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A Study of Alternative Imputation Techniques for Surveys in the Current Industrial Reports Series

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A STUDY OF ALTERNATIVE IMPUTATION TECHNIQUES FOR SURVEYS IN THE CURRENT INDUSTRIAL REPORTS SERIES

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ABSTRACT

The Current Industrial Reports (CIR) imputation research effort was designed to provide a general assessment of the effectiveness of the existing imputation methodology for surveys in the CIR series, and to identify, evaluate, and compare the potential statistical and practical effects of plausible alternative procedures. This report provides a summary of the principal results of the completed research effort and present specific recommendations for potential improvement in the current imputation methodology for the surveys in the CIR series.

A major conclusion of the CIR imputation research was that the presentlyused screened sums imputation methodology is reasonably effective for many of the CIR surveys, particularly for the monthly surveys. Consequently continuation of that procedure for the monthly surveys has been recommended. Moreover, the use of two distinct ratio adjustments for both the quarterly and annual surveys is suggested.

1. Introduction

For more than a year a staff of researchers in SRD, with support from survey analysts and researchers from Industry Division, has been examining the effectiveness of various establishment-level imputation techniques for surveys in the Current Industrial Reports (CIR) series. The principal procedure that is used to produce imputes for missing establishments in CIR surveys is based on aggregate measures of change for specific survey respondents or on perceived item relationships. However, there was no formal documentation that provided justification for this procedure, referred to as the screened sums or ratio of identicals adjustment, based on either its theoretical properties or on empirical results and evaluations. The recently completed CIR imputation research effort was designed to provide a general assessment of the existing CIR imputation methodology, and to identify, evaluate and compare the potential statistical and practical effects of plausible alternatives.

Five preliminary reports on the CIR imputation research have been issued; they provided a general evaluation of the imputation methodology currently in use and partially examined the merits of other suggested procedures. This report summarizes the principal results of the preliminary reports and offers specific recommendations for potential improvements in the imputation methodology for the CIR surveys.

2. Evaluation of Current Procedures

The examination of the existing CIR imputation techniques covered four general areas -- statistical properties, general utility, procedural complexity and plausibility. To enhance the manageability of the project, which related to all of the more than 100 CIR surveys, the research staff categorized the surveys by product line, unit and average item nonresponse rates, reporting frequency and size. A random selection of surveys was selected from the resultant categories and formed the empirical basis for the research and evaluation of the effects of alternative imputation procedures on survey estimates. The major items of the surveys selected for the imputation research are shown in Table 1.

2.1 Statistical Properties

For the ith establishment and the tth reporting period (month, quarter, or year), let $Y_{it}(k)$ represent the kth survey characteristic for a given CIR survey. The following are the analytical expressions and brief -characterizations of the existing CIR imputation methods.

For Delinquent Respondents or Unit Nonrespondents

Two imputation options are used for most items for unit nonrespondents, which are referred to by the survey methodologists as delinquent respondents.

Method 1 -
$$\hat{Y}_{1it}(k) = Y_{i(t-1)}(k) \begin{bmatrix} \sum_{j \in S} Y_{jt}(k) \\ \sum_{j \in S} Y_{j(t-1)}(k) \end{bmatrix}$$

where S represents the group of responding establishments which passed the screened sums ratio test of the computer editing process for the current reporting period. The ratio within the brackets will be called the screened sums ratio or adjustment factor. The major assumptions of this approach are that the screened sums ratio and therefore the industry's overall period-to-period rates of change are "good" estimates of the trend or change ratios for the establishments in question.

Method 2 -
$$\hat{Y}_{2it}(k) = Y_{i(t-1)}(k) \left[\frac{\sum_{j \in S} Y_{jt}(l)}{\sum_{j \in S} Y_{j(t-1)}(l)} \right]$$

This estimator is analogous to that shown as Method 1, however the distinguishing assumption is that the perceived relationship between the *l*th and *k*th items would permit the effective use of the screened sums ratio for item *l* to estimate the current period value for the *k*th item.

For Item Nonresponse

The four principal estimators designated for item nonresponse are provided below.

Method 3 -
$$\hat{Y}_{3it}(k) = Y_{i(t-1)}(k) \left[\frac{Y_{it}(l)}{Y_{i(t-1)}(l)} \right]$$

Unlike the delinquent respondents, survey establishments which are identified as "partial respondents" may respond to one item, but not to another. For those partial respondents for which there is a response for a "related" or strongly correlated item, Method 3 requires the use of the period-to-period ratio for the related item i.e., $Y_{it}(\ell) / Y_{i(t-1)}(\ell)$, as an estimate of the corresponding rate for the kth item.

Method 4 -
$$\hat{Y}_{4it}(k) = Y_{it}(l) \left[\hat{T}_{t}(k)/\hat{T}_{t}(l)\right],$$

where the estimated total for item * for the current period can be represented by

$$\hat{T}_{t}(*) = T_{t-1}(*) \left[\sum_{j \in S} Y_{it}(*) / \sum_{j \in S} Y_{i(t-1)}(*) \right]$$

Here T_{t-1} (*) is the total that was published for the item for the previous reporting period. This procedure is also designed to take advantage of the relationship believed to exist between items k and l. It is analogous to the more familiar representation of a combined ratio estimator.

Method 5 -
$$\hat{Y}_{5it}(k) = Y_{i(t-1)}(k) \left[\sum_{j \in S} Y_{jt}(k) / \sum_{j \in S} Y_{j(t-1)}(k) \right]$$

This estimator is identical in form to that of Method 1; however, a survey respondent that fails to respond to, say item k may respond to item l and therefore has an opportunity to be included in the screened sums ratio for item k.

Method 6 -
$$\hat{Y}_{6it}(k) = Y_{i(t-1)}(k) \left[\frac{Y_{it}(k)}{Y_{i(t-1)}(k)} \right] \left[\frac{\sum_{j \in S} Y_{jt}(k)}{\sum_{j \in S} Y_{j(t-1)}(k)} / \frac{\sum_{j \in S} Y_{jt}(k)}{\sum_{j \in S} Y_{j(t-1)}(k)} \right]$$

For this estimator the adjustment to $Y_{i(t-1)}$ takes the form of a double ratio, it is the product of the current-to-previous period ratio for item l and an estimate of the ratio of the current-to-previous period change ratios for items k and l.

In view of the similarities between the six estimators given above, our look at the primary statistical properties of the current imputation methods was restricted to the most frequently used technique, Method 1 (Method 5 for partial respondents).

• The linear model that best describes the screened sums estimator for establishment-level nonresponse is:

$$Y_{it} = \beta_1 Y_{i(t-1)} + \epsilon_{it}; \epsilon_{it} (0, Y_{i(t-1)})$$
 (2.1.1)

The regression coefficient is given by β_1 and ϵ_{it} denotes the associated error term. Equation (2.1.1) leads to the transformed model

$$Y_{it} / Y_{i(t-1)}^{1/2} = \beta_1 Y_{i(t-1)}^{1/2} + \epsilon_{it} / Y_{i(t-1)}^{1/2}; Y_{i(t-1)} \neq 0$$

and

$$\epsilon_{it} / \Upsilon_{i(t-1)}^{1/2} \sim (0, \sigma^2)$$

Assume a sample of size n from a population of size N for which there are r respondents and n-r nonrespondents to a survey item. Then the estimate corresponding to the least squares estimate of Y_{it} under the model given in (2.1.1) is

$$Y_{it} = b_1 Y_{i(t-1)}$$

where $b_1 = \frac{\sum_{j \in P} Y_{jt}}{\sum_{j \in P} Y_{j(t-1)}}$ and P represents the set of survey respondents for a

given item. This is essentially the screened sums estimator.

Let's consider the bias of $\hat{Y}_{1it}(k)$. Given knowledge of the previous period estimate or value for a given item, the bias of $\hat{Y}_{1it}(k)$ can be expressed as

$$\hat{B(Y_{1it}(k))} = Y_{i(t-1)}(k) E(\hat{R}(k)) - Y_{it}(k),$$

where R(k) is the screened sums ratio for the kth item. Now if we let R'(k) represent the value of the screened sums ratio if the imputes in the denominator (from the previous reporting period) are replaced by their true values, and let $R_i(k)$ denote the "true" change ratio for establishment i, $B(\hat{Y}_{1it}(k))$ can then be further decomposed as follows.

$$B(\hat{Y}_{1it}(k)) = Y_{i(t-1)}(k) \left[E \hat{R}(k) - R_{i}(k) \right]$$

= $Y_{i(t-1)}(k) \left\{ E \left[\hat{R}(k) - R'(k) \right] \right\}$
+ $\left[E (R'(k)) - R_{i}(k) \right] \right\}$ (2.1.2)

Therefore \hat{Y}_{1it} is generally a biased estimator and the magnitude of the bias depends on how well the basic assumptions of the imputation approach are met. As shown in (2.1.2), the first component of the bias is a function of the mean of the difference between the "true" screened sums ratio for a given response pattern, and the corresponding survey estimate of this ratio, which may include a number of imputes. The second component is a multiple of the difference between the mean (over all possible response patterns) of the true screened sums ratio and the true change ratio for establishment i. From this we concluded that a small imputation rate (the percentage of the item total ascribed to imputed data) for the previous reporting period or for those establishments included in the screened sums ratio, coupled with limited variability among the establishments, would ensure that the bias of the current imputation procedure is small.

The samples for most of the CIR surveys are intended to include the entire target population. Therefore our discussion of variability in survey estimates will relate to those surveys. For such surveys we have essentially no sampling variation; however, we have what can be referred to as "imputation variance" relating to the possibility of different response/nonresponse patterns for the surveys and the mechanism that determines what establishments are included in the screened sums ratio. In order to develop some sense of the nature of the imputation variance of CIR estimates, we present below an expression based on assumptions consistent with those used in determining sampling variability under simple random sampling. The current CIR estimators for an item total for a given establishment can be shown to conform to the expressions for either a ratio or a double ratio estimator of a mean. Under the assumption that the nonresponding CIR establishments are missing at random,

$$\operatorname{Var}\left[\hat{\mathbf{x}}_{1:t}^{(k)}\right] \doteq \frac{(N-r)}{Nr} \left[Y_{1:(t-1)}^{(k)} \hat{\mathbf{R}}_{(k)}\right]^{2} \left[\frac{S_{tk}^{2}}{\tilde{Y}_{tk}^{2}} + \frac{S_{(t-1)k}^{2}}{\tilde{Y}_{(t-1)k}^{2}} - \frac{2 R_{12}S_{tk}S_{(t-1)k}}{\tilde{Y}_{tk}\tilde{Y}_{(t-1)k}}\right]$$

$$(2.1.3)$$

where N and r are the size of the target population and the number of survey respondents; \tilde{Y}_{tk} and $\tilde{Y}_{(t-1)k}$ are the current and previous reporting period screened sums totals for the kth item (or the two items involved in an interitem ratio); S_{tk} and $S_{(t-1)k}$ are the corresponding standard deviations; and R_{12} is the correlation coefficient for the two variables. Therefore under the implicit general assumptions of the current CIR imputation procedures, (2.1.3) suggests that the variability of the survey estimates could be quite dependent on the quality and behavior of the screened sums adjustment.

2.2 General Utility

The concept of general utility for imputation techniques stemming from the imputation research went beyond considering the application of the techniques to different survey items and survey diversity; it also included the sensitivity of the procedures to changes in general survey conditions over

time. For example, if there is a major change in the distribution of a survey characteristic among the survey respondents or a change in the overall level of imputation, how does this affect the effectiveness of the designated methods of imputation?

As can be noted from Table 2.1-2.3 and Figures 1.1-2.4 of Appendix B, imputation rates for a survey item can be quite different for different years and for different reporting periods within a given year. Moreover, different items of a specific survey behave quite differently relative to imputation rates, and as will be observed in section 3, there is considerable variation in the statistical models to which the various items are fitted. Therefore the empirical results from the 12 surveys included in the imputation study suggest that the optimal fit of survey data could require the use of several different imputation techniques to account for different items and changes in the items over time. Specifically, the utility of the screened sums imputation approach was limited in some cases, particularly for some of the quarterly surveys. More appropriate procedures have been recommended for those situations. However in general, for the selected items, the differences between item totals based on the models which achieved the best fits and the models that are recommended were insignificant. We again note that this conclusion is based on no more than four items for each of the 12 surveys studied, which were examined for a period of three to five years. Nevertheless we believe the results adequately reflect the potential for the suggested imputation procedures for other items. surveys and reporting periods.

2.3 Plausibility

The effectiveness of the current CIR procedures is largely dependent on the application of aggregate level inter-item relationships and items' rates

of change to the establishment level. Moreover important assumptions that undergird the procedures can be violated by various patterns of nonresponse and the consequential imputes.

If within reporting periods the variability of the establishment's contribution to specific item totals is small, the contributions of the responding establishments to estimates of period-to-period change will be similar. Under that assumption the screened sums ratio adjustment should be reasonably accurate.

We observed between establishment variation in the survey estimates for all three types of reporting periods, and often found that the variability was considerable. Table 2.4 provides examples of this result. It gives the 1984 coefficients of variation (CV's) between the establishments for a selected set of items from monthly surveys. For a given item the CV is defined as the ratio of the square root of the variance between the establishments to the mean estimate over the establishments. Note that all of the CV's are quite large; they range from a low of 0.932 in March for item 11112 of the Iron and Steel Castings Survey, to a high of 6.907 in September for item 1202 of the Finished Fabrics Survey. Therefore an initial concern regarding the plausibility of the current imputation procedures, was that the size of the observed between establishment variability in the estimates for the five selected surveys could easily occasion unacceptable biases in the survey estimates.

Finally recall that the currently-used approaches to CIR imputation assumes considerable similarity of the distribution of survey items among the responding and nonresponding items. Our preliminary review of 1982-84 data from the Flour Milling Survey (2001) indicated that the imputes for the nonrespondents in the survey tended to be smaller than the corresponding

reported data for the other establishments. However, this pattern did not persist over the other surveys that were examined, nor were we able to identify other characteristics that drew a distinction between survey respondents and nonrespondents for these surveys.

Thus, relative to the appropriateness of assuming similar characteristics for responding and nonresponding establishments, our results suggested that this assumption was not a major drawback of the screened sums approach or to the development of other imputation models.

2.4 Procedural Complexity

Based on the description of the existing CIR imputation methodology and our perception of its implications, we considered it a relatively simplistic approach, irrespective of its many facets. In general we found little reason to be concerned about the level of the complexity of the techniques; however, we were apprehensive about the capability of the imputation process to develop a sufficiently detailed history of the data that could facilitate the monitoring and evaluation of the adjustment procedures. In addition we thought that the procedure was deficient in its ability to utilize late reported data. Although such data may not have been included in current period estimates, it is desirable to have imputation methods that will include these data on computer files and ensure that they are available for use in imputation during the next reporting period.

The evaluation results that have been discussed are obviously less than definitive. In addition to their conformity to an intuitive sense about the data, there is some statistical justification for the currently-used CIR imputation procedures. The relevant concern is still the effect of deviation from the basic assumptions of the underlying models. The other empirical

results of the evaluation of the current imputation techniques will be presented in the next section with those of alternative approaches.

3. Detailed Results and Recommendations

To supplement our efforts to evaluate the current CIR imputation methodology and to identify acceptable alternatives, we attempted to fit data from the 12 selected surveys to known statistical models and proceeded with the adaptation of these models or the development of others based on the initial results. We produced and reviewed extensive summary statistics and 'graphical representations based on data from the 1979-84 CIR historical data files of the selected surveys. This section will identify the "reasonable" alternatives that resulted from this process and present specific recommendations for the CIR imputation process, based on the complete set of results from the imputation study.

3.1 Model Selection

Efforts were made to ensure that the recommended CIR imputation procedures have desirable statistical properties and rather general applicability. In addition, we believed that the level of complexity associated with the implementation of the procedures should also be included among the principal criteria that are used to evaluate various techniques. With this in mind we sought desirable imputation alternatives that would (1) take advantage of perceived functional relationships between reporting periods; and (2) assume an ignorable response mechanism, i.e. the nonrespondents would be considered missing at random.

In determining the more plausible imputation options, regression analysis techniques were used to identify the strength of the functional relationships and to assess the quality of the fits of the corresponding models. Prescribed regression procedures were performed for a set of proposed models, and the

following are the models associated with what was considered the more desirable imputation procedures among those considered.

