

Mechanical and Transport Constitutive Models for Fractures Subject to Dissolution and Precipitation

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ABSTRACT

Transient changes in the permeability of fractures in systems driven far-from-equilibrium are described in terms of proxy roles of stress, temperature and chemistry. The combined effects of stress and temperature are accommodated in the response of asperity bridges where mineral mass is mobilized from the bridge to the surrounding fluid. Mass balance within the fluid accommodates mineral mass either removed from the

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flow system by precipitation or advection, or augmented by either dissolution or advection. Where the system is hydraulically closed and initially at equilibrium, reduction in aperture driven by the effects of applied stresses and temperatures will be augmented by precipitation on the fracture walls. Where the system is open, the initial drop in aperture may continue, and accelerate, where the influent fluid is oversaturated with respect to the equilibrium mineral concentration within the fluid, or may reverse, if under-saturated. This simple zero-dimensional model is capable of representing the intricate behavior observed in experiments where the feasibility of fracture sealing concurrent with net dissolution is observed.

1 INTRODUCTION

The evolution of transport characteristics in fractured rocks is controlled by competition between the chemical and mechanical effects which either generate (including dilatant shear, microcracking, thermal cracking and focused dissolution) or destroy (including shear and hydrostatic compaction, fracture healing, dislocation creep, and pressure solution prompted by water-film and free-face diffusion) porosity. Crucial in this understanding of chemical effects, are the mechanisms in which mechanical deformation contributes to changes in permeability, and by which the mechanical response in turn is modified. These effects are especially important in fractured rocks, where both permeability and stiffness are intrinsically controlled by the most hydraulically conductive, and most mechanically soft, elements – *viz.* the fractures.

These effects are known to be important at relatively modest stresses, temperatures, and typically for systems pushed far from chemical equilibrium, such as in geothermal or hydrocarbon reservoirs or around waste repositories. Sealing is suggested in some instances of vapor and fluid transport under low [1-3] and moderate stresses [4] and gapping is suggested in the acidizing literature of the petroleum field [5-7] and in the development of karst [8-11]. The controlling processes and feedbacks apply, in varying degree, to a variety of disciplines, and at a variety of spatial and temporal scales. These include our understanding of diagenetic processes at basin scale [12-15] where the implicated minerals comprising the aggregate may be quartz [16-18], halite [19], feldspars [20], calcite [9, 21], or clays [22, 23], and where veining [24] or crack sealing [22, 25-27], or the timing of the earthquake cycle [28-36] are affected by the evolution of mechanical and transport properties. These properties may relate to granular [37-39] or fractured media [40-42], and may be moderated by effects of chemical response [41, 43] or of brittle deformation [37, 44]. In all cases, the processes and feedbacks apparent in these complex systems are wide ranging, and have broad significance.

Key issues in this understanding relate to the strength and sense of various feedbacks, and their influence in defining the effect of reactive mass transport on permeability change. Important questions remain regarding the magnitude of anticipated changes in permeability or stiffnesses in response to these coupled

chemical- and mechanical-effects, and indeed their sense. Enigmatically, systems subject to compressive loads and net chemical dissolution have been observed to gape, rather than to seal – the key issue is the source and destination for the redistribution of mineral mass which contributes to these changes.

This work presents relationships describing the evolution of permeability based on mechanistically consistent but idealized models of contacting fractures, to define the evolution of transport and mechanical properties with paths of chemical potential.

2 MECHANISTIC MODEL

Model describes behavior of a system subject to the serial effects of pressure solution, free-face dissolution, including advection from the control volume. To describe behavior we evaluate closure of the fracture driven by pressure solution, to a new equilibrium configuration as controlled by a contact model. This closure of the fracture is a function of pressure solution only, and is not influenced by free-face dissolution. As the system approaches this equilibrium configuration, it may be acted upon by free-face dissolution, with material advected from the system.

2.1 Contact Model

Closure between two contacting rough fracture surfaces, as illustrated in Figure 1, is driven by a change in the applied effective stress. The average normal stress, $\bar{\sigma}$, acting over a nominal area of the fracture, \bar{R} , results in a local asperity stress, σ_f , beneath the contact area, R_f , as,

$$R_f = \bar{R} \frac{\bar{\sigma}}{\sigma_f} \quad (1)$$

The equilibrium contact area of the fracture is defined by the equilibrium stress, σ_f , as [39]

$$s_f = \frac{E_m(1 - T / T_m)}{4V_m} \quad (2)$$

Where T is temperature, T_m is the temperature of fusion, E_m is the heat of fusion, and V_m is the molar volume of the mineral comprising the fracture asperity. The total volume removed as the fracture adjusts to a new equilibrium stress, σ_f , that is related to a new equilibrium contact area, R_f , must be determined from the architecture of the fracture porosity. The equivalent aperture, $\langle b \rangle$ may be defined in terms of residual aperture, b_r , and ‘reference stress’ aperture, b_0 , in terms of [41, 43]

$$\langle b \rangle = b_r + (b_0 - b_r) e^{-(R_c - R_{c_0})a} \quad (3)$$

where R_{c_0} is the relative contact area at the reference stress, and R_c is the contact area, a defines the form of the contact-area-aperture relationship, and $\langle b \rangle$ is the mean aperture. If the equilibrium stress is defined from equation (2), and the equilibrium contact area from equation (1), then the volume lost during fracture closure, V , may be determined as,

$$\begin{aligned} V &= -A_f \int_{b_i}^{b_f} \frac{R_c}{1 - R_c} d\langle b \rangle = - \int_{R_i}^{R_f} \frac{R_c}{1 - R_c} \frac{d\langle b \rangle}{dR_c} dR_c \\ &= A_f (b_0 - b_r) e^{-(1 - R_{c_0})a} \left(e^{-(1 - R_f)a} - e^{-(1 - R_i)a} - a \text{Ei}((1 - R_f)a) + a \text{Ei}((1 - R_i)a) \right) \end{aligned} \quad (4)$$

where $\text{Ei}(x)$ is the exponential integral function. This evaluates the loss of material which must occur as the opposing walls of the fracture interpenetrate, due to pressure-solution-like closure of the fracture, and enables the volume of mineral removed to be directly determined.

