

1 Efficient Probabilistic Estimates of Surface Ozone Concentration Using an
2 Ensemble of Model Configurations and Direct Sensitivity Calculations

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10 ABSTRACT

11 Because all models are a simplification of the phenomenon they aim to represent, it is
12 often more useful to estimate the probability of an event rather than a single “best” model
13 result. Previous air quality ensemble approaches have used computationally expensive
14 simulations of separately developed modeling systems. We present an efficient method
15 to generate ensembles with hundreds of members based on several structural
16 configurations of a single air quality modeling system. We use the Decoupled Direct
17 Method in 3D (DDM-3D) to directly calculate how ozone concentrations change as a
18 result of changes in input parameters. The modeled probability estimate is compared to
19 observations and is shown to have a high level of skill and improved resolution and
20 sharpness. This approach can help resolve the practical limits of incorporating
21 uncertainty estimation into deterministic air quality management modeling applications.

22

23 **1. Introduction**

24 Atmospheric chemical and physical processes are complex. Air quality models offer a
25 simplified representation of the fate and transport of air pollutants that can be used to
26 manage and gain insight into air quality problems. Such models rely on parameterization
27 in order to make the mathematical solutions tractable and the results intelligible. Despite
28 these simplifications, air quality models remain computationally intensive. Continental-
29 scale spatial domains are necessary in order to capture long-range transport of ozone. On
30 such a scale, sources of air pollution range from organic gases from natural forests to
31 thousands of automobile tailpipes trapped in suburban congestion. Direct measurement
32 of all of these sources is impossibly expensive, so most applications rely on relatively
33 few observations and many extrapolations.

34 Because of the necessary parameterizations and extensive data requirements, it is not
35 possible to eliminate uncertainty in air quality modeling. However, air quality modeling
36 is still a critical component of air quality management decision support tools. When
37 weighing the societal benefits of different air quality management options, policy-makers
38 need quantitative information about the relative risks and likelihood of success to guide
39 their decisions. Developing an air quality modeling approach that can estimate both the
40 probability of an event, as well as a single “best-estimate”, would advance the current air
41 quality tools available for these management decisions.

42 Many have shown in air quality forecasting applications that an ensemble of
43 deterministic models can be used to estimate a probabilistic range [1, 2]. Previous work
44 has explored structural uncertainty related to the form of the model [3-6], parametric
45 uncertainty related to the inputs to the model [7] or both [8-11].

46 The challenge with these approaches is that air quality models require significant input
47 data and computational resources to complete a single simulation. Some of the more
48 successful ensemble results have been generated using a collection of modeling systems
49 developed by independent institutions [3-5]. Developing, maintaining, and meeting the
50 input data requirements for multiple modeling systems is time consuming, expensive, and
51 redundant. Is it possible to achieve similar success with an ensemble of multiple
52 configurations of a single air quality model?

53 Additionally, traditional ensemble modeling efforts still do not fully address the range
54 of possible uncertainties involving emissions, which is one of the largest parametric
55 uncertainties. Practical constraints have limited the degree to which emission
56 uncertainties, or other parametric uncertainties, can be addressed. For example, the
57 emissions data for a one month of simulation of the Eastern United States domain
58 typically has 26 species, 720 hourly time steps, and a horizontal grid of 205 by 199 cells
59 with 9 vertical layers, yielding on the order of 10^9 input values. These models are
60 computationally intensive, so repeated sampling of the uncertain input space is costly. In
61 theory, to consider uncertainty in all of the inputs, ensemble populations need to be large.
62 Improved sampling methods can reduce the number of simulations [12, 13], but for many
63 air quality practitioners, such additional computational expenses are not feasible. Is it
64 possible to more efficiently create an ensemble of members that reflect the uncertainty in
65 the input data?

66 In the approach presented here, our goal is to develop an engineering approach that can
67 accurately and efficiently estimate the probability of exceeding an ozone concentration
68 threshold. We use several configurations of a single air quality model and the Decoupled

69 Direct Method in 3-D (numerous references available in Cohan et al. [14]) to
70 simultaneously calculate the impact of uncertainty in the model form and input values.
71 Finally, we apply methods from the air quality forecasting community and observed
72 ozone concentrations to evaluate the quality ensemble for use as air quality management
73 and decision making tools.

74 **2. Methods**

75 Our method for efficiently developing an ensemble of air quality simulations consists
76 of seven steps shown in Figure 1. The models, relevant datasets, and each of the steps are
77 described in detail below.

