

# ENSEMBLE PREDICTION: STRENGTHS AND LIMITATIONS

Zoltan Toth<sup>1</sup>

Environmental Modeling Center, NCEP

## *Acknowledgements:*

Yuejian Zhu	EMC <sup>1</sup>
Richard Wobus	EMC <sup>1</sup>
Tim Marchok	GFDL <sup>2</sup>
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<http://sgi62.www.noaa.gov:8080/ens/enshome.html>

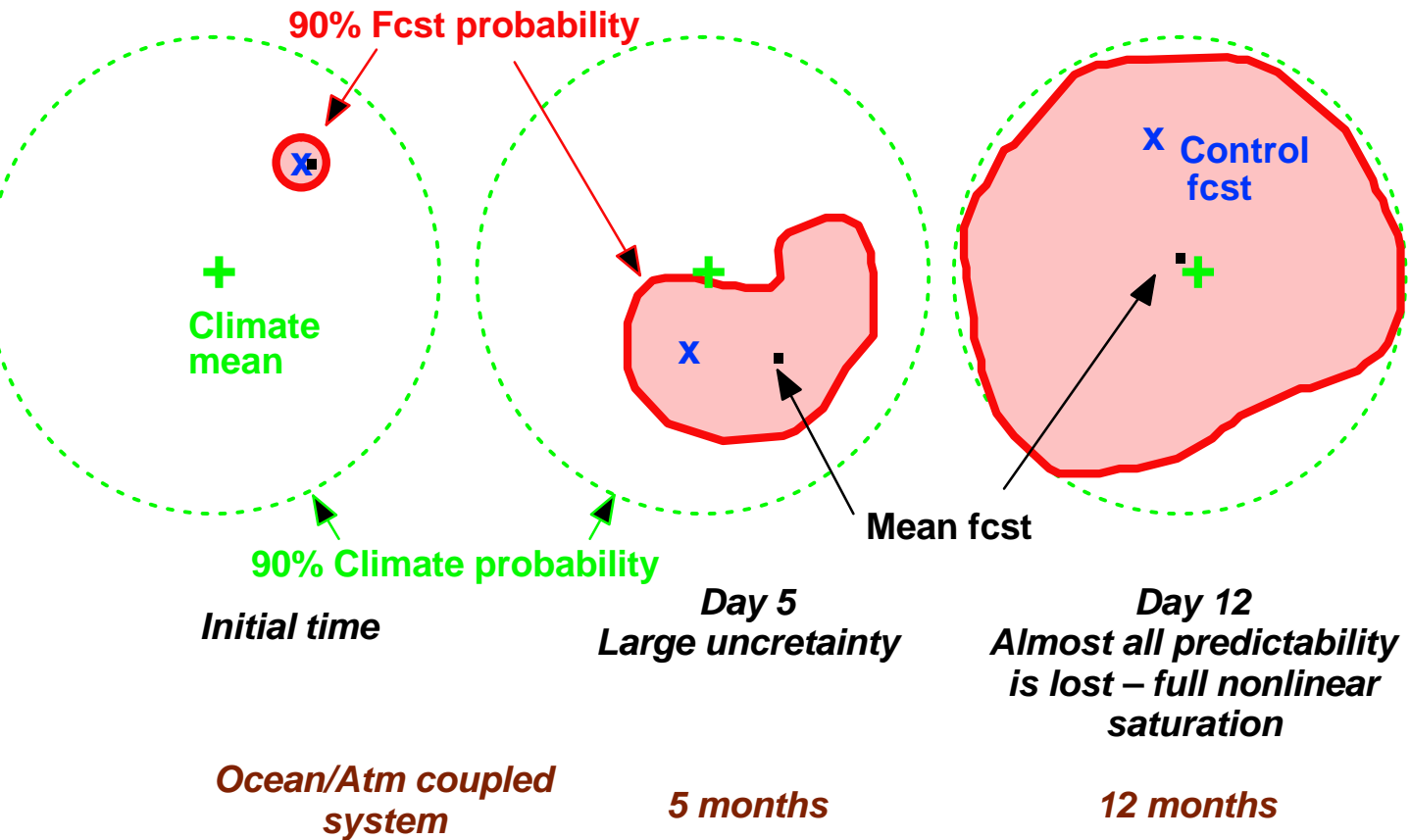
## ***ENSEMBLE FORECASTING: STRENGTHS AND LIMITS***

- 1) DEFINITION OF CHAOS**
- 2) INITIAL VALUE RELATED PREDICTABILITY/UNCERTAINTY**
- 3) BOUNDARY CONDITION RELATED PREDICT./UNCERTAINTY**
- 4) BRIDGING THE GAP BETWEEN WEATHER AND CLIMATE**
- 5) ADVANTAGES OF USING ENSEMBLE FCSTS**
- 6) PROBLEMS WITH ENSEMBLES**
- 7) VERIFICATION**
- 8) POSTPROCESSING**

TOTH: CLIMATE ENSEMBLE PREDICTION  
**INITIAL VALUE RELATED PREDICTABILITY**

- 1) The atmosphere is a **deterministic system** *AND* has at least one direction in which **perturbations grow**
- 2) **Initial** state has **error** in it ==>

*Chaotic system + Initial error =(Loss of) Predictability*



**Even with perfect model, fcsts diverge and fail** – example

**CONSEQUENCE:**

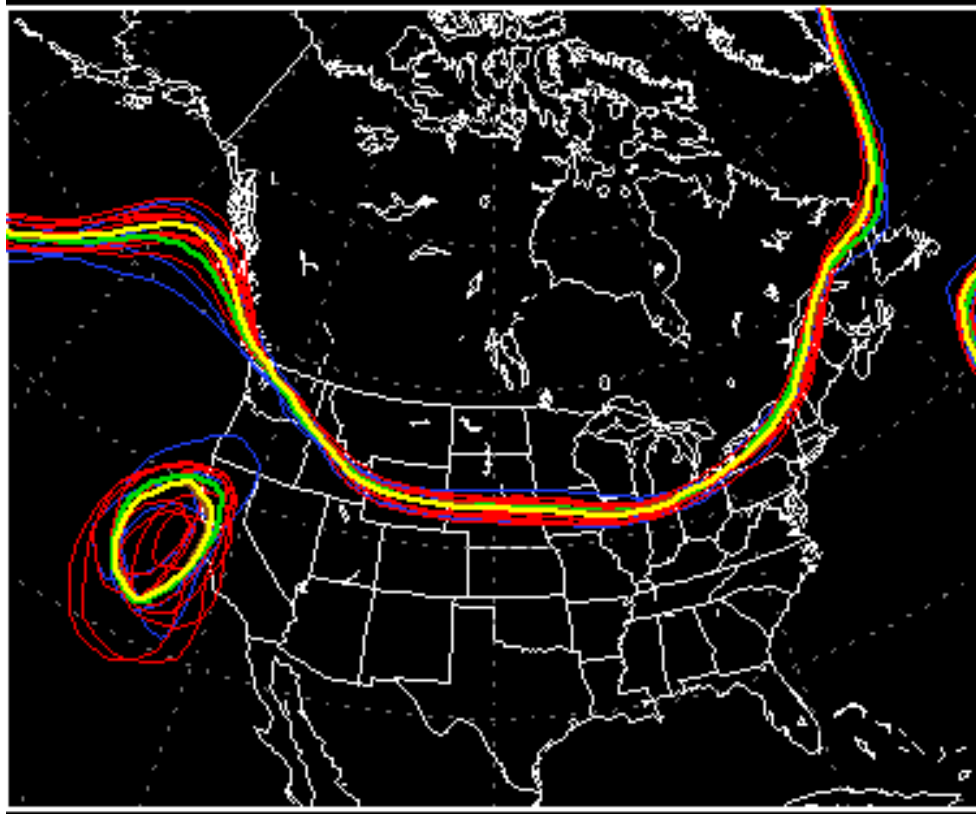
Single control forecast does not contain all information

- a) How likely this scenario is?
- b) What other solutions possible?

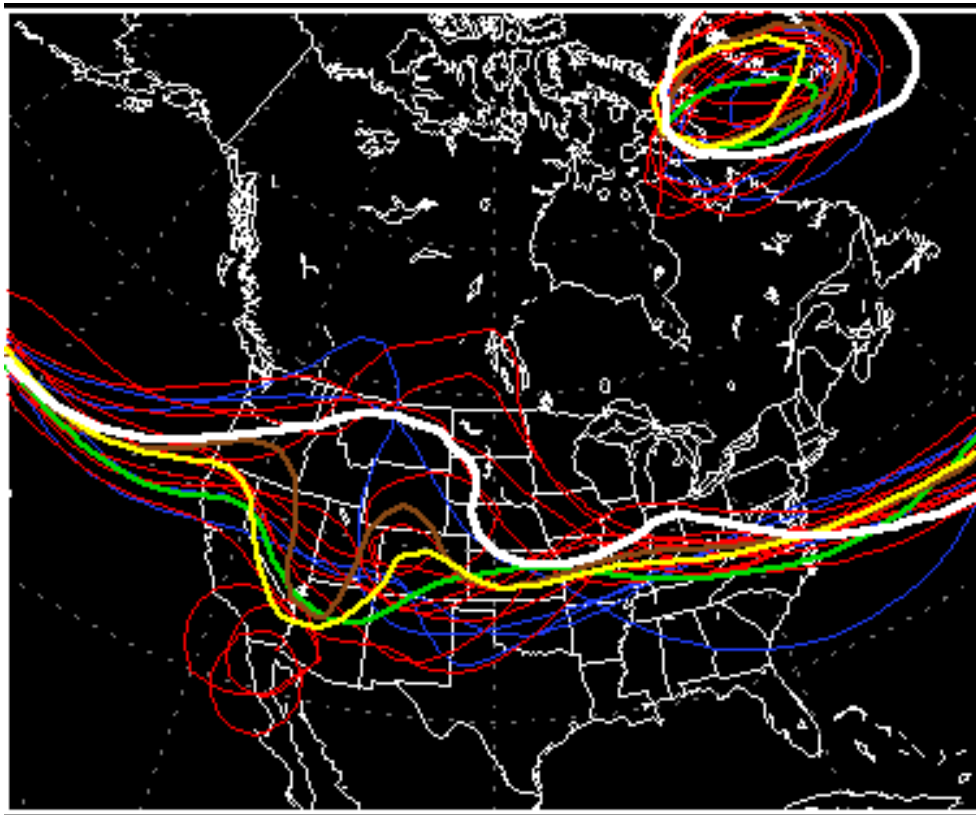
Due to nonlinearities, control fcst is not best estimate

