

1548 **PART 5. METHODS FOR ESTIMATING UNCERTAINTY**

1549

1550 Many of the key variables and functional relationships which are important to understanding the
1551 climate system and how the climate may change over the coming decades and centuries will
1552 likely remain uncertain for years to come. While a variety of evidence can be brought to bear to
1553 gain insight about these uncertainties, in most cases no single piece of evidence or experimental
1554 result can provide definitive answers. Yet research planners, groups attempting to do impact
1555 assessment, policy makers addressing emissions reductions, public and private parties making
1556 long-lived capital investment decisions, and many others, all need some informed judgment
1557 about the nature and extent of the associated uncertainties.

1558

1559 *Model-Generated Uncertainty Estimates*

1560 In some cases probability distributions for key climate parameters can be extracted directly from
1561 available data and models. Note, however, that the models themselves often contain a myriad of
1562 implicit expert judgments. In recent years, several research groups have derived probability
1563 distributions for climate sensitivity via statistical comparisons of climate model results to recent
1564 climate records. For instance, Figure 5.1 shows an estimate of climate sensitivity (Andronova
1565 and Schlesinger, 2001) made by simulating the observed hemispheric-mean near-surface
1566 temperature changes since 1856 with a simple climate/ocean model forced radiatively by
1567 greenhouse gases, sulfate aerosols and solar-irradiance variations. The authors account for
1568 uncertainty in climatic radiative forcing by considering 16 radiative forcing models. To account
1569 for natural variability in instrumental measurements of temperature, a bootstrap procedure is
1570 used to generate surrogate observed temperature records. Figure 4.1 shows the probability

1571 distribution function for estimated climate sensitivity based on 80,000 model runs, aggregated
1572 across radiative forcing models and bootstrapped temperature records. The resultant 90%
1573 confidence interval for temperature sensitivity is between 1.0° C and 9.2° C. Note that this
1574 analysis suggests a much wider spread than the IPCC range, consistent with the observation that
1575 experts routinely underestimate uncertainty. A number of other investigators have also used
1576 models together with historical climate data and other evidence to develop probability
1577 distributions for climate sensitivity or bound estimates of climate sensitivity or other variables.
1578 Several additional efforts of this sort are discussed below in Section 6.

1579
1580 Researchers have also used data and models to derive uncertainty estimates for future socio-
1581 economic and technological driving forces. For instance, Gritsevskiy and Nakicenovic (2000)
1582 and Nakicenovic and Riahi, (2002) have estimated probability distributions for the investment
1583 costs and learning rates of new technologies based on the historical distributions of cost and
1584 performance for many similar technologies and then used these probability estimates to forecast
1585 distributions of future emission paths. Some authors have estimated probability distributions for
1586 future emissions by assessing the frequency of results over different emissions models or by
1587 propagating subjective probability distributions for key inputs through such emission models
1588 (Webster *et al.*, 2003). Such approaches can suggest which uncertainties are most important in
1589 determining any significant deviations from a base-case projection and can prove particularly
1590 important in helping to make clear when proposed emissions scenarios differ in important ways
1591 from past trends. Care must be taken, however, with such estimates because unlike physical
1592 parameters of the climate system, socioeconomic and technological factors needs not remain
1593 constant over time and may be strongly interrelated and conditional on each other. Since we

1594 expect the 21st century will differ in important ways from the 20th, as the 20th differed in
1595 important ways from the 19th, *etc.*, we should regard these uncertainty estimates of future socio-
1596 economic outcomes with less confidence than those of physical parameters of the climate system
1597 when they are thought to be fundamentally constant through time.

1598

1599 *Expert Elicitation*

1600 Model and data generated uncertainty estimates can be very valuable in many cases. In
1601 particular, they are most germane for judgments about well-established knowledge, represented
1602 by the upper right-hand corner of Figure 1.1²³. But in many situations, limitations of data,
1603 scientific understanding, and the predictive capacity of models will make such estimates
1604 unavailable, with the result that they must be supplemented with other sources of information.

1605

1606 In such circumstances, the best strategy is to ask a number of leading experts to consider and
1607 carefully synthesize the full range of current scientific theory and available evidence and then
1608 provide their judgments in the form of subjective probability distributions.