Model Alternatives for Monthly Surveys Model MS 1: $Y_{it} = \beta_1 Y_{i(t-1)} + \epsilon_{it}$, $\epsilon_{it} - (0, \sigma^2)$ Model MS 2: $Y_{it} = \beta_1 Y_{i(t-1)} + \epsilon_{it}$, $\epsilon_{it} - (0, Y_{i(t-1)}\sigma^2)$

Model Alternatives for Quarterly Surveys

Model QS 1: $Y_{it} = \beta_1 Y_{i(t-1)} + \varepsilon_{it}$; $\varepsilon_{it} - (0, \sigma^2)$ Model QS 2: $Y_{it} = \beta_4 Y_{i(t-4)} + \varepsilon_{it}$, $\varepsilon_{it} - (0, \sigma^2)$ Model QS 3: $Y_{it} = \beta_1 Y_{i(t-1)} + \beta_4 Y_{i(t-4)} + \varepsilon_{it}$, $\varepsilon_{it} - (0, \sigma^2)$ Model QS 4: $Y_{it} = \beta_1 Y_{i(t-1)} + \varepsilon_{it}$, $\varepsilon_{it} - (0, Y_{i(t-1)}\sigma^2)$ Model QS 5: $Y_{it} = \beta_4 Y_{i(t-4)} + \varepsilon_{it}$, $\varepsilon_{it} - (0, Y_{i(t-4)}\sigma^2)$

Model Alternatives for Annual Surveys

Model AS 1:
$$Y_{it} = \beta_1 Y_{i(t-1)} + \epsilon_{it}; \epsilon_{it} - (0, \sigma^2)$$

Model AS 2: $Y_{it} = \beta_1 Y_{i(t-1)} + \epsilon_{it}; \epsilon_{it} - (0, Y_{i(t-1)}\sigma^2)$
Model AS 3: $Y_{it} = \beta_1 Y_{i(t-1)} + \beta_2 Y_{i(t-2)} + \epsilon_{it}$
 $\epsilon_{it} - (0, \sigma^2)^{-1}$

The definitions of the notation given earlier in the section also apply for the above expressions.

In addition to those considerations relating to statistical properties and general application, the major factors that led to the selection of the alternatives included the following:

- The basic results of the analysis of variance associated with the models;
- The relative sizes of the comparable coefficients of determination (R²);
- The precision with which the parameters of the models could be estimated.

Models were considered acceptable if (1) the significance level relating to

the regression was 0.05 or better; (2) the R²'s (R² = 1 - $\frac{\sum (Y_{it} - \hat{Y}_{it})^2}{\sum (Y_{it} - \bar{Y})^2}$)

were at least 0.85; (3) the principal scatter and residual plots did not provide indications of "serious" violations of the model assumptions; and (4) the coefficients of variation of the estimates of the model parameters were less than 30 percent.

3.2 Discussion of Summary Results

Tables 4.1-4.11 provide 1983-84 summary statistics for the major items of the 12 surveys considered for the study and estimates of the model parameters. We should note that for the transformed models, which assumed that the variance of the error term was directly proportional to the regressor or "independent" variable, the R²'s were not completely comparable to those of other models, and the model estimates and other summary statistics must be appropriately adjusted to describe the results relating to the original models.

Summary results relating to the monthly surveys are given in Tables 4.1-4.5. We can observe indications of a number of reasonably good "fits" of the data from these results. Again the results were examined in conjunction with the review of the corresponding plots, some of which are provided in Appendix B. For models MS 1 and MS 2 we detected considerable variation in the corresponding statistics for 1983 and 1984 and for different months in the same year. This variability was very noticeable for MS 2, which we have

identified as the model that most closely resembles the principal imputation procedures used for the establishment-level imputation. The value of R^2 for the model was as low as 0.002 in June, 1984 for item 1201 of the Finished Fabrics Survey, however the corresponding value for 1983 was 0.950. In general the parameter estimates and coefficients of determination for the two models were reasonably close, which increased the importance of the data plots and other criteria used in determining the recommended procedures.

Summary results for the quarterly surveys are included in Tables 4.6 and 4.7. The data entries have been arbitrarily restricted to 1984 to help keep the number of tables included in the report to a manageable size. However the principal results are essentially applicable to data for 1980 and 1982-84.

Like the monthly surveys, one model was not appropriate for all of the quarterly surveys. However some of the models, for example QS 5, provided good fits of the data more frequently than did other models.

Notice that for Survey 2220, the simple linear models (Model QS 2) with the zero intercept and the value of the survey item one year earlier as the regressor variable performed well in 1984. Based on the summary statistics and the corresponding plots, the model would be the preferable alternative for three of the four selected items for the survey. The existing imputation procedure, represented by Model QS 4, appeared to be the most appropriate choice only for item 13041. Model QS 5 which surfaced as the more dominant model for the Sheets, Pillowcases, and Towels Survey, is closely related to Model QS 4. However the model requires the value of the response variable for the previous year to be the regressor variable, rather than the corresponding value for the preceding quarter. The other model that seemed promising for the survey was Model QS 3, which is a weighted combination of QS 1 and QS 2.

We can observe the selected summary statistics for the annual surveys in Tables 4.8-4.11. These statistics and their attending plots tend to suggest the continuation of the screened sums imputation approach for the annual surveys, which is represented by Model AS 2. It was identified as the preferred alternative (over four years) for each of the items for three of the four selected surveys. The simple linear model with the zero intercept, Model AS 1, was preferable for the Industrial Gases Survey (2802). Model AS 3, which used the survey values of the two previous years as auxiliary Variables, was generally less desirable because of the level of precision for estimates of its regression coefficients.

3.2 Other Considerations for Decisions on Imputation Methodology

Although imputation techniques other than those that are currently used for the CIR's may improve the overall quality of the reported data, the improvement may not be statistically significant or the cost of the improvement may be unacceptable.

Rather crude estimates based on the data that were used for the imputation research suggest that the cost of regularly fitting the CIR data to regression models may increase the cost of the imputation process by 10-15 percent, depending on the model that's used. At this point we are not in a position to assess the effect of the increase on the total processing costs.

Tables 5.1a and 5.1b give us indications of how the two imputation alternatives for the monthly surveys compared for March and December of 1984. For most of the survey items the estimated totals for the two estimators were very close. For the two smallest surveys with the larger imputation rates, relative changes of six or seven percent for three of the four items were noted when the simple linear model estimates with the zero intercept is substituted for the screened sums adjustments during

imputation. However, none of the changes were considered statistically significant.

In Tables 5.2a-5.3d summary data from a simulation study involving the quarterly surveys are included. The respondents for surveys 2220 and 2324 were established as quasi-sampling frames from which a set of establishments was randomly selected. Imputes were developed for these establishments based on the five models proposed for the quarterly surveys, and they were combined with the corresponding reported data from the other establishment to form five separate estimates of the item totals for simulated response/nonresponse patterns. Estimates of the bias of the respective estimator were obtained by comparing the five estimates with the reported item totals. We caution that these estimates are based only on those responding establishments for which the data from previous quarters required for the specified models were available. With that limitation in mind we note the estimated relative biases ranged from 0.00 to nearly 50 percent. There did not seem to be any discernible pattern in the data other than that the estimates for the smaller survey (2324) were usually larger than the corresponding estimates within the quarter for survey 2220. There was a great deal of variation in the data over models, items and quarters. This, of course, does not facilitate the task of selecting imputation strategies.

Our coarse analysis of the computing costs for imputation alternatives and some of the empirical results for the monthly and annual surveys seem to favor continued use of the screened sums approach to CIR imputation. However, other results from the annual surveys and those from the quarterly surveys suggest the need to at least consider using other procedures for a limited number of surveys in these groups. Recommendations to that effect will follow.

4. Final Recommendations

4.1 Suggested Imputation Procedures

The various results (both theoretical and empirical) of the CIR imputation research have led us to conclude that the presently-used imputation procedures based on the screened sums adjustment are reasonably effective for many of the CIR survey situations and particularly for those of the monthly and annual surveys. If cost, data processing constraints or some other factors force the planners of surveys in the CIR series to use a uniform "approach to imputation, then we would have to recommend a continuation of the current methodology. But if such constraints are not imposed, we recommend the use of the screened sums model for the monthly surveys and the application of two distinct models for both the quarterly and annual surveys. This recommendation is summarized in the table below.

Recommended Imputation Models for CIR Surveys

Survey Type	Survey Code	Recommended Model					
Monthly	All monthly surveys	MS 2 (current procedure)					
Quarterly	2324 3201 3411 3602 3603 3704	QS 5					
Annual.	All other quarterly surveys 2206 2305 2307 2420 2508 2601 2602 2701 2801 2802 2807 3514	QS 2 AS 1					
	All other annual surveys	AS 2 (current procedure)					

The analytical form of the screened sums estimator has already been given. The estimator associated with Model QS 5 is of the same form but the previous quarter estimate is replaced by the value for the current quarter in the preceding year as the regressor variable. The least squares solution or estimator for Model AS 1 is

$$\hat{Y}_{it} = b_1 Y_{i(t-1)},$$

where $b_1 = \frac{\sum_{j \in P} Y_{jt} Y_{j(t-1)}}{\sum_{j \in P} Y_{i(t-1)}^2}$

and P is the set of responding establishments.

The recommendations are again based on the review of the regression analysis results, including the related plots; computing cost estimates; perceived computing convenience of the alternatives; various simulation results; and other empirical observations relating to the imputation options and the surveys that were considered. If drastic changes have occurred in the survey estimates or response patterns during recent reporting periods or if such changes will occur in the near future, the suggested procedures may not be appropriate. At that point the relevant aspects of the data processing for the surveys should be reevaluated relative to their effects on imputation methodology.

4.2 Other Related Suggestions

The following recommendations represent a reiteration of suggestions that surfaced repeatedly during discussions throughout the conduct of the project.

Initially we raise the question of whether there is an inordinate dependency of the CIR imputation procedures on the data editing operation. For establishments that respond to some of the survey items, but not to all of them (item nonrespondents) the general editing procedure could produce imputes derived from various combinations of several estimators, depending on the results of the reliability testing. Although the editing procedure may produce good edits, it is not clear that the procedure could routinely lead to estimates or imputes that are at least as good as those taken directly from a determined model. We recommend that the extent to which the editing influences imputation be reassessed, and that the relationship be relaxed if it is warranted.

We also reassert the need to make better use of late reported data for imputation and in assessing the properties of proposed data adjustment methodology. These data should be readily accessible and incorporated in the surveys' historical files.

Finally we recommend recurring monitoring of the effectiveness of the imputation process and its effects on survey estimates. Routine tabulation of descriptive statistics for establishment-level measures of change, delinquent and respondent imputation rates and establishments' response status codes should probably be among those data that are reviewed and available for short term research efforts. Moreover, as we have mentioned previously, the behavior of the establishment can change considerably; and if we are able to determine how such changes influence the effectiveness of the imputation procedures during periodic reviews, we would be in a better position to detect and to compensate for unacceptable measurement errors.

5. Concluding Remarks

The constraints imposed by the number of surveys and items involved in the CIR series did not permit a very comprehensive study of alternative imputation procedures. Therefore our findings are, and we would hope, understandably general; we have alluded to some of their limitations.

Nevertheless we believe that we have gained considerable insight into the effectiveness of the current imputation techniques and of other imputation options and how those alternatives compared. We believe that the final recommendations should improve the imputation process, but more narrowly-focused research in this area is certainly warranted.

Detailed research proposals for some of this work will follow subsequently. However as an example of needed research we suggest that modified weighting procedures for the larger surveys can be explored further. In addition we should consider developing procedures that are more appropriate for the small surveys which experience frequent change and have "large" imputation rates. The suggested procedures may work fairly well for many of these surveys, but there are obviously a number of situations where the predicted values are of poor quality in deference to the more general utility of the suggested procedure. As another example, the researchers should work more closely with survey analysts in search of some explanations for some of the phenomena and disparities encountered in the research data, so as to enhance their proposals and sharpen the direction of the research.

We have concluded a phase of an investigation that should be part of a recurring effort and we hope that appropriate research activities will be developed to ensure that the effects of missing data are adequately assessed and considered in the estimation process.

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Appendix A - Summary Data Tables

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Table 1a. Principal Items for Selected Monthly Surveys

Survey Code	Item	Description						
2001	2120	Flour Milling: Wheat - Flour Manufactured						
	2130	Flour Milling: Wheat - Millfeed Produced						
2202	1201	Cotton Whites						
	1202	Cotton Plain Dyes						
2806	2001	Architectural Coatings - Quantity of Shipments						
	2002	Architectural Coatings - Value of Shipments						
3207	11101	Narrow Neck-Food, Net Packed Weight						
•	11903	Narrow Neck Beverage Refillable Production						
3301	11111	Gray Iron Castings Molds - Shipments for Sale						
•	11112	Shipment for Own Use						

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Table 1b. Principal Items for Selected Quarterly Surveys

Survey Code	Item	Description
2220	1 301 1	Consumption of 100% Carded Cotton Yarns
	13021	Consumption of 100% Carded Cotton Yarns
	13031	Consumption of 100% Filament Rayon Acetate, and Triacetate Yarns
	13041	Consumption of 100% Filament Polyester Yarns
• 2324	13011 13012 13013	Sheets, Total - Production Sheets, Total - Quantity Sheets, Total - Value
	13111	Flat Sheets - Production
3603	1 01 01	Uncorrected Power Factor Type: Rapid Start - Quantity of Shipments
	10102	Uncorrected Power Factor Type: Rapid Start - Value of Shipments
	10103	Uncorrected Power Factor Type: Rapid Start - Produced and Consumed in Plant
	10104	Uncorrected Power Factor Type: Switch Start - Quantity of Shipments

Table 1c. Principal Items for Selected Annual Surveys

Survey Code	Item	Description
2304	31200 31210 33200 33210	All Leather - Total Quantity Shipped All Leather - Total Net Value of Shipments All Fabric - Total Quantity Shipped All Fabric - Total Net Value of Shipments
2802	441 41	Oxygen Produced for Pipeline Shipment - Quantity Produced
	44142	Oxygen Produced for Pipeline Shipment - Quantity of Shipments
	44143	Oxygen Produced for Pipeline Shipment - Value of Shipments
•	44251	Oxygen Produced for Bulk Shipment to Pipelines or to Other Air Separation Plants - Quantity Produced
3002	1 31 21	Rubber Hose, Mandrel Made and All Hydraulic - Textile HydraulicProduction
	16631	Types of Construction Not Elsewhere Classified - Production
	16632	Types of Construction Not Elsewhere Classified - Total Shipments (Quantity)
	16633	Types of Construction Not Elsewhere Classified - Total Shipments (Value)
3611	31 291	Special Purpose Switches (Excluding Dimmers), Automotive Types - Quantity
	31 292	Special Purpose Switches (Excluding Dimmers), Automotive Types - Value
	41122	Pole and Transmission Line Construction Materials - Value of Shipments
	42291	Electric Metallic Tubing - Quantity

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Table 2.1a Monthly Imputation Rates (\$) for Selected Monthly CIR Survey Items - 1982

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Survey and Item Codes	Jan	Feb	Mar	<u>Apr</u>	May	Jun	<u>Ju1</u>	Aug	<u>Sep</u>	Oct	Nov	Dec	<u>N</u>
Flour Milling (2001)							-						
2120	4.786	5.184	4.873	9.294	5.423	6.492	5.729	5.877	6.433	6.474	6.204	7.377	182
21 30	8.059	4,920	5.202	9.344	5.161	6.335	6.522	6.284	6.326	6.299	6.083	6.534	183
Finished Fabrics (2202)													
1201	15.258	25.198	25.478	15.839	32.352	3.023	16.442	17.255	9.325	9.112	12.449	11.620	80
1202	30.887	30.898	32.643	31.185	1.286	27.108	27.783	30.062	27.389	27.397	30.241	30.642	103
Paint, Varnish, Lacquer (2806)													
2001	6.686	0.830	5.367	21.210	2.178	11.241	2.138	36.460	36.630	38.163	42.196	48.023	174
2002	99.973	80.321	40.827	32.279	33.614	14.555	12.126	41.850	41.801	42.705	47.939	53.823	174
Glass Containers (3207)													
11101	24.759	24.908	25.075	24.948	26.954	26.959	26.937	28.747	42.210	28.621	29.318	40.949	23
11903	0.000	0.000	0.000	0.000	26.338	0.000	0.000	0.000	2.475	0.000	0.000	5.349	16
Iron and Steel Castings (3301)													
11111	4.251	4.250	4.324	4.343	4.318	4.351	4.310	3.085	3.450	3.586	4.401	3.729	25
11112	71.190	47.261	40.969	24.893	21.695	22.375	21.134	34.921	31.816	36.754	42.673	65.578	20

N - Number of establishments from which survey data were expected.

