

A synoptic-dynamic model of subseasonal atmospheric variability

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ABSTRACT

A global synoptic-dynamic model (GSDM) of subseasonal variability is proposed to provide a framework for real-time weather-climate monitoring and to assist with preparation of medium range (e.g., week 1-3) predictions. The GSDM is used with a regional focus over North America during northern winter. A case study introduces the time scales of the GSDM and illustrates two circulation transitions related to eastward moving wave energy signals and their connection to remote tropical forcing. Global and zonal atmospheric angular momentum (AAM) is used to help define the synoptic evolution of the GSDM components and to link regional synoptic variations with physical processes like the global mountain and frictional torque. The core of the GSDM consists of four stages based on the Madden-Julian Oscillation (MJO) recurrence time. Additionally, extratropical behaviors including teleconnection patterns, baroclinic life cycles and ~monthly oscillations, provide intermediate and fast time scales that are combined with the quasi-oscillatory (30-70 day) MJO to define multiple time/space-scale linear relationships. A unique feature of the GSDM is its focus on global and regional circulation transitions, and the related extreme weather events during periods of large global AAM tendency.

1. Introduction

a. Background

Synoptic models of atmospheric phenomena and dynamical or physical processes have been used extensively to communicate the results of diagnostic research and help develop the science and art of weather forecasting. The extratropical cyclone and its baroclinic-barotropic life cycle is the most well known subject of synoptic modeling in meteorology. It has been studied with numerical models and observed datasets for more than 70 years (e.g., Bjerknes 1919; Haynes 1940; AMS 1999). Coherent and easily recognized, the behavior of baroclinic waves is the “bread and butter” of short-term prediction models, which have very good forecast skill in the 1-3 day range, at least on average (Simmons and Hollingsworth 2002).

No comparable synoptic model exists for subseasonal (3-90 days) variability and medium-range predictions. In fact, several additions to the baroclinic life cycle model would be required to construct a “useful” medium-range synoptic model. For one, the regional domain of the short-term prediction problem is no longer viable for the medium range (e.g., Smagorinsky 1967). Wave packets or other organized atmospheric energy pulses can spread signals from regional interactions around the hemisphere in < 10 days (Chang 1993; 1999a,b). The inherent scales of motion are also larger, in particular encompassing zonal wavenumbers 0-3. In the time domain the model should consist of multiple time scales and their interaction in time and space. In terms of coherent phenomena, the quasi-oscillatory Madden-Julian Oscillation (MJO; Madden and Julian 1971, 1972, 1994) is a viable candidate to provide structure to a global subseasonal synoptic model in the same way ENSO does for interannual variability. But the MJO is far from adequate by itself. Extratropical phenomena must also be included.

Historically, the most well known extratropical variations are baroclinic waves, “blocking” and zonal index cycles (e.g., Namias 1954). The latter involve hemispheric variations between blocked and strong zonal flows. In modern times, teleconnection patterns (Wallace and Gutzler 1981, hereafter WG; Branstator 1992) have been emphasized and recognized as a general mode of circulation variability, of which blocking is a special case (Dole 1986, 2006). More recently zonal mean or “annular” modes of variability are again being highlighted in diagnostic studies, especially those based on surface pressure or height (Thompson and Wallace 2000). Studies of the evolutionary behavior of zonal mean anomalies have revealed episodes of coherent propagation all the way from equatorial regions to high polar latitudes (Feldstein 2001). In the southern hemisphere, the MJO’s quasi-stationary wave component (Weickmann et al. 1997; hereafter WKS) and a midlatitude component forced by baroclinic waves (e.g., Lorenz and Hartmann 2003) likely contribute to such episodes.

Although spatial differences are important, all these phenomena tend to be characterized by 5-10 day decay time scales (Feldstein 2000) and by large zonal scales. Studies have sought to explain such low frequency phenomena in terms of multiple equilibria (e.g., Charney and DeVore 1979) or normal modes (Simmons et al, 1982) although current evidence suggests forcing helps determine their time behavior (Newman et al. 1997). Prominent forcing is supplied by the MJO, topography, the storm tracks and sea surface temperature variations. A representative component from this class of red noise processes will make up the intermediate time scale of the GSDM. We specifically focus on a large scale disturbance that develops over the Pacific-North American sector

in association with orographically perturbed flow over eastern Asian and western North American mountains and will refer to the phenomenon as the “ τ_F - τ_M index cycle¹”. Regionally it includes teleconnection patterns like the Pacific North American pattern (PNA; WG). Weickmann (2003, hereafter W03) has studied its synoptic evolution and Weickmann et al (2000, hereafter WRP) argue it is the dominant mode of AAM exchange and anomaly decay on intermediate subseasonal time scales.

The fast baroclinic life cycle has been studied for various background flows and meridional shears (Simmons and Hoskins 1978, 1979, 1980). Disturbance growth, phase propagation, energy dispersion and breaking are prominent features of such studies (Thorncroft et al. 1993; Whitaker and Sardeshmukh 1998), and of the observed atmosphere. Regional baroclinic wave breaking (Neilsen-Gammon 2001) in particular produces a rapid meridional momentum exchange that influences even the zonal mean zonal wind. The residual of breaking waves has recently been linked with the initiation of teleconnection patterns like the North Atlantic Oscillation (NAO, Franzke et al. 2004). The fast time scale of the GSDM will focus on wave energy dispersion that accompanies baroclinic developments and their interaction with the major mountain ranges.

Specifically, synoptic-scale wave energy dispersion within the northern and subtropical waveguides over Asia and the Pacific Ocean (Hoskins and Ambrizzi, 1993; Chang, 2005) will represent the model’s fast time scale. The process is linked with 10-30 day oscillations of the circulation, which have been observed throughout the atmosphere. Wave retrogression at high northern latitudes (Branstator 1987), mountain torques over Asia and North America, (Lott et al. 2001; Lott and D’Andrea 2005), equatorial convectively-coupled Rossby and Kelvin waves (Wheeler et al. 2000) and monsoon oscillations (Hartmann et al. 1992) all display coherent behavior on this time scale. This component can be energetic for an extended time period as during the 1996-97 rainy season over central California (Mo 1999). The specific ~25 day oscillation represented in the GSDM involves subtropical flow variations, a likely candidate for the behavior described by Mo (1999). Mo (2001) has incorporated the intermediate time scale explicitly into the week 1-3 prediction process.

The GSDM organizes these multiple subseasonal phenomena into a repeatable sequence. The relationship among the time scales is based on maximizing global and zonal AAM anomalies. The GSDM emphasizes four primary stages but the duration of the cycle and the days between stages are variable. The model is valid during persistent forcing by sea surface temperature (SST) anomalies as well as during the time-varying MJO. In fact, two of the stages represent behavior observed also during El Nino and La Nina events. The GSDM is similar to using composites of El Nino-Southern Oscillation (ENSO) or MJO for real time monitoring or seasonal or weekly predictions, although we seek to explain and account for more variance through the multiple time scale approach.

A dynamical underpinning for the model is atmospheric angular momentum (AAM), which is determined by the three-dimensional distribution of atmospheric zonal wind and

¹ A zonal index fluctuation with a broad anomaly center in the tropics (30N-30S) and an opposite signed anomaly at 50N. The pattern is amplified and extended in time by the meridional transports of AAM associated with Rossby wavetrains that induce a large Northern Hemisphere mountain torque. The zonal wind anomalies eventually decay via the frictional torque.

mass (Peixoto and Oort 1992). Its global integral is an excellent index of ENSO, the MJO and other subseasonal variability. Moreover, processes that change global AAM; i.e., the frictional torque and the mountain torque, have medium and fast time scales, respectively (WRP). Thus indices involving these processes are used to define the components of the GSDM. WRP show the mountain torque forces AAM anomalies and the frictional torque damps them (Egger and Hoinka 2002), and this will be evident in the GSDM. Atmospheric dynamics linked with wave growth and dispersion processes, connect the mountain source regions of AAM anomalies with the subtropical frictional sink regions. The latter tend to occur near the seasonally-varying zero zonal wind line. The torques are produced by a variety of known, large-scale patterns of wind and pressure as described by WRP and W03.

There are two primary motivations for the synoptic modeling effort. The first is scientific understanding of the evolving atmospheric circulation with a practical goal of attribution of weather-climate anomalies. Diagnostic tools and analysis results derived from the science and research side are used on the monitoring and prediction side to examine cause and effect or attribution of weather-climate variations. The application of diagnostics to actual forecasting is mostly neglected in meteorology due to strong reliance on numerical forecast models and lack of a useful synoptic framework. The second motivation is daily monitoring of the circulation to evaluate numerical model predictions in the subseasonal band including the potential predictability of transitions of the circulation and of extreme weather events. Extreme events of global AAM are used as a framework within the GSDM. The specific intent is to target the boundary between weather and climate, which encompasses the transition from deterministic to probabilistic forecasts. An evaluation of numerical forecasts based on synoptic reasoning is expected to add value because there are well-known, stubborn model errors, particularly in the prediction of tropical convection (Lin et al. 2005) and the subsequent circulation response.

Section 2 introduces aspects of the GSDM with a case study presentation of the 2001-02 northern winter season. Two rapid transitions of the circulation involving tropical-extratropical interaction, and the predictive skill of an ensemble forecast model out to day 15 are described. The derivation of the GSDM is then presented in Section 3. The evolving circulation anomalies of the different components of the synoptic model are organized using a linear superposition based on the time tendency of global relative AAM. Summary and conclusions follow in Section 4.

2. A Case Study: December-February 2001-02

The purpose of this case study is to introduce phenomena and variability that will be used to construct the GSDM. Two transitions of the circulation will be examined that occur in association with two moderate MJOs. The case begins in a low AAM state typical of a La Nina circulation regime. A transition then occurs to a high AAM state typical of El Nino and the case ends with a transition back to a La Nina state. The use of the ENSO cycle to describe subseasonal variations of the circulation and convection emphasizes the strong similarity between the response to tropical convection on interannual and subseasonal time scales. In fact, Stages 1 and 3 of the GSDM, which is introduced in the next section, closely resemble the well-known La Nina and El Nino circulation anomalies, respectively. In the following, when we will refer to Stage 1 and

Stage 3, the reader should know what we mean. The other outstanding forcing during the case was by the mountain torque, which represented the other two time scales of the GSDM reasonably well. The fast time scale will be obvious but the intermediate time scale is represented because regressions on the daily frictional torque closely resemble regressions on 5-7 day means of the mountain torque (not shown). To focus the study, the roles of the MJO convective signal, the midlatitude mountain torque and synoptic scale wavetrains are described during two transitions of the large scale flow.

The MJO activity during 2001-02 not only influenced the tropical convection and circulation during the study period but also the SST anomalies in the tropical Indo-Pacific Ocean. SST anomalies were recovering from a series of weak to moderate La Ninas in the previous three years and, during northern fall 2001, positive SST anomalies were found in the tropical west Pacific Ocean. The first MJO during November 2001 helped force a further eastward shift of the ocean warm pool toward the date line. This SST change led to a “regime” of ~25 day tropical convective variability over the west Pacific Ocean, a good example of the behavior described by the <30 day filtered global relative AAM tendency used in the GSDM.

a. Tropical Convection

The two MJOs are shown in a time-longitude format in Fig. 1. MJO#1 forms over the Indian Ocean in November 2001, shifts to the west Pacific in early December 2001 and stalls west of the date line. The stalling may reflect a feedback from the eastward shift of warm ocean water cited above. MJO#2 forms over the Indian Ocean in mid-January 2002 and reaches the date line in mid-February. It contains more Kelvin and equatorial Rossby wave activity than MJO#1 and has its convective signal south of the equator for most of February 2002 (see Fig. 1). Both MJOs have significant amplitude in the filtered field, especially at ~120E. Using this longitude as a reference gives a recurrence interval of 65 days, which is on the long end of the MJO period range.

To start the process of telescoping to the two transitions and their link to MJO-related convective forcing, seven numbers have been marked on Fig. 1. These numbers “sample” rapid changes within the two MJOs’ convective envelope and in the ~25 day quasi-oscillation along 160E. They will be referred to as “tropical convective flare-ups”. The dates for the flare-ups were determined from a time series of the first two EOFs of 20-100 day filtered OLR anomalies (shown below). The two GSDM transitions are associated with flare-ups 3 and 5. T1 represents the transition to Stage 3 (i.e., like El Nino) when MJO 1 is located over the west-central Pacific and T2 is the transition to Stage 1 (i.e., like La Nina) when MJO 2 is over the Indian Ocean. Table 1 gives the calendar dates corresponding to the numbered events and the two transitions. Although only flareups 3 and 5 are studied in what follows, the other cases also produced regional and downstream transient impacts on the atmospheric circulation and on weather producing disturbances.

b. Midlatitude 250-mb meridional wind

The midlatitude circulation anomalies that accompany the tropical OLR signal are depicted using a daily time-longitude plot. Fig. 2 shows the 250mb meridional wind anomalies averaged between 30-60N and depicts: a) signatures of storms in the storm track regions, b) energy dispersion in midlatitudes regions and c) slow, quasi-oscillations

in the midlatitude meridional wind pattern. The latter will be discussed in terms of the implied geopotential height anomalies, which are marked on the figure. These height patterns involve ridging near 150W (Hs) during the first half of December 2001, troughing in the same location (Ls) during the rest of December into early January 2002, and a return to ridging (Hs) in mid-January to early February 2002. Each persistent episode includes 3-5 synoptic scale events whose ridges and troughs tend to develop or amplify at the same longitude. The synoptic events have been numbered for each persistent “regime”.

The boundaries of T1 and T2 are marked on Fig. 2 and a wavetrain that extends from 120E to 90W is highlighted during each transition. The wavetrains are linked with retrogression of existing anomalies (red arrows) and are followed by a series of similar synoptic events. After T2 and the return of ridging to the eastern North Pacific, the synoptic activity is more spatially variable than during Stage 3. It also includes a slow westward drift of circulation anomalies (light dashed lines) during the time positive tropical convection anomalies are over the Indian Ocean and Indonesia. The final synoptic regime seen in Fig. 2 is a progressive one (light solid lines), which coincides with the return of convection to the date line around 12 February 2002.

c. Low frequency indices and their forcing

Fig. 3 shows indices that capture the low frequency (> 10 day) variations described in Fig. 2, and illustrate the atmospheric response to tropical diabatic heating and orographic forcing to be detailed later. The indices include: a) the global integral of AAM, b) the first EOF of the combined 200/850 mb vector windfield (with the zonal mean removed) and c) the PNA teleconnection pattern. These represent global, hemispheric-subtropical and regional anomaly patterns respectively. All have similar low frequency behavior; i.e., minima in early December 2001 (day 30), maxima in late December, early January 2002 (day 60) and back to minima in late January 2002 (day 80). The center of transitions T1 and T2 are again marked on the curves. The PNA slightly lags the other curves, which is consistent with a signal that starts in the tropics, expands to the subtropics and eventually effects the regional circulation over the midlatitude Pacific Ocean.