78 2.1 Air Quality Model and Inputs Description

79 We employ the Community Multiscale Air Quality (CMAQ) model to simulate the
80 chemical concentrations and deposition over a continental-scale region using an Eulerian
81 grid structure [15]. The inputs include chemical emissions and a representation of the
82 atmosphere from a numerical weather simulation model. Important processes are
83 dispersion, gas-phase chemistry, aerosol thermodynamics and mass-transfer, and
84 deposition. The horizontal resolution is 12 x 12 km and there are 14 vertical layers from
85 the surface to 100 hPa. Meteorological inputs are from the PSU/NCAR 5th generation
86 mesoscale model, also known as MM5 [16]. We simulate the time period from June 24,
87 2002 to July 28, 2002. The first seven days are excluded from the analysis to eliminate
88 sensitivity to initial conditions. The spatial domain includes most of the Eastern United
89 States (Figure S2 in Supplemental Information). Emissions are generated using the
90 SMOKE emissions processing system ([http://www.smoke-](http://www.smoke-model.org/version2.3.2/html/ch02s16.html)
91 [model.org/version2.3.2/html/ch02s16.html](http://www.smoke-model.org/version2.3.2/html/ch02s16.html)). Year 2002 specific emissions data for motor

92 vehicles are from MOBILE 6 (<http://www.epa.gov/otaq/m6.htm>); power plant emissions
93 are from Continuous Emission Monitors (<http://www.epa.gov/camddataandmaps/>).
94 Biogenic volatile organic carbon and NO_x emissions are simulated using BEIS v.3.13
95 [17] and are derived using the same meteorological fields as the air quality simulations.
96 All other emission sources are from the 2001 National Emission Inventory
97 (<http://www.epa.gov/ttn/chief/net/critsummary.html>).

98 The Higher-Order Decoupled Direct Method in three dimensions [14, 18] is
99 implemented in CMAQ version 4.5 (CMAQ-DDM-3D [19]) for CB-IV and SAPRC99
100 chemical mechanisms. Our study is focused on the Atlanta and Birmingham
101 metropolitan areas; therefore, for the nested CMAQ-DDM-3D simulations, we use a sub-
102 domain over the Southeastern United States (map in Figure 2). This sub-domain includes
103 a region-wide episode of high ozone during the first two weeks and a period of variable
104 clouds and precipitation that cause low ozone concentrations during the third and fourth
105 week. The emission inputs to CMAQ-DDM-3D are as described above; the
106 meteorological inputs, boundary conditions and initial conditions are from the structural
107 uncertainty simulations, described in Section 2.2.

108 Our analysis focuses on the hourly-average ozone concentrations reported at Air
109 Quality System (AQS) monitoring stations (<http://www.epa.gov/air/data/aqsdb.html>) in
110 the Birmingham and Atlanta metropolitan areas. The location of these 38 monitors and
111 the location of the 97 monitors used to estimate the uncertainty in the boundary
112 conditions are shown in Section S1 in the Supplemental Information.

113 2.2 Structural Uncertainty

114 *Structural uncertainty* refers to a lack of knowledge about the fundamental mechanisms
115 underlying the environmental process. This kind of uncertainty can be addressed by an
116 ensemble that includes multiple representations of a single process. To build our six
117 structural uncertainty cases, we develop three different configurations of the
118 meteorological model and two different gas-phase chemical mechanisms. After an
119 analysis of previous meteorological model configurations and sensitivity tests, we
120 determined that the choice of land surface model (LSM) and the planetary boundary layer
121 model (PBLM) are among the meteorological factors that have the largest impact on the
122 air quality simulation [20, 21]. These processes control the mixing depth, mixing
123 intensity, and temporal evolution of the surface mixed layer. The three configurations are
124 the Pleim-Xiu (P-X) LSM with the Asymmetric Convective Model (ACM) PBLM, the
125 Noah LSM with Medium Range Forecast (MRF) PBLM, and Noah LSM with Mellor-
126 Yamada-Janjic (M-Y-J) PBLM. Each meteorological simulation is constrained using
127 analysis nudging that employs the three hourly National Centers for Environmental
128 Prediction (NCEP) Eta Data Assimilation System (EDAS) analysis. This reduces
129 simulation errors but restricts the variability between the three cases. We also select two
130 different gas-phase chemical mechanisms, Carbon Bond IV (CB-IV) and SAPRC99. In
131 the CMAQ implementation, these mechanisms have similar representation of the
132 inorganic reactions; however, the grouping and reactivity of the organic gases differ
133 significantly. The supplemental information contains the details of the model
134 configurations, relevant references, and spatial maps of ozone anomalies.