Table 2.1b Monthly Imputation Rates (\$) for Selected Monthly CIR Survey Items - 1983

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Survey and Item Codes	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	_Oct	Nov	Dec	<u>N</u>
Flour Milling (2001)													
21 20	3.869	15.831	7.211	14.789	6.684	8.540	10.625	9.498	5.884	6.458	5.045	7.620	193
2130	3.249	15.915	6.970	15.313	6.445	8.475	10.212	9.256	5.262	6.095	4.451	7.096	194
Finished Fabrics (2202)													
1201	14.829	15.458	17.578	18.851	17.829	18.344	13.733	15.038	17.421	15.671	13.031	18.718	71
1202	25.564	26.383	28.560	27.627	26.191	26.018	26.967	26.335	26.613	28.376	26.148	26.512	89
Paint, Varnish, Lacquer (2806)													
2001	11.646	6.078	38.122	19.328	25.980	9.682	36.732	9.742	10.408	8.475	36.865	36.388	211
2002	42.232	80.153	80.473	20.920	29.677	11.471	34.691	11.008	10.535	9.588	33.230	35.260	210
Glass Containers (3207)													
11101	29.245	29.186	29.390	0.000	19.291	20,101	20.277	19.808	21.396	20.062	22.434	28.965	23
11903	0.893	1.672	4.762	0.000	0.000	10.405	0.000	9.357	5.556	3.879	16.387	18.421	17
Iron and Steel Castings (3301)													
11111	3.499	3.580	3.615	3.535	2.818	27.336	23.784	3.450	3.450	3.775	3.477	3.481	21
11112	19.081	46.268	39.792	38.622	21.746	38.054	27.823	42.943	42.793	43.060	27.328	45.112	17

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Table 2.1c Monthly Imputation Rates (\$) for Selected Monthly CIR Survey Items - 1984

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Survey and Item Codes	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec	<u> N </u>
Flour Milling (2001)													
21 20	6.153	6.507	5.286	5.218	7.643	8.858	6.665	7.016	6.338	6.605	5.630	12.531	202
2130	5.673	5.946	5.243	4.746	7.647	8.998	7.161	6.759	5.981	6.207	5.766	12.322	203
Finished Fabrics (2202)													
1201	17.260	14.639	14.201	15.097	14.143	7.365	12.544	13.000	7.442	17.627	16.181	22.708	73
1202	23.401	34.612	25.620	25.089	24.930	23.467	18.618	18.189	4.623	27.966	30.409	27.353	96
Paint, Varnish, Lacquer (2806)													
2001	19.196	19.725	20,157	21.012	20.058	19.871	21.994	21.798	24.499	22.083	21.499	39.902	76
2002	21.035	19.918	20.950	21.976	20.864	20.793	23.392	25.275	23.977	23.835	22.921	37.809	75
Glass Containers (3207)													
11101	20.977	20.853	21.812	22.684	38.302	37.709	42.443	33.477	32.717	23.431	29.127	30.724	26
11903	0.000	0.000	0.000	0.000	42.000	1.800	58.187	3.042	1.980	0.000	0.000	0.000	13
Iron and Steel Castings (3301)													
11111	3. 259	3.254	1.854	3.368	3.372	3.421	3.233	3.233	3.324	3.573	3.689	7.620	24
11112	29.546	26.558	10.985	26.865	29.602	30.459	38.502	43.117	29.687	41.236	32.178	39.875	14

Table 2.2a Quarterly Imputation Rates (\$) for Selected Quarterly CIR Survey Items - 1982

Survey and Item Codes	Quarter 1	Quarter 2	Quarter 3	Quarter 4	<u>N</u>
Broadwoven Fabrics (2220)					
1 301 1	15.639	9.585	11.423	10.070	176
13021	13.241	12.815	15.537	14.389	54
1 3031	35.043	37.822	38.157	40.988	76
13041	10.904	43.763	44.542	45.333	118

Sheets, Pillowcases, and Towels (2324)

1 3 011	*	×	*	¥	¥
13012	*	*	¥	¥	¥
1 301 3	¥	*	¥	*	¥
13111	¥	*	*	×	¥

Fluorescent Lamp Ballasts (3603)

10101	0.000	0.000	0.945	0.000	10
10102	0.000	0.000	0.845	0.000	10
10201	0.000	0.000	0.124	0.000	9
10202	0.000	0.000	0.127	0.000	9

*-Data required to compute imputation rate were inaccessible.

2.2b Quarterly Imputation Rates (\$) for Selected Quarterly CIR Survey Items - 1983

Survey and Item Codes	Quarter 1	Quarter 2	Quarter 3	Quarter 4	<u>N</u>
Broadwoven Fabrics (2220)					
13011	7.583	3.939	9.422	13.926	162
13021	13.555	4.039	14.480	15.902	47
1 3031	17.502	7.917	18.348	32.215	68
13041	21.096	31.013	40.247	47.113	113
Sheets, Pillowcases, and Towels (2324)					
13011	5.223	23.196	22.293	1.235	12
13012	5.691	23.699	24.516	1.361	12
1 301 3	7.614	24.118	24.110	39.463	12
13111	0.000	0.221	19.156	39.411	13

Fluorescent Lamp Ballasts (3603)

10101	0.000	0.000	0.000	0.000	8
10102	0.000	0.000	0.000	0.000	8
10201	0.000	0.000	0.000	0.000	7
10202	0.000	0.000	0.000	0.000	7

Table 2.2c Quarterly Imputation Rates (\$) for Selected Quarterly CIR Survey Items - 1984

Survey and Item Codes	Quarter 1	Quarter 2	Quarter 3	Quarter 4	<u>N</u>
Broadwoven Fabrics (2220)					
13011	8.473	7.441	4.515	16.481	170
13021	14.999	14.940	17.720	20.790	54
1 3031	1.955	5.480	22.286	25.260	75
13041	7.512	6.618	16.158	19.926	123

Sheets, Pillowcases,

and Towels (2324)

1 301 1	2.380	2.752	33.607	52.459	11
1-3012	2.778	3.030	29.007	32.432	11
1 301 3	4.551	4.360	34.390	34.991	11
13111	1.865	1.836	7.328	23.986	20

Fluorescent Lamp Ballasts (3603)

10101	0.000	0.000	0.011	0.008	8
10102	0.000	0.000	0.954	0.038	8
10201	0.000	0.000	0.054	0.059	7
10202	0.000	0.000	0.134	0.141	4

Table 2.3 Imputation Rates (\$) for Selected Annual CIR Surveys--1982-84

Survey and Item Codes	1982	<u>N</u>	1983	<u>N</u>	1984	<u>N</u>
Gloves and Mittens (2304)						
31 200	0.004	50	0.006	41	0.003	41
31210	0.436	49	0.007	41	0.270	41
33200	1.617	81	0.373	74	0.669	69
33210	0.000	80	0.235	73	0.586	69
Industrial Gases (2802)						
14 14 1-44 1	0.000	98	0.000	91	0.000	88
44142	0.000	97	0.000	92	0.000	87
44143	0.000	96	0.000	91	0.089	84
44251	0.000	51	0.000	52	0.000	60
Rubber & Plastic Hose and Beltings (3002)						
13121	0.200	12	0.124	15	8.832	13
16631	2.731	13	0.119	16	0.000	15
16632	3.314	18	0.745	20	0.000	17
16633	0.872	17	0.191	21	0.000	18
Wiring Devices and Supplies (3611)						
31 291	0.000	21	1.694	32	1.608	32
31292	0.000	21	2.099	32	2.033	32
41122	0.000	39	0.000	43	0.000	41
42291	0.000	15	7.664	14	0.000	15

N - Number of establishments for which survey data were expected.

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Table 2.4 Coefficients of Variation (Between Establishments) in Monthly Estimates - 1984 ,

Survey and Item Codes	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
Flour Milling (2001)												
2120	1.041	0.999	1.049	1.011	1.054	1.076	1.063	1.061	1.103	1.043	1.032	1.089
21 30	1.066	1.027	1.207	1.039	1.070	1.085	1.081	1.078	1.127	1.054	1.050	1.109
Finished Fabrics (2202)												
1201	1.962	2.068	2.043	2.042	2.093	4.174	2.004	2.165	4.068	1.984	1.984	1.992
1202	1.723	1.612	1.645	1.653	1.639	1.700	2.599	1.878	6.907	1.777	1.688	1.828
Paint, Varnish, Lacquer (2806)												
2001	1.963	1.994	2.105	1.982	1.977	2.036	1.932	1.954	1.945	1.959	2.267	1.996
2002	1.809	1.795	1.933	1.779	1.862	1.925	1.814	1.853	1.802	1.856	2.167	1.871
Glass Containers (3207)												
11101	1.622	1.509	1.636	1.568	1.609	1.738	1.540	1.562	1.554	1.704	1.534	1.714
11903	1.396	1.826	1.337	1.440	1.489	1.780	2.046	1.734	2.251	1.730	1.719	2.324
Iron and Steel Castings (3301)												
11111	1.465	1.494	1.497	1.330	1.560	1.683	1.671	1.755	1.895	1.726	2.082	2.030
11112	0.999	1.104	0.932	0.939	0.921	1.228	1.313	1.284	1.395	1.139	1.269	1.238

Table 3.1 Distribution of Survey Establishments by Imputation Frequency for the "Principal" Items of Selected Surveys

Flour Milling - Item 2120

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Imputation Frequency (Number of Imputes During The Year)	Number 1982	of Establi <u>1983</u>	shments 1984
0	120	115	134
1-3	18	36	24
4-6	4	1	4
7-9	1	3	4
• 10-12	39	38_	36
Totals	182	193	202

Finished Fabrics - Item 1201

Imputation Frequency		Number of 1982	Establish <u>1983</u>	ments 1984
0		45	44	47
1 - 3		5	6	4
4-6		9	0	3
7-9		1	2	2
10-12		20	<u>19</u>	17
	Totals	80	71	73

Table 3.1 Distribution of Survey Establishments by Imputation Frequency for the "Principal" Items of Selected Surveys - Continued

Paint,	Varnish,	Lacquer	-	Item	2001
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Imputation Frequency		Number o 1982	f Establi <u>1983</u>	shments <u>1984</u>
0		49	58	30
1-3		24	138	13
4-6		4	4	1
7 -9		2	6	1
10-12		95	5	31
•	Totals	174	211	76

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Glass Containers - Item 11101

Imputation Frequency		Number (1982	of Establi. <u>1983</u>	shments 1984
0		19	16	15
1-3		3	6	5
4-6		0	0	4
7-9		0	0	1
10-12		1		_1
	Totals	23	23	26

Table 3.1 Distribution of Survey Establishments by Imputation Frequency for the "Principal" Items of Selected Surveys - Continued

Imputation Frequency		Number of 1982	Establishn <u>1983</u>	1984 <u>1984</u>
0		14	12	13
1-3		2	2	2
4-6		1	0	3
7-9		1	0	2
• 10-12		7	7	<u> </u>
1	fotals	25	25	24

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Iron and Steel Castings - Item 11111

Table 4.1 Parameter Estimates and Summary Statistics for Alternative Regression Models - Flour Milling (2001)

		Item 212	0 - 1984			
	Fel	b	Maı	n	Jun	e
Estimates/Statistics	<u>MS 1</u>	MS 2	MS 1	MS 2	MS 1	MS 2
^b 1	0.980	1.028	1.032	0.929	0.893	0.905
SD(b ₁)	0.018	0.023	0.013	0.035	0.018	0.034
R ²	0.878	0.934	0.945	0.836	0.869	0.845

Item 2130 - 1984

	Jul		Aug		Dec	
Estimates/Statistics	MS 1	MS 2	<u>MS 1</u>	MS 2	MS 1	MS 2
p ¹	0.906	0.953	1.042	1.072	0.977	0.917
SD(b ₁)	0.023	0.082	0.038	0.179	0.020	0.024
R ²	0.800	0.504	0.618	0.211	0.871	0.928

Table 4.2 Parameter Estimates and Summary Statistics for Alternative Regression Models - Finished Fabrics (2202)

		Item 120	1 - 1984			
	Feb		Mar		June	
Estimates/Statistics	<u>MS 1</u>	<u>MS 2</u>	<u>MS 1</u>	<u>MS 2</u>	MS 1	<u>MS 2</u>
b ₁	0.998	0.971	1.282	1.317	1.151	2.465
SD(b ₁)	0.032	0.047	0.030	0.411	0.581	7.465
R ²	0.939	0.905	0.965	0.192	0.005	0.002

		Item 120	2 - 1984			
•	Ju	1	Au	g	Dec	
Estimates/Statistics	<u>MS 1</u>	<u>MS 2</u>	<u>MS 1</u>	MS 2	<u>MS 1</u>	MS 2
• b ₁	0.614	0.669	0.367	0.985	1.060	1.243
SD(b ₁)	0.152	0.968	0.077	0.106	0.110	0.173
R ²	0.072	0.652	0.009	0.612	0.474	0.512

Table 4.3 Parameter Estimates and Summary Statistics for Alternative Regression Models - Paint, Varnish, and Lacquer (2806)

		1 - 1984				
	Fel	b	Mai	r	Jun	е
Estimates/Statistics	<u>MS 1</u>	<u>MS 2</u>	<u>MS 1</u>	MS 2	MS 1	MS 2
^b 1	1.146	1.147	1.290	1.248	1.053	1.041
SD(b ₁)	0.035	0.046	0.431	0.047	0.024	0.027
R ²	0.950	0.942	0.942	0.946	0.971	0.973

			Item 200	2 - 1984			
		Ju	1	Au	g	Dec	;
•	Estimates/Statistics	MS 1	MS 2	<u>MS 1</u>	<u>MS 2</u>	<u>MS 1</u>	MS 2
	b ₁	0.812	0.865	0.865	0.926	0.647	0.761
	• SD(b ₁)	0.029	0.035	0.064	0.061	0.022	0.033
	R ²	0.930	0.941	0.752	0.860	0.948	0.931

Table 4.4 Parameter Estimates and Summary Statistics for Alternative Regression Models - Glass Containers (3207)

		Item 111	01 - 1984			
	Fel	b	Mar	n -	Jun	e
Estimates/Statistics	MS 1	MS 2	MS 1	MS 2	MS 1	<u>MS 2</u>
^b 1	0.975	1.098	1.133	1.039	0.950	0.919
SD(b ₁)	0.065	0.107	0.059	0.090	0.744	0.144
R ²	0.859	0.868	0.924	0.893	0.862	0.772

		Item 119	03 - 1984			
•	Ju	1	Au	g	Dec	:
Estimates/Statistics	<u>MS 1</u>	MS 2	MS 1	MS 2	MS 1	MS 2
≁ b ₁	0.994	1.051	0.600	0.752	2.136	1.947
SD(b ₁)	0.229	0.410	0.095	0.274	0.366	0.654
R ²	0.525	0.552	0.705	0.600	0.687	0.689

Table 4.5 Parameter Estimates and Summary Statistics for Alternative Regression Models - Iron and Steel Castings (3301)

		Item 111	11 - 1984			
	Fel	0	Mai	^	Jun	e
Estimates/Statistics	<u>MS 1</u>	MS 2	MS 1	MS 2	MS 1	MS 2
D ₁	1.047	1.176	1.063	1.073	0.752	0.727
SD(b ₁)	0.142	0.218	0.039	0.080	0.078	0.097
R ²	0.607	0.726	0.961	0.932	0.773	0.837

		Item 111	12 - 1984			
	Ju	1	Au	g	Dec	:
Estimates/Statistics	<u>MS 1</u>	<u>MS 2</u>	<u>MS 1</u>	MS 2	<u>MS 1</u>	MS 2
b1	0.596	0.587	0.881	0.923	0.703	0.716
SD(b ₁)	0.073	0.117	0.064	0.789	0.030	0.055
R ²	0.868	0.834	0.953	0.215	0.977	0.977

Table 4.6a Parameter Estimates and Summary Statistics for Alternative Regression Models-Broadwoven Fabrics (2220) -- Quarter 1, 1984

	Alt	ernative Mod	dels	
QS 1	QS 2	QS 3	QS 4	QS 5
0.836	0.961	0.126	0.966	1.027
		0.838		
0.379	0.023	0.051	0.035	0.063
~~	~-	0.055		
0.823	0.942	0.945	0.884	0.729
	Item 13021	<u>1</u>		
<u>QS 1</u>	QS 2	QS 3	QS 4	QS 5
0.948	1.376	0.235	0.867	1.343
		1.096		
0.079	0.051	0.068	0.855	0.098
	~ =	0.091		
0.836	0.962	0.974	0.798	0.883
	Item 13031	<u>L</u>		
QS 1	QS 2	QS 3	QS 4	QS 5
1.096	1.237	1.035	1.076	1.236
		0.071		
0.025	0.441	0.130	0.040	0.078
		0.149	~ -	
0.977	0.945	0.977	0.941	0.854
	Item 13041	-		
QS 1	QS 2	QS 3	QS 4	QS 5
0.900	1.019	0.843	0.966	0.109
		0.067		
0.018	0.027	0.117	0.039	0.062
		0.134		
0.968	0.947	0.968	0.882	0.806
	0.379 0.823 <u>QS 1</u> 0.948 0.079 0.079 0.836 <u>QS 1</u> 1.096 0.025 0.977 <u>QS 1</u> 0.977 <u>QS 1</u> 0.977	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	QS 1QS 2QS 3 0.836 0.961 0.126 0.838 0.379 0.023 0.051 0.055 0.823 0.942 0.945 Item 13021QS 1QS 2QS 3 0.948 1.376 0.235 1.096 0.079 0.051 0.068 0.091 0.836 0.962 0.974 Item 13031QS 1QS 2QS 3 1.096 1.237 1.035 0.071 0.025 0.441 0.130 0.149 0.977 0.945 0.977 Item 13041QS 1QS 2QS 3 0.900 1.019 0.843 0.067 0.018 0.027 0.117 0.134	0.836 0.961 0.126 0.966 $$ 0.838 $$ 0.379 0.023 0.051 0.035 $$ $$ 0.055 $$ 0.823 0.942 0.945 0.884 Item 13021 $QS 1$ $QS 2$ $QS 3$ $QS 4$ 0.948 1.376 0.235 0.867 $$ $$ 1.096 $$ 0.079 0.051 0.068 0.855 $$ $$ 0.91 $$ 0.836 0.962 0.974 0.798 Item 13031 QS 1 $QS 2$ $QS 3$ $QS 4$ 1.096 1.237 1.035 1.076 $$ $$ 0.071 $$ 0.025 0.441 0.130 0.040 $$ $$ 0.977 0.941 Item 13041 QS 1 $QS 2$ $QS 3$ $QS 4$ 0

