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THE CANADIAN SECTOR OF THE MULTI-COUNTRY MODEL

by

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Introduction

The quarterly econometric model of Canada described in this paper is based on the prototype model of MCM presented in previous papers and in the forthcoming book, The U.S. Economy in an Interdependent World. $\frac{1}{}$ Few departures from the prototype specification were required to represent the functioning of the Canadian economy. The most critical area for adaptation of the prototype to Canada lay in the financial sector. The Canadian financial system is characterized by close linkage to U.S. financial markets. Consequently, Canadian interest rates have traditionally moved closely with U.S. interest rates. Because of this linkage, the Bank of Canada, in its RDX2 model, chose to model the process of interest rate determination by postulating a central bank reaction function for the shortterm interest rate. Thus, the application of the MCM prototype to Canada represents a departure from accepted procedure for an influential group of Canadian modelers and merits further discussion. The first part of this paper reviews the model's financial sector. The second and third parts present dynamic simulation results and selected multiplier responses that characterize the Canadian model.

The Canadian Financial Sector

Aside from the departure from the RDX2 interest-rate reaction function, several features of the Canadian financial system required adaptation in the prototype model:

(1) Canada has a secondary reserve requirement against time and demand deposits that is to be filled by Treasury bill holdings,

- (2) The bulk of Canadian foreign exchange reserves are not held by the Bank of Canada,
- (3) The reserve requirement is lagged, and
- (4) Borrowed reserves are a very small fraction of central bank assets $\frac{2}{}$

Secondary reserves. -- Most Canadian financial modelers do not seem to think that the secondary reserve requirement has been a binding condition. If it were, however, the requirement would add another component in the demand for Treasury bills. Suppose that the demand for Treasury bills in the absence of a secondary reserve requirement followed a conventional portfolio demand specification where the nonbank demand component is a function of private wealth, income, and rates of return and the bank demand component is a function of deposits (time plus demand), net of the cash reserve requirement and rates of return. Now, if a secondary reserve requirement is imposed, the banks' demand for Treasury bills is the maximum of either the conventional demand for Treasury bills or the secondary reserve ratio times total deposits.

Recall, however, that the MCM does not model the bond market. 3/
Hence, secondary reserves are important only insofar as they might affect
the demand for money or other assets (foreign short- or long-term capital
inflows and outflows). This indirect effect on the banks' demand for
money is probably small. Early tests for this effect by including the
secondary reserve requirement in the inverted free reserves equation
and the capital flow equations showed no significant effect.

Exchange Fund Account. -- The bulk of Canadian foreign exchange reserves are held in the Exchange Fund Account (EFA). Therefore, to get a meaningful

measure of net foreign assets in the monetary base equation, it is necessary to work with a balance sheet for the consolidated monetary authorities. (This was done for Japan also.) The consolidated account is generated from the balance sheets of the Bank of Canada (BOC) and the Exchange Fund Account (EFA). For our purposes the balance sheets can be written:

Bank of Canad	a (BOC)	Exchange Fund Account (EFA)						
Assets	Liabilities	Assets	Liabilities					
Net Foreign	Currency (CUR)	Net Foreign	Claims of the					
Assets (NFABOC)		Assets (NFAEFA)	Government of					
Net Government	Total Reserves (RT))	Canada on the EFA					
Position (NGPBOC)								
Borrowed								
Reserves (RB)								
Other Assets (OTH)								

The assets of the EFA are combined with those of the BOC to yield total foreign exchange reserves. The liabilities of the EFA are subtracted from the net government position of the BOC (NGPBOC) to obtain NBP of the consolidated monetary authorities (NGP = NGPBOC - NFAEFA).

Assets	Liabilities
NFA ⁴ /	CUR
NGP	RT
RB	
отн	

Within the framework of the consolidated monetary authorities, the sources and uses of the unborrowed monetary base are similar to those of the German and Japanese cases.

(1) Sources: BU \equiv NFA + NGP + OTH (net)

(2) Uses: BU \equiv RR + RF + CUR

where:

BU = unborrowed monetary base;

NFA = net foreign assets;

NGP = net government position;

OTH = other assets (net);

RR = required reserves;

RF = free reserves; and

CUR = currency.

Unlike the German and Japanese cases, vault cash is an eligible component of reserves and is included there. There is no need for the variable ${\rm CURB}^{6/}$, included in the prototype.

Canadian reserve requirements are much simpler than in the German and Japanese cases. There is no distinction by size of bank. Furthermore, the reserve requirement changed only once over the sample period. Unlike the U.S. monetary system, changes in reserve requirements are not used for monetary control. Prior to 1967, the primary reserve requirement on both demand and time deposits was held at 8 percent. After a 3 quarter transition period, the requirements were set to 12 percent for demand deposits and 4 percent for time deposits. This was a statutory change made for institutional purposes rather than monetary control.

Lagged reserve requirements.—Required reserves are actually based on average deposits over the four consecutive Wednesdays ending with the second last Wednesday of the previous month. The current averaging period for meeting reserve requirements is 15 days. Because U.S. reserve requirements are also lagged, this difference with respect to the prototype is one of degree. The reserves computed from end-of-month deposit data do not correspond to the "true" reserves based on deposits during the previous month. Required reserves are reported on a daily average basis for the month. All other items in the monetary base equation are reported on an end-of-month basis.

On a monthly basis, then, bank deposits are not at all tied to primary reserves. On a quarterly basis, however, a large component (roughly two-thirds) of required reseves are contemporaneous with bank deposits. The procedure in the MCM databank constructs mid-quarter averages of bank deposits and then computes required reserves from the statutory requirements. This computed reserve requirement is linked to the mid-quarter average of the reported daily-average required reserves with a bridge equation. The use of actual required reserves gives a better measure of free reserves than would computed required reserves for use in the inverted reserve identity.

Chartered banks. -- Reserves and time and demand deposits are obtained from the balance sheet of the chartered banks. In the Canadian case, the balance sheet was constructed according to a slightly disaggregated version of the balance sheet in the prototype model.

Chartered Banks

Assets	Liabilities
Required Reserves (RR)	Demand Deposits (DD)
Excess Reserves (RX) Total Reserves (RT)	Time Deposits (TD)
less: Required Reserves (-RR)	Borrowed Reserves (RB) (Includes purchase and resale
Long-term Securities (LTS)	agreements)
Short-term Securities (STS)	
Foreign Assets (net) (FA)	
Other Assets (OTHCH)	Net Worth (NWCH)

In this scheme of generating the data, NFA, NGP, RB, CUR, and RT come from the balance sheet of the Consolidated Monetary Authorities. RR, RX, DD, TD, SD are generated from the Chartered Bank balance sheet. It is useful to note that RR is obtained on a different basis from all the other data (daily average for the month). In terms of the balance sheet, assets still equal liabilities exactly because excess reserves are calculated as a residual from total reserves. RT, as all other items in the balance sheet except RR, is available on an end of month basis.

The apparent time pattern of reserve assets over the 15-day averaging period permits RR on a daily-average basis to exceed total reserves on an end-of-month basis. Computation of RX from RT-RR thus leads to negative excess reserves for most observations in the sample. Another difficulty with this procedure for creating data on excess reserves is that all the discrepancy between end-of-month and daily-average measurement of total reserves is picked up in RX. This discrepancy is then passed on to free reserves when RF is calculated as RX-RB. However, a discrepancy of some kind will always be present in RF because RB is also measured on an end-of-month basis.

The final difference between the prototype balance sheets and those for Canada relates to the importance of government securities held by the Chartered Banks under purchase and resale agreements (PRA). Holding eligible securities in a PRA is a legitimate means for a chartered bank to comply with its reserve requirement. In fact, borrowed reserves are very small in Canadian banking, and PRAs exceed borrowed reserves. Thus, in the MCM, FB is defined as borrowed reserves plus PRAs. This procedure requires the assumption that the spread between the purchase and resale price of the security is equivalent to the interest payment on borrowed reserves of the same magnitude at the bank rate (discount rate).

Monetary Sector. -- From this point on, the structure of the Canadian monetary sector follows closely that laid out for the prototype model.

RRC is computed from statutory reserve requirements as

(3) RRC = $a \cdot DD + b \cdot TD$

where a and b are the primary reserve requirements. The bridge equation is given by:

(4) RR = $\alpha + \beta RRC + \epsilon$

Substituting computed required reserves from (3) into the bridge equation (4) and that result into the uses of the unborrowed base (3) yields

(5) BU =
$$\hat{\alpha}$$
 + $\hat{\beta}$ aDD + $\hat{\beta}$ bTD + $\hat{\epsilon}$ + RF + CUR

Equation (5) can be expressed in terms of demand deposits.

(6)
$$DD = [BU - \hat{\alpha} - \hat{\beta} bTD - \hat{\epsilon} - RF - CUR]/\hat{\beta} a$$

Equation (6) is a rearrangement of the uses side of the monetary base equation. Given BU (from the sources side of the base, eq. (1)), reserve requirements a and b, and n-1 uses of reserves (RF and CUR), the stock of demand deposits that can be supported by the remaining reserves (RR) is determined.

The specifications of the equations determining the four components of equation (6) are as follows:

(7)
$$\frac{DD}{NW} = DD(GNPV/NW, RS, URS, (EE-E)/E)$$

Unlike the German case, there are no appreciable government holdings of time deposits. TD is composed of savings deposits (82% in 1969IV) and other notice deposits or "deposit receipts." Deposit receipts are sold in denominations of \$C 100,000 or more and are described as temporary repositories of excess balances of corporations, governments and other organizations. These corporate notice deposits seem essentially to be negotiable certificates of

deposit. Since government deposits could not have been more than part of the remaining 18 percent of time deposits in 1969, wealth (NW) is used as a scale variable for the aggregate TD equations. Savings deposits are not handled separately in the Canadian financial sector.

(8)
$$\frac{\text{TD}}{\text{NW}} = \text{TD} \text{ (GNPV/NW, RS, URS, (EE-E)/E)}$$

The equation for free reserves is of the same form as the prototype.

(9)
$$\frac{RF}{NDD}$$
 = RF(RS, RS-RD, URS, Δ RU, Δ RR)

where:

NDD \equiv (1 - $\hat{\beta}$ a) DD, net demand deposits;

URS = U.S. short-term interest rate;

RU ≡ BU - CUR and, unborrowed reserves; and

 $\Delta RR = \Delta a(DD_{-1}) + \Delta b(TD_{-1})$, change in required reserves.

ARR is zero except for a transition period of 3 quarters in 1967 when reserve requirements were changed from a uniform 8 percent to 12 percent on DD and 4 percent on TD. The sign pattern in equation (9) is important for determining the eventual sign on the U.S. short-term interest rate in the Canadian interest rate equation. Borrowed reserves including purchase and resale agreements (PRA) are a negative component of free reserves. Borrowed reserves and PRAs will increase with an increase in the domestic or foreign (U.S.) short-term interest rate, so both the domestic and U.S. short-term rates carry a negative sign.

Public holdings of currency are a simple function of consumption (as a proxy for transactions) and the short-term interest rate.

(10) CUR = CUR(CV, RS)

A term-structure equation explains the long-term interest rate.

(11)
$$RL = RL(RS, RS_{-1}, ..., RS_{-n})$$

Five behavioral equations (7) - (11) along with (1) and (6) are used to determine BU, DD, TD, RF, CUR, and RL.

