



# **A method for improved utilization of data from experiments with fishing gear**

**AFS San Francisco**

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DIFRES & Uni. of Southern Denmark, Denmark



# Outline

- ▷ Outline
- ▷ Selectivity - Single Haul
- ▷ Cruise - Multiple Hauls
- ▷ Mean Curves and Interpretations
- ▷ Multiple Cruises
- ▷ Application
- ▷ Data
- ▷ Method - **Conditional Model**
- ▷ Method - **Marginal Model**
- ▷ Results
- ▷ Mean Curves - varying mesh sizes
- ▷ Discussion
- ▷ In the end

- ▲ Fishing gear selectivity - notions and concepts
- ▲ Motivation - Data
- ▲ Methods - Non-technical
- ▲ Results
- ▲ Discussion



# Selectivity - Single Haul

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**Selectivity:** Probability of retention for a length  $l$  fish given it has entered the codend  $r(l)$

$$r(l; \beta) = \frac{\exp(\beta_0 + \beta_1 l)}{1 + \exp(\beta_0 + \beta_1 l)}$$



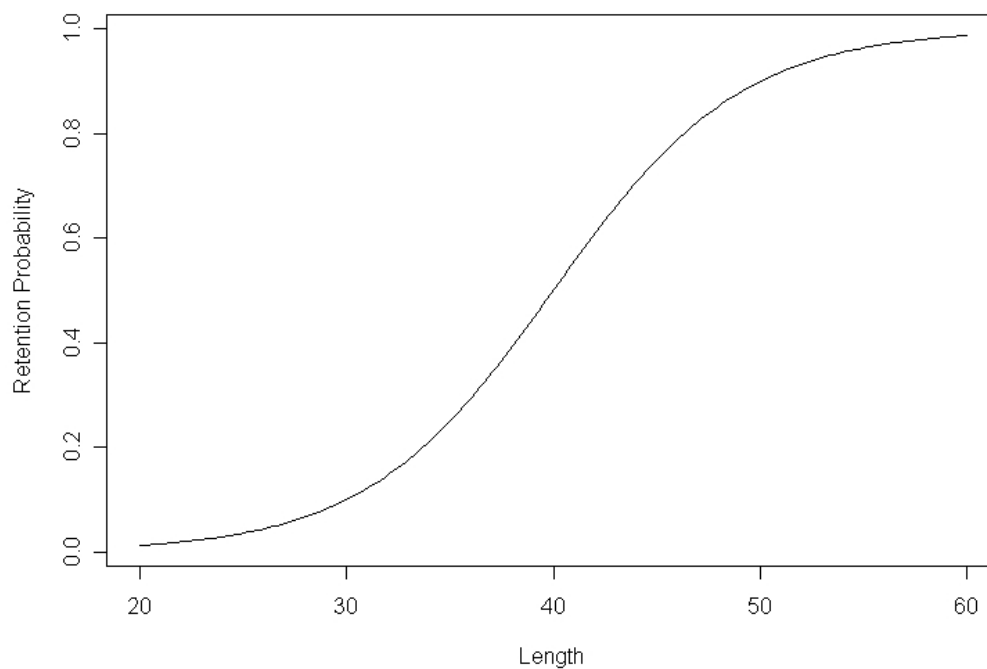
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**Selectivity Curve**





