

Optimization Tools for *in silico* **Proteomics**



Peter A. DiMaggio Jr. and Christodoulos A. Floudas Department of Chemical Engineering Princeton University March 14th, 2007





Discovery at the Microscopic Level

Computational Biology and Genomics

- Structure Prediction in Protein Folding
 - Secondary Structure
 - Tertiary Structure
- Structure Refinement for NMR
- Dynamics of Protein Folding
- Protein-Protein Interactions
- De Novo Protein Design
- Topology of Signal Transduction Networks and Metabolic Pathways
- Proteomics: Peptide & Protein Identification



REVOLUTION OF GENOMICS





Computational Biology and Genomics

Structure Prediction in Lennard-Jones Clusters & Acyclic Molecules (90-95)

Structure Prediction in Protein Folding (95-)









Force Field Development (01-)

De Novo Protein Design (01-)

Protein-Peptide Interactions (95-03)

Metabolic and Signal Transduction Networks (95-)

Proteomics: Peptide & Protein Identification (05-)





Computer Aided Systems Laboratory

Professor Christodoulos A. Floudas – Pl



CASI Members:

Scott R. McAllister, Ashwin Subramani – protein structure prediction Ho Ki Fung, Meghan Bellows – *de novo* protein design Rohit Rajgaria – high-resolution force field development Peter A. DiMaggio – peptide and protein identification Meng Piao Tan – signal transduction pathways



All components are aimed towards the development of optimization tools for in silico proteomics



Proteomics

Specific Aim 1: Investigate and develop a de novo computational approach for peptide identification based exclusively on information of the ion peaks in the peptide spectrum

Specific Aim 2: Study and develop a new hybrid in silico method which will combine the de novo approach of Specific Aim 1 with database techniques for peptide identification

Specific Aim 3: Incorporate uncertainty into the de novo framework to address experimental uncertainty in problem parameters

Specific Aim 4: Study and develop computational methods for protein identification given the de novo prediction and/or hybrid prediction of the individual peptides

Specific Aim 5: Research and develop computational methods and experimental protocols for protein quantification

Problem Definition and Introduction

Fundamental problem in proteomics:

Protein and peptide identification and quantification

Advances in high-throughput experimentation

High-performance liquid chromatography (HPLC) coupled with tandem mass spectrometry (MS/MS)





Mass spec facilities at Princeton University

Need for rigorous computational tools for peptide/protein identification

Peptide & Protein Identification via Tandem MS

Database-based methods

- Correlate the experimental spectra with spectra of peptides/proteins which exist in the databases
- SEQUEST Eng et al. (1994), Mascot Perkins et. al (1999), SCOPE Bafna and Edwards (2001), MS-CONVOLUTION and MS-ALIGNMENT – Pevzner et. al (2001), Poptiam – Hernandez et. al (2003)

De Novo Methods

- Predict peptides without sequence databases
- Exhaustive listing; sub-sequencing; graphical
- Graph theory and shortest path algorithms
- Graph theory and dynamic programming
- Bayesian scoring of random peptides

Lutefisk – Taylor and Johnson (1997,2001), SHERENGA – Dancik et. al (1999), PEAKS – Ma et al. (2003), NovoHMM – Fischer et al. (2005), PepNovo – Frank and Pevzner (2005), EigenMS – Bern and Goldberg (2006)

Challenges

• Tandem MS are missing ion peaks due to incomplete fragmentation and/or instruments with low mass-to-charge ratio (m/z) cutoff (i.e., ion trap mass analyzers)

- Incorporating parametric uncertainty in the measured values for ion peaks during peptide identification
- Existing de novo techniques enumerate an exhaustive number of candidate sequences from the tandem mass spectrum
- No straightforward method for including posttranslational modifications into existing frameworks

Tandem MS/MS

□ Collision-induced dissociation (CID) causes a positively-charged peptide to fragment along its backbone and results in many types of fragment ions in the tandem mass spectrum (i.e., a, b, c, x, y, x, etc.)



