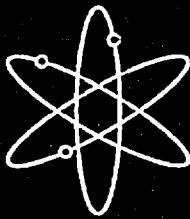
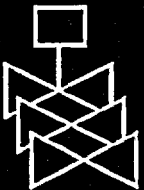


# **Handbook of Parameter Estimation for Probabilistic Risk Assessment**



**Sandia National Laboratories**



**U.S. Nuclear Regulatory Commission  
Office of Nuclear Regulatory Research  
Washington, DC 20555-0001**



## AVAILABILITY OF REFERENCE MATERIALS IN NRC PUBLICATIONS

### NRC Reference Material

As of November 1999, you may electronically access NUREG-series publications and other NRC records at NRC's Public Electronic Reading Room at <http://www.nrc.gov/reading-rm.html>. Publicly released records include, to name a few, NUREG-series publications; *Federal Register* notices; applicant, licensee, and vendor documents and correspondence; NRC correspondence and internal memoranda; bulletins and information notices; inspection and investigative reports; licensee event reports; and Commission papers and their attachments.

NRC publications in the NUREG series, NRC regulations, and *Title 10, Energy*, in the Code of *Federal Regulations* may also be purchased from one of these two sources.

1. The Superintendent of Documents  
U.S. Government Printing Office  
Mail Stop SSOP  
Washington, DC 20402-0001  
Internet: [bookstore.gpo.gov](http://bookstore.gpo.gov)  
Telephone: 202-512-1800  
Fax: 202-512-2250
2. The National Technical Information Service  
Springfield, VA 22161-0002  
[www.ntis.gov](http://www.ntis.gov)  
1-800-553-6847 or, locally, 703-605-6000

A single copy of each NRC draft report for comment is available free, to the extent of supply, upon written request as follows:

Address: Office of the Chief Information Officer,  
Reproduction and Distribution  
Services Section  
U.S. Nuclear Regulatory Commission  
Washington, DC 20555-0001

E-mail: [DISTRIBUTION@nrc.gov](mailto:DISTRIBUTION@nrc.gov)  
Facsimile: 301-415-2289

Some publications in the NUREG series that are posted at NRC's Web site address <http://www.nrc.gov/reading-rm/doc-collections/nuregs> are updated periodically and may differ from the last printed version. Although references to material found on a Web site bear the date the material was accessed, the material available on the date cited may subsequently be removed from the site.

### Non-NRC Reference Material

Documents available from public and special technical libraries include all open literature items, such as books, journal articles, and transactions, *Federal Register* notices, Federal and State legislation, and congressional reports. Such documents as theses, dissertations, foreign reports and translations, and non-NRC conference proceedings may be purchased from their sponsoring organization.

Copies of industry codes and standards used in a substantive manner in the NRC regulatory process are maintained at—

The NRC Technical Library  
Two White Flint North  
11545 Rockville Pike  
Rockville, MD 20852-2738

These standards are available in the library for reference use by the public. Codes and standards are usually copyrighted and may be purchased from the originating organization or, if they are American National Standards, from—

American National Standards Institute  
11 West 42<sup>nd</sup> Street  
New York, NY 10036-8002  
[www.ansi.org](http://www.ansi.org)  
212-642-4900

Legally binding regulatory requirements are stated only in laws; NRC regulations; licenses, including technical specifications; or orders, not in NUREG-series publications. The views expressed in contractor-prepared publications in this series are not necessarily those of the NRC.

The NUREG series comprises (1) technical and administrative reports and books prepared by the staff (NUREG-XXXX) or agency contractors (NUREG/CR-XXXX), (2) proceedings of conferences (NUREG/CP-XXXX), (3) reports resulting from international agreements (NUREG/IA-XXXX), (4) brochures (NUREG/BR-XXXX), and (5) compilations of legal decisions and orders of the Commission and Atomic and Safety Licensing Boards and of Directors' decisions under Section 2.206 of NRC's regulations (NUREG-0750).

**DISCLAIMER:** This report was prepared as an account of work sponsored by an agency of the U.S. Government. Neither the U.S. Government nor any agency thereof, nor any employee, makes any warranty, expressed or implied, or assumes any legal liability or responsibility for any third party's use, or the results of such use, of any information, apparatus, product, or process disclosed in this publication, or represents that its use by such third party would not infringe privately owned rights.

# Handbook of Parameter Estimation for Probabilistic Risk Assessment

---

---

Manuscript Completed: November 2002  
Date Published: September 2003

Prepared by  
C.L. Atwood<sup>1</sup>, J.L. LaChance<sup>2</sup>, H.F. Martz<sup>3</sup>,  
D.J. Anderson<sup>2</sup>, M. Englehardt<sup>4</sup>, D. Whitehead<sup>2</sup>,  
T. Wheeler<sup>2</sup>

<sup>2</sup>Sandia National Laboratories  
Albuquerque, NM 87185-0748

<sup>1</sup>Statwood Consulting  
Silver Spring, MD 20910

<sup>3</sup>Los Alamos National Laboratory  
Los Alamos, NM 87545

<sup>4</sup>Formerly with Idaho National Engineering and Environmental Laboratory  
Idaho Falls, ID 83415

A.D. Salomon, NRC Technical Monitor

Prepared for  
Division of Risk Analysis and Applications  
Office of Nuclear Regulatory Research  
U.S. Nuclear Regulatory Commission  
Washington, DC 20555-0001  
NRC Job Code W6970



## ABSTRACT

Probabilistic risk assessment (PRA) is a mature technology that can provide a quantitative assessment of the risk from accidents in nuclear power plants. It involves the development of models that delineate the response of systems and operators to accident initiating events. Additional models are generated to identify the component failure modes required to cause the accident mitigating systems to fail. Each component failure mode is represented as an individual "basic event" in the systems models. Estimates of risk are obtained by propagating the uncertainty distributions for each of the parameters through the PRA models.

The data analysis portion of a nuclear power plant PRA provides estimates of the parameters used to determine the frequencies and probabilities of the various events modeled in a PRA. This handbook provides guidance on sources of information and methods for estimating the parameters used in PRA models and for quantifying the uncertainties in the estimates. This includes determination of both plant-specific and generic estimates for initiating event frequencies, component failure rates and unavailabilities, and equipment non-recovery probabilities.