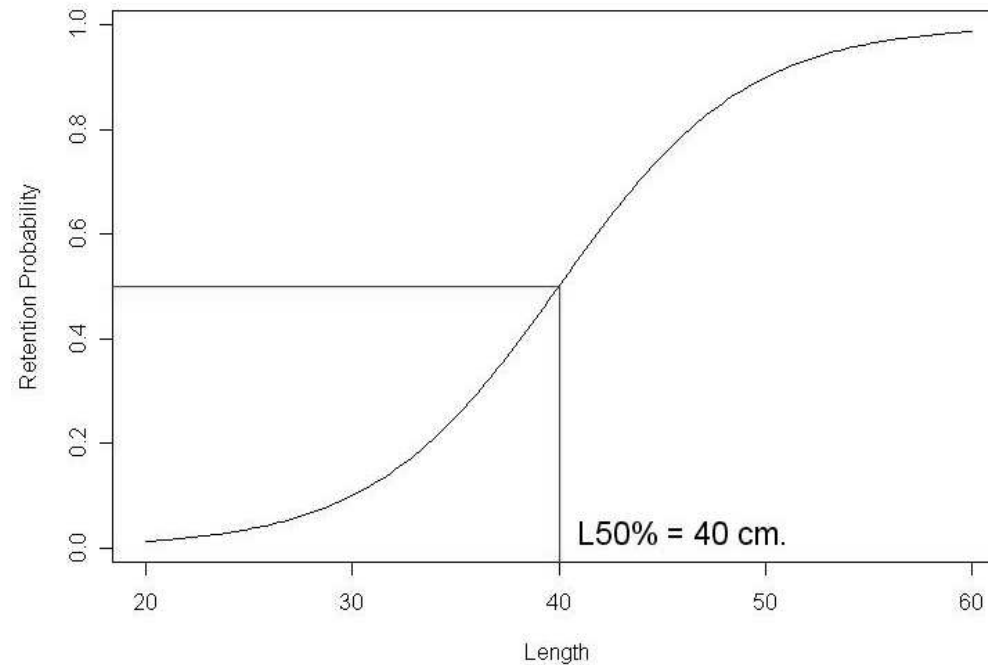
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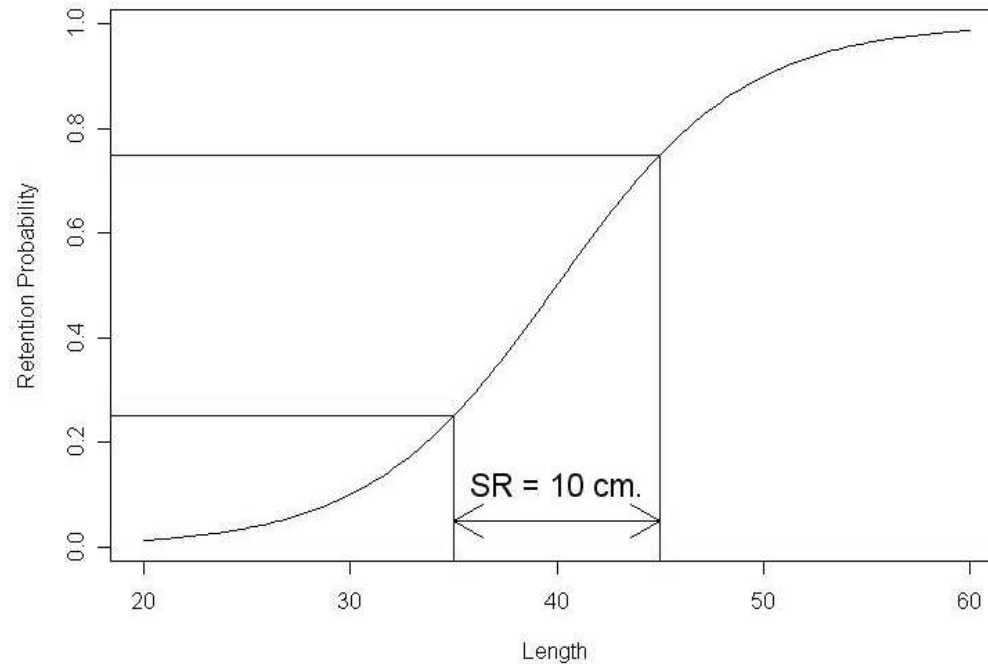