Hypothetical parent peptide*

□ Objective:

Use these fragment ions to predict the amino acid sequence of the parent peptide

□ Issues: Identifying ion types in the mass spectrum is nontrivial

ebCTC

Introduction to De Novo Peptide Identification

The De Novo Peptide Identification Problem:

Given the tandem mass spectrum (MS/MS) of a peptide, derive the primary sequence of the peptide without consulting other sources of information (i.e., protein databases) Q: Which of these possible primary sequences corresponds to the correct peptide?



Traditional De Novo Methods



^{(2003),} Chen and Bingwen (2003), Jarman et. al (2003), Frank and Pevzner (2005), Bern and Goldberg (2006)

ebCTC



Database Methods (cont'd)

□ Cross-Correlation (e.g., SEQUEST*)



*Eng et. al (1994)

Database Methods (cont'd)

□ Probabilistic Matching* (e.g., Mascot, SCOPE)

Predict primarily y- and b-ions, and their offsets, based on the following formulae:

$$b_{i} = \sum_{j=1}^{i} mass(AA_{j}) + 1 \qquad y_{n-i} = 19 + \sum_{j=i+1}^{n} mass(AA_{j})$$

Q: Is ion match with experimental spectrum
Random?

"A": Likelihood ratio hypothesis test (Bafna and Edwards (2001), Havilio et. al (2003))

□ Null hypothesis (Sadygov and Yates (2003))

□ Integration of spectral dependencies into model (Bafna and Edwards (2001), Havilio et. al (2003))

Empirically estimated probabilities

*Perkins et. al (1999), Bafna and Edwards (2001), Pevzner et. al (2001), Havilio et. al (2003), Hernandez et. al (2003), Sadygov and Yates (2003)

Drawbacks of Existing Methods

De Novo Methods

- Exhibit variable prediction accuracies
- Computationally intensive \rightarrow exhaustive enumeration
- Many are instrument dependent

Database Methods

- False predictions if missing protein in database
- Difficult to identify post-translational modifications / mutations
- Often exhibit dependencies on training data sets and databases

Our Approach to Solve Peptide the Identification Problem

Novel Technique: Using Mixed-Integer Linear Optimization (MILP) to formulate the peptide sequencing problem



Binary variables {0-1 variables} define whether or not peaks (p_i) and paths between peaks (w_{ij}) are used in the construction of the candidate sequence, where 1 indicates yes and 0 indicates no

Algorithmic Overview





Output: Peptide / Rank Ordered List of Peptides

Components of Framework:



II. Mathematical Model for Peptide Identification

III. Postprocessing of Candidate Sequences

I. Preprocessing Algorithm

Determine the boundary condition (BC^{tail}) for the N-terminus of the y-ion series



21 Threshold = 0.1* Maximum intensity peak in spectrum



II. Mathematical Model: Constraints

Conservation of Mass

$$\sum_{\substack{(i,j)\in S_{i,j}\\(i,j)\in S_{i,j}}} M_{i,j} \cdot w_{i,j} \le m_P + tolerance$$

tolerance "relaxes" equality

Boundary Conditions (BC)

$$\sum_{i \in BC_i^{head}} \sum_{j \in S_{i,j}} w_{i,j} = 1$$
$$\sum_{j \in BC_j^{tail}} \sum_{i \in S_{i,j}} w_{i,j} = 1$$

- BC elements are dependent on ion type
- BC elements are checked in a preprocessing algorithm
- If elements missing then BC set is adjusted