2.2 Pore-Void Continuity

The idealized geometry is shown in Figure 2. The mass of mineral removed from the asperity by stress-enhanced dissolution is ejected into the fluid within the pore volume, V_p . This mass is dissolved within the fluid, but is also available to be precipitated onto the pore (fracture) walls, or advected from the control volume. From mass conservation, the change in concentration within the fluid may be defined as,

$$\frac{dc}{dt} - A e^{-Ft} + B(c - c_{eq}) + Q(c - c_{in}) = 0 \quad (5)$$

where the evolving concentration, c , with time, t , is controlled relative to the equilibrium concentration, c_{eq} , and influent concentration, c_{in} , through constants representing the magnitude of pressure dissolution, A , the rate of pressure-dissolution, F , the rates of free-face precipitation and dissolution, B , and the mass flux, Q , defined in pore volumes per unit time.

Where only the effects of pressure solution are considered, the volume removed by pressure solution may be defined as V_{ps} , by augmenting the concentration in the pore fluid by an amount, c_{ps} , and the rate of removal as,

$$\frac{dV_{ps}}{dt} = \frac{dc_{ps}}{dt} \frac{V_p}{r} \quad (6)$$

and from equation (5), $dc_{ps}/dt = A e^{-Ft}$. Substituting this into equation (6) yields

$$V = \int_0^{\infty} \frac{dV_{ps}}{dt} dt = \frac{V_p}{r} \int_0^{\infty} A e^{-Ft} dt = \frac{V_p}{r} \frac{A}{F} \quad (7)$$

Equating this with the mass removed from the asperity (equation (4)), enables the magnitude of A to be determined, and the rate of closure is conditioned by F . This ultimate volume removed into solution is equivalent to the product of equilibrium concentration, $c[t] = c[\infty] = A/F$, and V_p/r as identified in equation (7).

2.3 System Response

The response of the system to changes in pore fluid concentration may be determined from consideration of the combined effects of pressure dissolution, precipitation/dissolution, and advection. For an REV, this is defined through solution of

$$\frac{dc}{dt} - \frac{A e^{-Ft}}{-dc_A/dt} + \frac{B(c - c_{eq})}{-dc_B/dt} + \frac{Q(c - c_{in})}{-dc_Q/dt} = 0 \quad (8)$$

where the components representing the processes of pressure solution (dc_A / dt), precipitation/dissolution (dc_B / dt), and advection (dc_Q / dt) are defined sequentially. Solving equation (8) for the initial conditions of $c = c_0$ at $t = 0^+$ yields

$$\begin{aligned}
c[t] = & e^{-(B+Q)t} \left[\frac{A}{(B+Q-F)} (e^{(B+Q-F)t} - 1) \right. \\
& + \frac{B}{(B+Q)} (c_0 - c_{eq}(1 - e^{(B+Q)t})) \\
& \left. + \frac{Q}{(B+Q)} (c_0 - c_{in}(1 - e^{(B+Q)t})) \right]
\end{aligned} \tag{9}$$

The change in displacement, u , driven by this process may be directly evaluated from the shortening of the supporting rock pedestal covering a proportion of the total area, R_c , as illustrated in Figure 2. The updated displacement is given as,

$$u = u_i + Du = u_i + \int_0^t \frac{du}{dt} dt = u_i - \frac{V_p}{A_{fr}} \int_0^t \frac{1}{R_c} \frac{dc_A}{dt} dt \tag{10}$$

where

$$\int_0^t \frac{dc_A}{dt} dt = \frac{A}{F} (1 - e^{-Ft}). \tag{11}$$

The change in the mean hydraulic aperture, b , is generally different from the change in the mechanical aperture [45], since the flow domain has an intervening obstruction of relative area, R_c . Correspondingly, the change in hydraulic aperture, db , is related to mechanical closure, du , via the shortening of the asperity pedestal, as $db = (1 - R_c) du$. This results in

$$b = b_i + Db = b_i + \int_0^t \frac{db}{dt} dt = b_i - \frac{V_p}{A_{fr}} \int_0^t \left[\frac{1 - R_c}{R_c} \frac{dc_A}{dt} - \frac{dc_B}{dt} \right] dt \tag{12}$$

where

$$\int_0^t \frac{dc_B}{dt} dt = - \int_0^t B(c[t] - c_{eq}) dt . \quad (13)$$

It is important to note that the hydraulic aperture is defined as the average over the entire area of the fracture, A_f , therefore $V_p = A_f b$, but $du = \frac{1}{1 - R_c} db$. Finally, substituting equation (9) into equation

(13), yields the change in aperture due to dissolution of the free face of the fracture, as

$$\int_0^t \frac{dc_B}{dt} dt = B(c_{eq}t - \frac{(B(c_0 - c_{eq}) + Q(c_0 - c_{in}))}{(B + Q)^2} (1 - e^{-(B+Q)t}) - \frac{A(1 - e^{-Ft})}{F(B + Q - F)} + \frac{A(1 - e^{-(B+Q)t})}{(B + Q)(B + Q - F)} - \frac{Bc_{eq}t + Qc_{in}t}{B + Q}) . \quad (14)$$

Thus, the deformation and hydraulic response of the fracture may be tracked as a consequence of both dissolution from beneath the intervening asperity anvil, and as a result of free face dissolution or precipitation. This response may be followed for systems which are arbitrarily hydraulically open ($Q \neq 0$) or closed ($Q = 0$).

2.4 Observational Data

This model may be compared with behavior observed in a variety of flow-through experiments conducted on both novaculite [2, 41], and in limestone [6, 7, 46], to define the fidelity of the proposed characterization. Both the novaculite and limestone have near-zero matrix porosity, so the full observed response is that due to the fracture.

