

# Using MIMIC Models to Assess the Influence of Differential Item Functioning

# John A. Fleishman, Ph.D. AHRQ



#### Demographic Differences in Health

- Older persons have lower physical health than younger persons.
- Mental health does not decline with age, and may even rise.
- Women report lower physical and mental health than men.
- Persons with more education report better physical health than those with less.
- Blacks report higher mental health than Whites or Hispanics.

#### Demographic Differences in Health

To what extent do these observed differences reflect "true" group differences in underlying physical or mental health status, versus DIF??

#### Measurement Invariance

- Valid comparisons of different groups require that measures be invariant.
- Measures can be construed as reflecting a latent variable (e.g., mental health).
- Invariant item has identical relationship with latent variable in all groups.
- If relationship between item and latent variable varies across groups, DIF is present.

# Unadjusted vs. Adjusted Group Differences

- Unadjusted comparisons of group means may, in part, reflect DIF.
- They may also reflect true differences between groups.
- Control for any DIF effects when comparing groups (i.e., "adjust for" DIF).
- Multiple-indicator multiple-cause (MIMIC) model as one method of adjustment.

#### **SF-12**

- Health-related quality of life is an important outcome variable in many studies.
- SF-12 is an established, reliable, validated measure of health status.
- Twelve items, conceptualized as measuring two aspects of health status
  - Physical health
  - Mental health

#### **Data**

- Medical Expenditure Panel Survey in 2000
- Nationally representative sample
- Adult respondents (>17) received selfadministered questionnaire (SAQ).
- SF-12 included in SAQ.
- Response rate among eligibles: 93.5%
- Size of analytic sample: 11,682 persons

## DIF Adjustment Strategies

- Examine individual items for DIF.
- Discard or revise items with DIF.
- Examine revised measure.

- Requires large pool of candidate items.
- Requires resources and opportunity to develop measures.

#### **Constraints**

- Opportunity to develop measures may be limited.
- Secondary analysis of existing data.
- Use of established measure limits options to discard or revise items.
  - Non-comparability with prior studies
  - Alters content validity of measure

## **Modeling Strategy**

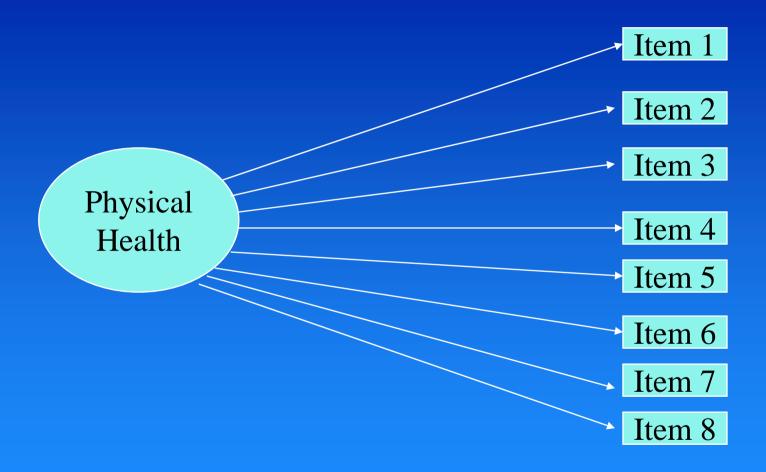
- Develop statistical model that controls for the influence of DIF.
- Decompose unadjusted group difference into
  - Group difference in latent variable means
  - DIF effect
- Incorporate parameters representing DIF in model.

#### **MIMIC Model**

- Assume underlying characteristic ("latent variable") that cannot be measured directly.
- $\blacksquare$  This is theta ( $\theta$ ) in IRT.
- Latent variable is measured indirectly, through its influence on multiple observed indicators.
- MIMIC model is confirmatory factor analysis with covariates.

### **Basic Factor Model**

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#### **CFA and IRT**

- Under certain conditions, CFA model is equivalent to IRT model.
  - Factor represents latent trait.
  - Arrows represent influence of (latent) factor on observed questionnaire items (factor loading).
  - Loading of item on factor corresponds to IRT discrimination parameter.
  - Item intercept corresponds to IRT difficulty parameter.