Item 13011

Table 4.6b Parameter Estimates and Summary Statistics for Alternative Regression Models-Broadwoven Fabrics (2220) -- Quarter 2, 1984

		Item 1301	<u>1</u>		
Estimates/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
٥ ₁	0.961	0.917	0.935	0.972	0.965
b ₂			0.025		~-
SD(b ₁)	0.012	0.024	0.058	0.015	0.040
SD(b ₂)	~~		0.056		
R ²	0.981	0.932	0.981	0.972	0.856
		Item 1302	1		
Estimates/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
^b 1	0.582	0.820	0.349	0.727	0.831
b ₂			0.353		
SD(b ₁)	0.025	0.049	0.070	0.053	0.073
SD(b ₂)			0.101		
R ²	0.963	0.908	0.952	0.836	0.838
		Item 13031	<u>I</u>		
Estimates/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
b ₁	0.938	0.901	1.056	0.916	0.925
^b 2			-0.223		
SD(b ₁)	0.030	0.053	0.254	0.035	0.071
SD(b ₂)			0.276		
R ²	0.937	0.864	0.902	0.923	0.791
		Item 13041	<u>l</u>		
Estimates/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
ъ ₁	0.984	0.870	1.093	0.935	0.914
^b 2			-0.018		
SD(b ₁)	0.014	0.025	0.077	0.028	0.063
SD(b ₂)			0.070		~-
R ²	0.977	0.934	0.979	0.923	0.719

Table 4.6c Parameter Estimates and Summary Statistics for Alternative Regression Models-Broadwoven Fabrics (2220) -- Quarter 3, 1984

Item 13011

Estimates/Statistics	QS 1	Alternativ _QS 2	e Models QS 3	QS 4	QS 5
^b 1	0.831	0.796	0.619	0.891	0.873
b ₂			0.210		
SD(b ₁)	0.148	0.018	0.063	0.027	0.040
SD(b ₂)			0.061		
R ²	0.962	0.950	0.974	0.911	0.833
•		Item 13021			
Estimates/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
^b 1	1.152	0.895	0.526	0.959	0.762
b ₂			0.525		
SD(b ₁)	0.086	0.074	0.250	0.087	0.077
SD(b ₂)			0.189		
R ²	0.815	0.844	0.867	0.796	0.804
		Item 13031			
Estimates/Statistics	<u>QS 1</u>	QS 2	QS 3	QS 4	QS 5
^b 1	1.184	0.914	0.904	1.044	0.918
b ₂			0.044		
SD(b ₁)	0.025	0.052	0.056	0.032	0.065
SD(b ₂)			0.057		
R ²	0.978	0.886	0.985	0.958	0.831
		Item 13041			
Estimates/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
ъ ₁	0.881	0.798	0.840	0.855	0.782
^b 2			0.038		
SD(b ₁)	0.012	0.023	0.067	0.022	0.049
SD(b ₂)			0.062		
R ²	0.982	0.944	0.982	0.948	0.776

Table 4.6d Parameter Estimates and Summary Statistics for Alternative Regression Models-Broadwoven Fabrics (2220) -- Quarter 4, 1984

		Item 1301	<u>1</u>		
Estimates/Statistics	QS 1	Alternat: QS 2	ive Models QS_3	QS 4	QS 5
Þ	0.938	0.632	0.879	0.977	0.792
۵ ₂			0.049		
SD(b ₁)	0.020	0.036	0.047	0.035	0.060
SD(b ₂)			0.035	~-	
R ²	0.950	0.765	0.951	0.880	0.658
		Item 13021	L		
Estimates/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
• ^b 1	0.954	0.844	0.384	1.184	0.771
p5			0.573		
SD(b ₁)	0.074	0.056	0.097	0.143	0.072
SD(b ₂)			0.081		*-
R ²	0.815	0.900	0.940	0.703	0.834
		Item 13031	_		
Estimates/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
⁰ 1	0.520	0.584	0.578	0.682	0.653
^b 2			0.085		
SD(b ₁)	0.025	0.056	0.154	0.049	0.082
SD(b ₂)			0.142		
R ²	0.900	0.740	0.812	0.825	0.632
		Item 13041	-		
Estimates/Statistics	QS 1	Alternati QS_2	ve Models QS 3	QS 4	QS 5
b ₁	0.966	0.768	0.529	1.027	0.768
b ₂			0.359		
SD(b ₁)	0.017	0.016	0.056	0.033	0.050
SD(b ₂)			0.045		
R ²	0.974	0.969	0.986	0.926	0.770

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Table 4.7a Parameter Estimates and Summary Statistics for Alternative Regression Models-Sheets, Pillowcases and Towels (2324) -- Quarter 1, 1984

			Item 13011	<u> </u>		
Estimat	tes/Statistics	QS 1	Alternati QS 2	ve Models QS 3	QS 4	QS 5
	D ₁	0.880	1.237	0.096	1.010	1.276
	b ₂			1.113		
	SD(b ₁)	0.132	0.095	0.253	0.218	0.197
	SD(b ₂)			0.343		
	R ²	0.899	0.971	0.972	0.812	0.894
-			Item 13012	2		
Estimat	tes/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
	b ₁	0.858	1.132	-1.155	0.952	1.179
	^b 2			2.549		
	SD(b ₁)	0.169	0.131	0.344	0.210	0.226
	SD(b ₂)	~-		0.428		
	R ²	0.837	0.937	0.983	0.805	0.845
			Item 1301	<u>3</u>		
Estimat	tes/Statistics	QS 1		ye Models QS 3	QS 4	<u>QS 5</u>
<u>Estimat</u>	<u>b₁</u>	<u>QS 1</u> 0.999	Alternati	.ve Models	<u>QS 4</u> 1.059	<u>QS 5</u> 1.377
Estimat			Alternati QS 2	ve Models QS 3		
<u>Estima</u>	^b 1		Alternati QS 2	ve Models <u>QS 3</u> -0.704		
<u>Estima</u>	^b 1 ^b 2 SD(b ₁) SD(b ₂)	0.999	Alternati QS 2 1.359 	ve Models <u>QS 3</u> -0.704 2.266	1.059	1.377
<u>Estima</u>	^b 1 ^b 2 SD(b ₁)	0.999	Alternati QS 2 1.359 	ve Models QS 3 -0.704 2.266 0.327	1.059	1.377
<u>Estimat</u>	^b 1 ^b 2 SD(b ₁) SD(b ₂)	0.999 0.146 	Alternati QS 2 1.359 0.099 	Ve Models QS 3 -0.704 2.266 0.327 0.429 0.988	1.059 0.194 	1.377 0.172
	^b 1 ^b 2 SD(b ₁) SD(b ₂)	0.999 0.146 	Alternati QS 2 1.359 0.099 0.974	Ve Models QS 3 -0.704 2.266 0.327 0.429 0.988	1.059 0.194 	1.377 0.172
	^b 1 ^b 2 SD(b ₁) SD(b ₂) R ²	0.999 0.146 0.904	Alternati QS 2 1.359 0.099 0.974 Item 13111	ve Models QS 3 -0.704 2.266 0.327 0.429 0.988	1.059 0.194 0.857	1.377 0.172 0.927
	b_1 b_2 $SD(b_1)$ $SD(b_2)$ R^2 tes/Statistics	0.999 0.146 0.904 QS 1	Alternati QS 2 1.359 0.099 0.974 Item 13111 QS 2	ve Models QS 3 -0.704 2.266 0.327 0.429 0.988	1.059 0.194 0.857 QS 4	1.377 0.172 0.927 QS 5
	b ₁ b ₂ SD(b ₁) SD(b ₂) R ² tes/Statistics b ₁	0.999 0.146 0.904 <u>QS 1</u> 0.869	Alternati QS 2 1.359 0.099 0.974 Item 13111 QS 2 1.120		1.059 0.194 0.857 QS 4 0.877	1.377 0.172 0.927 <u>QS 5</u> 1.122
	b_{1} b_{2} $SD(b_{1})$ $SD(b_{2})$ R^{2} $tes/Statistics$ b_{1} b_{2}	0.999 0.146 0.904 <u>QS 1</u> 0.869	Alternati QS 2 1.359 0.099 0.974 Item 13111 QS 2 1.120 	QS 3 -0.704 2.266 0.327 0.429 0.988 QS 3 0.610 0.341	1.059 0.194 0.857 <u>QS 4</u> 0.877 	1.377 0.172 0.927 <u>QS 5</u> 1.122

Table 4.7b Parameter Estimates and Summary Statistics for Alternative Regression Models-Sheets, Pillowcases and Towels (2324) -- Quarter 2, 1984

		Item 13011	<u> </u>		
Estimates/Statistics	_QS_1	Alternati QS 2	ve Models QS 3	QS 4	QS 5
b ₁	0.847	0.620	0.690	0.862	0.667
^b 2			0.100		
SD(b ₁)	0.033	0.070	0.071	0.042	0.136
SD(b ₂)			0.056		~~
R ²	0.989	0.941	0.997	0.986	0.827
•		Item 13012	2		
Estimates/Statistics	<u>QS 1</u>	QS 2	QS 3	QS 4	QS 5
• b ₁	0.885	0.654	0.531	0.914	0.693
b2		-	0.255		
SD(b ₁)	0.053	0.063	0.206	0.064	0.140
SD(b ₂)			0.160		
R ²	0.976	0.955	0.983	0.971	0.830
		Item 1301	<u>3</u>		
Estimates/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
b ₁	0.841	0.694	0.557	0.885	0.755
b2			0.237		
SD(b ₁)	0.051	0.093	0.043	0.077	0.136
SD(b ₂)			0.038		
R ²	0.975	0.917	0.998	0.950	0.860
		Item 13111	<u> </u>		
Estimates/Statistics	QS 1	QS 2	QS 3	<u>QS 4</u>	QS 5
⁰ 1	1.016	0.982	1.169	1.016	1.012
b ₂			-0.159		
SD(b ₁)	0.020	0.099	0.095	0.025	0.135
SD(b ₂)			0.096		
R ²	0,993	0.907	0.995	0.990	0.849

Table 4.7c Parameter Estimates and Summary Statistics for Atlernative Regression Models-Sheets, Pillowcases and Towels (2324) -- Quarter 3, 1984

		Item 13011	<u> </u>		
Estimates/Statistics	QS 1	Alternati QS 2	ve Models QS 3	QS 4	QS 5
^b 1	1.141	0.946	1.141	1.110	0.930
b ₂			0.383		
SD(b ₁)	0.118	0.142	0.146	0.129	0.154
SD(b ₂)			2.054		
R ²	0.968	0.957	0.968	0.961	0.948
•		Item 13012	2		
Estimates/Statistics	QS 1	Alternati QS 2	ive Models QS 3	QS 4	QS 5
• •	1.313	1.031	0.602	1.328	1.082
b ₂			0.577	~-	
SD(b ₁)	0.104	0.079	0.208	0.116	0.182
SD(b ₂)			0.163		
R ²	0.976	0.983	0.997	0.970	0.922
		Item 1301	<u>3</u>		
Estimates/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
^b 1	1.311	1.089	1.531	1.265	1.075
b ₂		→-	-0.182		
SD(b ₁)	0.048	0.097	0.338	0.109	0.099
SD(b ₂)			0.283		~~
R ²	0.995	0.977	0.998	0.971	0.975
		Item 13111	<u>L</u>		
Estimates/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
b ₁	.0904	1.010	0.715	0.869	0.993
^b 2			0.216		
SD(b ₁)	0.035	0.060	0.262	0.048	0.067
SD(b ₂)			0.294		
R ²	0.986	0.972	0.986	0.970	0.965

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Table 4.7d Parameter Estimates and Summary Statistics for Alternative Regression Models-Sheets, Pillowcases and Towels (2324) -- Quarter 4, 1984

			Item 13011	L		
Estimat	es/Statistics	QS 1	Alternati QS 2	ve Models QS 3	QS 4	QS 5
	b ₁	0.365	0.381	-0.733	0.358	0.304
	^b 2			0.988	⇒~	
	SD(b ₁)	0.211	0.164	0.610	0.205	0.173
	SD(b ₂)			0.527	~ ~	
	R ²	0.500	0.729	0.889	0.504	0.608
			Item 13012	2		
Estimat	es/Statistics	_QS 1	Alternati QS 2	ve Models QS 3	QS 4	QS 5
•	b ₁	0.890	0.941	0.478	0.882	0.949
	^b 2			0.447		~~
	SD(b ₁)	0.071	0.099	0.382	0.076	0.103
	SD(b ₂)			0.404		
	R ²	0.981	0.978	0.991	0.978	0.977
			Item 13013	_		
Estimate	es/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
	b ₁	0.787	0.834	0.895	0.785	0.853
	^b 2			-0.124		
	SD(b ₁)	0.027	0.177	0.145	0.066	0.175
	SD(b ₂)			0.160		
	R ²	0.996	0.917	0.998	0.979	0.922
			Item 13111			
Estimate	es/Statistics	QS 1	QS 2	QS 3	QS 4	QS 5
	b ₁	0.984	0.835	0.828	1.017	0.821
	^b 2			0.139		
	SD(b ₁)	0.042	0.077	0.167	0.048	0.084
	SD(b ₂)			0.145		-
	R ²	0.987	0.944	0.989	0.985	0.932

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Table 4.8a Parameter Estimates and Summary Statistics for Alternative Regression Models -Gloves and Mittens (2304) - 1983

	Item 31200		
Estimates/Statistics	AS 1	AS 2	_AS 3_
^b 1	1.298	1.146	1.651
b ₂			-0.253
SD(b ₁)	0.073	0.067	0.362
SD(b ₂)			0.280
R ²	0.900	0.892	0.894
	Item 31210	2	
Estimates/Statistics	AS 1	AS 2	AS 3
* b ₁	1.046	1.015	2.076
b ₂		~~~	-0.266
SD(b ₁)	0.021	0.042	0.516
SD(b ₂)			0.316
R ²	0.986	0.944	0.832
	Item 33200	2	
Estimates/Statistics	AS 1	AS 2	AS 3
^b 1	0.942	0.956	0.412
b ₂			0.382
SD(b ₁)	0.022	0.030	0.082
SD(b ₂)			0.070
R ²	0.967	0.942	0.875
	Item 33210	2	
Estimates/Statistics	AS 1	AS 2	AS 3
^ь 1	0.930	0,953	0.889
۶			0.059
SD(b ₁)	0.017	0.026	0.033
SD(b ₂)			0.035
R ²	0.978	0.954	0.978

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Table 4.8b Parameter Estimates and Summary Statistics for Alternative Regression Models -Gloves and Mittens (2304) - 1984

	Item 31200	<u>0</u>	
Estimates/Statistics	<u>AS 1</u>	AS 2	AS 3
^b 1	0.812	0.888	0.052
b ₂			0.793
SD(b ₁)	0.051	0.065	0.237
SD(b ₂)			0.248
r ²	0.861	0.841	0.886
	Item 31210	<u>)</u>	
Estimates/Statistics	AS 1	AS 2	AS 3
• ^b 1	0.740	0.841	0.391
^b 2		~==	0.680
SD(b ₁)	0.034	0.053	0.055
SD(b ₂)			0.101
R ²	0.934	0.881	0.975
	Item 33200	<u>_</u>	
Estimates/Statistics	<u>AS 1</u>	AS 2	AS 3
<u>Estimates/Statistics</u>		-	<u>AS 3</u> 0.325
	AS 1	AS 2	
Þ ₁	AS 1	AS 2	0.325
b ₁ b ₂ SD(b ₁) SD(b ₂)	<u>AS 1</u> 1.166	<u>AS 2</u> 1.171	0.325 0.843
b ₁ b ₂ SD(b ₁)	<u>AS 1</u> 1.166	<u>AS 2</u> 1.171	0.325 0.843 0.077
b ₁ b ₂ SD(b ₁) SD(b ₂)	<u>AS 1</u> 1.166 0.024 	AS 2 1.171 0.074 0.812	0.325 0.843 0.077 0.071
b ₁ b ₂ SD(b ₁) SD(b ₂)	<u>AS 1</u> 1.166 0.024 0.975	AS 2 1.171 0.074 0.812	0.325 0.843 0.077 0.071
b_1 b_2 $SD(b_1)$ $SD(b_2)$ R^2	<u>AS 1</u> 1.166 0.024 0.975 Item 33210	<u>AS 2</u> 1.171 0.074 0.812	0.325 0.843 0.077 0.071 0.962
b ₁ b ₂ SD(b ₁) SD(b ₂) R ² Estimates/Statistics	<u>AS 1</u> 1.166 0.024 0.975 Item 33210 <u>AS 1</u>	<u>AS 2</u> 1.171 0.074 0.812 <u>AS 2</u>	0.325 0.843 0.077 0.071 0.962 AS 3
b_{1} b_{2} $SD(b_{1})$ $SD(b_{2})$ R^{2} <u>Estimates/Statistics</u> b_{1}	<u>AS 1</u> 1.166 0.024 0.975 Item 33210 <u>AS 1</u>	<u>AS 2</u> 1.171 0.074 0.812 <u>AS 2</u>	0.325 0.843 0.077 0.071 0.962 <u>AS 3</u> 2.895
b_{1} b_{2} $SD(b_{1})$ $SD(b_{2})$ R^{2} <u>Estimates/Statistics</u> b_{1} b_{2} $SD(b_{1})$ $SD(b_{2})$	<u>AS 1</u> 1.166 0.024 0.975 <u>Item 33210</u> <u>AS 1</u> 1.175 	<u>AS 2</u> 1.171 0.074 0.812 <u>AS 2</u> 1.186 	0. 325 0.843 0.077 0.071 0.962 <u>AS 3</u> 2.895 -1.725
b_{1} b_{2} $SD(b_{1})$ $SD(b_{2})$ R^{2} Estimates/Statistics b_{1} b_{2} $SD(b_{1})$	<u>AS 1</u> 1.166 0.024 0.975 <u>Item 33210</u> <u>AS 1</u> 1.175 	<u>AS 2</u> 1.171 0.074 0.812 <u>AS 2</u> 1.186 	0. 325 0.843 0.077 0.071 0.962 <u>AS 3</u> 2.895 -1.725 0.402