135 2.3 Parametric Uncertainty

136 *Parametric uncertainty* refers to uncertainty in the inputs and parameter values. To
137 address this type of uncertainty, CMAQ-DDM-3D is used to estimate a reduced form
138 model of ozone concentration. While there are many sources of uncertainty, we limit this
139 study to NO_x emissions (ENO_x), VOC emissions (EVOC), and ozone boundary
140 conditions (BO₃). Previous work has shown these to be among the inputs that have the
141 most significant impact on ozone concentration [22, 23]. Our calculations are with
142 respect to temporally-invariant, domain-wide changes in these inputs. We select a range
143 of scaling factors from 0.4-1.2 for uncertainty in NO_x emissions and a range of 0.5-1.5
144 for uncertainty in VOC emissions. Because these scaling factors represent domain-wide
145 bias in the emission inventory over the entire simulation period, we selected from the
146 lower range of emission uncertainty estimates for a particular source or location as
147 estimated in [24]. Based on a previous study that found that the urban NO_x emissions are
148 over estimated for this domain, NO_x emission uncertainty is not centered at zero [25].
149 For ozone boundary conditions we select a range of 0.62-1.12, based on the distribution
150 of errors for 97 ozone monitoring sites near the border of our sub-domain, as described in
151 the Supplemental Information.

152 To estimate the range of ozone concentrations that result from these uncertainties, we
153 use CMAQ-DDM-3D to directly calculate the sensitivity of ozone concentration to a
154 change in the input values. Following the approach and notation of Cohan et al [14], we
155 first define the semi-normalized first-order sensitivity $\mathbf{S}^{(1)}$ and second-order sensitivity
156 $\mathbf{S}^{(2)}$ as

$$157 \quad \mathbf{S}_j^{(1)}(x, t) = \frac{\partial \mathbf{C}(x, t)}{\partial \varepsilon_j} \quad (1)$$

$$158 \quad \mathbf{S}_{j,k}^{(2)}(x,t) = \frac{\partial^2 \mathbf{C}(x,t)}{\partial \varepsilon_j \partial \varepsilon_k} \quad (2)$$

159 where ε_j is a constant scaling factor applied to the CMAQ inputs, and the subscript j and k
 160 refer to one of ENO_x , EVOC, or BO_3 . The ozone concentration matrix, \mathbf{C} , and sensitivity
 161 matrices, \mathbf{S} , are calculated across the spatial domain, x , and for each hour of the
 162 simulation, t . We use a Taylor Series expansion to estimate the change in ozone
 163 concentration due to simultaneous changes in multiple parameters. Equation 3 describes
 164 the reduced form model, where m refers to BO_3 , j refers to ENO_x , and k refers to EVOC:

$$165 \quad \mathbf{C}_{j+k+m} \approx \mathbf{C}_0 + \Delta \varepsilon_m \mathbf{S}_m^{(1)} + \Delta \varepsilon_j \mathbf{S}_j^{(1)} + \Delta \varepsilon_k \mathbf{S}_k^{(1)} + \\ + \frac{1}{2} \Delta \varepsilon_j^2 \mathbf{S}_j^{(2)} + \frac{1}{2} \Delta \varepsilon_k^2 \mathbf{S}_k^{(2)} + \Delta \varepsilon_j \Delta \varepsilon_k \mathbf{S}_{j,k}^{(2)} \quad (3)$$

166 Terms higher than second-order are neglected, which is sufficient to reproduce the brute-
 167 force simulated ozone concentration to within a few percent [14]. We found that the
 168 cross sensitivities of emissions to boundary conditions and second-order boundary
 169 condition sensitivities are small, so they are excluded from this analysis.

170 The first- and second-order sensitivities are calculated using CMAQ-DDM-3D for
 171 ENO_x , EVOC, and BO_3 for each time and grid cell and for each of the six structural
 172 uncertainty cases over the SE US sub-domain. We use the reduced form model described
 173 by Equation 3 to calculate the ozone concentration at each hour and grid cell after the
 174 emissions inputs and the boundary conditions from the base model have each been
 175 increased or decreased by a constant factor.

176 2.4 Monte Carlo Methods

177 A single ensemble member consists of the 8-hour maximum ozone for each location at
178 each day, given a level of NO_x emissions, VOC emissions, ozone boundary conditions,
179 and a specific structural uncertainty case. First, we randomly select one of the six
180 structural uncertainty cases. The NO_x emission, VOC emission, and ozone boundary
181 condition scaling factor are sampled from a uniform distribution that spans the range of
182 uncertainty described in Section 2.3. Using the sensitivities relevant to that structural
183 uncertainty case, we calculate the ozone concentration at each monitoring location for
184 each hour of the simulation. We then repeat this process 40,000 times to build a
185 population of results, and find that a 1,000-member ensemble achieves sufficient
186 convergence.

187 2.5 Evaluating the Ensemble Quality

188 To test the properties of this ensemble technique, we devise three test cases:

189 **Structural Ensemble:** A six-member ensemble that includes each of the
190 structural uncertainty cases and no parametric uncertainty

191 **Range Ensemble:** A 54-member ensemble that includes the six structural cases
192 each with eight combinations of the maximum and minimum range for each of the
193 parametric uncertainty parameters ($2^3 \times 6 = 48$ members) plus an additional six
194 structural case simulations using the central value of each parametric uncertainty
195 distribution: $BO_3 = 0.88$, $ENO_x = 0.8$, $EVO_3 = 1.0$.

