Noncompartmental vs. Compartmental Approaches to
Pharmacokinetic Data Analysis

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## Questions To Be Asked

> Pharmacokinetics

- What the body does to the drug
> Pharmacodynamics
- What the drug does to the body
> Disease progression
- Measurable therapeutic effect
$>$ Variability
- Sources of error and biological variation
> Pharmacokinetics
"What the body does to the drug"
Fairly well known
Useful to get to the PD

Pharmacodynamics
"What the drug does to the body"
> Largely unknown Has clinical relevance Pharmacokinetics / Pharmacodynamics

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Hierarchical Variability

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## Pharmacokinetic Parameters

> Definition of pharmacokinetic parameters $\qquad$

- Descriptive or observational
- Quantitative (requiring a formula and a means to estimate using the formula)
> Formulas for the pharmacokinetic parameters
$>$ Methods to estimate the parameters from the formulas using measured data


## Models For Estimation

Noncompartmental
Compartmental
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## Goals Of This Lecture

> Description of the parameters of interest $\qquad$
> Underlying assumptions of
noncompartmental and compartmental models
> Parameter estimation methods
$>$ What to expect from the analysis
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## Goals Of This Lecture

$>$ What this lecture is about $\qquad$

- What are the assumptions, and how can these affect the conclusions $\qquad$
- Make an intelligent choice of methods depending upon what information is required from the data
$>$ What this lecture is not about
- To conclude that one method is "better" than another

A Drug In The Body:
Constantly Undergoing Change
$>$ Absorption
$>$ Transport in the circulation
> Transport across membranes
> Biochemical transformation
> Elimination

A Drug In The Body:
Constantly Undergoing Change

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## Definition Of Kinetics:

Consequences
Spatial: Where in the system

- Spatial coordinates
- Key variable: $s=(x, y, z)$


Temporal: When in the system

- Temporal coordinates
- Key variable: t
$\frac{\partial c(\vec{s}, t)}{\partial x}, \quad \frac{\partial c(\vec{s}, t)}{\partial y}, \quad \frac{\partial c(\vec{s}, t)}{\partial z}, \quad \frac{\partial c(\vec{s}, t)}{\partial t}$

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A Drug In The Body:
Constantly Undergoing Change

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## Spatially Distributed Models

$>$ Spatially realistic models:

- Require a knowledge of physical chemistry, irreversible thermodynamics and circulatory dynamics.
- Are difficult to solve.
- It is difficult to design an experiment to estimate their parameter values.
$>$ While desirable, normally not practical.
> Question: What can one do?
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## Resolving The Problem

$>$ Reducing the system to a finite number of components
> Lumping processes together based upon time, location or a combination of the two
> Space is not taken directly into account: rather, spatial heterogeneity is modeled through changes that occur in time
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## Lumped Parameter Models

$>$ Models which make the system discrete through a lumping process thus eliminating the need to deal with partial differential equations.
> Classes of such models:

- Noncompartmental models

Based on algebraic equations

- Compartmental models

Based on linear or nonlinear differential equations

## Probing The System

> Accessible pools: These are system spaces that are available to the
experimentalist for test input and/or measurement.
Nonaccessible pools:
These are spaces comprising the rest of the system which are not available for test input and/or measurement.

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Focus On The Accessible Pool $\qquad$ INPUT

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## Characteristics Of The Accessible Pool

Kinetically Homogeneous Instantaneously Well-mixed

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## The Pharmacokinetic Parameters

$>$ Which pharmacokinetic parameters can
$\qquad$ we estimate based on measurements in the accessible pool? $\qquad$
> Estimation requires a model

- Conceptualization of how the system works
> Depending on assumptions:
- Noncompartmental approaches
- Compartmental approaches
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Accessible Pool \& System
Assumptions $\rightarrow$ Information
> Accessible pool

- Initial volume of distribution
- Clearance rate
- Elimination rate constant
- Mean residence time
- System
- Equivalent volume of distribution
- System mean residence time
- Bioavailability
- Absorption rate constant
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## Compartmental and Noncompartmental Analysis

The only difference between the two methods is in how the nonaccessible portion of the system is described