Novaculite: In this experiment, distilled water was flowed through the fracture for a total of ~900 hours, at relatively high flow rates ranging from 0.2 to 0.9 cc/min, and under a constant confining stress of 3.5 MPa ([2]. The system is far from equilibrium. During the experiment, the change in hydraulic aperture of the fracture is evaluated continuously from the prescribed flow rate, and measured pressure drop. The aperture drops from 12 mm to 3 mm with the progress of the experiment, representing a hundredfold drop in permeability, as the temperature is augmented from 20°, to 80°, to 120° to 150°C. This behavior is shown in

Figure 3 together with change in the measured efflux of Si in the first 80 hours of the experiment.

Fits with these data are completed, to concurrently match both the aperture change and chemical data. These fits are shown in

Figure 3 for the full experiment, and the parameters utilized for the fits are identified in Table 1. The change in aperture is evaluated from equation (12), and the corresponding change in concentration is evaluated from equation (9). The calculated changes in aperture closely follow the observed response. Notably, the maximum closure of the fracture is well represented by the ultimate modeled closure. Where the behavior over the first 80 hours is magnified, as shown in

Figure 4, the match for this period, at temperatures of 20° and 80°C is quite good. Similarly, the fitting parameters of A, B, and F provide consistent fits in log-linear space. Both parameters A and B remain approximately constant within the range of temperatures explored in the experiment, suggesting that the behavior of the system is consistently represented by the phenomenology of the model. The time constant for stress-driven dissolution is represented by F, and its inverse Arrhenius dependency on temperature. These dependencies are consistent with the expected dimensional response of the system.

Limestone: This flow-through experiment is similar to the prior test: total applied stress on the sample is retained constant (~3.5 MPa) at a fixed flow rate of 2 cc/min, but the experiment is isothermal, and conducted at 20° C. The experiment was conducted in two stages: the first involving the circulation of “groundwater” at pH~8, and the second when distilled water (pH~6) is then introduced. The response to this experiment has been reported elsewhere [7], and preliminary analyses completed to represent

behavior [6]. Significant in the response is that the aperture first reduces in response to the effects of pressure solution, in response to circulation by “groundwater.” Once the system is pushed further from equilibrium, with the introduction of distilled water, the closure first accelerates, and then the flow impedance drop drastically as a large through-going conduit is etched through the sample [7].

The response observed in this experiment may also be matched by this model, as illustrated in

Figure 5, using consistent parameters identified in **Table 2**. The model is capable of closely replicating the aperture-closure when pressure solution dominates. The matches for Ca concentrations are also adequate, but in the early period, the resolution of the measurements are inadequately constrained [7]. Once the through-going conduit is etched (wormhole), the simple lumped parameter model is incapable of following the response. In this instance, the implementation of such a constitutive model into a spatial model is mandatory. Only through this, can the development of a strongly heterogeneous system be followed.

3 PARAMETRIC RESPONSE

With the capability to replicate observed responses clear from the previous, anticipated features in the response of idealized hydraulically closed and open systems may be investigated. These will reveal important features in their anticipated behavior, characteristic responses, and the magnitudes of various parameters which condition this response. These behaviors are examined in the following.

3.1 Closed System ($Q = 0$)

Where the system is both hydraulically closed ($Q = 0$), and where dissolution at the fracture wall is discounted ($B = 0$), then the equilibrium response at $t \gg \tau$ may be determined from equation (9) as

$$c[\Psi] \approx \frac{A}{F}. \quad (15)$$

For this simplest of cases, the equilibrium displacement results directly from equation (10) as

$$u[\Psi] = u_i + Du = u_i - \frac{V_p}{A_f r} \frac{1 - R_c}{R_c} \frac{A}{F} \quad (16)$$

and, again where $B = 0$ only, the change in aperture is equivalent to the displacement, as implied by equation (12) as

$$b[\Psi] = b_i + Db = b_i - \frac{V_p}{A_f r} \frac{1 - R_c}{R_c} \frac{A}{F} \quad (17)$$

Where the initial equivalent hydraulic aperture (measured relative to the entire fracture area, A_f) is set to b_i , the geometry of Figure 2 defines the pore volume, V_p as $V_p = b_i A_f$ and the displacement is given as

$$u[\Psi] = u_i + Du = u_i - \frac{b_i}{r} \frac{1 - R_c}{R_c} \frac{A}{F} \quad (18)$$

or in non-dimensional form,

$$u[\Psi] / b_i = u_i / b_i + Du / b_i = u_i / b_i - \frac{1}{r} \frac{1 - R_c}{R_c} \frac{A}{F} \quad (19)$$

The corresponding change in aperture is

$$b[\Psi] = b_i + Db = b_i - \frac{b_i(1 - R_c)}{r} \frac{1}{R_c} \frac{A}{F} \quad (20)$$

Or in non-dimensional form,

$$b[\Psi] / b_i = b_i / b_i + Db / b_i = 1 - \frac{(1 - R_c)}{r} \frac{1}{R_c} \frac{A}{F} \quad (21)$$

Typical observations during experiments (see previous) are for closures to be of the order of 20% of the original aperture. Therefore, for typical contact areas of $R_c \sim 1/3$ then $\frac{A}{rF} \sim 0.1$. Clearly the admissible range of non-dimensional closure is for $0 < b[\Psi] / b_i < 1$, and for $R_c \sim 1/3$, then this corresponds to $1/2 > \frac{A}{rF} > 0$.

Where dissolution is important, then $B \neq 0$, and although displacement will asymptote to a static magnitude of equation (19) as $t \rightarrow \infty$, aperture will continue to change after the effects of pressure solution have been largely completed. In this instance, free-face dissolution or precipitation drives a change in aperture; the sense of this effect is controlled by the magnitude of the peak concentration (c_A) driven by pressure solution. If peak $c_A < c_{eq}$ then aperture will increase with time, to an equilibrium magnitude, and if $c_A > c_{eq}$, then aperture will decrease. The final aperture magnitude as $t \rightarrow \infty$ is given as

$$b[\Psi] = b_i + Db = b_i - \frac{V_p}{A_f r} \left[\frac{1}{R_c} \frac{A}{F} - \frac{1}{1 - R_c} [(c_0 - c_{eq}) + \frac{A}{F}] \right] \quad (22)$$

in dimensional form, and as

$$b[\Psi] / b_i = 1 - \frac{(1 - R_c)}{r} \left[\frac{1}{R_c} \frac{A}{F} - \frac{1}{1 - R_c} [(c_0 - c_{eq}) + \frac{A}{F}] \right] \quad (23)$$

in non-dimensional form.

