GRB RADIATIVE EFFICIENCIES DERIVED FROM THE *SWIFT* DATA: GRBs VERSUS XRFs, LONG VERSUS SHORT

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ABSTRACT

We systematically analyze the prompt emission and the early afterglow data of a sample of 31 GRBs detected by *Swift* before 2005 September and estimate the GRB radiative efficiency. BAT's narrow band inhibits a precise determination of the GRB spectral parameters, and we have developed a method to estimate these parameters with the hardness ratio information. The shallow decay component commonly existing in early X-ray afterglows, if interpreted as continuous energy injection in the external shock, suggests that the GRB efficiencies previously derived from the late-time X-ray data were not reliable. We calculate two radiative efficiencies using the afterglow kinetic energy E_K derived at the putative deceleration time ($t_{\rm dec}$) and at the break time (t_b), when the energy injection phase ends, respectively. At t_b XRFs appear to be less efficient than normal GRBs. However, when we analyze the data at $t_{\rm dec}$, XRFs are found to be as efficient as GRBs. Short GRBs have similar radiative efficiencies to long GRBs despite of their different progenitors. Twenty-two bursts in the sample are identified to have the afterglow cooling frequency below the X-ray band. Assuming $\epsilon_e = 0.1$, we find $\eta_{\gamma}(t_b)$ usually <10% and $\eta_{\gamma}(t_{\rm dec})$ varying from a few percent to >90%. Nine GRBs in the sample have the afterglow cooling frequency above the X-ray band for a very long time. This suggests a very small ϵ_B and/or a very low ambient density n.

Subject headings: gamma rays: bursts — methods: statistical — radiation mechanisms: nonthermal — shock waves

Online material: color figures

1. INTRODUCTION

Gamma-ray bursts (GRBs) are believed to be the most luminous electromagnetic explosions in the universe. These erratic, transient events in gamma-rays are followed by long-lived, decaying afterglows in longer wavelengths. The widely accepted model of this phenomenon is the fireball model (Mészáros 2002; Zhang & Mészáros 2004; Piran 2005), which depicts the observed prompt gamma-ray emission as the synchrotron emission from the internal shocks in an erratic, unsteady, relativistic fireball (Rees & Mészáros 1994) and interprets the broadband afterglow emission as the synchrotron emission from an external shock that expands into the circumburst medium (Mészáros & Rees 1997; Sari et al. 1998). The GRB radiative efficiency, which is defined as

$$\eta_{\gamma} \equiv \frac{E_{\gamma}}{E_{\gamma} + E_{K}},\tag{1}$$

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is an essential quantity to understand the nature of the bursts. Here E_{γ} is the isotropic gamma-ray energy ¹¹ and E_{K} is the isotropic kinetic energy of the fireball right after the prompt gamma-ray emission is over. It gives a direct measure of how efficient the burster dissipates the total energy into radiation during the GRB prompt emission phase.

In the pre-Swift era only the late-time fireball kinetic energy E_K was derived or estimated using the late-time afterglow data. Two methods have been proposed. The most adequate one is through broadband afterglow modeling (e.g., Panaitescu & Kumar 2001). This method requires well-sampled multiwavelength afterglow data. The method thus can only be applied to a small sample of GRBs. A more convenient method is to use the X-ray afterglow data alone (Freedman & Waxman 2001; Berger et al. 2003; Lloyd-Ronning & Zhang 2004). At a late enough epoch (e.g., 10 hr after the burst trigger), the X-ray band is likely above the cooling frequency, so that the X-ray flux gives a good measure of the degenerate quantity $\epsilon_e E_K$, where ϵ_e is the fraction of the electron energy in the internal energy of the shock. If ϵ_e could be estimated, it would then be possible to derive E_K directly from the X-ray data. Assuming a simple extrapolation of the late-time light curve to earlier epochs, Lloyd-Ronning & Zhang (2004) took into account the fireball radiative loss correction to estimate E_K right after the prompt emission phase and estimated the efficiency of 17 GRBs/ XRFs observed in the pre-Swift era. They discovered a shallow positive correlation between η_{γ} and E_{γ} or E_p . According to this shallow correlation, softer, underluminous bursts (e.g., X-ray

Notice that the notation E_{γ} is different from that used in some other papers (e.g., Frail et al. 2001) that denotes the geometry-corrected gamma-ray energy.

flashes) tend to have a lower radiative efficiency. Similar conclusions were also drawn by Lamb et al (2005).

These previous GRB efficiency studies employing the lateafterglow data inevitably introduce some uncertainties on the E_K measurements, including the possible corrections of radiative fireball energy loss and additional energy injection in the early afterglow phase. In order to reduce these uncertainties very early afterglow observations are needed. The successful operation of NASA's Swift GRB mission (Gehrels et al. 2004) makes this possible. Very early X-ray afterglow data for a large number of GRBs have been recorded by the X-Ray Telescope (XRT) on board Swift (Burrows et al. 2005a). A large sample of early X-ray afterglow data have been collected, typically 100 s after the triggers. These observations indeed show novel, unexpected behaviors in the early afterglow phase (Tagliaferri et al. 2005; Burrows et al. 2005b; Nousek et al. 2006; Zhang et al. 2006; O'Brien et al. 2006) and make it feasible to more robustly estimate E_K , and hence η_{γ} .

The XRT light curves of many bursts could be synthesized to a canonical light curve that is composed of five components (Zhang et al. 2006), an early rapid decay component consistent with the tail of the prompt emission, a frequently seen shallower than normal decay component likely originated from a refreshed external forward shock, a normal decay component due to a decelerating fireball, an occasionally seen postjet break segment, as well as erratic X-ray flares harboring in nearly half of Swift GRBs that are likely due to reactivation of the GRB central engine. The most relevant segment for the efficiency problem is the shallow decay component (Zhang et al. 2006; Nousek et al. 2006). Most of the Swift XRT afterglow light curves in our sample have such an early shallow decay segment. The origin of this segment is currently not identified. If it is due to continuous energy injection, the initial afterglow energy E_K must be significantly smaller than estimated using the late-time data. The previous efficiency analysis using late X-ray afterglow data then tend to overestimate E_K , and hence underestimate η_{γ} . The early tight UVOT upper limits for many Swift GRBs are also likely related to this shallow decay component (Roming et al. 2006). It is therefore of great interest to revisit the efficiency problem using the very early XRT data.

X-ray flashes (XRFs; Heise et al. 2003; Kippen et al. 2003) naturally extend long-duration GRBs into the softer and fainter regime (e.g., Lamb et al. 2005; Sakamoto et al. 2006). It is now known that the softness of the bursts is not due to their possible high redshifts (Soderberg et al. 2004, 2005). The remaining possibilities include either extrinsic factors (e.g., object viewed at different viewing angles; Yamazaki et al. 2002, 2004; Zhang et al. 2004a, 2004b; Liang & Dai 2004; Huang et al. 2004) or intrinsic factors (e.g., different burst parameters, such as Lorentz factor, luminosity, etc.; Dermer et al. 1999; Kobayashi et al. 2002; Mészáros et al. 2002; Zhang & Mészáros 2002c; Huang et al. 2002; Rees & Mészáros 2005; Barraud et al. 2005). The radiative efficiency of XRFs may provide a clue to identify the correct mechanism. Previous analyses of late-time X-ray data suggest that the XRFs typically have lower radiative efficiencies (Soderberg et al. 2004; Lloyd-Ronning & Zhang 2004; Lamb et al. 2005). It is desirable to investigate whether this is still true with the early afterglow

Recently, afterglows of several short-duration GRBs have been detected (Gehrels et al. 2005; Fox et al. 2005; Villasenor et al. 2005; Hjorth et al. 2005; Barthelmy et al. 2005a; Berger et al. 2005c). The data suggest that they are distinct from long GRBs and very likely have different progenitor systems. It is therefore of great interest to explore the radiative efficiencies of short-hard GRBs (SHGs) and compare them with those of long GRBs.

In this paper we systematically analyze the prompt emission and the early afterglow data for a sample of 31 GRBs detected by *Swift* before 2005 September by reducing the Burst Alert Telescope (BAT; Barthelmy et al. 2005b) and XRT data. We present the sample and the BAT/XRT data analysis methods in § 2. The gamma-to-X fluence ratio $(R_{\gamma/X})$ is an observation-defined apparent GRB efficiency indicator. We perform statistical analysis of this parameter in § 3. In § 4 we perform more detailed theoretical modeling to estimate E_K (§ 4.1) and η_{γ} (§ 4.2). Our results are summarized in § 5 with some discussion. Throughout the paper the cosmological parameters $H_0=71~{\rm km~s^{-1}~Mpc^{-1}}$, $\Omega_M=0.3$, and $\Omega_{\Lambda}=0.7$ have been adopted.

2. DATA

Our sample includes 31 GRBs observed by *Swift* before 2005 September 1. The BAT-XRT joint early X-ray afterglow light curves of these bursts and the detailed data reduction procedures have been presented in O'Brien et al. (2006).

2.1. Prompt Gamma-Rays

The BAT data have been processed using the standard BAT analysis software (*Swift* software ver. 2.0). The BAT-band gammaray fluence $S_{\gamma,\rm obs}$ could be directly derived from the data. For the purpose of estimating GRB efficiency, on the other hand, one needs to estimate the total energy output of the GRB, which requires that $S_{\gamma,\rm obs}$ be extrapolated to a wider bandpass to get S_{γ} (1–10⁴ keV adopted in this paper). This requires the knowledge of the spectral parameters of the prompt emission.

It is well known that the GRB spectrum is typically fitted by a Band function (Band et al. 1993), which is a smoothly jointbroken power law characterized by two photon indices Γ_1 and Γ_2 (with the convention $N(E)dE \propto E^{\Gamma}dE$ adopted throughout the text) and a break energy E_0 . The peak energy of the νf_{ν} spectrum is $E_p = (2 + \Gamma_1)E_0$. In order to derive these parameters, the observed spectrum of a burst should cover the energy band around E_0 . The spectra of both long and short GRBs observed by BATSE on board the Compton Gamma-Ray Observatory (CGRO; covering 20-2000 keV) are well fitted by the Band function, with the typical values of $\Gamma_1 \sim -1$, $\Gamma_2 \sim -2.3$, and $E_p \sim 250$ keV (Preece et al. 2000; Ghirlanda et al. 2003). The spectra of XRFs could be also fitted by the Band function, typically with $\Gamma_1 \sim -1$ and a lower Γ_2 than typical GRBs (Lamb et al. 2005; Sakamoto et al. 2005; 2006; Cui et al. 2005). BAT has a narrower energy band (15–150 keV) than BATSE and *HETE-2*. The typical E_p of the bright BATSE sample is well above the BAT band. BAT's observations therefore cannot well constrain E_n and Γ_2 for many GRBs. Most observed spectra by BAT are well fitted by a simple power law. However, this is due to the intrinsic limitation of the instrument. Four GRBs in our sample (050401, 050525A, 050713A, and 050717), were simultaneously observed by the WIND Konus instrument (with an energy band of 20–2000 keV). The spectra of these bursts could be also well fitted by a Band function or a cutoff power-law spectrum (Golenetskii et al. 2005a, 2005b, 2005c, 2005d; Krimm et al. 2006). We assume that the broadband spectra of all the bursts in our sample could be fitted by the Band function and then make the corrections to the observed fluences. Our procedure to derive spectral parameters are as follows.