**USE ENSEMBLES**

NCEP ENSEMBLE, INITIAL TIME, 20010226 0000 UTC



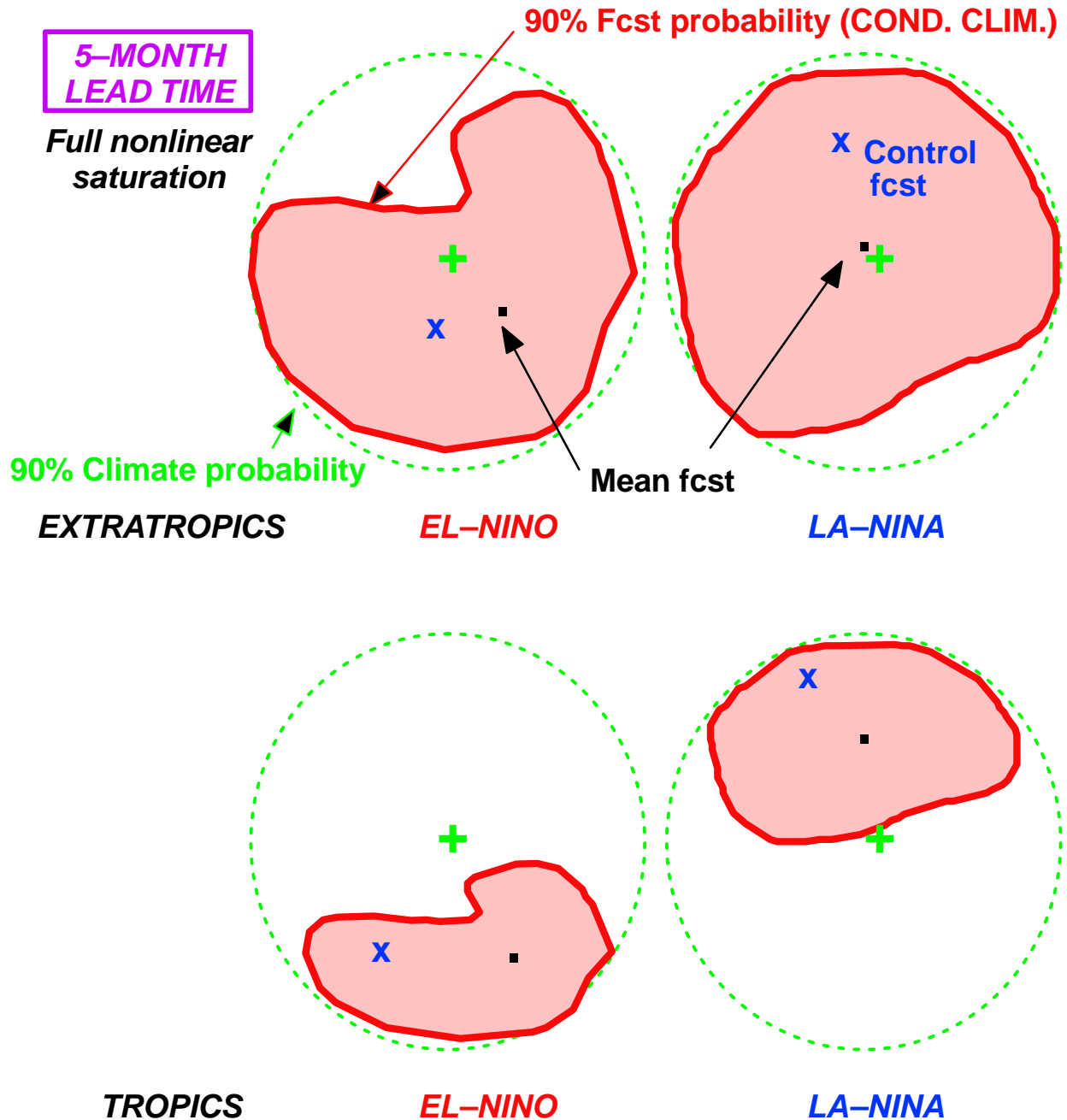
96-HR FORECAST



# BOUNDARY FORCING RELATED PREDICTABILITY

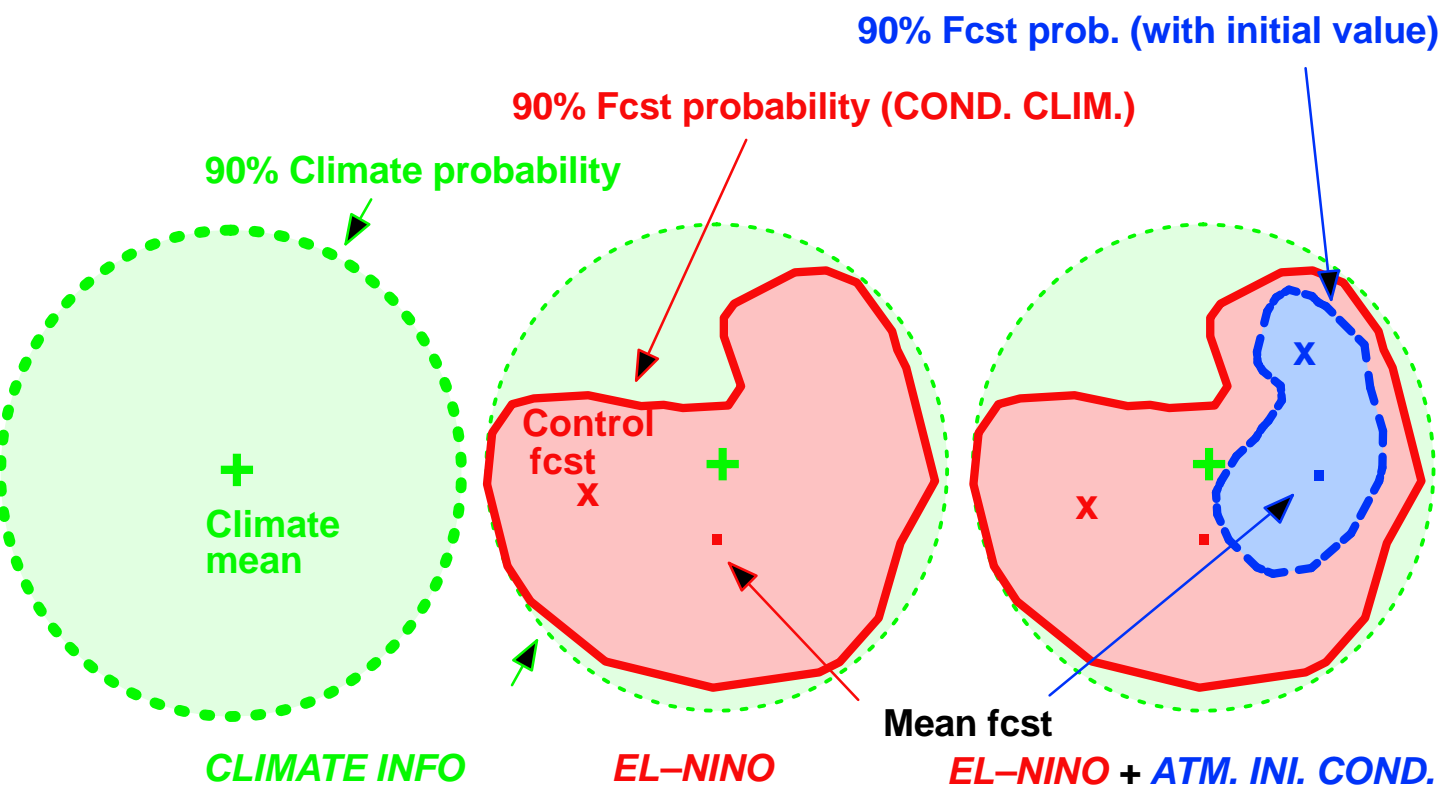
- 1) **Different boundary conditions** (eg, SSTA) => Different climates – **Conditional Climatology**
- 2) **Predict** slowly varying **boundary conditions** – **Run** atmosph. **ensemble** to find **corresponding climate**

## 2nd kind of predictability due to boundary forcing

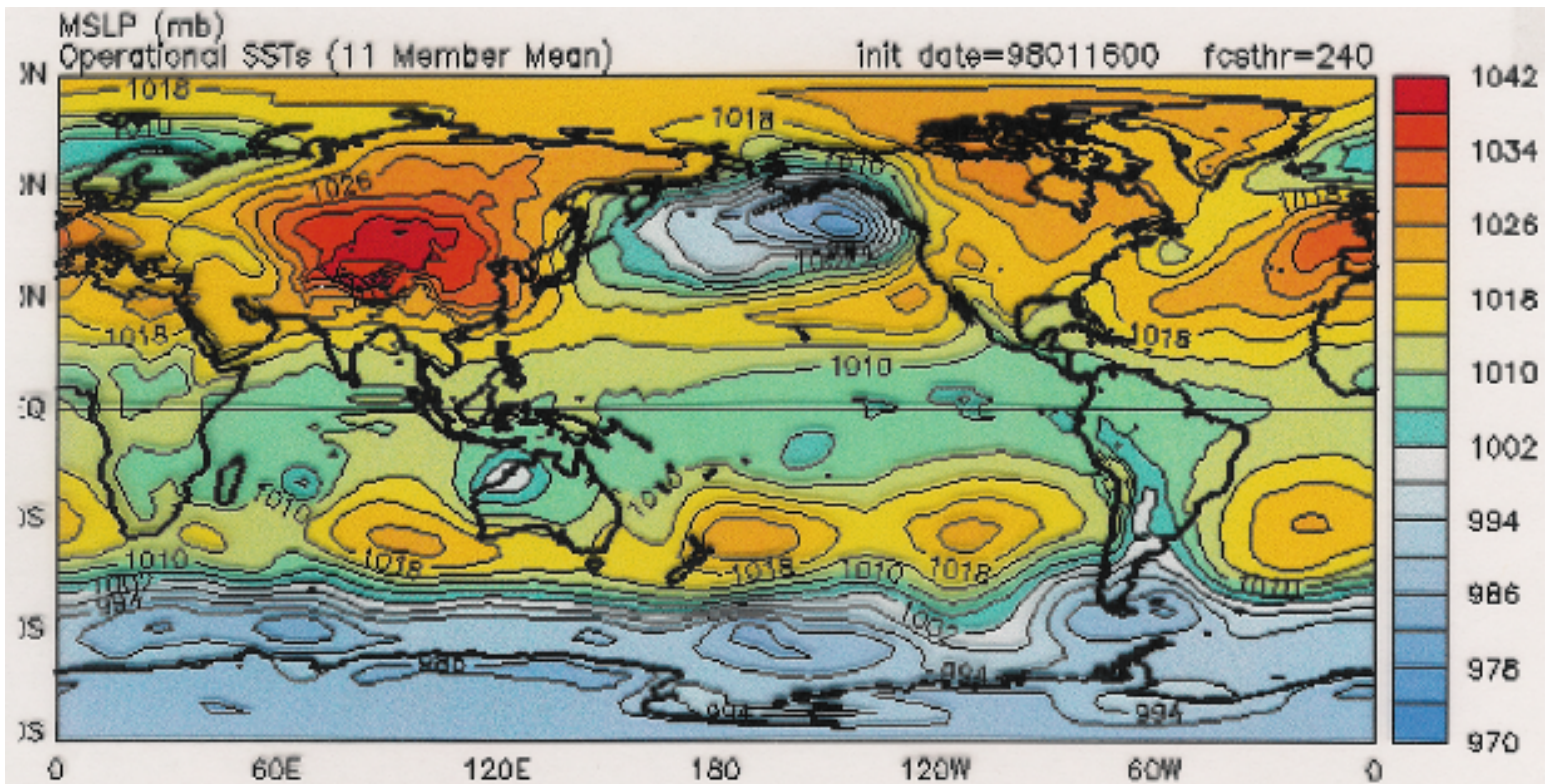


## WEATHER FORECASTING, DAY 10

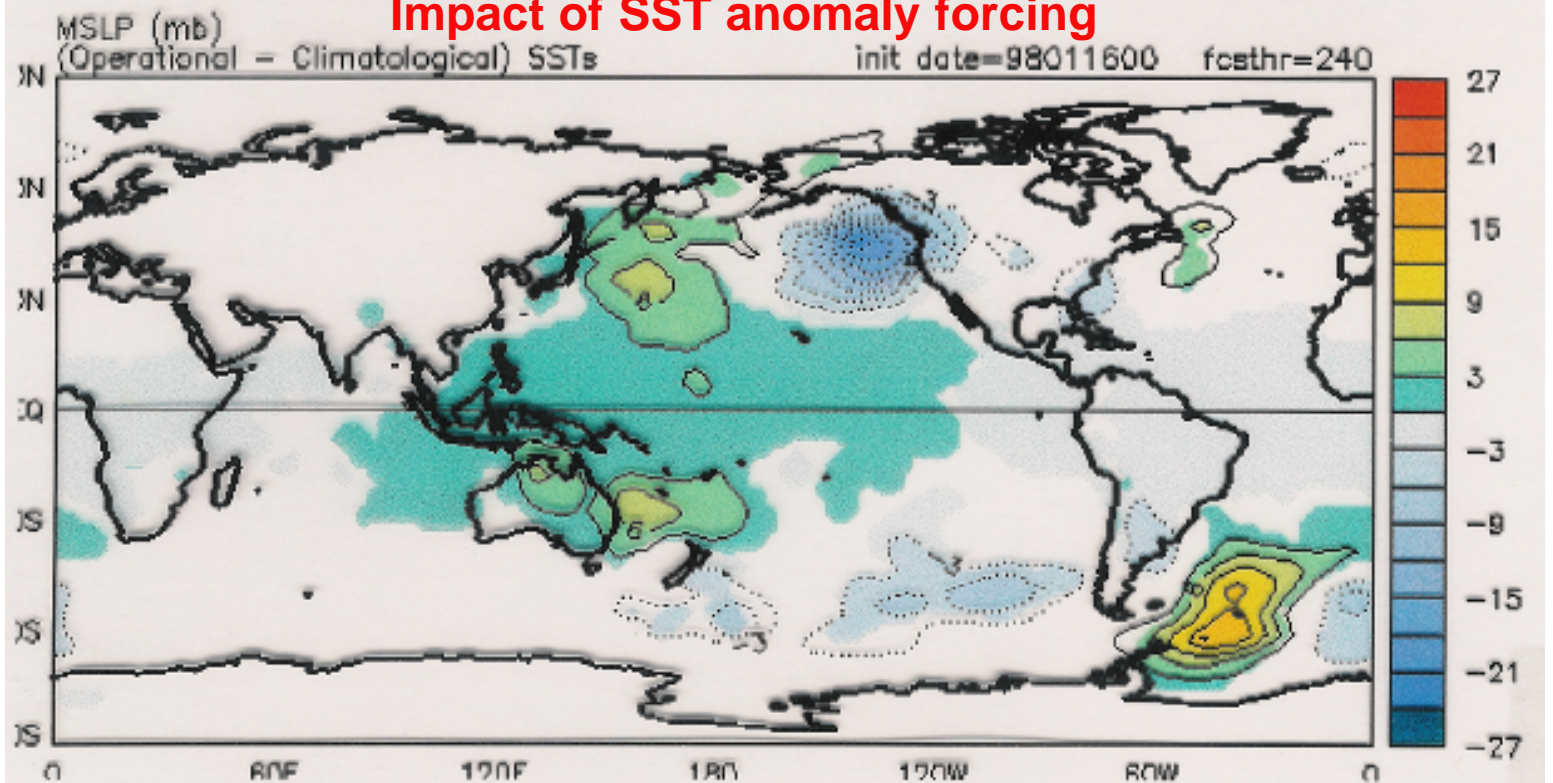
- 1) **Unconditional climate distribution**  
*No forecast made*
- 2) **Conditional climate (ENSO forcing)**  
*AGCM ensemble, El-Nino forcing –  
Second kind of predictability*
- 3) **Initial + Boundary condition forecast**  
*Initial value + boundary forcing  
Full predictability (First & second kinds)*



