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Title: A Tutorial on Using MCNP for 1-Group Transport Calculations

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A Tutorial on Using MCNP for 1-group Transport Calculations

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Abstract



A Tutorial on Using MCNP for 1-Group Transport Calculations

Forrest Brown (LANL) & Nathan Barnett (Oregon St. Univ.)

1-group transport calculations are an invaluable R&D tool for developing new algorithms and calculational methods for particle transport applications. They are also important for verifying the correctness of existing transport codes, since many 1-group transport analytical problems exist for which exact solutions are known. MCNP is a general-purpose, 3D, continuous-energy Monte Carlo particle transport code used for a wide variety of applications. In this tutorial, we describe how MCNP can be used to perform 1-group transport calculations. An auxilliary code called ONEGXS is first used to construct 1-group cross-section files in the ACE format required by MCNP. Then, MCNP can be run in a multigroup mode using the 1-group data files. This procedure is illustrated by several examples. It is important for users to understand the limitations on the MCNP Monte Carlo methods: For 1-group problems with isotropic scattering, MCNP results match exact analytical solutions. For linearly anisotropic scattering, MCNP results match exact analytical solutions when $|\vec{\mu}| \leq \frac{1}{3}$, but will generally not match exact analytical solutions otherwise, due to the non-physical effects of truncating the scattering data representation.

Outline



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 - Truncation errors for highly forward- or backward-peaked scatter

1-Group Transport - Background



- 1-group transport calculations are an important R&D tool
 - Useful for developing new algorithms & computational methods that do <u>not</u> involve energy-dependence

Examples: geometry tracking, criticality, void streaming

Simplifies & speeds up calculations

- 1-group calculations are important for verifying correctness of codes
 - Many transport problems have known, <u>exact</u>, analytical solutions
 - Typically, these are 1-group with simple geometry

1-Group Transport - Background



Criticality benchmarks

- A. Sood, R.A. Forster, D.K. Parsons, "Analytic Benchmark Test Set for Criticality Code Verification", LA-UR-01-3082 (2001)
- Compilation of 75 criticality problems with exact analytical solutions
 - 30 problems 1-group, isotropic scatter
 - 13 problems 1-group, anisotropic scatter
 - 26 problems 2-group, isotropic scatter
 - 4 problems 2-group, anisotropic scatter
 - 1 problem 3-group, isotropic scatter
 - 1 problem 6-group, isotropic scatter

Kobiyashi void-streaming benchmark

- K. Kobayashi, N. Sugimura, Y. Nagaya, "3-D Radiation Transport Benchmark Problems and Results for Simple Geometries with Void Regions", OECD/NEA (2000).
- Many others

Generating 1-Group Cross-section Files



- MCNP reads ACE-format cross-section files to obtain crosssection data, scattering distributions, etc., required for performing transport calculations
 - ACE files described in MCNP manual, Volume III, Appendix F
 - Very general, to accommodate continuous-energy neutron/photon/electron data & also multigroup data
 - Compact (but complex) data layout

onegxs

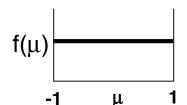
- Auxilliary code to simplify preparing 1-group cross-section datafiles
 - Includes basic cross-section data: total, scatter, capture, fission, nu
 - Provides scattering distribution data in the <u>lab</u> system:
 isotropic (P₀) or linearly-anisotropic (P₁) scattering
- Creates datafile in ACF format

Generating 1-Group Cross-section Files

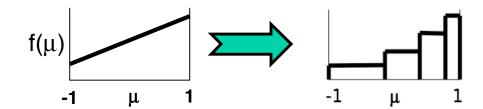


• Scattering distributions from onegxs are either isotropic (P_0) or linearly anisotropic (P_1) in the lab system for multigroup MCNP

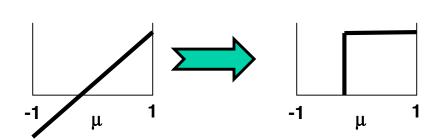
- Isotropic (P₀)
 - Flag, no data needed
 - Exact form used in MCNP



- P_1 scatter, with $|\overline{\mu}| \le \frac{1}{3}$
 - 1000 steps, equal-area



- P₁ scatter, with $|\bar{\mu}| > \frac{1}{3}$
 - Linear PDF replaced by 1 step
 - Step bounds chosen to preserve $\bar{\mu}$ & remain positive



onegxs Input



OneGXS

- Takes user-specified, one-group cross sections & writes a cross section file that MCNP can read.
- The program is driven from the command prompt & has a variety of input options. Use "onegxs -h" for help.
- It can handle multiplying or non-multiplying media, and isotropic or linearly anisotropic scattering.

