

# Implementing Efficient Dynamic Formal Verification Methods for MPI Programs<sup>\*</sup>

Sarvani Vakkalanka<sup>1</sup>, Michael DeLisi<sup>1</sup>, Ganesh Gopalakrishnan<sup>1</sup>,  
Robert M. Kirby<sup>1</sup>, Rajeev Thakur<sup>2</sup>, and William Gropp<sup>3</sup>

<sup>1</sup> School of Computing, Univ. of Utah, Salt Lake City, UT 84112, USA

<sup>2</sup> Math. and Comp. Sci. Div., Argonne Nat. Lab., Argonne, IL 60439, USA

<sup>3</sup> Dept. of Computer Sci., Univ. of Illinois, Urbana, Illinois, 61801, USA

**Abstract.** We examine the problem of formally verifying MPI programs for safety properties through an efficient dynamic (runtime) method in which the processes of a given MPI program are executed under the control of an interleaving scheduler. To ensure full coverage for given input test data, the algorithm must take into consideration MPI’s out-of-order completion semantics. The algorithm must also ensure that nondeterministic constructs (e.g., MPI wildcard receive matches) are executed in all possible ways. Our new algorithm rewrites wildcard receives to specific receives, one for *each* sender that can potentially match with the receive. It then recursively explores each case of the specific receives. The list of potential senders matching a receive is determined through a runtime algorithm that exploits MPI’s operation ordering semantics. Our verification tool ISP that incorporates this algorithm efficiently verifies several programs and finds bugs missed by existing informal verification tools.

## 1 Introduction

With the increasing use of MPI for the distributed programming of virtually all high-performance computing clusters in the world, it is important that MPI programs be verified to be free of bugs. With the need to re-verify MPI programs after each optimization step, the process of verification must involve only modest computing resources and limit manual tedium. As MPI programs can contain many types of bugs, including deadlocks, resource leaks, and numerical inaccuracies, it is practically impossible for a single tool to guarantee the coverage of bugs in all these classes. Therefore, approaches that focus on a limited bug class and guarantee full coverage for that class are preferred.

In this paper, we present our C MPI program verification tool, named In-situ Partial Order (ISP), that incorporates a novel scheduling algorithm called POE (Partial Order reduction avoiding Elusive interleavings). ISP guarantees to detect *all* deadlocks and local assertion violations in MPI programs containing 24 of the most commonly used MPI functions. For these MPI programs, the ISP tool will explore close to the minimal number of interleavings. Furthermore, ISP

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does not require any modeling effort on part of users, allowing it to be easily re-run during program development. ISP enjoys the same ease of use as the dynamic verification tools Umpire [2], Marmot [3], ConTest [4], and Jitterbug [5] (to name a few). However, the POE algorithm offers the formal guarantee of finding *all* deadlocks. As shown by experiments on our web site [13], of the 69 Umpire tests, 30 contain deadlocks, and ISP detects all of them, while exploring a very small number of interleavings. In contrast, Marmot fails to find deadlocks in eight of these tests, despite being run multiple times. When these tests were run with MPICH2 repeatedly, the deadlock detection success was unpredictable. Tools that rely on perturbing schedules simply cannot guarantee coverage.

The main feature of POE is that it explores only *relevant* interleavings, using a technique known as *partial order reduction* [6]. Without this idea, any exploration method for MPI will go out of hand. For instance, consider the short MPI program in Figure 1 that begins with two sends in P0 and P2, and a wildcard receive in P1. The total number of interleavings of all these MPI calls is 210.<sup>4</sup> However, to trigger `error1`, we need to consider the interleavings in which the send of P2 matches the wildcard receive. Testing-oriented tools may easily miss these interleavings. Thanks to partial order reduction, ISP will: (i) pick an arbitrary order for executing P0’s first send and P1’s first receive, (ii) pick an arbitrary order to execute P2’s first send and P1’s second receive, and then (iii) consider *both* the `Send` matches with the wildcard receive (shown by `*`).

```
P0: MPI_Send(to P1...);    MPI_Send(to P1, data = 22);
P1: MPI_Recv(from P0...);  MPI_Recv(from P2...);
    MPI_Recv(*, x);        IF (x==22) THEN error1 ELSE MPI_Recv(*, x);
P2: MPI_Send(to P1...);    MPI_Send(to P1, data = 33);
```

**Fig. 1.** A Simple MPI Example with Wildcard Receives

ISP has built-in knowledge of the commuting properties of MPI functions. For example, consider an MPI program in which `MPI_Barrier` is invoked by  $N$  processes. ISP would, in general, explore only one of the  $N!$  ways in which to have invoked the barrier calls. In our implementation of the 24 MPI functions, alternate interleavings are explored for wildcard receives, `WAIT_ANY`, and `TEST_ANY`.

