

## AN ESTIMATION OF THE GAMMA-RAY BURST AFTERGLOW APPARENT OPTICAL BRIGHTNESS DISTRIBUTION FUNCTION

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### ABSTRACT

By using recent publicly available observational data obtained in conjunction with the NASA *Swift* gamma-ray burst (GRB) mission and a novel data analysis technique, we have been able to make some rough estimates of the GRB afterglow apparent optical brightness distribution function. The results suggest that 71% of all burst afterglows have optical magnitudes with  $m_R < 22.1$  at 1000 s after the burst onset, the dimmest detected object in the data sample. There is a strong indication that the apparent optical magnitude distribution function peaks at  $m_R \approx 19.5$ . Such estimates may prove useful in guiding future plans to improve GRB counterpart observation programs. The employed numerical techniques might find application in a variety of other data analysis problems in which the intrinsic distributions must be inferred from a heterogeneous sample.

*Subject headings:* gamma rays: bursts — methods: statistical

### 1. INTRODUCTION

One of the outstanding questions about gamma-ray burst (GRB) afterglows is their optical luminosity. Since the first counterpart (van Paradijs et al. 1997) was identified in 1997 February 28, GRBs have been detected optically over an intensity range that spans at least 14 mag using instruments ranging in aperture from 10 cm to 10 m. Although the NASA *Swift* mission successfully determines celestial coordinates to accuracies that are often better than a few arcseconds, less than 50% of all *Swift* detections have led to identifiable optical counterparts. The reason for this relatively low rate has been the subject of much speculation. The three popular views are that: (1) GRBs are born in dusty, opaque star-forming regions (Reichart & Price 2002; Klose et al. 2003; Vergani et al. 2004; Levan et al. 2006); or (2) originate at redshifts that make them invisible to us at optical wavelengths (Jakobsson et al. 2004, 2006); or (3) are intrinsically dimmer than average (Fynbo et al. 2001; Rol et al. 2005). No doubt, the truth is some combination of these possibilities. We do not address these questions directly in this paper. Instead, we have tried to estimate the fraction of bursts with afterglows that are reasonably accessible to detection with observatories now in existence. We have developed a fairly simple procedure for using the reported instrumental detection thresholds in conjunction with the actual distribution of detected magnitudes to infer the underlying apparent afterglow optical brightness function.

### 2. OVERVIEW OF ANALYSIS TECHNIQUE

There are now more than 200 *Swift* GRB detections since the launch of this mission on 2004 November 20. The world community of ground-based astronomers has responded with optical observations of essentially all of these events, greatly augmenting the onboard measurements of the *Swift* UVOT camera. From the data that have been reported, principally via the GCN, one can obtain the optical brightness for detected events,  $m_{\text{det}}$ , and the limiting magnitudes,  $m_{\text{lim}}$ , for those that are not. With this primary data, we have estimated the detected and limiting magnitudes at a fixed time of 1000 s postburst and extrapolated the limiting magnitude data to include the detected events as well. For each of these steps, we will demonstrate that the statistical

techniques appear to be quite robust. This is principally due to the fact that the analysis is based solely on cumulative probability distributions for  $m_{\text{det}}$  and  $m_{\text{lim}}$ . Thus, estimation errors for individual events tend to get washed out in the mean as long as gross systematic effects are avoided. It is easy to see that one reason that less than 50% of all bursts have detected optical counterparts is due to the limited sensitivities of the ensemble of instruments that was available at any given time. That can be framed more precisely by assuming that nature has provided some intrinsic optical afterglow luminosity distribution to us on Earth, specified in magnitudes. For each GRB detected by *Swift*, there is one best observational limiting magnitude. The convolution of these two distributions must be the observed distribution of  $m_{\text{det}}$ . This equality can be converted to an optimization problem of finding the best intrinsic afterglow distribution that satisfies this constraint. This estimate is probably the best we can do with the extremely heterogeneous observations that have been reported and the finite statistics of the sample.

### 3. DATA SELECTION AND CORRECTION

The data for the ensuing analysis were collected from 118 *Swift*-identified GRBs that spanned a 447 day period from 2005 February 15 through 2006 May 7. Both the GRB detection magnitudes and limiting magnitudes were subjected to some identical selection criteria and corrections. Foremost, the midpoint of the optical observations were required to lie within a factor of 10 of a nominal postburst time of 1000 s, i.e., between 100 and 10,000 s. Observations were restricted to  $V$  or  $R$  band with unfiltered counting as  $R$ . These restrictions eliminated 10 bursts from further consideration: nine due to the time cut and one due to the observing wavelength ( $K_s$  band). Explicitly, a few events were labeled as nondetections when the only actual detections evaded the allowed time window or filter constraints. All magnitudes were also compensated for galactic absorption using the NASA/IPAC Extragalactic Database Web-based calculator<sup>2</sup> that, in turn, is based on the work of Schlegel et al. (1998). For data taken under  $V$  filters, a further adjustment of  $-0.41$  mag was applied to compensate for the average GRB color difference between  $V$  and  $R$ . This adjustment is the average difference between  $V$  and  $R$  for time periods ranging from 0.2 to 1 days for five GRBs that had

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<sup>2</sup> See <http://nedwww.ipac.caltech.edu/forms/calculator.html>.

many measurements of  $V$  and  $R$  at many different times: 990510 (Stanek et al. 1999), 021004 (Bersier et al. 2003), 050502A (Guidorzi et al. 2005b), 020813 (Covino et al. 2003), and 030329 (Burenin et al. 2003; Rumyantsev et al. 2003; Zharikov et al. 2003). The light curves were characterized by identical power-law decays, so there is no evidence of chromatic variability over these time spans.

Beyond this point, the additional selection criteria for  $m_{\text{det}}$  and  $m_{\text{lim}}$  somewhat diverged. For each of the 43 events with valid detections, the measurement with an observation time logarithmically closest to 1000 s was chosen. The list is displayed in Table 1. (Much of the data for this paper were obtained from the GRBlog Web pages<sup>3</sup> maintained by Quimby et al. [2003], which enormously facilitated this project.) In order to proceed further, we must compare the optical brightnesses at a common postburst time delay.