Instructions for Use

- OneGXS accepts arguments through a flag, followed by data.
- The one exception is that the first argument is the name of the output file and does not use a flag.
- General form:

onegxs Input



File Name of the output file that MCNP will read & always required. Should be the first item listed.

- -c This flag indicates that the next item in the command line is the capture cross section. The capture cross section is defined as the absorption minus the fission, $\Sigma_C = \Sigma_A \Sigma_E$
- -f This flag indicates that the next item in the command line is the fission cross section, $\Sigma_{\rm F}$
- -h This flag will print the help page, with a list of all options available for running the program. After displaying the help page, the program will immediately exit. Note: the help page will also be displayed if no arguments are given.
- -n This flag indicates that the next item in the command line is v (nu-bar), the average number of neutrons produced in each fission event.
- -s This flag indicates that the next item in the command line is the scattering cross section, Σ_s . This is the isotropic, or P_0 , scattering cross section.
- -s0 This flag indicates that the next item in the command line is the P_0 , or isotropic, scattering cross section, Σ_s . This is the same value as the previous option.
- -s1 This flag indicates that the next item in the command line is the P_1 scattering cross section, Σ_{S1} . This provides the next term in the Legendre expansion, causing the scattering to be anisotropic.
- -t This flag indicates that the next item in the command line is the total cross section. The total cross section is defined as the sum of the capture, fission, and P₀ scattering cross sections,

$$\Sigma_{T} = \Sigma_{A} + \Sigma_{S} = \Sigma_{C} + \Sigma_{F} + \Sigma_{S}$$

- This flag indicates that the next item in the command line is μ (mu-bar), the average cosine of the scattering angle, $\mu = \Sigma_{S1} / \Sigma_{S0} = \Sigma_{S1} / \Sigma_{S}$. If mu-bar is zero, scattering is isotropic. Note: special caution should be taken with mu-bar, since problems with lmu-barl > 1/3 can give wrong answers. Please read the section on mu-bar.
- -z This flag indicates that the next item in the command line is the two digit material identifier that accompanies the ZAID number in MCNP. The ZAID will always be 92250. (e.g. 92250.32m)

onegxs Output



Using onegxs

- Not all of the options are needed to run the program.
- If the program can not calculate what it needs from the given data, then it will exit.
- Redundant data is checked against the overlapping data for differences.

Onegxs screen output, example

```
Created MCNP cross section file:
```

xsec02

The following cross sections were used:

```
sigT= 0.3264, sigF= 0.0816, sigC= 0.019584, sigS0= 0.225216, nu= 3.24, uBar= 0
```

Please use the following line in your MCNP deck on the xsn card:

92250.02m 1.0 xsec02 0 1 1 11 0 0 0.0

Running 1-Group Calculations with MCNP



Run MCNP in multigroup mode

- Don't use the MODE card (assume neutron multigroup)
- Importances should all be given in the form: imp:n
- Use default energy for any SDEF source cards
- Supply the MGOPT card as one of the data cards

Supply XSn cards in the MCNP input to describe the xsec files

```
xsfile1
xs1
     92250.12m
                 1.0
                                            13
                                                       0.0
                                          1013
                 1.0 xsfile2
                                0 1 1
xs2
     92250.27m
                                                       0.0
xs3
     92250.01m
                 1.0
                      xsfile3
                                0
                                   1
                                     1
                                            11
                                                   0
                                                       0.0
```