1609

1610 Such formal individually-focused elicitation of expert judgment has been widely used in applied
1611 Bayesian decision analysis (DeGroot, 1970; Spetzler and Staël von Holstein, 1975; Watson and
1612 Buede, 1987; von Winterfeldt and Edwards, 1986; Morgan and Henrion, 1990; Cooke, 1991),
1613 often in business applications, and in climate and other areas of environmental policy through the
1614 process of "expert elicitation" (Morgan *et al.*, 1978a; Morgan *et al.*, 1978b; National Defense

²³The drive to produce estimates using model-based methods may also stem from a reluctance to confront the use of expert judgment explicitly.

1615 University, 1978; Morgan *et al.*, 1984; Morgan *et al.*, 1985; Wallsten and Whitfield, 1986;
1616 Stewart *et al.*, 1992; Nordhaus, 1994; Evans *et al.*, 1994a; Evans *et al.*, 1994b; Morgan and Keith,
1617 1995; Budnitz *et al.*, 1995; Budnitz *et al.*, 1998; Morgan *et al.*, 2001; Garthwaite *et al.*, 2005;
1618 Morgan *et al.*, 2006). An advantage of such expert elicitation is that it can effectively enumerate
1619 the range of expert judgments unhampered by social interactions, which may constrain discussion
1620 of extreme views in group-based settings.

1621
1622 Figures 5.2, 5.3 and 5.4 provide examples of results from expert elicitations done respectively on
1623 climate science in 1995, on forest ecosystem impacts in 2001, and on aerosol forcing in 2005.
1624 These are summary plots. Much greater detail, including judgments of time dynamics, and
1625 research needs are available in the relevant papers.

1626
1627 The comparison of individual expert judgments in Figure 5.4 with the summary judgment of the
1628 IPCC fourth assessment report (IPCC, 2007) suggests that the IPCC estimate of uncertainty in
1629 total aerosol forcing may be overconfident. A private communication from David Keith on the
1630 first eight responses of a detailed expert elicitation that he and Shawn Marshall (both of the
1631 University of Calgary) are conducting with leading glaciologists, indicates that they are finding
1632 even greater signs of overconfidence in the IPCC fourth assessment of sea level rise – suggesting
1633 that current strategies for producing IPCC summary statements of uncertainty may need to be
1634 reassessed.

1635
1636 Of course, expert judgment is not a substitute for definitive scientific research. Nor is it a
1637 substitute for careful deliberative expert reviews of the literature of the sort undertaken by the

1638 IPCC. However, its use within such review processes could enable a better expression of both the
1639 diversity of expert judgment and could allow expression of expert judgments, which are not
1640 adequately reflected, in the existing literature. It can also provide insights for policy makers and
1641 research planners while research to produce more definitive results is ongoing. It is for these
1642 reasons that Moss and Schneider have argued that such elicitations should become a standard
1643 input to the IPCC assessment process (Moss and Schneider, 2000).

1644

1645 In selecting experts to participate in an expert elicitation, it is important to draw upon
1646 representatives from across all the relevant disciplines and schools of thought. At the same time,
1647 this process is fundamentally different from that of drawing a random sample to estimate some
1648 underlying true value. In the case of expert elicitation, it is entirely possible that one expert,
1649 perhaps even one whose views are an outlier, may be correctly reflecting the underlying
1650 physical reality, and all the others may be wrong. For this same reason, when different experts
1651 hold different views it is often best not to combine the results before using them in analysis, but
1652 rather to explore the implications of each expert's views so that decision makers have a clear
1653 understanding of whether and how much the differences matter in the context of the overall
1654 decision (Morgan and Henrion, 1990; Keith, 1996).

1655

1656 While it has been our experience that when asked to participate in such elicitation exercises, with
1657 very few exceptions, experts strive to provide their best judgments about the quantity or issue at
1658 hand, without considering how those judgments might be used or the implications they may
1659 carry for the conclusions that may be drawn when they are subsequently incorporated in models
1660 or other analysis. In addition to the strong sense of professional integrity possessed by most

1661 leading experts, the risk of possible "motivational bias" in experts' responses in elicitation
1662 processes is further reduced by the fact that even if the results are nominally anonymous,
1663 respondents know that they may be called upon to defend their responses to their peers.

1664

1665 As noted in Section 2, unless they are accompanied by some form of quantitative calibration,
1666 qualitative summaries of uncertainty can often mask large disagreements, since the same
1667 descriptors of qualitative uncertainty can mean very different things to different people. Thus, a
1668 quantitative expert elicitation can often provide a better indication of the diversity of opinion
1669 within an expert community than is provided in many consensus summaries. For example, the
1670 expert elicitation of climate change damage estimates by Nordhaus (1994) revealed a systematic
1671 divide between social and natural scientists' considered opinions. Such results can allow others
1672 to draw their own conclusions about how important the range of expert opinions is to the overall
1673 policy debate. Sometimes apparent deep disagreements make little difference to the policy
1674 conclusions; sometimes they are of critical importance (Morgan *et al.*, 1984; Morgan and
1675 Henrion, 1990).