To make this project work, we needed to establish that it was possible to extrapolate each observed magnitude at  $t$  in the range [100, 10,000] to a fixed time,  $t_c = 1000$  s. Fortunately, there were sufficient data for 37 of the 43 events to extract a power-law exponent,  $\alpha$ , for the temporal behavior of each burst. With these values, we could make a reasonable estimate of  $m_{\text{det}}$  at  $t_c$ . We also performed a similar calculation assuming a *fixed* value for  $\alpha = -0.70$ . The two cumulative probability distributions for the extrapolated values of  $m_{\text{det}}$  are plotted in Figure 1. Application of the Smirnov-Cramér-von Mises test shows that the two distributions are effectively identical (Eadie et al. 1971, p. 268; Kendall & Stuart 1979, p. 474). This gives us some confidence that the same power-law extrapolation is appropriate when the burst afterglows are NOT detected. This is verified by looking at the cumulative distributions of the observation times for the detections and nondetection upper limits (to be described below). This is shown in Figure 2. As expected, the detected events lie close to  $t_c$  by virtue of the imposed selection criteria. The undetected events have no such bias. Nevertheless, their median lies close to 1000 s as well. We can make this more quantitative by comparing the rms average magnitude shifts for the detections and upper limits due to translating from  $t_{\text{burst}}$  to  $t_c$ . With  $\alpha = -0.70$ , the average detected magnitude is shifted by 0.59 when extrapolating from  $t_{\text{burst}}$  to  $t_c$ , while the similar number for upper limits is 1.06. Thus, the estimated cumulative distribution for the upper limits will be somewhat poorer, but the plots in Figure 1 demonstrate that this is unlikely to be significant.

The estimation of the instrumental upper limits for afterglows,  $m_{\text{lim}}$ , is more complex. First of all, very few research groups report  $m_{\text{lim}}$  if there has been a detection. Even if they do, there is a serious bias that will tend to shift  $m_{\text{lim}}$  to greater values: a large telescope is much more likely to observe a GRB if the optical counterpart has already been announced. We have found a slightly devious way to get around these difficulties by using the unbiased limiting magnitude distribution for nondetections to estimate the limiting magnitude distribution for all bursts. For each undetected GRB, all limiting magnitude reports are transformed as if they were detections to  $t_c$ , only requiring an observation time within the [100, 10,000] s window. The maximum magnitude of each set is adopted as  $m_{\text{lim}}$  for that burst; 65 events survived this analysis and are listed in Table 2.

Our task now is to create a distribution of all limiting magnitudes, both detected and undetected, knowing only the values for the undetected. One obvious fact is that the limiting magnitudes for detections will, on average, be deeper. In fact, if a de-

tection is made at  $m_{\text{det}}$ , the value for  $m_{\text{lim}}$  will lie somewhere between  $m_{\text{det}} + \sigma_{\text{det}}$  (where  $\sigma_{\text{det}}$  is the measurement error associated with  $m_{\text{det}}$ ) and the best limiting magnitude ever reported. If  $m_{\text{lim}}$  truly represents the maximum sensitivities for the ensemble of bursts, the simplest tactic is to take the median of the subset of  $m_{\text{lim}}$  in the prescribed range and incorporate that value into the entire set of  $m_{\text{lim}}$ . By performing this recursively over the set of detected GRB afterglows, ordered by decreasing  $m_{\text{det}}$ , one can fill out the otherwise missing entries.

We carried this one step further to better understand the stability of this method. We generated 1001  $m_{\text{lim}}$  distributions using a uniform random number generator to select the interpolated values. For each successive element of  $m_{\text{det}}$ , a modified subset of  $m_{\text{lim}}$  is considered that includes all elements of  $m_{\text{lim}}$  with values greater than  $m_{\text{det}} + \sigma_{\text{det}}$  adjoined to the lower limit value. A uniformly distributed random number then uses the cumulative distribution of the restricted set to select an appropriate random value to be adjoined to  $m_{\text{lim}}$ . In the limit of a large sample of  $m_{\text{lim}}$  distributions, all possible sets for  $m_{\text{lim}}$  will be generated consistent with the constraints imposed by the values for the undetected  $m_{\text{lim}}$  and the detected  $m_{\text{det}}$ . To recover the best estimate for  $m_{\text{lim}}$ , the 1001 distributions were individually ordered by value. To select the 108 elements of  $m_{\text{lim}}$ , the first value was chosen as the median of the set of first values of the 1001 Monte Carlo sets, the second value from the set of second values, etc. A similar procedure defines the first and third quartile distributions. If the distribution of such sets is tightly confined, we have reason to anticipate that this is an adequate approximation of reality. The results are shown in Figure 3. The median distribution lies within tight bounds constrained by the first and third quartiles.

The validity of this procedure was verified by modeling this deconvolution process assuming knowledge of the true  $m_{\text{lim}}$  distribution. For the sake of computational simplicity, the  $m_{\text{lim}}$  cumulative distribution was approximated by a Fermi-Dirac distribution with the two free parameters chosen to best fit the apparent shape inferred from the analysis described above. The  $m_{\text{det}}$  distribution was taken from the four-parameter B-spline representation described in § 4 below. This allowed us to create for  $N$  events, a list of simulated Monte Carlo GRBs with values for the afterglow and limiting instrumental detector magnitudes determined by the two assumed cumulative distributions. Comparing the two values, event by event, generated two subsamples: the “detected” events for which the afterglow was brighter than the instrumental limit and the “undetected” events for which the opposite was true. The Monte Carlo samples reproduced the detected/undetected event ratios essentially exactly. Applying the deconvolution scheme that has been described, we found excellent agreement with the input assumptions for the distribution of  $m_{\text{lim}}$ . One reason for the stability of this technique is the broad dispersion of sensitivities of ground-based instruments reporting results. One measure is the distribution of apertures: it is approximately logarithmic from 0.2 to 8.2 m with  $dN \propto d(\text{aperture})/\text{aperture}$ .

Figure 4 shows the histogram distributions of detected GRBs and the limiting magnitudes for nondetections, both scaled to  $t_c = 1000$  s. The distributions are roughly similar with the latter edging just a bit deeper. Such rough equality is what one might naively expect for the situation in which about half of all events evade detection. Above  $m_R = 19$ , there are twice as many nondetections (29) as detections (14).

#### 4. FINDING THE OPTICAL BRIGHTNESS DISTRIBUTION FUNCTION

The basic idea of this calculation is to specify the apparent optical brightness function by a small set of parameters and, with

<sup>3</sup> See <http://grad40.as.utexas.edu/>.