Values in red must match the output information from onegxs

Example - MCNP Input



PUa-1-1-SL Criticality Benchmark Problem

```
PUa-1-1-SL
        1.0 -1 2
10 1
                     $SEMI-INFINITE SLAB
20 0
                     $OUTSIDE WORLD
               1:-2
 px 0.77032
2 px -0.77032
kcode 20000 1.0 50
                     550
ksrc 0.0 0.0 0.0
hsrc 1 -1e20 1e20 1 -1e20 1e20 1 -1e20 1e20
xs1 92250.32m 1.0 xsec32 0 1 1 1013 0 0 0.0
m1 92250.32m 1.0
imp:n 1 0
mgopt f 1
```



Problem PUa-1-0-SL from Analytic Criticality Benchmark Set



- Problem 2 from the analytic criticality benchmark set
 - Identifier: PUa-1-0-SL
 - 1-group slab, with isotropic scatter (in lab)
 - From Table 2 in reference:

$$\Sigma_{\rm T} = .326400, \qquad \Sigma_{\rm S} = .225216, \qquad \Sigma_{\rm C} = .019584,$$

$$\Sigma_{\rm F} = .081600, \quad \nu = 3.24$$

– From Table 3 in reference:

critical half-thickness = 1.853722

– Exact eigenvalue: Keff = 1.000000



onegxs input for problem PUa-1-0-SL

```
onegxs xsec02 -z 02 -t .326400 -s .225216 \
-c .019584 -f .081600 -n 3.24
```

onegxs screen <u>output</u> for problem PUa-1-0-SL

```
Created MCNP cross section file:

xsec02

The following cross sections were used:

sigT= 0.3264, sigF= 0.0816, sigC= 0.019584, sigS0= 0.225216, nu= 3.24, uBar= 0

Please use the following line in your MCNP deck on the xsn card:

92250.02m 1.0 xsec02 0 1 1 11 0 0 0.0
```



onegxs file created for problem PUa-1-0-SL (xsec02)

```
92250.02m
                  250
                                0
                                    20070629
sigT= 0.3264, sigF= 0.0816, sigC= 0.019584, sigS0= 0.225216, nu= 3.24, uBar= 0
      11
            92250
                                  0
                                           1
                                                     0
                                                              0
                                                                       0
       0
                                           0
                                                     0
                1
                                                              0
                                                                       0
       1
                3
       0
                0
                         0
                                           8
                                                     0
                                                              0
                                                                      10
                0
      11
       0
                0
                                                     0
                         0
                                  0
                                                                       0
5.00000000000e+01
                     1.00000000000e+02
                                         3.26400000000e-01
                                                              8.16000000000e-02
                     1.00000000000e+00
3.24000000000e+00
                                         1.95840000000e-02
                                                              9.00000000000e+00
2.252160000000e-01 0.00000000000e+00
                                         0.00000000000e+00
```

For isotropic scattering, no angular distribution data is needed

PUa-1-0-SL



MCNP input file for problem PUa-1-0-SL, for 500M histories

```
1.0 -1 2
10
   1
                     $SEMI-INFINITE SLAB
20 0
               1:-2
                     $OUTSIDE WORLD
      1.853722
  рх
  px -1.853722
kcode 20000 1.0 50
                     2550
hsrc
       5 -1.853722 1.853722 1 -1e20 1e20 1 -1e20 1e20
ksrc 0.0 0.0 0.0
xs1
       92250.02m 1.0 xsec02 0 1 1 11 0 0 0.0
    92250.02m 1.0
m1
imp:n 1 0
mgopt
     f 1
```



MCNP output for problem PUa-1-0-SL

cycle	k(col)	ctm	entropy	active	k(col)	std dev	fom
1	1.11109	0.01	2.20E+00				
2	1.01883	0.03	2.29E+00				
3	1.02007	0.04	2.31E+00				
• • •							
2544	1.00112	38.41	2.31E+00	2494	1.00004	0.00012	1707942
2545	0.98849	38.43	2.31E+00	2495	1.00003	0.00012	1706282
2546	0.99955	38.44	2.31E+00	2496	1.00003	0.00012	1706999
2547	0.99067	38.46	2.31E+00	2497	1.00003	0.00012	1706142
2548	0.99723	38.47	2.30E+00	2498	1.00003	0.00012	1706712
2549	1.00831	38.49	2.31E+00	2499	1.00003	0.00012	1706216
2550	0.99519	38.50	2.31E+00	2500	1.00003	0.00012	1706499
final	k(col/abs/tr	k len) =	1.00009	std dev	= 0.00010		