We first fit an observed spectrum with a Band function, a power law with exponential cutoff, and a simple power law, respectively. By comparing reduced χ^2 of these fits, we pick up the best-fit model among the three. In our sample, only four GRBs (050128, 050219A, 050525A, and 050716) could be well fitted by a Band

 $TABLE \ 1$ Prompt Gamma-Ray Data for the GRBs in Our Sample

	T ₉₀ ^a				$\log S_{\gamma, { m obs}}$ d			E_p^{e}		$\log S_{\gamma}^{\ m f}$		
GRB	(s)	Γ_{PL}^{b}	χ^{2b}	HR _{obs} ^c	(ergs s ⁻¹)	$\Gamma_1^{\ e}$	$\Gamma_2^{\ e}$	(keV)	χ^{2e}	(ergs s ⁻¹)	Z	Ref.
050126	30.0	$-1.36^{+0.15}_{-0.15}$	1.20	1.60 ± 0.23	-6.07 ± 0.04	-1.00	-2.30	$157^{+129.}_{-53.}$	1.19	-5.63 ± 0.23	1.290	1
050128	13.8	NaN		1.66 ± 0.14	-5.29 ± 0.02	-0.71	-2.19	$118^{+18.}_{-14.}$	0.87	-4.87 ± 0.05		
050215B	10.4	$-2.45^{+0.73}_{-1.02}$	0.84	0.84 ± 0.23	-6.63 ± 0.07	-1.00	-2.45	~ 18	0.83	~ -6.24		
050219A	23.0	NaN		1.73 ± 0.11	-5.38 ± 0.02	-0.32	-2.30	$102^{+8.}_{-8.}$	0.91	-5.01 ± 0.03		
GRB050315	96.0	$-2.10^{+0.09}_{-0.09}$	0.87	0.93 ± 0.08	-5.49 ± 0.02	-1.28	-2.20	$37^{+8.}_{-8.}$	0.88	-5.10 ± 0.03	1.950	2
050319	15.0	$-2.15^{+0.20}_{-0.21}$	0.83	0.99 ± 0.19	-5.91 ± 0.05	-1.25	-2.15	$\sim \! 28$	0.82	~ -5.51	3.240	3
050401 ^g	38.0	NaN		1.50 ± 0.11	-5.07 ± 0.02	-1.15	-2.65	$132^{+16.}_{-16.}$	0.96	-4.74 ± 0.04	2.900	4
050406	5.0	$-2.59^{+0.38}_{-0.45}$	1.23	0.74 ± 0.32	-7.09 ± 0.10	-1.00	-2.59	\sim 24	1.22	~ -6.70		
050416A	5.4	$-3.09^{+0.22}_{-0.24}$	0.93	0.44 ± 0.16	-6.37 ± 0.06	-1.00	-3.22	<15	0.90	~ -5.97	0.654	5
050422	60.0	$-1.38^{+0.23}_{-0.22}$	0.98	1.54 ± 0.28	-6.21 ± 0.05	-0.90	-2.30	$123^{+99.}_{-42.}$	0.79	-5.83 ± 0.20		
050502B	17.5	$-1.65^{+0.14}_{-0.15}$	1.02	1.31 ± 0.18	-6.33 ± 0.04	-1.30	-2.30	102^{+85}_{-36}	1.03	-5.95 ± 0.10		
050525 ^g	11.5	NaN		1.30 ± 0.03	-4.81 ± 0.01	-1.01	-2.72	80^{+3}_{-3}	0.41	-4.55 ± 0.01	0.606	6
050607	26.5	$-1.20\substack{+0.07 \\ -0.07}$	0.98	1.75 ± 0.16	-6.22 ± 0.04	-1.04	-2.00	393^{+368}_{-132}	0.99	-5.52 ± 0.27		
050712	48.0	$-1.48^{+0.18}_{-0.18}$	0.99	1.42 ± 0.24	-5.96 ± 0.05	-1.00	-2.30	126^{+103}_{-44}	1.02	-5.57 ± 0.18		
050713A ^g	70.0	NaN		1.39 ± 0.09	-5.28 ± 0.02	-1.12	-2.30	312^{+50}_{-50}	1.22	-4.72 ± 0.08		
050713B	75.0	$-1.53^{+0.17}_{-0.17}$	0.83	1.40 ± 0.22	-5.34 ± 0.04	-1.00	-2.30	109^{+59}_{-32}	0.83	-4.97 ± 0.11		
050714B	87.0	$-2.59_{-0.37}^{+0.32}$	0.88	0.69 ± 0.43	-6.24 ± 0.08	-1.00	-2.59	~20	0.86	~ -5.85		
050716	69.0	NaN		1.57 ± 0.10	-5.20 ± 0.02	-0.87	-2.00	$119^{+19.}_{-16.}$	0.88	-4.70 ± 0.04		
050717 ^g	70.0	NaN		1.63 ± 0.07	-5.84 ± 0.03	-1.12	-2.30	1890^{+1600}_{-760}	0.78	-4.85 ± 0.22		
050721	39.0	$-1.87^{+0.16}_{-0.17}$	1.04	1.06 ± 0.25	-5.51 ± 0.06	-1.12	-2.05	45^{+23}_{-35}	1.04	-5.08 ± 0.09		
050724 ^h	3.0	$-2.11^{+0.24}_{-0.26}$	0.84	0.88 ± 0.22	-5.93 ± 0.06	-0.65	-2.11	\sim 25	0.83	\sim -5.45	0.258	7
050726	30.0	$-0.99^{+0.21}_{-0.20}$	1.23	2.14 ± 0.43	-5.70 ± 0.05	-1.00	-2.30	>984	1.20	>-4.79		
050801	20.0	$-1.95^{+0.19}_{-0.20}$	1.16	1.03 ± 0.27	-6.51 ± 0.07	-1.40	-2.00	~33	1.14	\sim -6.02		
050802	20.0	$-1.54^{+0.14}_{-0.14}$	0.93	1.37 ± 0.19	-5.66 ± 0.04	-1.12	-2.30	$118^{+77.}_{-40.}$	0.95	-5.27 ± 0.13	1.710	8
050803	150.0	$-1.43^{+0.11}_{-0.11}$	0.97	1.51 ± 0.15	-5.65 ± 0.03	-1.05	-2.30	150^{+68}_{-38}	0.97	-5.24 ± 0.12		
050813	0.6	$-1.42^{+0.39}_{-0.39} \ -1.85^{+0.18}_{-0.18}$	1.35	1.66 ± 0.65	-7.37 ± 0.11	-0.40	-2.30	86^{+101}_{-59}	1.29	-7.03 ± 0.27		
050814	65.0	$-1.85^{+0.18}_{-0.18}$	1.09	1.10 ± 0.20	-5.74 ± 0.05	-1.23	-2.77	$58^{+28.}_{-16.}$	1.05	-5.48 ± 0.05		
050819	40.0	$-2.64^{+0.29}_{-0.32}$	0.99	0.61 ± 0.22	-6.45 ± 0.07	-1.00	-2.64	<15	1.04	$< -6.06 \pm 0.07$		
050820A	270.0	$-1.24^{+0.17}_{-0.17}$	1.26	1.73 ± 0.16	-5.08 ± 0.02	-1.00	-2.25	$284^{+82.}_{-55.}$	1.27	-4.52 ± 0.12	2.612	9
050822	102.0	$-2.48^{+0.15}_{-0.15}$	0.97	0.73 ± 0.10	-5.58 ± 0.03	-1.00	-2.48	~36	0.96	~ -5.19		
050826	45.0	$-1.12^{+0.29}_{-0.28}$	0.81	1.76 ± 0.43	-6.35 ± 0.07	-0.93	-2.30	>240	0.81	>-5.82		
051221A ^g	1.4	NaN		1.53 ± 0.08	-5.94 ± 0.01	-1.08	-2.30	402^{+93}_{-72}	1.06	-5.27 ± 0.11	0.547	10

^a GRB duration in 15-150 keV.

function, if one assigns Γ_2 in the range of -5 to $-2.^{12}$ Due to the great uncertainty of Γ_2 , the cutoff power-law model could also fit these four bursts, with the cutoff energy being in the BAT band. The remaining 27 bursts in the sample are best fitted by a simple power law, with the photon index Γ^{PL} ranging from ~ -1 to ~ -3 (see Table 1). For the eight GRBs with the Band function parameters available (GRBs 050128, 050219A, 050401, 050525A, 050713A, 050716, 050717, and 051221) either from a fit to the BAT data or from a joint BAT-Konus *WIND* fit, we make straightforward extrapolation of $S_{\gamma, \text{obs}}$ to derive S_{γ} in the $1-10^4$ keV band. For the remaining 24 bursts whose observed spectra are fitted by a simple power law, the extrapolation is not straightforward. Generally we employ the hardness ratio information to place additional constraints to the spectral parameters. The analyses are carried

out on case-to-case base. Nonetheless, depending on the value of Γ^{PL} , one could crudely group the cases into three categories.

Case I: $-2.3 \lesssim \Gamma^{\text{PL}} \lesssim -1.2$ (16 out of 24 in the sample). Since for typical bursts in the BATSE sample one has $\Gamma_1 \sim -1$ and $\Gamma_2 \sim -2.3$ (Preece et al. 2000), it is expected that a rough fit to the Band function by a simple power law would lead to Γ^{PL} in this range. The break energy E_0 of these bursts should be within or near the edges of the BAT band. The hardness ratio (HR), which in our analysis is defined as the ratio of the fluence in the 50–100 keV band to that in the 25–50 keV band, could be directly measured from the simple PL fit model. Theoretically, on the other hand, HR is a function of Γ_1 , Γ_2 , and E_0 for the Band function model (Cui et al. 2005; see Fig. 1). One can then in principle apply HR as another agent to constrain the spectral parameters by requiring

$$HR^{mod} = HR^{obs},$$
 (2)

 $^{^{\}rm b}$ The power-law index and the reduced χ^2 of the best fit to the BAT data.

^c The hardness ratio is calculated by gamma-ray fluence in 50–100 keV band to that in 25–50 keV band.

^d The logarithm of the observed gamma-ray fluence and its error in the 15-150 keV band.

^e The spectral parameters derived from the best Band function fit with the constraint of $HR^{obs} = HR^{mod}$, except for those bursts with marks. The errors of E_p (in 90% confidence level) are derived from the best fits with Xspec package by fixing both Γ_1 and Γ_2 .

f Logarithm of extrapolated gamma-ray fluence in 1-104 keV band.

g The spectral parameters are taken from the WIND Konus data (Golenetskii et al. 2005a, 2005b, 2005c, 2005d, 2005e; Krimm et al. 2006.)

h Most of the prompt emission was in one peak with 0.25 s, and therefore the burst was considered as a short burst (Barthelmy et al. 2005a).

REFERENCES.— (1) Berger et al. 2005a; (2) Berger et al. 2005b; (3) Fynbo et al. 2005a; (4) Fynbo et al. 2005c; (5) Cenko et al. 2005; (6) Foley et al. 2005; (7) Berger et al. 2005c; (8) Fynbo et al. 2005b; (9) Ledoux et al. 2005; (10) Berger & Soderberg 2005.