The time series of processes that can force these changes are shown in Fig. 4. Fig. 4a shows the first EOF of the zonal mean mountain (red) and frictional torque (blue) over the northern hemisphere. EOF 1 of the mountain torque (not shown) is a monopole pattern between 20-60N and EOF1 of the frictional torque (not shown) is a north-south shift in the winter mean boundary of the surface westerly flow. Fig. 4b shows coefficients of the first two EOFs of OLR, which describe an eastward movement of the MJO. The convective flareups numbered in Fig. 1 (see also Table 1) were derived from these OLR EOFs and are also marked.

These forcing time series have some distinct low frequency behavior in addition to the rapid convection changes see in Fig. 4b and the highly variable synoptic component seen in the mountain torque time series of Fig. 4a. From Fig. 1, a 65-day recurrence interval for MJO convection was estimated for 120E and this is marked at the bottom of each panel on Fig. 4. Negative values of OLR EOF2, seen at the endpoints of the interval, signify that indeed convection is located over Indonesia at these times. More generally OLR EOF1 (red) leads EOF2 (blue) consistent with eastward propagation of anomalies.

Another low-frequency behavior marked on Fig. 4a is a 50-day recurrence interval in the midlatitude mountain torque (Lott et al., 2001). The frictional torque (Fig. 4a) acts to damp angular momentum anomalies forced by the mountain torque but it is also involved in producing the MJO AAM signal. In the GSDM the MJO, the intermediate ~ 6 day decay time scale and the 10-30 day oscillation can contribute to circulation anomalies during Stages 1 and 3. These phenomena are difficult to disentangle since in all a positive mountain torque is followed by a negative friction torque and vice versa. A section of each time series has been highlighted with a dotted line that shows this lag relationship for a ~ 50 -day oscillation. It is perhaps clearest after T2. Namely, as the large negative mountain torque removes westerly momentum from the atmosphere, easterly wind anomalies and a positive friction torque develop. This slowly removes easterly momentum from the atmosphere, thereby bringing AAM back into temporary balance. It is during this damping process that circulation anomalies of interest to monitoring and prediction occur, in this case a negative PNA. Another example but with opposite sign is also highlighted during December 2001 on Fig. 4a with two black arrows.

The location of T1 and T2 are marked with shading on Fig. 4. The transitions follow closely after the very large positive and negative maxima in the mountain torque anomaly, which are embedded in strong daily variability as synoptic systems move over the topography. Asian-Europe topography is a strong contributor to both the positive and negative anomaly while North American topography contributes primarily to the later negative anomaly (not shown). The mountain torque events are linked with amplification of a baroclinic wave downstream over the North Pacific. During T1, the amplifying wave leads to a cyclonic wave break over the east Pacific that brings westerlies south and ushers in Stage 3. The opposite happens during the transition to Stage 1.

Fig. 4b shows the transitions occur 5-10 days after flareup 3 and 1-3 days after flareup 5. This suggests a loose relationship between rapid transitions in the circulation and the sudden shift of convection within the MJO convective envelope. In this case it is the midlatitude mountain torque that is more directly linked with both transitions. However, the persistence of tropical forcing, as represented by the horizontal bars on the EOF1 OLR time series, undoubtedly contributed to the persistence of the resulting large-scale circulation anomalies.

d. Synoptic maps during circulation transitions

Fig. 5 shows selected daily maps of 150mb vector wind anomaly during T1. The key anomalies from an MJO perspective are suppressed convection over the Indian Ocean and active convection near the date line (not shown but see Fig. 1). Early in the sequence (Fig. 5a, b) a wavetrain is evident across the Indian Ocean/south Asia with a trough near 20N, 70E. The trough is quasi-stationary and eventually evolves into a large cyclonic anomaly covering the entire region (Fig. 5f). The MJO at this stage helps force the trough and set the phase of a wavenumber 5-6 wavetrain through which energy flows eastward. Another more stationary wavetrain farther north (60N) combines with the subtropical wavetrain over the midlatitude North Pacific in Fig. 5b, which precedes the wave amplification over the west Pacific seen in Figs. 5d-f. The phase of the amplifying couplet west of the date line is consistent with the orographic response to a positive mountain torque (W03). Baroclinic processes and upper level outflow from the tropical

convection near the date line help the amplification process. By Fig. 5f, the downstream low over the northeast Pacific has developed a negative tilt and a full cyclonic breaking event is in progress. This behavior also becomes linked with a retrograding anticyclonic anomaly across Canada and the North Atlantic, which allowed for a strong projection onto the positive phase of the PNA and the negative phase of the NAO. This pattern of strong tropical-subtropical westerlies stays in place for ~15 days.

Almost the opposite behavior was observed during T2 whose synoptic evolution to GSDM Stage 1 is shown in Fig. 6. Now instead of a trough, there is a ridge at 20N, 70E (Fig. 6a, b), which is being forced by the strong convection over the Indian Ocean. The phase of the wavetrain is reversed compared to Fig. 5 and the Indian Ocean ridge grows into a large anticyclonic anomaly over south Asia as the transition matures (see Fig. 6f). The downstream amplification over the west North Pacific also occurs, but with the phase reversed (Fig. 6 b-d) and little evidence of a pre-existing wavetrain further north. This leads to a wave break over the east Pacific (Fig. 6e, f) that becomes anticyclonic along the US west coast. The Stage 1 pattern was maintained by additional meridional to zonal flow variations leading to more anticyclonic wave breaking along the USA west coast (not shown). The final wave break occurred during late January 2002 and linked up with an anomalously strong subtropical jet, forced by tropical convective flare-up #6 near the date line, to produce an extreme winter weather event (snow and freezing rain) over the USA Great Plains. The GSDM Stage 1 characteristics of the circulation finally broke down in middle February 2002 (see Fig. 2).

e. Predictive skill of circulation transitions

The abrupt onset of Stage 3 and Stage 1 circulation regimes has forecast implications for the medium range. Fig. 7 shows the ensemble mean forecast skill out to 15 days during the 2001-02 winter season using a 1997 version of the NCEP MRF. This model has a 25-year reforecast dataset available and real time predictions are posted on the web (Hamill et. al. 2004). The skill measure is the spatial correlation between verifications and predictions of Northern Hemisphere 150mb streamfunction anomalies. There are three periods where the 11-day ensemble-mean forecast skill of northern hemisphere 150-hPa streamfunction anomaly is relatively poor (< 0.5). The common thread in these low skill regimes is that a major change in tropical convective forcing is observed (and presumably not captured) during the forecast cycle. The major convective changes are highlighted with arrows in the top panel of Fig. 7, i.e., flareups 3, 5 and 7. Note that the 5 and 7 transitions occur near the end of the forecast cycle implying a rapid impact on the circulation anomalies of the northern hemisphere, if indeed they are the cause for the low forecast skill.

For T1 and T2, the amplification of a wave disturbance over the western North Pacific is a key synoptic event. On December 23-24, 2001, the “low-high” couplet west of the date line (Fig. 5d) was predicted 11 days in advance but the “high-low” couplet in the same place on January 15-16 (Fig. 6d) was not. A clue about what may be happening is derived from the general pattern of forecast skill described above for the 2001-02 winter. The forecast for December 23-24, 2001 is initialized after flareup 3 while the forecast for January 15-16, 2002 is initialized before event 5. Failure to capture the start of flareup 5 and the large negative mountain torque in the forecast cycle presumably

contributed to low forecast skill during the second transition. Many more cases need to be examined to confirm these assertions.

f. Discussion

Several atmospheric phenomena and processes were introduced during the case study description. Tropical convective forcing involved multiple time scales including the 30-60 day MJO, 20-30 day convective flare-ups and other convectively coupled equatorial waves. Topographic forcing from synoptic-scale disturbances was clustered on a 50 day time interval and produced zonal momentum anomalies that were removed by the frictional torque. The PNA teleconnection pattern was involved in the removal process. Finally, the phase of synoptic scale wavetrains over the Asian-Pacific sector were related to tropical convective forcing over the Indo-Pacific warm pool region and to subsequent anticyclonic and cyclonic wave breaking over the eastern North Pacific.

The 50-day “oscillation” in the mountain torque is consistent with the 6-day decay time scale of the τ_F - τ_M index cycle. A red noise process with a 6-day decay time has its variance concentrated in a band with periods at around $6 \text{ days} * 2\pi = \sim 38 \text{ days}$. Plotting its spectrum in a variance-conserving format shows this view of red noise spectrum (e.g., see Fig. 2 of WRP) versus other misleading, but popular approaches. A 50-day oscillation is a representative example from such a process, but, of course, no coherent forcing exists at 50 days or any other period in the red noise background.

In the case study, these and other processes are seen as working together to produce the evolving atmospheric circulation anomalies. The indices in Fig. 3 show a slow evolution while Fig. 2 has the transition occurring rapidly in association with synoptic-scale wavetrains. The latter are seen as a mechanism for the spatial spreading of information about the changes in forcing from key regions around the hemisphere; e.g., western ocean baroclinic zones, tropical convective zones and centers of low frequency variability. Certainly, a fortuitous or random nature must be assumed about these fast (30 m/s) eastward moving disturbances and their role in transitions of the circulation; i.e., there is always the next synoptic system or wavetrain that can play the transition role. After the transition, repeatable synoptic events were superimposed on the quasi-stationary flow and these represent the opportunities for skillful extended forecasts of synoptic-scale behavior.

The basic perspective is that forcing is of primary importance for determining the evolution of the atmospheric circulation and that different sources produce circulation responses that combine linearly to give the circulation anomalies at any particular time. Anomalies may be maintained by feedbacks but eventually disperse as the forcing waxes and wanes, even when coupling from persistent SST anomalies is involved. This perspective is supported by Sardeshmukh et al. (1997), Newman and Sardeshmukh (1998) and Newman et al. (1997), who demonstrate the importance of forcing for the evolution of low frequency circulation anomalies. The success of the Winkler et al. (2001, hereafter WNS) linear inverse model (LIM) of weekly circulation anomalies is based on the importance of tropical and other forcing as a source for week 1 to 3 predictive skill.

WNS’s linear inverse model (LIM) of 7-day averages has features in common with the GSDM introduced in the next section. The LIM has three optimal structures that undergo non-modal growth over a wide range of truncations and maximized growth rates.

Two optimals are linked with forcing from the MJO and ENSO, while the third is a PNA pattern linked to eddy feedbacks in midlatitudes. The LIM is objective so it can be used for dynamical feedback studies (WNS) as well as predictability studies (Newman, et al., 2003).

The GSDM is subjective but includes a synoptic component and a submonthly oscillation in addition to the MJO and the PNA, arguably four “modes” versus three for LIM. Its dynamics are based on the terms in the global and zonal AAM budget. Meridional and vertical transports help produce the torques at the surface. A linear phasing of GSDM components is assumed, and this unites several time and space scales within the model. The model does not explicitly include ENSO but knowledge of the ENSO cycle is critical when applying it in real time. Both models can be further extended and are tools for monitoring, attribution and prediction. The GSDM is introduced next.

3. A Global Synoptic-Dynamic Model (GSDM) of Subseasonal Variability

The synoptic model organizes four subseasonal time scales into a single repeatable picture that describes the evolution of global and regional weather-climate patterns. Numerous indices could have been chosen to define a representative spatial evolution for each time scale. We use: 1) the first empirical orthogonal function (EOF) of 20-100 day filtered outgoing longwave radiation (OLR) to represent the MJO, 2) the daily global frictional torque with the MJO linearly removed to represent the “ τ_F - τ_M index cycle” (W03) and 3) the <30 day filtered relative AAM tendency to represent wave energy dispersion over the mountains (W03) and 10-30 day oscillations. The indices are computed for the sixteen winter segments, November-March 1979-80 through 1994-95. The segment mean is removed prior to the regression analysis to minimize contributions from interannual variability. Resulting anomalies will be interpreted relative to a smoothed seasonal cycle.

Fig. 8 shows the three indices. Their different time behavior is self-evident and ranges from quasi-oscillatory (Fig. 8a) to red noise (Fig. 8b) to white noise plus a ~20-25 day oscillation (Fig. 8c)². We implicitly assume these time scales are adequate to account for some interesting variations in the subseasonal band, with a focus over the tropics, Asia and the Pacific North American region. First, however, we examine the relationship to global and zonal mean AAM, which are used to “phase” the model components.

a. Atmospheric Angular Momentum

In the case study, global AAM (Fig. 3) undergoes a relatively smooth evolution despite the complicated forcing depicted in Fig. 4. A careful examination of the AAM time series can discern the responses to the fast and medium excursions of the global mountain and frictional torques seen in Fig. 4 while the overall ~60-day oscillation implies a forcing by the weaker but more persistent torques associated with the MJO. Different time scales are clearly working together to produce the observed behavior. We now illustrate these building blocks and suggest why and how they may be related.

² A statistically significant ~25 day oscillation appears in the spectra of global relative AAM in two different 16-winter periods, 1962-78 and 1979-95

Fig. 9b-d shows the global and zonal AAM anomalies obtained when regressing onto the three indices of the GSDM illustrated in Fig. 8a-c. The heavy solid lines on the Fig. 9 panels indicate all three indices have a global AAM signal. The lag at which the AAM anomaly crosses zero is $\sim+2$ days (Fig. 9b), $+7$ days (Fig. 9c) and 0 days (Fig. 9d) for the three GSDM components. This is the key assumption made in constructing our model³. The point is that a linear combination of the three time scales, when shifted by these amounts, would result in a large relative AAM time tendency. We are specifically interested in large anomalies because synoptic experience indicates extreme events consist of multiple time scales “working together”. Such a linear combination would produce torques whose sum resembles the time series seen in Fig. 4a of the case study. Maximum AAM tendency would occur at Stage 2 of the GSDM and would have contributions from all model components.

The zonal mean AAM anomalies when added depict a coherent signal of AAM anomalies moving out of equatorial regions toward the subtropics (Fig. 9a) and a weaker signal of anomalies moving equatorward around 50N. The intermediate time scale $\tau_F - \tau_M$ index cycle (W03), imposes an asymmetry around day 0. Momentum transports by different types of eddies (e.g., subtropical wavenumber 1, midlatitude teleconnections and midlatitude synoptic transients) play an important role in forcing all three of the zonal mean anomaly fields and provide a dynamical link between the time scales.