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Table 4.9a Parameter Estimates and Summary Statistics for Alternative Regression Models -Industrial Gases (2802) - 1983

	Item 4414	<u>1</u>	
Estimates/Statistics	AS 1	AS 2	<u>AS 3</u>
۵ ₁	1.062	0.992	0.416
^b 2			0.597
SD(b1)	0.033	0.038	0.127
SD(b ₂)			0.122
R ²	0.927	0.893	0.818
	Item 4414	2	
Estimates/Statistics	AS 1	AS 2	AS 3
^b 1	1.062	0.992	0.421
^b 2			0.572
SD(b ₁)	0.033	0.038	0.147
SD(b ₂)			0.141
R ²	0.927	0.893	0.792
	Item 4414	<u>3</u>	
Estimates/Statistics	AS 1	AS 2	AS 3
b ₁	1.244	1.308	1.359
b ₂			-0.296
SD(b ₁)	1.131	0.181	0.271
SD(b ₂)			0.297
R ²	0.539	0.404	0.454
	Item 44251	<u> </u>	
Estimates/Statistics	AS 1	AS 2	AS 3
Þ ₁	0.983	1.069	0.504
^b 2			0.442

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Table 4.9b Parameter Estimates and Summary Statistics for Alternative Regression Models -Industrial Gases (2802) - 1984

	Item 44141		
Estimates/Statistics	AS 1	AS 2	_AS 3_
ь ₁	1.005	1.118	0.770
^b 2			0.085
SD(b ₁)	0.042	0.107	0.194
SD(b ₂)			0.231
R ²	0.887	0.599	0.611
	Item 44142		
Estimates/Statistics	AS 1	AS 2	AS 3
• ^b 1	1.005	1.118	0.393
b ₂			0.519
SD(b ₁)	0.042	0.107	0.182
SD(b ₂)		~~~	0.204
R ²	0.887	0.599	0.594
	Item 44143		
<u>Estimates/Statistics</u>	Item 44143 AS 1	AS 2	<u>AS 3</u>
<u>Estimates/Statistics</u>		<u>AS 2</u> 1.068	<u>AS 3</u> 0.081
	<u>AS 1</u>		
p ¹	<u>AS 1</u>		0.081
b_1 b_2 $SD(b_1)$ $SD(b_2)$	<u>AS 1</u> 0.958	1.068	0.081
^b 1 ^b 2 SD(b ₁)	<u>AS 1</u> 0.958	1.068	0.081 0.829 0.076
b_1 b_2 $SD(b_1)$ $SD(b_2)$	<u>AS 1</u> 0.958 0.041	1.068 0.062 	0.081 0.829 0.076 0.132
b_1 b_2 $SD(b_1)$ $SD(b_2)$	<u>AS 1</u> 0.958 0.041 0.885	1.068 0.062 	0.081 0.829 0.076 0.132
b_1 b_2 $SD(b_1)$ $SD(b_2)$ R^2	<u>AS 1</u> 0.958 0.041 0.885 <u>Item 44251</u>	1.068 0.062 0.801	0.081 0.829 0.076 0.132 0.595
$\frac{b_1}{SD(b_1)}$ $\frac{SD(b_2)}{R^2}$ Estimates/Statistics	<u>AS 1</u> 0.958 0.041 0.885 <u>Item 44251</u> <u>AS 1</u>	1.068 0.062 0.801 AS 2	0.081 0.829 0.076 0.132 0.595 AS 3
$\frac{b_{1}}{b_{2}}$ $SD(b_{1})$ $SD(b_{2})$ R^{2} Estimates/Statistics b_{1}	<u>AS 1</u> 0.958 0.041 0.885 <u>Item 44251</u> <u>AS 1</u> 0.861	1.068 0.062 0.801 AS 2	0.081 0.829 0.076 0.132 0.595 <u>AS 3</u> 0.629
$\frac{b_{1}}{b_{2}}$ $SD(b_{1})$ $SD(b_{2})$ R^{2} <u>Estimates/Statistics</u> $\frac{b_{1}}{b_{2}}$	<u>AS 1</u> 0.958 0.041 0.885 <u>Item 44251</u> <u>AS 1</u> 0.861 	1.068 0.062 0.801 <u>AS 2</u> 0.934 	0.081 0.829 0.076 0.132 0.595 <u>AS 3</u> 0.629 0.337

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Table 4.10a Parameter Estimates and Summary Statistics for Alternative Regression Models -Rubber & Plastic Hose and Beltings (3002) - 1983

	Item 13121	-	
Estimates/Statistics	AS 1	AS 2	AS 3
b ₁	1.285	1.347	1.418
b ₂			-0.387
SD(b ₁)	0.090	0.357	0.024
SD(b ₂)			0.268
R ²	0.953	0.587	0.997
	Item 16631	<u>_</u>	
Estimates/Statistics	AS 1	AS 2	AS 3
• b ₁	0.994	1.086	
b ₂			1.365
SD(b ₁)	0.070	0.123	
SD(b ₂)			0.116
R ²	0,953	0.887	0.958
	Item 16632	2	
Estimates/Statistics	<u>AS 1</u>	AS 2	AS 3
^b 1	1.147	1.266	
b ₂			1.364
SD(b ₁)	0.113	0.119	at as as
SD(b ₂)			0.118
R ²	0.888	0.897	0.957
	Item 16633	<u>3</u>	
Estimates/Statistics	AS 1	AS 2	AS 3
b1	1.240	1.239	1.593
b ₂			-0.133
SD(b ₁)	0.043	0.058	0.181
SD(b ₂)			0.196
R ²	0.984	0.970	0.995

Table 4.10b Parameter Estimates and Summary Statistics for Alternative Regression Models -Rubber & Plastic Hose and Beltings (3002) - 1984

	Item 1312	21	
Estimates/Statistics	AS 1	AS 2	<u>AS 3</u>
b ₁	1.283	1.285	0.621
^b 2		~~~	0.905
SD(b ₁)	0.086	0.098	0.363
SD(b ₂)	***		0.485
R ²	0.965	0.956	0.978
	Item 1663	1	
Estimates/Statistics	_AS 1	AS 2	_AS 3_
• ^b 1	1.218	1.200	2.667
b ₂			-1.452
SD(b ₁)	0.039	• 0.059	0.241
SD(b ₂)			0.250
R ²	0.986	0.968	0.991
	Item 1663:	2	
Estimates/Statistics	Item 1663: AS 1	AS 2	AS 3
<u>Estimates/Statistics</u>		-	
	AS 1	AS 2	1.769
ъ ₁	AS 1	AS 2	1.769 -0.540
b_1 b_2 $SD(b_1)$ $SD(b_2)$	<u>AS 1</u> 1.172	<u>AS 2</u> 1.171	1.769 -0.540 0.280
^b 1 ^b 2 SD(b ₁)	<u>AS 1</u> 1.172	<u>AS 2</u> 1.171	1.769 -0.540
b_1 b_2 $SD(b_1)$ $SD(b_2)$	<u>AS 1</u> 1.172 0.043 	<u>AS 2</u> 1.171 0.053 0.972	1.769 -0.540 0.280 0.287
b_1 b_2 SD(b_1) SD(b_2)	<u>AS 1</u> 1.172 0.043 0.982	<u>AS 2</u> 1.171 0.053 0.972	1.769 -0.540 0.280 0.287
b_1 b_2 $SD(b_1)$ $SD(b_2)$ R^2	<u>AS 1</u> 1.172 0.043 0.982 <u>Item 16633</u>	<u>AS 2</u> 1.171 0.053 0.972	1.769 -0.540 0.280 0.287 0.953 AS 3
$\frac{b_1}{SD(b_1)}$ $\frac{SD(b_2)}{R^2}$ Estimates/Statistics	<u>AS 1</u> 1.172 0.043 0.982 <u>Item 16633</u> <u>AS 1</u>	<u>AS 2</u> 1.171 0.053 0.972 <u>AS 2</u>	1.769 -0.540 0.280 0.287 0.953
b_{1} b_{2} $SD(b_{1})$ $SD(b_{2})$ R^{2} Estimates/Statistics b_{1}	<u>AS 1</u> 1.172 0.043 0.982 <u>Item 16633</u> <u>AS 1</u>	<u>AS 2</u> 1.171 0.053 0.972 <u>AS 2</u>	1.769 -0.540 0.280 0.287 0.953 <u>AS 3</u> 1.279 -0.125
$\frac{b_1}{SD(b_1)}$ $\frac{SD(b_2)}{R^2}$ <u>Estimates/Statistics</u> $\frac{b_1}{b_2}$	<u>AS 1</u> 1.172 0.043 0.982 <u>Item 16633</u> <u>AS 1</u> 1.178 	<u>AS 2</u> 1.171 0.053 0.972 <u>AS 2</u> 1.172 	1.769 -0.540 0.280 0.287 0.953 <u>AS 3</u> 1.279

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Table	4.11a	Parameter	Estimates	and	Summary	Statistics
	for	Alternati	ive Regress	sion	Models -	-
	Wirin	g Devices	and Suppli	es (3611) -	1983

	Item 31291	<u>L</u>	
Estimates/Statistics	AS 1	AS 2	AS 3
b ₁	1.239	1.233	0.302
b ₂			1.071
SD(b ₁)	0.065	0.070	0.316
$SD(b_2)$			0.328
R ²	0.933	0.922	0.887
	Item 31292	2	
Estimates/Statistics	AS 1	AS 2	AS 3
^b 1	1.173	1.206	1.203
b ₂			0.037
SD(b ₁)	0.044	0.066	0.118
SD(b ₂)			0.108
R ²	0.965	0.927	0.986
	Item 4112	2	
Estimates/Statistics	AS 1	AS 2	AS 3
b1	0.978	0.969	0.517
b ₂	~ ~ =		0.441
SD(b ₁)	0.017	0.025	0.165
SD(b ₂)	**=		0.170
R ²	0.988	0.975	0.898
	0. 900		
	Item 42291		
Estimates/Statistics			_AS_3_
<u>Estimates/Statistics</u> ^D 1	Item 42291	L	
	Item 42291 AS 1	AS 2	<u>AS 3</u>
ь ¹	Item 42291 AS 1	AS 2	<u>AS 3</u> 1.081
b ₁ b ₂	<u>Item 42291</u> <u>AS 1</u> 1.093 	<u>AS 2</u> 1.075	<u>AS 3</u> 1.081 -0.231
^b 1 ^b 2 SD(b ₁)	<u>Item 42291</u> <u>AS 1</u> 1.093 	<u>AS 2</u> 1.075	<u>AS 3</u> 1.081 -0.231 1.295

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Table 4.11b Parameter Estimates and Summary Statistics for Alternative Regression Models -Wiring Devices and Supplies (3611) - 1984

	Item 3129	<u>1</u>	
Estimates/Statistics	AS 1	AS 2	AS 3
b1	1.134	1.155	0.045
b ₂			1.109
SD(b1)	0.024	0.172	0.192
SD(b ₂)			0.165
R ²	0.987	0.608	0.863
	Item 31292	2	
Estimates/Statistics	AS 1	AS 2	AS 3
• ^b 1	1.248	1.244	0.712
^b 2	~~~		0.341
SD(b ₁)	0.014	0.079	1.531
$SD(b_2)$			2.262
R ²	0.996	0.895	0.699
	Item 41122	2	
Estimates/Statistics	<u>AS 1</u>	AS 2	<u>AS 3</u>
^b 1	1.021	1.051	0.847
^b 2			0.138
SD(b ₁)	0.011	0.019	0.082
SD(b ₂)			0.077
R ²	0.996	0.989	0.980
	Item 42291	-	
Estimates/Statistics	<u>AS 1</u>	AS 2	AS 3
٥ ₁	1.053	1.086	1.033
^b 2			0.007
SD(b ₁)	0.045	0.050	0.038
SD(b ₂)			0.042
R ²	0.980	0.977	0.995

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Table 5.1a Comparison of Alternative Estimators for Selected Monthly Surveys - March, 1984

Survey and	Model Alt	ernative	Relative Change MS 1 - MS 2
Item Code	MS 1	<u>MS 2</u>	MS 2
Flour Milling			
21 20	25,993	25,972	0.0008
2130	494,243	492,961	0.0026
Finished Fabrics			
1201	135,988	135,839	0.0011
1202	99,282	99,601	-0.0032
Paint, Varnish and Lacquer			
2001	30,668	30,576	0.0030
2002	223,683	221,578	0.0095
Glass Containers			
11101	264,374	261,162	0.0123
11903	No Imputatio	on Required	
Iron and Steel Castings			
11111	90,025	90,052	-0.0003
11112	70,148	72,662	-0.0346

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Table 5.1b Comparison of Alternative Estimators for Selected Monthly Survey - December, 1984

Survey and	Model Alt	ernati ve	Relative Change MS 1 - MS 2
Item Code	<u>MS 1</u>	MS 2	MS 2
Flour Milling			
2120	24,531	24,548	-0.0007
2130	439,401	439,621	-0.0005
Finished Fabrics			
1201	96,340	97,382	-0.0107
1202	74,278	74,487	-0.0028
Paint, Varnish and Lacquer			
2001	14,990	16,098	-0.0688
- 2002	118,185	126,754	-0.0676
Glass Containers			
11101	138,224	137,372	0.0062
11903	No Imputati		
Iron and Steel Castings			
11111	55,252	55,379	-0.0023
11112	24,105	25,614	-0.0589
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Table 5.2a Reported and Estimated Totals for Selected Quarterly Surveys - Quarter 1, 1984

Survey 2220

		Estimated Totals					
Item	Reported Total	Model 1	Model 2	Model 3	Model 4	Model 5	<u>N</u>
1 301 1	286356	282831	291041	290517	286438	293197	130
13021	14623	15724	14648	15023	15425	14589	39
1 3031	41 01 9	41045	41160	41 053	41 036	41174	63
13041	127875	127769	126501	127708	128465	119151	107
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	Estimated Totals						
Item	Reported Total	Model 1	Model 2	Model 3	Model 4	Model 5	<u>_N</u>
1 301 1	123	118	118	118	118	119	8
13012	87	0	89	81	88	82	7
13013	3817	3741	3752	3756	3744	3753	8
13111	4260	4394	4274	4360	4398	4275	17

Table 5.2b Reported and Estimated Totals for Selected Quarterly Surveys - Quarter 2, 1984

Survey 2220

	Estimated Totals						
Item	Reported Total	Model 1	Model 2	Model 3	Model 4	Model 5	<u>N</u>
1 301 1	280292	281 360	278450	280866	281606	279420	134
13021	10557	10467	10606	10576	10884	10630	45
1 3031	401 21	40387	39756	40232	40329	39803	65
13041	121605	1 21 921	118355	122809	121417	118686	107

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	Estimated Totals									
Item	Reported Total	Model 1	Model 2	Model 3	Model 4	Model 5	<u>_N</u>			
1 301 1	105	105	112	105	106	114	8			
13021	96	97	101	98	97	102	8			
1 3031	3378	3371	3330	3360	3407	3386	8			
13111	4345	4381	4396	4370	4381	4404	18			

Table 5.2c Reported and Estimated Totals for Selected Quarterly Surveys - Quarter 3, 1984

Sur ve y 2220

		Estimated Totals					
Item	Reported Total	Model 1	Model 2	Model 3	Model 4	Model 5	<u> </u>
1 301 1	265626	265316	264659	265241	2661 31	265687	126
13021	9966	11025	1 01 31	10582	10555	9847	42
1 3031	32726	35274	34155	33014	34219	34190	53
13041	94624	97589	95072	96821	97057	94762	94

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	Estimated Totals									
Item	Reported Total	Model 1	Model 2	Model 3	Model 4	Model 5	<u>N</u>			
1 301 1	81	79	81	92	78	80	4			
13012	92	95	93	94	96	94	5			
1 301 3	2940	3006	3036	3001	2974	3025	5			
13111	3503	3524	3445	3510	3503	3437	11			

Table 5.2d Reported and Estimated Totals for Selected Quarterly Surveys - Quarter 4, 1984

Sur vey 2220

	Estimated Totals						
Item	Reported Total	Model 1	Model 2	Model 3	Model 4	Model 5	<u>N</u>
1 301 1	266396	229289	233844	228387	230719	243702	114
13021	10949	10466	11346	11178	10830	11139	39
1 3031	22162	20407	20854	21177	21 261	21 231	49
13041	89549	92945	90685	90457	94060	90685	89