Reduced form interest rate equation.—In estimating the Canadian monetary sector, equation (9) for free reserves was normalized on the short-term interest rate. In this respect, the MCM monetary sector is similar to that of RDX2. But because RF is tied to the monetary base equations, there is a difference in the signs of arguments in the interest rate equation and, indeed, in the roles the equations perform in their respective models. When inverted, equation (9) takes the form

(12)
$$RS_{MCM} = f(RS(-1), RD, URS, RF/NDD, ...)$$

The U.S. interest rate enters with a negative sign because the return on U.S. securities represents an opportunity cost of excess reserves in the free reserve equation. Using the same mnemonics, the key conceptual elements of the RDX2 short-term interest rate equation can be written as

⁽¹³⁾ $RS_{RDX2} = f(RS(-1), JRS, chartered bank loans, private holdings of government securities)$

Emprical testing revealed that the Canadian short-term interest rate behaved somewhat differently when the discount rate acted as a penalty rate (RD > RS) than when short-term rates exceeded the discount rate. There are two versions of equation (12) in the MCM, each is switched on during its respective regime. $\frac{7}{}$ In the penalty-rate regime, the U.S. short-term rate enters the inverted free reserve equation (with a small negative coefficient). In the regime where the discount rate was less that the short-term rate, the U.S. interest rate does not enter the equation at all. The small direct presence of the U.S. interest rate in the MCM equation contrasts sharply with the dominant presence of the U.S. rate in the RDX2 equation. This has important structural ramifications for the functioning of the model. In the MCM, changes in the U.S. interest rate alter the differential between U.S. and Canadian interest rates, cause a capital flow, a change in the level of foreign exchange holdings, thereby affecting the sources of the monetary base and free reserves (on the uses side of the monetary base) and, in this way, cause a change in Canadian interest rates. In the RDX2 approach, the U.S. effect occurs directly via the reduced form equation, thus, circumventing these important channels of financial flow. The three key differences in the two interest rate functions can be summarized as:

(1) The MCM makes use of the discount rate as one of three policy instruments whereas RDX2 does not. Canadian scholars argue that borrowed reserves and PRAs are a very small share of financial flows and constitute an unreliable link to interest rates. We argue that while smallness may cause estimation problems, the link to the monetary base exists. We also argue that the market rate functions as a signal mechanism much as the discount rate in the United States.

- in the MCM interest rate equation whereas it appears with a large (0.5) positive sign in the RDX2 equation. While the linkages between the U.S. and Canadian financial markets are strong and the total effect of U.S. rates on Canadian rates must be positive (as shown in the multiplier experiments to follow), the MCM equation is a structural representation in that it captures the substitution effect between U.S. and Canadian assets. When U.S. rates increase, free reserves should decline as indicated in equation (9). But for a ceteris paribus interpretation of equation (12), holding free reserves constant would require an expansion of the Canadian monetary base resulting in a decrease in the Canadian short-term interest rate.
- reserves in the MCM transmit the portfolio effects of changes in foreign financial conditions, via capital flows and changes in foreign exchange holdings, to the Canadian short-term interest rate. As far as responsiveness to Candian policy instruments, the RDX2 interest rate equation responds only indirectly through portfolio holdings (bank loans and private holdings of government securities). Thus, while the MCM may be vulnerable through the small size and volatility of free reserves, the RDX2 structure depends crucially on the ability to model dependably the domestic short- and long-term securities markets. Additionally, while small size and volatility could cause some difficulties in dynamic tracking performance, once the model is aligned on a solution path, the dependability of multipliers depends upon estimation accuracy and the fidelity of the model

structure. On this count we had a decided preference for the monetary base approach over the reduced-form reaction function approach taken in RDX2. In estimation, the discount rate tends to dominate (and stabilize) the MCM short-term interest rate equation while the U.S. rate performs the same function in the RDX2 equation.

The verdict clearly remains open on these two approaches to interest rate determination in the Canadian economy. The MCM approach represents a conscious risk on estimation and tracking performance (although these are not decidedly inferior to other Canadian results as can be seen in the results of the following section) in order to attempt a structural representation of the interdependence between domestic and international financial flows. It is hoped that this work will stimulate additional efforts on structural modeling of the Canadian financial system.

Reaction functions. -- Because the model's sample period spanned both fixed and floating rate regimes, different operating rules for the financial authorities were invoked. During the fixed exchange rate period (1961I to 1970 II), the model allows changes in foreign exchange reserves to be determined from the balance of payments identity. Because uncompensated reserve changes during a fixed-rate regime would cause severe fluctuations in the monetary base, we tested for central bank behavior attempting some degree of sterilization of the foreign flows. Systematic partial offset (-.46) of foreign exchange reserves was observed in the equation for changes in the open market position of the monetary authorities.

During the floating exchange rate regime, a stabilizing reaction of "leaning against the wind" to dampen exchange rate fluctuations was observed.

Expected exchange rate changes were resisted by foreign exchange market intervention. The stock of foreign exchange reserves entered the equation with a negative sign representing an "ability to intervene". $\frac{8}{}$ Both these functions were operating during the dynamic simulation of and shocks to the model analyzed in the following sections.

Expected exchange rate.—Another significant difference from the specification of the prototype model occurs in the treatment of the expected future spot exchange rate (equation 31a of the prototype, see IFDP No. 115, p. 68). For the fixed exchange rate regime, the Canadian equation uses the product of the relative Canadian export price and net foreign assets scaled by the value of imports, just as specified in the prototype model.

For the floating exchange rate regime, however, the Canadian model uses the specification originally sought in the MCM. The expected future spot rate is assumed to equal the actual spot rate observed one quarter ahead plus a random error. Only for Canada did this specification provide good estimation results. In simulation of the model, the value of the spot rate one period ahead is replaced by an estimated value obtained from a regression using past exchange rates and changes in net foreign assets as explanatory variables (see ELEAD in the equation list of the appendix to this paper).

Analysis of Errors

The equations of the prototype model, modified in the financial sector and the expected exchange rate equation as described above, were estimated with quarterly Canadian data from the first quarter of 1961 to the fourth quarter of 1975. Ordinary least squares regressions were employed for estimation. Thus, the equation estimates may be subject to simultaneous equation bias.

In-sample tracking. -- The Canadian model by itself was simulated dynamically over the eleven-year period between the fourth quarter of 1964 and the fourth quarter of 1975. This simulation period spans both fixed and floating exchange rate regimes. The first column of Table 1 presents the mean percentage errors and the root mean squared percentage errors for key variables in the sample period; the second column presents the same statistics for the five-quarter post-sample period available at the time the model was tested before inclusion in the MCM.

In-sample errors are, by and large, within the range of acceptable error for medium-sized macroeconomic models. The root mean square percentage error (RMSE) for GNP is 2.4 percent over the 45 quarter sample period. This error falls within the bounds for other MCM models winc range from 2.4 percent for the U.S. model to 4.4 percent for the German model. It compares favorably with the 1.7 percent in-sample error of the RDX2 model of the Bank of Canada. The domestic absorption deflator tracks very well at a RMSE of 0.6 percent, the lowest of the MCM models. Unemployment rates, being a residual number, normally track with a RMSE in the double-digit range; the Canadian model's RMSE for the unemployment rate is 14.1 percent, the lowest of the MCM models.

The interest rate performs worse than the other domestic variables. While interest rate equations normally track on the high side of other variables, the RMSE of 26 percent is the highest of the errors for MCM interest rates This RMSE compares unfavorably with the 6.8 percent error observed for the RDX2 model. $\frac{9}{}$ The tracking properties of the Canadian interest rate could have been improved considerably by linking the rate directly to the U.S. short-term interest rate. But as explained in the previous section on the financial sector, this approach was eschewed in favor of the specification

Table 1 Dynamic Simulation of the Canadian Model in Isolation from the MCM

<u>Variables</u>		In-Sample Errors	Post-Sample Errors
		64:4-75:4	76:177:1
GNP	· ME ¹	0.087	0.3787
	RMSE ²	2.403	1.403
P	ME	0.161	-0.324
	RMSE	0.633	0.600
CU	ME	0.428	-0.659
	RMSE	3.980	1.067
UN	ME	2.705	-8.896
	RMSE	14.130	12.798
RS	ME	-8.683	16.170
	RMSE	26.064	17.494
MG	ME	-0.554	0.055
	RMSE	6.660	3.630
MGV	ME	-0.490	9.321
	RMSE	5.821	12.959
PMGUV	ME	0.178	9.094
	RMSE	2.557	10.612
XG	ME	-0.232	5.076
	RMSE	1.208	7.393
PXGUV	ME	0.214	9.775
	RMSE	2.200	10.616
E .	ME	1.044	-10.062
	RMSE	2.512	10.765
NFAEOQ	ME	39.732	-22.402
	RMSE	57.732	23.713

¹Mean percentage error.

 $^{^{2}\}mathrm{Root}$ mean squared percentage error.

that linked interest rate determination more directly to the monetary base.

While Canadian exchange rate tracking was good over the sample period with a RMSE of 2.5 percent, the error on the stock of foreign exchange reserves (NFAEOQ) was the highest of all the MCM models at 58 percent. In a simultaneous system it is difficult to establish cause and effect, but the large error on foreign exchange reserves disrupts the monetary base and the interest rate. Correspondingly, large errors in the interest rate cause large errors in capital flows and the change in foreign exchange reserves.

Exports track more closely during the sample period (1.2 percent) than do imports (6.6 percent) largely because foreign activity is exogenous and only the export price and exchange rate are subject to solution error. For imports, the exchange rate and domestic activity are simultaneous. Because the GNP tracking errors (2.4 percent) are larger than those for domestic prices (0.6 percent), imports tend to be thrown off track more than exports.

Post-sample tracking. -- Except for the exchange rate and the trade flows affected by it, tracking errors are smaller in the post-sample period than in the sample period. The GNP and interest rate errors decrease to 1.4 percent and 12.8 percent, respectively. The exchange rate error increases to 10.7 percent, and because it affects the relative competitiveness of exports, the errors on exports increase to 7.4 percent. Evidently the individual errors on the exchange rate and GNF are offsetting because the import error declines to 3.6 percent in the post-sample period. Although the post-sample period is relatively short, the goodness of the tracking errors outside the estimation period indicates that the model is a reliable representation of the Canadian economy in the mid-1970s.

Multipliers of the Canadian Model

The multipliers presented in this section were calculated by comparing a solution of the Canadian model that was aligned to history by adding the regression residuals to the estimated equations with a solution using the same regression residuals and a change in the policy instrument. These multipliers solutions were made with the Canadian model in isolation from the rest of the MCM; that is, all foreign variables remained exogenous.

The single-model multipliers presented here differ from those of the MCM version of the model in one crucial aspect. The single model results were obtained with an aggregate export equation used before the MCM bilateral trade system was completed. This is a significant difference in the case of the Canadian model because the export price elasticities in the two trade systems differed significantly. The aggregate export equation had an export price elasticity of -0.73, whereas the trade-weighted average of the bilateral price elasticities was -1.08. With the lower export price elasticity, these multipliers using the aggregate export equation are larger than those of the final MCM version using the bilateral trade equations.

In that the multipliers depend on the magnitudes of activity and prices existing in the period for which the model is solved, it is useful to recall the economic environment between 1973 and 1975. In late 1974 Canada and the rest of the world economy entered a recession. The general effect of this environment on the multiplier paths studied here is a downward bias in the initial real effects and an upward bias in the initial price effects of an economic stimulus.

Government spending.—Table 2 presents key multipliers for a sustained increase in real government purchases of \$C 1 billion. The real GNP multiplier starts from 1.013 and increases to 1.428 by the end of the two-year period. The price level also increases steadily over the two-year period to a maximum of 28 percentage points higher than its historical value.