# Table of Contents

ABSTRACT .....	iii
LIST OF FIGURES .....	xiv
LIST OF TABLES .....	xviii
LIST OF EXAMPLES .....	xix
FOREWORD .....	xxi
ACKNOWLEDGEMENTS .....	xxii
ABBREVIATIONS .....	xxiii
<b>1. INTRODUCTION .....</b>	<b>1-1</b>
1.1 Objective .....	1-1
1.2 Background .....	1-1
1.3 Scope .....	1-1
1.4 Contents of the Handbook .....	1-2
1.4.1 Identification of Probability Models .....	1-2
1.4.2 Collection of Plant Specific Data .....	1-2
1.4.3 Quantification of Probability Model Parameters .....	1-3
1.4.3.1 Parameter Estimation from Plant-Specific Data .....	1-3
1.4.3.2 Parameter Estimation from Existing Data Bases .....	1-3
1.4.4 Advanced Methods .....	1-3
1.4.4.1 Analyzing Data for Trends and Aging .....	1-3
1.4.4.2 Parameter Estimation Using Data from Different Sources .....	1-3
1.5 How to Use This Handbook .....	1-3
<b>2. BASIC EVENT PROBABILITY MODELS .....</b>	<b>2-1</b>
2.1 Overview .....	2-1
2.2 Initiating Events .....	2-2
2.2.1 Examples .....	2-2
2.2.2 Probability Model .....	2-4
2.2.3 Data Needed to Validate the Model and Estimate $\lambda$ .....	2-4
2.2.4 Case Studies: Validity of Model Assumptions in Examples .....	2-5
2.2.5 Discussion .....	2-6
2.2.5.1 More General Models .....	2-6
2.2.5.2 Non-randomness of $t$ .....	2-6
2.3 Failure to Change State .....	2-7
2.3.1 Examples .....	2-7
2.3.2 Failure on Demand .....	2-7
2.3.2.1 Probability Model .....	2-7
2.3.2.2 Data Needed to Validate the Model and Estimate $p$ .....	2-8
2.3.2.3 Case Studies: Validity of Model Assumptions in Examples .....	2-8
2.3.2.4 Discussion .....	2-9
2.3.2.4.1 More General Models .....	2-9
2.3.2.4.2 Non-randomness of $n$ .....	2-9
2.3.3 Standby Failure .....	2-10
2.3.3.1 Probability Model .....	2-10
2.3.3.1.1 Probability Model for the Data .....	2-10
2.3.3.1.2 Application of the Model to PRA .....	2-10
2.3.3.2 Data Needed to Validate the Model and Estimate $\lambda$ .....	2-11
2.3.3.3 Case Studies: Validity of Model Assumptions in Examples .....	2-11
2.3.4 Comparison of the Two Models for Failure to Change State .....	2-12
2.3.4.1 Ease of Estimation .....	2-12
2.3.4.2 Use in PRA Cut Sets .....	2-12

## Table of Contents

	2.3.4.3	Estimates Obtained .....	2-12
	2.3.4.4	A Model Involving Both Terms .....	2-13
	2.3.4.5	Choosing a Model .....	2-13
2.4		Failure to Run during Mission .....	2-13
	2.4.1	Examples .....	2-14
	2.4.2	Probability Model .....	2-14
	2.4.3	Data Needed to Validate the Model and Estimate $\lambda$ .....	2-15
	2.4.4	Case Studies: Validity of Model Assumptions in Examples .....	2-15
	2.4.5	Discussion .....	2-15
2.5		Recovery Times and Other Random Duration Times .....	2-15
	2.5.1	Examples .....	2-16
	2.5.2	Duration-Time Models .....	2-16
	2.5.3	Data Needed to Estimate Distribution of Durations and Validate Model .....	2-18
	2.5.4	Case Studies: Validity of Model Assumptions in the Examples .....	2-18
2.6		Unavailability .....	2-18
	2.6.1	Example .....	2-19
	2.6.2	Probability Model .....	2-19
	2.6.3	Data Needed to Validate the Model and Estimate $q$ .....	2-19
	2.6.4	Case Study: Validity of Model Assumptions in Example .....	2-20
3. COMPONENT FAILURE AND BOUNDARY DEFINITIONS .....			3-1
	3.1	Failure Definitions .....	3-1
	3.2	Component Boundary Definitions .....	3-1
	3.3	Failure Severity .....	3-1
4. DATA SOURCES .....			4-1
	4.1	Plant-Specific Data Sources .....	4-1
	4.1.1	Requirements on Data Sources .....	4-1
		4.1.1.1 Initiating Events .....	4-1
		4.1.1.2 Component Failures .....	4-1
		4.1.1.3 Recovery Events .....	4-2
	4.1.2	Data Sources .....	4-2
		4.1.2.1 Regulatory Reports .....	4-2
		4.1.2.2 Internal Plant Failure Reports .....	4-3
		4.1.2.3 Maintenance Records .....	4-3
		4.1.2.4 Plant Logs .....	4-4
		4.1.2.5 Component Exposure Data Sources .....	4-4
	4.1.3	Plant-Specific Data Bases .....	4-4
		4.1.3.1 Nuclear Plant Reliability Data System (NPRDS) .....	4-5
		4.1.3.1.1 Limitations in the Data Available from the NPRDS .....	4-5
		4.1.3.2 Equipment Performance and Information Exchange (EPIX) System .....	4-5
		4.1.3.3 Reliability and Availability Data System (RADS) .....	4-6
	4.2	Generic Data Sources .....	4-6
	4.2.1	NRC-Sponsored Generic Data Bases .....	4-6
		4.2.1.1 Current Data Bases .....	4-6
		4.2.1.1.1 Severe Accident Risks Study Generic Data Base (NUREG-1150) .....	4-6
		4.2.1.1.2 Evaluation of Loss of Offsite Power Events at Nuclear Power Plants: 1980 - 1996 .....	4-7
		4.2.1.1.3 Rates of Initiating Events at U.S. Nuclear Power Plants: 1987 - 1995 .....	4-8
		4.2.1.1.4 System Reliability Studies .....	4-8

4.2.1.1.5	Component Performance Studies .....	4-9
4.2.1.2	Historical Data Bases .....	4-9
4.2.2	DOE-Sponsored Generic Data Bases .....	4-9
4.2.2.1	Component External Leakage and Rupture Frequency Estimates .....	4-10
4.2.2.2	Generic Component Failure Data Base for Light Water and Liquid Sodium Reactor PRAs .....	4-10
4.2.3	Industry Data Bases .....	4-10
4.2.3.1	EQE, International .....	4-10
4.2.3.2	Science Applications International Corporation .....	4-11
4.2.3.3	Advanced Light Water Reactor Data Base .....	4-12
4.2.4	Foreign Sources .....	4-12
4.2.4.1	Sweden's T-Book for Nordic Nuclear Power Plants .....	4-12
4.2.4.2	Sweden's I-Book for Nordic Nuclear Power Plants .....	4-13
4.2.5	Non-Nuclear Power Data Bases .....	4-13
4.2.5.1	Reliability Analysis Center .....	4-13
4.2.5.2	Offshore Reliability Data Project .....	4-13
4.2.5.3	IEEE-500 .....	4-14
4.2.6	Selection of Parameter Estimates from Existing Data Bases .....	4-14
<b>5.</b>	<b>PLANT-SPECIFIC DATA COLLECTION AND INTERPRETATION .....</b>	<b>5-1</b>
5.1	Initiating Event Data .....	5-1
5.1.1	Initiating Event Categories .....	5-1
5.1.2	Data Window .....	5-1
5.1.3	Initiating Event Data Allocation and Screening .....	5-2
5.1.4	Selection of Exposure Time .....	5-2
5.2	Component Failure Data .....	5-3
5.2.1	Component Data Identification .....	5-3
5.2.1.1	Data Window .....	5-3
5.2.1.2	Data Collection .....	5-4
5.2.2	Event Screening and Severity Classification .....	5-4
5.2.2.1	Event Screening .....	5-4
5.2.2.2	Event Severity Classification .....	5-4
5.2.3	Component Data Allocation .....	5-5
5.2.3.1	Component Failure Event Allocation .....	5-5
5.2.3.2	Allocation of Unavailability Data .....	5-7
5.2.4	Component Exposure Evaluation .....	5-9
5.2.4.1	Time-Related Exposures .....	5-9
5.2.4.2	Demand-Related Exposures .....	5-10
5.2.4.2.1	Test Demands .....	5-10
5.2.4.2.2	Automatic and Manual Initiation .....	5-11
5.2.4.2.3	Corrective Maintenance .....	5-11
5.2.5	Determination of Unavailable Time .....	5-11
5.3	Recovery Event Data .....	5-12
5.3.1	Recovery Data Identification .....	5-12
5.3.2	Recovery Data Allocation .....	5-13
<b>6.</b>	<b>PARAMETER ESTIMATION AND MODEL VALIDATION .....</b>	<b>6-1</b>
6.1	Overview .....	6-1
6.1.1	Chapter Contents .....	6-1
6.1.2	Bayesian and Frequentist Inference .....	6-2
6.1.3	Uncertainties Other Than Parametric Uncertainty .....	6-3
6.1.3.1	Uncertainty from Nonrepresentativeness of the Data Sources .....	6-3