In the next subsection, the synoptic patterns related to the global and zonal AAM changes seen in Fig. 9 are presented. Since the <30 day tendency and frictional torque regressions are performed on global indices, the results will emphasize those patterns that contribute to global AAM changes. For the <30 day tendency the three main topographic regions are represented while for the global frictional torque the northern hemisphere surface wind over both ocean basins will be important. During individual cases of subseasonal variation not all regions will always contribute to the forcing. For example, in the case study Asia was the primary contributor to the positive mountain torque before T1 while Asia and North America both contributed to the negative torque before T2. Nonetheless, a simultaneous forcing from the three regions is not unusual and can be organized by poleward propagation of zonal mean wind anomalies or by the dispersion of Rossby waves into each hemisphere from west Pacific tropical heating. In general, however, the phasing of regional patterns is influenced by the use of a global measure on which to base the analysis and can distort important regional behavior

b. Lagged Regression Sequences

Lagged linear regressions of global, 2-D fields onto each index are used to define an evolution of circulation anomalies and will be referred to as a lagged regression sequence. Figs. 10-12 show sequences 1-3 of 200mb vector wind and sea level pressure anomalies when regressed onto the three indices of Fig. 8. The duration and time interval of each sequence emphasize its time scale. Sequence 1 is 40 days long with a 10 day interval, sequence 2 is 18 days long with a 4 day interval, and sequence 3 is 8 days long with a 2 day interval. Global fields are shown because real time monitoring suggests coherent subseasonal interactions occur across broad latitudinal bands, often centered on

³ One could also use the time of maximum zonal AAM tendency at the equator and get slightly different numbers.

either side of the equator. The sequences illustrate the well-known observation that large spatial scales coincide with long time scales. Beyond this, there are other features familiar to climate scientists.

In sequence 1 (Fig. 10), the subtropical cyclones/anticyclones of the MJO are seen as they slowly propagate eastward from day -20 through day 0 to day 20. At day 0 (Fig. 10) convection is active over the equatorial western Pacific and global AAM has a large positive time tendency, at which time equatorial westerlies are already present over the western hemisphere. In sequence 2 (Fig. 11), a negative Pacific/North American teleconnection pattern (W03) develops by day -2 as Rossby waves disperse across Asia and then North America during the 18 day sequence; this contributes to a large positive frictional torque anomaly at day 0 (not shown). In sequence 3 (Fig. 12), rapid energy dispersion events (30 m/s) are seen centered over the east Asian, North American and South American mountains at day 0 and contribute to a positive global mountain torque anomaly. The events are embedded in a pattern of wavenumber 0-2 zonal wind anomalies, some of which are highlighted by arrows. Four days after the positive torque, westerly flow anomalies extend from the equatorial east Pacific eastward and poleward to the midlatitude central Pacific. These anomalies represent the ~ 20 day quasi-oscillatory component of the GSDM (see also Fig. 9d).

Interestingly, sequences 1-3 all have local statistically significant wind and SLP anomalies in tropical regions, even the two faster modes of variability. The features are characterized by wavenumber 0-1 zonal wind anomalies at upper levels and provide a synoptic pattern that links the different types of subseasonal variability. This complements and extends the results for the global and zonal AAM relationship that is the basis for the model.

c. The Synoptic-Dynamic Model (GSDM)

Figure 13 shows the four stages of the GSDM nominally centered about 12 days apart with a ~ 50 day oscillation due to the MJO. These numbers have a wide range since the subseasonal band is broad, and transition between phases can occur rapidly. A complete temporal evolution of anomalies is shown only for the MJO. Twenty-two maps representing 11 lags for both OLR EOF1 and EOF2 were examined and the four lags in Fig. 13 were chosen to represent the MJO. The EOFs are in-quadrature and show similar patterns when shifted by ~ 10 days. Table 2 shows the correspondence between the stages and the lags for the two EOFs. The Hs and Ls for the other components are placed with a specific stage based on the “large AAM tendency” criterion discussed in relation to Fig. 9. Specifically, the colored Hs and Ls shown on sequence 2 (Fig. 11) and 3 (Fig. 12) are used to complete construction of the stages.

1. Stage 1

This stage represents a particular phasing of the MJO and the intermediate time scale of the model. Stage 1 and Stage 3 are considered the more persistent stages of the GSDM. During Stage 1 the anomalous anticyclones linked with the MJO cover most of the tropical eastern hemisphere with downstream cyclones over the subtropical west Pacific Ocean. Tropical convection anomalies are consolidated over the eastern Indian Ocean as the MJO convective forcing has intensified from Stage 4. In the subtropics easterly flow anomalies cover the west Pacific and weakly also the Atlantic Ocean. The

anomalies represent an amplification of the wintertime climatological stationary waves in the tropics and subtropics (see Fig. 9a of WKS), although the Pacific jet is retracted.

The brown Hs and Ls over the northern hemisphere represent the “ τ_F - τ_M index cycle”. A negative PNA pattern is a prominent feature of the wavetrain disturbance. The circulation centers of this stochastic mode approximately phase with some of the circulation anomalies associated with the MJO. Together, easterly zonal wind anomalies in subtropical latitudes of the western hemisphere and in the tropics of the eastern hemisphere lead to the very low relative AAM. As these easterly flow anomalies reach the surface, they lead to a positive frictional torque, which sets the stage for an increase in AAM and a possible transition to Stage 2.

Although not depicted in Fig. 9, the general anomalous pattern of synoptic variability is similar to what occurs during La Nina. It involves a northward shifted storm track and enhanced wave energy propagating into the tropics. Matthews and Kiladis (1999) show that during this phase of the MJO the Pacific waveguide tends to be “leakier” since the jet stream is weaker and westerly winds extend over a broad latitudinal band. As wave energy disperses southeastward into the east Pacific ITCZ resulting convection anomalies (Kiladis and Weickmann 1997; Matthews and Kiladis 1999) can lead to subtropical jets that combine with the western USA trough and produce baroclinic developments over the North American Great Plains.

Stage 1 can be characterized by a ~weekly variation between strong meridional flow anomalies and strong zonal flow anomalies during northern winter. Transitions from meridional to zonal flows occur in association with baroclinic waves that tend to break anticyclonically over the east Pacific Ocean. Broadly speaking Stage 1 represents a “La Nina” basic state, which has been shown to support greater intraseasonal variance over the North Pacific Ocean (Compo et al 2001) and Life Cycle 1 (LC1; anticyclonic) of baroclinic waves (Shapiro et al. 2000).

2. Stage 2

Stage 2 represents a transitional phase of the GSDM where the MJO moves into the Pacific Ocean region and synoptic-scale energy dispersion contributes to strong positive mountain torques. Positive MJO convection anomalies that were previously centered west of 120E now set up over the western Pacific at around 150E. Weickmann and Khalsa (1990) have shown that this transition can occur rapidly in association with high frequency tropical transients, since identified as convectively coupled equatorial Kelvin waves by Wheeler and Kiladis (1999). The MJO circulation anomalies are also transitional as twin anticyclones move into the western Pacific and twin cyclones cover the remainder of the tropics including the western Indian Ocean. The anomaly pattern represents an eastward shift of the climatological flow in the tropics and subtropics (see Fig. 9b of WKS).

The green Hs and Ls are the fast time scale pattern that gives a large positive mountain torque and precedes stronger westerly flow in the subtropics from 10-30 day oscillations. In the Northern Hemisphere, two wavetrains over Asia meet over the west Pacific and disperse downstream. In the Southern Hemisphere, wavetrains are shown that produce positive mountain torques over the South American Andes and the African Highlands.

Stage 2 often represents a sudden transition to new tropical heat sources and considerable transient Rossby wave activity emanates from the new sources over the east Indian and the west Pacific Oceans. Over the west Pacific Ocean, this is characterized by the spin-up of upper level anticyclones, whose circulation then interacts with midlatitude weather systems. One such interaction can initiate a growing Pacific Ocean wavetrain (the heavy gray Hs and Ls) that extends downstream across North America. Although the wavetrain is depicted in Stage 2, it is best developed 6-10 days after convection moves into the western Pacific Ocean region. In that case the green Hs and Ls are precursors to the dark gray Hs and Ls.

WNS obtain a similar wavetrain in their study of the response to tropical heating. The initial state of their singular vector 2 (SV2) would project onto both the convection and green circulation centers shown at Stage 2. The gray Hs and Ls emanating from the tropical west Pacific Ocean region represent the final state of SV2. Other studies of MJO composite circulation anomalies (e.g., Knutson and Weickmann 1987) find a similar feature. The wavetrain is seldom a simple Rossby wave dispersing from a tropical heat source (Hoskins and Karoly 1981; Sardeshmukh and Hoskins 1988) but often involves tropical-extratropical interaction on fast time scales.

3. Stage 3

As the GSDM convection anomaly moves eastward, the circulation anomalies now act to weaken the normal wintertime climatological flow in the tropics and subtropics (see Fig. 9c of WKS), but at the same time extend and strengthen the jet across the Pacific. The brown Hs and Ls connecting Asia and North America now project on a positive PNA. Strong westerly flow occurs at 35N over the Western Hemisphere and in the tropics over the Eastern Hemisphere, from the combination of the MJO and the intermediate time scale τ_F - τ_M index cycle. The storm track is further south over the Pacific and can give rise to extreme rainfall events along the USA west coast. Cyclonic wave breaking is often observed over the east Pacific Ocean, upstream of North America. Stage 3 represents an “El Nino” basic state and while the patterns are opposite to Stage 1, the synoptic variability tends to be less extreme during Stage 3.

4. Stage 4

Stage 4 is similar to Stage 2 but with opposite sign and slightly earlier in the MJO life cycle. For example, suppressed convection still covers western Indonesia in Stage 4 whereas enhanced convection is further east at Stage 2. The MJO circulation anomalies now produce a westward shift of the wintertime climatological flow in the tropics and subtropics. Over the Indian Ocean, the strong subtropical cyclones of Stage 3 are transitioning to anticyclones as convection redevelops over the central Indian Ocean. This stage has three centers of MJO convection: east of the dateline, over South America and over Africa/west Indian Ocean.

On the synoptic time scale, Stage 4 is represented by the sequence of green Ls and Hs, the opposite phase to Stage 2. The phase of the south Asian wavetrain is set by the Indian Ocean convection anomaly located south and east of the anomalous anticyclone at around 60E. This wavetrain phases with a separate wavetrain in the north Asian waveguide that produces a negative mountain torque there and then together they disperse east and amplify across the North Pacific toward North America. The

combination of a negative mountain and frictional torque from the MJO and a negative mountain torque from the synoptic scale dispersion leads to a strong negative AAM tendency and sets the stage for decreasing westerly flow in the atmosphere.

d. The Combined AAM cycle

Much is known about the subseasonal budget of global and zonal AAM based on recent diagnostics studies using reanalysis data. For the global budget, Weickmann et al. (2000) and Egger and Hoinka (2002) show that the mountain torques forces AAM anomalies and the frictional torque damps them. In the semantics of Fourier analysis, this means the friction torque leads the mountain torque. All subseasonal variability has this character. The zonal budget brings in the role of AAM transports, which are zero in a global integral. Meridional transports provide a link back to the structure and orientation of troughs and ridges within the spatial patterns shown in Fig. 13. Subseasonal zonal AAM anomalies have well-developed poleward (Feldstein, 2001) and downward propagation that extends from the equatorial tropopause to the subtropical solid earth (Egger and Hoinka, 2003; 2005). Dynamically many questions remain about the contribution from different mechanisms in this process. For example, Moncrieff (2004) proposes a role for vertical transport of zonal momentum due to the structure of organized mesoscale convective complexes. Unfortunately, the zonal AAM budget cannot provide even rudimentary answers because it is not balanced in either the NCEP/NCAR (WKS) nor the ECMWF reanalyses (Egger and Hoinka, 2005). The zonal mean flux convergence of relative AAM is large compared to the sum of zonal mean torques, even when the coriolis and gravity wave drag torques are included. This contributes to a systematic dipole in latitude error in the zonal AAM budget as shown by W03 (see his Fig. 3c, d).

In this section we are not so much interested in the AAM budget as in using it to bring out additional features of the GSDM, and to relate its spatial patterns in Fig. 13 with the combined AAM cycle. Some of the features of the cycle are summarized in Table 3. Figure 14 shows the lag regression of the global and zonal AAM, the flux convergence of AAM, and the mountain and frictional torque onto daily time series of global relative AAM tendency for the November-March seasons 1979-95. The approximate locations of the GSDM stages are shown at the bottom of the figure.

In Fig. 13, the Hs and Ls from different time scales were placed on the four stages without considering the actual time behavior that might ensue. Fig. 14 shows this in an average sense for the global and zonal mean fields by regressing on an index that contains all the components of the GSDM; i.e., the daily global relative AAM tendency. The time behavior is clearly asymmetric with respect to zero lag as would be expected, if only because of the intermediate time scale τ_F - τ_M index cycle. There appears to be a buildup phase during Stage 1 (see Fig. 14 prior to day -5) where several processes are persistent and there is a gradual decrease (increase) in relative AAM (frictional torque) anomaly due to a negative mountain torque. This occurs early in the MJO's life cycle when positive convection anomalies are over the Indian Ocean and the intermediate time scale contributes a negative PNA as positive frictional torques increase (Fig. 14c).

There then appears an abrupt reversal or weakening in all anomalies around day -2, arguably led by a reversal in the meridional AAM transport across 30N, from poleward before to equatorward after. This occurs just as the zonal mean easterly flow anomalies

in the subtropics reach their peak values at 25N. At the same time, the dominant wavetrain in the GSDM shifts from the intermediate time scale teleconnection type (Stage 1) to the wave-packet-dominated fast time scale type (Stage 2). The latter helps reverse the mountain torque and possibly initiates the “flip” in meridional transports. Fig. 14b has a momentum source due to transports that extends from the northern to the southern subtropics. The MJO is also undergoing a transition at this time when tropical convection moves out of the Indian Ocean and into the west Pacific Ocean region. A further forcing of the torques by the MJO could then lead to a continued oscillation. Fig. 14a shows more damped anomalies after day 0 again reflecting the $\tau_F - \tau_M$ index cycle.

During an oscillation, the vertically integrated AAM anomaly (Fig. 14a) alternates between easterly and westerly flow anomalies that propagate from equatorial regions to the subtropics. The oscillation represents the MJO along with a sharpening of the curve by 10-30 day variations. Global angular momentum is a minimum at Stage 1 when negative AAM anomalies (easterly wind anomalies) are moving off the equator and tropical sea level pressure (SLP) is low. By Stage 2 the easterly anomalies are approaching the subtropics and weakening on the equator. Tropical SLP is on the rise and MJO convection is active over the western Pacific. By Stage 3, westerly flow anomalies are lifting off the equator, tropical SLP is high and global AAM reaches a maximum. Convection is near the date line but it is strongly suppressed over the Indian Ocean from both the MJO and 10-30 day oscillations. The cycle ends with Stage 4 as westerly wind anomalies move off the equator and convection is active in the three separate centers.