Complementary lons

 $p_i + p_j \le 1 \qquad \forall (i,j) \in C_{i,j}$

 $b \longleftrightarrow y$ $a \longleftrightarrow x$

C ←→ Z

Eliminates different ions of different type

II. Mathematical Model: MILP

$$\begin{split} & \underset{p_{k}, w_{i,j}}{\overset{MAX}{p_{k}, w_{i,j}}} \sum_{(i,j) \in S_{i,j}} \lambda_{j} \cdot w_{i,j} \\ s.t. & \sum_{(i,j) \in S_{i,j}} M_{i,j} \cdot w_{i,j} \leq m_{P} + tolerance \\ & \sum_{(i,j) \in S_{i,j}} M_{i,j} \cdot w_{i,j} \geq m_{P} - tolerance \\ & p_{i} + p_{j} \leq 1 \qquad \forall (i,j) \in C_{i,j} \\ & & \sum_{j \in S_{i,j}} w_{i,j} = p_{i} \\ & between p_{i} \& w_{i,j} \\ & & \sum_{j \in S_{i,j}} w_{j,i} = p_{i} \\ & & \forall i \in BC_{i}^{head} \\ & & \sum_{\substack{j \in S_{i,j}} \sum_{j \in S_{i,j}} w_{i,j} = 1 \\ & & \sum_{j \in BC_{j}^{tail}} \sum_{i \in S_{i,j}} w_{i,j} = 1 \\ & & \sum_{j \in BC_{j}^{tail}} \sum_{i \in S_{i,j}} w_{i,j} = 1 \\ & & Flow \ conservation \ law \\ & & \sum_{\substack{j \in S_{j,i}} \sum_{w_{i,j} - \sum_{k \in S_{i,k}} w_{i,k} = 0 \\ & & w_{i,j}, \ p_{k} = 0 - 1 \\ & & \forall (i,j), (k) \\ \end{split}$$

ebCTC

P.A. DiMaggio and C.A. Floudas, AIChE Journal, 53(1), 160-173 (2007).

II. Two-Stage Framework

During the Stage I calculations, the derivation of the candidate sequence is done using only single amino acid weights



□ It is common that tandem MS are missing ion peaks due to incomplete fragmentation and/or instruments with low m/z cutoff (i.e., ion trap mass analyzers)

□ Stage II calculations allow for combinations of amino acids to connect ion peaks

Combinations of amino acids are penalized in objective function to bias use of single amino acid weights in derivation of candidate sequences

III. Post-Processing Algorithm

□ Amino acid permutations substituted for weights in candidate sequences from Stage II calculations

□ No current models exist for accurate prediction of ion intensity trends as a function of peptide composition for generalized mass analyzers

Assume normalized intensity distribution + reward / penalty based on observation/absence of supporting ions

□ Cross-correlate of all theoretical mass spectra of candidate peptide sequences with experimental tandem mass spectrum



Peptide identification via Integer Linear Optimization and Tandem mass spectrometry

Illustrative Example for PILOT: DAFLGSFLYEYSR



PostProcessing: DAFLGSFLYEYSR

ebCTC

X = low confidence residue

P.A. DiMaggio and C.A. Floudas, AIChE Journal, 53(1), 160-173 (2007).

Comparative Study

To benchmark the performance of **PILOT**, we tested it on several tandem mass spectra from

- Quadrupole time-of-flight spectra, QTOF (higher resolution)
- Ion trap spectra (lower resolution, low m/z cutoff)

and compared the predictions to other state-of-the-art *de novo* methods, namely:

- Lutefisk, LutefiskXP J.A. Taylor and R.S. Johnson, Anal. Chem., 73, 2594-2604 (2001).
- PEAKS B. Ma et al., Rapid Commun. Mass Spec., 17, 2337-2342 (2003).
- NovoHMM B. Fischer et al., Anal. Chem., 77, 7265-7273 (2005).
- **PepNovo** A. Frank and P. Pevzner, Anal. Chem., 77, 964-973 (2005).
- EigenMS M. Bern and D. Goldberg, J. Comp. Biol., 13(2), 364-378 (2006).

Comparative Study: Ion Trap MS/MS

□ Open Proteomics Database*: contains MS/MS spectra for 5 different organisms recorded with ESI-Ion Trap mass spectrometers

□ Mass spectra accompanied with predictions from SEQUEST

Which identifications are correct?