 $^{^{12}}$ Although $\Gamma_2\sim-2.3$ for typical GRBs, Γ_2 could be as low as $\sim\!-5$ for XRFs (e.g., Cui et al. 2005; Sakamoto et al. 2005).

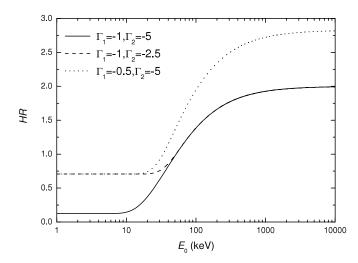


Fig. 1.—HR- E_0 relation for a Band spectrum. Different sets of (Γ_1, Γ_2) have been plotted.

where HR^{mod} and HR^{obs} are the hardness ratio derived from the Band function model and from the data, respectively. To proceed, we first assign a set of "standard" guess values to the spectral parameters, e.g., $\Gamma_1 = -1$, $\Gamma_2 = -2.3$, and $E_p = 250$ keV, and then perform a Band function fit to the data. We then derive Γ_1 , Γ_2 , and E_0 from the best fit, which usually deviate from the guess values. Generally, these parameters have very large error bars. We then apply the HR criterion to the results. If the calculated HR^{mod} using the best-fit parameters match HR^{obs} well, this set of parameters is taken. Otherwise, we adjust spectral parameters to achieve the best match. The process is eased thanks to several properties of the HR- E_0 relation (Fig. 1). First, when E_0 is high enough (say, higher than 30 keV), HR is essentially independent of Γ_2 . Also, for $\Gamma_2 < -2$ most energy is emitted around E_p , and the extrapolated broad band fluence is insensitive to Γ_2 . We therefore take the best-fit Γ_2 value or fix it to \sim -2.3 when Γ_2 is poorly constrained. HR^{mod} therefore mainly depends on Γ_1 and E_0 . Another interesting feature is that as one decreases Γ_1 (i.e., softer spectrum), the corresponding E_0 would increase given the same observed spectrum. The resulting $E_p = (2 + \Gamma_1)E_0$, on the other hand, is not very sensitive to Γ_1 , since the variations of Γ_1 and E_0 cancel out each other. As a result, we simply adjust Γ_1 to refit the spectrum until HR^{mod} is consistent with HR^{obs} within the error range. These spectral parameters (Γ_1 , E_p , and Γ_2) are then taken to perform extrapolation to estimate S_{γ} . Since the determinations of both Γ_1 and Γ_2 are not fully based on fitting procedures, it is very difficult to quantify their errors, and we only report their estimated values. The error of E_0 is taken whenever possible based on the best Band function fit (see Table 1).

Case II: $\Gamma^{PL} > -1.2$ (2 out of 24 in the sample: GRB 050726 and GRB 050826). In this case E_0 should be far beyond the BAT band, and BAT only covers the low-energy part of the spectrum ($E < E_0$). One has $\Gamma_1 \sim \Gamma^{PL}$ or slightly larger (if E_p is not very far above the band). It is very difficult to estimate E_0 (E_p) in this case. Nonetheless, one could use HR^{obs} to pose some constraints. Figure 1 suggests that HR^{mod} converges to a maximum value at high E_p values given a certain Γ_1 . We first let $\Gamma_1 = \Gamma^{PL}$ and check whether HR^{obs} is consistent with HR^{mod}. For both bursts in our sample one has HR^{obs} > HR^{mod}_{max}. This suggests that Γ_1 should be larger than Γ^{PL} . We then gradually increase Γ_1 until HR^{mod}_{max}(Γ_1) becomes consistent with HR^{obs}. Using this Γ_1 one can then fit for E_0 (and E_p). According to Figure 1, there is great degeneracy of E_0 (E_p) at HR^{mod}_{max}. The fitted E_0 (E_p) therefore

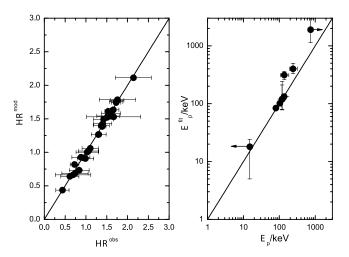


Fig. 2.—Left: Comparison of $\mathrm{HR}^{\mathrm{mod}}$ with $\mathrm{HR}^{\mathrm{obs}}$. Right: Comparison of E_p derived from our method with E_p^{fi} derived from the joint fit using BAT, WIND Konus, or HETE-2 data for eight bursts, including GRB 050128, GRB 050219A, GRB 050401, GRB 050525A, GRB 050713A, GRB 050716, 050717, and GRB 051221. The solid line is $E_p = E_p^{\mathrm{fit}}$.

has very large errors and is unstable. In practice, one could only set a lower limit of E_0 (E_p) below which HR^{mod} starts to deviate from HR^{obs} . As a result only lower limits of E_p of these two bursts are reported in Table 1.

Case III: $\Gamma^{\rm PL} < -2.3$ (6 out of 24 in the sample). In this case, the burst is likely an XRF with E_p near or below the low-energy end of BAT. BAT's observation likely only covers the high-energy part of the spectrum ($E > E_0$). In order to constrain the spectral parameters using the hardness ratio data, we assume $\Gamma_1 = -1$ and $\Gamma_2 = \Gamma^{\rm PL}$ and fit for E_0 by requiring $HR^{\rm mod}(E_0) = HR^{\rm obs}$. According to Figure 1, near $HR^{\rm mod}_{\rm min}$, $HR^{\rm mod}$ is rather insensitive to E_0 (E_p). For most of the cases, one could find a solution of E_0 , but with very large errors. The solutions are also unstable. For these cases we do not report errors in Table 1, but only report the best-fit value with a similar-to symbol. ¹³ For two cases (GRB 050416A and GRB 050819), there is no solution since $HR^{\rm obs} < HR^{\rm mod}_{\rm min}$. Similar to case II, we then lower Γ_2 until a solution is found. Due to the degeneracy of E_0 (E_p) with HR, only upper limits of E_0 (E_p) are found, which are reported in Table 1.

With the spectral parameters derived from the above method, we have extrapolated the observed 15–150 keV fluence $S_{\gamma,\text{obs}}$ to a broader energy range (1–10⁴ keV). The derived S_{γ} is regarded as the total energy output during the prompt phase for further efficiency studies. The results of prompt emission data are reported in Table 1. We caution that due to the intrinsic instrumental limitation, the uncertainties of the results are large. Nonetheless, we have made the best use of the available data (especially the hardness ratio information) to derive the parameters. Figure 2 displays the robustness of the method. Figure 2a shows the criterion adopted in analyzing each burst (eq. [2]). Figure 2b shows how the E_p values derived with our method compares with the E_n^{fit} derived from the WIND Konus or HETE-2 data for eight bursts. The result suggests that our derived E_p meets E_p^{fit} well for moderate E_p values (i.e., those falling into the BAT band) but deviate from E_p^{fit} when E_p is very large. Notice that the reported E_p errors in our method are derived from the best fit by fixing Γ_1

¹³ Similarly, GRB 050319, GRB 050724, and GRB 050801 in case I also have unstable solutions, so that the errors of their E_p values are not reported.

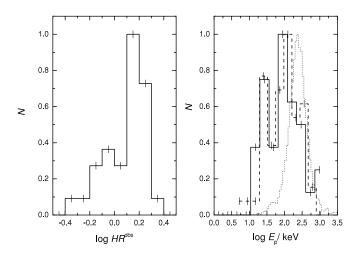


Fig. 3.— Distributions of HR^{obs} (*left*) and E_p (*right*) derived from our method. For the E_p distribution, the histograms of BATSE (*dotted line*) and *HETE-2* (*step-dashed line*) samples are also plotted.

and Γ_2 . The real errors should also include the uncertainties of Γ_1 and Γ_2 . In such cases the errors in the E_p values could be larger to be more consistent with $E_p^{\rm fit}$ in the high- E_p regime. However, due to the difficulty of estimating these errors, they are not included in reported errors.

In Figure 3 we show the distributions of HR and E_p of our sample. For the E_p distribution (right panel), those of the BATSE sample (Preece et al. 2000) and the HETE-2 sample (Lamb et al. 2005) are also plotted for comparison. Our sample is generally consistent with the *HETE-2* sample and tends to be softer than the BATSE sample (as is expected because of a softer bandpass of BAT as compared with BATSE). If one defines XRFs as those bursts with $H\dot{R}^{obs}$ < 1, the number ratio of the XRFs and the GRBs in our sample is \sim 1:2, being consistent the *HETE-2* result (Lamb et al. 2005). An interesting feature is the marginal bimodal distribution of XRFs and GRBs, which is consistent with the previous result derived with the HETE-2 data (Liang & Dai 2004; cf. Sakamoto et al. 2005). In Figure 4 we plot the distribution of S_{γ} as compared with the BATSE results. The energy range of S_{γ} is rescaled to 20–2000 keV (BATSE's energy band). We find that the two distributions are generally consistent with each other, except that Swift GRB sample extends the BATSE sample to lower fluences. This is expected because *Swift* is more sensitive than BATSE.

2.2. X-Ray Afterglows

The X-ray afterglow light curves and the spectra of the bursts in our sample have been presented by O'Brien et al. (2006). Among the five components of the synthetic X-ray light curve (e.g., Zhang et al. 2006), the steep decay component is due to the GRB tail emission (Kumar & Panaitescu 2000; Zhang et al. 2006) and the X-ray flares are due to the late central engine activity (Burrows et al. 2005b; Zhang et al. 2006; Fan & Wei 2005; Ioka et al. 2005; Liang et al. 2006; Wu et al. 2006; King et al. 2005; Perna et al. 2006; Proga & Zhang 2006; Dai et al. 2006). We therefore identify the steep decay component as well as the X-ray flares and remove them from the light-curve contribution. We then fit the light curves by either a broken power law, for those bursts with shallow-to-normal transition, or by a single power law otherwise. Table 2 lists the X-ray data and the fitting results of our sample.

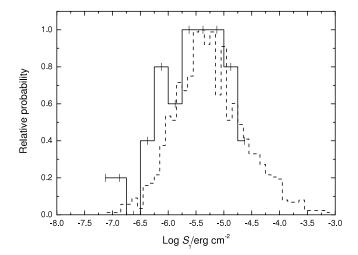


Fig. 4.— Comparison of $\log S_{\gamma}$ distribution (in the 20–2000 keV band) of our sample (*solid histogram*) to that of the BATSE sample (*dashed histogram*).