196 **Full Ensemble:** A 1,000-member ensemble that includes both structural and
197 parametric uncertainty, generated using Monte Carlo methods described in
198 Section 2.4

199 For n different parametric uncertainty ranges, the range ensemble requires $2^n + 1$ times
200 more computation time than the structural case. For the full ensemble with α parameters
201 with negligible second derivatives and β parameters with non-negligible second
202 derivatives ($\alpha + \beta = n$), the number of sensitivity calculations is

$$203 \quad \alpha + 2\beta + \sum_{i=1}^{\beta-1} i \quad (4)$$

204 In the full ensemble where $\alpha = 1$ and $\beta = 2$, 6 sensitivity calculations (the **S** terms in
205 Equation 3) are required. These calculations require 6.8 times more computational time
206 than a single CMAQ run. The full ensemble is $1 - (6.8 / 9) = 24\%$ more efficient than the
207 range case; for an ensemble study where $n = \beta = 10$ the full ensemble is an order of
208 magnitude more efficient.

209 For each of the ensemble members in each case for each monitoring location and day,
210 we calculate the observed and simulated mean concentration from 9 am to 5 pm local
211 time. These values are used for all statistical calculations described here. For each
212 ensemble case at each location and day, we calculate the probability of exceeding the
213 ozone concentration threshold of 68 ppb, which is equal to one standard deviation (14
214 ppb) greater than the observed mean ozone concentration (54 ppb). As a reference, we
215 calculate the climatological frequency (0.17) as the mean observed frequency of
216 exceeding this threshold over the 38 locations and 28 days in our modeling domain. For
217 a given location and time, the ensemble estimated probability of exceeding the threshold
218 is the number of ensemble members greater than 68 ppb divided by the total number of
219 members. This assumes that each ensemble member has equal likelihood.

220 The probability that a particular location will exceed a threshold ozone concentration
221 on a specific day can not be directly measured – we can only measure the outcome. To
222 evaluate the model estimated probability, it is useful to define three properties of
223 ensembles frequently used by the meteorological forecasting community: reliability,
224 resolution, and sharpness [2]. *Reliability* refers to the skill of the ensemble-estimated
225 probability. To calculate reliability, we aggregate together all of the locations and times
226 with a similar estimated probability of exceeding a threshold and compare with the
227 observed frequency. That is, for all locations and times where the model estimated
228 probability of exceeding 68 ppb is 20%, is the observed frequency of exceeding 68 ppb at
229 those times and locations also 20%? *Resolution* is a measure of differentiation – how
230 well does the ensemble sort observed events into groups that are different from each
231 other? Lastly, *sharpness* is the extent to which the ensemble deviates from the
232 climatological average. Sharpness is an inherent feature that is not dependent on the
233 observed values. We calculate sharpness as the absolute mean difference between the
234 ensemble-estimated probability of exceeding 68 ppb and the climatological average. In a
235 trivial example, if the ensemble estimated probability always equaled the domain average
236 climatological frequency, then the ensemble estimate would be very reliable, but would
237 not be useful at capturing the day to day and location to location changes. Such an
238 ensemble estimated probability would have poor resolution and poor sharpness. A key
239 challenge is to develop a probabilistic system that expresses all three properties.

240 When calculated with respect to the climatological probabilities, the Brier Skill Score
241 (BSS) is often used as a scalar representation of the skill of the ensemble. It is expressed
242 as a percentage improvement over climatological probability. The BSS can be calculated

243 as the difference between the resolution score and the reliability score (here a low
244 reliability score implies high reliability). The derivation of this decomposition is
245 described by Wilks [2]. These metrics are used to assess the quality of the three
246 ensemble test cases (structural, range, and full).

247 Another test of the quality of the uncertainty estimates is the spread-skill relationship,
248 defined as the correlation of the spread of the ensemble with the error in the mean
249 estimate. When the uncertainty is large, the ensemble members should diverge and the
250 spread should increase. We calculate the spread-skill relationship as the correlation
251 between the standard deviation of the ensemble members and the mean absolute error in
252 the ozone concentration.