## Operational 10-day fcst, persisted SST forcing



## Impact of SST anomaly forcing



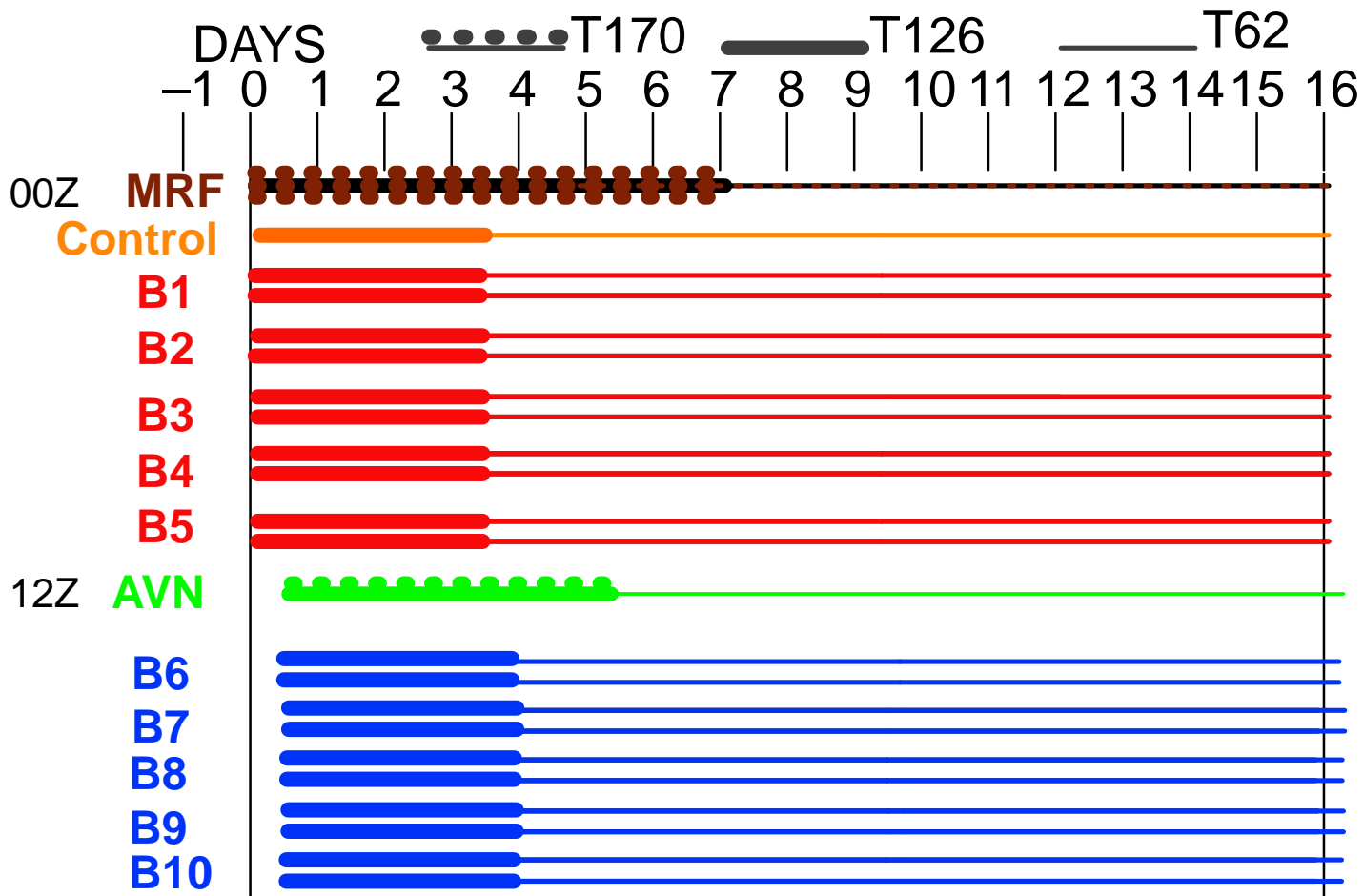
Barsugli et al.

# BRIDGING THE GAP BETWEEN WEATHER AND CLIMATE

## CURRENT NWS PRACTICE

### 1) "WEATHER" ENSEMBLE:

With damped persistence SST boundary forcing



### PLANNED CHANGES FOR ENSEMBLE IN 2002:

- a) 10 forecasts four times per day
- b) T126 resolution extended to 180 hrs

### SHORTCOMING:

No forecast SST information used from coupled system



# BRIDGING THE GAP BETWEEN WEATHER AND CLIMATE

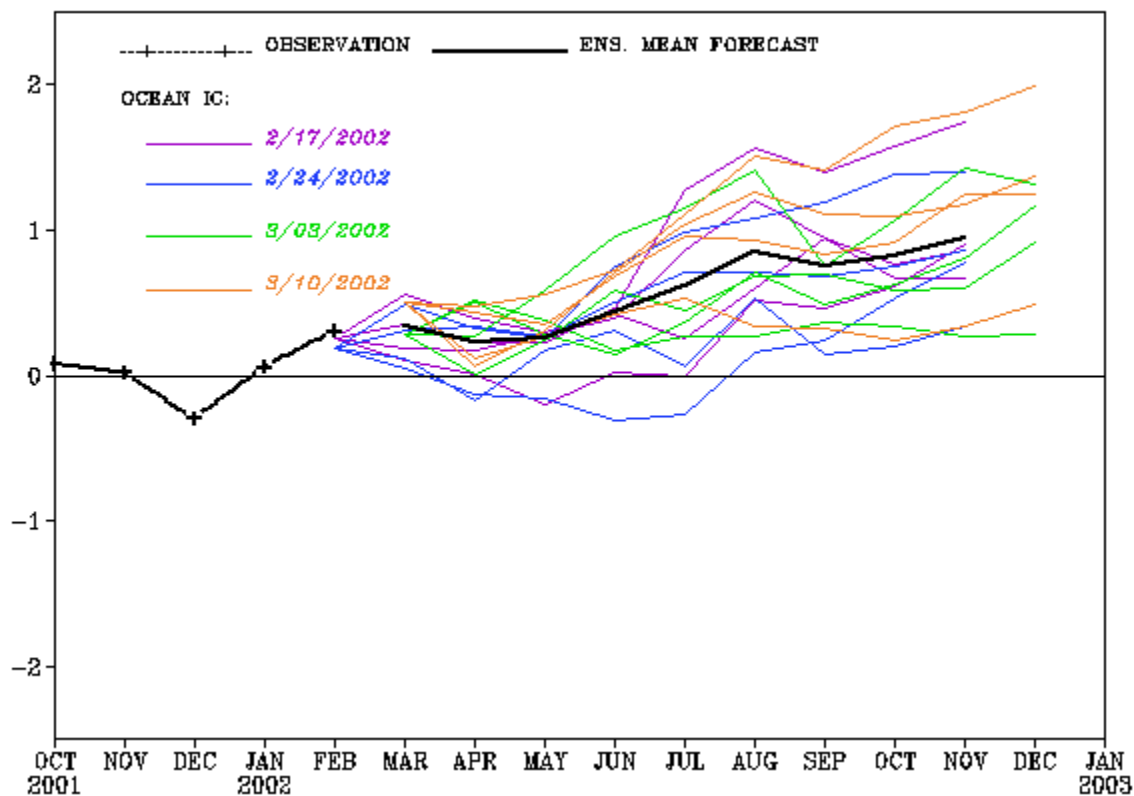
## CURRENT NWS PRACTICE

### 2) "CLIMATE" ENSEMBLE:

- a) 12-months coupled ocean-atm fcsts
- b) Average the SST fcsts



### FORECAST NINO3.4 SST ANOMALIES



- c) Run AGCM ensemble forced by average SST fcst

### STRENGTH:

Ensemble approach used both for coupled and AGCM model fcsts  
for enhancing (weak) signal

### SHORTCOMINGS:

- a) Coupled ensemble (lagged fcst) perturbations not optimal
- b) Uncertainty information related to SST fcst is discarded
- c) Initial condition information from atmosphere not used

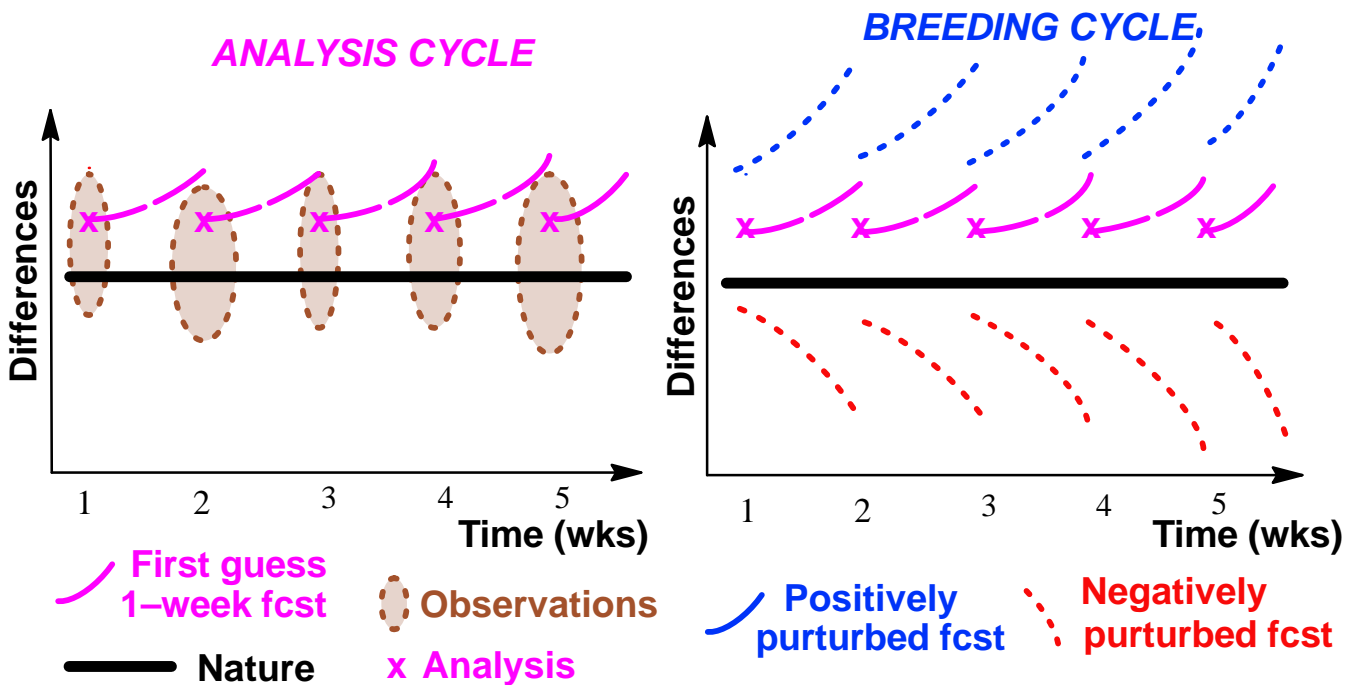
# BRIDGING THE GAP BETWEEN WEATHER AND CLIMATE PLANS

## 3) POSSIBLE FUTURE SYSTEM:

### “WEATHER AND CLIMATE” ENSEMBLE?

#### COUPLED MODEL ENSEMBLE –

Use dynamically constructed perturbations



- Nonlinear bred perturbations capture dominant ENSO instability*
- Initial error present in analysis dominated by same instability*
- Symmetrically placed perturbed fcsts provide optimal ensemble*

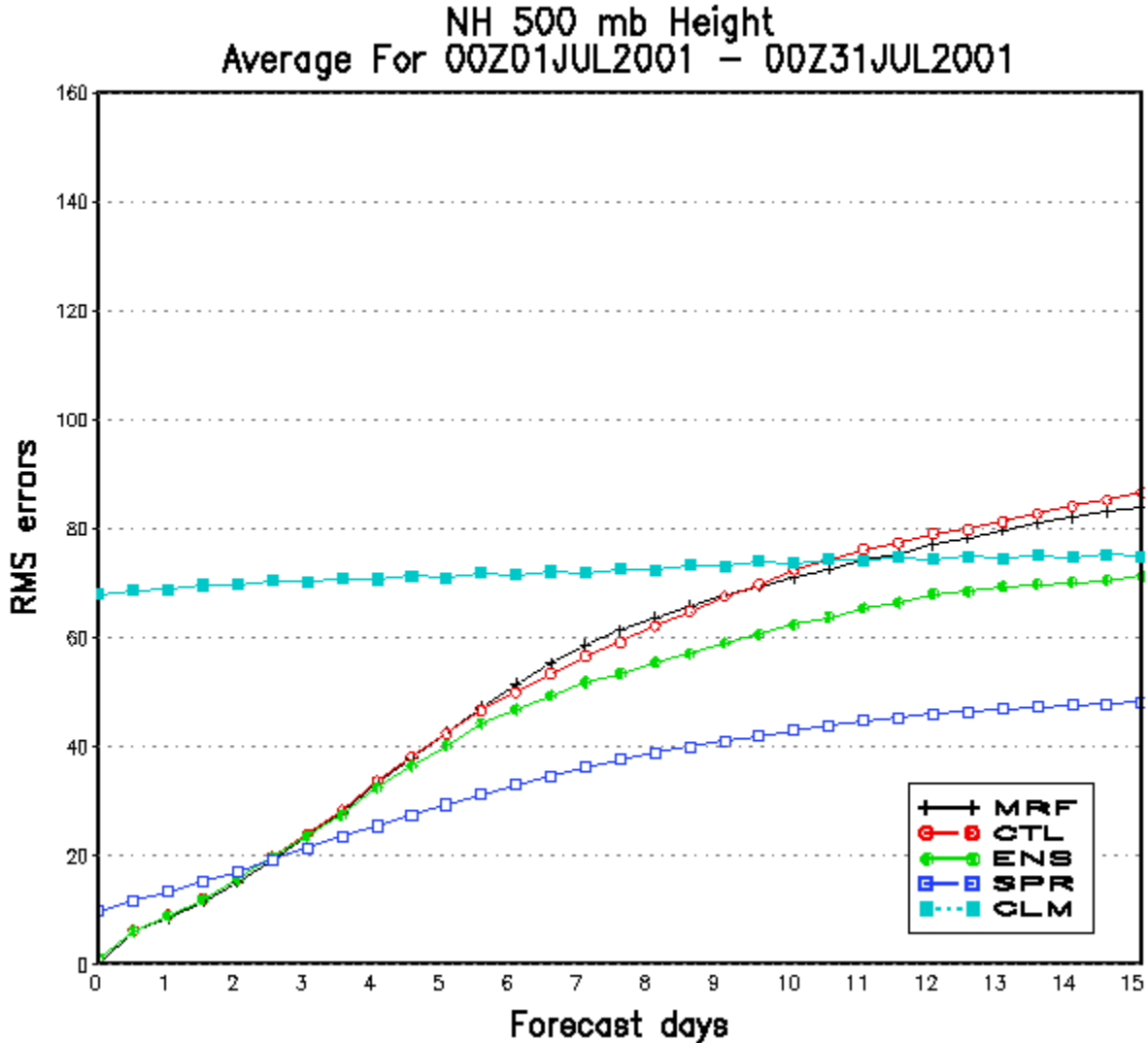
#### AGCM ENSEMBLE –

- Use ensemble SST fcsts as various boundary scenarios
- Single set of AGCM fcsts for all time ranges (*D1-climate*)

#### ONE-TIER SYSTEM – If possible, with new ocean model

# ENSEMBLE APPROACH – ADVANTAGES

## 1) Improved estimate of first moment (ens mean)



## 2) Estimates fcst uncertainty (probabilistic fcsting)

## 3) “Traces” of weather provided by ensemble members – Most queries can be answered – eg:

*What is the probability of 3 consecutive days with frost next week?*

## 4) Offers flow dependent filter – no need for time means

**PROBABIL. DAILY WEATHER FCSTS – DAY 1 through CLIMATE**

PDF varies slower in time/space as predictability diminishes

**CAN REGIME TRANSITIONS BE PREDICTED BEYOND DAY 10?**

# RESOLUTION OF ENSEMBLE BASED PROB. FCSTS

## QUESTION:

What are the typical **variations in foreseeable forecast uncertainty**?  
 What variations in predictability can the ensemble resolve?