The Noncompartmental Model $\qquad$

SOURCE


ELIMINATION

Recirculation-exchange Assumptions

Recirculation/

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Single Accessible Pool
Noncompartmental Model
> Parameters (IV bolus and infusion)

- Mean residence time
- Clearance rate
- Volume of distribution
> Estimating the parameters from data
> Additional assumption:
- Constancy of kinetic distribution parameters

Mean Residence Time
$>$ The average time that a molecule of drug spends in the system


## Areas Under The Curve

$>$ AUMC

- Area Under the Moment Curve
> AUC
- Area Under the Curve
$>$ MRT
- "Normalized" AUMC (units = time)
$M R T=\frac{\int_{0}^{+\infty} t(t) d t}{\int_{0}^{+\infty} C(t) d t}=\frac{A U M C}{A U C}$

What Is Needed For MRT?
> Estimates for AUC and AUMC. $\qquad$

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## What Is Needed For MRT?

> Estimates for AUC and AUMC. $\qquad$

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AUC= \int
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$A U M C=\int_{0}^{\infty} t \cdot C(t) d t=\int_{0}^{t_{1}} t \cdot C(t) d t+\int_{t_{1}}^{t_{n}} t \cdot C(t) d t+\int_{t_{n}}^{\infty} t \cdot C(t) d t$ $\qquad$
> They require extrapolations beyond the time frame of the experiment $\qquad$
> Thus this method is not model independent as often claimed. $\qquad$
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Estimating AUC And AUMC Using Sums Of Exponentials

AUMC $=\int_{0}^{t} \cdot C(t) d t=\int_{0}^{4 t} t \cdot C(t) d t+\int_{4}^{4 t} t \cdot C(t) d t+\int_{a}^{s} t \cdot C(t) d t$
$C(t)=A_{1} e^{-\lambda_{1} t}+\cdots+A_{n} e^{-\lambda_{n} t}$

Bolus IV Injection
Formulas can be extended to other administration sites

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\begin{aligned}
\mathrm{AUC} & =\int_{0}^{\infty} \mathrm{C}(\mathrm{t}) \mathrm{dt}=\frac{\mathrm{A}_{1}}{\lambda_{1}}+\cdots+\frac{\mathrm{A}_{\mathrm{n}}}{\lambda_{n}} \\
\mathrm{AUMC} & =\int_{0}^{\infty} \mathrm{t} \cdot \mathrm{C}(\mathrm{t}) \mathrm{dt}=\frac{\mathrm{A}_{1}}{\lambda_{1}^{2}}+\cdots+\frac{\mathrm{A}_{n}}{\lambda_{n}^{2}}
\end{aligned}
$$

$$
C(0)=A_{1}+\cdots+A_{n}
$$

## Estimating AUC And AUMC Using Other Methods

> Trapezoidal
> Log-trapezoidal
$>$ Combinations
$>$ Other
$>$ Role of extrapolation


## The Integrals

> These other methods provide formulas for the integrals between $t_{1}$ and $t_{n}$ leaving it up to the researcher to extrapolate to time zero and time infinity.
$A U C=\int_{0}^{\infty} C(t) d t=\int_{0}^{t_{1}} C(t) d t+\int_{t_{1}}^{t_{n}} C(t) d t+\int_{t_{n}}^{\infty} C(t) d t$
$A U M C=\int_{0}^{\infty} t \cdot C(t) d t=\int_{0}^{t_{1}} t \cdot C(t) d t+\int_{t_{1}}^{t_{n}} t \cdot C(t) d t+\int_{t_{n}}^{\infty} t \cdot C(t) d t$
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## Trapezoidal Rule

> For every time $t_{i}, i=1, \ldots, n$

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A \cup C_{i-1}^{i}=\frac{1}{2}\left[y_{\text {obs }}\left(t_{i}\right)+y_{\text {obs }}\left(t_{i-1}\right)\right]\left(t_{i}-t_{i-1}\right)
$$

AUMC $_{\mathrm{i}-1}^{i}=\frac{1}{2}\left[\mathrm{t}_{\mathrm{i}} \cdot \mathrm{y}_{\text {obs }}\left(\mathrm{t}_{\mathrm{i}}\right)+\mathrm{t}_{\mathrm{i}-1} \cdot \mathrm{y}_{\text {obs }}\left(\mathrm{t}_{\mathrm{i}-1}\right)\right]\left(\mathrm{t}_{\mathrm{i}}-\mathrm{t}_{\mathrm{i}-1}\right)$