Table of Contents

	6.1.3.2	Uncertainty in the Data Counts Themselves	6-3
	6.1.3.3	Uncertainty in the Correct Model to Use	6-4
6.2	Initiating Events		6-4
	6.2.1	Frequentist or Classical Estimation	6-5
	6.2.1.1	Point Estimate	6-5
	6.2.1.2	Standard Deviation of the Estimator	6-5
	6.2.1.3	Confidence Interval for $\lambda$	6-6
	6.2.2	Bayesian Estimation	6-7
	6.2.2.1	Overview	6-7
	6.2.2.2	Choosing a Prior	6-8
	6.2.2.3	Estimation with a Discrete Prior	6-9
	6.2.2.4	Estimation with a Conjugate Prior	6-11
	6.2.2.4.1	Definitions	6-11
	6.2.2.4.2	Update Formulas	6-11
	6.2.2.5	Possible Conjugate Priors	6-12
	6.2.2.5.1	Informative Priors	6-12
	6.2.2.5.2	Noninformative Prior	6-14
	6.2.2.5.3	Constrained Noninformative Prior	6-15
	6.2.2.5.4	Example Comparisons Using Above Priors	6-15
	6.2.2.6	Estimation with a Continuous Nonconjugate Prior	6-16
	6.2.2.6.1	Direct Numerical Integration	6-16
	6.2.2.6.2	Simple Random Sampling	6-17
	6.2.2.6.3	More Complicated Random Sampling	6-17
	6.2.2.7	Examples Involving Nonconjugate Priors	6-18
	6.2.2.7.1	Example with Lognormal Prior	6-18
	6.2.2.7.2	Example with "Moment-Matching" Conjugate Prior	6-18
	6.2.2.7.3	Comparison of Example Analyses	6-19
	6.2.2.8	Analysis with Fixed Count and Random Time	6-20
6.2.3	Model Validation		6-20
	6.2.3.1	Poolability of Data Subsets	6-20
	6.2.3.1.1	Graphical Technique	6-21
	6.2.3.1.2	Statistical Test	6-22
	6.2.3.2	No Time Trend	6-25
	6.2.3.2.1	Graphical Techniques	6-25
	6.2.3.2.2	Statistical Tests for a Trend in $\lambda$	6-26
	6.2.3.3	No Multiple Failures	6-28
	6.2.3.4	Independence of Disjoint Time Periods	6-28
	6.2.3.4.1	Graphical Method	6-29
	6.2.3.4.2	Statistical Tests	6-30
	6.2.3.5	Consistency of Data and Prior	6-30
6.3	Failures to Change State:		
		Failure on Demand	6-31
6.3.1	Frequentist or Classical Estimation		6-31
	6.3.1.1	Point Estimate	6-31
	6.3.1.2	Standard Deviation of Estimator	6-32
	6.3.1.3	Confidence Interval for $p$	6-32
6.3.2	Bayesian Estimation		6-33
	6.3.2.1	Estimation with a Discrete Prior	6-33
	6.3.2.2	Estimation with a Conjugate Prior	6-35
	6.3.2.2.1	Definitions	6-35
	6.3.2.2.2	Update Formulas	6-36
	6.3.2.3	Possible Conjugate Priors	6-36



	6.3.2.3.1	Informative Prior .....	6-36
	6.3.2.3.2	Noninformative Prior .....	6-37
	6.3.2.3.3	Constrained Noninformative Prior .....	6-38
	6.3.2.3.4	Example Comparison of Above Methods .....	6-38
	6.3.2.4	Estimation with a Continuous Nonconjugate Prior .....	6-39
	6.3.2.4.1	Direct Numerical Integration .....	6-39
	6.3.2.4.2	Simple Random Sampling .....	6-39
	6.3.2.4.3	More Complicated Random Sampling .....	6-39
	6.3.2.5	Examples with Nonconjugate Priors .....	6-39
	6.3.2.5.1	Lognormal Distribution .....	6-40
	6.3.2.5.2	Logistic-Normal Distribution .....	6-40
	6.3.2.5.3	Exact Constrained Noninformative Distribution .....	6-40
	6.3.2.5.4	Maximum Entropy Prior .....	6-41
	6.3.2.5.5	Example Calculation .....	6-42
	6.3.2.6	Estimation with Fixed Number of Failures and Random Number of Demands .....	6-43
6.3.3		Model Validation .....	6-43
	6.3.3.1	Poolability of Data Sources .....	6-44
	6.3.3.1.1	Graphical Technique .....	6-44
	6.3.3.1.2	Statistical Tests .....	6-45
	6.3.3.2	No Time Trend .....	6-48
	6.3.3.2.1	Graphical Techniques .....	6-48
	6.3.3.2.2	Statistical Tests for a Trend in $p$ .....	6-49
	6.3.3.3	Independence of Outcomes .....	6-49
	6.3.3.4	Consistency of Data and Prior .....	6-50
6.4		Failure to Change State: Standby Failure .....	6-51
6.5		Failures to Run during Mission .....	6-52
	6.5.1	Estimates and Tests .....	6-52
	6.5.1.1	Likelihood-Based Methods: MLEs and Bayesian Methods .....	6-53
	6.5.1.2	Confidence Intervals .....	6-53
	6.5.1.3	Jeffreys Noninformative Prior .....	6-53
	6.5.1.4	Tests for Poolability .....	6-54
	6.5.2	Hazard Function Plot .....	6-54
6.6		Recovery Times and Other Random Duration Times .....	6-55
	6.6.1	Characterization of Distribution .....	6-56
	6.6.1.1	Nonparametric Description .....	6-56
	6.6.1.1.1	Moments .....	6-56
	6.6.1.1.2	Percentiles .....	6-57
	6.6.1.1.3	The Empirical Distribution Function .....	6-58
	6.6.1.1.4	Histogram Estimate of the Density .....	6-58
	6.6.1.2	Fitting a Parametric Distribution .....	6-59
	6.6.1.2.1	Lognormal Distribution .....	6-59
	6.6.1.2.2	Exponential Distribution .....	6-61
	6.6.1.2.3	Gamma Distribution .....	6-62
	6.6.1.2.4	Weibull Distribution .....	6-62
	6.6.2	Model Validation .....	6-63
	6.6.2.1	Poolability of Data Sources .....	6-63
	6.6.2.1.1	Graphical Methods .....	6-63
	6.6.2.1.2	Statistical Tests .....	6-65
	6.6.2.2	No Time Trend .....	6-66
	6.6.2.2.1	Graphical Methods .....	6-66
	6.6.2.2.2	Statistical Tests .....	6-67