253 **3. Results**

254 3.1 Ozone Concentrations and Sensitivity

255 The differences between the structural uncertainty simulations are small. The average
256 ozone concentration anomaly, defined as the difference from the mean of all six structural
257 cases, is shown in the Supplemental Information Figure S2. The largest difference is due
258 to the chemical mechanism: SAPRC99 has higher ozone concentrations compared to
259 CB-IV. The different meteorological options impact the spatial distribution of the ozone.
260 There are also minor structural differences in the sensitivity results, shown in Figure 2.
261 The highest NO_x sensitivity gradients are in and around the urban core of large cities,
262 such as Atlanta. The urban center has considerably lower NO_x emission sensitivity, but
263 higher VOC sensitivity. This feature is more exaggerated in the SAPRC99 chemical
264 mechanism simulations. The absolute value of the VOC emission sensitivities (first-
265 order, second-order, and cross-sensitivities) are largest in the MRF configurations. The

266 diversity in the results is due to structural differences in the simulation of key physical
267 and chemical processes. However, compared to the total uncertainty and un-captured
268 variability, this diversity is small.

269 Each of the three ensemble test cases (structural, range, and full), have differing
270 properties. For illustration, the observed concentrations and ensemble values for a single
271 ozone monitoring site near Atlanta, Georgia is shown in Figure 3. The structural
272 ensemble (blue open circles) is biased high; over all of the monitoring locations, only
273 24% of the observations fall within the bounds of the highest and lowest ensemble
274 members. The range ensemble (orange) has the largest spread, with 64% of observed
275 values falling within the 25th and 75th inter-quartile range and 96% are between the
276 highest and lowest members. The full ensemble (grey box-whisker) has less spread than
277 the range case but captures 42% of all observed values within the 25th and 75th inter-
278 quartile range and 94% are between the highest and lowest members.

279 3.2 Ensemble Evaluation Metrics: Resolution, Reliability, & Sharpness

280 The reliability diagram (Figure 4) is used to assess the skill of the ensemble
281 estimated probability: for all times and locations when the ensemble estimated
282 probability of exceeding the threshold is p (the x-axis), is the observed frequency of
283 exceeding the threshold at those times and locations also p (the y-axis)? The x-axis of the
284 diagram is ensemble estimated probability of exceeding the threshold, grouped into seven
285 ascending bins. For each of the times and locations grouped in these bins, the observed
286 frequency of exceeding the threshold is plotted on the y-axis. The grey shaded area
287 represents ensemble estimates that have overall skill greater than a climatological
288 estimate, denoted by the dotted lines as the observed probability of exceeding the

289 threshold (0.17). The structural ensemble (blue) overestimates the probability of
290 exceeding the threshold. The range ensemble (orange) and full ensemble (black) have
291 similarly improved performance. The range ensemble performs better for higher
292 probabilities, while the full ensemble performs better for lower probabilities. Further
293 analysis using the Rank Histogram is available in Section S3 of the Supplemental
294 Information.

295 The BSS and its relative decomposition into the resolution and reliability components
296 underscore the key differences between the full and range cases. As shown in Table 1,
297 both cases have relatively similar BSS, but the decomposition is quite different. The full
298 case has lower reliability and higher bias, due to asymmetry in the relative impact of
299 changes in BO_3 , ENO_x , and EVOC. However, the full case has higher resolution and is
300 also sharper than the range case. With more individual members that further resolve the
301 uncertainty space, the full ensemble can more effectively differentiate between high and
302 low ozone events (Supplemental Information Figure S4). Finally, the full ensemble has
303 the highest spread-skill correlation at 0.45, followed by the structural and range cases
304 with 0.39 and 0.37, respectively.

305 **4. Discussion**

306 We have demonstrated that a single air quality modeling system can combine aspects
307 of structural and parametric uncertainty to provide reliable estimates of the probability of
308 exceeding an ozone threshold concentration. By directly calculating the sensitivities, it is
309 possible to generate large ensembles that have similar skill but greater resolution and
310 sharpness compared to simply simulating the bounds of the uncertainty range. Future
311 work should focus on improving the calibration and reliability, potentially by pairing this

312 method with an ensemble weighting scheme (such as Raftery et al. [26]). Future work
313 should also explore additional sensitivities such as chemical rate parameters and spatially
314 variable emissions sensitivities.