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## Log-trapezoidal Rule

$>$ For every time $t_{i}, i=1, \ldots, n$ $\qquad$

$\operatorname{AUMC}_{\mathrm{i}-1}^{\mathrm{i}}=\frac{1}{\ln \left(\frac{\mathrm{y}_{\text {obs }}\left(\mathrm{t}_{\mathrm{i}}\right)}{\mathrm{y}_{\text {obs }}\left(\mathrm{t}_{\mathrm{i}-1}\right)}\right)}\left[\mathrm{t}_{\mathrm{i}} \cdot \mathrm{y}_{\text {obs }}\left(\mathrm{t}_{\mathrm{i}}\right)+\mathrm{t}_{\mathrm{i}-1} \mathrm{y}_{\text {obs }}\left(\mathrm{t}_{\mathrm{i}-1}\right)\right]\left(\mathrm{t}_{\mathrm{i}}-\mathrm{t}_{\mathrm{i}-1}\right)$
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Trapezoidal Rule Potential Pitfalls

> As the number of samples decreases, the interpolation may not be accurate (depends on the shape of the curve)
Extrapolation from last measurement necessary

Extrapolating From $t_{n}$ To Infinity
$>$ Terminal decay is assumed to be a $\qquad$ monoexponential
$>$ The corresponding exponent is often called $\lambda_{z}$.
$>$ Half-life of terminal decay can be calculated: $\qquad$ $t_{z / 1 / 2}=\ln (2) / \lambda_{z}$

## Extrapolating From $t_{n}$ To Infinity

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From last data point:
$\qquad$
$A \cup C_{\text {extrap-dat }}=\int_{t_{n}}^{\infty} C(t) d t=\frac{y_{\text {obs }}\left(t_{n}\right)}{\lambda_{z}}$
$\mathrm{AUMC}_{\text {extrap-dat }}=\int_{\mathrm{t}_{n}}^{\infty} \mathrm{t} \cdot \mathrm{C}(\mathrm{t}) \mathrm{dt}=\frac{\mathrm{t}_{\mathrm{n}} \cdot \mathrm{Y}_{\text {obs }}\left(\mathrm{t}_{\mathrm{n}}\right)}{\lambda_{z}}+\frac{\mathrm{y}_{\text {obs }}\left(\mathrm{t}_{n}\right)}{\lambda_{\mathrm{z}}^{2}}$
From last calculated value:

$$
\begin{gathered}
\mathrm{AUC}_{\text {extrap-calc }}=\int_{t_{n}}^{\infty} C(t) d t=\frac{A_{z} e^{-\lambda_{z} t_{n}}}{\lambda_{z}} \\
\mathrm{AUMC}_{\text {extrap-calc }}=\int_{t_{n}}^{\infty} t \cdot C(t) d t=\frac{t_{n} \cdot A_{z} e^{-\lambda_{2} t_{n}}}{\lambda_{z}}+\frac{A_{z} e^{-\lambda_{z} t_{n}}}{\lambda_{z}^{2}}
\end{gathered}
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Extrapolating From $t_{n}$ To Infinity
> Extrapolating function crucial $\qquad$
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## Estimating The Integrals

$>$ To estimate the integrals, one sums up the $\qquad$ individual components.

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## Advantages Of Using Sums

 Of Exponentials> Extrapolation done as part of the data $\qquad$ fitting

- Statistical information of all parameters calculated
> Natural connection with the solution of linear, constant coefficient compartmental models
Software available
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## Clearance Rate

- The volume of blood cleared per unit time,
$\qquad$ relative to the drug


## $\mathrm{CL}=\frac{\text { Elimination rate }}{\text { Con }}$ <br> Concentratoninblood

> It can be shown that $\qquad$


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The Compartmental Model
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Single Accessible Pool Models
Noncompartmental $>$ Compartmental $\qquad$
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A Model Of The System $\qquad$

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## Compartmental Model

$>$ Compartment $\qquad$

- Instantaneously well-mixed
- Kinetically homogeneous
> Compartmental model
- Finite number of compartments
- Specifically connected
- Specific input and output