Table of Contents

6.6.2.3	Goodness of Fit to Parametric Models	6-68
6.6.2.3.1	Graphical Methods	6-68
6.6.2.3.2	Statistical Tests	6-70
6.6.2.4	Consistency of Data with Prior in Bayesian Parametric Estimation	6-72
6.6.2.4.1	Exponential Durations	6-72
6.6.2.4.2	Distributions Having Two or More Parameters	6-73
6.6.3	Nonparametric Density Estimation	6-73
6.6.3.1	Smoothing Techniques and Kernel Estimators	6-73
6.6.3.1.1	The Rectangular Kernel	6-74
6.6.3.1.2	Boundary Problems	6-75
6.6.3.1.3	The Triangular Kernel	6-75
6.6.3.1.4	The Standard Normal Kernel	6-76
6.6.3.2	Choosing the Bandwidth	6-76
6.7	Unavailability	6-77
6.7.1	Analysis of Detailed Data	6-77
6.7.1.1	Frequentist Point Estimate	6-78
6.7.1.2	Bayesian Estimation under Simple Assumptions	6-78
6.7.1.3	Model Validation	6-80
6.7.1.4	Bayesian Estimation under Other Assumptions	6-80
6.7.2	Analysis of Summary Data	6-80
6.7.2.1	Data Aggregation	6-80
6.7.2.2	Frequentist Estimation	6-82
6.7.2.3	Bayesian Estimation	6-83
6.7.2.3.1	Noninformative Prior	6-83
6.7.2.3.2	Informative Priors	6-83
6.7.2.4	Model Validation	6-84
6.7.3	Comparison of the Analyses with the Two Types of Data	6-84
7.	TRENDS AND AGING	7-1
7.1	Overview	7-1
7.2	Binned Poisson Data	7-1
7.2.1	Examples	7-1
7.2.2	Model	7-2
7.2.2.1	General Model	7-2
7.2.2.2	Loglinear Model	7-3
7.2.2.3	Power-Law Model	7-4
7.2.3	Bayesian Estimation with Loglinear Model	7-4
7.2.4	Frequentist Estimation with Loglinear Model	7-6
7.2.4.1	Point Estimation	7-6
7.2.4.2	Confidence Intervals for $a$ and $b$	7-7
7.2.4.3	Test for Presence of Trend	7-7
7.2.4.4	Confidence Interval for $\lambda(t)$ at Fixed $t$	7-8
7.2.4.5	Simultaneous Confidence Band at All $t$	7-8
7.2.4.6	Alternative Using Least-Squares	7-9
7.2.5	Comparison of Methods	7-10
7.2.6	Model Validation	7-12
7.2.6.1	Graphical Check for Goodness of Fit	7-12
7.2.6.2	Statistical Test for Goodness of Fit	7-14
7.2.6.2.1	Test Based on Poisson Maximum Likelihood	7-14
7.2.6.2.2	Test Based on Weighted Least-Squares Fit	7-15
7.3	Unbinned Poisson Data	7-15
7.3.1	Bayesian Analysis	7-16

7.3.2	Frequentist Analysis	7-16
7.4	Binomial Data	7-16
7.4.1	Examples	7-16
7.4.2	Model	7-17
7.4.2.1	General Model	7-17
7.4.2.2	Logit Model	7-17
7.4.2.3	Loglinear Model	7-18
7.4.3	Bayesian Estimation with Logit Model	7-18
7.4.4	Frequentist Estimation with Logit Model	7-19
7.4.4.1	Point Estimation	7-19
7.4.4.2	Confidence Intervals for $a$ and $b$	7-19
7.4.4.3	Test for Presence of Trend	7-19
7.4.4.4	Confidence Intervals and Confidence Bands	7-20
7.4.4.5	Alternative Using Least-Squares Software	7-20
7.4.5	Comparison of Bayesian and Frequentist Estimation with Logit Model	7-22
7.4.6	Model Validation	7-22
7.4.6.1	Graphical Check for Goodness of Fit	7-22
7.4.6.2	Statistical Test for Goodness of Fit	7-23
7.4.6.2.1	Test Based on Binomial Maximum Likelihood	7-23
7.4.6.2.2	Test Based on Weighted Least-Squares Fit	7-23
7.5	Discussion	7-23
7.5.1	Generalized Linear Models	7-23
7.5.2	The Many Appearances of the Chi-Squared Test	7-24
7.5.3	Nonparametric Estimators of $\lambda(t)$	7-25
8.	PARAMETER ESTIMATION USING DATA FROM DIFFERENT SOURCES	8-1
8.1	The Hierarchical Model	8-1
8.2	The Parametric Empirical Bayes Method	8-3
8.2.1	General Approach	8-3
8.2.2	MLE Equations for the Gamma-Poisson Model	8-3
8.2.3	MLE Equations for the Beta-Binomial Model	8-4
8.2.4	Adjustment for Uncertainty in the Estimate of $g$	8-6
8.2.4.1	Equations for the Gamma-Poisson Case	8-6
8.2.4.2	Equations for the Beta-Binomial Case	8-7
8.2.5	Application to Examples	8-7
8.2.5.1	Example 8.1, Initiating Events	8-8
8.2.5.2	Example 8.2, AFW Segment Failures to Start	8-10
8.3	The Hierarchical Bayes Method	8-12
8.3.1	General Approach	8-12
8.3.2	Directed Graphs	8-13
8.3.3	Markov Chain Monte Carlo (MCMC) Simulation	8-13
8.3.3.1	Gibbs Sampling	8-14
8.3.3.2	Metropolis-Hastings Step	8-14
8.3.3.3	BUGS (Bayesian Inference Using Gibbs Sampling)	8-15
8.3.4	Application to Example 8.1, Initiating Events	8-15
8.3.4.1	Development of Hyperprior Distributions	8-15
8.3.4.2	Example Analysis	8-16
8.3.5	Application to Example 8.2, AFW Segment Failures to Start	8-16
8.3.5.1	Analysis with Beta Prior	8-17
8.3.5.2	Analysis with Logistic-Normal Prior	8-18
8.4	Discussion	8-20
8.4.1	Hierarchical Bayes Is Still Bayes	8-20