Typical behaviors for a closed system are shown in

Figure 6.

3.2 Open System ($Q \neq 0$)

When the system is open, then $Q \neq 0$, and again the system reaches an equilibrium response in terms of a steady magnitude of the fluid concentration, $c[\text{‰}]$. This behavior is reached as the injection of mass controlled by pressure solution has been fully depleted, and the resulting concentration is a balance between the rate of flow and the dissolution rate from the walls, moderated by the injection and equilibrium concentrations. Thus, as $t \rightarrow \infty$, then the equilibrium effluent concentration is given as

$$c[\text{‰}] = \frac{Bc_{eq} + Qc_{in}}{(B + Q)}. \quad (24)$$

The initial displacement is controlled by the response to pressure solution, but once this process is complete, no further displacement will occur, unless the rock bridge is so weakened that collapse must ensue. Correspondingly, displacements are identical to those in the closed system, and are as defined by equation (18), with non-dimensional displacements defined by equation (19). However, apertures will continue to change in the presence of dissolution, and no steady state is reached, although the rate of change of aperture will approach a steady magnitude. Substituting equation (14) into (12) yields, for the case where pressure solution effects have completed

$$b[t \rightarrow \infty] = b_i + \Delta b = b_i - \frac{V_p (1 - R_c)}{A_f r} \left[\frac{1}{R_c} \frac{A}{F} - \frac{1}{1 - R_c} \left[B \left(\frac{(B(c_0 - c_{eq}) + Q(c_0 - c_{in}))}{(B + Q)^2} + \frac{A}{F(B + Q - F)} - \frac{A}{(B + Q)(B + Q - F)} + \frac{Bc_{eq}t + Qc_{in}t}{B + Q} - c_{eq}t \right) \right] \right] \quad (25)$$

The response of an open system is shown in Figure 7. In this, the aperture drops rapidly with the evolution of pressure-dissolution, but once this process is complete, free-face dissolution overtakes this

effect, and results in the net opening of the fracture. This gaping continues unabated, as illustrated by the straight-line portion of the response in time.

4 CONCLUSIONS

A model is developed to accommodate the effects of dissolution and precipitation on the transport properties of fractures where the role of stress is appropriately accommodated. In this, changes in stresses and in temperature is able to elicit a response of preferentially mobilizing mineral mass from fracture bridges, without any supposition of the mechanism by which it may occur. It may result from the effects of increased chemical potential which results from “pressure solution” type effects, or it may result from the advance of sub-critical crack growth at these locations. The principal requirement is that some equilibrium mineral mass is mobilized, which may then be ejected into the flow-field.

The consideration of mass continuity for the dissolved mineral mass, and the establishment for a rate law to describe precipitation or dissolution relative to the aqueous concentration of the infiltrating fluid, enables the progress of fracture sealing effects to be followed. Importantly, these considerations make feasible the response that fracture apertures may reduce, and permeabilities concomitantly fall, where mineral mass is net dissolved from the system. Of principal importance are the sources and destinations of the redistributed mineral mass within the fracture, in conditioning this response. Where prior equilibrium is disturbed by an increase in either stress or temperature, mineral mass is injected into the aqueous system, and correspondingly reduces aperture. This reduction in aperture is time dependent, with a characteristic time controlled by the destruction of the fracture bridge. Overprinted on this response is the influence of the mass ejected from the fracture bridge. In a closed system, originally at aqueous equilibrium, this mineral mass is trapped within the REV of the fracture, and will precipitate on the fracture walls, additively reducing the aperture. In an open system, this mass will be added to the interstitial fluid, and depending on the influent chemistry, will affect the response of the system in a variety of ways – apertures must initially drop, but will subsequently either build, or continue to drop, depending on the specifics of the flow system. Thus, a variety of complex behaviors may result,

depending on the initial and boundary conditions applied to the system. These models are applied to observational data for open systems, far-from-equilibrium, where both closure and gaping of the fractures is observed, and satisfactory agreement obtained.

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Table 1: Magnitudes of model constants for flow in Novaculite.

Temperature [°C]	A [kg m ⁻³ s ⁻¹]	F [s ⁻¹]	B [s ⁻¹]	Q [s ⁻¹] ^a	Pore volume, V_p [m ³] ^b	Initial aperture, b_i [mm]	Solubility, C_{eq} [kg m ⁻³]	Contact -area ratio, R_c
20	6.0×10^{-4}	1.0×10^{-5}	1.0×10^{-5}	0.30	2.83×10^{-8}	12.0	5.43×10^{-3}	0.10
80	7.0×10^{-4}	4.0×10^{-6}	1.0×10^{-5}	0.56	2.83×10^{-8}	12.0	3.42×10^{-2}	0.10
120	6.5×10^{-4}	3.0×10^{-6}	1.0×10^{-5}	0.24	2.83×10^{-8}	12.0	8.54×10^{-2}	0.10
150	6.2×10^{-4}	2.6×10^{-6}	1.0×10^{-5}	0.14	2.83×10^{-8}	12.0	1.51×10^{-1}	0.10

^aDefined as the flow rates prescribed in the experiment over pore volume.

^bDefined as the product of initial aperture and nominal fracture area.

Table 2: Magnitudes of model constants for flow in Limestone.

Permeant	A [kg m ⁻³ s ⁻¹]	F [s ⁻¹]	B [s ⁻¹]	Q [s ⁻¹] ^a	Pore volume, V_p [m ³] ^b	Initial aperture, b_i [mm]	Solubility, C_{eq} [kg m ⁻³]	Contact -area ratio, R_c
Ground water	1.2×10^{-4}	1.0×10^{-6}	1.0×10^{-3}	2.88×10^{-2}	1.30×10^{-7}	24.0	3.74×10^{-2}	0.15
Distilled water	1.2×10^{-4}	7.0×10^{-6}	4.0×10^{-4}	3.86×10^{-3}	9.72×10^{-7}	18.0	3.74×10^{-2}	0.15

^aDefined as the flow rates prescribed in the experiment over pore volume, V_p .