## METHOD:

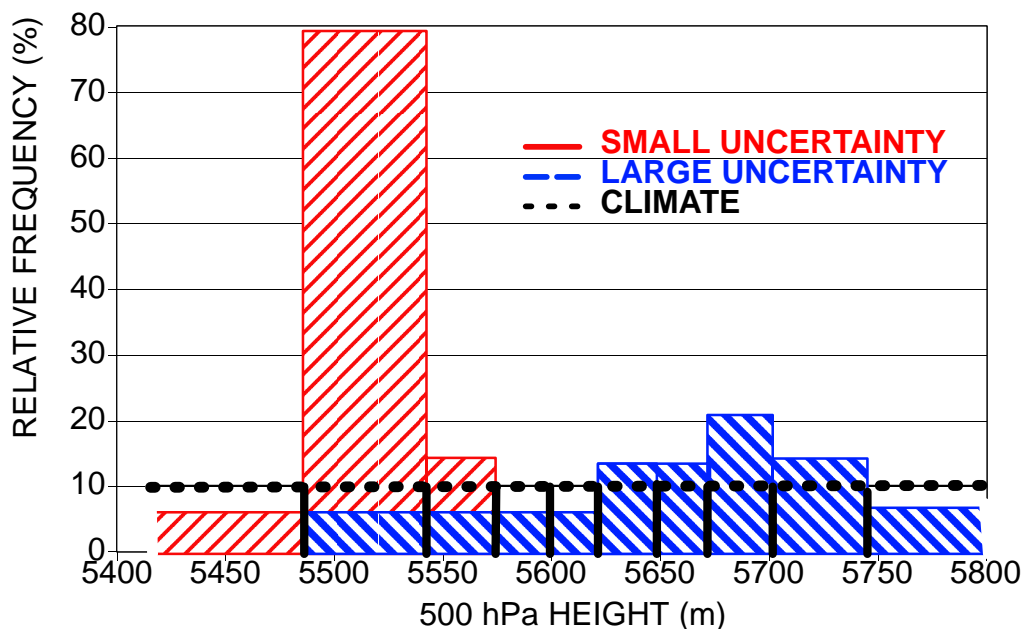
**Ensemble mode value to distinguish high/low predictability** cases  
**Stratify cases** according to ensemble mode value –  
 Use 10–15% of cases when ensemble mode is highest/lowest

## DATA:

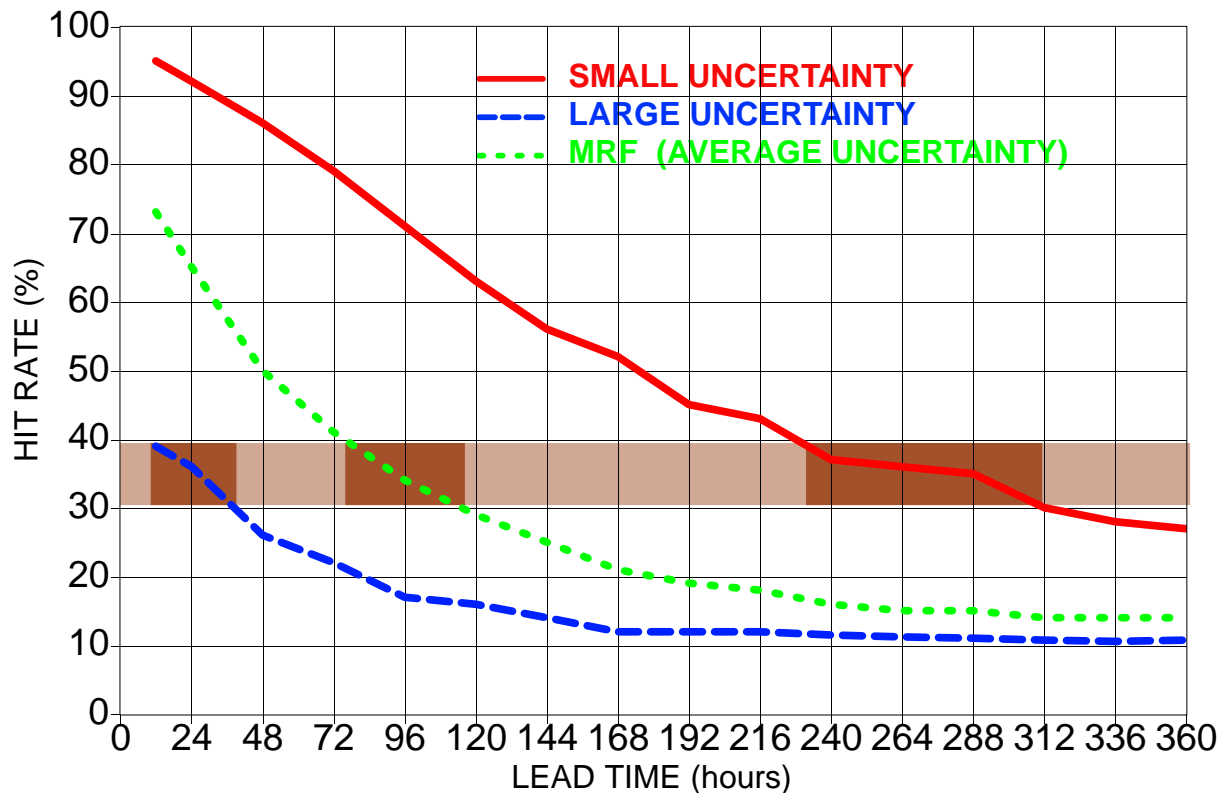
NCEP **500 hPa NH extratropical ensemble fcsts** for March–May 1997  
 14 perturbed fcsts and high resolution control

## VERIFICATION:

**Hit rate** for ensemble mode and hires control fcst



# SEPARATING HIGH VS. LOW UNCERTAINTY FCSTS



**THE UNCERTAINTY OF FCSTS CAN BE QUANTIFIED IN ADVANCE**

## HIT RATES FOR 1-DAY FCSTS

**CAN BE AS LOW AS 36%, OR AS HIGH AS 92%**

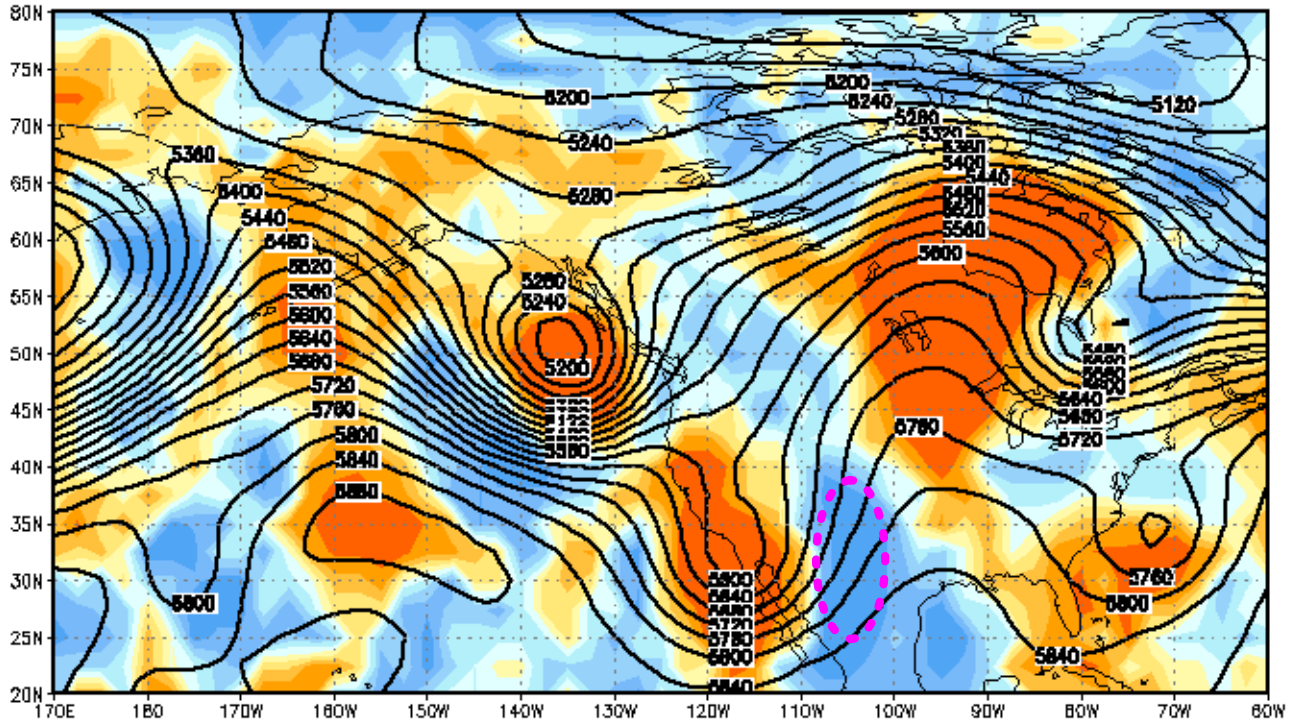
**10–15% OF THE TIME A 12-DAY FCST CAN BE AS GOOD, OR A 1-DAY FCST CAN BE AS POOR AS AN AVERAGE 4-DAY FCAST**

**1–2% OF ALL DAYS THE 12-DAY FCST CAN BE MADE WITH MORE CONFIDENCE THAN THE 1-DAY FCST**

**AVERAGE HIT RATE FOR EXTENDED-RANGE FCSTS IS LOW – VALUE IS IN KNOWING WHEN FCST IS RELIABLE**

TOTH: CLIMATE ENSEMBLE PREDICTION

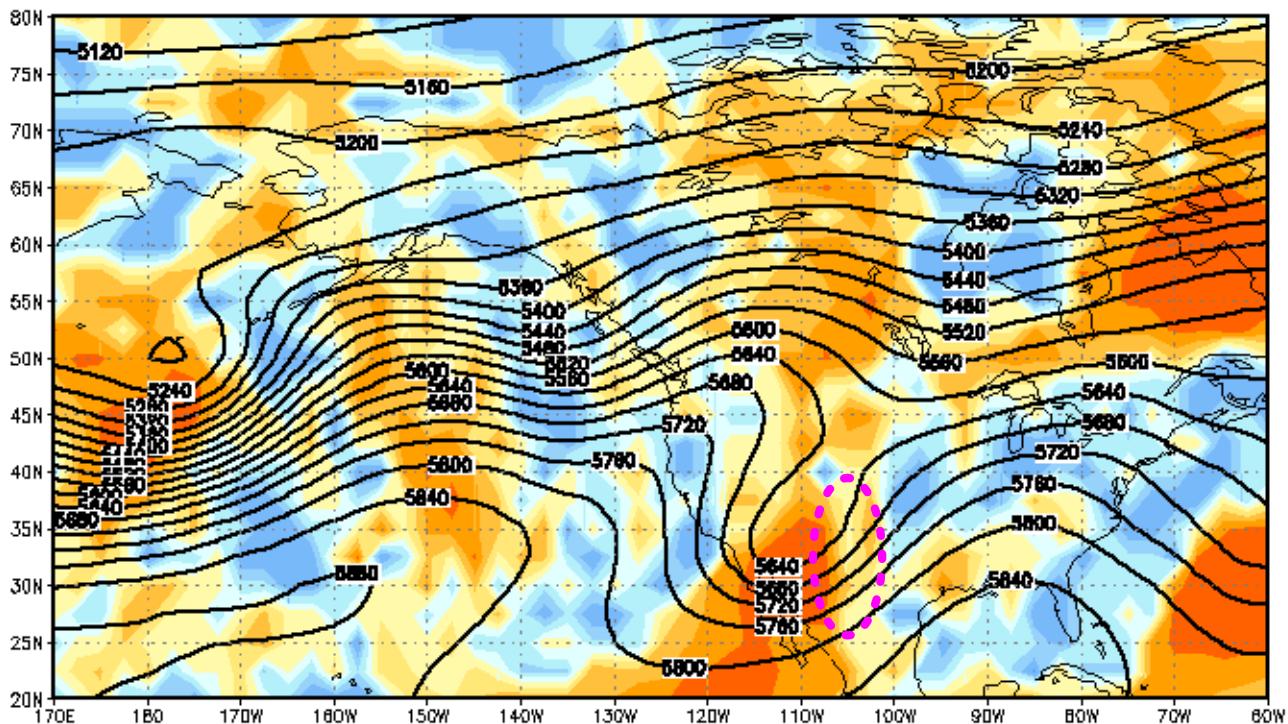
Relative measure of predictability (colors)  
for ensemble mean forecast (contours) of 500 hPa height  
ini: 2000102700 valid: 2000102800 feat: 24 hours



Probability (%) 8 18 22 29 35 44 54 62 74 91

Measure of predictability (%) 10 20 30 40 50 60 70 80 90

Relative measure of predictability (colors)  
for ensemble mean forecast (contours) of 500 hPa height  
ini: 2000102700 valid: 2000110400 feat: 192 hours