For 1-group problems with isotropic scattering, results using onegxs + MCNP match the exact analytic solution (within statistics)



Problem Ua-1-1-CY from Analytic Criticality Benchmark Set



- Problem 36 from the analytic criticality benchmark set
 - Identifier: Ua-1-1-CY
 - 1-group infinite cyclinder, with anisotropic scatter (in lab), $\bar{\mu}$ = .171052631
 - From Table 23 in reference:

$$\Sigma_{\rm T} = .32640, \qquad \Sigma_{\rm S} = .248064, \qquad \Sigma_{\rm S1} = .042432$$

$$\Sigma_{\rm C}$$
 = .013056, $\Sigma_{\rm F}$ = .065280, ν = 2.70

– From Table 24 in reference:

critical radius = 5.514296811

– Exact eigenvalue: Keff = 1.000000



onegxs input for problem Ua-1-1-CY

```
onegxs xsec36 -z 36 -t .326400 -s .248064 \
-c .013056 -f .065280 -n 2.70 \
-s1 .042432
```

onegxs screen <u>output</u> for problem Ua-1-1-CY

```
Created MCNP cross section file:

xsec36

The following cross sections were used:

sigT= 0.3264, sigF= 0.06528, sigC= 0.013056, sigS0= 0.248064, nu= 2.7, uBar= 0.171053

Please use the following line in your MCNP deck on the xsn card:

92250.36m 1.0 xsec36 0 1 1 1013 0 0 0.0
```



onegxs file created for problem Ua-1-1-CY (xsec36)

1001

1013

92250

```
92250.36m 250 0 20070702
sigT= 0.3264, sigF= 0.06528, sigC= 0.013056, sigS0= 0.248064, nu= 2.7, uBar= 0.171053
```

1

```
0
                                          0
      1
               3
                                         6
                                                  7
                                                           0
                                                                    0
      0
               0
                        0
                                         8
                                                           0
                                                                   10
     12
               0
                                                  0
                                                                    0
5.00000000000e+01 1.0000000000e+02
                                       3.26400000000e-01
                                                           6.52800000000e-02
2.7000000000e+00 1.0000000000e+00 1.30560000000e-02
                                                           9.00000000000e+00
2.48064000000e-01 1.10000000000e+01 1.0000000000e+00 1.3000000000e+01
-1.00000000000000000+00 -9.959007501602e-01 -9.918190625466e-01 -9.877547078747e-01
-9.837074733325e-01 -9.796771402444e-01 -9.756634988818e-01 -9.716663483741e-01
9.894070569220e-01 9.907332609147e-01 9.920588675273e-01 9.933838764883e-01
9.947082892934e-01 9.960321076894e-01 9.973553312983e-01 9.986779607410e-01
1.00000000000e+00
```

For linearly-anisotropic scatter, with $l\mu$ -barl < 1/3, 1000 equiprobable steps are used to represent the angular distribution



MCNP input file for problem Ua-1-1-CY, for 500M histories

```
Ua-1-1-CY
       1.0 -1
  1
                     $SEMI-INFINITE CYLINDER
2
              1
                     $OUTSIDE WORLD
  0
  rcc 0 0 0 0 0 1e12 5.514296811
imp:n 1 0
kcode 20000 1.0 50 2550
hsrc 1 -1e20 1e20 1 -1e20 1e20 1 -1e20 1e20
ksrc
       0.0 0.0 .5e12
xs1 92250.36m 1.0 xsec36 0 1 1 1013 0 0 0.0
m1 92250.36m 1.0
mgopt f 1
```