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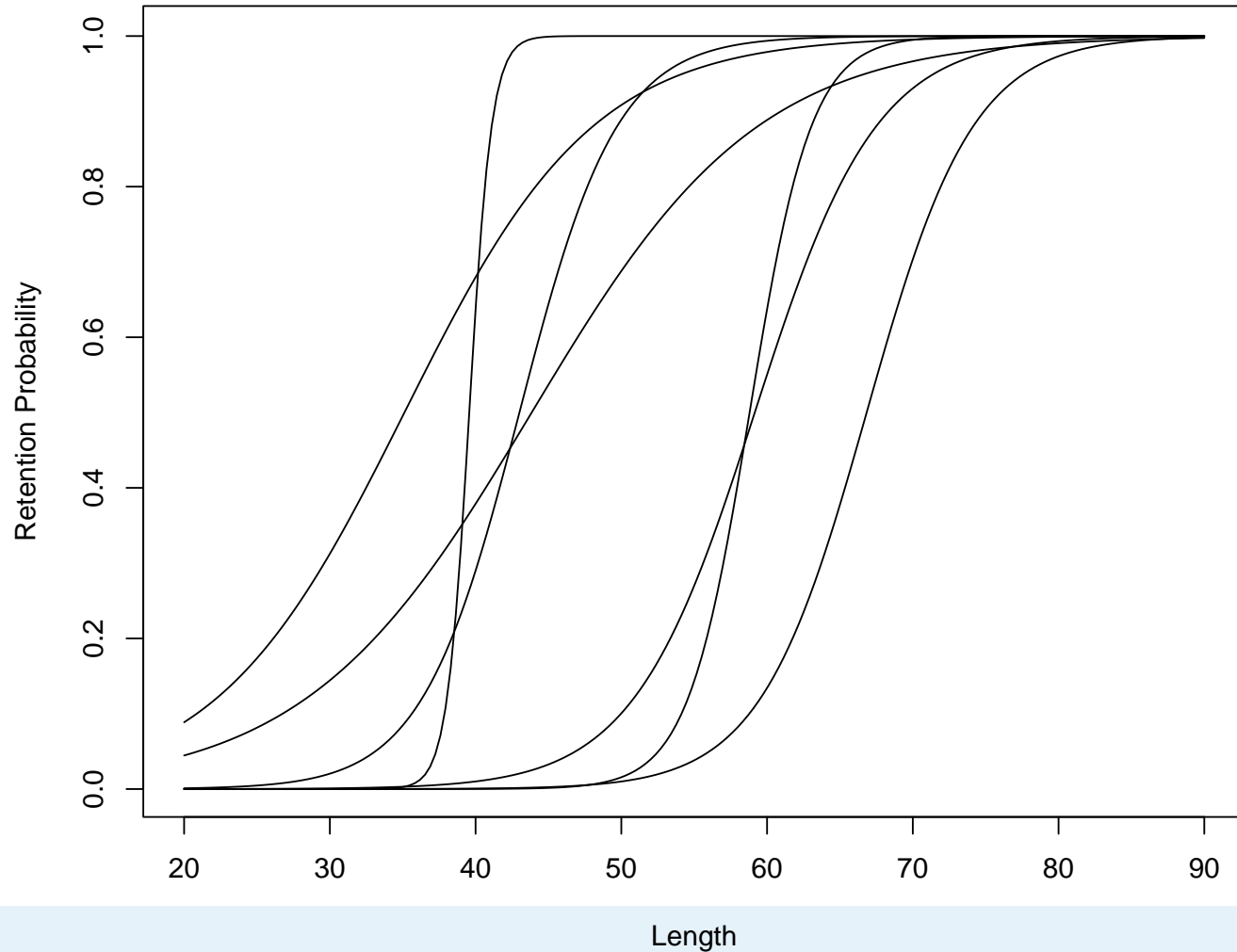
$$(\beta_0, \beta_1)^\top \leftrightarrow (\mathbf{L}_{50}, \mathbf{SR})^\top$$