TABLE 1  
GRB AFTERGLOW DETECTIONS

GRB	R.A.	Decl.	Filter	$A_V$	$A_R$	$\alpha$	$m_{\text{det}}^{\text{a}}$	$t_{\text{burst}}$ (s)	$m_{\text{det}} @ t_c^{\text{b}}$	Reference
050318.....	03 18 51.15	-46 23 43.70	<i>V</i>	0.054	0.043	-0.87	17.80	3230.00	16.445	1
050319.....	10 16 50.76	+43 32 59.90	None	0.036	0.029	-0.88	18.00	1015.00	17.960	2
050401.....	16 31 28.82	+02 11 14.83	None	0.216	0.174	-0.76	18.58	241.35	19.486	3
050406.....	02 17 52.30	-50 11 15.00	<i>V</i>	0.073	0.059	-0.75	19.44	138.00	20.462	4
050416A.....	12 33 54.60	+21 03 24.00	<i>V</i>	0.098	0.079	*	19.38	115.00	20.516	5
050505.....	09 27 03.20	+30 16 21.50	None	0.071	0.057	*	18.40	1009.00	18.336	6
050525.....	18 32 32.57	+26 20 22.50	None	0.315	0.254	-1.23	16.12	1002.30	15.864	7
050607A.....	20 00 42.79	+09 08 31.50	<i>R</i>	0.516	0.416	-1.00	22.50	960.00	22.115	8
050712A.....	05 10 47.90	+64 54 51.50	<i>V</i>	0.753	0.607	-0.73	17.38	959.00	16.249	9
050713A.....	21 22 09.53	+77 04 29.50	<i>R</i>	1.371	1.106	-0.67	21.41	2963.00	19.478	10
050721.....	16 53 44.53	-28 22 51.80	<i>R</i>	0.894	0.721	-1.29	17.93	1484.00	16.909	11
050726.....	13 20 12.30	-32 03 50.80	<i>V</i>	0.206	0.166	0	17.35	173.00	18.067	12
050730.....	14 08 17.13	-03 46 16.70	<i>R</i>	0.168	0.135	-0.54	17.07	1848.00	16.468	13
050801.....	13 36 35.00	-21 55 41.00	None	0.319	0.257	-1.31	16.93	996.00	16.676	14
050802.....	14 37 05.69	+27 47 12.20	<i>V</i>	0.070	0.057	-0.85	18.35	1463.00	17.581	15
050815.....	19 34 23.15	+09 08 47.47	<i>V</i>	1.457	1.175	*	20.00	117.00	19.764	16
050820A.....	22 29 38.11	+19 33 37.10	<i>Rc</i>	0.146	0.118	-0.97	15.42	1146.00	15.198	17
050824.....	00 48 56.05	+22 36 28.50	None	0.116	0.093	-0.55	18.60	1440.00	18.230	18
050908.....	01 21 50.75	-12 57 17.20	<i>Rc</i>	0.083	0.067	-0.93	18.80	900.00	18.813	19
050922C.....	21 09 33.30	-08 45 27.50	None	0.342	0.276	-1.00	16.00	640.00	16.063	20
051109A.....	22 01 15.31	+40 49 23.31	None	0.630	0.508	-0.65	17.59	1004.00	17.079	21
051111.....	23 12 33.36	+18 22 29.53	None	0.537	0.433	-0.74	16.13	1007.00	15.692	21
051117A.....	15 13 34.09	+30 52 12.70	<i>V</i>	0.080	0.065	-0.35	20.01	210.00	20.706	22
051221A.....	21 54 48.63	+16 53 27.16	<i>R</i>	0.227	0.183	-0.93	20.20	4680.00	18.844	23
060108.....	09 48 01.98	+31 55 08.60	<i>R</i>	0.059	0.047	-0.43	21.84	879.00	21.891	24
060110.....	04 50 57.85	+28 25 55.70	None	2.107	1.699	-0.70	17.90	847.00	16.327	25
060111A.....	18 24 49.00	+37 36 16.10	None	0.094	0.076	*	18.30	173.50	19.555	26
060111B.....	19 05 42.47	+70 22 33.10	None	0.368	0.297	-1.08	18.90	792.00	18.780	27
060115.....	03 36 08.40	+17 20 43.00	<i>Rc</i>	0.441	0.356	0.00	19.10	1190.00	18.612	28
060116.....	05 38 46.28	-05 26 13.14	None	0.873	0.704	-1.09	20.78	926.08	20.134	29
060117.....	21 51 36.13	+59 58 39.10	<i>R</i>	4.292	0.010	-1.70	12.62	502.90	13.132	30
060124.....	05 08 25.50	+69 44 26.00	<i>V</i>	0.449	0.362	0.15	16.79	663.00	16.243	31
060203.....	06 54 03.85	+71 48 38.40	<i>Rc</i>	0.514	0.414	-0.90	19.90	3240.00	18.593	32
060204B.....	14 07 14.80	+27 40 34.00	<i>R</i>	0.059	0.048	-0.80	20.40	3096.00	19.493	33
060206.....	13 31 43.42	+35 03 03.60	<i>r'</i>	0.041	0.033	-1.00	17.80	1036.00	17.740	34
060210.....	03 50 57.37	+27 01 34.40	None	0.309	0.249	-1.30	18.12	835.00	18.008	35
060218.....	03 21 39.68	+16 52 01.82	None	0.471	0.380	*	18.09	858.95	17.826	36
060223.....	03 40 49.56	-17 07 48.36	<i>V</i>	0.385	0.311	-0.75	19.60	935.00	18.856	37
060313.....	04 26 28.40	-10 50 40.10	<i>R</i>	0.230	0.186	-0.13	19.90	1134.00	19.618	38
060323.....	11 37 45.40	+49 59 05.50	None	0.050	0.040	*	18.20	540.00	18.628	39
060418.....	15 45 42.40	-03 38 22.80	<i>Rc</i>	0.743	0.599	-1.20	16.47	2412.00	15.202	40
060428B.....	15 41 25.63	+62 01 30.30	None	0.049	0.040	0.05	19.64	1013.00	19.590	41
060502A.....	16 03 42.48	+66 36 02.50	<i>R</i>	0.109	0.088	-0.45	19.80	2400.00	19.047	42

NOTE.—Units of right ascension are hours, minutes, and seconds, and units of declination are degrees, arcminutes, and arcseconds.

<sup>a</sup> The quantity  $m_{\text{det}}$  is the measured magnitude at  $t_{\text{burst}}$  seconds after the GRB trigger.