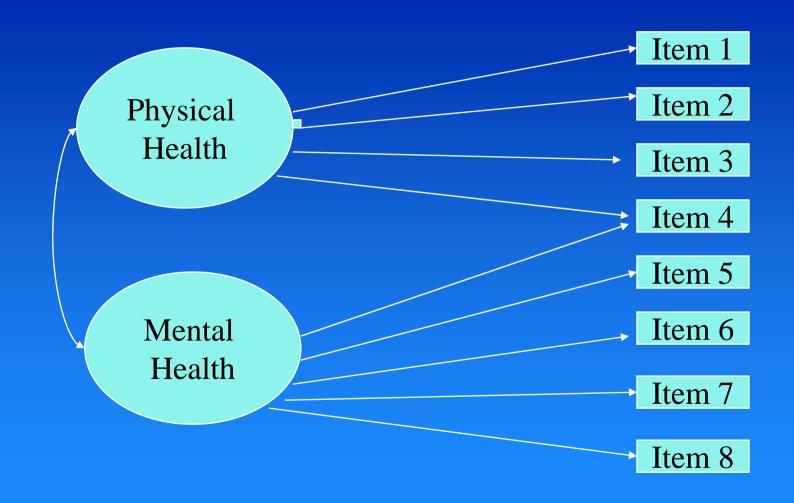


#### **CFA and IRT**

- Although multidimensional IRT models have been developed, they are rarely used in practice.
- Adding more latent dimensions (factors) is straightforward in CFA/MIMIC approach.



### **CFA Model with Two Factors**



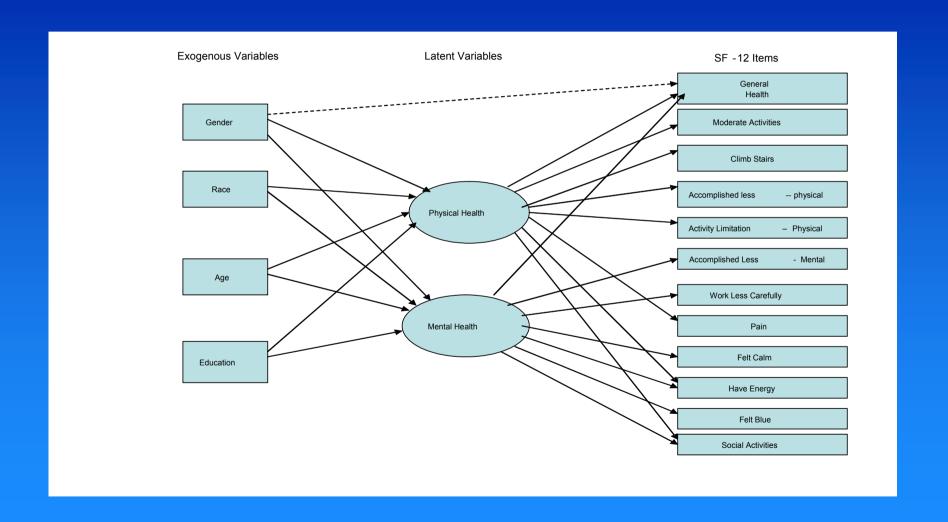
#### **MIMIC Model**

- MIMIC model adds covariates to CFA model.
- Demographic differences in mean levels of latent factors represented by arrows from demographic variable to factor.
- Demographic differences in observed variables are mediated through latent factors (indirect effect).

#### **MIMIC Model**

- A demographic variable can also affect an observed item directly – unmediated by latent factors.
- This is a DIF effect.
- Examine DIF by adding direct effect parameters from demographic variables to items.

### Full MIMIC Model



### **Analyses**

- SF-12 scoring algorithm yields two summary scores: PCS and MCS.
  - Derived from principal component analysis
  - Does not involve latent variable model
- Regressed PCS and MCS on demographic variables.
- Estimated and compared 2 MIMIC models:
  - One had no DIF effects
  - Other had significant DIF effects.

#### Mean PCS and MCS by Demographic Variables

<u>Variable</u>	PCS	MCS
Female	49.35	50.69
Male	50.83	52.28
White	49.87	51.43
Black	50.25	51.62
Hispanic	50.42	50.88
Other race	51.63	51.82
Age 18-39	52.78	51.07
Age 40-59	49.76	51.16
Age 60-69	46.08	53.00
Age 70+	41.24	52.54
Less than high school	47.03	49.67
High school degree	49.27	51.46
College	51.48	51.95

