 0.243 \pm 0.013 \times 10^{-2} eV^2,$$

$$\sin^2 2\theta_{12} = 0.87 \pm 0.03$$

$$\sin^2 2\theta_{23} > 0.92$$

$$\sin^2 2\theta_{13} < 0.19, CL = 90\%$$

## Most popular mechanism for light neutrino mass generation: Type I see-saw

- Add a right handed neutrino,  $N_R$  to the SM  
Then we have

$$L = y_\nu \bar{L} N_R \tilde{H} + M N_R^T C^{-1} N_R.$$

For the light  $\nu$  mass matrix, we obtain

$$M_\nu = \begin{pmatrix} 0 & y_\nu v \\ y_\nu v & M \end{pmatrix}$$

$$\Rightarrow m_\nu = y_\nu^2 \frac{v^2}{M}, \text{ or } m_\nu M = y_\nu^2 v^2$$

## Type I see-saw

- $m_\nu \sim \frac{m_D^2}{M}$

The corresponding effective interaction in SM  $\Rightarrow$  dimension 5 operator:  $L_{eff} = \frac{f}{M} l l H H$

The observed neutrino mass,  $m_\nu \sim 10^{-2}$  eV.

- If  $M = M_{PL}$ , then  $m_\nu$  is too small
- If  $M = M_{GUT}$ , then  $m_\nu$  is still too small
- $M \sim 10^{14}$  GeV is needed  
 $\rightarrow$  A new symmetry breaking scale ( $N_R$ )
- This scale is too high  $\rightarrow$  No connection can be made to the physics to be explored at the LHC or Tevatron  
 $\Rightarrow$  need  $M \sim$  TeV.

## Type II see-saw

- Introduce a Higgs triplet,  $\Delta = (\Delta^{++}, \Delta^+, \Delta^0)$ ,

Then we can write

$$L = y_\nu l l \Delta$$

$$\Rightarrow m_\nu = y_\nu \langle \Delta \rangle$$

- The potential

$$V(H, \Delta) = -\mu H H \Delta + M_\Delta^2 \Delta^\dagger \Delta \Rightarrow \langle \Delta \rangle = \frac{\mu v^2}{M_\Delta^2}$$

- Effective operator :  $L = \frac{1}{M} l l H H$ , with  $M = \frac{M_\Delta^2}{\mu}$ .

- If  $\mu \sim M_\Delta$ , then,  $M_\Delta \sim 10^{14}$  GeV.

- If  $\mu \sim v$ , then,  $M_\Delta \sim 10^3$  GeV requires  $y_\nu \sim 10^{-10} \Rightarrow$  highly unnatural



## Type III see-saw

- Introduce a triplet lepton,  $\Sigma = (\Sigma^+, \Sigma^0, \Sigma^-)$ ,  
 $\Sigma$  has zero hypercharge.
- This gives an effective dimension 5 operator,

$$L = \frac{1}{M} \llcorner \llcorner H H,$$
$$\Rightarrow m_\nu = y_\nu^2 \frac{v^2}{M_\Sigma}$$

- $\Sigma \sim 10^{14}$  GeV.

- It is possible the dim. 5 operator does not contribute to neutrino masses in a significant way.  
 $\Rightarrow$  next operator (dim. 7) :  $L_{eff.} = \frac{f}{M^3} \llcorner\llcorner H H (H^\dagger H)$
- This by itself is not enough to make  $M \sim \text{TeV}$ , need  $f \sim 10^{-9}$ .
- We propose a model in which  $f \sim y_1 y_2 \lambda_4$  with each  $\sim 10^{-3}$  (domain of natural values)
- This gives  $M \sim \text{TeV}$  scale to obtain neutrino masses in the range  $10^{-2} - 10^{-1}$  eV.  
 $\Rightarrow$  connect to physics at the LHC and Tevatron.