3. PROMPT GAMMA-RAY FLUENCE VERSUS X-RAY AFTERGLOW FLUENCE

In order to calculate the absolute value of the GRB radiative efficiency η_{γ} (eq. [1]), both E_{γ} and E_K need to be derived. This requires detailed modeling of E_K and the redshift information. The results depend on some unknown parameters (e.g., the shock electron/magnetic field equipartition factors, ϵ_e , ϵ_B , etc.), which we discuss in detail in § 4. Nonetheless, using the directly measured quantities listed in Tables 1 and 2, one can analyze the relative energetics between the prompt emission and the afterglow. The prompt emission fluence S_{γ} is a rough measure of the prompt emission energetics. According to the standard afterglow model and assuming that electron spectral index is $p \sim 2$, that the X-ray band is above both the typical synchrotron emission frequency ν_m and the synchrotron cooling frequency ν_c , and that the inverse Compton cooling is unimportant, the afterglow kinetic energy could be roughly indicated by the quantity $\epsilon_e^{-1} F_{\nu,X}(t) t$, where t is a particular epoch in the afterglow phase (e.g., Freedman & Waxman 2001; Berger et al. 2003; Lloyd-Ronning & Zhang 2004). Since the quantity $S_X(t) = F_{\nu,X}(t)t$ also has the dimension of fluence, the S_{γ} -to- $S_{\rm X}(t)$ ratio could give a rough indication of the relative energetics between the prompt emission and the afterglow. The unknown redshift essentially does not enter the problem.

The shallow decay phase commonly observed in *Swift* GRBs has been generally interpreted as a refreshed external shock (e.g., Rees & Mészáros 1998; Dai & Lu 1998; Panaitescu et al. 1998; Kumar & Piran 2000; Sari & Mészáros 2000; Zhang & Mészáros 2001, 2002a; Dai 2004; Zhang et al. 2006; Nousek et al. 2006; Panaitescu et al. 2006; Granot & Kumar 2006). Within this interpretation, the kinetic energy of the afterglow E_K increases with time for an extended period. This brings extra complication to the efficiency problem. One needs to identify at which epoch the corresponding E_K represents the kinetic energy left over right after the prompt gamma-ray emission. This is a model-dependent problem, and we take an approach to accommodate different possibilities. We pay special attention to two epochs. One is the break time t_b at the shallow-to-normal-decay transition epoch, which corresponds to the epoch when the putative injection phase is over. Within the injection interpretation, another important time is the fireball deceleration time (t_{dec}), which is usually earlier or around the first data point in the shallow decay phase. The kinetic

TABLE 2 Observations and Fitting Results of X-Ray Afterglows

GRB	eta^{a}	$\alpha_1^{\ b}$	$\alpha_2^{\ b}$	$\log (t_b/s)^b$	$\log S_{\mathrm{x},t_{\mathrm{dec}}}{}^{\mathrm{c}}$	$\log S_{x, t_b}^{c}$	$\log S_{x,1h}^{c}$	$\log S_{\mathrm{x},10h}^{\mathrm{c}}$
050126	1.59 ± 0.38	0.95 ± 0.27			-8.37 ± 1.05	-8.23 ± 0.60	-8.27 ± 0.69	-8.22 ± 0.59
050128	0.85 ± 0.12	0.65 ± 0.10	1.25 ± 0.10	3.36 ± 0.10	-7.30 ± 0.16	-6.78 ± 0.18	-6.79 ± 0.19	-7.02 ± 0.23
050215B	0.51 ± 0.50	0.82 ± 0.08			-8.31 ± 0.75	-7.79 ± 0.70	-7.98 ± 0.71	-7.80 ± 0.70
050219A	1.02 ± 0.20	0.59 ± 0.08			-8.40 ± 0.40	-7.26 ± 0.30	-7.64 ± 0.32	-7.23 ± 0.30
050315	1.50 ± 0.40	0.01 ± 0.09	0.74 ± 0.05	4.10 ± 0.14	-9.11 ± 0.08	-7.07 ± 0.10	-7.55 ± 0.08	-6.89 ± 0.13
050319	2.02 ± 0.47	0.52 ± 0.03	1.77 ± 0.19	4.94 ± 0.13	-8.14 ± 0.12	-6.64 ± 0.18	-7.24 ± 0.12	-6.76 ± 0.12
050401	0.98 ± 0.05	0.68 ± 0.05	1.35 ± 0.05	3.74 ± 0.04	-7.01 ± 0.10	-6.42 ± 0.11	-6.44 ± 0.11	-6.65 ± 0.12
050406	1.37 ± 0.25	0.51 ± 0.10			-10.11 ± 0.33	-8.05 ± 0.11	-9.20 ± 0.14	-8.71 ± 0.06
050416A	0.80 ± 0.29	0.40 ± 0.05	0.95 ± 0.05	3.18 ± 0.03	-8.51 ± 0.10	-7.68 ± 0.10	-7.61 ± 0.10	-7.55 ± 0.12
050422	2.23 ± 1.09	0.86 ± 0.04			-8.60 ± 0.20	-8.20 ± 0.16	-8.35 ± 0.17	-8.21 ± 0.16
050502B	0.81 ± 0.28	0.86 ± 0.01			-8.38 ± 0.04	-7.97 ± 0.03	-8.12 ± 0.03	-7.98 ± 0.03
050525	1.07 ± 0.02	1.10 ± 0.05	1.45 ± 0.05	3.44 ± 0.05	-6.29 ± 0.11	-6.52 ± 0.12	-6.56 ± 0.12	-6.96 ± 0.13
050607	0.77 ± 0.48	1.01 ± 0.05	2.46 ± 1.65	5.11 ± 0.24	-7.97 ± 0.36	-8.06 ± 0.49	-7.99 ± 0.36	-8.00 ± 0.36
050712	0.90 ± 0.06	0.72 ± 0.01			-7.86 ± 0.17	-7.48 ± 0.14	-7.62 ± 0.15	-7.49 ± 0.14
050713A	1.30 ± 0.07	0.65 ± 0.10	1.15 ± 0.10	4.00 ± 0.04	-7.55 ± 0.27	-6.86 ± 0.27	-6.96 ± 0.27	-6.89 ± 0.28
050713B	0.70 ± 0.11	0.30 ± 0.11	0.97 ± 0.07	4.21 ± 0.23	-8.23 ± 0.20	-6.66 ± 0.24	-7.06 ± 0.20	-6.59 ± 0.29
050714B	4.50 ± 0.70	0.50 ± 0.06			-8.17 ± 0.32	-6.82 ± 0.26	-7.36 ± 0.27	-6.86 ± 0.26
050716	0.33 ± 0.03	1.06 ± 0.07			-7.41 ± 0.38	-7.58 ± 0.31	-7.51 ± 0.32	-7.57 ± 0.31
050717	1.15 ± 0.10	1.49 ± 0.01			-6.63 ± 0.05	-8.00 ± 0.04	-7.47 ± 0.04	-7.96 ± 0.04
050721	0.74 ± 0.15	1.28 ± 0.01			-6.78 ± 0.06	-7.60 ± 0.05	-7.30 ± 0.05	-7.58 ± 0.05
050724	0.95 ± 0.07	$0.90\pm0.0.1$			-9.21 ± 0.33	-7.86 ± 0.07	-8.56 ± 0.14	-8.21 ± 0.06
050726	0.94 ± 0.07	0.91 ± 0.10	2.45 ± 0.10	4.06 ± 0.04	-7.45 ± 0.11	-7.30 ± 0.12	-7.28 ± 0.11	-7.96 ± 0.14
050801	0.72 ± 0.54	1.10 ± 0.02			-7.70 ± 0.09	-7.99 ± 0.06	-7.89 ± 0.07	-7.99 ± 0.06
050802	0.91 ± 0.19	0.65 ± 0.10	1.65 ± 0.10	3.76 ± 0.04	-7.46 ± 0.10	-6.80 ± 0.11	-6.82 ± 0.10	-7.26 ± 0.14
050803	0.71 ± 0.16	0.61 ± 0.10			-7.58 ± 0.28	-6.77 ± 0.08	-7.04 ± 0.14	-6.65 ± 0.06
050813	2.42 ± 0.89	0.70 ± 0.10	2.12 ± 0.10	2.26 ± 0.12	-9.40 ± 0.13	-9.29 ± 0.20	-10.69 ± 0.30	-11.81 ± 0.36
050814	1.08 ± 0.08	0.62 ± 0.06			-8.63 ± 0.34	-7.51 ± 0.28	-7.97 ± 0.29	-7.59 ± 0.28
050819	1.18 ± 0.23	-0.06 ± 0.06	0.65 ± 0.10	4.26 ± 0.16	-10.85 ± 0.10	-8.20 ± 0.11	-8.89 ± 0.10	-8.04 ± 0.14
050820A	0.87 ± 0.09	1.18 ± 0.01			-6.07 ± 0.03	-6.46 ± 0.01	-6.27 ± 0.02	-6.45 ± 0.01
050822	1.60 ± 0.06	0.46 ± 0.11	0.95 ± 0.04	4.14 ± 0.31	-8.20 ± 0.29	-7.11 ± 0.33	-7.37 ± 0.29	-7.03 ± 0.38
050826	1.27 ± 0.47	1.10 ± 0.01			-7.41 ± 0.05	-7.70 ± 0.04	-7.60 ± 0.05	-7.70 ± 0.04
051221A	1.04 ± 0.20	1.07 ± 0.03			-7.99 ± 0.11	-8.13 ± 0.06	-8.12 ± 0.06	-8.19 ± 0.05

^a X-ray spectral index.

energy at t_{dec} [$E_K(t_{\text{dec}})$] is relevant to the GRB efficiency problem, if the injected energy during the shallow decay phase is due to a long-term central engine (e.g., Dai & Lu 1998; Zhang & Mészáros 2001; Dai 2004), since the bulk of kinetic energy is injected at later epochs. In the scenario that the injection is due to an instantaneous injection with variable Lorentz factors (Rees & Mészáros 1998; Kumar & Piran 2000; Sari & Mészáros 2000; Zhang & Mészáros 2002a; Granot & Kumar 2006), the total kinetic energy of the outflow right after the prompt emission is over should be defined by the kinetic energy measured at t_h [$E_K(t_h)$] when the injection phase is over. However, the kinetic energy of the ejecta that give rise to the gamma-ray emission may be still roughly $E_K(t_{\rm dec})$, since the gamma-ray emission from the low Lorentz factor ejecta can not escape due to the well-known compactness problem (e.g., Piran 1999). Nonetheless, some other scenarios do not interpret the shallow decay as additional energy injection (e.g., Eichler & Granot 2006; Toma et al. 2006; Ioka et al. 2006; Kobayashi & Zhang 2007). In some of these cases $E_K(t_b)$ is the more relevant quantity to define the GRB efficiency, e.g., in the models invoking precursors (e.g., Ioka et al. 2006) and the models involving delayed energy transfer (e.g., Kobayashi & Zhang 2007; Zhang & Kobayashi 2005). In this paper we use both $E_K(t_{\text{dec}})$ and $E_K(t_b)$ to define GRB radiative efficiencies.

The injection break time t_b can be directly measured from the light curves. The fireball deceleration time (for burst durations shorter than this time scale, the so-called thin shell regime) $t_{\text{dec}} \sim$

 $5(1+z)(E_{K,52}/n)^{1/3}(\gamma_0/300)^{-8/3}$, on the other hand, is not directly measured and is very likely buried beneath the steep-decay prompt emission tail component. Here $E_{K,52}=E_K/10^{52}$ ergs (the convention $Q_n=Q/10^n$ in cgs units is adopted throughout the paper), n is the ambient medium density in unit of 1 proton cm⁻³, and γ_0 is the initial Lorentz factor of the fireball. Without knowing γ_0 (noticing the sensitive dependence on this unknown parameter), one cannot accurately estimate this time with the observables. For typical parameters (e.g., z=1, $\gamma_0=150$, and $E_{K,52}/n=1$) we get $t_{\rm dec}\sim 60$ s. Considering also the thick shell regime (i.e., the burst duration is longer than the above critical time, Kobayashi et al. 1999), we finally roughly estimate the deceleration time as $t_{\rm dec}\sim \max(60 \text{ s},\ T_{90})$.