<sup>b</sup> The quantity  $m_{\text{det}} @ t_c$  is the inferred value for  $m_{\text{det}}$  at  $t_c = 1000$  s after correcting for galactic absorption and average GRB color differences.

REFERENCES.—(1) Still et al. 2005; (2) Quimby et al. 2006b; (3) Rykoff et al. 2005c; (4) Schady et al. 2005a; (5) Klotz et al. 2005a; (7) Klotz et al. 2005d; (8) Pagani et al. 2006; (9) De Pasquale et al. 2006a; (10) Guetta et al. 2007; (11) Antonelli et al. 2006; (12) Poole et al. 2005b; (13) Pandey et al. 2006; (14) Rykoff et al. 2006b; (15) McGowan et al. 2005a; (16) Schady et al. 2005b; (17) Cenko et al. 2006b; (18) Lipunov et al. 2005; (19) Torii 2005a; (20) Rykoff et al. 2005a; (21) Yost et al. 2007; (22) Holland et al. 2005a; (23) Wren et al. 2005; (24) Oates et al. 2006; (25) Li 2006; (26) Klotz et al. 2006a; (27) Klotz et al. 2006b; (28) Yanagisawa et al. 2006; (29) H. F. Swan et al. 2008, in preparation; (30) Jelínek et al. 2006; (31) Romano et al. 2006; (32) Bikmaev et al. 2006; (33) Guidorzi et al. 2006; (34) Monfardini et al. 2006a; (35) Stanek et al. 2007; (36) Quimby et al. 2006a; (37) Marshall et al. 2006; (38) Cobb 2006; (39) Zheng et al. 2006; (40) Koppelman 2006; (41) Li et al. 2006; (42) Cenko et al. 2006a.

this input, estimate the magnitude distribution of detected events modulated by the actual probability of making such a set of measurements with the required threshold sensitivity. By the usual least-squares techniques, the parameter set describing the afterglow brightness function is adjusted so that the predicted distribution of detections closely matches the actual measurements. With that in mind, we originally set out to represent the integral brightness distribution function,  $F(m)$ , by a set of cubic B-splines uniformly spaced over the range of observed magnitudes. Work-

ing with the integral distribution function removes the ambiguity of selecting the binning interval that is implicitly required for defining the associated differential distribution. However, the trade-off is that the representation of the integral distribution must guarantee that the function is monotonic over its entire range. In detail, it was realized that computing  $F$  as a function of the magnitude,  $m$ , led to problems near the endpoints where  $F$  must approach either zero or 1. Inverting the representation so that  $m(F)$  is described by uniform B-splines over the interval, [0, 1], takes care of the

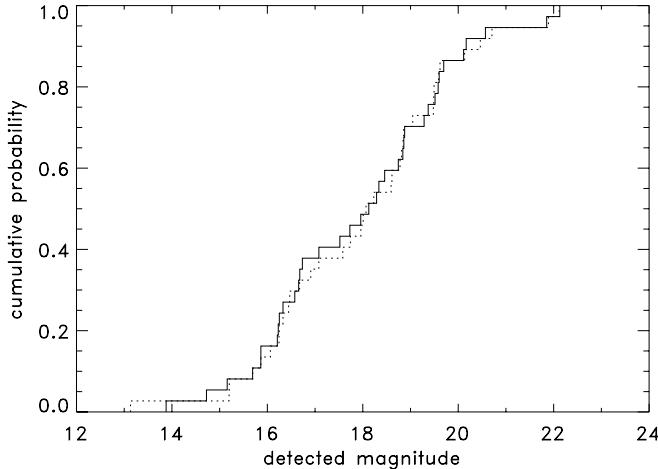


FIG. 1.—Cumulative distributions of afterglow magnitudes for 37 detected GRBs transformed to  $t_c = 1000$  s according to a power-law extrapolation. The solid line shows the distribution using a value of  $\alpha$  computed individually for each burst; the dotted line represents the similar distribution when  $\alpha$  is set to a fixed value of  $-0.70$  for all events. There is no apparent statistical difference between these curves.

endpoint problem nicely, although at the expense of denying solution by linear regression.

Despite some misgivings about poor computational speed, it was found that the downhill simplex minimization method of Nelder & Mead (1965) was quite capable of finding solutions quickly for spline curves defined by up to 7 degrees of freedom. The IDL numerical analysis package<sup>4</sup> was used for these computations, in particular the AMOEBA routine adapted from § 10.4 of *Numerical Recipes in C* (2nd ed.; Press et al. 1992). This approach made it convenient to enforce the monotonicity of the integral distribution function—whenever an evaluation of the goodness-of-fit function was requested with B-spline coefficients leading to zeros or negative values of the distribution function derivative,  $dm/dF$ , the returned value was set to exceed the maximum of all previous values over the simplex. Thus, nonmonotonic integral distributions were easily rejected along with other computational problems.

As sketched above, we fold the estimated detection limiting magnitude distribution with a parametrically defined function describing the true GRB afterglow distribution to predict the observed distribution of actual detections. The starting point for this calculation is the integral distribution of detection upper limits,  $m_{\text{lim}}$ , described earlier. This is a staircase function with uniform vertical steps between irregular intervals,  $\Delta m = m_i - m_{i-1}$ , in which the probability of observing with a given limiting sensitivity,  $p_i \equiv p(m_{i-1} \rightarrow m_i)$ , is uniform. Within each of these intervals of magnitude, the expected number of detected GRB events will increase by an amount,  $\Delta f_i^{\text{calc}} = \Delta F_i p_i$ , where  $\Delta F_i = F(m_i) - F(m_{i-1})$  is the associated change in the optical brightness distribution function over  $\Delta m$ . The sequence of values for  $F(m_i)$  are computed by inversion of the cubic spline representation,  $m(F)$ .