□ Assignments examined on individual basis for quality

- 1. Xcorr > 2.2 and ΔCn > 0.1 for +2 charge state
- 2. Consistent identification with Mascot
- 3. Number of observed b and y ions Number of predicted b and y ions

□ Organism studied: Mycobacterium smegmatis

Xcorr = cross correlation score computed by SEQUEST

 Δ Cn = normalized difference in crosscorrelation value between #1 and #2 hit in the search

Comparative Study: Ion Trap MS/MS

	LutefiskXP	PepNovo	PEAKS Online	NovoHMM	EigenMS	PILOT
Correct Identifications	2 (0.056)	8 (0.222)	6 (0.167)	9 (0.250)	6 (0.167)	17 (0.472)
with in 1 Residue	3 (0.083)	9 (0.250)	7 (0.194)	10 (0.278)	8 (0.222)	17 (0.472)
with in 2 Residue	11 (0.306)	20 (0.556)	12 (0.333)	18 (0.500)	18 (0.500)	29 (0.806)
with in 3 Residue	17 (0.472)	23 (0.639)	17 (0.472)	25 (0.694)	19 (0.528)	32 (0.889)
Total Correct Residues	222 (0.544)	310 (0.760)	281 (0.689)	309 (0.757)	289 (0.708)	359 (0.880)

Subsequence Length	x = 3	x = 4	x = 5	x = 6	x = 7	x = 8	x = 9	x = 10
Number of								
Peptides of Length $\ge x$	36	36	36	36	36	36	35	32
LutefiskXP	28 (0.778)	25 (0.694)	23 (0.639)	20 (0.556)	16 (0.444)	13 (0.361)	9 (0.257)	8 (0.250)
PepNovo	36 (1.000)	34 (0.944)	31 (0.861)	27 (0.750)	21 (0.583)	17 (0.472)	15 (0.429)	12 (0.375)
PEAKS Online	35 (0.972)	34 (0.944)	29 (0.806)	22 (0.611)	17 (0.472)	13 (0.361)	10 (0.286)	7 (0.219)
NovoHMM	35 (0.972)	33 (0.917)	31 (0.861)	29 (0.806)	21 (0.583)	17 (0.472)	14 (0.400)	11 (0.344)
EigenMS	34 (0.944)	32 (0.889)	30 (0.833)	26 (0.722)	17 (0.472)	12 (0.333)	10 (0.286)	7 (0.219)
PILOT	36 (1.000)	36 (1.000)	36 (1.000)	34 (0.944)	33 (0.917)	30 (0.833)	22 (0.629)	16 (0.500)

ebCTC

P.A. DiMaggio and C.A. Floudas, Anal. Chem., 79, 1433-1446 (2007).

Comparative Study: Ion Trap MS/MS



ebCTC

P.A. DiMaggio and C.A. Floudas, Anal. Chem., 79, 1433-1446 (2007).

Comparative Study: QTOF MS/MS

□ *Quadrupole time-of-flight* (QTOF) spectra have better resolution that ion trap spectra

□ Examined QTOF data for a mixture of 4 known proteins*:

✓ Alcohol dehydrogenase (yeast)

✓ Myoglobin (horse)

✓ Albumin (horse, BSA)

✓ Cytochrome C (horse)

□ Spectra were assessed for quality based on the metric:

$$\frac{s}{m} = \frac{\sum_{\{i : \lambda_i > 2\}} \lambda_i}{\text{Peptide Mass}}$$

 $(\lambda_i = intensity of ion peak i)$

Comparative Study: QTOF MS/MS

	Lutefisk	LutefiskXP	PepNovo	PEAKS Online	EigenMS	PILOT
Correct Identifications	10 (0.263)	9 (0.237)	16 (0.421)	21 (0.553)	20 (0.526)	25(0.658)
with in 1 Residue	11 (0.290)	10 (0.263)	17 (0.447)	22 (0.579)	21 (0.553)	25~(0.658)
with in 2 Residue	23 (0.605)	22 (0.579)	25~(0.658)	29 (0.763)	29 (0.763)	33 (0.868)
with in 3 Residue	23 (0.605)	25 (0.658)	27 (0.711)	32 (0.842)	30 (0.790)	35(0.921)
Total Correct Residues	245 (0.586)	294 (0.703)	337 (0.806)	366 (0.876)	353 (0.845)	381 (0.912)