The frictional torque tends to be large during Stages 1/2 and 3, when anomalies are more persistent than during Stages 2 and 4. Synoptically Stage 1 is represented by strong trade winds and a northward shifted westerly flow, especially over the Atlantic and Pacific Oceans. Sometimes, blocking can contribute to the torque through easterly flow anomalies that are large and farther north. The mountain torque tends to be large during Stages 2 and 4, which also tend to be more transient with faster time scales involved. The positive mountain torque in the southern hemisphere is due to the Andes and develops as convection shifts into the western Pacific between Stages 1 and 2 (Madden and Julian, 1972; Milliff and Madden 1996). In the northern hemisphere the positive mountain torque is produced by high pressure anomalies east of the Tibetan Plateau and cold air outbreaks that accompany the shift of convection to the west Pacific.

4. Summary and Conclusions

We have proposed a synoptic-dynamic model of subseasonal variability that is useful for weather-climate monitoring and for medium-range prediction assessment. The monitoring involves daily subseasonal variability while the prediction focuses on forecast lead times from 3 days to 3 weeks. The GSDM is constructed for the northern hemisphere cool season but the same processes are active during the rest of the seasonal cycle. For example, to first order the MJO circulation and convective anomalies merely shift northwest during northern summer and become larger in the southern (winter) hemisphere. There is also a summer analogue to the Stage 2 wavetrain seen in Fig. 13. The approach discussed in Section 3 will be applied to the other seasons in future work. Newman and Sardeshmukh (1998) provide some clues about the sensitivity of forcing and response during the course of the seasonal cycle.

By keying on the global relative AAM tendency, construction of the GSDM is made easier although the regional anomaly patterns and their relationships are blurred. A version of Fig. 13 (not shown) made from lag regression of the 200-hPa streamfunction and OLR fields onto the daily AAM tendency supports the idea that the composite variations around day 0 (Stage 2) consist of different time scales of forcing, sometimes contributing to large global AAM tendencies. In our approach, we have defined the dominant time scales that drive the global AAM tendency and then the preferred phase relationships that give a large time tendency. As a result Stages 2 and 4 contain a specific phase of the fast time scale component whereas only general storm track changes are invoked in Stages 1 and 3.

The GSDM is used in conjunction with daily real time monitoring of a broad range of weather-climate indices, maps and forecasts. These range from the large-scale patterns of SST down to ongoing baroclinic life cycles or tropical convectively coupled Kelvin waves. The multiple time scales contribute to rapid transitions of the tropical and extratropical circulation which are difficult for operational GCMs to capture and can lead to large forecast errors. The 2001-02 case study examined two such transitions and their relationship to tropical forcing from two MJOs and midlatitude mountain torques. It highlighted a link between the MJO, extratropical wavetrains and baroclinic wave processes over the Pacific-North American region. The transition included a cyclonic (an anticyclonic) wave break that ushered in strong (weaker) subtropical westerlies and a positive (negative) PNA.

An operational forecast model's 11-day prediction showed that the three periods of relatively low model skill in 150mb streamfunction at 11-days occur when a major longitudinal shift of tropical convection is observed during the period of the forecast. The model is more successful at capturing the initial conditions of tropical precipitation and persisting them, a sometimes useful attribute for the week 1 forecast. The relationship between objectively defined "flare-ups" of convection and the time evolution of predicted and observed fields will be examined in a longer reforecast dataset in future work.

The GSDM was developed to provide an additional tool to the medium range forecaster to assess the state of the atmosphere-ocean at the initial time and thereby evaluate the predictions of numerical models. The GSDM is being used in real time weather-climate discussions and experimental week 1-3 predictions, which are being posted at (http://www.cdc.noaa.gov/MJO/Forecasts/climate_discussions.html). Whether the GSDM can be used to improve subseasonal predictions on average remains to be determined. However, real-time weather-climate monitoring within the framework of the GSDM should help capture sudden shifts in tropical convective forcing and may improve interpretation of numerical model predictions of high impact, extreme weather events.

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Figure Captions

Figure 1. Hovmoller plot (time-longitude section) of OLR anomalies averaged between 7.5 deg. N-S, where the contours illustrate space-time filtered coherent tropical convection modes for 25 September 2001-26 March 2002. The blue contours represent the MJO (solid blue for enhanced convective phase/dashed for suppressed phase). The green contours are for Kelvin waves and the brown contours isolate an equatorial Rossby mode. See Wheeler and Kiladis (1999) for additional details. MJOs 1 and 2, T1 and T2, and the 1-7 numbering refer to important developments discussed in the text and listed in Table 1. The lightly shaded horizontal bars highlight the transitions for the case study, with T1 (T2) from 19-25 December 2001 (12-18 January 2002).

Figure 2. Hovmoller plot of 250mb meridional wind anomalies averaged from 30-60N during the period of 1 December 2001-28 February 2002. The solid horizontal lines depict the periods for T1 and T2, and the “Hs” and “Ls” highlight positions of anomalous synoptic-scale troughs and ridges, respectively. The red arrows indicate retrogression of existing anomalies while the light dashed lines show a slow westward regime shift. The slanted solid black lines indicate progressive circulation anomalies after 1 February 2002.

Figure 3. Time series plots of indices describing low frequency variations for the period of 1 November 2001-28 February 2002. The days are on the abscissa, where day 0 is for 1 November and increasing from left to right. The numbers on the ordinate of the upper panel are AAM units = $1.0 \times 10^{24} \text{kgm}^2 \text{s}^{-1}$ and on the lower panel are dimensionless measures of amplitude. The top panel is for the global integral of AAM while the bottom shows the plots for the first EOF of the combined 200/850mb vector wind field (red) and the PNA (blue). The vertical lines depict the center date for T1 and T2.

Figure 4. Time series plots (same format as Fig. 9) for the period of 1 November-28 February. a) the first EOF of the zonal integral of the mountain and frictional torque (top panel; red is mountain torque/blue is frictional torque). b) the first 2 EOFs of 20-100 day filtered OLR (red is EOF1/blue is EOF2). The text on the right indicates the location of anomalous convection corresponding to positive and negative values of each EOF. IO refers to Indian Ocean. Shaded vertical bars represent T1 and T2. Additional details are in the text.

Figure 5. The daily evolution of 150mb vector wind anomalies for T1, the transition to Stage 3 of the GSDM. “Hs” and “Ls” refer to anomalous anticyclonic and cyclonic circulations. From a) to f) the dates are: December 19, 20, 21, 22, 23 and 25. The vertical lines highlight 90E, 180E and 90W.

Figure 6. Same as Fig. 5 but for T2, the transition to Stage 1 of the GSDM. Dates are a) to f): January 12, 13, 14, 15, 16 and 18.

Figure 7. Time series plots of OLR EOFs 1 and 2 (as in Fig. 4), top panel, and forecast skill for a forecast model ensemble mean, bottom panel, during the period of 1 December 2001-28 February 2002 (abscissa, days increasing from left to right). “IC” and “V”, and

the vertical lines highlight the model initial condition and verification times for the three cases discussed in the text. Verification is expressed in terms of anomaly correlation coefficient over the entire northern hemisphere of 150-mb streamfunction. The contour interval on the bottom panel is 0.3, and the black dots show the dates of lowest day 11 forecast skill. The slanted lines indicate the model forecast cycle (day 1 to day 15 lead) for T1 and T2. The horizontal line highlights day 11 lead.

Figure 8. Indices for 16 winter segments from November-March 1979-1980 to 1994 1995 for (a) the first EOF of 20-100 day filtered outgoing longwave radiation (OLR) represents the MJO, (b) the daily global frictional torque with the MJO linearly removed represents teleconnection patterns, and (c) the <30 day filtered global relative AAM tendency represents wave energy dispersion over the mountains. The abscissas are time expressed as days while the ordinates are non-dimensional measures of amplitude.

Figure 9. The total global atmospheric angular momentum (solid curve), the global mountain torque (long dash curve) and the global frictional torque (short dash curve) anomalies obtained by lag regressions onto various indices using sixteen northern winter seasons (November-March 1979-95). The left ordinate labels are Hadleys ($1 \text{ Hadley} = 1.0 \times 10^{18} \text{ kgm}^2 \text{ s}^{-2}$) and the right labels are AAM units ($1 \text{ unit} = 1.0 \times 10^{24} \text{ kgm}^2 \text{ s}^{-1}$). The abscissa is lag where negative (positive) values mean the regressed quantity leads (lags) the index. For the contours, the right labels also represent latitude/10, i.e., 6=60N, etc. The contour and shading interval is $0.1 \times 10^{24} \text{ kgm}^2 \text{ s}^{-1}$ (the value corresponds to a vertical and zonal mean zonal wind anomaly of 0.3 ms^{-1} at 30N). The contours start at $0.05 \times 10^{24} \text{ kgm}^2 \text{ s}^{-1}$ in Fig. 9d. The indices used are: a) the daily global AAM tendency, b) the first EOF of 20-100 day filtered outgoing longwave radiation, c) the global frictional torque minus the MJO (see text), d) the global relative AAM filtered to retain < 30 day periods and e) the global mountain torque.

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Figure 11. Same as Fig. 10 except regressed onto the daily global frictional torque shown in Fig. 8b (sequence 2). The brown Hs and Ls are placed on Fig. 13 as part of Stage 1 and Stage 3 (opposite phase) of the GSDM.

Figure 12. Same as Fig. 10 except lag regressions on the <30 day filtered, global relative AAM tendency index given on Fig. 8c (sequence 3). The green Hs and Ls are placed on Fig. 13 as part of Stage 2 and Stage 4 (opposite phase) of the GSDM.

Figure 13. The four stages of the global synoptic-dynamic model (GSDM) of subseasonal variability for the northern hemisphere cold season (November-March). The

red (blue) isopleths and shading depict subtropical anticyclonic (cyclonic) 200mb streamfunction anomalies (inter-hemispheric sign reversal is understood) that accompany MJO tropical convection anomalies as they move east. The black (hatched) shading shows the areas of enhanced (suppressed) convection with the MJO. The “Hs” and “Ls” are used to show the associated anomalous anticyclonic (or “high pressure”) and cyclonic (or “low “pressure”) gyres. The lighter gray Hs and Ls are for the MJO while the heavier gray ones illustrate a west Pacific wavetrain linked to the MJO at Stage 2. The brown “Hs” and “Ls” depict teleconnection patterns associated with the frictional torque, and the green ones show synoptic-scale wavetrains. See text for additional details.

Figure 14. Zonal (contours and shading) and global (curves) anomalies obtained by lag regression onto the daily relative AAM tendency for November- March 1979-80 to 1994-95. (a) Total AAM: contour interval is $0.1 \times 10^{24} \text{ kgm}^2 \text{ s}^{-1}$, left ordinate labels are for global curve in AAM units (1 unit = $1.0 \times 10^{24} \text{ kgm}^2 \text{ s}^{-1}$). b) The flux convergence of relative AAM: contour/shading interval is 0.2 Hadleys, left ordinate labels are Hadleys. c) the frictional torque: same as b) except contour/shading interval is 0.1 Hadleys. d) the mountain torque, same as c). Note that the contour interval in b) is twice that in c) and d). The right ordinate labels are latitude for the zonal contours.