MCNP output for problem Ua-1-1-CY

cycle	k(col)	ctm	entropy	active	k(col)	std dev	fom
1	1.23829	0.01	0.00E+00				
2	1.09388	0.02	0.00E+00				
3	1.03832	0.02	0.00E+00				
2544	0.99772	45.99	0.00E+00	2494	0.99995	0.00010	2066295
2545	1.00139	46.01	0.00E+00	2495	0.99995	0.00010	2067075
2546	1.01269	46.03	0.00E+00	2496	0.99995	0.00010	2062917
2547	0.99399	46.05	0.00E+00	2497	0.99995	0.00010	2062640
2548	0.99587	46.07	0.00E+00	2498	0.99995	0.00010	2062971
2549	1.00074	46.08	0.00E+00	2499	0.99995	0.00010	2063786
2550	0.99770	46.10	0.00E+00	2500	0.99995	0.00010	2064459
	• •						
final	k(col/abs/tr	k len) =	1.00005	std dev	= 0.00008		

For 1-group problems with linearly-anisotropic scattering, with μ -barl < 1/3, results using onegxs + MCNP match the exact analytic solution (within statistics)



Problem Ub-1-1-CY from Analytic Criticality Benchmark Set



- Problem 37 from the analytic criticality benchmark set
 - Identifier: Ub-1-1-CY
 - 1-group infinite cyclinder, with **anisotropic scatter (in lab)**, $\bar{\mu}$ = .855263157
 - From Table 23 in reference:

$$\Sigma_{\rm T} = .32640, \qquad \Sigma_{\rm S} = .248064, \qquad \Sigma_{\rm S1} = .212160$$

$$\Sigma_{\rm C} = .013056, \qquad \Sigma_{\rm F} = .065280, \qquad \nu = 2.70$$

– From Table 24 in reference:

critical radius = 6.940205668

– Exact eigenvalue: Keff = 1.000000



onegxs input for problem Ub-1-1-CY

```
onegxs xsec37 -z 37 -t .326400 -s .248064 \
-c .013056 -f .065280 -n 2.70 \
-s1 .212160
```

onegxs screen <u>output</u> for problem Ub-1-1-CY

```
Created MCNP cross section file:

xsec37

The following cross sections were used:

sigT= 0.3264, sigF= 0.06528, sigC= 0.013056, sigS0= 0.248064, nu= 2.7, uBar= 0.855263

Please use the following line in your MCNP deck on the xsn card:

92250.37m 1.0 xsec37 0 1 1 14 0 0 0.0
```



onegxs file created for problem Ub-1-1-CY (xsec37)

```
92250.37m 250 0 20070702
sigT= 0.3264, sigF= 0.06528, sigC= 0.013056, sigS0= 0.248064, nu= 2.7, uBar= 0.855263
```

14	92250	2	0	1	0	0	0
0	1	0	1	0	0	0	0
1	3	4	5	6	7	0	0
0	0	0	0	8	0	0	10
12	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

```
5.0000000000e+01 1.0000000000e+02 3.26400000000e-01 6.52800000000e-02 2.7000000000e+00 1.0000000000e+00 1.30560000000e-02 9.0000000000e+00 2.48064000000e-01 1.10000000000e+01 1.00000000000e+00 1.30000000000e+01
```

7.105263157895e-01 1.00000000000e+00

For linearly-anisotropic scatter, with $l\mu$ -barl > 1/3, the angular distribution is represented by 1 step is used, with bounds chosen to preserve $l\mu$ -barl



MCNP input file for problem PUa-1-0-SL, for 500M histories

```
Ub-1-1-CY
       1.0 -1
 1
1
                     $SEMI-INFINITE CYLINDER
2 0
               1
                     $OUTSIDE WORLD
  rcc 0 0 0 0 0 1e12 6.940205668
       1 0
imp:n
kcode 20000 1.0 50 2550
hsrc 1 -1e20 1e20 1 -1e20 1e20 1 -1e20 1e20
ksrc
       0.0
             0.0 .5e12
xs1 92250.37m 1.0 xsec37 0 1 1 14 0 0 0.0
m1 92250.37m 1.0
mgopt f 1
```