1676

1677 We believe that in most cases it is best to avoid discussion of second-order uncertainty. Very
1678 often people are interested in using ranges or even second-order probability distributions on
1679 probabilities - to express "uncertainty about their uncertainty." In our experience, this usually
1680 arises from an implicit confusion that there is a "true" probability out there, in the same way that
1681 there is a true value for the rainfall in a specific location last year -- and people want to express
1682 uncertainty about that "true" probability. Of course, there is no such thing. The probability itself
1683 is a way to express uncertainty. A second-order distribution rarely adds anything useful.

1684
1685 It is, of course, possible to use a second-order distribution to express the possible effect of
1686 specific new information on a probability. For example, suppose your probability that there will
1687 be an increase of more than 1°C in average global temperature by 2020 is 0.5. It makes sense
1688 then to ask "what is your current probability distribution over the probability you will assess for
1689 that event in five years time, when you will have seen five years more climate data and climate
1690 research?" Bayesians sometimes call this a pre-posterior distribution. Note that the pre-posterior
1691 distribution is a representation of the informativeness of a defined but currently unknown source
1692 of information, in this case the next five years of data. It depends specifically on your beliefs
1693 about that information source.

1694
1695 Most people find pre-posterior distributions hard to think about. It is possible to use them in
1696 elicitation (Morgan and Keith, 1995). However, in public forums, they are often confused with
1697 ambiguity and other kinds of second-order probability and are liable to provoke ideological
1698 debates with proponents of alternative formalisms of uncertainty. Hence, our view is that it is
1699 usually wisest to avoid them in public forums and reserve them for that sub-set of specialist
1700 applications where they are really needed. This is particularly true when one is already eliciting
1701 full probability distributions about the value of uncertain quantities.

1702
1703 There is one exception to this general guidance, which perhaps deserves special treatment.
1704 Suppose we have two experts A and B who are both asked to judge the probability that a well
1705 specified event will occur (*i.e.*, not a full PDF but just a single probability on the binary yes/no
1706 outcome). Suppose A knows a great deal about the relevant science and B knows relatively little,

1707 but they both judge the probability of the event's occurrence to be 0.3. In this case, A might give
1708 a rather tight distribution if asked to state how confident he is about his judgment (or how likely
1709 he thinks it is that additional information would modify that judgment) while B might give a
1710 rather broad distribution. In this case, the resulting distribution provides a way for the two
1711 experts to provide information about the confidence they have in their judgment.

1712

1713 To date, elicitation of individual experts has been the most widely used method of using expert
1714 judgment to characterize uncertainty about climate-related issues. After experts have provided
1715 their responses, many of these studies later give participants the opportunity to review their own
1716 results and those of others, and make revisions should they so desire, but they are not focused on
1717 trying to achieve group consensus.

1718

1719 While they have not seen extensive use in climate applications, there are a number of group-
1720 based methods, which have been used in other settings. Of these, the best known is the Delphi
1721 method (Dalkey, 1969; Linstone and Turoff, 1975). Delphi studies involve multiple rounds in
1722 which participants are asked to make and explain judgments about uncertain quantities of
1723 interest, and then are iteratively shown the judgments and explanations of others, and asked to
1724 make revisions, in the hope that over time a consensus judgment will emerge. Such a procedure
1725 typically will not support the depth of technical detail that has been characteristic of some of the
1726 protocols that have been used in elicitation of individual climate experts.

1727

1728 Budnitz *et al.* (1995, 1998) have recently developed a much more elaborate group method in the
1729 context of probabilistic seismic hazard analysis. Meeting for an extended period, a group of
1730 experts work collectively, not as proponents of specific viewpoints but rather as:

1731 ...informed *evaluators* of a range of viewpoints. (These individual viewpoints or models
1732 may be defended by proponents experts invited to present their views and ‘debate’ the
1733 panel). Separately the experts on the panel also play the role of *integrators*, providing
1734 advice... on the appropriate representation of the composite position of the community as
1735 a whole.
1736

1737 A technical facilitator/integrator (TFI):

1738 ...conducts both individual elicitations and group interactions, and with the help of the
1739 experts themselves the TFI integrates data, models and interpretations to arrive at the
1740 final product: a full probabilistic characterization of the seismic hazard at a site, including
1741 the uncertainty. Together with the experts acting as evaluators, the TFI "owns" the study
1742 and defends it as appropriate. (Budnitz *et al.*, 1998)

1743 Needless to say the process is very time consuming and expensive, requiring weeks or more of
1744 the expert’s time.