Once the set of  $\Delta f_i^{\text{calc}}$  is constructed, the cumulative probability distribution for the expected number of detected events can be obtained by summation:  $f_i^{\text{calc}} = \sum_j \Delta f_j^{\text{calc}}$ . A trivial modification of this procedure allows one to compute  $f_i^{\text{calc}}$  for the sequence of ordered values of  $m_{\text{det}}$  that characterize the actual GRB detections. The experimentally observed cumulative distribution for these events,  $f_i^{\text{obs}}$ , is just a sequence of rational fractions,

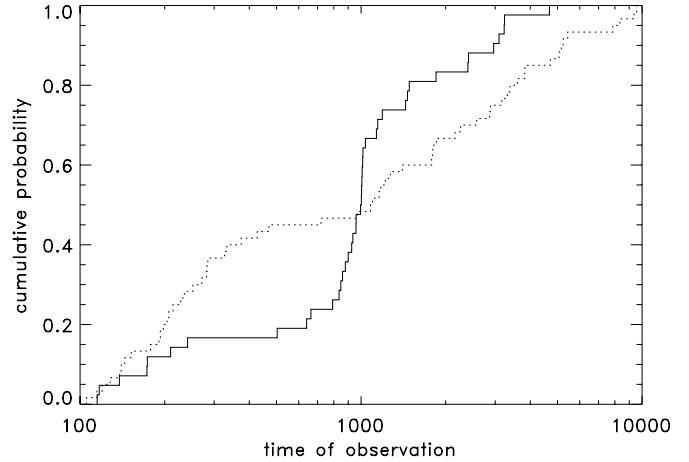


FIG. 2.—Cumulative distributions for the time of observation for detected afterglows (solid line) and undetected afterglows (dotted line) relative to the burst onset. The apparent step function for the detected events at 1000 s is an artifact of the selection criteria. Note that the undetected GRBs have a “best” limiting magnitude at a median time also close to 1000 s. This is not a selection effect.

( $1, 2, 3, \dots, n_{\text{det}}$ )/ $n_{\text{total}}$ , where  $n_{\text{det}}$  is the number of detected GRBs and  $n_{\text{total}}$  is the number of all events considered, detected and undetected alike. The strategy to optimize the shape of  $F(m)$  is now fairly simple: form the differences,  $\delta_i = (f_i^{\text{calc}} - f_i^{\text{obs}})$ , and minimize the sum of squares,  $\sum_i \delta_i^2$ . This last quantity defines the least-squares goodness-of-fit function that drives the downhill simplex routine mentioned previously. The monotonicity of the cumulative distribution function helps ensure the stability of the optimum fit.

## 5. RESULTS AND DISCUSSION

The calculation described above was carried out with 4–7 degrees of freedom for the cubic spline representation, corresponding to dividing the range of  $F$ , [0, 1], into one to four equal segments. The resulting fit is shown in Figure 5 along with the actual GRB detections. The fits are qualitatively excellent.

The corresponding integral distribution function for the apparent optical brightness is shown in Figure 6. The curves all follow the same shape. The range of validity of these curves extends at least to the 90th percentile of the  $m_{\text{det}}$ , 20.5. At this point, the cumulative intrinsic afterglow distribution accounts for 57% of all *Swift*-identified GRBs. The most extreme useful point corresponds to the deepest detection at  $m_{\text{det}} = 22.1$ , where the intrinsic distribution reaches 71%. The remaining 29% may constitute two populations: GRBs inside optically dense regions or at redshifts beyond the Ly $\alpha$  cutoff. Since our statistical method relies on actual detections, the 29% could easily be somewhat lower and details of the high-magnitude afterglow distribution cannot be resolved. Similar conclusions about the population of dim or dark GRBs have been reached by others from far different arguments (Jakobsson et al. 2004, 2006). Thus, the original question of why half or less of all GRBs are optically identified has been resolved by the realization that roughly 25% are lost because they are dimmer than  $m_{\text{det}} \simeq 22$ , and the rest are missed because the available instrumentation is inadequate. This partially answers one of the issues that led us to this analysis, our observations of the afterglow of GRB 060116 (Swan et al. 2006). Within 2000 s, the afterglow became dimmer than  $m_R \sim 22$ , making it an exceedingly difficult target for further measurements. It is apparent that some but not all of the missing optical counterparts are due to such dim but detectable objects.

<sup>4</sup> ITT Visual Information Solutions, ITT Industries, Inc.