**Overview of ISP’s use of PMPI:** We use the well-known PMPI mechanism, normally used for performance studies, to support runtime model checking in ISP. We introduce an extra process called the *verification scheduler*. ISP provides its own version of “MPI\_” for each MPI function  $f$ . Within `MPI_`, we arrange for handshakes with the scheduler that realizes the POE algorithm. When the scheduler finally gives permission to fire  $f$ , we invoke `PMPI_` from within our version of `MPI_`. The MPI runtime only sees the `PMPI_` calls.

<sup>4</sup>  $(7!)/((2!).(3!).(2!))$

**Related Work:** Techniques for eliminating nondeterminacy for testing parallel programs were studied in [14]. A dynamic verification approach for reactive C programs was first proposed by Godefroid [7]. Flanagan and Godefroid [8] extend this work, incorporating a more efficient *dynamic partial order reduction* (DPOR) algorithm. In [1], we presented the first DPOR-based verification method for MPI programs that employ one-sided communication. In [9], we reported a preliminary implementation of DPOR for MPI’s two-sided operations. This algorithm did not address the full range of out-of-order behaviors of MPI. It also proved incapable of controlling the MPI runtime to force the desired wildcard receive matches (see Section 2). POE overcomes both these limitations, and replaces DPOR – the former algorithm implemented within ISP. Exploiting MPI’s semantics, POE employs a strategy of *lookahead computation* to discover how sends and receives in an MPI program match. A formal presentation of the POE algorithm is given in [10].

**Roadmap:** The remainder of this introduction presents in detail the three new ideas used in POE: *Forcing Wildcard Matches* (Section 1.1), *Handling Out-of-order Completion* (Section 1.2), and *Discovering Match-Sets* (Section 1.3). Section 2 presents the POE algorithm in detail, focusing on sends, receives, and barriers. Section 2.2 describes how many additional MPI commands are smoothly handled by the extended POE algorithm implemented in ISP. We also discuss how the user interface of a Visual Studio integration of POE works: we strive to preserve the users’ view of their MPI program, despite the fact that our POE algorithm changes the internal computation through dynamic rewriting. Section 3 presents experimental results and Section 4 concludes.

## 1.1 Forcing Wildcard Matches

Consider the example in Figure 2, with line 2 containing a wildcard receive. A match between the `Isend` on line 6 and `Irecv` on line 2 (wildcard) will enable `Recv` on line 3 to match with the `Isend` on line 9. However, if the `Isend` on line 9 were to match the `Irecv` on line 2, a *deadlock* would result, with `Recv` (line 3) no longer able to match `Isend` (line 6). Clearly, we cannot leave out this second option (process interleaving) during testing.

The role of a dynamic verification tool for MPI is to determine, at runtime, the specific matches possible, and explore *all relevant* ones - that is, a representative of each equivalence class of equivalent interleavings. This method must be carried out at runtime: (i) the outcomes of control branches through conditional statements will be known only at runtime and (ii) the send/receive targets/sources,

```

0 : // * means MPI_ANY_SOURCE
1 : if (rank == 0)
2 : { MPI_Irecv(&buff1, *, &req);
3 :   MPI_Recv (&buff2, from 2);
4 :   MPI_Wait (&req) }
5 : else if (rank == 1)
6 : { MPI_Isend(buff1, to 0, &req);
7 :   MPI_Wait (&req); }
8 : else if (rank == 2)
9 : { MPI_Isend(buff2, to 0, &req);
10:  MPI_Wait (&req); }

```

**Fig. 2.** *Relevant Interleavings and Elusive Matches during Dynamic Verification of MPI Programs*

and other details (communicator, tag, etc.) may be values that are computed at runtime.<sup>5</sup>