^bDefined as the product of initial aperture, b_i , and nominal fracture area, A_f .

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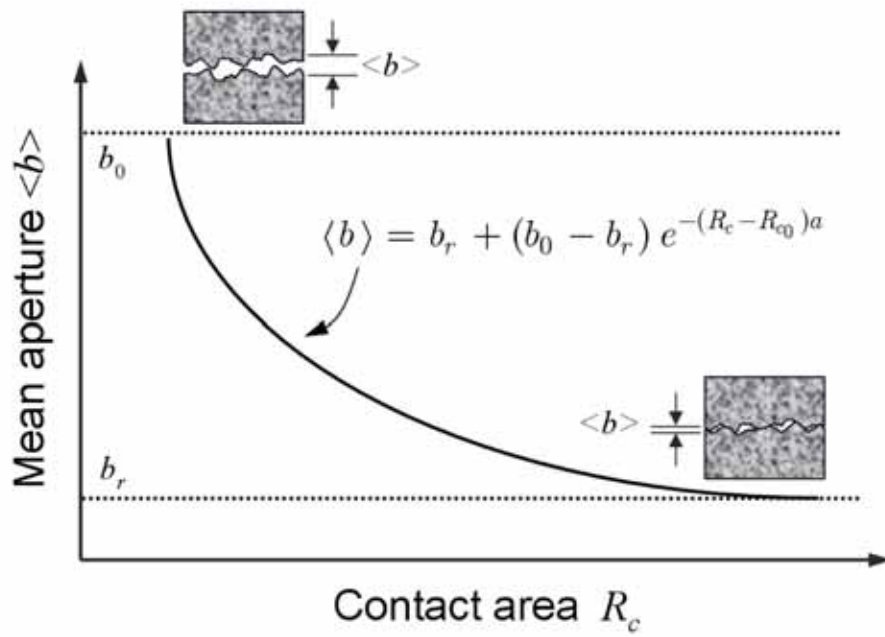


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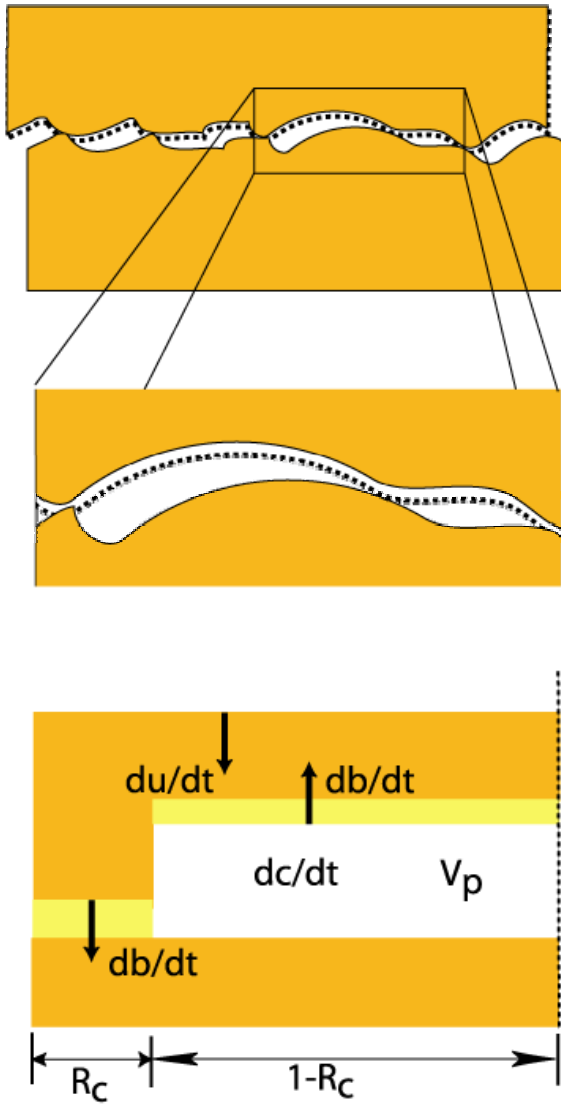