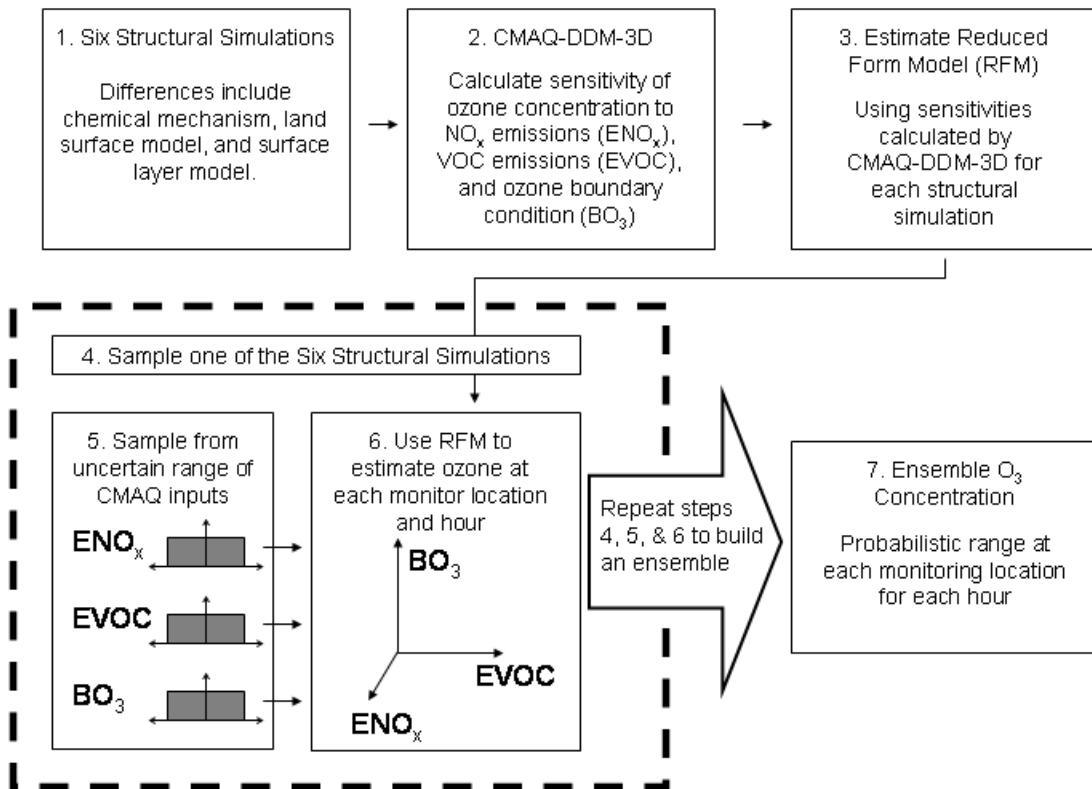
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320 **Supporting Information Available** including a description of boundary condition
321 uncertainty, meteorological simulations, and additional evaluation metrics.

322 **Figure 1.** Flowchart to generate ensemble including structural and parametric uncertainty
323 using a direct calculation of higher-order sensitivities