We now explain briefly why DPOR does not work for MPI. Suppose a DPOR-based algorithm is able to determine that `Isend` (line 6) matched `Irecv` (line 2), and that `Isend` (line 9) is also a potential alternate match for this `Irecv`. According to the algorithm of [8], the dynamic verification scheduler must now somehow force this alternative match – say by firing the `Isend` (line 9) in real-time order before firing `Isend` (line 6). However, we know from MPI’s semantics that the MPI runtime environments *do not guarantee that this alternative matching will occur*. We call these scenarios (*potentially*) *elusive matches*. Tricks such as inserting ‘padding’ delays that can perturb schedules may make elusive matches more likely, but still provide no guarantees. Therefore, we need an algorithm different from DPOR, and POE is our answer.

POE solves the problem of elusive matches *without requiring changes to the MPI library* and *without adding padding delays*. It *dynamically rewrites* wildcard receives into specific receives, one for each actual sender that it computes to be a *certain* match. In the context of the example in Figure 2, if we can force two recursive explorations, with `MPI_Irecv(buffer, from 1, &req);` and `MPI_Irecv(buffer, from 2, &req);` used successively in lieu of the existing line 2, we would have force-matched both the sends. The crucial fact is, of course, to *never* force-match with a send that is not going to be issued – this can cause a deadlock that does not exist. POE employs a strategy to discover all potential senders precisely, as outlined in Section 1.2, and Section 2.

## 1.2 Handling Out-of-order Completion

In MPI, (i) two `Isend`s targeting two different processes may finish out of order (with respect to issue order), while two `Isend`s targeting the same process must match in order. Likewise, (ii) two non-wildcard receives sourcing from the same source process must also match sends in order. Similarly, (iii) if the first receive or both receives are wildcards, even then they must match in issue order. As for waits and tests, (iv) they must not complete before their corresponding send/receive operations. Finally, (v) operations appearing *after* MPI barriers and MPI waits must not finish before the barrier or wait. *Notice that we did not say that operations before a barrier must finish before the barrier!* Section 2 will show that operations issued before a barrier can linger even after crossing the barrier.

## 1.3 Discovering Match-Sets

POE employs an approach to bound the scope of search for locating potential matching sends for a wildcard receive. It relies on a formal notion of *fences* to determine when two operations issued by a dynamic verification scheduler through the PMPI layer will be carried out (i) by the MPI runtime, (ii) in that order. We are not saying that MPI has “fence instructions” akin to how CPUs have assembly instructions to order intra-core execution. However, there are still conceptually equivalent ordering points defined by the MPI semantics! Based on

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<sup>5</sup> In this paper, we suppress details pertaining to communicators and tags.

a formulation of MPI fences, we can form *match-sets* – sets of MPI operations that can be issued out of order by a dynamic verification scheduler. This is the idea of POE’s *lookahead computation* alluded to earlier.

## 2 Basic POE Algorithm

Consider Figure 3. Note that although the `Isend` on line 8 is issued *after* the barrier on line 7, it is a potential match for the `Irecv(*)` on line 2. This is precisely because MPI’s `Isend` can linger across a `Barrier`. The only ordering that MPI guarantees is that functions *after* a barrier will not be called until all functions before (and including) the barrier have been called on any process (rank). The following steps describe how the dynamic verification scheduler implementing the POE algorithm handles this example. Our POE scheduler will intercept every MPI operation `MPI_f` issued from every MPI process. It will often not issue these operations (through `PMPI_f`) immediately – but only make a note of it, and *later* issue them. We employ a central scheduler process which helps issue MPI operations in a serialized manner, and currently replays executions by re-execution from `MPI_Init`.<sup>6</sup>