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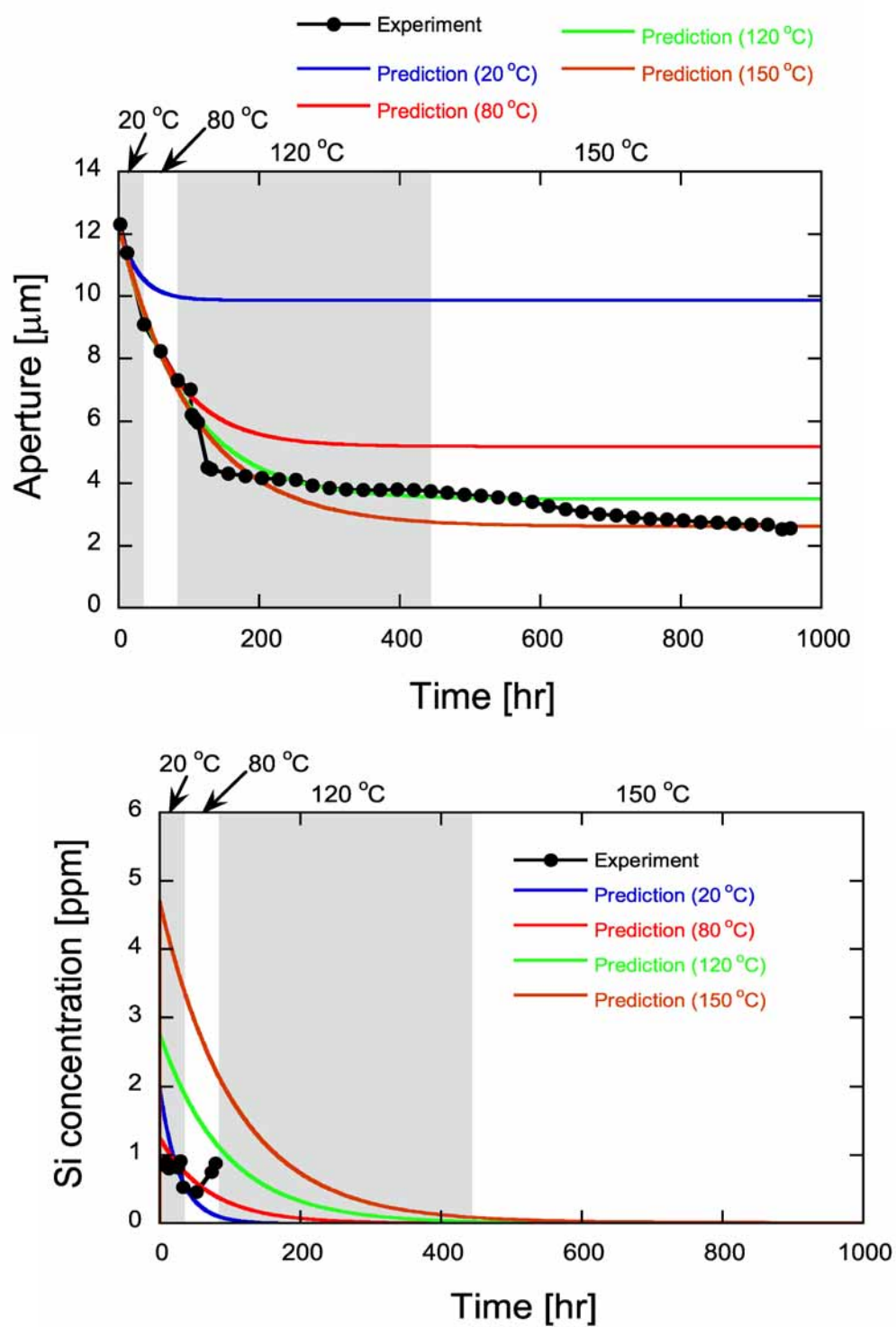


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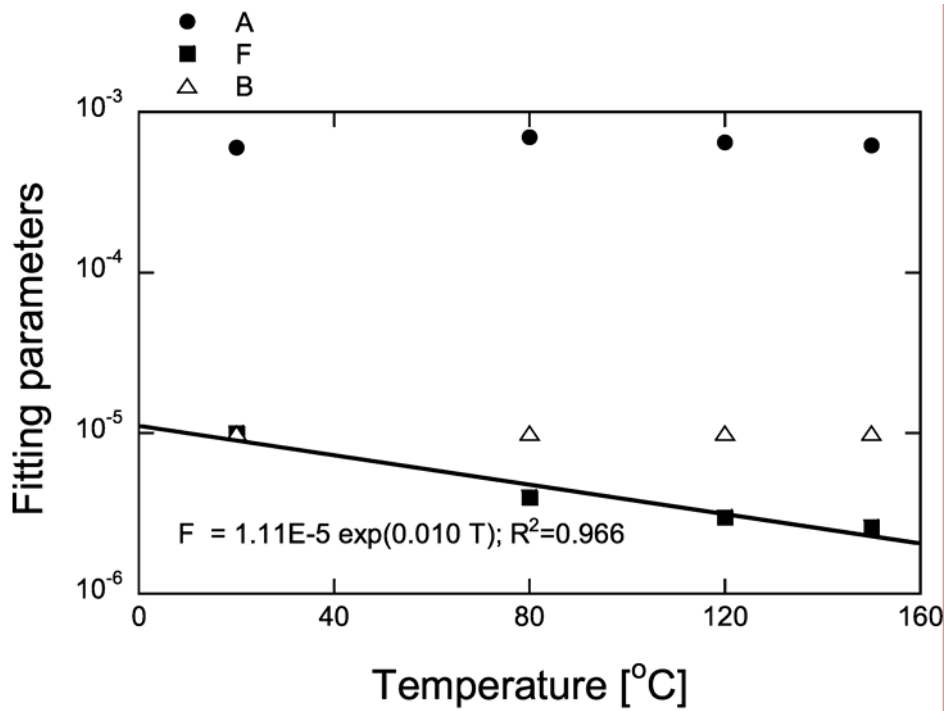
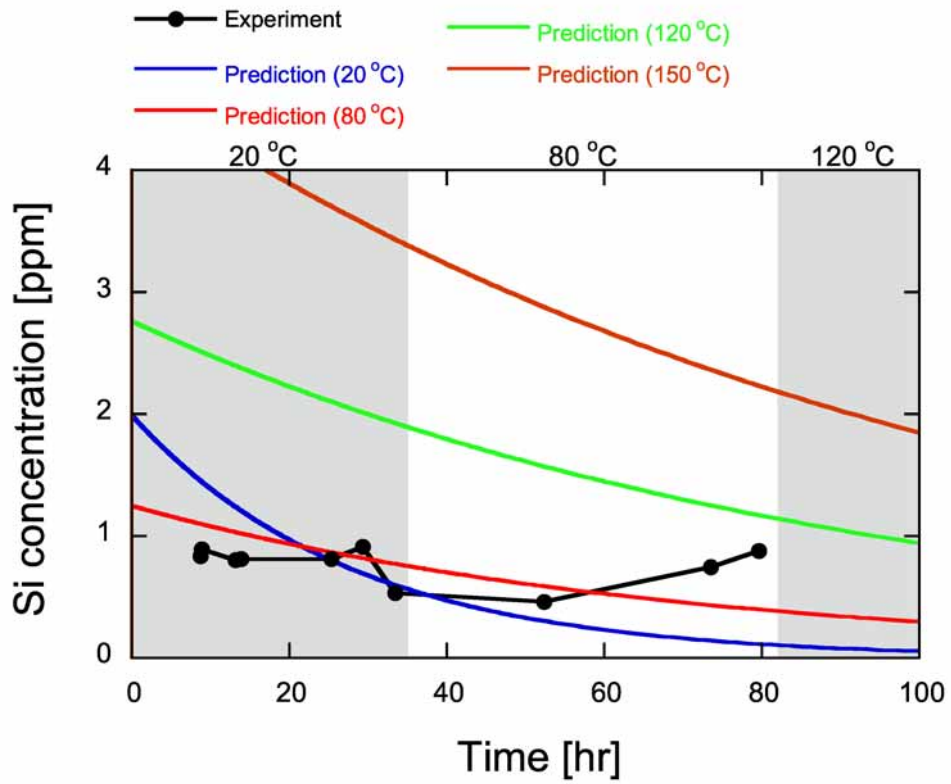