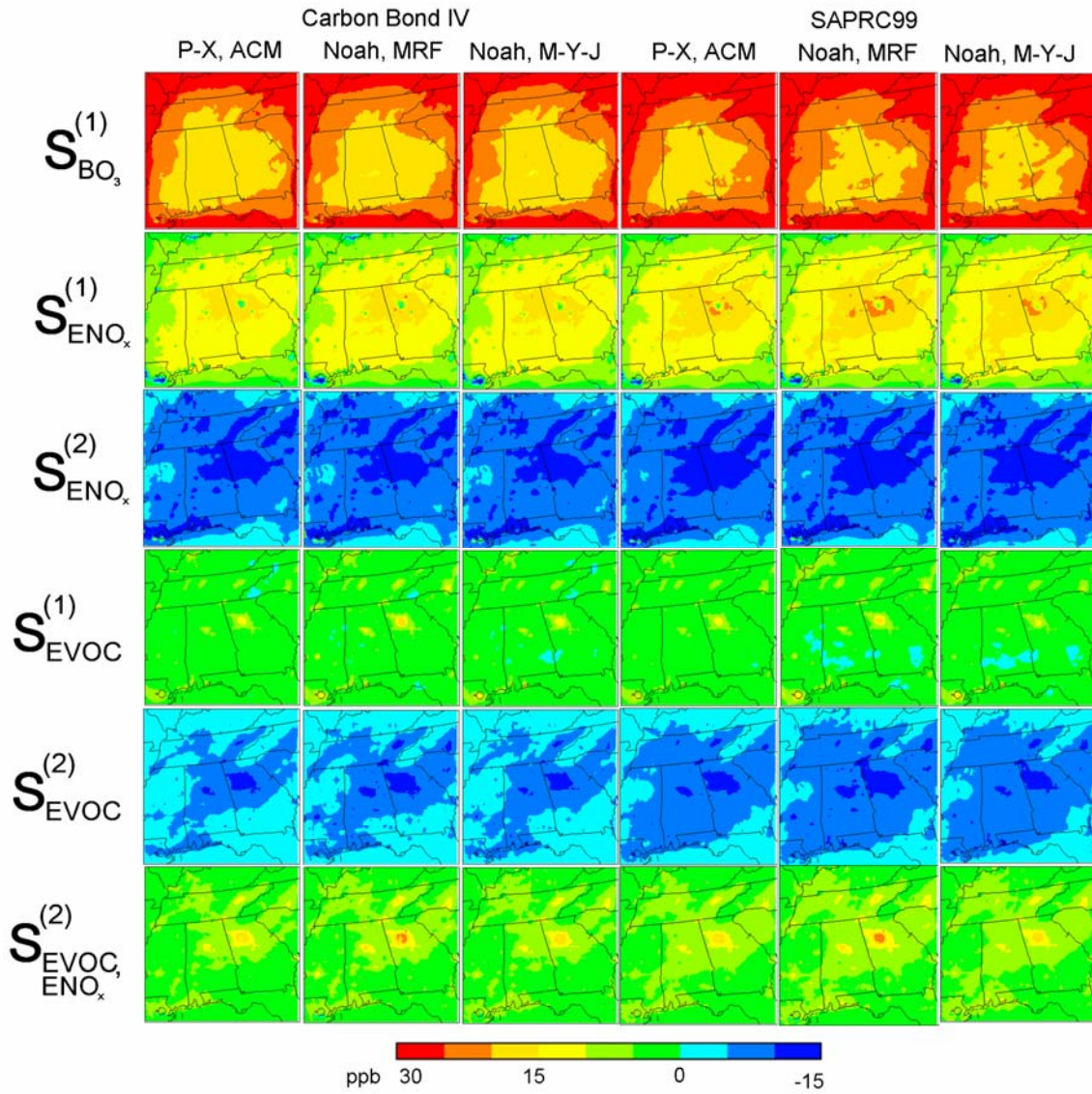
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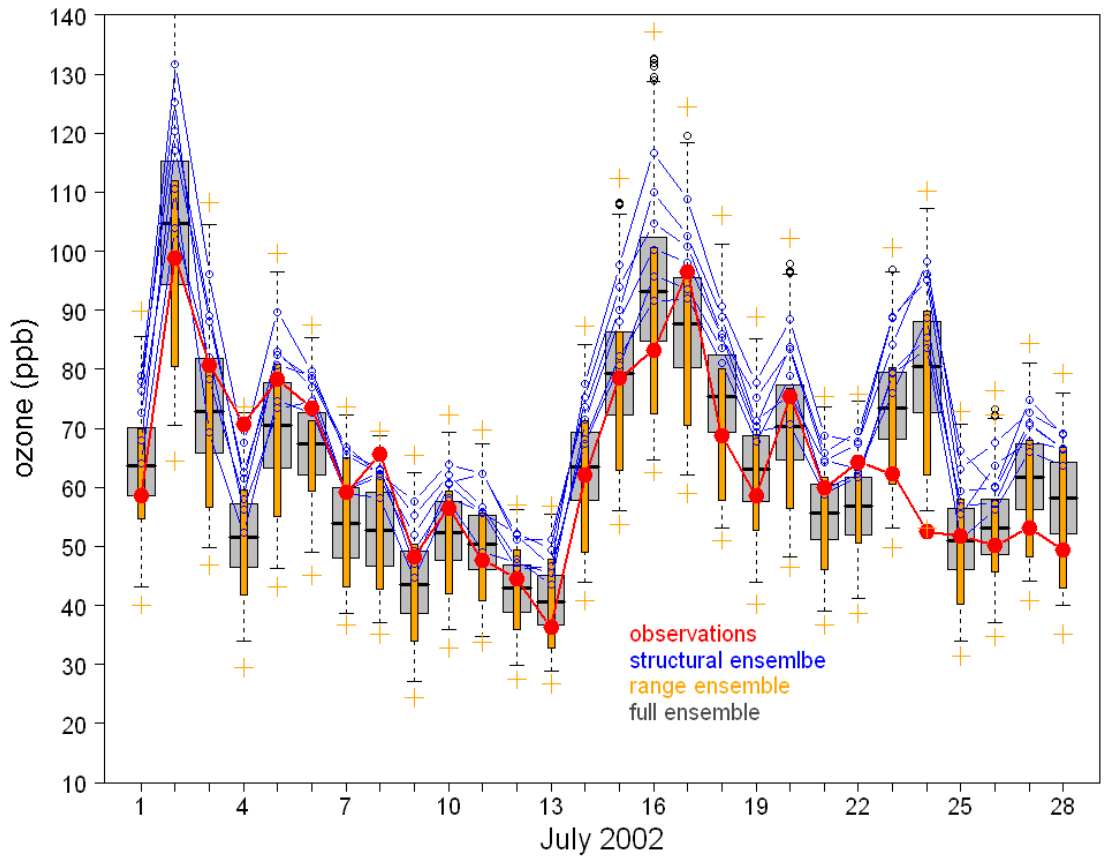
327 **Figure 2.** The first-order ($S_j^{(1)}$), second-order ($S_j^{(2)}$), and cross-sensitivity ($S_{jk}^{(2)}$) of the
 328 ozone concentration to ozone boundary concentrations (BO_3), NO_x emissions (ENO_x),
 329 and VOC emissions (EVOC) for each of the six structural uncertainty cases, averaged
 330 over the entire simulation period.