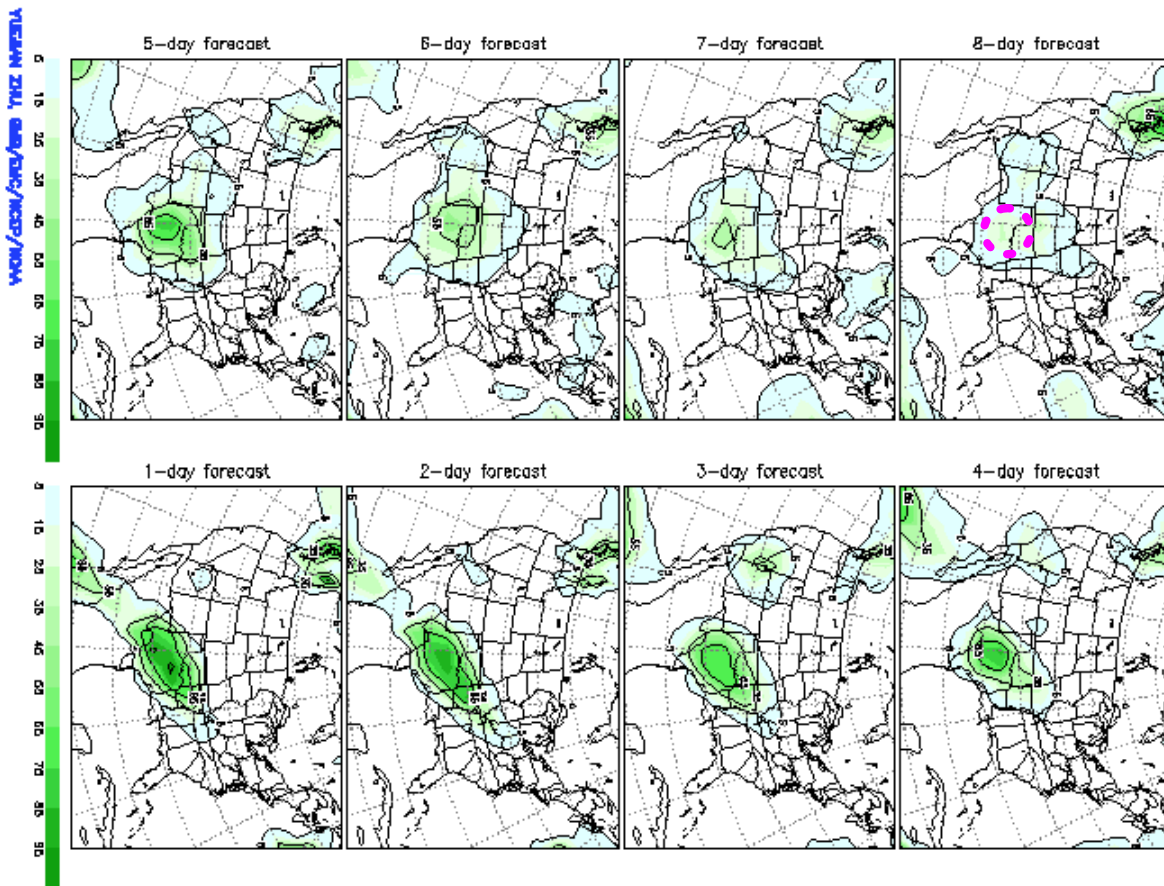
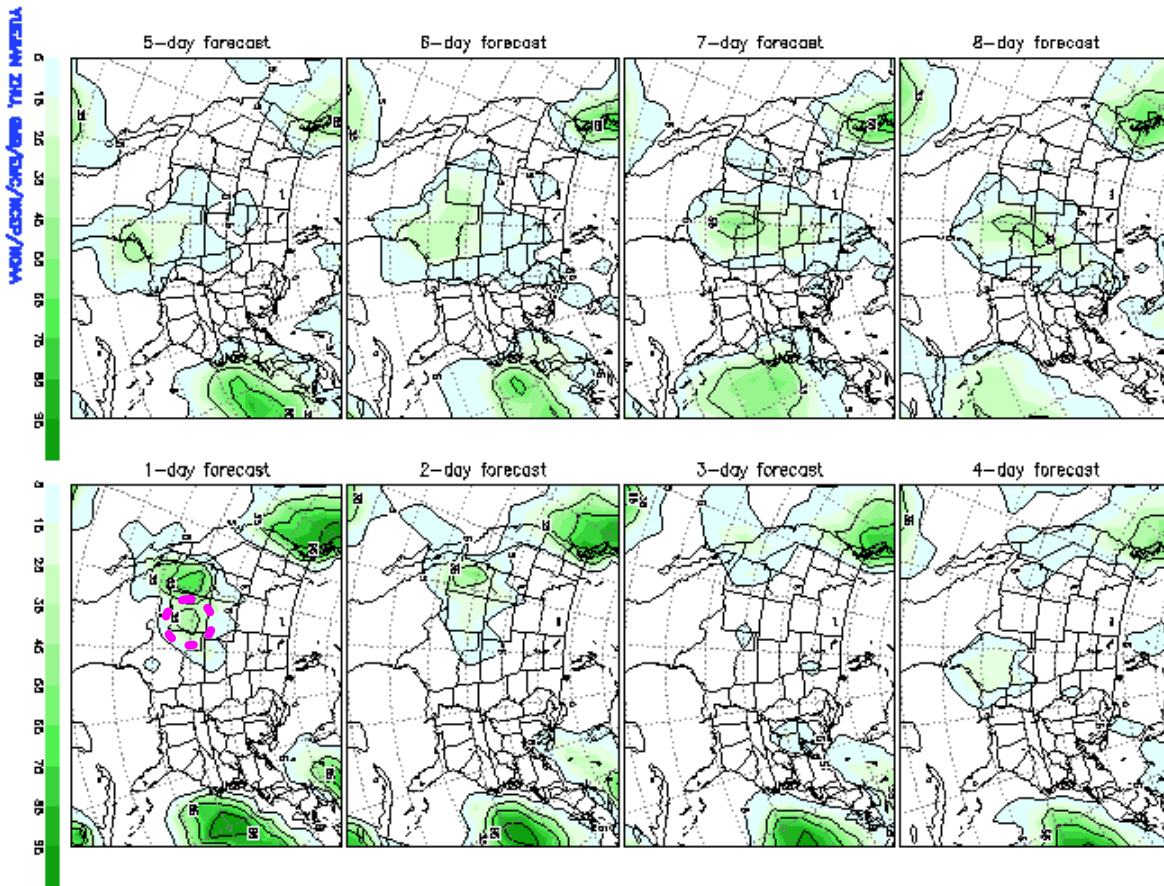
Probability (%) 7 10 10 11 12 12 14 15 22 29

Measure of predictability (%) 10 20 30 40 50 60 70 80 90

TOTAL CLIMATE ENSEMBLE PREDICTION

Ens Prob of Precip Amount Exceeding 0.5 Inch (12.7 mm/day) Valid Period: 2000102712-2000102812

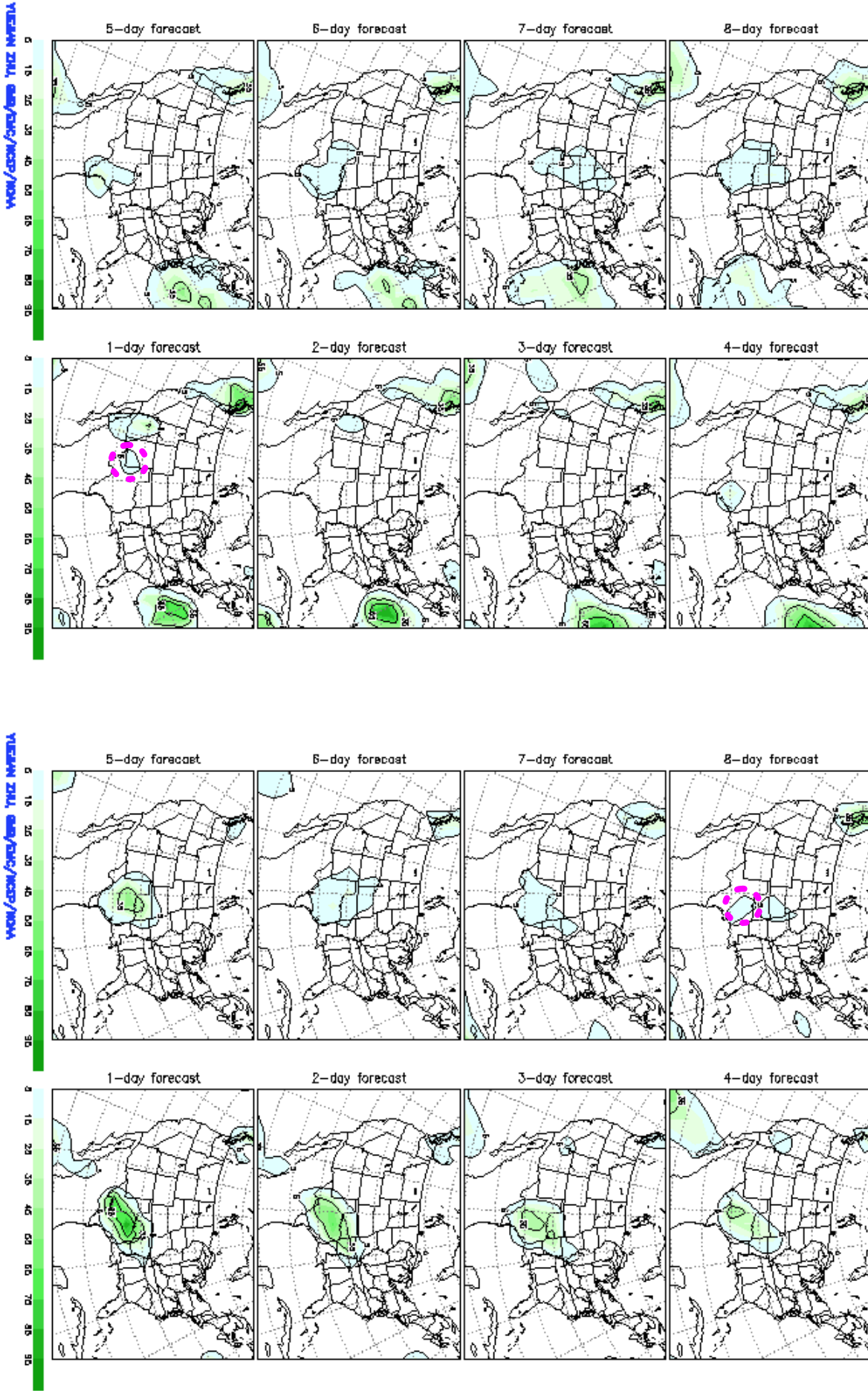
Ens Prob of Precip Amount Exceeding 0.5 Inch (12.7 mm/day) Valid Period: 2000110312-2000110412



TOTH: CLIMATE ENSEMBLE PREDICTION

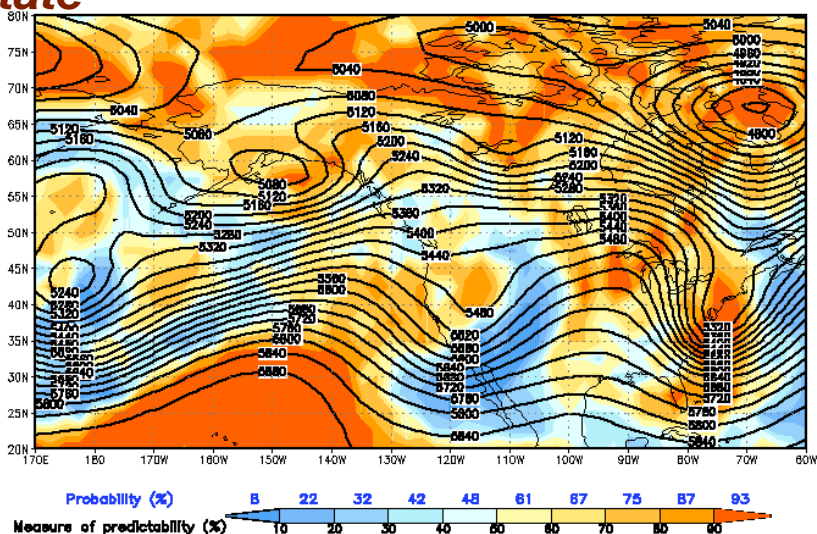
Ens Prob of Precip Amount Exceeding 1.0 Inch (25.4 mm/day) Valid Period: 2000102712-2000102812

Ens Prob of Precip Amount Exceeding 1.0 Inch (25.4 mm/day) Valid Period: 2000110312-2000110412





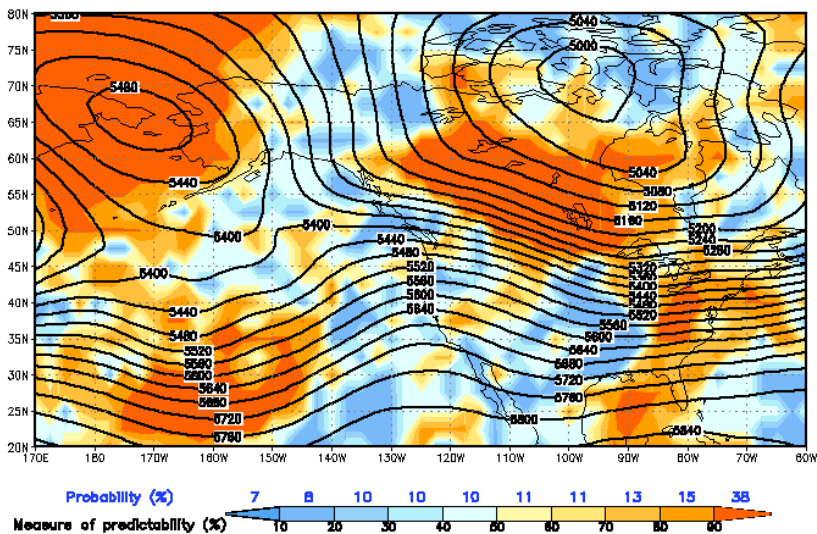
**Initial state** Relative measure of predictability (colors) for ensemble mean forecast (contours) of 500 hPa height  
ini: 2002021700 valid: 2002021800 fcst: 24 hours



**GREAT CHALLENGE:**  
**PREDICTING REGIME TRANSITION AT EXTENDED RANGE**

**ENSEMBLE APPROACH:**  
**CAN BE DONE SUCCESSFULLY**  
(FROM TIME TO TIME)

**15-Day fcst** Relative measure of predictability (colors) for ensemble mean forecast (contours) of 500 hPa height  
ini: 2002021700 valid: 2002030400 fcst: 360 hours