Subsequence Length	x = 3	x = 4	x = 5	$\mathbf{x} = 6$	x = 7	x = 8	$\mathbf{x} = 9$	x = 10
Number of								
$\mathbf{Peptides \ of \ Length} \geq \mathbf{x}$	38	38	38	38	38	37	30	25
Lutefisk	29 (0.763)	27 (0.711)	25 (0.658)	22 (0.579)	17 (0.447)	14 (0.378)	11 (0.367)	10 (0.400)
LutefiskXP	36 (0.947)	34 (0.895)	31 (0.816)	29 (0.763)	26 (0.684)	19 (0.514)	13 (0.433)	10 (0.400)
PepNovo	38 (1.000)	36 (0.947)	35 (0.921)	30 (0.789)	26 (0.684)	21 (0.568)	14 (0.467)	12 (0.480)
PEAKS Online	37 (0.974)	37 (0.974)	36 (0.947)	36 (0.947)	31 (0.816)	27 (0.730)	20 (0.667)	16 (0.640)
EigenMS	37 (0.974)	36 (0.947)	35 (0.921)	33 (0.868)	29 (0.763)	22 (0.595)	20 (0.667)	16 (0.640)
PILOT	38 (1.000)	38 (1.000)	38 (1.000)	38 (1.000)	34 (0.895)	31 (0.838)	23 (0.767)	18 (0.720)

ebCTC

P.A. DiMaggio and C.A. Floudas, Anal. Chem., 79, 1433-1446 (2007).

Comparative Study: QTOF MS/MS



P.A. DiMaggio and C.A. Floudas, Anal. Chem., 79, 1433-1446 (2007).

Hybrid Approach for Peptide Identification

□ In de novo predictions – incomplete fragmentation can yield regions of ambiguity in peptide sequence

PEYAVEGLLR mass(EG) = mass(SV) = mass(DA) = mass(W) = 186 Da

□ Utilize protein database to validate amino acid assignments to subsequences of low confidence

□ **FASTA*** – tool for locally aligning a peptide query with the protein sequences in a database

301 CCDKPVLEKS HCIAEVDKDA VPENLPPLTA DFAEDKEVCK NYQEAKDVFL GSFLYEYSRR
DAFL GSFLYEYSR

Modify traditional scoring matrices (i.e., BLOSUM or PAM) to emphasize mass conservation instead of evolutionary distance

ebCTC

*W.R. Pearson and D.J. Lipman, PNAS, 85, 2444-2448 (1988).

Hybrid Approach for Peptide Identification Parallel Implementation



Worker Nodes

- Execute sequence alignment
- Parse results

Beowulf Cluster : 80 nodes with dual Intel Xeon 3.0 GHz processors

ebCTC

Hybrid Results for QTOF Spectra

Peptide	De Novo Predictions	Hybrid Predictions	
AEFVEVTK	AEFEVTK	AEFEVTK	
YLYELAR	YLYELAR	YLYELAR	
LKAWSVAR	LKAWSVAR	LKAWSVAR	
ALKAWSVAR	ALKAWSVAR	ALKAWSVAR	
QTALVELLK	QTALVELLK	QTALVELLK	
KQTALVELLK	KQTALVELLK	KQTALVELLK	
LVNELTEFAK	LVNELTEFAK	LVNELTEFAK	
HPEYAVSVLLR	HPEYAVEGLLR	HPEYAVSVLLR	
HLVDEPQNLIK	HLVDEPQNLIK	HLVDEPQNLIK	
SLHTLFGDELCK	AE <u>HTLFGDELCK</u>	SLHTLFGDELCK	
YICDNQDTISSK	YICDNQDTISSK	YICDNQDTISSK	
LGEYGFQNALIVR	LGEYGFQNALIVR	LGEYGFQNALIVR	
VPQVSTPTLVEVSR	VPQVSTDPV <u>VEVSR</u>	VPQVSTPTVEVSR	
DAFLGSFLYEYSR	DAFLGSFLYEYSR	DAFLGSFLYEYSR	
KVPQVSTPTLVEVSR	KVPQVSTPTLVEVSR	KVPQVSTPTLVEVSR	
IGDYAGIK	IGDYAGIK	IGDYAGIK	
DIPVPKPK	EV <u>PVPKPK</u>	DIPVPKPK / PMPVPKPK	
EALDFFAR	EALDFFAR	EALDFFAR	
TLPEIYEK	LT <u>PELYEK</u>	TLPELYEK / LT <u>PELYEK</u>	
ANELLINVK	ANELLLNVK	ANELLLNVK	
SIVGSYVGNR	EAVGSYVGNR	SIVGSYVGNR	
EKDIVGAVLK	KE <u>DIVGAVLK</u>	EKDIVGAVLK	
STLPEIYEK	STLPEIYEK	STLPEIYEK	
VSEAAIEASTR	VSEAAIEASTR	VSEAAIEASTR	
DGGEGKEELFR	DGGEGKEELFR	DGGEGKEELFR	
SISIVGSYVGNR	AESIVGSYVGNR	SISIVGSYVGNR	