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332

333 **Figure 3.** For a location near sub-urban Atlanta, observed (red) and ensemble ozone
 334 concentrations as estimated by including only structural uncertainty (blue), both
 335 structural and the bounds of the parametric uncertainty (orange: box = 25th and 75th
 336 percentile, crosses = range), and 1,000 member ensemble composed of sampling both the
 337 structural cases and from the range of uncertain input parameters (grey: box = 25th and
 338 75th percentile, dashed line = range, open circles = outliers).

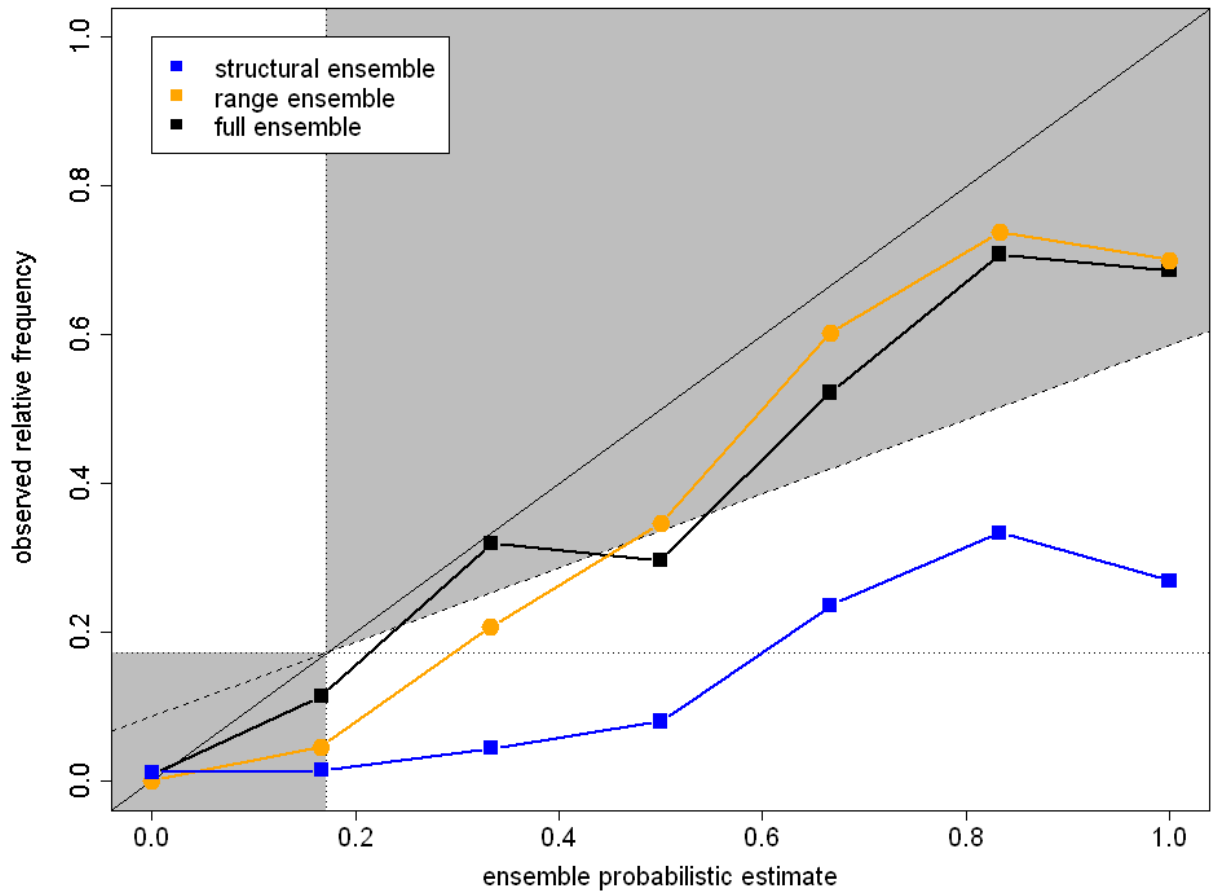


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341 **Figure 4.** The Reliability Diagram

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345 **Table 1.** Ensemble performance metrics

Case	Structural Ensemble	Range Ensemble	Full Ensemble
Mean Correlation	0.73	0.70	0.71
Mean Error (ppb)	11	1.3	3.2
Mean Standard Deviation (ppb)	4.2	11	7.1
Spread-skill Correlation	0.39	0.37	0.45
Brier Skill Score	-0.15	0.36	0.35
Reliability	0.47	0.019	0.14
Resolution	0.32	0.38	0.49
Sharpness	0.36	0.19	0.24

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