Table of Contents

8.4.2	The "Two-Stage" Bayesian Method .....	8-20
8.4.3	Lower Bounds on Parameters .....	8-20
8.4.4	Empirical Bayes as an Approximation to Hierarchical Bayes .....	8-21
9. REFERENCES .....		9-1
APPENDICES		
A. BASICS OF PROBABILITY .....		A-1
A.1	Events .....	A-1
A.2	Basic Probability Concepts .....	A-1
A.3	Basic Rules and Principles of Probability .....	A-2
A.4	Random Variables and Probability Distributions .....	A-5
A.4.1	Random Variables .....	A-5
A.4.2	Probability Distributions .....	A-5
A.4.3	Cumulative Distribution Functions .....	A-5
A.4.4	Reliability and Hazard Functions .....	A-6
A.4.4.1	Definitions .....	A-6
A.4.4.2	Relations among p.d.f., Reliability, and Hazard .....	A-7
A.4.5	Joint, Marginal, and Conditional Distributions .....	A-7
A.4.6	Characterizing Random Variables and Their Distributions .....	A-8
A.4.6.1	Distribution Characteristics .....	A-8
A.4.6.2	Mathematical Expectation .....	A-9
A.4.6.3	Moment-Generating Functions .....	A-10
A.4.6.4	Covariance and Correlation .....	A-10
A.4.7	Distribution of a Transformed Random Variable .....	A-11
A.5	Bayes' Theorem .....	A-11
A.6	Discrete Random Variables .....	A-12
A.6.1	The Binomial Distribution .....	A-12
A.6.2	The Poisson Distribution .....	A-13
A.7	Continuous Random Variables .....	A-14
A.7.1	The Uniform Distribution .....	A-14
A.7.2	The Normal Distribution .....	A-15
A.7.3	The Lognormal Distribution .....	A-16
A.7.4	The Exponential Distribution .....	A-17
A.7.5	The Weibull Distribution .....	A-18
A.7.6	The Gamma and Chi-Squared Distributions .....	A-18
A.7.7	The Inverted Gamma and Inverted Chi-Squared Distributions .....	A-20
A.7.8	The Beta Distribution .....	A-21
A.7.9	The Logistic-Normal Distribution .....	A-22
A.7.10	Student's $t$ Distribution .....	A-23
A.7.11	$F$ Distribution .....	A-23
A.7.12	Dirichlet Distribution .....	A-24
B. BASICS OF STATISTICS .....		B-1
B.1	Random Samples .....	B-1
B.2	Sample Moments .....	B-1
B.3	Statistical Inference .....	B-1
B.4	Frequentist Inference .....	B-2
B.4.1	Point Estimation .....	B-2
B.4.2	Interval Estimation .....	B-5
B.4.3	Hypothesis Testing .....	B-6

Table of Contents

	B.4.4	Goodness-of-Fit Tests .....	B-8
B.5		Bayesian Estimation .....	B-11
	B.5.1	Purpose and Use .....	B-11
	B.5.2	Point and Interval Estimates .....	B-11
	B.5.3	Prior Distributions .....	B-12
		B.5.3.1 Noninformative Prior Distributions .....	B-12
		B.5.3.2 Conjugate Prior Distributions .....	B-13
		B.5.3.3 Other Prior Distribution Approaches .....	B-14
C.		STATISTICAL TABLES .....	C-1
D.		GLOSSARY .....	D-1
INDEX		.....	I-1

## LIST OF FIGURES

<u>Figure</u>	<u>Page</u>
1.1	Relation of sections of this handbook. . . . . 1-5
2.1	Probability density function (p.d.f.) and cumulative distribution function (c.d.f.). . . . . 2-17
2.2	Uptime and downtime status for one system. . . . . 2-19
6.1	Schematic outline of Chapter 6. . . . . 6-1
6.2	Two possible analysis paths for uncertain data. . . . . 6-4
6.3	Likelihood as a function of $\lambda$ , for data of Example 6.1. . . . . 6-5
6.4	Confidence intervals from random data, all generated from the same process. . . . . 6-7
6.5	Prior distribution and posterior distributions corresponding to three hypothetical data sets. . . . . 6-8
6.6	Coarse discrete prior distribution for $\lambda$ . . . . . 6-10
6.7	Discrete posterior distribution of $\lambda$ based on 10 events in 6 years. . . . . 6-10
6.8	Discrete prior and posterior distributions plotted together. . . . . 6-10
6.9	Discrete prior and posterior distributions for 10 events in 6 years, with finely discretized prior. . . . . 6-10
6.10	Discrete prior and posterior distributions for 10 events in six years, with very finely discretized prior. . . . . 6-10
6.11	Prior density for $\lambda$ , gamma(1.53, 10.63). . . . . 6-13
6.12	Posterior density of $\lambda$ , gamma(2.53, 15.52), for Example 6.1 with industry prior. The 5th and 95th percentiles are shown. . . . . 6-13
6.13	Posterior cumulative distribution of $\lambda$ for Example 6.1 with industry prior. The 5th and 95th percentiles are shown. . . . . 6-13
6.14	Jeffreys noninformative prior distribution for an event frequency. . . . . 6-14
6.15	Comparison of four point estimates and interval estimates for $\lambda$ . . . . . 6-16
6.16	Script for analyzing Example 6.3 using BUGS. . . . . 6-18
6.17	Two prior distributions having the same means and variances. . . . . 6-19
6.18	The same prior distributions as in the previous figure, with $\lambda$ plotted on a logarithmic scale. . . . . 6-19
6.19	Two posterior distributions, from priors in previous figures. . . . . 6-19
6.20	The same posterior distributions as in the previous figure, with $\lambda$ plotted on logarithmic scale. . . . . 6-20
6.21	MLEs and 90% confidence intervals for $\lambda$ , based on each plant's data and based on pooled data from all the plants. . . . . 6-21
6.22	MLEs and 90% confidence intervals for $\lambda$ , each based on data from one calendar year. . . . . 6-25
6.23	Cumulative number of HPCI demands, by date. . . . . 6-26
6.24	Scatter plot of rank(x) versus rank(y). . . . . 6-29
6.25	Likelihood as a function of $p$ , for the data of Example 6.7. . . . . 6-32
6.26	Discrete informative prior distribution for $p$ . . . . . 6-34
6.27	Discrete prior and posterior distribution for data in Example 6.7. . . . . 6-34
6.28	Likelihood as a function of $p$ , for ten times the data of Example 6.7. . . . . 6-34
6.29	Discrete prior and posterior distributions for $p$ , with 10 times as much data as in previous figure. . . . . 6-35
6.30	Prior density for $p$ , beta(4.2, 153.1). . . . . 6-37
6.31	Posterior density for $p$ , beta(5.2, 160.1). The 5th and 95th percentiles are shown. . . . . 6-37
6.32	Posterior cumulative distribution of $p$ . The 5th and 95th percentiles are shown. . . . . 6-37
6.33	Jeffreys noninformative prior distribution for $p$ . . . . . 6-37
6.34	Comparison of four point estimates and interval estimates for $p$ . . . . . 6-38
6.35	Lognormal prior density and posterior density for $p$ . . . . . 6-42
6.36	Script for analyzing Example 6.7 with BUGS. . . . . 6-43
6.37	MLEs and 90% confidence intervals for $p$ , for three types of demand and for the pooled data. . . . . 6-44
6.38	Point and interval estimates of $p$ , each based on one year's data. . . . . 6-48
6.39	Cumulative number of failures versus cumulative number of demands. . . . . 6-48
6.40	Script for analyzing standby failure data exactly. . . . . 6-52