The effect of the increase in government spending on the unemployment rate peaks at a reduction of .192 percentage points three quarters after the fiscal stimulus begins. Thereafter, the unemployment rate remains below that of the control baseline, but the difference oscillates slightly before diminshing in the eleventh period. The early peak is due to the productivity effects of the increase in investment. In the early periods, the rise in investment affects the capital stock only slightly, most of the increased output must come from added labor. As the stimulus continues, the capital stock becomes larger than otherwise and productivity increases. Additionally, the increase in economic activity draws new entrants into the labor force and puts upward pressure on the unemployment rate. These countervailing effects turn back the path of the decline in the unemployment rate and cause its oscillation.

The added activity creates increased loan demand. Since monetary policy remains unchanged with the fiscal stimulus, the added loan demand leads to a steady increase in the short-term interest rate. By the end of 11 quarters, the interest rate is 1.3 percentage points above that of the control path.

The stimulus to activity draws in a large and increasing flow of imports. Table 3 presents the historical levels for the selected multiplier responses reported in this section. With a base level of imports (in current dollar terms) of \$C 47.6 billion, the increase of \$C 1.9 billion amounts to a 4 percent increase in the value of imports after 11 periods.

Table 2

Effects of a \$C 1 billion Increase in Real Government Purchases of Goods and Services (1972 dollars)

		1973			. , 1	974		1975				
,	2	3	4	1	2	3	4	1	2	3	4	
GNP 1	1.013	1.066	1.106	1.108	1.145	1.167	1.287	1.310	1.362	1.400	1.428	
P ²	.001	.002	.004	.006	.007	.010	.013	.017	.021	.025	.028	
אט 3	136	192	192	170	159	150	113	088	111	129	090	
RS ³	.115	.258	. 384	.541	.740	. 895	.946	.3925	.418 ⁵	.555	1.309	
MGSNIVS ¹	. 336							1.621				
E ⁴	001	005	009	012	015	019	022	030	034	035	031	

billions of Canadian dollars, annual rate.

² 1972 = 1.00

Percentage points.

U.S. dollars per Canadian dollar, 1972 = 1.0.

This drop in the interest rate effect is spurious. It occurs historically at a point where the interest rate equation experiences a behavioral shift between discount rate regimes. See discussion of the two interest rate equations above in the financial sector of this paper. The 50-odd basis point drop is related to the first quarter of 1975 and not to the eighth period after the fiscal stimulus.

Table 3

Historical Values for Key Variables in Canadian Multiplier Experiments

		1973		1974				1975			
į	2	3	4	1	2	3	4	1	2	3	4
GNP ¹	112.0	113.1	116.1	117.8	117.4	117.2	116.9	116.7	117.9	119.6	120.0
p ²	1.067	1.089	1.118	1.152	1.200	1.249	1.284	1.329	1.353	1.388	1.416
UN 3	5.45	5.38	5.57	5.30	5.23	5.20	5.53	6.55	6.95	7.07	7.07
R5 ⁴	6,27	8.20	9.43	9.20	11.00	11.60	10.20	7.43	7.27	8.09	9.10
HG\$NIVS ¹	31.6	29.3	34.8	35.4	41.6	40.9	46.0	43.3	47.7	43.4	47.6
8 4	.991	.987	.991	1.011	1.026	1.010	1.004	.992	.969	.961	.975

¹ billions of Canadian dollars, annual rate.

 $^{^{2}}$ 1972 = 1.00

³ Percentage points.

U.S. dollars per Canadian dollar, 1972 = 1.0.

Under the fiscal stimulus, the capital inflow resulting from portfolio rebalancing in response to the widening of the Canadian interest rate differential is not sufficient to offset the currency outflows resulting from the increase in imports. Consequently, the Canadian dollar depreciates steadily over the period, reaching a peak of 3.5 percentage points 10 quarters after introducing the stimulus.

Taxes.--Table 4 presents the multipliers for a 1 billion (current Canadian dollars) increase in personal income taxes. The multipliers are all smaller (in absolute magnitude) than those for the increase in government spending because the tax increase of \$C l billion in current dollars is less than \$C l billion in constant dollars and because the increase in tax revenues affects GNP indirectly by changing disposable income. The patterns on the GNP and price paths are similar (with opposite sign) to those of the government spending increase. The unemployment rate effect, however, peaks in the sixth quarter after the stimulus rather than the third. This is most likely the result of smaller productivity effects than in the case of the larger fiscal stimulus.

Interest rates decline because of the slackening in loan demand. The narrowing interest differential and \$C 1.2 billion decrease in imports lead to an appreciation of the Canadian dollar. As the fiscal restraint is about 1/3 the magnitude of the fiscal stimulus (measured by the change in GNP), so is the appreciation of the Canadian dollar about 2/3 the size of the depreciation under the stimulus.

Monetary policy. -- The contractionary effects of a tightening in Canadian monetary policy are shown in Table 5 with a one percentage point increase in the discount rate. GNP eventually declines by one half billion Canadian dollars

Effects of a \$C l billion Increase in Personal Tax Revenues (current dollars)

Table 4

		1973		; ; ;	1974			1975			
	2	3	4	1	2	3	4	1	2	3	4
GNP ¹	207	347	489	612	724	748	825	881	925	936	971
p ²	0.000	001	001	002	004	005	007	010	013	015	017
un ³	.028	4.058	.096	.114	. 129	.133	.129	.116	.114	.111	.092
rs ⁴	037	097	172	262	381	482	589	234 ⁵	260 ⁵	352 ⁵	853
mgsnivs ¹	085	170	268	398	541	709	842	-1.001	-1.140	-1.225	-1.262
E ⁴	.001	.003	.004	.006	.008	.011	.014	.020	.028	.023	.021

billions of Canadian dollars, annual rate.

 $^{^{2}}$ 1972 = 1.0.

Percentage points.

⁴ U.S. dollars per Canadian dollar, 1972 = 1.0.

⁵ This drop in the interest rate effect is spurious. It occurs historically at a point where the interest rate equation experiences a behavioral shift between discount rate regimes. See discussion of the two interest rate equations above in the financial sector of this paper. The 50-odd basis point drop is related to the first quarter of 1975 and not to the eighth period after the fiscal stimulus.

Table 5

Effects of a One Percentage Point Increase in the Canadian Discount Rate (Bank Rate)

		1973			19	74			197	75	
	2	3	4	1	2	3	4	1	2	3	4
GNP ¹	090	130	163	217	266	319	377	413	452	481	507
P ²	001	001	002	002	002	003	004	005	006	007	008
UN ³	.010	.031	.046	.051	.048	.049	.049	.044	.047	.051	.049
rs ⁴	. 835	.907	.840	. 805	.798	.798	.798	.812	.871	.823	.630 ⁵
mgnivs ¹	048	072	077	104	171	266	3 60 ,	489	509	→.559	-,588
E ⁴	.006	.007	.005	.003	.003	.005	,006	.009	.010	,011	.010

billions of Canadian dollars, annual rate.

 $[\]frac{2}{1972} = 1.0$

³ Percentage points.

 $^{^4}$ U.S. dollars per Canadian dollar, 1972 = 1.0.

In this experiment, the discount did not exceed the short-term rate until the last quarter of 1975, so the switch of interest rate equations occurred here rather than in the first quarter. Like the previous multiplier responses, the drop in the interest rate response is the result of switching between interest rate equations and not the number of periods after the introduction of the shock.

eleven periods after the increase in the discount rate. In response to this decline in activity, the domestic price level falls slowly at first, eventually declining six tenths of one percent below its base level at the end of 11 quarters. Unemployment increases by one-half percentage point four quarters afer the monetary contraction begins and then fluctuates slightly about that change for the remainder of the period.

The short-term interest rate increases 83 basis points initially, and then by 90 basis points in the second quarter. As activity and loan demand slow, the increase in the short-term interest rate drops back to the 80 basis point range for the remainder of the period. In response to both the slowing of imports and capital inflows responding to the widening of the Canadian-foreign interest rate differential, the Canadian dollar appreciates by roughly 10 percent at the end of two years.

Foreign interest rates.—The final experiment presented for the floating exchange rate period tests the effects of a 100 basis point increase in the U.S. short-term rate accompanied by a 70 basis point increase in the Eurodollar rate. Table 6 presents the multiplier responses indicating that the narrowing of the Canadian-foreign interest rate differential leads intially to a 0.7 percent depreciation of the Canadian dollar. As a result of the depreciation the import price in local currency increases and real imports decrease. The average import price elasticity is less than one, however, (the import price elasticities for the United States and the rest of the world are 0.6 and 0.3, respectively) so the value of imports increases by 0.3 percent in the initial period. As the size of the depreciation diminishes over time, so does the increase in the value of imports.

Table 6

Effects of an Increase in Foreign Interest Rates (100 basis points in the U.S. Short-term rate and 70 basis points in the Eurodollar rate).

	1 1	1973			. 19:	74		1975			
	2	3	4	1	2	3	4	1	2	3	4
GNP ¹	.007	.030	.045	.061	.048	.032	.017	.018	.013	.015	.011
p ²	.001	.001	.001	.001	.001	.001	.001	.002	.002	.002	.001
un ³	.001	014	025	024	014	006	.001	.010	.014	.011	.006
RS ⁴	.054	.114	. 169	. 145	.086	.045	.028	119 ⁵	129 ⁵	120 ⁵	009 ⁵
MGSNIVS 1	.127	.122	.078	.062	.062	.065	.053	.052	.049	.036	.026
E	004	006	003	001	001	001	001	002	001	061	0

billions of Canadian dollars, annual rate.

 $^{^{2}}$ 1972 = 1.0.

Percentage points.

U.S. dollars per Canadian dollar, 1972 = 1.0.

In this experiment, the discount did not exceed the short-term rate until the last quarter of 1975, so the switch of interest rate equations occurred here rather than in the first quarter. Like the previous multiplier responses, the drop in the interest rate response is the result of switching between interest rate equations and not the number of periods after the introduction of the shock.

Export volume increases as a result of the depreciation and acts as a stimulus to GNP. The domestic price level increases slightly in response to the increase in domestic activity.

The depreciation is caused by the narrowing of the Canadian-foreign interest rate differential. The resulting portfolio readjustment results in capital outflows from Canada. These outflows reduce the monetary base. The intervention reaction function which resists the depreciation also results in a reduction in the monetary base. The reduction in the base, in turn, results in a small increase in the Canadian interest rate which peaks at 17 basis points three quarters after the increase in foreign interest rates.

Revaluation of the Canadian dollar.—The final experiment presented in this section explores the effects of a 10 percent revaluation of the Canadian dollar. The experiment was performed during the fixed exchange rate period to illustrate the properties of the Canadian model operating as a fixed exchange rate system. $\frac{10}{}$ The exchange rate index had the value of .920 (1972 = 1.0) in the first quarter of 1967, so the exchange rate was increased by .092 for the duration of the experiment.

The contractionary effects are best traced through the trade response first. By raising the relative price of Canadian exports and reducing the relative price of imports, the trade balance in real terms is reduced. As indicated in the last two rows of Table 7, the responses on exports and imports are initially similar in magnitude. But by the fourth period after the shock, the decline in exports is about twice the size of the increase in imports. The resulting increase in the trade deficit is reinforced by a decrease in capital inflows.