Table continued

SISIVGSYVGNR	AESIVGSYVGNR	SISIVGSYVGNR	
GAAGGLGSLAVQYAK	QAGGLGSLAVQYAK	GAAGGLGSLAVQYAK	
ANGTTVLVGMPAGAK	[444.18]TVLVGMPAGAK	ANGTTVLVGMPAGAK	
GIDGGEGKEELFR	GIDGGEGKEELFR	GIDGGEGKEELFR	
ADTREALDFFAR	[443.20] <u>EALDFFAR</u>	ADTREALDFFAR	
VLGIDGGEGKEELFR	VIGIDGGKSVEELFR	VLGIDGGEGKEELFR	
EDLIAYLK	EDLLAYLK	EDLLAYLK	
PNLHGLFGR	PNLHGLFGR	PNLHGLFGR	
GLSDGEWQQVLNVWGK	[558.55]WEQVLNVWGK	GLSDGEWQQVLNVWGK	
EETLMEYLENPK	EETLMEYLENPK	EETLMEYLENPK	
TGPNLHGLFGR	TGPNLHGLFGR	TGPNLHGLFGR	
TGQAPGFTYTDANK	TGQAPGFTYTDANK	TGQAPGFTYTDANK	
EETLMoEYLNPK	EETLMoEYLENPK	EETLMoEYLENPK	

✓ Presented are the 38 QTOF spectra accompanied by the best de novo and hybrid predictions

✓ Recall the de novo method correctly identified 25 peptides

✓ The hybrid method correctly identifies 36 peptides

Conclusions

Developed accurate de novo and hybrid framework, PILOT, for the identification of peptides via tandem mass spectrometry (MS/MS)

□ **PILOT** outperformed several state-of-the-art de novo methods in a comparative study for ion trap and QTOF tandem mass spectra.

□ Key elements of proposed method:

- Novel mixed-integer linear optimization (MILP) formulation for peptide identification
- Preprocessing algorithm for filtering spectra and identifying important ion peaks
- Post-processing algorithm for cross-correlating theoretical tandem mass spectra with experimental tandem mass spectrum

Future Directions...

Preliminary studies validate prediction enhancements by integrating parametric uncertainty into de novo framework

Enhance performance of hybrid peptide identification method which combines the strengths of the proposed de novo method and protein database search algorithms

Incorporation of post-translational modifications into current framework

Create workbench to make PILOT available to the scientific community

Acknowledgements

Financial Support

- US Environmental Protection Agency, EPA (R 832721-010)*
- National Institutes of Health

Relevant Publications

• P.A. DiMaggio and C.A. Floudas, A mixed-integer optimization framework for de novo peptide identification, *AIChE Journal*, 53(1), 160-173 (2007).

• P.A. DiMaggio and C.A. Floudas, De novo peptide identification via tandem mass spectrometry and integer linear optimization, *Anal. Chem.*, 79, 1433-1446 (2007).

*This work has not been reviewed by and does not represent the opinions of this funding agency. etc. TC 41