<u>Figure</u>	<u>Page</u>	
6.41	Plot of cumulative failure count, a close approximation of plot of cumulative hazard function when only a small fraction of the systems fail. . . . .	6-55
6.42	Empirical distribution function (EDF) for the data from group T in Example 6.12. . . . .	6-58
6.43	Histogram of the data from group T in Table 6.16, with bin width 50. . . . .	6-59
6.44	Histogram of same data, with bin width 10. . . . .	6-59
6.45	One form of a box plot. The box shows the lower and upper quartiles, with the median marked. The whiskers show most of the range, from 4 to 118, and individual outlying points are plotted. . . . .	6-64
6.46	A different style box plot of the same data. The box shows the upper and lower quartiles, with the median indicated by a stripe. The whiskers show much of the range, with dots marking outliers. . . . .	6-64
6.47	Side-by-side box plots of the three groups of data from Table 6.16, based on $\log_{10}(\text{recovery time})$ . . . . .	6-64
6.48	$\log_{10}(\text{recovery time})$ plotted against event date, for data from groups S and T in Example 6.13. . . . .	6-66
6.49	Cumulative duration of LOSP events versus cumulative number of events. . . . .	6-67
6.50	Histogram of data from Table 6.19, with multiple of lognormal density overlaid. The skewness makes goodness of fit difficult to assess. . . . .	6-68
6.51	Histogram of $\ln(\text{time})$ , with a multiple of a normal density overlaid. Fit appears as good as achievable without using a bimodal distribution. . . . .	6-68
6.52	Empirical and theoretical reliability functions, where the reliability function is defined as 1 minus the c.d.f. . . . .	6-69
6.53	Quantile-quantile plot of $\ln(\text{recovery time})$ and fitted normal distribution. The points fall nearly on a straight line, indicating good fit. . . . .	6-69
6.54	Quantile-quantile plot of raw recovery times against fitted normal distribution. The strong curvature indicates bad fit. . . . .	6-69
6.55	Q-Q plot for checking exponential distribution in Example 6.6. . . . .	6-70
6.56	Density estimate of the data from group T in Example 6.12, with rectangular kernel and bandwidth 25. . . . .	6-74
6.57	Density estimate of the data from group T in Example 6.12 with rectangular kernel and bandwidth 50. . . . .	6-74
6.58	Density estimate from group T of Example 6.13, with rectangular kernel and bandwidth 50, forced to be nonzero on positive axis only. . . . .	6-75
6.59	Density estimate of the data from group T in Example 6.12, with standard normal kernel and bandwidth 25. . . . .	6-76
6.60	Density estimate of the data from group T in Example 6.12, with standard normal kernel and bandwidth 50. . . . .	6-76
6.61	Q-Q plot for checking whether durations have exponential distribution in Example 2.16. . . . .	6-79
6.62	Q-Q plot for examining whether times between outages are exponential. . . . .	6-80
6.63	Q-Q plot for investigating normality of $x$ when trains are pooled and months withing quarters are pooled. . . . .	6-82
7.1	Loglinear model, $\ln \lambda(t) = a + bt$ , for $a = 0.1$ and three possible values of $b$ . The vertical axis shows $\ln \lambda(t)$ . . . . .	7-3
7.2	Same model as in previous figure, showing $\lambda(t)$ instead of $\ln \lambda(t)$ . . . . .	7-3
7.3	Power-law model, showing $\ln \lambda(t)$ as a linear function of $\ln(t)$ , with $A = 1.0$ and several values of $b$ . . . . .	7-4
7.4	Same model as in previous figure, with $\lambda(t)$ shown as function of $t$ . . . . .	7-4
7.5	Directed graph for analysis of Poisson trend in Example 6.5. . . . .	7-5
7.6	BUGS script for analyzing data of Example 6.6. . . . .	7-5
7.7	Posterior distribution of $\lambda$ , assuming exponential trend in Example 6.5. . . . .	7-6
7.8	Frequency of unplanned HPCI demands, from Figure 6.22, with exponentially decreasing fitted trend line overlaid. . . . .	7-7
7.9	Simultaneous 90% confidence band and band formed by individual 90% confidence intervals for Poisson event rate, $\lambda(t)$ . . . . .	7-9

Table of Contents

<u>Figure</u>	<u>Page</u>
7.10 Simultaneous 90% confidence band for $\lambda(t)$ , and 90% confidence interval for one frequency of special interest, $\lambda(93)$ . . . . .	7-9
7.11 Fitted Poisson event occurrence rate and simultaneous 90% confidence band, based on three ways of fitting the HPCI unplanned-demands data. . . . .	7-11
7.12 Annual frequency of initiating events, with fitted exponentially decreasing $\lambda(t)$ and simultaneous 90% confidence band on $\lambda(t)$ . . . . .	7-13
7.13 Standardized residuals, also called the Pearson chi-squared residuals, for data of 7.12. . . . .	7-13
7.14 Cumulative count of initiating events, for data of Table 7.3 (Example 2.1). . . . .	7-14
7.15 Plot of $\ln\{ p(t)/[1 - p(t)] \} = a + bt$ , with $a = -2$ and three values of $b$ . . . . .	7-17
7.16 Plot of $p(t)$ as a function of $t$ , corresponding to Figure 7.15. . . . .	7-17
7.17 BUGS script for analyzing data of Example 6.10. . . . .	7-18
7.18 Posterior trend line for $p$ with 90% credible band, for data of Table 7.5. In addition, annual estimates and 90% credible intervals are shown, based on constrained noninformative prior. . . . .	7-19
7.19 Annual estimates of $p$ , fitted trend line and 90% confidence band for $p(t)$ , for data of Table 7.5. . . . .	7-21
7.20 Estimate of $\lambda(t)$ using standard normal kernel, with bandwidth $h = 400$ . . . . .	7-26
7.21 Estimate of $\lambda(t)$ using standard normal kernel, with bandwidth $h = 200$ . . . . .	7-26
8.1 Hierarchical model for Poisson data. . . . .	8-1
8.2 Plant-specific MLEs and 90% confidence intervals for $\lambda$ . . . . .	8-8
8.3 Plant-specific posterior means and 90% credible intervals for $\lambda$ . . . . .	8-8
8.4 Plant-specific MLEs and 90% confidence intervals for $p$ . . . . .	8-10
8.5 Plant-specific posterior means and 90% credible intervals for $p$ . . . . .	8-11
8.6 Hierarchical Bayes model for Poisson data. . . . .	8-12
8.7 Directed graph for the hierarchical Bayes analysis of Example 8.1. . . . .	8-13
8.8 WinBUGS model specification for Example 8.1. . . . .	8-16
8.9 Plant-specific posterior means and 90% credible intervals for $\lambda$ , from hierarchical Bayes analysis. . . . .	8-17
8.10 WinBUGS model specification for a beta prior in Example 8.2. . . . .	8-17
8.11 Plant-specific posterior means and 90% credible intervals for $p$ , from hierarchical Bayes analysis with beta population-variability distribution. . . . .	8-18
8.12 WinBUGS model specification for a logistic-normal prior in Example 8.2. . . . .	8-19
8.13 Fitted population-variability distributions in Example 8.2. . . . .	8-19
8.14 Plant-specific posterior means and 90% credible intervals for $p$ , from hierarchical Bayes analysis with logistic-normal population-variability distribution. . . . .	8-19
A.1 Venn diagram, showing ten outcomes and three events. . . . .	A-1
A.2 Probability density function (p.d.f.) and cumulative distribution function (c.d.f.). . . . .	A-6
A.3 The reliability function, hazard function and cumulative hazard function. . . . .	A-7
A.4 Density, showing quartiles, median, and mean. . . . .	A-9
A.5 Cumulative distribution function (c.d.f.) showing quartiles, median, and mean. . . . .	A-9
A.6 Three binomial probability distribution functions. . . . .	A-13
A.7 Three Poisson probability distribution functions. . . . .	A-14
A.8 Density of uniform( $a, b$ ) distribution. . . . .	A-15
A.9 Two normal densities. . . . .	A-15
A.10 Three lognormal densities. . . . .	A-17
A.11 Two exponential densities. . . . .	A-17
A.12 Four Weibull densities, all having $\theta = 0$ and all having the same $\alpha$ . . . . .	A-19
A.13 Gamma densities with four shape parameters. . . . .	A-20
A.14 Four inverted gamma densities, having the same scale parameter, $\beta$ , and various shape parameters, $\alpha$ . . . . .	A-20
A.15 Beta distributions with mean = 0.5. . . . .	A-21
A.16 Four beta distributions with mean 0.1. . . . .	A-21
A.17 Three logistic-normal densities with median = 0.5. . . . .	A-22
A.18 Three logistic-normal densities with median = 0.1. . . . .	A-23