Effects of a 10 percent Revaluation of the Canadian Dollar

Table 7

	•	19	967			. 19	068		1969			
	1	2	3	4	1	2	3	4	1	2	3	4
GNP 1	009	107	205	251	227	218	407	029	613	495	689	597
p ²	006	012	017	021	024	027	030	032	034	036	038	040
UN ³	126	.056	.145	.273	.338	.381	.401	.418	. 382	.409	. 395	.118
RS ⁴	103	. 346	.642	.949	. 386	.494	1.33	1.69	1.82	2.26	2.12	2.09
MGSNIVS 1	781	757	743	786	-1.04	-1.09	-1.17	-1.26	-1.58	-1.6 1	-1.80	-1.97
E ⁴	.092	.092	.092	.092	.092	.092	.092	.092	.092	.05.2	.092	.092
,								7				
DNFA ¹	-1.08	781	-1.03	971	-1.34	924	598	676	796	472	723	541
MG ¹	.312	.520	.512	.546	.516	.543	.444	.597	.407	.459	. 368	.409
xg ¹	.035	481	679	970	-1.03	-1.16	-1.06	-1.15	-1.05	-1.13	-1.03	-1.17
ī								ı				

billions of Canadian dollars, annual rate.

 $[\]frac{2}{1972} = 1.0.$

Percentage points.

 $^{^4}$ U.S. dollars per Canadian dollar, 1972 = 1.0.

In this experiment, the discount did not exceed the short-term rate until the last quarter of 1975, so the switch of interest rate equations occurred here rather than in the first quarter. Like the previous multiplier responses, the drop in the interest rate response is the result of switching between interest rate equations and no the number of periods after the introduction of the shock.

The expected exchange rate function during a fixed exchange rate regime in the Canadian model is an inverse function of the Canadian export price. 11/With an exogenous revaluation of the currency, the relative export price increases and agents' expectations of a future devaluation increase. With these expectations, capital inflows decrease and contribute to the decline in exchange rate reserves.

In response to the contraction in the monetary base resulting from the decline in the stock of reserves, the interest rate increases by 94 basis points at the end of the first year. Since the effect on the monetary base is cumulative, the three-year continuation of an increased trade deficit and decreased capital inflows eventually lead to an increase in the short-term interest rate on the order of 200 basis points.

The increases in both the trade deficit and the interest rate reinforce each other in reducing the level of GNP. The effect is small initally and increases to the order of \$C 0.6 billion at the end of three years. The domestic price level declines accordingly. Corresponding to the decline in activity, the unemployment rate increases, eventually by 0.4 percentage points. The initial decline in the unemployment rate is the result of an initial decline in the real wage resulting from a larger decrease in nominal GNP than in the money wage.

Footnotes

- $\frac{*}{}$ The work described in this paper was carried out while I was an Economist in the International Finance Division. I am very grateful to John Boschen and Joseph Formoso for their important contributions to the construction and testing of the Canadian model. The views expressed in this paper are mine and do not necessarily represent the views of the Federal Reserve System.
- 1/ The book will be published by the Board of Governors of the Federal Reserve System in late 1982. See also Richard Berner, et al., "Modeling the International Influences on the U.S. Economy: A Multi-Country Approach" (IFDP No. 93) and Richard Berner, et. al. "A Multi-Country Model of the International Influences on the U.S. Economy: Preliminary Results," (IFDP No. 115).
- 2/ For a useful presentation of Canadian central banking and the financial system see D. E. Bond and R. A. Sherer The Economics of the Canadian Financial System: Theory, Policy and Institutions Prentice Hall Canada Scarborough: Ontario 1972, especially chaps. 16-18.
- $\frac{3}{1}$ Refer to the arguments in IFDP No. 98 (pp. 32-37) for the justification behind the substitution of the balance of payments conditions for the bond market.
- 4/ NFA (which excludes valuation adjustments and SDR allocations) is constructed by accumulating CDNFA (D50712 D50710) from 19731V benchmark. The benchmark is B3800 (total reserves) converted to \$C by CE x 1.00937. The 1973IV benchmark is chosen for consistency with the stocks of international claims and liabilities. The fourth quarter of 1973 was the latest date for Canada's balance of international indebtedness (Cat. 67-202, Table 1, pp. 72-73) at the time of constructing the MCM databank.
- 5/ Borrowed reserves, RB, consist of advances to chartered and savings banks plus bankers acceptance plus GOC securities held under repurchase agreements (B209). This last item is netted out from the BOC holdings of own advances to chartered banks, B658, appears as ADV.
- 6/ Currency held by banks (B252) counts as a reserve asset. Total reserves are B608 = B252 + B255. Comparison of B603 for Jan. 75 end-of-month (3370) with B819, actual reserves of chartered banks, for daily average for second half of Jan. 75 (3571) verifies this. There is no need to handle vault cash separately.
- $\frac{7}{\text{different}}$ two versions have the effect of giving different elasticities over different time periods. This problem shows up in the multiplier responses of Tables 2 through 7.
- 8/ Purchase of foreign exchange reserves to resist an expected appreciation of the Canadian dollar will be lower, as the stock of foreign exchange reserves is higher. Note that this intervention function also behaves as if it were specified as a "target level of reserves" function.

- 9/ "The Equations of RDX2 Revised and Estimated to 4Q72", Bank of Canada Technical Report 5, 1967, pp. 262, 263.
- 10/ The MCM models can be operated as both fixed and floating exchange rate systems. When fixed, the exchange rate is declared exogenous and the change in reserves is declared endogenous. When solved as a floating rate system, the exchange rate is declared endogenous and the change in reserve is declared exogenous or explained behaviorally with and additional intervention function.
- 11/ See equation 31a and related discussion in IFDP No. 115, pp. 12, 68.

Appendix

The Equations of the Canadian Sector of the Multi-Country Model

I.	List of behavioral equations
II.	Behavioral equations
III.	IdentitiesA-63
IV.	Sources and definitions of variablesA-69

LIST OF BEHAVIORAL EQUATIONS

		PAGE
Α.	Domestic expenditure sector	
	Disposable income bridge	A-5
	Consumption function	A-6
	Private fixed investment	A-7
	Inventory investment	A-8
	Capital consumption allowance	A-9
В.	Government sector	
	Tax functions:	
	Personal	A-10
	Nonresidential	A-11
	Corporate	A-12
	Government transfers	A-14
c.	Current account	
	Exports of goods: bridge equation (customs clearance basis to balance of payments basis)	A-15
	Imports of goods: bridge equation (customs clearance basis to balance of payment basis)	A-16
	Bilateral import demand functions:	
	Imports from Germany	A-17
	Imports from Japan	A-18
	Imports from the rest-of-the-world	A-19
•	Imports from the United Kingdom	A-20
	Imports from the United States	A-21

		PAGE
Bilateral bridge equation:		
Imports from Germany		A22
Imports from Japan		A23
Imports from the rest-of-the-world	y	A24
Imports from the United Kingdom	egwin (*)	A25
Imports from the United States	¥	A26
Exports of goods (volume)	**************************************	A27
Exports of other services		A28
Imports of other services		A29
Exports of goods and services: bridge equation		
(balance of payments basis to national income accounts basis)		A30
Imports of goods and services: bridge equation (balance of payments basis to national income		
accounts basis)	•	A31
Transfer receipts	1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -	A32
Transfer payments		A33
Investment income receipts		A34
Investment income payments		A35
D. Price determination and capacity utilization		
Domestic price (absorption deflator)	· · · · · · · · · · · · · · · · · · ·	A36
Export unit value		A37
Import unit value		A38
Service deflator, exports		A39
Service deflator, imports		A40
Capacity utilization		A41

		PAGE
Ε.	Labor Market	
	Wages	A-42
	Wage Bill	A-43
	Employment	A-44
	Labor force participation	A-45
F.	Domestic asset demand and interest rate determination	
	Demand deposits	A-46
	Savings deposits	A-47
	Notice deposits	A-48
	Currency	A-49
	Required reserves	A-50
	Short-term interest rate	
	When short-term rate exceeds the discount rate	A-51
	When the discount rate exceeds short-term rate	A-52
	Long-term interest rate	A-53
G.	Capital Movements, official reserves, forward and led exchange rates	
	Errors and omissions	A-54
	Change in short-term liabilities	A-55
	Change in short-term claims	A-56
	Change in long-term liabilities	A-57
	Change in long-term claims	A-58
	Forward exchange rate	A-59
	Led exchange rate	A-60

		PAGE
G.	Capital Movements, official reserves, forward and led exchange rates (continued)	
	Reaction function for change in net foreign assets	A-61
	Reaction function for change in net government position	A-62

DISPOSABLE INCOME BRIDGE

YDVNSA = -1.311 + 2.655 Q1 + 1.259 Q2 + 1.116 Q3 + 0.955 YDPVNSA (4.1) (8.8) (4.2) (3.7) (230.6)

 $\overline{R}^2 = 0.9989$ SEE = 0.818 DW = 1.87

CONSUMPT ION

$$C = -10.873 + 0.484 C_{-1} + 0.387 YDV/P + 0.119 NW_{-1} / P$$
(5.4) (6.6) (7.0) (6.2)

 $\frac{-2}{R} = 0.9987$ SEE = 0.387 DW = 1.72

PRIVATE FIXED INVESTMENT

(3.1)

(3.3)

(3.3)

IFP =
$$-5.275 + 0.083$$
 KP₋₁ + $\frac{5}{120}$ a₁ Δ (RL_{-i-1}) + $\frac{11}{120}$ b₁ Δ (GNP_{-i-1} - G_{-i-1})

 $\overline{R}^2 = 0.760$ SEE = 0.375 DW = 1.5 p = 0.919

i 0 1 2 3 4 5 SUM a₁ -0.349 -0.781 -0.985 -0.984 -0.803 -0.467 -4.369 (2.2) (3.8) (4.2) (4.1) (3.5) (2.8) (4.1)

i 0 1 2 3 4 5 b₁ 0.105 0.102 0.119 0.148 0.185 0.222 (2.1) (2.1) (2.0) (2.2) (2.5) (2.9)

(3.3)

(3.2)

(3.1)

(3.3)

INVENTORY INVESTMENT

II = -1.719 + 0.493
$$\Sigma_{i=1}$$
 (C_{-i} + IFP_{-i} + IFG_{-i} + XG_{-i}) /4
-0.865 $\Sigma_{i=1}$ (MG_{-i}) /4 + 0.551 MG - 0.404 (C + IFP + IFG + XG)
(2.9) $\Sigma_{i=1}$ (4.8) (4.5) $\Sigma_{i=1}$ (4.8) $\Sigma_{i=1}$ (4.8) $\Sigma_{i=1}$ (4.8) $\Sigma_{i=1}$ (4.8)

no lagged stock

CAPITAL CONSUMPTION ALLOWANCE

CCAV =
$$-8.570 + 0.073$$
 Q2 -0.270 Q3 $+0.229$ Q4 $+0.016$ KP₋₁
(45.2) (0.9) (1.7) (2.7) (6.9)

+ 15.402 P₋₁ + 0.038 (GNPVNSA - TV - CVNSA)
(22.8) (2.9)

 $\overline{R}^2 = 0.996$ SEE = 0.226 DW = 0.54

TAXES -- PERSONAL

TPERV =
$$-4.489 + 0.604 + 0.217 + 0.217 + 0.110 + 0.321 + 0.3$$

- 0.013 WBNSA * P * QTAXI (3.9)

$$\overline{R}^2 = 0.991$$
 SEE = 0.627 DW = 1.61

TAXES -- NONRESIDENT

TNRESV = 0.087 - 0.086 Q1 - 0.043 Q2 - 0.163 Q3 + 0.003 GNPVNSA(5.0) (5.3) (2.7) (10.1) (18.0)