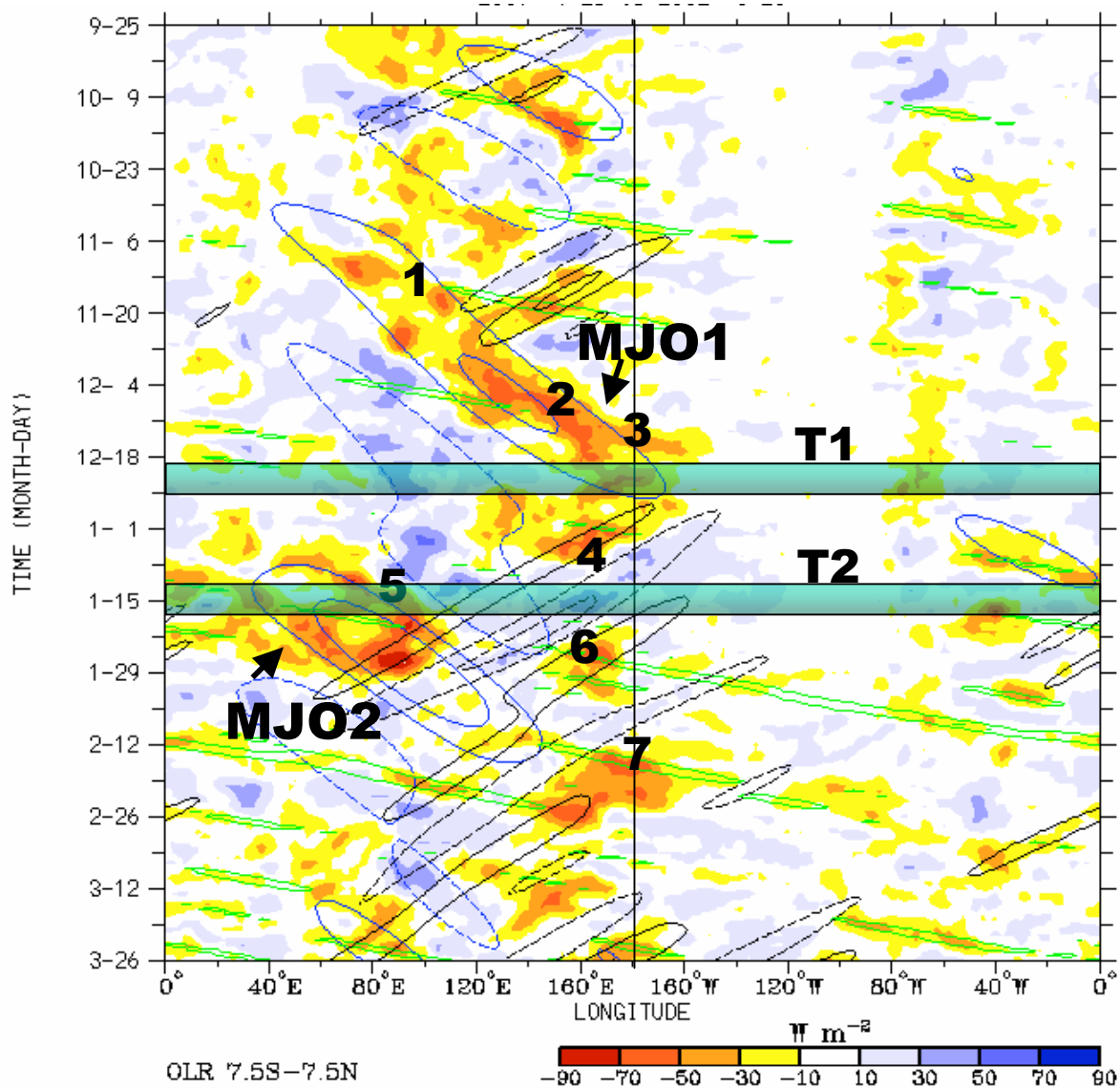


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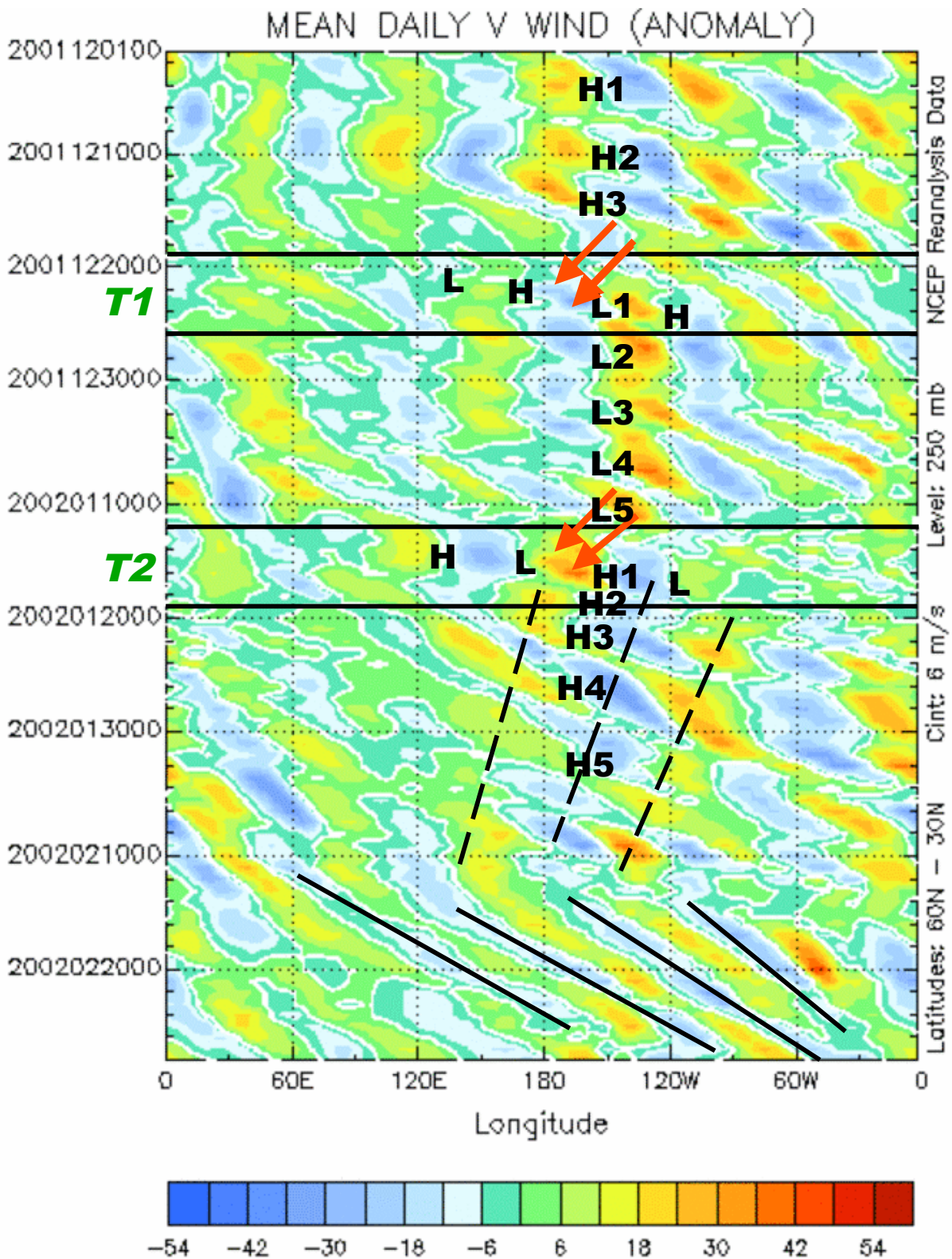
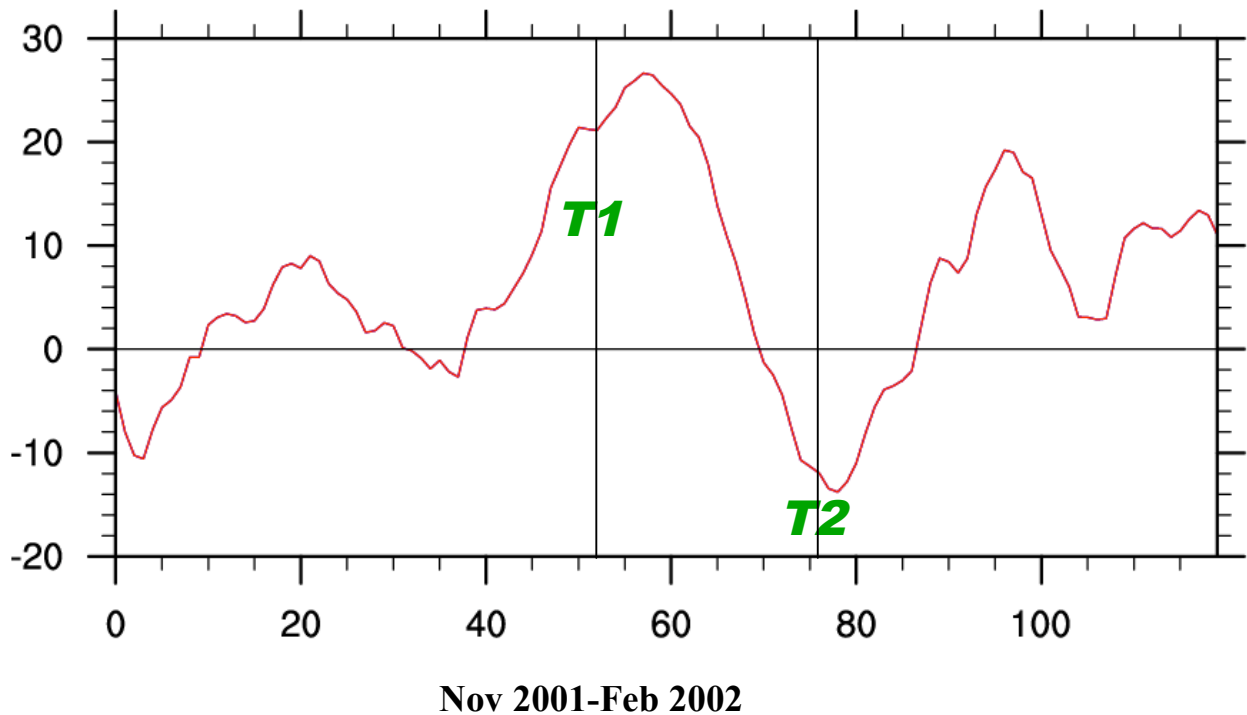


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Global relative AAM



PNA and Global wind EOF 1

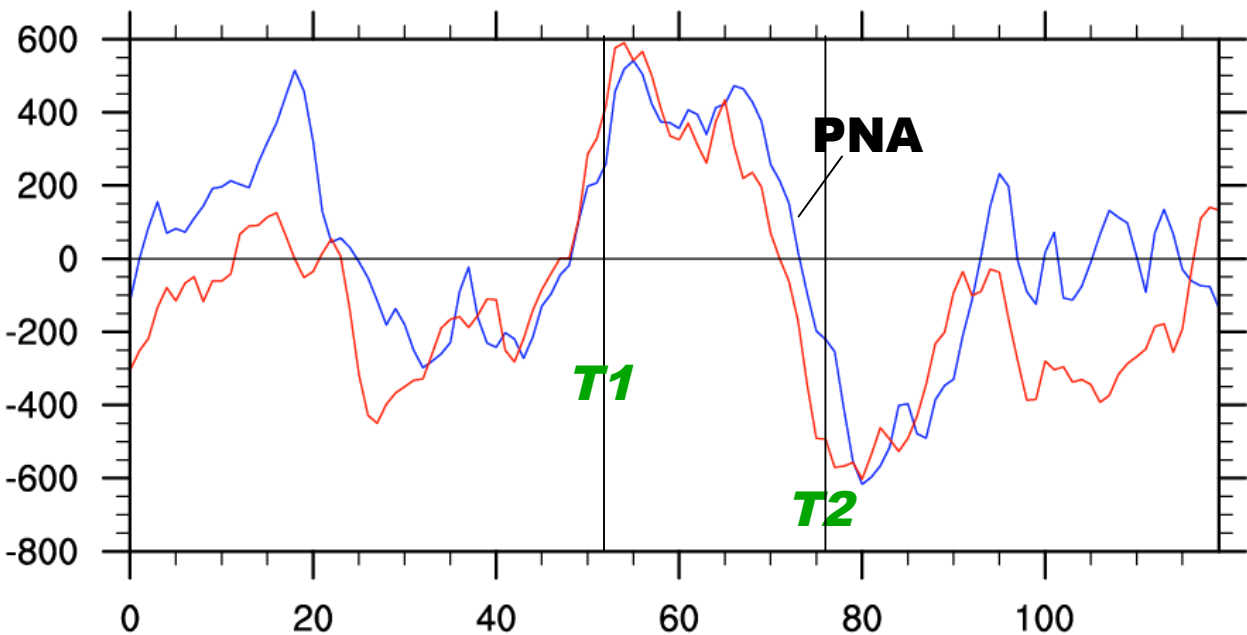
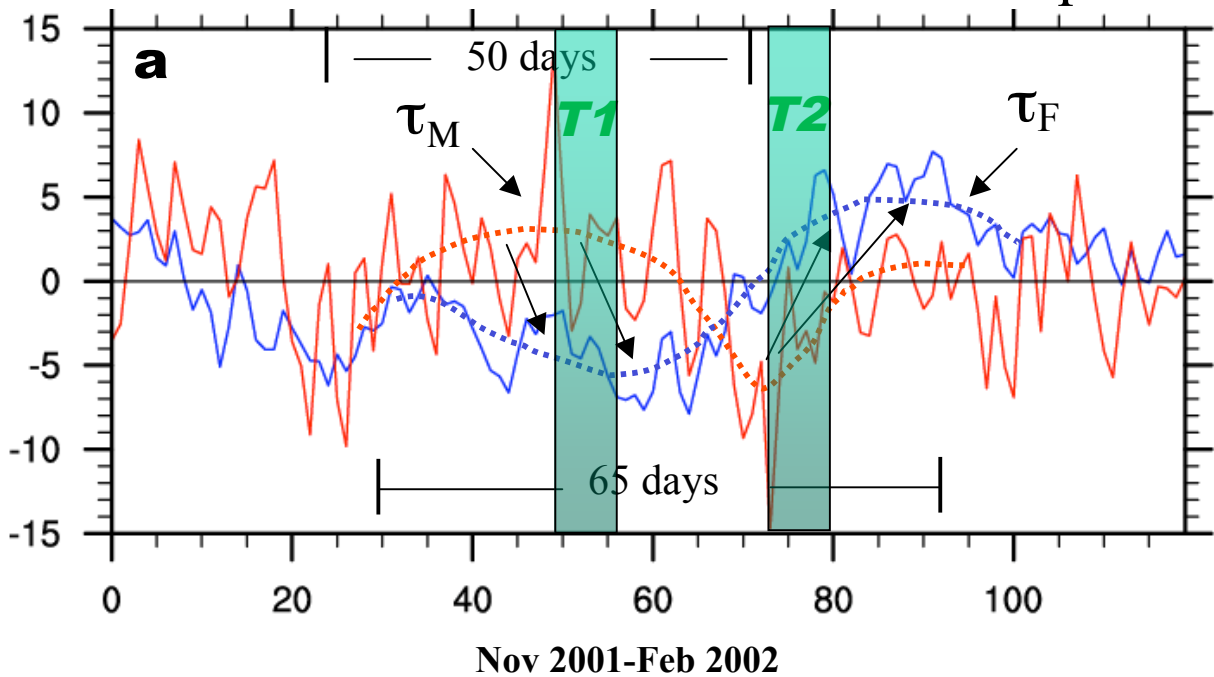


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EOF1 of mountain and friction torque



EOF1/2 of 20-100 day filtered OLR

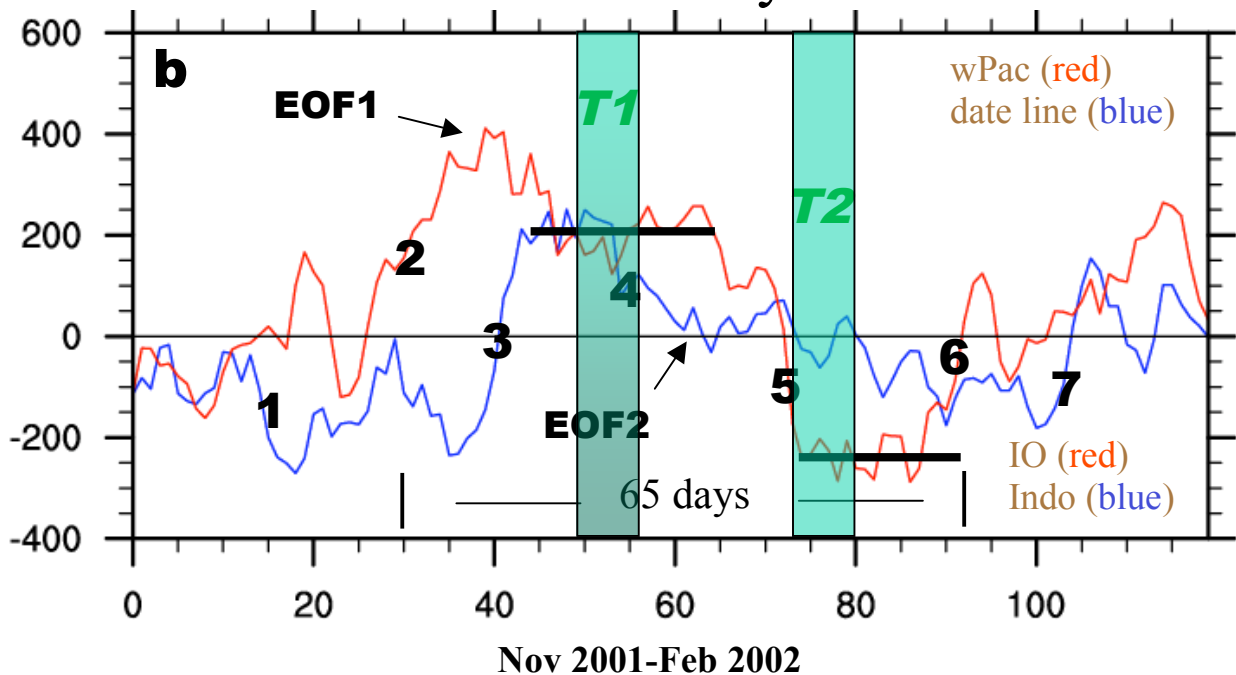


Figure 4. Time series plots (same format as Fig. 3) for the period of 1 November-28 February. a) the first EOF of the zonal integral of the mountain and frictional torque (top panel; red is mountain torque/blue is frictional torque). b) the first 2 EOFs of 20-100 day filtered OLR (red is EOF1/blue is EOF2). The text indicates the location of anomalous convection corresponding to positive and negative values of each EOF. IO refers to Indian Ocean. Shaded vertical bars represent T1 and T2. Additional details are in the text.