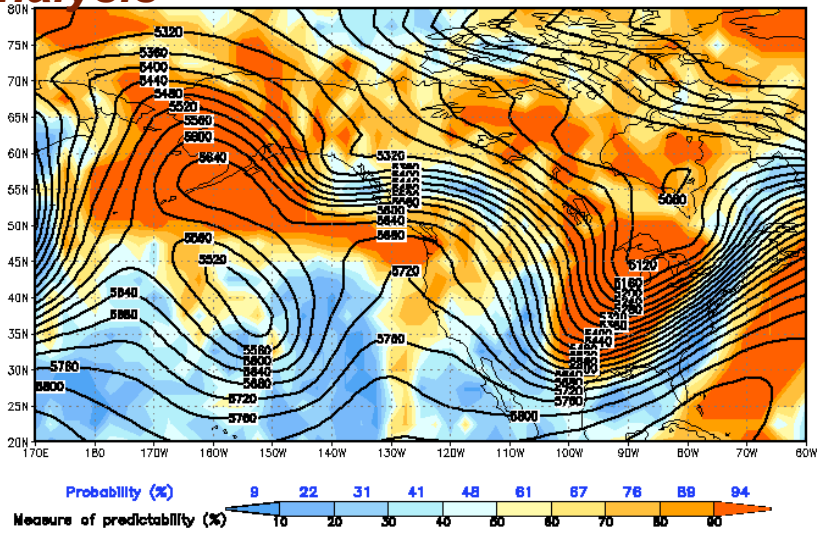


**LOW LEVEL OF SKILL:**  
USE PROBABILISTIC FCSTS

**+/- 24 HR TIMING ACCURACY:**  
USE DAILY FCST DATA  
(NOT TIME MEAN)

**FALSE ALARMS:**  
NEED TO SIMULATE NATURE'S  
DIVERSITY IN NWP MODEL

**Verifying analysis** Relative measure of predictability (colors) for ensemble mean forecast (contours) of 500 hPa height  
ini: 2002030300 valid: 2002030400 fcst: 24 hours



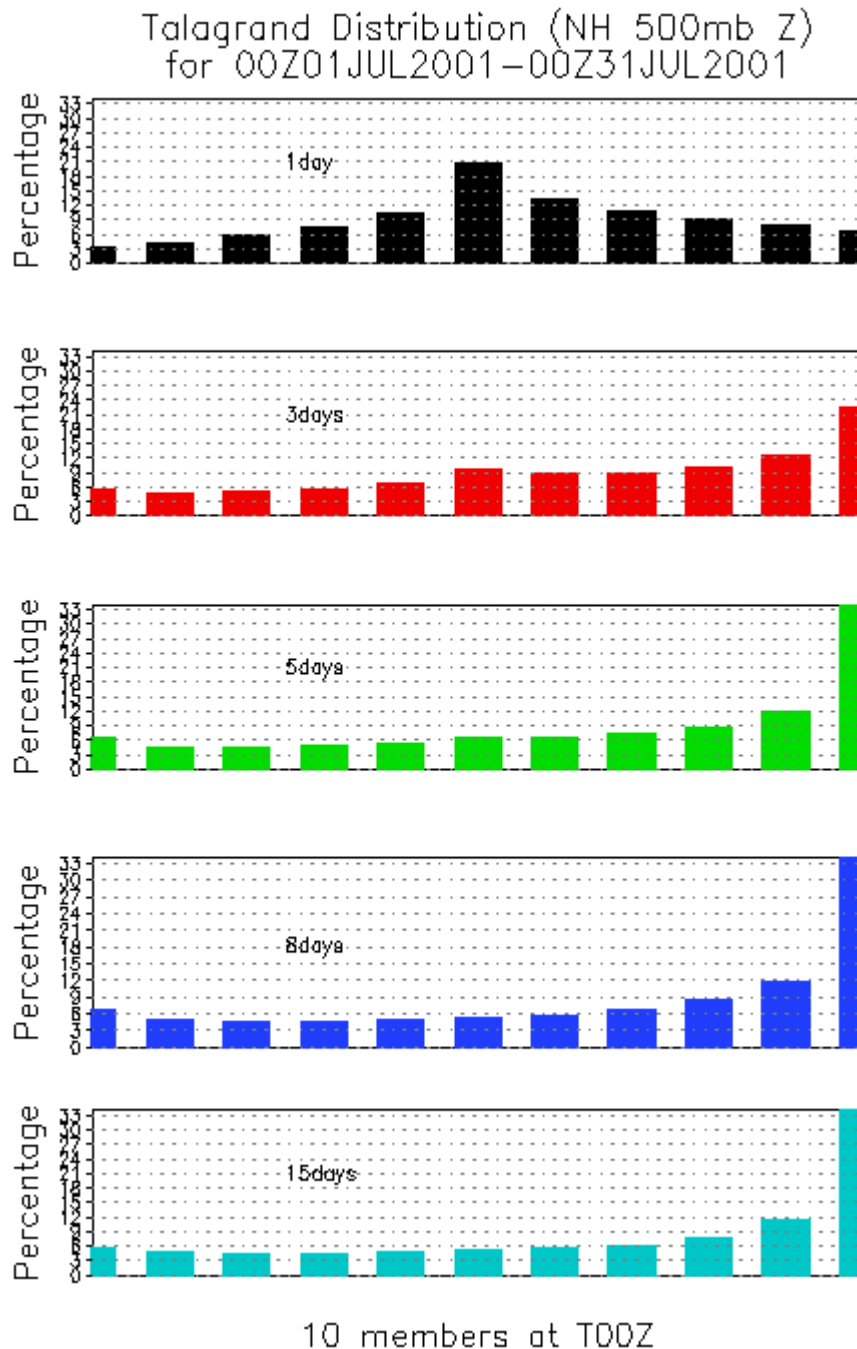
**MISSED EVENTS:**

- 1) LIMIT OF PREDICTABILITY – NO PROBLEM
- 2) MODEL FAILURE – NEED TO INCREASE MODEL DIVERSITY (NOT "ACCURACY")

TOTH: CLIMATE ENSEMBLE PREDICTION  
**ENSEMBLE APPROACH – PROBLEM**

**UNCERTAINTY DUE TO MODEL ERROR IS NOT ACCOUNTED FOR YET**

- => Bias in first and second moment of ensemble
- => 10–25% of time ensemble misses verifying analysis



**NEED TO INCORPORATE MODEL RELATED UNCERTAINTY –**

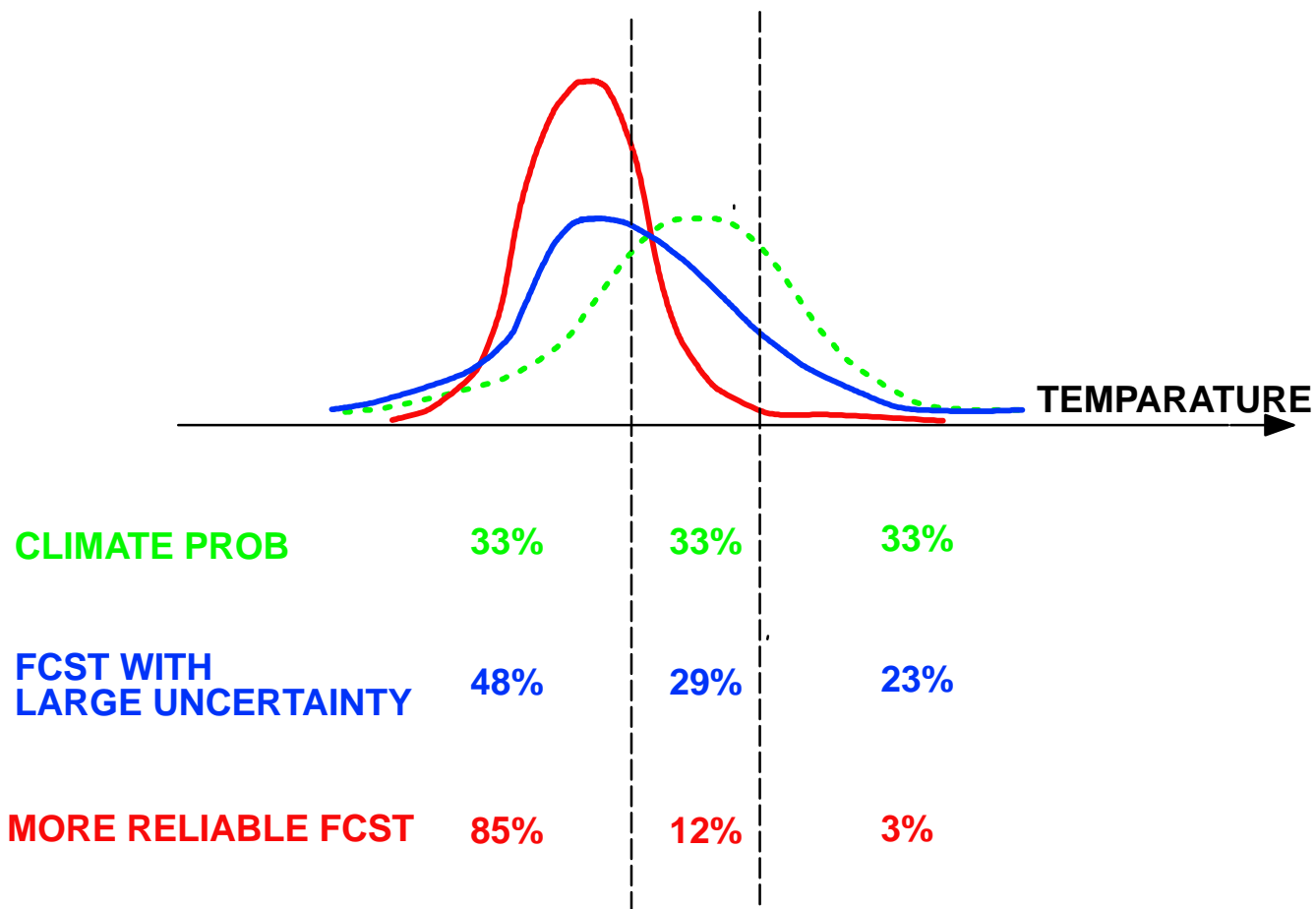
*Vary components/parameters in model*

UNTIL THEN:

**STATISTICAL POSTPROCESSING** – Need large sample

Climate Variability Workshop, Boulder, CO, March 2002

# WHY SHOULD USERS (AND NOT ONLY FCSTERS) CARE ABOUT UNCERTAINTIES IN WEATHER FCSTS?



**BOTH FCSTS CALL FOR BELOW AVERAGE TEMPERATURES**

**ECONOMIC EXAMPLE: COMPANY SELLING "WEATHER DERIVATIVES" (INSURANCE THAT FCST IS CORRECT)**

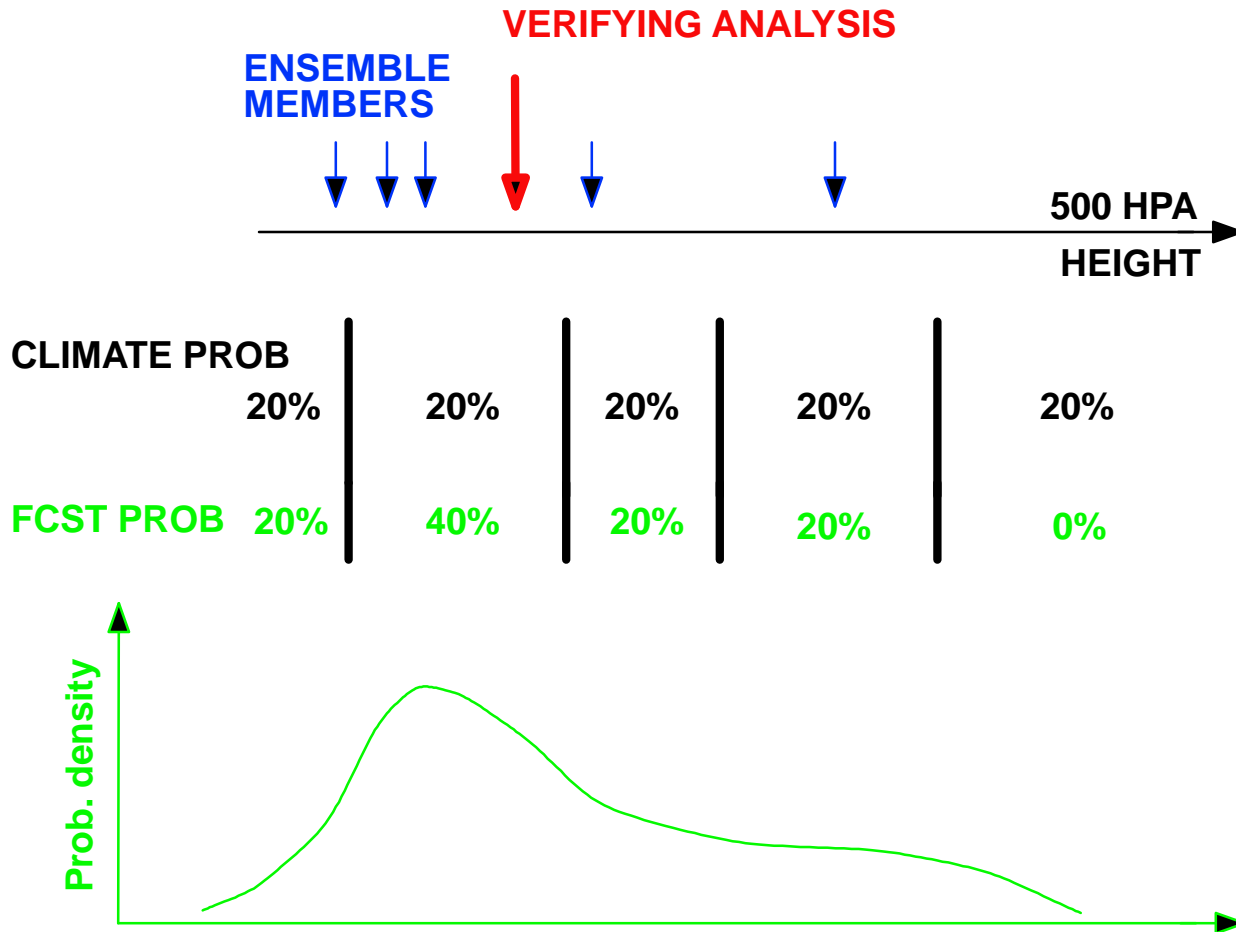
**FOR UNCERTAIN FCST, INSURANCE PREMIUM MUST BE HIGHER**