1745

1746 *Protocols for Individual Expert Elicitation*

1747 Developing a protocol for an effective expert elicitation in a substantively complex domain, such
1748 as climate science or climate impacts, typically requires many months of development, testing
1749 and refinement²⁴. Typically the designers of such protocols start with many more questions they
1750 would like to pose than experts are likely to have patience or the ability to answer. Iteration is
1751 required to reduce the list of questions to those most essential and to formulate questions of a
1752 form that is unambiguous and compatible with the way in which experts frame and think about
1753 the issues at hand. To achieve this latter, sometimes it is necessary to provide a number of

²⁴Roger Cooke (1991) and his colleagues have developed a number of elicitation programs in much shorter periods of time, working primarily in problem domains in which the problem is well specified and the specific quantities of interest are well defined.

1754 different response modes. In this case, designers need to think about how they will process
1755 results to allow appropriate comparisons of different expert responses. To support this objective,
1756 it is often desirable to include some redundancy in the protocol enabling tests of the internal
1757 consistency of the experts' judgments.

1758

1759 A number of basic protocol designs have been outlined in the literature (see Chapter 7 in Morgan
1760 and Henrion (1990) and associated references). Typically they begin with some explanation of
1761 why the study is being conducted and how the results will be used. In most cases, experts are told
1762 that their names will be made public but that their identity will not be linked to any specific
1763 answer. This is done to minimize the possible impact of peer pressure, especially in connection
1764 with requests to estimate extreme values. Next, some explanation is typically provided of the
1765 problems posed by cognitive heuristics and overconfidence. Some interviewers in the decision
1766 analysis community ask experts to respond to various "encyclopedia questions" or perform other
1767 exercises to demonstrate the ubiquitous nature of over confidence in the hopes that this "training"
1768 will help to reduce overconfidence in the answers received. Unfortunately, the literature suggests
1769 that such efforts have little, if any, effect²⁵. However, asking specific "disconfirming" questions,
1770 or "stretching" questions such as "Can you explain how the true value could turn out to be much
1771 larger (smaller) than your extreme value?" (see below) can be quite effective in reducing
1772 overconfidence.

1773

²⁵See, for example, the discussion on pp. 120-122 of Morgan and Henrion (1990).

1774 In elicitation they have done on rather well defined topics, Cooke (1991) and his colleagues²⁶
1775 have placed considerable emphasis on checking expert calibration and performance by
1776 presenting them with related questions for which values are well known, and then giving greater
1777 weight to experts who perform well on those questions. Others in the decision science
1778 community are not persuaded that such weighting strategies are advisable.

1779
1780 While eliciting a cumulative density function (CDF) of a probability distribution to characterize
1781 the uncertainty about the value of a coefficient of interest is the canonical question form in expert
1782 elicitation. Many of the elicitation protocols used in climate science have involved a wide range
1783 of other response modes (Morgan and Keith, 1995; Morgan *et al.*, 2001; Morgan *et al.*, 2006;
1784 Zickfeld *et al.*, 2006). In eliciting a CDF, it is essential to first clearly resolve with the expert
1785 exactly what quantity is being considered so as to remove ambiguity that might be interpreted
1786 differently by different experts. Looking back across a number of past elicitation, it appears that
1787 the uncertainty in question formulation and interpretation can sometimes be as large or larger
1788 than uncertainty arising from the specific formulation used to elicit CDFs. However, this is an
1789 uncertainty that can be largely eliminated with careful pilot testing, refinement and
1790 administration of the interview protocol.

1791
1792 Once a clear understanding about the definition of the quantity has been reached, the usual
1793 practice is to begin by asking the expert to estimate upper and lower bounds. This is done in an
1794 effort to minimize the impact of anchoring and adjustment and associated overconfidence. After
1795 receiving a response, the interviewer typically then chooses a slightly more extreme value (or, if

²⁶Additional information about some of this work can be found at <http://www.rff.org/rff/Events/Copy-of-Expert-Judgment-Workshop-Documents.cfm#CP_JUMP_21423>. See also Kurowicka and Cooke (2006).