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	Estimated Total								
Item	Reported Total	Model 1	Model 2	Model 3	Model 4	Model 5	<u>N</u>		
1 301 1	28	15	21	24	15	17	4		
13012	75	71	78	75	71	78	4		
1 301 3	2261	2316	2282	2314	2315	2296	4		
13111	3017	2936	2853	2931	2971	2837	8		

Table 5.3a Relative Bias (\$) of Estimated Totals for Items - Quarter 1, 1984

Survey 2220 Alternative Models								
Item	_QS 1	QS 2	QS 3	QS 4	QS 5	<u>N</u>		
13011	1.23	1.64	-1.45	-0.03	-2.39	130		
13021	-10.24	-2.70	-5.33	- 8.15	-2.29	39		
13031	-0.06	-0.34	-0.08	-0.04	-0.38	63		
13041	0.08	1.07	0.13	-0.46	6.82	107		

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	Alternative Models								
Item	QS 1	QS 2	QS 3	QS 4	QS 5	N			
13011	4.07	4.07	4.07	4.07	3.25	8			
1 301 2	0.00	- 2.30	6.90	-1.15	5.75	7			
13013	1.99	1.70	1.60	1.91	1.68	8			
13111	3.15	-0.33	-2. 35	-3.24	-0.35	17			

Table 5.3b Relative Bias (\$) of Estimated Totals for Selected Items - Quarter 2, 1984

Survey 2220

	Alternative Models								
Item	QS 1	QS 2	QS 3	QS 4	QS 5	<u>N</u>			
13011	-0.38	0.66	-0.20	-0.63	0. 31	134			
1 3021	0.85	-0.46	-0.18	-3.10	-0.69	45			
13031	0.66	0.91	0.28	-0.52	0.79	65			
1 3041	-0.26	2.67	0.99	0.15	2.40	107			

Survey 2324

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		Alt	ternative Mod	dels		
Item	QS 1	QS 2	QS 3	QS 4	QS 5	<u>N</u>
13011		-6.67		-0.95	-8.57	8
1 301 2	-1.04	-5.21	-2.08	-1.04	-6.25	8
13013	0.21	1.42	0.53	-0.86	-0.24	8
13111	-0.83	-1.17	-0.58	-0.83	-1.36	18

Table 5.3c Relative Bias (\$) of Estimated Totals for Selected Items - Quarter 3, 1984

Survey 2220

	Alternative Models								
Item	QS 1	QS 2	QS 3	QS 4	QS 5	<u>_N</u>			
13011	0.12	0.36	0.14	-0.19	-0.02	126			
1 302 1	-10.63	-1.66	-6.18	-5.91	1.19	42			
13031	-7.79	-4.37	-0.88	-4.56	-4.47	53			
13041	-3.04	-0.47	-2.32	-2.57	-0.15	94			

Survey 2324

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		Al	ternative Mod	dels		
Item	QS 1	QS 2	QS 3	QS 4	QS 5	<u>N</u>
13011	2.47		-13.58	3.70	1.23	4
1 301 2	-3.26	-1.09	-2.17	-4.35	- 2.17	5
13013	-2.24	-3.27	-2.07	-1.16	-2.89	5
13111	-0.60	1.66	-0.20	0.00	1.88	11

Table 5.3d Relative Bias (\$) of Estimated Totals for Selected Items - Quarter 4, 1984

Sur vey 2220

		Alt	cernative Mod	dels		
Item	QS 1	QS 2	QS 3	QS 4	QS 5	<u>N</u>
13011	-1.28	-3.29	-0.88	-1.91	-7.64	114
13021	4.41	-3.63	-2.09	1.09	-1.74	39
13031	7.92	-0.07	4.44	4.07	4.20	49
1 3041 -	-3.79	-1.27	-1.01	-5.04	1.27	89

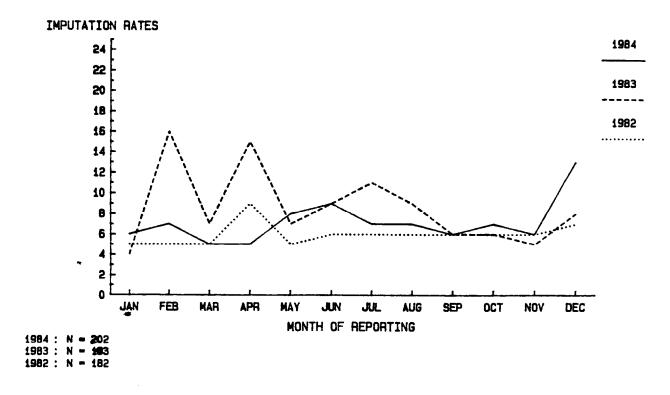
Survey 2324

Alternative Models						
Item	_QS_1	QS 2	QS 3	QS 4	QS 5	<u>N</u>
13011	46.43	25.00	14.29	46.43	39.29	4
13012	5.33	-4.00		5.33	-4.00	4
13013	-2.43	-0.93	-2.34	-2.39	- 1.55	4
13111	2.68	5.44	2.85	1.52	5.97	8

Appendix B - Data Plots

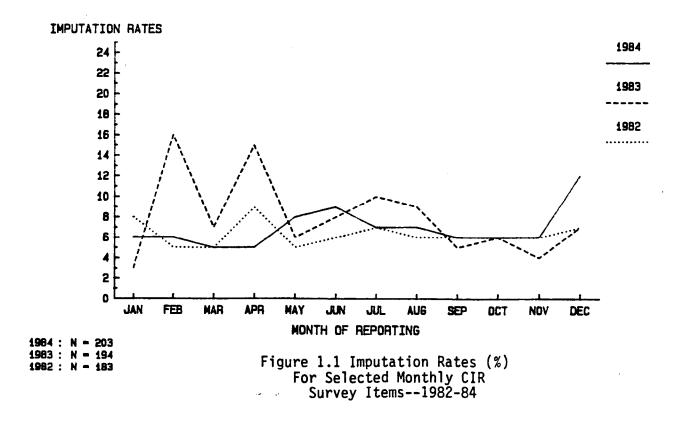
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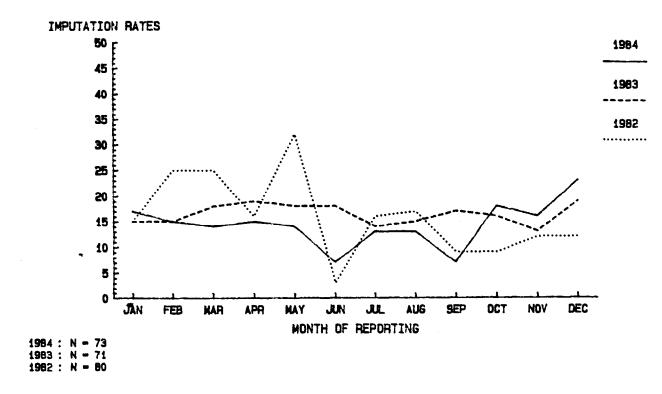
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SURVEY 2001 AND ITEM 2120

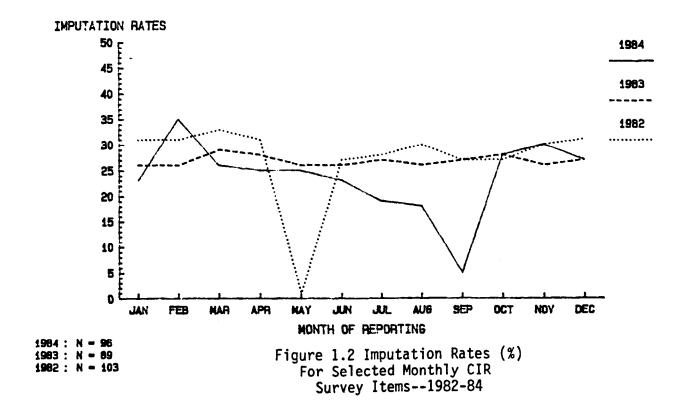
SURVEY 2001 AND ITEM 2130

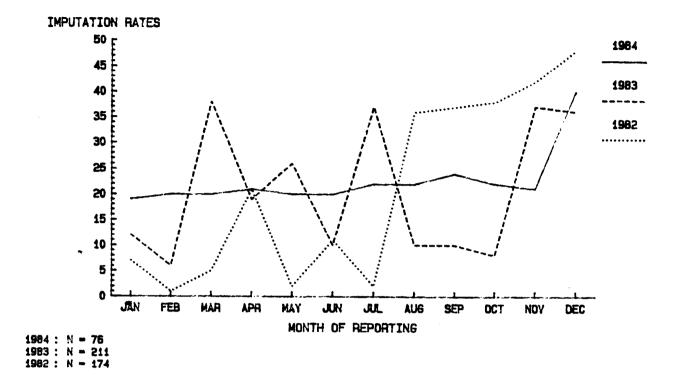




SURVEY 2202 AND ITEM 1201

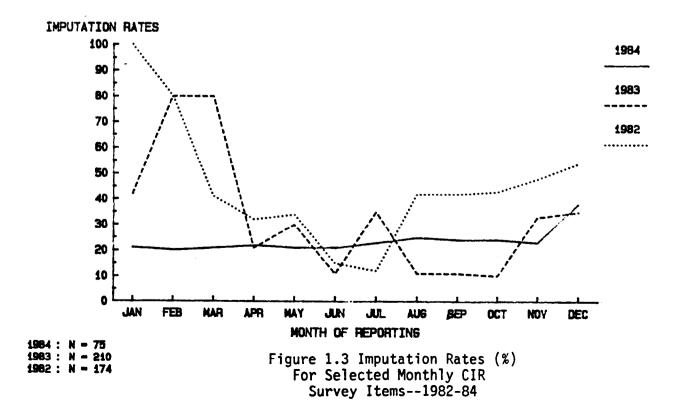




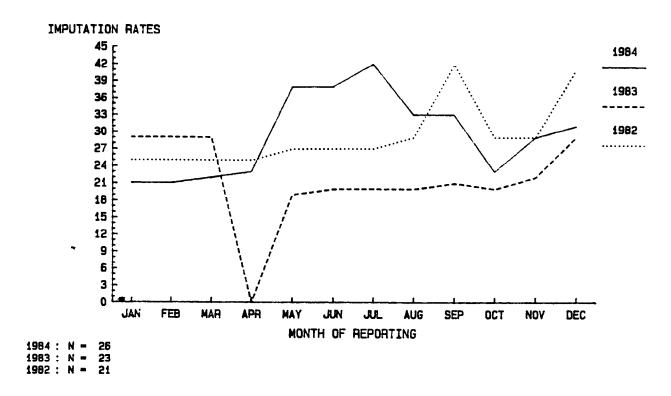


SURVEY 2806 AND ITEM 2001

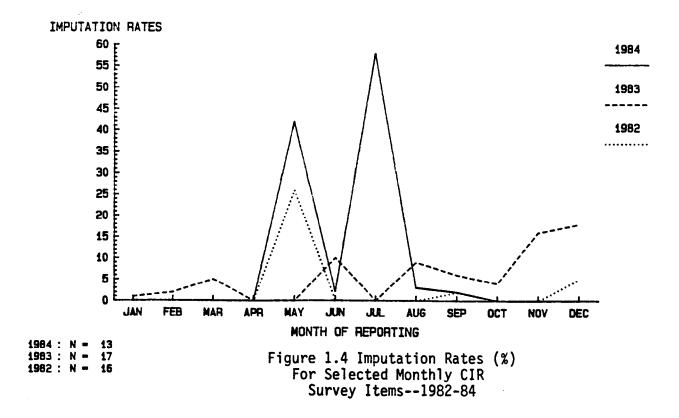




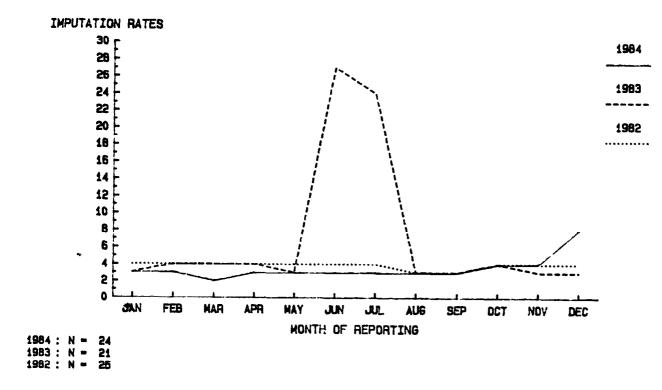
SURVEY 3207 AND ITEM 11101



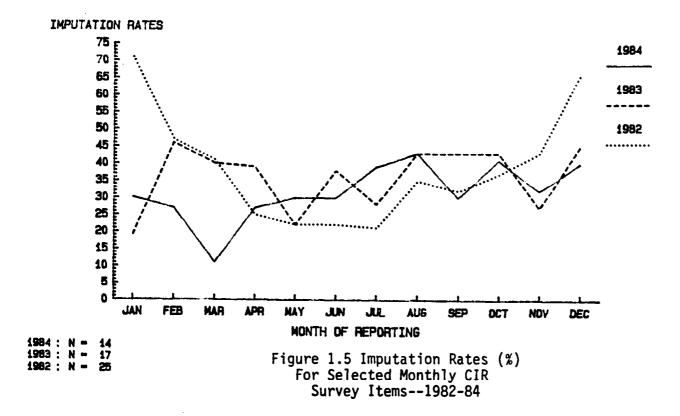


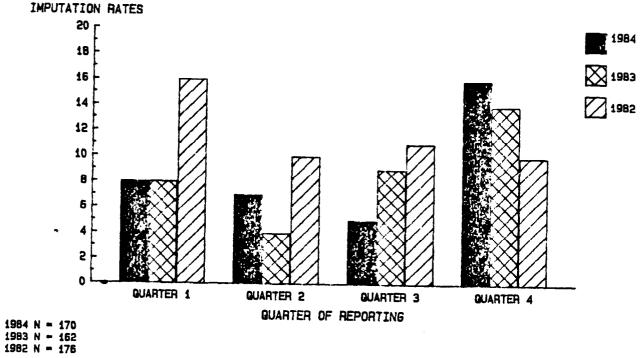


SURVEY 3301 AND ITEM 11111



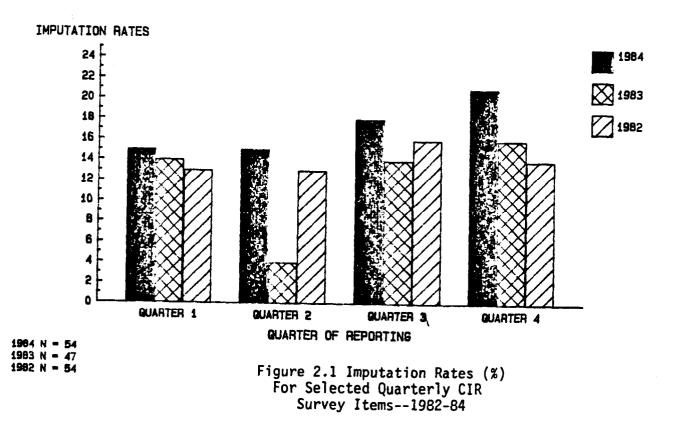
SURVEY 3301 AND ITEM 11112





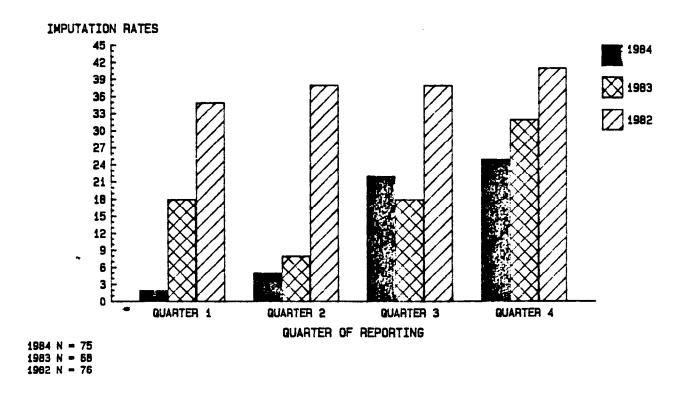
SURVEY 2220 AND ITEM 13011

SURVEY 2220 AND ITEM 13021

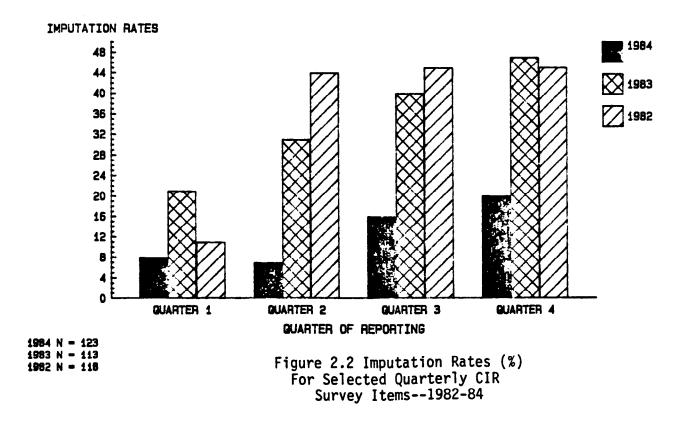


SURVEY 2220 AND ITEM 13031

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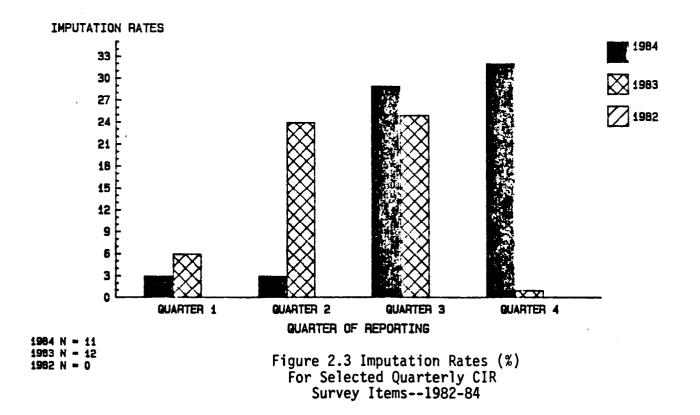
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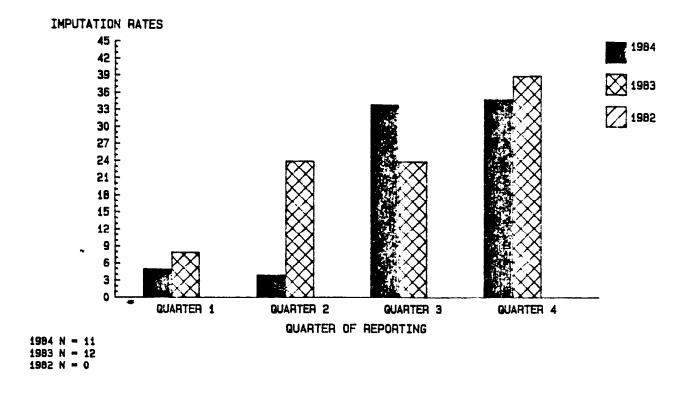
IMPUTATION RATES Ē QUARTER 2 QUARTER 4 QUARTER 1 QUARTER 3 QUARTER OF REPORTING 1984 N = 11 1983 N = 12 1982 N = 0