TABLE 2  
GRB AFTERGLOW NONDETECTIONS

GRB	R.A.	Decl.	Filter	$A_V$	$A_R$	$m_{\text{lim}}^{\text{a}}$	$t_{\text{burst}}$ (s)	$m_{\text{lim}} @ t_c^{\text{b}}$	Reference
050215A.....	23 13 31.68	+49 19 19.20	None	0.715	0.577	17.40	1080.00	16.765	1
050215B.....	11 37 48.03	+40 47 43.40	<i>V</i>	0.063	0.050	19.50	1797.00	18.582	2
050219A.....	11 05 39.24	-40 40 58.00	<i>V</i>	0.536	0.432	20.70	971.00	19.776	3
050219B.....	05 25 16.31	-57 45 27.31	<i>V</i>	0.109	0.088	19.41	3186.00	18.010	4
050223.....	18 05 32.49	-62 28 21.07	None	0.295	0.238	18.00	2580.00	17.042	5
050306.....	18 49 14.00	-09 09 10.40	None	2.255	1.818	17.50	3600.29	14.708	6
050315.....	20 25 54.10	-42 36 02.20	<i>V</i>	0.159	0.128	18.50	140.19	19.424	7
050326.....	00 27 49.10	-71 22 16.30	<i>V</i>	0.123	0.099	18.91	3313.33	17.467	8
050410.....	05 59 12.90	+79 36 09.20	<i>V</i>	0.369	0.297	19.90	2865.50	18.321	9
050412.....	12 04 25.06	-01 12 03.60	<i>Rc</i>	0.066	0.053	24.90	8336.74	23.235	10
050416B.....	08 55 35.20	+11 10 32.00	r	0.102	0.082	20.00	5160.00	18.671	11
050421.....	20 29 00.94	+73 39 11.40	None	2.693	2.172	18.40	144.29	17.699	12
050422.....	21 37 54.50	+55 46 46.60	<i>V</i>	4.609	3.716	17.90	374.10	13.628	13
050502B.....	09 30 10.10	+16 59 44.30	<i>V</i>	0.098	0.079	21.80	1219.97	21.141	14
050509A.....	20 42 19.70	+54 04 16.20	<i>V</i>	1.981	1.597	18.23	1853.00	15.370	15
050509B.....	12 36 13.67	+28 58 57.00	<i>R</i>	0.064	0.051	21.80	1402.27	21.492	16
050528A.....	23 34 03.60	+45 56 16.80	<i>R</i>	0.533	0.430	20.00	1799.71	19.123	17
050713B.....	20 31 15.50	+60 56 38.40	<i>R</i>	1.548	1.248	21.60	1782.43	19.913	18
050714B.....	11 18 48.00	-15 32 49.90	<i>R</i>	0.181	0.146	20.00	3387.74	18.927	19
050716.....	22 34 20.40	+38 40 56.70	<i>R</i>	0.358	0.289	19.80	228.10	20.634	20
050717.....	14 17 24.90	-50 32 13.20	<i>V</i>	0.786	0.634	18.71	128.00	19.076	21
050724.....	16 24 44.37	-27 32 27.50	<i>V</i>	2.032	1.639	18.84	1663.00	16.011	22
050803.....	23 22 38.00	+05 47 02.30	<i>V</i>	0.246	0.198	18.80	235.01	19.245	23
050813.....	16 07 57.00	+11 14 52.00	<i>V</i>	0.185	0.149	18.15	152.00	18.987	24
050814.....	17 36 45.39	+46 20 21.60	<i>V</i>	0.093	0.075	18.00	217.00	18.658	25
050819.....	23 55 01.20	+24 51 36.50	<i>R</i>	0.406	0.327	21.60	7864.99	19.706	26
050820B.....	09 02 25.03	-72 38 44.00	<i>R</i>	0.417	0.336	15.30	4716.00	13.785	27
050822.....	03 24 26.70	-46 02 01.70	<i>V</i>	0.049	0.040	19.50	138.24	20.545	28
050826.....	05 51 01.58	-02 38 35.80	<i>V</i>	1.944	1.568	19.00	155.00	18.063	29
050904.....	00 54 50.79	+14 05 09.42	<i>V</i>	0.200	0.161	18.90	214.00	19.462	30
050906.....	03 31 11.75	-14 37 18.10	<i>R</i>	0.220	0.177	19.70	470.02	20.097	31
050911.....	00 54 37.70	-38 50 57.70	<i>R</i>	0.034	0.028	21.00	2160.00	20.387	32
050915A.....	05 26 44.80	-28 00 59.27	<i>R</i>	0.086	0.070	21.00	1098.14	20.859	33
050915B.....	14 36 26.50	-67 24 36.50	<i>V</i>	1.292	1.041	21.40	9360.00	17.998	34
050922B.....	00 23 13.20	-05 36 16.40	<i>V</i>	0.122	0.098	20.10	3169.50	18.691	35
050925.....	20 13 54.24	+34 19 55.20	<i>R</i>	7.510	6.056	19.00	197.86	14.175	36
051001.....	23 23 48.80	-31 31 17.00	<i>R</i>	0.051	0.041	21.50	1175.90	21.336	37
051006.....	07 23 13.52	+09 30 24.48	<i>V</i>	0.218	0.176	18.80	207.00	19.369	38
051008.....	13 31 29.30	+42 05 59.00	<i>R</i>	0.039	0.031	22.60	3822.34	21.550	39
051016.....	08 11 16.30	-18 17 49.20	<i>V</i>	0.293	0.236	19.10	114.91	20.041	40
051016B.....	08 48 27.60	+13 39 25.50	<i>Rc</i>	0.123	0.099	15.70	105.41	17.311	41
051021B.....	08 24 11.80	-45 32 30.80	<i>V</i>	3.852	3.106	19.00	178.00	16.050	42
051105.....	17 41 03.28	+34 59 03.60	<i>V</i>	0.112	0.090	20.00	9566.50	17.762	43
051109B.....	23 01 50.21	+38 40 46.00	<i>R</i>	0.557	0.449	21.00	5436.29	19.264	44
051117B.....	05 40 43.00	-19 16 26.50	<i>R</i>	0.185	0.149	20.80	2885.76	19.846	45
051221B.....	20 49 35.10	+53 02 12.20	<i>R</i>	4.543	3.663	18.20	281.66	15.500	46
051227.....	08 20 58.11	+31 55 31.89	<i>Rc</i>	0.140	0.113	17.70	3944.16	16.544	47
060105.....	19 50 00.60	+46 20 58.00	<i>V</i>	0.568	0.458	18.00	191.00	18.280	48
060109.....	18 50 43.50	+31 59 29.70	<i>V</i>	0.478	0.386	19.00	204.00	19.320	49
060202.....	02 23 22.88	+38 23 04.30	<i>R</i>	0.157	0.126	21.50	252.29	22.421	50
060211A.....	03 53 32.80	+21 29 21.00	<i>V</i>	0.637	0.514	19.00	283.00	18.912	51
060211B.....	05 00 17.20	+14 56 58.90	<i>R</i>	1.349	1.088	22.10	2257.63	20.393	52
060219.....	16 07 21.10	+32 18 56.30	<i>V</i>	0.108	0.087	18.60	120.10	19.693	53
060223B.....	16 56 58.80	-30 48 46.00	<i>R</i>	1.301	1.049	13.70	326.59	13.501	54
060306.....	02 44 23.00	-02 08 52.80	<i>V</i>	0.118	0.096	18.40	193.00	19.122	55
060312.....	03 03 06.12	+12 50 03.50	None	0.585	0.472	18.30	1270.94	17.646	56
060319.....	11 45 33.80	+60 00 39.00	<i>R</i>	0.073	0.059	21.00	5238.43	19.682	57
060403.....	18 49 21.80	+08 19 45.30	<i>V</i>	4.251	3.428	19.25	5066.50	13.356	58
060413.....	19 25 07.70	+13 45 27.30	<i>V</i>	6.472	5.219	19.20	1160.00	12.205	59
060421.....	22 54 32.63	+62 43 50.07	<i>V</i>	4.236	3.416	17.70	285.00	14.008	60

TABLE 2—Continued

GRB	R.A.	Decl.	Filter	$A_V$	$A_R$	$m_{\text{lim}}^{\text{a}}$	$t_{\text{burst}}$ (s)	$m_{\text{lim}} @ t_c^{\text{b}}$	Reference
060427.....	08 17 04.40	+62 40 18.30	<i>V</i>	0.165	0.133	18.50	333.00	18.761	61
060428A.....	08 14 10.98	-37 10 10.30	<i>V</i>	4.128	3.328	19.10	271.00	15.554	62
060501.....	21 53 29.90	+43 59 53.40	None	0.951	0.767	17.40	426.82	17.280	63
060502B.....	18 35 45.89	+52 37 56.20	None	0.145	0.117	20.00	719.71	20.133	64
060507.....	05 59 51.70	+75 14 56.60	<i>R</i>	0.514	0.414	19.20	3828.38	17.766	65

NOTE.—Units of right ascension are hours, minutes, and seconds, and units of declination are degrees, arcminutes, and arcseconds.