1796 it exists, cites contradictory evidence from the literature) and asks if the expert can provide an
1797 explanation of how that more extreme value could occur. If an explanation is forthcoming, the
1798 expert is then asked to consider extending the bound. Only after the outer range of the possible
1799 values of the quantity of interest has been established does the interviewer go on to pose
1800 questions to fill in the balance of the distribution, using standard methods from the literature
1801 (Morgan and Henrion, 1990).

1802

1803 Experts often have great difficulty in thinking about extreme values. Sometimes they are more
1804 comfortable if given an associated probability (*e.g.*, a 1:100 upper bound rather than an absolute
1805 upper bound). Sometimes they give very different (much wider) ranges if explicitly asked to
1806 include "surprises," even though the task at hand has been clearly defined as identifying the
1807 range of all possible values. Therefore, where appropriate, the investigator should remind experts
1808 that "surprises" are to be incorporated in the estimates of uncertainty.

1809

1810 Hammitt and Shlyakhter (1999) have noted that overconfidence can give rise to an underestimate
1811 of the value of information in decision analytic applications. They note that because "the
1812 expected value of information depends on the prior distribution used to represent current
1813 uncertainty, and observe that "if the prior distribution is too narrow, in many risk-analytic cases,
1814 the calculated expected value of information will be biased downward." They have suggested a
1815 number of procedures to guard against this problem.

1816

1817 Most substantively detailed climate expert elicitation conducted to date have involved extended
1818 face-to-face interviews, typically in the expert's own office so that they can access reference

1819 material (and in a few cases even ask colleagues to run analyses, *etc.*). This has several clear
1820 advantages over mail or web-based methods. The interviewers can:

- 1821 • Have confidence that the expert is giving his or her full attention and careful
1822 consideration to the questions being posed and to performing other tasks;
- 1823 • More readily identify and resolve confusion over the meaning of questions, or
1824 inconsistencies in an expert's responses;
- 1825 • More easily offer conflicting evidence from the literature to make sure that the expert
1826 has considered the full range of possible views;
- 1827 • Build the greater rapport typically needed to pose more challenging questions and
1828 other tasks (such as ranking research priorities).

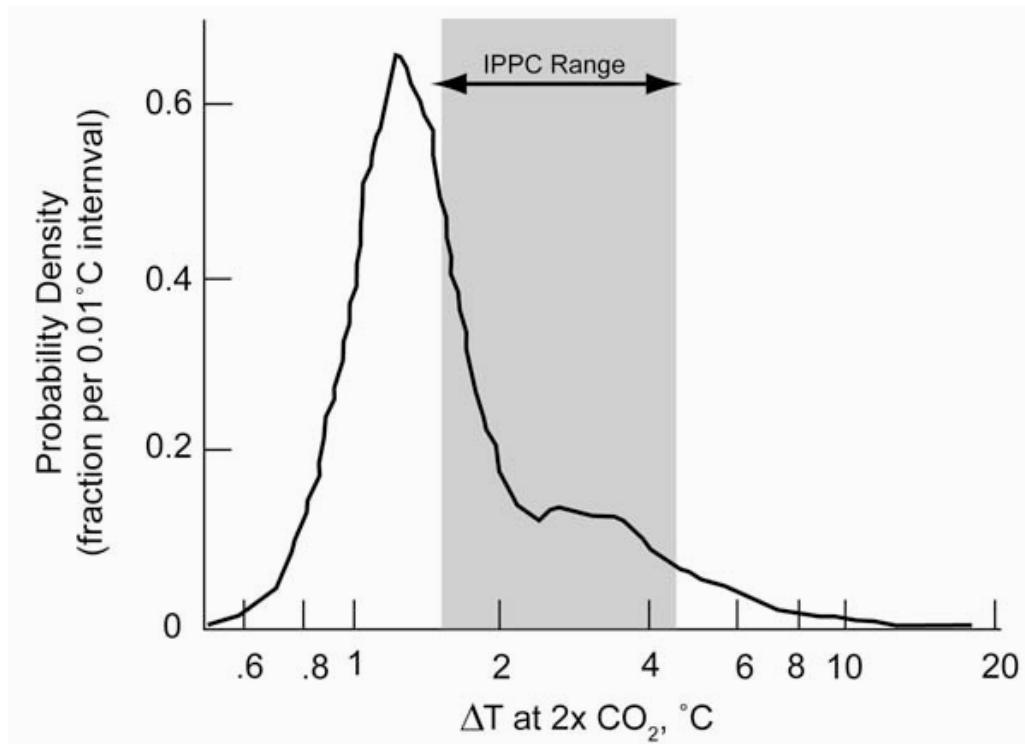
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1830 While developing probabilistic estimates of the value of key variables (*i.e.*, empirical quantities)
1831 can be extremely useful, it is often even more important to develop an understanding of how
1832 experts view uncertainty about functional relationships among variables. To date, this has
1833 received rather less attention in most elicitation studies; however, several have attempted to pose
1834 questions that address such uncertainties.