Table of Contents

<u>Figure</u>		<u>Page</u>
B.1	Probability of rejecting $H_0$ : $\mu = 3.388$ , if in fact $H_0$ is true (upper distribution), and if $H_0$ is false with $\mu = 4.09$ (lower distribution). . . . .	B-8
B.2	Power curves when $n = 5$ and $n = 10$ . The graph shows the probability of rejecting $H_0$ , as a function of the true $\mu$ . . . . .	B-8
B.3	The hypothesized distribution, the empirical distribution, and the Kolmogorov test statistic, $D$ . . . . .	B-10
B.4	Schematic diagram of types of priors. . . . .	B-14

## LIST OF TABLES

<u>Table</u>	<u>Page</u>	
2.1	Kinds of models considered. . . . .	2-2
3.1	Examples of component boundaries . . . . .	3-2
6.1	Comparison of Bayesian and frequentist approaches in PRA. . . . .	6-3
6.2	Example 6.2, first sample (10 events in 6 years) with coarse prior. . . . .	6-9
6.3	Comparison of Bayesian and frequentist estimates for the data in Example 6.2. . . . .	6-11
6.4	Comparison of estimates with 1 event in 4.89 reactor-critical-years. . . . .	6-15
6.5	Posterior distributions from two analyses. . . . .	6-19
6.6	Quantities for calculation of chi-squared test. . . . .	6-22
6.7	Shutdown LOSP events at three sites, 1980-96. . . . .	6-24
6.8	HPCI demands and reactor-critical-years. . . . .	6-25
6.9	Calculations for analyzing LOSP dates . . . . .	6-29
6.10	Comparison of Bayesian distributions. . . . .	6-35
6.11	Comparison of estimates with one failure in eight demands. . . . .	6-39
6.12	Contingency table for Example 6.8. . . . .	6-45
6.13	Counts, expected counts, and contributions to $X^2$ , for Example 6.8. . . . .	6-46
6.14	HPCI failures on demand, by year. . . . .	6-48
6.15	Contingency table for successive outcomes in Example 6.10. . . . .	6-50
6.16	Statistics based on the recovery times (minutes) of Example 6.12. . . . .	6-57
6.17	Detailed data for Example 2.16. . . . .	6-78
6.18	Summary data for Example 2.16. . . . .	6-78
6.19	Sample statistics for estimates of $q$ , with different levels of aggregation. . . . .	6-81
6.20	Comparison of Bayesian results from two approaches, using noninformative priors. . . . .	6-84
7.1	HPCI demands and reactor-critical-years (from Example 6.5). . . . .	7-1
7.2	Posterior statistics for $a$ and $b$ , for loglinear model of Example 6.5. . . . .	7-6
7.3	Dates of initiating events at one plant, 1987-1995. (from Example 2.1) . . . . .	7-12
7.4	Initiating events and reactor-critical-years. . . . .	7-13
7.5	HPCI failures on demand, by year (from Example 6.10). . . . .	7-17
7.6	Posterior statistics for $a$ and $b$ , for loglinear model of Example 6.5. . . . .	7-18
8.1	Portion of frequentist analysis results for Example 8.1. . . . .	8-9
8.2	Portion of empirical Bayes analysis, without Kass-Steffey adjustment . . . . .	8-9
8.3	Portion of empirical Bayes analysis, with Kass-Steffey adjustment . . . . .	8-9
8.4	Portion of frequentist analysis results for Example 8.2 . . . . .	8-11
8.5	Portion of empirical Bayes analysis, without Kass-Steffey adjustment . . . . .	8-11
8.6	Portion of empirical Bayes analysis, with Kass-Steffey adjustment . . . . .	8-11
8.7	Portion of hierarchical Bayes analysis results for Example 8.1 . . . . .	8-17
8.8	Portion of hierarchical Bayes analysis results using beta prior for Example 8.2 . . . . .	8-18
8.9	Portion of hierarchical Bayes analysis results using logistic-normal prior for Example 8.2 . . . . .	8-20
B.1	Features of Bayesian and Frequentist Approaches . . . . .	B-3
B.2	Possible Hypothesis Test Outcomes. . . . .	B-6
C.1	Standard normal cumulative distribution function, $\Phi$ . . . . .	C-1
C.2	Percentiles of the chi-squared distribution.. . . .	C-4
C.3	Percentiles of the Student's $t$ distribution.. . . .	C-6
C.4	90th and 10th percentiles of beta( $\alpha$ , $\beta$ ) distribution.. . . .	C-8
C.5	95th and 5th percentiles of beta( $\alpha$ , $\beta$ ) distribution . . . . .	C-10
C.6	97.5th and 2.5th percentiles of beta( $\alpha$ , $\beta$ ) distribution.. . . .	C-12
C.7	Acceptance limits for the Kolmogorov test of goodness of fit . . . . .	C-14
C.8	Parameters of constrained noninformative prior for binomial $p$ . . . . .	C-15

## LIST OF EXAMPLES

<u>Example</u>	<u>Page</u>
2.1	Unplanned reactor trips ..... 2-3
2.2	Shutdown loss of offsite power ..... 2-3
2.3	Through-wall pipe leaks ..... 2-3
2.4	Temperature sensor/ transmitters ..... 2-3
2.5	HPCI failures to start ..... 2-7
2.6	EDG failures to start ..... 2-7
2.7	Steam binding in AFW ..... 2-7
2.8	Failures of isolation valves ..... 2-7
2.9	EDG failures to run ..... 2-14
2.10	AFW turbine train failures to run ..... 2-14
2.11	Recovery times from loss of offsite power ..... 2-16
2.12	Repair times for turbine-driven pumps ..... 2-16
2.13	Time to failure of a component ..... 2-16
2.14	Times to suppress fires ..... 2-16
2.15	Gradual degradation until failure ..... 2-16
2.16	CVC unavailability for test and maintenance ..... 2-19
6.1	Initiating events with loss of heat sink. .... 6-5
6.2	Confidence intervals from computer-generated data. .... 6-7
6.3	Small-break LOCAs. .... 6-18
6.4	Shutdown LOSP events at five plants, 1980-96. .... 6-21
6.5	Unplanned HPCI demands. .... 6-25
6.6	Dates of shutdown LOSP events and days between them. .... 6-29
6.7	AFW turbine-train failure to start ..... 6-31
6.8	EDG failures to start on demand. .... 6-44
6.9	Hypothetical unbalanced data. .... 6-47
6.10	Dates of HPCI failures and unplanned demands, 1987-1993. .... 6-48
6.11	EDG failure-to-run times. .... 6-54
6.12	LOSP recovery times. .... 6-56
6.13	LOSP recovery times and event dates. .... 6-66
7.1	Thermal-fatigue leak events, by plant age. .... 7-1
8.1	Initiating events from many plants. .... 8-2
8.2	Failure to start of AFW motor-driven segments at many plants. .... 8-2