## Kinetics And The Compartmental Model

> Time and space
$\frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z}, \frac{\partial}{\partial t}$
$\partial x$ ' $\partial y^{\prime} \partial z$ ' $\partial t$
$\rightarrow X(x, y, z, t)$
$\rightarrow \frac{\partial X(x, y, z, t)}{\partial x}, \frac{\partial X(x, y, z, t)}{\partial y}, \frac{\partial X(x, y, z, t)}{\partial z}, \frac{\partial X(x, y, z, t)}{\partial t}$
$>$ Time


Demystifying Differential Equations
$>$ It is all about modeling rates of change, i.e. slopes, or derivatives:

$>$ Rates of change may be constant or not

## Ingredients Of Model Building

$>$ Model of the system

- Independent of experiment design
- Principal components of the biological system
> Experimental design
- Two parts:

Input function (dose, shape, protocol)
Measurement function (sampling, location)
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Single Compartment Model

$\frac{d q_{1}(t)}{d t}=-k(0,1) q_{1}(t)$
> The rate of change of the amount in the compartment, $q_{1}(t)$, is equal to what enters the compartment (inputs or initial conditions), minus what leaves the compartment, a quantity proportional to $\mathrm{q}_{1}(\mathrm{t})$
$k(0,1)$ is a rate constant

Experiment Design
Modeling Input Sites


- The rate of change of the amount in the compartment, $q_{1}(t)$, is equal to what enters the compartment (Dose), minus what leaves the compartment, a quantity proportional to $q(t)$
Dose(t) can be any
function of time


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## The $F_{i j}$

$>$ Describe movement among, into or out of
$\qquad$ a compartment
> A composite of metabolic activity

- transport
- biochemical transformation
- both
> Similar (compatible) time frame

A Proportional Model For The Compartmental Fluxes
$>q=$ compartmental masses $\qquad$
$>p=$ (unknown) system parameters
$>\mathrm{k}_{\mathrm{ji}}=\mathrm{a}$ (nonlinear) function specific to the transfer from $i$ to $j$ $\qquad$

$$
F_{\mathrm{ji}}(\mathrm{q}, \mathrm{p}, \mathrm{t})=\mathrm{k}_{\mathrm{ji}}(\mathrm{q}, \mathrm{p}, \mathrm{t}) \cdot \mathrm{q}_{\mathrm{i}}(\mathrm{t})
$$

## The $\mathrm{k}_{\mathrm{ij}}$

- The fractional coefficients $\mathrm{k}_{\mathrm{ij}}$ are called $\qquad$ fractional transfer functions
- If $\mathrm{k}_{\mathrm{ij}}$ does not depend on the compartmental masses, then the kij is called a fractional transfer (or rate) constant.

$$
\mathrm{k}_{\mathrm{ij}}(\mathrm{q}, \mathrm{p}, \mathrm{t})=\mathrm{k}_{\mathrm{ij}}
$$

Compartmental Models And Systems Of Ordinary Differential Equations
$>$ Good mixing

- permits writing $Q_{f}(t)$ for the $i^{i t h}$ compartment.
$>$ Kinetic homogeneity
- permits connecting compartments via the $\mathrm{k}_{\mathrm{ij}}$.
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## Linear, Constant Coefficient

 Compartmental Models> All transfer rates $\mathrm{k}_{\mathrm{ij}}$ are constant.

- This facilitates the required computations $\qquad$ greatly
> Assume "steady state" conditions.
- Changes in compartmental mass do not affect the values for the transfer rates

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The Compartmental Matrix

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$>$ A detailed postulation of how one believes a system functions.
$>$ The need to perform the same experiment on the model as one did in the laboratory.

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## Experiments

> Need to recreate the laboratory
experiment on the model.
$>$ Need to specify input and measurements
$>$ Key: UNITS

- Input usually in mass, or mass/time
- Measurement usually concentration

Mass per unit volume
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Model Of The System?

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Pharmacokinetic Experiment
Collecting System Knowledge


The model starts as a qualitative construct, based on known physiology and further
$\qquad$ assumptions $\qquad$

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## Parameter Estimates

$>$ Model parameters: $\mathrm{k}_{\mathrm{ij}}$ and volumes
> Pharmacokinetic parameters: volumes, clearance, residence times, etc.
$>$ Reparameterization - changing the parameters from $\mathrm{k}_{\mathrm{ij}}$ to the PK parameters.