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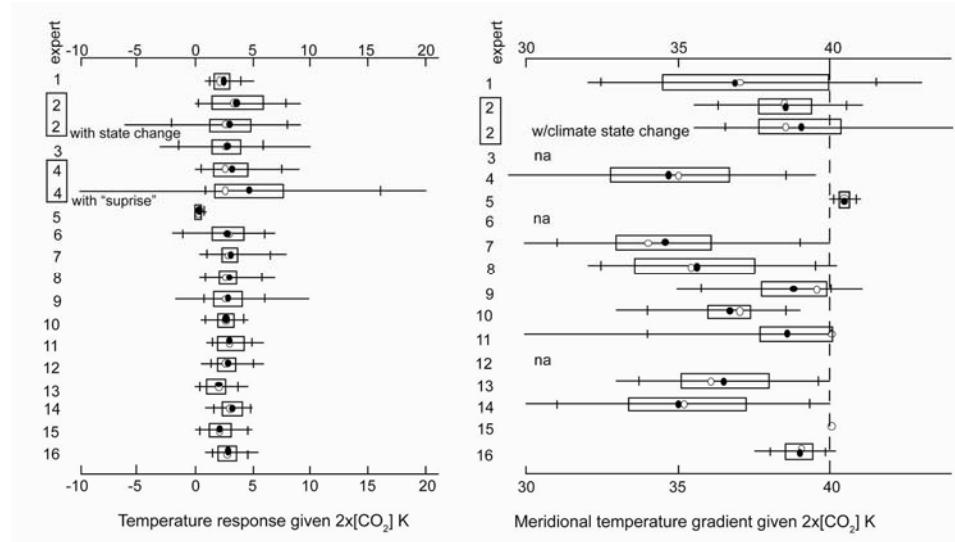


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1839 **Figure 5.1** The probability density function for climate sensitivity (ΔT at $2x$) estimated by Andronova and
1840 Schlesinger (2001). Using coupled atmosphere-ocean models, the observed near-surface temperature record and a
1841 bootstrap re-sampling technique, the authors examined the effect of natural variability and uncertainty in climatic
1842 radiative forcing on estimates of temperature change from the mid-19th century to the present. Their findings show a
1843 much wider range of climate sensitivity values to be consistent with our knowledge, than values presented in the
1844 IPCC Third Assessment. [Figure redrawn from Andronova and Schlesinger (2001).]