<sup>a</sup> The quantity  $m_{\text{lim}}$  is the magnitude upper limit at  $t_{\text{burst}}$  seconds after the GRB trigger.

<sup>b</sup> The quantity  $m_{\text{lim}} @ t_c$  is the inferred value for  $m_{\text{lim}}$  at  $t_c = 1000$  s after correcting for galactic absorption and average GRB color differences.

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While recognizing that differentiation amplifies errors, it is still useful to look at the differential GRB afterglow magnitude distribution determined directly from the cumulative distribution discussed above. As shown in Figure 7, a peak appears at  $m_{\text{det}} \approx 19.5$ , which is only slightly displaced from the peak in the actual observed  $m_{\text{det}}$  distribution. One might argue that statistical errors in evaluating  $m_{\text{lim}}$  could shift this somewhat rightward, but unitarity puts limits on how much further the integral distribution can rise without changing slope. Thus, the overall behavior of the apparent GRB afterglow distribution is likely to follow closely the curves shown. Some caution should be exercised about over-interpreting the physical significance of this peak. Since the Burst Alert Telescope (BAT) detector on *Swift* operates in flux-limited mode, cutoffs at low brightness may simply be a reflection of a proportional correlation to lower fluxes in  $\gamma$ -rays.

We have described a statistical analysis of GRB optical afterglows that has attempted to obtain the brightness distribution

for observers on Earth to better understand the population of dimmer events and the criteria for improving such investigations. By including the distortion effects of instrumental characteristics and by comparing at a time accessible to almost all observers, our results are largely biased only by the trigger threshold of the BAT detector on board *Swift*. A rather different approach has been attempted by two groups during the past 2 years (Gendre & Boér 2005; Nardini et al. 2006a, 2006b). Their aim is to find discriminants that would identify subclasses of GRB events by translating observed fluxes to the rest frame of the GRB. In particular, Nardini et al. have found that by using those events with redshift information, they could project the optical flux in *R* band back to the GRB rest frame at a proper time of 12 hr. For a typical burst with  $z \sim 2$ , this corresponds to an observation 1.5 days following the burst trigger,  $\sim 100$  times greater than the value of  $t_c$  of 1000 s employed in our analysis. At this late epoch, they find that the majority of events are clustered in luminosity with a standard deviation of 0.70 mag. A low-luminosity population is also identified as a minority constituent of an apparently bimodal distribution

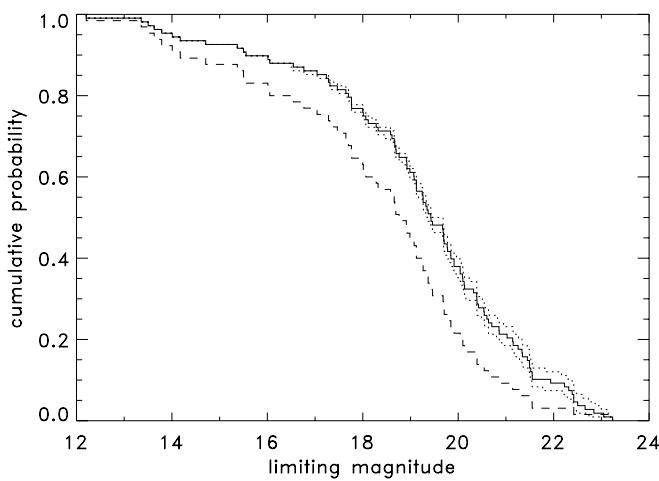


Fig. 3.—Cumulative distribution for observation limiting magnitudes. The dashed line corresponds to the distribution for the best sensitivity for each nondetection; the solid line is the estimate obtained for all observations, both detections and nondetections, using the iterative technique described in the text. The dotted lines show the first and third quartile distributions obtained in the Monte Carlo process. These clearly bracket the median quite closely.

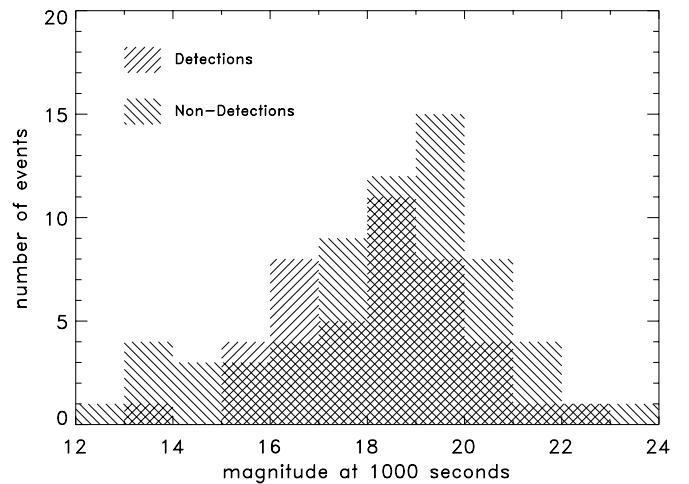


Fig. 4.—Histogram of GRB optical afterglow detections and nondetections transformed to  $t_c = 1000$  s. Despite a large overlap region, a substantial number of nondetections occur at limiting magnitudes deeper than most detections.

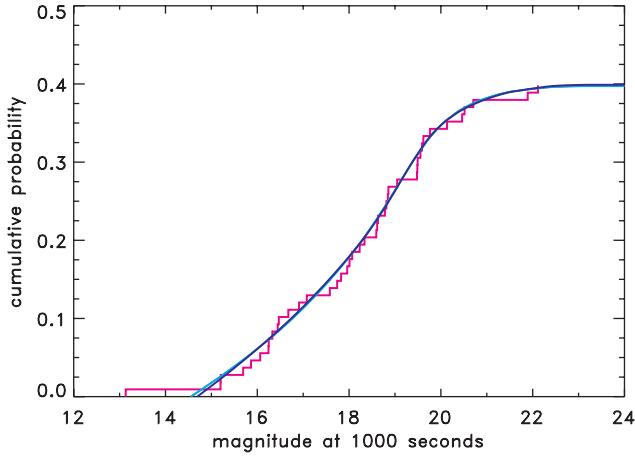


FIG. 5.—Cumulative distribution of detected GRB optical afterglows. The violet “staircase” line shows the experimentally observed distribution. The least-squares estimates are shown in red, green, cyan, and blue, corresponding respectively to 4, 5, 6, and 7 degrees of freedom of the B-spline representation.

and exhibits a factor of 15 lower flux. In their most recent paper, they include 25 *Swift* bursts, of which 17 are referenced in this present paper. The high-flux fraction of Nardini events has a mean observer frame brightness about 1 mag greater than our entire detection sample, while the low-flux cluster, with only four events, is statistically indistinguishable. Given the different methods and goals of the Nardini analysis, no further comparison is likely to be meaningful.