***IT IS ESSENTIAL THAT THE USERS KNOW ABOUT THE UNCERTAINTIES ASSOCIATED WITH THE WEATHER FCSTS***

TOTH: CLIMATE ENSEMBLE PREDICTION  
**HOW TO CONSTRUCT PROB FCSTS?**

Ensemble gives forecast probability estimates based on finite sample

NEED TO **INTERPOLATE/EXTRAPOLATE** probabilities



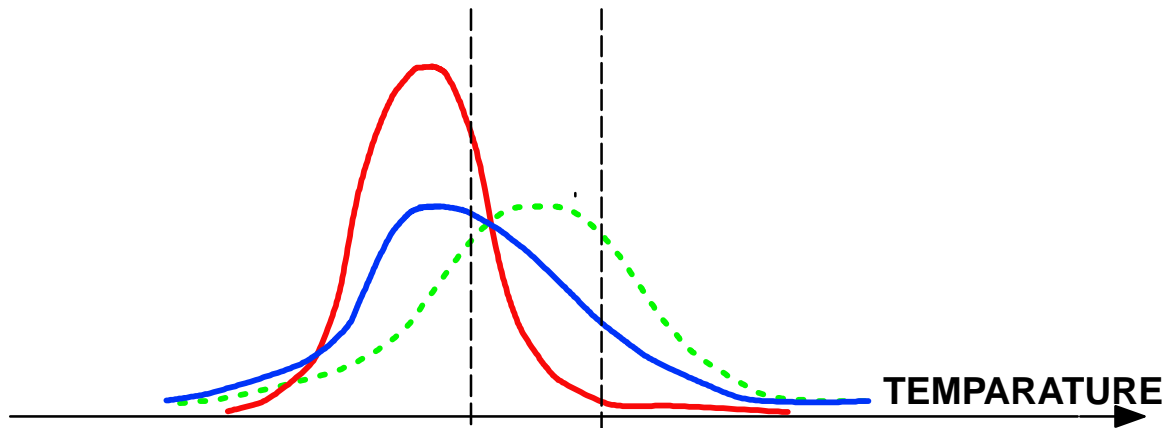
**METHODOLOGY:**

Fit an analytical probability distribution to finite sample from ensemble

**QUESTION:** Finite ens sample has sampling noise in it –  
 How much detail can we trust?

Need to analyze prob fcst performance – **VERIFICATION**

TOTH: CLIMATE ENSEMBLE PREDICTION  
**MAIN CHARACTERISTICS OF PROB FCSTS**



CLIMATE PROB	33%	33%	33%
FCST WITH LARGE UNCERTAINTY	48%	29%	23%
FCST WITH MORE INFO	85%	12%	3%

↑  
**VERIFYING ANALYSIS**

- 1) Must be different from climatology – SHARPNESS
  - 2) Must be consistent with observations – RELIABILITY
- (ie fcst probabilities match observed frequencies)

**Sharpness itself is not a virtue unless fcsts are also reliable**

If both the fcst & obs systems are stationary,

**fcsts can be made perfectly reliable** through calibration

Remaining sharpness is **RESOLUTION** –

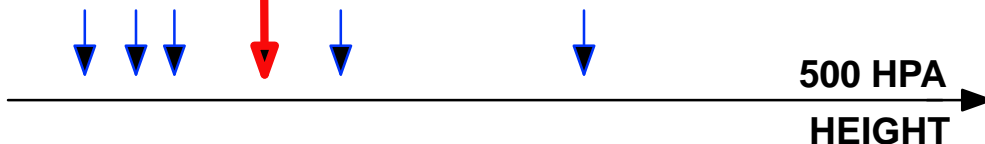
*Real virtue of prob fcsts –*

*Cannot be increased through trivial postprocessing*

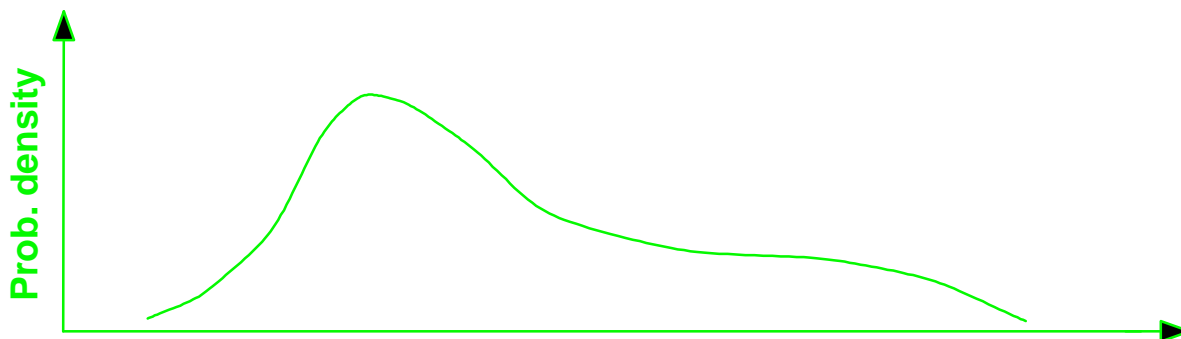
TOTH: CLIMATE ENSEMBLE PREDICTION  
**ENSEMBLE BASED PROBABILISTIC FORECASTS  
 AND THEIR CALIBRATION**

**VERIFYING ANALYSIS**

**ENSEMBLE MEMBERS**

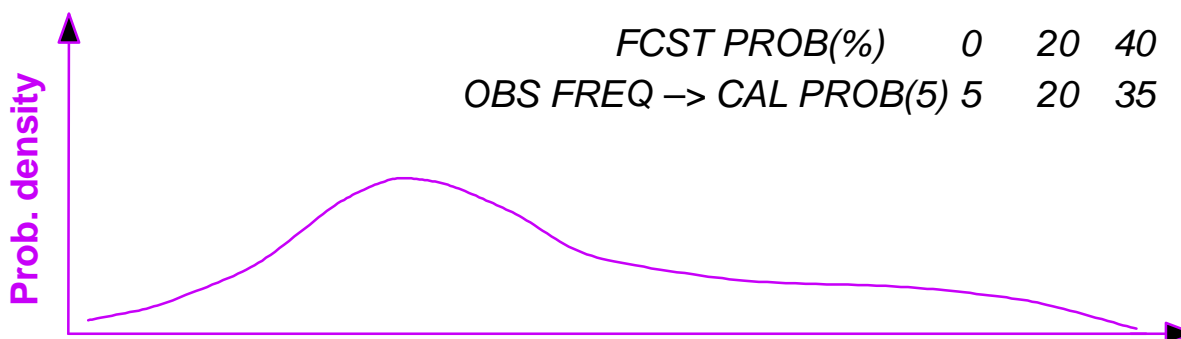


CLIMATE PROB	20%	20%	20%	20%	20%
FCST PROB	20%	40%	20%	20%	0%

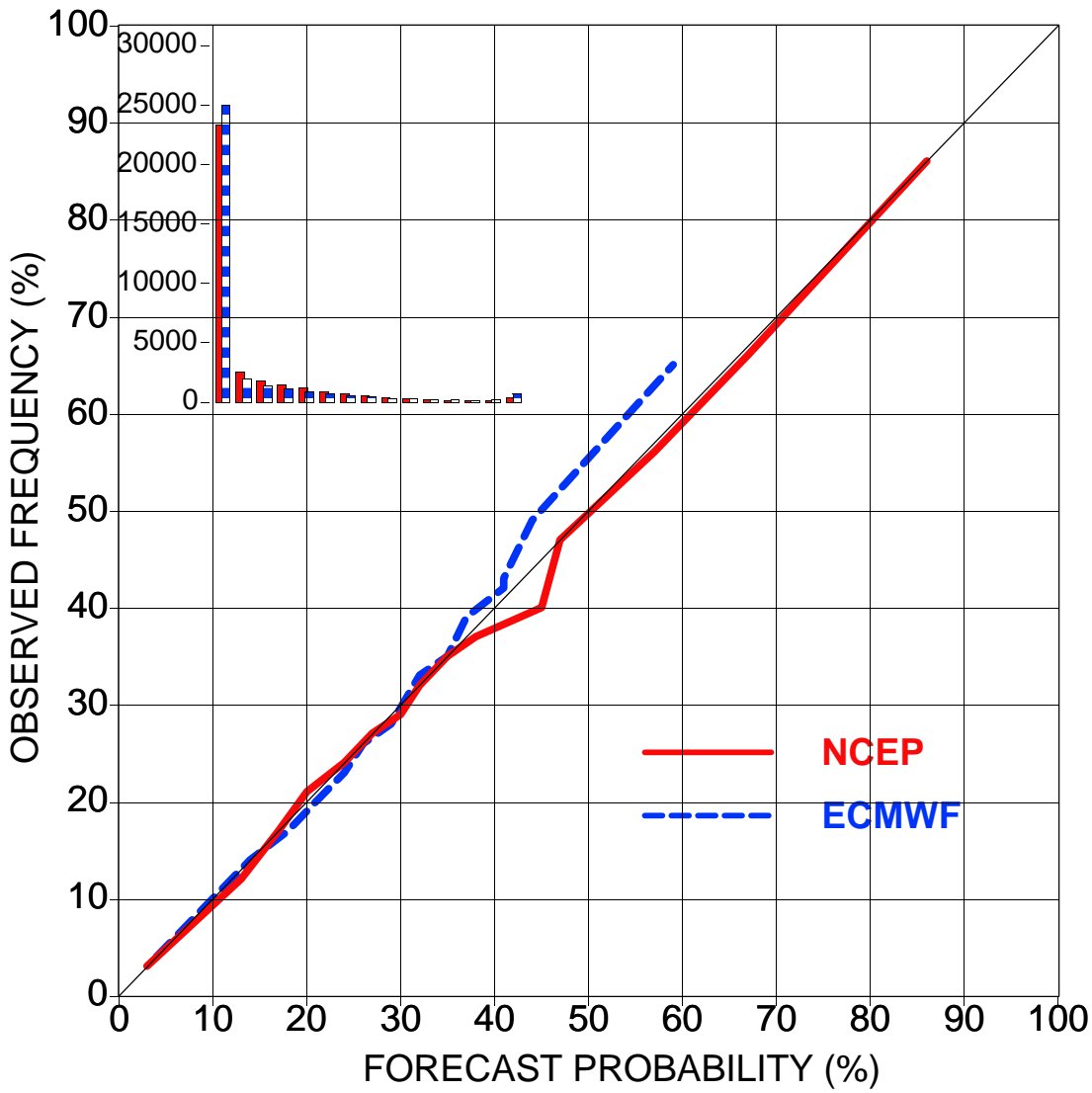


**CALIBRATION, based on observed frequency of each fcst prob. value:**

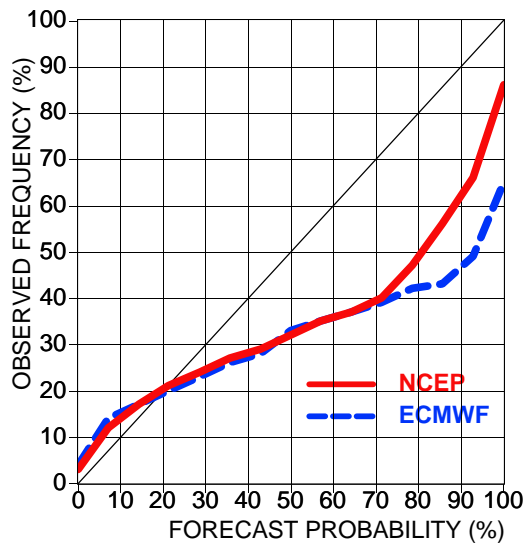
CAL. PROB.	20%	35%	20%	20%	5%
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TOTH: CLIMATE ENSEMBLE PREDICTION



*Reliability diagram for 3-day lead time ensembles for January 1996. Forecast probabilities are based on observed frequencies associated with the same number of ensemble members falling in a particular bin during December 1-20, 1995. The diagram for uncalibrated forecasts is shown on the right.*



1) **TRADITIONAL MEASURES:**

*Categorical fcsts:* Average success rate for modus

*Point fcsts:* Error in expected value, median, etc  
(RMS, Pattern Anomaly Correlation)

2) **DISTRIBUTIONAL MEASURES:**

- a) Talagrand (Verification Rank) diagram  
– measures reliability/consistency only
- b) Reliability diagrams
- c) Brier Skill Score
- d) Ranked Probability Skill Score
- e) Relative Operating Characteristics
- f) Information content
- g) Economic Value



TOT: CLIMATE ENSEMBLE PREDICTION  
**ECONOMIC VALUE OF FORECASTS**

Given a particular forecast, a user either does or does not take action (eg, protects its crop against frost) *Mylne & Harrison, 1999*