1845 Climate sensitivity:

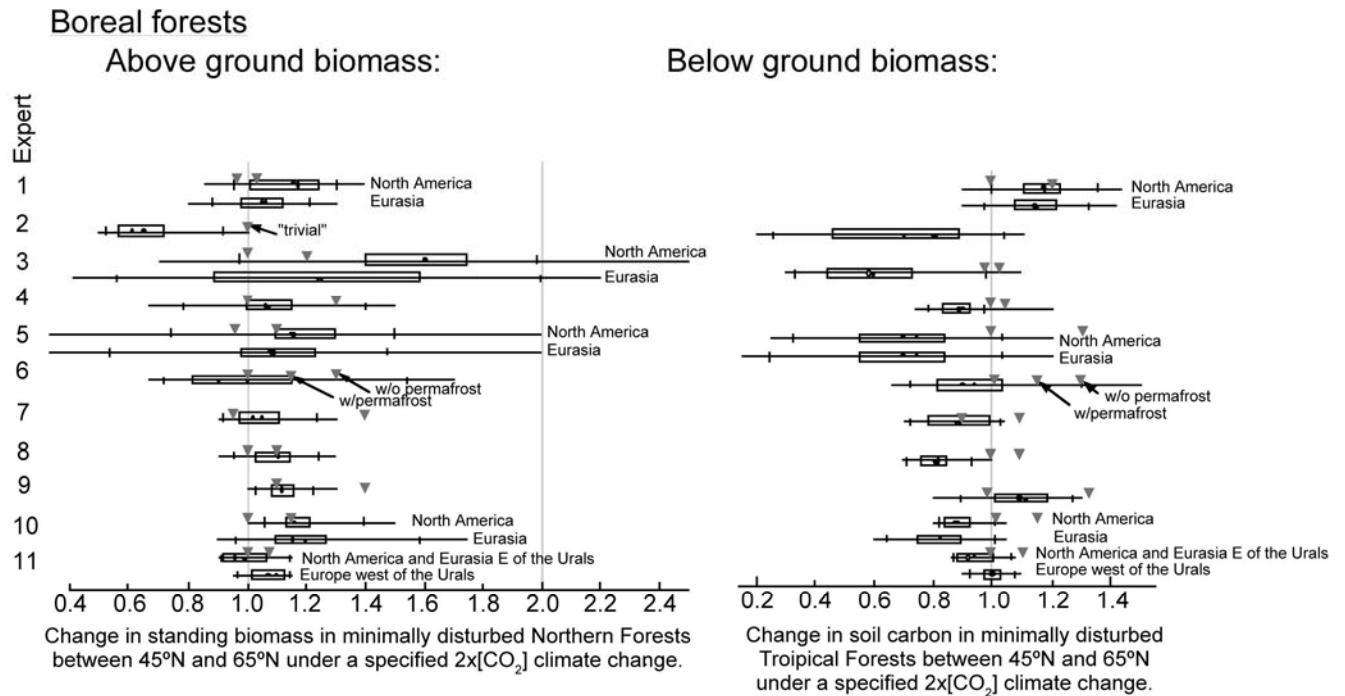
Pole-to-equator temperature gradient:



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1847 **Figure 5.2** Examples of results from expert elicitations conducted by Morgan and Keith (1995) reported as box
 1848 plots. Climate sensitivity is shown on the left and pole-to-equator temperature gradient on the right. Lines show the
 1849 full range of the distribution; vertical tick marks show the 0.95 confidence intervals; boxes report the 0.25 to 0.75
 1850 central interval; open dots are best estimates and closed dots are means of the distributions. While there is apparently
 1851 large agreement among all but one of the experts about the climate sensitivity, a quantity that has been widely
 1852 discussed, judgments about the closely related pole-to-equator temperature gradient show much greater inter-expert
 1853 variability.

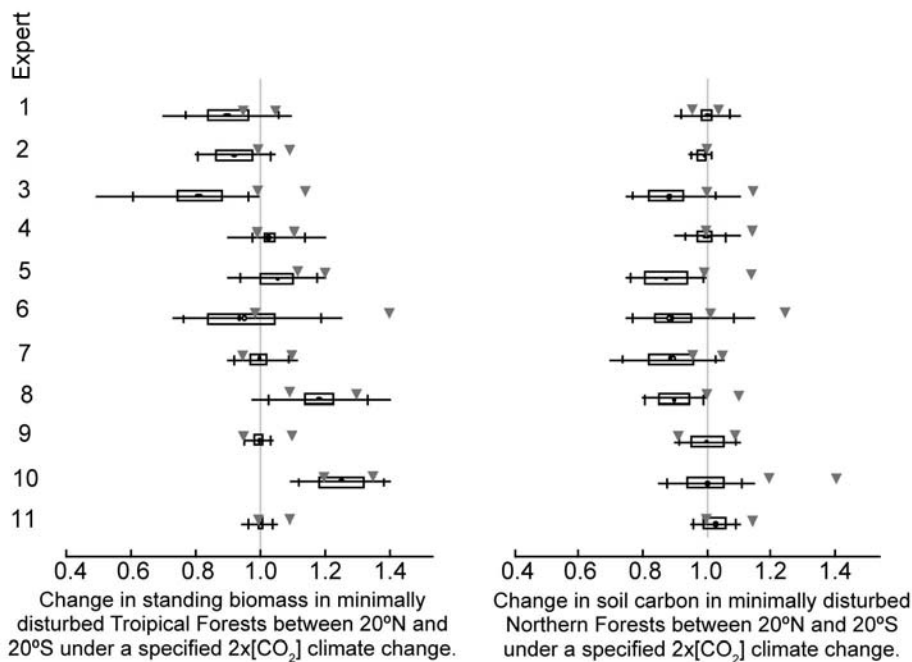
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Tropical forests