# Regressions of PCS and MCS on Demographic Variables

	PCS	MCS
Male	1.36 (.19)***	1.58 (.15)***
Black	0.01 (.30)	0.68 (.34)*
Hispanic	0.05 (.25)	0.23 (.33)
Other race	0.39 (.52)	0.56 (.74)
Age 40-59	- 3.24 (.19)***	-0.04 (.21)*
Age 60-69	- 6.62 (.37)***	2.00 (.35)***
Age 70+	-11.01 (.43)***	1.92 (.41)***
No high school degree	- 3.75 (.29)***	-2.56 (.30)***
High school degree	- 1.90 (.21)***	-0.57 (.22)*

# Effects of Demographic Variables on Physical and Mental Health: No-DIF Model

	Physical Factor	Mental Factor
Male	0.205 (.022)*	0.186 (.018)*
Black	0.020 (.034)	0.114 (.027)*
Hispanic	0.008 (.030)	0.082 (.024)
Other race	0.072 (.068)	0.108 (.054)
Age 40-59	-0.407 (.025)*	-0.034 (.020)
Age 60-69	-0.710 (.039)*	0.099 (.032)
Age 70+	-1.062 (.039)*	0.001 (.032)
No high school degree	-0.459 (.030)*	-0.224 (.024)*
High school degree	-0.238 (.025)*	-0.059 (.021)

# Goodness-of-Fit of No-DIF and DIF Models

	No DIF	DIF
Chi-square	3676.98	1845.699
DfF	135	96
CFI	0.989	0.994
RMSEA	0.047	0.039

# Effects of Demographic Variables on Physical Health in No-DIF and DIF Models

Variable	No DIF	DIF .
Male	0.205 (.022)*	0.193 (.023)*
Black	0.020 (.034)	0.079 (.034)
Hispanic	0.008 (.030)	0.025 (.032)
Other race	0.072 (.068)	0.073 (.068)
Age 40-59	-0.407 (.025)*	-0.348 (.026)*
Age 60-69	-0.710 (.039)*	-0.654 (.039)*
Age 70+	-1.062 (.039)*	-1.048 (.046)*
No high school degree	-0.459 (.030)*	-0.350 (.031)*
High school degree	-0.238 (.025)*	-0.158 (.028)*

# Effects of Demographic Variables on Mental Health in No-DIF and DIF Models

Variable	No DIF	DIF
Male	0.186 (.018)*	0.181(.019)*
Black	0.114 (.027)*	0.056 (.029)
Hispanic	0.082 (.024)	-0.037 (.027)
Other race	0.108 (.054)	0.108 (.054)
Age 40-59	-0.034 (.020)	-0.064 (.022)
Age 60-69	0.099 (.032)	-0.111 (.040)
Age 70+	0.001 (.032)	-0.279(.040)*
No high school degree	-0.224 (.024)*	-0.237(.026)*
High school degree	-0.059 (.021)	-0.077 (.022)

# **Summary of DIF Influence**

- DIF has minimal influence on estimates of demographic differences in physical health.
- Gender and educational differences in mental health relatively unaffected by DIF.
- Adjusting for DIF, oldest age group is lower on mental health
- Adjusting for DIF, Blacks do not differ from whites on mental health.

# **Major DIF Effects**

SF-12 Item	Male	Age 40-59	Age 60-69	Age 70+	Black
<b>General health</b>	-0.076*	-0.084*		-0.004	-0.165*
Moderate		-0.121*	-0.186*	-0.197*	-0.128*
Climbing	0.111*	-0.173*	-0.245*	-0.278*	
Pain				0.278*	
Accomp. less -					
emotional			-0.021	-0.093	
Calm		0.062	0.335*	0.546*	0.242*
Downhearted			0.276*	0.445*	
Energy	0.073*		0.228*	0.235*	
Social		0.106*	0.329*	0.470*	

# **Major DIF Effects**

SF-12 Item	Hispanic	Other race	Education < 12	High school
General health	1 -0.175*		-0.303*	-0.221*
Moderate			-0.167*	
Climbing			-0.166*	-0.117*
Pain				-0.089*
Accomp less -				
emotional			-0.117	
Calm	0.314*		0.129*	0.082*
Downhearted				
Energy	0.281*			
Social				

## **Advantages of MIMIC Model**

- Analyses can proceed without deleting items with DIF.
- DIF detection can be embedded in larger, substantively focused model.
- Incorporates multiple groups easily.
- Can incorporate multiple latent variables simultaneously.



## Disadvantages of MIMIC Model

- Assumes that DIF is uniform (i.e., no interaction between factor loadings and exogenous variables).
- Not oriented to producing a DIF-free score for each individual.
- Technical details of estimation differ from some IRT approaches.