### Illustration of POE on the example of Figure 3

- Collect `Irecv` (line 2), and do not issue.
- Collect `Barrier` (line 3), and do not issue.
- Since `Barrier` is a fence, do not collect anything more from rank 0; switch to rank 1.
- Collect `Barrier` (line 7), and do not issue; switch to rank 2.
- Collect `Isend` (line 11), and do not issue. Then collect `Barrier` (line 12), and do not issue.
- A fence has been reached in every rank. Now, form a *match set* in priority order, with the following priority order followed: barriers first, then non wildcard send/receives, and finally wildcard send/receives.
- In our current state, there is indeed a highest-priority match set formed by the barriers. *Now, POE sends these Barriers* into the MPI runtime through `PMPI_Barrier` calls.
- The next ordering points (fences) are attained at `Wait`.
- No match-sets of non wildcard receives exist. Skip this priority order.
- At this point, we know the full list of senders that can match the wildcard receive.
- Dynamically rewrite `Irecv(*)` into `Irecv(1)` and `Irecv(2)`, in two different executions.
- Form the first match set of `Irecv(1)` and `Isend()` of line 8. Pursue this interleaving.
- Form the second match set of `Irecv(2)` and `Isend()` of line 11. Pursue this interleaving through re-execution of the MPI program.

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<sup>6</sup> A distributed strategy allowing concurrent issues is slated for development; also a more efficient re-execution method is reported in [9].

Note that for MPI programs with no wildcards, POE will examine the entire program under exactly one interleaving.

## 2.1 Semi-Formal Description of POE

```

1: if (rank == 0)
2: { MPI_Irecv (&buf0, *, &req);
3:   MPI_Barrier ();
4:   MPI_Wait (&req);
5:   MPI_Recv (&buf1, from 2); }
6: else if (rank == 1)
7: { MPI_Barrier ();
8:   MPI_Isend(buf1, to 0, &req);
9:   MPI_Wait (&req); }
10: else if (rank == 2)
11: { MPI_Isend(buf0, to 0, &req);
12:  MPI_Barrier ();
13:  MPI_Wait (&req); }

```

**Fig. 3.** *Ordering Semantics and Operation Lifetimes*

For simplicity, we only deal with the following MPI operations in this section: `MPI_Barrier`, `MPI_Isend`, `MPI_Wait`, `MPI_Irecv`. We also assume that the operations have the same tag and that the communicator is `MPI_COMM_WORLD` for simplicity.

Since MPI semantics allow for nonblocking operations to linger across barriers, POE needs to emulate this out-of-order completion behavior of the MPI runtime. In addition, POE must also respect MPI's send and receive ordering guarantees. Therefore, rather than emulating the issue order of MPI operations, POE must emulate the *completion order* of MPI operations. Before going into more detail, we first define what we call *fence MPI operations*.

**MPI Fence Operations:** A *fence* is an MPI operation that must be completed before any following MPI operations from the same process can be issued. Any blocking MPI operation is a fence, as are `MPI_Barrier`, `MPI_Wait`, and `MPI_Recv`.

POE executes all C statements in program order; however, it issues MPI operations to the MPI runtime only when they are guaranteed to complete immediately. For example, an MPI receive (send) is issued only if a matching send (receive) is found. This is the idea of POE forming *match-sets* as introduced in Section 1.3. In order to correctly emulate the out-of-order completion inherent within the MPI semantics (Section 1.2 presents it through examples; our web page [13] has details), POE builds a graph data structure of *completes-before* edges across MPI operations within the same process. We call these edges as *intra completes-before* (IntraCB) edges. For an MPI process  $P_i$  with two MPI operations  $i, j$  and  $i < j$ : an intra completes-before edge exists from  $i$  to  $j$  iff one of the following holds:

The POE algorithm works by finding *match-sets* of MPI operations and issuing them (possibly out-of-order) to the MPI runtime (using the PMPI versions of these operations). An MPI operation can essentially be in one of the two states: *issued* and *completed*. When an MPI operation is *issued*, it means that the MPI runtime is aware of the MPI operation. When an MPI operation is *completed*, it means that the operation has no presence in the MPI runtime. For example, when we say that an MPI receive operation is complete, we mean that a matching send has been found for that receive.

- $i$  is a fence MPI operation.
- $i$  and  $j$  are MPI send operations to the same destination.
- $i$  and  $j$  are MPI receive operations from the same source.
- If  $i$  is a wildcard receive and  $j$  is an MPI receive operation (either wildcard or non-wildcard).