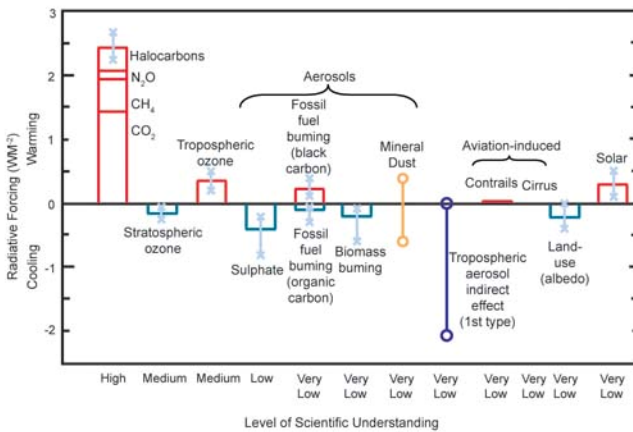
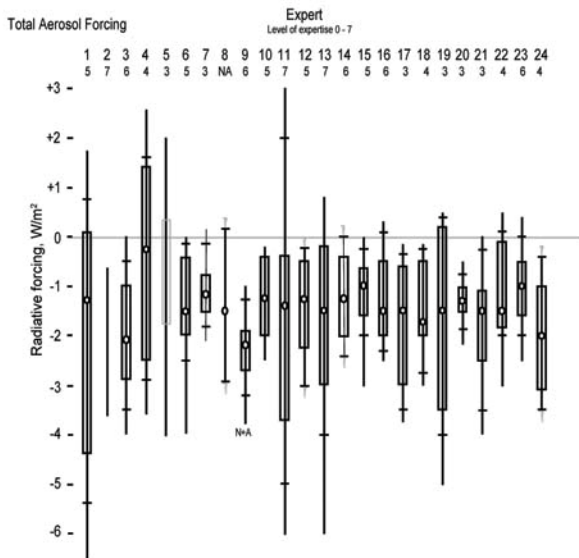
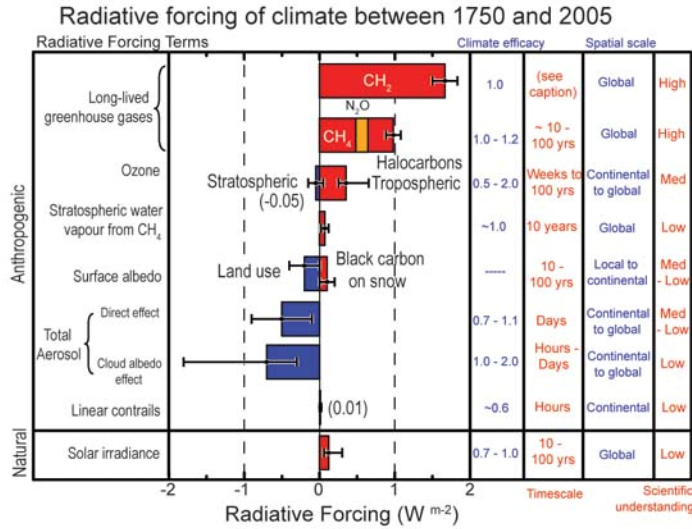
Above ground biomass:

Below ground biomass:



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Figure 5.3 Examples of results from expert elicitations of forest ecosystem experts on change in above and below ground biomass for a specified 2xCO₂ climate change forcing (Morgan *et al.*, 2001). Note that in several cases there is not even agreement about the sign of the impact on carbon stocks. Notation is the same as in Figure 4.2. Gray inverted triangles show ranges for changes due to doubling of atmospheric CO₂, excluding a climate effect.



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Figure 5.4 Comparison of estimates of aerosol forcing from the IPCC Third Assessment or TAR (bottom), an expert elicitation of 24 leading aerosol experts (center) and the IPCC Fourth Assessment or FAR (top). All radiative

1864 forcing scales (in W per m^2) are identical. In this example, one gains a rather different impression of the state of
1865 uncertainty from individual expert elicitations than is reflected in the consensus summary. Uncertainty ranges in the
1866 FAR are 90% confidence intervals. The horizontal tick marks on the box plots in center are also 90% confidence
1867 intervals. Note that 13 of the 24 experts (54%) interviewed produced lower 5% confidence value that are clearly
1868 below that of the FAR, and 7 out of 24 (29%) produced upper 5% confidence values above that of the FAR. This
1869 suggests that the consensus statement of uncertainty from FAR may be overconfident.
1870

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