Recovering The PK Parameters From Compartmental Models
> Parameters can be based upon

- The model primary parameters

Differential equation parameters
Measurement parameters

- The compartmental matrix

Aggregates of model parameters


Compartmental Residence Times

> Rate constants
> Residence times

- Intercompartmental clearances
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## Parameters Based Upon The Compartmental Matrix

$K=\left[\begin{array}{cccc}k_{11} & k_{12} & \cdots & k_{1 n} \\ k_{21} & k_{22} & \cdots & k_{2 n} \\ \vdots & \vdots & \ddots & \vdots \\ k_{n 1} & k_{n 2} & \cdots & k_{n n}\end{array}\right] \quad \Theta=-K^{-1}=\left(\begin{array}{cccc}\vartheta_{11} & \vartheta_{12} & \cdots & \vartheta_{1 n} \\ \vartheta_{21} & \vartheta_{22} & \cdots & \vartheta_{2 n} \\ \vdots & \vdots & \ddots & \vdots \\ \vartheta_{n 1} & \vartheta_{n 2} & \cdots & \vartheta_{n n}\end{array}\right)$

Theta, the negative of the inverse of the compartmental matrix, is called the mean residence time matrix.

## Parameters Based Upon The Compartmental Matrix <br> Generalization of Mean Residence Time

$母_{\mathrm{ij}} \quad$ The average time the drug entering compartment for the first time spends in compartment i before leaving the system.
$\frac{\Im_{\mathrm{ij}}}{\Im_{\mathrm{ii}}}, \quad \mathrm{i} \neq \mathrm{j} \quad \begin{aligned} & \text { The probability that a drug particle in } \\ & \text { compartment } \mathrm{j} \text { will eventually pass through } \\ & \text { compartment } \mathrm{i} \text { before leaving the system. }\end{aligned}$

## Compartmental Models:

Advantages
$>$ Can handle nonlinearities
> Provide hypotheses about system structure
> Can aid in experimental design, for example to design dosing regimens
$>$ Can support translational research
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Noncompartmental Versus Compartmental Approaches To PK Analysis: A Example
$>$ Bolus injection of 100 mg of a drug into plasma. Serial plasma samples taken for 60 hours.
> Analysis using:

- Trapezoidal integration
- Sums of exponentials
- Linear compartmental model

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| Trapezoidal <br> Analysis | Sum of <br> Exponentials | Compartmental <br> Model |
| :---: | ---: | ---: |
|  | $10.2(9 \%)$ | $10.2(3 \%)$ |
| 1.02 | $1.02(2 \%)$ | $1.02(1 \%)$ |
| 19.5 | $20.1(2 \%)$ | $20.1(1 \%)$ |
| 0.0504 | $0.0458(3 \%)$ | $0.0458(1 \%)$ |
| 97.8 | $97.9(2 \%)$ | $97.9(1 \%)$ |
| 1908 | $1964(3 \%)$ | $1964(1 \%)$ |

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## Take Home Message

$>$ To estimate traditional pharmacokinetic $\qquad$ parameters, either model is probably okay when the sampling schedule is dense $\qquad$
> Sparse sampling schedule may be an issue for noncompartmental analysis $\qquad$
$>$ Noncompartmental models are not predictive $\qquad$
> Best strategy is probably a blend: but, careful about assumptions! $\qquad$
$\qquad$

## Some References

> JJ DiStefano III. Noncompartmental vs
compartmental analysis: some bases for choice. Am J. Physiol. 1982;243:R1-R6

- DG Covell et. al. Mean Residence Time. Math. Biosci. 1984;72:213-2444
- Jacquez, JA and SP Simon. Qualitative theory of compartmental analysis. SIAM Review 1993;35:4379
Jacquez, JA. Compartmental Analysis in Biology and Medicine. BioMedware 1996. Ann Arbor, MI.
Cobelli, C, D Foster and G Toffolo. Tracer Kinetics in Biomedical Research. Kluwer Academic/Plenum Publishers. 2000, New York.