In Figure 5 we plot $S_X(t_{\rm dec})$ (dots) and $S_X(t_b)$ (triangles) against S_γ . The large differences between $S_X(t_{\rm dec})$ and $S_X(t_b)$ indicate that significant energy injection happens in many bursts. One interesting signature evidenced in Figure 5 is that S_γ is positively correlated to S_X . This is consistent with the previous knowledge that the radiated energy is positively correlated to the afterglow kinetic energy. For the case of $S_X(t_b)$, the S_γ - S_X correlation slope is 0.78 ± 0.17 , which is shallower than unity. This suggests that considering the total kinetic energy when the energy injection phase is over $[E_K(t_b)]$, the fainter bursts are not as efficient as brighter ones in converting kinetic energy into radiation. This is consistent with the pre-Swift finding of a shallow correlation between the efficiency η_γ and E_γ (Lloyd-Ronning & Zhang 2004;

b The values α_1 and α_2 are the temporal decay indices before and after the break time (t_b) . If a light curve is fitted by a simple power law, only α_1 is available. The values of S_x at a given time are calculated by the flux times the corresponding time, in units of ergs cm⁻².

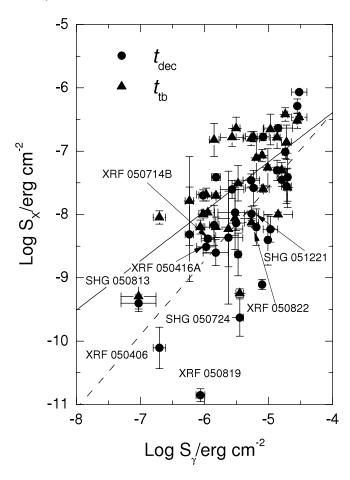


Fig. 5.—Extrapolated prompt emission fluence S_{γ} against the X-ray fluence at $t_{\rm dec}$ (dots) and at t_b (triangles). The solid and dashed lines, with slopes of 0.78 and 1.17, are the best fit to the data at t_b and $t_{\rm dec}$, respectively. The SHGs and XRFs are marked. [See the electronic edition of the Journal for a color version of this figure.]

Lamb et al. 2005). Since generally there is a positive correlation between the E_{γ} and E_p (Lloyd et al. 2000; Amati et al. 2002; Liang et al. 2004; Lamb et al. 2005), this also suggests that softer bursts (e.g., XRFs) tend to have lower efficiencies (Soderberg et al. 2004; Lloyd-Ronning & Zhang 2004). For the case of $t_{\rm dec}$, however, the S_{γ} - S_X correlation slope is very close to unity (1.17 \pm 0.22). This means that the efficiency defined by $E_K(t_{\rm dec})$ (the "true" efficiency in the models invoking additional energy injection) is not sensitively related to E_{γ} , and hence, to E_p according to the positive E_{γ} - E_p correlations. This means that XRFs are not intrinsically inefficient GRBs if the injection hypothesis is true.

To show the effect more clearly, in Figure 6 we plot the ratios $R(t_{\rm dec}) = S_{\gamma}/S_{\rm X}(t_{\rm dec})$ (dots) and $R(t_{t_b}) = S_{\gamma}/S_{\rm X}(t_b)$ (triangles) against the hardness ratio HR ^{obs}. It is found that while the soft bursts (e.g., XRFs) tend to have a lower gamma-to-X ratio (and hence lower radiative efficiency) than the typical GRBs at t_b (a shallow linear dependence with index 0.61 ± 0.21), they do not differ too much from hard GRBs at $t_{\rm dec}$. This means that XRFs are radiatively as efficient as hard GRBs. Such a possibility has been speculated by Lloyd-Ronning & Zhang (2004) and was first recognized by Schady et al. (2006) when analyzing the early UVOT data of XRF 050406. Now we extend the analysis to a larger sample and verify that it is common for other XRFs as well. This conclusion is strengthened by a more careful treatment of radiative efficiency in § 4.2, and we discuss the implications of this result for the XRF models in § 5.

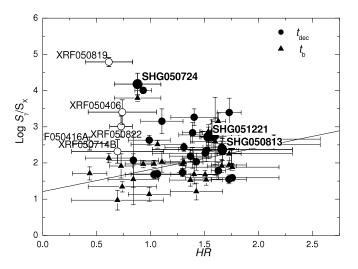


Fig. 6.—Ratios of $S_{\gamma}/S_{\rm X}$ against the hardness ratio HR. The circles represent the data at $t_{\rm dec}$, and the triangles represent the data at t_b . The SHGs (*larger solid circles*) and the XRFs (*open circles*) at $t_{\rm dec}$ are marked. The straight line is the best fit of the data at t_b , which shows a shallow correction between the two quantities, with a linear correlation coefficient 0.61 and a chance probability <0.01. [See the electronic edition of the Journal for a color version of this figure.]

4. GRB EFFICIENCY

4.1. Theoretical Models

In this section we explicitly derive the radiative efficiency for the GRBs in our sample according to equation (1). The isotropic prompt emission energy E_{γ} is derived from the extrapolated 1–10,000 keV band fluence (S_{γ}) according to

$$E_{\gamma} = 4\pi D_L^2 S_{\gamma} (1+z)^{-1}$$

= 1.3×10⁵¹ ergs $D_{L,28}^2 (1+z)^{-1} S_{\gamma,-6}$, (3)

where D_L is the luminosity distance.

The derivation of E_K requires detailed afterglow modeling. Regardless of whether there is indeed a long-lasting central engine, the energy injection process could be mimicked by introducing an "effective" long-lasting central engine with luminosity $L = L_0(t/t_0)^{-q}$. For the varying Lorentz factor injection model the Lorentz factor index s could be related to an effective q through q = (10 - 2s)/(7 + s) for an interstellar medium (ISM) and q = 4/(3 + s) for a wind medium (Zhang et al. 2006). The injection then results in an evolving kinetic energy $E_K \propto t^{(1-q)}$. After the energy injection is over, the fireball can be described by the standard afterglow model. At any epoch during the injection phase, the afterglow emission level could be calculated by taking the kinetic energy at that time. So in our treatment, we still use the standard afterglow model to derive various parameters as functions of E_K , bearing in mind that E_K may be time dependent.

For a constant density medium, the typical synchrotron emission frequency, the cooling frequency, and the peak spectral flux read (Sari et al. 1998; coefficients taken from Yost et al. 2003)¹⁴

$$\nu_m = 3.3 \times 10^{12} \text{ Hz} \left(\frac{p-2}{p-1}\right)^2 (1+z)^{1/2} \epsilon_{B,-2}^{1/2} \epsilon_{e,-1}^2 E_{K,52}^{1/2} t_d^{-3/2}$$
(4)

 14 Lloyd-Ronning & Zhang (2004) adopted the coefficients from Hurley et al. (2002). The ν_m coefficient is larger than adopted here. This effect, together with the ignorance of the inverse Compton (IC) effect, leads to systematic underestimating of E_K and overestimating of η_γ , as also pointed out by Fan & Piran (2006) and Granot et al. (2006). This systematic deviation does not affect the global dependences of η_γ on other parameters, as are reproduced in this paper.

$$\nu_c = 6.3 \times 10^{15} \text{ Hz } (1+z)^{-1/2}$$

$$\times (1+Y)^{-2} \epsilon_{B,-2}^{-3/2} E_{K,52}^{-1/2} n^{-1} t_d^{-1/2}$$
(5)

$$F_{\nu,\,{\rm max}} = 1.6~{\rm mJy}(1+z)D_{28}^{-2}\epsilon_{B,-2}^{1/2}E_{K,52}n^{1/2}. \eqno(6)$$

Here t_d is the observer's time in unit of days,

$$Y = \left[-1 + (1 + 4\eta_1 \eta_2 \epsilon_e / \epsilon_B)^{1/2} \right] / 2 \tag{7}$$

is the IC parameter, where $\eta_1 = \min[1, (\nu_c/\nu_m)^{(2-p)/2}]$ (Sari & Esin 2001), and $\eta_2 \le 1$ is a correction factor introduced by the Klein-Nishina correction. The latter effect was treated in detail by Fan & Piran (2006). Here we adopt an alternative, approximate treatment. For the electron Lorentz factor $\gamma_{e,X}$ corresponding to the X-ray band emission, the synchrotron self-IC effect is significantly suppressed in the Klein-Nishina regime for the photons with energy $\nu > \nu_{KN}$, where

$$\nu_{\rm KN} = h^{-1} \Gamma m_e c^2 \gamma_{e,X}^{-1} (1+z)^{-1}$$

$$\simeq 2.4 \times 10^{15} \text{ Hz } (1+z)^{-3/4} E_{52}^{1/4} \epsilon_{B,-2}^{1/4} t_d^{-3/4} \nu_{18}^{-1/2}, \quad (8)$$

and h is Planck's constant. Based on the νF_{ν} spectrum of the standard synchrotron emission model (Sari et al. 1998), one can roughly estimate $\eta_2 = \min[1, (\nu_{\rm KN}/\nu_c)^{(3-p)/2}]$ for slow cooling $(\nu_m < \nu_c)$ and $\eta_2 = \min[1, (\nu_{\rm KN}/\nu_m)^{1/2}]$ for fast cooling $(\nu_c < \nu_m)$, where the factors $(\nu_{\rm KN}/\nu_c)^{(3-p)/2}$ and $(\nu_{\rm KN}/\nu_m)^{1/2}$ denote the fractions of the photon energy density that contributes to self-IC in the X-ray band in the slow and fast cooling regimes, respectively.

In previous analyses (e.g., Freedman & Waxman 2001; Berger et al. 2003; Lloyd-Ronning & Zhang 2004), the IC cooling was usually not taken into account. The inclusion of IC cooling modifies the X-ray afterglow light curves considerably (e.g., Wu et al. 2005), which also influences the derived GRB efficiency η_{γ} . Here we generally include the IC factor [power of (1+Y)] in the treatment (see also Fan & Piran 2006). The results are reduced to the previous pure synchrotron-dominated case when $Y \ll 1$.