- Gauge Symmetry :  $SM = SU(3)_c \times SU(2)_L \times U(1)_Y$
- Usual SM model fermions,  
+ a pair of vector-like  $SU(2)_L$  triplet leptons transforming as  $(1, 3, 2)$  and  $(1, 3, -2)$  ,  $\Sigma + \bar{\Sigma}$ ,  $\Sigma = (\Sigma^{++}, \Sigma^+, \Sigma^0)$  ,  
+ a new isospin  $\frac{3}{2}$  Higgs,  $\Phi$ ,  $\Phi = (\Phi^{+++}, \Phi^{++}, \Phi^+, \Phi^0)$
- $\Phi$  has positive mass square, but acquires a tiny VEV through Higgs potential via interaction with H.
- $\Sigma$  has interactions with SM lepton doublets, H as well as  $\Phi$ .

- Higgs Potential

$$\begin{aligned} V = & -\mu_H^2 H^\dagger H + M_\Phi^2 \Phi^\dagger \Phi \\ & + \lambda(H^\dagger H)^2 + \lambda_1(\Phi^\dagger \Phi)^2 \\ & + \lambda_2(H^\dagger H)(\Phi^\dagger \Phi) \\ & + \lambda_3(H^\dagger \frac{t_a}{2} H)(\Phi^\dagger \frac{T_A}{2} \Phi) \\ & + \lambda_4(HHH\Phi + \Phi^\dagger H^\dagger H^\dagger H^\dagger) \end{aligned}$$

- Minimization of  $V \Rightarrow \langle \Phi_0 \rangle \equiv v_\Phi \sim -\lambda_4 \frac{v_H^3}{M_\Phi^2}$

## Light neutrino mass generation:

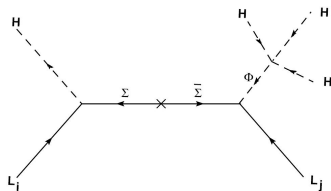
- $L = y_i l_i H^* \Sigma + \bar{y}_i l_i \Phi \bar{\Sigma} + M_\Sigma \Sigma \bar{\Sigma}$   
 $y_i, \bar{y}_i \Rightarrow$  dimensionless Yukawa couplings.
- $\rightarrow L_{eff} = \frac{(y_i \bar{y}_j + y_j \bar{y}_i)}{M_\Sigma} l_i l_j H^* \Phi + h.c.$

with  $v_\Phi = -\lambda_4 \frac{v_H^3}{M_\Phi^2}$

with  $(y_1, y_2, \lambda_4) \sim 10^{-3}$ ,

$\Rightarrow$  This is the dimension 7 neutrino mass generation mechanism with  $\Phi$  replaced by  $HHH/M_\Phi^2$ .

- $m_\nu \sim 10^{-2} - 10^{-1}$  eV range with  $M_\Sigma$  and  $M_\Phi$  at the TeV scale.

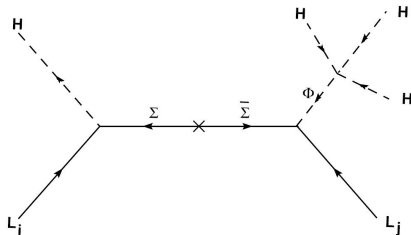


## Light neutrino mass generation: Comments

- $L_{eff} = \frac{y_i \bar{y}_j}{M_\Sigma} l_i l_j H^* \Phi$ ;  $m_\nu = \frac{\lambda_4}{2} (y_i \bar{y}_j + \bar{y}_i y_j) \frac{v_H^4}{M_\Sigma M_\Phi^2}$
- Neutrino mass relation is  $m_\nu M^3 \sim v^4$ .  
This is distinct from the traditional see-saw relation  $m_\nu M \sim v^2$ .
- We can realize both the normal hierarchy and the inverted mass hierarchy.
- This is the highest isospin multiplet we can use with renormalizable interaction (dimension 4).
- With just one  $\Sigma$ , one of light neutrino is massless. This is consistent with current data. However, adding more than one  $\Sigma$ , all neutrinos can acquire masses.

## One loop correction in our model

- While  $d = 5$  neutrino masses are not induced at tree level, they do arise at 1-loop in our model via diagrams which connect two of the  $H$  legs. We find  $\Delta m_\nu / m_\nu \sim \frac{3}{64\pi^2} \frac{M^2}{v^2}$ , which is  $\ll 1$  for  $M < \text{TeV}$ .



- In the SUSY version of our model, the loop diagrams will be further suppressed.

