**Subject:** OFFICIAL COMMENT: Vortex - simple correlation on some of the output bits
**From:** Niels Ferguson <niels@microsoft.com>
**Date:** Sun, 14 Dec 2008 17:38:29 -0800
**To:** "hash-function@nist.gov" <hash-function@nist.gov>
**CC:** "hash-forum@nist.gov" <hash-forum@nist.gov>

I think I found a simple correlation on some of the output bits of Vortex.

The hash result is the output of the V function. I'll use the notation of Figure 4 in the Vortex documentation, and use X[0] to refer to the least significant bit of word X.

new_B0 and new_A0 are two of the output words of the function V.
new_B0[0] is a function of three bits B1[0], B0[0], and A0[0].
new_A0[0] is a function of three bits B0[0], A1[0], and A0[0].

These two functions share inputs and are correlated. new_B0[0] = new_A0[0] with probability 5/8. This leads to a trivially detectable output bias, and makes the hash function unsuitable for many applications, including key derivation and Hash_DRBG from SP800-90.

Let's rename the four input bits to A, B, C, and D, and the two output bits to X and Y. We have:

X = (A & D) ^ B
Y = (B & C) ^ D

If A=0 then X = B and Y = <some expression> ^ D so both output bits are uncorrelated and unbiased.
If C=0 the same applies.

But if A=C=1 we have
X = D ^ B
Y = B ^ D
and thus
X = Y

So 3/4 of the time the two output bits are unrelated, and 1/4 of the time they are the same, which leads to X=Y for 5/8 of all inputs.

I haven't verified this experimentally, but the submitters of Vortex agreed with this analysis.

Cheers!

Niels

**From:** Michael Kounavis [michael_kounavis@hotmail.com]
**Sent:** Saturday, May 30, 2009 3:40 AM
**To:** hash-function@nist.gov
**Cc:** hash-forum@nist.gov
**Subject:** OFFICIAL COMMENT: Vortex - New paper and web page

Hello,

In response to the bit correlation remark posted by Niels and the other published attacks we have posted a new paper titled: "Security Enhancement of the Vortex Family of Hash Functions" that can be found in our algorithm's new web site: http://math.haifa.ac.il/~vortex

Regards
Shay and Michael