## 6. IMPLICATIONS FOR FUTURE GRB OBSERVATIONS

Observations of GRBs are difficult and expensive primarily because of the reliance on large X-ray and  $\gamma$ -ray detectors in space such as *Swift* and *GLAST*, each of which costs a good fraction of a billion dollars. Recent history has shown that multiwavelength observations considerably enhance the amount of information about these elusive events. At the present time, we still do not have a definite theory of the energy transport within a GRB jet—it could be baryonic,  $e^\pm$  pairs, or electromagnetic Poynting flux.

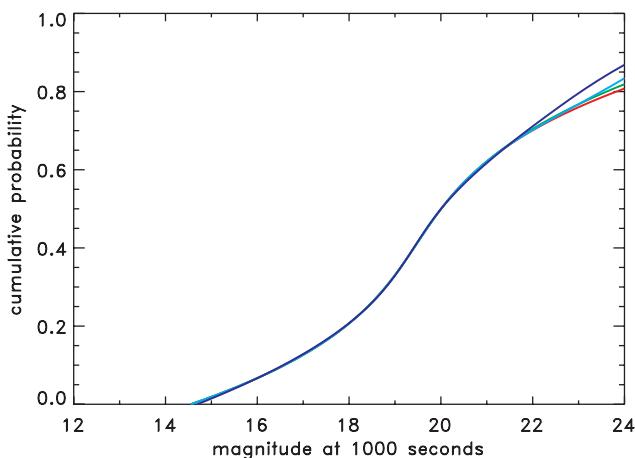


FIG. 6.—Intrinsic cumulative GRB apparent optical afterglow distribution. The colors, red, green, cyan, and blue, correspond respectively to B-spline curves with 4, 5, 6, and 7 degrees of freedom. Crudely speaking, 71% of all GRB afterglows have  $m_R < 22.1$  at  $t_{\text{obs}} = 1000$  s, the dimmest GRB optically detected.

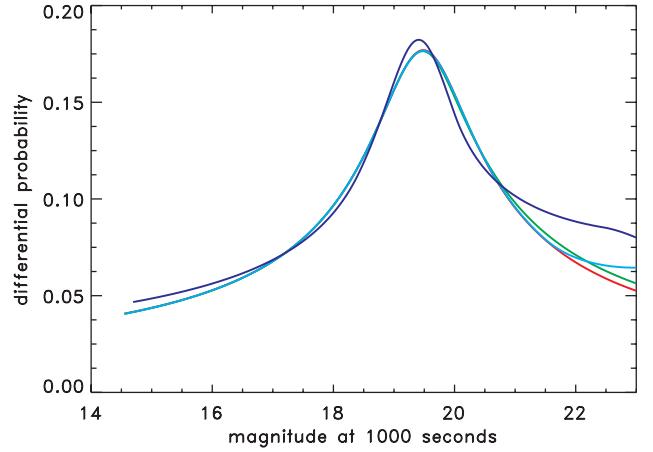


FIG. 7.—Differential GRB apparent optical afterglow distribution. The colors, red, green, cyan, and blue, correspond respectively to B-spline curves with 4, 5, 6, and 7 degrees of freedom. The peak at  $m_{\text{det}} \approx 19.5$  seems to be an unavoidable feature.

Many hope that if GRBs are better understood, they could help improve our understanding of the early star formation period of our universe. In any case, research is bound to continue in this area for many years to come, although launching of new space missions dedicated to GRBs will likely be infrequent. The analysis in this paper suggests that a natural threshold sensitivity for optical observations of *Swift*-detected bursts is  $m_R \approx 20$ . The data gathered for this paper show that such levels are routinely achieved by 2 m telescopes. The cost of such instruments is in the neighborhood of \$5 million, especially if purchased in multiple units. The total number of such units can be gauged by the following simple argument: the sky is dark above any specific site for about 1/3 of the day, a randomly detected GRB will be at an immediately accessible zenith angle about 1/3 of the time, and the weather at a good site will be suitable with probability of 3/5. The joint probability of all three independent conditions is 1/15, implying that optimal coverage is achieved with  $\approx 15$  instruments globally distributed around the Earth. The overall optical detection probability is modified to some extent by details of  $\gamma$ -ray detector pointing constraints. Clearly, a number of areas on Earth are already well populated with research-grade telescopes, particularly Chile and southwestern United States. Many parts of the world are not so well blessed. Some nations such as Thailand and Iran have recognized the scientific niche for observing optical transients and expect to install 2 m optical telescopes within a few years. That still leaves a number of sites in Asia and elsewhere that could successfully enhance global coverage of rare phenomena such as GRBs. An alternative is to launch rapid-response optical/IR telescopes in space that would obviate the need for ground-based facilities. Unfortunately, the cost of even a modest 1/2 m aperture telescope far exceeds installing two dozen much larger instruments located on Earth.

Any instrument dedicated to GRB optical afterglow detection must be robotic, with a slew time of tens of seconds in order to maximize the time overlap with the most variable periods of X-ray and  $\gamma$ -ray emission. Such a telescope would be more useful for a broader range of research if the field of view (FOV) can be kept large, at least a square degree. The best example for this argument is the Sloan Digital Sky Survey, whose telescope primary has an aperture of 2.5 m and a FOV of  $1.5 \text{ deg}^2$ . To complete this picture, the imaging focal plane could be populated with a  $2 \times 2$  array of large format silicon CCDs. This would be even more

useful if the instrument could operate as a two-band system with a dichroic splitter to separate *R* band and *I* or *J* band to two different cameras. Such multiband coverage might better elucidate the origin of “dark” bursts, whether hidden by optical extinction of dense molecular clouds or redshifted and destroyed by Ly $\alpha$  absorption edges. Instruments such as described above run counter to the current government funding trend to shut down many 2 m telescopes in favor of fewer but more powerful 8 m class and larger. Such policies work well for the majority of astronomical objects that evolve exceedingly slowly with time but are inappropriate for relatively rare events with durations of minutes or seconds. It also behooves agencies such as NASA that fund

space missions to help organize ground-based programs that will optimize the entire scientific return on investment.

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