In addition to IntraCB, POE also maintains a *conditional completes before* (CCB) edge which is added as follows. The purpose of this edge is to model how wildcard receives may *trump* non wildcard receives. For example, suppose an MPI process P0 has the code sequence `Recv(from 1); Recv(from *)`; and MPI process P2 has code sequence `Send(to 0);`. Then this `Send` matches `Recv(from *)` because the first offered match “from 1” requires a send from P1 which is not present. In this case, a CCB edge is not introduced between the receives in P0. However, now if we consider the same P0 process, but a P1 process which is `Send(to 0);`, then this `Send` matches `Recv(from 1);`. In this case, a CCB edge is introduced between the receives in P0.

If there is an IntraCB or CCB edge from  $i$  to  $j$ , then we call  $i$  as the *ancestor* of  $j$ . The POE algorithm described on Page 5 guarantees that no PMPI operation will be issued contrary to the IntraCB or CCB edges, thus guaranteeing the correctness of message matches within the MPI runtime.

It must be observed that the code snippet in Figure 1 can be verified with DPOR if the technique of dynamic rewriting of the wildcard receives is employed. However, the code snippet in Figure 3 cannot be verified with DPOR even with dynamic rewriting of wildcard receives employed. Due to the presence of the barrier, the `MPI_Isend` at line 8 can never be executed *before* the `MPI_Isend` at line 11, whereas in DPOR, we will need dependent actions to be replayable in both orders. In any interleaving of this example, however the send at line 11 is always issued before the send at line 8. The POE algorithm overcomes this problem by executing the big-step move of `MPI_Barrier` of the three processes, and then forming match-sets of the wildcard receive with `MPI_Isends` by recursively employing dynamic rewriting for both the match-sets each in a different interleaving.

## 2.2 Implementing WAIT\_ANY and TEST\_ANY

ISP implements the POE algorithm that allows for executing MPI operations in an order different from the actual program order. Hence, when ISP traps an MPI request such as `MPI_Irecv(buffer, count, datatype, source, mpi_request)`, ISP stores the arguments for later issuance. Let  $op$  be an MPI operation.

When  $op$  is one of `MPI_Wait`, `MPI_Waitall`, `MPI_Test`, or `MPI_Testall`, the out-of-order issuance does not cause any problems since the POE algorithm’s IntraCB edges ensure that all ancestors, *i.e.*, the `MPI_Isends` and `MPI_Irecvs` corresponding to the requests are issued before  $op$  itself is actually issued. When  $op$  is one of `MPI_Testany` or `MPI_Waitany`, all `MPI_Irecv` and `MPI_Isend` ancestors of  $op$  are not necessarily issued before  $op$  itself is issued. Hence, when ISP invokes  $op$ , an error is thrown by the MPI runtime that the request structure is

invalid (since the MPI runtime is not aware of the as yet unissued `MPI_Isend` or `MPI_Irecv` requests). In order to circumvent this problem, ISP issues `op` with `MPI_REQUEST_NULL` for those send and receive requests that are not yet issued and hence are ignored by the MPI runtime.

This allows the `MPI_Testany` and `MPI_Waitany` to work with POE's out of order issue when the MPI runtime does not know *all* the requests it is supposed know as it would during an in-order execution.

### 3 Experimental Results

We have experimented with all 69 Umpire [2] test cases, and in all 30 tests that have deadlocks, ISP finds the deadlocks, generating the fewest number of interleavings. We have also run ISP on the Monte-Carlo calculation of  $Pi$ , and the Game of Life example used in the EuroPVM/MPI 2007 Tutorial [12]. In all examples that do not employ wildcard receives, `WAIT_ANY`, or `TEST_ANY`, *ISP examines exactly one interleaving*. Some of these examples were instrumented to detect resource leaks (*e.g.*, `MPI_Isend` or `MPI_Irecv` without an `MPI_Wait`, `MPI_Comm_create` without an `MPI_Comm_free`, etc.). For these examples, a successful verification run using ISP implies a complete absence of these types of issues in the program (more discussions under 'data dependent control' below).

Since ISP works by re-executing the given MPI program, the restart time of the MPI system can become a significant overhead. This price is being paid because as opposed to existing model checkers which maintain state hash-tables, we cannot easily maintain a hash-table of visited states including the state of the MPI program as well as the MPI run-time system. (Note: In resorting to re-execution, we are, in effect, banking on deterministic replay.) One very promising approach to eliminate restart overheads is the following. At `MPI_Finalize`, one can reasonably assume that the MPI run-time state is equivalent to the one just after `MPI_Init`, and therefore simply reset user state variables and transition each process to the label after `MPI_Init`. We are further looking into when it is appropriate to use this technique (see [9] for details).