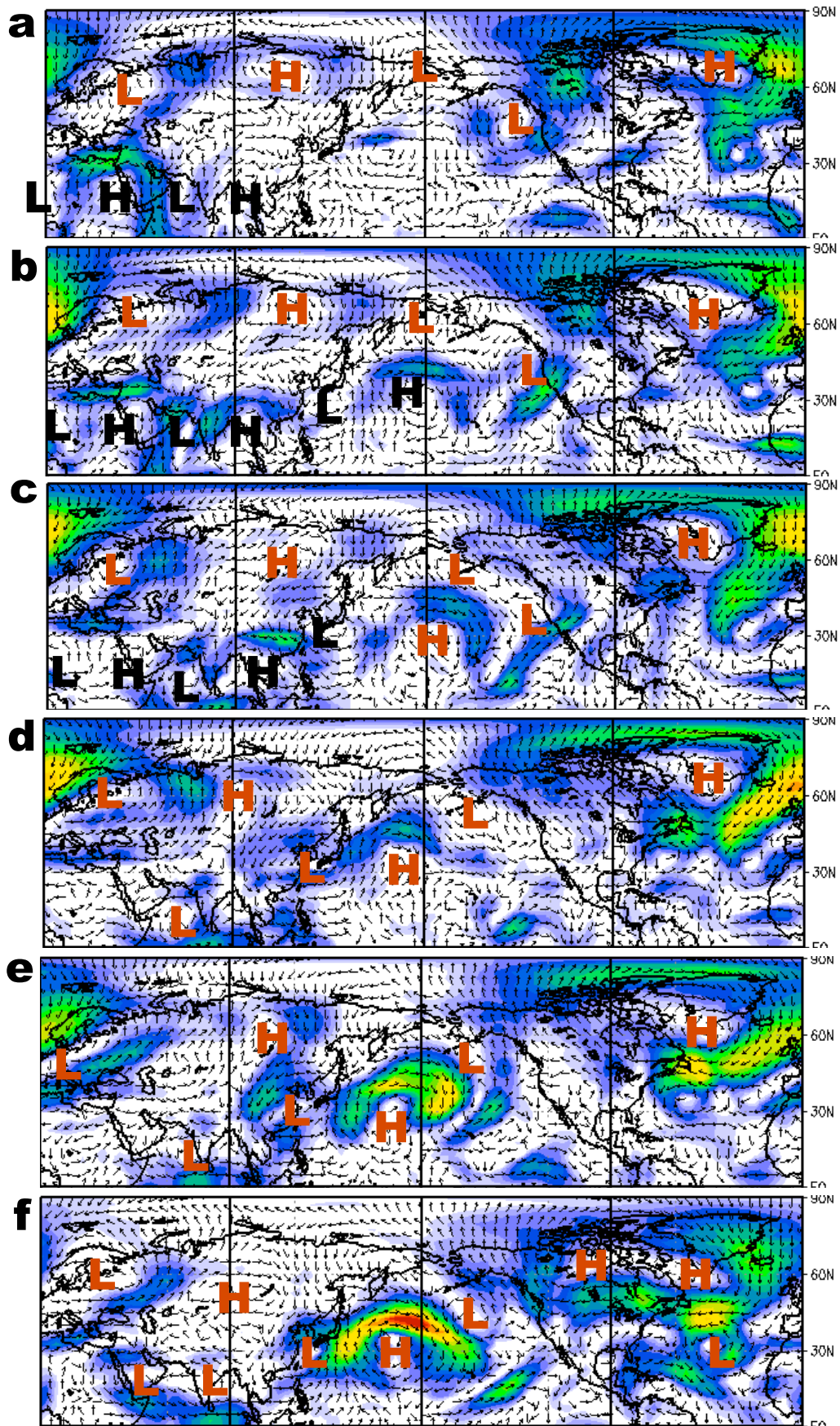


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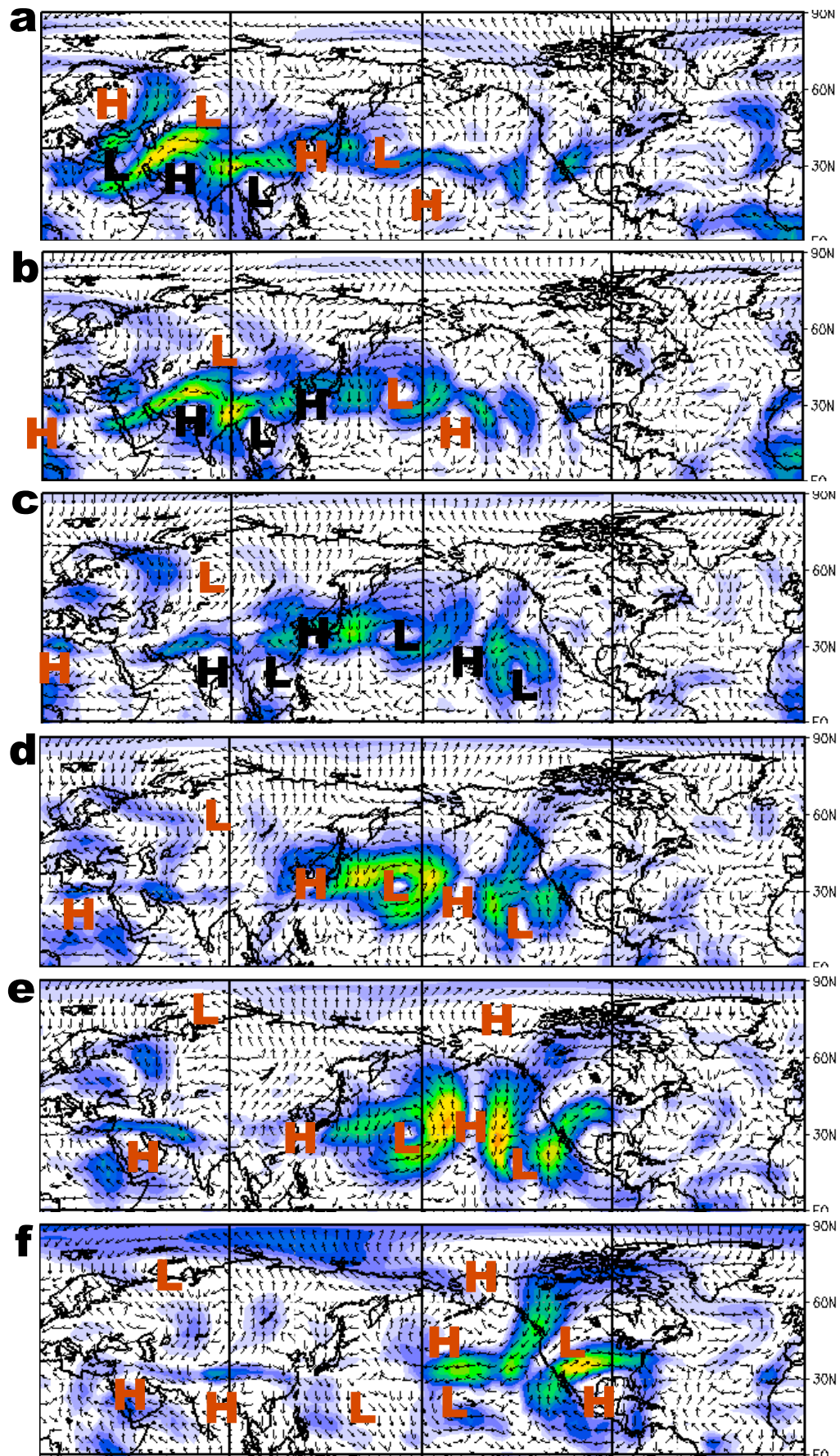


Figure 6. Same as Fig. 5 but for T2, the transition to Stage 1 of the GSDM. Dates are (top to bottom): January 12, 13, 14, 15, 16 and 18.

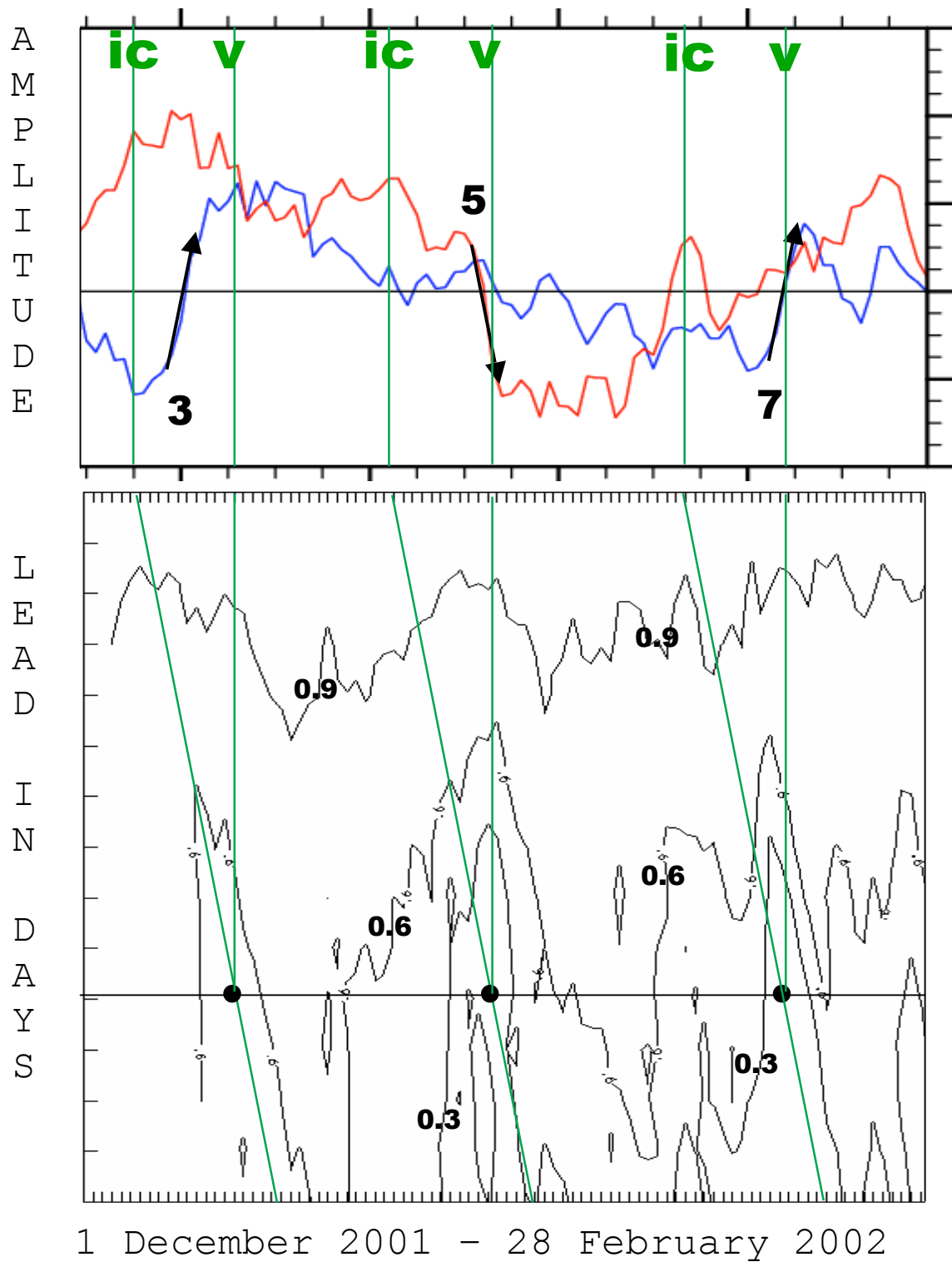


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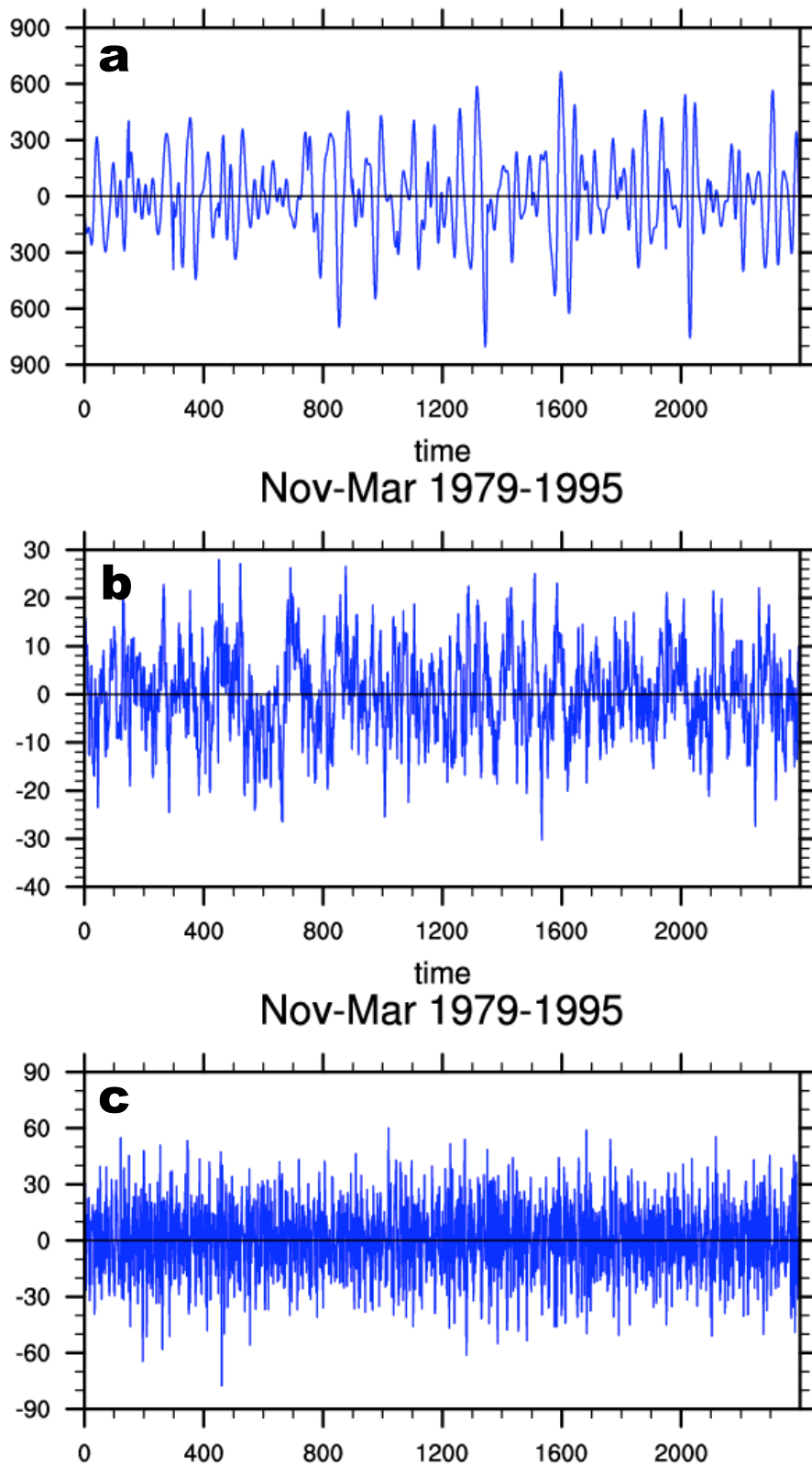