SURVEY 2324 AND ITEM 13011

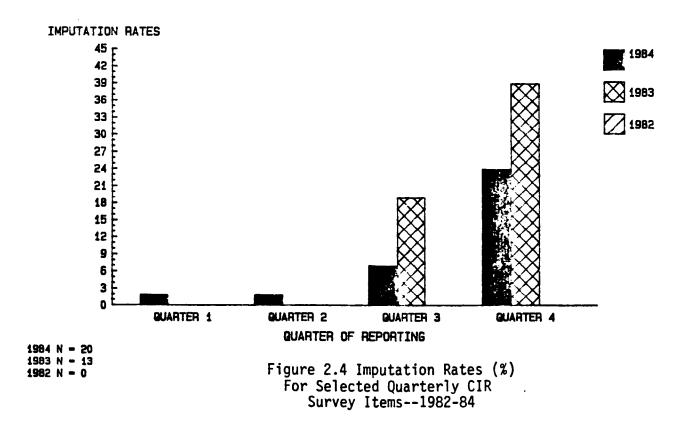
SURVEY 2324 AND ITEM 13012

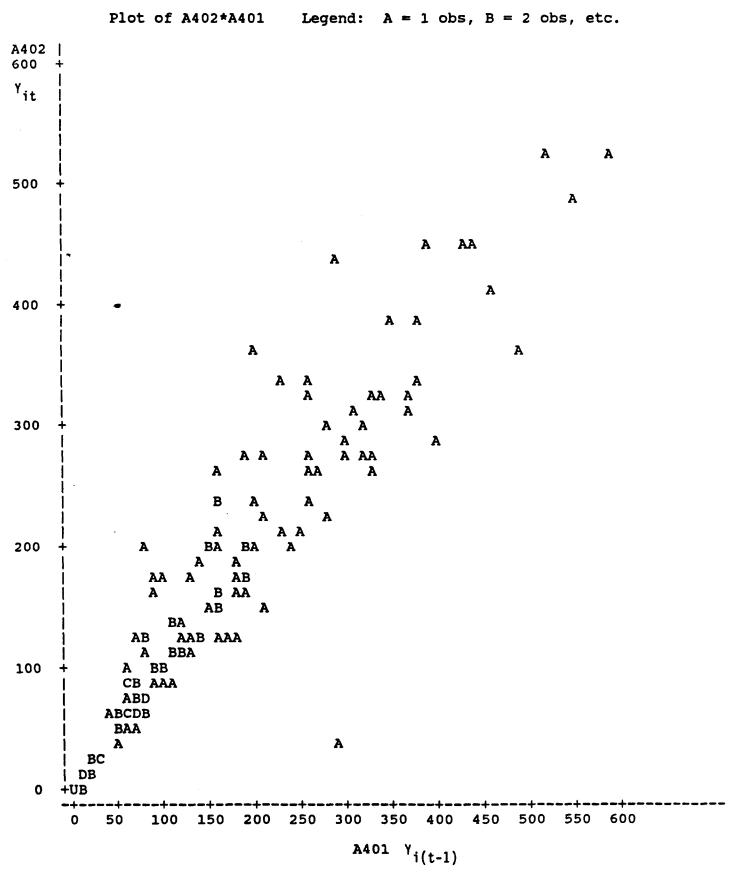


SURVEY 2324 AND ITEM 13013









FLOUR MANUFACTURED - ITEM 2120

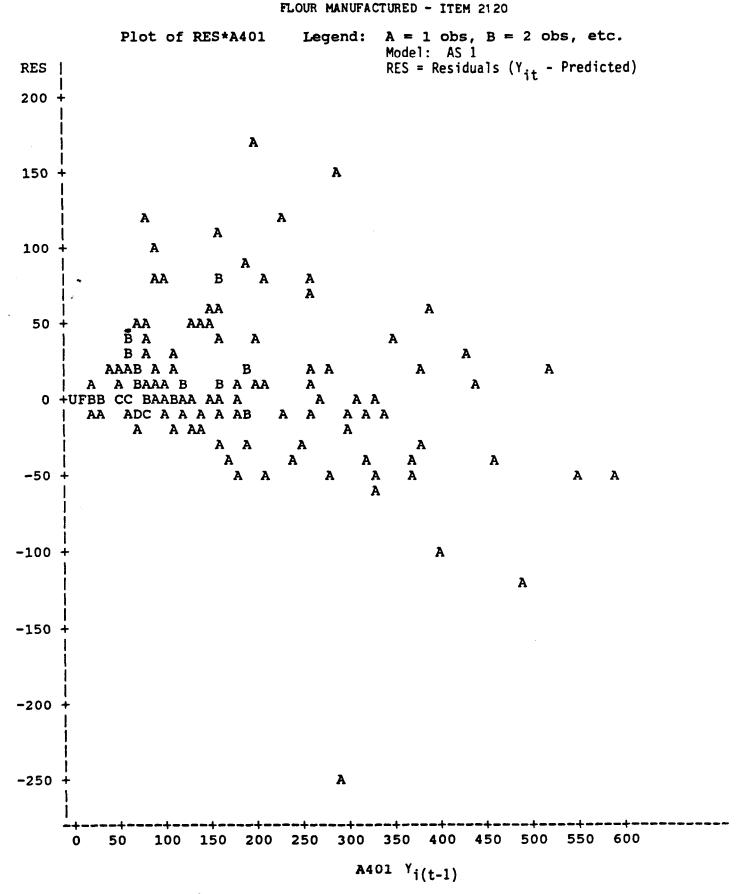


FIGURE 3.15 RESIDUAL PLOT FOR MONTHLY SURVEY 2001 - FEBRUARY, 1984

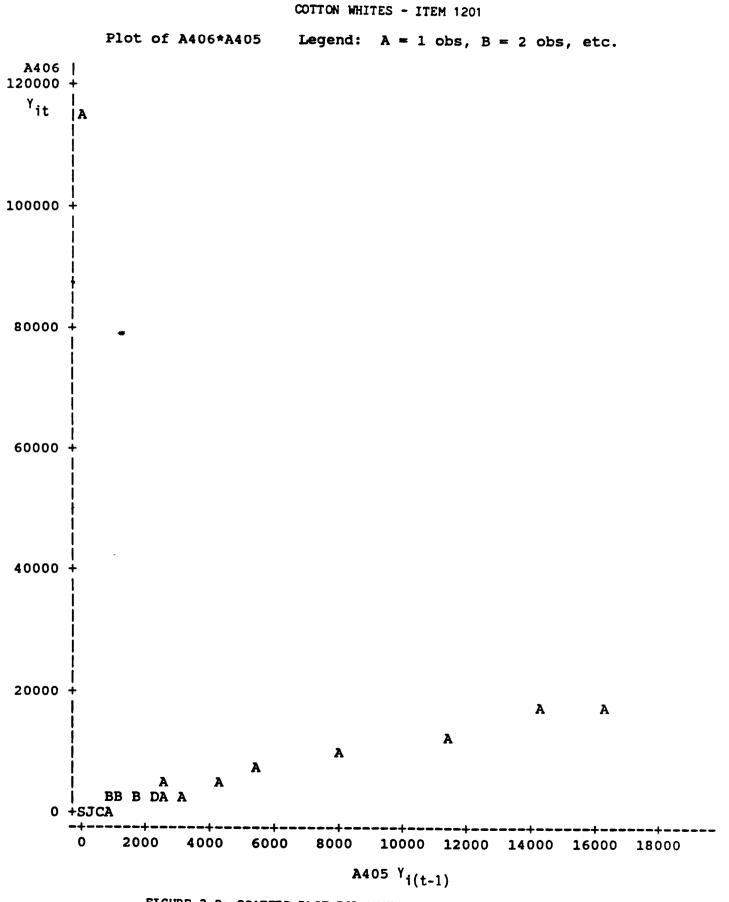


FIGURE 3.2a SCATTER PLOT FOR MONTHLY SURVEY 2202 - JUNE, 1984

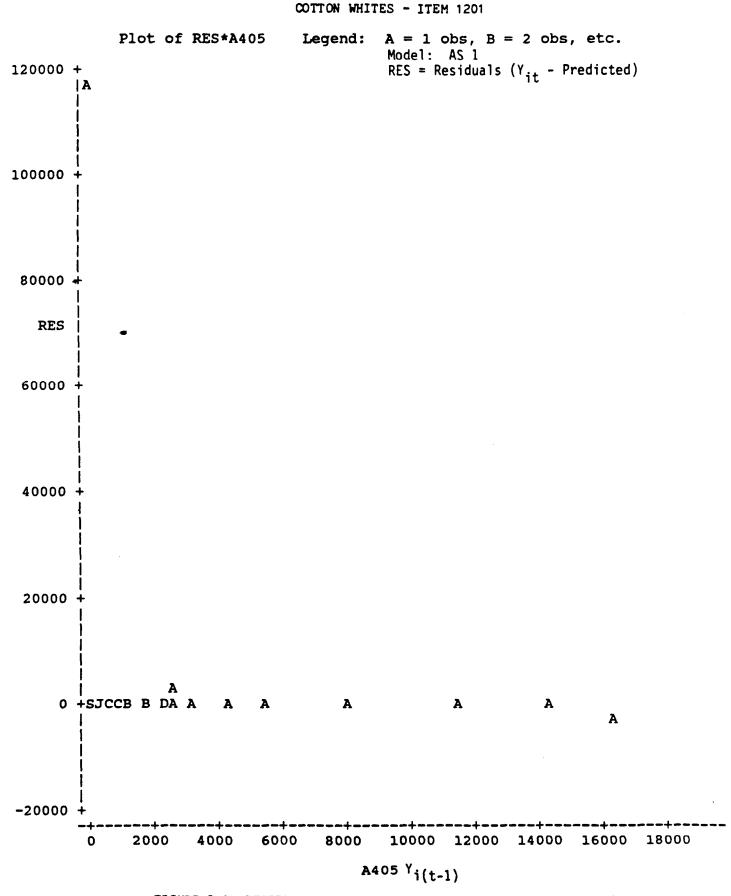
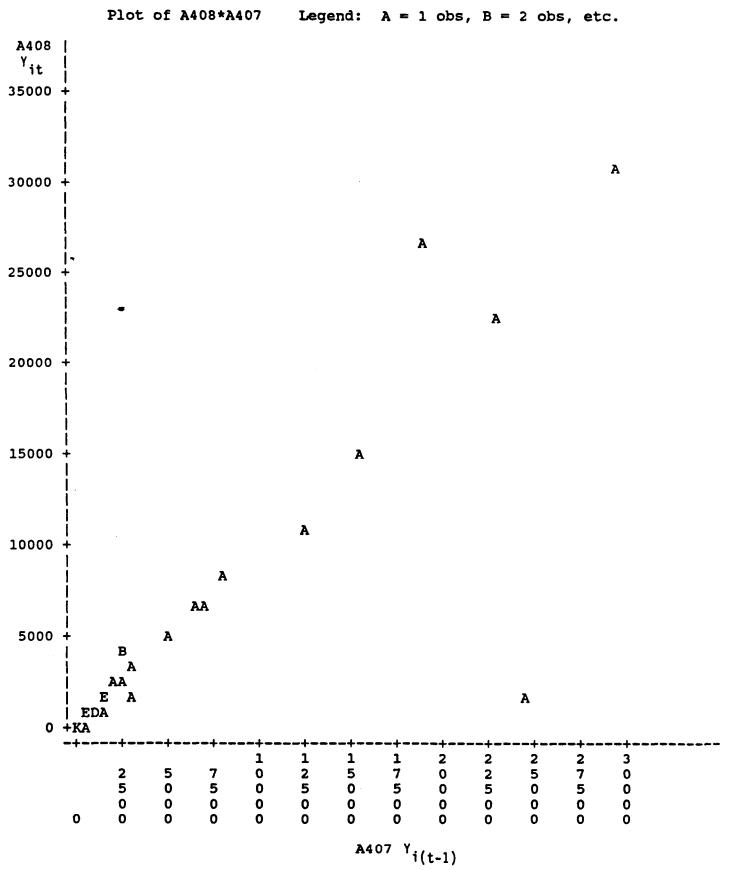


FIGURE 3.25 RESIDUAL PLOT FOR MONTHLY SURVEY 2202 - JUNE, 1984



ARCHITECTURAL COATINGS - ITEM 2002

FIGURE 3.3a SCATTER PLOT FOR MONTHLY SURVEY 2806 - AUGUST, 1984

ARCHITECTURAL COATINGS - ITEM 2002

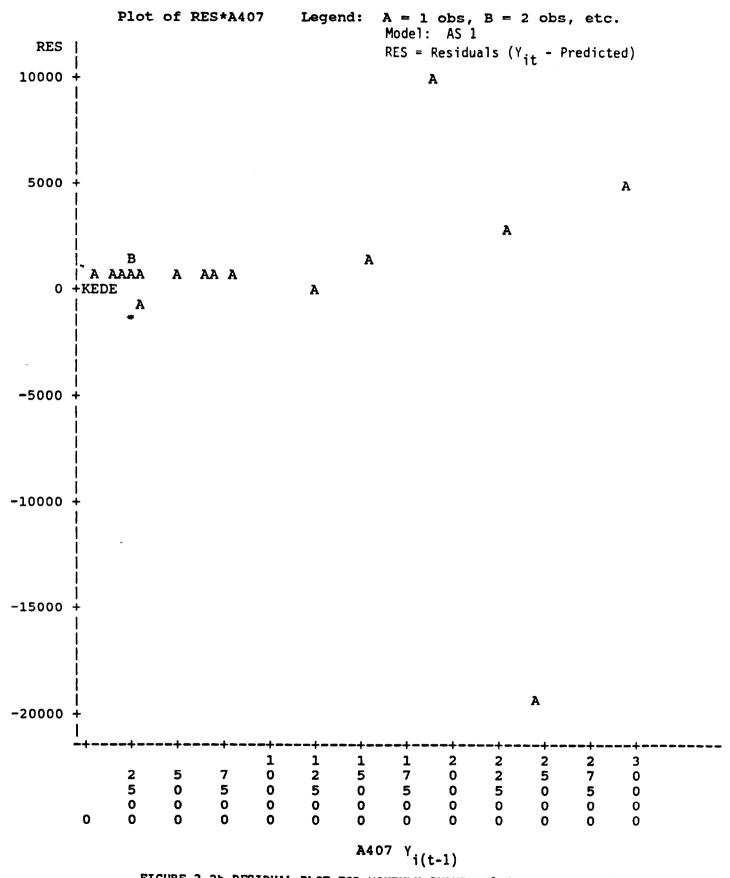
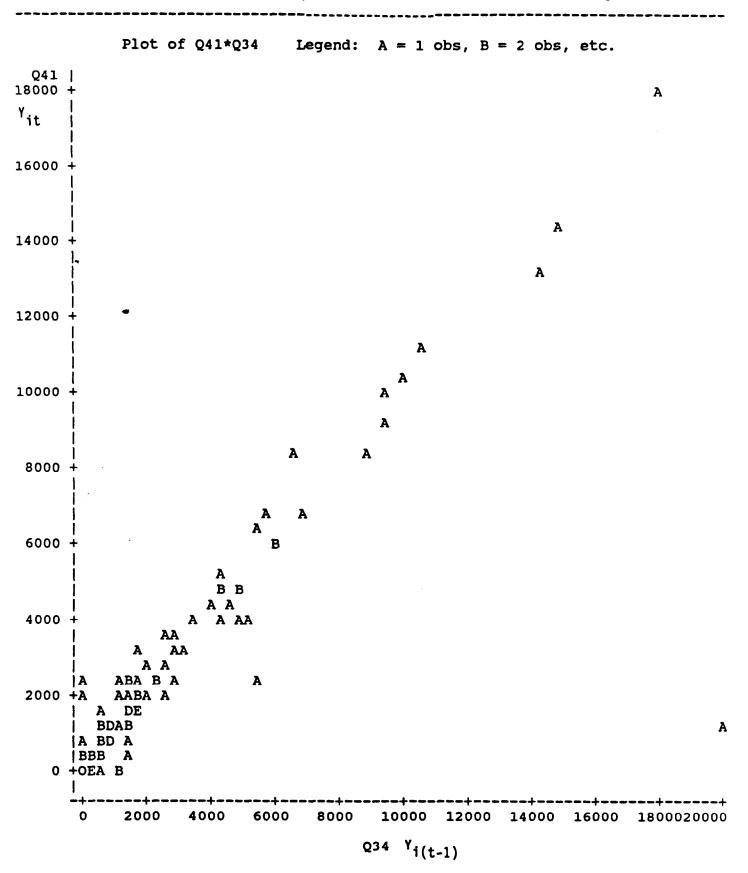