- Mass Spectrum of  $\Phi$

$$M_{\Phi_i}^2 = M_{\Phi}^2 + \lambda_2 v_H^2 - \frac{1}{2} \lambda_3 I_{3i} v^2,$$

where  $I_{3i} = (3/2, 1/2, -1/2, -3/2)$  for  $(\Phi^{+++}, \Phi^{++}, \Phi^+, \Phi^0)$  respectively.

- Two possible hierarchies for the spectrum of  $\Phi$   
Positive  $\lambda_3$  :  $M_{\Phi^{+++}} < M_{\Phi^{++}} < M_{\Phi^+} < M_{\Phi^0}$   
Negative  $\lambda_3$  :  $M_{\Phi^{+++}} > M_{\Phi^{++}} > M_{\Phi^+} > M_{\Phi^0}$ .
- Note that the mass square difference,  $\Delta M^2$  among consecutive components are the same, and is equal to  $(1/2)\lambda_3 v_H^2$ .



## Relevant parameters in our model and existing constraints:

- Parameters :  $v_\Phi$ ,  $\Delta M$ ,  $M_\Phi$ ,  $M_\Sigma$  (  $\Delta M =$  mass splitting)
- $v_\Phi$  :  $\Phi$  has isospin 3/2, contribute to  $\rho$  parameter at the tree level.  $\rho = 1 - (6v_\Phi^2/v_H^2)$ . Experiment:  $\rho = 1.0000_{-0.0007}^{+0.0011}$ , At  $3\sigma$  level  $v_\Phi < 2.5$  GeV.
- The mass splittings between the components of  $\Phi$  induces an additional positive contribution to  $\rho$  at one loop level,  $\Delta\rho \simeq (5\alpha_2)/(6\pi)(\Delta M/m_W)^2$ .  $\Rightarrow \Delta M < 38$  GeV .
- There is also a theoretical lower limit on  $\Delta M$  arising from the radiative correction at the one loop  $\Rightarrow \Delta M \geq 1.4$  GeV for  $M_\Phi \sim 1$  TeV  
(This is actually a naturalness lower limit, since these corrections are not finite, with the infinity absorbed in the renormalization of  $\lambda_4$ .)

## Experimental constraints

- Mass of  $\Phi$ : LEP2:  $> 100$  GeV for charged  $\Phi$ ,
- CDF and D0 Collaborations have looked for stable CHAMPS (charged massive particle).
- Using CDF cross sections times branching ratio limits, we obtain  
 $> 120$  GeV for stable, charged  $\Phi^{+++}$

# Phenomenological Implications

- Decays of  $\Phi$ 's in the model
- Production
- Signals
- Other implications
- Two possible scenarios:  $\Phi^{+++}$  lightest or  $\Phi^{+++}$  heaviest.  
Consider the case in which  $\Phi^{+++}$  lightest  
 $\Rightarrow$  phenomenological implications most distinctive with displaced vertices.

## A. Decays

- Two possible decay modes

$$\Phi^{+++} \rightarrow W^+ W^+ W^+$$

$$\Phi^{+++} \rightarrow W^+ l^+ l^+$$

- These decays arise through the diagrams where  $\Phi^{+++}$  emits a real  $W^+$  and an off-shell  $\Phi^{++}$  which subsequently decays to either two real  $W^+$ , or two same sign charged leptons.

- Couplings ( $\Phi^{+++} \Phi^{--} W^-$ ):  $\sqrt{\frac{3}{2}} g (p_1 - p_2)_\mu$

$$(\Phi^{++} W^- W^-) : \sqrt{3} g^2 v_\Phi$$

$$(\Phi^{++} l_i^- l_j^-) : m_{ij}^\nu / (2\sqrt{3} v_\Phi)$$

## A. Decays

- Decay widths

decay rates are found to be

$$\Gamma(\Phi^{+++} \rightarrow 3W) = \frac{3g^6}{2048\pi^3} \frac{v_\Phi^2 M_\Phi^5}{m_W^6} I,$$

$$\Gamma(\Phi^{+++} \rightarrow W^+ \ell^+ \ell^+) = \frac{g^2}{6144\pi^3} \frac{M_\Phi \sum_i m_i^2}{v_\Phi^2} J,$$

where  $I, J$  are dimensionless integrals ( $\simeq 1$  for  $M_\Phi \gg m_W$ ).