For about two-thirds of the cases in our sample (22 out of 31), the X-ray band temporal decay index and the spectral index are consistent with the spectral regime $\nu > \max(\nu_m, \nu_c)$. This is the regime where E_K is independent of n and only weakly depends on ϵ_B and p, and therefore an ideal regime to measure E_K . One can derive the X-ray band energy flux as¹⁵

$$\begin{split} \nu F_{\nu} \left(\nu = & 10^{18} \text{ Hz} \right) = F_{\nu, \, \text{max}} \nu_c^{1/2} \nu_m^{(p-1)/2} \nu_{\text{X}}^{(2-p)/2} \\ &= 5.2 \times 10^{-14} \, \text{ergs s}^{-1} \, \text{cm}^{-2} D_{28}^{-2} (1+z)^{(p+2)/4} \\ &\times (1+Y)^{-1} f_p \epsilon_{B,-2}^{(p-2)/4} \epsilon_{e,-1}^{p-1} \\ &\times E_{K,52}^{(p+2)/4} t_d^{(2-3p)/4} \nu_{18}^{(2-p)/2}, \end{split} \tag{9}$$

where

$$f_p = 6.73 \left(\frac{p-2}{p-1}\right)^{(p-1)} \left(3.3 \times 10^{-6}\right)^{(p-2.3)/2} \tag{10}$$

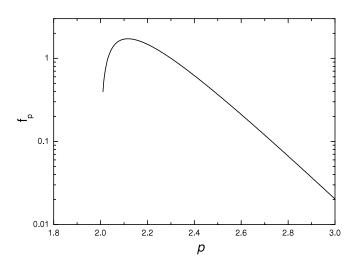


Fig. 7.—Function f_p .

is a function of p, which is calculated in Figure 7. It peaks at \sim 1.72 when $p \sim$ 2.12 and declines monotonically at large p values. For example, at $p \sim$ 3, f_p is only \sim 0.02. This gives a nearly 2 orders of magnitude variation for p = (2.01-3) and thus demands more careful treatments of individual bursts presumably having quite different p-values.

With equation (9), one can derive E_K at any time t_d as

$$E_{K,52} = \left[\frac{\nu F_{\nu}(\nu = 10^{18} \text{ Hz})}{5.2 \times 10^{-14} \text{ ergs s}^{-1} \text{ cm}^{-2}} \right]^{4/(p+2)}$$

$$\times D_{28}^{8/(p+2)} (1+z)^{-1} t_d^{(3p-2)/(p+2)}$$

$$\times (1+Y)^{4/(p+2)} f_p^{-4/(p+2)} \epsilon_{B,-2}^{(2-p)/(p+2)}$$

$$\times \epsilon_{e,-1}^{4(1-p)/(p+2)} \nu_{18}^{2(p-2)/(p+2)}.$$
(11)

This could be reduced to $E_K \sim \epsilon_e^{-1} S_X D_L^2/(1+z)$ for $p \sim 2$. Comparing with equation (3), we can see that as far as the efficiency problem is concerned the redshift-dependence is very weak.

For nearly one-third of the cases in our sample (9 out of 31), the X-ray data are not consistent with being in the regime $\nu_X > \max(\nu_m, \ \nu_c)$ [which requires $\alpha = (3\beta-1)/2$ for the $F_{\nu} \propto t^{-\alpha}\nu^{-\beta}$ convention]. The temporal decay slope in the normal decay phase is close to -1. This rules out the fast-cooling case $\nu_c < \nu_X < \nu_m$ for both ISM and wind models. For slow-cooling models ($\nu_m < \nu_X < \nu_c$), the temporal decay index derived from the wind model [$\alpha = (3\beta+1)/2$ for the $F_{\nu} \propto t^{-\alpha}\nu^{-\beta}$ convention; Chevalier & Li (2000)] is too steep compared with the data in our sample. One is then left with the only possibility, $\nu_m < \nu_X < \nu_c$ in the ISM model. In fact the observed α and β are consistent with being in this regime [$\alpha = (3/2)\beta$]. The derived X-ray-band energy flux is then

$$\nu F_{\nu} \left(\nu = 10^{18} \text{ Hz} \right)
= F_{\nu, \text{ max}} \left(\nu_m / \nu_X \right)^{(p-1)/2}
= 6.5 \times 10^{-13} \text{ ergs s}^{-1} \text{ cm}^{-2} D_{28}^{-2} (1+z)^{(p+3)/4}
\times f_p \epsilon_{B-2}^{(p+1)/4} \epsilon_{e,-1}^{p-1} E_{K.52}^{(p+3)/4} n^{1/2} t_d^{(3-3p)/4} \nu_{18}^{(3-p)/2},$$
(12)

¹⁵ Although our treatment is for a constant-density medium, eq. (9) is valid for more general cases (e.g., wind medium) since in this regime the flux does not depend on the medium density.

This gives

$$E_{K,52} = \left[\frac{\nu F_{\nu}(\nu = 10^{18} \text{ Hz})}{6.5 \times 10^{-13} \text{ ergs s}^{-1} \text{ cm}^{-2}} \right]^{4/(p+3)}$$

$$\times D_{28}^{8/(p+3)} (1+z)^{-1} t_d^{3(p-1)/(p+3)}$$

$$\times f_p^{-4/(p+3)} \epsilon_{B,-2}^{-(p+1)/(p+3)} \epsilon_{e,-1}^{4(1-p)/(p+3)}$$

$$\times n^{-2/(p+3)} \nu_{18}^{2(p-3)/(p+3)}. \tag{13}$$

Inspecting equation (5), one can draw the conclusion that in order to have $\nu_c > \nu_X$ in the normal decay regime $(t_d \sim 1)$, ϵ_B must be very small (e.g., $<(10^{-3} \text{ to } 10^{-4})]$). Keeping a more or less constant $\epsilon_e \sim 0.1$, the Y parameter (eq. [7]) does not increase significantly for a smaller ϵ_B , since the η_2 parameter becomes much smaller due to the Klein-Nishina suppression. In order not to derive a unreasonably large E_K value (limited by the total energy budget of the progenitor system), the data also require a small ambient density (e.g., n < 0.1).

4.2. Calculation Results

Equations (11) and (13) suggest that the absolute value of E_K depends on several unknown shock parameters. In order to calculate η_{γ} , the absolute value of E_K is needed. This requires a detailed multiwavelength study (e.g., Panaitescu & Kumar 2001; Yost et al. 2003) to constrain unknown shock parameters as well. Limited by the X-ray data alone, one inevitably needs to make some assumptions on the unknown shock parameters.

Our first step is to use the X-ray data (temporal index α_X and spectral index β_X) to determine the spectral regime the burst belongs to. In all the cases, we choose the "normal" decay phase for the temporal index (α_2 for the broken power-law fit; or α_1 for the single power-law fit if α_1 is close to unity). This is because this segment has no contamination of energy injection (with unknown q parameter). Using α_X and β_X we check the spectral regime of the X-ray band by comparing the α - β relation of various models (e.g., Table 1 of Zhang & Mészáros 2004). We find that within the error uncertainties of the data, most bursts could be grouped into two spectral regimes: (1) $\nu_X > \max(\nu_m, \nu_c)$ (20 out of 31); and (2) $\nu_m < \nu_X < \nu_c$ in the ISM model (9 out of 31). Two bursts have unexpectedly large spectral indices, i.e., GRB 050319 $(\beta_{\rm X} = 2.02 \pm 0.47)$ and GRB 050714B $(\beta_{\rm X} = 4.50 \pm 0.70)$. The spectrum is likely dominated by the contribution of the GRB tail emission, and we assume that in the afterglow phase they are in the regime of $\nu_{\rm X}>\max(\nu_{\rm m},\nu_{\rm c})$, the default case. GRB $050215 \mathrm{B} \, (eta_{\mathrm{X}} \sim \! 0.5 \pm 0.5) \, \mathrm{and \, GRB} \, 050716 \, (eta_{\mathrm{X}} = 0.33 \pm 0.03)$ have very small spectral indices, and we assume that it is in the regime $\nu_m < \nu_X < \nu_c$. After determining the spectral regimes, we derive p from β_X ($\beta_X = -p/2$ for $\nu_X > \max(\nu_m, \nu_c)$ and $\beta_{\rm X} = -(p-1)/2$ for $\nu_m < \nu_{\rm X} < \nu_c$). Given the large error bars usually associated with the spectral indices, whenever $p \le 2$ and p > 3 we take p = 2.01 and 3, respectively.

4.2.1.
$$\nu_{\rm X} > \max(\nu_m, \ \nu_c)$$

Since there are too many unknown parameters for the regime 2 bursts (eq. [13]), we first ignore them and focus on the regime 1 bursts, whose E_K essentially only depend on ϵ_e . Previous broadband fitting suggests that ϵ_e is typically around 0.1 (Wijers & Galama 1999; Panaitescu & Kumar 2001; Yost et al. 2003; Liang et al. 2004; Wu et al. 2004). The value of ϵ_B has a large scatter for previous bursts but nonetheless has a typical value of 0.01 (e.g., Panaitescu & Kumar 2001). The existence of regime 2 bursts suggest that at least some bursts have very small ϵ_B . We therefore

also consider the cases with a smaller ϵ_B , say, $\sim 10^{-4}$. In any case E_K is insensitive to ϵ_B in regime 1.

Our calculation procedure for regime 1 GRBs is as follows:

- 1. Use the extrapolated S_{γ} in the 1–10,000 keV band to derive E_{γ} according to equation (3). Since η_{γ} is insensitive to z, we take a moderate redshift, z=2, for those bursts whose redshifts are not directly measured.
- 2. Use $\beta_{\rm X}$ and the 0.3–10 keV band flux to calculate the monochromatic flux at 10^{18} Hz, $F_{\nu}(\nu=10^{18}$ Hz).
- 3. Calculate $E_{K,52}$ with equation (11) at two epochs, $t_{\rm dec}$ and t_b . For each epoch we calculate two values: one value $(E_{K,52}^{(1)})$ for $(\epsilon_e, \epsilon_B) = (0.1, 0.01)$ and another $(E_{K,52}^{(2)})$ for $(\epsilon_e, \epsilon_B) = (0.1, 10^{-4})$. The Y parameter is searched self-consistently according to the method described in \S 4.1.
 - 4. Use equation (1) to derive $\eta_{\gamma}^{(1)}$ and $\eta_{\gamma}^{(2)}$ at t_{dec} and t_b .

Table 3 displays our calculation results for regime 1 GRBs. Equation (11) indicates that the apparent dependence on ϵ_B is weak. This is strengthened by the Klein-Nishina effect, since Y does not increase significantly as ϵ_B is lowered. Comparing $E_K^{(1)}$ and $E_K^{(2)}$ (or $E_K^{(1)}$ and $E_K^{(2)}$) at a same epoch, we can see that the difference introduced by changing $\epsilon_B = 0.01$ to $E_K^{(2)}$ is not significant. In Figure 8 we show the $E_K^{(2)}$ contour in the $E_K^{(2)}$ plane for GRB 050219A. It again shows the result is insensitive to $E_K^{(2)}$ so that $E_K^{(2)}$ is the most sensitive parameter for determining $E_K^{(2)}$ and hence, for determining $E_K^{(2)}$ and hence, for determining $E_K^{(2)}$ and hence, for determining $E_K^{(2)}$ is usually suggests that if shock parameters are not too different from burst to burst, the $E_K^{(2)}$ value for the regime 1 bursts may be also low (e.g., the second parameter set, $E_K^{(2)}$ equal to $E_K^{(2)}$ in the regime 1 calculations). This suggests slightly lower radiative efficiencies than previously estimated (typically taken as $E_K^{(2)}$ despite a very shallow dependence.