# Cruise - Multiple Hauls

- Outline
- Selectivity - Single Haul
- **Cruise - Multiple Hauls**
- Mean Curves and Interpretations
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Mean Curves

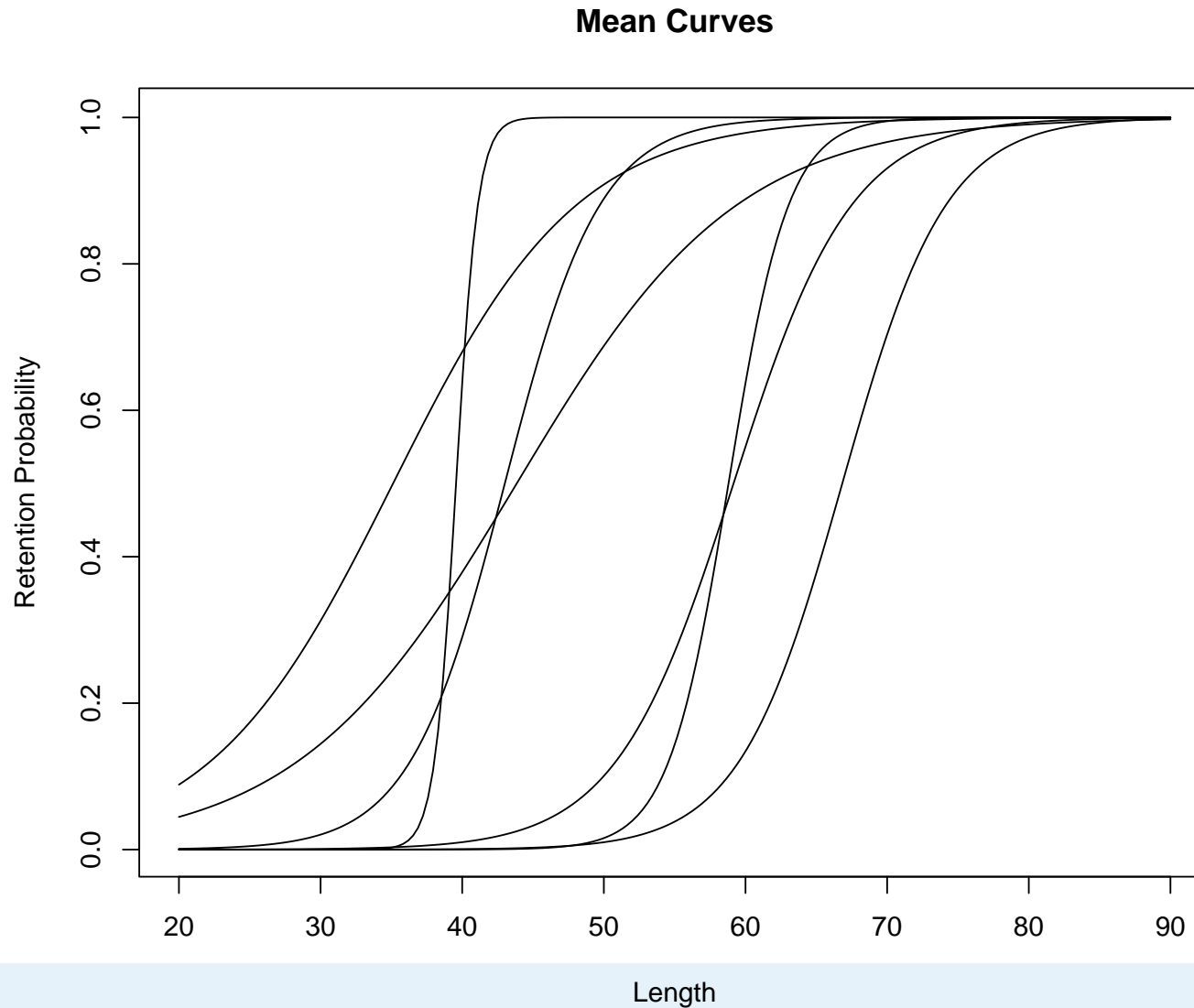






# Mean Curves and Interpretations

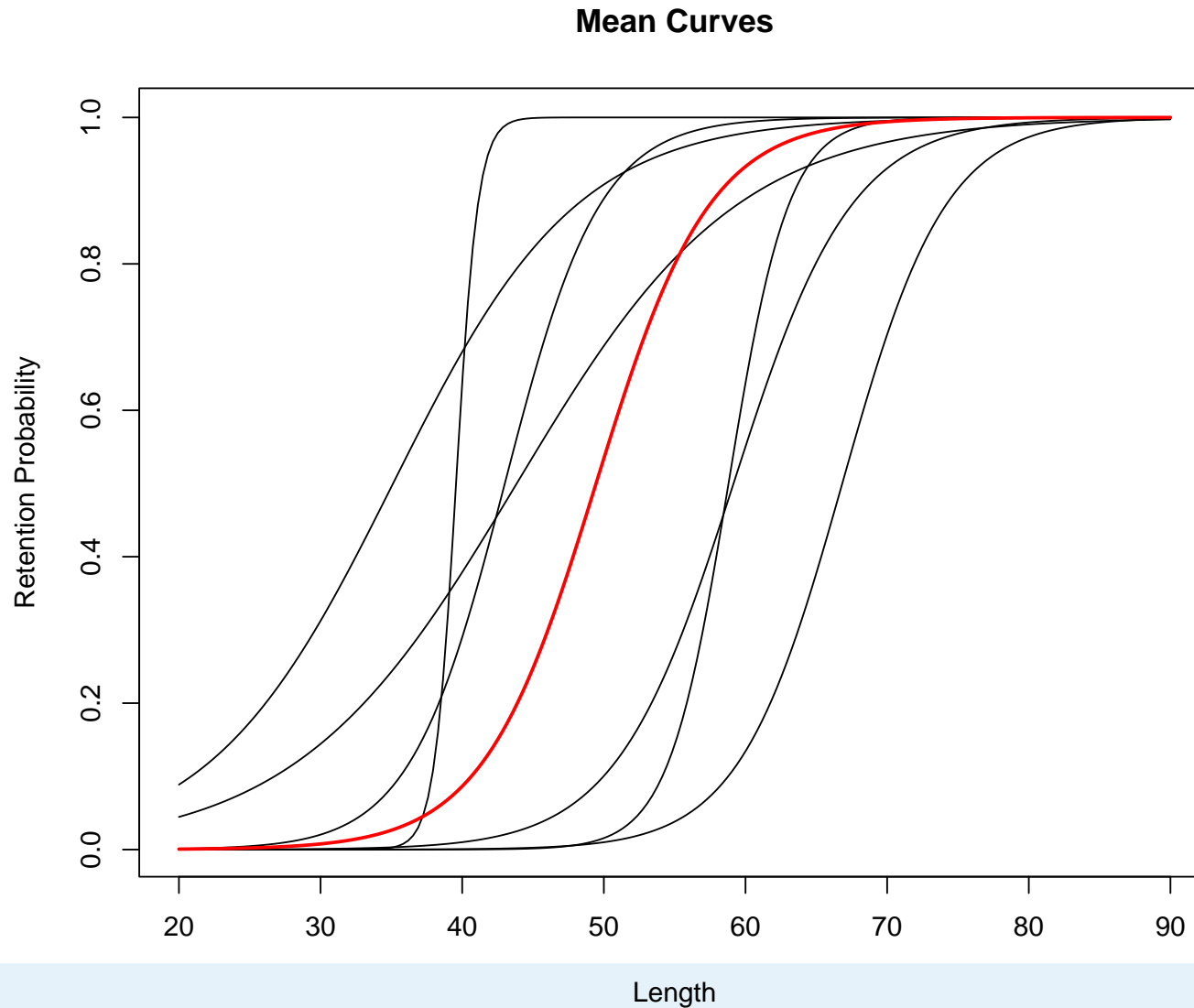
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# Mean Curves and Interpretations