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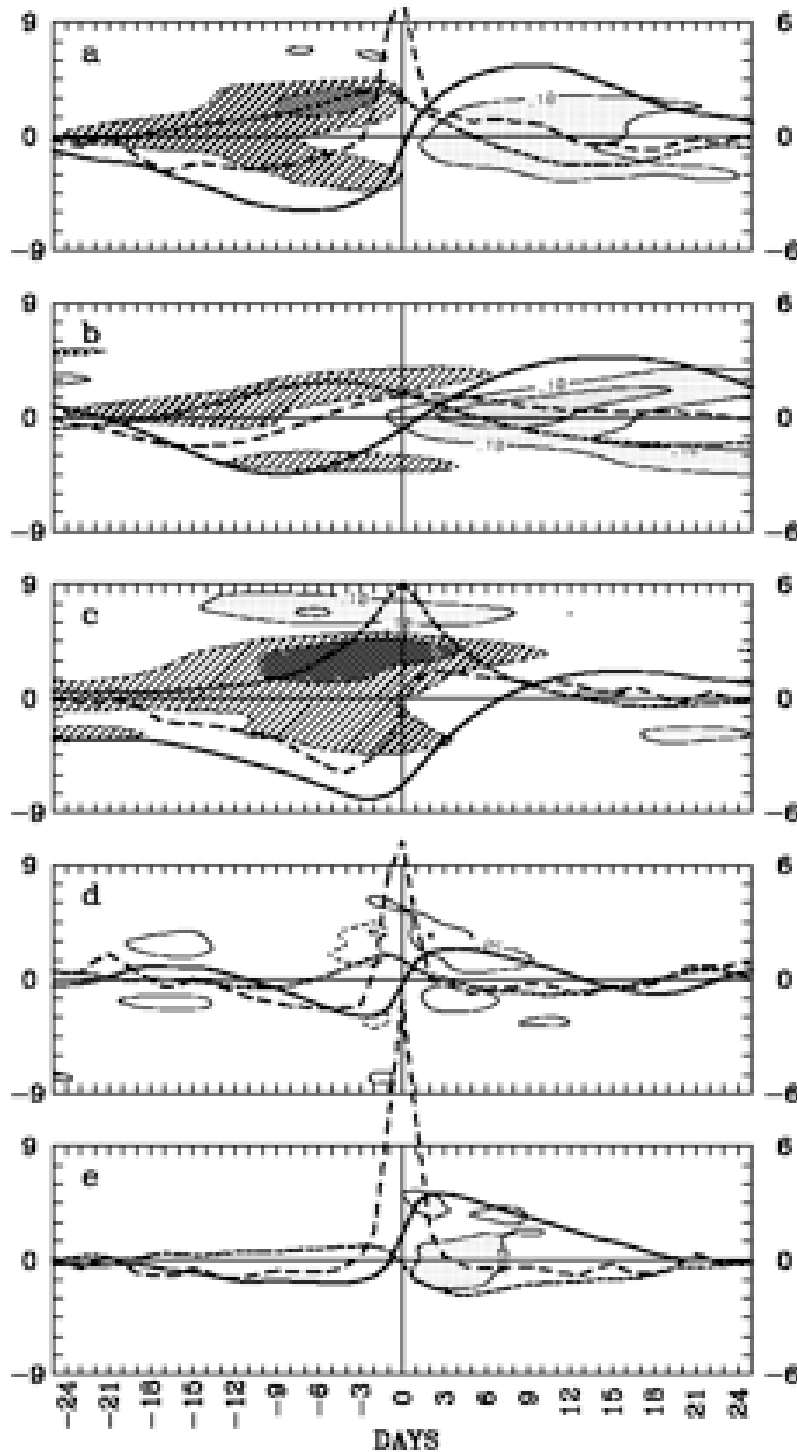


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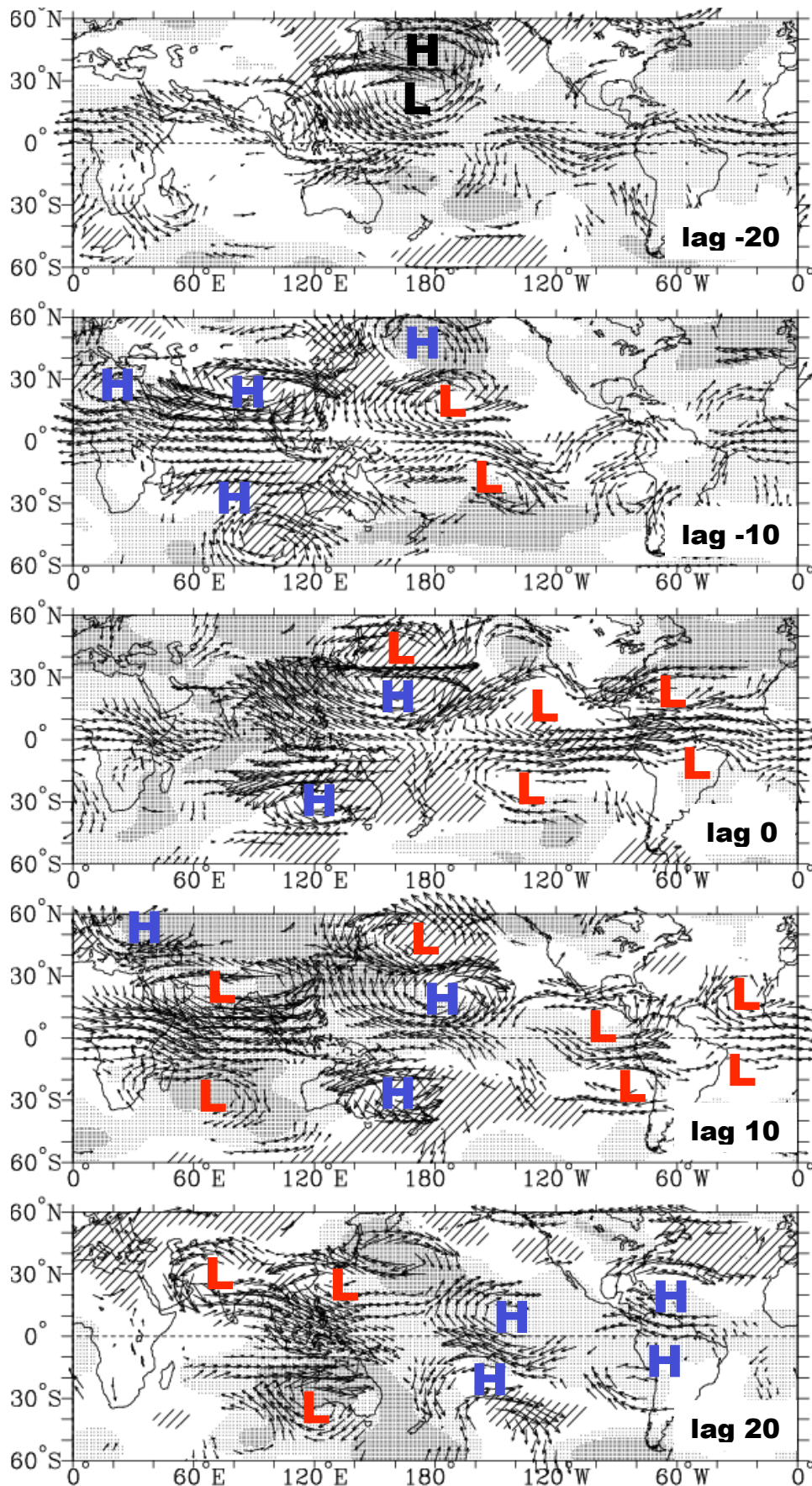


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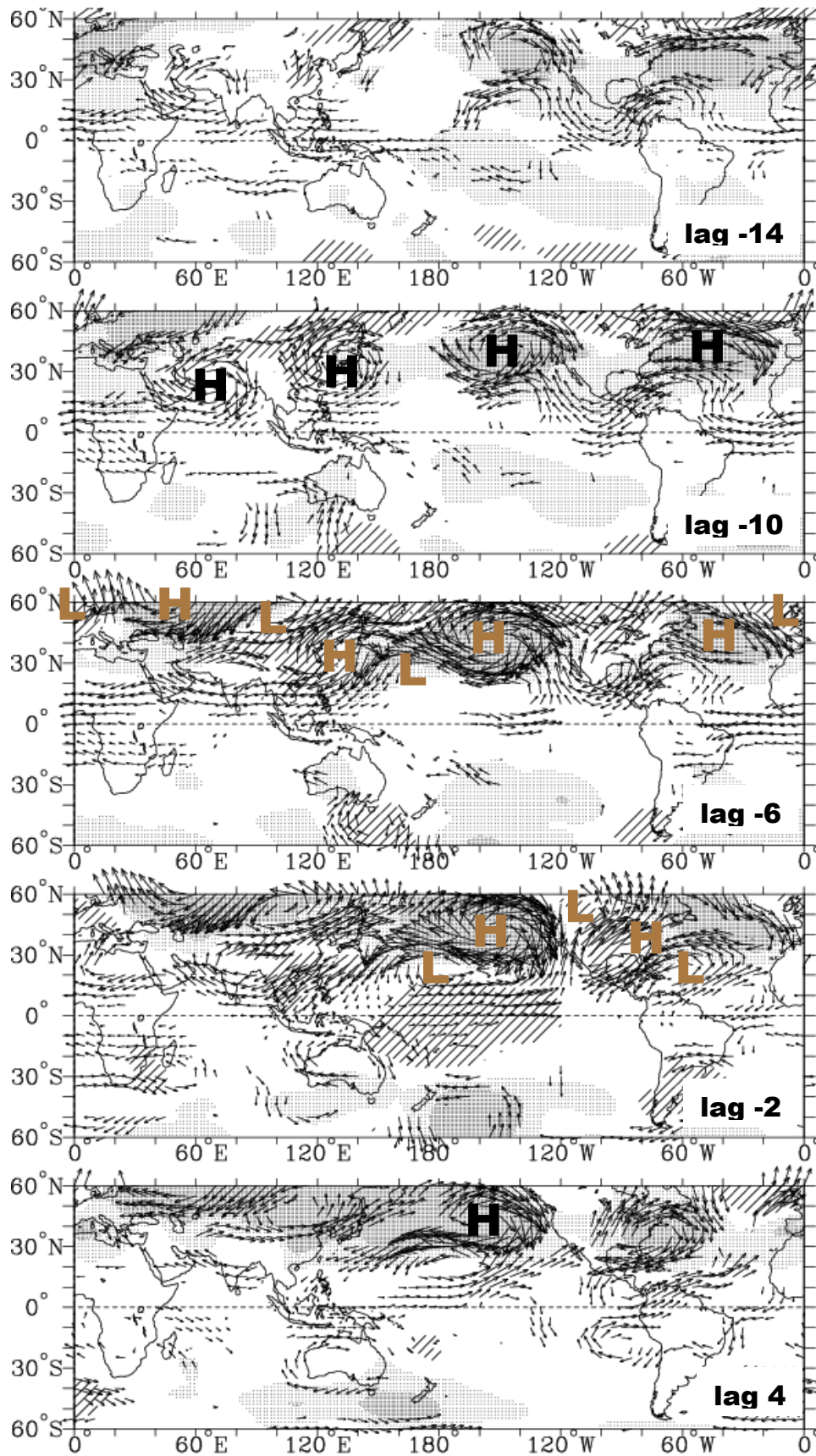