Inspecting the calculated η_{γ} for the bursts in the spectral regime 1, we find that at t_{dec} , 10 out of 22 bursts have a radiative efficiency $\eta_{\gamma}^{(1)}$ higher than 60%, sometimes even as high as 98% (GRB 050819). The rest have much lower efficiencies, sometimes only a few percent. At t_b , on the other hand, the values of η_{γ} are typically several percent or even lower. Those bursts with low efficiencies from the very beginning correspond to the cases without significant energy injection in the early phase. For illustration, in Figure 9 we present the combined BAT-XRT light curves in the XRT band for some GRBs having extremely high or low efficiencies at t_{dec} (see also O'Brien et al. 2006). It is evident that the XRT light curves of the high- $\eta_{\gamma}(t_{\text{dec}})$ GRBs have a very flat energy injection component and a prominent steeply decaying prompt emission tail (e.g., GRB 050315 and GRB 050714B). Those with low- $\eta_{\gamma}(t_h)$, on the other hand, typically have a smooth transition from prompt emission to afterglow without a significant steep decay component and/or a shallow decay component due to energy injection (e.g., GRB 050401 and GRB 050712).

In Figure 10 we plot $\eta_{\gamma}^{(1)}$ as a function of the hardness ratio HR. We again find that while there exists a shallow correlation between $\eta_{\gamma,t_b}^{(1)}$ and HR (with index 1.12 ± 0.90), such a correlation essentially disappears when η_{γ} at $t_{\rm dec}$ is considered. This is consistent with the analysis in § 2.2. The results suggest that if $E_K(t_{\rm dec})$ is the relevant afterglow energy left over after the prompt emission, XRFs and GRBs intrinsically have similar radiative efficiencies, as opposed to the conclusion drawn using late-time X-ray data only.

Two short-hard GRB 050724 and GRB 050813 are in the spectral regime 1. The results in Table 3 suggest that there is no noticeable difference between short, hard GRBs and long, soft

 ${\bf TABLE~3}$ The Derived Kinetic Energies and Gamma-Ray Efficiencies

GRB	$\log E_K^{(1)}(t_{\rm dec})$ (ergs)	$\eta_{\gamma}^{(1)}(t_{\text{dec}})^{\text{a}}$ (100%)	$\log E_K^{(1)}(t_b)$ (ergs)	$\eta_{\gamma}^{(1)}(t_b)^{\rm a} \ (100\%)$	$\log E_K^{(2)}(t_{\rm dec})$ (ergs)	$\eta_{\gamma}^{(2)}(t_{\text{dec}})^{\text{a}}$ (100%)	$\log E_K^{(2)}(t_b)$ (ergs)	$\eta_{\gamma}^{(2)}(t_b)^{\mathrm{a}} \ (100\%)$
050126	51.86(0.84)	57.78(48.81)	53.60(0.48)	2.39(2.84)	52.26(0.84)	35.27(45.68)	54.00(0.48)	0.97(1.16)
050128	54.48(0.16)	4.03(1.51)	55.01(0.17)	1.22(0.50)	54.49(0.16)	3.99(1.49)	55.02(0.17)	1.21(0.50)
050219A	52.84(0.39)	57.21(22.20)	54.05(0.30)	7.57(4.85)	52.85(0.39)	56.09(22.33)	54.07(0.30)	7.25(4.66)
050315	51.69(0.06)	93.55(0.96)	54.59(0.08)	1.79(0.33)	52.09(0.06)	85.24(2.00)	54.99(0.08)	0.72(0.13)
050319	52.45(0.10)	~ 70	55.59(0.14)	\sim 0.2	52.85(0.10)	\sim 48	55.99(0.14)	~ 0.1
050401	55.05(0.10)	2.79(0.70)	55.66(0.11)	0.70(0.19)	55.06(0.10)	2.76(0.69)	55.66(0.11)	0.70(0.18)
050406	50.67(0.28)	~80	54.38(0.09)	~0.1	50.99(0.28)	~66	54.69(0.09)	\sim .04
050416A	52.34(0.10)	\sim 5	53.18(0.10)	$\sim \! 0.8$	52.35(0.10)	\sim 5	53.18(0.10)	~ 0.8
050422	51.80(0.16)	68.99(12.56)	53.83(0.13)	2.01(1.06)	52.20(0.16)	46.97(14.62)	54.23(0.13)	0.81(0.43)
050502B	53.40(0.04)	3.99(0.99)	53.84(0.03)	1.51(0.37)	53.41(0.04)	3.95(0.98)	53.84(0.03)	1.50(0.37)
050525	53.50(0.11)	7.64(1.78)	53.45(0.11)	8.49(2.03)	53.56(0.11)	6.61(1.55)	53.52(0.11)	7.36(1.78)
050607	53.82(0.36)	4.11(4.06)	53.75(0.49)	4.78(5.86)	53.82(0.36)	4.06(4.02)	53.75(0.49)	4.72(5.80)
050712	54.18(0.14)	1.63(0.86)	55.03(0.14)	0.24(0.13)	54.19(0.14)	1.61(0.85)	55.03(0.14)	0.23(0.12)
050713A	52.92(0.24)	68.02(12.41)	54.37(0.24)	7.07(3.76)	53.19(0.24)	53.84(14.18)	54.63(0.24)	4.00(2.20)
050714B	50.80(0.25)	~96	53.49(0.21)	~4	51.20(0.25)	~89	53.89(0.21)	~ 2
050717	53.91(0.05)	14.11(6.38)	53.22(0.04)	44.47(12.90)	54.05(0.05)	10.65(5.01)	53.36(0.04)	36.74(12.14)
050724	50.40(0.29)	69.23(14.68)	50.81(0.07)	46.54(5.16)	50.40(0.29)	68.98(14.75)	50.81(0.07)	46.26(5.15)
050813	51.03(0.10)	44.81(16.69)	51.45(0.16)	23.63(13.13)	51.43(0.10)	24.43(12.46)	51.85(0.16)	10.96(7.10)
050814	52.17(0.32)	67.78(16.47)	53.59(0.27)	7.38(4.31)	52.25(0.32)	63.80(17.42)	53.67(0.27)	6.26(3.70)
050819	49.95(0.09)	~99	53.02(0.10)	~7	50.11(0.09)	~98.	53.18(0.10)	~5
050822	52.43(0.23)	~69	54.59(0.27)	$\sim 1.55(0.94)$	52.83(0.23)	\sim 47	54.99(0.27)	0.6
050826	53.01(0.05)	>12	53.80(0.04)	>2	53.25(0.05)	>7	54.04(0.04)	>1
051221A	51.92(0.11)	32.56(7.83)	51.90(0.06)	33.57(6.54)	51.96(0.11)	30.61(7.57)	51.94(0.06)	31.59(6.33)

Note.—At t_{dec} and t_b for the GRBs in the spectral regime $\nu_X > \max(\nu_m, \nu_c)$ by assuming $(\epsilon_e, \epsilon_B) = (0.1, 0.01)^{(1)}$, and $(\epsilon_e, \epsilon_B) = (0.1, 0.0001)^{(2)}$.

GRBs as far as the radiative efficiencies are concerned. The same conclusion was drawn for the first short GRB with X-ray afterglow detection (GRB 050509b; Gehrels et al. 2005; Bloom et al. 2006) and is being verified by a larger sample of short GRBs in accumulation. To increase the short GRB sample, we have also performed the same analysis to GRB 051221A (e.g., Golenetskii

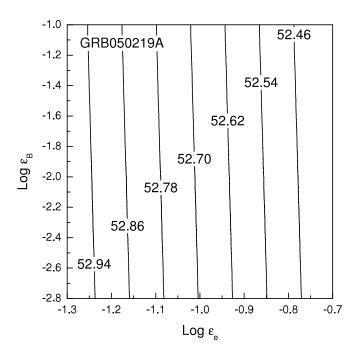


Fig. 8.—Contours of log E_K in the (ϵ_e, ϵ_B) plane for GRB 050219A.

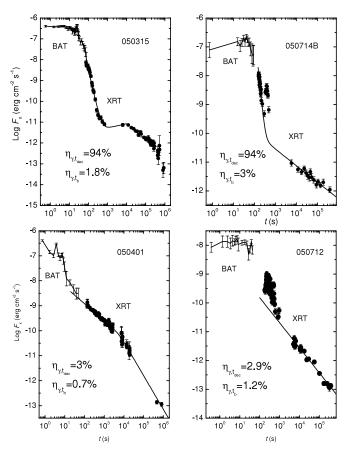


Fig. 9.—Comparisons of the joint BAT-XRT light curves in the XRT band for some GRBs having extremely high or low efficiencies at $t_{\rm dec}$.

^a The derived η is insensitive to the redshift. For those bursts whose redshifts are not available we take z=2 in the calculation. The errors of η are calculated by considering only the errors from the extrapolated gamma-ray fluences and the observed X-ray fluxes. Therefore, the errors of η only reflect the observational errors. E_K is sensitive to microphysics parameters that are poorly constrained. The *true* errors of η should be significantly larger than what are reported here.

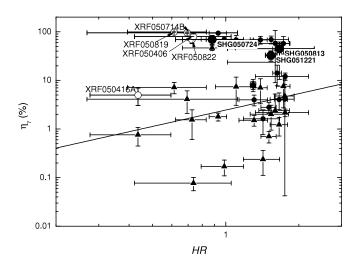


Fig. 10.—Radiative efficiency $\eta_{\gamma}^{(1)}$ against the hardness ratio HR. The circles represent the data at $t_{\rm dec}$, and the triangles represent the data at t_b . The SHGs (larger solid circles) and the XRFs (open circles) at $t_{\rm dec}$ are also marked. The dashed line is the best fit of the data at t_b , which shows a shallow correction between the two quantities similar to that shown in Fig. 6. [See the electronic edition of the Journal for a color version of this figure.]

et al. 2005e). The results are included in all the tables and figures, making the total number of bursts in our sample 32. The inclusion of this burst strengthens the conclusion that short GRBs are no different from long GRBs in radiative efficiencies.

4.2.2.
$$\nu_m < \nu_X < \nu_c$$

For the regime 2 bursts, we can set up an upper limit on ϵ_B using the light curves. Typically this limit is very low (say, $<10^{-4}$) since the afterglow light curves usually extend to very late epochs (say, >1 day). The efficiency estimated for these bursts have even larger uncertainties because E_K depends on many unknown parameters, e.g., ϵ_e , ϵ_B , n, etc. Nonetheless, we perform some rough estimates with the following procedure.

To keep ν_c above ν_X for a long period of time (say, days), one must have a small ϵ_B and/or a small n. Sometimes one even needs to lower ϵ_e if one is reluctant to lower n. A lower ϵ_B and a lower ϵ_e would lead to a larger E_K and hence, a lower η_γ . Since we do not know which parameter is in operation, we fix $\epsilon_e = 0.1$ and n = 0.1, and search ϵ_B downward to find the highest ϵ_B that allows $\nu_m < \nu_X < \nu_c$ to be satisfied. In Table 4 we present our search results for the regime 2 bursts. The efficiency value listed does not represent the real value. There are no obvious reasons to argue for ϵ_e being 0.1, n being 0.1, or ϵ_B not being even lower.