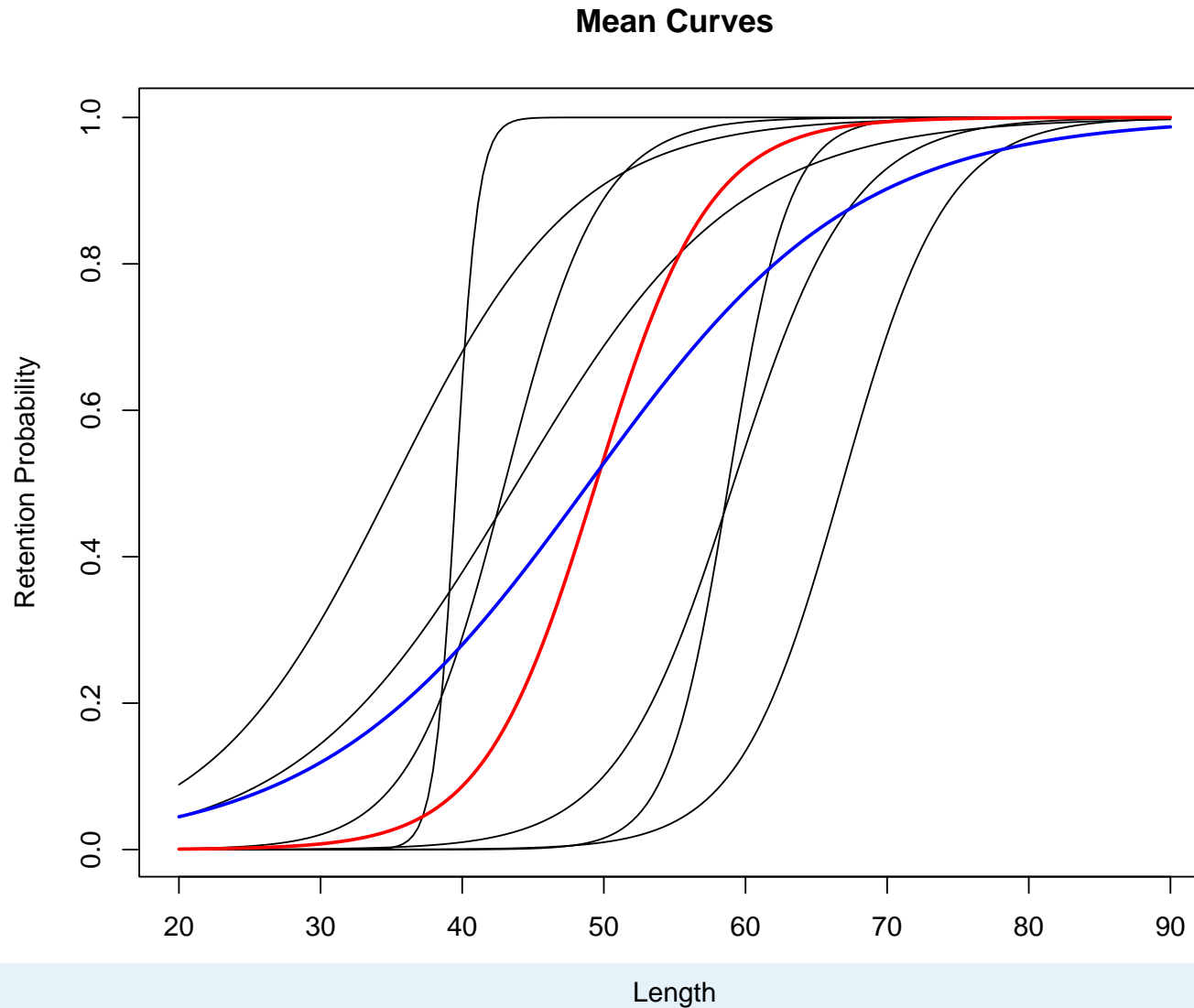
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# Mean Curves and Interpretations