MCNP output for problem Ub-1-1-CY

cycle	k(col)	ctm	entropy	active	k(col)	std dev	fom
1	1.22206	0.02	0.00E+00				
2	1.09928	0.04	0.00E+00				
3	1.05035	0.06	0.00E+00				
	•						
2544	1.01522	45.23	0.00E+00	2494	1.01865	0.00010	2560777
2545	1.01316	45.25	0.00E+00	2495	1.01865	0.00010	2560448
2546	1.01781	45.27	0.00E+00	2496	1.01865	0.00010	2561446
2547	1.01126	45.28	0.00E+00	2497	1.01864	0.00010	2560008
2548	1.01934	45.30	0.00E+00	2498	1.01864	0.00010	2561015
2549	1.01609	45.32	0.00E+00	2499	1.01864	0.00010	2561737
2550	1.01955	45.34	0.00E+00	2500	1.01864	0.00010	2562728
	•						
final	k(col/abs/trk	len) =	1.01870	std dev =	0.00008		

For 1-group problems with linearly-anisotropic scattering, with $l\mu$ -barl > 1/3, results using onegxs + MCNP will generally NOT match the exact analytic solution



Angular Scattering Distributions & Truncation Errors



Scattering angle PDFs

 Scattering distributions are usually represented by a Legendre polynomial expansion in data libraries (eg, ENDF/B)

$$f(\mu) = \sum_{n=0}^{N} \frac{2n+1}{2} a_n P_n(\mu), \qquad -1 \le \mu \le 1$$

- Typically N=20 Legendre moments a_n are stored
- The Legendre representation is converted to histogram or piecewise-linear PDFs for use in Monte Carlo codes by NJOY or some other processing program

Sometimes, truncated angular PDFs must be used

- S_N codes typically use P1, P3, P5, ..., truncated expansions
- May want to compare MC & S_N using same cross-section data
- Truncated Legendre expansions may produce angular PDFs with negative data over part of range



Simplest case - P1 scattering

$$f(\mu) = \frac{1 + a\mu}{2},$$

$$\left|\overline{\mu}\right| \leq \frac{1}{3}$$

$$f(\mu) > 0$$
 in [-1,1]

$$-1 \le \mu \le 1$$
, $a = 3\overline{\mu}$

$$\left|\overline{\mu}\right| > \frac{1}{3}$$

 $f(\mu) < 0$ for some μ

- If $|\overline{\mu}| > \frac{1}{3}$, need to replace $f(\mu)$ by another PDF $g(\mu)$
 - Non-negative PDF:
 - Preserve physical condition:

$$g(\mu) \ge 0$$

$$\int_{-1}^{1} \mu g(\mu) d\mu = \overline{\mu}$$

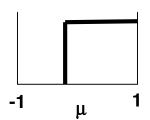


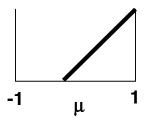
Non-physical PDF, linear with

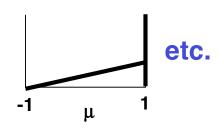
$$\left|\overline{\mu}\right| > \frac{1}{3}$$

Alternate forms of PDF that can preserve 1st moment









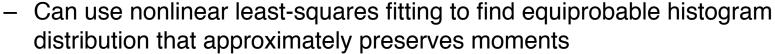
- All of these can be chosen to preserve the physical data, $< \mu >$
- The second form, a 1-step histogram, can be accommodated by MCNP using the standard data formats, and does not require code modifications

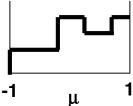
For
$$\overline{\mu} > \frac{1}{3}$$
, choose bounds $[2\overline{\mu} - 1, 1]$

For
$$\overline{\mu} < -\frac{1}{3}$$
, choose bounds $[-1, 2\overline{\mu} + 1]$



- For higher order truncated Legendre expansions, more elaborate schemes must be used to preserve the moments & guarantee nonnegative PDFs
 - For a P_N expansion, can find (N+1)/2 discrete angles which preserve all N moments & have positive weights
 - Use generalized orthogonal polynomials
 - See description in MORSE code manual





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