Nonetheless, the value roughly indicates how E_K and η_γ look when the regime 2 spectral condition is satisfied. The results suggest that ϵ_B is rather low, in most cases lower than 10^{-4} . The estimated E_K is typically very high, and hence the radiative efficiency is very low. This suggests that either these GRBs are intrinsically inefficient or the ambient densities of at least these GRBs are quite low, say $n \ll 0.1 \text{ cm}^{-3}$.

5. CONCLUSIONS AND DISCUSSION

We present a detailed analysis on the prompt gamma-ray emission and the early X-ray afterglow emission for a sample of 31 GRBs detected by *Swift* and derived their radiative efficiencies. The sample includes both long and short GRBs and both normal GRBs and softer XRFs. This allows us to investigate how the GRB radiative efficiency vary globally within different populations. We summarize our findings in the following.

- 1. Due to the intrinsic limitation of the BAT instrument, it is very difficult to derive spectral parameters of the prompt emission and to extrapolate the BAT fluence to a broader band. We have developed a method by making use the hardness ratio information to derive spectral parameters assuming a Band function spectrum for all the bursts. This is probably the best effort with the available BAT data. The uncertainties involved are still large. It is also difficult to set errors to the quantities. The errors of Γ_1 and Γ_2 of the Band function are not accounted for in our analysis, but those of E_0 are included whenever possible. These errors are included to derive the errors of S_γ , which also include the uncertainties in the observations. Due to the intrinsic limitation of the method, the errors of S_γ are likely underestimated.
- 2. We compare our prompt emission data with those of BATSE (Preece et al. 2000) and *HETE-2* (Lamb et al. 2005; Sakamoto et al. 2005) and generally find consistent results. *Swift* extends the fluence to the fainter regime and the hardness ratio to the softer regime with respect to BATSE. The derived properties of XRFs (including the 2:1 relative population between GRBs and XRFs) are generally consistent with those derived from the *HETE-2* data.
- 3. The shallow decay component commonly detected in X-ray afterglows complicates the efficiency study. Previous analyses using late-time X-ray afterglow data (say, 10 hr) inevitably overestimated E_K and hence underestimated the GRB efficiency if the shallow decay is due to energy injection. We define two characteristic time epoches, the putative fireball deceleration time ($t_{\rm dec}$) and the epoch when the shallow decay is over (t_b), to study the efficiency problem. The efficiency derived at the former epoch [i.e., $\eta_{\gamma}(t_{\rm dec})$] is likely the true efficiency for the models

TABLE 4
Derived Kinetic Energies and Gamma-Ray Efficiencies

GRB	ϵ_B	$\log E_{K,52}(t_{\rm dec})$ (ergs)	$\eta_{\gamma}(t_{\rm dec})$ (100%)	$\log E_{K,52}(t_b)$ (ergs)	$\eta_{\gamma}(t_b)$ (100%)
050215B	3×10^{-6}	53.65(1.49)	~1	54.17(1.40)	~0.4
050713B	4×10^{-6}	52.01(0.35)	90.68(7.19)	54.98(0.42)	1.03(1.02)
050716	3×10^{-7}	55.96(0.76)	0.20(0.36)	55.09(0.62)	1.48(2.10)
050721	9×10^{-5}	54.55(0.10)	2.11(0.66)	53.54(0.08)	18.29(4.35)
050726	5×10^{-5}	53.22(0.16)	>48	54.38(0.18)	>6
050801	2×10^{-4}	52.84(0.15)	~11	52.93(0.10)	~9
050802	2×10^{-5}	52.95(0.16)	29.60(9.72)	54.79(0.17)	0.61(0.29)
050803	6×10^{-6}	53.12(0.48)	29.37(23.78)	54.79(0.14)	0.88(0.37)
050820A	7×10^{-7}	56.50(0.04)	0.14(0.04)	56.22(0.02)	0.27(0.07)

that interpret the shallow decay phase as due to energy injection (Zhang et al. 2006; Nousek et al. 2006; Panaitescu et al. 2006), while that derived at the later epoch [i.e., $\eta_{\gamma}(t_b)$] is the true efficiency for some models that invoke precursor injection (Ioka et al. 2006) or delayed energy transfer from the fireball to the circumburst medium (Kobayashi & Zhang 2007; Zhang & Kobayashi 2005).

4. We investigate both the observationally defined gammato-X fluence ratio $(R_{\gamma/X})$ and the theoretically defined efficiency (η_{γ}) at the two epochs. The former invokes direct observables and therefore is subject to fewer uncertainties. The latter involve theoretical modeling, which depends on the uncertainties of many unknown microphysics parameters. The error of the latter is therefore difficult to quantify. Our approach is to fix model parameters and only derive the errors introduced from the uncertainties of observations and data analyses. The errors of calculated efficiencies are therefore underestimated. Nonetheless, some interesting features emerge from both the $R_{\gamma/X}$ analysis and the η_{γ} analysis. At t_b , a shallow correlation between $R_{\gamma/X}$ or η_{γ} and the hardness ratio is found. This is consistent with previous findings (Soderberg et al. 2004; Lloyd-Ronning & Zhang 2004; Lamb et al. 2005) that XRFs appear to be less efficient. However, the shallow correlation disappears when the analysis is performed at t_{dec} . This suggests that if the shallow decay is indeed due to energy injection, XRFs have similar radiative efficiencies as normal GRBs. The apparent low efficiency inferred using late time data must be attributed to some other reasons.

The result has important implications for understanding the nature of XRFs. In particular, it disfavors the model that interprets XRFs as events similar to GRBs but having smaller Lorentz factor contrasts and therefore lower radiative efficiencies (e.g., Barraud et al. 2005), if the shallow decay phase is due to energy injection. It suggests that XRFs are dim because the initial kinetic energy is also low and that they gain larger kinetic energies later through energy injection. While there is no straightforward reason for energy injection in the radial direction (e.g., due to a long-lived central engine or pile-up of slow ejecta) for XRFs, some geometric models of XRFs indeed expect energy "injection" from the horizontal directions. These models, such as the quasiuniversal Gaussian-like structured jet model (Zhang et al. 2004a; Dai & Zhang 2005; Yamazaki et al. 2004), invoke relativistic ejecta with variable luminosities and possibly variable Lorentz factors in a wide range of angles. While GRBs correspond to the cases when observers view the bright core component (e.g., the line of sight is inside the typical Gaussian angle), XRFs are those cases when observers view the off-axis jet at a larger viewing angle. As long as the bulk Lorentz factor of the ejecta is still relativistic in these directions, the prompt emission of XRFs is weaker (because of the low energy in the direction) but with a comparable efficiency as in the core direction, since the initial kinetic energy in the direction is also low. Later as the jet is decelerated, the observer in the off-axis direction would progressively receive the energy contribution from the energetic core so that the light curve shows an early shallow decay (e.g., Kumar & Granot 2003; Salmonson 2003). At later times, the effective kinetic energy in the viewing direction is enhanced, leading to an apparently high kinetic energy (and hence, an apparently low radiative efficiency). Such a picture might be consistent with the data. In fact, the long-term X-ray afterglow light curve of XRF 050416A could be modeled by such a model (Mangano et al.

Other geometric models of XRFs have been also discussed in the literature. The model involving sharp-edge jets viewed offbeam (Yamazaki et al. 2002) predicts an initial rising light curve and a steep decay after reaching the peak due to sideways expansion, which is not favored by the data. Granot et al. (2005) suggested a smoother edge, which in effect is similar to the Gaussian jet model (Zhang et al. 2004a). The two-component jet model (Zhang et al. 2004b; Huang et al. 2004; Liang & Dai 2004; Peng et al. 2005) could be consistent with the data as long as the second component is not distinct enough to result in noticeable light curve features that are not detected. Power-law structured jets (Zhang & Mészáros 2002b; Rossi et al. 2002) may also interpret XRFs (Jin & Wei 2004; D'Alessio et al. 2006), but the model predicts too large an XRF population (Lamb et al. 2005; Zhang et al. 2004a). Finally, the varying opening angle model for XRFs invoke very wide jets for XRFs (Lamb et al. 2005). However, there is no straightforward reason to expect the significant change of E_K (and hence, η_{γ}) at early times in this model.

It is possible that the shallow decay phase is not due to energy injection. Numerical simulations (Kobayashi & Zhang 2007) suggest that the timescale for a fireball to transfer energy from the ejecta to the medium is long. It could be that the observed shallow decay phase reflects the epochs during which the energy transfer is going on. A Poynting-flux-dominated flow may further extend the energy transfer period further due to the inability of tapping kinetic energy of the shell with the presence of a reverse shock (Zhang & Kobayashi 2005). If this is the case, $E_K(t_b)$ is the relevant kinetic energy to define GRB efficiency, and XRFs are then indeed intrinsically inefficient GRBs (e.g., Barraud et al. 2005). More detailed early data and modeling are needed to reveal whether such a possibility holds.

5. The absolute value of radiative efficiency is subject to the uncertainties of afterglow parameters. By inspecting the spectral index and the temporal decay index of the X-ray afterglows, we identify 22 bursts whose afterglow cooling frequency is below the X-ray band. In this regime the radiative efficiency is insensitive to parameters except for ϵ_e . Assuming $\epsilon_e = 0.1$, we find that $\eta_{\gamma}(t_b)$ of most bursts are smaller than 10%, while $\eta_{\gamma}(t_{\rm dec})$ ranges from a few percent to >90%. Some bursts have a low efficiency throughout, and they correspond to the ones whose X-ray afterglow light curve smoothly join the prompt emission light curve without a distinct steep decay component or an extended shallow decay component.

The standard internal shock models predict that the GRB efficiency is only around 1% (Kumar 1999; Panaitescu et al. 1999). Our results indicate that some GRBs satisfy such a constraint. On the other hand, a group of GRBs with an early shallow decay component challenge the internal shock model if $E_K(t_{\rm dec})$ is the relevant quantity to define the efficiency, as is required in most energy injection models. Suggestions have been made in the literature to increase the efficiency (e.g., Beloborodov 2000; Kobayashi & Sari 2001; Fan et al. 2004; Rees & Mészáros 2005; Pe'er et al. 2005). For those models that invoke $E_K(t_b)$ to define the efficiency (e.g., Ioka et al. 2006; Kobayashi & Zhang 2007), the data are consistent with the expectation of the internal shock model. The typical efficiency in such a case is 10% or lower.

- 6. The three short GRBs (050724, 050813, and 051221A) have similar efficiencies as long GRBs at both $t_{\rm dec}$ and t_b , despite their distinct progenitor systems (Gehrels et al. 2005; Fox et al. 2005; Villasenor et al. 2005; Hjorth et al. 2005; Barthelmy et al. 2005a; Berger et al. 2005c; Bloom et al. 2006). This trend is being verified by more and more short GRB data and will be reinforced by a larger sample of short GRBs in the future.
- 7. Although most of the X-ray afterglows in our sample are above the cooling frequency, nine GRBs do have a cooling frequency higher than the X-ray band for a very long time, suggesting a very small ϵ_B and/or a low medium density $n \ll 0.1$ cm⁻³.

An extremely low medium density may not be at odd for long GRBs. If some of these long GRBs explode in superbubbles created by preceding supernovae or GRBs, the ambient medium could reach such a low density.

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