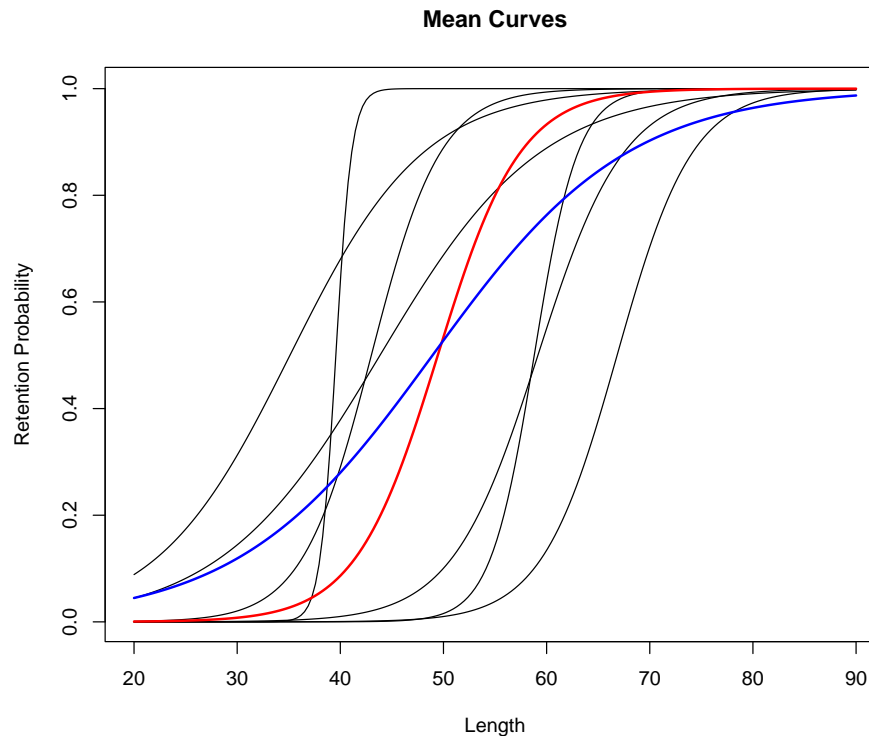
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- ▲ **Conditional Mean - Subject Specific - GLMM**
- ▲ **Marginal Mean - Population Average - GEE**



# Multiple Cruises

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## ▲ Meta Analysis - Combine information from several sources



# Multiple Cruises

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- ◻ In the end

- ▲ Meta Analysis - Combine information from several sources
- ▲ Account for cluster structure in data



# Multiple Cruises

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- ▲ Meta Analysis - Combine information from several sources
- ▲ Account for cluster structure in data
  - Heterogeneity between Hauls within Cruise



# Multiple Cruises

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- ▲ Meta Analysis - Combine information from several sources
- ▲ Account for cluster structure in data
  - Heterogeneity between Hauls within Cruise
  - Heterogeneity between Cruises





# Multiple Cruises

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- ◊ Discussion
- ◊ In the end

- ▲ Meta Analysis - Combine information from several sources
- ▲ Account for cluster structure in data
  - Heterogeneity between Hauls within Cruise
  - Heterogeneity between Cruises
- ▲ Purpose of the analysis? Conditional or Marginal



# Multiple Cruises

- ◊ Outline
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- ◊ In the end

- ▲ Meta Analysis - Combine information from several sources
- ▲ Account for cluster structure in data
  - Heterogeneity between Hauls within Cruise
  - Heterogeneity between Cruises
- ▲ Purpose of the analysis? Conditional or Marginal
- ▲ Non-compatible data



# Multiple Cruises

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- ▲ Meta Analysis - Combine information from several sources
- ▲ Account for cluster structure in data
  - Heterogeneity between Hauls within Cruise
  - Heterogeneity between Cruises
- ▲ Purpose of the analysis? Conditional or Marginal
- ▲ Non-compatible data
- ▲ Different covariates



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- ▲ Meta Analysis - Combine information from several sources
- ▲ Account for cluster structure in data
  - Heterogeneity between Hauls within Cruise
  - Heterogeneity between Cruises
- ▲ Purpose of the analysis? Conditional or Marginal
- ▲ Non-compatible data
- ▲ Different covariates
- ▲ **PRAGMATIC APPROACH TO DATA!**



# Application

- ◂ Outline
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## ▲ Baltic Sea - Cod stock at critical level



# Application

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- ▲ Baltic Sea - Cod stock at critical level
  - BACOMA Codend



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- ▲ Baltic Sea - Cod stock at critical level
  - BACOMA Codend
  - T90 Codend



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- ▲ Baltic Sea - Cod stock at critical level
  - BACOMA Codend
  - T90 Codend
- ▲ Request for advice from IBSC to ICES ACFM





# Application

- ◻ Outline
- ◻ Selectivity - Single Haul
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- ▲ Baltic Sea - Cod stock at critical level
  - BACOMA Codend
  - T90 Codend
- ▲ Request for advice from IBSC to ICES ACFM
- ▲ Meta Analysis based on all available and relevant data