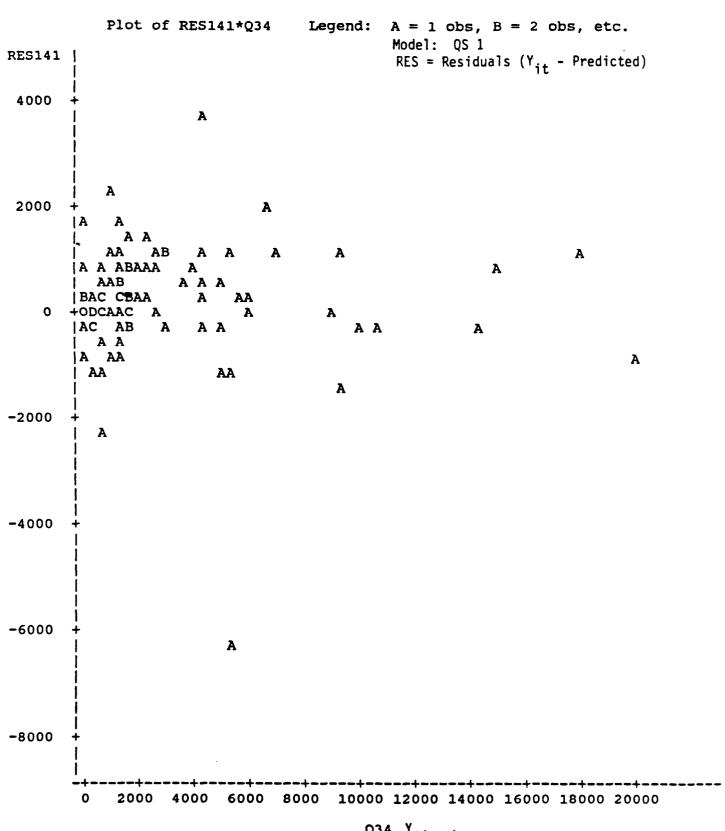
FIGURE 3.3D RESIDUAL PLOT FOR MONTHLY SURVEY 2806 - AUGUST, 1984



SHEETS, PILLOWCASES, AND TOWELS - TOTAL PRODUCTION - ITEM 13011

FIGURE 4.1a SCATTER PLOT FOR QUARTERLY SURVEY 2324 - QUARTER 1, 1984

SHEETS, PILLOWCASES, AND TOWELS - TOTAL PRODUCTION - ITEM 13011



Q34 ^Yi(t-1)

FIGURE 4.1b RESIDUAL PLOT FOR QUARTERLY SURVEY 2324 - QUARTER 1, 1984

Plot of Q41*Q31 Legend: A = 1 obs, B = 2 obs, etc. Q41 | 18000 + Α ^Yit 16000 + A 14000 + A 12000 + Α А 10000 + A A A A 8000 + A A A 6000 ÷ В Α A Α Α Α AA 4000 + С A AA ΑB A A AAA AAAA A A 2000 + ABBB A BCBA A A AAB B B A AACC |CCA 0 +NDBBA I 2000 0 4000 6000 8000 10000 12000 14000 16000 18000 Q31 Y_{i(t-1)}

FIGURE 4.2a SCATTER PLOT FOR QUARTERLY SURVEY 2220 - QUARTER 1, 1984

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BROADWOVEN FABRICS - ITEM 13011

BROADWOVEN FABRICS - ITEM 13011

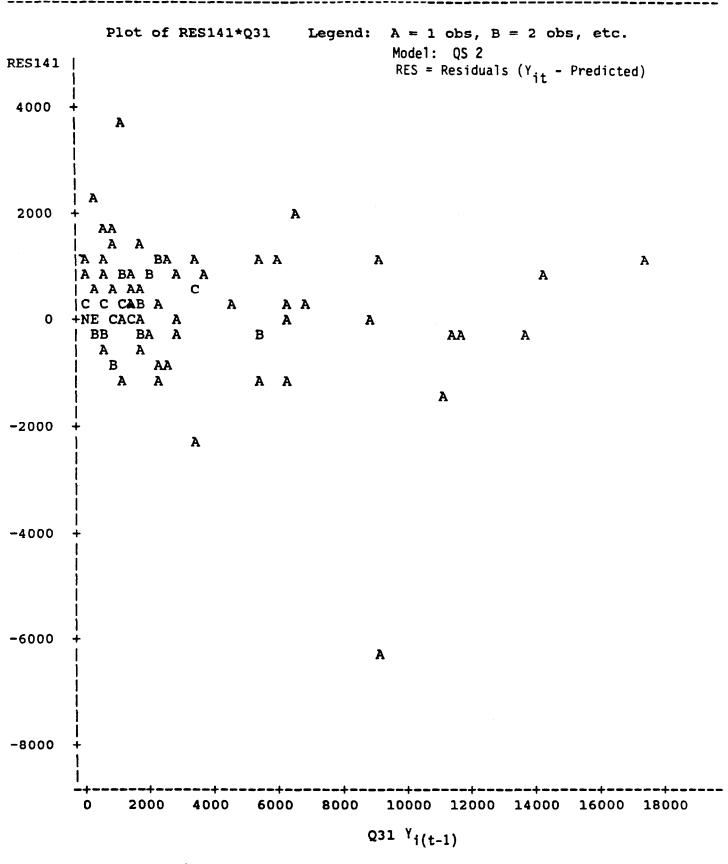
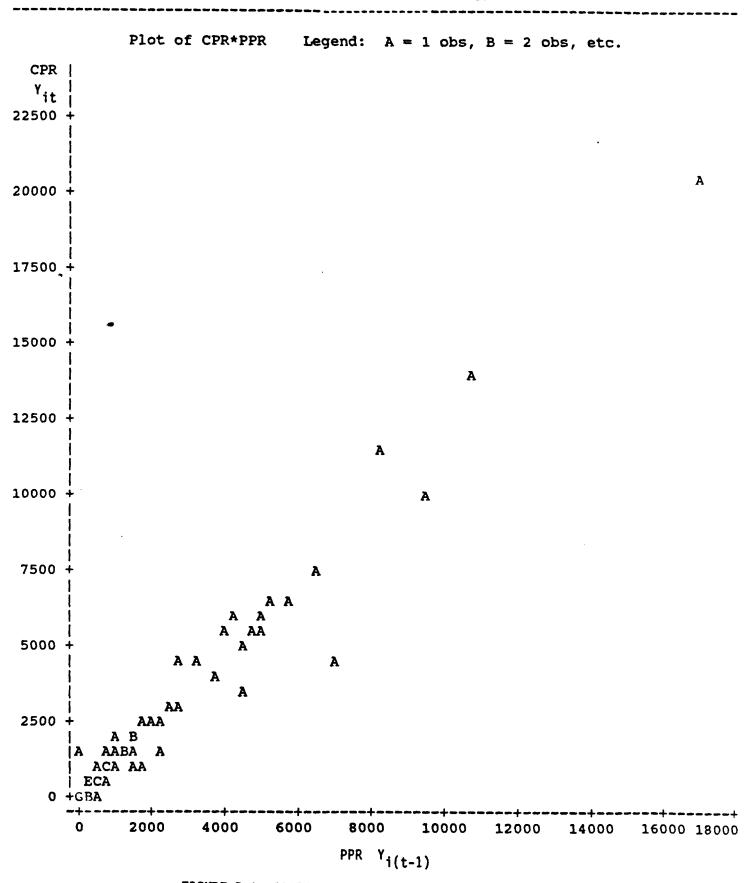
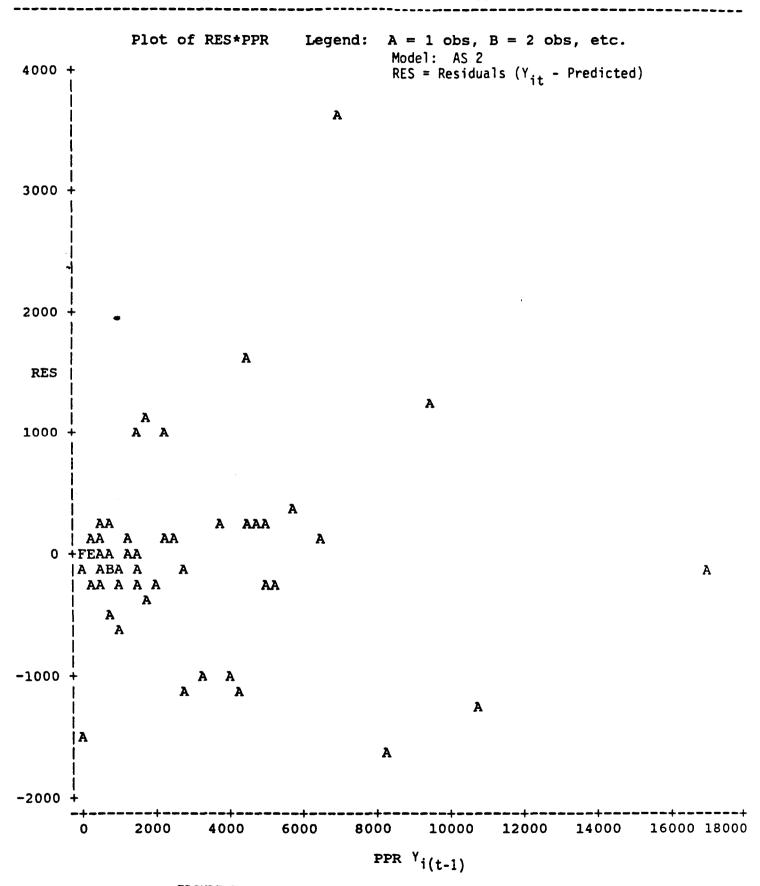


FIGURE 4.2b RESIDUAL PLOT FOR QUARTERLY SURVEY 2220 - QUARTER 1, 1984



GLOVES AND MITTENS - ITEM 33210

FIGURE 5.1a SCATTER PLOT FOR ANNUAL SURVEY 2304 - 1984



GLOVES AND MITTENS - ITEM 33210

INDUSTRIAL GASES - ITEM 44142 Plot of CPR*PPR Legend: A = 1 obs, B = 2 obs, etc. 4000000 + Α 35000000 + 30000000 + 25000000 + CPR Υ_{it} 20000000 + A A A 15000000 + A 10000000 + λÀ A А AA А 5000000 AAA AAA CBC A AB | NEA 0 +ND A -+-2000000 3000000 0 10000000 4000000 PPR Y i(t-1)

.

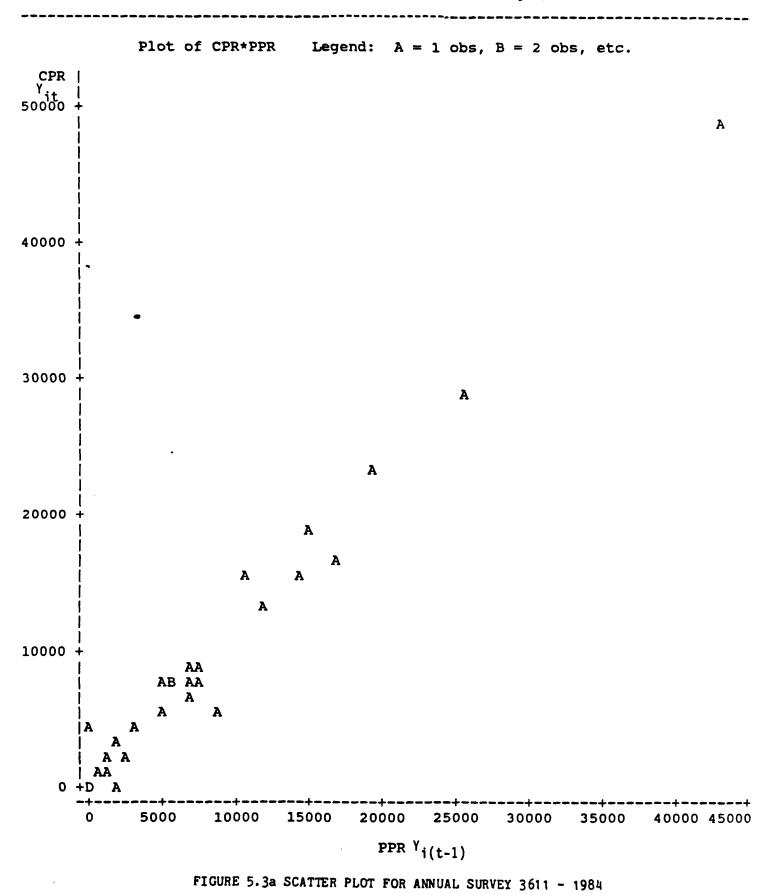
89

FIGURE 5.2a SCATTER PLOT FOR ANNUAL SURVEY 2802 - 1984

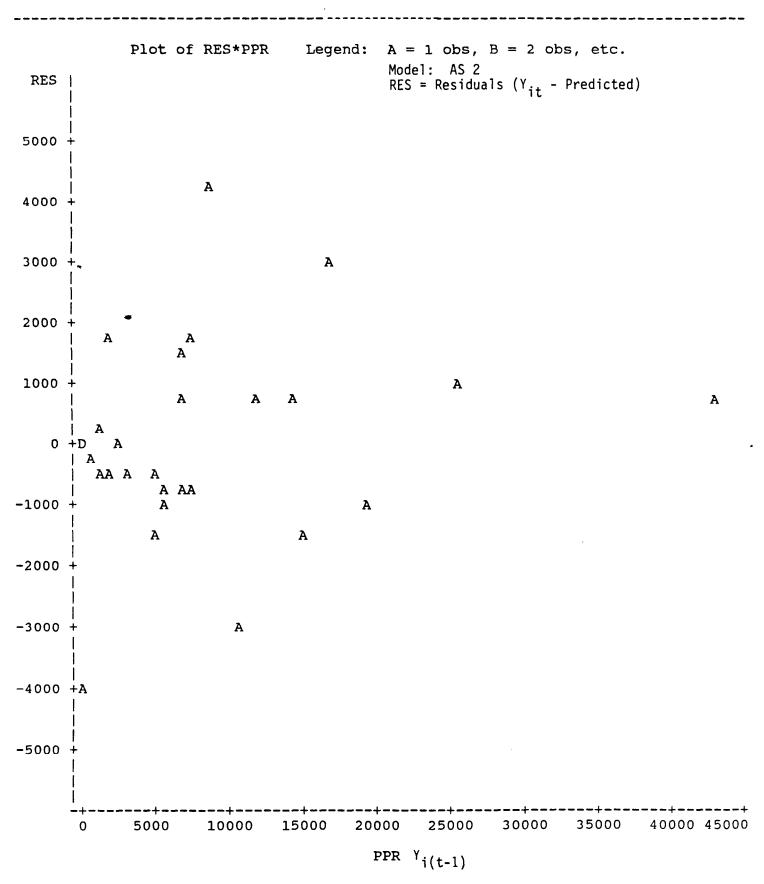
Plot of RES*PPR A = 1 obs, B = 2 obs, etc. Legend: Model: AS 1 RES | RES = Residuals (Y_{it} - Predicted) 7500000 + Α Α 5000000 + Α 2500000 А Ā В 0 +NQE Α AA ААСВАА АА А Α A A В A A AA -2500000 + Α -5000000 + A A -7500000 + -10000000 +-12500000 +A -15000000 2000000 3000000 4000000 20000000 0 10000000 PPR $\gamma_{i(t-1)}$

INDUSTRIAL GASES - ITEM 44142

FIGURE 5.2b RESIDUAL PLOT FOR ANNUAL SURVEY 2802 - 1984



WIRING DEVICES AND SUPPLIES - ITEM 31291



WIRING DEVICES AND SUPPLIES - ITEM 31291

FIGURE 5.3b RESIDUAL PLOT FOR ANNUAL SURVEY 3611 - 1984