# Phenomenological Implications

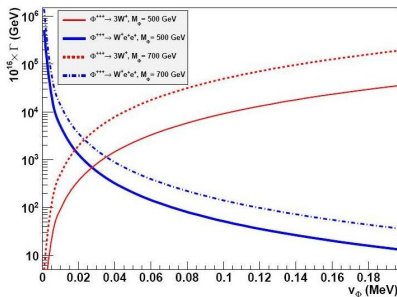
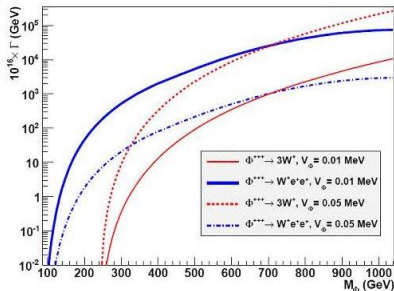
## A. Decays

- Two possible decay modes

$$\Phi^{+++} \rightarrow W^+ W^+ W^+$$

$$\Phi^{+++} \rightarrow W^+ I^+ I^+$$

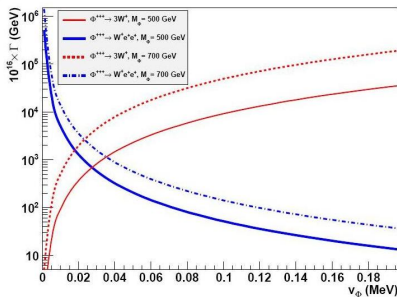
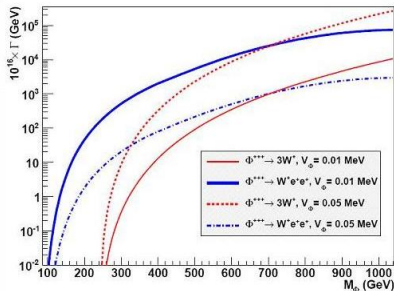
- $W^+ W^+ W^+$  mode dominate for higher values of  $\nu_\phi$
- $W^+ I^+ I^+$  dominate for smaller values of  $\nu_\phi$



# Phenomenological Implications

## A. Decays

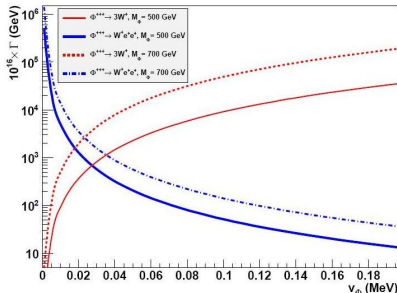
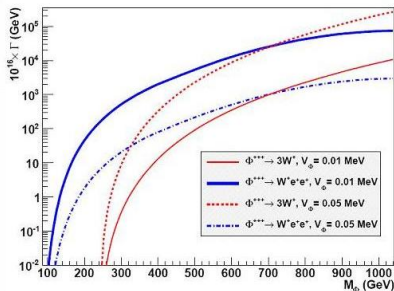
- Crossing point:  
 $v_\phi \sim 0.02 - 0.03$  MeV.
- For  $v_\phi \sim 0.02 - 0.03$  MeV, for  $M_\phi = 500$  GeV,  
 $\Gamma < 10^{-12} - 6 \times 10^{-14}$  GeV  
 $\Rightarrow$  Displaced Vertices.
- For lower masses, widths are even smaller  $\rightarrow \Phi^{+++}$  can escape the detector !!
- For  $v_\phi > 0.2$  MeV,  $\Phi^{+++}$  will immediately decay to  $W^+ W^+ W^+$ .