 $\bar{R}^2 = 0.878$ SEE = 0.044 DW = 2.83

TAXES - CORPORATE

TCORPV =
$$-0.320 + 0.480 Q1 + 0.451 Q2 - 1.242 Q3$$

(1.4) (2.6) (2.6) (6.7)

$$\overline{R}^2 = 0.9368$$
 SEE = 0.468 DW = 1.56

TAXES - INDIRECT

TINDV =
$$0.471 + 0.697 Q1 - 0.371 Q2 - 0.866 Q3 + 0.134 GNPVNSA$$

(1.8) (2.9) (1.6) (3.6) (59.3)

$$\overline{R}^2 = 0.983$$
 SEE = 0.653 DW = 1.16

GOVERNMENT TRANSFERS

TRANV =
$$-1.119 - 1.738 Q2 - 2.764 Q3 - 2.033 Q4 + 0.152 (GNPVNSA - XGV)$$

(1.7) (5.6) (7.3) (6.4) (7.5)

+ 0.283 XGV + 2.965 (UN * LF/100) - 46.473
$$\Delta$$
 (LOG(P)) - 0.085 TIME (4.2) (2.1) (2.0) (4.6)

$$\overline{R}^2 = 0.982$$
 SEE = 0.732 DW = 1.57

<u>EXPORTS OF GOODS: BRIDGE EQUATION</u> (Customs clearance to balance of payments basis)

XGV * ER = 0.679 - 0.205 Q1 - 0.024 Q2 - 0.172 Q3 + 0.950 XCTV (6.9) (2.0) (0.2) (1.7) (244.5)

 $\overline{R}^2 = 0.999$ SEE = 0.282 DW = 1.27

IMPORTS OF GOODS: BRIDGE EQUATION (Customs clearance to balance of payments basis)

MGV * ER = 0.133 + 0.942 MCTV/1.1(3.0) (366.8)

 $\overline{R}^2 = 0.999$ SEE = 0.184 DW = 0.94

BILATERAL IMPORT DEMAND FUNCTION: IMPORTS FROM GERMANY

LOG
$$(XGCV/(GPXGUV * GE)) = -8.268 - 0.164 Q1 - 0.046 Q2 - 0.273 Q3$$

(7.5) (4.0) (1.3) (6.6)

$$\overline{R}^2 = 0.941$$
 SEE = 0.100 DW = 2.04

BILATERAL IMPORT DEMAND FUNCTION: IMPORTS FROM JAPAN

LOG
$$(XJCV/JPXGUV * JE)) = -10.502 + 0.052 Q1 + 0.043 Q2 - 0.130 Q3$$

(7.1) (1.4) (1.4) (3.5)

$$\frac{1}{R^2} = 0.615$$
 SEE = 0.111 DW = 1.86 ρ = 0.853

BILATERAL IMPORT DEMAND FUNCTION: IMPORTS FROM THE REST-OF-THE-WORLD

+ 1.529 LOG(GNFVNSA/PGNP) + 0.290 LOG(P/(ROWPXG/E)) (30.8) (4.0)

 $\overline{R}^2 = 0.949$ SEE = 0.083 DW = 1.57

BILATERAL IMPORT DEMAND FUNCTION: IMPORTS FROM THE U.K.

LOG(XECV/(EPXGUV * EE)) =
$$-0.734 - 0.128 \text{ Q1} + 0.039 \text{ Q2} - 0.093 \text{ Q3}$$

(1.3) (4.0) (1.2) (3.0)
+ $0.153 \text{ LOG(GNPVNSA/PGNP)} - 0.141 \text{ EDV41} - 0.150 \text{ EDV50}$
(1.2) (1.5) (1.7)
- $0.043 \text{ EDV30} + 0.064 \text{ EDV49} - 0.125 \text{ EDV5} + \sum_{i=0}^{4} a_i$
(0.7) (0.7) (1.4) $i=0$
LOG(P_{-i} /(EPXGUV_{-i} * EE_{-i} / E_{-i}))
 $\overline{R}^2 = 0.604 \text{ SEE} = 0.089 \text{ DW} = 2.02 \text{ } \rho = 0.329$

BILATERAL IMPORT DEMAND FUNCTION: IMPORTS FROM THE U.S.

LOG(XUCV/UPXGUV) =
$$-4.237 + 0.024 \text{ Q1} + 0.084 \text{ Q2} - 0.218 \text{ Q3}$$

 $(16.1) (1.6) (5.5) (15.5)$
 $+1.460 \text{ LOG(GNPVNSA/PGNP)} + \sum_{i=0}^{2} a_i \text{ LOG(P}_{-i}/(\text{UPXGUV}_{-i}/\text{E}_{-i}))$
 $+0.017 \text{ QAUTST}$
 (2.9)

$$\overline{R}^2 = 0.944$$
 SEE = 0.047 DW = 2.35 $\rho = 0.568$

BILATERAL BRIDGE EQUATION: IMPORTS FROM GERMANY

$$MCGV = -0.004 + 0.974 \times GCV + 0.172 \times GCV$$
(0.3) (14.1) (2.3)

$$\overline{R}^2 = 0.971$$
 SEE = 0.042 DW = 1.95

BILATERAL BRIDGE EQUATION: IMPORTS FROM JAPAN

MCJV = 0.004 + 0.518 XJCV + 0.564 XJCV - 1 $(0.4) \quad (8.6) \quad (9.2)$

 $\overline{R}^2 = 0.987$ SEE = 0.057 DW = 3.27

BILATERAL BRIDGE EQUATION: IMPORTS FROM THE REST-OF-THE-WORLD

 $MCRV = 0.209 + 0.643 \ XRCV + 0.271 \ XRCV_{-1}$ (3.8) (10.5) (4.3)

 $\overline{R}^2 = 0.991$ SEE = 0.263 DW = 1.39

BILATERAL BRIDGE EQUATION: IMPORTS FROM THE U.K.

 $MCEV = -0.003 + 0.941 \text{ XECV} + 0.155 \text{ XECV}_{-1}$ (0.1) (19.1) (3.1)

 $\overline{R}^2 = 0.967$ SEE = 0.047 DW = 1.94

BILATERAL BRIDGE EQUATION: IMPORTS FROM THE U.S.

$$MCUV = -0.411 + 1.182 \text{ XUCV} + 0.018 \text{ XUCV}_{-1}$$
(4.7) (39.8) (0.6)

 $\overline{R}^2 = 0.997$ SEE = 0.337 DW = 1.32

EXPORT OF GOODS $\frac{1}{}$

$$\overline{R}^2 = 0.9661$$
 SEE = 0.045 DW = 1.77 $\rho = 0.418$

^{1/} This equation is used only when the Canadian model is simulated in isolation from the other models of the MCM.

EXPORTS OF OTHER SERVICES

$$LOG(XSOV/PXS) = -1.095 + 0.387 Q2 + 0.527 Q3 - 0.028 Q4 + (2.1) (11.6) (17.5) (0.5)$$

$$+ 0.500 LOG(XSOV_{-1}/PXS_{-1}) + 0.202 LOG(FGNP) + 0.060 QEXPO (3.6) (2.3) (1.4)$$

$$+ 0.034 QAUTO + 0.197 LOG(FP/PXS) (2.0) (1.1)$$

 $\overline{R}^2 = 0.9681$ SEE = 0.061 DW = 2.34

IMPORTS OF OTHER SERVICES

$$LOG(MSOV/PMS) = -\frac{1.471 + 0.132 \text{ Q2} + 0.083 \text{ Q3} - 0.081 \text{ Q4}}{(3.8) (8.5) (4.3) (4.0)}$$

$$+\frac{0.617 \text{ LOG(MSOV} - 1/PMS}{(6.6)} - 1) + \frac{0.450 \text{ LOG(GNP)} + 0.388 \text{ LOG(P/PMS)}}{(3.9) (1.3)}$$

$$\overline{R}^2 = 0.9794 \cdot \text{SEE} = 0.042 \quad DW = 1.97$$

EXPORTS OF GOODS AND SERVICES: BRIDGE EQUATION (balance of payments basis to National Income Accounts basis)

XGSNIVS = -0.003 + 1.000 (XGV + XSOV + XSYV)(0.2) (1578.4)

 $\overline{R}^2 = 0.999$ SEE = 0.051 DW = 3.08

IMPORTS OF GOODS AND SERVICES: BRIDGE EQUATION (balance of payments basis to National Income Accounts basis)

MGSNIVS = -0.002 + 1.000 (MGV + MSOV + MSYV)(0.2) (2263.9)

 $R^2 = 0.999$ SEE = 0.038 DW = 2.17

TRANSFER RECEIPTS

XTRANV = 0.009 + 0.137 Q2 + 0.099 Q3 0.131 Q4 + 0.001 FYDVNSA (0.3) (5.9) (3.8) (5.6) (21.2)

 $\overline{R}^2 = 0.9014$ SEE = 0.077 DW = 2.08 $\rho = 0.404$

TRANSFER PAYMENTS

MTRANV = 0.183 + 0.007 YDVNSA (8.2) (18.4)

 $R^2 = 0.8515$ SEE = 0.073 DW = 1.87

INVESTMENT INCOME RECEIPTS

$$XSYV = 0.003 \text{ FC} + 0.003 \text{ Q2} * \text{FC} - 0.001 \text{ Q3} * \text{FC}$$
(0.9) (2.0) (0.8)

+ 0.006 Q4 * FC + 0.004 (
$$E_{-1}/E$$
) * NFAEOQ * FRSC (4.2) (2.1)

+ 0.008 (
$$E_{-1}/E$$
) * URL * LTDC₋₁ (3.9)

$$\overline{R}^2 = 0.7934$$
 SEE = 0.091 DW = 1.9 $\rho = 0.315$

INVESTMENT INCOME PAYMENTS

MSYV = 0.057 FL - 0.0002 Q2 * FL - 0.002 Q3 * FL + 0.011 Q4 * FL (5.4) (0.2) (1.8) (11.0)
$$+ 0.026 \text{ (RS * (-STL_{-1}) + RL * (-LTPL_{-1}))} - 0.032 \text{ RL * (-LTDL_{-1})}$$

$$(7.0) \qquad \qquad (5.0)$$

$$\overline{R}^2 = 0.9178 \quad \text{SEE} = 0.155 \quad \text{DW} = 1.95 \quad \text{p} = 0.415$$