## FOREWORD

During the last several years, both the U.S. Nuclear Regulatory Commission (NRC) and the nuclear industry have recognized that probabilistic risk assessment (PRA) has evolved to the point where it can be used in a variety of applications including as a tool in the regulatory decision-making process. The increased use of PRA has led to the conclusion that the PRA scope and model must be commensurate with the applications. Several procedural guides and standards have been and are being developed that identify requirements for the PRA models. For example, the "Standard For Probabilistic Risk Assessment For Nuclear Power Plant Applications" published by The American Society of Mechanical Engineers (ASME) in 2002 (ASME-RA-S-2002) defines requirements for PRA analysis used to develop risk-informed decisions for commercial nuclear power plants, and describes a process for applying these requirements in specific applications. This handbook was generated to support these documents by providing a compendium of good practices that a PRA analyst can use to generate the parameter distributions required for quantifying PRA models.

The increased use of risk assessment has also helped promote the idea that the collection and analysis of event data is an important activity in and of itself. In particular, the monitoring of equipment performance and evaluation of equipment trends can be used to enhance plant performance and reliability. The reference material provided in this handbook can support those efforts.

This handbook provides references on sources of information and methods for estimating parameter distributions. This includes determination of both plant-specific and generic estimates for initiating event frequencies, component failure rates and unavailability, and equipment non-recovery probabilities, all of which directly supplement the ASME PRA standard.

This handbook provides the basic information needed to generate estimates of the parameters listed above. It begins by describing the probability models and plant data used to evaluate each of the parameters. Possible sources for the plant data are identified and guidance on the collection, screening, and interpretation is provided. The statistical techniques (both Bayesian and classical methods) required to analyze the collected data and test the validity of statistical models are described. Examples are provided to help the PRA analyst utilize the different techniques.

This handbook also provides advanced techniques that address modeling of time trends. Methods for combining data from a number of similar, but not identical, sources are also provided. This includes empirical and hierarchical Bayesian approaches. Again, examples are provided to guide the analyst.

This handbook does not provide guidance on parameter estimation for all types of events included in a PRA. Specifically, common cause failure and human error probabilities are not addressed. In addition, guidance is not provided with regard to the use of expert elicitation. For analysis of these events, the PRA analyst should consult other sources, some of which are cited in Chapter 1.

## ACKNOWLEDGMENTS

The authors wish to acknowledge Dennis C. Bley, Iyjin Chang, Mary T. Drouin, Leslie E. Lancaster, Gareth W. Parry, Dale M. Rasmuson, David Robinson, Arthur D. Salomon, and Nathan O. Siu, who gave extensive and insightful written comments. In particular, it was Mary Drouin's initiative that started the project. She provided the early guidance and support for the development of the document. Bley and Parry not only provided comments, but also contributed text that was included in the final report. W. Jay Conover gave helpful advice on tests of serial independence, and David S. Moore gave advice on the relation of the chi-squared statistic and the deviance. Robert F. Cavedo and Steven A. Eide supplied information on the treatment of unavailability in current PRAs. Robert W. Youngblood contributed ideas and references on the relation of the two models for failure to start. Steven M. Alferink, William J. Galyean, Cynthia D. Gentillon, Dana L. Kelly, and Martin B. Sattison supplied examples and constructive comments. Ralph Nyman provided information about the Swedish I-Book. Teresa Sype provided help in formatting the report. Christine E. White produced many of the figures.

## ABBREVIATIONS

AC	alternating current
AFW	auxiliary feedwater
ALWR	Advanced Light Water Reactor
ANO	Arkansas Nuclear One
ANSI	American National Standards Institute
ASEP	Accident Sequence Evaluation Program
ASME	American Society of Mechanical Engineers
ATWS	anticipated transient without scram
BWR	boiling water reactor
CDF	core damage frequency
c.d.f.	cumulative distribution function
ComEd	Commonwealth Edison
ConEd	Consolidated Edison
CPC	Consumers Power Company
CREDO	Centralized Reliability Data Organization
CVC	chemical and volume control
DC	direct current
DG	diesel generator
DOE	Department of Energy
ECCS	emergency core cooling system
EDF	empirical distribution function
EDG	emergency diesel generator
EEI	Edison Electric Institute
EF	error factor
EPIX	Equipment Performance and Information Exchange System
EPRI	Electric Power Research Institute
FTR	failure to run
FTS	failure to start
GE	General Electric
HCF	Hardware Component Failure
HEP	human error probability
HHRAG	Human and Hardware Reliability Analysis Group
HPCI	high pressure coolant injection
HPP	homogeneous Poisson process
HRA	human reliability analysis
HVAC	heating, ventilation and air conditioning
IEEE	Institute of Electrical and Electronics Engineers
IGSCC	intergranular stress corrosion cracking
i.i.d.	independent identically distributed
INEL	Idaho National Engineering Laboratory
INEEL	Idaho National Engineering and Environmental Laboratory
INPO	Institute of Nuclear Power Operations
IPE	Individual Plant Examination
IPEEE	Individual Plant Examination of External Events
IPRDS	In-Plant Reliability Data Base for Nuclear Power Plant Components
IREP	Interim Reliability Evaluation Program
LER	Licensee Event Report
LCO	limiting conditions of operation
LOCA	loss of coolant accident
LOSP	loss of offsite power
MCMC	Markov Chain Monte Carlo

MLE	maximum likelihood estimate, or maximum likelihood estimator, depending on the context (see <i>estimate</i> in glossary)
MOV	motor-operated valve
MSE	mean square error
MSIV	main steam isolation valve
MTTF	mean time to failure
MTTR	mean time to repair
NA	not applicable
NHPP	nonhomogeneous Poisson process
NPE	Nuclear Power Experience
NPP	Nuclear Power Plant
NPRDS	Nuclear Plant Reliability Data System
NRC	U.S. Nuclear Regulatory Commission
NREP	Nuclear Reliability Evaluation Program
NSAC	Nuclear Safety Analysis Center
NUCLARR	Nuclear Computerized Library for Assessing Reactor Reliability
OREDA	Offshore Reliability Data
PCS	Power Conversion System
PECO	Philadelphia Electric Company
p.d.f.	probability density or distribution function
PLG	Pickard, Lowe and Garrick, Inc.
PORV	power operated relief valve
PRA	Probabilistic Risk Assessment
PSA	Probabilistic Safety Assessment
PWR	pressurized water reactor
RAC	Reliability Analysis Center
RADS	Reliability and Availability Data System
RCIC	reactor core isolation cooling
RHR	residual heat removal
RMIEP	Risk Methods Integration and Evaluation Program
RPS	reactor protection system
RSSMAP	Reactor Safety Study Methodology Application Program
SAIC	Scientific Applications International Corporation
SBLOCAs	small-break loss-of-coolant accidents
SCSS	Sequence Coding and Search System
SKi	Swedish Nuclear Power Inspectorate
SRV	safety relief valve
SSPI	Safety System Performance Indicator
SwRI	Southwest Research Institute
U.K.	United Kingdom
U.S.	United States