**Data Independent Control Flow:** In most MPI programs, control flows are unaffected by 'data' variables. For such MPI programs, a successful verification using ISP on a fixed input data set is tantamount to verifying the program for all possible input data. Also, for such programs, one can eliminate data variables, and their associated update functions, since they would not contribute either to control flow decisions or to the truth of the local assertions being checked. A preliminary implementation exists to detect and eliminate such data variables from MPI programs.

A preliminary Microsoft Visual Studio integration of ISP has also been implemented. A problem faced in this implementation was due to the fact that the actual run that occurs under ISP does not ever send wildcard receives into the MPI runtime. Visual Studio issued wildcard receives would not necessarily match with the correct sends, and mask the deadlock ISP found. This problem was solved through a novel technique that (i) obtains trace information from



ISP, and (ii) mimics the dynamic rewriting of wildcard receives while making the Visual Studio debugger step through error traces. With this approach, the user’s view of their program is preserved (more details on our web page [13]).

## 4 Concluding Remarks

We described our dynamic verification approach for MPI C programs that incorporates partial order reduction and dynamic rewriting based scheduling of MPI function call interleavings. ISP guarantees to detect *all* deadlocks and local assertion violations in C MPI programs that fall within ISP’s range of supported commands (the commands and our verification results are documented on our website). MPI programs with additional calls may also be checked using ISP if they do not interfere with the commands currently supported (these commands will directly issue into the MPI runtime, without going through the PMPI mechanism). We detailed how we solved special problems posed by `WAIT_ANY` and `TEST_ANY`, and also how we reconcile a user-interface view with our dynamic rewriting process. We plan to release the full sources of ISP for experimentation, parallelize ISP itself using MPI, and make ISP widely available.

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## References

1. Salman Pervez, Robert Palmer, Ganesh Gopalakrishnan, Robert M. Kirby, Rajeev Thakur, and William Gropp. Practical model checking method for verifying correctness of MPI programs. In *EuroPVM/MPI*, pages 344–353, 2007.
2. Jeffrey S. Vetter and Bronis R. de Supinski. Dynamic Software Testing of MPI Applications with Umpire. *Proc. of SC2000*, pages 70–79, 2000.
3. Bettina Krammer and Michael M. Resch. Correctness checking of MPI one-sided communication using Marmot. *EuroPVM/MPI, LNCS 4192*, pages 105–114, 2006.
4. O. Edelstein et.al, Framework for testing multi-threaded Java programs. *Concurrency and Computation*, 15(3-5):485–499, 2003.
5. R. Vuduc, M. Schulz, D. Quinlan, B. de Supinski, and A. Saebjornsen. Improved distributed memory applications testing by message perturbation. *PADTAD 2006*.
6. E. M. Clarke, O. Grumberg, and D. A. Peled. *Model Checking*. MIT Press, 2000.
7. Patrice Godefroid. Model checking for programming languages using Verisoft. *POPL*, pages 174–186, 1997.
8. Cormac Flanagan and Patrice Godefroid. Dynamic partial-order reduction for model checking software. *POPL*, pages 110–121. ACM, 2005.
9. Sarvani Vakkalanka, Subodh V. Sharma, Ganesh Gopalakrishnan, and Robert M. Kirby. ISP: A tool for model checking MPI programs. *PPoPP 2008*. 285-286.

10. Sarvani Vakkalanka, Ganesh Gopalakrishnan, and Robert M. Kirby. Dynamic Verification With Reductions in Presence of Split Operations, Relaxed Orderings, and Elusive Interleavings CAV 2008 (to appear).
11. Gerard J. Holzmann. *The Spin Model Checker*. Addison-Wesley, 2004.
12. William D. Gropp and Ewing Lusk. *Using MPI-2: A Problem-based Approach*, 2007. Tutorial.
13. [http://www.cs.utah.edu/formal\\_verification/europvm-mpi08](http://www.cs.utah.edu/formal_verification/europvm-mpi08)
14. Michael Oberhuber, "Elimination of Nondeterminacy for Testing and Debugging Parallel Programs," *Automated and Algorithmic Debugging*, 315-316, 1995.