DOMESTIC PRICE

$$LOG(P) = -0.185 + 0.732 LOG(P_{-1}) + 0.122 LOG(W) + 0.096 LOG(PMGSNI)$$

$$(4.5) (10.2) (3.9) (3.1)$$

$$+ 0.0004 CU + 0.017 LOG(PPC)$$

$$(2.6) (3.7)$$

$$\overline{R}^2 = 0.999$$
 SEE = 4.09 E-3 DW = 2.30

EXPORT UNIT VALUE

$$\overline{R}^2 = 0.967$$
 SEE = 0.012 DW = 1.76 $\rho = 0.746$

IMPORT UNIT VALUE

$$LOG(PMGUV) + LOG(E) = -0.027 + 0.370 LOG(FPXGUVD) + 0.369 LOG(FPXGUVD_{-1})$$
(4.0) (4.3) (4.2)

$$\frac{-2}{R}$$
 = 0.951 SEE = 0.011 DW = 1.77 ρ = 0.798

SERVICE DEFLATOR, EXPORTS

$$LOG(PXS) = -0.017 + 1.111 LOG(P)$$
(2.7) (41.9)

$$\overline{R}^2 = 0.9675$$
 SEE = 0.041 DW = 2.15

SERVICE DEFLATOR, IMPORTS

$$LOG(PMS) = 0.496 LOG(PMS_{-1}) + 0.550 LOG(FP)$$
(5.2) (5.3)

$$\overline{R}^2 = 0.9856$$
 SEE = 0.023 DW = 2.05

CAPACITY UTILIZATION

$$LOG(GNP/LF) - 0.28 * LOG(KP/LF) = 1.286 + 0.003 TIME + 0.584 LOG(CU/100)$$
(110.6) (20.0) (10.4)

$$\overline{R}^2 = 0.933$$
 SEE = 0.008 DW = 2.03 $\rho = 0.637$

WAGES

$$(W-W_{-4})/W_{-4} = -0.001 + 0.069 \text{ QUI} + 0.0003 \text{ TIME} - 0.008 \text{ QCNTRL}$$
 $(0.2) (2.4) (1.4) (0.9)$

$$+ 0.210 \left(\sum_{i=0}^{3} (P_i - P_{i-4})/P_{i-4})/4 - 0.0001 \text{ UN}_{-1} - 0.012 \text{ UN}_{-1}*QUI$$
 $(2.2) i=0 (0.1)$

$$+ 0.737 (W_{-1} - W_{-5})/W_{-5}$$
 (6.1)

$$\overline{R}^2 = 0.9663 \quad \text{SEE} = 0.007 \quad \text{DW} = 2.19$$
Period 62:2 to 75:4

WAGE BILL

WB =
$$-10.667 + 1.019$$
 LF * $(1 - UN/100)$ * W * 2 + 0.104 CU (4.1) (168.7) (3.7)

$$\overline{R}^2$$
 = 0.998 SEE = 0.438 DW = 1.83 ρ = 0.586 Period 61:1 to 75:4

EMPLOYMENT

$$LOG(1 - UN/100) + LOG(LF) = 0.675 + 0.005 TIME + (3.7) (11.4)$$

$$\begin{array}{ccc} & & & \\ \Sigma & & \\ \mathbf{a_i} & \text{LOG}(\text{GNPV}_{-i}/(\text{W}_{-i})) \end{array}$$

$$\overline{R}^2 = 0.9826$$
 SEE = 0.005 DW = 1.62 $\rho = 0.768$

LABOR FORCE PARTICIPATION

$$LOG(LF/POP15) = -0.709 + 0.279 LOG(W_{-1}/P_{-1}) - 0.014 LOG(UN_{-1})$$
(8.8) (5.9) (1.4)

$$\overline{R}^2 = 0.4371$$
 SEE = 0.004 DW = 1.68 $\rho = 0.906$

DEMAND DEPOSITS

$$\begin{array}{l} DD/NWNSA = -0.001 - 0.007 \ Q2 - 0.009 \ Q3 - 0.001 \ Q4 - 2.2E-04 \ TIME \\ (0.3) \quad (6.0) \quad (4.4) \quad (0.8) \quad (2.0) \\ \\ +0.698 \ DD_{-1}/NWNSA + 0.072 \ GNPVNSA/NWNSA - 0.001 \ RS \\ (8.0) \quad (3.6) \quad (4.5) \end{array}$$

 $\overline{R}^2 = 0.950$ SEE = 0.002 DW = 1.21

SAVING DEPOSITS

NOTICE DEPOSITS

ND/NWNSA =
$$-0.044 - 0.004 Q2 - 0.011 Q3 - 0.006 Q4 + 0.129 GNPVNSA/NWNSA (15.3) (3.1) (7.7) (4.1) (31.2)$$

$$\bar{R}^2 = 0.957$$
 SEE = 0.004 DW = 0.52

CURRENCY

CUR/NWNSA = 0.004 - 0.002 Q2 - 0.004 Q3 - 0.002 Q4 - 1.5E-04 TIME (4.0) (4.8) (7.7) (5.0) (4.4)

+ 0.047 GNPVNSA/NWNSA - 3.3E-04 RS (9.4) (4.0)

 $R^2 = 0.941$ SEE = 7.5E-04 DW = 0.80

REQUIRED RESERVES

RR = 0.083 + 0.908 (A * DD + B * TD)/100(7.0) (158.6)

 $\overline{R}^2 = 0.998$ SEE 0.035 DW = 1.41

SHORT-TERM INTEREST RATE: WHEN SHORT-TERM RATE EXCEEDS THE DISCOUNT RATE

RSLD = - 1.190 - 27.949 RF/NDD + 12.057
$$\triangle$$
 (RU)/NDD - 67.746 DRR/NDD (2.4) (2.0) (1.2) (2.7)

$$\overline{R}^2 = .9525$$
 SEE = 0.469 DW = 1.00

Period 61:1 to 62:1, 63:1, 63:3.to 67:4, 68:3 to 70:3, 72:2 to 74:4, 75:4

SHORT TERM INTEREST RATE: WHEN DISCOUNT RATE EXCEEDS SHORT-TERM RATE

RSHD = - 5.558 RF/NDD - 0.143 URS - 38.880 DRR/NDD + 1.034 RD (0.5) (1.0) (1.1) (8.7)

- 0.048 DEFLOAT * (1 - KFIX) (1.7)

 $\overline{R}^2 = 0.934$ SEE = 0.383 DW = 1.70

Period: 62:2 to 62:4, 63:2, 68:1 to 68:2, 70:4 to 72:1, 75:1 to 75:3

LONG-TERM INTEREST RATE

RL = 1.735 +
$$\sum_{i=0}^{15} a_i RS_{-i} + \sum_{i=0}^{5} b_i \Delta(LOG(P_{-i}))$$

$$\overline{R}^2 = 0.743$$
 SEE = 0.289 DW = 1.58 $\rho = 0.667$

					•				
i	0	1	2	3	4	5	. 6	7	;
a	0.079	0.077	0.074	0.071	0.068	0.064	0.597	0.055	
	(3.1)	(3.7)	(4.5)	(5.4)	(6,2)	(6.7)	(6.6)	(6.0)	
	8	9	10	11	12	1.3	14	15	SUM
	0.050	0.045	0.040	0.034	0.028	0.021	0.015	0.007	0.789
	(5.3)	(4.7)	(4.2)	(3.7)	(3.4)	(3.1)	(2.9)	(2.7)	(6.7)
			٠.		•				
1	· • • •	1	2	3	4	. 5			SUM
Ъ	13.076	9.804	6.970	4.572	2.611	1.087			38.120
	(1.8)	(2.3)	(1.5)	(0.8)	(0.5)	(0.3)			(1.8)

ERRORS AND OMISSIONS

EANDO =
$$-1.123 + 1.531$$
 Q2 + 2.192 Q3 + 0.930 Q4 -0.338 \triangle (NWNSA) (4.0) (4.4) (4.6) (2.6) (3.6)

- 0.528 (
$$\triangle$$
 (XGV) - \triangle (MGV)) - 0.229 (XGV + XSOV + XSYV + XTRANV (3.1)

$$\overline{R}^2 = 0.3805$$
 SEE = 0.898 DW = 2.48

CHANGE IN SHORT-TERM LIABILITIES

DSTL =
$$-0.387 - 0.943 \text{ Q2} - 0.324 \text{ Q3} - 0.466 \text{ Q4} + 0.091 \Delta(MGV)$$

 $(0.2) (3.6) (1.9) (2.0) (1.7)$
 $-0.406 \text{ QCRISIS} - 0.115 \Delta(\text{URS}) + 0.265 \Delta(\text{MGV}) * \text{KFIX}$
 $(1.5) (1.5) (3.2)$
 $-0.446 \text{ QIET2} - 0.914 \text{ QRFID} + 0.307 \text{ QEREG69} + \sum_{i=0}^{5} a_i \Delta(\text{UNW}_{-i})$
 $(3.0) (1.9) (1.6)$
 $+\sum_{i=0}^{3} b_i 1/\text{ER}_{-i} + 0.850 \text{ QSMITH}$
 $i=0 (1.9)$
 $\overline{R}^2 = 0.4256 \text{ SEE} = 0.424 \text{ DW} = 2.45$

i :	() 0.014 (3.2)	0.011		0.004	5 0.002 (3.2)	SUM 0.048 (3.2)
ъ		0.140 (0.2)	-0.929 (0.5)			0.468 (0.3)

CHANGE IN SHORT-TERM CLAIMS

- DSTC = - 0.534 - 0.160 Q2 + 0.952 Q3 + 0.423 Q4 - 0.483
$$\Delta$$
(RS) (1.7) (0.4) (3.0) (1.1) (2.5)

+ 0.549
$$\triangle$$
FRSC + 0.757 QEREG69 + 0.035 \triangle (DEFLOAT) * (1-KFIX) (3.4) (2.2) (1.5)

+ 0.157
$$\Delta$$
(XGV) + 0.129 DLTPL - 1.172 QFRID + 0.282 QIET1 (2.0) (1.5) (1.4) (0.7)

$$\overline{R}^2 = 0.404$$
 SEE = 0.771 DW = 2.18

CHANGE IN LONG-TERM LIABILITIES

DLTPL = -8.439 - 0.327 Q2 - 0.203 Q3 + 0.304 Q4 + 0.155 QMIDEA
(1.3) (0.9) (0.5) (0.8) (0.2)
+ 0.590
$$\Delta$$
(RL - URL) - 1.037 QIET1 - 1.261 QIET2
(1.0) (1.7) (2.8)
+ 0.009 QZEUROF + 1.019 QEREG69 - 0.579 QLOBO + 0.791 QEIETB
(1.5) (2.3) (0.8) (0.8)
+ $\sum_{i=0}^{5} a_i \Delta$ (UNW_{-i}) + $\sum_{i=0}^{5} b_i 1/ER_{-i} - 1.369$ QSMITH
 $\sum_{i=0}^{7} a_i \Delta$ (UNW_{-i}) + $\sum_{i=0}^{7} b_i 1/ER_{-i} - 1.369$ QSMITH

CHANGE IN LONG-TERM CLAIMS

- DLTPC =
$$0.072 - 0.117 Q2 + 0.020 Q3 + 0.098 Q4 + 0.098 Q2 * KFIX (0.7) (1.6) (0.3) (1.4) (1.1)$$

- 0.005 Q3 * KFIX - 0.106 Q4 * KFIX + 0.191
$$\triangle$$
(URL) - \triangle (RL) (0.1) (1.2) (2.3)

+ 0.002 (1 - KFIX) *
$$\triangle$$
 (DEFLOAT) - 0.167 QFRID (0.5) (1.1)

$$\overline{R}^2 = 0.082$$
 SEE = 0.174 DW = 1.84 $\rho = 0.774$

FORWARD EXCHANGE RATE

$$EF = 0.022 + 8.142E-05 Q2 + 1.108E-04 Q3 - 3.449E-04 Q4 + 0.002 E * FRSL (2.8) (0.3) (0.4) (1.1) (16.2)$$

$$\overline{R}^2 = 0.9995$$
 SEE = 8.18E-04 DW = 1.18

LED EXCHANGE RATE

ELEAD = 0.588 - 0.241 KFIX +
$$\sum_{i=0}^{2} a_i$$
 E_{-i-1} + $\sum_{i=0}^{2} b_i$ E_{-i-1}