# Data

- ▷ Outline
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## ▲ 25 Cruises



# Data

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▲ 25 Cruises

▲ 483 Hauls



# Data

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- ▲ 25 Cruises
- ▲ 483 Hauls
- ▲ Two experimental type
  - Covered Codend
  - Twin Trawls



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- ▲ 25 Cruises
- ▲ 483 Hauls
- ▲ Two experimental type
  - Covered Codend
  - Twin Trawls
- ▲ Key Variables



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- ▲ 25 Cruises
- ▲ 483 Hauls
- ▲ Two experimental type
  - Covered Codend
  - Twin Trawls
- ▲ Key Variables
  - GEAR TYPE: BACOMA and T90



# Data

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  - Covered Codend
  - Twin Trawls
- ▲ Key Variables
  - GEAR TYPE: BACOMA and T90
  - MESH SIZE



# Data

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- ▲ Key Variables
  - GEAR TYPE: BACOMA and T90
  - MESH SIZE
  - OPEN MESHES CIRCUMF.





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## ▲ 25 Cruises

## ▲ 483 Hauls

## ▲ Two experimental type

- Covered Codend
- Twin Trawls

## ▲ Key Variables

- GEAR TYPE: BACOMA and T90
- MESH SIZE
- OPEN MESHES CIRCUMF.
- EXPERIMENTAL TYPE: Cov. Codend and Twin Trawl



# Data

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- ▲ Key Variables
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  - MESH SIZE
  - OPEN MESHES CIRCUMF.
  - EXPERIMENTAL TYPE: Cov. Codend and Twin Trawl
  - VESSEL TYPE: Research and Commercial



# Data

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## ▲ 25 Cruises

## ▲ 483 Hauls

## ▲ Two experimental type

- Covered Codend
- Twin Trawls

## ▲ Key Variables

- GEAR TYPE: BACOMA and T90
- MESH SIZE
- OPEN MESHES CIRCUMF.
- EXPERIMENTAL TYPE: Cov. Codend and Twin Trawl
- VESSEL TYPE: Research and Commercial
- Other variables



# Method - Conditional Model

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A proxy pragmatic approach:

▲ **SELECT Model:** Estimates of  $(L_{50}, SR)$  for each haul in each cruise



# Method - Conditional Model

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A proxy pragmatic approach:

- ▲ **SELECT Model**: Estimates of  $(L_{50}, SR)$  for each haul in each cruise
- ▲ Apply **Fryers method** to each cruise to obtain cruise level estimates of  $(L_{50}, SR)$



# Method - Conditional Model

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A proxy pragmatic approach:

- ▲ **SELECT Model:** Estimates of  $(L_{50}, SR)$  for each haul in each cruise
- ▲ Apply **Fryers method** to each cruise to obtain cruise level estimates of  $(L_{50}, SR)$
- ▲ Apply **Fryers method** to cruise level estimates



# Method - Marginal Model

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## ▲ GEE: Generalized Estimating Equations



# Method - Marginal Model

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## ▲ **GEE**: Generalized Estimating Equations

## ▲ **CONSs**:

- **NOT** a likelihood approach
- No explicit model for random cluster variation





# Method - Marginal Model

- ◻ Outline
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## ▲ **GEE**: Generalized Estimating Equations

### ▲ **CONSs**:

- **NOT** a likelihood approach
- No explicit model for random cluster variation

### ▲ **PROs**

- Implemented in many standard packages (e.g. SAS, R)
- "Good" asymptotic behaviour of estimators
- Robust



# Method - Marginal Model

- ◊ Outline
- ◊ Selectivity - Single Haul
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## ▲ **GEE**: Generalized Estimating Equations

### ▲ **CONSs**:

- **NOT** a likelihood approach
- No explicit model for random cluster variation

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- "Good" asymptotic behaviour of estimators
- Robust



# Method - Marginal Model

- ◻ Outline
- ◻ Selectivity - Single Haul
- ◻ Cruise - Multiple Hauls
- ◻ Mean Curves and Interpretations
- ◻ Multiple Cruises
- ◻ Application
- ◻ Data
- ◻ Method - **Conditional Model**
- ◻ Method - **Marginal Model**
- ◻ Results
- ◻ Mean Curves - varying mesh sizes
- ◻ Discussion
- ◻ In the end

## ▲ **GEE**: Generalized Estimating Equations

### ▲ **CONSs**:

- **NOT** a likelihood approach
- No explicit model for random cluster variation

### ▲ **PROs**

- Implemented in many standard packages (e.g. SAS, R)
- "Good" asymptotic behaviour of estimators
- Robust