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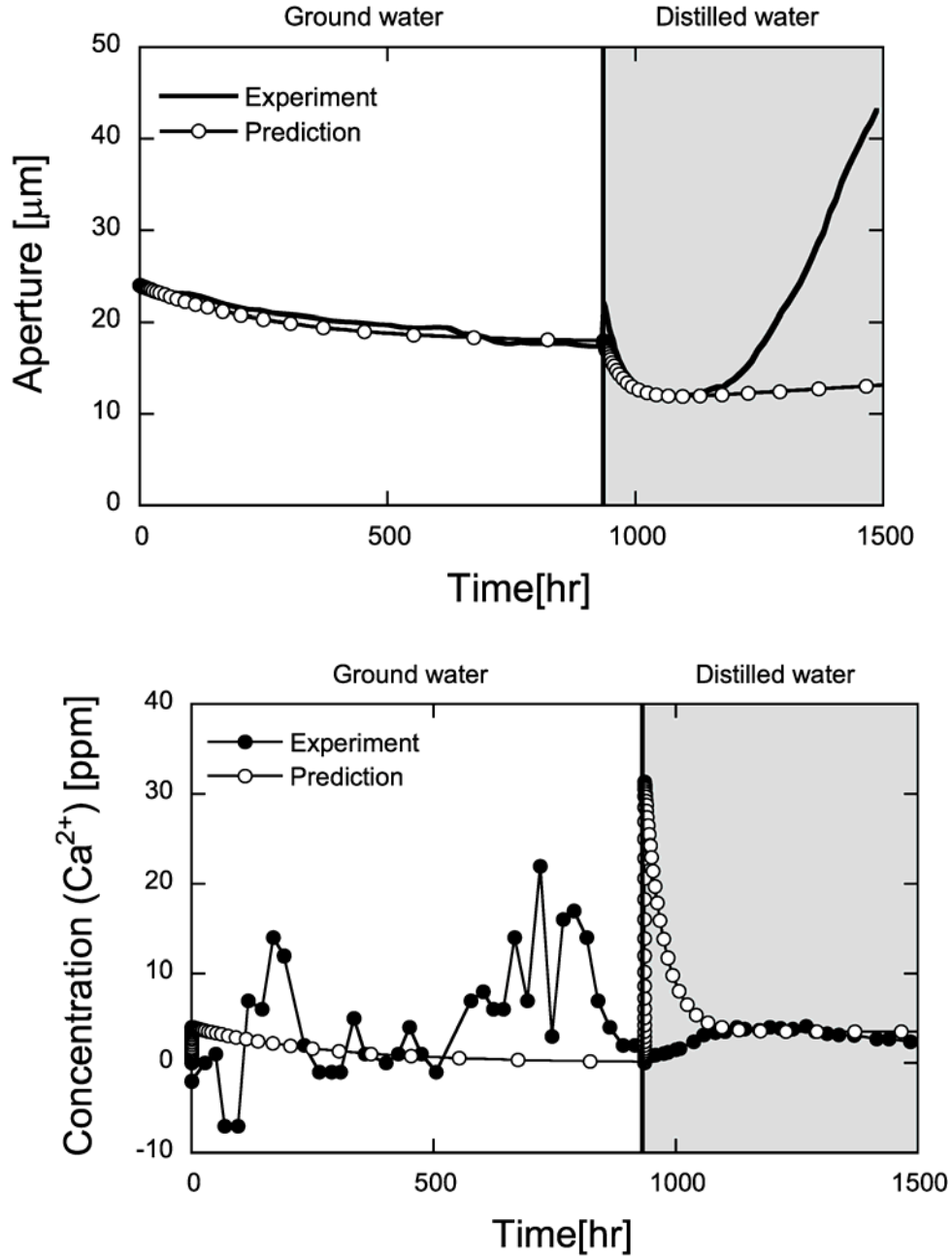