* KFIX + $\sum_{i=0}^{2} c_i$ DNFA_{-i} + $\sum_{i=0}^{2} d_i$ DNFA_{-i} * KFIX

+ $\sum_{i=0}^{1} e_i$ NGP_{-i} + $\sum_{i=0}^{1} f_i$ NGP_{-i} * KFIX

$$\bar{R}^2 = 0.923$$
 SEE = 0.010 DW = 1.33

NET FOREIGN ASSETS: FLOATING EXCHANGE RATE PERIOD

$$\overline{R}^2 = 0.5011$$
 SEE = 0.650 DW = 1.72

Period 70:3 to 75:4

CHANGE IN NET COVERNMENT POSITION: FIXED EXCHANGE RATE PERIOD

DNGPFX = - 0.139 KFIX - 0.457 DNFA * KFIX + 0.173
$$\triangle$$
 (GNP) * KFIX (0.9) (7.0) (1.5)

- 0.247
$$\triangle$$
 (URS - RS) * KFIX (1.4)

$$\overline{R}^2 = 0.5671$$
 SEE = 0.444 DW = 1.60

LIST OF IDENTITIES

GNP identities

- 1. GNP = C + IFP + IFG + II + G + XGSNI MGSNI + RES
- 2. GNPV = CV + IFPV + IFGV + IIV + GV + XGSNIV MGSNIV + RESV
- 3. CNPVNSA = CNPV / SAFGNPV
- 4. PCHGNP = Δ (LOG(GNP)) * 400

Components of GNP

- 5. G = GV / P
- 6. CV = C * P
- 7. IFPV = IFP * P
- B. IFGV = IFG * P
- 9. IIV = II * P
- 10. MGSNIV = SAFMNIV * MGSNIVS
- 11. XGSNIV = SAFXNIV * XGSNIVS
- 12. CVNSA = CV / SAFCV
- 13. IFGVNSA = IFGV / SAFIFGV
- 14. IFPVNSA = IFPV / SAFIFPV

Disposable income proxy

- 15. YDPVNSA = GNPVNSA TV + TRANV CCAV
- 16. YDV = YDVNSA * SAFYDV

Capital stock

- 17. $KG = (1 SCRG / 4) * KG_{-1} + IFG / 4$
- 18. $KP = (1 SCRP / 4) * KP_1 + IFP / 4$

Private net worth proxy

- 19. DNWNSA = YDPVNSA CVNSA + XTRANV MTRANV RESNSA
- 20. $NWNSA = NWNSA_{-1} + DNWNSA / 4$
- 21. DNW = DNWNSA * SAFDNW
- 22. $NW = NW_{-1} + DNW / 4$

Exports of goods and services

- 23. XGSNINS = XG + (XSOV + XSYV) / PXS
- 24. XGSNI = SAFXNI * XGSNINS

Imports of goods and services

- 25. MGSNINS = MG + (MSOV + MSYV) / PMS
- 26. MGSNI = SAFMNI * MGSNINS

Merchandise exports, balance of payments basis

27. XGV = XG * PXGUV

Merchandise exports, customs clearance basis (U.S.\$)

28. XCTV = XCJV + XCGV + XCEV + XCUV + XCRV + XCJUNK

Merchandise imports, balance of payments basis

29. MGV = GM * PMGUV

Merchandise imports, customs clearance basis (U.S.\$)1

30. MCTV = MCJV + MCGV + MCEV + MCUV + MCRV

Total tax revenue

31. TV = TPERV + TNRESV + TCORPV + TINDV

Wage Bill

32. WBNSA = WB / SAFWB

Applied only to linked version of the model.

Trade balance

33. TB = XGV - MGV

Total world exports, excluding Canada

34. WTV = XGTV + XJTV + XUTV + XETV + XRTV

Canadian exports to trading partners

35. XUJEGV = XCUV + XCJV + XCEV + XCGV

Canadian imports to trading partners

36. MUJEGV = XUCV + XJCV + XECV + XGCV

Weighted foreign averages of competitors price, capacity utilization price of exports, gross national product, domestic deflator, and disposable income

- 37. PCOMP = $(GE * GPXGUV)^{XGTV/WTV} * (JE * JPXGUV)^{XJTV/WTV}$
 - * (EE * EPXGUV) XETV/WTV * UPXGUV XUTV/WTV
 - * ROWPXGXRTV/WTV/E
- 38. CUSTCU = UCUXCUV/XUJEGV * JCUXCJV/XUJEGV

 ECUXCEV/XUJEGV * GCUXCGV/XUJEGV
- 39. FPXGUVD = UPXGUV^{MCUV}/MCTV * (JPXGUV * JE)^{MCJV}/MCTV
 - * (EPXGUV * EE) MCEV/MCTV * (GPXGUV * GE) MCGV/MCTV
 - * ROWPXGMCRV/MCTV
- 40. FGNP = UGNPXCUV/XUJEGV * JGNPXCJV/XUJEGV
 - * EGDPXCEV/XUJEGV * GGNPXCGV/XUJEGV

42. FYDVNSA = UYDVXCUV/XUJEGV * JYDVNSAXCJV/XUJEGV

* EYDVNSAXCEV/XUJEGV * GYDVNSAXCGV/XUJEGV

Percentage change in domestic deflator

43. PCHP = $\Delta(LOG(P)) * 400$

Percentage change in wages

44. PCHW = $\Delta(LOG(W))$ * 400

GNP deflator

45. PGNP = GNPV / GNP

Deflator for imports of goods and services

46. PMGSNI = MGSNIV / MGSNI

Net foreign assets

- 47. DNFA = XGV + XSYV + XSOV + XTRANV MGV MSYV MSOV
 MTRANV + DSTL + DLTPL + DSTC + DLTPC + DLTDL

 + DLTDC + EANDO + NGKA
- 48. $NFAEOQ = NFAEOQ_{-1} + DNFA / 4$
- 49. NFAFED = (NFAEOQ NFAEOQR) * ER

Net government position of the monetary authority

- 50. DNGP = DNGPFX \star KFIX + DNGPFL \star (1 KFIX)
- 51. $NGP = NGP_{-1} + DNGP / 4$

Short-term liabilities and claims, stocks

- 52. STL = STL₋₁ DSTL / 4
- 53. STC = STC₋₁ DSTC / 4

Long-term direct liabilities and claims, stocks

- 54. LTDL = LTDL $_{-1}$ DLTDL / 4
- 55. LTDC = LTDC $_{-1}$ ~ DLTDC / 4

Long-term protfolio liabilities and claims, stocks

- 56. LTPL = LTPL $_{-1}$ DLTPL / 4
- 57. LTPC = LTPC $_{-1}$ DLTPC / 4

Net government capital account, stock

58. $NGK = NGK_{-1} - NGKA / 4$

Stock of financial liabilities and claims by foreigners

- 59. FL = (STL + LTPL + LTDL)
- 60. FC = STC + LTPC + LTDC + NFAEOQ + NGK

Foreign average short-term interest rate

- 61. FRSC = .268 * URS + .732 * RED
- 62. FRSL = .219 * URS + .781 * RED

Proxy for expected exchange rate

- 63. DEFLOAT = (E / ELEAD 1) \star 400
- 64. DEFIXED = MGV_{-1} / (NFAEOQ₋₁ + NFAEOQ₋₂) * 2 * PXGUV₋₁ / PCOMP₋₁
- 65. DEFIXE2 = MGV_{-1} / (NFAEOQ₋₁ + NFAEOQ₋₂) * 2

Change in reserve requirement

66. DRR =
$$\Delta(A) * (DD_{-1} - TD_{-1}) / 100$$

Net demand deposit

67. NDD - (1 - .9078 * A / 100) * DD

Unborrowed monetary base, sources and uses

68.
$$BU = (NFAEOQ_{-1} + NFAEOQ) * 0.5 + SDRVAL + NGP + OTH$$

69. BU =
$$RR + RF + CUR$$

Unborrowed reserves

70. RU = BU - CUR

Time deposits

71. TD = SD + ND

Short-term interest rate

72. RS = RSHD * QRD + RSLD * (1 - QRD)

Spot exchange rate

73. ER = E * 1.00937

Official reserves changes and exchange rate

74.
$$E = EFX * KFIX + EFL * (1 - KFIX)$$

75. DNFA = DNFAFX * KFIX + DNFAFL *
$$(1 - KFIX)$$

76. O = EFL * KFIX + DNFAFX * (1 - KFIX)

DEFINITION AND SOURCES OF VARIABLES

All national product and income account variables are expressed at annual rates and are seasonally adjusted (unless indicated by the mremonic "NSA"). All balance of payments variables are expressed at annual rates and are not seasonally adjusted (unless indicated by the mremonic "SA"). The prefix "SAF" indicates a seasonal adjustment factor used to translate variables from an "NSA" to an "SA" basis or vice-versa. All monetary stock items are measured as mid-quarter averages and are not seasonally adjusted. Where monetary stocks are measured at end of quarter, the suffix "EOQ" is employed.

The letter "V" appended to a variable name indicates measurement in billions of Canadian dollars. When the "V" is absent, the variable is generally expressed in constant 1972 Canadian dollars. Exceptions to this role are financial variables, such as capital account items and components of the monetary sector, which are all in nominal terms.

Interest rates are in per cent per annum; and price variables are indexes based at 1.0 in 1972. Exchange rates and interest rates are averages of daily rates. The symbol "x" indicates an exogenous variable. The "*" indicates a variable endogenously determined within the multi-country model, but exogenous (or not included in the isolated Canadian model.

The following abbreviations are used:

STATCAN

Statistics Canada

BQC

Bank of Canada

DOT

Direction of Trade (IMF)

FRB

Federal Reserve Board

WHARTON

Wharton Econometric Forecasting Associates

IFS

International Financial Statistics

x A reserve requirements on demand deposits (STATCAN)

x B reserve requirements on time deposits (STATCAN)

BU unborrowed reserves (RR + RF + CUR)

C consumption expenditure (CV/P)

CCAV total capital consumption allowance (STATCAN)

CU capacity utilization rate -- total manfactures (WHARTON)

CUR currency held by nonbank public (STATCAN)

CUSTCU foreign weighted average of capacity utilization 1

CV consumption expenditure (STATCAN)

CVNSA consumption expenditure, not seasonally adjusted (STATCAN)

DD demand deposits held by residents (BOC)

DEFIXED proxy for expected exchange rate change during the fixedrate regime (before 70:2); the ratio of imports to foreign
exchange reserves times the ratio of Canadian export price to
competitors' export price index

DEFIXE2 proxy for expected exchange rate change during the fixedrate regime (before 70:2); the ratio of imports to foreign exchange reserves

DEFLOAT proxy for expected exchange rate change during the floating rate period (after 70:2); percentage change between current and led exchange rates

- x DLTDC change in long-term direct claims on foreigners (STATCAN)
- x DLTDL change in long-term direct liabilities to foreigners (STATCAN)

 DLTPC change in long-term protfolio claims on foreigners (STATCAN)

¹Trade weighted average for Germany, Japan, the United Kingdom and the United States.