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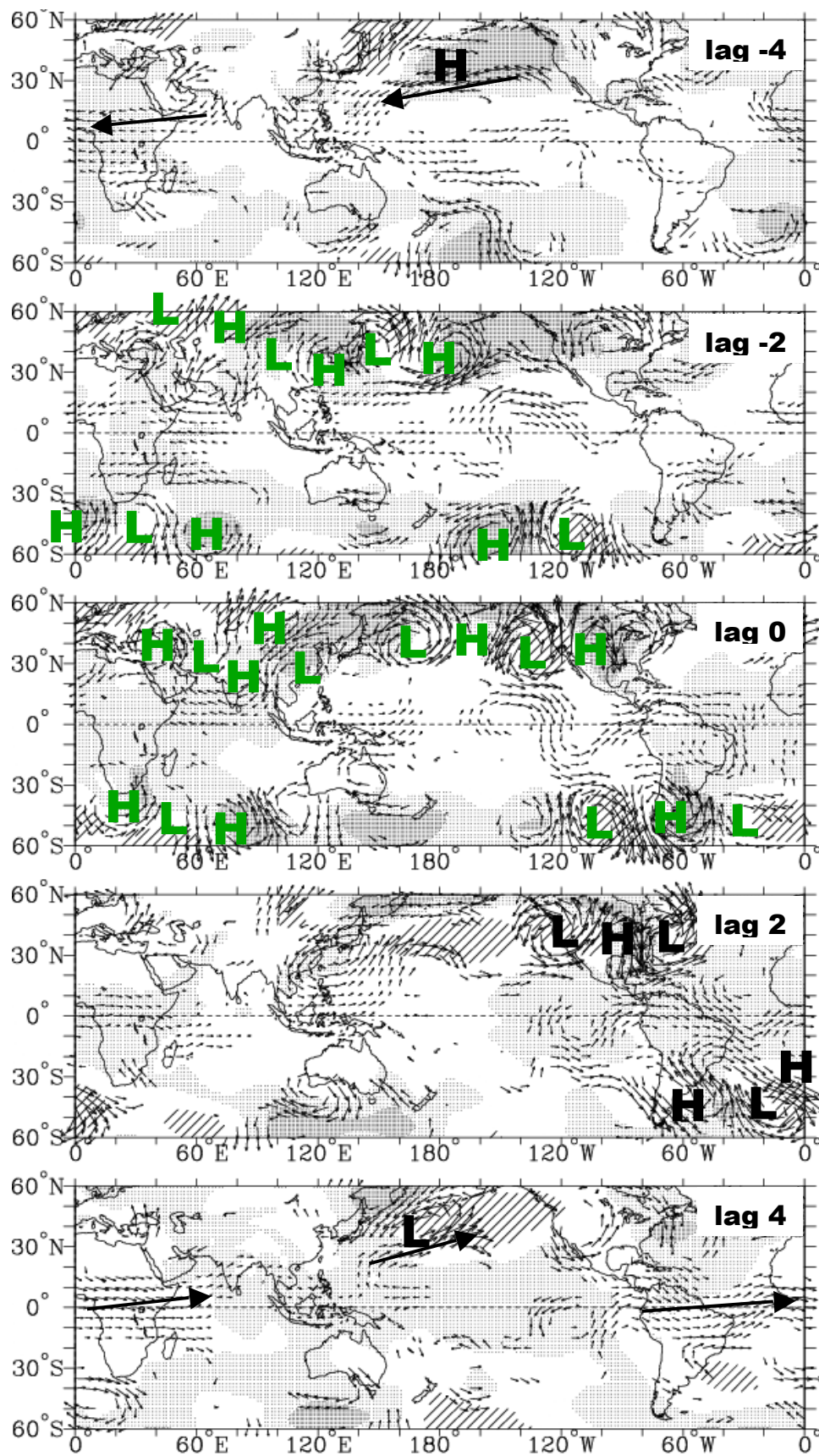


Figure 12. Same as Fig. 10 except lag regressions on the <30 day filtered, global relative AAM tendency index given on Fig. 8c (sequence 3). The green Hs and Ls are placed on Fig. 13 as part of Stage 2 and Stage 4 (opposite phase) of the GSDM.

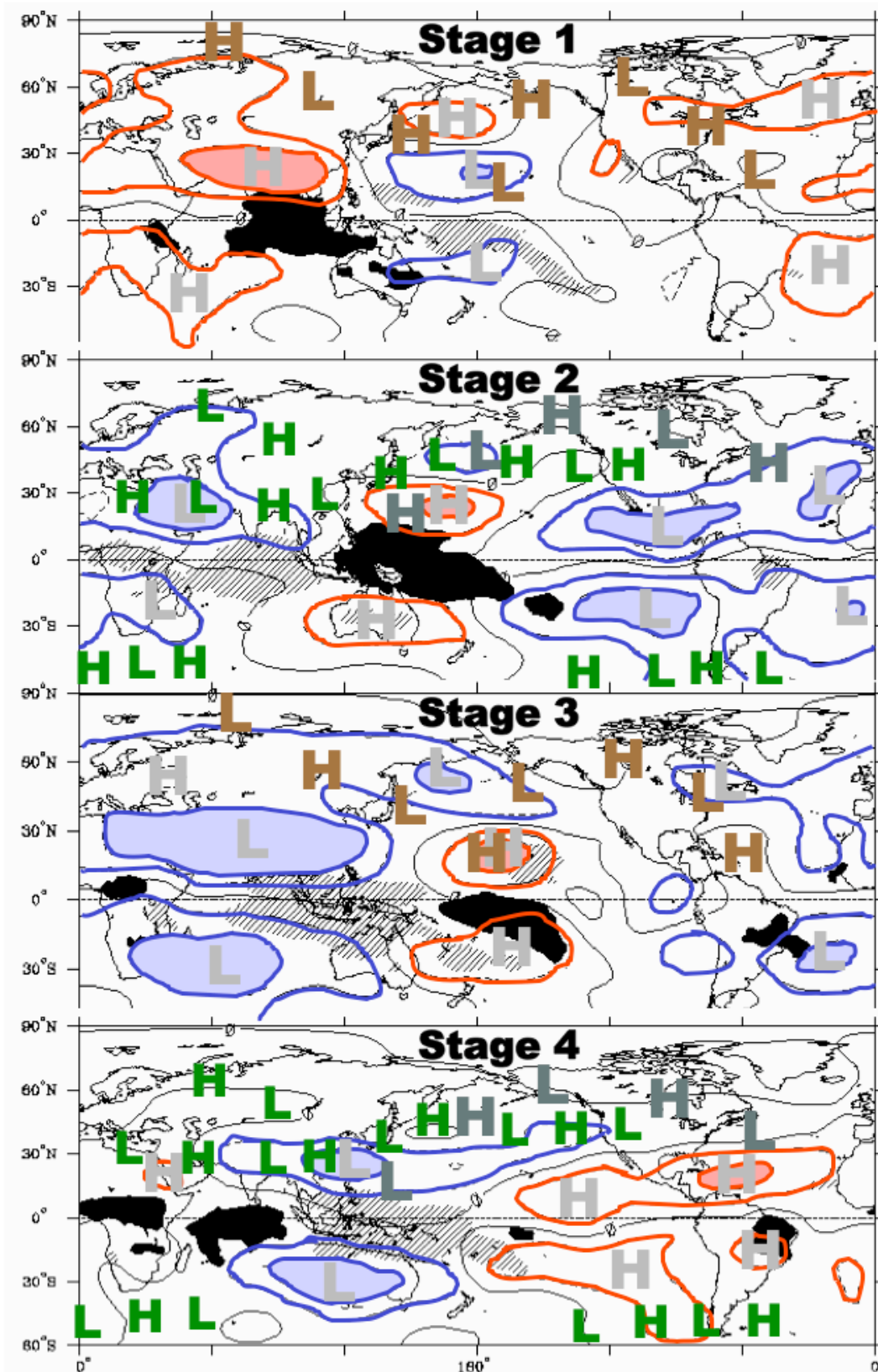


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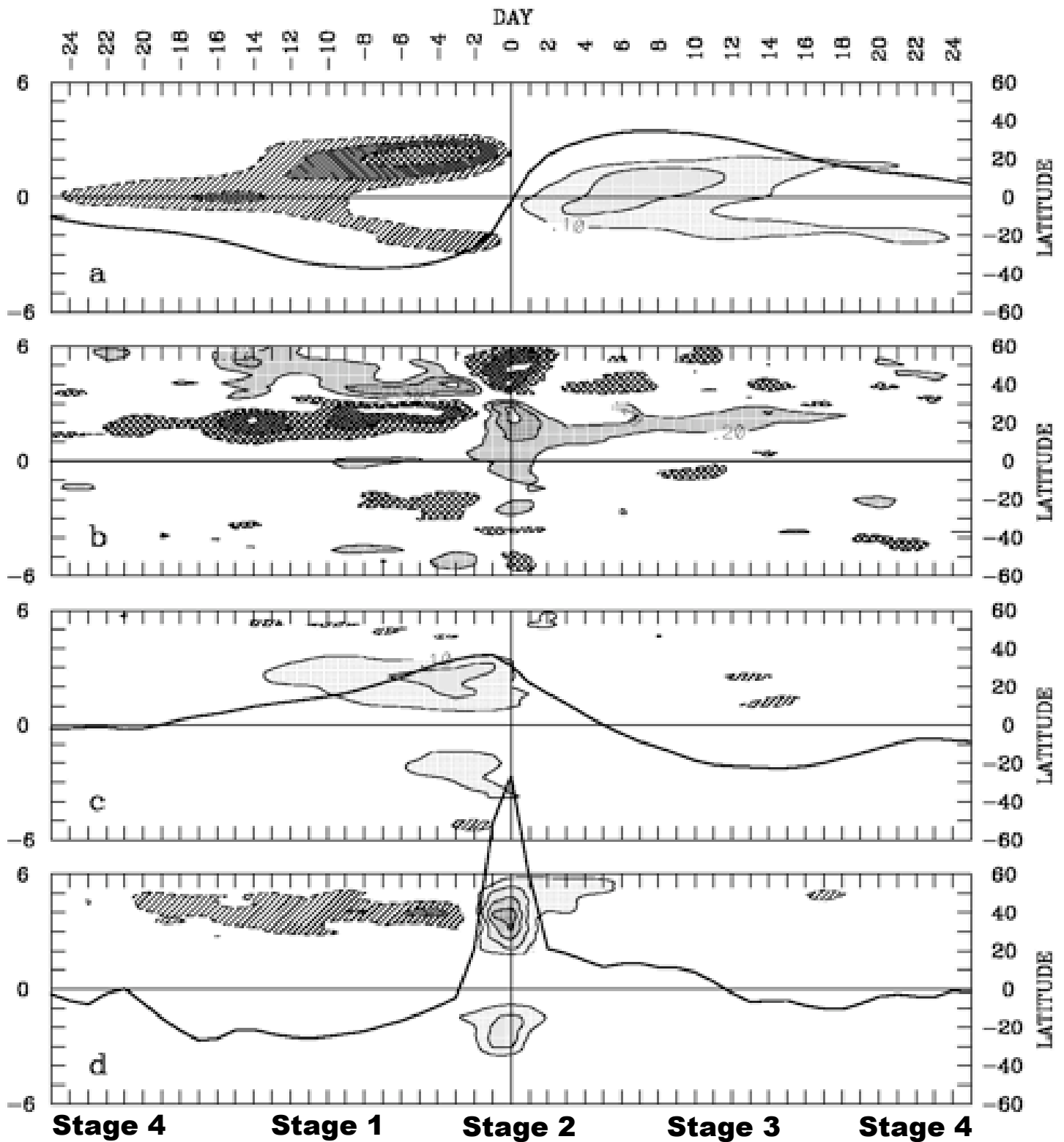


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Table 1. Key dates during the case study. Events 1-7 are tropical convective flare-ups while T1 and T2 are circulation transitions.

<i>Number</i>	<i>Event</i>
1	6 November 2001: Persistent eastern Indian Ocean convection from boreal fall 2001 evolves into MJO #1.
2	4 December 2001: MJO #1 moves into western Pacific Ocean.
3	10 December 2001: MJO # 1 moves to date line and convection then persists for roughly 20 days over relatively warm SSTs (~+0.5-1.0C anomalies). Convection is generally suppressed across Indian Ocean during this time.
4	5 January 2002: Enhanced convection finally ends west of the date line. A series of convectively coupled equatorial Rossby waves start to move west from the central Pacific to Africa.
5	10 January 2002: Enhanced convection over the Indian Ocean evolves into MJO #2.
6	20 January 2002: Convection again flares up in the equatorial date line region (~160E). This area persists for about 10 days while MJO # 2 is further west and moving east.
7	10 February 2002: Enhanced convection develops across the equatorial date line region in association with MJO #2.
T1	Transition number 1, from 19-25 December 2001 . The circulation of the atmosphere shifts to GSDM Stage 3, a response to enhanced central Pacific tropical forcing initiated by flareup 3 on 10 December 2001.
T2	Transition number 2, from 12-18 January 2002 . The atmospheric circulation shifts back to GSDM Stage 1, a response to the reversal of the tropical convective forcing shown by flareups 4 and 5.

Table 2. GSDM stages and their relation to OLR EOF1 and EOF2. The “OLR EOF and lag” column are the EOFs and lags that make up the MJO contribution to the four stages. None of these are shown explicitly in Fig. 10, which is based on EOF 1. It contributes only one phase, namely Stage 1, to the GSDM.

Stage	OLR EOF and lag	Lag of other EOF	Figure 10 shows:
1	EOF1, day -15	EOF2, day 0	neither is shown
2	EOF2, day -10	EOF1, day 0	c: EOF1, day 0
3	EOF2, day 0	EOF1, day +10	d: EOF1, day +10
4	EOF2 day +10	EOF1, day +20	e: EOF1, day +20

Table 3: *Summary of the GSDM stages*

	<i>Characteristics</i>
Stage 1	<ul style="list-style-type: none"> * MJO convection around 110E with enhanced (suppressed) tropical convective forcing across the eastern (western) hemisphere; * Amplified (tropical/subtropical) seasonal base state; * Low AAM / strengthened subtropical momentum sink; * PNA<0 forced by τ_F-τ_M index cycle ($\tau_M < 0$, $\tau_F > 0$ sequence); * Contracted east Asian and North American jets, displaced poleward/split flows over the oceans; * The MJO and τ_F-τ_M index cycle give large positive frictional torques; * La Nina like base state with Pacific Ocean anticyclonic wave breaking; * Wave energy dispersion favors high impact weather across the USA Plains.
Stage 2	<ul style="list-style-type: none"> * MJO convection around 150E * Eastward shifted seasonal base state; * $d(\text{AAM})/dt > 0$ / momentum sink shifting poleward; * The MJO and fast time scale component give large positive mountain torques; * Western Pacific to North American Rossby wavetrain/strong ridge from USA west coast into Alaska; * Asian-Pacific wavetrain favors east Pacific cyclonic wave break for transition to Stage 3; * Much below normal temperatures possible across central and eastern USA.
Stage 3	<ul style="list-style-type: none"> * MJO convection around date line with enhanced (suppressed) tropical convective signal across the western (eastern) hemisphere; * De-amplified seasonal base state; * High AAM / weakened subtropical momentum sink; * PNA>0 forced by mountain torque > 0, friction torque < 0 sequence; * Extended east Asian and North American jets, displaced equatorward /split flows across the continents; * The MJO and τ_F-τ_M index cycle give large negative frictional torques; * El Nino like base state with east Pacific Ocean cyclonic wave breaking; * High impact weather event possible along USA west coast.
Stage 4	<ul style="list-style-type: none"> * MJO convective signal across the western hemisphere, locations at ~160W, 60W and 60E * Westward shifted seasonal base state; * $d(\text{AAM})/dt < 0$ / weakened momentum sink shifting poleward; * MJO and fast component give large negative mountain torque; * Strong subtropical jets, with subtropical westerlies weakening; * Asian-Pacific wavetrain favors anticyclonic wave break across east Pacific Ocean for transition to Stage 1; * Heavy precipitation event possible across southwestern USA.