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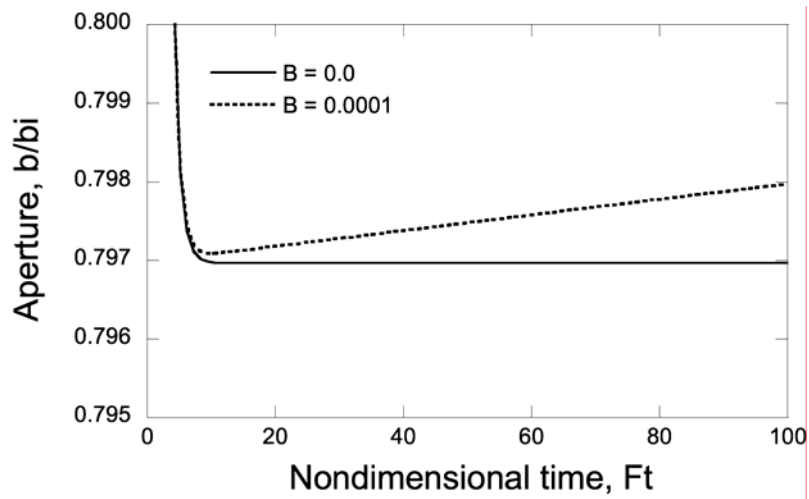
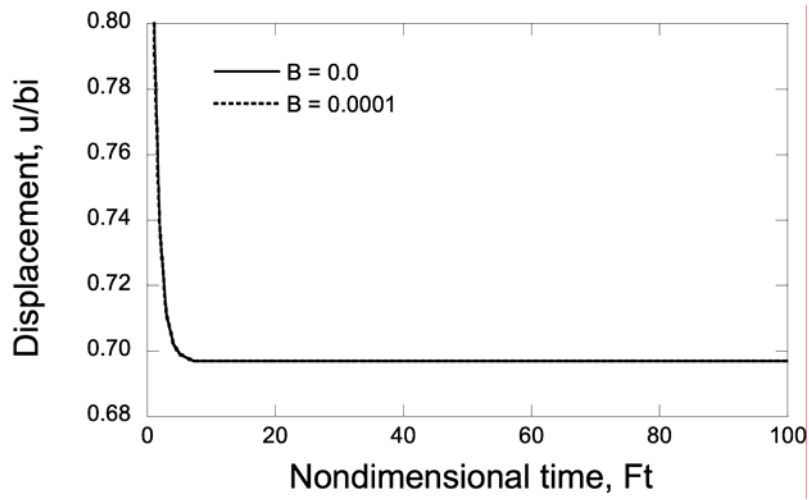
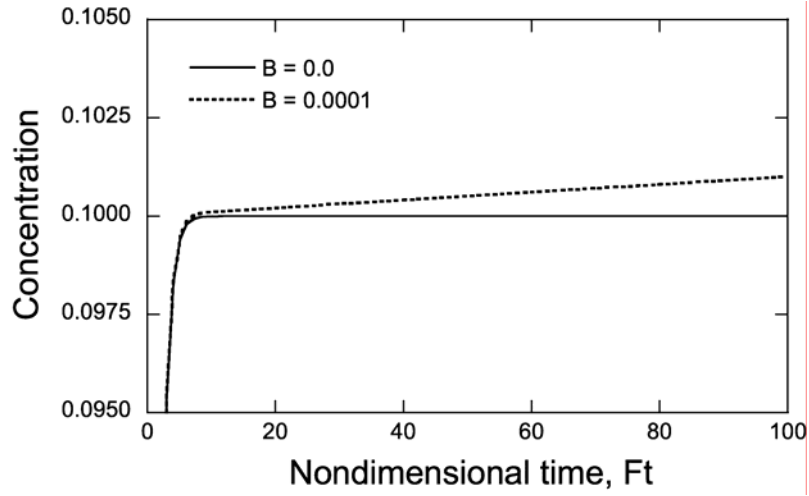


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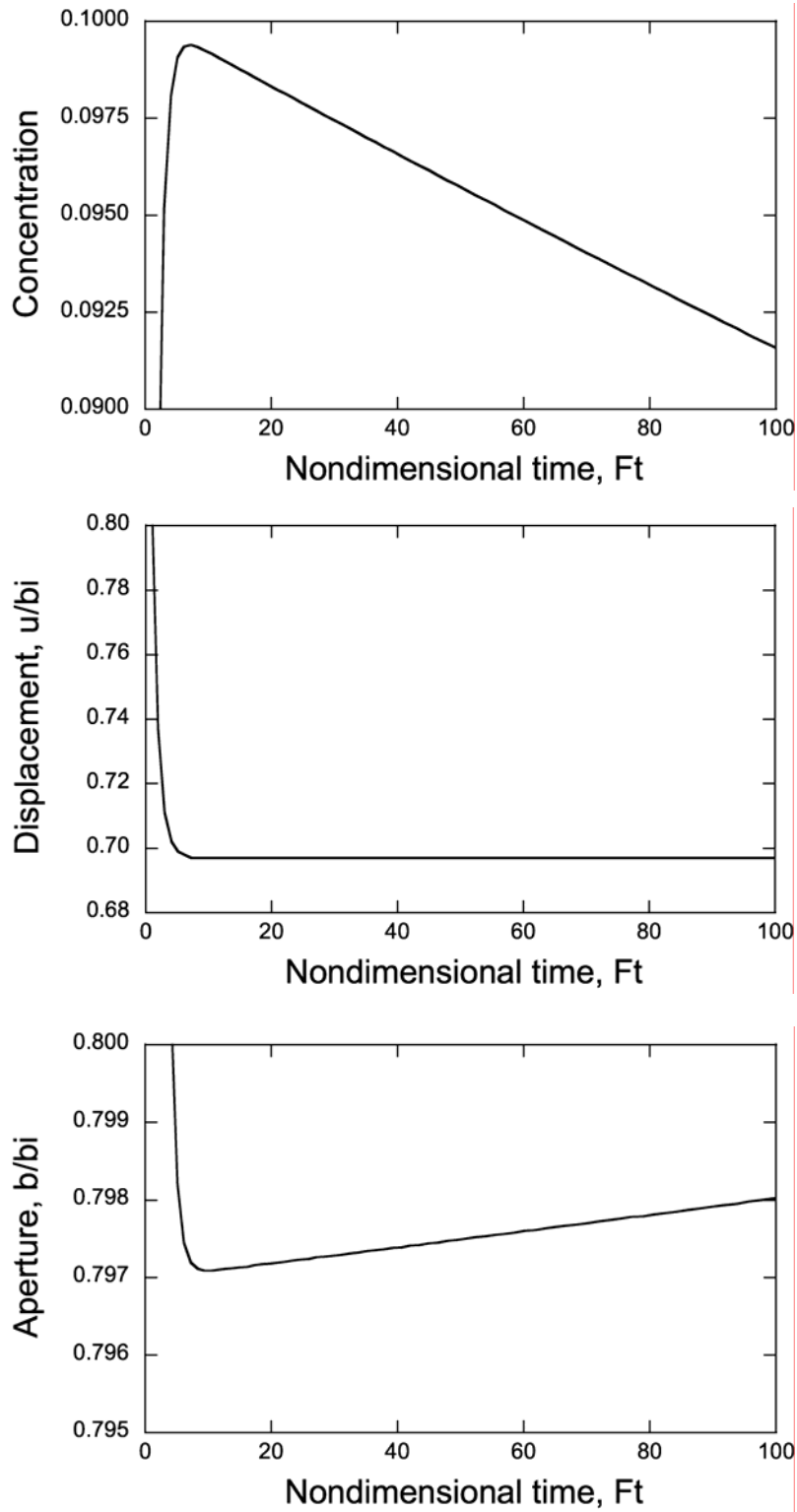


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