DLTPL change in long-term portfolio liabilities to foreigners (STATCAN)

DNFA change in net foreign assets of the central bank (STATCAN)

DNFAFL DNFA * (1-KFIX)

DNFAFX DNFA * KFIX

DNGP change in net government position of the consolidated monetary authorities

x DNGPFL DNGP * (1-KFIX)

DNGPFX DNGP * KFIX

DNW change in private net worth (STATCAN)

DRR change in required reserves

DSTC change in short-term claims on foreigners (STATCAN)

DSTL change in short-term liabilities to foreigners (STATCAN)

E Canadian spot exchange rate index, US\$/C\$, (ER/1.009)

EANDO errors and omissions (STATCAN)

- * ECU U.K. capacity utilization index (WHARTON)
- x EDV30 U.K. dummy for shift in automobile imports, 7001 = 1
- x EDV41 U.K. dock strike dummy, 7203 = 1
- \mathbf{x} EDV49 U.K. dummy for anticipation of floating of sterling, 7202 = 1
- x EDV5 U.K. dock strike dummy, 1 from 6701 to 6704 (LONDON BUSINESS SCHOOL)
- x EDV50 U.K. dock strike dummy, 7002 = 1
- * EE spot exchange rate index, U.S.\$/f (FRB)

EF Canadian forward exchange rate index, U.S.\$/C\$, (EFR/1.008)

EFL E * (1-KFIX)

EFX E * KFIX

* EGDP U.K. gross domestic product, output estimates

ELEAD Canadian led spot exchange rate index (E_{+1})

* EP U.K. absorption deflator (index, 1972=1.0)

* EPXGUV U.K. export unit value index (1972=1.0)

ER Canadian exchange rate, U.S.\$/C\$ (FEDERAL RESERVE BULLETIN)

* EYDVNSA U.K. disposable income proxy

FC stock of financial claims on foreigners (cumulated value of DFC)

FGNP foreign weighted average of gross national $product^1$

FL stock of financial liabilities to foreigners (cumulated value of DFL)

FP foreign weighted average of prices 1

FPXGUVD foreign weighted average of price of exports 2

FRSC weighted average of U.S. rate and Eurodoliar short-term rates. (Weights based on external claims and liabilities, respectively

FYDVNSA foreign weighted average of disposable $income^1$

x G government expenditure on goods and services (GV/P)

¹Trade weighted average for Japan, Germany, the United Kingdom, and the United States.

²Weights are percentages of Canadian imports from Germany, Japan, R.O.W., the United Kingdom and the United States.

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* GCU German capacity utilization rate
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- * GE German spot exchange rate index, \$/DM (FRB)
- * GGNP German gross national product

 GNP GNPV gross national product (STATCAN)
- * GP German absorption deflator
- * GPXGUV German export unit value index
 - GV government expenditure on goods and services, current value (STATCAN)
- * GYDVNSA German disposable income proxy

IFG government gross fixed capital formation (IFGV/P)

IFGV | government gross fixed capital formation (STATCAN)

IFPV private fixed investment, housing plus plant and equipment IFPVNSA (STATCAN)

II inventory investment (IIV/P)

IIV inventory investment, current value (STATCAN)

- x INTSHK dummy variable for simulating changes in foreign exchange intervention, normal value is zero.
- * JCU Japanese capacity utilization index, ratio of industrial production index to production capacity index (BANK OF JAPAN)
- * JE spot exchange rate index, U.S.\$/YEN, (FRB)

* JGNP Japanese gross national product (BANK OF JAPAN)

* JP Japanese deflator for aggregate expenditure

* JPXGUV Japanese unit value of merchandise exports, Yen (IFS)

* JYDVNSA Japanese disposable income proxy

x KFIX dummy to reflect a fixed exchange rate regime (1 in 6202 to 7002)

KG government gross fixed capital stock (cumulated value of IFG, less scrappage)

KP private gross fixed capital stock (cumulated value of IFP
less scrappage)

LF labor force (STATCAN)

LTDC stock of long-term direct claims on foreigners (cumulated value of DLTDC)

LTDL stock of long-term direct liabilities to foreigners

(cumulated value of DLTDL)

LTPC stock of long-term portfolio claims on foreigners

(cumulated value of DLTPC)

LTPL stock of long-term liabilities to foreigners (cumulated value of DLTPL)

MCEV merchandise imports from the U.K., c.i.f. (DOT)

MCGV merchandise imports from Germany, c.i.f. (DOT)

MCJV merchandise imports from Japan, c.i.f. (DOT)

MCRV merchandise imports from R.O.W., c.i.f. (DOT)

MCTV merchandise imports, c.i.f. customs clearance basis (DOT)

MCUV merchandise imports from the U.S., c.i.f. (DOT)

MG import of goods (STATCAN)

MGSNI import of goods and services, national income accounts basis (STATCAN)

MGSNINS import of goods and services, national income accounts basis, not seasonally adjusted (STATCAN)

MGSNIV import of goods and services, national income accounts

basis, current value (STATCAN)

MGSNIVS import of goods and services, national income accounts

basis, not seasonally adjusted (STATCAN)

MGV import of goods, current value (STATCAN)

MSOV service account payments, except investment income (STATCAN)

MSYV investment income payments, current value (STATCAN)

MTRANV BOP transfer payments, current value (STATCAN)

MUJEGV Canadian imports from Japan, Germany, the United Kingdom and the United States

ND notice deposits (BOC)

NDD net demand deposits, (1-A) * DD

NFAEOQ stock of net foreign assets of the monetary authorities, end of quarter (cumulated value of DNFA)

x NFAEOQR non-dollar component of stock of net foreign assets of the monetary authorities, end of quarter

NFAFED net foreign assets, foreign exchange in U.S. dollars, end of quarter

NGK stock of government assets -- excluding foreign private holding of government which are included in LTPL (cumulated value of NGKA)

x NGKA net government capital account (STATCAN)

NGP net government position of the consolidated monetary authorities (BOC)

NW NWNSA stock of private net worth (cumulated value of DNW)

x OTH other assets of the Bank of Canada (BOC)

P implicit deflator for domestic absorption ((CV + IFGV + IFPV + IIV + GV)/(C + IFG + IFP + II + G))

PCHGNP percentage change in gross national product

PCHP percentage change in domestic price level

PCHW percentage change in wages

PCOMP foreign weighted average of the price of exports 1

PGNP implicit deflator for GNP (GNPV/GNP)

PMGSNI implicit deflator for imports of goods and services,

national income accounts basis (MGSNIV/MGSNI)

PMGUV unit value of merchandise imports (STATCAN)

PMS implicit deflator of import services ((MGSNIVS - MGV)/
(MGSNINS - MG))

x POP15 Canadian population 15 years of age and older (STATCAN)

 $^{^{\}mathrm{l}}\mathrm{Trade}$ weighted average for Germany, Japan, the United Kingdom and the United States.

x PPC dollar export price index of cereals, 1972=100 (United Nations Monthly Bulletin of Statistics)

PXGUV unit value of merchandise exports (STATCAN)

PXS implicit deflator of export services ((XGSNIVS - XGV)
/(XGSNIVS - XG))

QAUTO dummy to reflect Canadian-U.S. auto agreement

- x QAUTST dummy to reflect U.S. auto strike
- x QBACTS dummy for enactment of bank acts of 1967
- x QCNTRL dummy to reflect Canadian wage and price controls
- x QCRISIS dummy for exchange rate crises in 1962 and 1968
- x QEIETB dummy for deferral of new bond issues in the U.S.
- x QEREG69 dummy for divergance of weighted foreign rate from true foreign rate
- x QEXPO dummy to reflect effects of Expo 67
- x QFRID dummy to reflect end of quarter occurring on a Friday
- x QIET1 dummy to reflect interest equalization tax
- x QIET2 dummy to reflect interest equalization tax
- x QLOBO dummy for exchange rate uncertainty and federal policy discouraging foreign borrowing
- x QMIDEA dummy for Suez Canel closing
- x QNEP dummy for new economic program in U.S.
- x QRD dumny for periods when the discount rate is greater than the short term interest rate

- x QSCALE dummy to reflect economies of scale in Canadian auto
- x QSMITH dummy to reflect the Smithsonian agreement
- x QTAXI dummy for indexation of tax structure to Canadian price level
- x QUI dummy for revision of the unemployment act
- x QZEUROF dummy to account for federal borrowing in Deutsche marks
- x Q1,Q2, seasonal dummies
- x RD discount rate (BOC)
- * RED three month Eurodollar deposit rate (FRB)
- x RES RESNSA residual error of estimate from GNP component
- x RESV residual error of estimate (STATCAN)
 - RF free reserves, excess reserves less borrowed reserves
 - RL long-term interest rate Government of Canada Bonds -10 years and over (BOC)
- * ROWPMG ROW import price index
- * ROWPXG ROW export price index
 - RR required reserves (BOC)
 - RS short-term interest rate, 90 day finance company paper (BOC)
 - RSLD short-term interest rate (when discount rate is lower than short-term interest rate)

RSHD short-term interest rate (when discount rate is higher than short term interest rate)

RU unborrowed reserves, total reserves less borrowed reserves

x SCRG discard rate for gross government fixed capital stock

x SCRP discard rate for gross private fixed capital stock

SD savings deposits (BOC)

x SDRVAL SDR allocations and valuation adjustment (NFAT - NFA)

stock of private short-term claims on foreigners

(cumulated value of DSTC)

Canadian stock private short-term liabilities on foreigners

(cumulated value of DSTL)

TB trade balance (XGV - MGV)

TCORPV direct taxes on corporate and government business enterprises (STATCAN)

TD time deposits held by residents (BOC)

x TIME linear time trend

TINDV indirect taxes (STATCAN)

TNRESV direct taxes on non-residents (STATCAN)

TPERV direct taxes, personal (STATCAN)

TRANV government transfers (STATCAN)

TV government tax revenue (STATCAN)'

* UCU U.S. capacity utilization index

* UGNP U.S. gross national product

UN unemployment rate (STATCAN)

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* UNW U.S. private net worth proxy (cumulated value of private savings)
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- * UP U.S. deflator for aggregate expenditure
- * UPXGUV U.S. export unit value (Department of Commerce, Survey of Current Business)
- * URL U.S. long-term interest rate
- * URS U.S. Treasury Bill rate (FRB)
- * UYDV U.S. disposable income proxy

W wage rate in manufacturing (STATCAN)

WB' WBNSA wage bill (STATCAN)

- * WMGV merchandise imports, balance of payments basis
 - WTV total exports of world excluding Canada
- * XCEV merchandise exports to the U.K., c.i.f. (DOT)
- * XCGV merchandise exports to Germany, c.i.f. (DOT)
 - XCJUNK slack variable to insulate bilateral export variables when Canadian model is shocked in isolation (normal value = 0)
- * XCJV merchandise exports to Japan, c.i.f. (DOT)
- * XCRV merchandise exports to R.O.W., c.i.f. (DOT)
 - XCTV total Canadian merchandise exports, c.i.f., customs clearence basis (DOT)
- * XCUV merchandise exports to the U.S., c.i.f. (DOT)
 - XECV U.K. exports to Canada, f.o.b. (DOT)
- * XETV total U.K. merchandise exports

XG export of goods (STATCAN)

XGCV German exports to Canada, f.o.b. (DOT)

XGSNI exports of goods and services, national income account basis (STATCAN)

XGSNINS export of goods and services, national income

accounts basis, not seasonally adjusted (STATCAN)

XGSNIV exports of goods and services, national income accounts basis, current value (STATCAN)

XGSNIVS export of goods and services, national income accounts basis, not seasonally adjusted (STATCAN)

* XGTV total German merchandise exports

XGV exports of goods (STATCAN)

- XJCV Japanese exports to Canada, f.o.b. (DOT)
- * XJTV total Japanese merchandise exports

XRCV R.O.W. exports to Canada, f.o.b. (DOT)

* XRTV total R.O.W. merchandise exports

XSOV service account receipts, excluding investment income (STATCAN)

XUCV U.S. exports to Canada, f.o.b. (DOT)

* XUTV total U.S. merchandise exports

XSYV investment income receipts (STATCAN).

XTRANV transfer receipts (STATCAN)

XUJEGV Canadian exports from Germany, Japan, the United Kingdom and the United States

YDPVNSA proxy for disposable income (GNPVNSA - TV + TRANV - CCAV)

YDV disposable income (STATCAN)