# Phenomenological Implications

## Test of the model

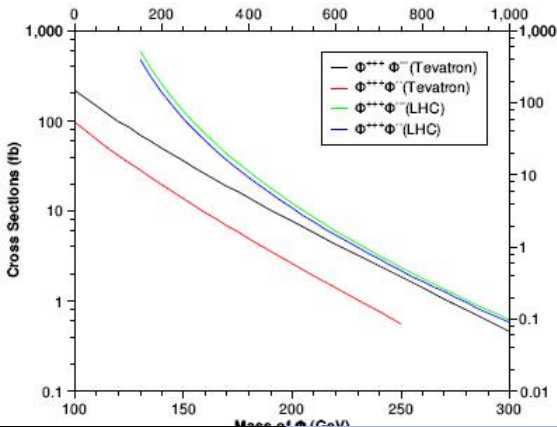
- for  $v_\phi > 0.05$  MeV,  
 $\Phi^{+++} \rightarrow W^+ W^+ W^+$
- For  $v_\phi \sim 0.01 - 0.06$  MeV,  
 $\Phi^{+++} \rightarrow W^+ W^+ W^+$ , or  
 $\Phi^{+++} \rightarrow W^+ I^+ I^+$  with  
displaced vertices
- For  $v_\phi < 0.01$  MeV,  
 $\Phi^{+++} \rightarrow W^+ I^+ I^+$  with no  
displaced vertices





## B. Productions

- $pp$  or  $p\bar{p} \rightarrow \Phi^{+++}\Phi^{---} \rightarrow 6W$  or  $4W I^+ I^+$ ,  $4W I^- I^-$  or  $2W I^+ I^+ I^- I^-$  with or without displaced vertices depending on  $v_\Phi$ .



# Phenomenological Implications

- With displaced vertices, only few events are needed.
- LHC Reach (with displaced vertices)
  - with 1 inverse fb,  $\sim 400$  GeV
  - with 10 inverse fb,  $\sim 650$  GeV
  - with 100 inverse fb,  $\sim 1$  TeV
- LHC Reach (without displaced vertices)
  - with 1 inverse fb,  $\sim 250$  GeV
  - with 10 inverse fb,  $\sim 400$  GeV
  - with 100 inverse fb,  $\sim 800$  GeV

## B. Productions of heavier states

- $\Phi^{+++}\Phi^{---} \rightarrow 6W \rightarrow 12$  jets with high  $p_T$
- $\Phi^{++}\Phi^{--} \rightarrow 8W \rightarrow 16$  jets with high  $p_T$
- $\Phi^+\Phi^- \rightarrow 10W \rightarrow 20$  jets with high  $p_T$
- $\Phi^0\Phi^0 \rightarrow 12W \rightarrow 24$  jets with high  $p_T$
- Each case also gives lesser number of jets plus charged leptons at high  $p_T$

## C. Other Implications

- $\Phi$  multiplet with tiny VEV essentially behaves like an inert Higgs  
⇒ SM Higgs mass can be raised to  $\sim 400 - 500$  GeV if  $v_\Phi$  is large  $\sim \text{few} - 38$  GeV.  
In that case,  $H \rightarrow \Phi^{+++}\Phi^{---}$
- Neutrino mass hierarchy  
If mass of  $\Phi^{+++} < 3W$ , then  $\Phi^{+++} \rightarrow W^+l^+l^+$  dominate  
⇒  $ee, e\mu, \mu\mu$ , along with  $\tau$ 's.  
Dominance of  $\mu\mu \rightarrow$  Normal Hierarchy  
Dominance of  $e\mu$  ( $ee$ )  $\Rightarrow$  Inverted Hierarchy

# Conclusions

- Presented a new mechanism for the generation of neutrino masses
- via dimension 7 operators:  $\frac{1}{M^3} \lll H H (H^\dagger H)$
- Leads to new formula for the light neutrino masses :  $m_\nu \sim \frac{v^4}{M^3}$
- This is distinct from the usual see-saw formulae :  $m_\nu \sim \frac{v^2}{M}$
- Scale of new physics can be naturally at the TeV scale

## Conclusions (continued)

- Microscopic theory that generated  $d = 7$  operator has an isospin  $3/2$  Higgs multiplet  $\Phi$  containing triply charged Higgs boson with mass around  $\sim \text{TeV}$  or less.
- Can be produced at the LHC (and possibly at the Tevatron)
- Distinctive multi- $W$  and multi-lepton final states
- Can be long-lived with the possibility of displaced vertices, or even escaping the detector
- Leptonic decay modes carry information about the nature of neutrino mass hierarchy