# Results

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## ▲ **Conditional Model:**

## ▲ **Marginal Model:**



# Results

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## ▲ **Conditional Model:**

- $L_{50} \sim 0.3534 * MeshSize$
- $SR \sim 0.05242 * MeshSize + 3.107 * I_{CommercialVessel}$

## ▲ **Marginal Model:**



# Results

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## ▲ **Conditional Model:**

- $L_{50} \sim 0.3534 * MeshSize$
- $SR \sim 0.05242 * MeshSize + 3.107 * I_{CommercialVessel}$

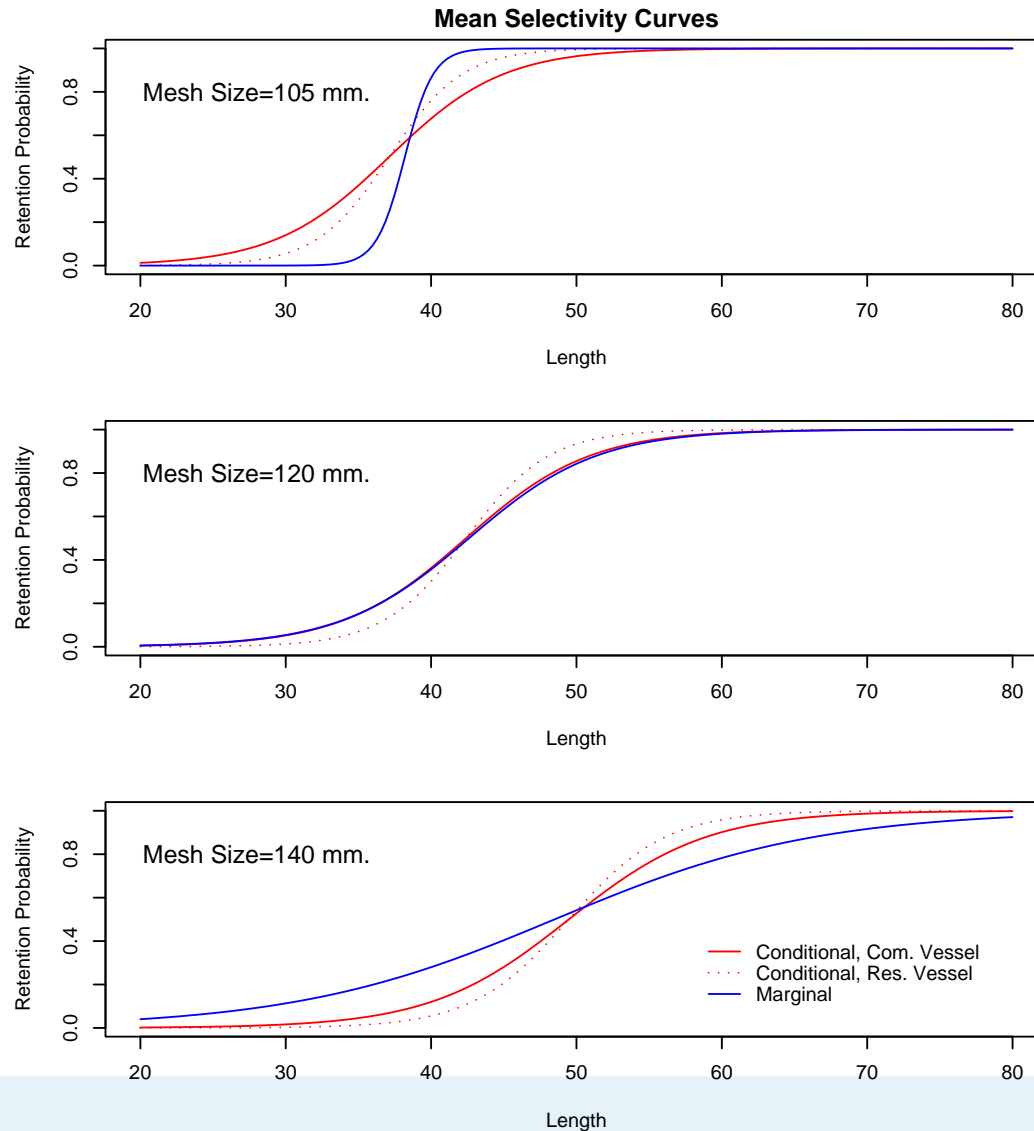
## ▲ **Marginal Model:**

- $L_{50} \sim 7.2815 + 0.2944 * MeshSize$
- $SR \sim -50.6758 + 0.503 * MeshSize$



# Mean Curves - varying mesh sizes

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# Discussion

- ◻ Outline
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- ▲ Room and need for further development
- ▲ Integrate over catch weight
- ▲ How can we improve the quality of data?
- ▲ Bayesian Approach





# In the end

- ◂ Outline
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*”I was so much older then,  
I’m younger than that now . . .”*

**Bob Dylan**