		FORECAST	
		YES	NO
OBSERVATION	YES	H(its) <b>Mitigated Loss</b>	M(isses) <b>Loss</b>
	NO	F(false alarms) <b>Cost</b>	C(orrect rejections) <b>No Cost</b>

$$\text{Mean Expense}_{fc} = hML + mL + fC$$

$$\text{Mean Expense}_{perf} = oML$$

$$ME_{cl} = \min[oL, oML + (1-o)C]$$

$$\text{Value} = \frac{ME_{cl} - ME_{fc}}{ME_{cl} - ME_{perf}}$$

$o = \text{climatological frequency}$

Use 10 climatologically equally likely bins to define events

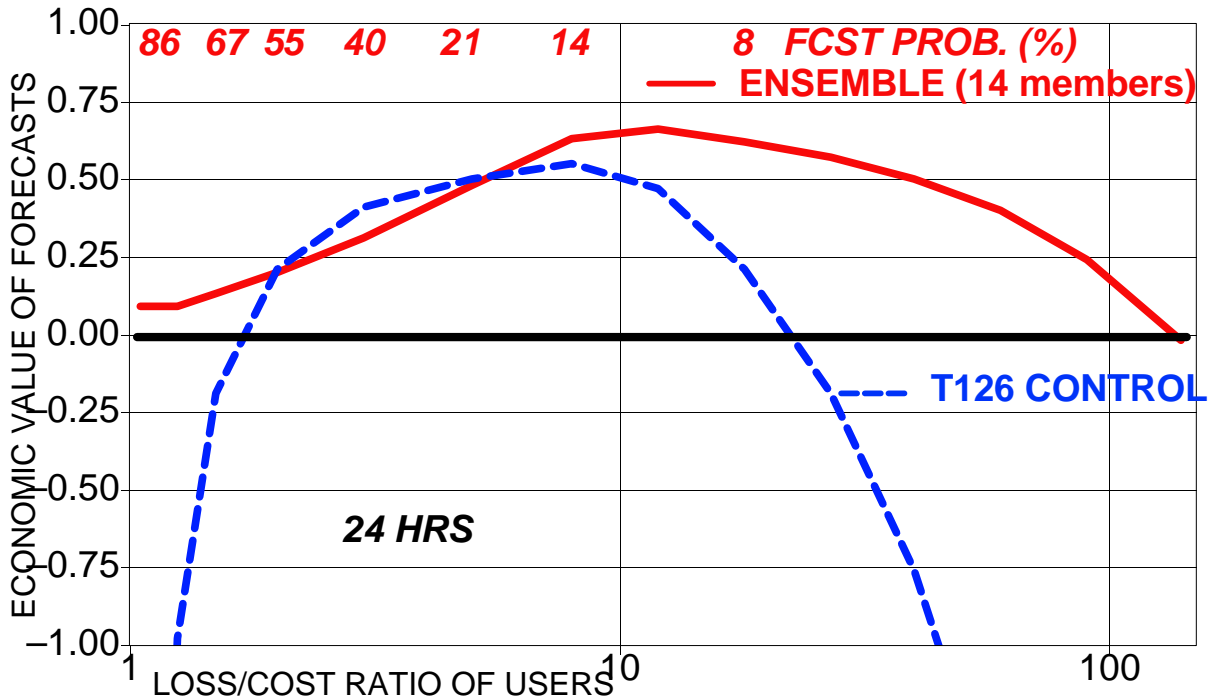
**Hi-res control forecast:** If MRF control falls in a given climate bin, forecast is YES and NO otherwise

**Lo-res ensemble forecast:** Probabilities converted to a categorical fcst given the probability exceeds a certain threshold. Eg., all 30% or higher probabilities count as YES. Among different threshold probabilities one can select the one that results in largest economic value.

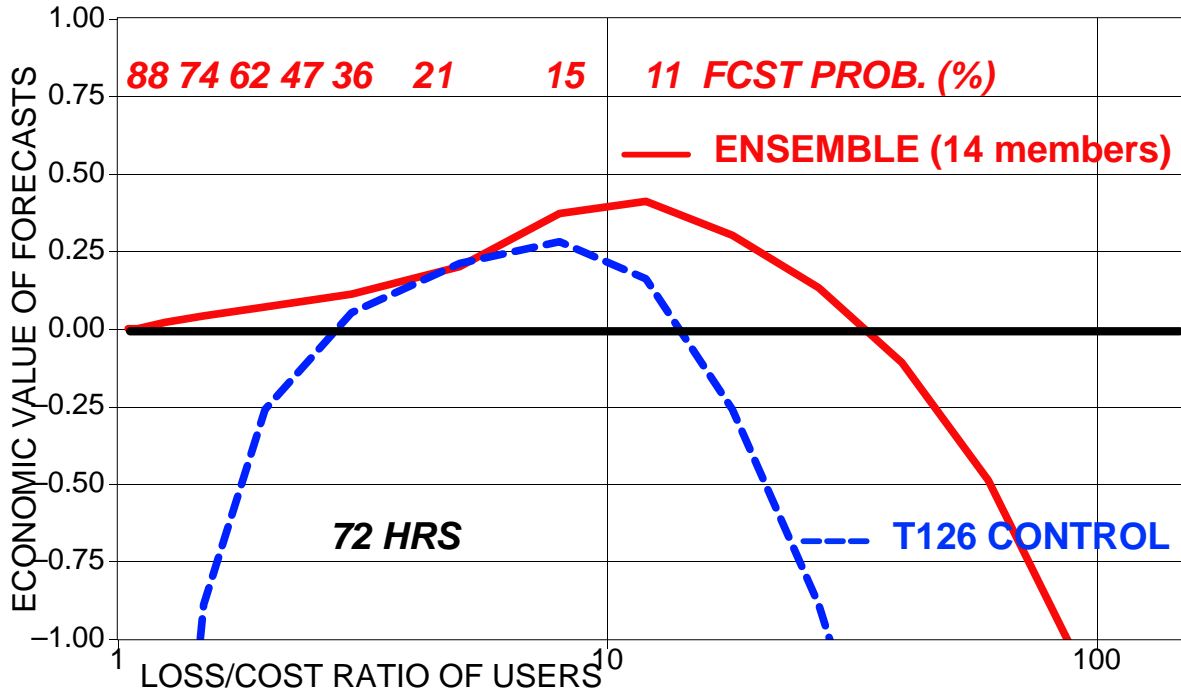
**Results:** For majority of users ensemble is more useful

**Question:** Is it because MRF is dichotomous, while ensemble provides full probability distribution?

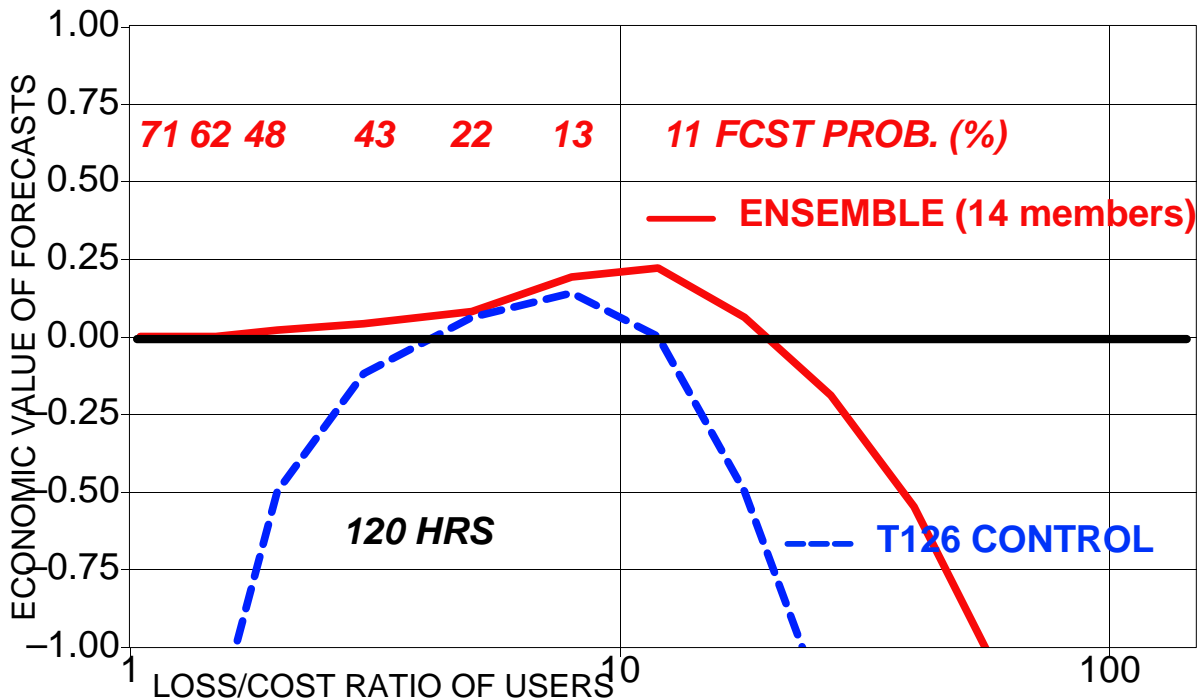
TOTH: CLIMATE ENSEMBLE PREDICTION



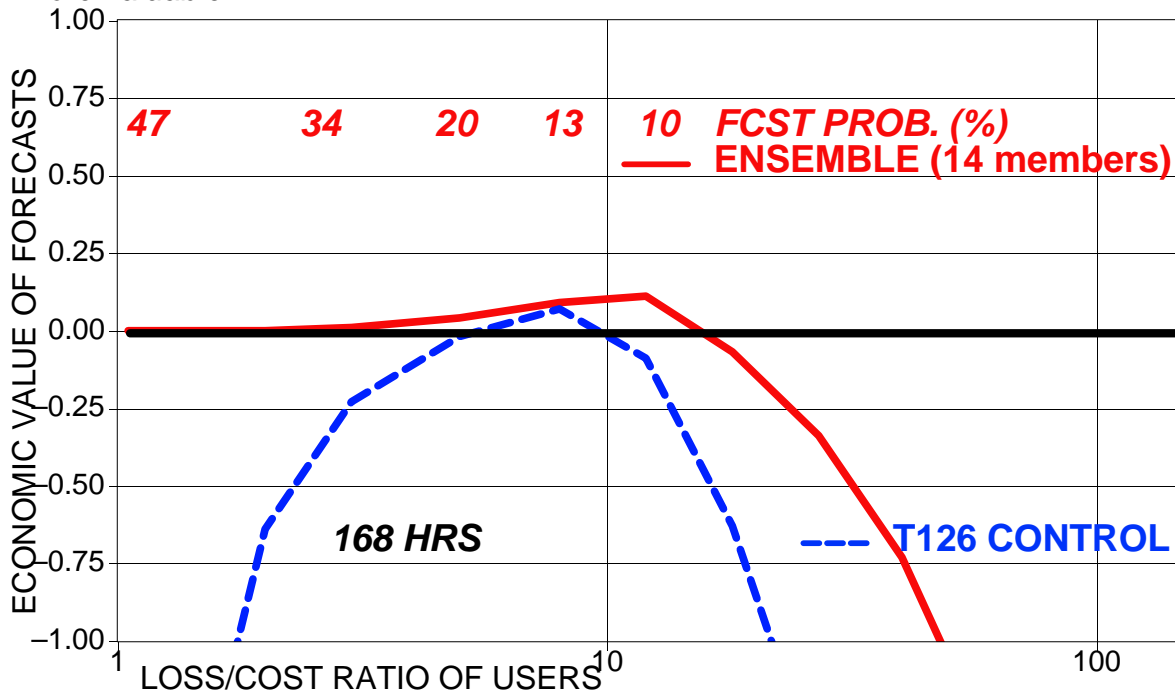
Economic value of 24-hour MRF T126 control, and 14-member T62 ensemble forecasts in predicting events defined in terms of 10 climatologically equally likely bins for 500 hPa height over the NH extratropics, for April–June 1999, for users characterized by different loss/cost ratios (horizontal axis, logarithmic scale). A value of 1.0 stands for using perfect forecasts while values below zero indicate that climatological forecasts are more valuable.



Economic value of 72-hour MRF T126 control, and 14-member T62 ensemble forecasts in predicting events defined in terms of 10 climatologically equally likely bins for 500 hPa height over the NH extratropics, for April–June 1999, for users characterized by different loss/cost ratios (horizontal axis, logarithmic scale). A value of 1.0 stands for using perfect forecasts while values below zero indicate that climatological forecasts are more valuable.



Economic value of 120-hour MRF T126 control, and 14-member T62 ensemble forecasts in predicting events defined in terms of 10 climatologically equally likely bins for 500 hPa height over the NH extratropics, for April–June 1999, for users characterized by different loss/cost ratios (horizontal axis, logarithmic scale). A value of 1.0 stands for using perfect forecasts while values below zero indicate that climatological forecasts are more valuable.



Economic value of 168-hour MRF T126 control, and 14-member T62 ensemble forecasts in predicting events defined in terms of 10 climatologically equally likely bins for 500 hPa height over the NH extratropics, for April–June 1999, for users characterized by different loss/cost ratios (horizontal axis, logarithmic scale). A value of 1.0 stands for using perfect forecasts while values below zero indicate that the use of climatological forecasts are more valuable.

## **SUMMARY**

### **ENSEMBLE FORECASTING: STRENGTHS AND LIMITS**

- 1) DEFINITION OF CHAOS  
***DETERMINISM + INITIAL VALUE SENSITIVITY***
- 2) INITIAL VALUE RELATED PREDICTABILITY/UNCERTAINTY  
***ATMOSPHER.: DAYS; COUPLED SYSTEM: MONTHS***
- 3) BOUNDARY CONDITION RELATED PREDICT./UNCERTAINTY  
***ATMOSPHER.: DAYS–MONTHS***
- 4) BRIDGING THE GAP BETWEEN WEATHER AND CLIMATE  
***COMBINE INITIAL VALUE AND BOUNDARY FORCING***
- 5) ADVANTAGES OF USING ENSEMBLE FCSTS  
***MORE ACCURATE FCST***  
***CASE DEPENDENT UNCERTAINTY ESTIMATE***  
***DAILY PROB FCSTS AT ALL TIME RANGES***
- 6) PROBLEMS WITH ENSEMBLES  
***MODEL RELATED ERRORS NOT ACCOUNTED FOR:***  
***BIAS IN FIRST & SECOND MOMENTS***  
***NEED TO BUILD VARIABILITY INTO MODELS –***  
***DIFFICULT TASK – IF SUCCESSFUL,***  
***CAN IMPROVE RESOLUTION***
- 7) VERIFICATION  
***RELIABILITY & RESOLUTION***
- 8) POSTPROCESSING  
***IMPROVES RELIABILITY, NOT RESOLUTION***  
***MODEL BIAS PROBLEM GREATLY REDUCED***